

# Core-Collapse Supernova Theory

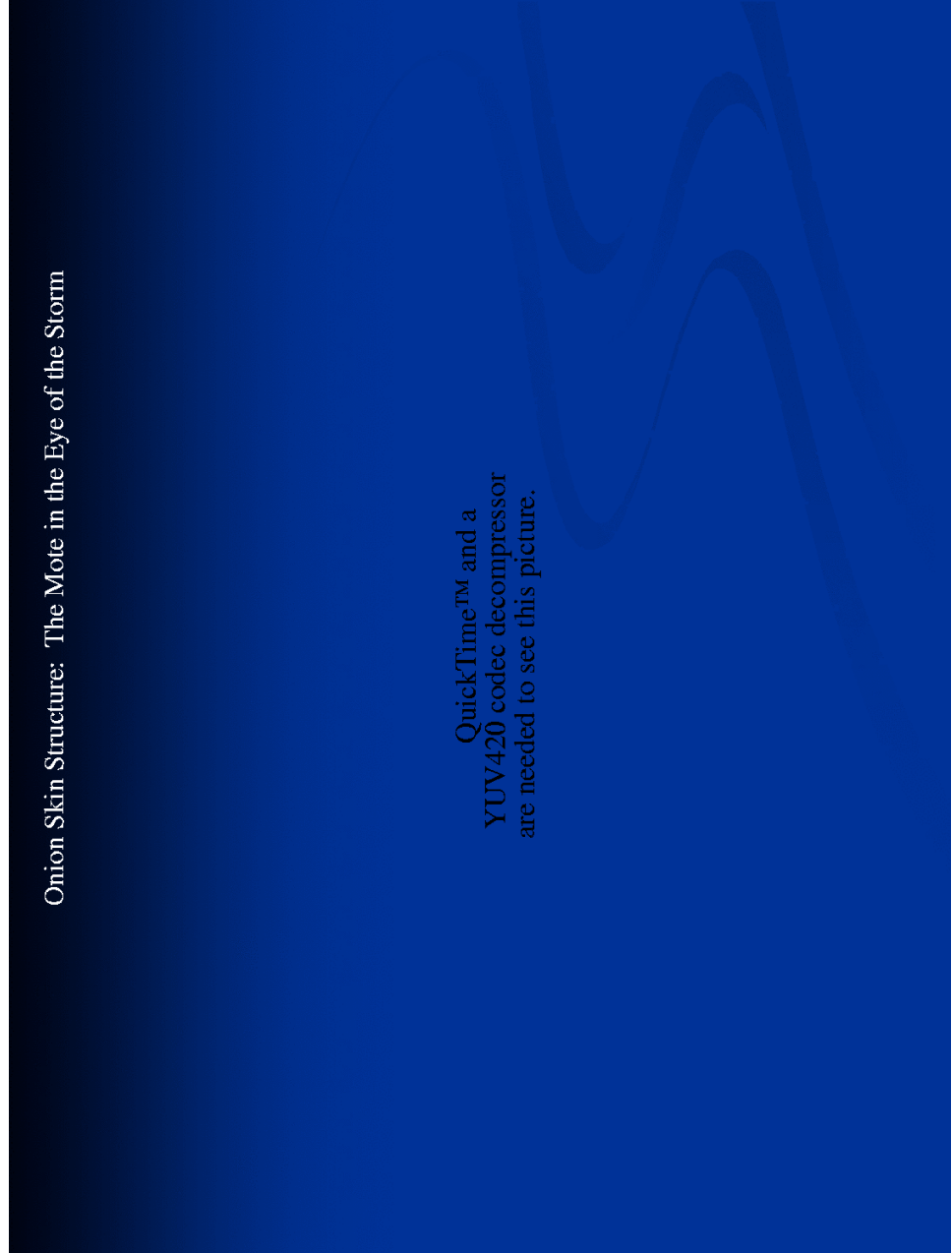
University of Arizona  
Core-Collapse Simulations

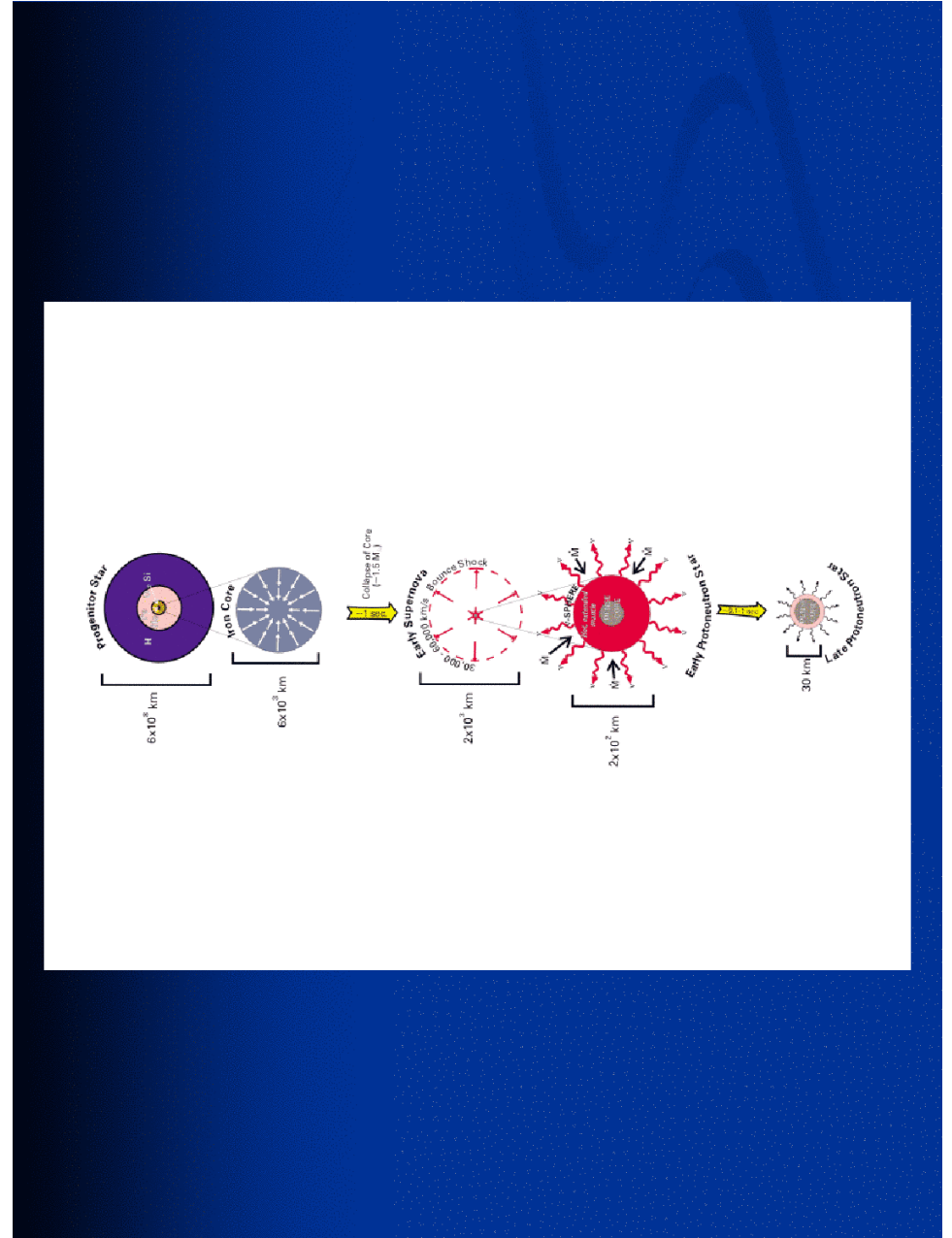
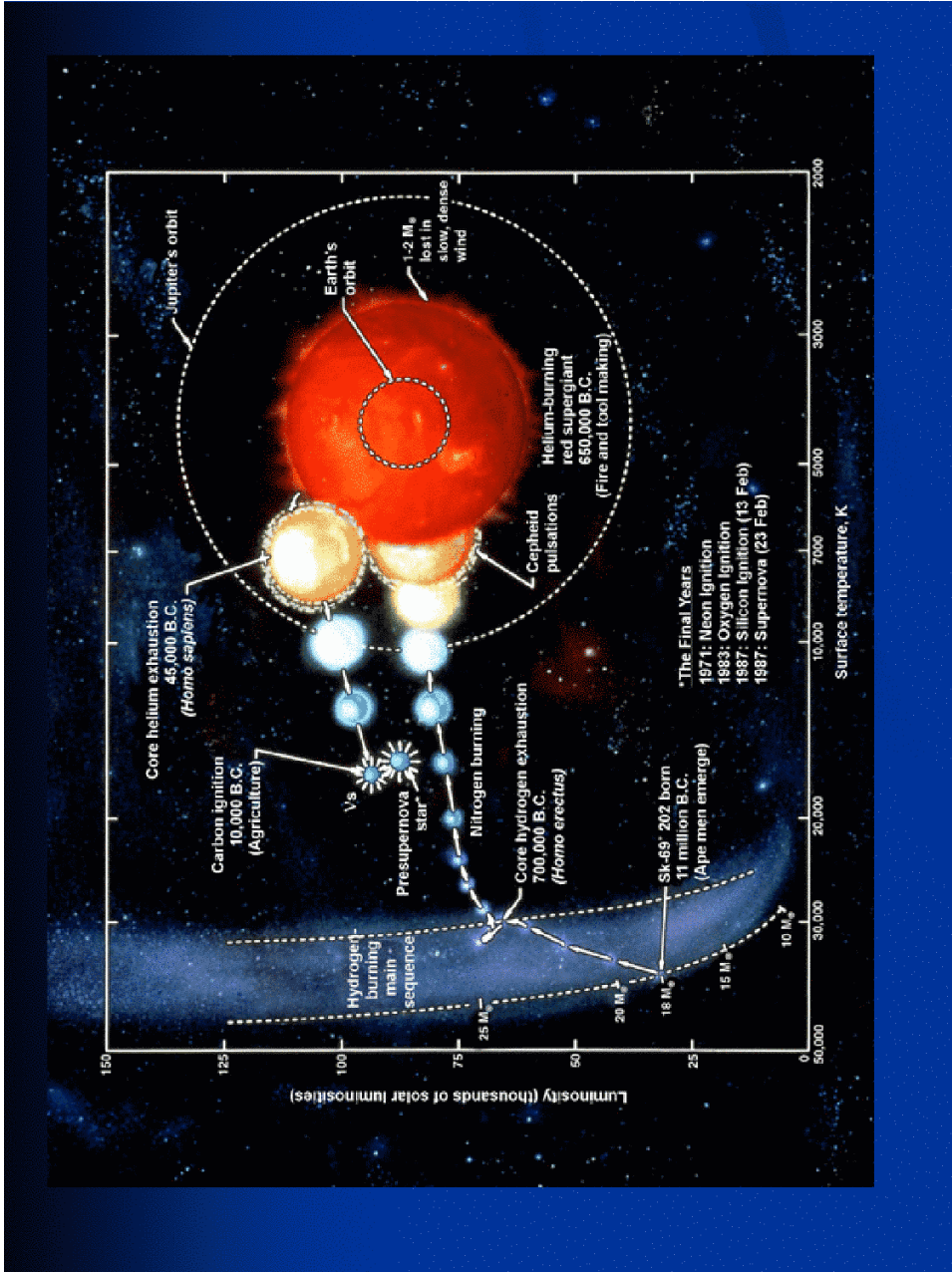
Adam Burrows, Rolf Walder, Christian Ott, Eli Livne, Itamar Lichtenstadt,  
Jeremiah Murphy, Todd Thompson

Friday, February 18, 2005

## Outline

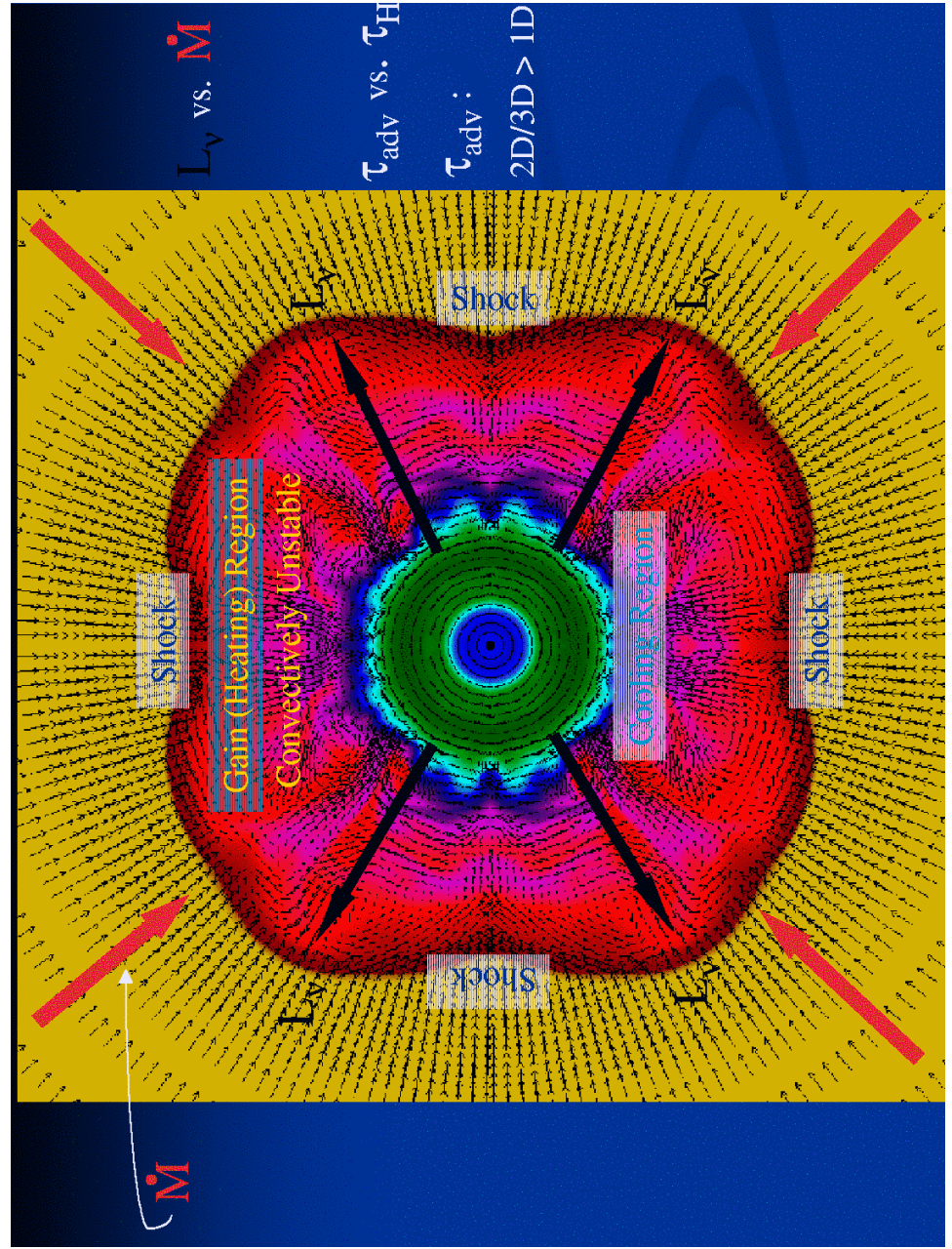
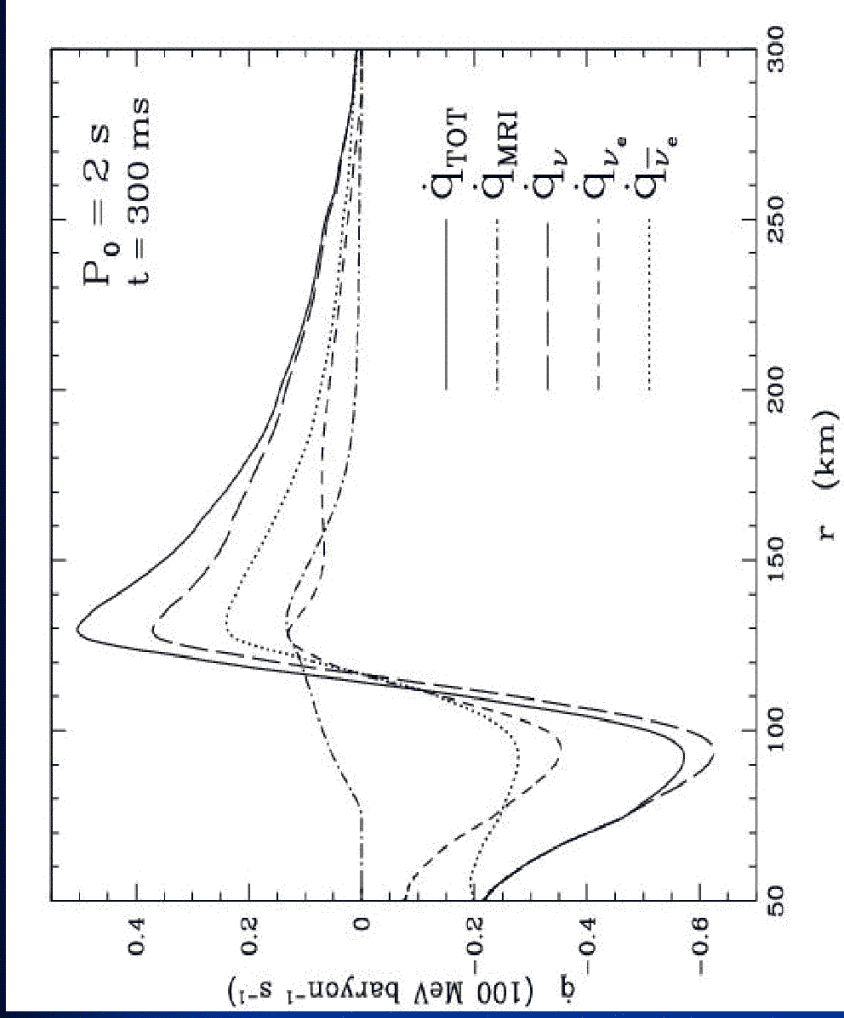
- Basic scenario of Core-Collapse Supernovae
- Rotation? Multi-D effects
- **VULCAN/2D**: 2D Radiation/hydrodynamics, (with rotation)
- 2D Flux, heating **Anisotropy**, with and without rotation
- 2D MGFLD Radiation/hydrodynamics results
- Gravitational radiation; Pulsar kicks
- **Mixed-Frame** 2D Radiation/Hydrodynamics
- Future theoretical work







Heating and Cooling; The Effect of an Extra Source





## Explosion Mechanism?

- Explosion driven by **neutrino heating** of shocked mantle after bounce shock stalls: delay? (Radiation pressure unimportant to mechanism)
- Neutrino-driven explosion is a **~10%** phenomenon, not a ~1% phenomenon
- Bounce shock always fizzles: “Direct” hydro mechanism aborts: killed by neutrino losses and photodissociation of heavy nuclei
- Delay is good: Neutron star mass and Ejecta  $Y_e$  (nucleosynthesis)
- **Explosion condition:**  $L_\nu$  (heating) vs. Mass accretion; “ $\tau_H < \tau_{adv}$ ”
- We know what would facilitate neutrino-driven explosions
- General relativity, EOS, neutrino-matter coupling details not very important at the 10-20% level (feedbacks), but ...

## Explosion Mechanism? II

- All groups get the same results in 1D: fizzle.  $\tau_H > \tau_{adv}$ .
- **Multi-D** instabilities/convection and radiation hydrodynamics important; 2D/3D may be crucial  $\longrightarrow$   
 $\tau_H < \tau_{adv}$  (?)
- Also, can core instabilities boost driving neutrino luminosity? Doubly-diffusive instabilities, mixing, eddy digging?
- **Rotation**’s role and final spin period(s): Angular momentum transport? Eddington-Sweet-type mixing instabilities?
- **B-fields**, MRI?
- **Viscous** heating and angular momentum transport?
- **Vortical-Acoustic** instability?  $l = 1$  modes?

## Rotation?

- Produces bi-polar explosions (SN1987A morphology; Type Ic polarization; rough correlation of pulsar spin axis with proper motion)
- **Naturally amplified by collapse**
- **Centrifugal support** (lower effective gravity)
- **Enlarges gain region**
- Generates funnels at poles!
- For rapid rotation, neutrino flux anisotropy: greater at poles?
- GRB connection
- How to shed angular momentum and rotational KE: pulsars?
- B-fields?
- Extra parameter(s)
- New generation of simulations required

QuickTime™ and a  
Sorenson Video 3 decompressor  
are needed to see this picture.

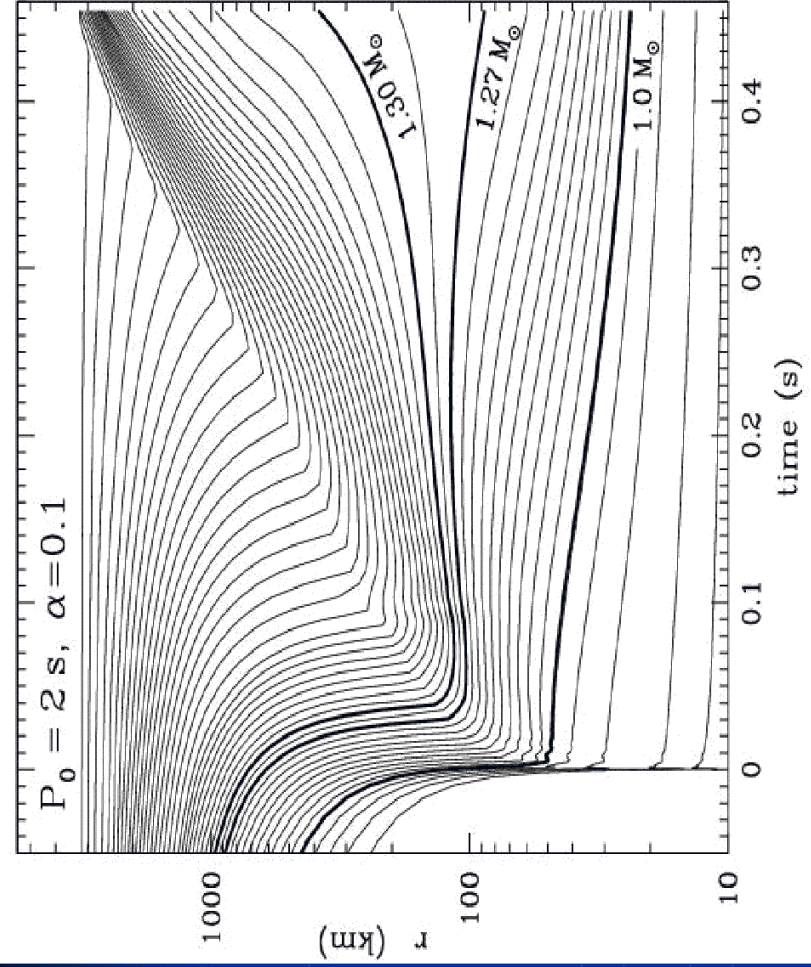




20 Solar Masses  
Modest Rotation  
Torus Formation

QuickTime™ and a  
Photo decompressor  
are needed to see this picture.

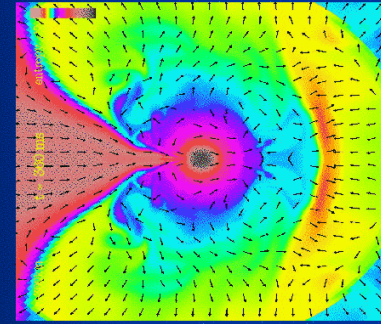
Thompson, Quataert, and Burrows 2004





Blondin et al.

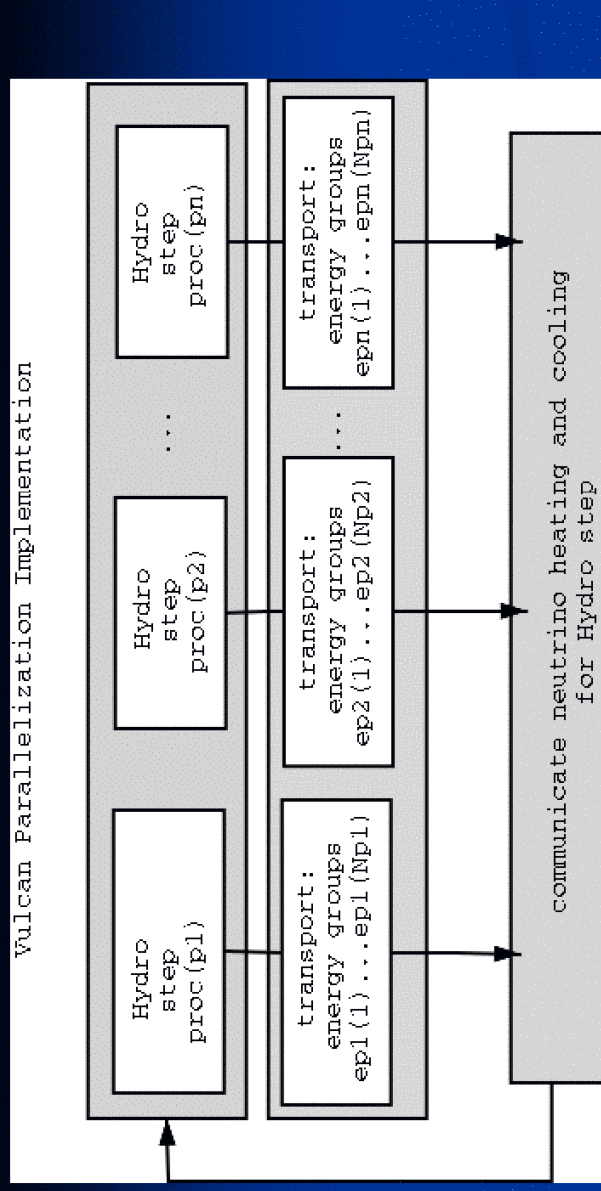
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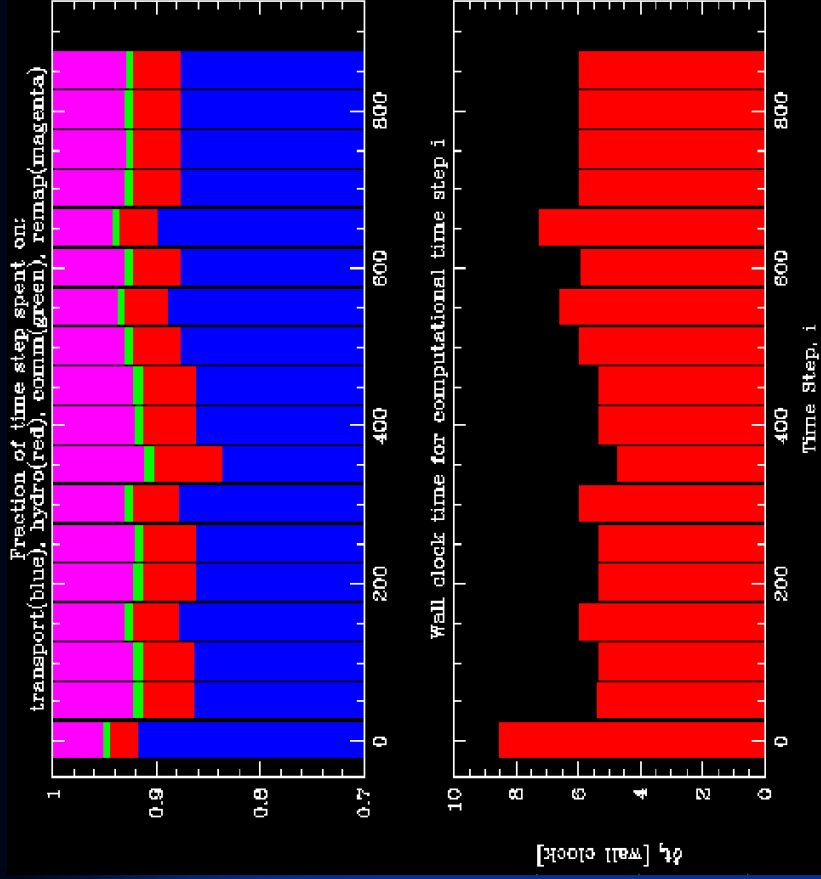
## VULCAN/2D Multi-Group, Multi-Angle, Time-dependent Boltzmann/Hydro (6D)

- Arbitrary Eulerian-Lagrangian (ALE); remapping
- 6 - dimensional (1(time) + 2(space) + 2(angles) + 1(energy-group))
- Moving Mesh (FE)
- **2D multi-group, multi-angle**,  $S_n$  (~150 angles), time-dependent, **implicit transport** (still slow)
- Axially-symmetric; **Rotation**
- Flux-conservative; smooth matching to diffusion limit
- Velocity-dependent terms: convective can be included if desired (DI/dt), but not yet Doppler/Aberration terms: will be handled explicitly
- Energy redistribution: explicit (done in 1D, not yet 2-D)
- Has a **2D MGFLD, rotating** version
- New **Implicit Hydro** version
- Livne, Burrows et al. (2004), Ap.J., 609, 277
- Walder et al. (2004), Ap.J., submitted
- Burrows et al. (2005), in preparation



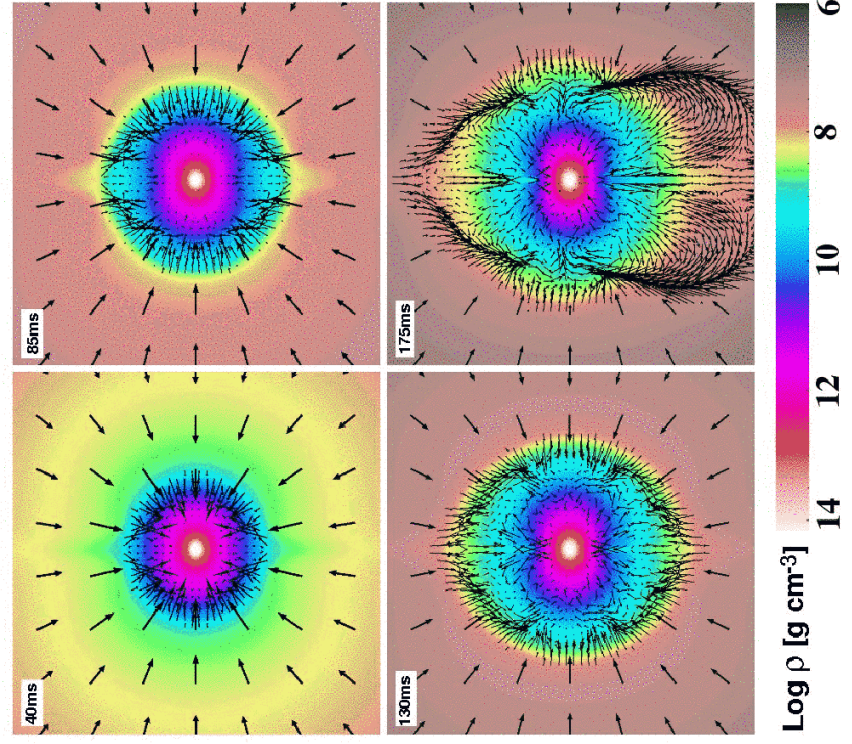
VULCAN/2D  
Numerical  
Paradigm





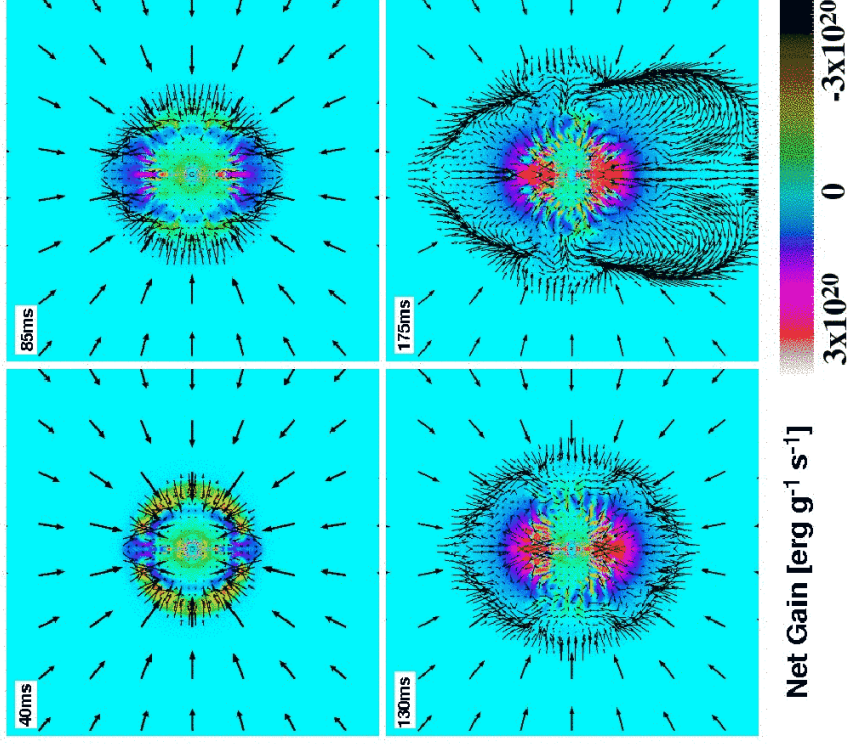
VULCAN/2D Timing

Density Contours  
For  $\Omega=2.68 \text{ rad s}^{-1}$ :

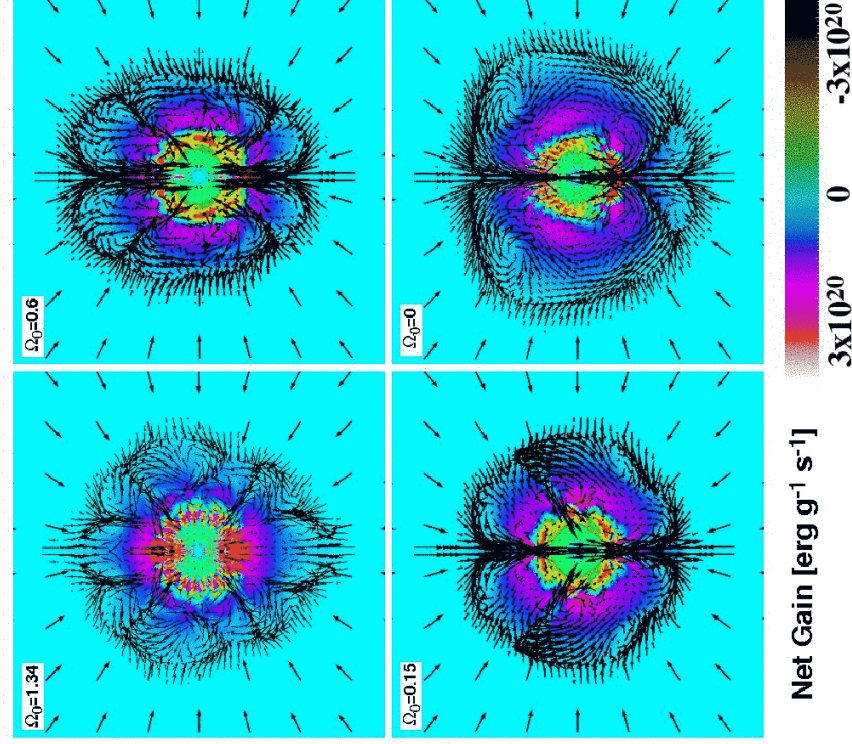


$\Omega = 2.68 \text{ rad s}^{-1}$ :

Net Gain:

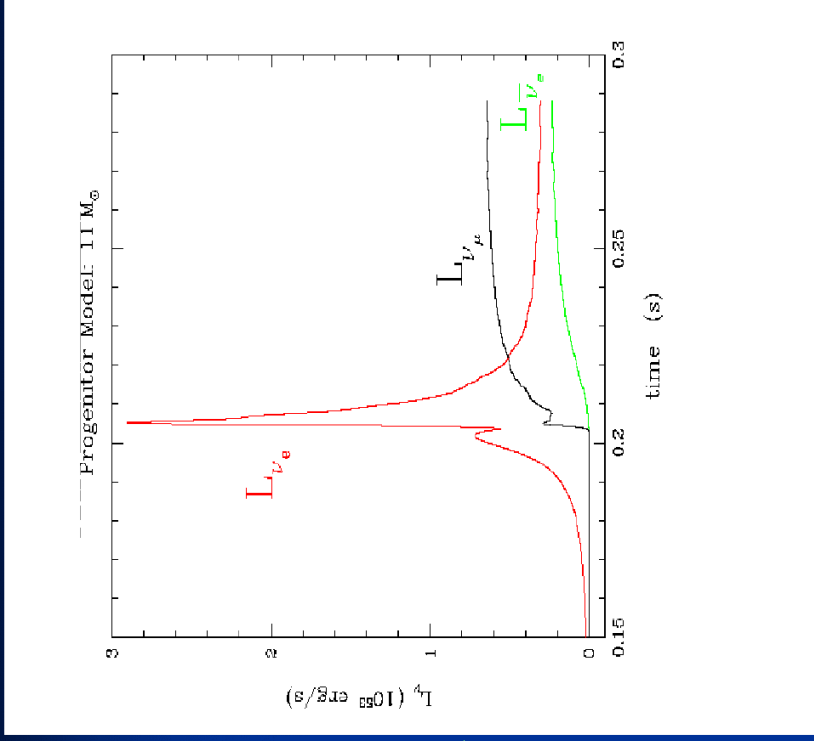


Net Gain at 175 ms:  
(Various spin rates)





Breakout Burst of Neutrinos: Precision Boltzmann Transfer



QuickTime™ and a YUV420 codec decompressor are needed to see this picture.

2D MGFLD: Entropy and Neutrino Flux (7.8 MeV)

QuickTime™ and a  
Photo decompressor  
are needed to see this picture.

2D MGFLD: Neutrino Energy Density and Flux (7.8 MeV)

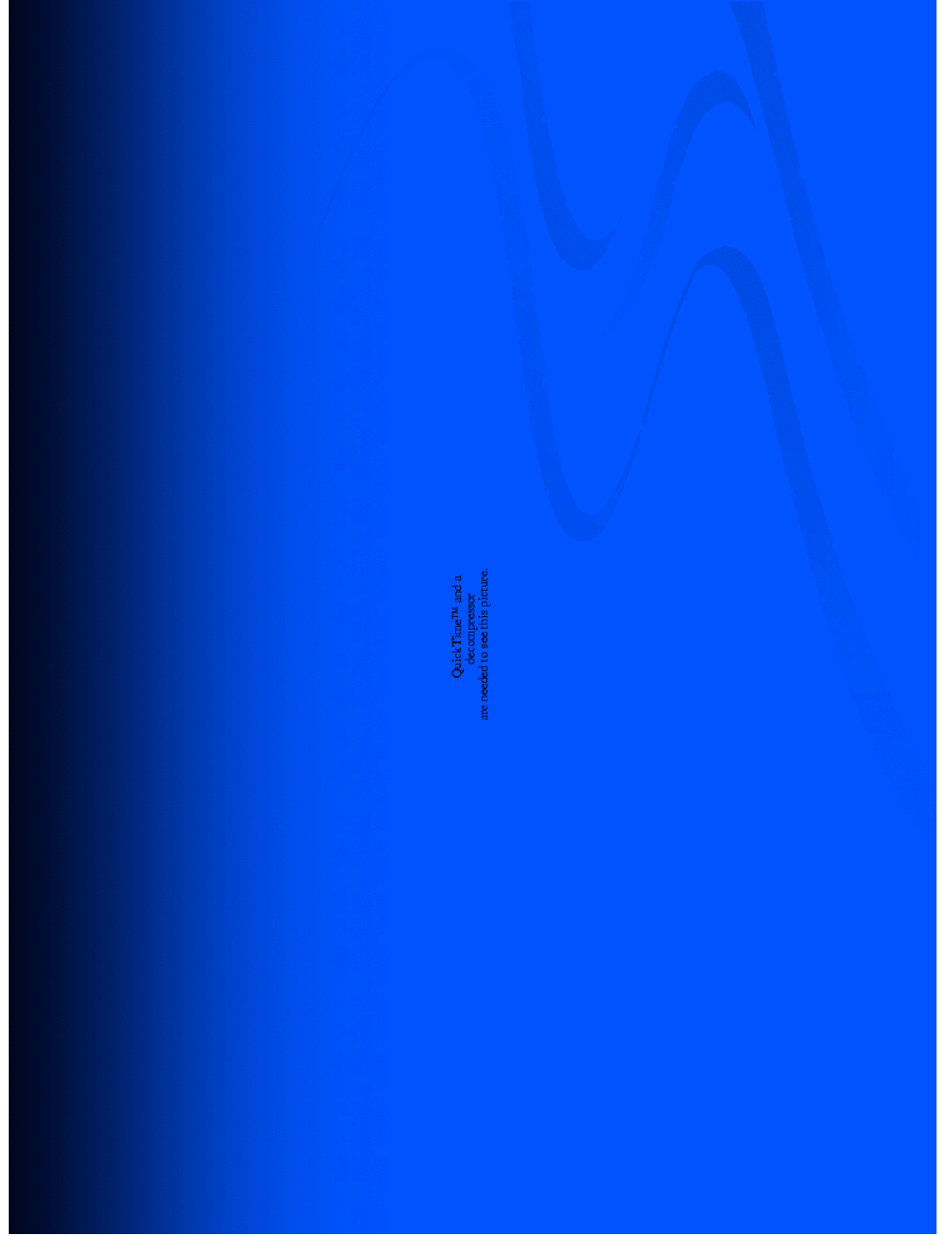
QuickTime™ and a  
Photo decompressor  
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2D MGFLD Rotating Collapse, Bounce, and Convection

QuickTime™ and a  
Photo decompressor  
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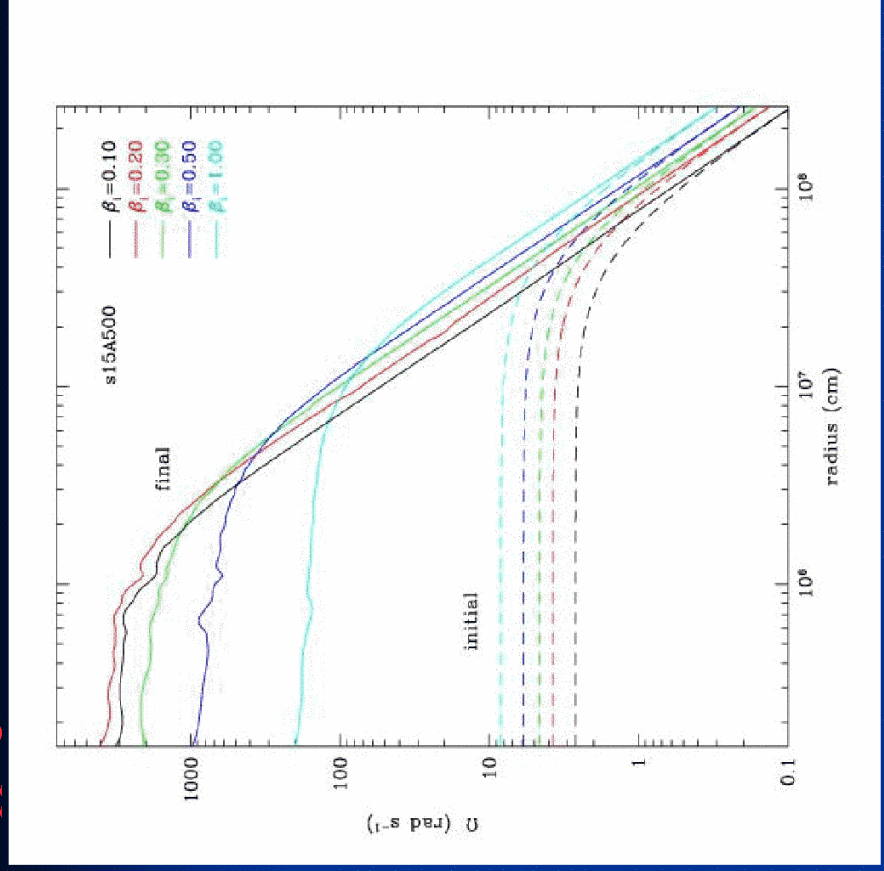
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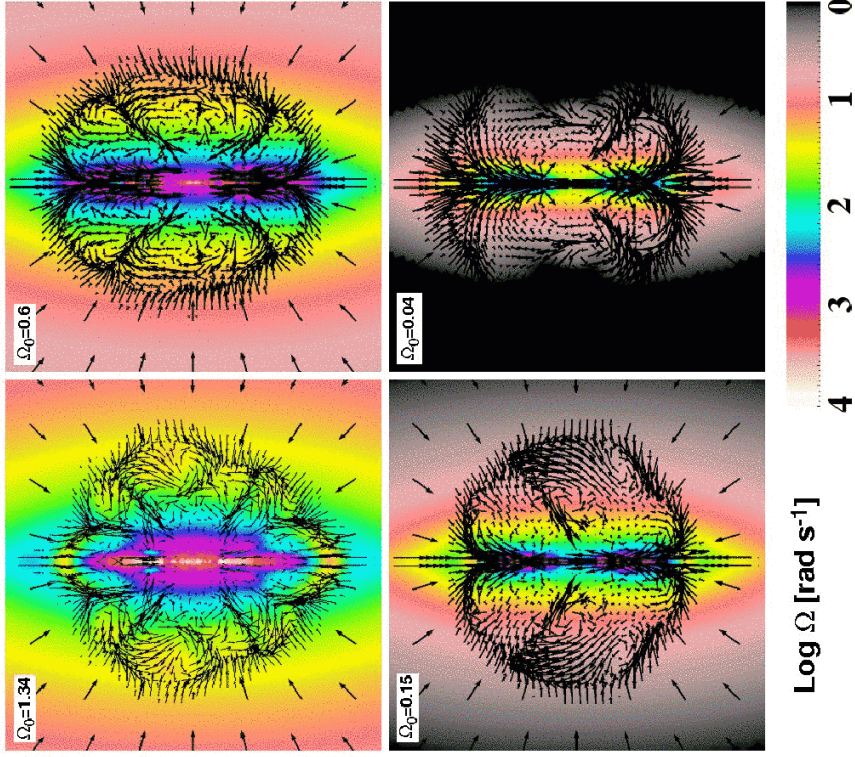




Mapping between Initial and ‘Final’ Rotation Rates

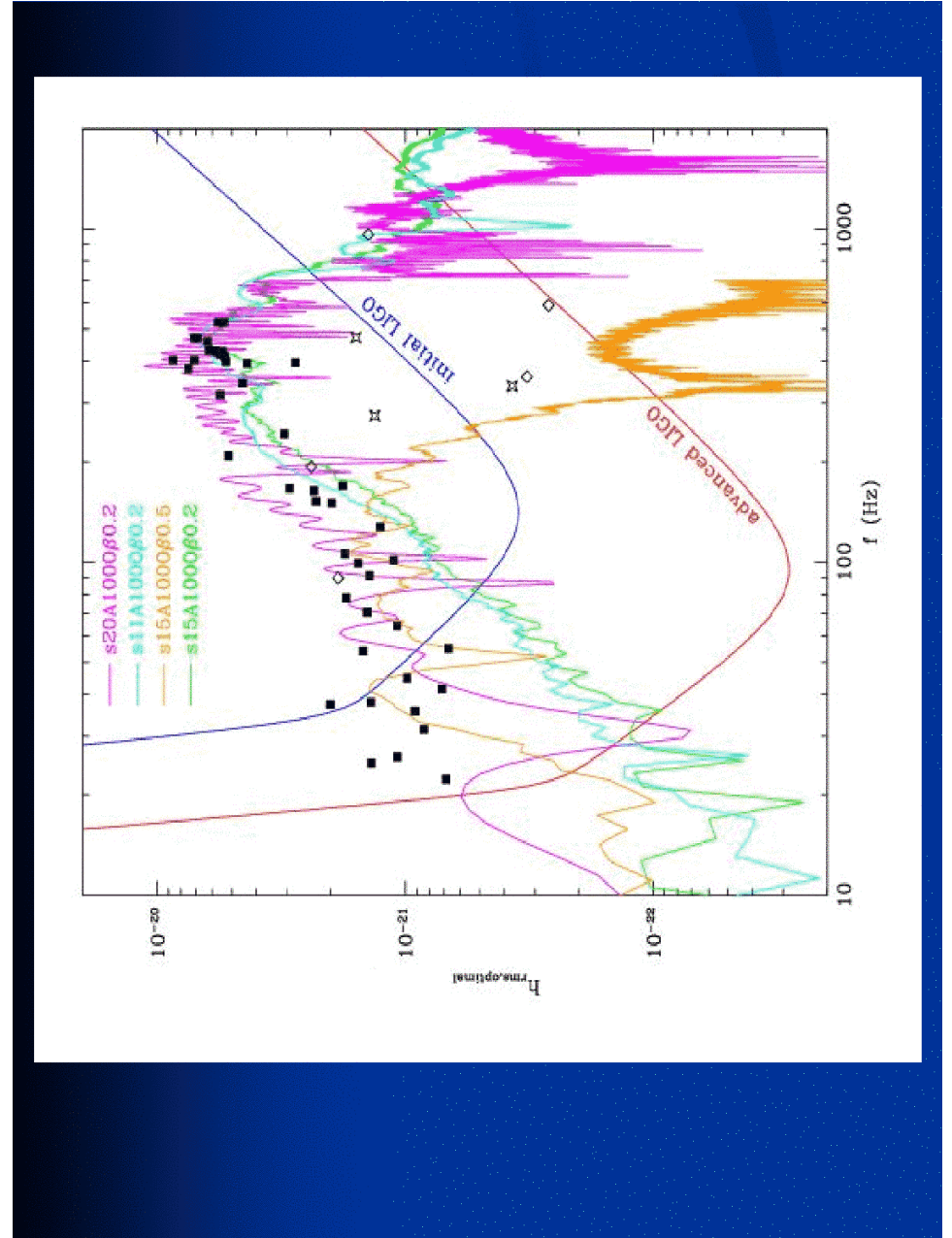
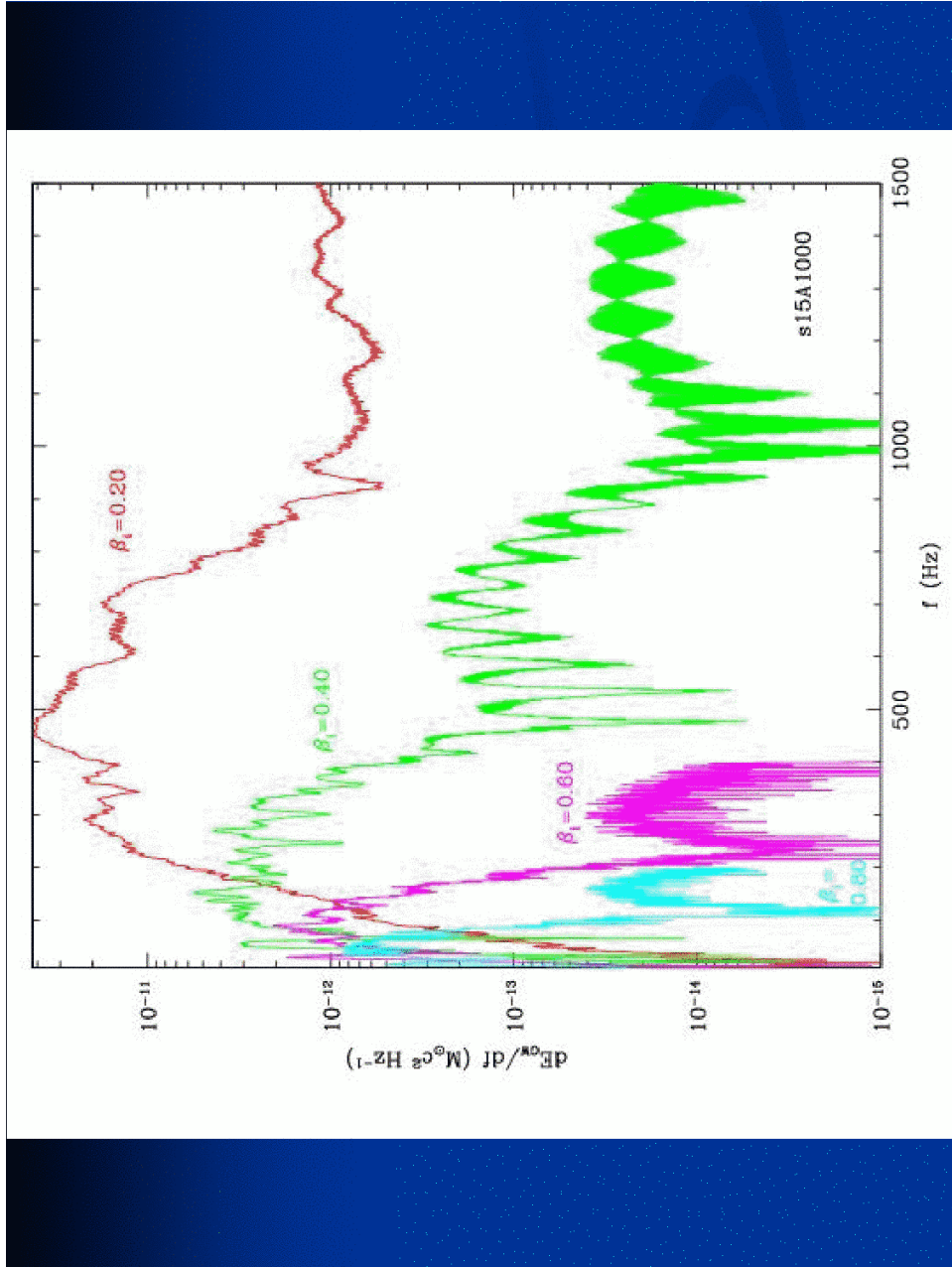


Angular Velocity  
Contours at 175 ms:

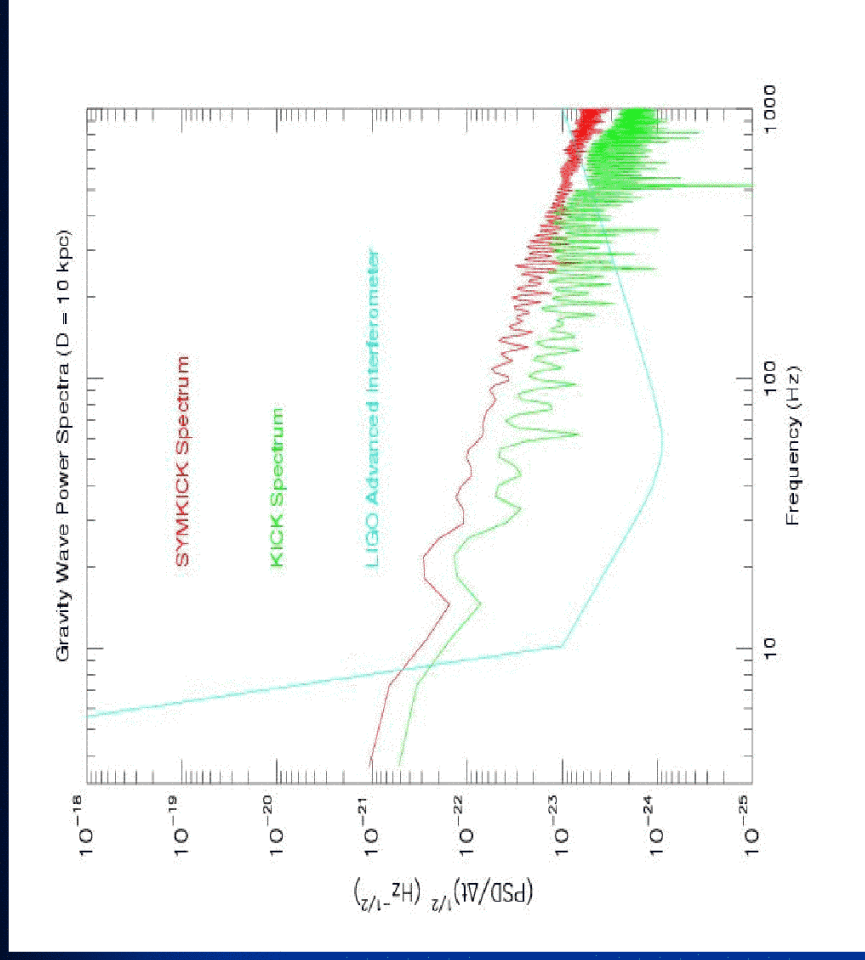


QuickTime™ and a  
Photo decompressor  
are needed to see this picture.





## Gravitational Waves off Neutrinos

Mixed-Frame Transport in 2<sup>1/2</sup>-D

- $\sigma_0, \kappa_0, \eta_0$  in Comoving frame (continuum opacities)
- $I(\nu, \mathbf{n})$  in Laboratory frame (generalization of MK82)
- Lorentz transformation to  $O(\nu/c)$
- Anisotropic scattering
- 0th and 1st moment equations
- 2<sup>1/2</sup>-D Cylindrical and Spherical coordinates
- Eddington tensor: 5 independent components

(Hubeny and Burrows 2005)



# Mixed-Frame Transport (cont.)

- Angular momentum, momentum, and neutrino viscosity
- Implicit transport
- ALI: Two-stepped solution method
- Preconditioning: Angle-averaged source function ( $S_2 \rightarrow S_n$ )
- Discontinuous Finite Element (DFE)
- Topological ordering: upwind to downwind
- Feautrier technique

## Mixed-Frame Transport Equations

(A generalization of Mihalas & Klein (1982), taking into account anisotropic scattering and the energy dependence of the scattering rate.)

$$\left( \frac{1}{c} \frac{\partial}{\partial t} + \mathbf{n} \cdot \nabla \right) I(\nu, \mathbf{n}) = \eta^{\text{th}}(\nu, \mathbf{n}) + \eta^{\text{sc}}(\nu, \mathbf{n}) - [\kappa(\nu, \mathbf{n}) + \sigma(\nu, \mathbf{n})] I(\nu, \mathbf{n}) \quad (1)$$

$$\kappa(\nu, \mathbf{n}) = \kappa_0(\nu) - \frac{\mathbf{n} \cdot \mathbf{v}}{c} \left[ \kappa_0(\nu) + \nu \frac{\partial \kappa_0}{\partial \nu} \right] \quad (2)$$

$$\sigma(\nu, \mathbf{n}) = \sigma_0(\nu) - \frac{\mathbf{n} \cdot \mathbf{v}}{c} \left[ \sigma_0(\nu) + \nu \frac{\partial \sigma_0}{\partial \nu} \right] \quad (3)$$

$$\eta^{\text{th}}(\nu, \mathbf{n}) = \eta_0^{\text{th}}(\nu) + \frac{\mathbf{n} \cdot \mathbf{v}}{c} \left[ 2\eta_0^{\text{th}}(\nu) - \nu \frac{\partial \eta_0^{\text{th}}}{\partial \nu} \right] \quad (4)$$

$$g_0(\mathbf{n}'_0, \mathbf{n}_0) = 1 + \delta \mathbf{n}'_0 \cdot \mathbf{n}_0 \quad (5)$$

$$\left( \frac{1}{c} \frac{\partial}{\partial t} + \mathbf{n} \cdot \nabla \right) I(\nu, \mathbf{n}) = r_{\text{w}}(\nu, \mathbf{n}) + r_{\text{v}}(\nu, \mathbf{n}) + r_{\text{t0}}(\nu, \mathbf{n}) + r_{\text{t1}}(\nu, \mathbf{n}), \quad (6)$$

where the subscripts refer to terms which are 0-th or 1-st order in  $v/c$  and  $\delta$ , respectively.

In cylindrical coordinates:

$$\begin{aligned} \frac{1}{c} \frac{\partial I_\nu}{\partial t} + \cos\theta \frac{\partial I_\nu}{\partial z} + \frac{\sin\theta \cos\psi}{r} \frac{\partial}{\partial \theta} (r I_\nu) - \frac{\sin\theta}{r} \frac{\partial}{\partial \psi} \left( \frac{\sin\psi}{r} I_\nu \right) \\ = r_{\text{w}} + r_{\text{v}} + r_{\text{t0}} + r_{\text{t1}} \end{aligned} \quad (7)$$

(1)

$$r_{00} = \eta_0^{\text{th}} - (\kappa_0 + \sigma_0) I(\nu, \mathbf{n}) + \sigma_0 J, \quad (1)$$

(2)

$$r_{01} = \sigma_0 \delta H^j n_j$$

$$r_{10} = n_j w^j \left[ \eta_0^{\text{th}} \left( 2 - \frac{\partial \ln \eta_0^{\text{th}}}{\partial \ln \nu} \right) + \kappa_0 \left( 1 + \frac{\partial \ln \kappa_0}{\partial \ln \nu} \right) I(\nu, \mathbf{n}) \right] + n_j w^j \left[ \sigma_0 \left( 1 + \frac{\partial \ln \sigma_0}{\partial \ln \nu} \right) I(\nu, \mathbf{n}) + \sigma_0 J \left( 2 - \frac{\partial \ln \sigma_0}{\partial \ln \nu} - \frac{\partial \ln J}{\partial \ln \nu} \right) \right] - \sigma_0 w_j H^j \left( 1 - \frac{\partial \ln H^j}{\partial \ln \nu} \right) \quad (3)$$

$$r_{11} = -\sigma_0 \delta \left[ n_j w^j J + n_j w_k K^{jk} \left( 2 - \frac{\partial \ln K^{jk}}{\partial \ln \nu} \right) \right] - \sigma_0 \delta H^j \left[ w_j + n_j n_k w^k \left( 1 + \frac{\partial \ln \sigma_0}{\partial \ln \nu} + \frac{\partial \ln H^j}{\partial \ln \nu} \right) \right] \quad (4)$$

## The Moment Equations (cylindrical coordinates):

$$\frac{1}{c} \frac{\partial J}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (\tau H_r) + \frac{\partial H_z}{\partial z} = \eta_0 - \kappa_0 J + \chi_r H_r w_r + \chi_z H_z w_z + \chi_\phi H_\phi w_\phi \quad (1)$$

$$\frac{1}{c} \frac{\partial H_r}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (\tau f_{rr} J) + \frac{\partial}{\partial z} (f_{rz} J) - \frac{1 - f_{rr} - f_{zz}}{r} J = -(\kappa_0 + \sigma_{\text{tr}}) H_r + w_r \tilde{\eta}_0 + \xi_r J \quad (2)$$

$$\frac{1}{c} \frac{\partial H_z}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (\tau f_{rz} J) + \frac{\partial}{\partial z} (f_{zz} J) = -(\kappa_0 + \sigma_{\text{tr}}) H_z + w_z \tilde{\eta}_0 + \xi_z J \quad (3)$$

$$\frac{1}{c} \frac{\partial H_\phi}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (\tau f_{r\phi} J) + \frac{\partial}{\partial z} (f_{z\phi} J) = -(\kappa_0 - \sigma_{\text{tr}}) H_\phi + w_\phi \tilde{\eta}_0 + \xi_\phi J \quad (4)$$

$$\xi_r = \tilde{\sigma}_2 w_r + (\tilde{\kappa}_0 + \tilde{\sigma}_3) (f w)_r + \frac{\sigma_0 \delta}{3} (\partial f w)_r + \frac{\partial \ln J}{\partial \ln \nu} \frac{\sigma_0}{3} [-w_r + \delta (f w)_r] \quad (5)$$

$$(f w)_r = f_{rr} w_r + f_{rz} w_z + f_{r\phi} w_\phi \quad (6)$$

$$(f w)_z = f_{rz} w_r + f_{zz} w_z + f_{z\phi} w_\phi \quad (7)$$

$$(f w)_\phi = f_{r\phi} w_r + f_{z\phi} w_z + f_{\phi\phi} w_\phi \quad (8)$$

and

$$(\partial f w)_r = \frac{\partial}{\partial \ln \nu} (f w)_r = \frac{\partial f_{rr}}{\partial \ln \nu} w_r + \frac{\partial f_{rz}}{\partial \ln \nu} w_z + \frac{\partial f_{r\phi}}{\partial \ln \nu} w_\phi \quad (9)$$

$$\chi_\phi = \tilde{\kappa}_0 + \tilde{\sigma}_1 + \sigma_{\text{tr}} \frac{\partial \ln H_\phi}{\partial \ln \nu} \quad (10)$$



## Core-Collapse Supernovae: The Future

- Collapse/Explosion **instabilities** and **rotation**: **Multi-D**
- Instabilities are generic
- **Neutrino-driven?**
- “**Vortical-acoustic**” instability,  $l=1$ ?
- **Multi-D radiation hydrodynamics**
- Is there an important role for Rotation?
- Is there a role for **Magnetic fields**? Pulsar fields?
- **Viscosity?** viscous heating and angular momentum transport
- Equation of state?
- Neutrino rates?
- Systematics with progenitor of observables/diagnostics?
- GRB/SN connection
- **Pulsar kicks**; black hole formation

QuickTime™ and a  
YUV420 codec decompressor  
are needed to see this picture.

## Computational Nuclear Astrophysics

- Core-Collapse Supernovae (Grid-based & Statistical methods)
- Thermonuclear Supernovae (Type Ia)
- Gamma-Ray Bursts
- X-ray Bursts
- Stellar Convection simulations (2D/3D)
- World-class Nuclear Data Archive
- 1-2-3-D Radiation/Hydrodynamics
- Astrophysical Flame Physics
- Collaboratory- Vertically Integrated Nuclear Astrophysics: Stellar Evolution -Nucleosynthesis - Supernova Explosions - Light Curves

## Codes and Capabilities

- 2D/3D Anelastic hydro; spectral methods (+MHD) (Glatzmaier)
- VULCAN/2D Boltzmann/hydro (6D) (TOPS)
- Implicit Stellar Evolution (Kepler)
- 2D/3D Stellar Evolution
- 3D Hydro/diffusion for core collapse (SPH)
- 2D/3D Thermonuclear combustion (APDEC)
- FLASH 2D/3D Hydro code
- 3D Monte Carlo radiation transport
- 3D Special-relativistic hydro (GRBs)
- Nuclear Network solver(s)
- Visualization infrastructure at Arizona (Hariri)



## Main Computers and Platforms

- NERSC/seaborg
- ORNL/cheetah, eagle
- Beowulfs at LANL, UCSC, U.Arizona
- ASCI Q (LANL)

## Major Accomplishments

- First 3D Simulation of Core-Collapse Supernova (Diffusion)
- First 2D Boltzmann Rad/Hydro Simulation in Core Collapse: Multi-group, multi-angle
- First Full Core-Collapse Simulation with 2D MGFLD
- First 3D Relativistic GRB Jet Calculation
- First Fully-Resolved 3D Rayleigh-Taylor Nuclear Burning Study in Type Ia Supernova Context and 3D Simulation of Onset of Ignition
- First 1600-Species Nuclear Network Calculation for X-Ray Bursts
- Assembly of the World's Most Comprehensive Nuclear Reaction Database
- 3D Stellar Convection simulations: sun, massive stars

Color Map: Ye

Vectors: Flux

Multi-Group

Multi-Angle

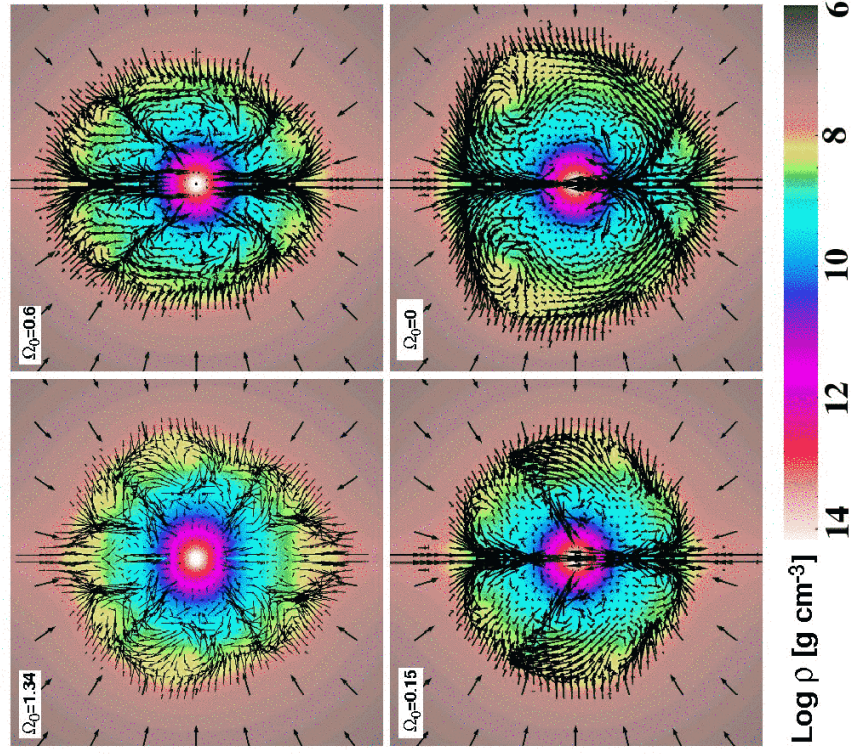
Boltzmann

Transport

Livne, Burrows,  
et al. 2004, Ap.J.  
in press

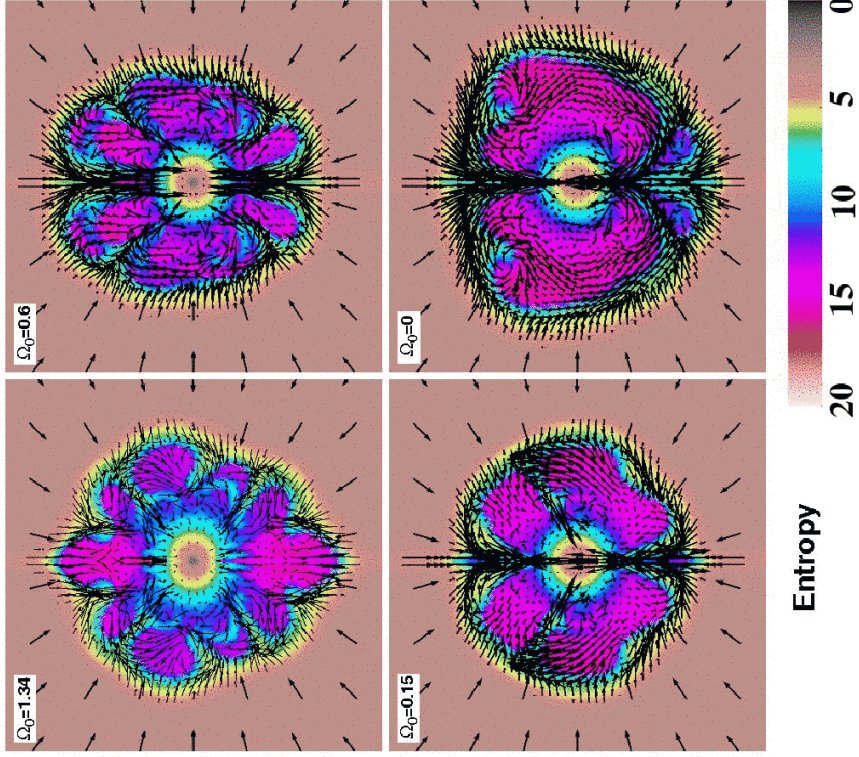
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Densities for Various  
 $\Omega$ 's at 175 ms:



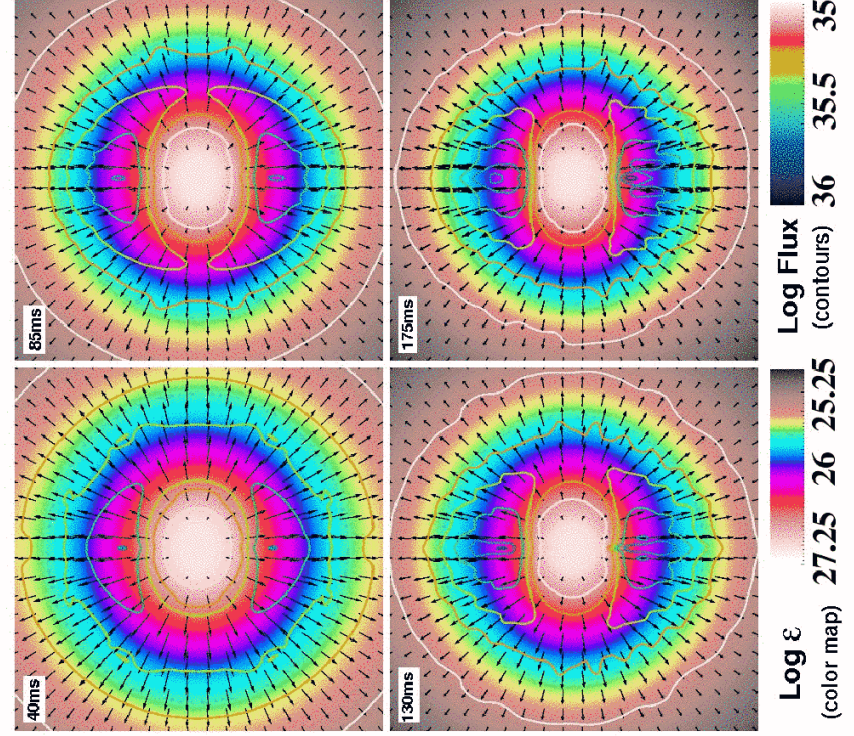


Entropy at 175 ms:



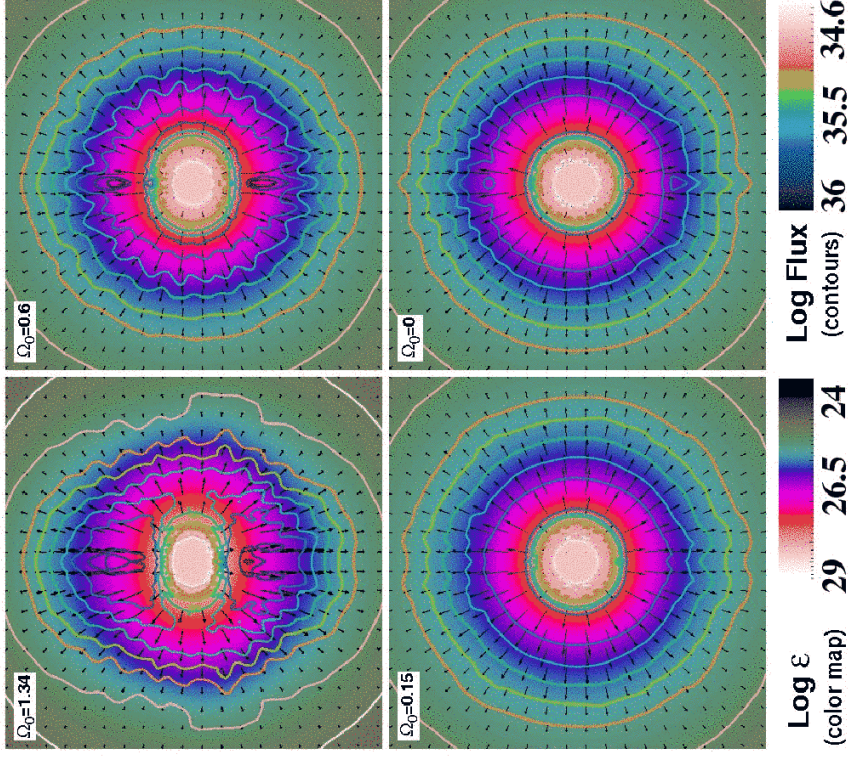
Electron Neutrinos  
At 6.89 MeV:

$\Omega_0 = 2.68 \text{ rad s}^{-1}$



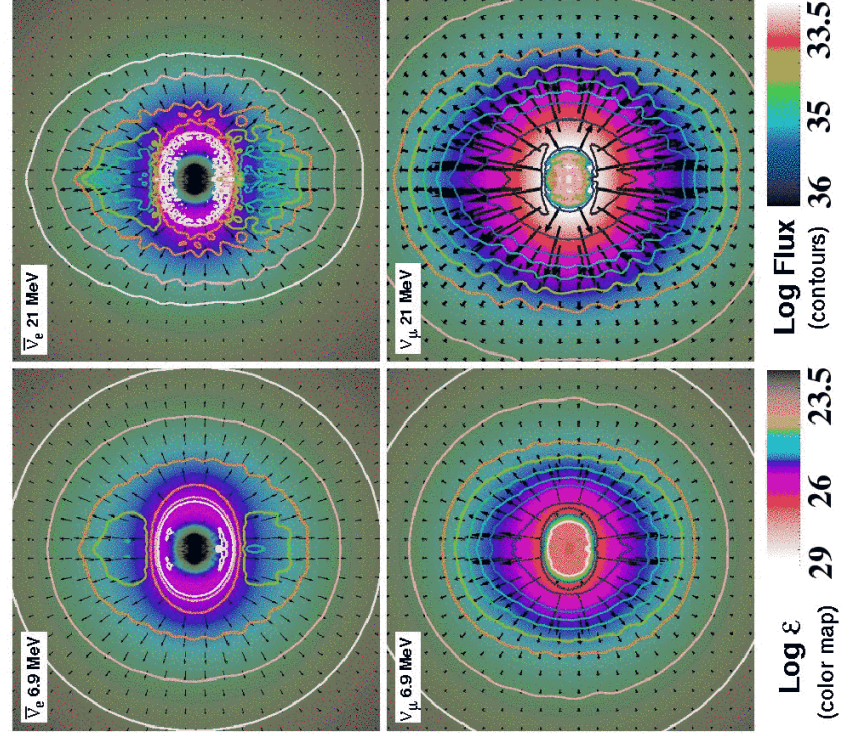


Fluxes and Spectral  
Energy Densities at  
175 ms and 6.9 MeV:

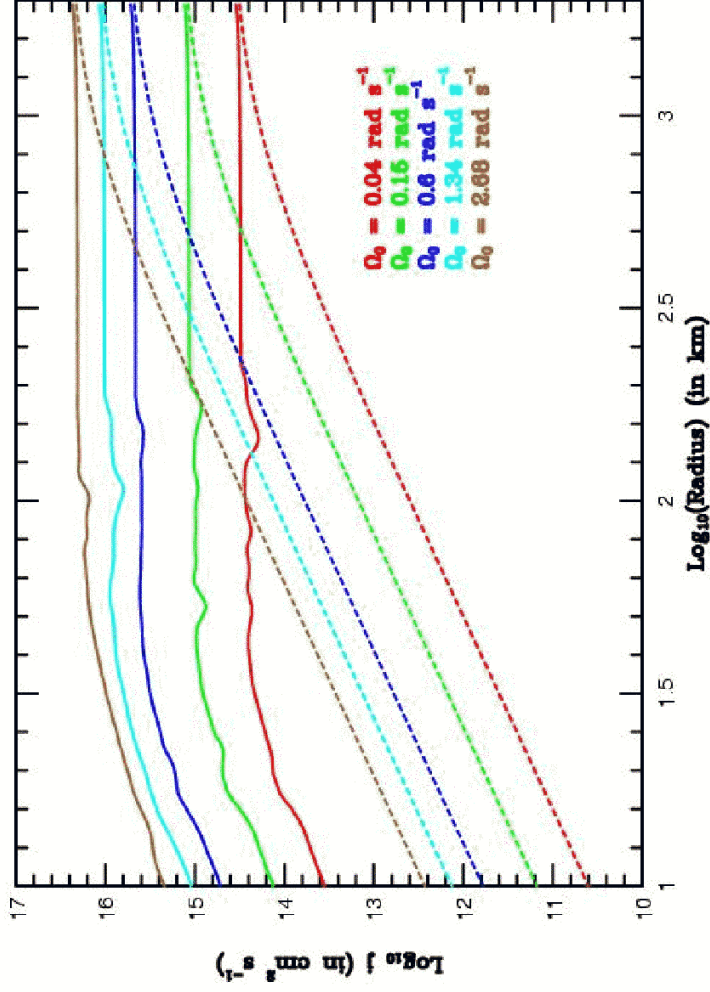


Energy- and Species-  
Dependence of  
Anisotropy for  
 $\Omega=2.68 \text{ rad s}^{-1}$ :

(At 175 ms)







20 Solar Masses  
 Modest Rotation  
 Torus Formation

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 Photo decompressor  
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2D MGFLD Rotating Collapse, Bounce, and Convection

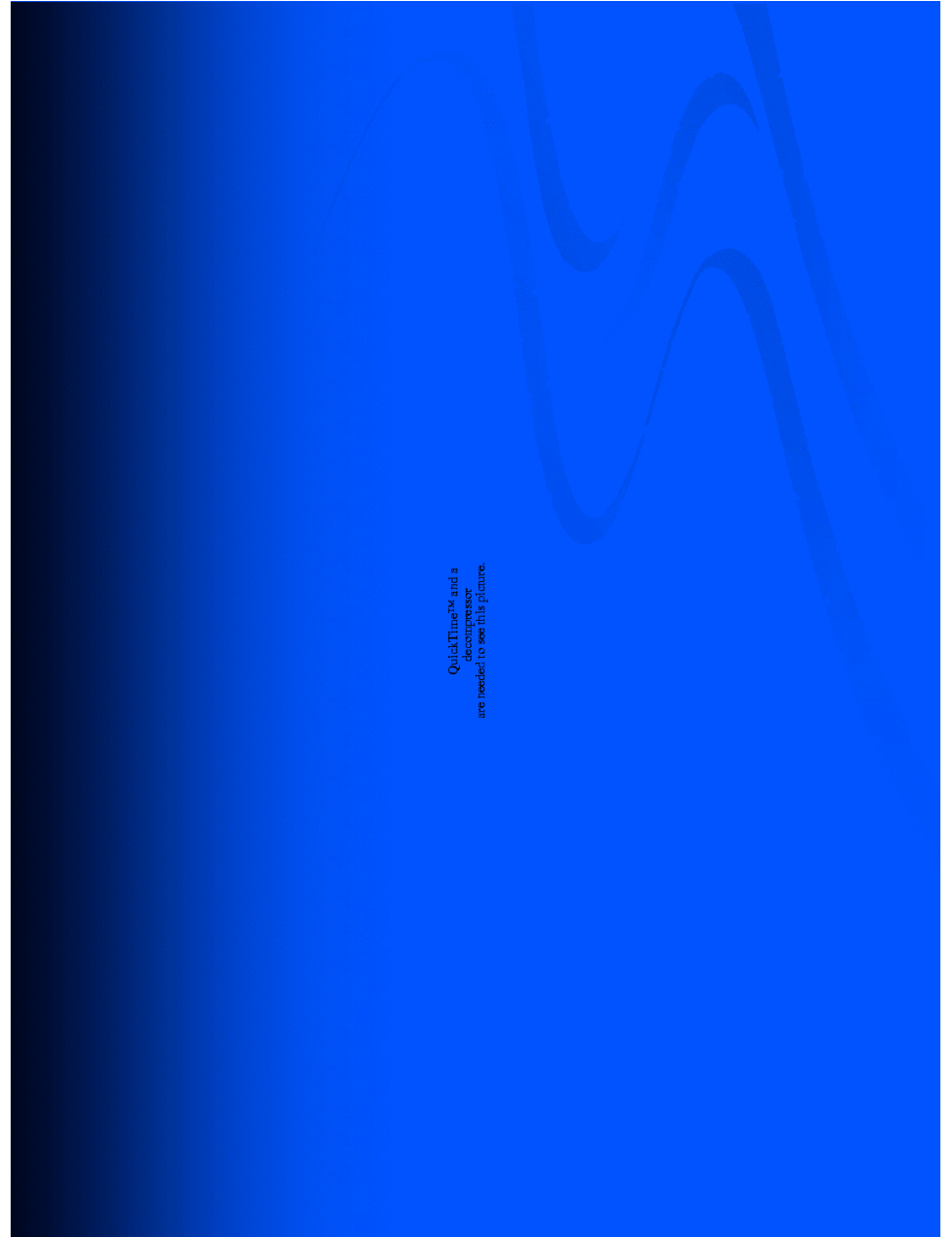
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2D MGFLD Rotating Collapse, Bounce, and Convection

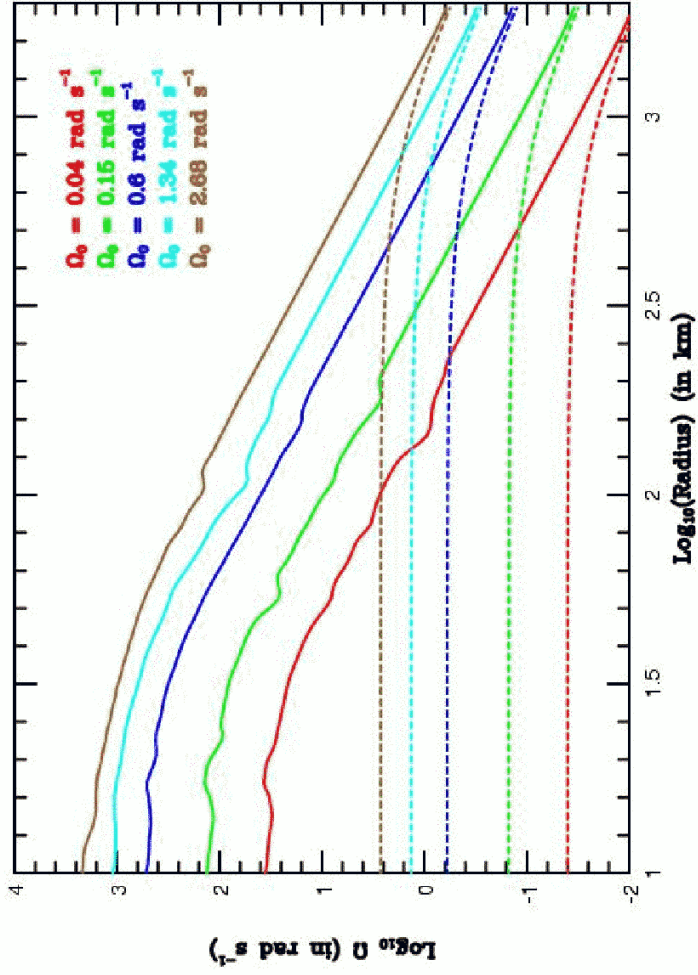
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QuickTime™ and a  
decompressor  
are needed to see this picture.

