

# Activities - Realistic Theories of CEM

(O. Andersen, A. Georges, B. Gabriel Kotliar, A. Lichtenstein)

Nov 18 2002 - Nov 22 2002

Testing the accuracy of the xc energy  
of electronic-structure theories  
for real materials

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# Testing the accuracy of the xc energy of electronic-structure theories for real materials

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Example: surface structure and surface chemical reactions at Si(001)

Silicon is one of the best examples of a nearly free electron material

Thus, correlation is not too important, and approximate xc functionals are doing fine

**This assessment is WRONG !!!**

# Testing the accuracy of the xc energy of electronic-structure theories for real materials

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Example: surface structure and  
surface chemical reactions at Si(001)

*Phys. Rev. Lett. 87, 016105 (2001) and Phys. Rev. Lett. 89, 166102 (2002)*

*Sorcha B. Healy<sup>1</sup>, Claudia Filippi<sup>2</sup>, Eckhard Pehlke<sup>3</sup>,  
Peter Kratzer<sup>4</sup>, Evgeni Penev<sup>4</sup>, Matthias Scheffler<sup>4</sup>*

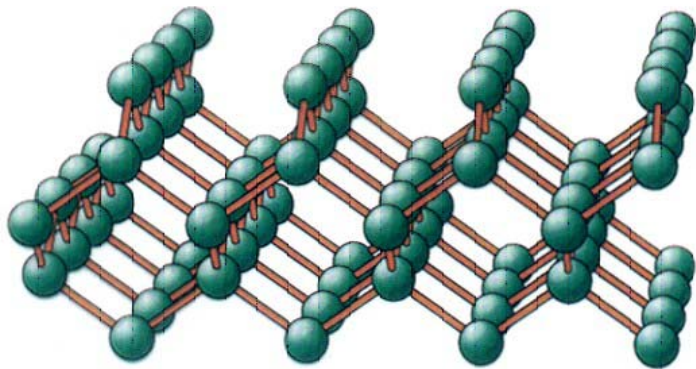
*<sup>1</sup>National University of Ireland, Cork, Ireland*

*<sup>2</sup>Universiteit Leiden, The Netherlands*

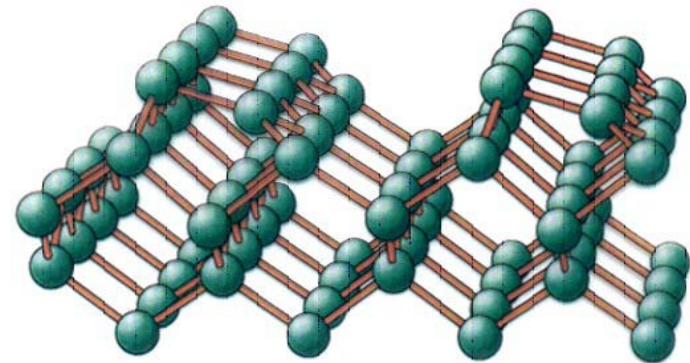
*<sup>3</sup>University of Essen, Germany*

*<sup>4</sup>Fritz-Haber-Institut der MPG, Berlin, Germany*

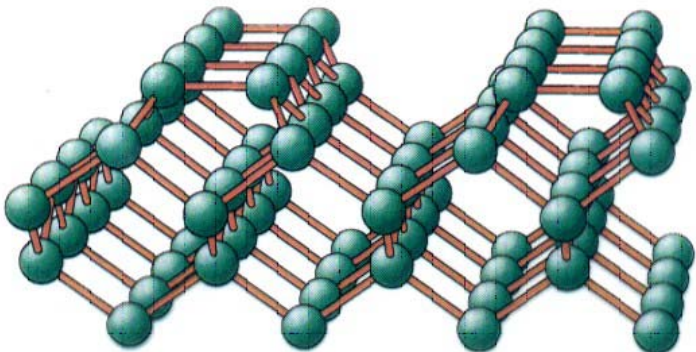
# Dimerization and dimer buckling at Si(001)



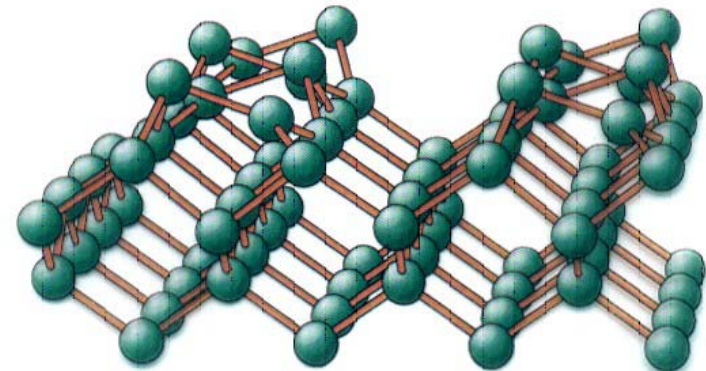
truncated bulk geometry



dimer buckling



formation of dimers



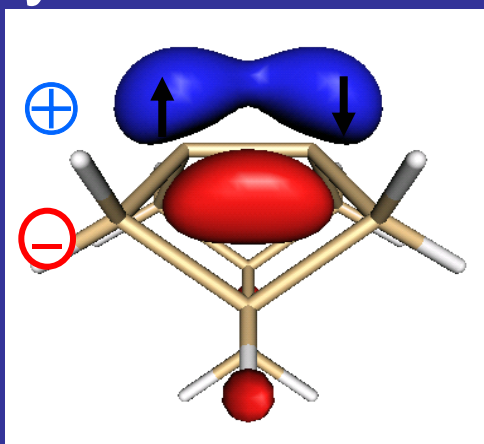
alternating buckling

# Buckling at the clean Si(001) surface is sensitive to electron correlation and electron-lattice coupling

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"A negative  $U$  system" ?

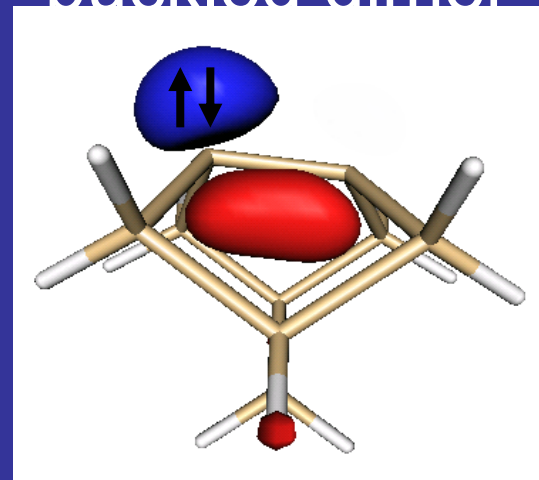
HOMO of symmetric dimer



favored by MCSCF  
(clusters)

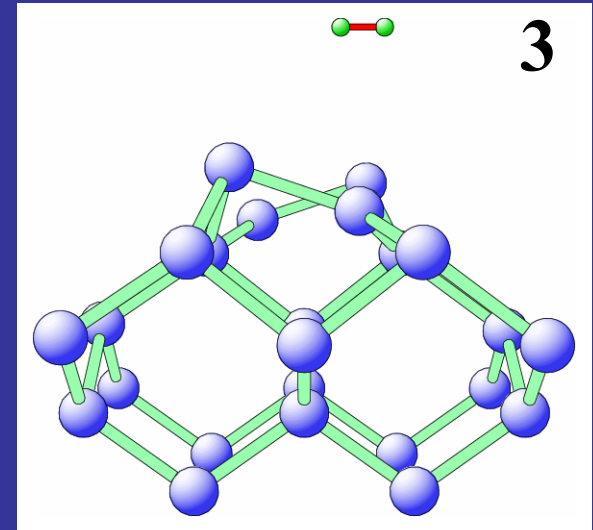
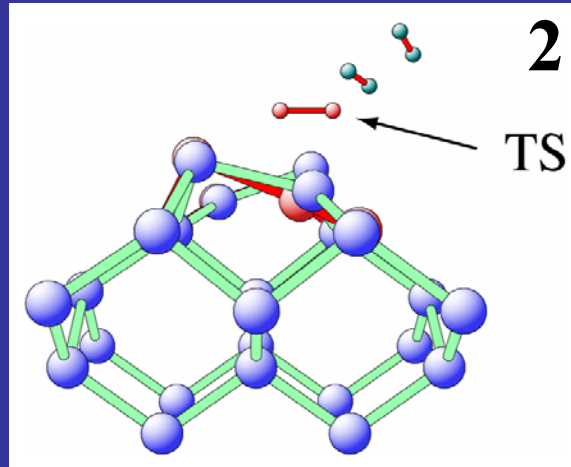
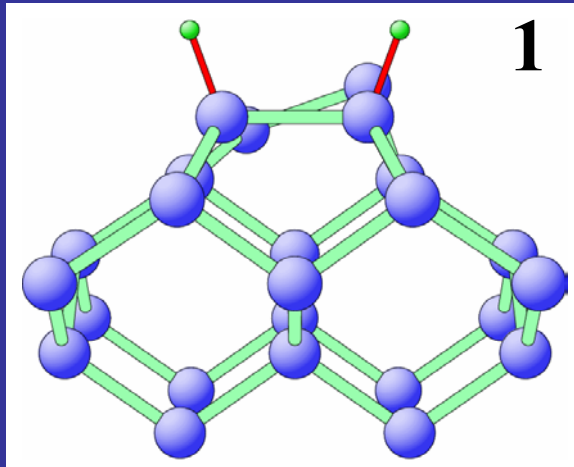
**Which configuration is the ground state ?**

HOMO of buckled dimer



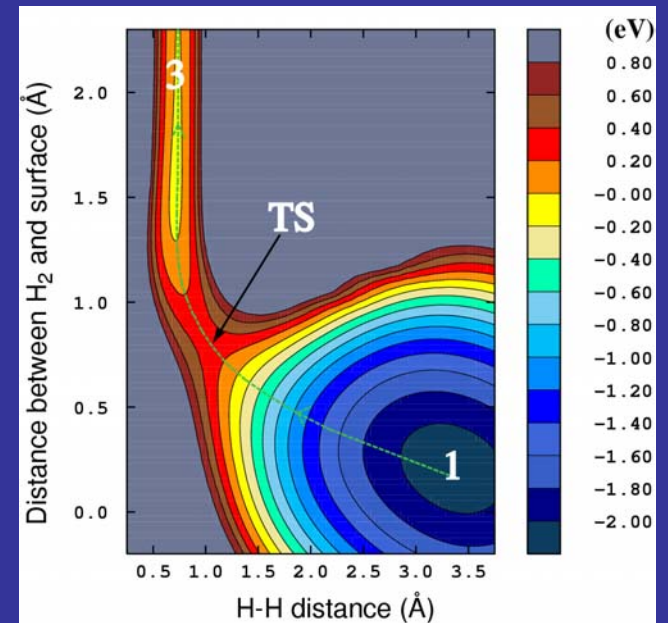
favored by DFT  
(slabs)

# The H<sub>2</sub> / Si(001) energy barrier puzzle



*A. Gross, A., M. Bockstedte, M. S., Phys. Rev. Lett. 79 (1997)*

- Adsorption experiments of H<sub>2</sub> at Si(001) show an adsorption energy barrier ( $> 0.6$  eV).
- Desorption experiments of H<sub>2</sub> from Si(001) show that there is no adsorption barrier.
- **CI and DFT calculations give very different descriptions.**



# Where do we stand with the first-principles description of materials?

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- Structure and vibrations are well described by DFT with available xc functionals !? However, for big systems (e.g. surfaces) such calculations are not a black box, and uncritical faith is not recommended [e.g. Si(001) and CO/Pt(111)].
- Errors in total energies can be noticeable. Even for energy *differences* they can be as large as several tenths of an eV.

We need to do better!!

... in particular for reaction energy barriers.

**This work: Correct the DFT xc energy by QMC.**

# Is the *direct* DFT route too complicated?

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- The xc energy,  $E_{xc}$ , stems from many-body theory.
- $E_{xc}$  is a functional of the density, but maybe impossible to handle as such. Maybe, for the accuracy we need, we have to use a "detour" (we do so already for  $T_s[n]$ ).

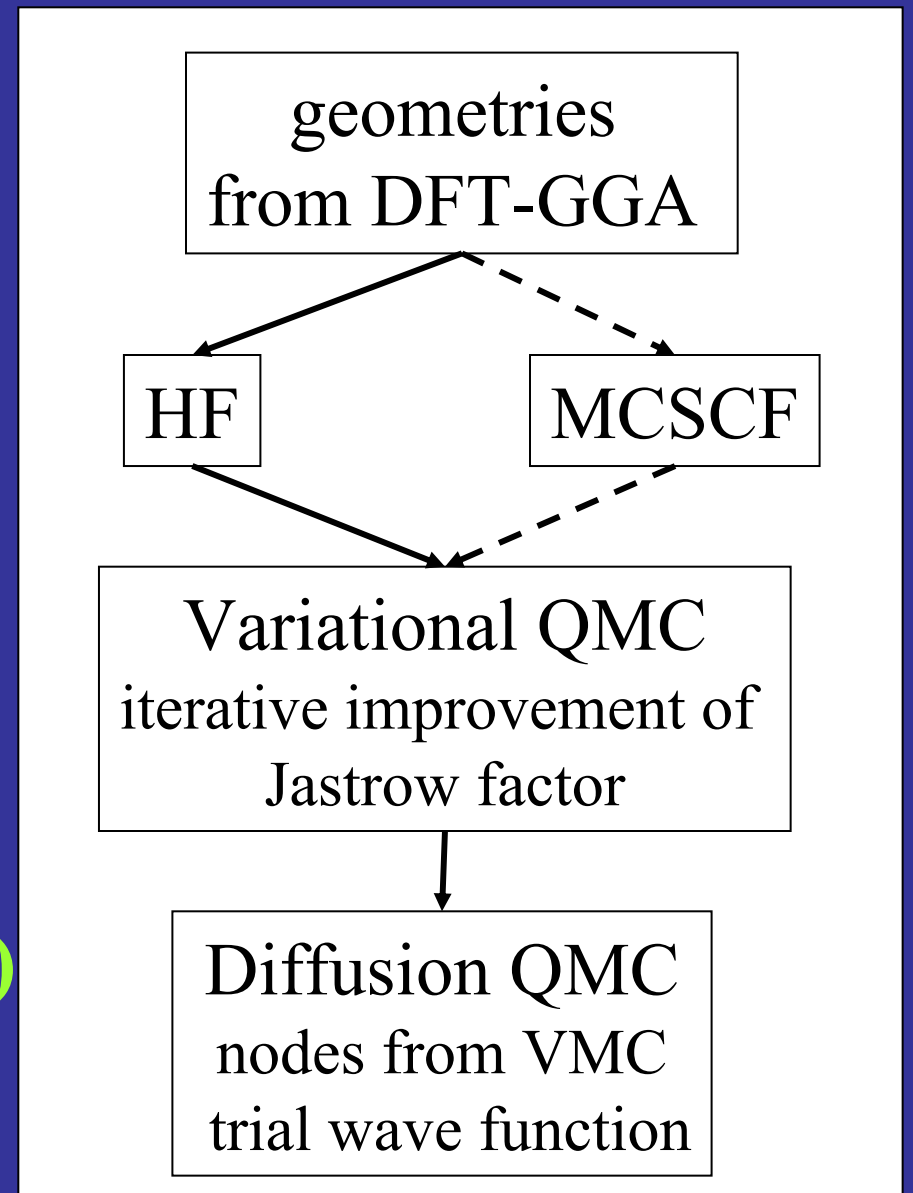
➔ Calculate a correction to  $E_{xc}^{\text{A}}[n]$  from the many-body wave function  $\Psi_0$ . (Recall:  $\Psi_0$ , is a functional of the density, as is the many-body Hamiltonian.)



# Methodology of this work

- DFT-GGA slab and cluster calculations
- QMC cluster calculations
- **correction of the DFT-GGA exchange-correlation energy**

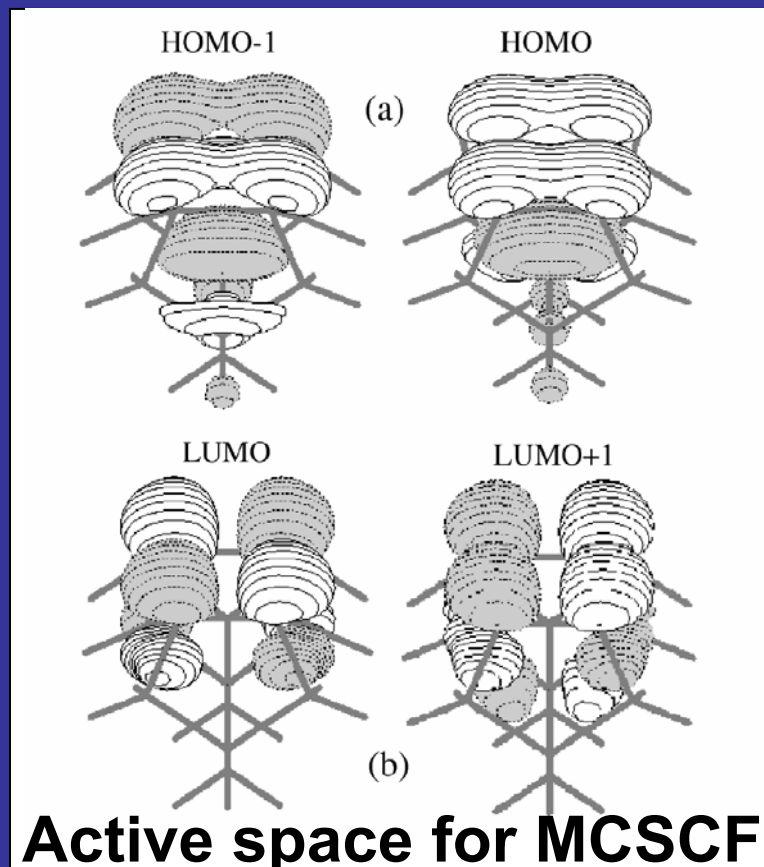
$$\Delta E_{\text{corr}} = E_{\text{cluster}}(\text{QMC}) - E_{\text{cluster}}(\text{DFT-GGA})$$



# Correlated wavefunctions in VMC

Zero-order wave function:  
Linear combination of Slater  
determinants (from HF or  
MCSCF)

$$\Psi_0(r_1, r_2, \dots, r_N) = \sum_n d_n \text{Det}_n \{ \varphi_\alpha \} \text{Det}_n \{ \varphi_\beta \}$$



Correlate this Slater wave function:

$$\Psi_T = \Psi_0 \exp(U_{corr})$$

$$U_{corr} = \sum_{i,j} \sum_I \sum_{k,l,m} c_{k,l,m} a_k(r_{ij}) b_l(r_{iI}) b_k(r_{jI})$$

# Variance minimization of the local energy to optimize the parameters

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Guess  $\Psi_T(\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_N) = \Psi_T(\mathbf{R})$

Evaluate 
$$E_T = \int \Psi_T^*(\mathbf{R}) H \Psi_T(\mathbf{R}) d\mathbf{R}$$
$$= \int \left( \frac{H \Psi_T(\mathbf{R})}{\Psi_T(\mathbf{R})} \right) |\Psi_T(\mathbf{R})|^2 d\mathbf{R}$$
$$= \int E_L(\mathbf{R}) |\Psi_T(\mathbf{R})|^2 d\mathbf{R}$$

using Monte Carlo integration

Adjust  $\Psi_T$  to minimize  $E_T$  or the variance of  $E_L$ .

# Beyond VMC: Diffusion Monte Carlo

- iterative projection technique

$$\Psi_{i+1} = \exp(-H \tau) \Psi_i$$

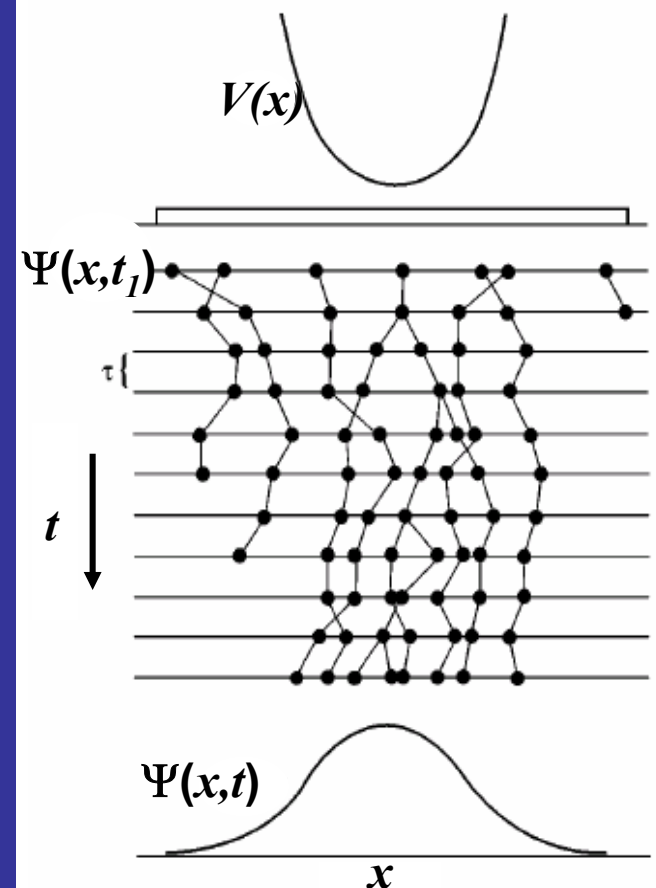
or

$$\Psi(\mathbf{R}, t+\tau) = \int d\mathbf{R}' G(\mathbf{R}, \mathbf{R}', \tau) \Psi(\mathbf{R}', t)$$

$$G(\mathbf{R}, \mathbf{R}', \tau) = \langle \mathbf{R} | e^{-H\tau} | \mathbf{R}' \rangle$$

- represent  $\Psi(\mathbf{R}, t)$  by an ensemble of 'walkers' that evolves according to the above equations
- constraint:  $\Psi$  must have unique sign in each nodal pocket  
→ fixed node approximation

schematic example  
for harmonic potential



*Example:*

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*The importance of correlations for  
Si(001) and H<sub>2</sub> adsorption and  
desorption at Si(001)*

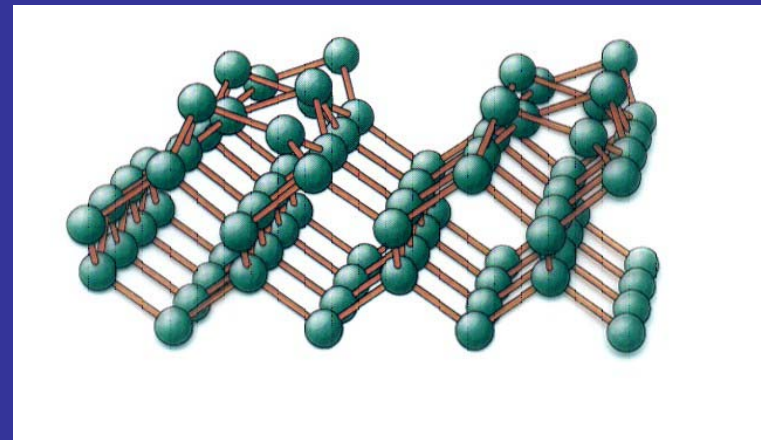
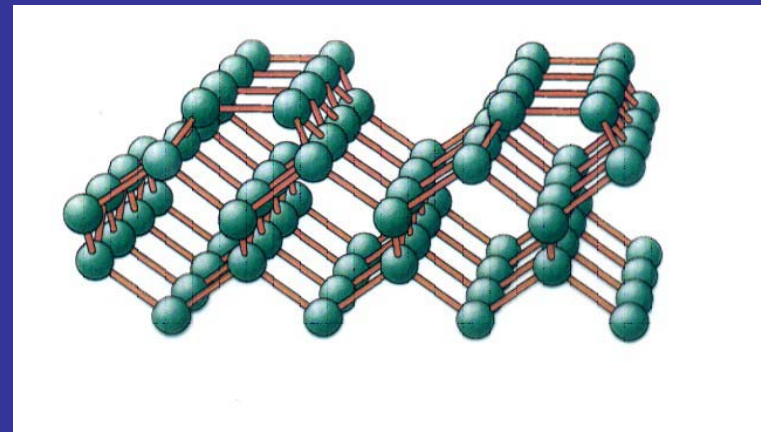
# Clean Si(001): experimental Results

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## STM

- Room temperature: symmetric dimers
- below 120 K: buckled dimers
- below 20 K: symmetric dimers

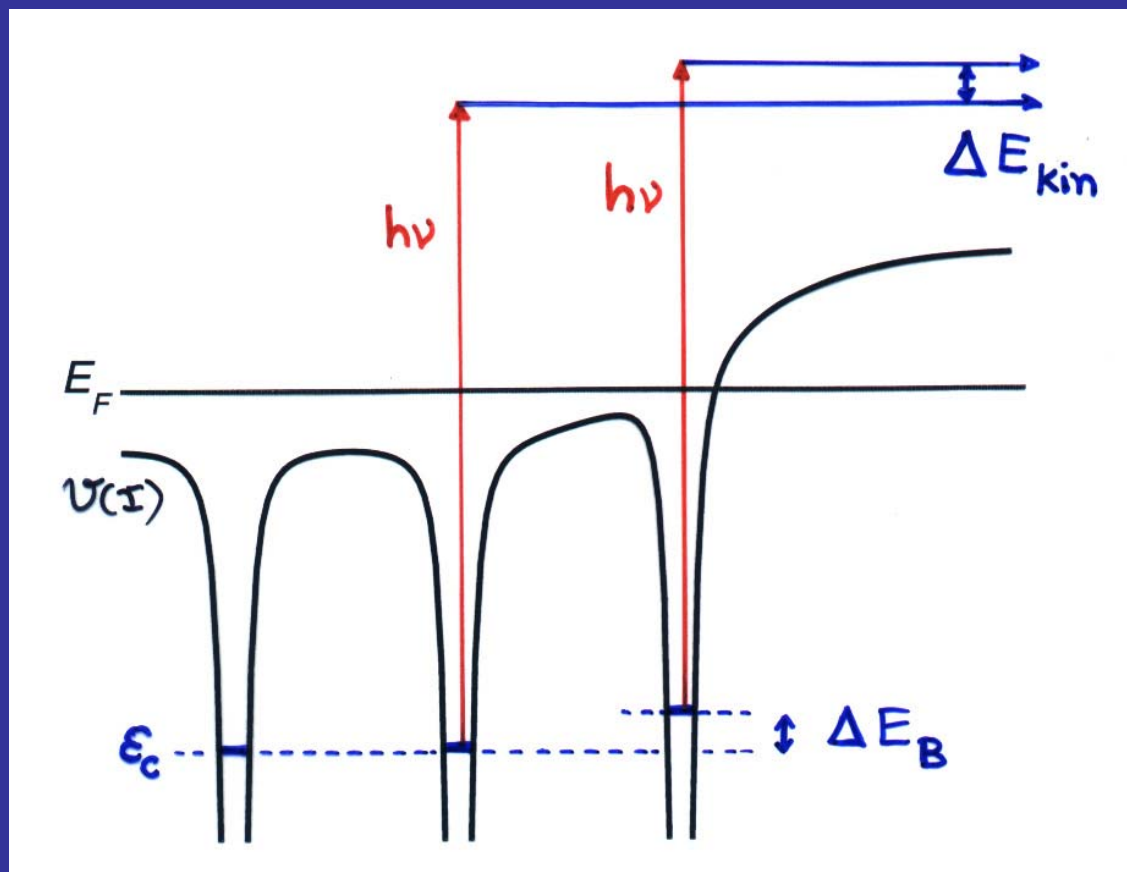


## SLCS

- buckled dimers

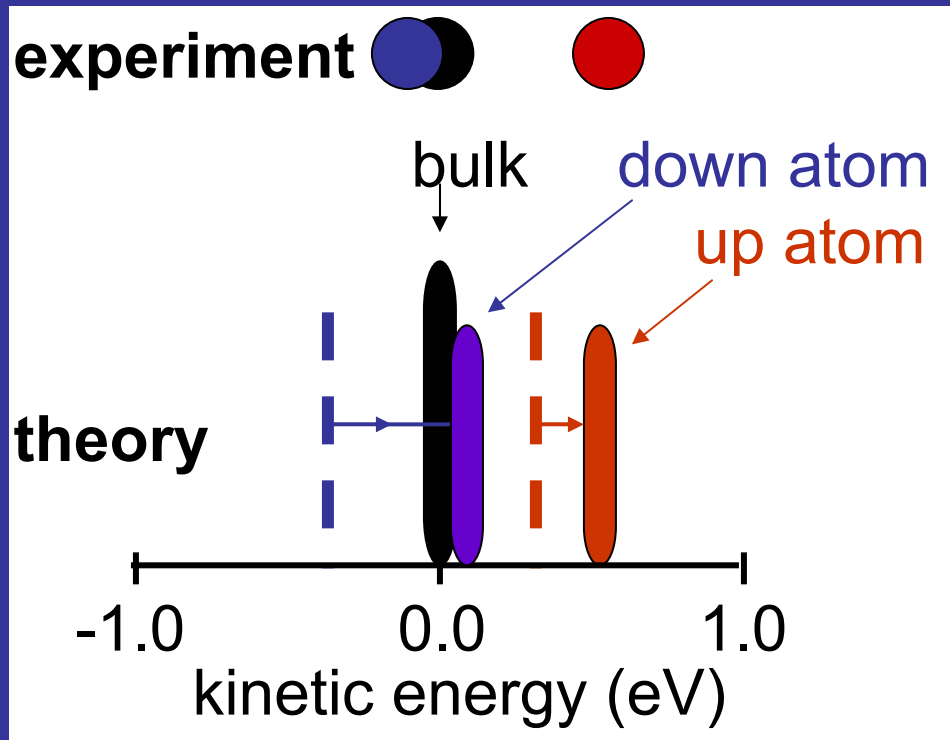
# Surface core level shifts (SCLS or ESCA)

Important tool for surface analysis (identification of atoms, electronic structure, nature of bonding).



Often surface core-level shifts are interpreted as an **initial-state effect**.

# Si $2p$ SCLS for Si(001) p(2x2)



For this system: screening at the surface is better than in the bulk

## Theory

dashed: initial-state effect only

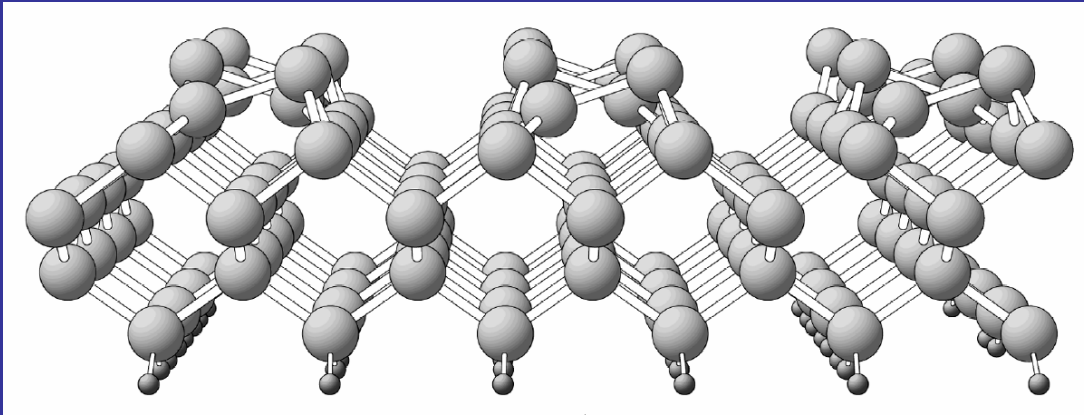
bars: including also final-state screening (by total-energy differences or transition-state theory)

*E. Pehlke and M.S.,  
PRL 71, 2338 (1993).*

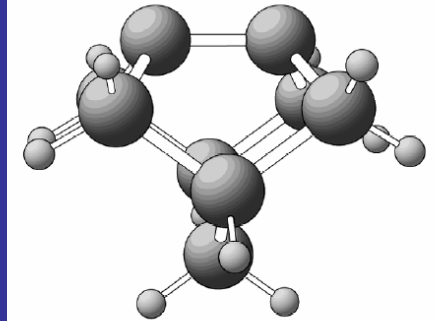
**Two peaks = clear proof for the buckling**



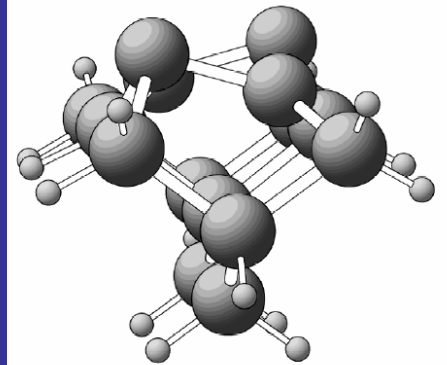
# DFT-GGA cluster calculations for Si(001)



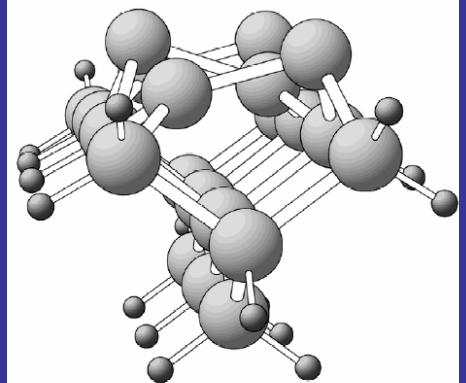
$\text{Si}_9\text{H}_{12}$



$\text{Si}_{15}\text{H}_{16}$



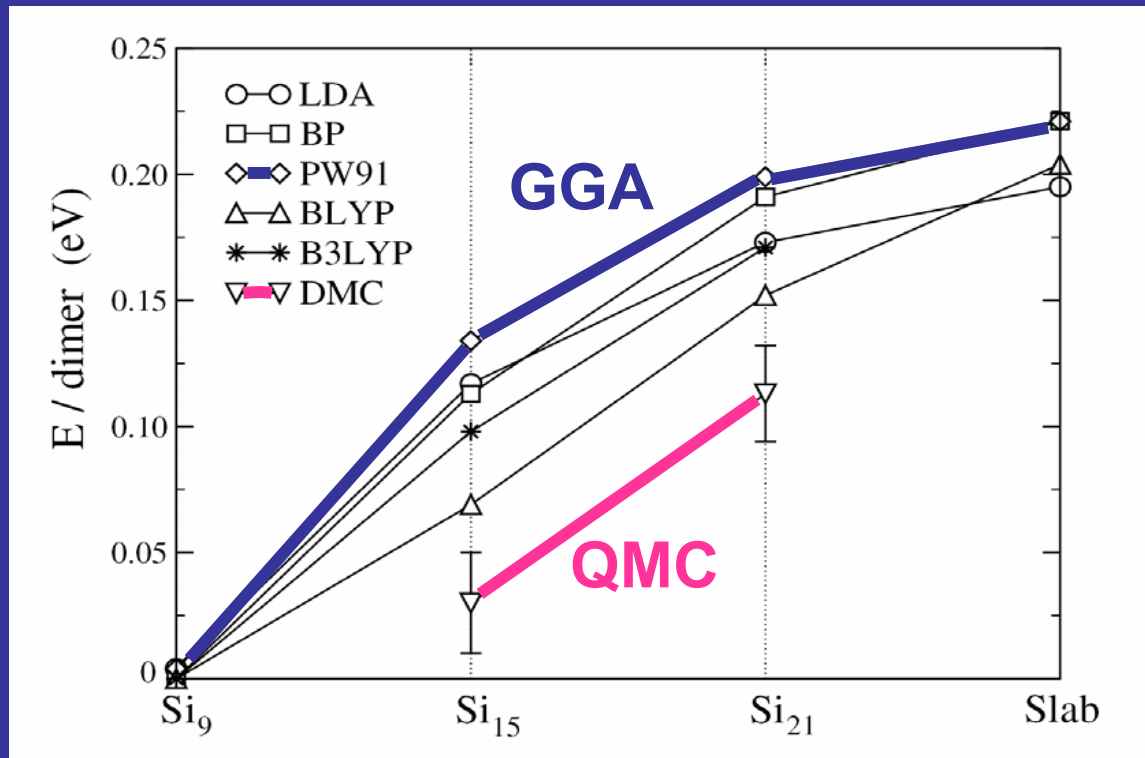
$\text{Si}_{21}\text{H}_{20}$



|                  | angle<br>(deg) | bond<br>(Å) | $\Delta E$<br>(eV) | gap<br>(eV) |
|------------------|----------------|-------------|--------------------|-------------|
| $\text{Si}_9$    | 4.9            | 2.24        | 0.0                | 1.1         |
| $\text{Si}_{15}$ | 15.7           | 2.32        | 0.1                | 0.9         |
| $\text{Si}_{21}$ | 18.0           | 2.40        | 0.2                | 0.7         |
| slab             | 18.3           | 2.40        | 0.2                | 0.0         |

The buckling only develops fully in bigger clusters.

# Energy gain from Si-dimer buckling



*S. B. Healy,  
C. Filippi,  
P. Kratzer,  
E. Penev & M. S.,  
Phys. Rev. Lett. 87  
(2001).*

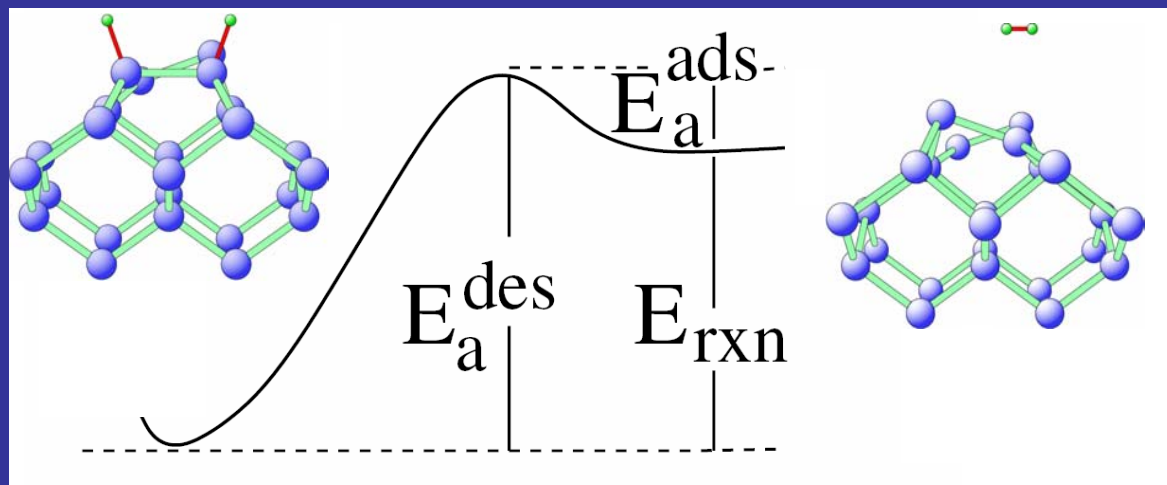
- QMC calculations confirm the buckled ground state, though with a smaller energy gain than DFT.
- It needs a large cluster with 3 dimers (Si<sub>21</sub>H<sub>20</sub>) to identify the effect.
- $\Delta E_{\text{corr}} = E_{\text{cluster}}(\text{QMC}) - E_{\text{cluster}}(\text{GGA}) \approx 0.1 \text{ eV}$

# Explanation of the experimental results for clean Si(001)

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- Room temperature: The symmetric dimers seen in STM are due to dynamic (fast) flipping
- Below 120 K: STM sees buckled dimers; thus, the exp. energy barrier is approx. 0.15 eV, in good agreement with our QMC extrapolation to infinitely large clusters.
- Below 20 K: STM sees symmetric dimers. This is possibly induced by the STM electrons.

# H<sub>2</sub> / Si(001)



experiments:

$$E_a^{\text{ads}} > 0.6 \text{ eV}$$

$$E_{\text{rxn}} = 1.9 \pm 0.3 \text{ eV}$$

$$E_a^{\text{des}} = 2.5 \pm 0.1 \text{ eV}$$

DFT calculations (slabs)

|      | $E_{\text{rxn}}[\text{eV}]$ | $E_{\text{des}}[\text{eV}]$ | $E_{\text{ads}}[\text{eV}]$ |
|------|-----------------------------|-----------------------------|-----------------------------|
| PW91 | 1.90                        | 2.27                        | 0.37                        |

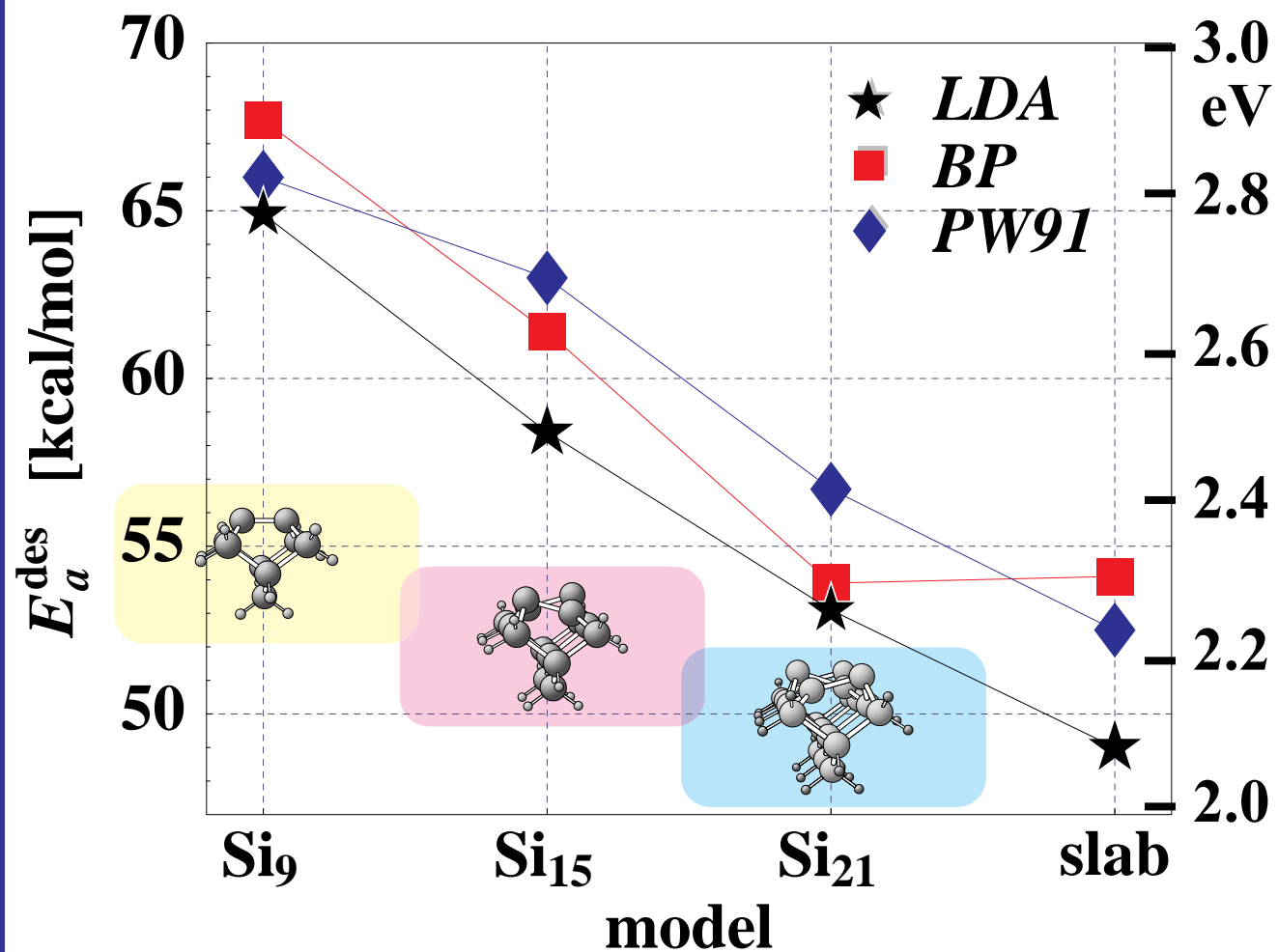
CI calculations (Si<sub>9</sub> clusters)

|                | $E_{\text{rxn}}[\text{eV}]$ | $E_{\text{des}}[\text{eV}]$ | $E_{\text{ads}}[\text{eV}]$ |
|----------------|-----------------------------|-----------------------------|-----------------------------|
| CCSD(T) ‡      | 2.65                        | 3.26                        | 0.61                        |
| CAS(4,4)+MRCI* | 2.60                        | 3.75                        | 1.15                        |

‡ J.A.Steckel et al., *J. Phys. Chem. B* **105**, 4031 (2001)

\*Z. Jing & J.L. Whitten, *J. Chem. Phys.* **98**, 7466 (1993)

# Cluster models: H<sub>2</sub> dissociative adsorption



Convergence  
with cluster  
size is slow.

*E. Penev, P. Kratzer  
and M. Scheffler,  
J. Chem. Phys. 110,  
3986 (1999)*

# QMC -- reliability checks

- geometries, in particular transition states
- pseudopotential error
- other technical aspects
  - basis set in HF
  - angular integration grid for non-local pseudopot.
- comparison to CI calculations for small clusters

Si<sub>9</sub>, intra-dimer pathway (H<sub>2</sub>\*)

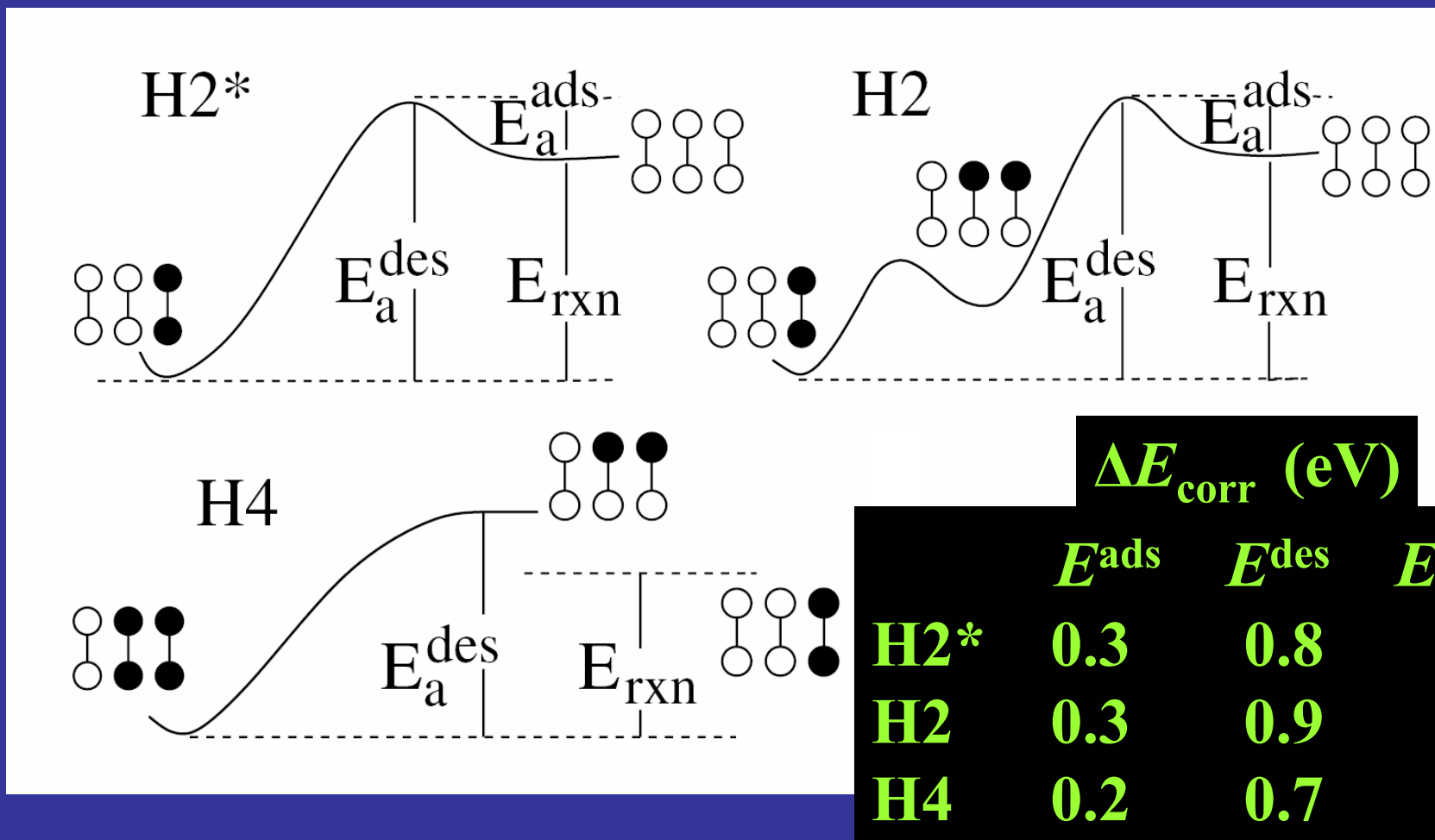
| method         | E <sub>rxn</sub> [eV] | E <sub>des</sub> [eV] | E <sub>ads</sub> [eV] |
|----------------|-----------------------|-----------------------|-----------------------|
| DMC (±0.06)    | 2.64                  | 3.65                  | 1.01                  |
| CAS(4,4)+MRCI* | 2.60                  | 3.75                  | 1.15                  |

\*Z. Jing &  
J.L. Whitten,  
*J. Chem. Phys*  
98 (1993)

# xc-energy correction for surface reactions

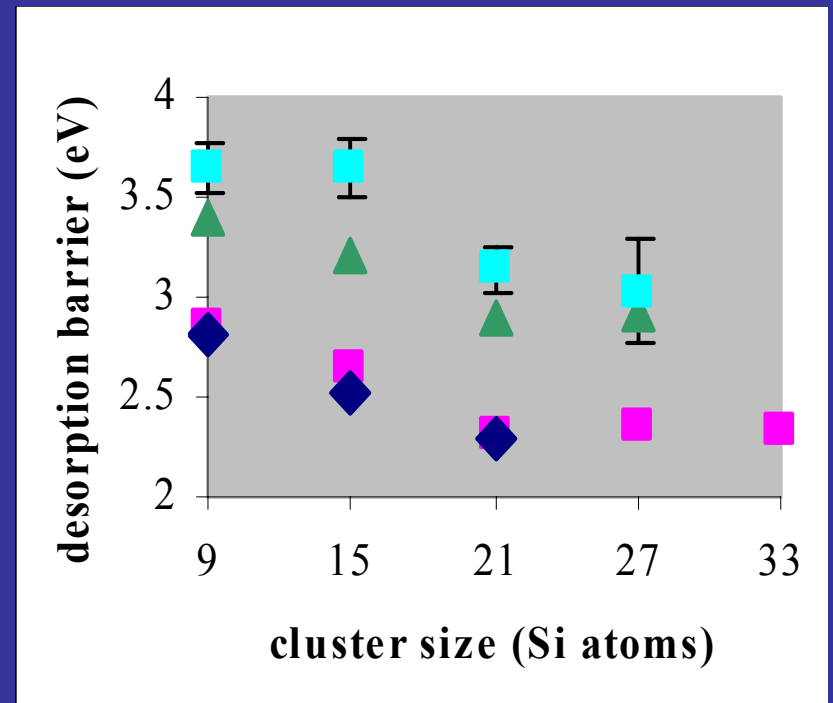
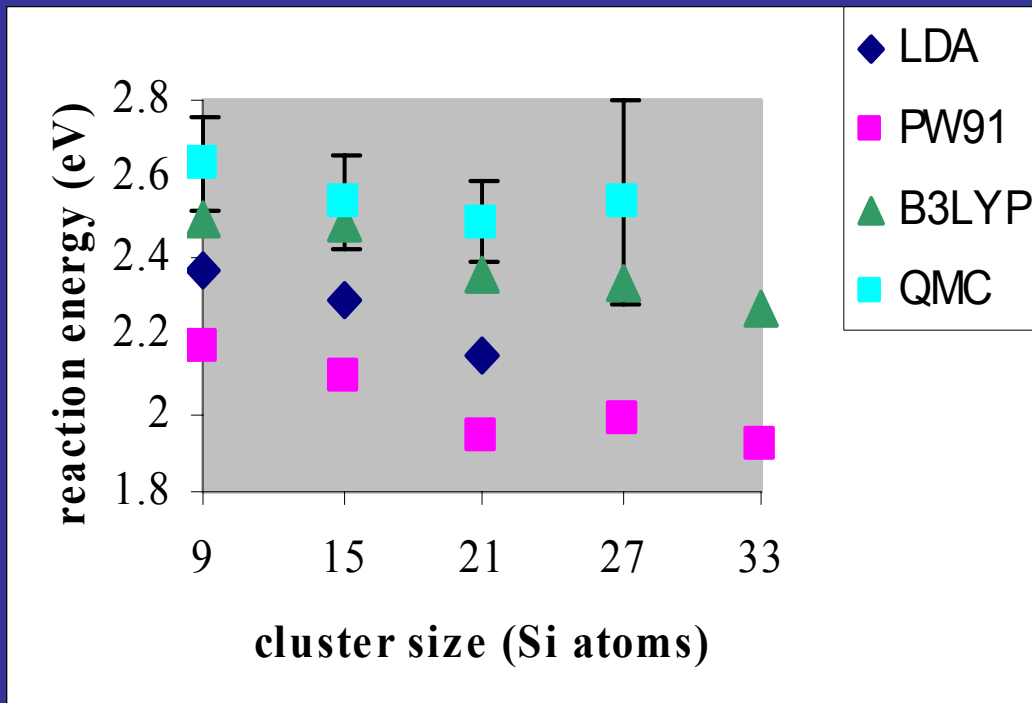
QMC calculations for Si<sub>9</sub>, Si<sub>15</sub>, Si<sub>21</sub>, Si<sub>27</sub> clusters

$$\Delta E_{\text{corr}} = E_{\text{cluster}}(\text{QMC}) - E_{\text{cluster}}(\text{PW91})$$



# Cluster size convergence

- Both the reaction energy and the barriers are underestimated by the PW91 functional.
- B3LYP comes close to the QMC results, but still gives slightly lower values.





# Results (slab)

|                                     | $E^{\text{ads}}(\text{eV})$ | $E^{\text{des}}(\text{eV})$ | $E_{\text{rxn}}(\text{eV})$ |
|-------------------------------------|-----------------------------|-----------------------------|-----------------------------|
| <b>H2* mechanism</b>                |                             |                             |                             |
| $E^{\text{PW91-slab}}$              | 0.46                        | 2.16                        | 1.70                        |
| $\Delta E_{\text{corr}} (\pm 0.05)$ | +0.29                       | +0.80                       | +0.50                       |
| $E_{\text{QMC}} (\pm 0.05)$         | 0.75                        | 2.96                        | 2.20                        |
| exp.                                | >0.6                        | 2.5±0.1                     | 1.9±0.3                     |
| <b>H2 mechanism</b>                 |                             |                             |                             |
| $E^{\text{PW91-slab}}$              | 0.29                        | 2.04                        | 1.75                        |
| $\Delta E_{\text{corr}} (\pm 0.09)$ | +0.34                       | +0.87                       | +0.53                       |
| $E_{\text{QMC}} (\pm 0.09)$         | 0.63                        | 2.91                        | 2.28                        |
| exp.                                | >0.6                        | 2.5±0.1                     | 1.9±0.3                     |
| <b>H4 mechanism</b>                 |                             |                             |                             |
| $E^{\text{PW91-slab}}$              | 0.00                        | 2.12                        | 1.81                        |
| $\Delta E_{\text{corr}} (\pm 0.12)$ | +0.19                       | +0.72                       | +0.48                       |
| $E_{\text{QMC}} (\pm 0.12)$         | 0.19                        | 2.84                        | 2.29                        |
| exp.                                | --                          | 2.5±0.1                     | --                          |

- QMC gives higher adsorption barrier, improving agreement with experiments.
- The inter-dimer path for desorption competes with the intra-dimer path -- in agreement with recent experiments.
- The absolute value of the desorption barrier in QMC is higher than the experimental data (from isothermal desorption).

# Conclusions

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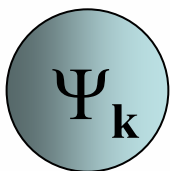
- Corrections to  $E_{xc}^{\text{A}}[n]$  can be significant -- much of the error is due to self interaction, but correlation is important as well.
- The QMC approach to evaluate such corrections is feasible (and accurate).
- Cluster approximations: The size is crucial.
- Comparison to experiment :
  - clean Si(001): buckled ground state persists at low temperatures.
  - QMC adsorption for H<sub>2</sub> / Si(001) in better agreement with experiment than previous calculations.

[www.fhi-berlin.mpg.de/th/Meetings/FHIInd2003/](http://www.fhi-berlin.mpg.de/th/Meetings/FHIInd2003/)

## Announcement: "hands on" Workshop



*Application of Density-Functional Theory in  
Condensed Matter Physics, Surface  
Physics, Chemistry, Engineering and Biology*



21-30 July 2003

Fritz-Haber-Institut der Max-Planck-Gesellschaft,  
Berlin, Germany

### Organisers

- [Catherine Stampfl](#) (Fritz-Haber-Institut der Max-Planck-Gesellschaft, Berlin and The University of Sydney, Australia)
- [Jörg Neugebauer](#) (Fritz-Haber-Institut der Max-Planck-Gesellschaft, Berlin)
- [Peter Kratzer](#) (Fritz-Haber-Institut der Max-Planck-Gesellschaft, Berlin)
- [Arno Schindlmayr](#) (Fritz-Haber-Institut der Max-Planck-Gesellschaft, Berlin)
- [Matthias Scheffler](#) (Fritz-Haber-Institut der Max-Planck-Gesellschaft, Berlin)

### Purpose of the Workshop

The main objectives of the workshop is to introduce density-functional theory calculations to a level such that the participants obtain a thorough understanding of what DFT can offer and are able to perform such calculations. The computer program [SFHIngX](#) developed at the Fritz-Haber-Institut, will be used for the