

HI-to-H₂ Transitions in Galaxy Star-Forming Regions

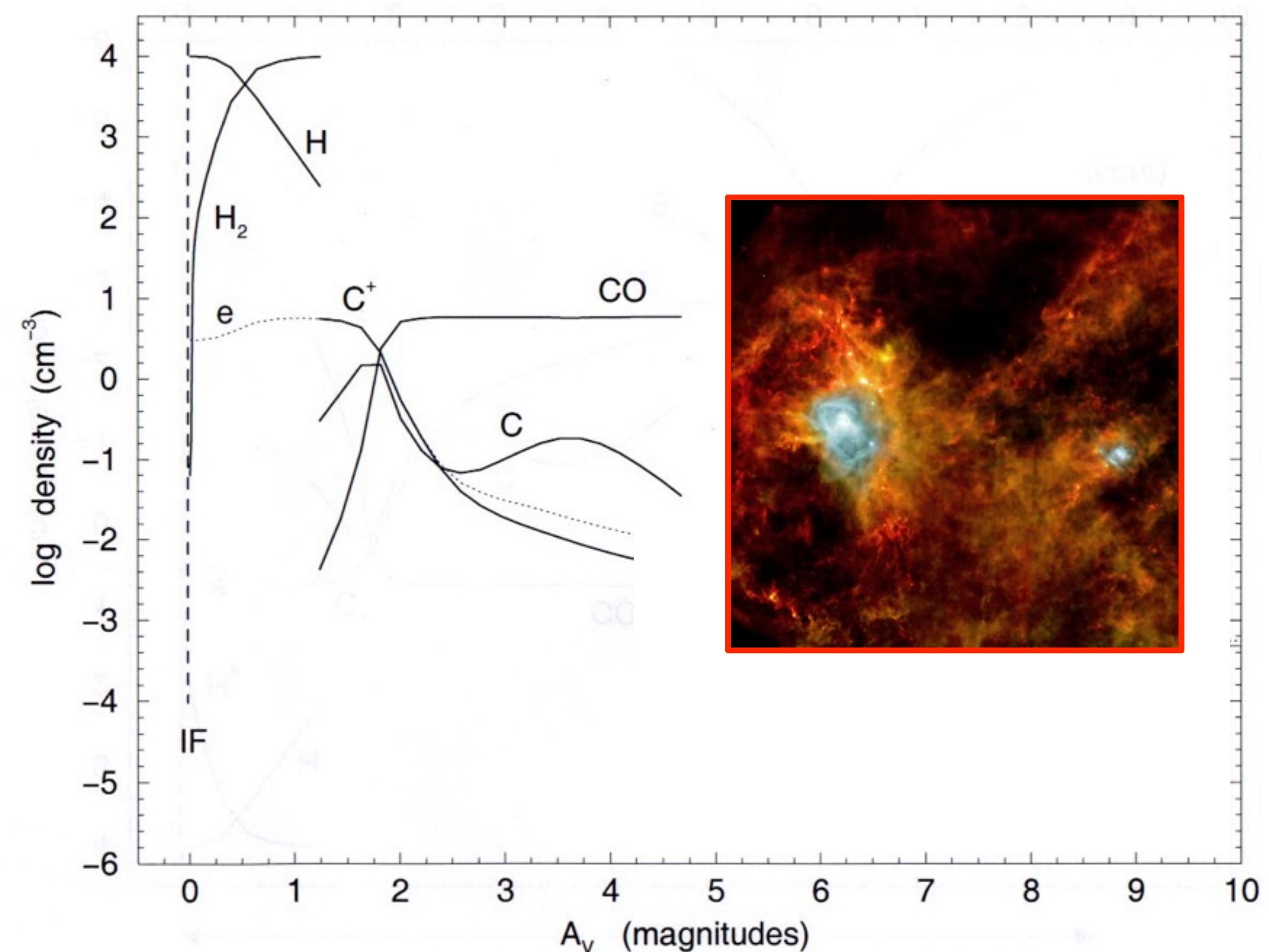
Amiel Sternberg
Sackler School of Physics & Astronomy
Tel Aviv University
ISRAEL

Molecules and Dust as Fuel for Star Formation
Kavli Institute for Theoretical Physics
June 2016



HI-to-H₂ Transitions in Galaxy Star-Forming Regions

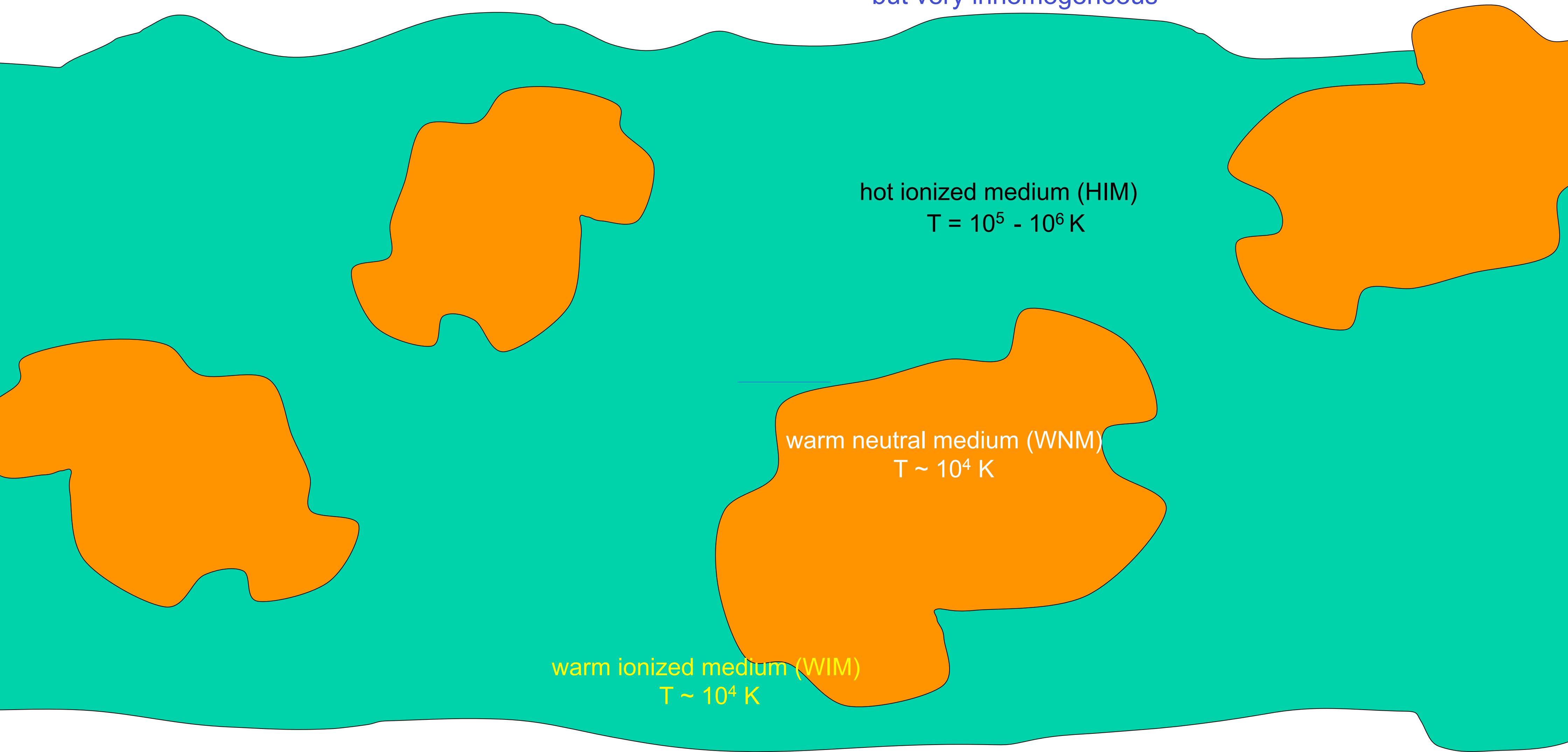
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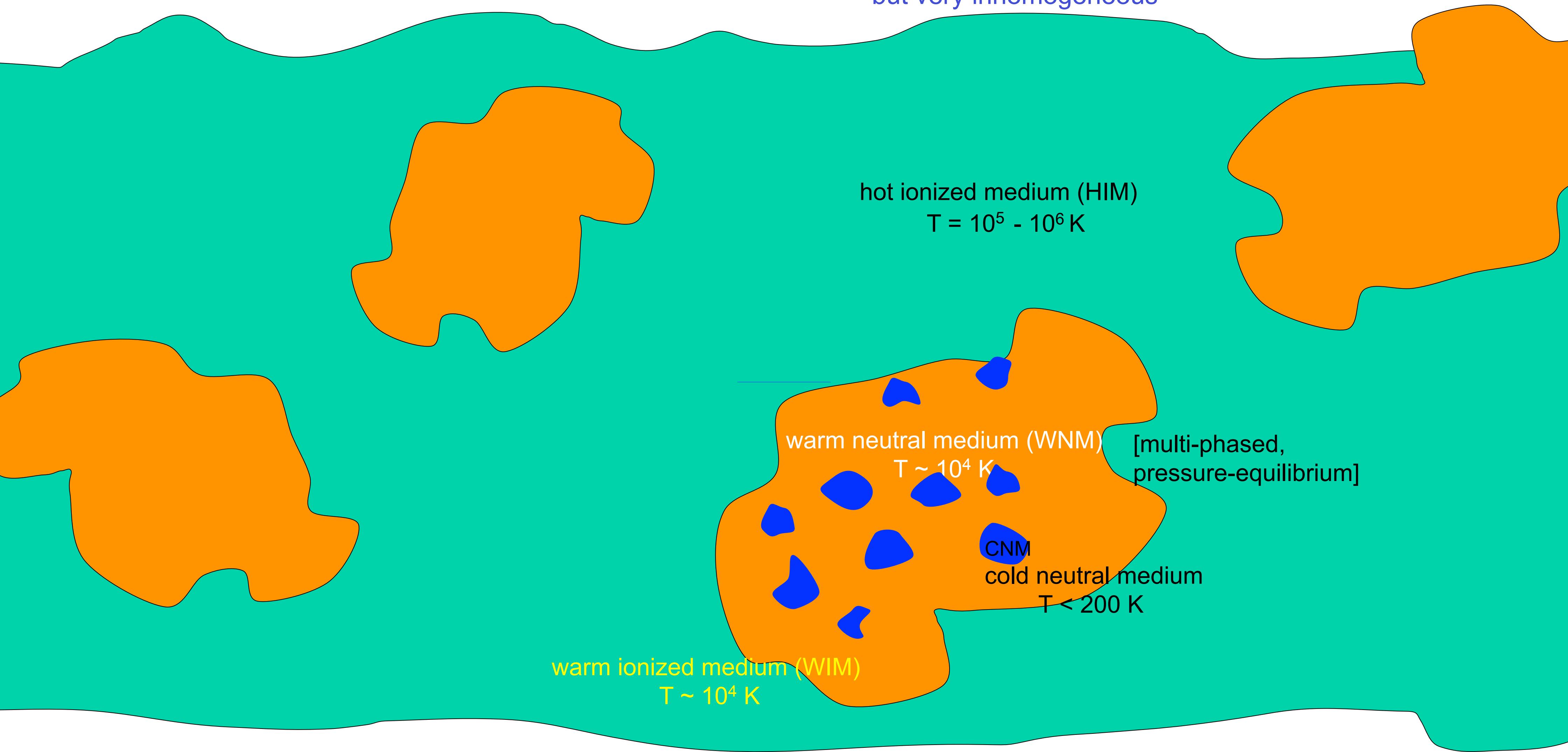
The Multi-Phased Interstellar Medium (ISM) and Star-Formation:

<density> = 1 cm^{-3}
but very inhomogeneous



The Multi-Phased Interstellar Medium (ISM) and Star-Formation:

<density> = 1 cm⁻³
but very inhomogeneous



The Multi-Phased Interstellar Medium (ISM) and Star-Formation:

Interstellar gas exposed to
starlight
shock waves
energetic particles (cosmic-rays)
magnetic fields

Global ISM heated and energized by stars
(outflows, radiation, and supernova explosions).

Turbulent. Dusty.

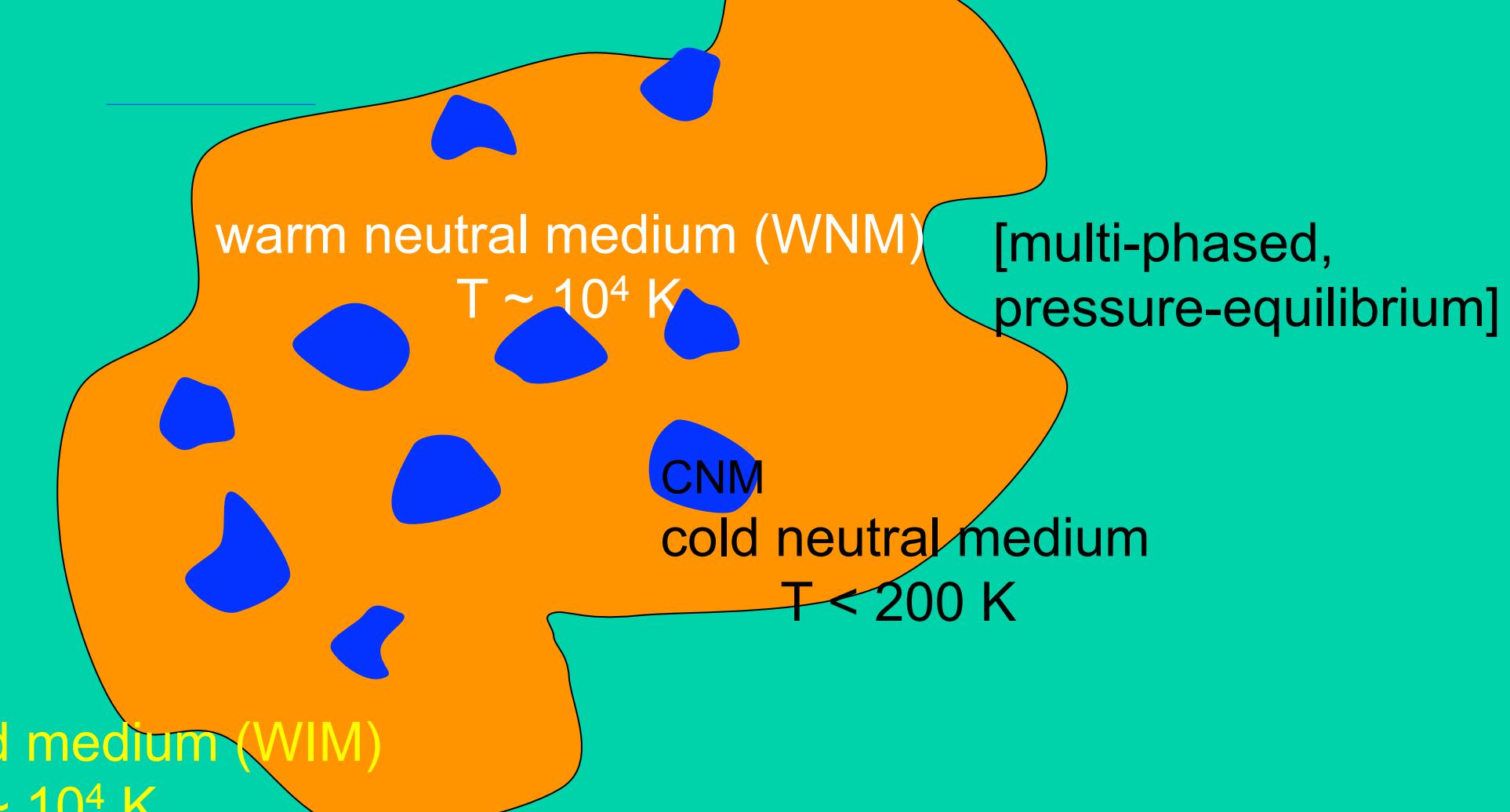
Total Galactic ISM mass = $5 \times 10^9 M_\odot$

Mid-plane thermal pressure = $2.5 \times 10^3 \text{ cm}^{-3} \text{ K}$
(at Solar circle)

most of the mass in cold neutral hydrogen phase
most of the volume in warm/hot ionized phase.

$\langle \text{density} \rangle = 1 \text{ cm}^{-3}$
but very inhomogeneous

hot ionized medium (HIM)
 $T = 10^5 - 10^6 \text{ K}$



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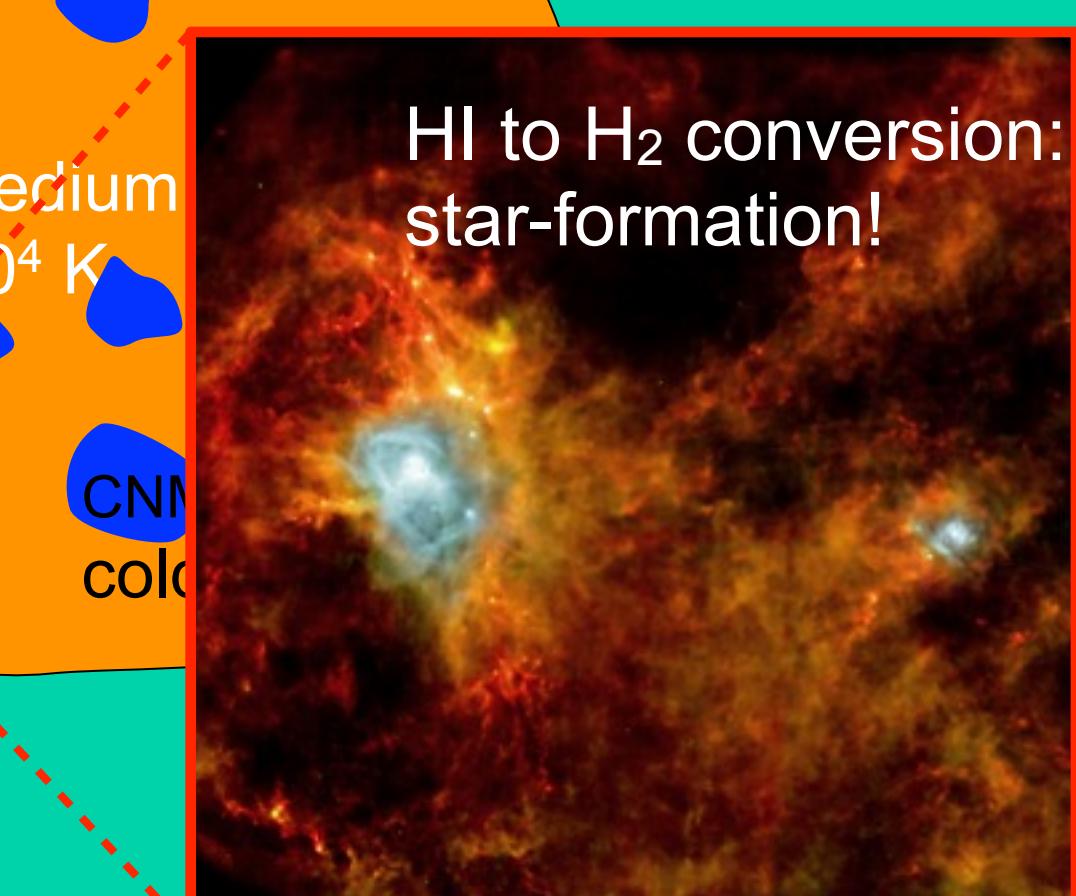
most of the mass in cold neutral hydrogen phase
most of the volume in warm/hot ionized phase.

stars form in cold molecular (H_2) clouds:
Galactic star-formation rate $\sim 3 M_\odot \text{ yr}^{-1}$

$\langle \text{density} \rangle = 1 \text{ cm}^{-3}$
but very inhomogeneous

hot ionized medium (HIM)
 $T = 10^5 - 10^6 \text{ K}$

warm neutral medium
 $T \sim 10^4 \text{ K}$



Herschel views Aquila

Talk Outline:

- brief history and motivation.
 - HI-to-H₂ transition, some radiative transfer computations.
 - analytic formula for the HI column density.
 - self-regulated media.
 - observations: from Perseus to galaxies.
-
- “HI-to-H₂ Transitions and HI Column Densities in Galaxy Star-forming Regions”
Sternberg, Le Petit, Roueff, & Le Bourlot, 2014 ApJ 790 10
 - “HI-to-H₂ Transitions in the Perseus Molecular Cloud”
Bialy, Sternberg, Min-Young, Le Petit, & Roueff, 2015 ApJ 809 122
 - “Analytic HI-to-H₂ Photodissociation Transition Profiles”
Bialy & Sternberg, 2016 ApJ 822 83

see also “C⁺/H₂ Gas in Star-Forming Clouds and Galaxies”
Nordon & Sternberg arXiv:1603.02300

THE TEMPERATURE OF INTERSTELLAR MATTER. I

LYMAN SPITZER, JR.

Yale University*

Received June 30, 1947

Molecular hydrogen may possibly be much more abundant in $H\text{I}$ regions of interstellar space than are the observed molecules CH and CN . However, the ionization

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MOLECULAR HYDROGEN IN $H\text{I}$ REGIONS

DAVID J. HOLLENBACH

Harvard College Observatory, Cambridge, Massachusetts

MICHAEL W. WERNER*

Institute of Theoretical Astronomy, Cambridge, England

AND

EDWIN E. SALPETER

Center for Radiophysics and Space Research, Cornell University, Ithaca, New York

Received 1970 March 24; revised 1970 June 3

ABSTRACT

Density profiles of molecular hydrogen are calculated for interstellar clouds of various densities n and radii R , on the assumption of equilibrium conditions. Rates of molecular formation on the surface of dust

1970 ApJ 161 L43

CARBON MONOXIDE IN THE ORION NEBULA

R. W. WILSON, K. B. JEFFERTS, AND A. A. PENZIAS

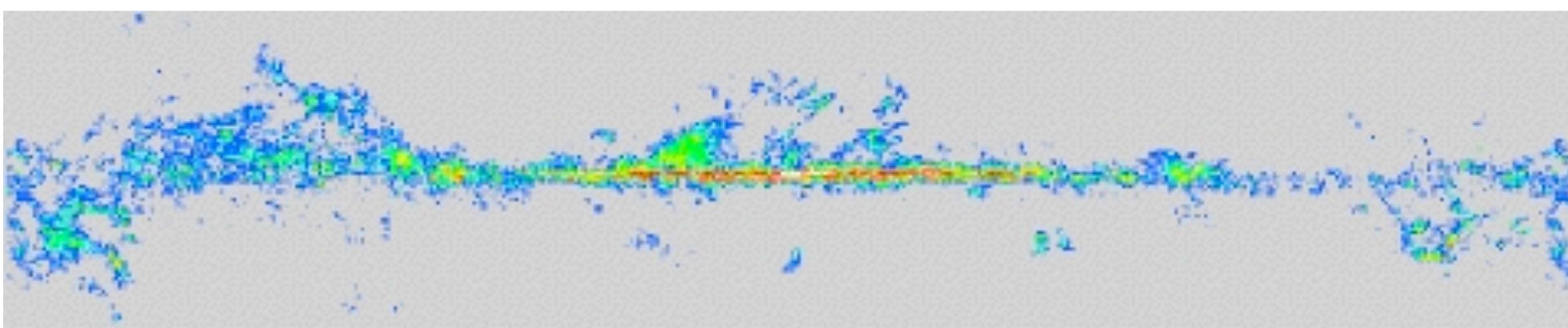
Bell Telephone Laboratories, Inc., Holmdel, New Jersey, and
Crawford Hill Laboratory, Murray Hill, New Jersey

Received 1970 June 5

ABSTRACT

We have found intense 2.6-mm line radiation from nine galactic sources which we attribute to carbon monoxide.

Milky-Way in CO 1-0



H₂ usually difficult to observe directly.
CO is the tracer molecule.

Dame, Hartmann & Thaddeus 2001 ApJ 546 792

1977 ApJS 34 405

MODELS OF INTERSTELLAR CLOUDS.
I. THE ZETA OPHIUCHI CLOUD

J. H. BLACK

School of Physics and Astronomy, University of Minnesota

AND

A. DALGARNO

Center for Astrophysics, Harvard College Observatory and Smithsonian Astrophysical Observatory

...HI-to-H₂ initiates chemistry...

Improved H₂ line transfer:

1988 ApJ 332 400

THE INFRARED RESPONSE OF MOLECULAR HYDROGEN GAS TO ULTRAVIOLET RADIATION: A SCALING LAW

AMIEL STERNBERG¹

School of Physics and Astronomy, Tel Aviv University

Received 1987 September 24; accepted 1988 February 22

1996 ApJ 468 269

STRUCTURE OF STATIONARY PHOTODISSOCIATION FRONTS

B. T. DRAINE

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AND

FRANK BERTOLDI

Max-Planck-Institut für Extraterrestrische Physik, D-85748 Garching, Germany; fkb@mpe-garching.mpg.de

Global Galaxy Properties:

2010 ApJ 709 308

THE ATOMIC-TO-MOLECULAR TRANSITION IN GALAXIES. III. A NEW METHOD FOR DETERMINING THE MOLECULAR CONTENT OF PRIMORDIAL AND DUSTY CLOUDS

CHRISTOPHER F. MCKEE¹ AND MARK R. KRUMHOLZ²

¹ Physics Department and Astronomy Department, University of California, Berkeley, CA 94720, USA; cmckee@astro.berkeley.edu

² Astronomy Department, University of California, Santa Cruz, CA 95060, USA; krumholz@ucolick.edu

Received 2009 July 31; accepted 2009 December 2; published 2009 December 30

2014 ApJ 790 10

H I-TO-H₂ TRANSITIONS AND H I COLUMN DENSITIES IN GALAXY STAR-FORMING REGIONS

AMIEL STERNBERG¹, FRANCK LE PETIT², EVELYNE ROUEFF², AND JACQUES LE BOURLOT^{2,3}

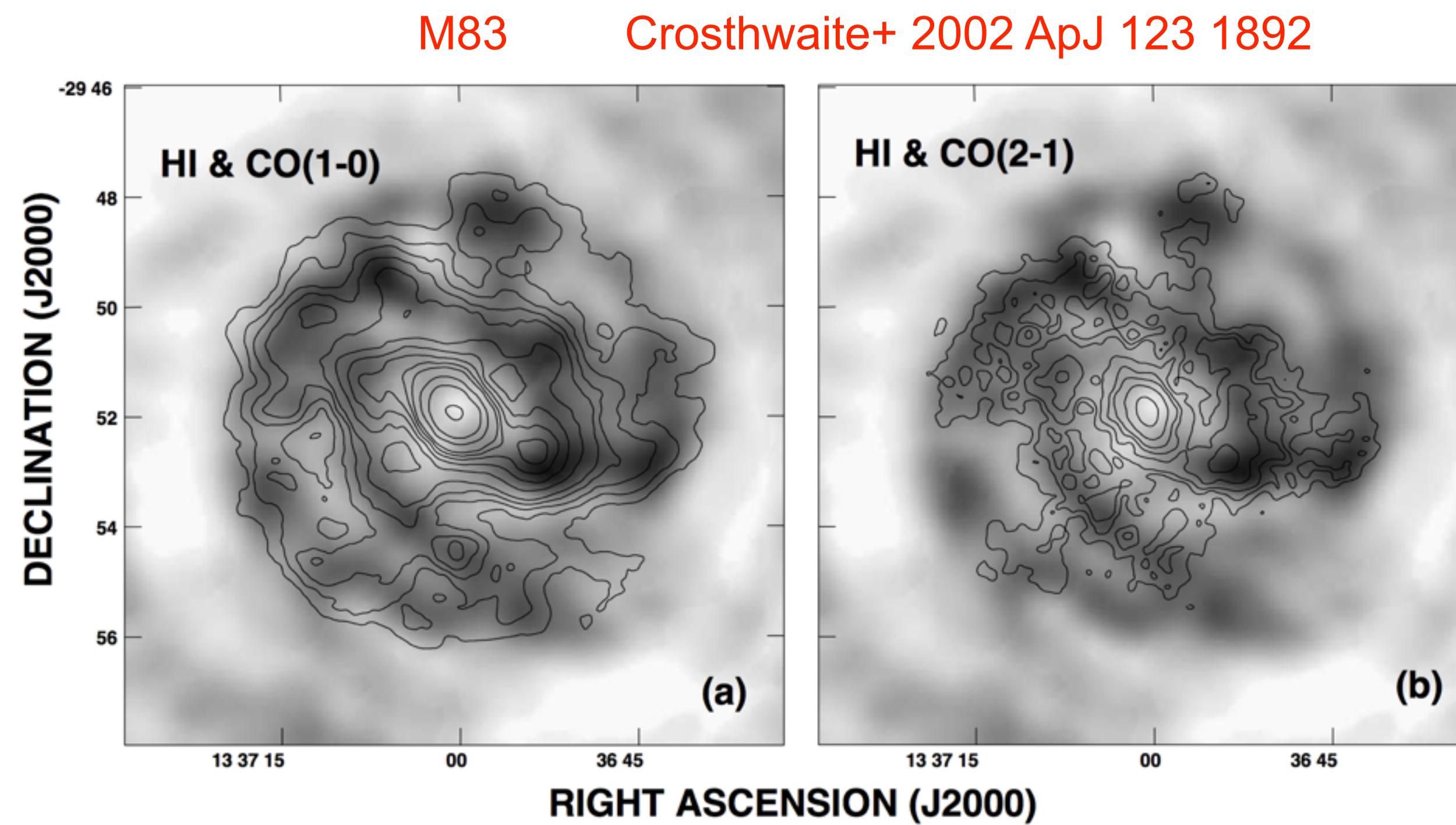
¹ Raymond and Beverly Sackler School of Physics & Astronomy, Tel Aviv University, Ramat Aviv 69978, Israel

² LERMA, Observatoire de Paris, CNRS, 5 place Jules Janssen, F-92190 Meudon, France

³ Université Paris Diderot, 5 rue Thomas-Mann, F-75205 Paris cedex 13, France

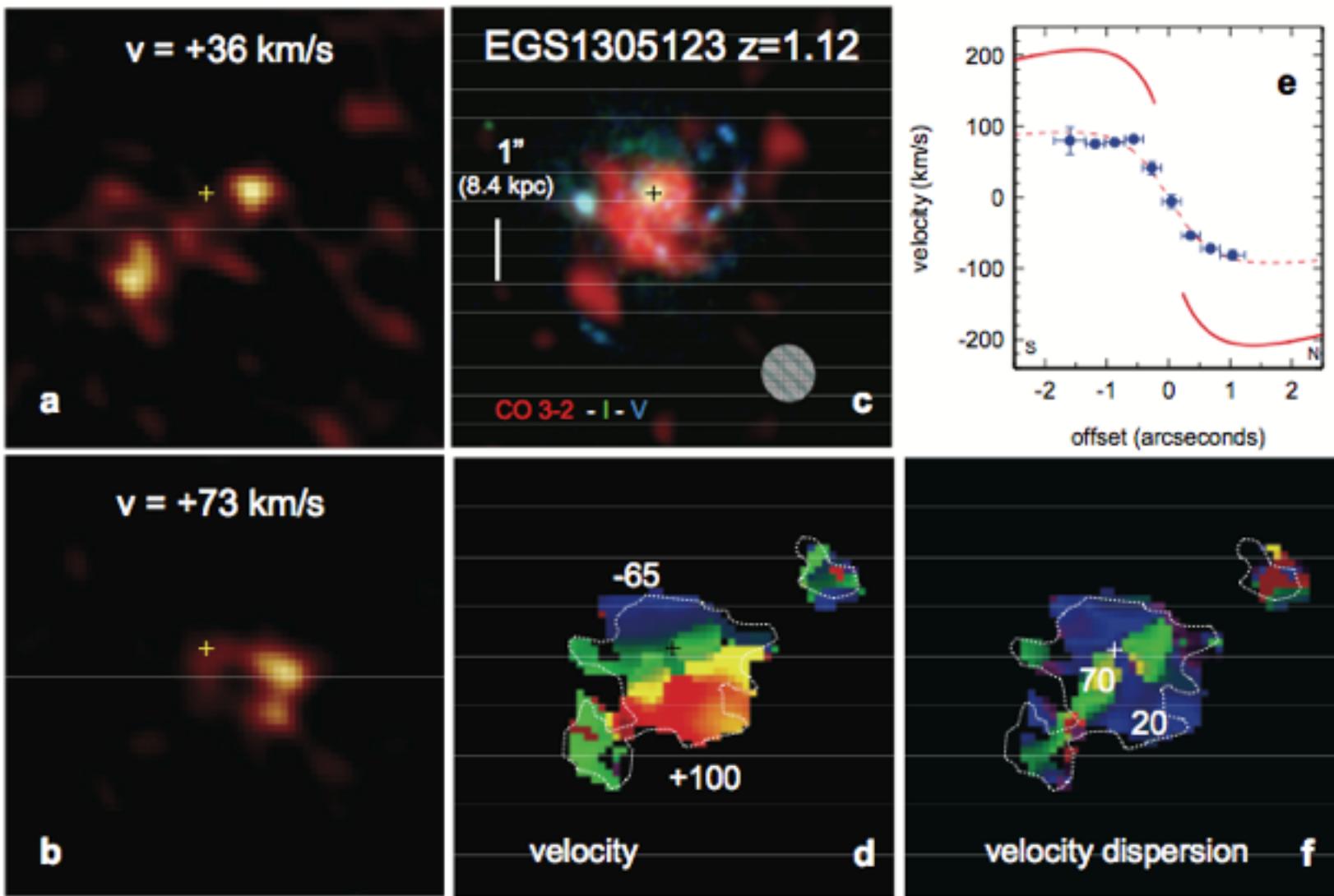
Received 2013 November 13; accepted 2014 April 16; published 2014 June 27

HI as a Photodissociation Product in Molecular Spiral Arms:

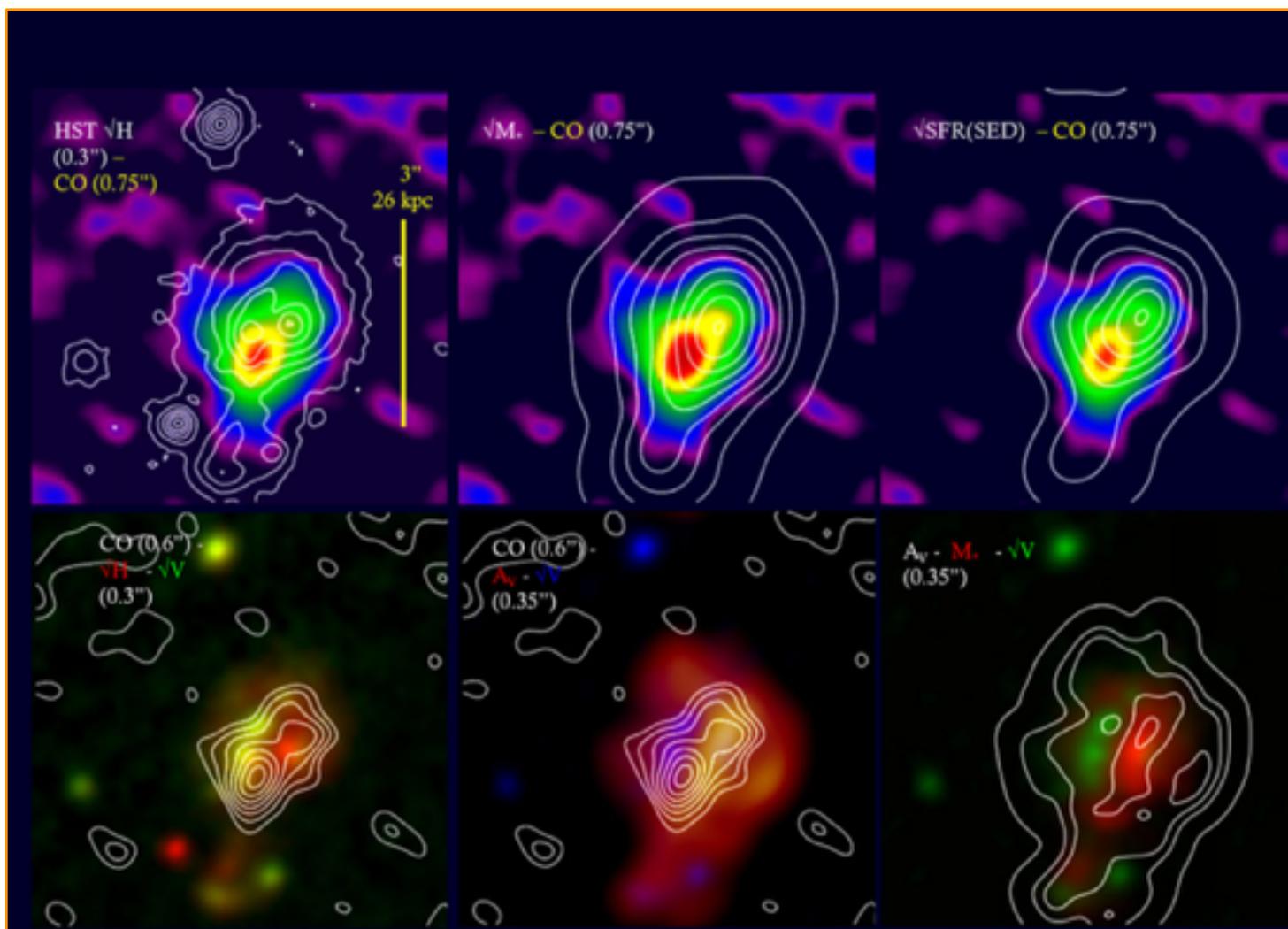


Conversion to molecular gas in high redshift galaxies:

Tacconi et al. 2010 Nature 463 781



Genzel+ 2013 EGS13011166 z=1.5



PdBI NOEMA

PHIBSS2

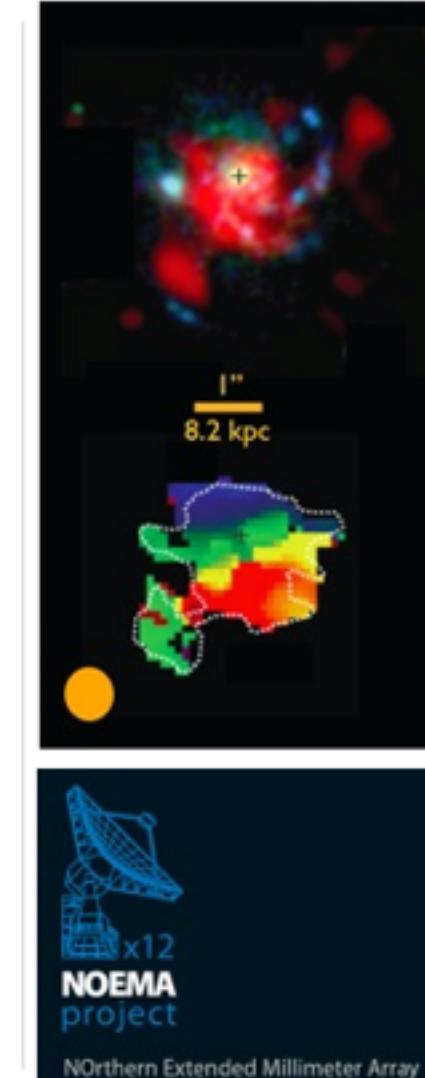
MOLECULAR GAS AT THE PEAK EPOCH OF GALAXY FORMATION

HOME SCIENCE TEAM DATA RELEASE PAPERS TEAM LOGIN

Team

PHIBSS2 is an international and IRAM-wide effort, involves collaborators from a broad variety of backgrounds, and builds upon and enhances previous IRAM PdBI studies of molecular gas in high-redshift galaxies.

Co-PI: Francoise Combes (Obs. Paris – France)
Co-PI: Santiago Garcia-Burillo (OAN – Spain)
Co-PI: Roberto Neri (IRAM – France)
Co-PI: Linda Tacconi (MPE – Germany)
R. Genzel (MPE – Germany)
T. Contini (IRAP – France)
A. Bolatto (UMd – USA)
S. Lilly (ETH – Switzerland)
F. Boone (IRAP – France)
N. Bouche (IRAP – France)
F. Bournaud (CEA – France)
A. Burkert (USM – Germany)
M. Carollo (ETH – Switzerland)
L. Colina (CSIC – Spain)
M. Cooper (UCI – US)
P. Cox (IRAM – France)
C. Feruglio (IRAM – France)
J. Freundlich (Obs.Paris – France)
N. Förster Schreiber (MPE – Germany)
S. Juneau (CEA – France)
K. Kovac (ETH – Switzerland)
M. Lippa (MPE – Germany)
D. Lutz (MPE – Germany)
T. Naab (MPA – Germany)
A. Omont (IAP – France)
A. Renzini (Univ.Padova – Italy)
A. Saintonge (MPE – Germany)
P. Salomé (Obs.Paris – France)
A. Sternberg (Univ.Tel Aviv – Israel)
F. Walter (MPIA – Germany)
B. Weiner (Steward Obs.Arizona – US)
A. Weiβ (MPIfR – Germany)
S. Wuyts (MPE – Germany)



NORthern Extended Millimeter Array



Kennicutt-Schmidt Relation:

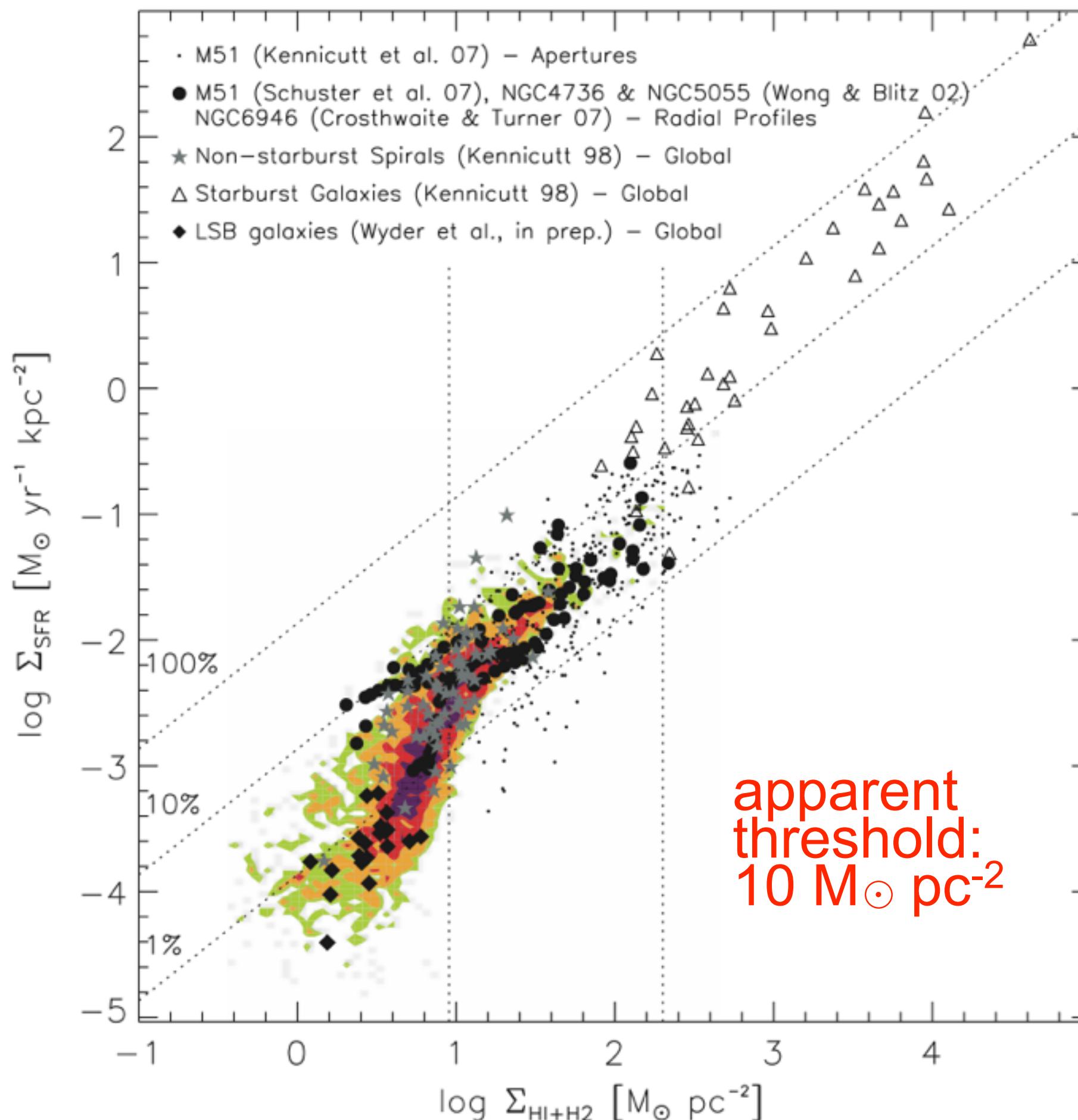
Schmidt 1959 ApJ 129 253

Kennicutt 1998 ApJ 498 541

Genzel, Tacconi, Sternberg, et al. 2010 MNRAS 407 2091 [SINS/KMOS(VLT) IRAM projects]



e.g., Bigiel+ 2008



$$\Sigma_{\text{SFR}} = \epsilon \frac{f_{\text{H}_2} \Sigma_{\text{gas}}}{\tau_d}$$

see also Semenov et al. poster

I am going to be juggling many parameters
- keep your eye on them!



I am going to be juggling many parameters
- keep your eye on them!



“...A perspicuous representation produces just that understanding which consists of ‘seeing connections’. Hence the importance of finding and inventing *intermediate cases*. The concept of a perspicuous representation is of fundamental significance for us. It earmarks the form of account we give, the way we look at things...”

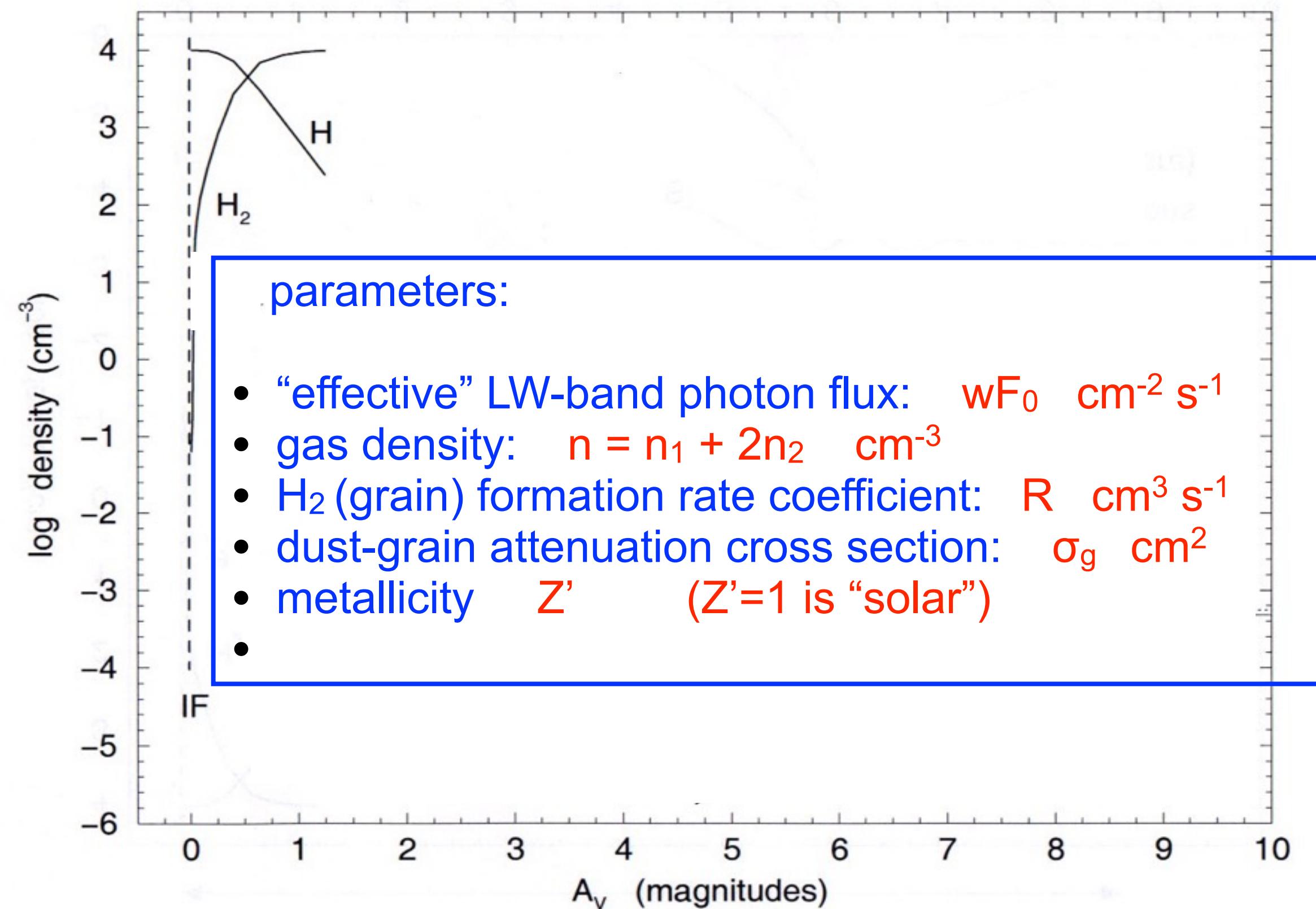
Part I, paragraph 122
Philosophical Investigations
Ludwig Wittgenstein

HI to H₂ Transition in Dense Star-Forming Molecular Clouds.

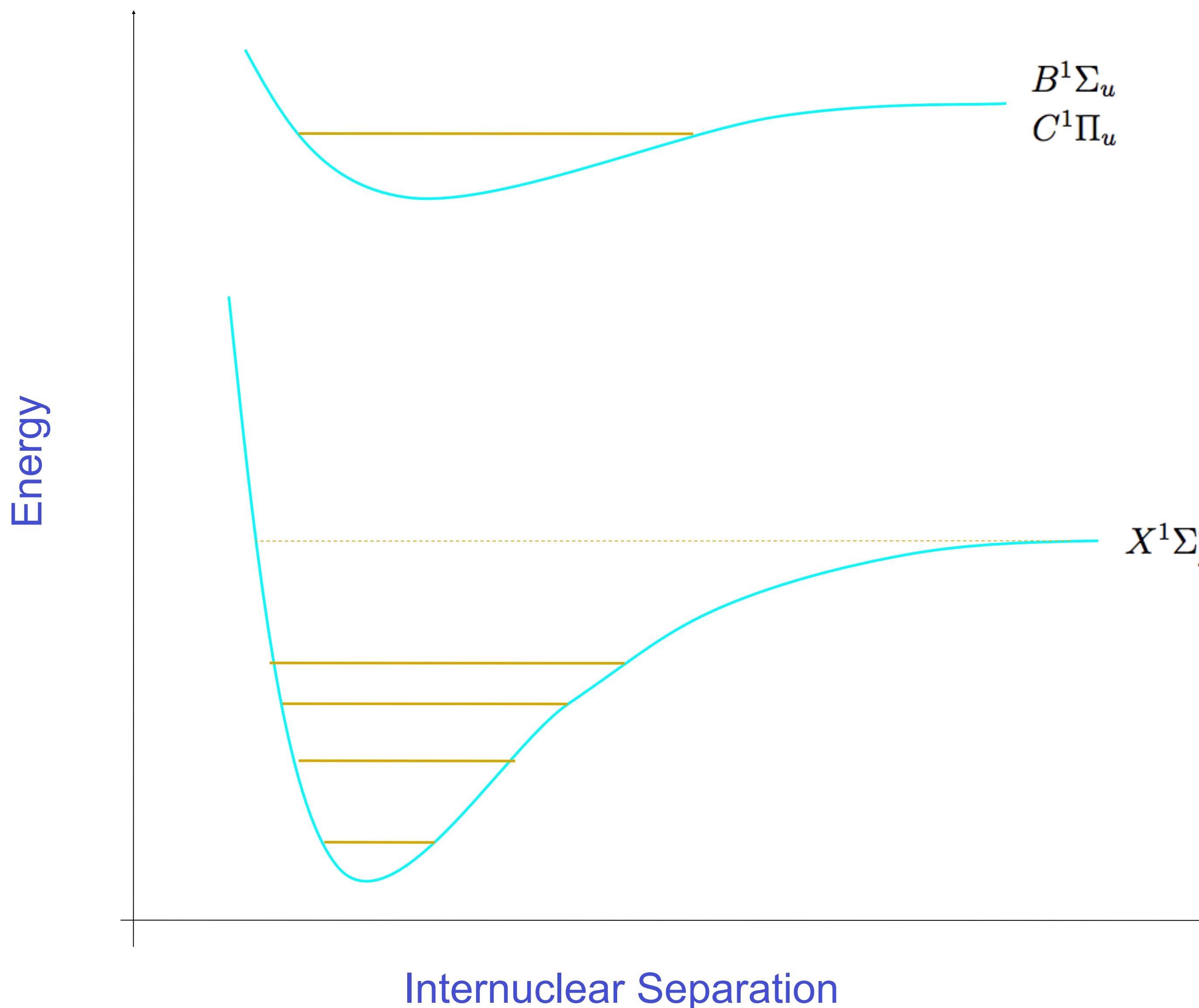
H₂ formation (by grain catalysis) versus far-UV photodissociation.

Shielding required.

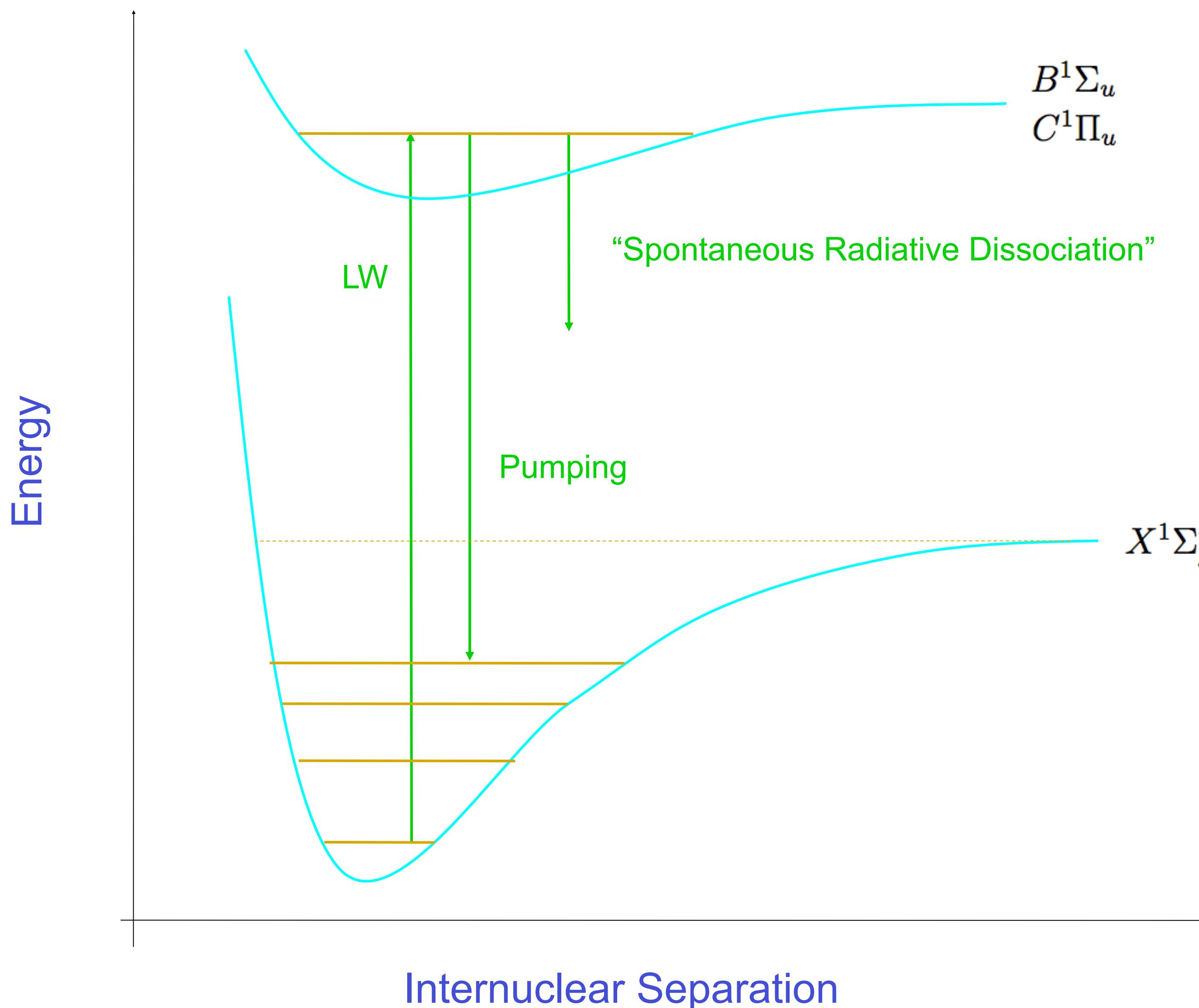
Stellar ultraviolet
“Lyman-Werner” radiation
11.2 - 13.6 eV



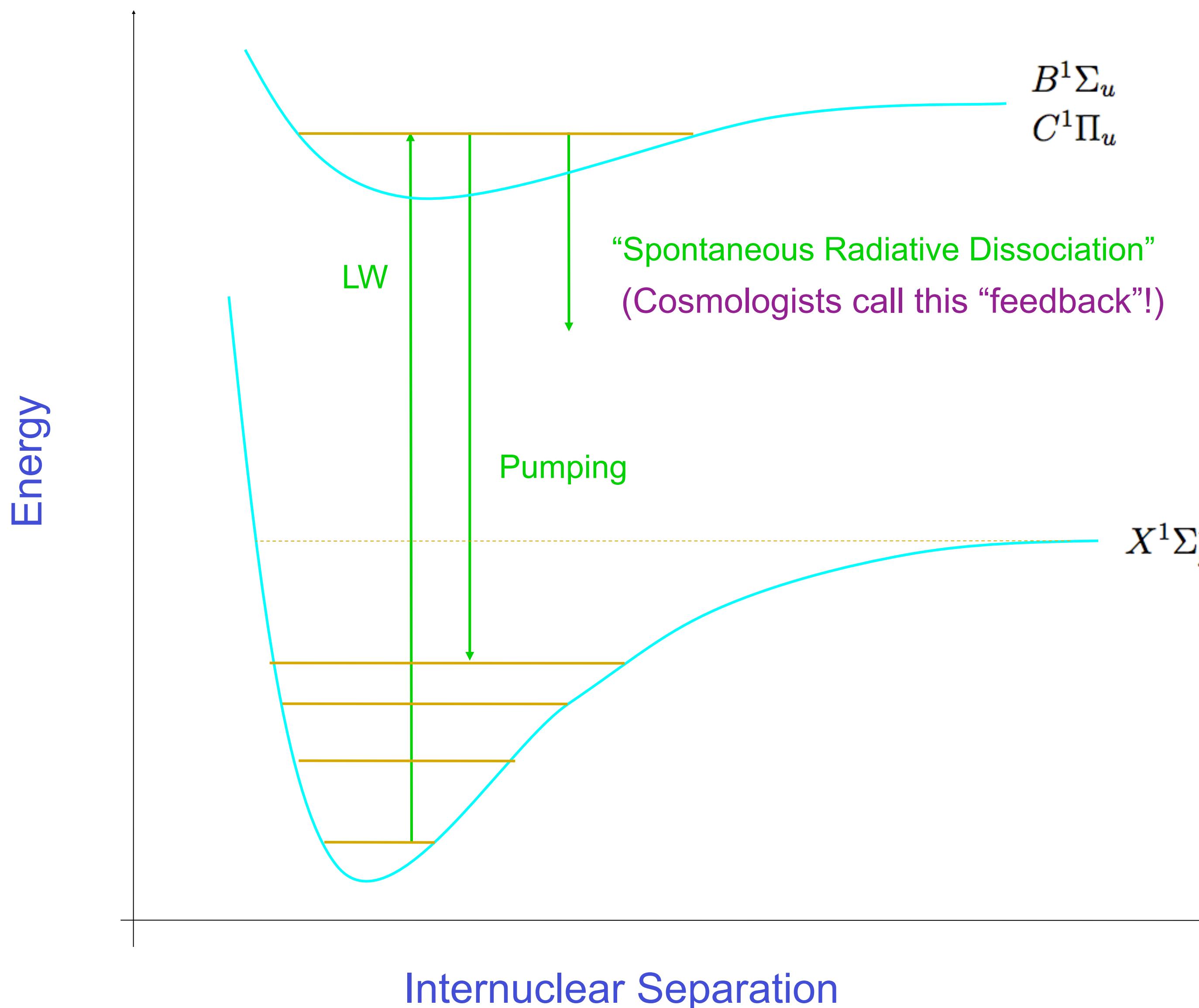
H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



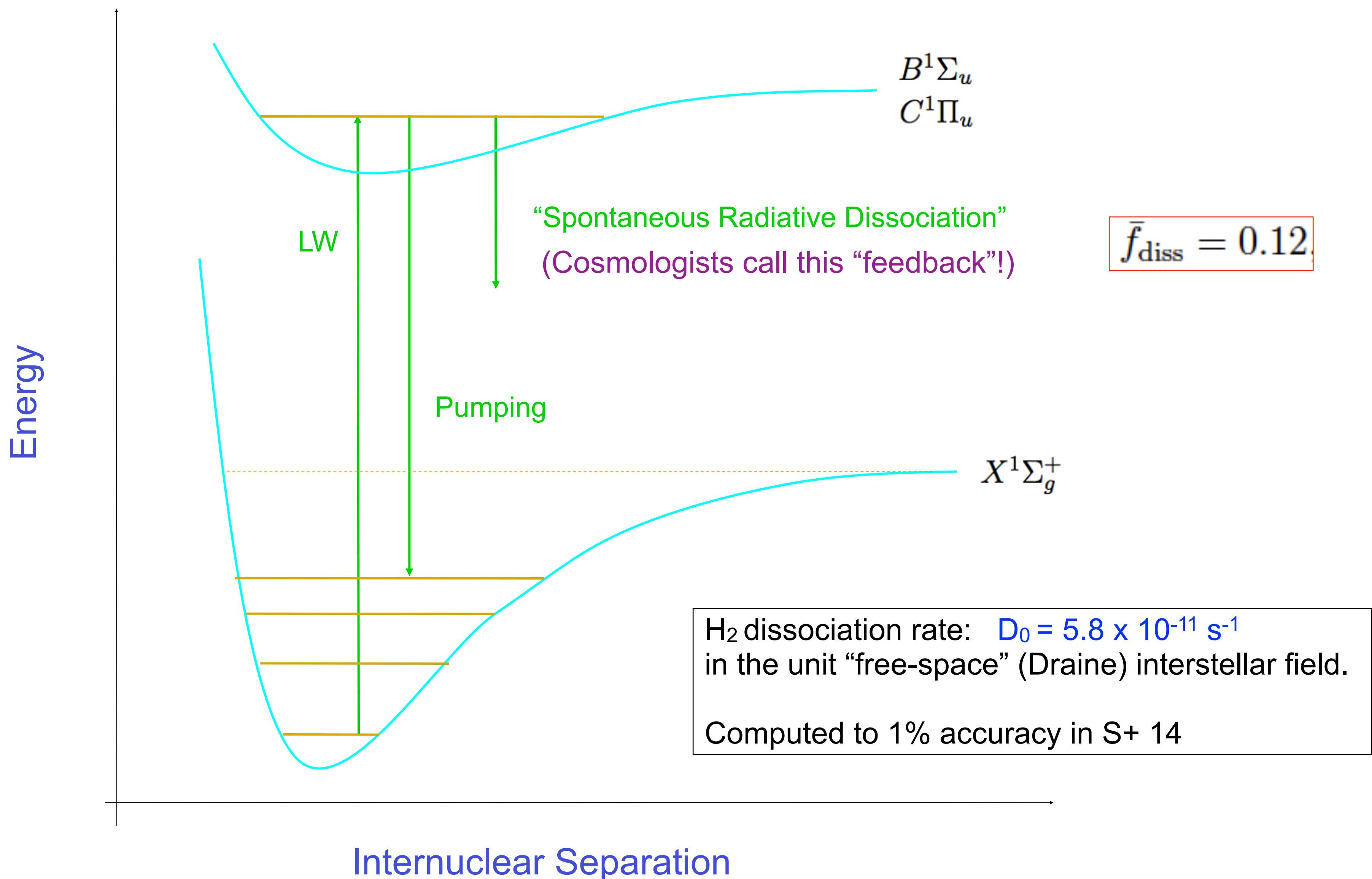
H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



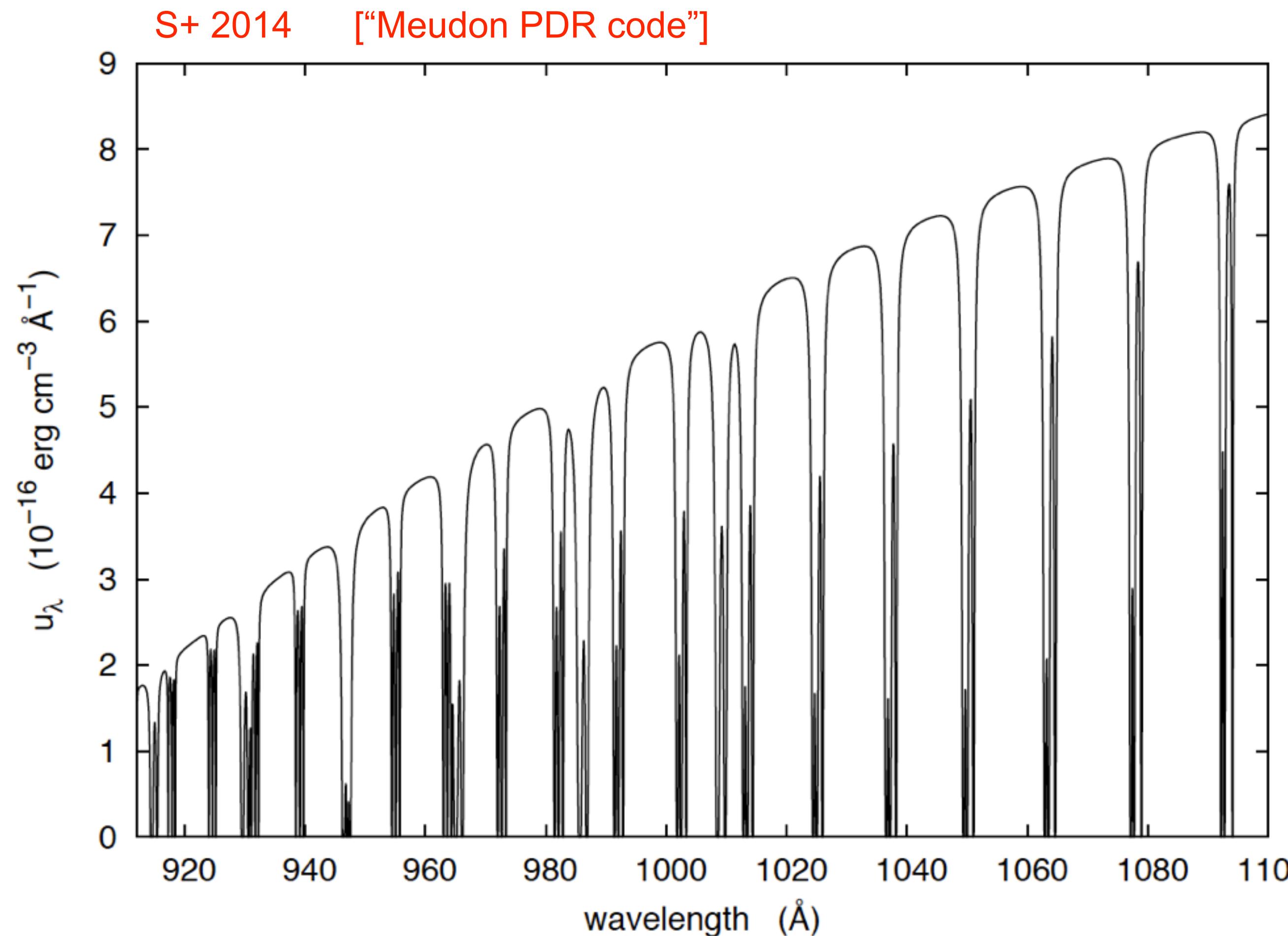
H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



H₂ Photodissociation in the Lyman-Werner bands (912-1108 Å):



Lyman-Werner Radiative Transfer:



Characteristic multi-line H₂ absorption spectrum, and “self-shielding”.

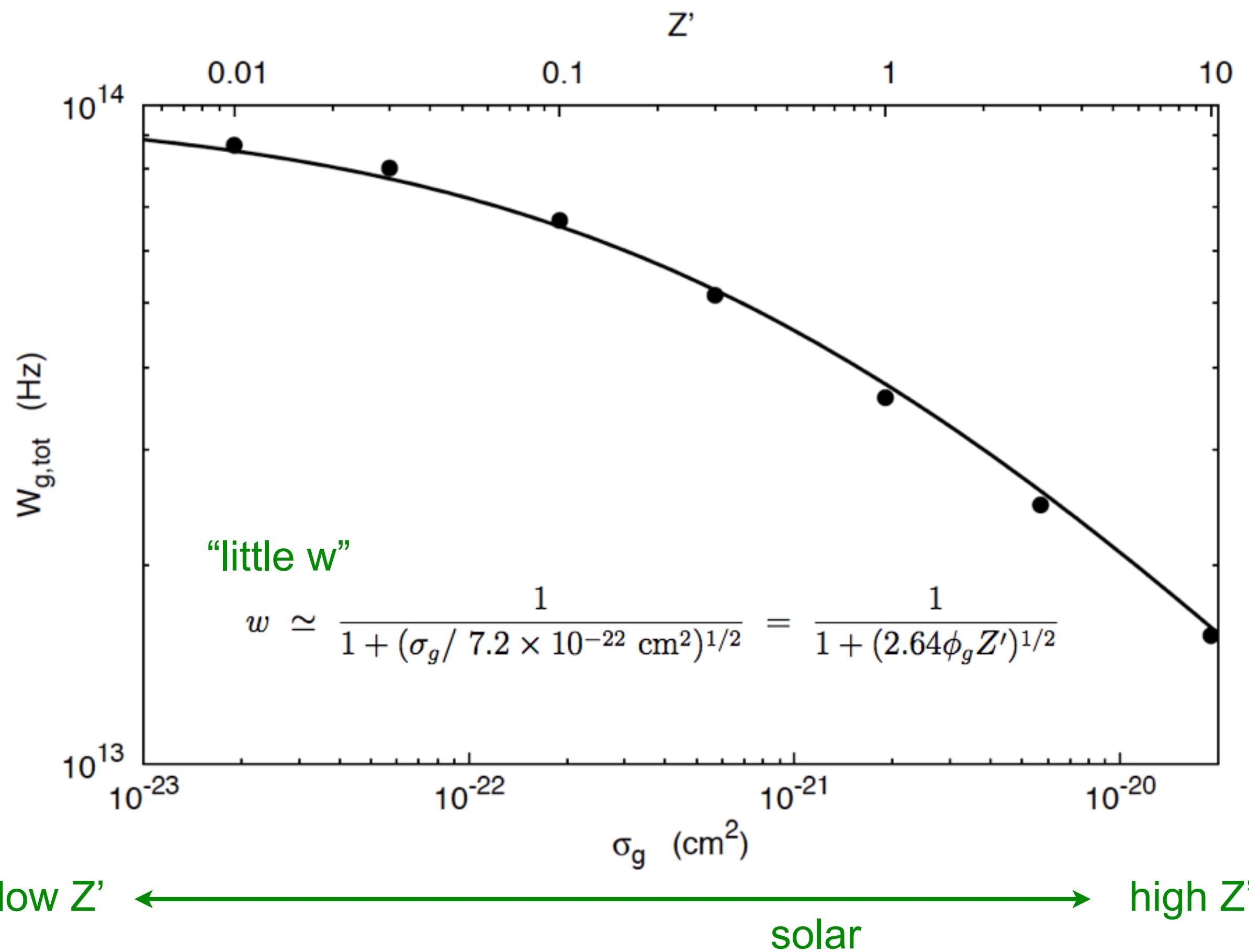
Dust absorption cross-section per hydrogen nucleus:

$$\sigma_g = 1.9 \times 10^{-21} \phi_g Z' \text{ cm}^2$$

Numerical radiative transfer on a fine frequency grid with a spectral resolution $\sim 10^5$.

“Universal” Total H₂ Dust Limited Dissociation Bandwidth:

S+ 2014



Total LW Flux:

$$F_0 \equiv \int_{\nu_1}^{\nu_2} F_{\nu} d\nu$$

“Effective Dissociation Flux”

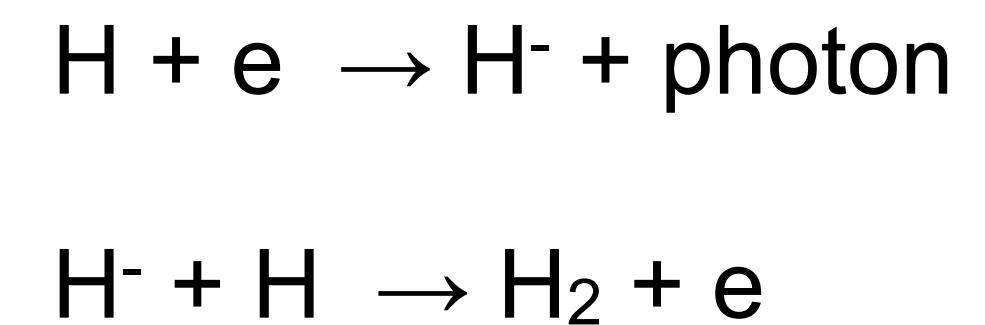
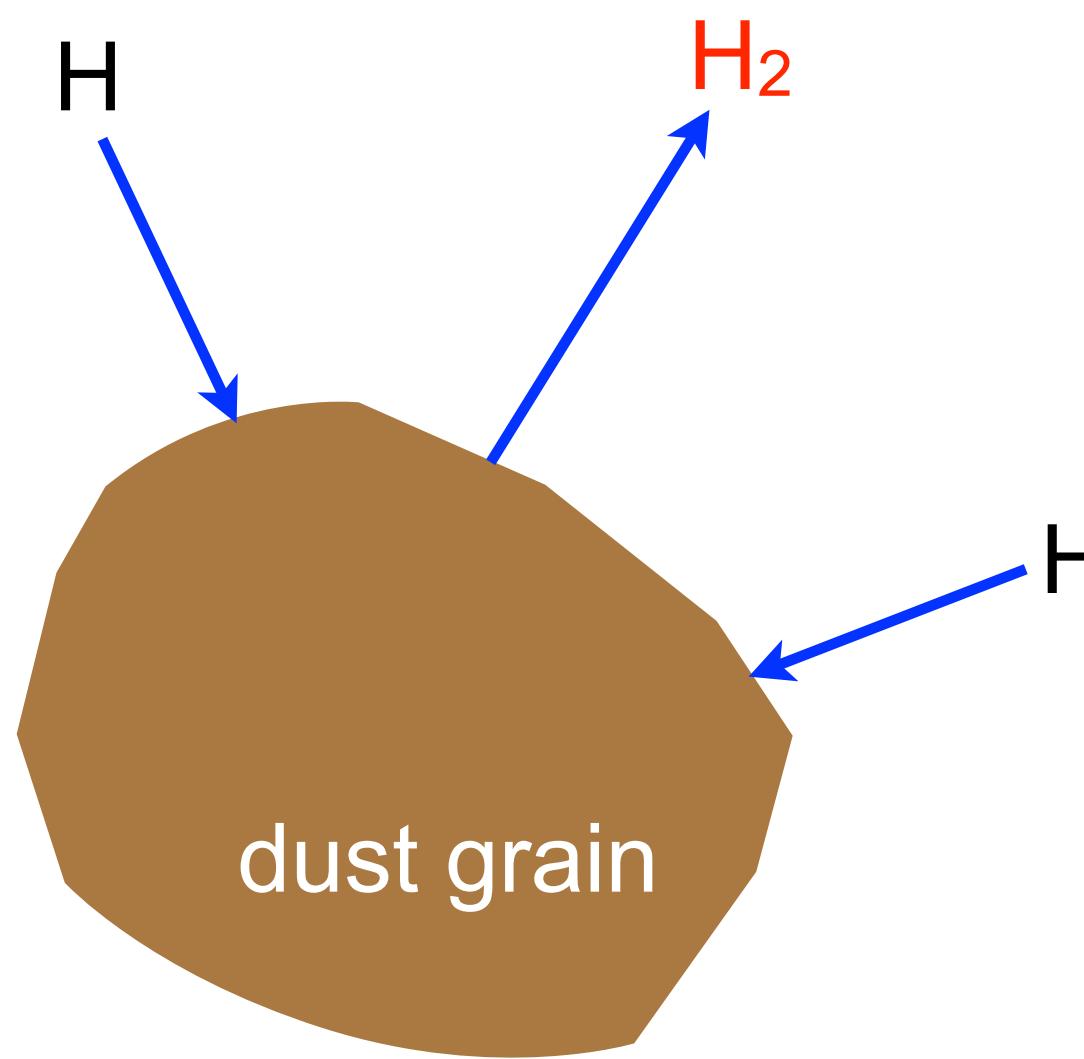
$$\bar{f}_{\text{diss}} \times w F_0$$

The bandwidth (Hz) of radiation absorbed in H₂ line dissociations in a dusty and fully molecular cloud.

“H₂ dust” versus “H₂ lines”

Universal: independent of radiation field intensity, or cloud gas density, etc.

H₂ Formation:



$$R = 3 \times 10^{-17} \left(\frac{T}{100 \text{ K}} \right)^{1/2} Z' \text{ cm}^3 \text{ s}^{-1}$$

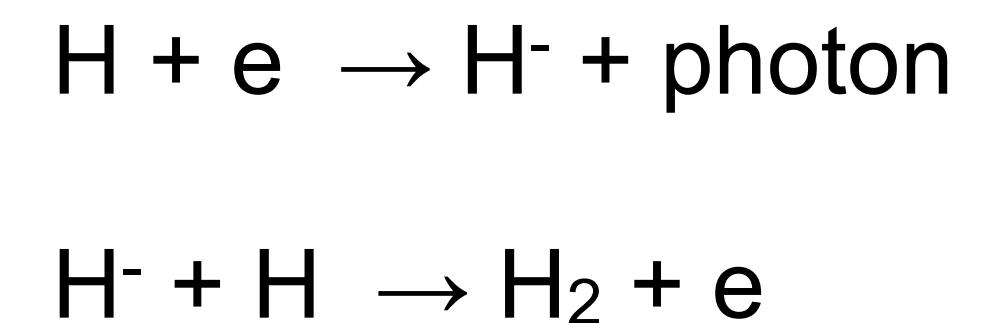
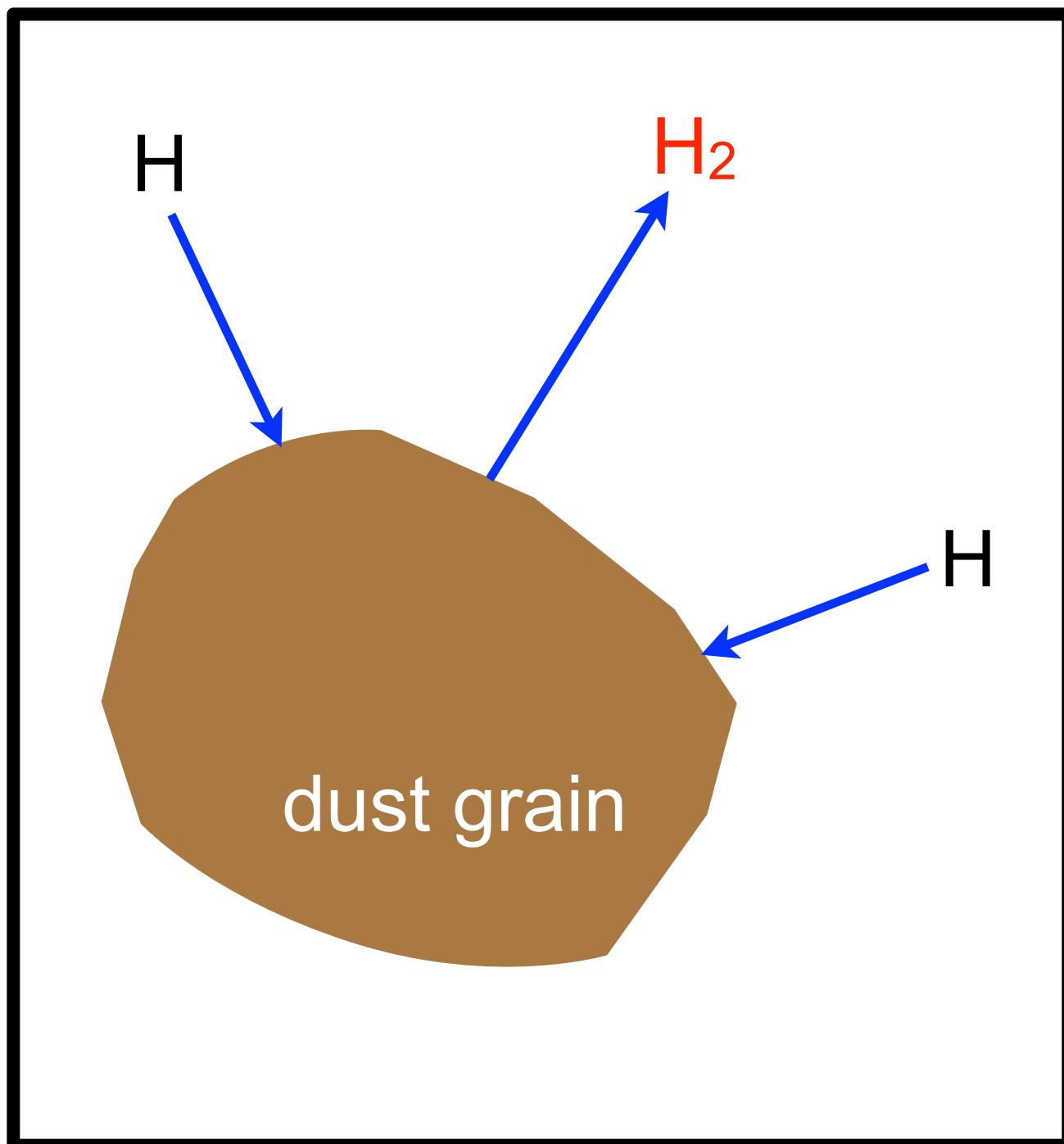
Z' is the “metallicity” (Z'=1 is solar)

$$t_{\text{eq}} = \frac{1}{Rn} = \frac{10^9}{Z'n} \text{ yr}$$

time scale for equilibrium

H₂ Formation:

a black box...
and another talk!



$$R = 3 \times 10^{-17} \left(\frac{T}{100 \text{ K}} \right)^{1/2} Z' \text{ cm}^3 \text{ s}^{-1}$$

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time scale for equilibrium

Basic Theory Questions:

- What do the depth-dependent HI-to-H₂ transition profiles look like for far-UV irradiated systems?
- What is the resulting total HI column densities (cm⁻²) or HI mass surface densities (M_{\odot} pc⁻²) ?

Dimensionless Parameter:

$$\alpha G \equiv \frac{D_0 G}{Rn}$$

Physical Meaning:

self-shielded H₂ dissociation rate

H₂ formation rate

Dimensionless Parameter:

Sternberg 1988; McKee & Krumholz 2010; Sternberg+ 2014

$$\alpha G = \frac{D_0 G}{Rn} = \bar{f}_{\text{diss}} \frac{\sigma_g w F_0}{Rn} = \bar{f}_{\text{diss}} \frac{\sigma_g w F_0}{D_0} \frac{n_1}{n_2} \Big|_{\text{freespace}}$$

Physical Meaning:

HI-dust absorption rate of the effective dissociation flux

free space H₂ photodissociation rate

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Sternberg 1988; McKee & Krumholz 2010; Sternberg+ 2014

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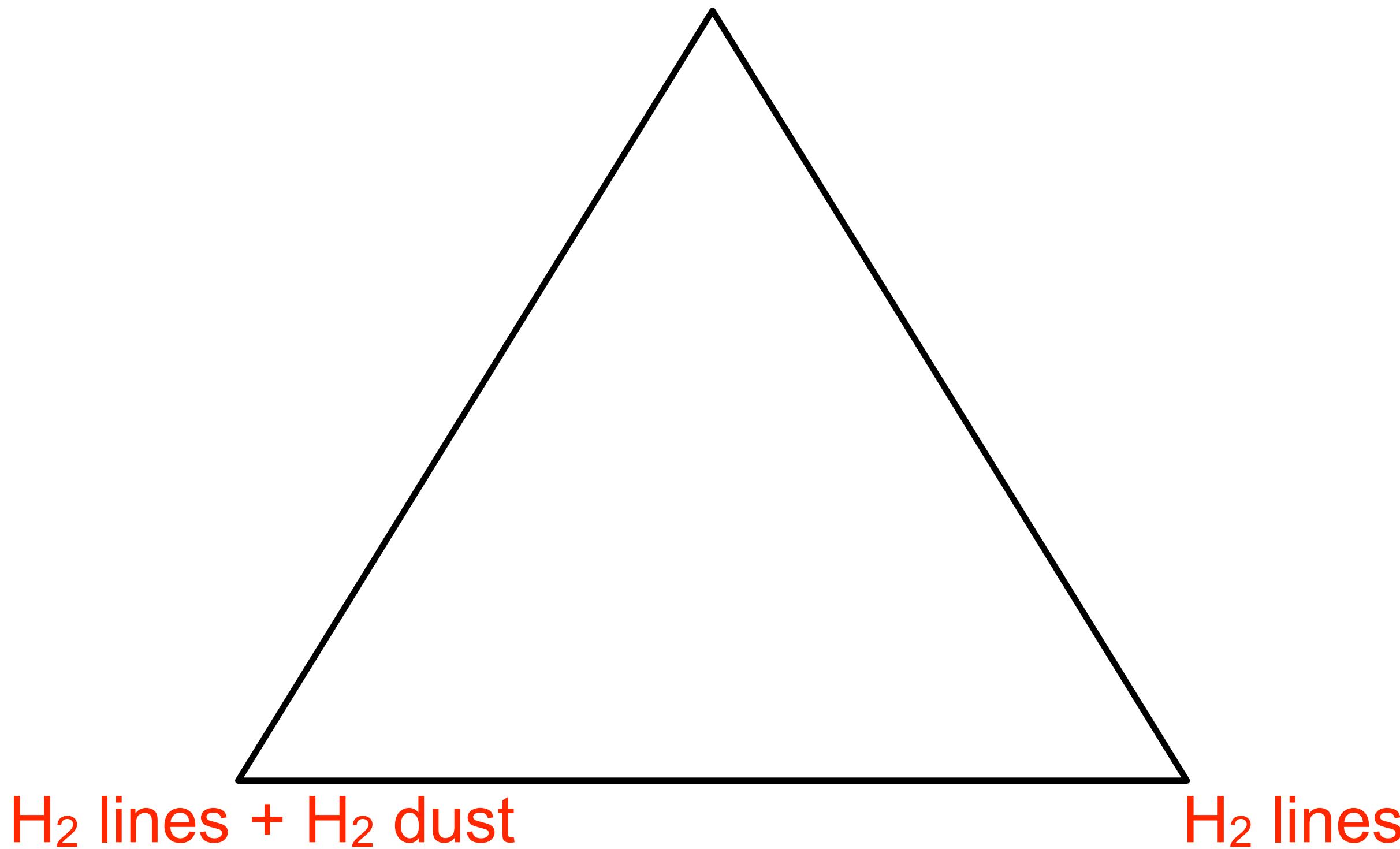
$$\begin{aligned} \alpha G = & 1.54 \left(\frac{\sigma_g}{1.9 \times 10^{-21} \text{ cm}^2} \right) \left(\frac{F_0}{2.07 \times 10^7 \text{ cm}^{-2} \text{ s}^{-1}} \right) \\ & \times \left(\frac{3 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}}{R} \right) \left(\frac{100 \text{ cm}^{-3}}{n} \right) \frac{1}{1 + (2.64 \phi_g Z')^{1/2}} \end{aligned}$$

...so can be small “weak-field”
or large “strong-field”

Three-Way Competition for the FUV Absorption:

$\alpha G \gg 1$ “strong-field”

HI dust



$\alpha G \ll 1$ “weak-field”

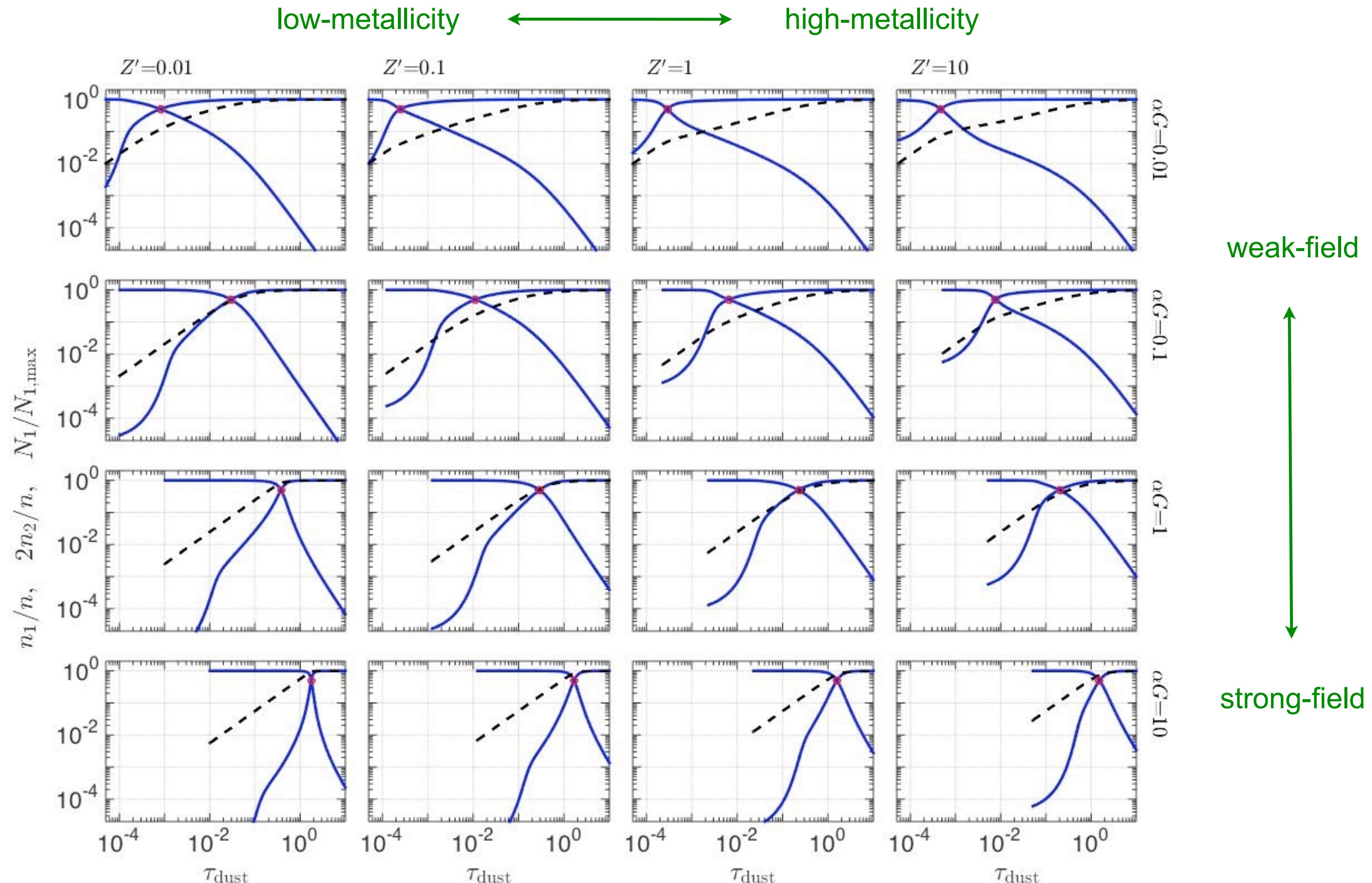
$Z' \gtrsim 1$ “high-metallicity”

$\alpha G \ll 1$ “weak-field”

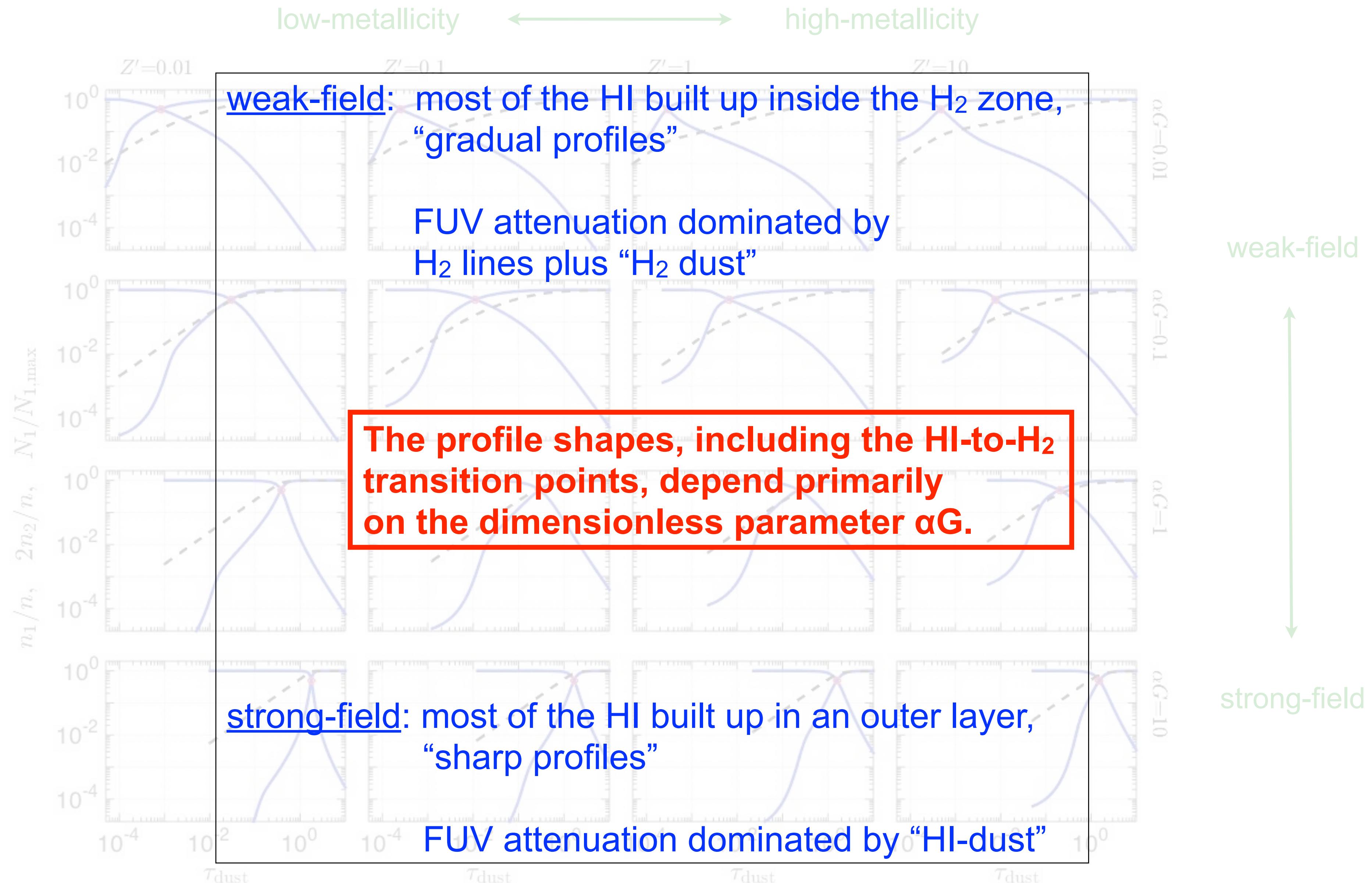
$Z' \lesssim 1$ “low-metallicity”

**The profile shapes depend primarily
on the dimensionless parameter αG .**

HI-to-H₂ Transition Profiles: S+14 Bialy & Sternberg 2016 ApJ 822 83



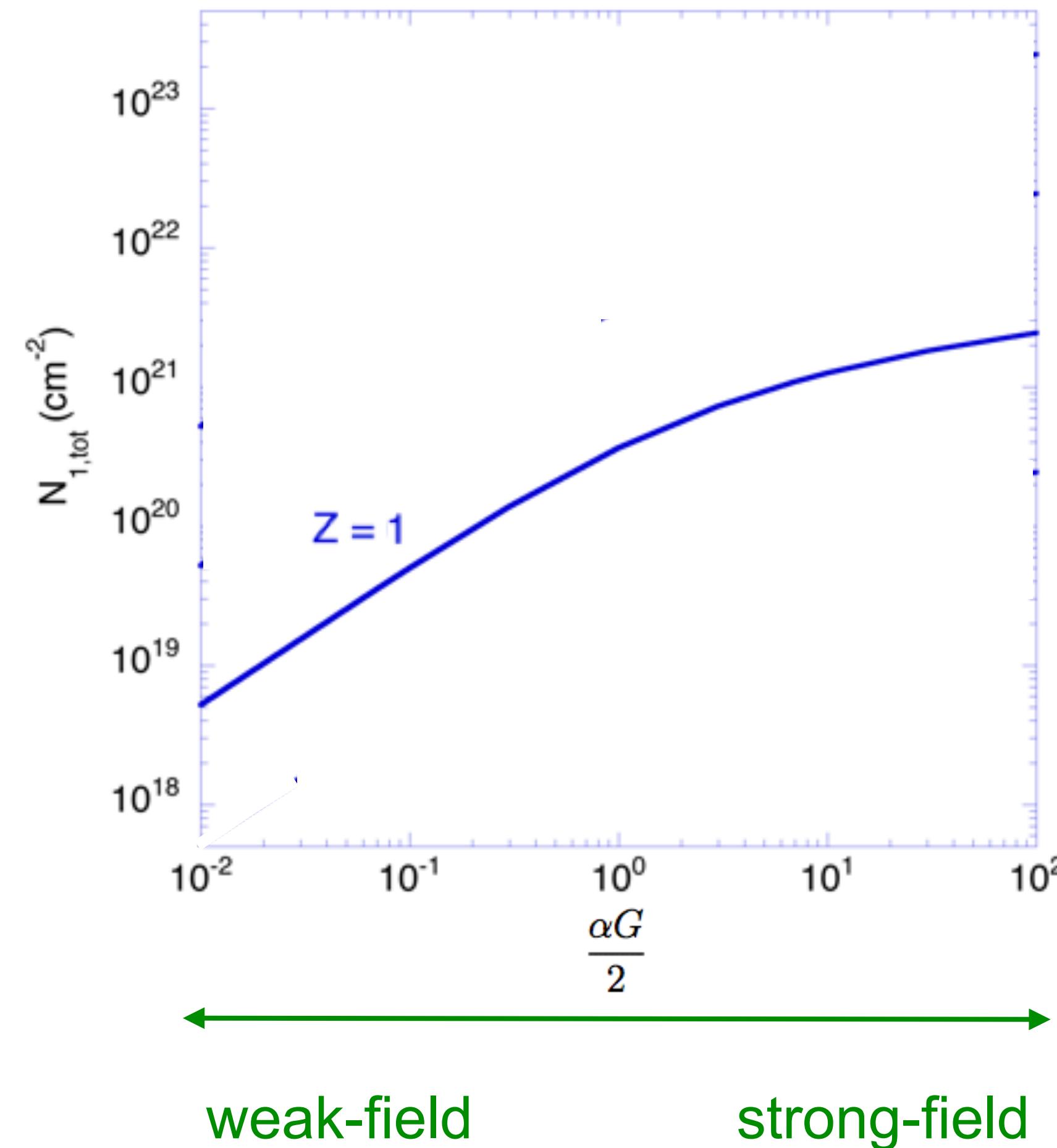
HI-to-H₂ Transition Profiles: S+14 Bialy & Sternberg 2016 arXiv:1601.02608



General Purpose Analytic Formula for the Total HI Column Density:

$$N_{1,\text{tot}} = \frac{1}{\sigma_g} \ln \left[\frac{\alpha G}{4} + 1 \right] = \frac{1}{\sigma_g} \ln \left[\frac{1}{4} \frac{\bar{f}_{\text{diss}} \sigma_g w F_0}{Rn} + 1 \right]$$

[derived in two ways in S+14]

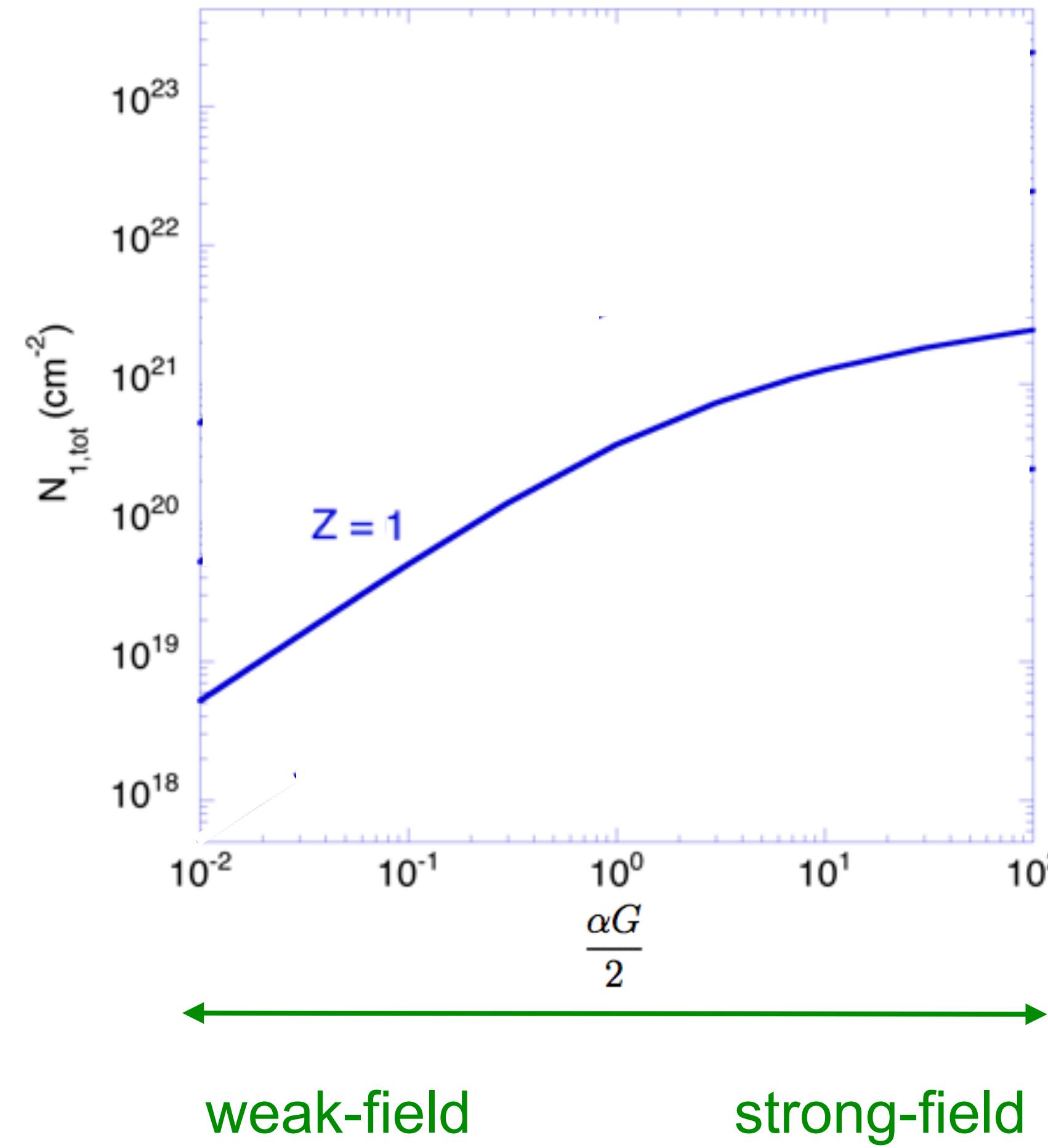


Valid for all regimes:

- weak and strong fields
- gradual to sharp transitions
- arbitrary metallicity

[note: no reference to the H₂ line photodissociation cross sections!]

Weak-Field Limit:



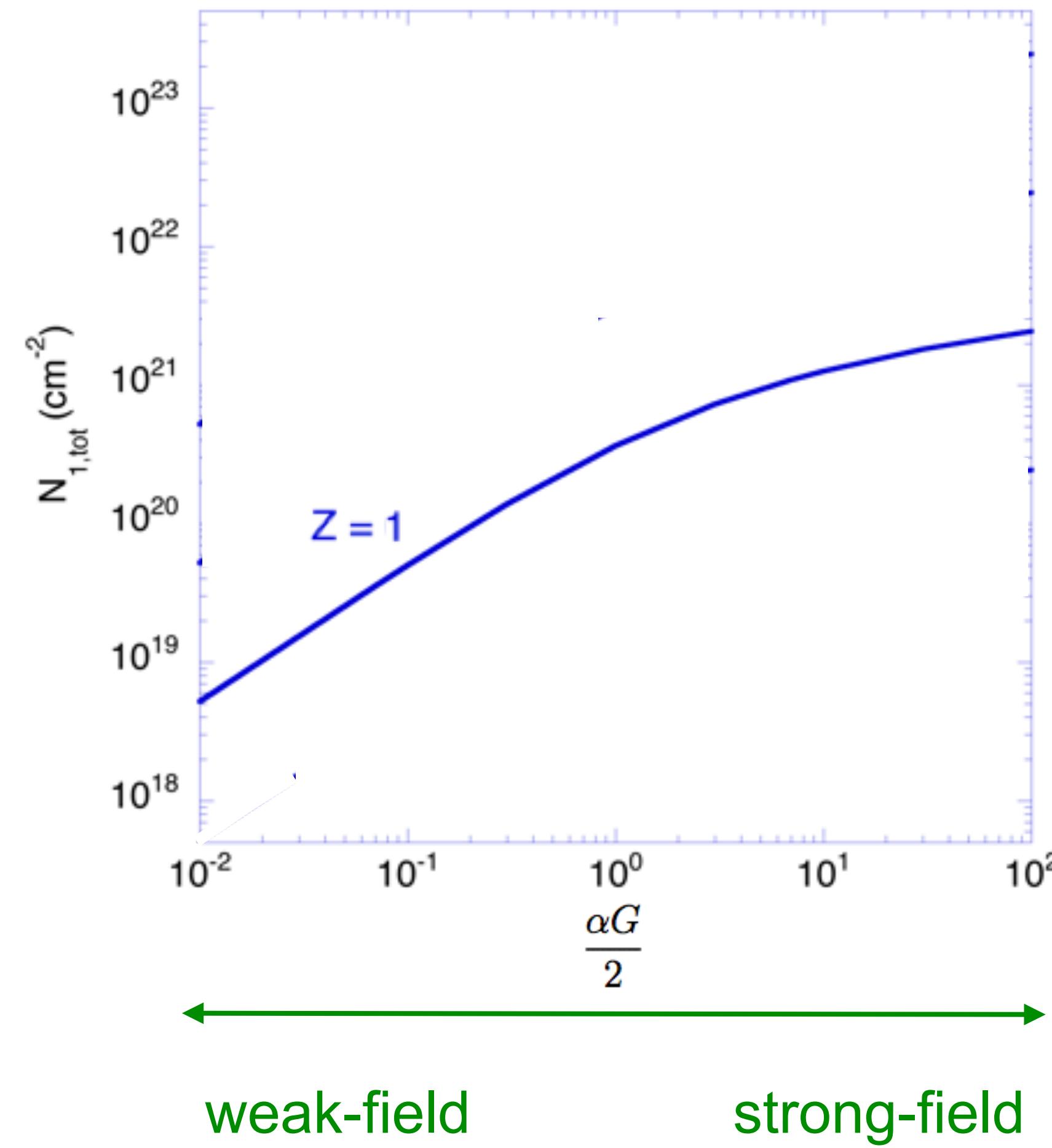
$$N_{1,\text{tot}} = \frac{1}{4} \bar{f}_{\text{diss}} w F_0$$

$$Rn \ N_{1,\text{tot}} = \frac{1}{4} \bar{f}_{\text{diss}} w F_0$$

formation rate per unit area = effective dissociation flux

(a “Strömgren Relation”)

Strong-Field Limit:



$$N_{1,\text{tot}} \approx \frac{1}{\sigma_g}$$

(neglecting the logarithmic term)

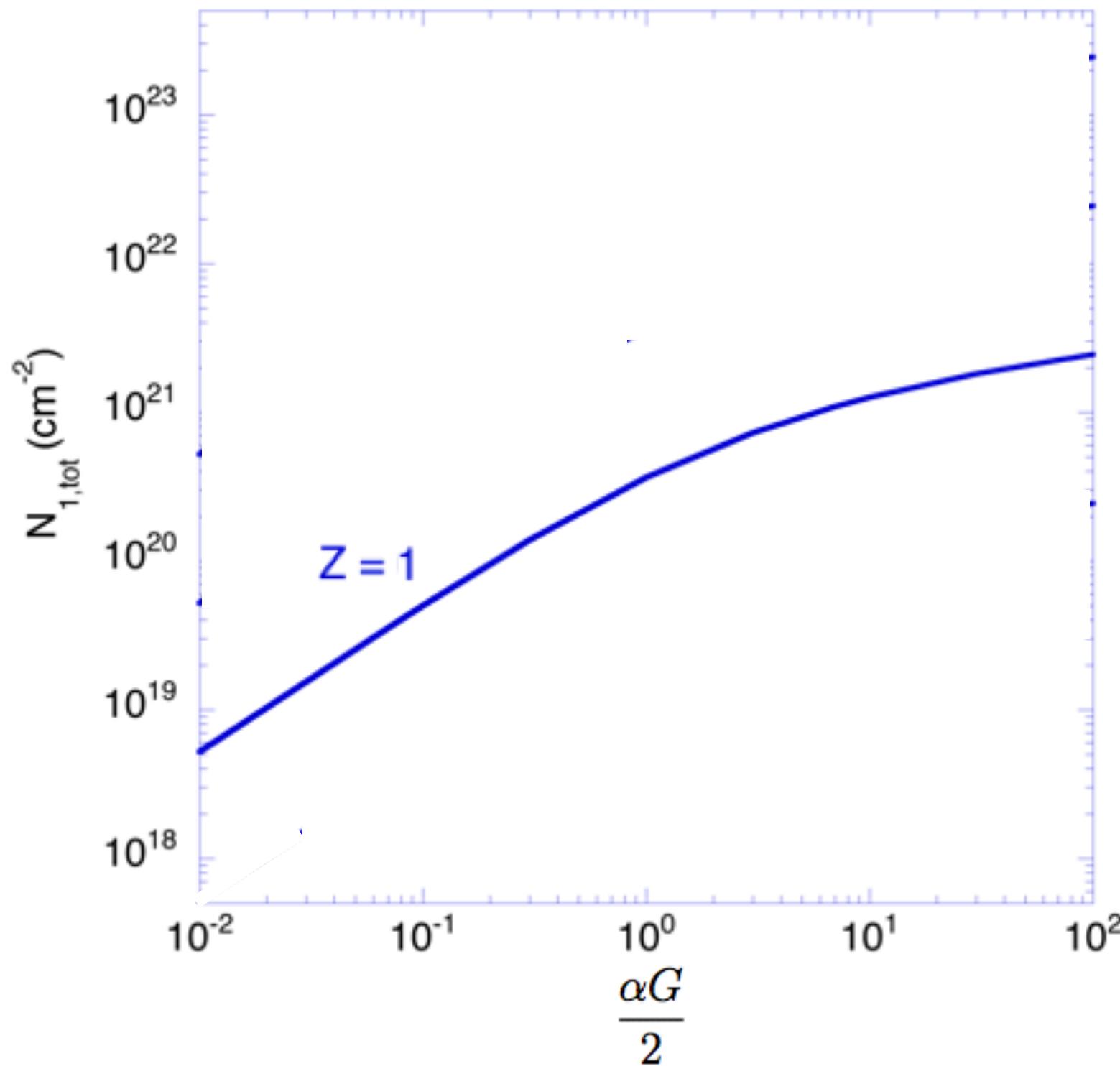
makes sense: When HI-dust dominates the attenuation of the far-UV field, the HI-column is “self-limited” and

$$\tau_{\text{HI dust}} = \sigma_g N_{1,\text{tot}} \approx 1$$

Heavy-Element Abundances “Metallicity”:

$$R \propto Z' \quad \sigma_g \propto Z'$$

H_2 formation rate coefficient
and dust absorption cross-section
both proportional to metallicity.



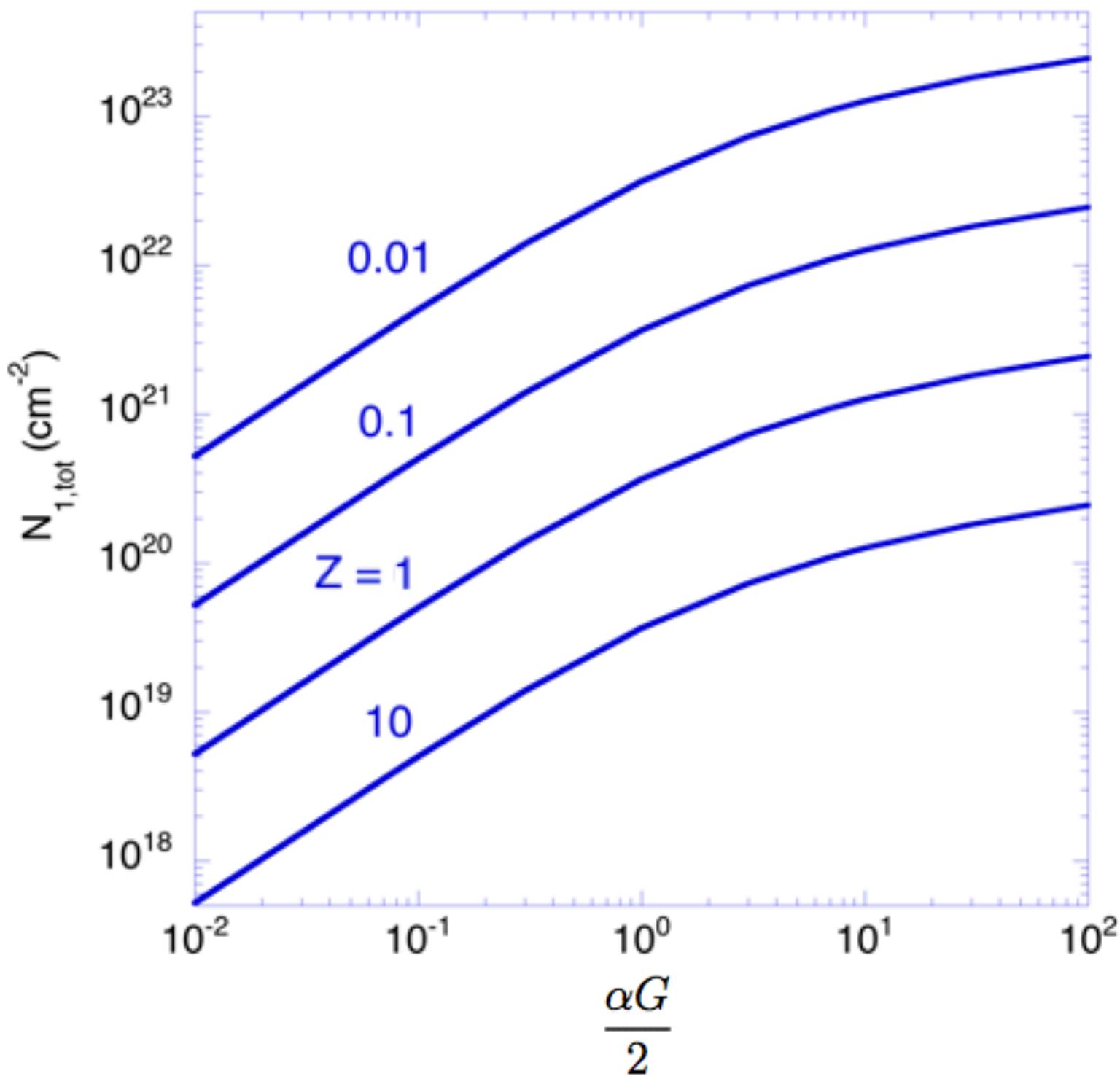
$$N_{1,\text{tot}} = \frac{1}{4} \frac{\bar{f}_{\text{diss}} w F_0}{Rn} \propto \frac{1}{Z'}$$

weak-field

$$N_{1,\text{tot}} \approx \frac{1}{\sigma_g} \propto \frac{1}{Z'}$$

strong-field

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strong-field

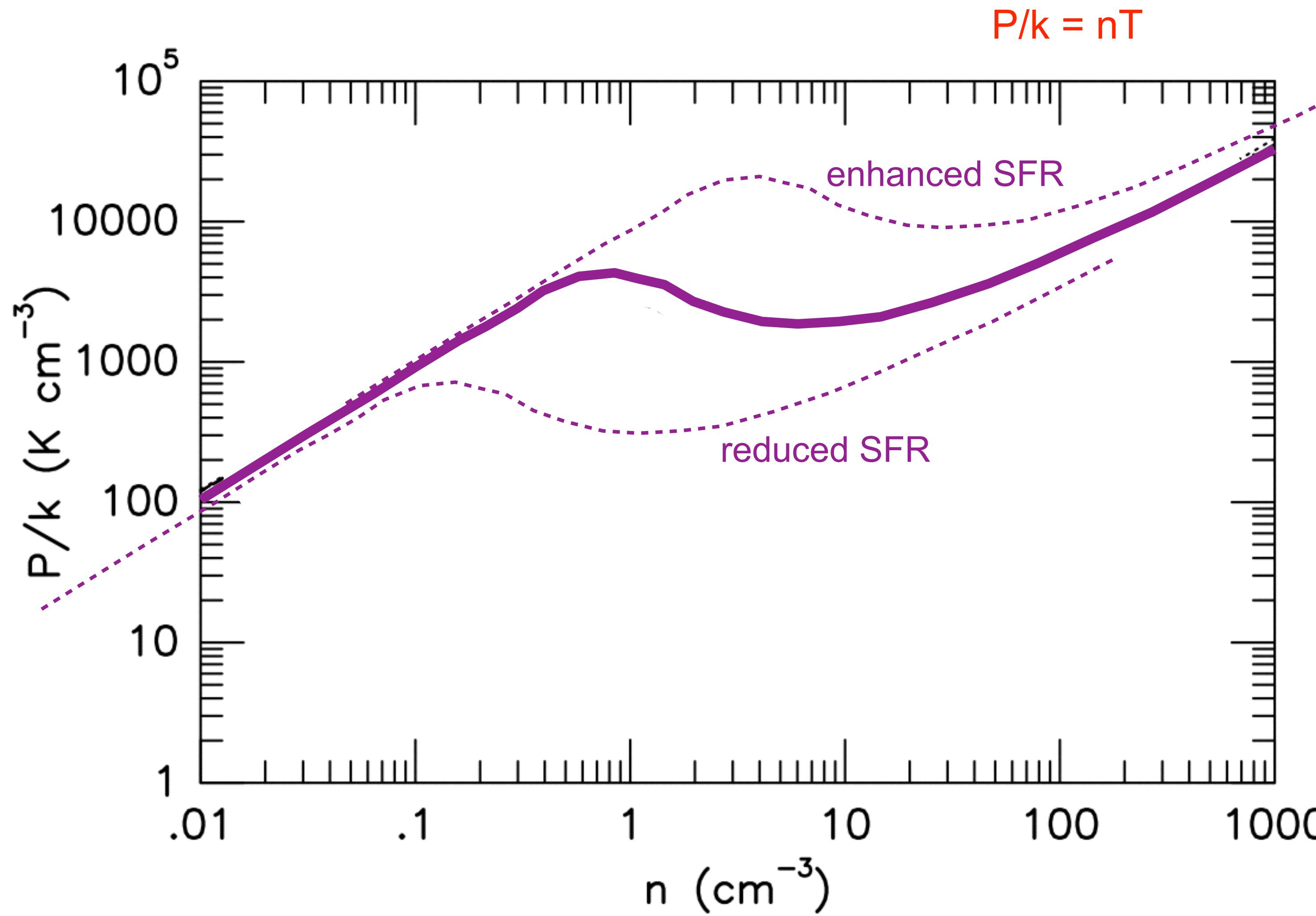
General Purpose Analytic Formula for the Total HI Column Density:

S+14

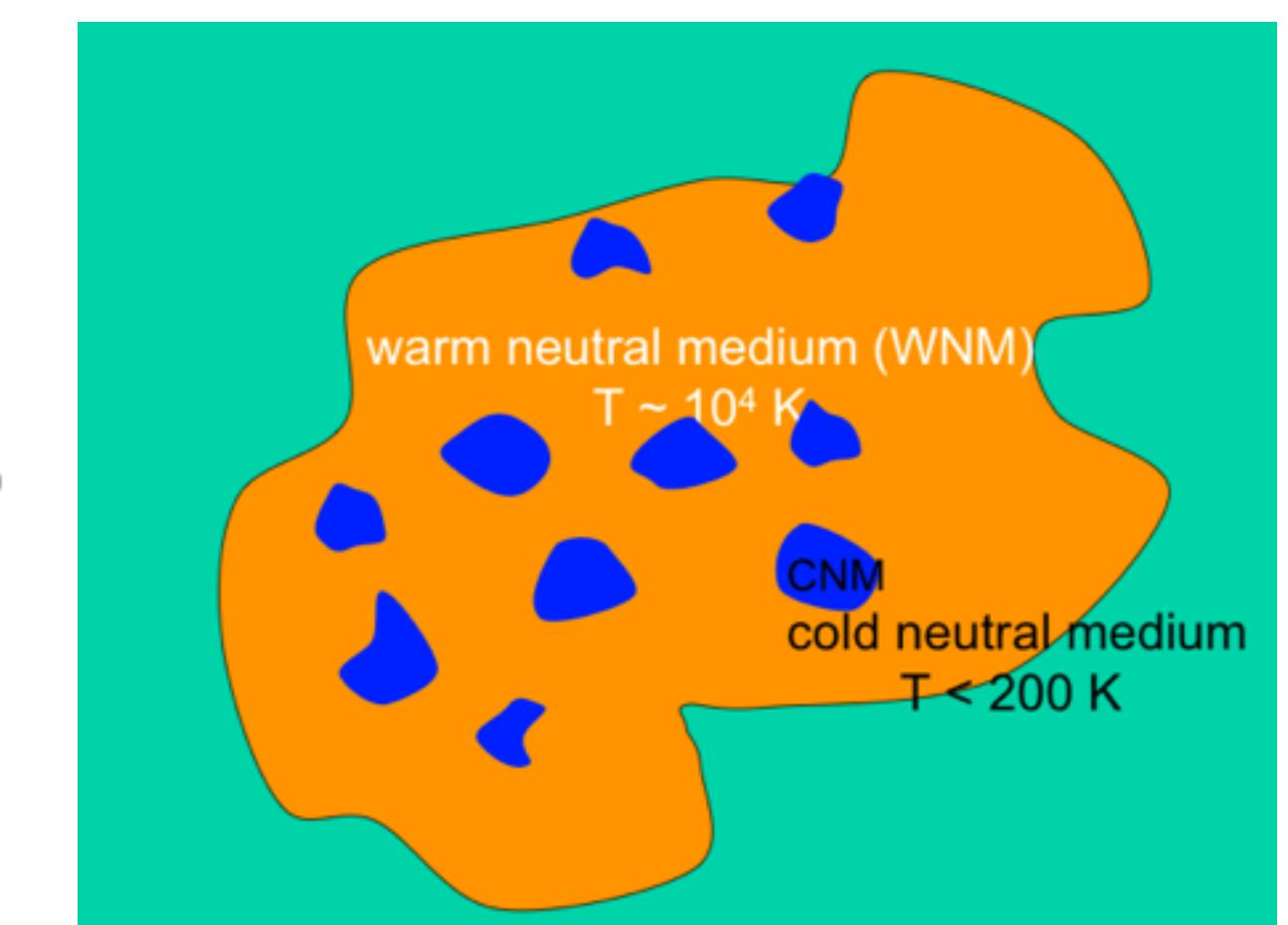
$$N_{1,\text{tot}} = \frac{1}{\sigma_g} \ln \left[\frac{\alpha G}{4} + 1 \right] = \frac{1}{\sigma_g} \ln \left[\frac{1}{4} \frac{\bar{f}_{\text{diss}} \sigma_g w F_0}{Rn} + 1 \right]$$

- useful for interpreting 21cm observations
- incorporation into hydrodynamics simulations
- application to “self-regulated” media

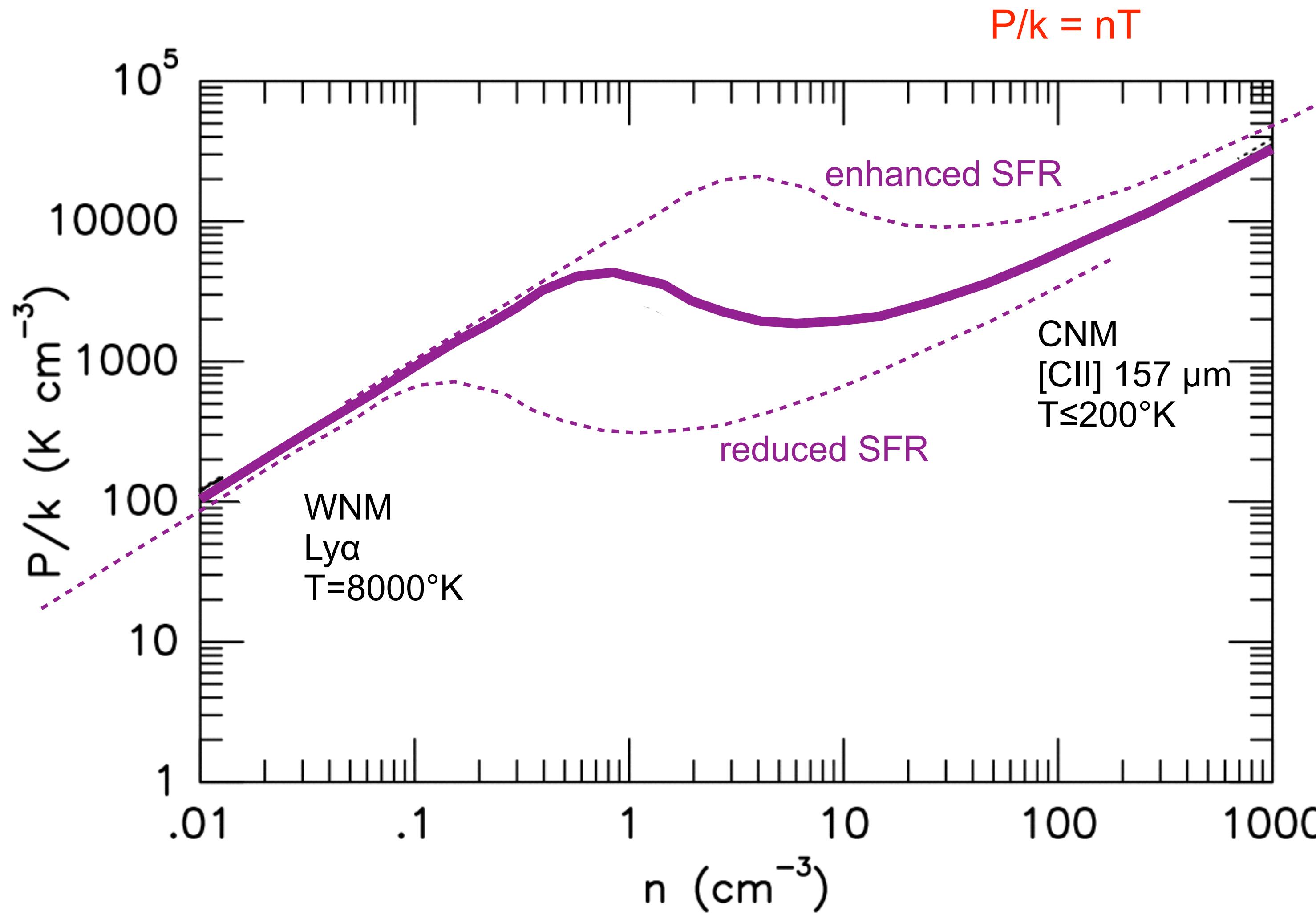
HI Thermal Phases in Self-Regulated Media:



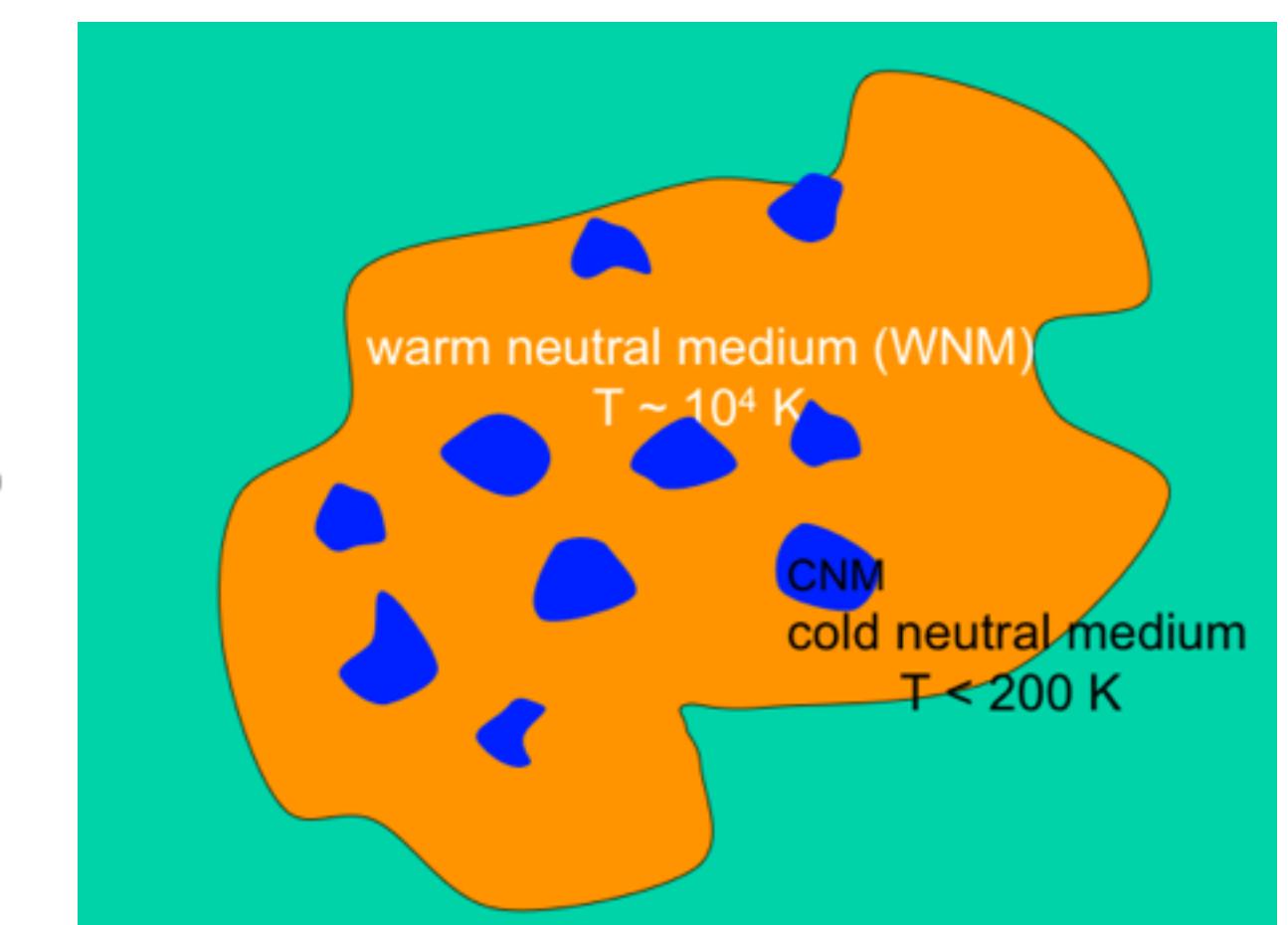
Field, Goldsmith & Habing 1969 ApJ 155 149



HI Thermal Phases in Self-Regulated Media:

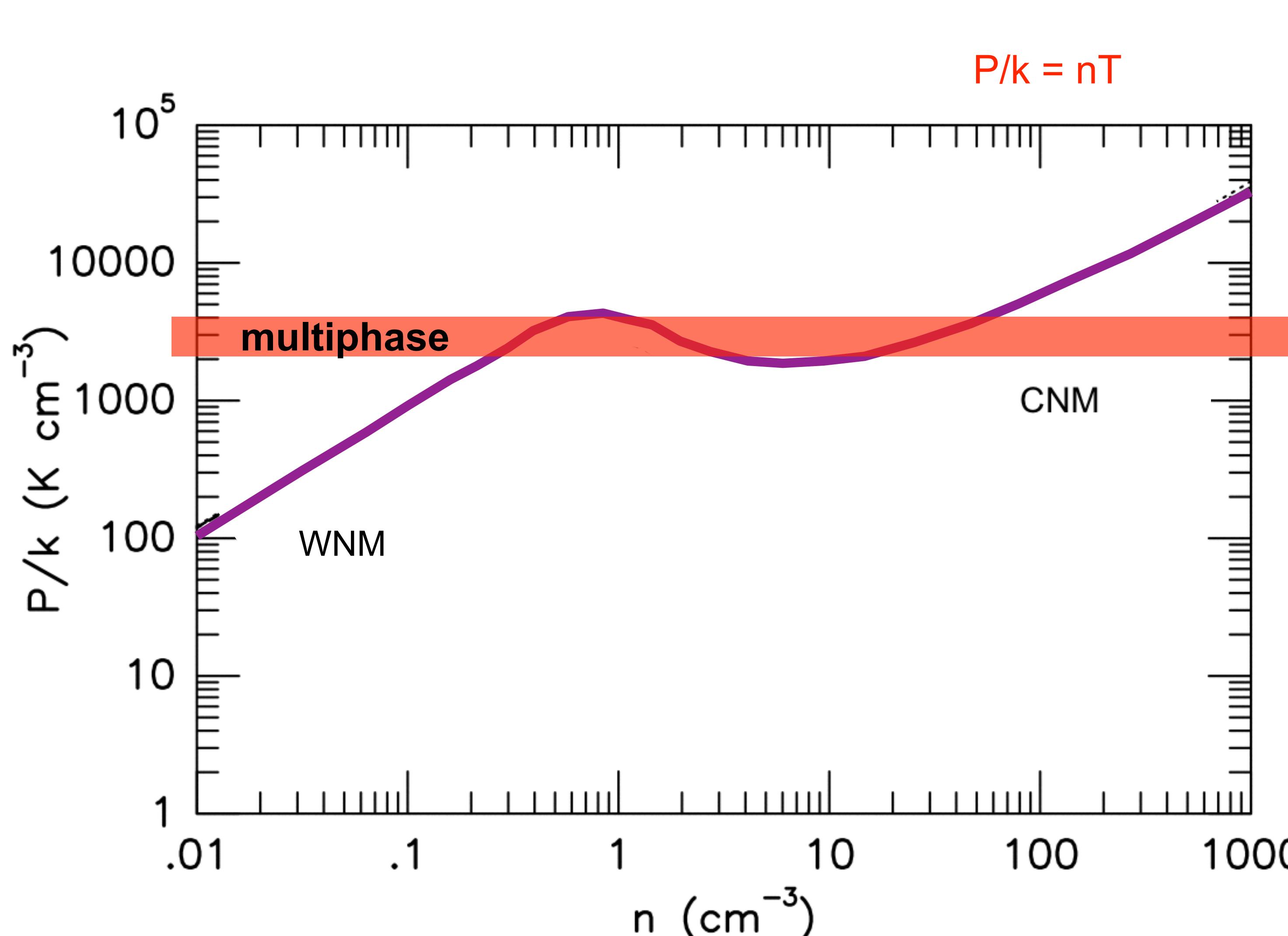


Field, Goldsmith & Habing 1969 ApJ 155 149

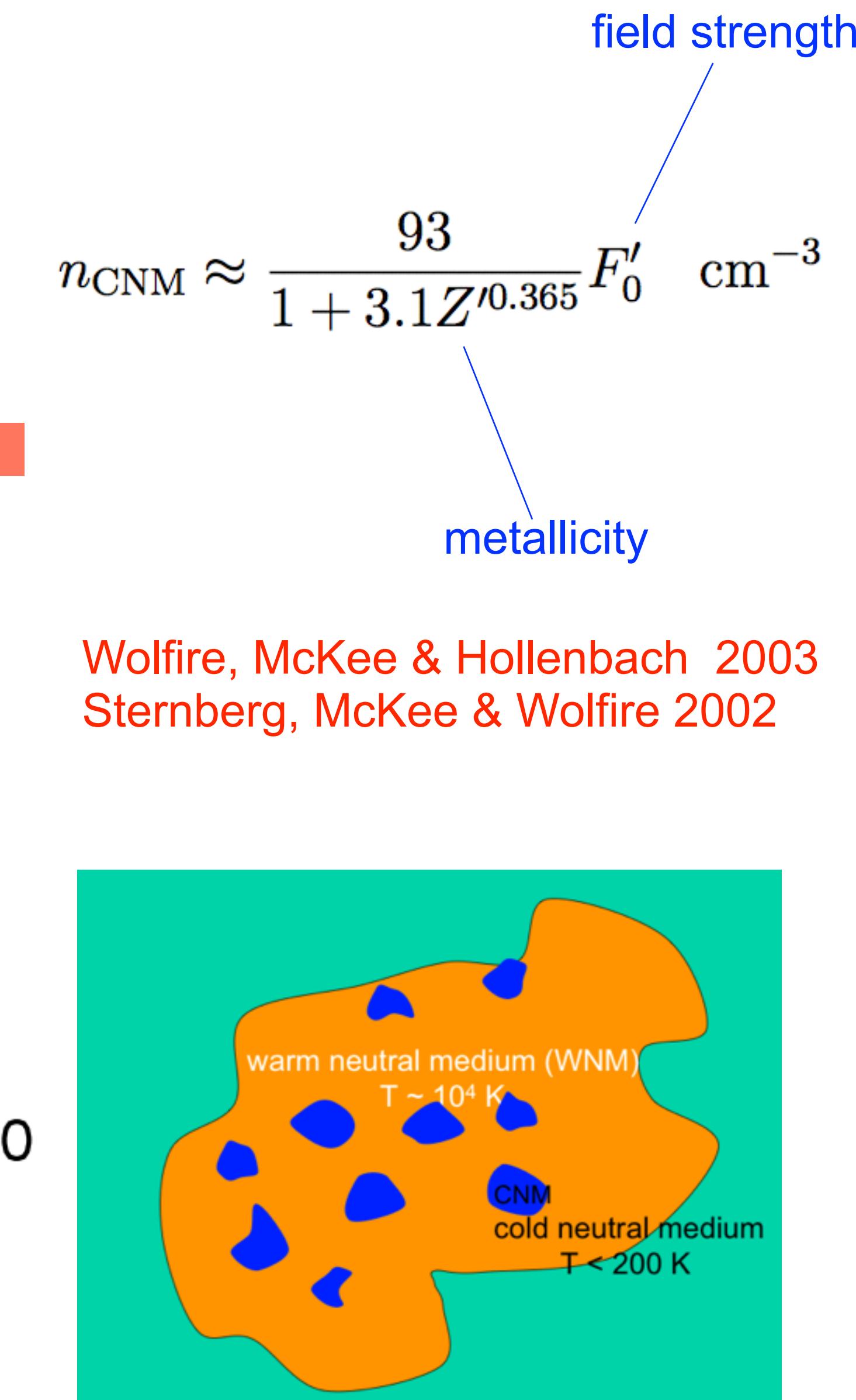


HI Thermal Phases in Self-Regulated Media:

Ansatz:
Krumholz McKee & Tumlinson 2009

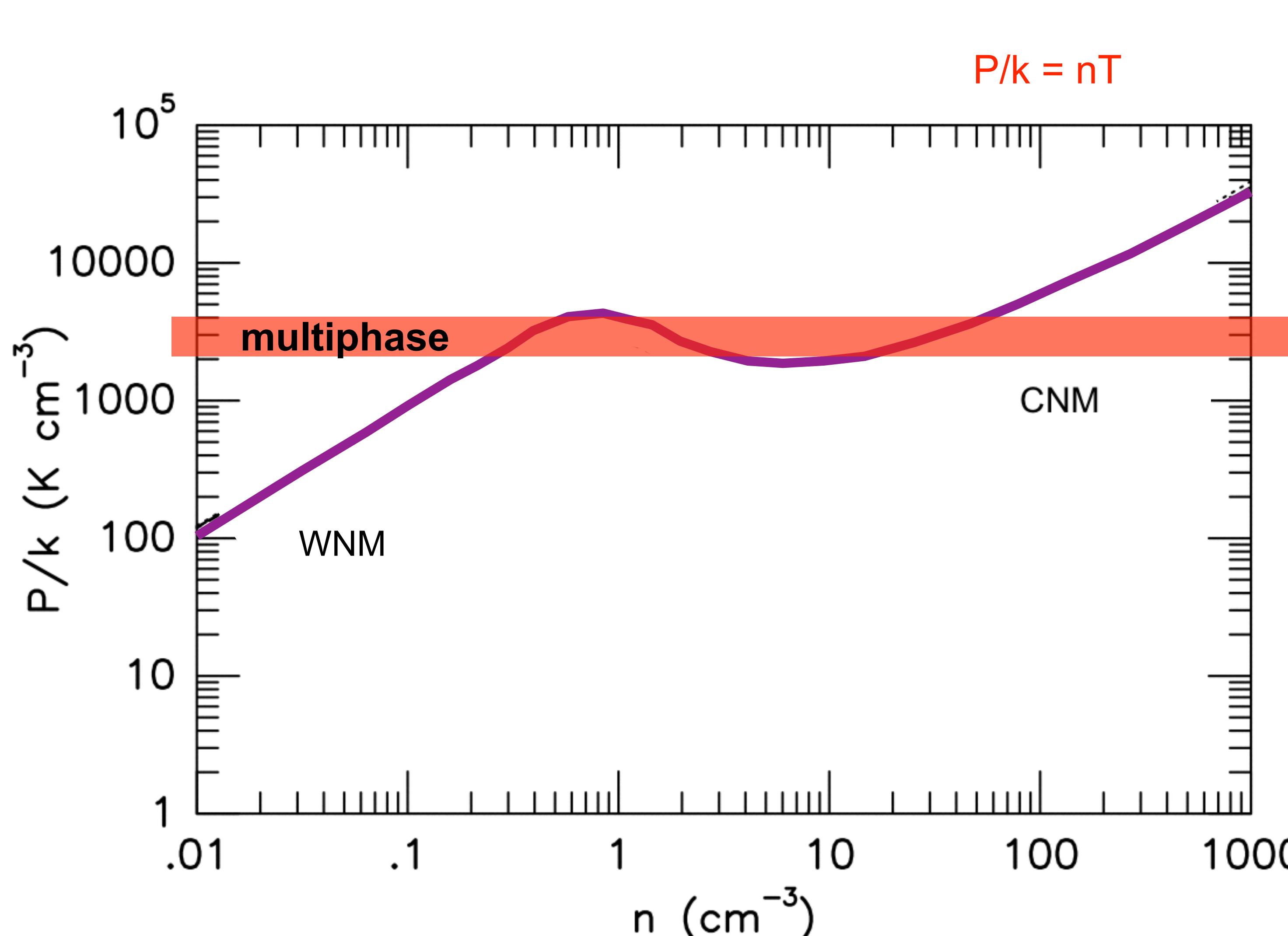


Field, Goldsmith & Habing 1969 ApJ 155 149

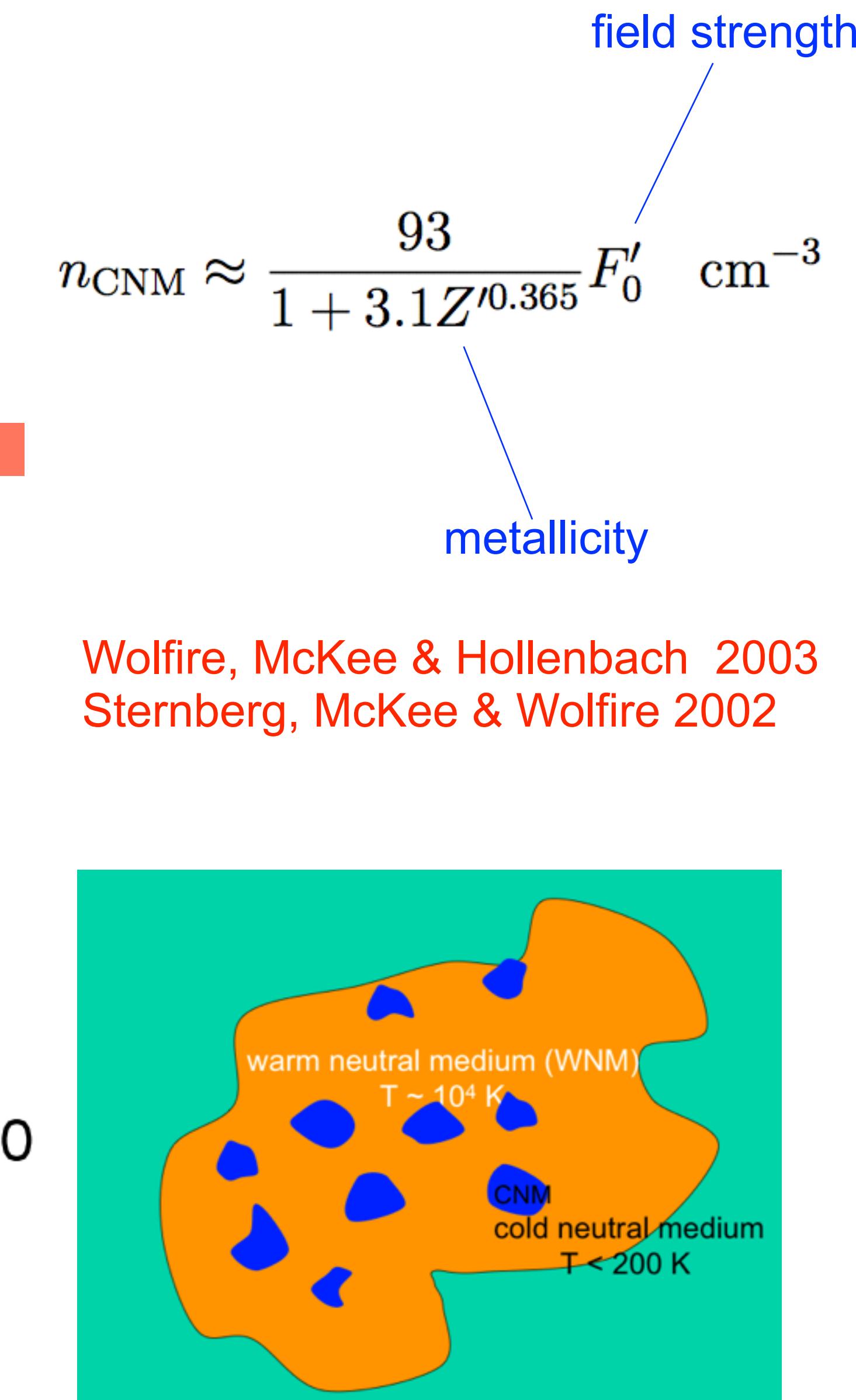


HI Thermal Phases in Self-Regulated Media:

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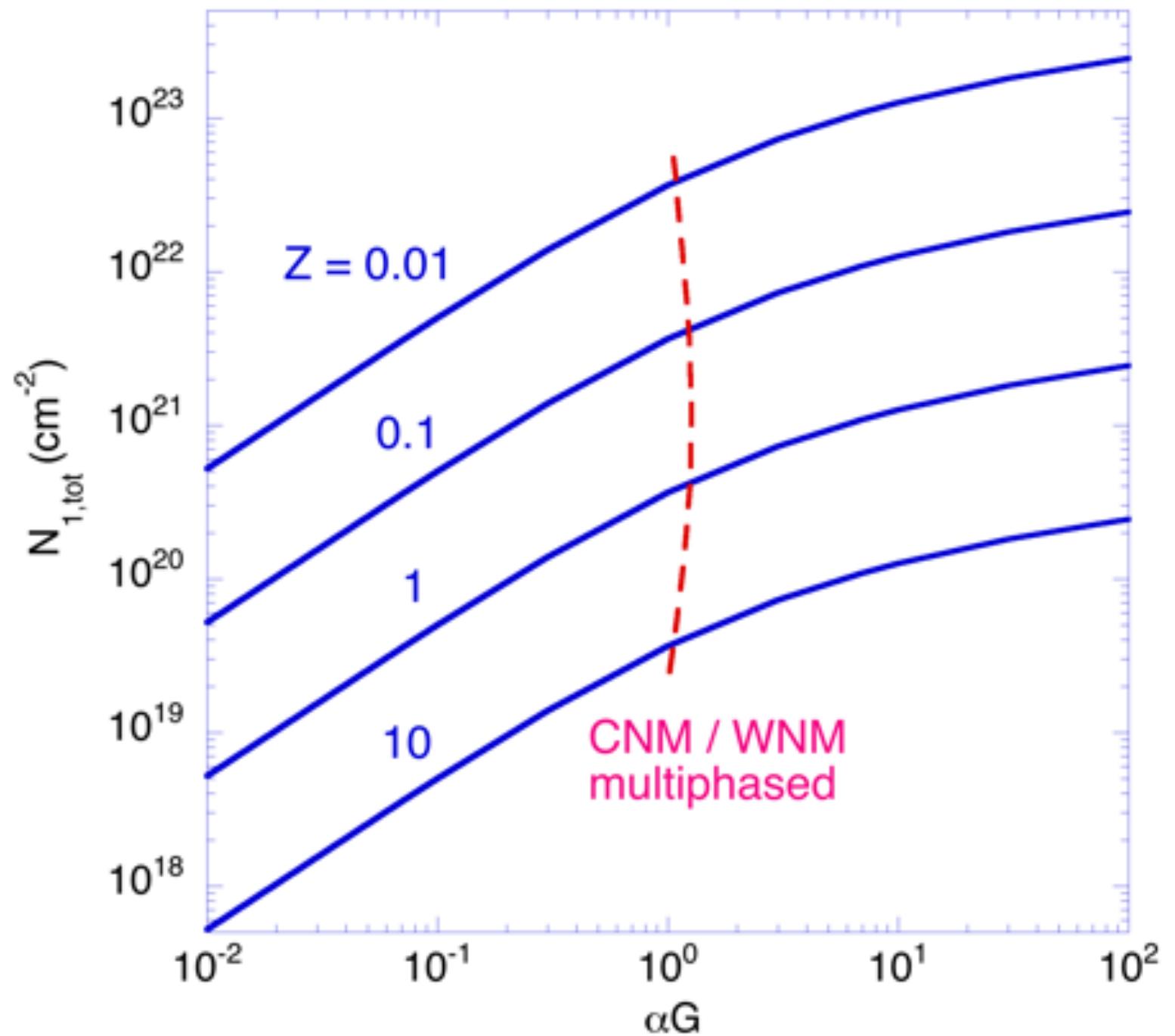


Wolfire, McKee & Hollenbach 2003
Sternberg, McKee & Wolfire 2002

HI Column Density for Self-Regulated Media:

$$\frac{(\alpha G)_{\text{CNM}}}{2} \approx 1$$

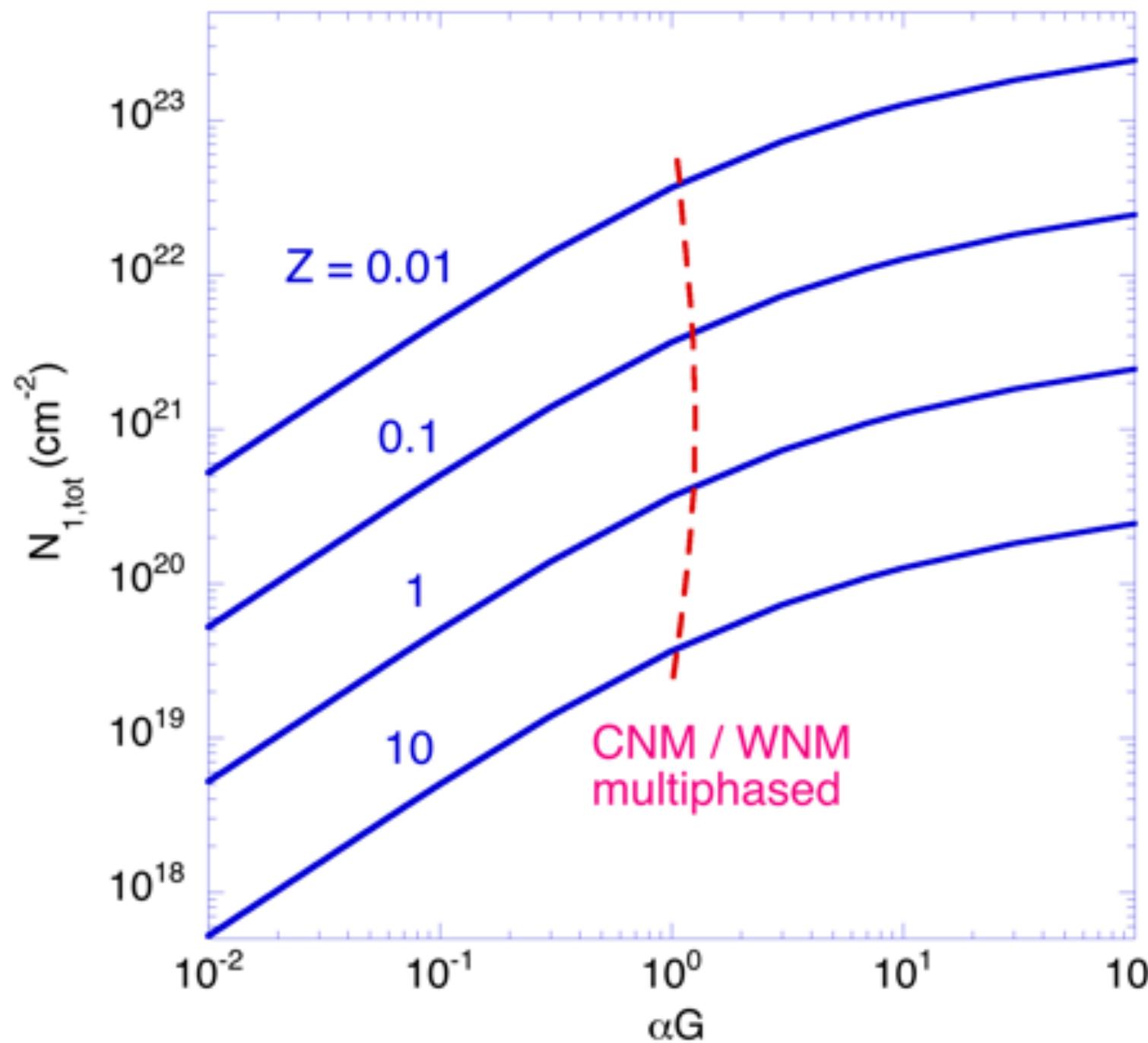
remarkable!



HI Column Density for Self-Regulated Media:

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$$\Sigma_{\text{HI}} \approx \frac{6}{\phi_g Z'} \text{ M}_\odot \text{ pc}^{-2}$$

characteristic HI photodissociation mass surface density in self-regulated systems

$$\Sigma_{\text{gas},*}(Z') \equiv 2 \times \Sigma_{\text{HI}} \approx \frac{12}{\phi_g Z'} \text{ M}_\odot \text{ pc}^{-2}$$

“transition” total gas mass surface density... star-formation threshold...galaxies.

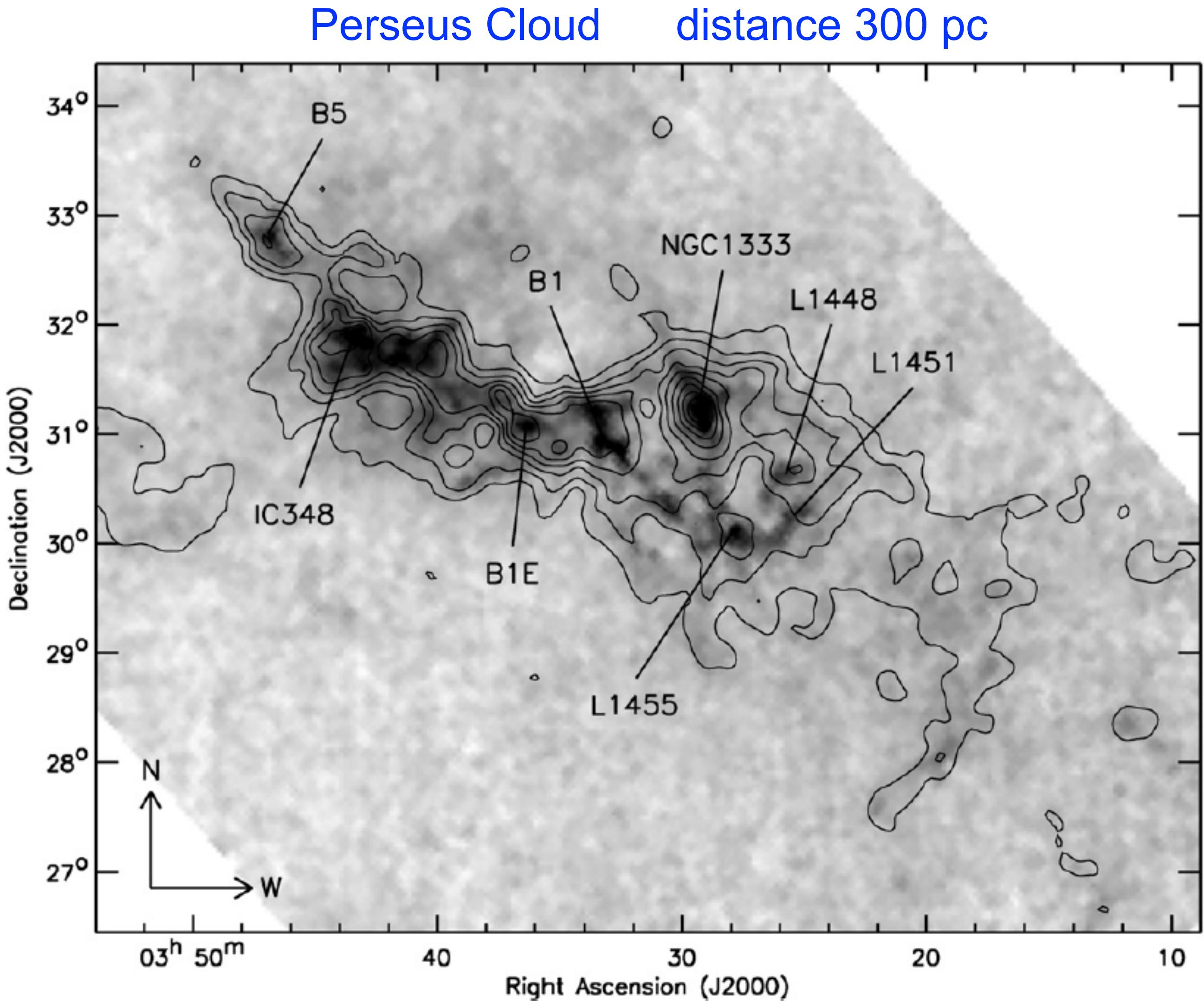
independent of radiation field intensity and/or gas density.

H_I-to-H₂ in the Perseus Molecular Cloud:

Giovanni Antonio Vanosino's celestial globe 1567 Vatican Museum



HI-to-H₂ in Perseus:



2MASS Av and Ico

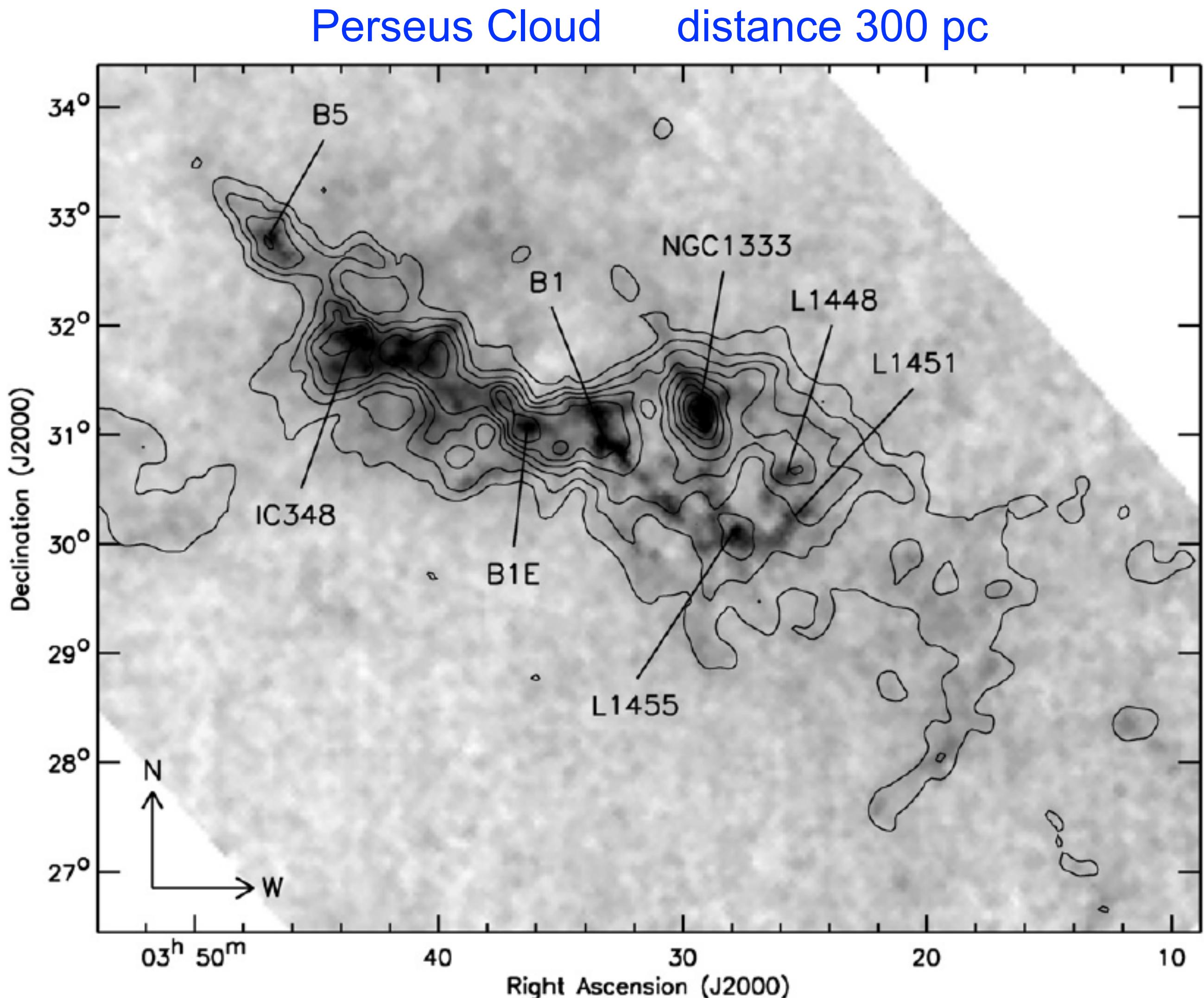
CfA & COMPLETE surveys

Dame+ 2001 Ridge+ 2006

HI-to-H₂ in Perseus:

dark clouds &
low-mass star-forming regions:

B1
B1E
B5
NGC1333
IC348



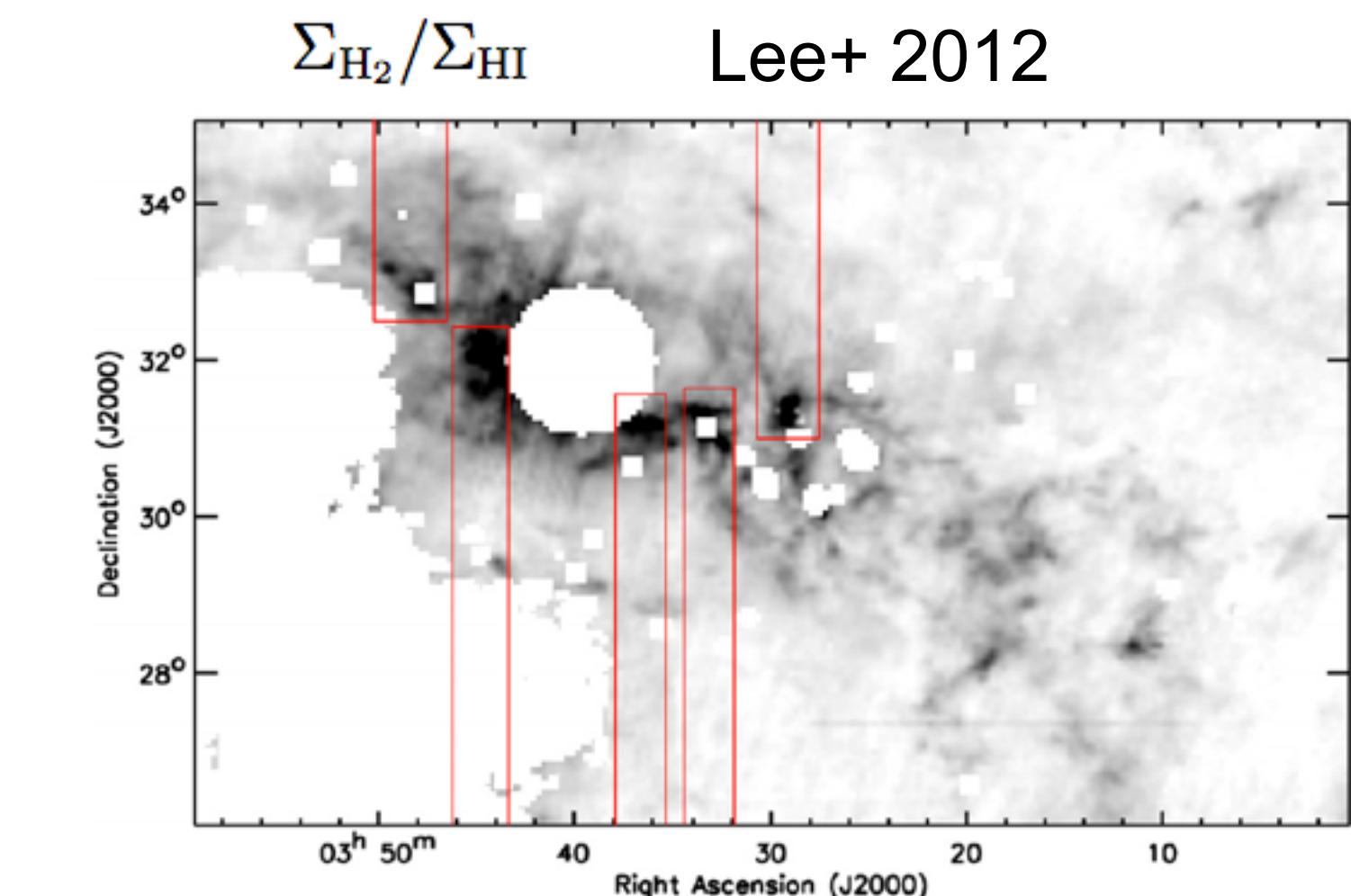
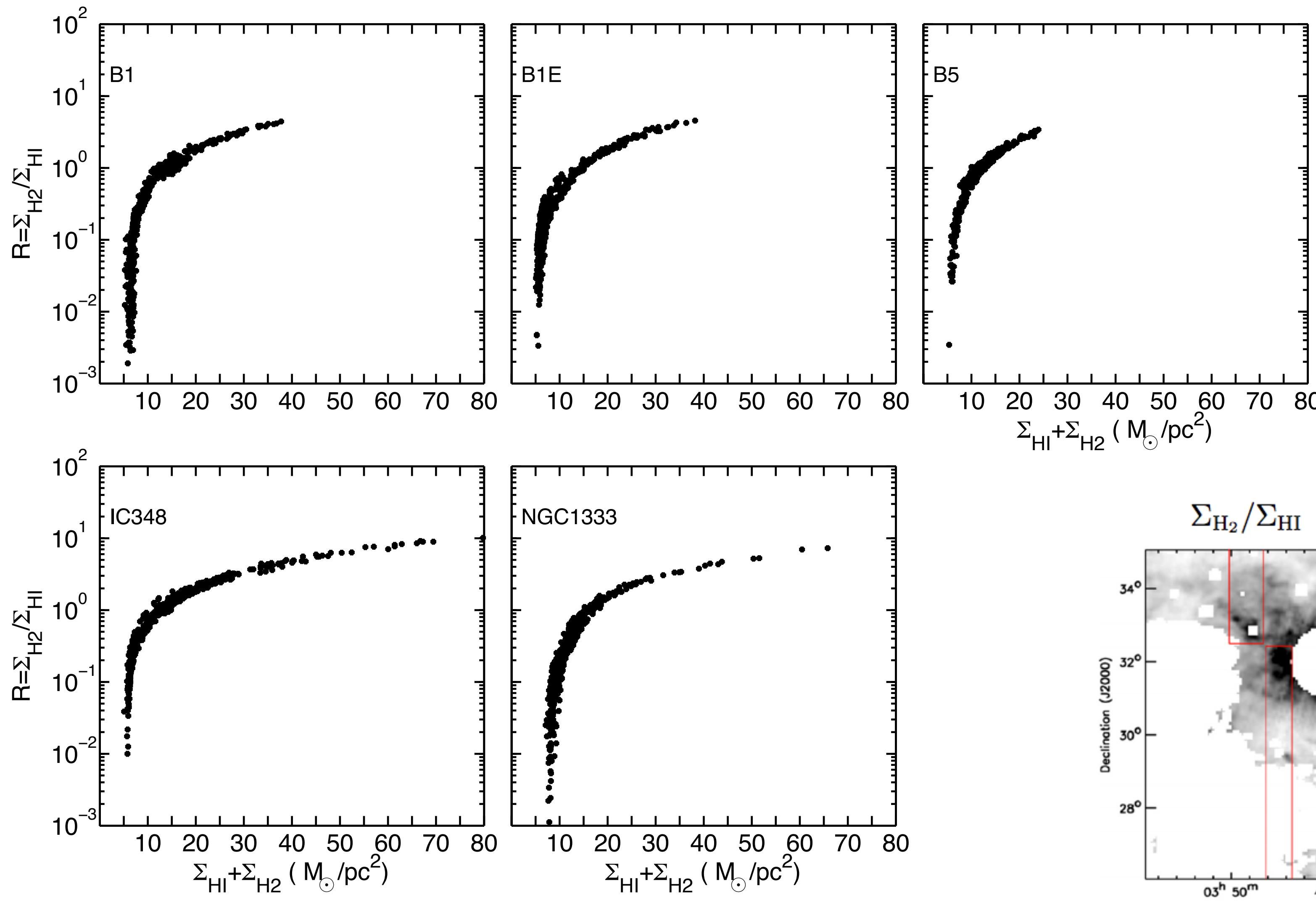
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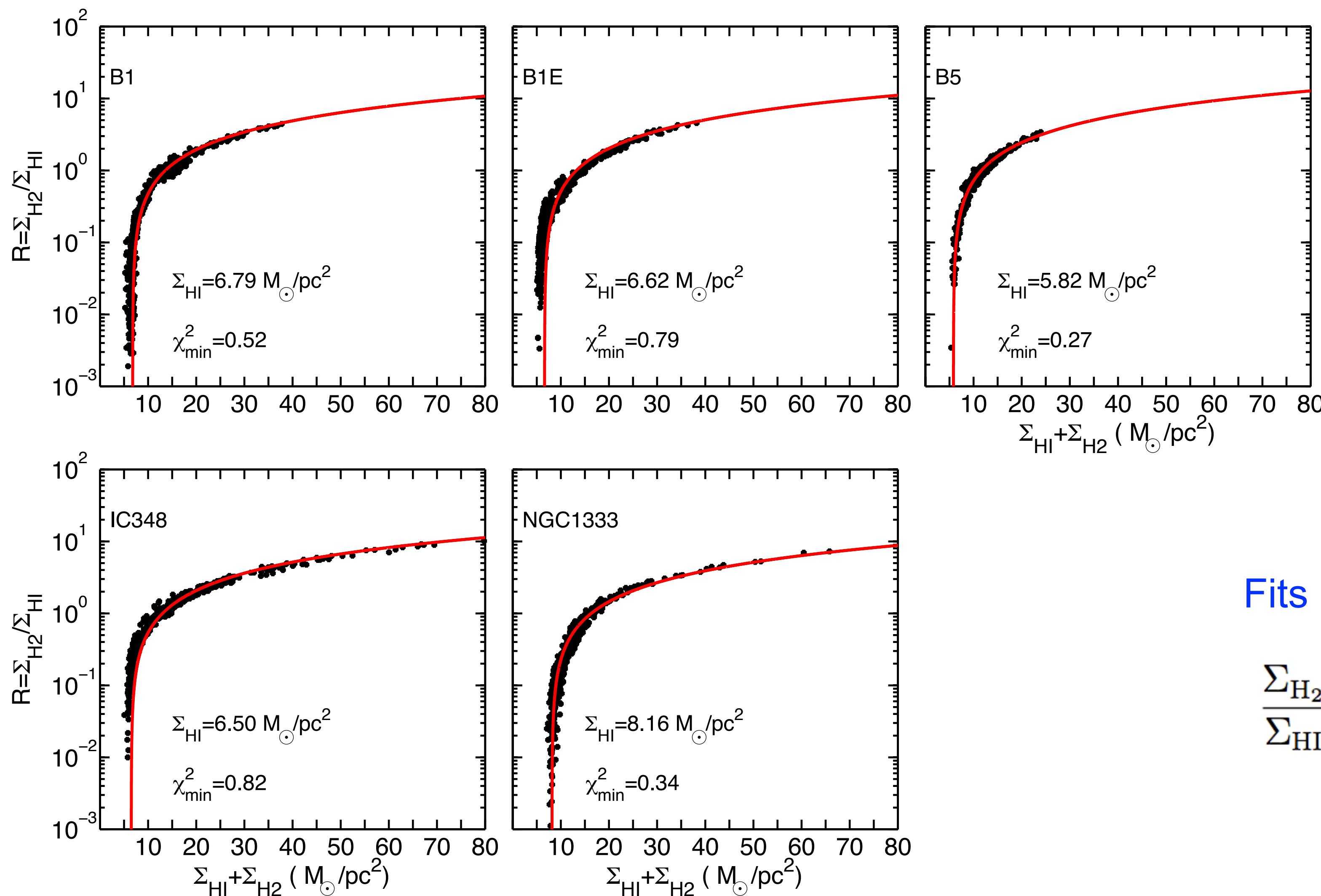
HI-to-H₂ in Perseus:

Lee+ 2012 Peek+ 2011 GALFA HI Survey (Arecibo 4arcmin)

$\frac{\Sigma_{H_2}}{\Sigma_{HI}}$ versus $\Sigma_{\text{gas}} \equiv \Sigma_{HI} + \Sigma_{H_2}$



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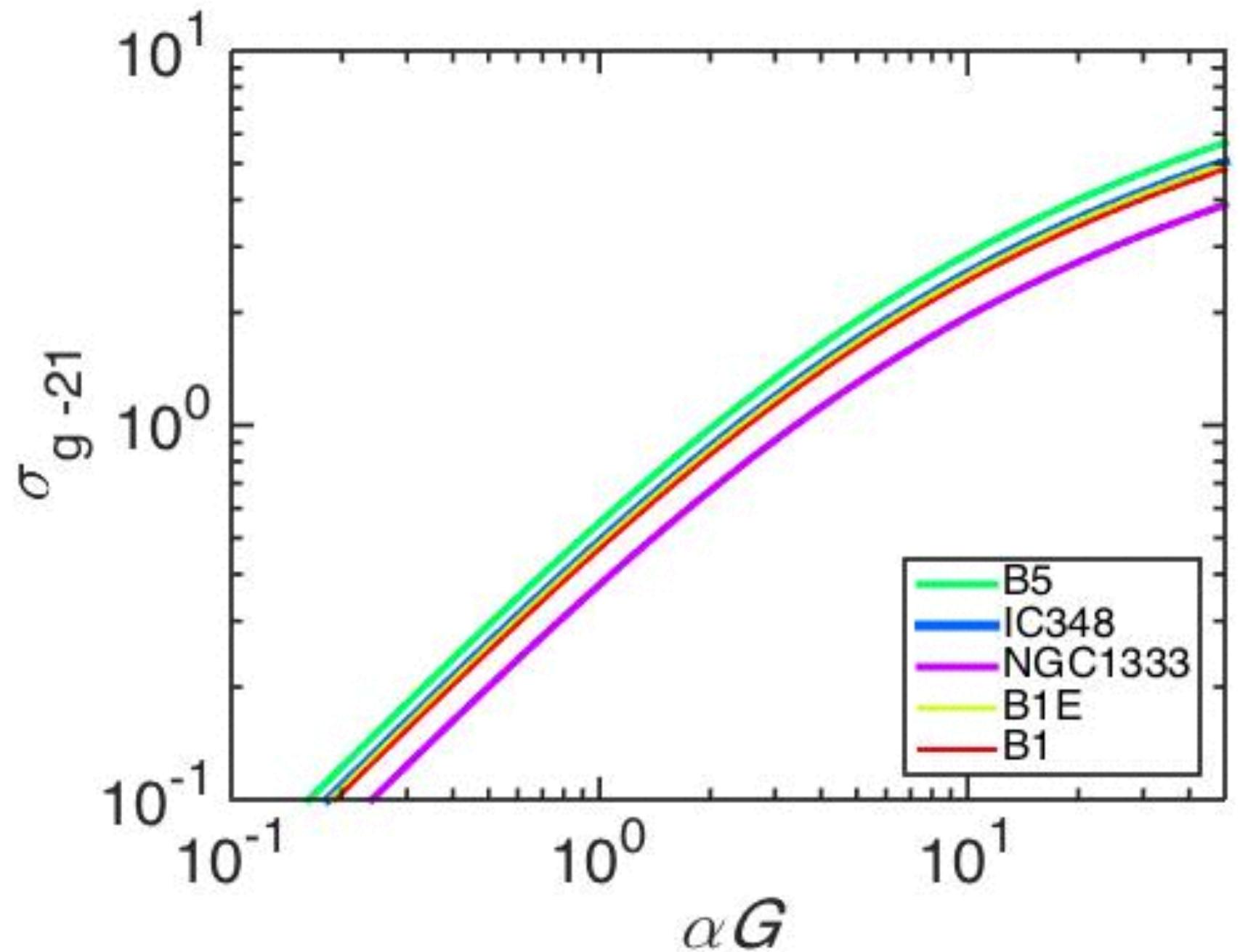
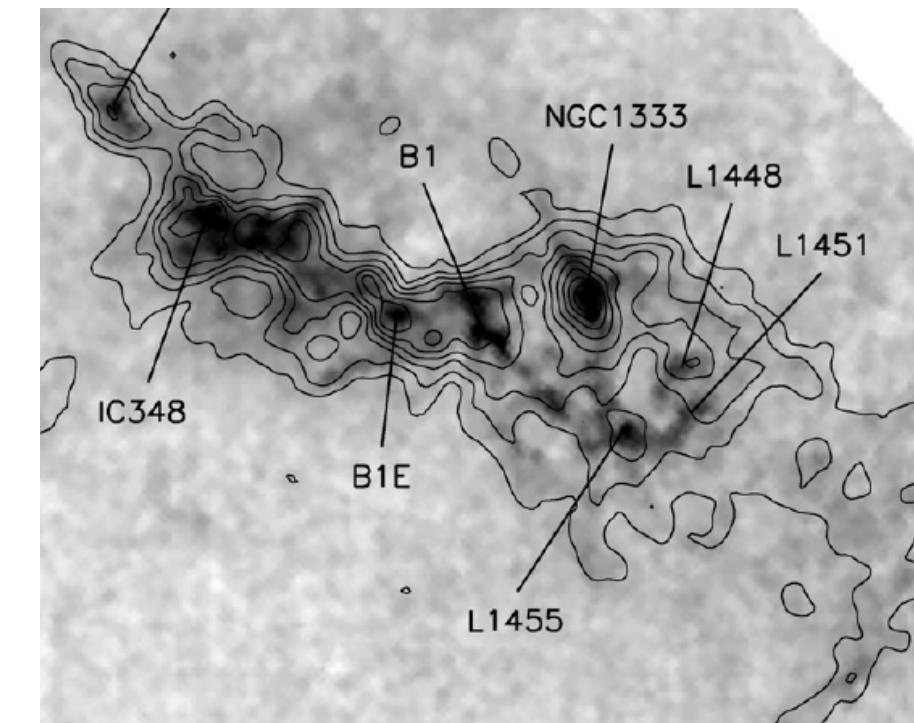


Fits using S+14:

$$\frac{\Sigma_{H_2}}{\Sigma_{HI}} = \frac{\Sigma_{\text{gas}}}{\Sigma_{HI}} - 1$$

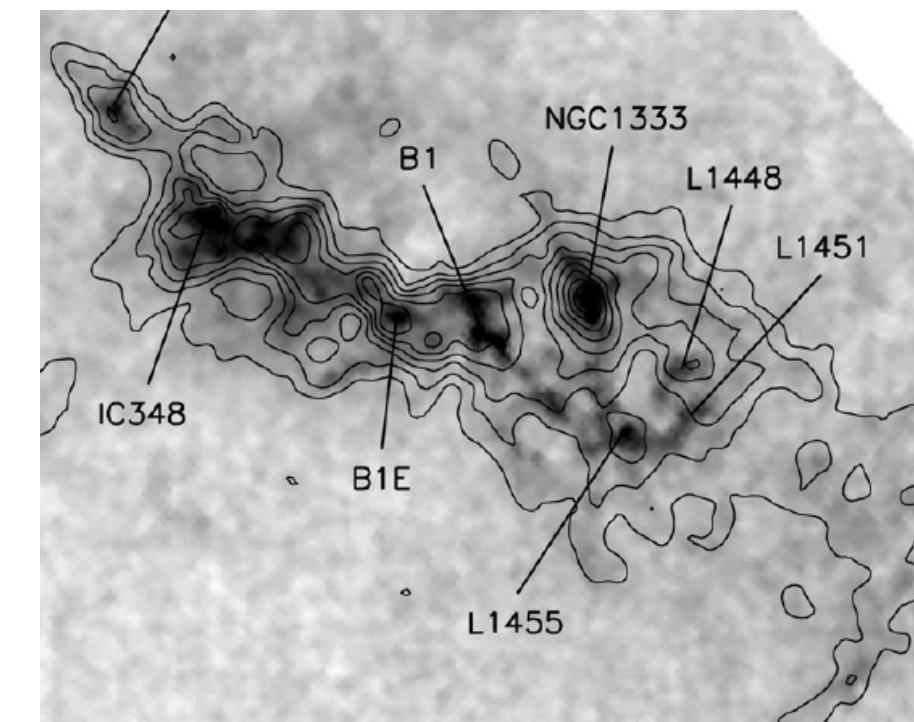
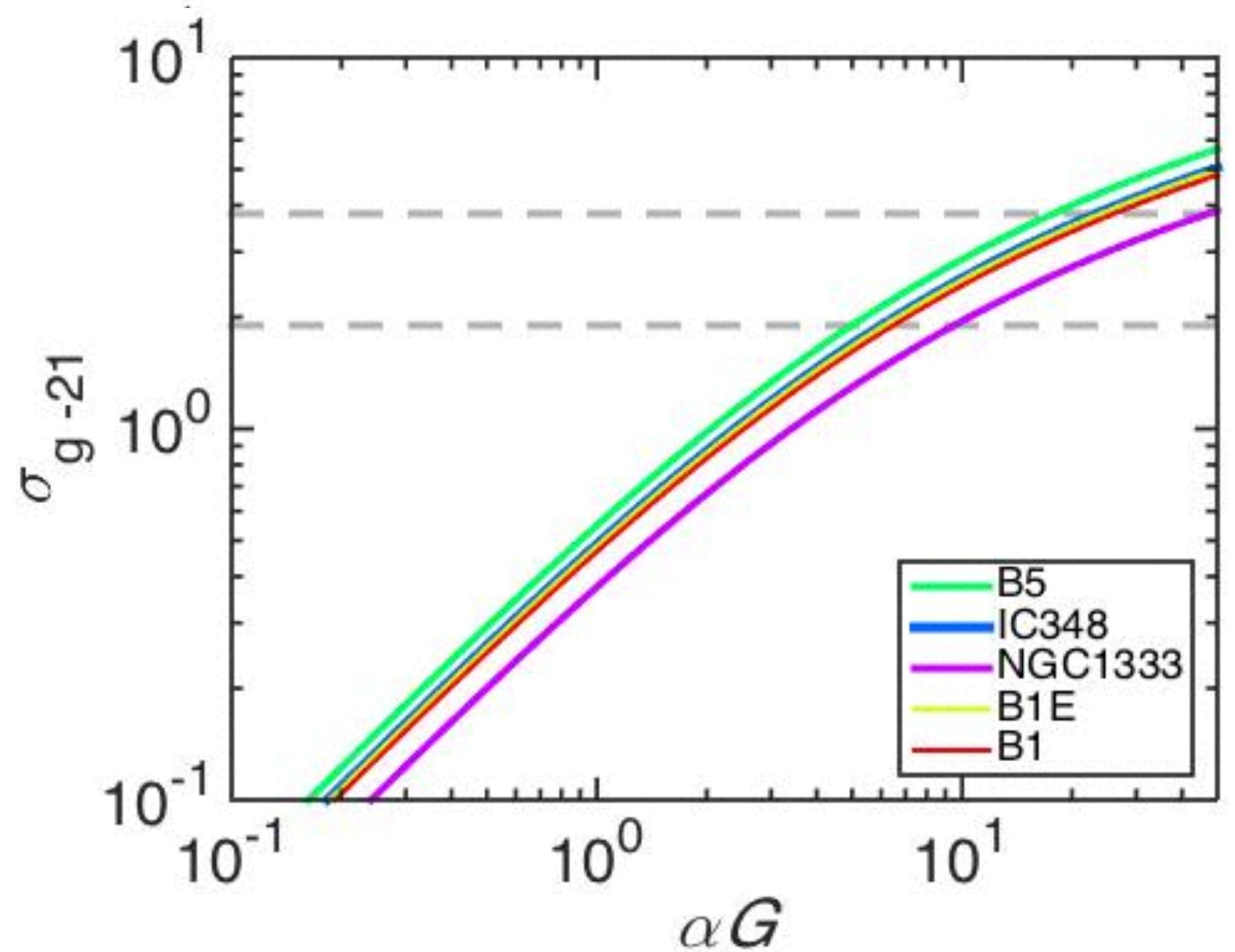
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$$N_{1,\text{tot}} = \frac{1}{\sigma_g} \ln \left[\frac{\alpha G}{4} + 1 \right]$$



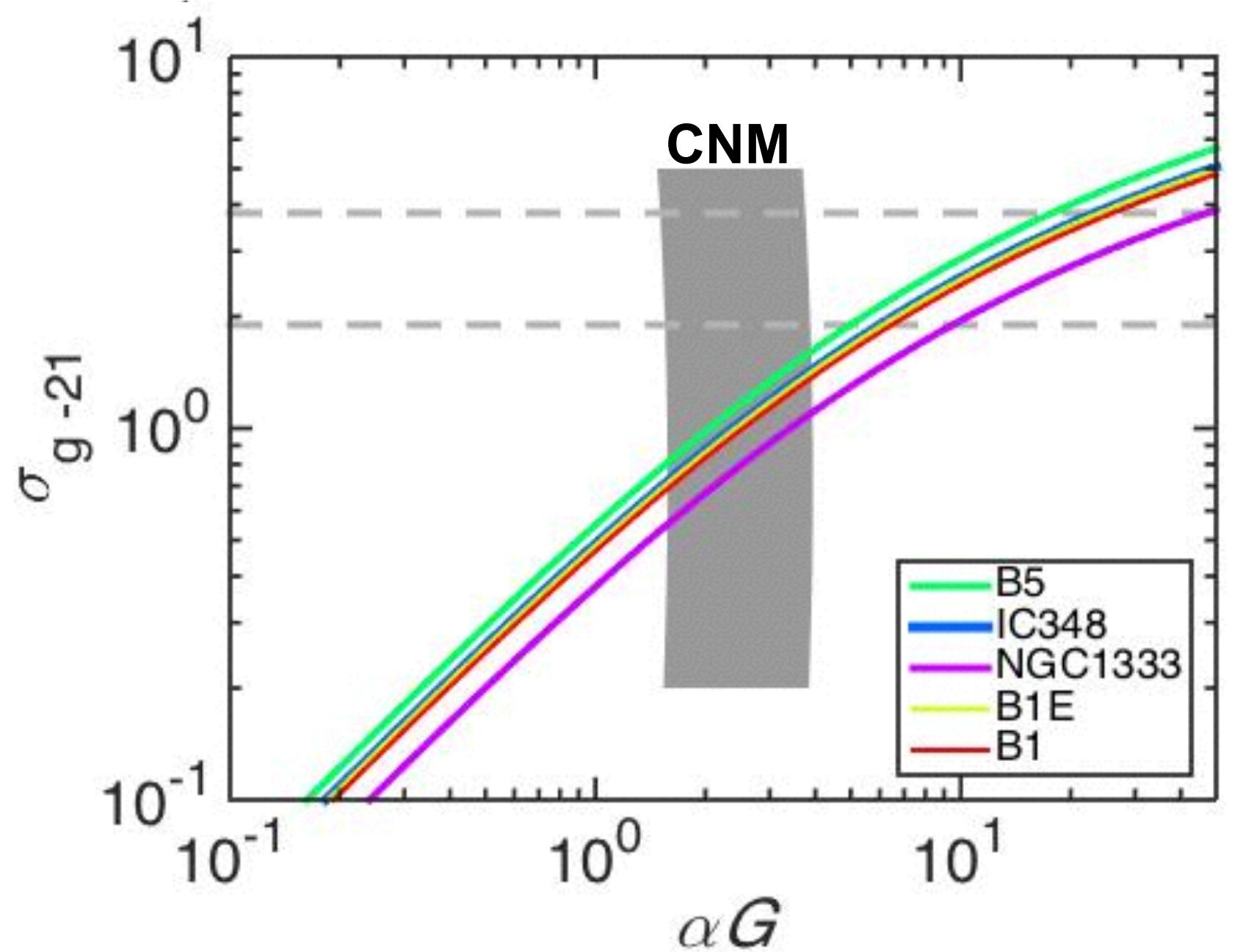
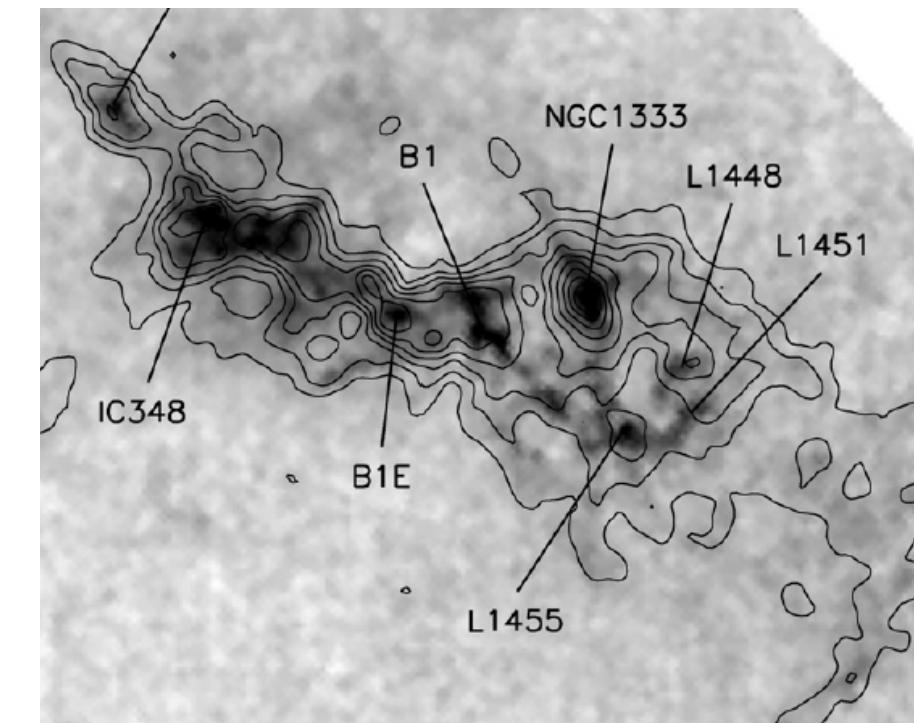
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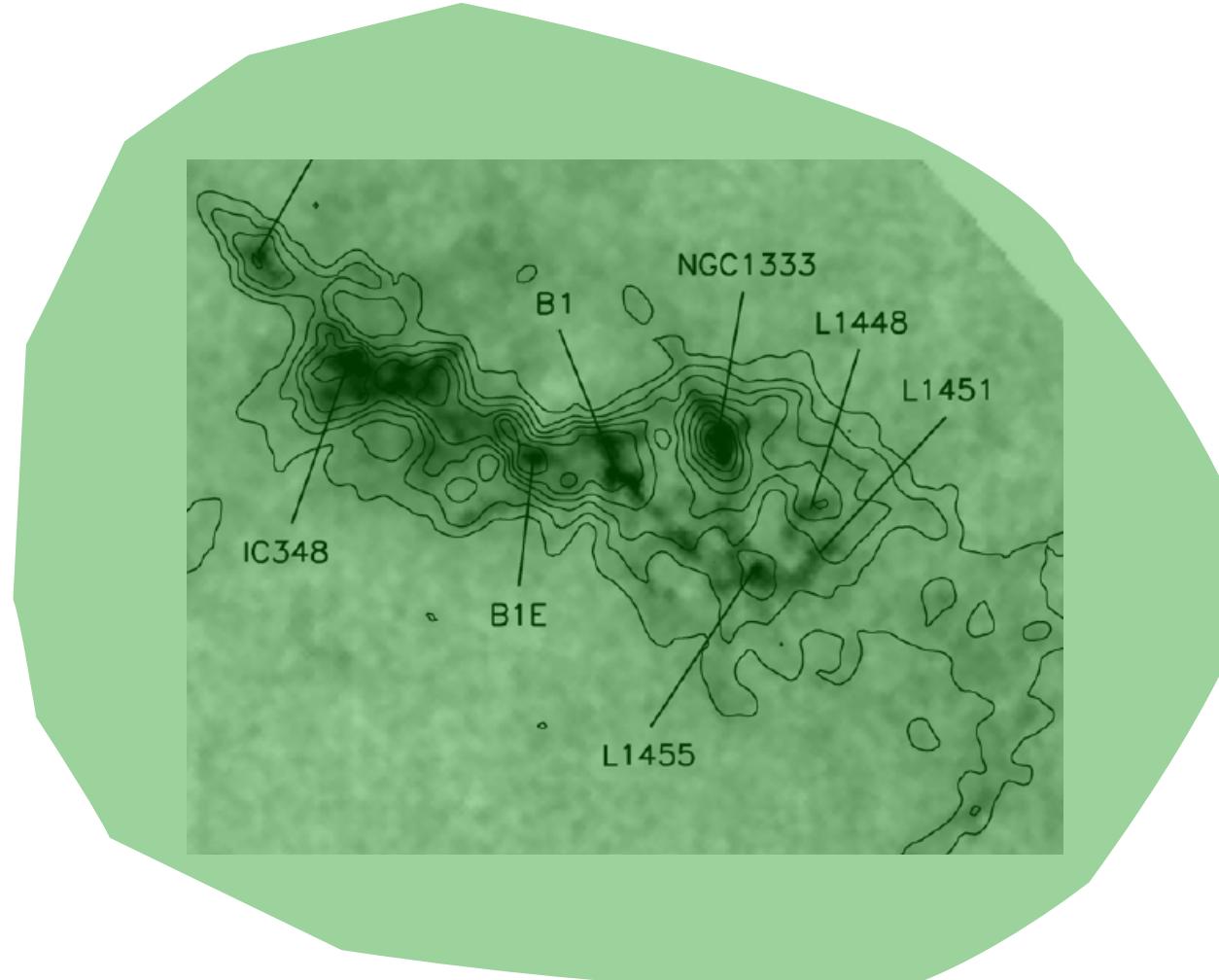
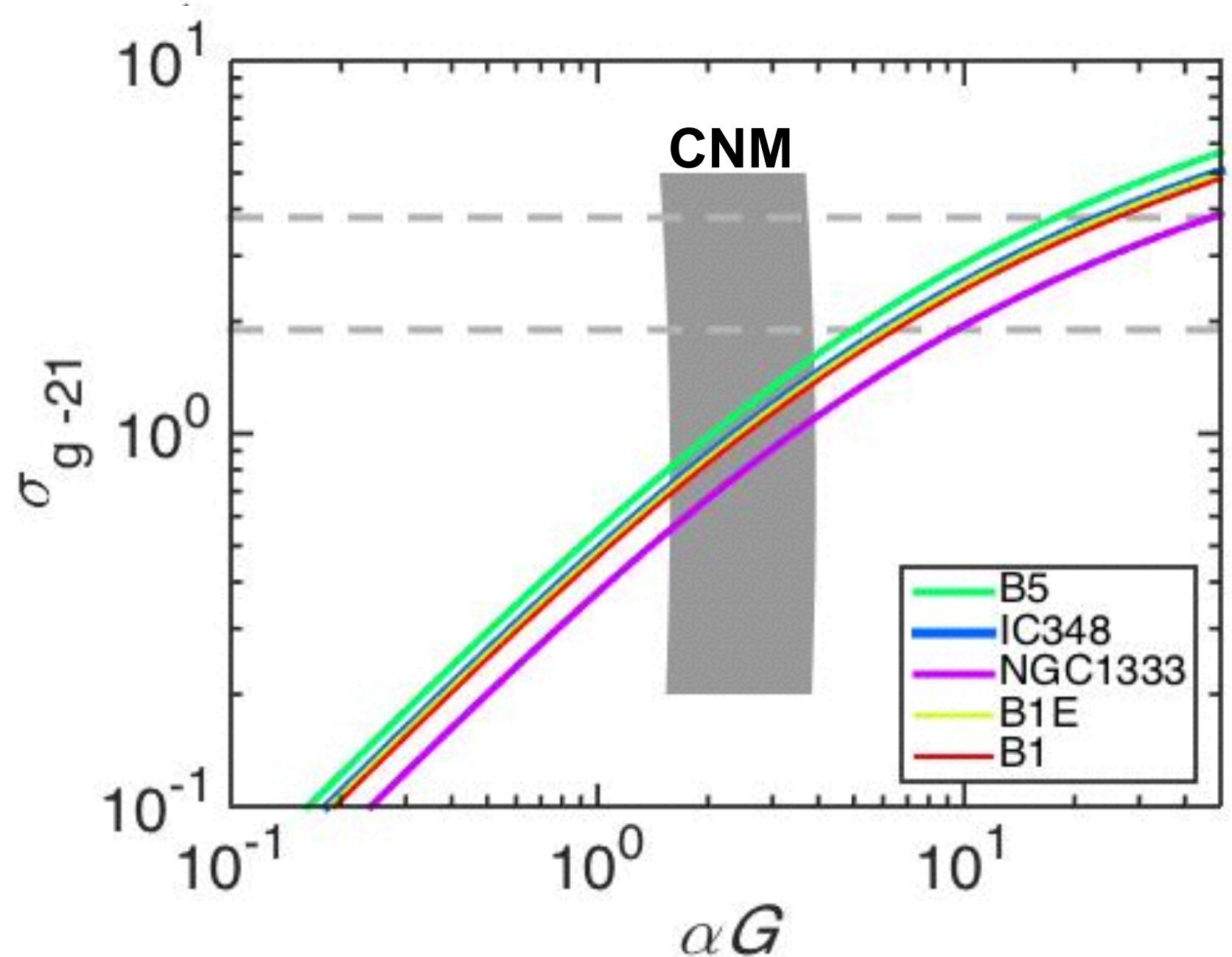
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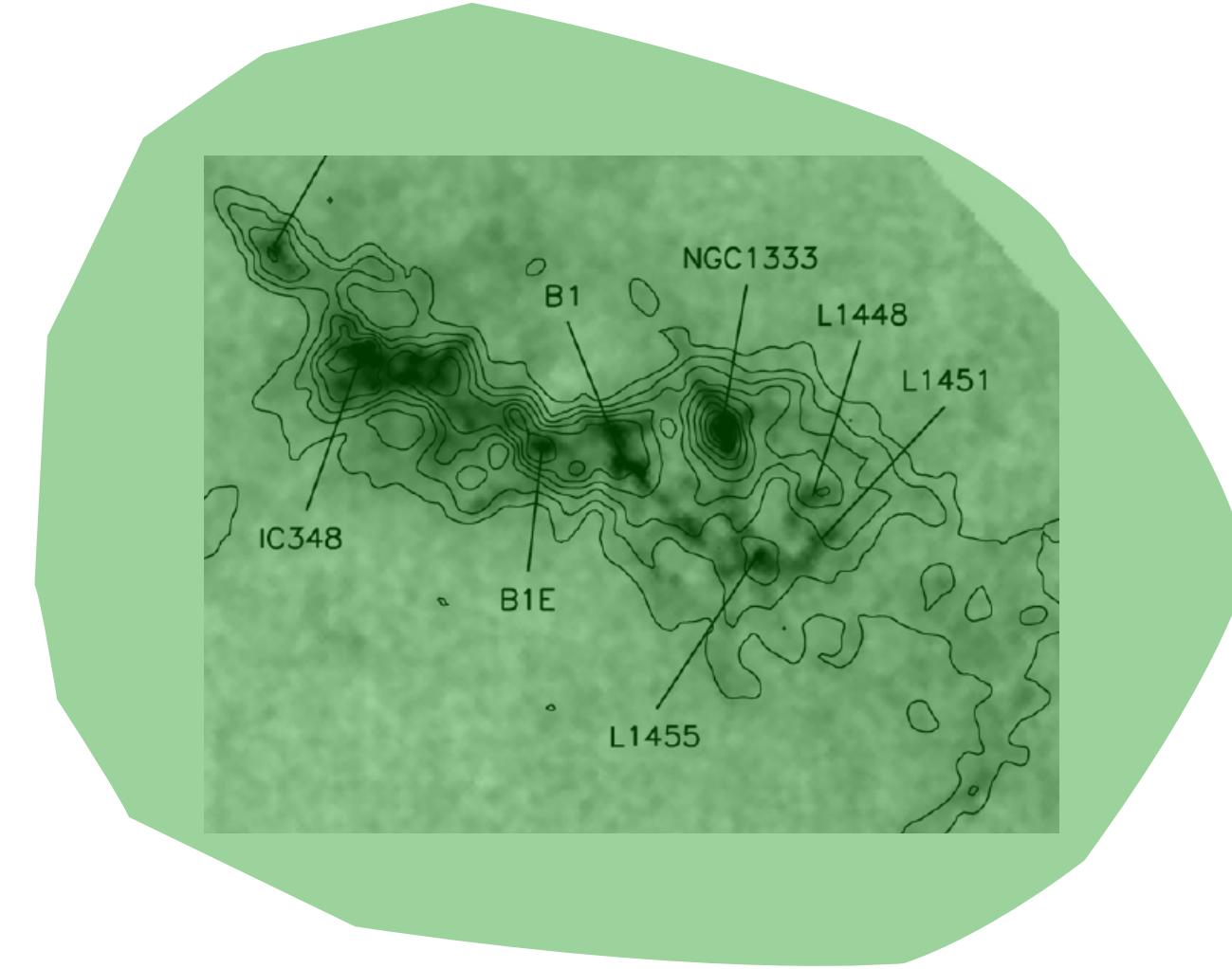
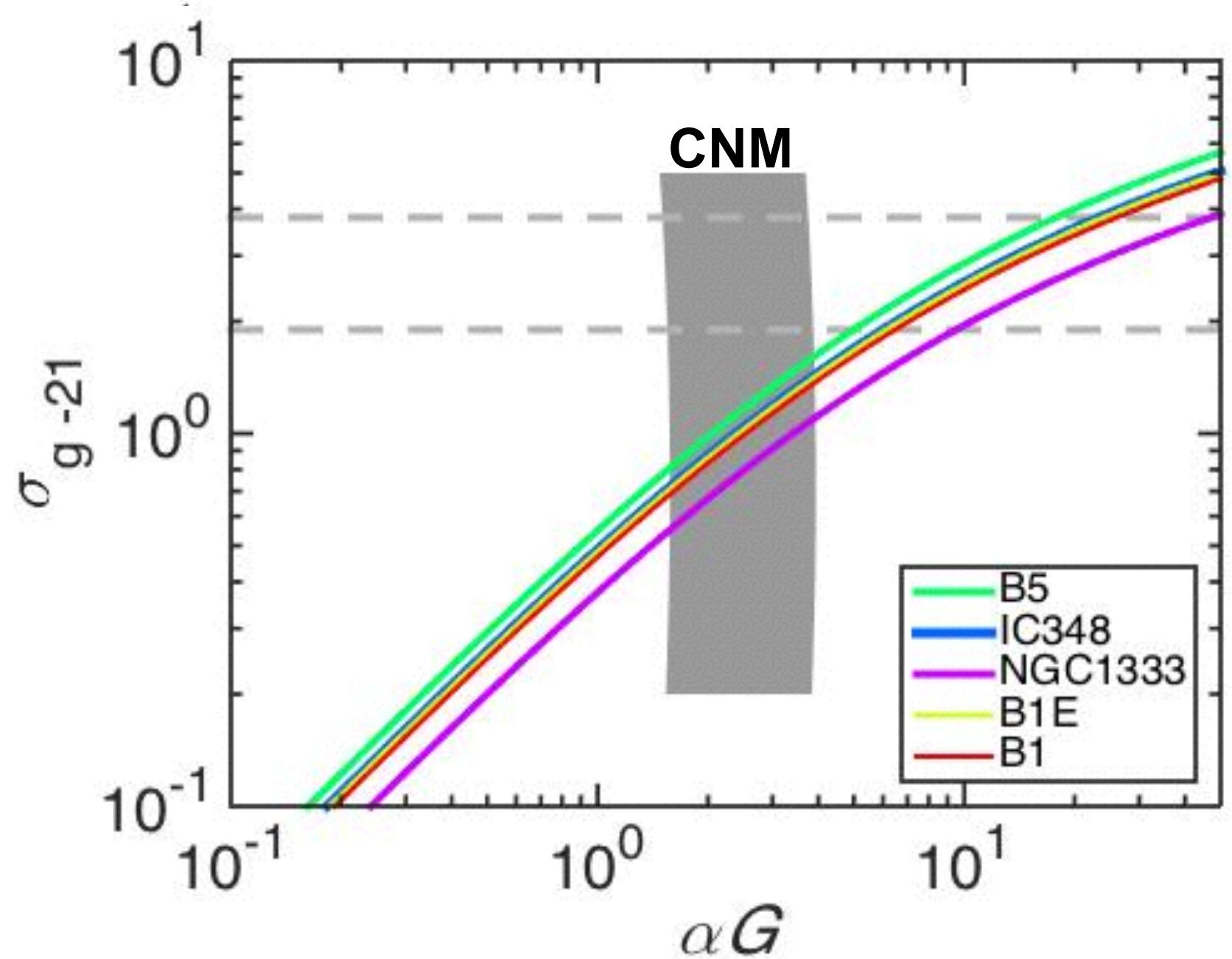
Galactic interstellar LW radiation field:
 $F_0 \approx 2 \times 10^7 \text{ photons cm}^{-2} \text{ s}^{-1}$

Conclusions: $\alpha G \approx 5 \text{ to } 50$

- FUV absorption dominated by HI-dust
- $n_{\text{HI}} \approx 10 \text{ to } 2 \text{ cm}^{-3}$
- probably a UNM/CNM multiphase

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consistent with spin-temperatures
Stanimirovic et al. 2015

Galaxies:

e.g. Bigiel+ 08

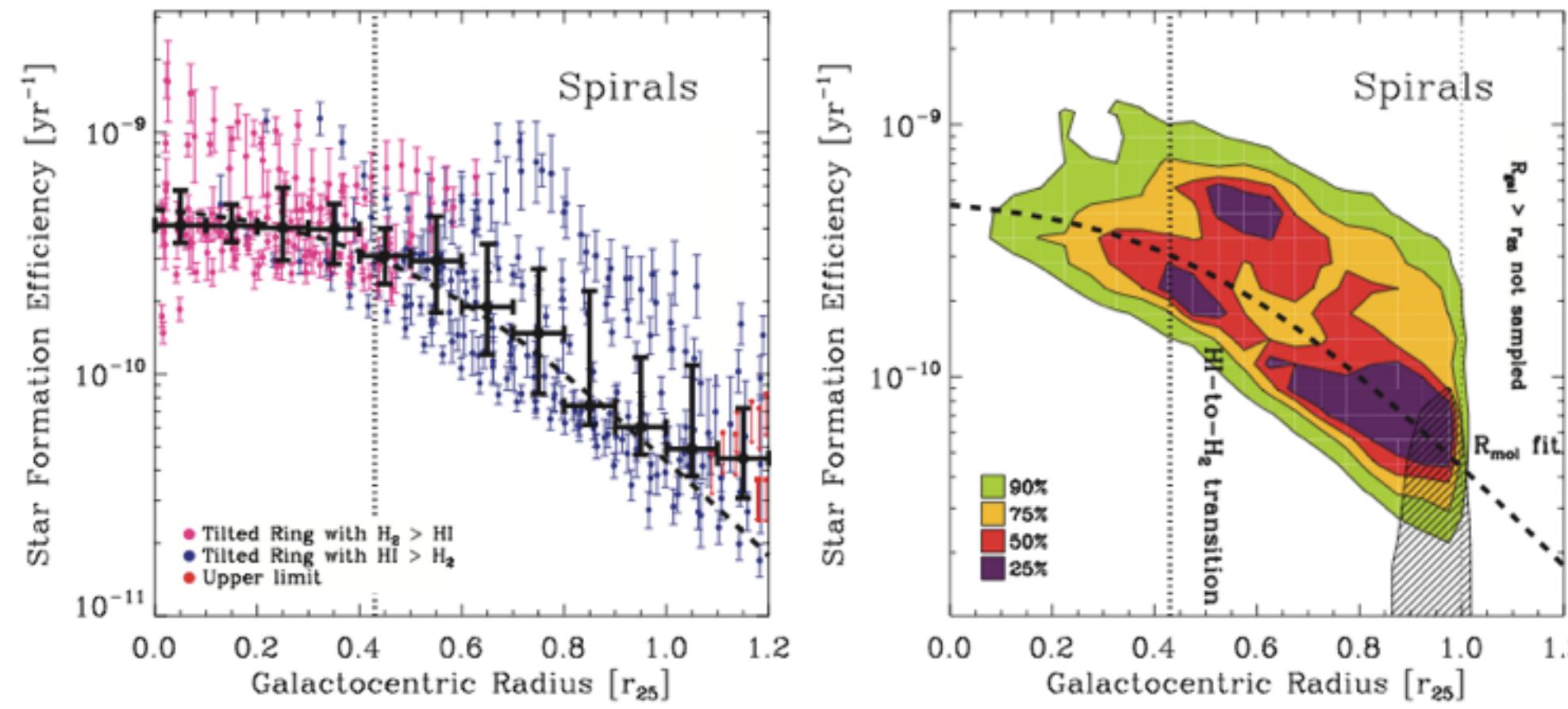
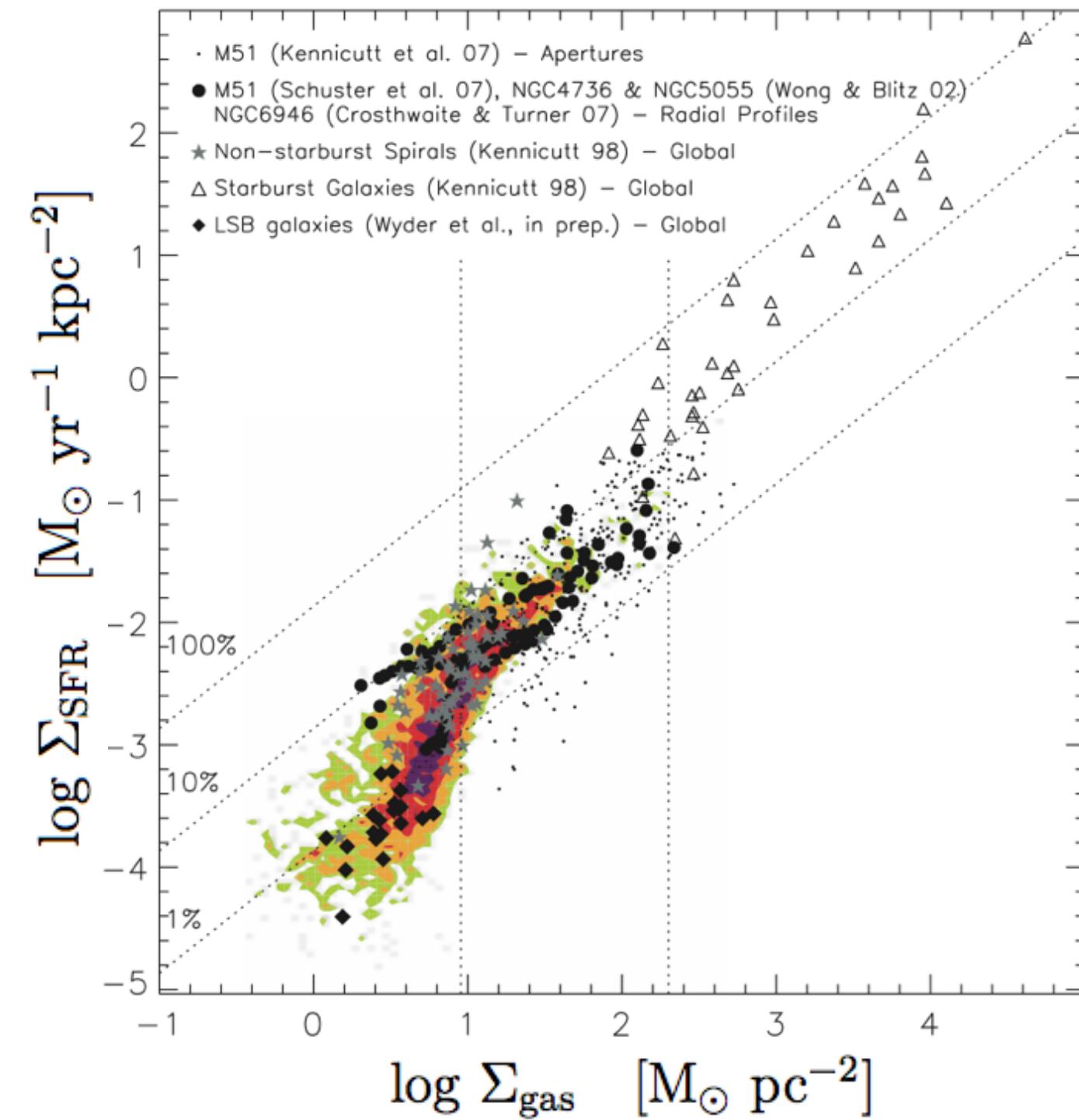


Table 5
Conditions at the H I-to-H₂ Transition

Quantity	Median Value ^a	Scatter	Scatter in log ₁₀
$r_{\text{gal}} (r_{25})$	0.43	0.18	0.17
$\Sigma_* (M_\odot \text{ pc}^{-2})$	81	25	0.15
$\Sigma_{\text{gas}} (M_\odot \text{ pc}^{-2})$	14	6	0.18
$P_h/k_B (\text{cm}^{-3} \text{ K})$	2.3×10^4	1.5×10^4	0.26
$\tau_{\text{ff}} (\text{yr})$	4.2×10^7	1.2×10^7	0.14
$\tau_{\text{orb}} (\text{yr})$	1.8×10^8	0.4×10^8	0.09
Q_{gas}	3.8	2.6	0.31
$Q_{\text{stars+gas}}$	1.6	0.4	0.09



Assuming $\alpha G = (\alpha G)_{\text{CNM}}$

$$\Sigma_{\text{gas},*} \approx \frac{12}{\phi_g Z'} \text{ M}_\odot \text{ pc}^{-2}$$

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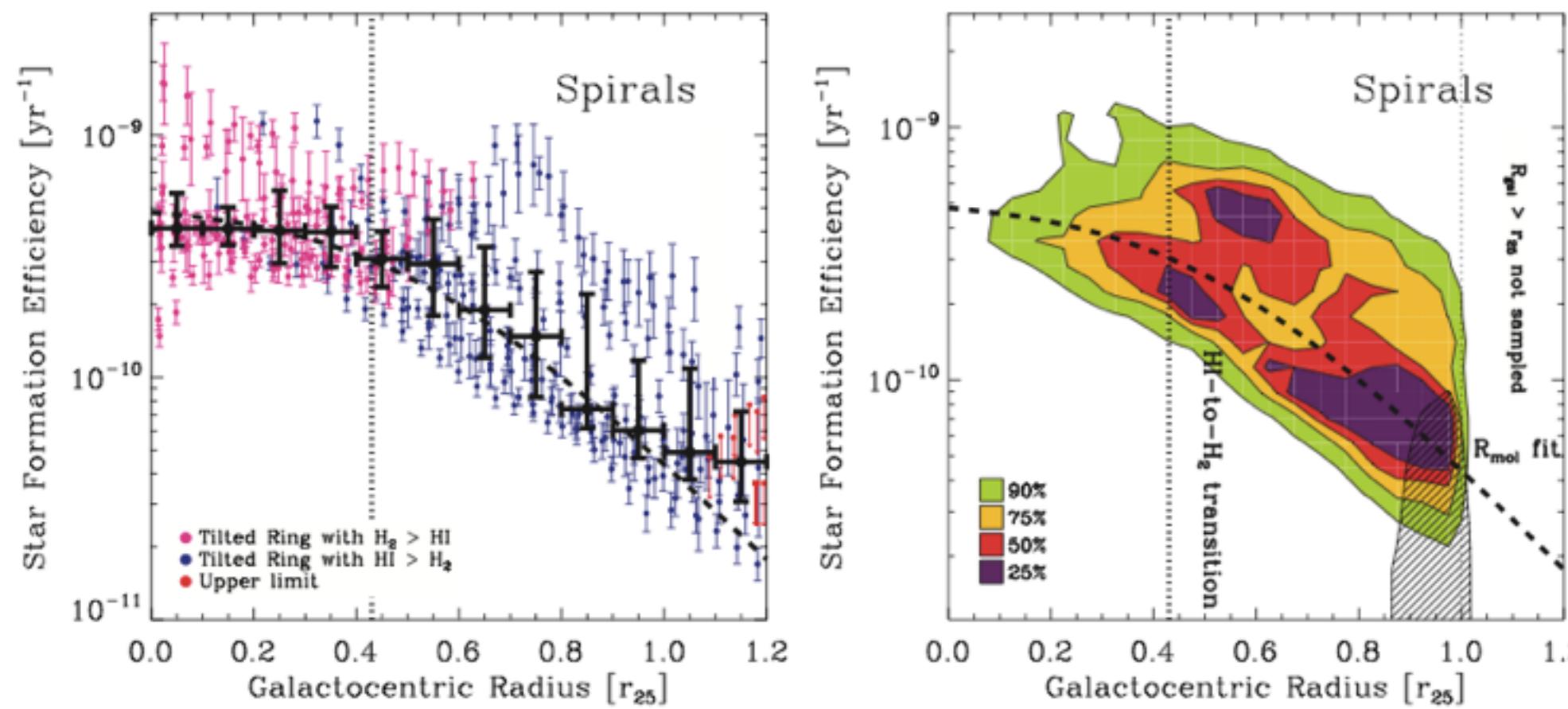
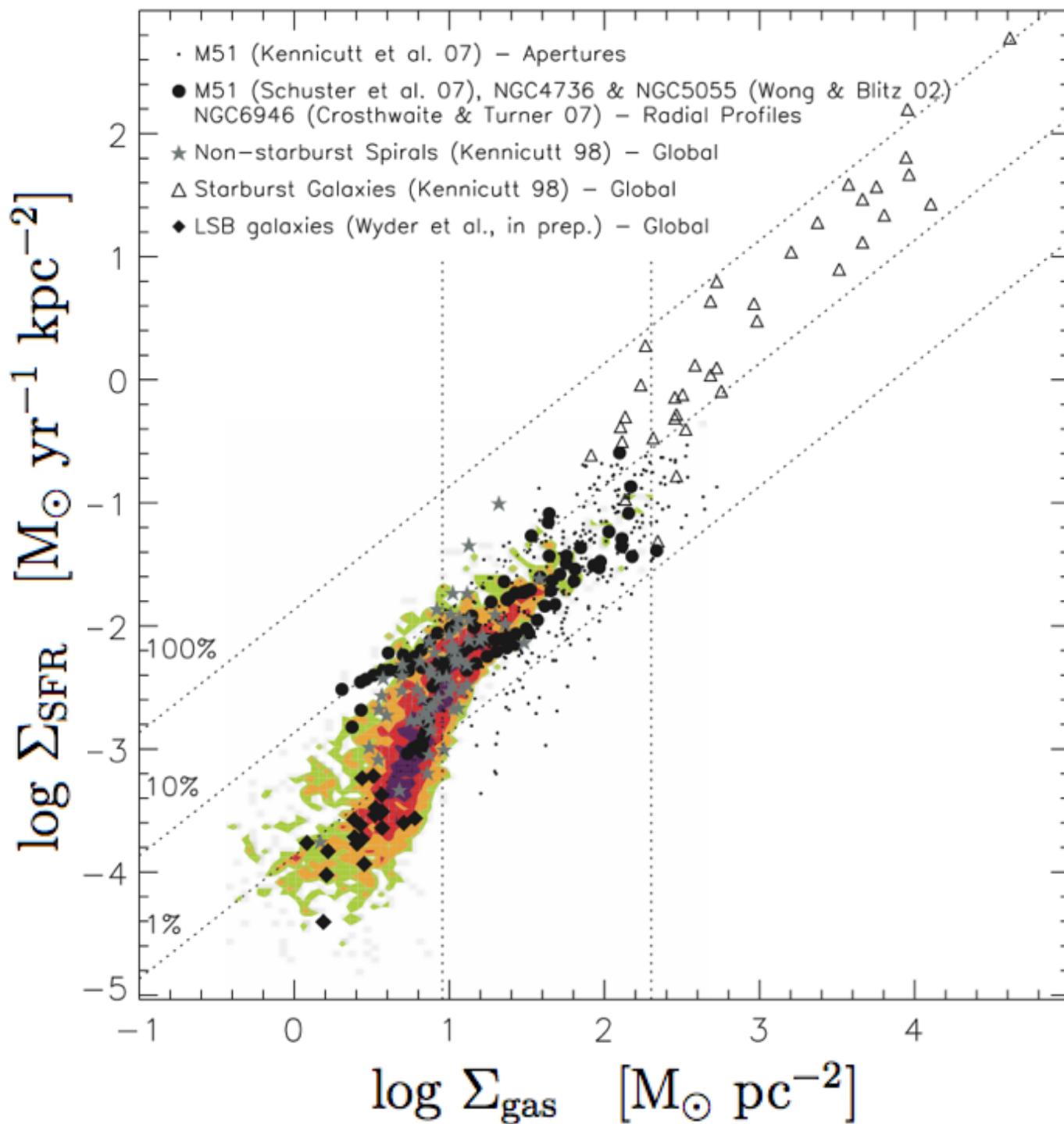


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Caveat: This interpretation requires typically “one” primary cloud per line-of-sight.

To Conclude:

$$N_{1,\text{tot}} = \frac{1}{\sigma_g} \ln \left[\frac{\alpha G}{4} + 1 \right] = \frac{1}{\sigma_g} \ln \left[\frac{1}{4} \frac{\bar{f}_{\text{diss}} \sigma_g w F_0}{Rn} + 1 \right]$$

HI-to-H₂ Transitions and HI Column Densities in Galaxy Star-Forming Regions

Amiel Sternberg¹, Franck Le Petit², Evelyne Roueff,² and Jacques Le Bourlot²

2014 ApJ 790 10 arXiv:1404.5042