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**HIGGS BOSON PLUS 2 JET PRODUCTION  
WBF SIGNAL AND QCD “BACKGROUNDS”**

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1. Introduction & Motivation
2. Production Dynamics and WBF Cuts
3. Results – Event Rates, Signal Purity, and  $HW$  Coupling Uncertainties
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# 1. Introduction and Motivation

- The Higgs boson is expected to be produced at the LHC through various partonic production processes and observed in its decays to SM particles

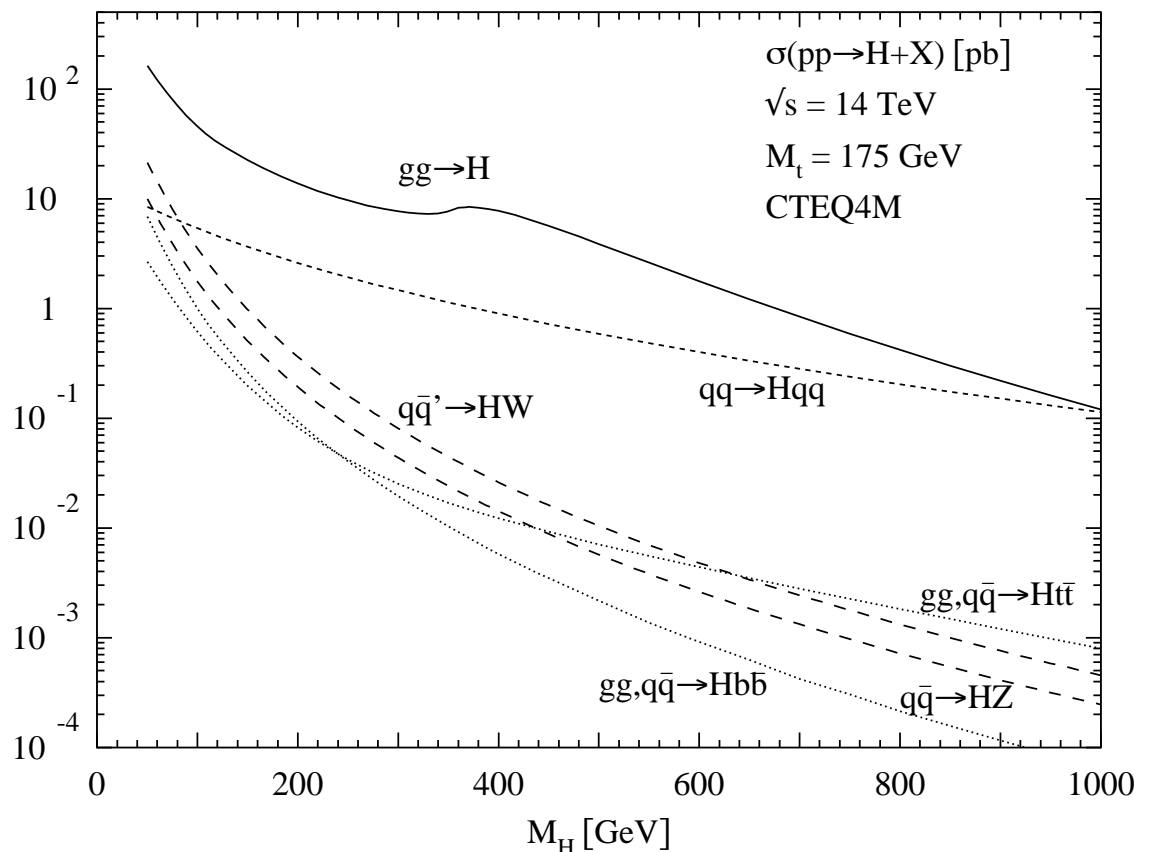
- $gg \rightarrow hX$ , with  $h \rightarrow \gamma\gamma$ ,  $h \rightarrow WW^*$ ,  $ZZ^*$  ;
- $gg \rightarrow t\bar{t}hX$ , with  $h \rightarrow b\bar{b}$  or  $h \rightarrow \gamma\gamma$  ;
- $qq \rightarrow hqqX$  via  $W^+W^- (ZZ) \rightarrow hX$ , with  $h \rightarrow WW^*$ ,  $h \rightarrow \gamma\gamma$ , or  $h \rightarrow \tau^+\tau^-$

- The fully inclusive gluon-gluon fusion subprocess

$gg \rightarrow hX$  is the dominant production mechanism;

$qq \rightarrow H + 2 \text{ jets}$  is next in line

(figure from M. Spira)



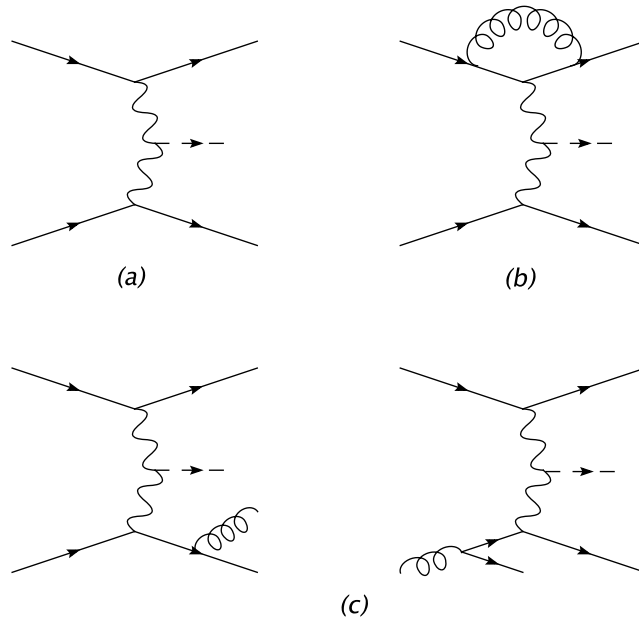
# 1. Introduction and Motivation

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- Assume a SM-like Higgs boson has been discovered,  $115 < m_H < 200$  at the Tevatron or LHC, and that a sample exists of  $H + 2$  jet events at the LHC
- Want to use these data to determine the Higgs boson couplings  $g$  to weak vector bosons,  $W$  and  $Z$
- Focus on two production subprocesses that contribute to  $H + 2$  jet events:
  - $W + W \rightarrow H$  and  $Z + Z \rightarrow H$  “WBF”
  - $g + g \rightarrow H$  “QCD background”
- Question: How well can we resolve WBF production of  $H$  from QCD production of  $H$ ?
- Independent calculation of  $H + 2$  jet processes
  - to gauge the effectiveness of cuts used to select the WBF signal, and
  - to evaluate the accuracy with which coupling  $g$  can be determined in experiments at the CERN LHC
- Define Purity  $P = \frac{S}{S+B}$   
Show results on  $P$  vs  $p_T$  of the jets
- Evaluate uncertainty  $\frac{\delta g}{g}$  of the coupling in terms of  $P$ ,  $\frac{\delta N}{N}$ ,  $\frac{\delta S}{S}$  and  $\frac{\delta B}{B}$

# $H + 2$ Jet Production – Signal

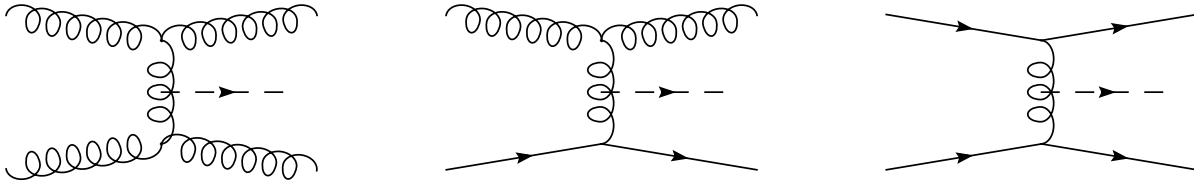
- Higgs boson  $H$  production via  $WW$  scattering in NLO QCD. Ex:



- QCD NLO calculation of  $H + 2$  jet with CTEQ6M parton densities; renormalization/factorization scale  $\mu = m_H$
- $\mu$  dependence  $\sim 2\%$  for  $\frac{1}{2}m_H < \mu < 2m_H$ , and CTEQ PDF uncertainty  $\sim 3\%$ , both in the WBF region of phase space
- Events generated with the MCFM code  
J. Campbell & R. K. Ellis PRD65,113007 (2002)
- Independent results (dipole subtraction method) verify the NLO calculation of  
Figy, Oleari, and Zeppenfeld, PRD68, 073005 (2003).  
 $K$ -factor  $\sim 10\%$ , with small variation over the phase space appropriate for the WBF signal

# $H + 2$ Jet Production – Background

- Higgs boson  $H$  production via  $gg$  scattering. Ex:



- Fully differential NLO calculation of  $H + 2$  jet production  $gg \rightarrow H + j + j + X$  does not exist; contribution computed at LO Kauffman Desai and Risal, PRD55, 4005 (1997); PRD58, 119901 (1998)
- Effective  $ggH$  coupling included in the limit of  $m_H \ll 2m_t$  (c.f. Del Duca et al NP B616, 367 (2001))
- NLO enhancement ( $K$ ) factor is needed in the region of the WBF cuts. It can be estimated from
  - inclusive NLO  $gg \rightarrow H$   $K \sim 1.7 - 1.8$   
Harlander & Kilgore PRD64, 013015 (2001); Anastasiou & Melnikov, NP B646, 220 (2002)
  - NLO  $gg \rightarrow H + 1$  jet  $K \sim 1.3 - 1.5$   
Ravindran, Smith, van Neerven NP B665, 325 (2003)
  - or from NLO  $pp \rightarrow Z + 2$  jets +  $X$ , but parton subprocesses are different  $K \sim 1 \pm 10\%$   
J. Campbell, R. K. Ellis, & D. Rainwater PRD68, 094021 (2003)
- Fully differential NLO calculation is needed of the QCD process  $gg \rightarrow H + 2$  jets so that the NLO enhancement can be obtained in the WBF region of phase space

## Event Characteristics

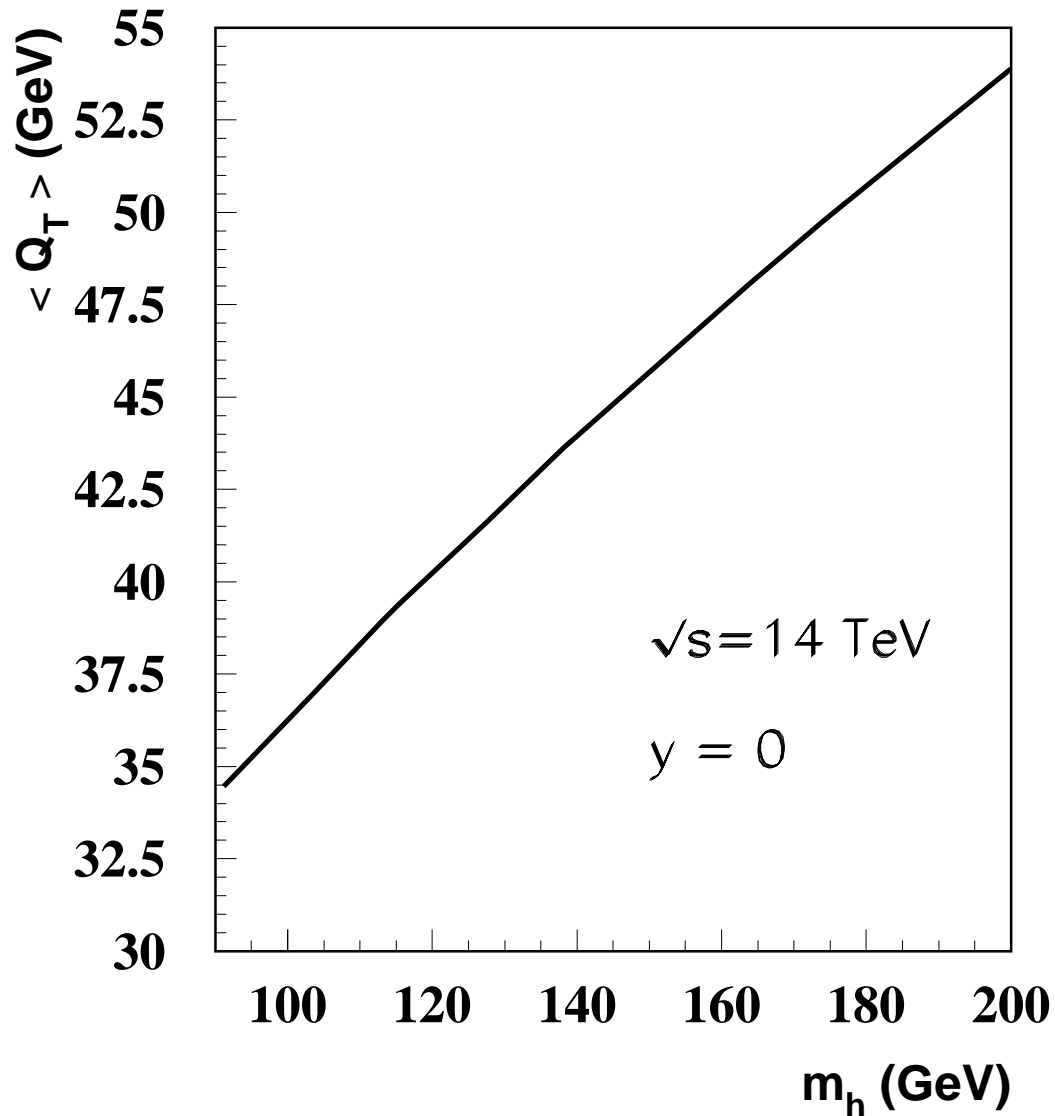
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- Hallmark of WBF events is a Higgs boson accompanied by two “tagging” jets having large  $p_T \sim \mathcal{O}(\frac{1}{2}M_W)$
- QCD  $gg \rightarrow H + 2 \text{ jets}$  will generate a softer  $p_T$  spectrum
- The rapidity spectra also differ **figures later**
- The  $p_T$  spectrum of the Higgs boson is also relatively hard. All-orders resummed calculation Berger and Qiu PRD 67, 034026 (2003) provides  $\langle p_T^H \rangle \sim 35 \text{ GeV}$  at  $m_H = M_Z$ , growing to  $\langle p_T^H \rangle \sim 54 \text{ GeV}$  at  $m_H = 200 \text{ GeV}$
- Require reliable QCD representation of  $Hjj$  for jets at large  $p_T$ . Hard matrix elements are needed. A showering approach for generating the momentum distributions of the jets would not suffice

## Mean Transverse Momentum of $H$ Production

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- All orders resummation for  $H$  production via  $gg$  scattering



$$\langle p_T^H \rangle \simeq 0.18m_H + 18\text{GeV}$$

## Generic Cuts

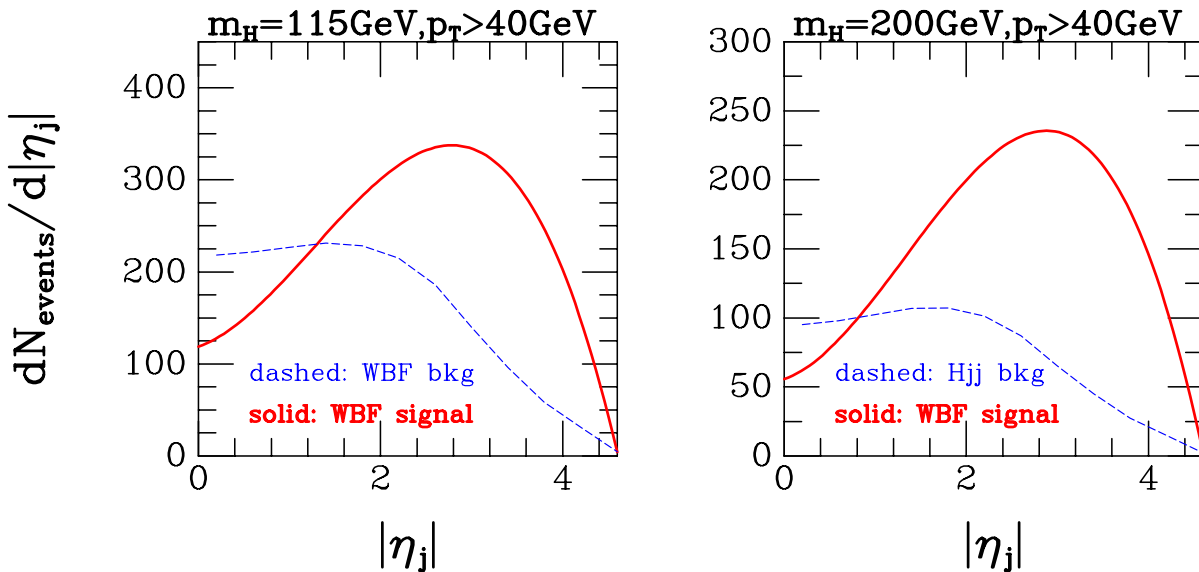
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- Generic cuts Figy et al. Jets from the Monte Carlo runs are clustered according to the  $k_T$  algorithm with
  - $p_T^{\text{jet}} > 20 \text{ GeV}$ , **to be raised**
  - jet pseudo-rapidity  $|\eta^{\text{jet}}| < 4.5$ , and
  - jet separation  $\Delta R_{jj} = \sqrt{\Delta\eta_{jj}^2 + \Delta\phi_{jj}^2} > 0.8$
- The two jets with the highest  $p_T$  are chosen as the tagging jets and ordered in rapidity,  $\eta_{j_1} < \eta_{j_2}$
- To approximate the acceptance for the Higgs boson decay products imagine a Higgs boson decay to two charged particles, denoted “leptons”
  - Require  $p_T^{\text{lept}} > 20 \text{ GeV}$ ,  $|\eta^{\text{lept}}| < 2.5$ ,  
 $\Delta R_{j\ell} > 0.6$ ,  $\eta_{j_1} < \eta_{\text{lept}} < \eta_{j_2}$
- Higgs decay products lie between the tagging jets



## $H + 2$ Jet Production – Jet Rapidity Distribution

- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO) (for  $1 \text{ fb}^{-1}$ , no BR included):



- Shape of the signal distribution depends very little on the Higgs boson mass or on the  $p_T$  cut for the tagging jets. Peak at  $|\eta| \sim 3$ . Full width at half-max  $\sim 2.8$
- Background falls off sharply beyond  $|\eta| \sim 2$
- Motivates a simple WBF prescription:

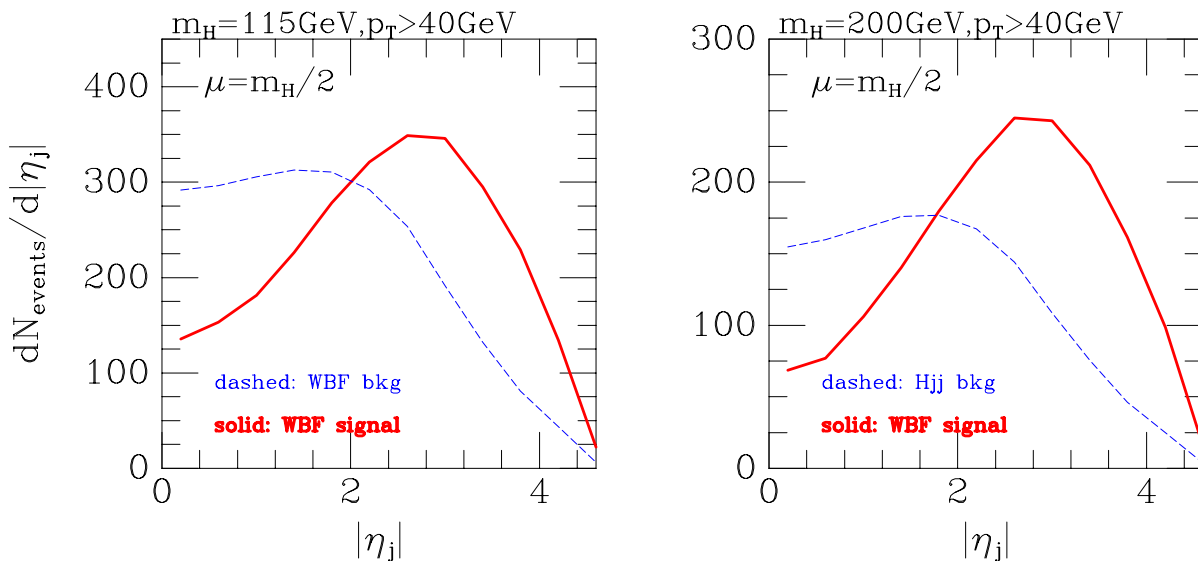
$$\eta_{\text{peak}} - \eta_{\text{width}}/2 < |\eta_j| < \eta_{\text{peak}} + \eta_{\text{width}}/2$$

$$j = j_1 \text{ or } j = j_2, \quad \eta_{\text{peak}}=3, \quad \text{and} \quad \eta_{\text{width}}=2.8$$

- Our working definition of the WBF region

## $H + 2$ Jet Production – $\mu$ dependence

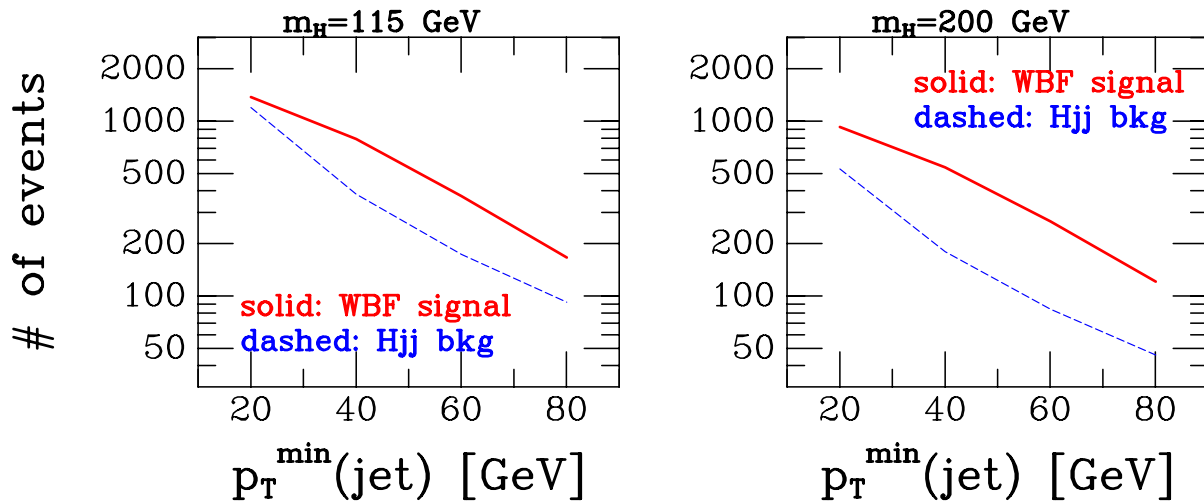
- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO) (for  $1 \text{ fb}^{-1}$ , no BR included)  $\mu = m_H/2$ :



- Magnitude and shape of the signal distribution depend very little on  $\mu$
- Magnitude of the background is much greater at  $\mu = m_H/2$ . Not much effect on the shape
- Not much question that a differential NLO calculation is needed for the background process  $H + 2$  jets

# H + 2 Jet Production – Event Rates for 1 fb<sup>-1</sup>

- Event rates for the  $Hjj$  WBF signal(NLO) and  $Hjj$  background(LO), including our WBF requirement that at least one jet have  $1.6 < |\eta| < 4.4$  (no BR included)



$p_T$ cut [GeV]	20	40	80
Signal ( $m_H = 115$ )	1374	789	166
Bkg	1196	382	92
Purity	0.53	0.67	0.64
Signal ( $m_H = 200$ )	928	545	121
Bkg	534	179	46
Purity	0.63	0.75	0.72

- Recall 
$$P = S/(S + B)$$
- $p_T$  cut of 40 GeV yields a good S/B across the range  $m_H = 115$ – $200$  GeV.  $p_T$  cut of 20 GeV is marginal

## $H + 2$ Jets – Derivation of Coupling Uncertainty

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- Both the signal and the background have  $H + 2$  jets
- Want the uncertainty  $\delta g/g$  on the coupling of the Higgs boson to vector bosons
- Define  $r = g_{\text{observed}}^2 / g_{\text{predicted}}^2$
- Assume deviation in the expected total number of events arises from the effective coupling  $\rightarrow r = \frac{(N-B)}{S}$
- Uncertainty in  $r$ :

$$\delta r / r = \sqrt{(\delta S / S)^2 + ((\delta N)^2 + (\delta B)^2) / (N - B)^2}$$

- In terms of purity  $P = S / (S + B)$

$$\frac{\delta g}{g} = \frac{1}{2} \sqrt{\left(\frac{\delta S}{S}\right)^2 + \frac{1}{P^2} \left(\frac{\delta N}{N}\right)^2 + \frac{(1-P)^2}{P^2} \left(\frac{\delta B}{B}\right)^2}$$

- Factor  $1/P$  that multiplies  $\delta N/N \rightarrow$   
 $P < 1$  dilutes statistical power of data
- Factor  $(1 - P)/P$  that multiplies  $\delta B/B \rightarrow$   
 $P \rightarrow 1$  reduces role of uncertainty in  $B$
- Size of background is included in  $P$

## Estimates of Uncertainties in $S$ , $B$ , and $N$

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- Let  $\delta S/S = 10\%$

NLO effects are known;  $\mu$  dep and PDF uncert are estimated

- Let  $\delta B/B = 30\%$

NLO effects not calculated yet for  $H + 2$  jets;  $\mu$  dep of the NLO inclusive process is  $\sim 20\%$  for  $\frac{1}{2}m_H < \mu < 2m_H$ ; PDF another  $\sim 5\%$

- For  $N$  and  $\delta N/N$ , we must specify decay modes of  $H$

- for  $m_H = 115$  GeV, pick  $H \rightarrow \tau^+ \tau^-$

with one  $\tau$  decaying to hadrons and one to leptons  
combined branching ratio 0.033

tagging efficiency 0.26; net reduction factor  $\epsilon \sim 0.01$

- for  $m_H = 200$  GeV, pick  $H \rightarrow W^+ W^-$ ; if both decay to leptons,  $\epsilon \sim 0.036$

- “Low luminosity” minimum of  $\sim 10 \text{ fb}^{-1}$  integrated luminosity is needed to discover  $H$  in the WBF process

ATLAS, S. Asai et al hep-ph/0402254 one (good) year of LHC operation at  $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

- $(S + B) \sim 12000 \times 0.01 = 120$  events at

$m_H = 115$  GeV and  $p_T^{\text{cut}} = 40$  GeV;

$\delta N/N \sim 10\%$

- $(S + B) \sim 7000 \times 0.036 \sim 250$  events at

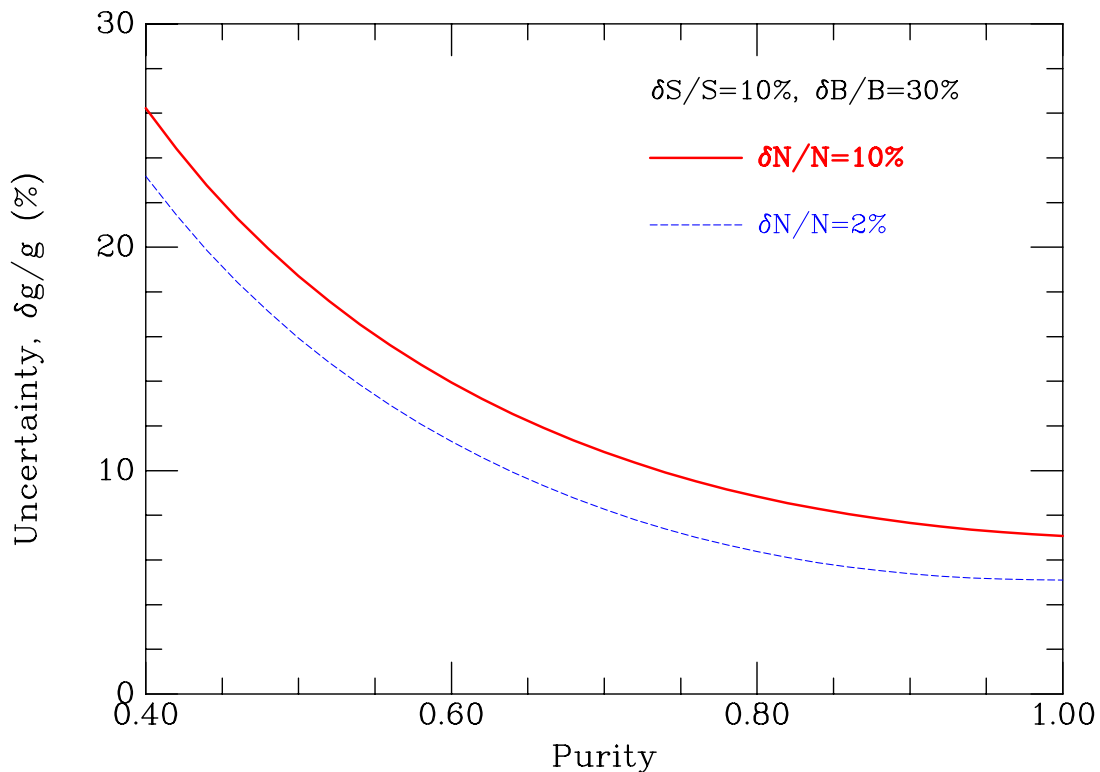
$m_H = 200$  GeV and  $p_T^{\text{cut}} = 40$  GeV;  $\delta N/N \sim 6\%$

## Estimates of Uncertainties in $S$ , $B$ , and $N$

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- “High luminosity” after 5 years of LHC operation, anticipate an integrated luminosity of  $\sim 200 \text{ fb}^{-1}$ 
  - at  $m_H = 115 \text{ GeV}$  and  $p_T^{\text{cut}} = 40 \text{ GeV}$ ;  
 $\delta N/N \sim 2\%$
  - at  $m_H = 200 \text{ GeV}$  and  $p_T^{\text{cut}} = 40 \text{ GeV}$ ;  
 $\delta N/N \sim 1.5\%$

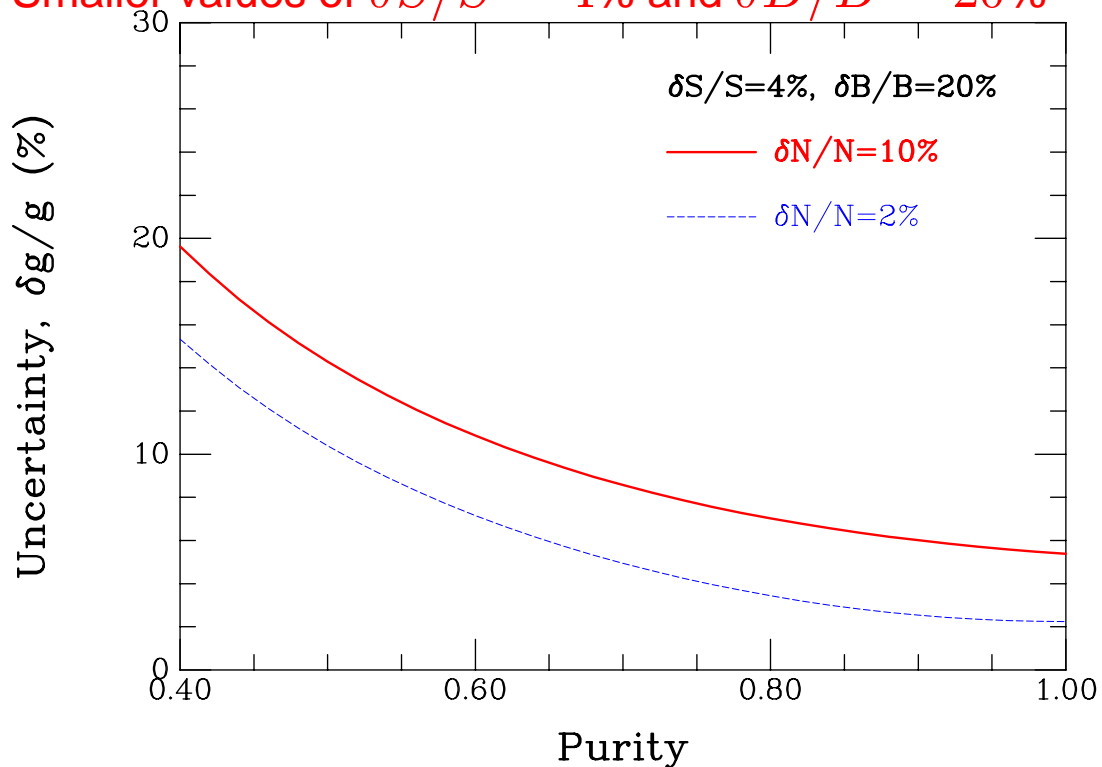
## Coupling Uncertainty vs Signal Purity



- If  $\delta N/N \sim 10\%$      $\delta g/g \sim 11\%$     for  $P = 0.7$
- If  $\delta N/N \sim 2\%$      $\delta g/g \sim 8\%$     for  $P = 0.7$
- **Uncertainties in  $S$  and in  $B$  dominate uncertainty in  $g$ .**  
 With  $P = 0.7$  and  $\delta N/N = 2\%$ , then  $\delta S/S$  and  $\delta B/B$  have to be reduced to 3% and 6% before statistics control the answer
- $P > 0.65$  permits  $\delta g/g \sim 10\%$  after  $200 \text{ fb}^{-1}$   
 Obtained for  $p_T^{\text{cut}} > 40 \text{ GeV}$  at  $m_H = 115 \text{ GeV}$  and  
 for  $p_T^{\text{cut}} > 20 \text{ GeV}$  at  $m_H = 200 \text{ GeV}$
- **Suppose  $K_{\text{background}}^{\text{NLO}} \sim 1.6$**   
 $P = 0.56$  for  $p_T^{\text{cut}} > 40 \text{ GeV}$  at  $m_H = 115 \text{ GeV} \rightarrow$   
 $\delta g/g = 13\%$   
 $P = 0.52$  for  $p_T^{\text{cut}} > 20 \text{ GeV}$  at  $m_H = 200 \text{ GeV} \rightarrow$   
 $\delta g/g = 15\%$

## Coupling Uncertainty vs Signal Purity

- Smaller values of  $\delta S/S = 4\%$  and  $\delta B/B = 20\%$

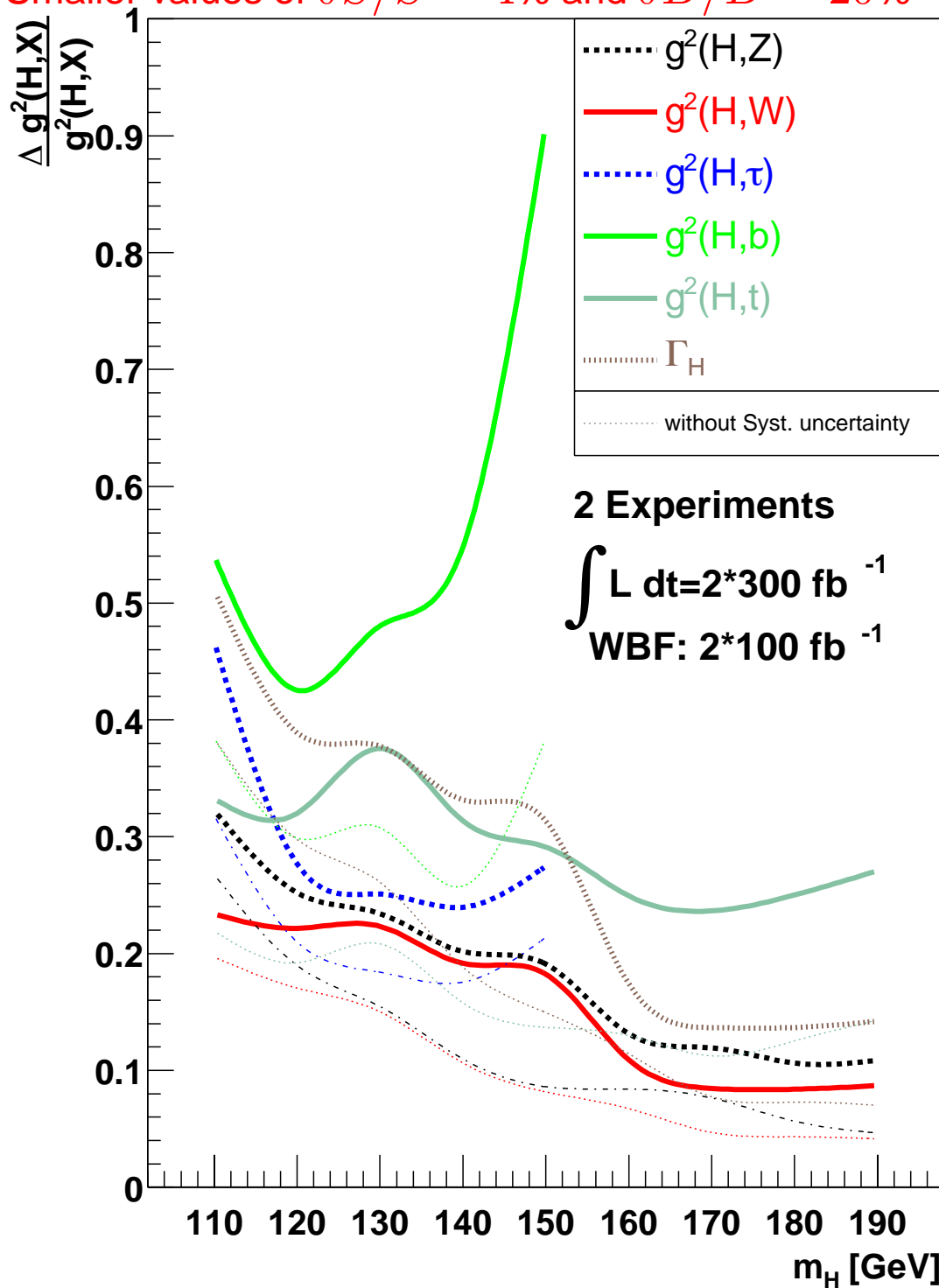


- If  $\delta N/N \sim 10\%$   $\delta g/g \sim 9\%$  for  $P = 0.7$
- If  $\delta N/N \sim 2\%$   $\delta g/g \sim 5\%$  for  $P = 0.7$
- New lower values of  $\delta g/g$  are very similar to Düehrsen et al, Les Houches 2003 for comparable luminosity
- Not evident from these figures that there is much to gain from  $P > 0.7$



# Coupling Uncertainty vs Les Houches Results

- Smaller values of  $\delta S/S = 4\%$  and  $\delta B/B = 20\%$



- Scope of the Les Houches study is more ambitious, but the WBF results at high luminosity are quite similar

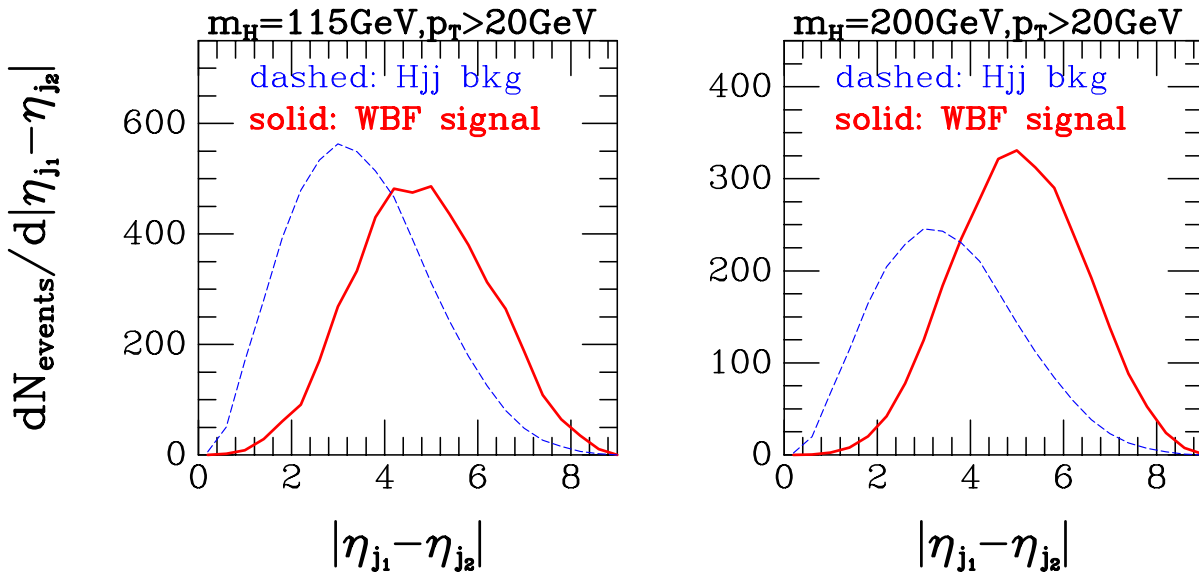
## 4. Alternative WBF Prescriptions

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- We use the requirement that at least one jet have  $1.6 < |\eta| < 4.4$
- A different prescription requires instead a rapidity separation requirement  $|\eta_{j1} - \eta_{j2}| > 4$
- Another requires an invariant mass cut  $M_{jj} > 800 \text{ GeV}$   
→ Figures and Tables
- With these alternatives, there is a significant gain in  $P$  for  $p_T^{\text{cut}} = 20 \text{ GeV}$ , but not for larger values. The gain is accompanied by loss in signal rate at all  $p_T$
- Potential advantages of simple cut on  $|\eta|$  of one jet in a high luminosity environment
  - In data (and at higher orders in QCD) there are several jets; our prescription may be easier to implement
  - In a high luminosity environment, with more than one event per beam crossing, selection on only one jet (plus the  $H$ ) reduces chance that jets from different events are used
- Full experimental simulation would be useful. One could begin with hard QCD LO  $H + 2$  jet matrix elements plus Pythia showering – improvement over current ATLAS studies (c.f., S. Asai et al hep-ph/0402254)

# H + 2 Jet Production – Jet Rapidity Separation

- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO) (for  $1 \text{ fb}^{-1}$ )



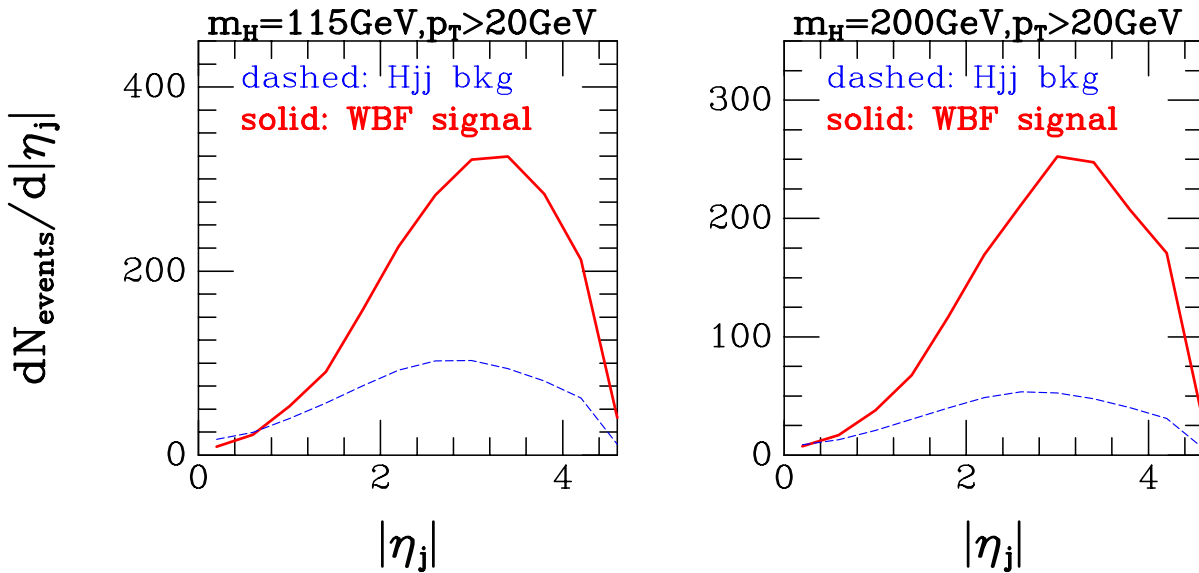
- Shape motivates a rapidity separation cut

$$|\eta_{j1} - \eta_{j2}| > 4$$

$p_T$ cut [GeV]	20	40	80
Signal ( $m_H = 115$ )	1297	718	137
Bkg	758	207	38
Purity	0.63	0.78	0.78
Signal ( $m_H = 200$ )	911	521	106
Bkg	349	102	20
Purity	0.72	0.84	0.84

# $H + 2$ Jet Production – Jet Rapidity with Mass Cut

- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO) (for  $1 \text{ fb}^{-1}$ )



- Alternative WBF prescription:

$$M_{jj} > 800 \text{ GeV}$$

$p_T$ cut [GeV]	20	40	80
Signal ( $m_H = 115$ )	808	561	158
Bkg	304	183	82
Purity	0.73	0.75	0.66
Signal ( $m_H = 200$ )	617	428	121
Bkg	157	95	43
Purity	0.80	0.82	0.74

## 5. Summary

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- Studied  $H + 2$  jet production at the energy of the LHC. WBF signal at NLO; QCD background at LO with estimates of NLO effects. Fully differential hard matrix elements used to generate  $p_T$  spectra
- Investigated effectiveness of 3 different prescriptions to separate/enhance the WBF signal with respect to the *irreducible* QCD background
- Evaluated the signal purity  $P$  (fraction of real  $H$  events produced by WBF) in each case as a function of the transverse momentum cut used to define the tagging jets
- All 3 methods work about equally well in the high-luminosity environment where a large value of the  $p_T$  cut is needed
- After  $200 \text{ fb}^{-1}$  are accumulated, it should be possible to achieve an accuracy  $\delta g/g \sim 10\%$  in the effective coupling of the Higgs boson to weak bosons
- A fully differential NLO calculation of the  $H + 2$  jet distributions is needed, applicable in the WBF region of phase space, so that  $P$  and  $\delta g/g$  can be determined more accurately