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3/18/04

CKM Unitarity, Lattice Pseudoscalar Decay Constants

and
"New Physics"

Outline

I. 3 Generation CKM Unitarity: $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$?

i) $|V_{ud}| = 0.9739(5)$

ii) $|V_{us}| = (0.215 \sim 0.227)$ A Big Mess! $\sim 6\%$ spread!

II. Lattice Pseudoscalar Decay Constants: f_π, f_K, f_D, f_B

* i) $f_K / f_\pi \rightarrow |V_{us}| = 0.222(3)$
 $\pm 1.4\%$! MILC Collaboration

III. Possible "New Physics" Effects (No Really Big Effects)

i) Supersymmetry?

ii) Heavy Quark (or Lepton) Mixing

iii) Exotic Muon Decays $\sim 0.2\%$ eg $\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu$ wrong neutrinos

iv) Z' \rightarrow Extra Dim. loops

v) Charged Higgs (H^\pm) \rightarrow large $\tan\beta \approx 40$

⋮

IV. Outlook

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I. 3 Generation CKM Unitarity

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1-\lambda^2/2 & \lambda & A\lambda^3(\rho-i\eta) \\ -\lambda & 1-\lambda^2/2 & A\lambda^2 \\ A\lambda^3(\rho-i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

$\lambda = |V_{us}| = \sin \theta_{Cabibbo} = \text{CKM Cornerstone}$ } Value of λ ?
 $J_{CP} = \lambda^6 A^2 \eta \approx 3 \times 10^{-5}$ CP Invariant

Unitarity Test: $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$

How well is it tested? $\sim \pm 0.15\%$ (25 sigma loop determination)
 Deviation \rightarrow "New Physics" (How sensitive?)

$|V_{ub}|^2 = (3.6 \pm 0.7 \times 10^{-3})^2 < 2 \times 10^{-5}$ Negligible

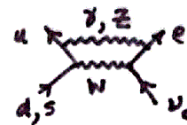
Becomes a Cabibbo angle problem

$|V_{us}| = \sin \theta_c$, $|V_{ud}| \approx \cos \theta_c$

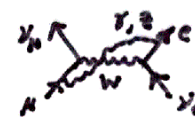
PDG (2002): $|V_{ud}| = 0.9734(8)$, $|V_{us}| = 0.2196(26)$

$|V_{ud}|^2 + |V_{us}|^2 = 0.9957(16 \times 11)$ 2.2 σ deviation

Without Rad. Corrections $|V_{ud}|^2 + |V_{us}|^2 = 1.04!$



or



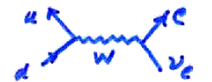
Large R.C. } SM Success
 A. Sirlin

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All semileptonic CC reactions renormalized using $G_\mu = 1.166370 \times 10^{-5} \text{ GeV}^{-2}$ from the muon lifetime.

$$G_\mu = g^2 / 4M_W^2$$

Assumes no exotic μ decays beyond SM, no big tree or loop beyond SM.

i) Status of $|V_{ud}|$  + R.C. / Muon decay amp.

9 Super-Allowed $0^+ \rightarrow 0^+$ Nuclear β -decays $\rightarrow |V_{ud}| = 0.9740(3) \times 4_{RC}$

* Neutron $\tau_n = 885.7(7) \text{ sec}$, $|g_A| = 1.2720(18) \rightarrow |V_{ud}| = 0.9729(4)(4)_{RC}$

Pion $\pi^+ \rightarrow \pi^0 e^+ \nu_e$ (BR $\sim 10^{-8}$!) $\rightarrow |V_{ud}| = 0.9737(39)(2)_{RC}$

Ave $|V_{ud}| = 0.9739(5)$ A. Czarnecki, G.M. + A. Sirlin (In progress)

ii) Status of $|V_{us}|$ Clouded \rightarrow Changing

 $\rightarrow V_{us}$ EW Rad. Corrections } $\pm 1\% \text{ goal}$ Hadronic Effects } (Less Important)

K_{e3} decays $K \rightarrow \pi e \nu$ Vector Current Corrections End Order in SU(3) BR Should be clear

PDG (2002) uses fits for $\bar{K}^0 \rightarrow \pi^+ e^- \nu$ + $K^+ \rightarrow \pi^0 e^+ \nu$ { Old Data } + $(m_u - m_d)$ + EW Rad. Corr. (Roos + Leutwyler)

$|V_{us}|_{PDG} = 0.2196(24)$ $\rightarrow 2.2\sigma$ deviation (Unitarity)

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Recent Advances ?

E865 at BNL $BR(K^+ \rightarrow \pi^0 e^+ \nu)$ increase $\sim +5\% \rightarrow |V_{us}| = 0.2272(30)$

KLOE (Preliminary) $BR(K_S^0 \rightarrow \pi^+ e^- \nu)$ unchanged $\rightarrow |V_{us}| = 0.2180(24)$

About 4.3% difference

Note $(0.9739)^2 + (0.2272)^2 = 1.0001$ Perfect Unitarity! E865

In fact $|V_{ud}| = 0.9739(5)$ + Unitarity $\rightarrow |V_{us}| = 0.2269(22)$

Recent Cirigliano, Neufeld + Pich (p^6 Chiral Corrections) $\sim 1.5\%$ reduction! Large!

E865 $|V_{us}| = 0.2238(30)$

K_{e3} $|V_{us}| = 0.2148(24) \rightarrow 3.8\sigma$ deviation from CKM Unit.

Something is wrong: PDG Fits? Ch Pert.? Both?

Test: $\frac{\Gamma(K_L^0 \rightarrow \pi^+ e^- \nu)_{PDG}}{\Gamma(K^+ \rightarrow \pi^0 e^+ \nu)_{E865}} = 1.81(2)(3)$ Expect 2 in isospin limit 9.5% difference!

$m_{K^0} = 497.67 \text{ MeV}$
 $m_{K^+} = 493.65 \text{ MeV}$ } mainly $m_d - m_u \rightarrow \pi^0 - \eta$ mixing

$m_{\pi^+} = 139.57 \text{ MeV}$
 $m_{\pi^0} = 134.97 \text{ MeV}$ } mainly em

Isospin Corrections: $\frac{1.034 \times 0.96}{0.9726 \times 1.023} \left\{ \begin{matrix} (m_u - m_d) \\ \text{em.} \end{matrix} \right\} = 0.9982$ Almost no isospin corr. (theorem) 9.5% discrepancy \rightarrow Exp (Fit) Errors!

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PDG Kaon Properties τ_K, BR May Be "Way" Off
 eg. All K_s off but $\sigma_P!$ eg $\Delta\tau_{K_s} \approx \pm 0.8\%$ Last measured 1972 (PPA)
 Meanwhile Cabibbo et al Hyperon Lifetimes + A_{sy}
 (Like neutron decay) use V_{ub}

$|V_{\text{us}}| = 0.2250(27)$

$|V_{\text{ud}}|^2 + |V_{\text{us}}|^2 + |V_{\text{ub}}|^2 = 0.9991(16)$ Agrees with Unitarity

Summary Table (Use $|V_{\text{ud}}| = 0.9739(5)$)

Input	$ V_{\text{us}} $	$ V_{\text{ud}} ^2 + V_{\text{us}} ^2 + V_{\text{ub}} ^2$
Unitarity	0.2269(22)	1 0.9991
Hyperons	0.2250(27)	0.9991(16)
K_{e3}^+	0.2238(30)	0.9986(17)
K_{e3}^0	0.2148 0.2148(24)	0.9946(14) significant deviation

II. Lattice Pseudoscalar Decay Constants: $f_\pi, f_K, f_D, f_B \dots$

MILC Collaboration C. Aubin, C. Bernard et al.
 Staggered Fermions + Ch. Corrections .. (Very Detailed)
 Leave Out a.m. + $m_s - m_l$ effects

use $m_{\pi^0}, m_\eta, \frac{m_{K^+} + m_{K^0}}{2} = m_K (?)$ as input

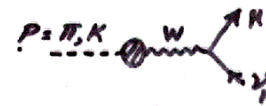
predict $f_\pi, f_K, L_i \dots$ Claim ~2-3% Exp. Agreement

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HEP-LAT/0309088 $\langle 0 | A_\mu | P \rangle = i f_P P_\mu$

Preliminary: $f_\pi = 129.3 \pm 1.1 \pm 3.5 \text{ MeV}$
 $f_K = 155.0 \pm 1.8 \pm 3.7 \text{ MeV}$

$f_K / f_\pi = 1.201(8)(16)$ Errors Partially Cancel!
 $\sim \pm 1.5\%$ error!
 Can be improved!



$\Gamma(K \rightarrow \mu \nu(\gamma)) = \frac{G_F^2 |V_{\text{us}}|^2}{8\pi} f_K^2 m_K m_\mu^2 \left(1 - \frac{m_\mu^2}{m_K^2}\right)^2 \left(1 + \frac{\alpha}{\pi} C_K\right)$
 $\Gamma(\pi \rightarrow \mu \nu(\gamma)) = \frac{G_F^2 |V_{\text{ud}}|^2}{8\pi} f_\pi^2 m_\pi m_\mu^2 \left(1 - \frac{m_\mu^2}{m_\pi^2}\right)^2 \left(1 + \frac{\alpha}{\pi} C_\pi\right)$
 EW R.C. (pointing to the C_K, C_π terms)

Exp. $\frac{\Gamma(K \rightarrow \mu \nu(\gamma))}{\Gamma(\pi \rightarrow \mu \nu(\gamma))} = 1.334(4)$ Very Precise
 (Should be checked)

Rad. Corrections Largely Cancel in ratio $C_K - C_\pi = -3.0 \pm 1.5$
 Short-distance ~2.4%

Finkemeier 1996 should be checked

$\frac{|V_{\text{us}}|^2 f_K^2}{|V_{\text{ud}}|^2 f_\pi^2} = 0.07602(23)_{\text{exp}}(27)_{\text{Re}}$ Tiny Errors!

lattice $f_K / f_\pi \rightarrow \frac{|V_{\text{us}}|^2}{|V_{\text{ud}}|^2} = 0.05271(16)(19)(149)_{\text{lattice}}$
 (2003 Preliminary)

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Assume Unitarity $\rightarrow |V_{us}| = 0.2238(30)$
 Use $|V_{ud}| = 0.9739(5) \rightarrow |V_{us}| = 0.2236(30)$ } Agree with E865 Unitarity

* Preliminary Revision of Preliminary f_K/f_π Lattice 3/12/04

$$f_K/f_\pi = 1.201(8)(15) \rightarrow 1.211(6)(15/13)$$

\rightarrow Assume Unitarity $|V_{us}| = 0.2220(30)$

Use $|V_{ud}| = 0.9739(5) \quad |V_{us}| = 0.2218(30)$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9977(16) \quad \text{small deviation}$$

Lattice calculations can be improved (already competitive).

Aim for $\Delta|V_{us}| \simeq \pm 0.0007$ (Phenomenal)

Different than K_{e3} (Vector Current) vs Axial

Not sensitive to G_F Normalization

Gives relatively pure $\tan \theta_c \rightarrow \lambda$

If other determinations differ \rightarrow "New Physics"

eg. Lattice $\rightarrow |V_{ud}| = 0.9750(6)$

β -decays $\rightarrow |V_{ud}| = 0.9739(5)$

diff = $11 \pm 8 \times 10^{-4}$ "New Physics"? Bound?

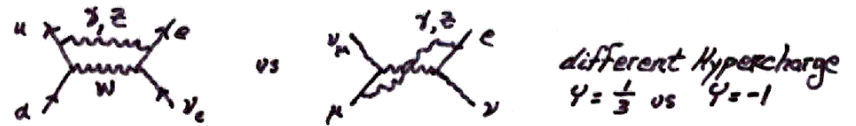
Differ by 0.1% Why? Not a big deal?

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III. Possible "New Physics" Effects (Hint or Constraint?)

What could cause a 0.1% shift in $|V_{ud}|_{exp.}$?

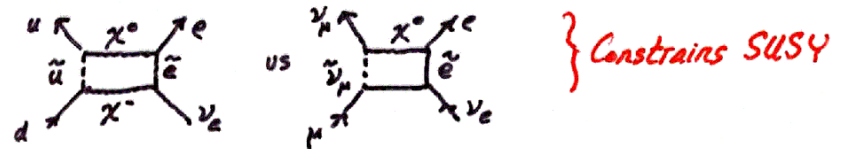
Total R.C. $\sim 2\%$ (How Precise?)



$$1 + \frac{\alpha}{\pi} \ln \frac{m_s}{E_{max}}$$

Other 0.1% sources 2 loop effects, matching ... No!

i) Supersymmetry



Tends to give the wrong sign! But can be forced to give -0.1% shift

Tests squark-slepton universality

ii) Heavy Quark Mixing

$|V_{ub}| = 0.05$ seems large ($|V_{ub}| \simeq 0.0036$)

Heavy Neutrino Mixing - Opposite Sign (Constraint)

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iii) Exotic Muon Decays BR $\approx 0.2\%$ Beyond SM.

If present $\rightarrow G_\mu = 1.16537 \times 10^{-5} \text{ GeV}^{-2}$ not $1.16637(1) \times 10^{-5} \text{ GeV}^{-2}$

Allowed by G_μ vs $\alpha, m_Z, m_W, \sin^2 \theta_W, P_Z \dots$

(Reduces m_H prediction)

eg $\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu$ Babu + Pakvasa (Cute idea)
antineutrino

At 0.2% BR responsible for LSND $\bar{\nu}_e$ signal

MiniBoone will not see it $\pi^+ \rightarrow \mu^+ \bar{\nu}_\mu$ source

Marginally Allowed

Predicts new scalars $\sim 300 \text{ GeV}$ in leptonic sector!

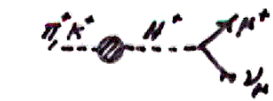
iv) Z' & Extra Dim. Loops eg Z'_X of $SO(10)$

Like SUSY tend to increase unitarity violation

β -decay vs μ decay (Constraint)

v) Charged Higgs H^\pm (2 doublet models)

Affect $K \rightarrow \mu \nu$ & $\pi \rightarrow \mu \nu$ not $B \rightarrow \mu$ decays Helicity



destructive interference
($1 - 2 \frac{m_p^2}{m_{H^\pm}^2} \tan^2 \beta$) reduction

$\tan \beta = v_2/v_1$

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To mimic 0.1% shift in $|V_{ud}|$ requires

$$\frac{m_K^2 - m_\pi^2}{m_{H^\pm}^2} \tan^2 \beta = 0.02$$

or $m_{H^\pm} = 3.4 \tan \beta \text{ GeV}$

if $\tan \beta = 40$ requires $\approx m_{H^\pm} \approx 140 \text{ GeV}$

Some Sensitivity to m_H
For large $\tan \beta$

Also constrains Leptoquark Interactions

IV. Outlook

Lattice Potentially Best $|V_{us}|$ goal factor 4-5 improvement

(Domain Wall Fermions? Very Large Computers)

R.C. Redone, New $P(K \rightarrow \pi \nu \bar{\nu})_{exp}$ (Doubts?) τ_{K^*}

* Need Independent $|V_{ud}|$ or $|V_{us}|$ for comparison

Reduce theory errors? $\pi^+ \rightarrow \pi^0 e^+ \nu$ Hard 10^{-8} BR

Lattice Calculation of R.C.? $n \rightarrow p e \nu$ or K_{e3}^*

Eventually see or constrain "New Physics"

Advance Theory Along The Way

Lattice Has Arrived

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Anticipated and Possible $|V_{ud}|$ & $|V_{us}|$ Advances $\pi^+ \rightarrow \pi^0 e^+ \nu_e$ at PSI $|V_{ud}| \rightarrow \pm 0.0025$ GoalTheory Clean to ± 0.0002 New Experiment Required (Very Hard $BR \sim 10^{-8}$)* $\pi^+ \rightarrow \rho^0 e^+ \nu_e$ Several New Exps. Being Prepared
Measure τ_π & g_A

$$|V_{ud}|^2 = \frac{4908(4) \text{ sec}}{\tau_\pi (1 + 3g_A^2)}$$

A. Czarnecki, W.M., A. Sirlin
(Preliminary)will reach ± 0.0004 (R.C. Uncertainty)
Lattice? $K_L \rightarrow \pi^+ e^+ \nu$ KLOE, KTeV, NA48 Data Exists
Analysis Needed

Normalization?

New K_L Lifetime NeededIf no changes \rightarrow Large Deviation From CKM Unitarity $K^+ \rightarrow \pi^0 e^+ \nu$ New Exp. Needed KLOE?New τ_{K^+} NeededHyperon Decays: Cabibbo et al Approach Needs Study
U & A
FNRL?Lattice f_π , f_ρ , τ_{π^2} , K_{π^2} Best Bet
Domain Wall Fermions?