

Discriminate MSSM Higgs Sector from its Alternative

C.-P. Yuan

Michigan State University

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Based on collaborations with:

- S. Kanemura, PLB 530 (2002) 188, hep-ph/0112165
- S. Kanemura, S. Kiyoura, Y. Okada, E. Senaha, PLB 558 (2003) 157, hep-ph/0211308
- Q.-H. Cao, S. Kanemura, PRD (2004), hep-ph/0311083.

Introduction

- After the discovery of the **Higgs bosons**, we have to ask whether we have detected the **Higgs bosons** predicted by the **MSSM** (Minimal Supersymmetry Standard Model), not, say, the **2HDM** (Two-Higgs-Doublet Model)?

(Both models predict h^0 , H^0 , H^\pm and A .)

⇒ Check their **Couplings** and **Masses**.

- Measuring the Higgs self-coupling (λ_{hhh})
- Testing the MSSM mass relation

$$M_{H^\pm}^2 = M_A^2 + m_W^2$$

via the associated production of A and H^\pm .

Introduction

LEP: $114\text{GeV} < m_h^{\text{SM}} < 196\text{ GeV}$ (95% CL)

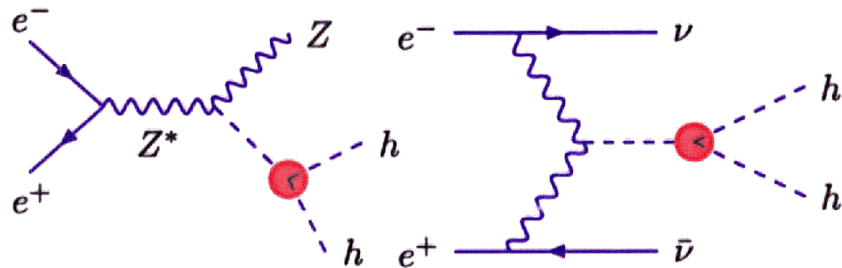
Tevatron, LHC: **Discovery** of at least one Higgs boson

Once a Higgs boson (h) is found, **precision study** at Linear Colliders (LC's) TESLA TDR
ACFA Report
Snowmass Resource Book

- Nature of EWSB g_{hWW}, g_{hZZ}
 $\sigma(e^+e^- \rightarrow Zh), \sigma(e^+e^- \rightarrow \bar{\nu}\nu h) \Rightarrow \mathcal{O}(1\%)$
- Origin of fermion masses: Yukawa couplings Y_f
 $B(h \rightarrow \bar{f}f') \Rightarrow \mathcal{O}(1\%)$.

- Higgs potential: Higgs self-coupling λ_{hhh}

Double Higgs production



λ_{hhh} can be measured in $\mathcal{O}(10 - 20\%)$ accuracy at
 LC: $\sqrt{s} = 0.5 - 1.5\text{ TeV}, \mathcal{L} = 1\text{ab}^{-1}$

Radiative corrections

Precision Measurement at a LC

$$\Delta^{\text{Exp}} g_{hVV}/g_{hVV} \sim 1\%$$

$$\Delta^{\text{Exp}} \lambda_{hhh}/\lambda_{hhh} \sim 10 - 20\%$$

\Leftrightarrow **Radiative Corrections**

Leading top-loop contribution

- hVV coupling

$$g_{hZZ} \simeq \frac{2m_Z^2}{v} \left(1 - \frac{5N_c m_t^2}{96\pi^2 v^2} + \dots \right),$$

loop effect $\sim 1\%$

- hhh coupling

$$\lambda_{hhh} \simeq \frac{3m_h^2}{v} \left(1 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} + \dots \right)$$

A m_t^4 term appears in the 1-loop correction.
loop effect $\sim 10\%$

The corrections are comparable to the measurement accuracy
 \Rightarrow **How about new physics effects?**

The two Higgs doublet model

A simplest extension of the SM Higgs sector for various physics motivations

(MSSM, extra CP phases, topcolor, etc)

- THDM with a softly-broken discrete symmetry:

$$(\Phi_1 \rightarrow \Phi_1; \Phi_2 \rightarrow -\Phi_2)$$

⇒ Natural FCNC suppression

Yukawa interaction (Model II):

$$\mathcal{L}_{II} = -y_D \bar{Q}_L \Phi_1 b_R - y_U \bar{t}_R \Phi_2^\dagger Q_L + (h.c.).$$

Higgs potential:

$$\begin{aligned} V_{\text{THDM}} = & +m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - \frac{m_3^2}{2} (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) \\ & + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 \\ & + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} \left[(\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2 \right]. \end{aligned}$$

Φ_1 and $\Phi_2 \Rightarrow h, H, A^0, H^\pm \oplus 3$ Goldstone bosons

$\begin{array}{ccc} \uparrow & \uparrow & \uparrow \text{charged} \\ \text{CPEven} & \text{CPodd} & \end{array}$

8 parameters : $\Rightarrow \{m_h, m_H, m_A, m_{H^\pm}, \alpha, \beta, v, M_{\text{soft}}\}$

v (VEV) $\simeq 246$ GeV, $\tan \beta (= \langle \Phi_2 \rangle / \langle \Phi_1 \rangle)$

α : mixing angle between h and H

$M_{\text{soft}} (= \frac{m_3}{\sqrt{\cos \beta \sin \beta}})$:

soft-breaking scale of the discrete symm.

- Masses of physical Higgs bosons:

$$m_h^2 = v^2 \left(\lambda_1 \cos^4 \beta + \lambda_2 \sin^4 \beta + \frac{\lambda}{2} \sin^2 2\beta \right) + \mathcal{O}\left(\frac{v^2}{M_{\text{soft}}^2}\right),$$

$$m_H^2 = M_{\text{soft}}^2 + v^2 (\lambda_1 + \lambda_2 - 2\lambda) \sin^2 \beta \cos^2 \beta + \mathcal{O}\left(\frac{v^2}{M_{\text{soft}}^2}\right),$$

$$m_{H^\pm}^2 = M_{\text{soft}}^2 - \frac{\lambda_4 + \lambda_5}{2} v^2,$$

$$m_A^2 = M_{\text{soft}}^2 - \lambda_5 v^2.$$

M_{soft} : soft breaking scale of the discrete symmetry

- M_{soft} determines decoupling/non-decoupling property of heavy Higgs bosons ($\Phi = A, H^\pm$ or H)

$$m_\Phi^2 = M_{\text{soft}}^2 + \lambda_i v^2,$$

Decoupling: for $m_\Phi^2 \sim M_{\text{soft}}^2$ ($M_{\text{soft}}^2 \gg \lambda v^2$)

Loop-effects of H, A, H^\pm decouple

(Decoupling Theorem)

Non-Decoupling: for $m_\Phi^2 \sim \lambda_i v^2$ ($M_{\text{soft}}^2 \lesssim \lambda v^2$)

$\mathcal{O}(m_\Phi^n)$ terms in the low energy observables

(similar to the top effects: $m_t^2 = y_t^2 v^2 / 2$)

The tree-level coupling constants in the THDM

$$g_{hZZ}^{\text{tree}} = +\frac{2m_Z^2}{v} \sin(\beta - \alpha)$$

$$\lambda_{hhh}^{\text{tree}} = -\frac{3}{2v \sin 2\beta} \left[\{\cos(3\alpha - \beta) + 3 \cos(\beta + \alpha)\} m_h^2 - 4 \cos^2(\alpha - \beta) \cos(\alpha + \beta) M_{\text{soft}}^2 \right]$$

- $\sin(\beta - \alpha) \simeq 1$ (Decoupling regime)

$$g_{hZZ}^{\text{tree}} \simeq \frac{2m_Z^2}{v} = g_{hZZ}^{\text{tree}}(\text{SM}),$$

$$\lambda_{hhh}^{\text{tree}} \simeq \frac{3m_h^2}{v} = \lambda_{hhh}^{\text{tree}}(\text{SM})$$

Loop correction is essentially important!

- $\sin(\beta - \alpha) \not\simeq 1$

The tree-level deviation from the SM prediction appears.

Tree-Level Deviation \oplus Loop Correction

Radiative corrections to g_{hZZ} and λ_{hhh} in the THDM

One-loop calculation in the on-shell scheme

The 1-loop contribution for $\sin(\beta - \alpha) \simeq 1$

$$g_{hZZ}^{\text{reno}} \simeq \frac{2m_Z^2}{v} \left[1 - \frac{1}{16\pi^2} \left\{ \frac{5N_c m_t^2}{6v^2} + \frac{2m_\Phi^2}{3v^2} \left(1 - \frac{M_{\text{soft}}^2}{m_\Phi^2} \right)^2 \right\} \right]$$

$$\lambda_{hhh}^{\text{reno}} \simeq -\frac{3m_h^2}{v} \left[1 + \frac{1}{16\pi^2} \left\{ -\frac{16N_c m_t^4}{3v^2 m_h^2} + \frac{16m_\Phi^4}{3m_h^2 v^2} \left(1 - \frac{M_{\text{soft}}^2}{m_\Phi^2} \right)^3 \right\} \right]$$

($\Phi = H, A, H^+$)

In $\lambda_{hhh}^{\text{reno}}$, $\mathcal{O}(m_\Phi^4)$ terms appear with a suppression factor

$$m_\Phi^4 \left(1 - \frac{M_{\text{soft}}^2}{m_\Phi^2} \right)^3 \rightarrow \begin{cases} \frac{\lambda_i v^2}{m_\Phi^2}, & (m_\Phi^2 \sim M_{\text{soft}}^2), & \text{MSSM} \\ & \text{decoupling for } m_\Phi \rightarrow \infty \\ \\ m_\Phi^4, & (m_\Phi^2 \sim \lambda_i v^2), & \\ & \text{non decoupling effect} & \\ & \text{Dynamical SB, EW baryogen.} & \end{cases}$$

Scan Analysis

Free parameters in the THDM:

$$\tan \beta, m_H, m_{H^\pm}, m_A, M_{\text{soft}}$$

for fixed $m_h = 120 \text{ GeV}$, and each $\delta \equiv 1 - \sin^2(\alpha - \beta)$.

Searching allowed region for the deviation in the hZZ and hhh vertices from the SM prediction.

Parameter constrained by

- LEP Precision Data:

Constraint on the (S,T) parameters

- Perturbative unitarity

Lee, Quigg, Thacker

$$|a^0(W_L^+ W_L^- \rightarrow W_L^+ W_L^-)| < \xi, \quad (\xi = 1/4)$$

for 15 channels $W_L^+ W_L^-, Z_L Z_L, Z_L h, hh, hH, \dots$

Kanemura, Kubota, Takasugi

Akeroyd, Arhrib, Naimi

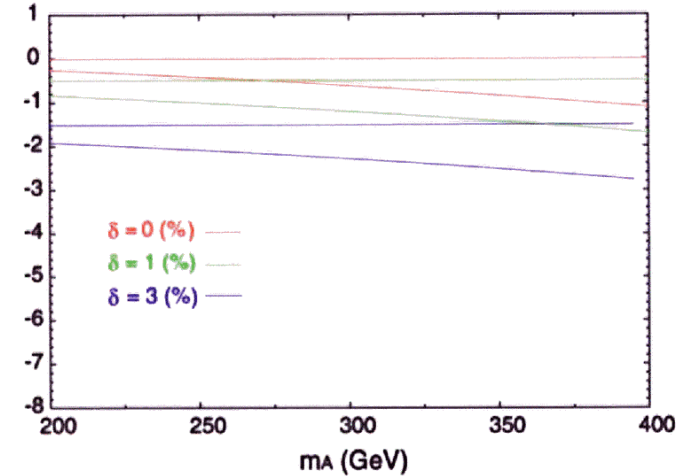
- Vacuum stability

$$V_{\text{eff}}(\langle \Phi_1 \rangle, \langle \Phi_2 \rangle) \geq 0 \text{ for } \langle \Phi_i \rangle \rightarrow \infty.$$

Deshpande, Ma; Sher

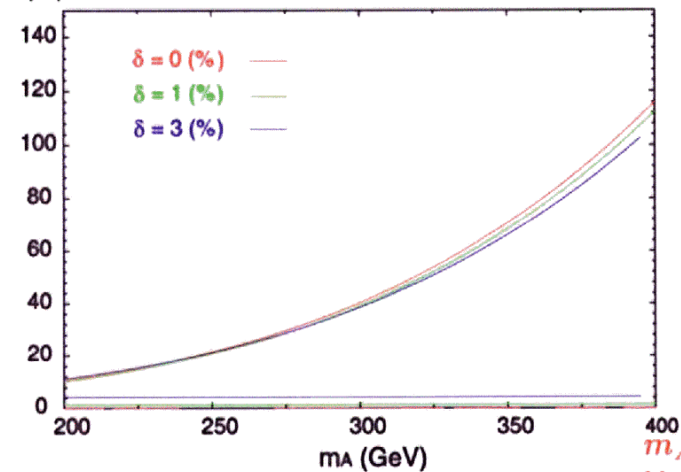
Non-decoupling Effects

(%) deviation of ZZh coupling from SM value



hZZ coupling
Radiative corr.
 $\sim 1\%$

(%) deviation of hhh coupling from SM value



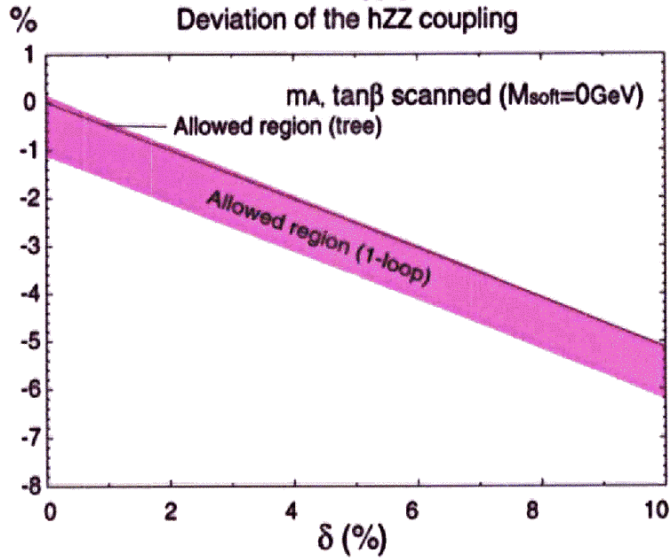
hhh coupling
Radiative corr.
 $\sim 30-100\%$
due to
the m_A^4 term

$$\delta \equiv 1 - \sin^2(\alpha - \beta)$$

$$M_{\text{soft}} = 0, \tan \beta = 1, m_A = m_H = m_{H^\pm}$$

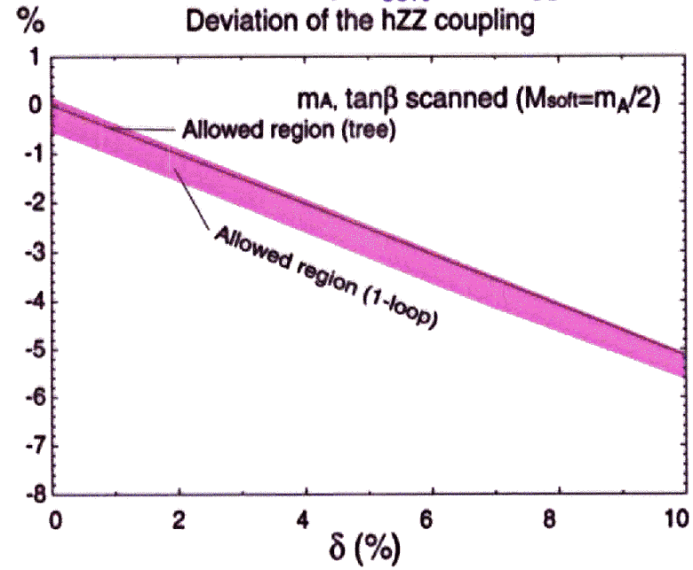
$m_A \lesssim 400 \text{ GeV}$
Unitarity Bound

Allowed Region ($M_{\text{soft}} = 0 \text{ GeV}$)

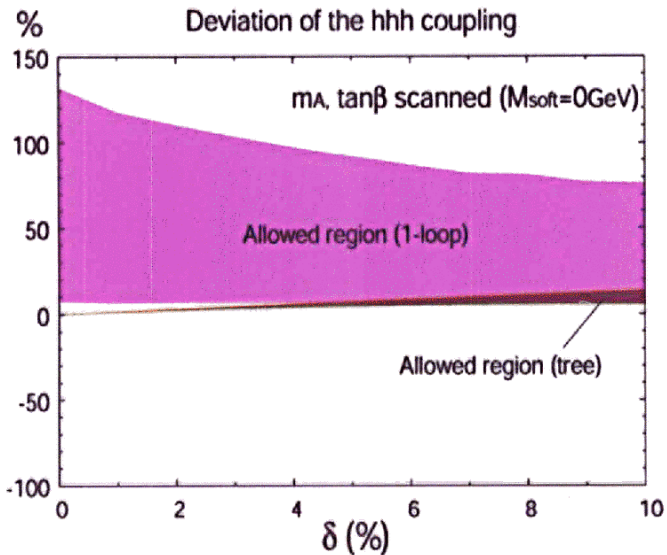


hZZ coupling
Deviation
from the SM
 $\sim 1\%$

Allowed Region ($M_{\text{soft}} = m_A/2$)

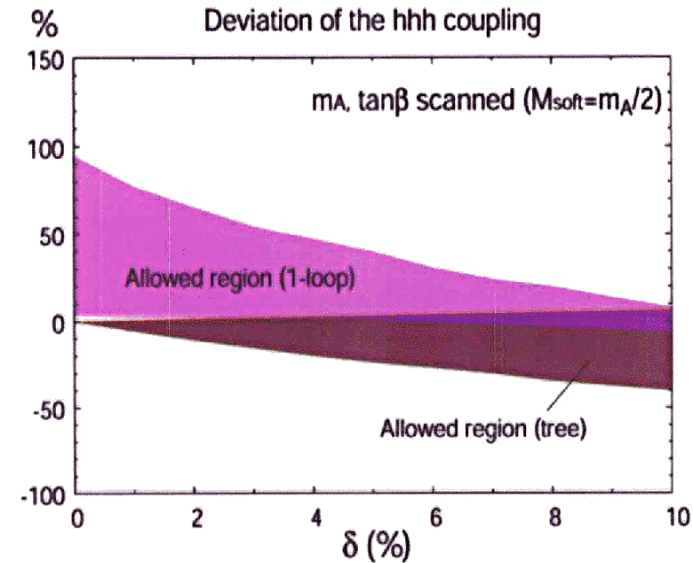


hZZ coupling
Deviation
from the SM
 $\lesssim 1\%$



hhh coupling
Deviation
from the SM
 $\sim 100\%$
due to
the m_A^4 term

$$\delta \equiv 1 - \sin^2(\alpha - \beta)$$



hhh coupling
Deviation
from the SM
 $\lesssim 30-90\%$
due to
the m_A^4 term

$$\delta \equiv 1 - \sin^2(\alpha - \beta)$$

Summary

One-loop effective couplings of hZZ and hhh in the SM and the THDM

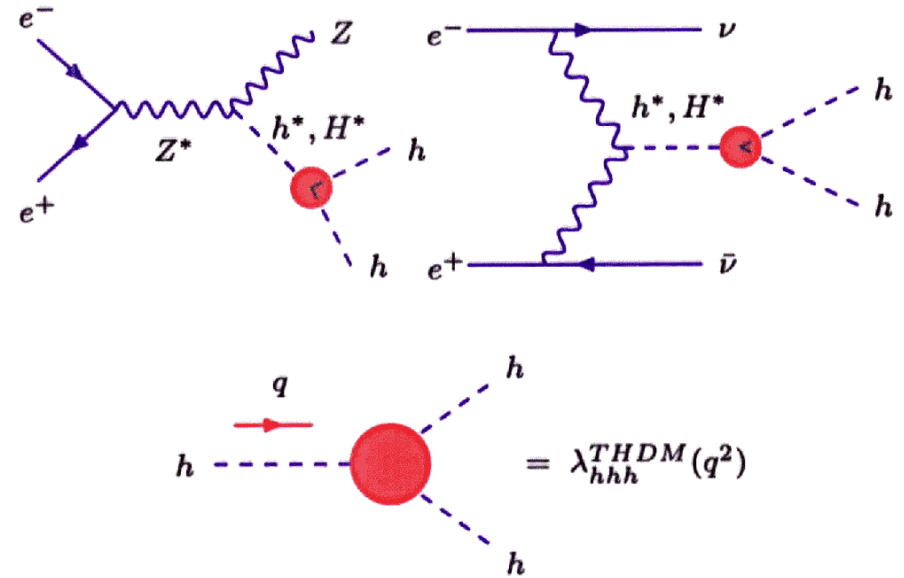
Scan Analysis:

- hZZ : deviation from the SM
 - One-loop contribution ($\sim 1\%$)
 - ⊕ Tree-level difference when $\delta = 1 - \sin^2(\alpha - \beta) \neq 0$
- hhh : deviation from the SM
 - One-loop $\mathcal{O}(m_A^4)$ contribution $\sim +30$ to $+100\%$
 - ⊕ Tree-level difference when $\delta \neq 0$

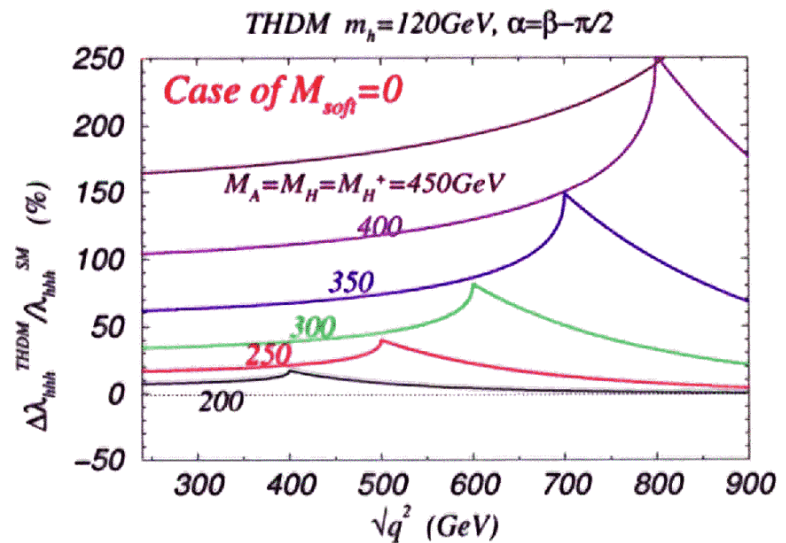
Even when the hZZ measurement is consistent with the SM by $\mathcal{O}(1)\%$, hhh can deviate from the SM by $+30$ to $+100\%$ due to the non-decoupling loop effect of heavy Higgs bosons

Such deviation in the hhh coupling is testable at a Linear Collider

Momentum dependences



Heavy Higgs effect on λ_{hhh}^{THDM} (one-loop)



Self-coupling λ_{hhh} in the MSSM

Hollik, Panaranda
Dobado et al.

The MSSM Higgs sector: a decoupling THDM ($\lambda_i \sim \mathcal{O}(g^2)$)

Relations among heavy Higgs bosons:

$$\begin{aligned} M_{\text{soft}}^2 &= m_A^2, \\ m_{H^+}^2 &= m_A^2 + m_W^2, \\ m_H^2 &\sim m_A^2, \quad (m_A \rightarrow \infty) \\ \sin^2(\alpha - \beta) &\sim 1, \quad (m_A \rightarrow \infty) \end{aligned}$$

$$\frac{\Delta\lambda_{hhh}^{\text{MSSM}}}{\lambda_{hhh}^{\text{SM}}} \propto m_{H^+}^4 \left(1 - \frac{M_{\text{soft}}^2}{m_{H^+}^2}\right)^3 \rightarrow \frac{m_W^6}{m_{H^+}^2}. \quad (\text{Decoupling})$$

Loop corrections due to H, H^+, A
 \Rightarrow small for $\sin^2(\alpha - \beta) \simeq 1$ (less than 1%)

- Stop (\tilde{t}) loop contributions to λ_{hhh}

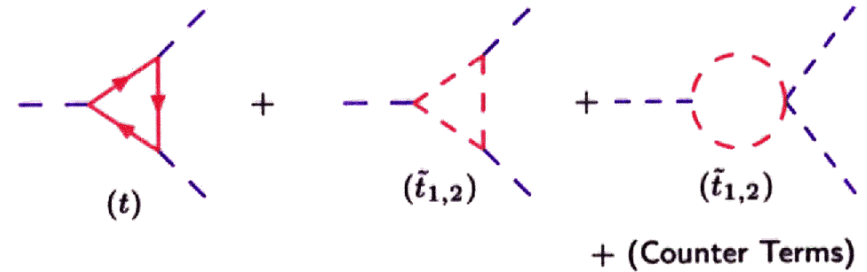
The stop mass matrix

$$M_{\tilde{t}}^2 = \begin{pmatrix} M_Q^2 + m_t^2 + \mathcal{O}(m_Z^2) & m_t X_t \\ m_t X_t & M_U^2 + m_t^2 + \mathcal{O}(m_Z^2) \end{pmatrix},$$

where $X_t = A_t + \mu \cot \beta$.

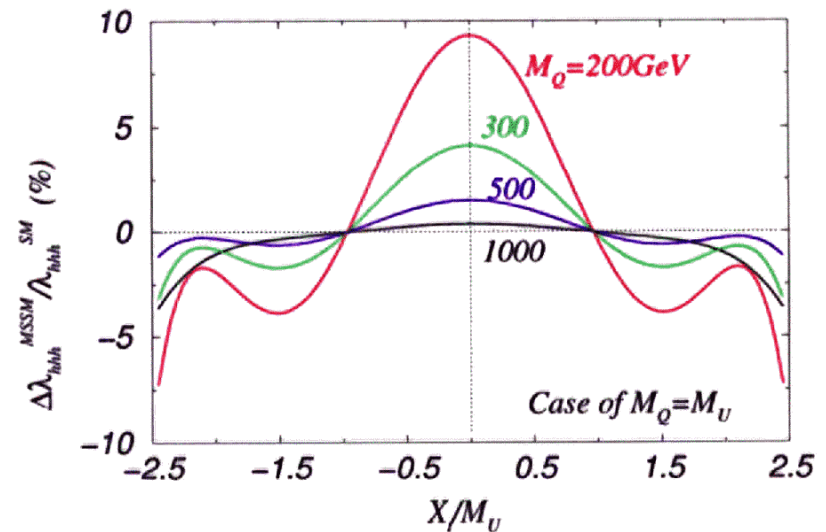
$$\begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_{\tilde{t}} & -\sin \theta_{\tilde{t}} \\ \sin \theta_{\tilde{t}} & \cos \theta_{\tilde{t}} \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}.$$

Feynman diagrams



The leading contributions of stops to λ_{hhh}

$$\begin{aligned} \frac{\Delta\lambda_{hhh}^{\text{MSSM}}}{\lambda_{hhh}^{\text{SM}}} &= \frac{N_{c_t} m_t^4}{3\pi^2 v^2 m_h^2} \frac{m_t^2}{M_Q^2} \left(+1 - \frac{3}{2} \frac{X_t^2}{M_Q^2} \right. \\ &\quad \left. + \frac{1}{2} \frac{X_t^4}{M_Q^4} - \frac{1}{20} \frac{X_t^6}{M_Q^6} \right). \quad (M_Q^2 = M_U^2) \end{aligned}$$



Summary

- In THDM, heavy Higgs (H , A and H^\pm) effects

$$\frac{\Delta\lambda_{hhh}^{THDM}}{\lambda_{hhh}^{SM}} \sim + \frac{M_\Phi^4}{16\pi^2 v^2 m_h^2} \left(1 - \frac{M_{\text{soft}}^2}{M_\Phi^2}\right)^3$$

The correction can be $\mathcal{O}(100\%)$
for a light h ($m_h \sim 120 - 160\text{GeV}$)

even if the data for

$\sigma(e^+e^- \rightarrow Xh)$, $Br(h \rightarrow X)$ and Γ_h
agree with the SM prediction.

↓

Such large non-decoupling effects
is testable at LC.

- MSSM

Decoupling for $m_A^2 \rightarrow \infty, M_Q^2 \rightarrow \infty$.

The stop-loop correction can
reach to 5-8% for small M_Q^2

↓

Physics predictions depend strongly on
the details of SUSY parameters.

- A typical SUSY phenomenology study depends on at least two SUSY parameters,
e.g. $\tan\beta$ and m_A ,
and
various physics reach depends on other SUSY parameters as well,
e.g. μ value and stop mixings.

⇒ Very often, the physics reach of a process is expressed in terms of bounds on

$$\sigma \text{ (production)} \times Br \text{ (decay branching ratio)}$$

where both σ and Br depend on SUSY parameters.

- In general, detection efficiency also depends on SUSY parameters,
e.g. a Higgsino and a gaugino type of chargino have different decay distributions.

Our task is to find a SUSY process

- whose tree level σ (production) only depends on **ONE** SUSY parameter that can be determined by kinematic variable (e.g. invariant mass).
- that is not sensitive to the detailed SUSY parameters via **radiative corrections**.
- that can bound the SUSY models by (product of) **Br (decay branching ratio)** without convoluting with σ (production).
- that can be used to **distinguish MSSM from its alternatives**, e.g. 2HDM.
- whose final state particle kinematics can be properly modeled without specifying any SUSY parameters.
 \Rightarrow The **detection efficiency** can be accurately determined.

Here is that promising process

$$p\bar{p}, pp \rightarrow W^\pm \rightarrow AH^\pm$$

- The vertex $W^\mu - A - H^\pm$ is determined by **gauge interaction**, which gives

$$\frac{g}{2}(p_A - p_{H^\pm})^\mu.$$

\Rightarrow

No SUSY parameter.

- The production cross section $\sigma(AH^\pm)$ in general depends on two masses:

$$M_A \text{ and } M_{H^\pm}$$

e.g. in 2HDM.

But, in MSSM,

$$M_{H^\pm}^2 = M_A^2 + m_W^2.$$

$\Rightarrow \sigma(AH^\pm)$ only depends on g and M_A .

(M_A can be determined from its decay kinematics, e.g. the invariant mass of $b\bar{b}$ in $A \rightarrow b\bar{b}$.)

Constraint on MSSM

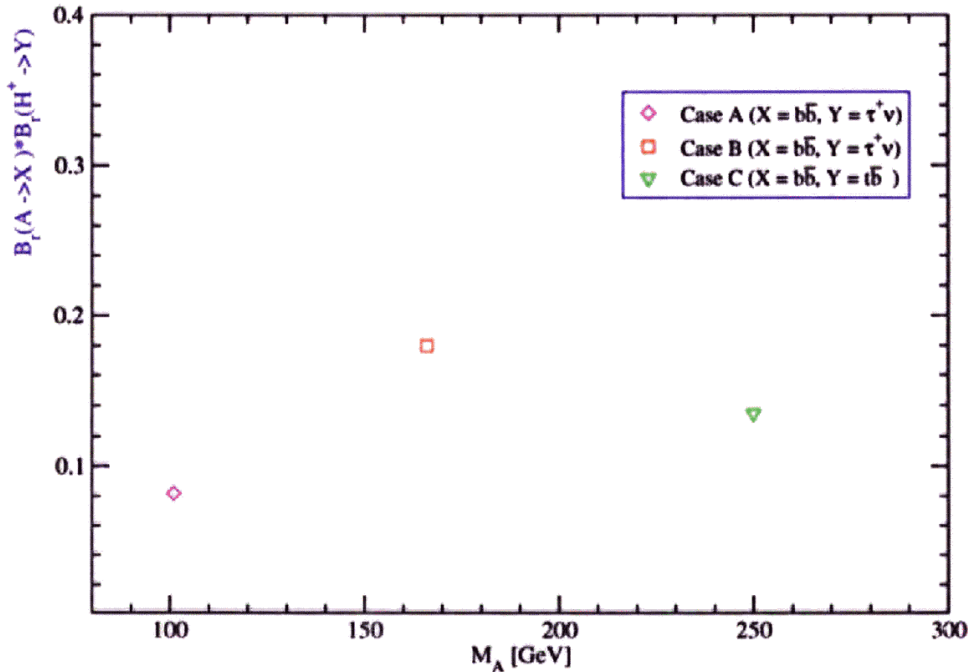
Constraints on the product of branching ratios

$$B(A \rightarrow b\bar{b}) \times B(H^+ \rightarrow \tau^+ \nu_\tau)$$

as a function of M_A for Case A and Case B, and

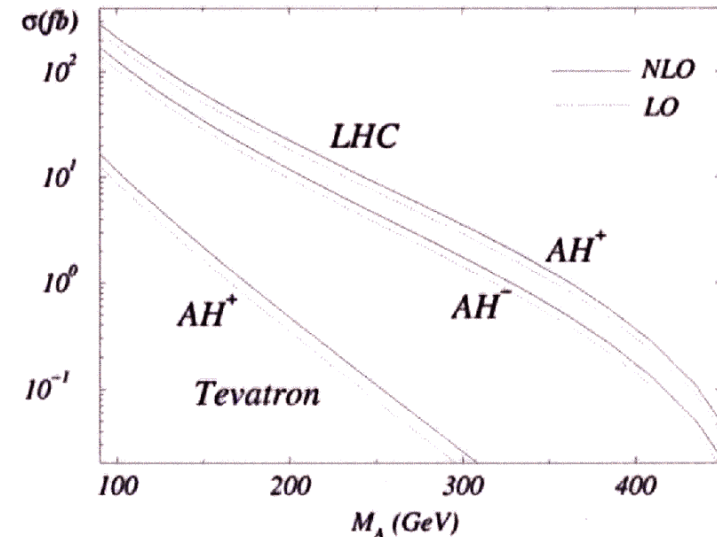
$$B(A \rightarrow b\bar{b}) \times B(H^+ \rightarrow t\bar{b})$$

for Case C, at the LHC, where τ^+ decays into $\pi^+ \bar{\nu}_\tau$ channel.



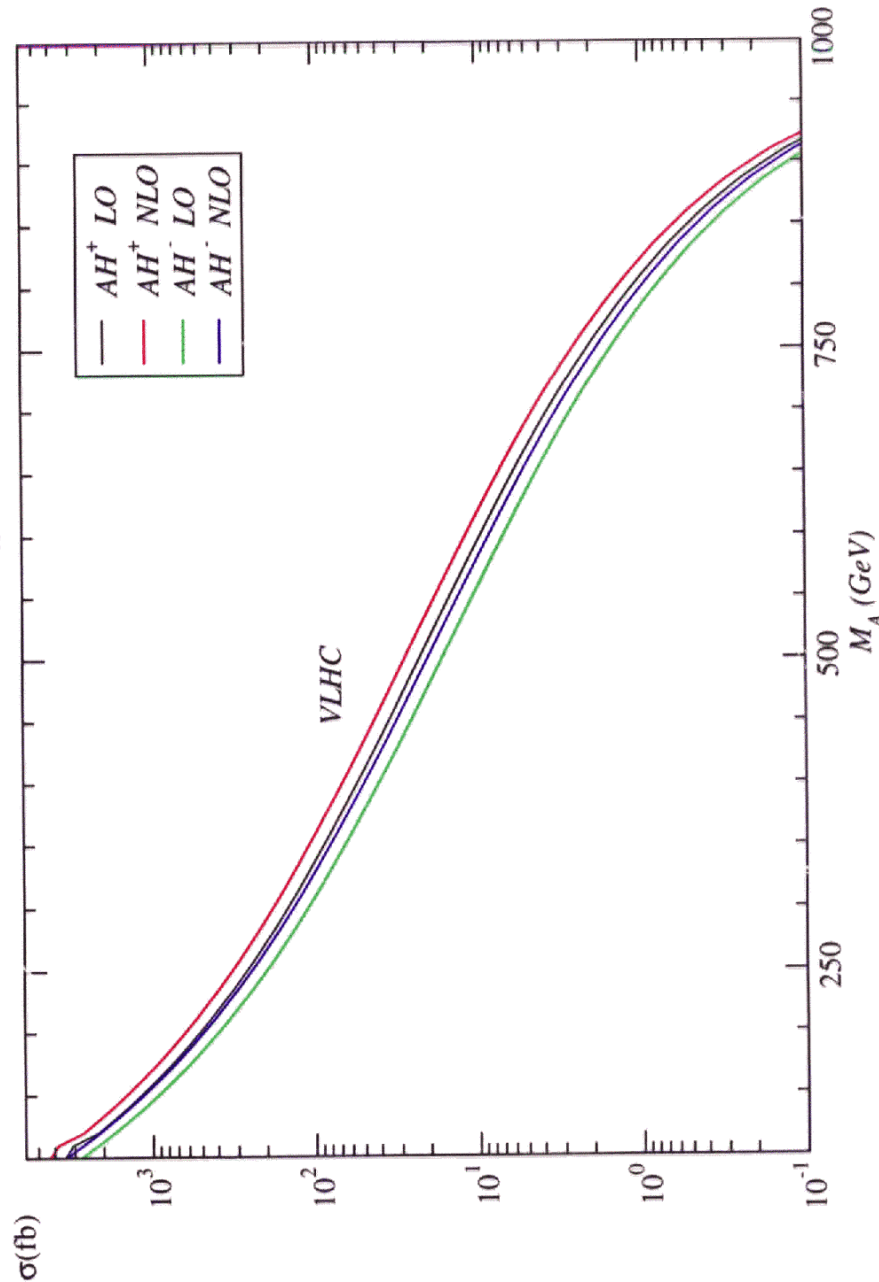
Production rates

The LO (dotted lines) and NLO QCD (solid lines) cross sections of the AH^+ and AH^- pairs as a function of M_A . The cross sections for AH^+ and AH^- coincide at the Tevatron for being a $p\bar{p}$ collider.



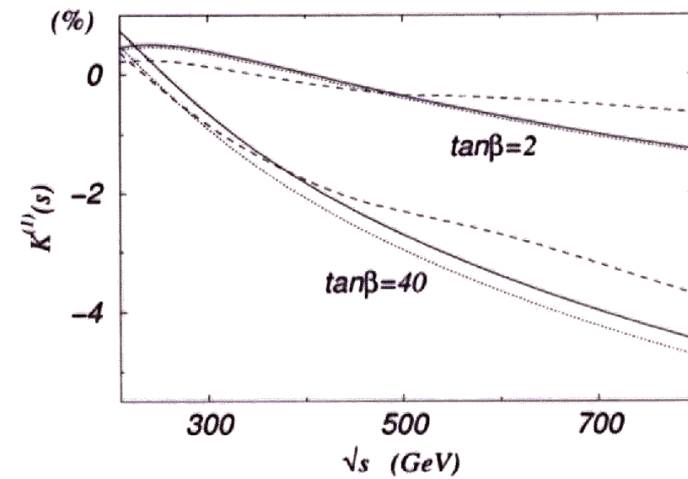
- The NLO QCD correction is about 20%.
- Uncertainty due to parton distribution is about 6% at Tevatron and 5% at LHC for $M_A = 120$ GeV, when applying the prescription given in hep-ph/0101032 (by Pumplin, Stump, Tung).
- The higher order QCD correction is estimated to be about 10% at Tevatron and less than 1% at LHC, when varying the factorization scale around the c.m. energy of $q\bar{q} \rightarrow AH^\pm$ by a factor of 2.

The LO and NLO QCD cross sections of the AH^+ and AH^- pairs as a function of M_A at VLHC



Electroweak K -factor

The K -factor of $q\bar{q} \rightarrow H^+ A$ for $M_A = 90$ GeV, as a function of the invariant mass \sqrt{s} of $q\bar{q}$. The solid curves come from the top and bottom quark contributions. The squark-loop contributions are shown by dotted curves for those without stop mixing and by dashed curves for those with maximal stop mixing, respectively.



- The K -factor at the parton level:

$$K^{(1)}(q^2) \equiv 2 \operatorname{Re} F^{(1)}(q^2).$$

- The one-loop electroweak correction to the production rate of $pp, p\bar{p} \rightarrow AH^\pm$ is smaller than the PDF uncertainties.

Radiative correction to the MSSM mass relation

$$M_{H^\pm}^2 = M_A^2 + m_W^2.$$

- In the on-shell scheme, after fixing M_A and $\tan\beta$, M_{H^\pm} is determined by

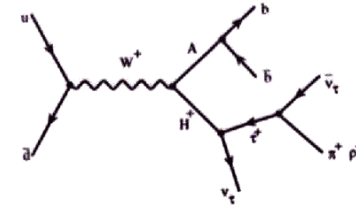
$$M_{H^\pm}^2 = M_A^2 + m_W^2 + \Pi_{AA}(M_A^2) - \Pi_{H^+H^-}(M_A^2 + m_W^2) + \Pi_{WW}(m_W^2),$$

where $\Pi(q^2)$ are the self-energies.

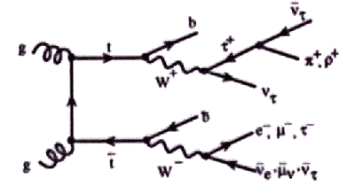
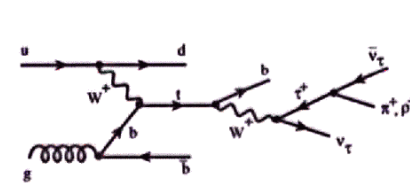
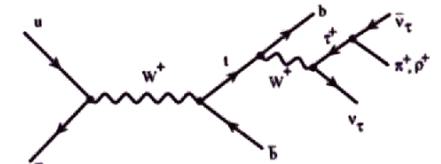
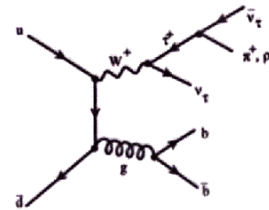
- There are 7 parameters in the Higgs sector of the MSSM. They are g' , g , v_1 , v_2 , m_1 , m_2 , and m_3 . Beyond the Born level, the wavefunction renormalization factors Z_{H_1} and Z_{H_2} are also needed.
- The standard model parameters are fixed by defining α_{em} , m_W and m_Z , and the additional SUSY parameters in the Higgs sector are fixed by the following renormalization conditions:
 - the tadpole contributions ($T_{H_1} = 0$, $T_{H_2} = 0$),
 - the on-shell condition for the mass of A ,
 - the on-shell condition for the wavefunction of A ,
 - a renormalization condition on $\tan\beta$ (which requires $\delta v_1/v_1 = \delta v_2/v_2$), and
 - a vanishing $A - Z$ mixing for an on-shell A .

Detecting the Signal Event

- Signal



- Backgrounds



- Veto additional lepton and jet from the parton level background events that satisfy $p_T(\text{lepton}) > 10 \text{ GeV}$, and $|\eta(\text{lepton})| < 3$. $p_T(\text{jet}) > 10 \text{ GeV}$, and $|\eta(\text{jet})| < 3.5$.

- The model parameters, production rates and decay branch ratios

Sets	A	B	C
m_A/Γ_A	101 / 3.7	165.7 / 5.6	250 / 7.9
m_h/Γ_h	96.8 / 3.3	112 / 0.04	112 / 0.01
m_H/Γ_H	113 / 0.38	163 / 5.5	247.8 / 7.8
m_{H^+}/Γ_{H^+}	126 / 0.43	182 / 0.68	261.4 / 4.2
$\sigma(AH^+) [fb]$	164	36	5.4
$\sigma(HH^+) [fb]$	137.4	37.4	5.4
$Br(A \rightarrow bb)$	0.91	0.90	0.89
$Br(H \rightarrow bb)$	0.90	0.90	0.89
$Br(H^+ \rightarrow \tau^+\nu)$	0.98	0.90	0.00
$Br(H^+ \rightarrow t\bar{b})$	0.00	0.09	0.79
$Br(\tau^+ \rightarrow \pi^+\nu)$	0.11	0.11	0.11

where $\tan\beta = 40, \mu = M = 500\text{GeV}$.

- Imposing the following **Basic Cuts** :

$$P_T(b, \bar{b}, \pi^+) > 15 \text{ GeV},$$

$$|\eta(b, \bar{b}, \pi^+)| < 3.5,$$

$$\Delta R(b, \bar{b}, \pi^+) > 0.4.$$

Set A ($m_A = 101\text{GeV}$)

- Numbers of signal and background events at the LHC with 100 fb^{-1} . The b -tagging efficiency (50%, for tagging both b and \bar{b} jets) is included, and the kinematic cuts listed in each column are applied sequentially.

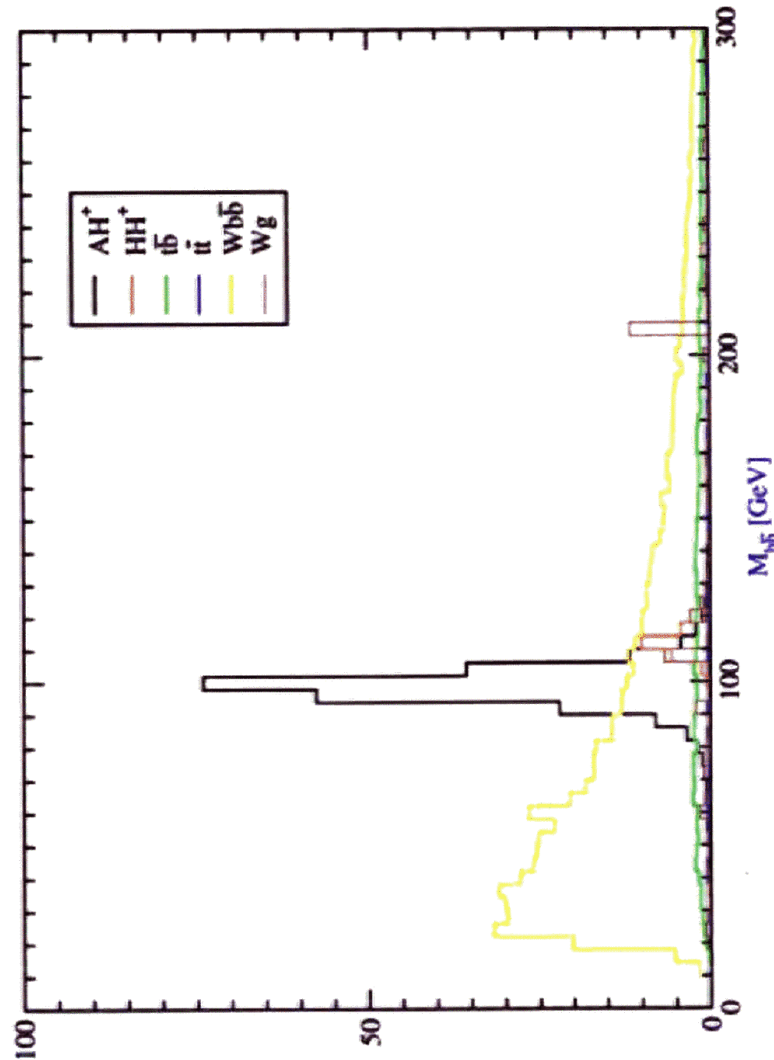
- Signal: AH^+

	Basic Cuts	$E_T > 50$	$P_T^b > 40$	$90 < M_{bb} < 110 [\text{GeV}]$
AH^+	507	391	241	216
HH^+	48	38	24	0
$Wb\bar{b}$	11555	3111	864	67
$t\bar{b}$	1228	614	163	12
Wg	567	236	68	11
$t\bar{t}$	110	80	17	2
Signal (S)	507	391	241	216
Bckg (B)	13507	4078	1135	92
S/B	0.038	0.095	0.212	2.35
S/\sqrt{B}	4.36	6.12	7.14	22.5
$\sqrt{S+B}/S$	0.23	0.17	0.15	0.08

- Signal: HH^+

	Basic Cuts	$E_T > 50$	$P_T^b > 40$	$105 < M_{bb} < 125 [\text{GeV}]$
HH^+	48	38	24	24
AH^+	507	391	241	26
$Wb\bar{b}$	11555	3111	864	58
$t\bar{b}$	1228	614	163	11
Wg	567	236	68	13
$t\bar{t}$	110	80	17	2
Signal (S)	48	38	24	24
Bckg (B)	13966	4431	1352	101
S/B	0.003	0.008	0.018	0.22
S/\sqrt{B}	0.41	0.57	0.65	2.26
$\sqrt{S+B}/S$	2.47	1.76	1.55	0.49

- The invariant mass of $b\bar{b}$, $M(b\bar{b})$:

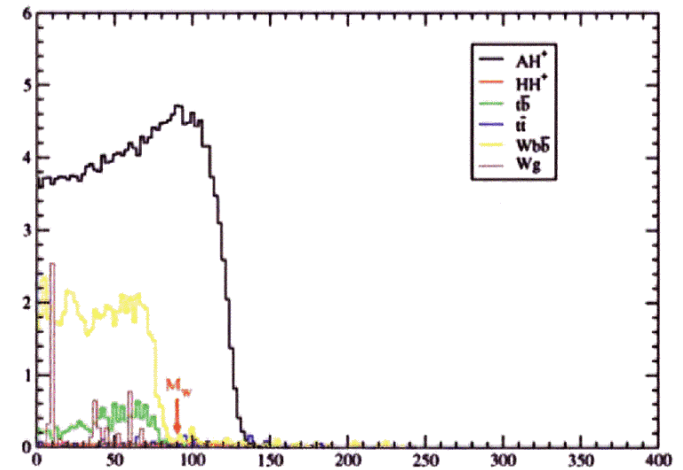


- The transverse mass of π^+ and E_T , i.e. of H^+ in the signal event, after imposing the additional cuts:

$$AH^+: |M(b\bar{b}) - 100| < 10 \text{ GeV}$$

OR

$$HH^+: |M(b\bar{b}) - 115| < 10 \text{ GeV}$$



- $\Delta\phi$ is the azimuthal angle between π^+ and E_T , the transverse mass

$$M_T = \sqrt{2 p_T(\pi) E_T (1 - \cos \Delta\phi)}$$

Summary

- Assuming the double b -tagging efficiency to be 50%, there will be about 190 signal events,

$$pp \rightarrow A(\rightarrow b\bar{b}) H^+(\rightarrow \tau^+(\rightarrow \pi^+\bar{\nu}) \nu)$$

detected at the LHC (with a 100 fb^{-1} integrated luminosity).

- The total number of background events is about half of the signal event.
- Including the negative charge of π^- increases the signal and the background rate by about 50%.
- One can also include the decay mode $\tau^\pm \rightarrow \rho^\pm \nu$ whose Br is about 22%. Hence, the event rate will roughly be tripled.

⇒ The observed signal event rate can be at the order of 500 to 1000 per LHC year.

⇒

The AH^\pm signal is a promising one, indeed.

Conclusion

- If a signal is **not found**, studying the AH^\pm associated production process can provide an upper bound on the product of the decay branching ratios of A and H^\pm as a function of the only one SUSY parameter – M_A .
- In case that a signal is **found**, the analysis is slightly more complicated.
 - For $M_A \gtrsim 120 \text{ GeV}$ and $\tan \beta \gtrsim 10$, $M_H \sim M_A$ (less than about 10 GeV).
For $M_A \gtrsim 190 \text{ GeV}$ and $\tan \beta \gtrsim 10$, $\sin^2(\alpha - \beta) \simeq 1$ and $\sigma(q\bar{q} \rightarrow HH^\pm) \sim \sigma(q\bar{q} \rightarrow AH^\pm)$.
[Generally, the coupling of $W^\pm HH^\mp$ depends on g and $\sin(\alpha - \beta)$.]
 - Studying different decay channels can help to separate these two production modes. For instance, a heavy H can decay into a ZZ pair at the Born level, but A cannot.
- In conclusion, if no signal is found experimentally, a **conservative bound** on the product of the decay branching ratios of A and H^\pm can be derived for a CP-conserving model. This is because in a CP-conserving model, the AH^+ and HH^+ production modes do not interfere even if the masses of A and H are about the same. (A is a CP-odd scalar, while H is CP-even.)