

# Off-diagonal scattering in the cuprates: inhomogeneity and ZBCP near Zn

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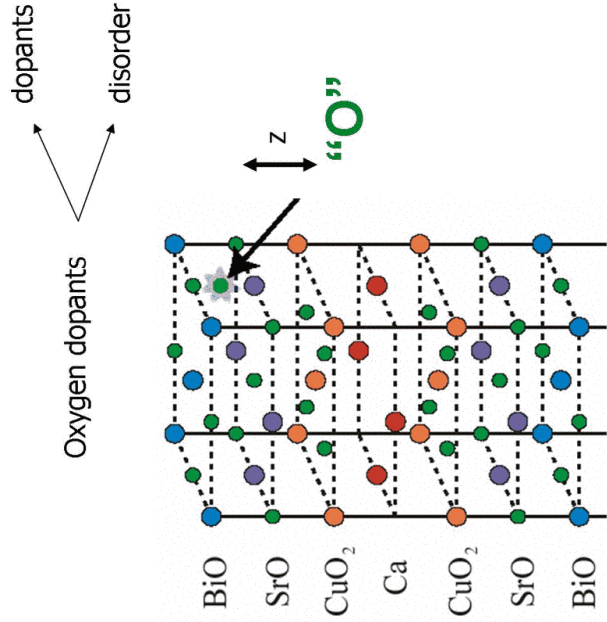


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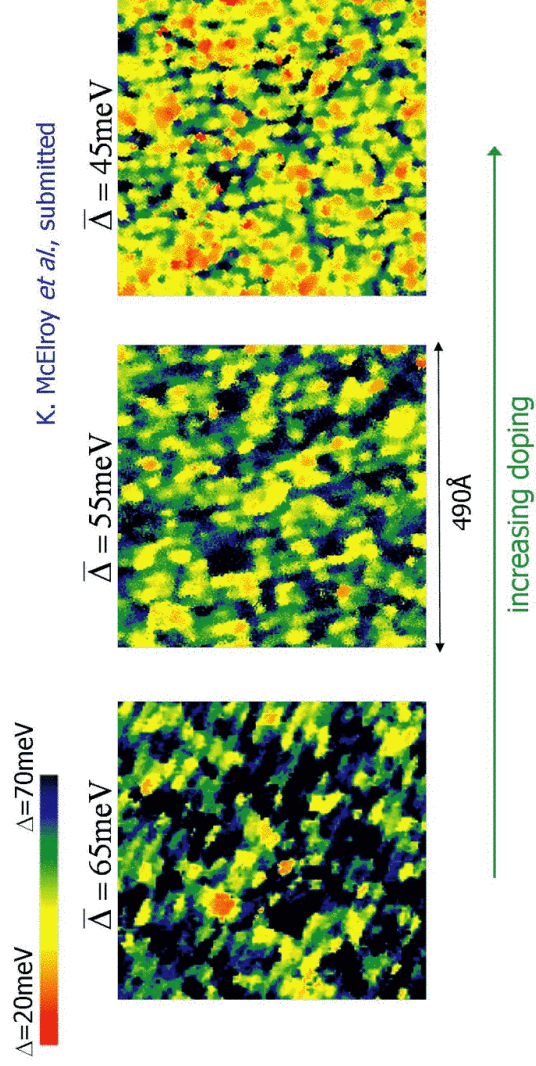
## Outline

- 1) STM Experiments:
  - Very brief review of nano-scale inhomogeneity.
- 2) Model: modulations in the off-diagonal channel:
  - Comparing correlations (potential scattering discussed in Tamara's talk)
  - Characteristics of Andreev scattering near point-like impurities
- 3) STM Experiments:
  - Zero bias conductance peaks near e.g. Zn impurities
- 4) Model: modulations in the off-diagonal channel:
  - Andreev resonant state near phase impurities

# Doping in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$



# Nano-scale disorder



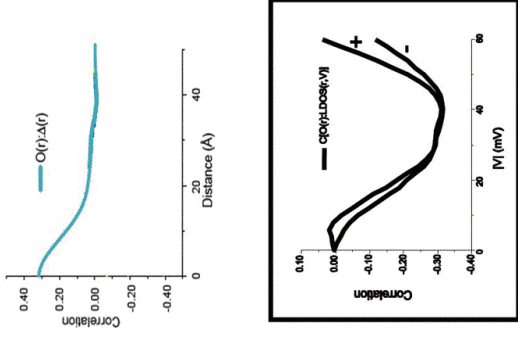
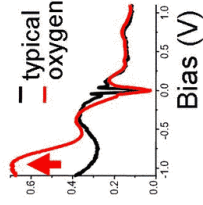
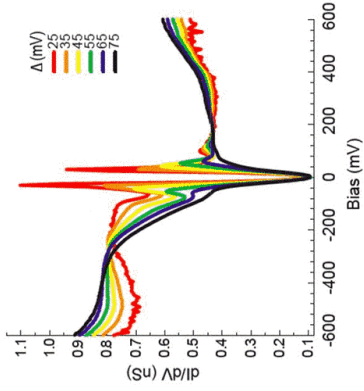
Fraction of large gap spectra increases with underdoping

Spectral line-shapes remain doping independent

## Relation: spectra $\leftrightarrow$ oxygen dopants

Experimental identification of oxygen dopant positions via  $-0.96\text{V}$  resonance

K. McElroy *et al.*,  
submitted



particle-hole symmetric at low energy

small charge modulations < 10%

## Model

Mean field Hamiltonian for d-wave BCS superconductor:

$$H = \sum_{k\sigma} \epsilon_k c_{k\sigma}^+ c_{k\sigma} + \sum_{i\sigma} V_i c_{i\sigma}^+ c_{i\sigma} + \sum_{\langle ij \rangle} (\Delta_{ij} c_{i\uparrow}^+ c_{j\downarrow}^+ + H.c.)$$

with:  $\epsilon_k = -2t(\cos k_x + \cos k_y) - 4t' \cos k_x \cos k_y - \mu$   $t' = -0.3t, \mu = -1.0t$

Self-consistency condition for the order parameter:

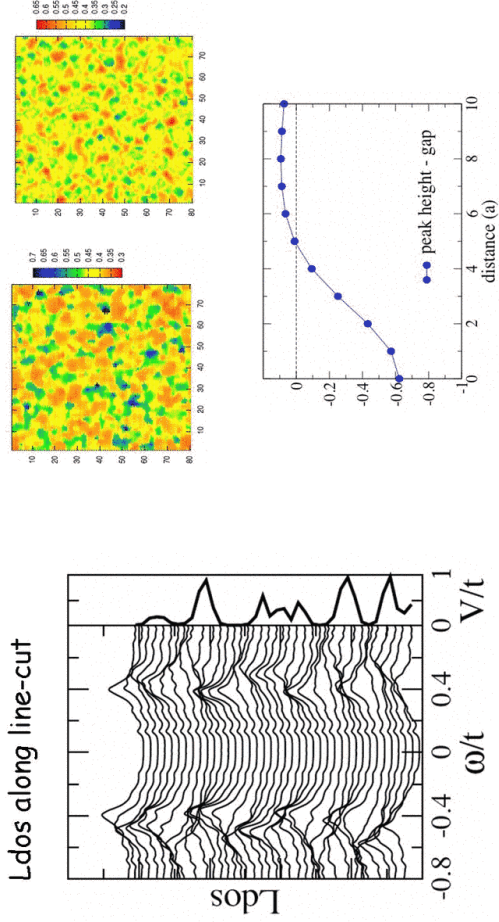
$$\Delta_{ij} = g_{ij} \langle c_{i\uparrow} c_{j\downarrow} - c_{i\downarrow} c_{j\uparrow} \rangle$$

Allow for dopant-modulated pair interaction:

Twinning-plane SC  
Khylyustikov & Buzdin  
Adv. Phys. (1987)

Solve selfconsistent BdG equations on lattices of order  $100 \times 100$  sites

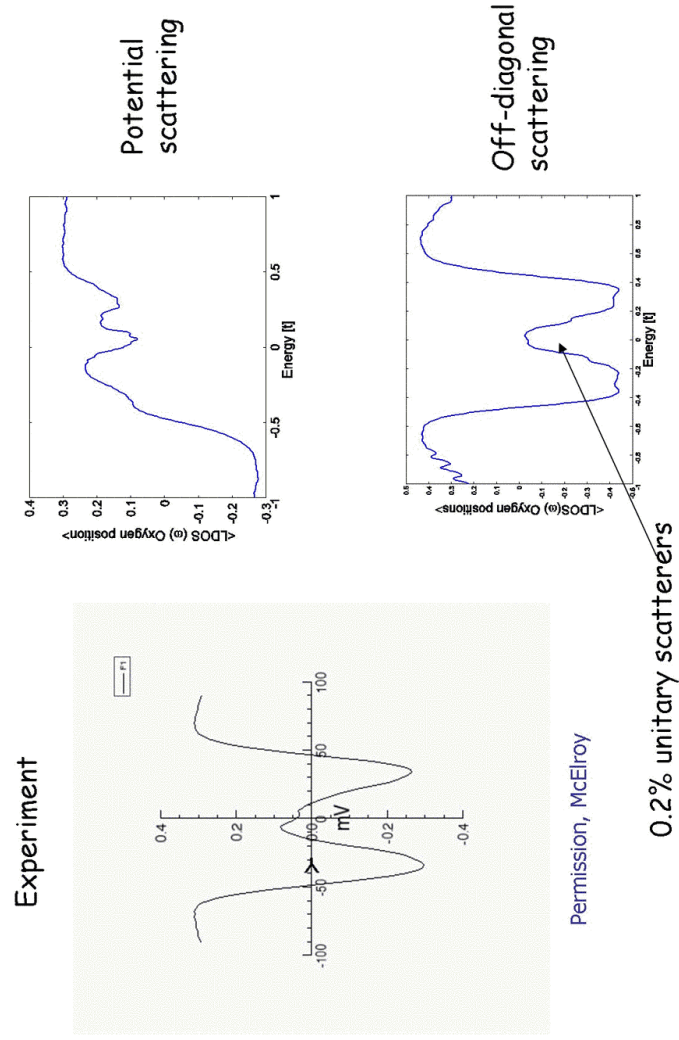
## Results with pair interaction modulations



T. Nunner *et al*  
cond-mat/0504693

- Results:
- Homogeneous low-energy Ldos
  - Positive correlation: dopants  $\leftrightarrow$  gap magnitude
  - **Anti-correlation: "coherence" peak height  $\leftrightarrow$  gap magnitude**
  - Small charge modulations

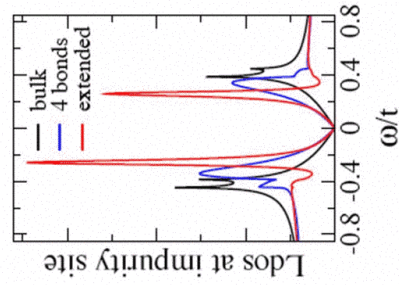
## LDOS - Oxygen correlations vs bias



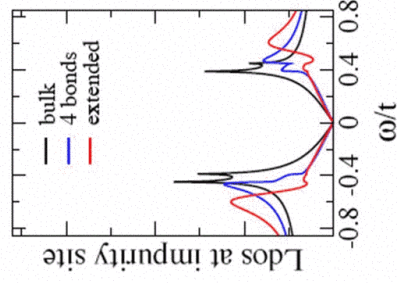


## Single off-diagonal impurity

Order parameter suppression



Order parameter enhancement



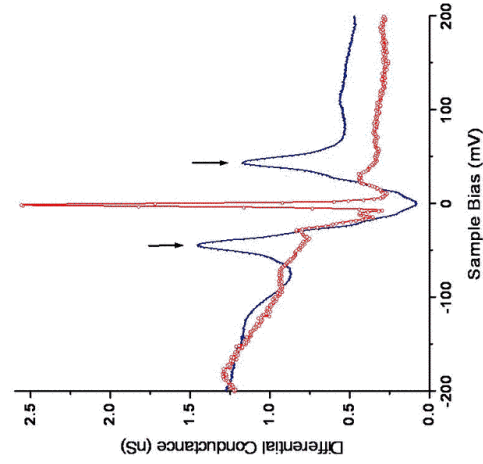
→ Formation of new Andreev-resonance below the gap edge

→ Suppression of coherence peaks

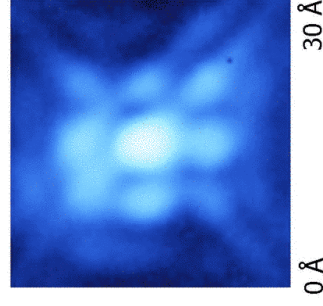
Similar calculations by Capriotti & Scalapino

## Zn resonance in STM

Zn-substitution for Cu in  $\text{CuO}_2$ -plane



-1.5 mV



Pan *et al.* Nature (1999)

# Zn resonance in STM

$$G^0(\mathbf{k}, i\omega_n) = \frac{i\omega_n\tau_0 + \xi_{\mathbf{k}}\tau_3 + \Delta_{\mathbf{k}}\tau_1}{(i\omega_n)^2 - E_{\mathbf{k}}^2}$$

Potential scattering dSC resonance,  
Balatsky *et al*, PRB (1995)

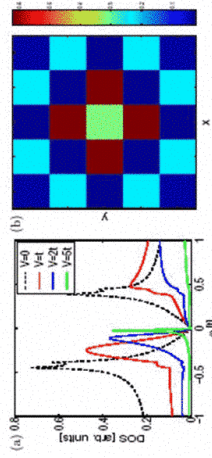
Kondo resonance,  
Polkovnikov *et al*, PRL (2001)

$$\mathcal{H}(\mathbf{r}, \mathbf{r}') = \psi_{\pm}^{\dagger} [V\delta(\mathbf{r})\delta(\mathbf{r}')\tau_3 - \delta\Delta(\mathbf{r}, \mathbf{r}')\tau_1] \psi_{\mathbf{r}}$$

$$G(\mathbf{r}, \mathbf{r}') = G^0(\mathbf{r} - \mathbf{r}') + \sum_{\mathbf{k}} G(\mathbf{r}, \mathbf{r}')H(\mathbf{r}'', \mathbf{r}''')G^0(\mathbf{r}'' - \mathbf{r}')$$

$$G(\mathbf{r}, \mathbf{r}') = G^0(\mathbf{r} - \mathbf{r}') + \sum_{\mathbf{k}} G^0(\mathbf{r} - \mathbf{r}'')T(\mathbf{r}'', \mathbf{r}''')G^0(\mathbf{r}''' - \mathbf{r}')$$

$$G^0(\mathbf{r}, i\omega_n) = \sum_{\mathbf{k}} \frac{(i\omega_n\tau_0 + \xi_{\mathbf{k}}\tau_3 + \Delta_{\mathbf{k}}\tau_1)}{(i\omega_n)^2 - E_{\mathbf{k}}^2} \exp(i\mathbf{k} \cdot \mathbf{r})$$

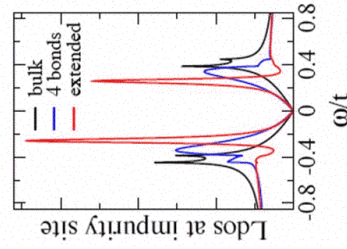


Balatsky *et al*, submitted RMP (2005)

Filter functions,  
I. Martin *et al* (2002)

# Zn resonance in STM

Andreev resonance ??

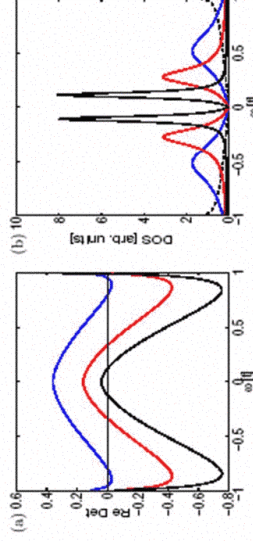


Particle-hole symmetric case

$$D(\omega) = 1 - \alpha L(\omega) (2 - \alpha L(\omega) + \alpha\omega P(\omega))$$

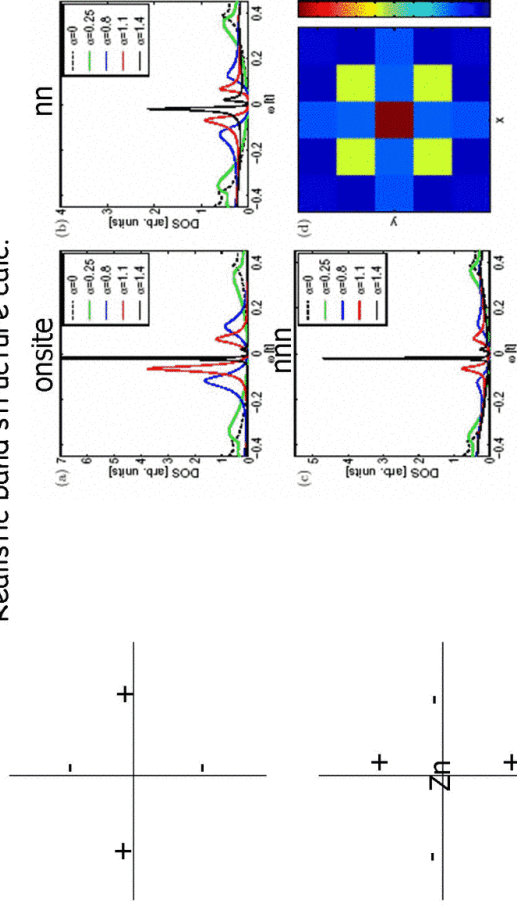
Shirman *et al*,  
PRB (1999)

$$P(\omega), L(\omega) = - \sum_{\mathbf{k}} \frac{(\omega, \Delta_{\mathbf{k}})}{\omega^2 - \xi_{\mathbf{k}}^2 - \Delta_{\mathbf{k}}^2}$$



# Zn resonance in STM

Realistic band structure calc.



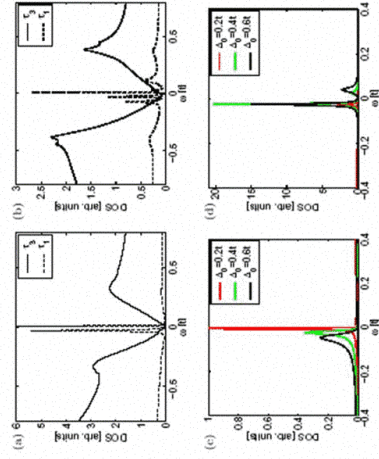
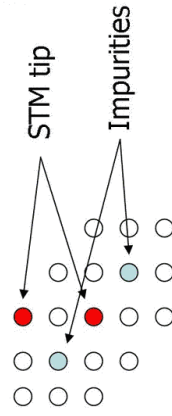
# Zn resonance in STM

How do we distinguish ?

Impurity interference:

- Morr *et al*/PRB (2002)
- Andersen PRB (2003)
- Zhu *et al*/PRB (2003)

Various gap regions



## Conclusions

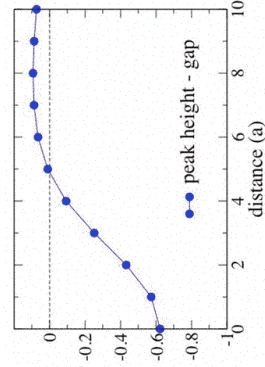
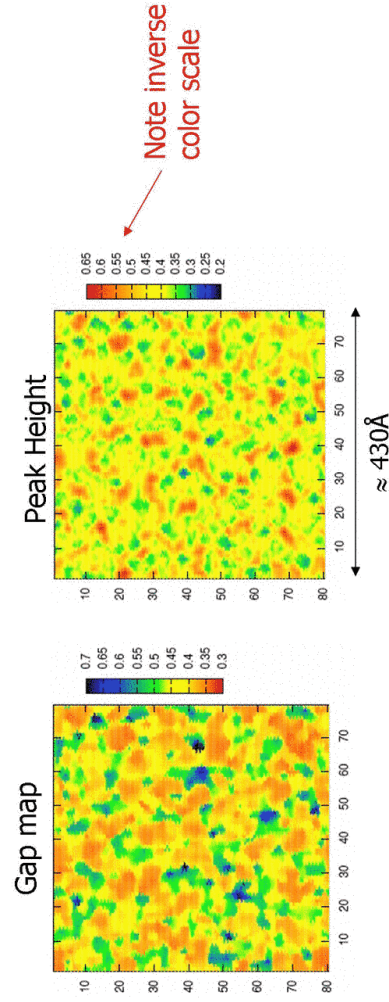
Off-diagonal scattering reproduce the following STM characteristics:

- Gap variations by a factor of two over a few lattice spacings
- Positive correlation between dopant positions and gap magnitude
- Anticorrelation between "coherence" peak height and gap magnitude
- Homogeneous low-energy Ldos
- Relatively particle-hole symmetric Ldos
- Small charge modulations
- Details of the <Oxygen LDOS> correlations

Is the ZBCP near Zn an Andreev state:

- phase impurities have ZBCP and real-space pattern agreeing with STM
- what stabilize phase impurities ?

## Peak Height ↔ Gap Magnitude



$$\text{Correlation function: } C_{fg}(j) = \frac{1}{N} \sum_i \frac{\langle \delta f(i) \delta g(i+j) \rangle}{\sqrt{\langle \delta f \rangle \langle \delta g \rangle}}$$

Anticorrelation: peak height ↔ gap