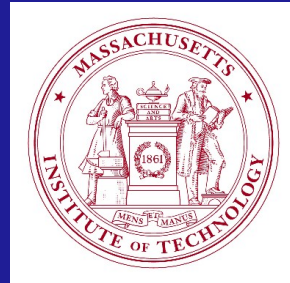


*Terrestrial Planet Formation:
A Blueprint for the Formation of Close-in Super-
Earths and Mini-Neptunes?*



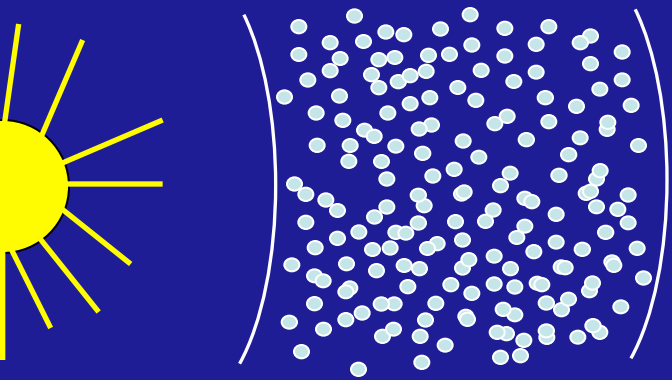
Hilke E. Schlichting

MIT

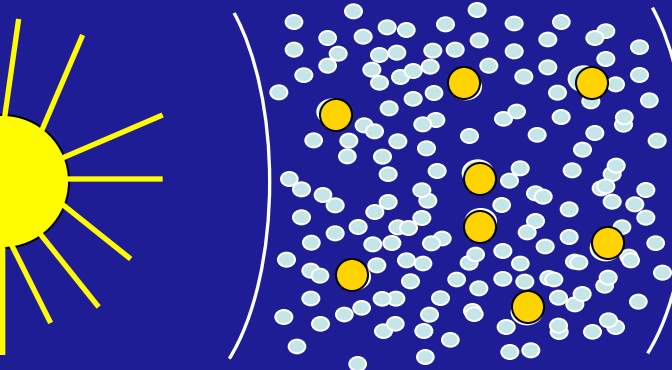
*Physics of Exoplanets: From Earth-sized to Mini-
Neptunes*

KITP

Feb 27th 2015



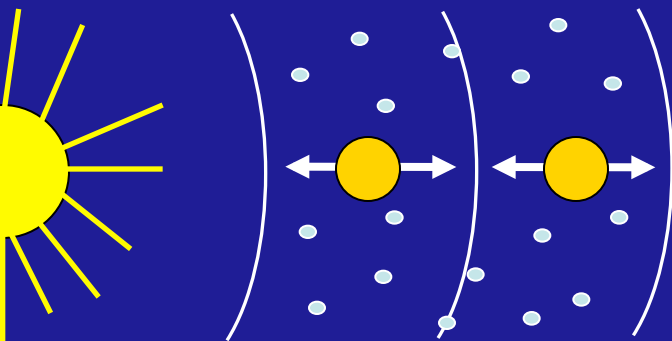
1. Planetesimal formation:



2. Runaway growth:

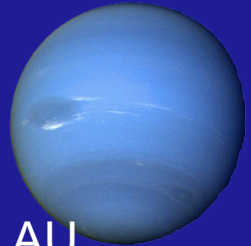
For $v_{\text{esc}} > u$ gravitational focusing enhances the accretion rate

$$\frac{1}{R} \frac{dR}{dt} \sim \frac{\sigma \Omega}{\rho R} \left(\frac{v_{\text{esc}}}{u} \right)^2 \longrightarrow t_{\text{grow}} \sim 10^7 \text{ years}$$

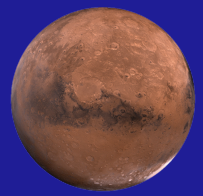


3. Oligarchic growth & Isolation:

$$M_{\text{iso}} \approx 2\pi a (\Delta a_{\text{zone}}) \Sigma \sim M_{\text{Neptune}} \quad @ \text{ 20-30 AU}$$



$$M_{\text{iso}} \approx 2\pi a (\Delta a_{\text{zone}}) \Sigma \sim M_{\text{Mars}} \quad @ \text{ 1.5 AU}$$

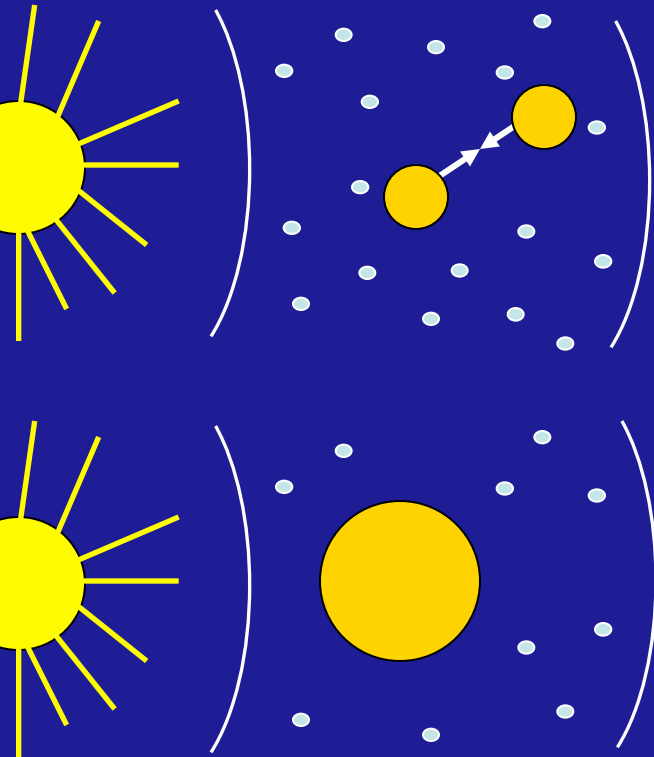


planetesimals protoplanets

u, σ

v, Σ

Last Stages of Terrestrial Planet Formation



Giant Impacts:

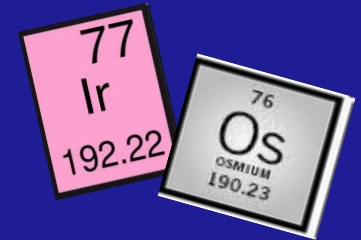
Protoplanets' velocity dispersion increases

→ Giant Impacts

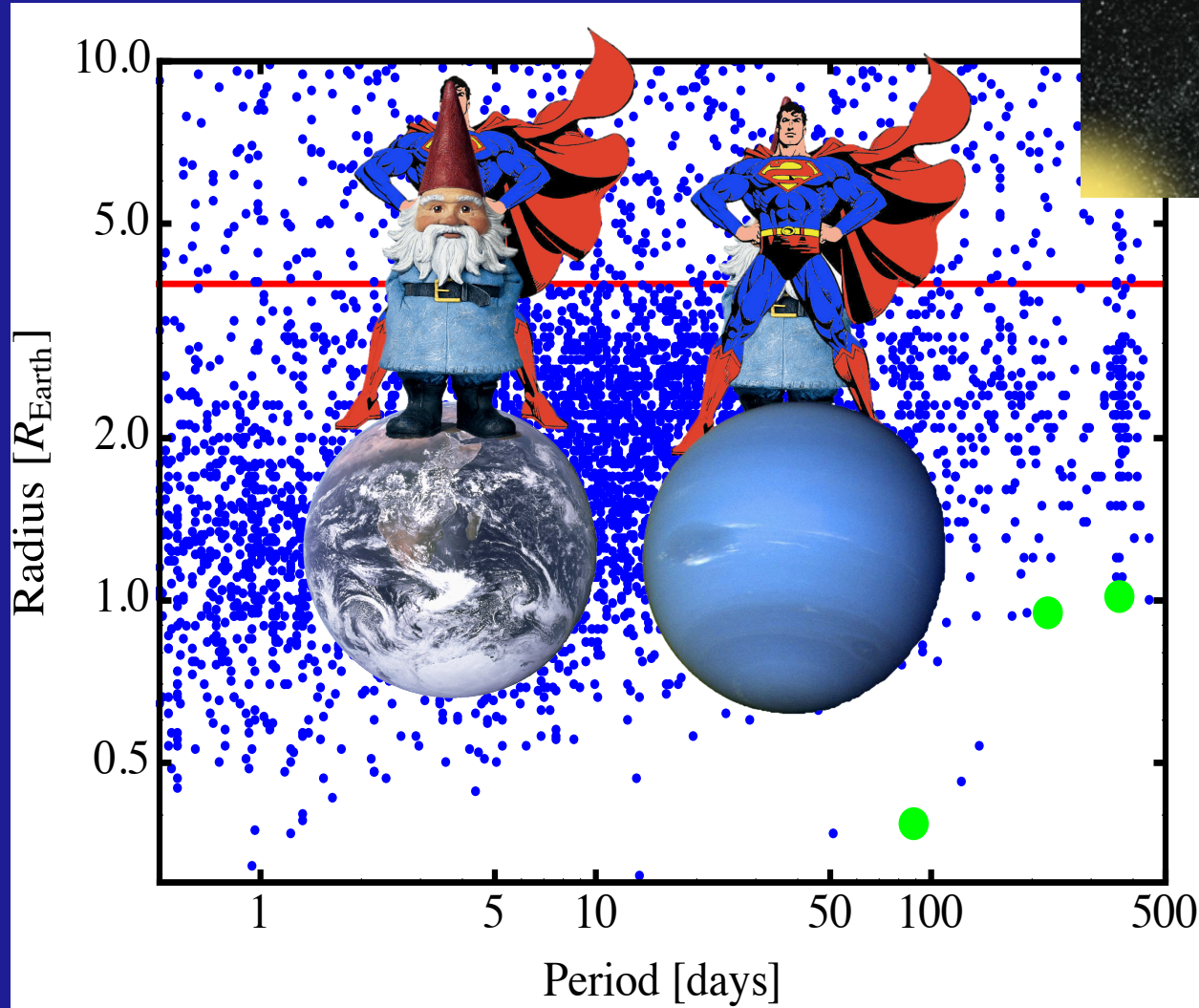
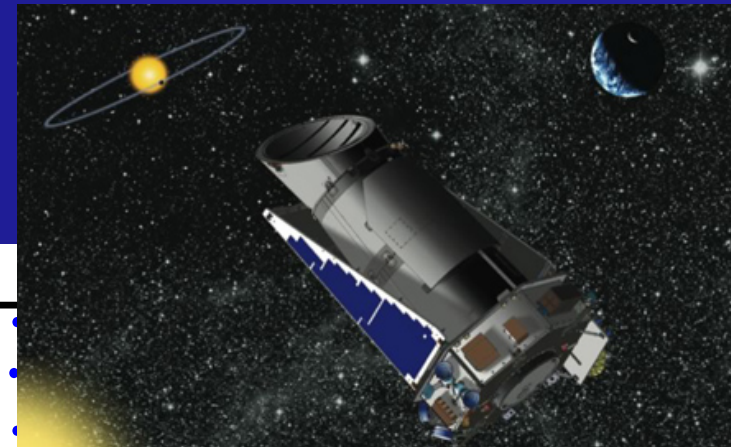
$$t_{\text{Giant-Impacts}} \sim 10^8 \text{ years (1AU)}$$

Clean up:

- Orbits planar & circular (e.g. Schlichting et al. 2012)
- Accretion & ejection of remaining planetesimals



Kepler Planets



4175 Planetary
Candidates

1218 Planets in
Multi-Planet Systems

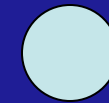
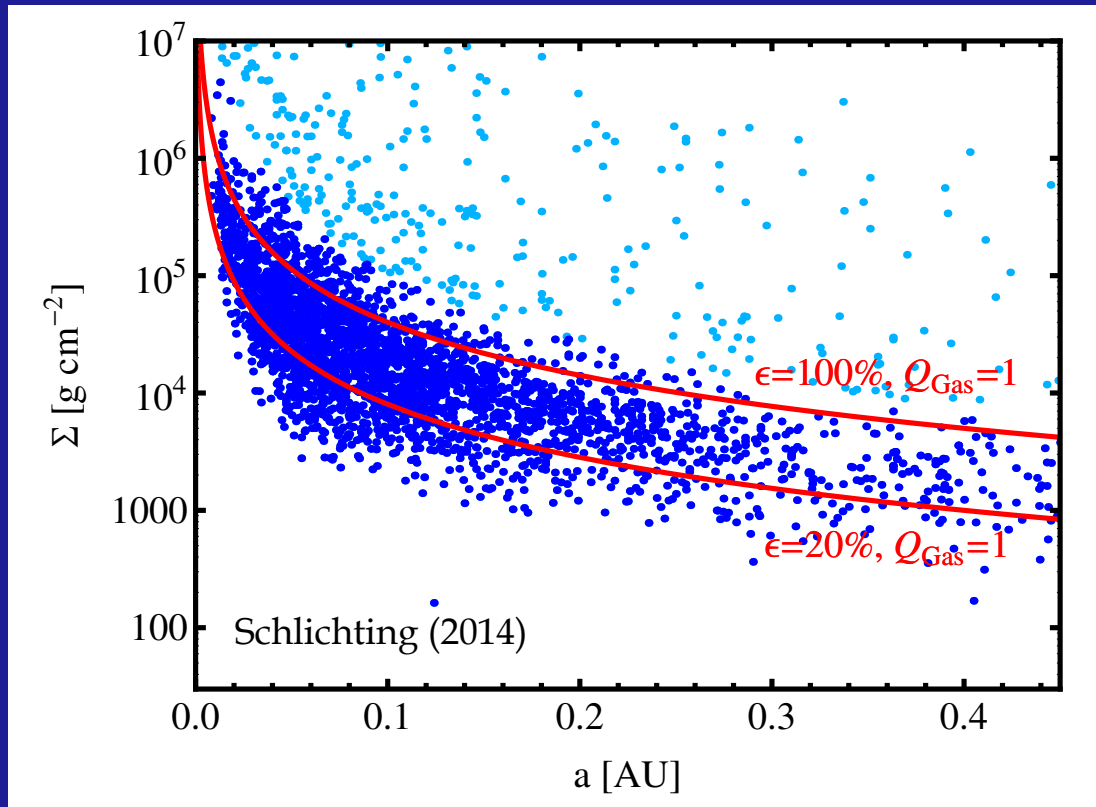
All planetary candidates discovered by Kepler as of Dec. 5th 2014.

Part I

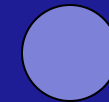
Materials & Supplies



Forming Close-In Planets as Isolation masses



$R > 5 R_{\text{Earth}}$



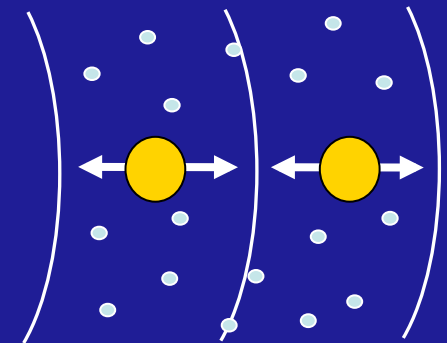
$R < 5 R_{\text{Earth}}$

$$Q_{\text{Gas}} \equiv \frac{c_s \Omega}{\pi G \Sigma_{\text{gas}}}$$

(Toomre 1964)

$$M_{\text{iso}} \approx 2\pi a (\Delta a_{\text{zone}}) \Sigma \sim M_{\text{Planet}}$$

$$\Delta a \sim 2v_H / \Omega$$

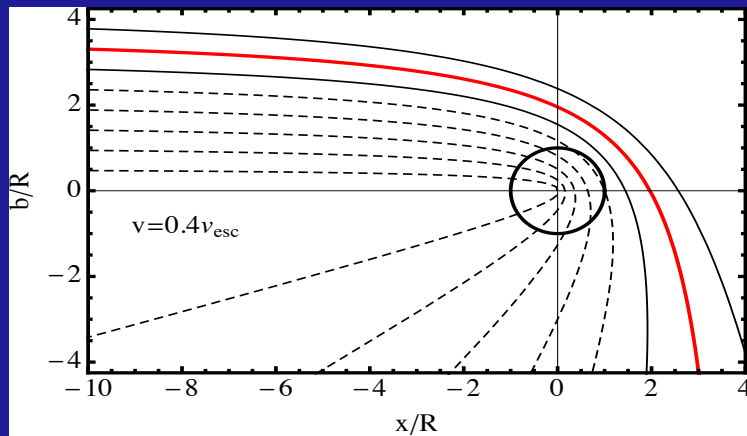


Viscous Stirring

Viscous stirring tends to increase the random kinetic energy all all bodies in the disk

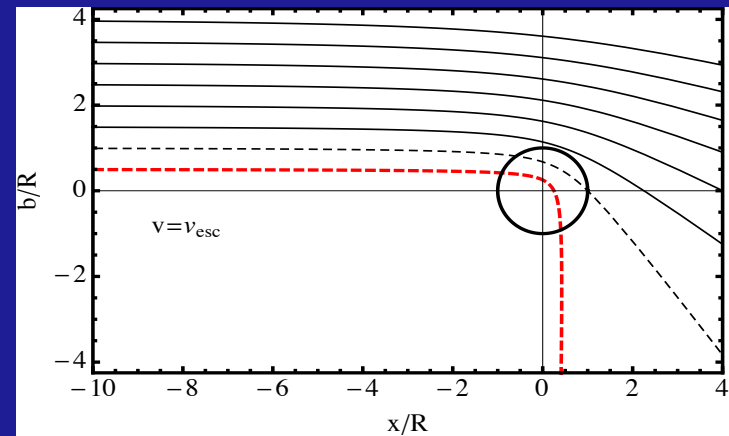
For $v \ll v_{esc}$

$$\sigma_{stirr} \gg \sigma_{coll}$$



For $v \gg v_{esc}$

$$\sigma_{stirr} \ll \sigma_{coll}$$



$$\sigma_{stirr} \sim \pi R^2 \left(\frac{v}{v_{esc}} \right)^{-4}$$

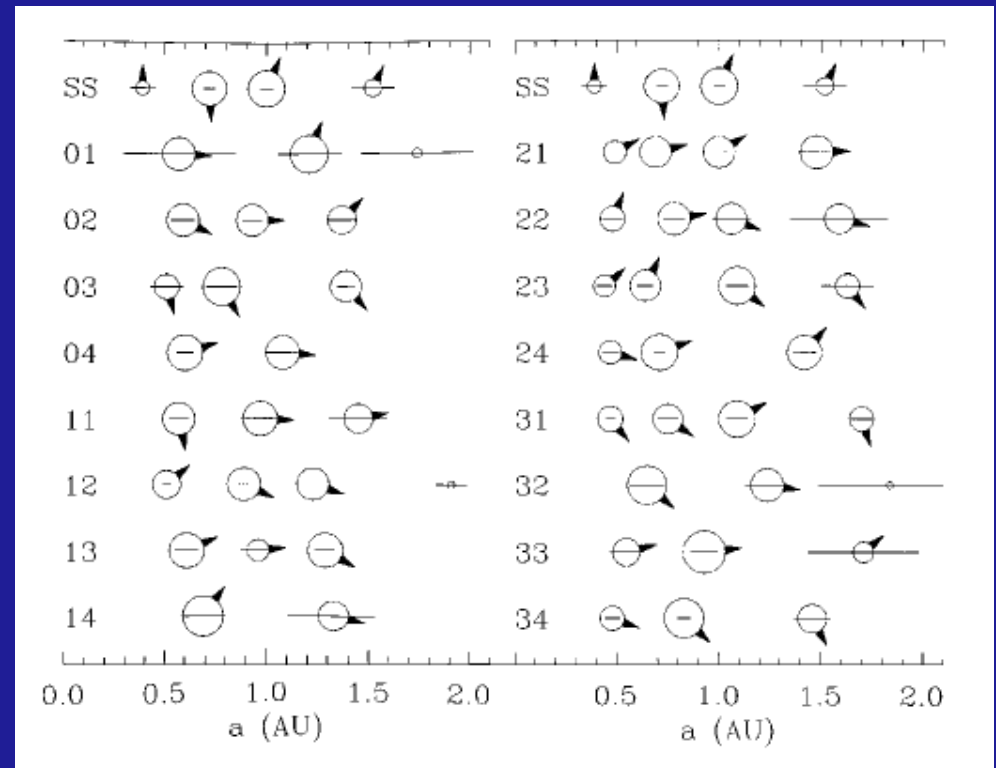
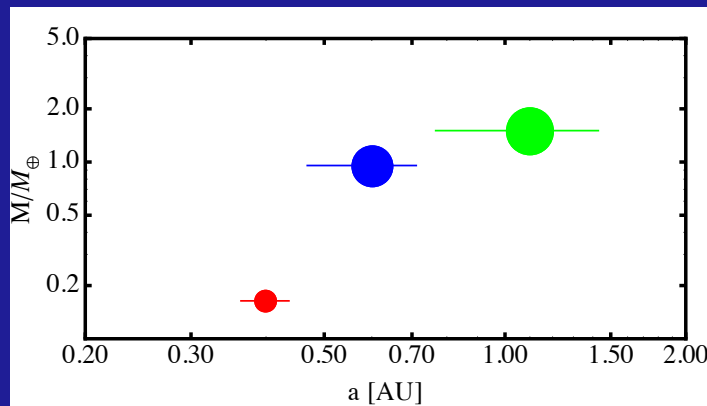
$$\sigma_{coll} \sim \pi R^2 \left(1 + \left(\frac{v}{v_{esc}} \right)^{-2} \right)$$

Example: Terrestrial Planets

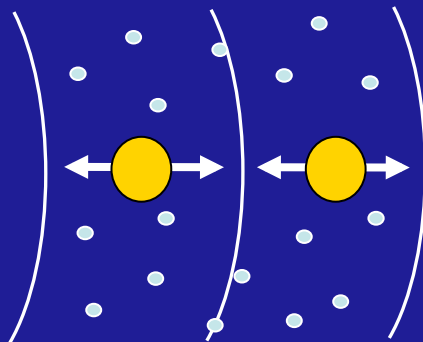
$$M_{GI} \simeq \frac{[2^{5/2} \pi a^2 \Sigma (\rho/\rho_{\odot})^{1/6} (a/R_{\odot})^{1/2}]^{3/2}}{M_{\odot}^{1/2}}$$



Schlichting 2014

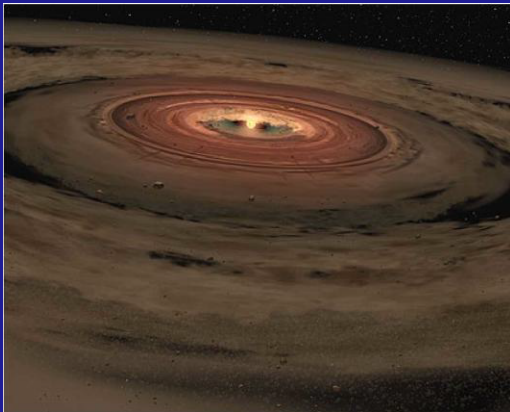
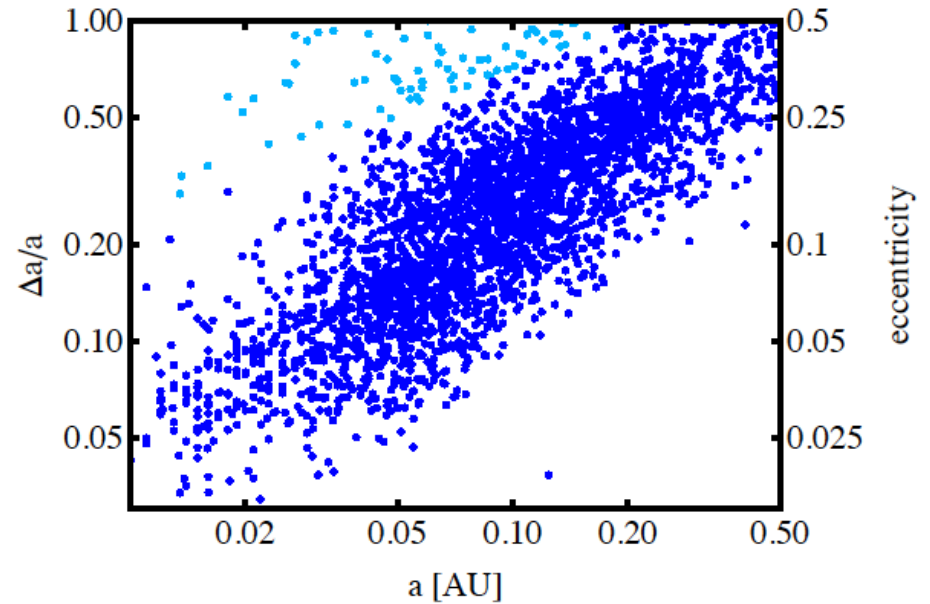
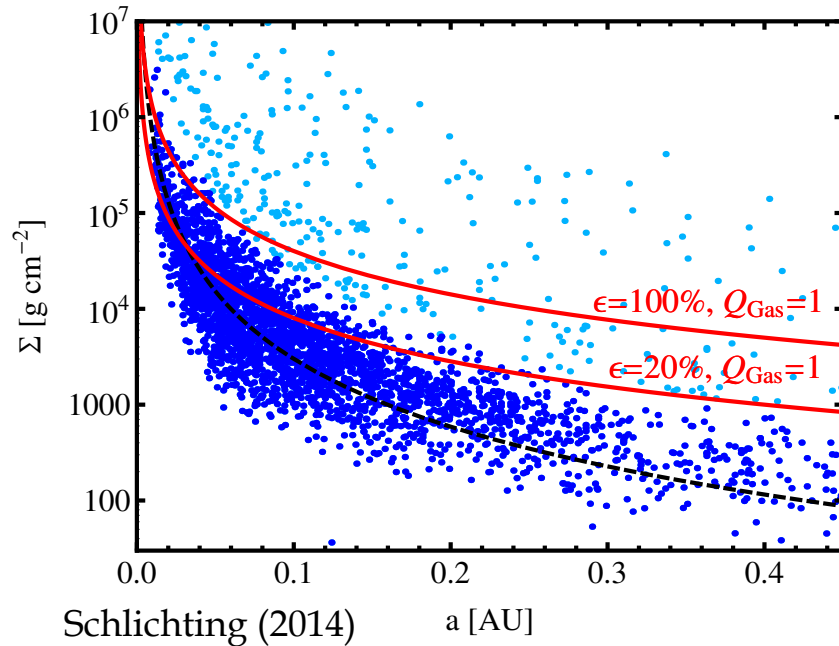


$$\Delta a \sim 2v_{esc} / \Omega$$

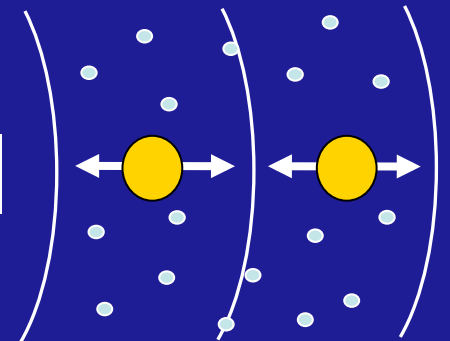


Chambers 2001

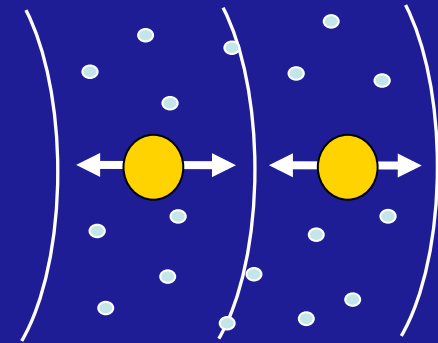
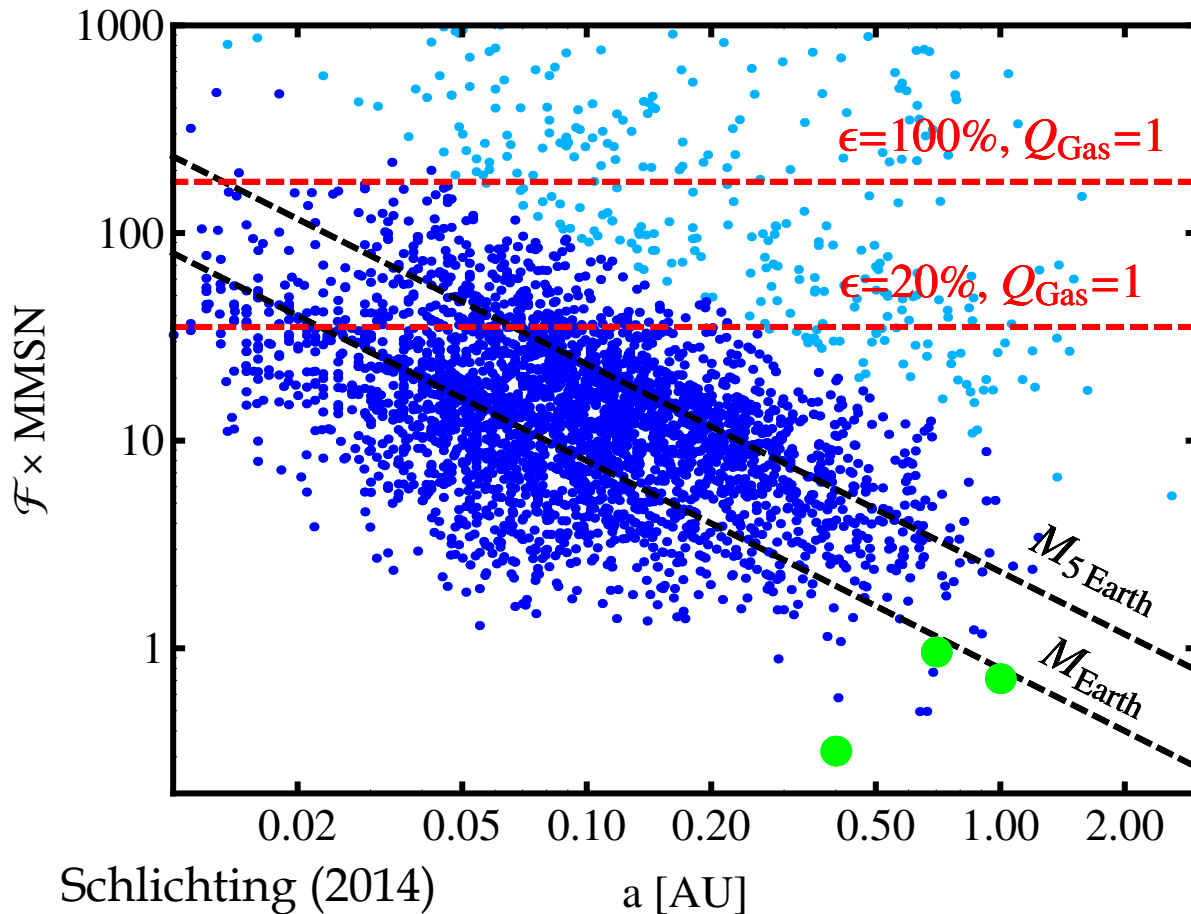
Forming Close-In Planet with Giant Impacts



$$\Delta a \sim 2v_{\text{esc}} / \Omega$$



Minimum Disk Masses Required



MMSN type disks consistent with formation further out and subsequent inward migration and/or radial inward drift of solids and subsequent local assembly.

Take Home Points I

Radial drift and/or migration must have played a key role in the origin of close-in Super-Earths and Mini-Neptunes

- Disk Stability (Schlichting 2014)
- Global Disk Masses
- Disk radial profiles (Raymond et al. 2014)
- Giant planet occurrence (Schlaufman 2014)

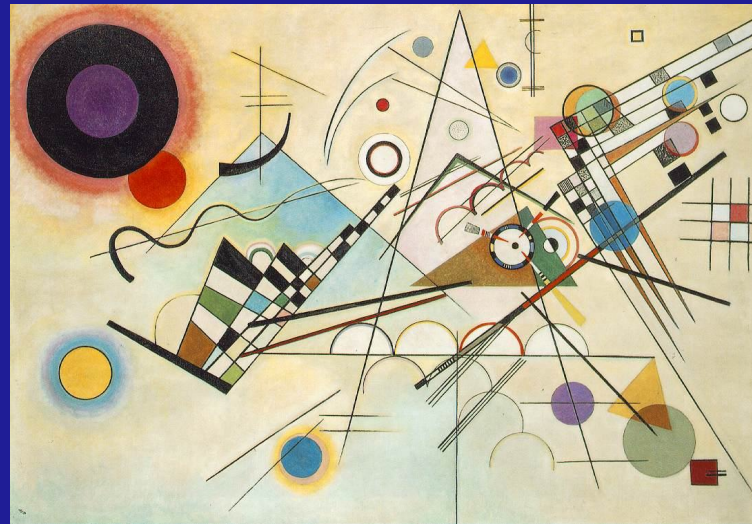
Formation of close in planets with Giant Impacts is a possibility, need massive inner disks, typically few tens MMSN (Raymond 2008, Hansen & Murray 2012).

MMSN type disks consistent with formation further out and subsequent inward migration and/or radial inward drift of solids and subsequent local assembly.

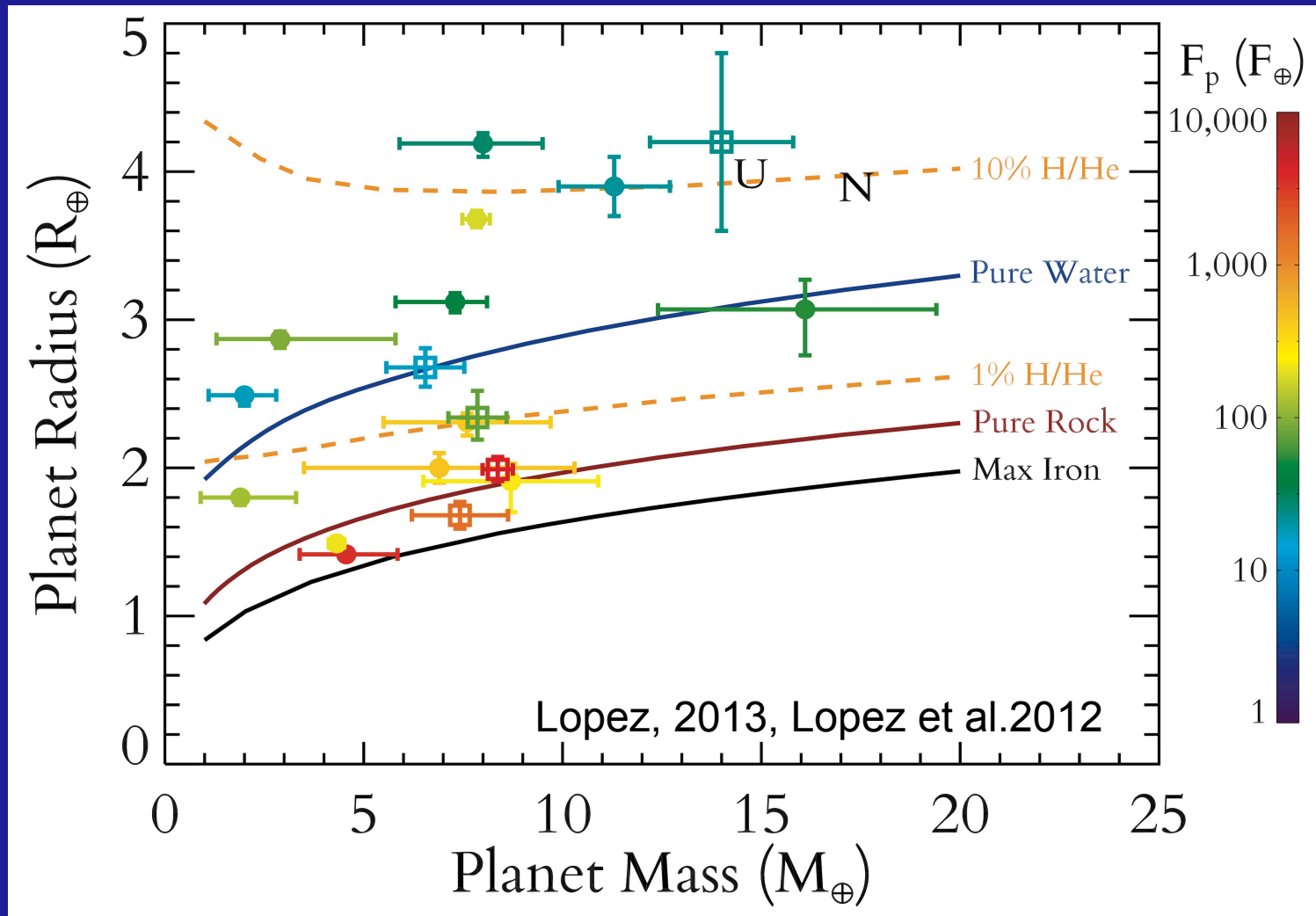
Need to examine planet formation with radial drift and/or migration
Growth times maybe determined by rate of material delivery into the inner disk

Part II

Composition & Structure



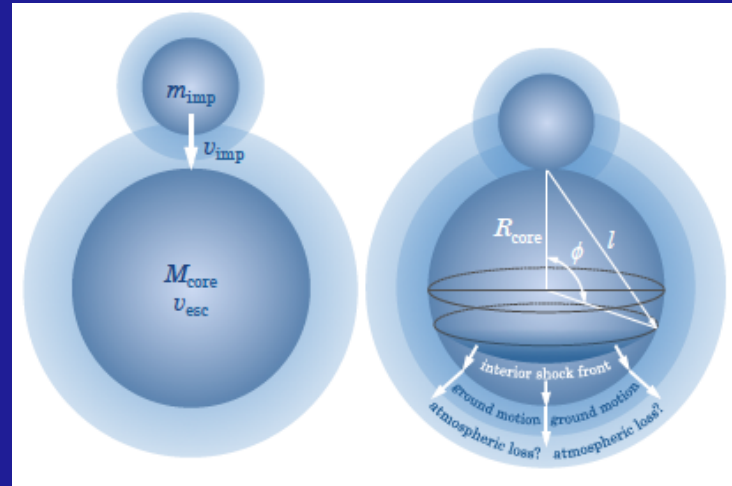
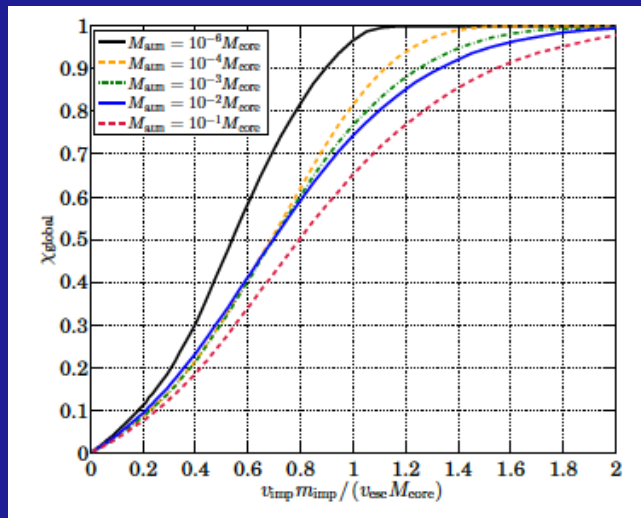
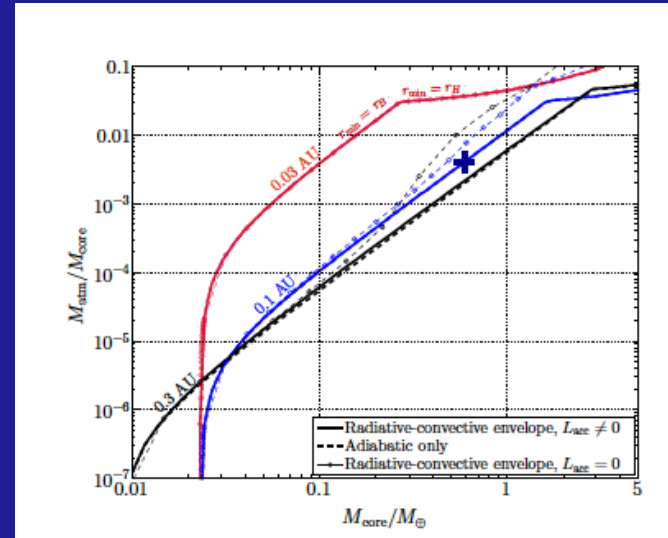
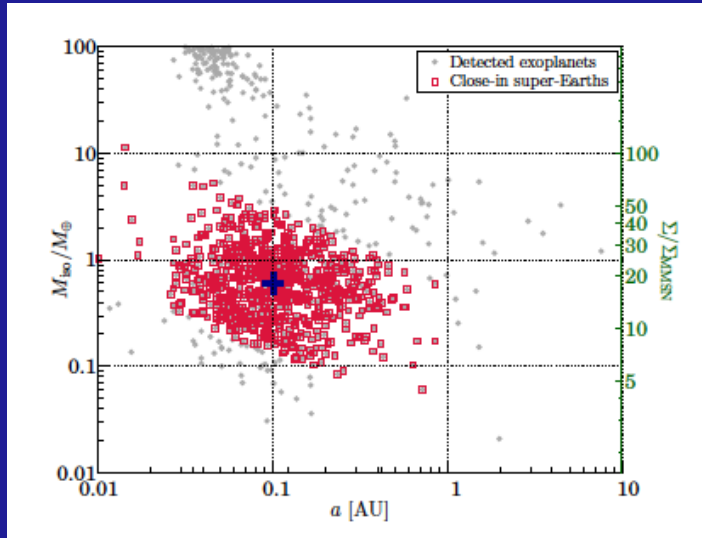
Exoplanet Atmospheres



Lopez, 2013, Lopez et al.2012

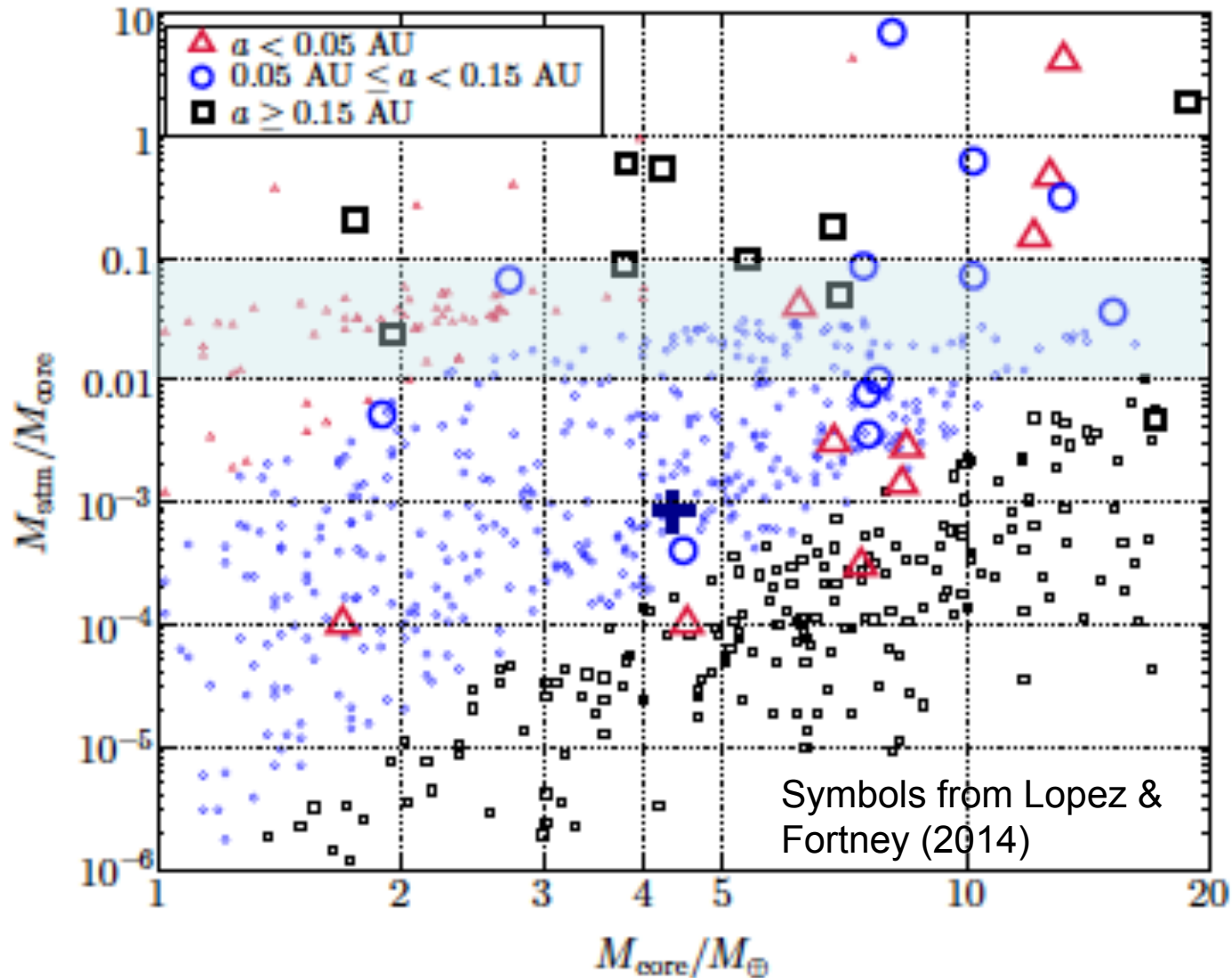
For comparison, the Earth's atmosphere contains less than 10^{-6} of its mass and has an atmospheric scale height that is only $\sim 0.1\%$ of its radius.

Formation of Close-In planets with Giant Impacts



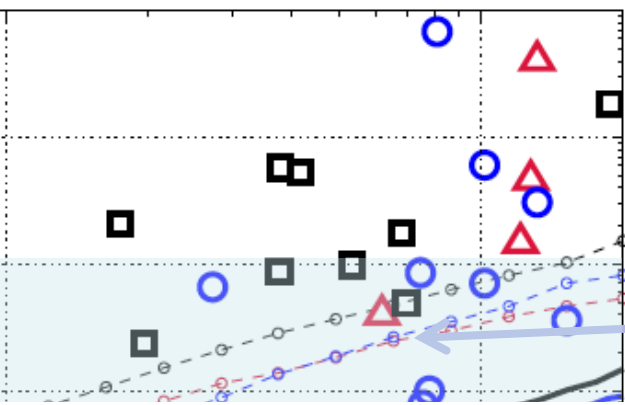
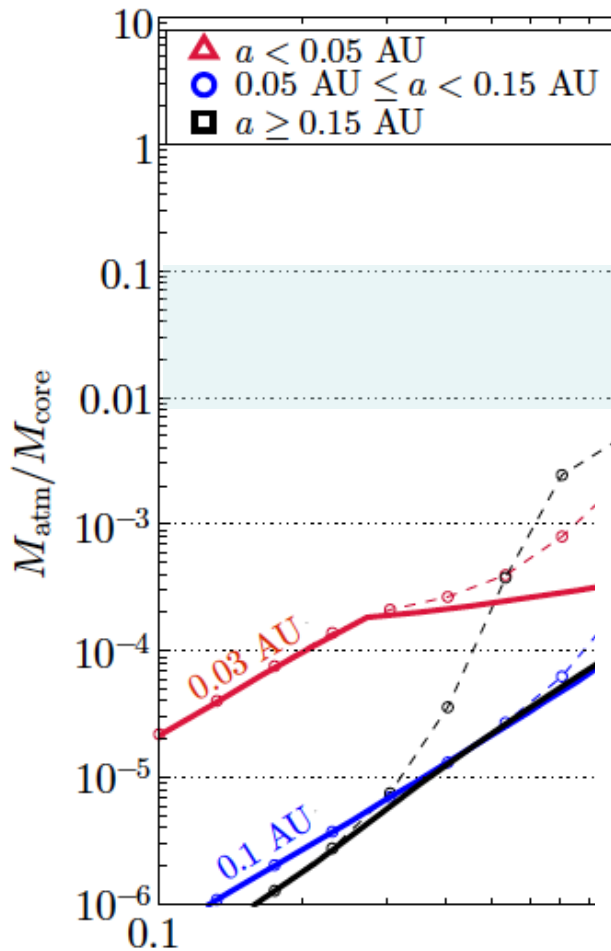
(Inamdar & Schlichting, 2015)

Formation of Close-In planets with Giant Impacts



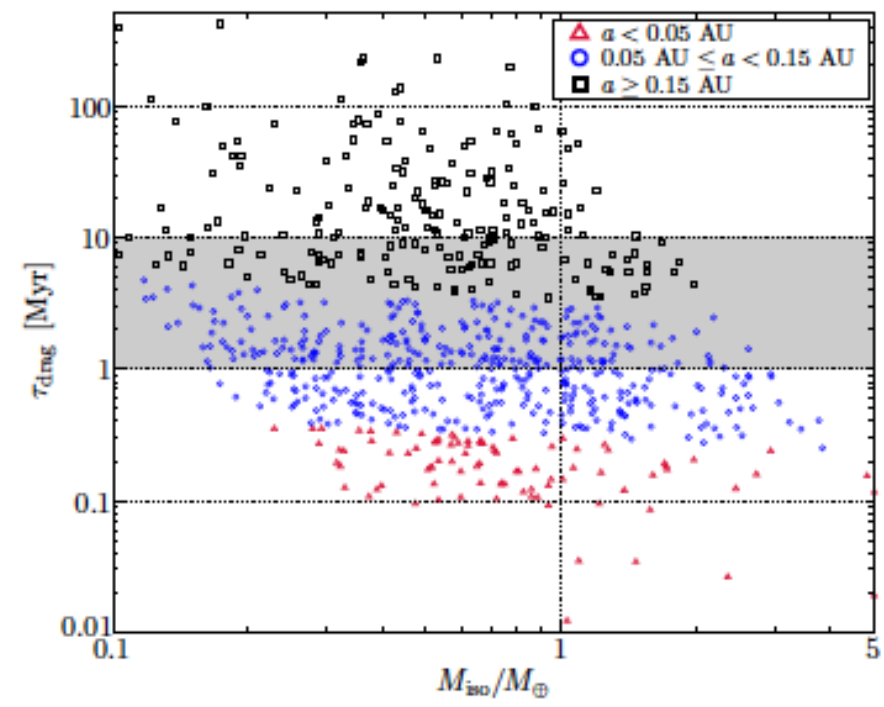
(Inamdar & Schlichting, 2015)

Envelope Accretion After Giant Impacts



Symbols from Lopez & Fortney (2014)

$L_{\text{acc}}=0$
 (Lee, Chiang & 2014)



(Inamdar & Schlichting, 2015)

Take Home Points II

Atmospheric masses of Isolation masses are small (10^{-3}) and atmospheric mass loss due to Giant Impacts significant leading to typical atmospheric masses of $\sim 0.1\%$



Formation of 'mostly' rocky planets no problem

Atmospheric Accretion from partially depleted gas disk after Giant Impacts can explain atmospheres of up to a few % and less if:

- 1) $L_{\text{acc}} \sim 0$
- 2) Have massive inner disks, typically few tens MMSN
- 3) $\Sigma_{\text{gas}} / \Sigma_{\text{dust}} < 10$ to prevent radial drift.

It seems challenging to explain atmospheric masses \gg several % with accretion from partially depleted gas disk after Giant Impacts.