

Towards First Principles Theories of **Strongly Correlated Materials** :What is Currently Possible and What Needs to be Done to Make it Happen ?



Please Give me Suggestions!!

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K. Haule (Rutgers) S. Savrasov (U.C Davis)

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From Basic Concepts to Real Materials

Towards Material Design Using Strongly Correlated Electron Systems

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Constrained dft

P.Dederichs, S. Blugel, R. Zeller and H. Akai, Phys. Rev. Lett. **53**, 2512 (1984)

Constrained RPA

Aryasetiawan Imada, A Georges, G Kotliar, S Biermann, A Lichtenstein, PRB 70, 195104 (2004)

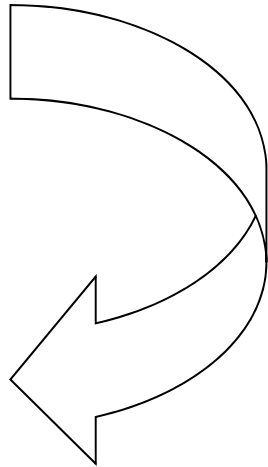
Historical Perspective Two roads to the electronic structure of strongly correlated materials, which one to chose ?

- a) direct vs indirect
- b) ab initio vs semi-empirical
- c) energy vs spectra

Crystal structure + Atomic positions

Model Hamiltonian

Correlation Functions Total Energies etc.



e.g.
DFT
HF

QMC
PT
DMFT
Etc.

e.g. Early work: M. M. Steiner, R. C. Albers, and L. J. Sham. Phys. Rev. B, 45:13272, 1992.
Hybersten et. al. Phys. Rev. B 39, 9028 - 9041 (1989)

DMFT for model Hamiltonians Hubbard model

$$\sum_{\langle i,j \rangle, \sigma} (t_{ij} - \mu \delta_{ij}) (c_{i\sigma}^\dagger c_{j\sigma} + c_{j\sigma}^\dagger c_{i\sigma}) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

Baym Kadanoff Functional, sum over two particle irreducible graphs.

$$\Gamma[G_{ii}, M] = -\text{Tr} \text{Ln}[i\omega + \mu - t_{ij} - M] - \text{Tr}[MG] + \Phi[G]$$

$$\Phi_{dmft}[G] \sim \Phi[G_{ii}, G_{ij \neq 0}] = \sum_i \Phi_{atom}[G_{ii}]$$

Paradigm Shift: partial selection of graphs \rightarrow sum ALL LOCAL graphs

Summation is done by considering an atom in a bath [Quantum Impurity Model]

$$G_{ii} = \sum_k \frac{1}{[i\omega + \mu - t(k) - M_{ii}]} \quad M_{ii} = \frac{\delta}{\delta G_{ii}} \Phi_{atom}[G_{ii}]$$

Review : A.Georges, G. Kotliar., W. Krauth and M. J. Rozenberg, R. M.P. 68, 13 (1996).
 Longer Ranges: Cluster Dynamical Mean Field Theories.

LDA+DMFT

V. Anisimov, A. Poteryaev, M. Korotin, A. Anokhin
and G. Kotliar, J. Phys. Cond. Mat. 35, 7359 (1997)

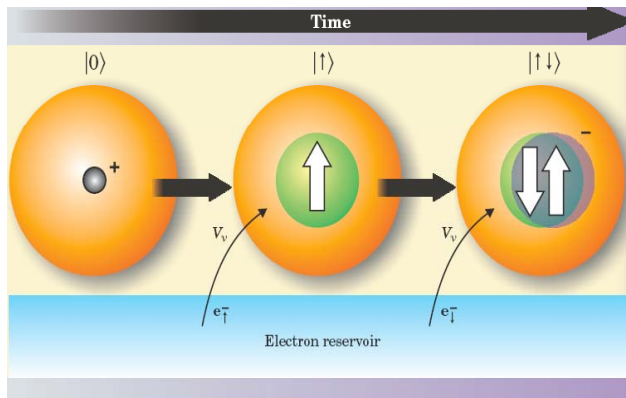
- The light, SP (or SPD) electrons are extended, well described by LDA. The heavy, D (or F) electrons are localized treat by DMFT.
- LDA Kohn Sham Hamiltonian already contains an average interaction of the heavy electrons, subtract this out by shifting the heavy level (double counting term)
- ❑ The U matrix can be estimated from first principles of viewed as parameters. Solve resulting model using DMFT.
- ❑ Brings chemistry [Local configuration interaction in a bath] — and Band Physics [Electrons in a frequency dependent potential] together.

See also LDA++. A Lichtenstein and M. Katsnelson PRB 57, 6884 (1988).

LDA+DMFT. V. Anisimov, A. Poteryaev, M. Korotin, A. Anokhin and G. Kotliar, *J. Phys. Cond. Mat.* 35, 7359 (1997).

$$U \longrightarrow U_{abcd}$$

$$\Sigma \longrightarrow \begin{pmatrix} 0 & 0 \\ 0 & \Sigma_{ff} \end{pmatrix}$$



$$t(k) \longrightarrow \begin{pmatrix} H[k]_{spd,sps} & H[k]_{spd,f} \\ H[k]_{f,spd} & H[k]_{ff} - E_{dc} \end{pmatrix}$$

$$|0\rangle, |\uparrow\rangle, |\downarrow\rangle, |\uparrow\downarrow\rangle \longrightarrow |LSJM_J\gamma\dots\rangle$$

Pros

- Freed Model Hamiltonian treatments from many parameters.
- Brought DMFT to the attention of the electronic structure community.
- Serious improvement over LDA+U
- Triggered numerous collaborations between electronic structure groups and many body theorists
- Implementation for Spectra of LaSrTiO₃ including Ti and ligands

Remaining Issues

- $H[k]$ is not affected by correlations. No feedback on the density.
- Parameters (i.e. U)
- How to compute total Energies ?
- Better Impurity Solvers (IPT)
- More accurate basis sets $H[k]$ LMTO-ASA
 - Foundation for the method.

Conceptual Underpinning : Chitra and Kotliar Phys. Rev. B 62, 12715 (2000)

and Phys. Rev.B (2001).

$$S = \int dx \psi^\dagger(x) [\partial_\tau - \nabla^2 + V_{ext}(x)] \psi(x) + \frac{1}{2} \int dx dx' \psi^\dagger(x) \psi^\dagger(x') v_C(x-x') \psi(x) \psi(x')$$

$$S = \int dx \psi^\dagger(x) [\partial_\tau - \nabla^2 + V_{ext}(x)] \psi(x) + \frac{1}{2} \int \int \phi(x) V_C^{-1}(x, x') \phi(x') + \int i \phi(x) \psi^\dagger(x) \psi(x)$$

$$G = - \langle \psi(x') \psi^\dagger(x) \rangle \quad \langle \phi(x') \phi(x) \rangle - \langle \phi(x') \rangle \langle \phi(x) \rangle = W$$

$$\Gamma[G, W, M, P] = -TrLn[G_0^{-1} - M] - Tr[MG] + \frac{1}{2} TrLn[V_C^{-1} - P] - \frac{1}{2} Tr[P]W + E_{hartree} + \Phi[G, W]$$

C.O.Almbladh, U.von Barth and R.vanLeeuwen Int.J.Mod.Phys. B13, 535 (1999)

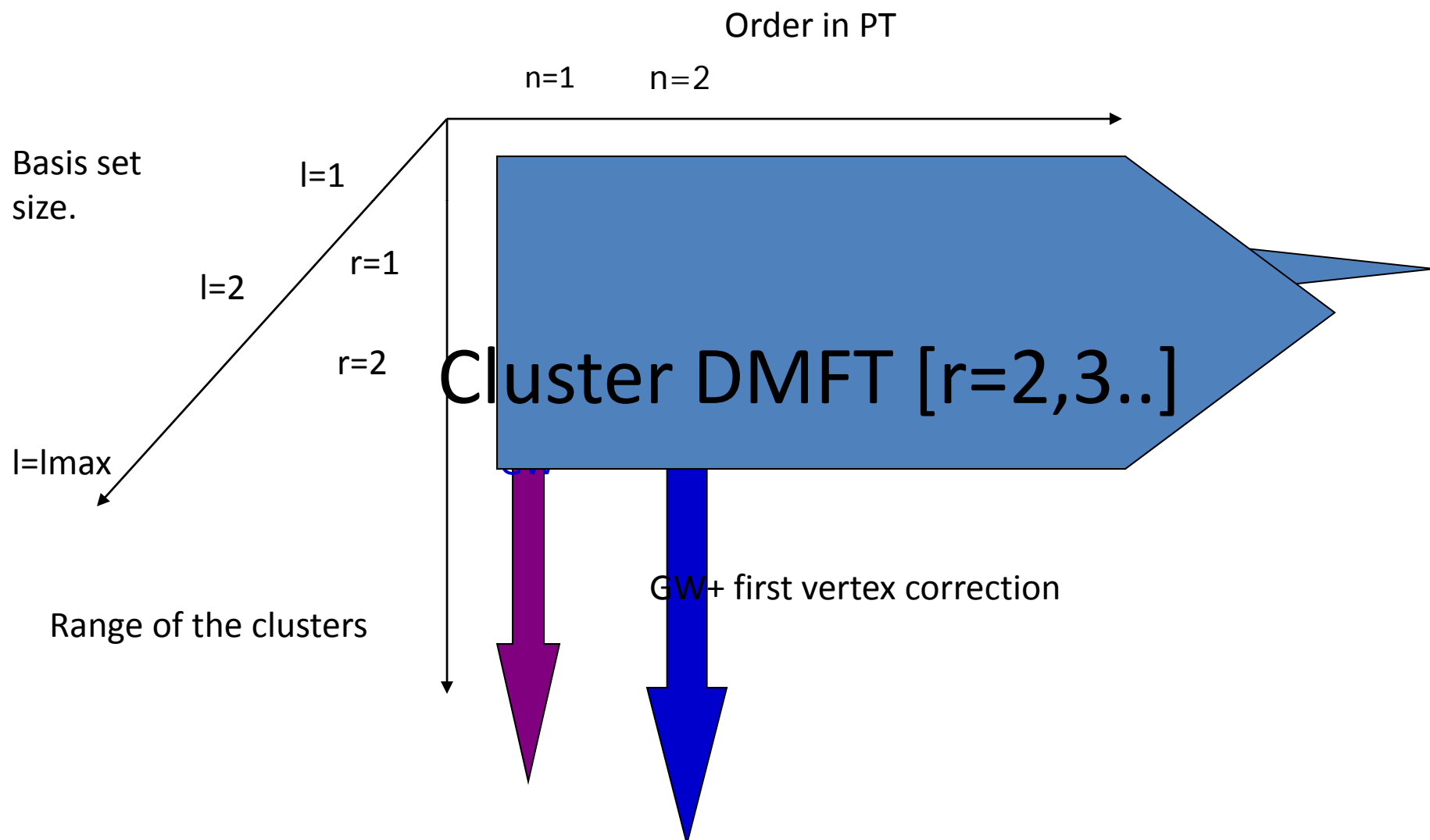
Introduce Notion of Local Greens functions, Wloc, Gloc $G = Gloc + Gnonloc$

$$Ex. \quad |r\rangle = |R, \rho\rangle \quad Gloc = G(R, \rho, R, \rho') \delta_{R, R'}$$

$$\Phi[G, W] \approx \Phi_{EDMFT}[G_{loc}, W_{loc}, G_{nonloc} = 0, W_{nonloc} = 0] \quad \Phi \quad \text{Sum of 2PI graphs}$$

One can also view as an approximation to an exact Spectral Density Functional of Gloc and Wloc . One can do further PT in Gloc Gnonloc by keeping perturbative theory in them. Φ

Space of all dressed diagrams for Sigma and Pi



Proof of Principle Implementation

Full implementation in the context of a **one orbital lattice model**.

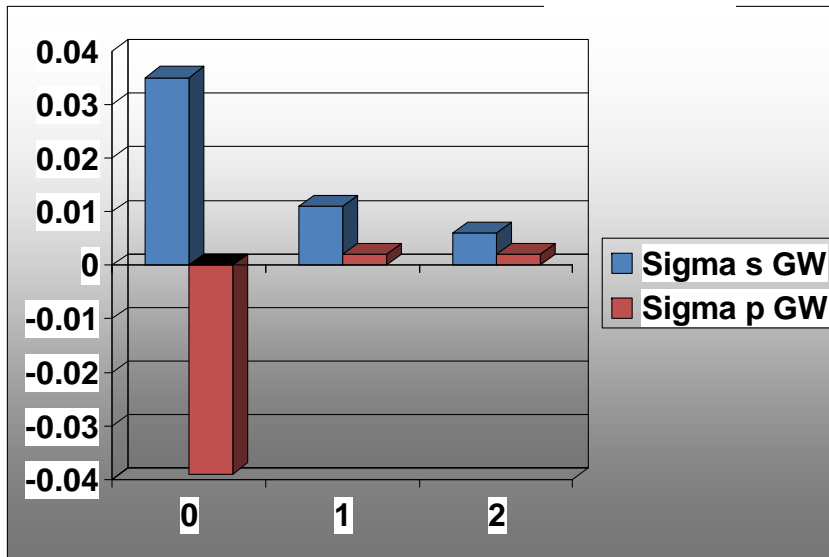
P Sun and G. Kotliar Phys. Rev. B 66, 85120 (2002). DMFT+non local GW corrections

P.Sun and GK PRL (2004): Test various levels of self consistency in Gnonloc Pinonloc

Test notion of locality (in LMTO basis) set in various materials.

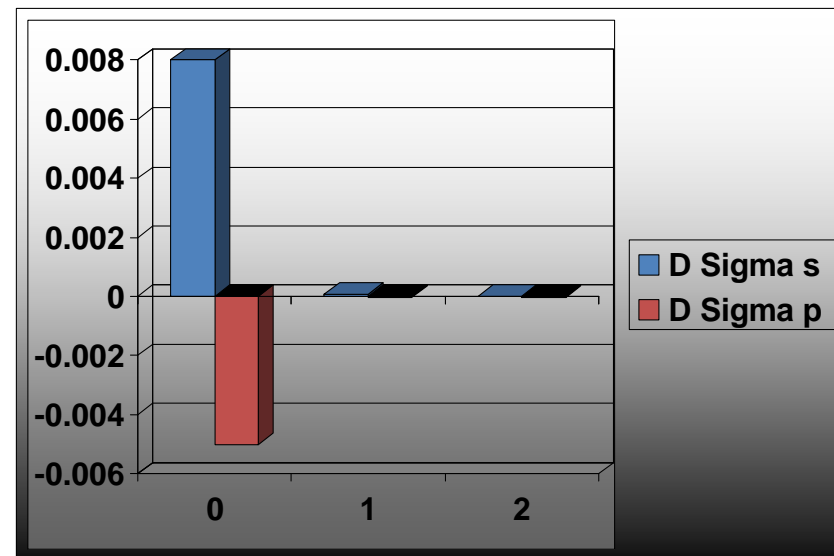
N. Zeyn S. Savrasov and G. Kotliar PRL 96, 226403, (2006)

GW self energy for Si



Coordination Sphere

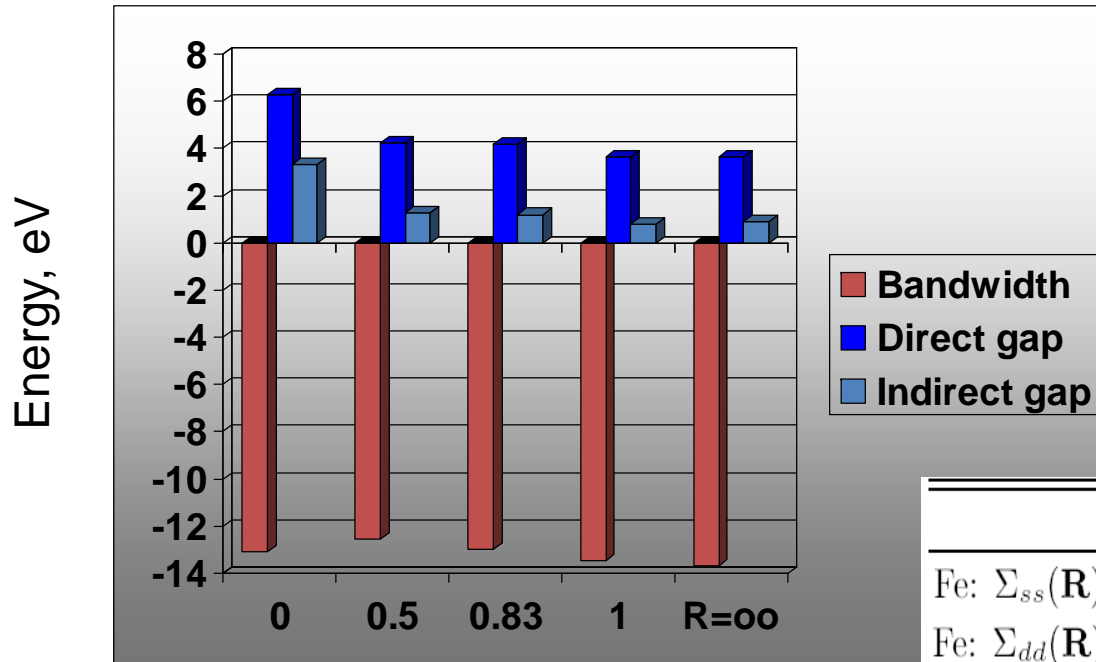
Beyond GW



Coordination Sphere

Zeyn and Antropov (local GW) Phys. Rev. Lett. **89**, 126402 (2002)

N Zeyn S. Savrasov and G. K PRL 96, 226403 (2006)



Cutoff Radius R

	$R = 0$	R_1	R_2	R_3
Fe: $\Sigma_{ss}(\mathbf{R})$	0.70	0.35	0.16	
Fe: $\Sigma_{dd}(\mathbf{R})$	6.53	0.05	0.08	
Ni: $\Sigma_{ss}(\mathbf{R})$	-0.54	0.05	0.03	
Ni: $\Sigma_{dd}(\mathbf{R})$	7.34	0.38	-0.03	
Na: $\Sigma_{ss}(\mathbf{R})$	-1.36	0.52	0.30	0.05
Al: $\Sigma_{pp}(\mathbf{R})$	0.46	0.16	-0.08	
Si: $\Sigma_{ss}(\mathbf{R})$	0.95	0.30	0.14	0.03
Si: $\Sigma_{pp}(\mathbf{R})$	-1.06	0.05	-0.27	-0.03

Practical Route to Total Energies LDA+DMFT functional

$$\Gamma_{LDA+DMFT} [\rho(r), \mathbf{G}_{ab}, V_{KS}(r), \Sigma_{ab}]$$

$$- Tr \log [i\omega_n + \nabla^2 / 2 - V_{KS} - \chi_{\alpha R}^*(r) \Sigma_{\alpha\beta R} \chi_{\beta R}(r)] -$$

$$\int V_{KS}(r) \rho(r) dr - \sum_{i\omega_n} Tr \Sigma(i\omega_n) G(i\omega_n) +$$

$$\int V_{ext}(r) \rho(r) dr + \frac{1}{2} \int \frac{\rho(r) \rho(r')}{|r - r'|} dr dr' + E_{xc}^{LDA}[\rho] +$$

$$\sum_R \Phi[G_{\alpha\beta R}] - \Phi_{DC}$$

Φ Sum of local 2PI graphs with local U matrix and local G

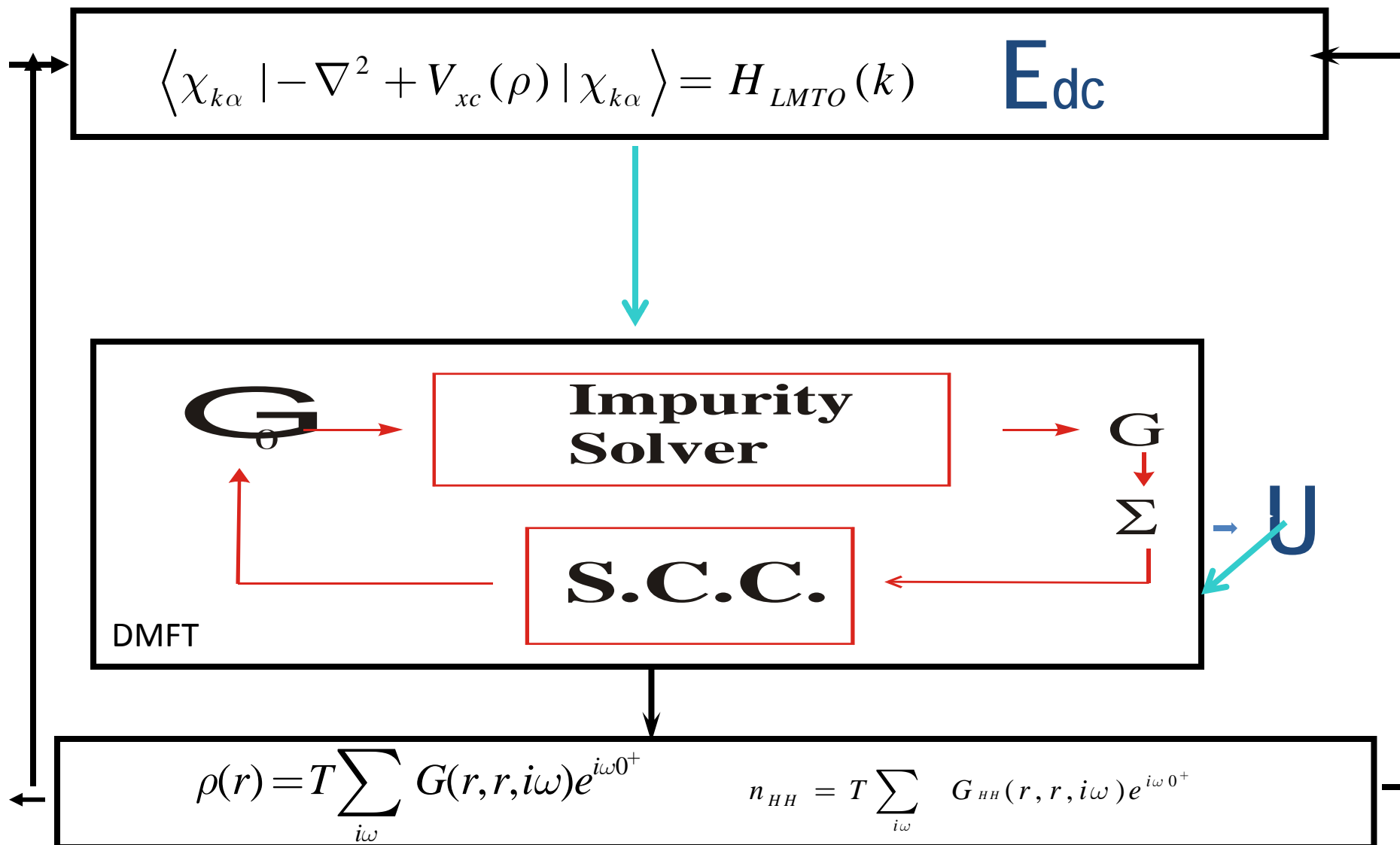
$$\Phi_{DC}[G] = Un(n-1) \frac{1}{2}$$

$$n = T \sum_{i\omega} (G_{aa}(i\omega) e^{i0^+})$$

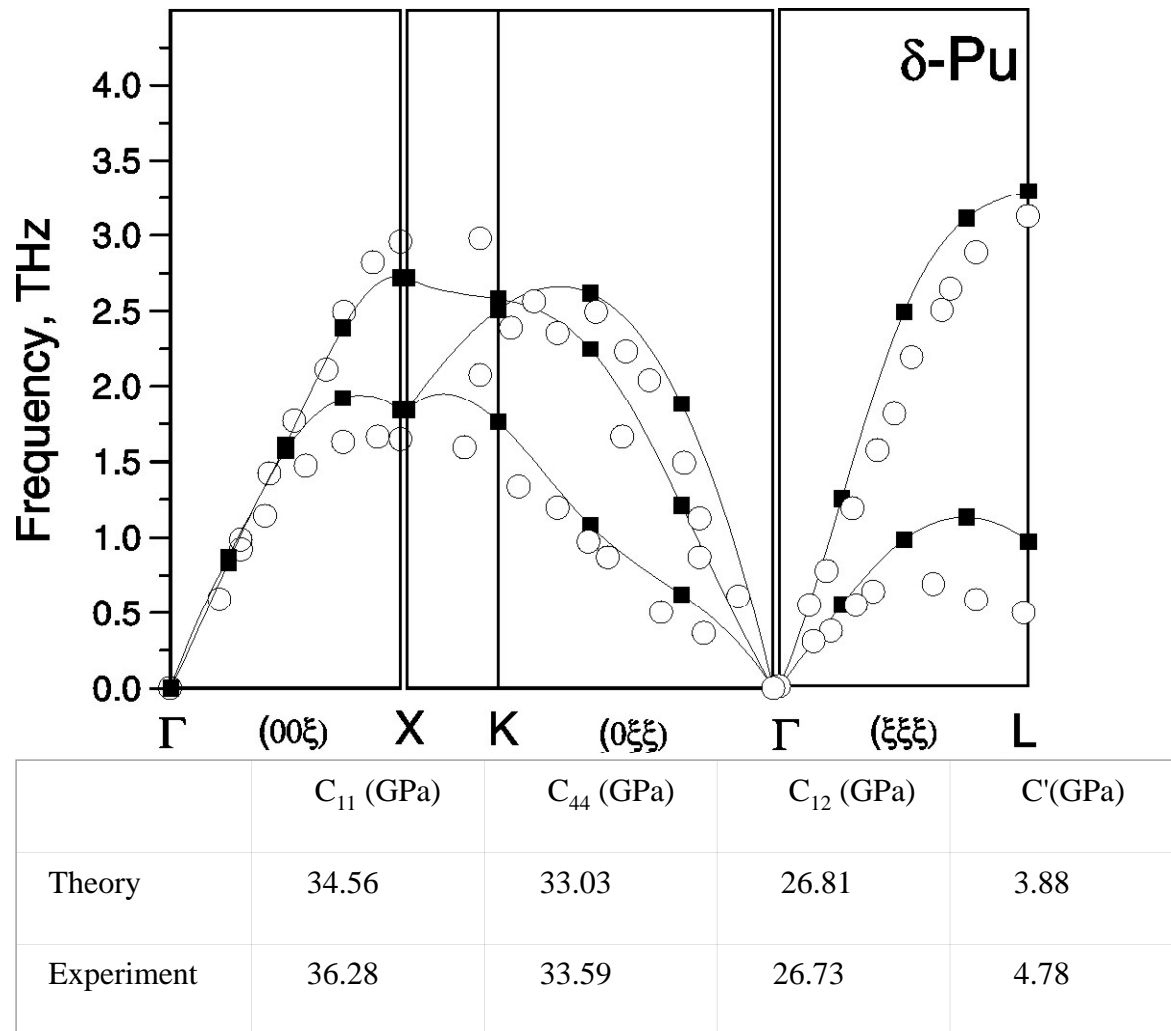
Notice Explicit **Dependence** on : U , DC, and Projectors [Orbitals], and **Independence** of basis set.

R. Chitra and G Kotliar Phys.Rev.B62:12715 (2000). S. Savrasov and G. Kotliar PRB Phys. Rev. B 69, 245101 (2004).

LDA+DMFT Self-Consistency loop



DMFT Phonons in fcc δ -Pu



(Dai, Savrasov, Kotliar, Ledbetter, Migliori, Abrahams, Science, 9 May 2003)

(experiments from Wong et.al, Science, 22 August 2003)

Physical Picture of Plutonium : Non Magnetic
Strongly Correlated Mixed Valent Metal.
Different Phases : Redistribution of Spectral Weight.
Total Energy and Spectra within the framework!

Remaining Issues

- Spectra: no multiplet structure due to solver limitations.
- Test quality and role of projectors / U's

Issues Largely Resolved in the past few years.

Introduction of methods starting from the atomic limit CTQMC and vertex corrected NCA's

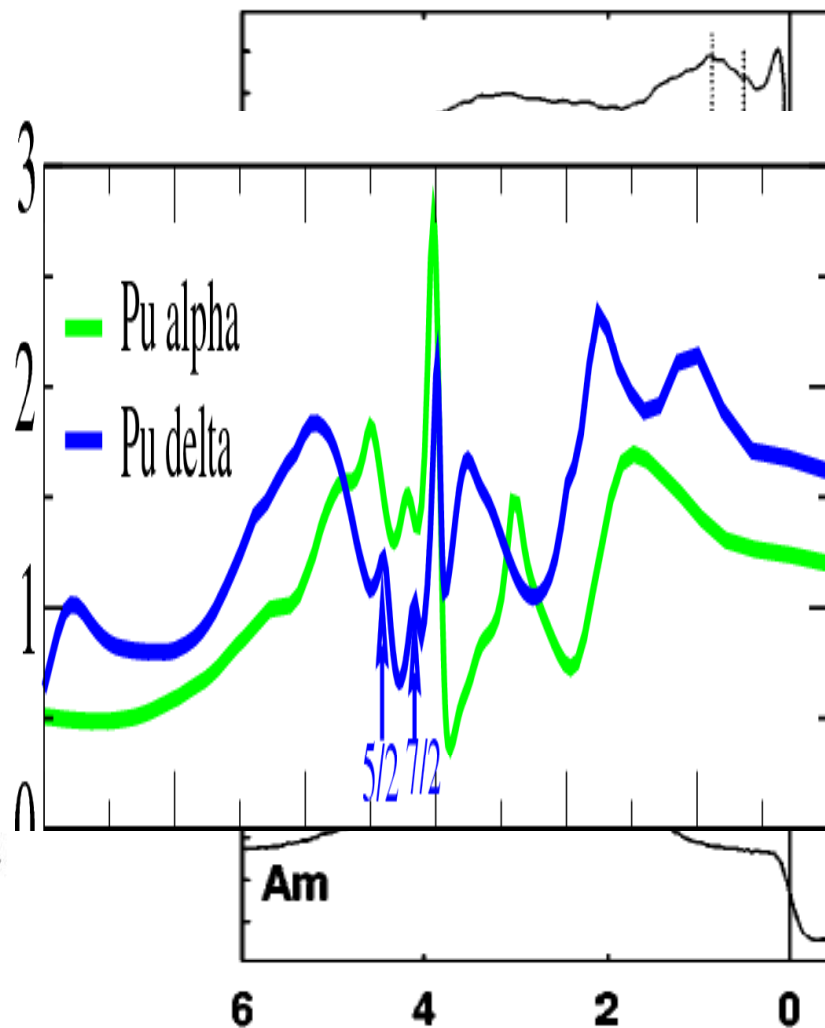
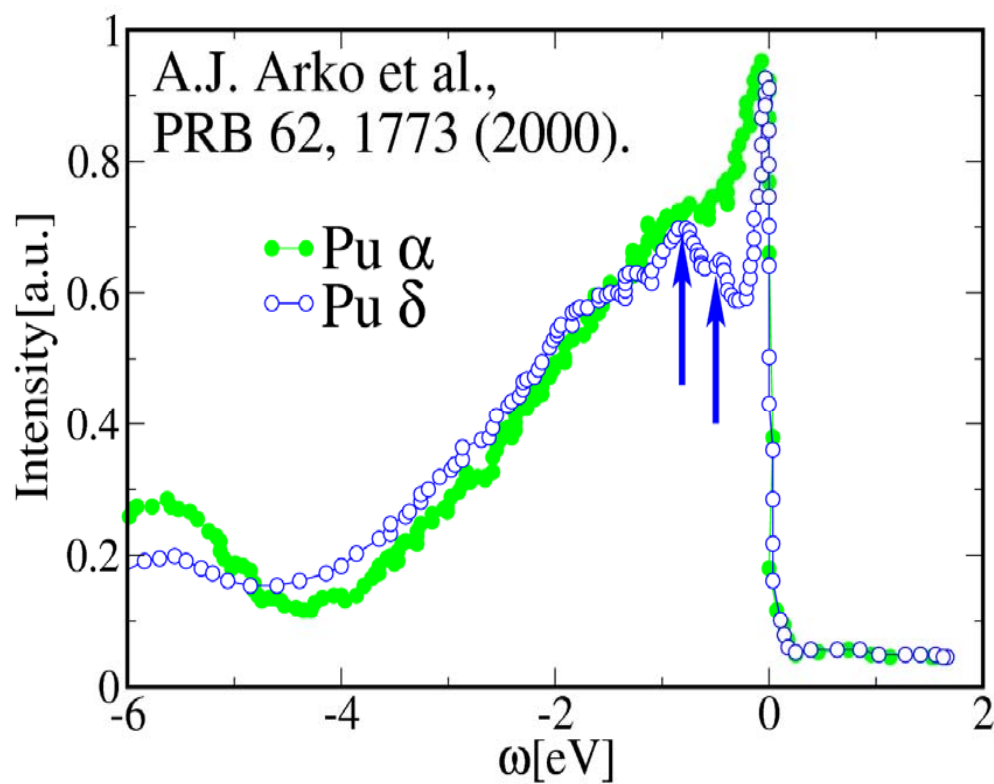
P. Werner et. al. PRL (2006) K.Haule Phys. Rev. B **75**, 155113 (2007)

K. Haule, J. Kroha, and P. Wölfle, Phys. Rev. B **64, 155111 (2001)**

Tests orbital-sensitive LDA+DMFT results against experiments.

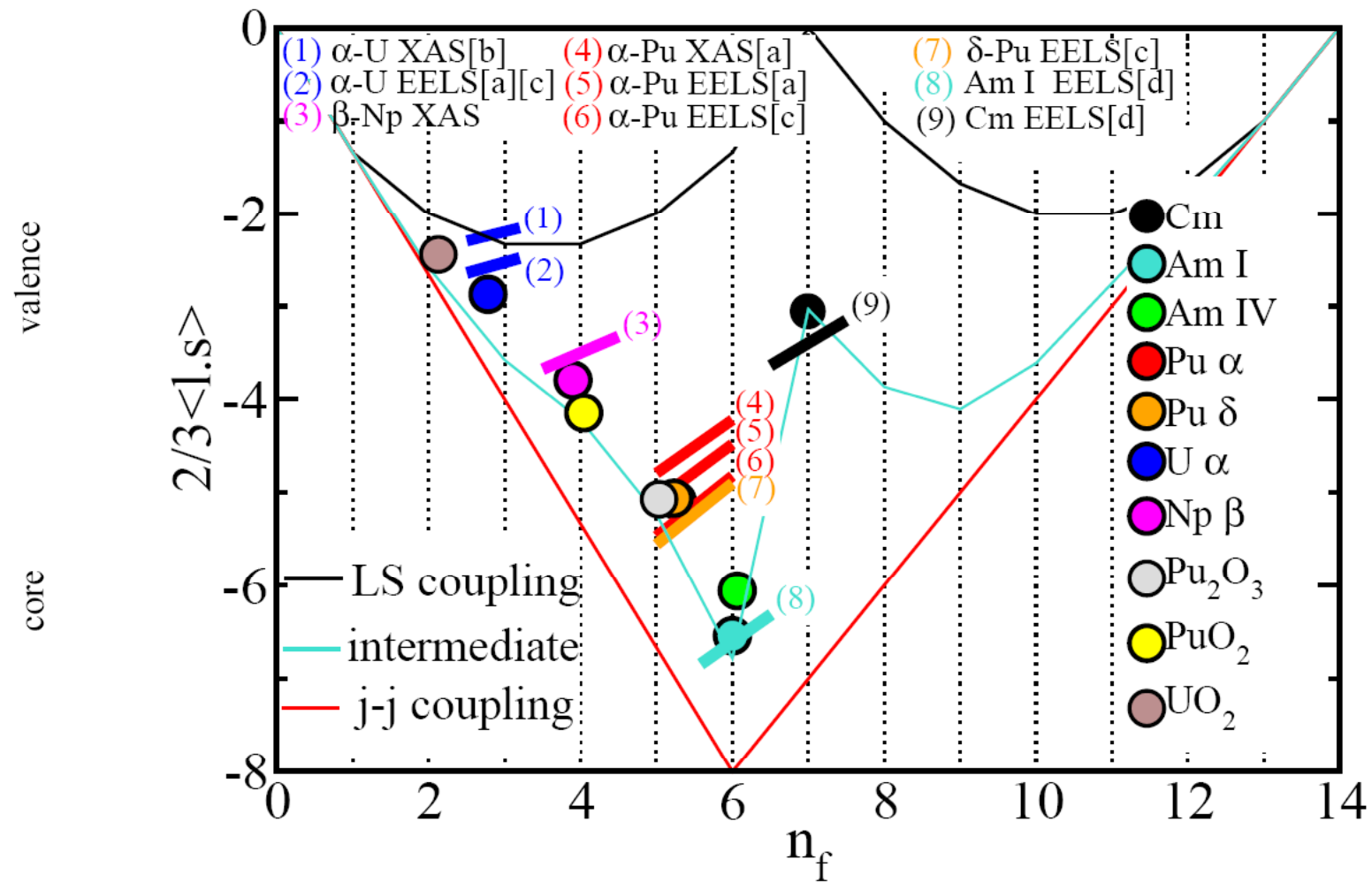
Photoemission

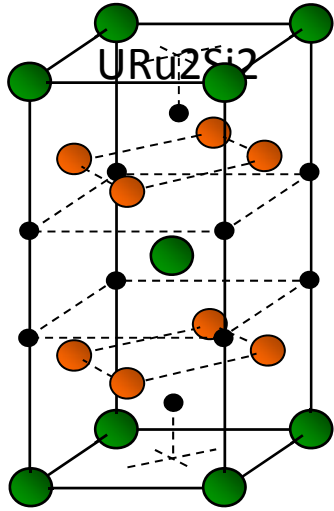
Havela et. al. Phys. Rev. B
68, 085101 (2003)



Finding the f occupancy Tobin et. al. PRB 72, 085109 2005 K. Moore and G. VanDerLaan RMP (2009). Shim Haule and Kotliar Europhysics Lett (2009)

$$B = \frac{3}{5} - \frac{4}{15} \frac{1}{\langle n^h \rangle} \sum_{i \in 5f} \langle \mathbf{l}_i \cdot \mathbf{s}_i \rangle. \quad B = \frac{I_{5/2}}{I_{5/2} + I_{3/2}}$$





A challenge
to the
electronic
structure
community ?

