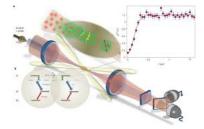
Krzysztof Jachymski, Przemysław Bienias, Hans Peter Büchler ITP3 Stuttgart

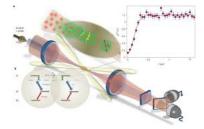
KITP, 13.12.2016



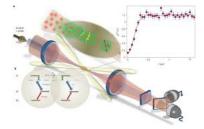
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- easy manipulation with (non)linear optics
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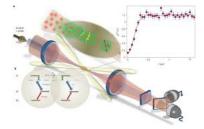
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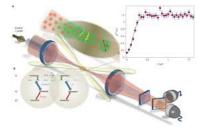
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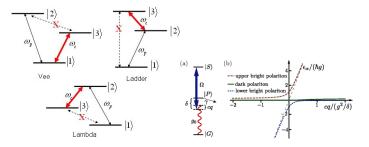


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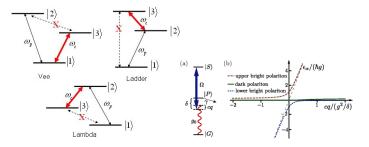


interaction of light with three-level atoms

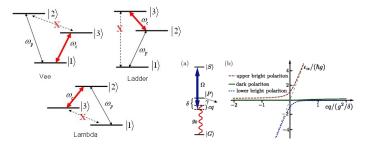
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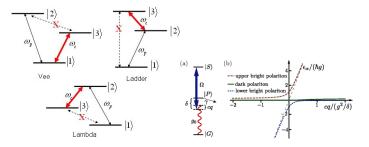
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Electromagnetically induced transparency



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Rydberg blockade

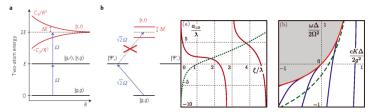


Figure: Gaetan et al, Nat. Phys. 5, 115 (2009); Bienias et al, PRA 90, 053804 (2014)

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- diagrammatic derivation of the interaction: Bienias et al, PRA 90, 053804 (2014)

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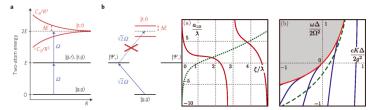


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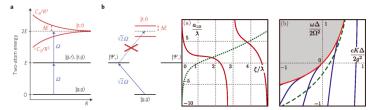


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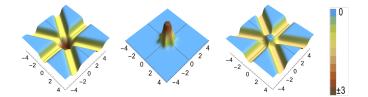
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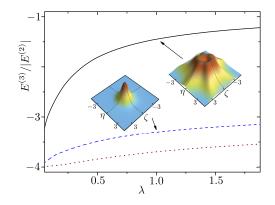
Three-body interaction and bound states

1D geometry, Jacoby cooridnates



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Prospects for cavity setups

- cavity photons, driven-dissipative system
- tuning the properties by altering the mode structure (Sommer et al, arXiv:1506.00341)
- two-dimensional nonequilibrium system with multi-body interactions?

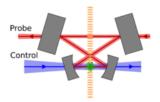


Figure: Ningyuan et al PRA 041802(R) (2016) (Jonathan Simon group)

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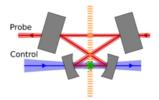


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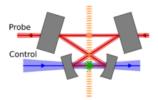


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strong effective many-body interactions between dark polaritons

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