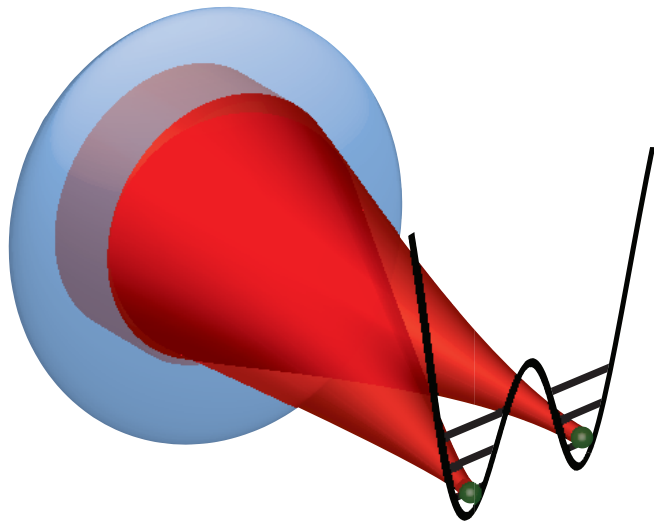


# Entanglement and spin-motional physics with bosons in optical tweezers



Cindy Regal

Brian Lester

Yiheng Lin

Adam Kaufman

Mark Brown

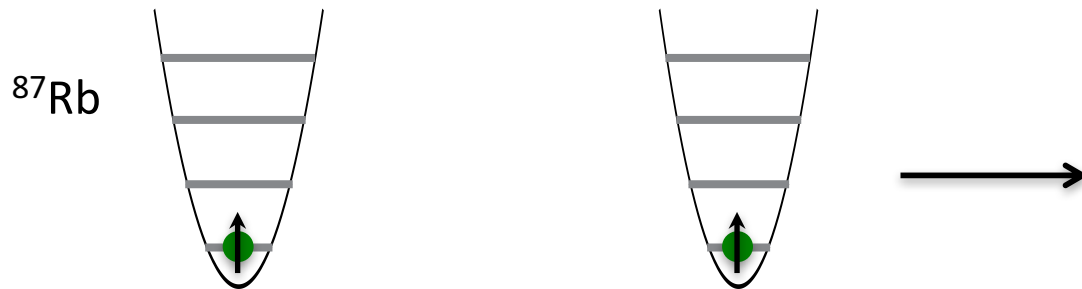


KITP few-body physics program  
2016

Michael Wall, Michael Foss-Feig,  
Leonid Isaev, Ana Maria Rey

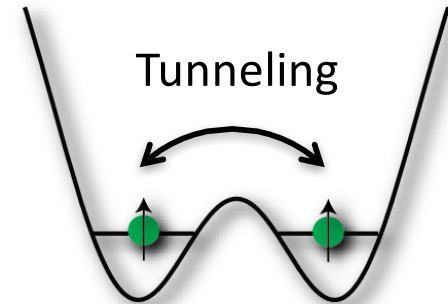
# Quantum statistics with independent atoms

Independent atoms in separated traps



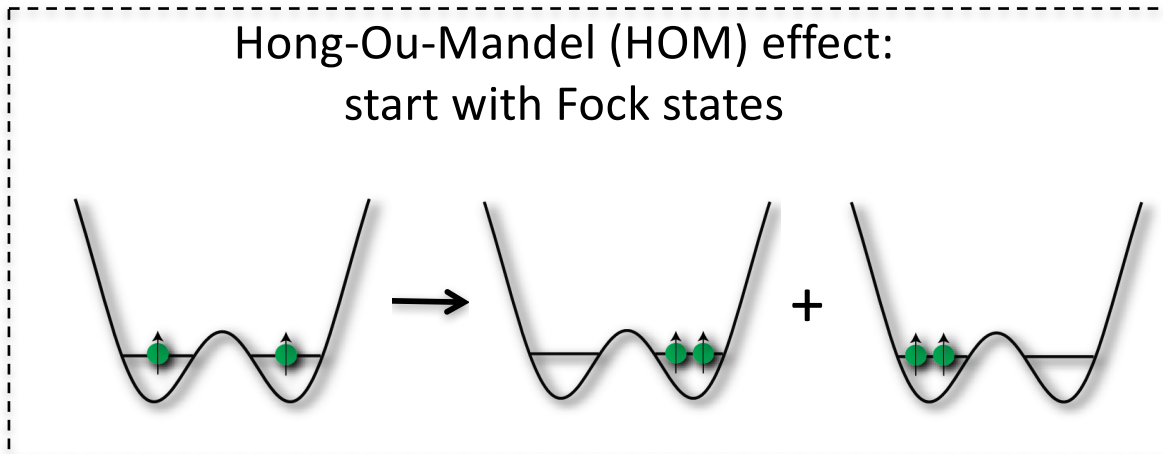
Ground state preparation via  
Raman-sideband cooling

Observe interference



Small interactions ( $U < J$ )

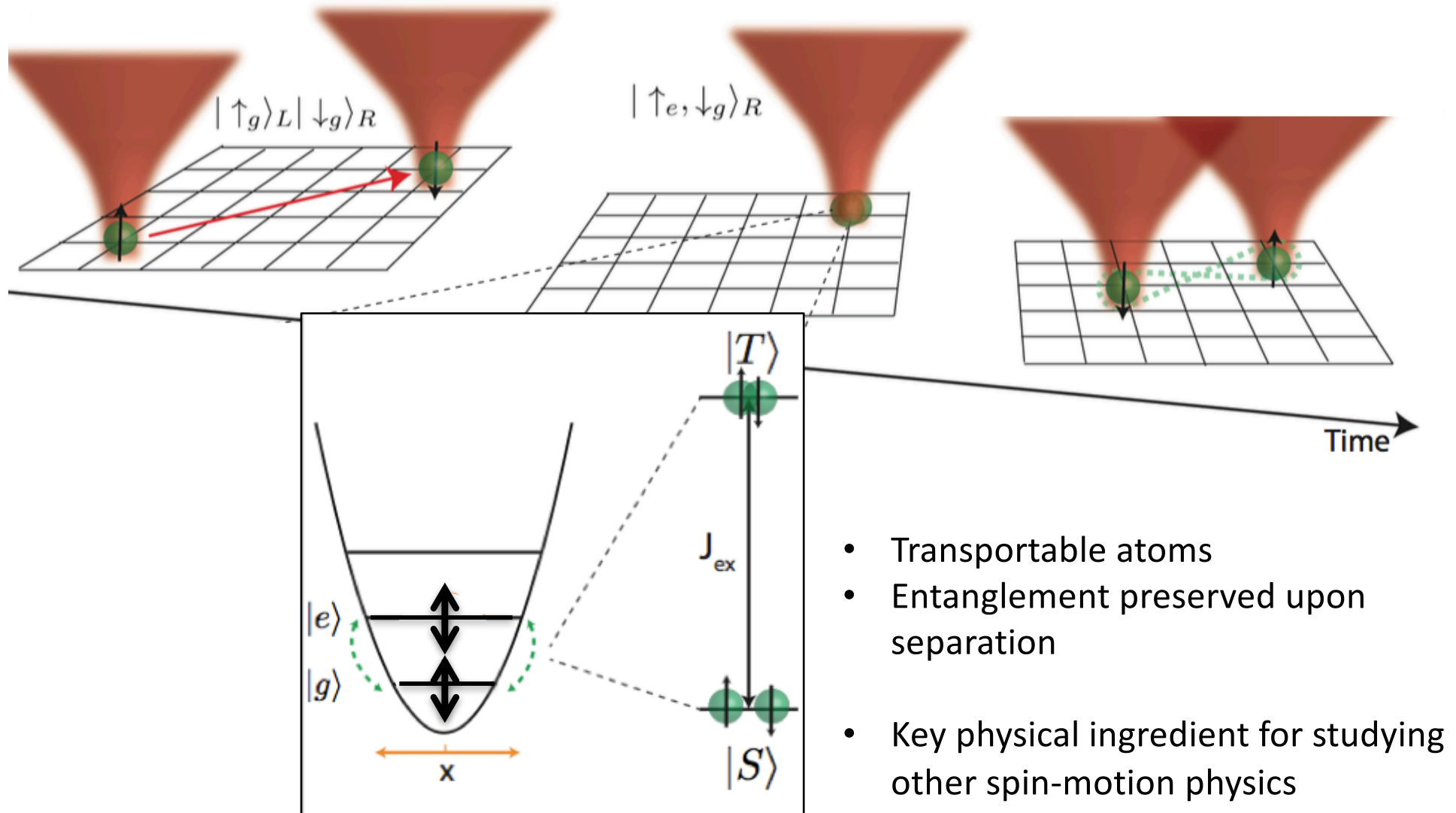
Hong-Ou-Mandel (HOM) effect:  
start with Fock states



Consequence of initial bosons in  
pure state – indistinguishable

- Single-atom optics

# Spin entanglement using spin exchange



Anderlini *et al.*, Nature (2007)

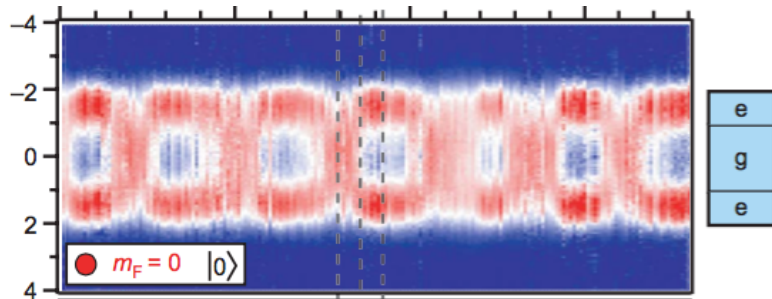
Hayes *et al.*, PRL (2007)

# Outline

- Introduction to techniques
- Examples:
  - HOM: Mixing spatial modes
  - Measuring spin entanglement
  - Interfering atoms: Post selection of singlet state
- To consider in context of few-body group
  - New probes and initialization
  - Collisional physics for state preparation
  - While this talk dwells on 2 atoms, 10 - 100 is natural goal
  - Rb – proof of concepts – larger gains yet to come with *alkaline earth atoms, molecules, fermions...*
  - More exotic traps with atom spacings 100 nm scale?
  - Adiabatically connect to ground state of less confining trap for delocalized states?
  - Here scattering length small (sometimes effectively zero); could combine with Feshbach resonance
  - Precise measurements that avoid inhomogeneous broadening?

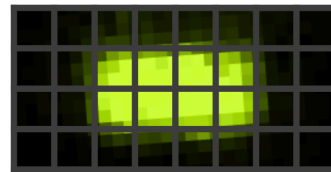
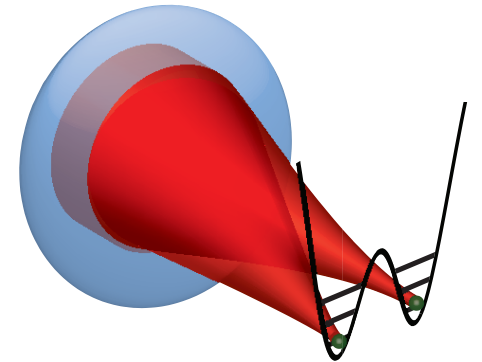
# Experimental context

Like experiments in superlattices and quantum gas microscopes

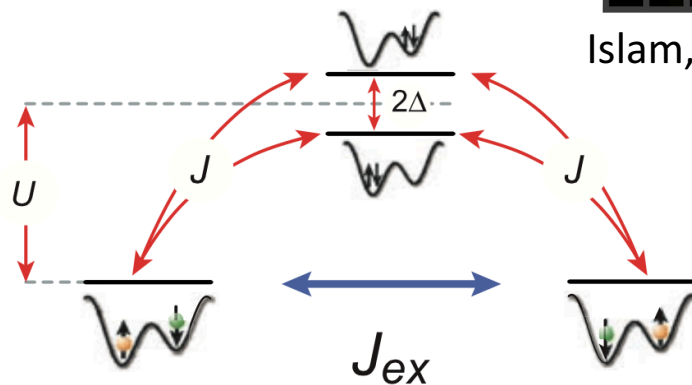


Exchange in array of double wells  
Anderlini *et al.*, Nature (2007)

Add different flavors of flexibility / natural experiments, building state gives access to *information* about initialized microscopics



Islam, *et al.*, Nature (2015)



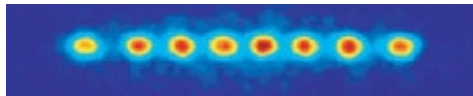
Evaporatively cooled fermions:  
Selim Jochim group

Superexchange  
Trotzky *et al.*, Science (2008)

# Raman sideband cooling atoms

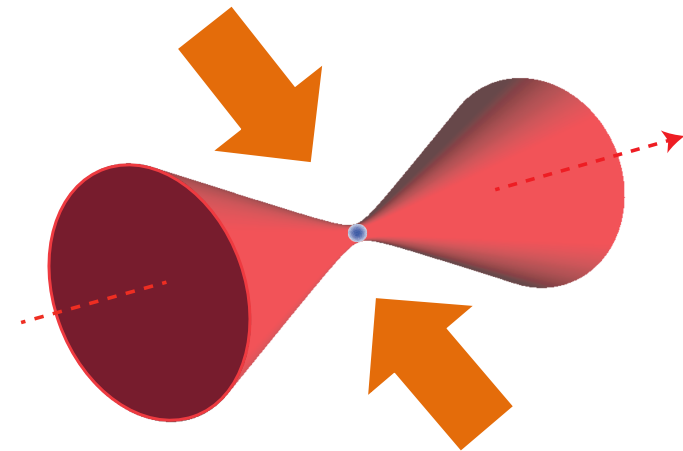
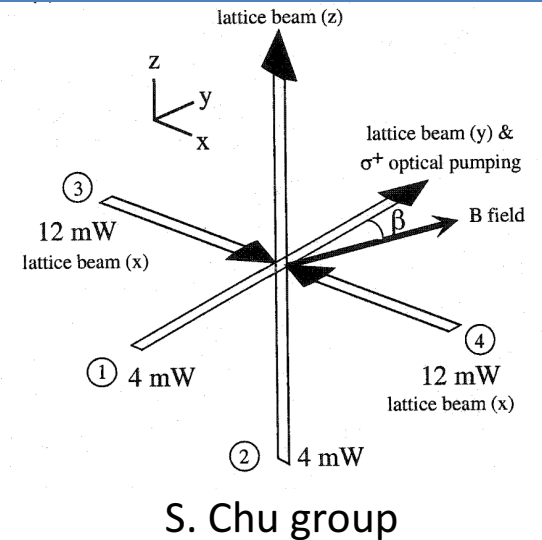
Considerable history:

- Ions

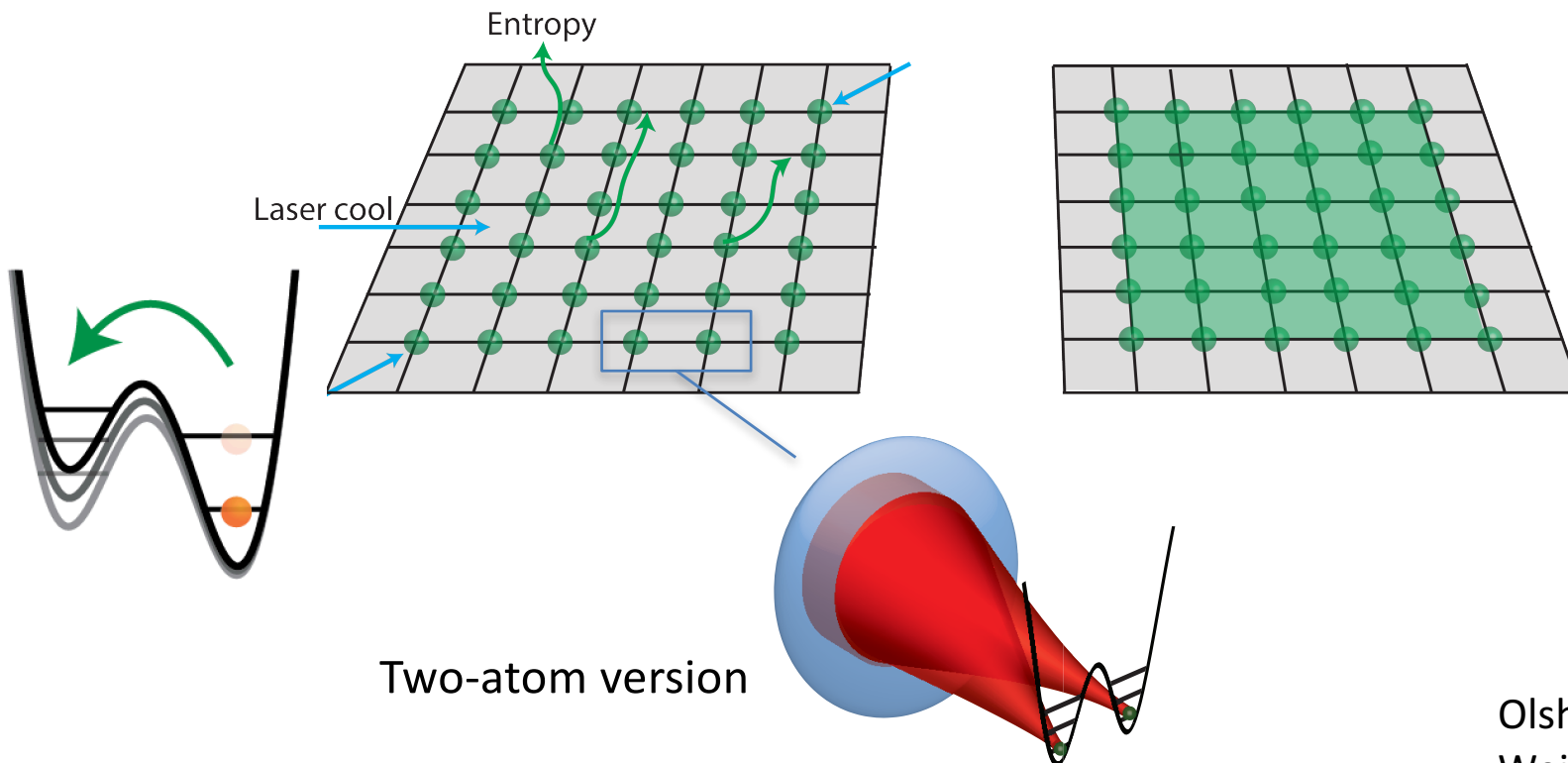
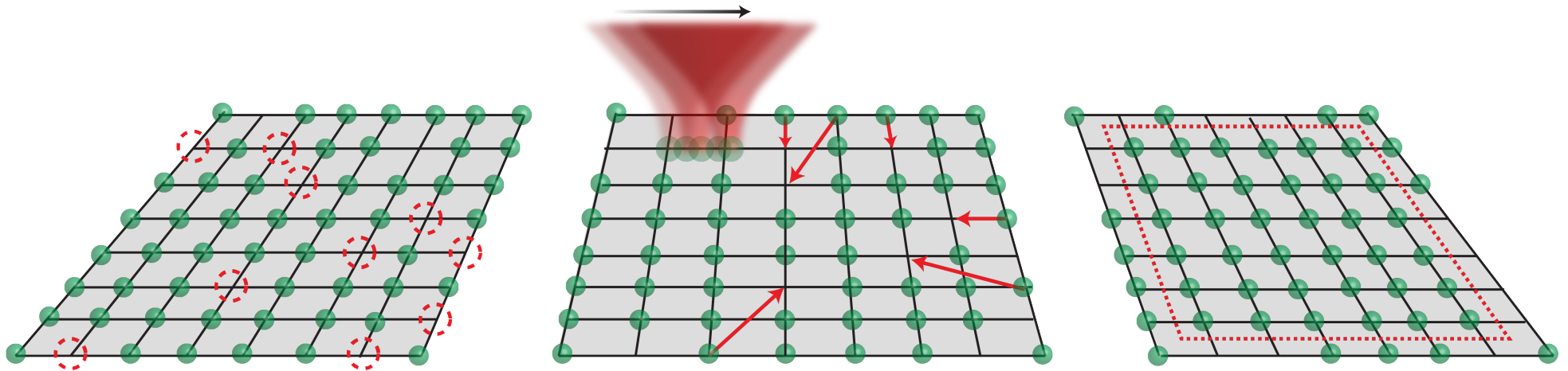


- Neutral atoms in lattices:
  - Large lattice experiments
  - Addressable atoms: Cavity lattice experiments, other recent work in lattices

- This talk:
  - Neutral atoms in movable, low-dimensional set of optical tweezers
  - Cooled like in *ion* experiments
  - But availability of particle overlap gives protocols more like *photons* or *quantum dots*
  - Of course ultimate goal is many atoms, or a few (for certain questions)



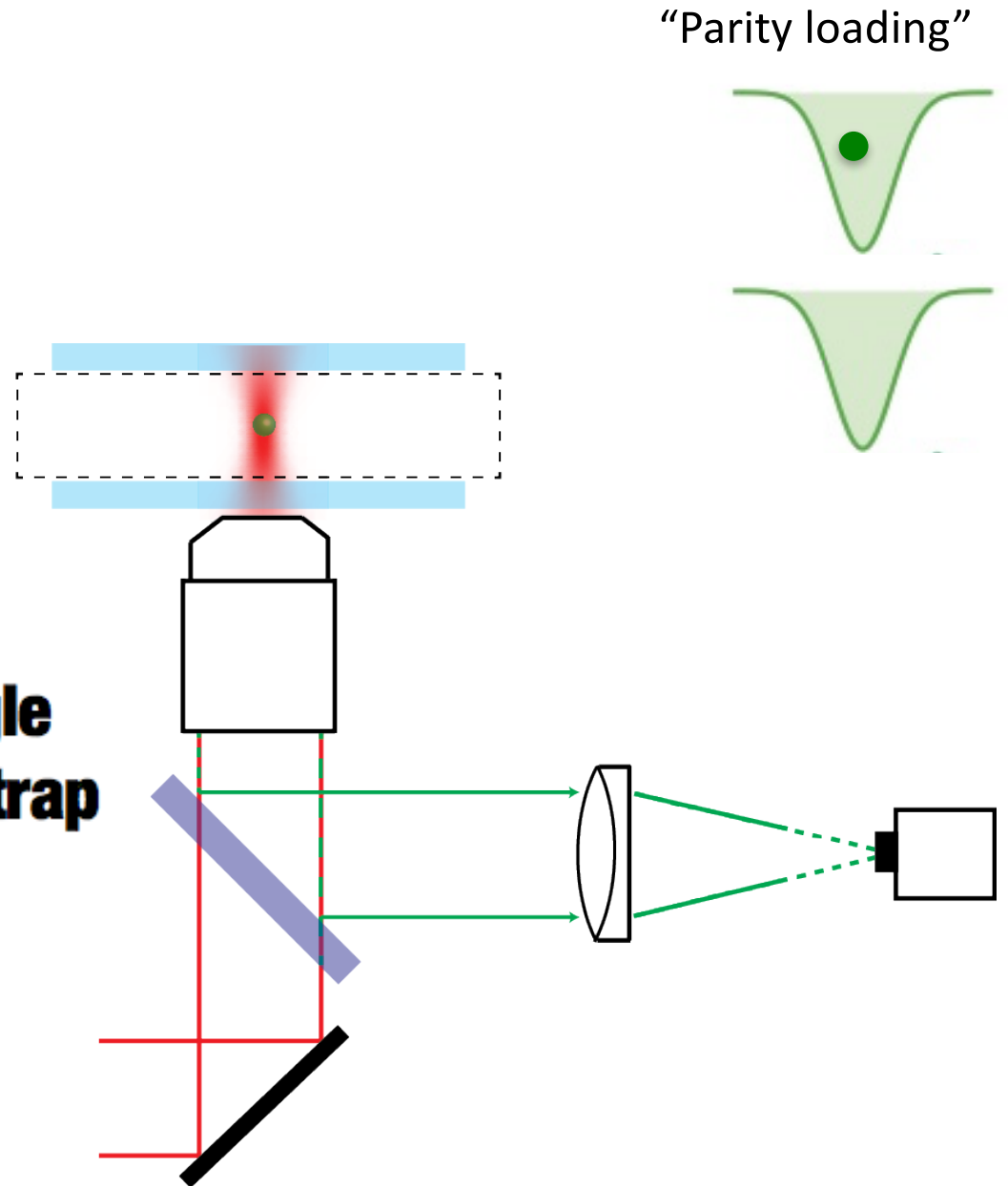
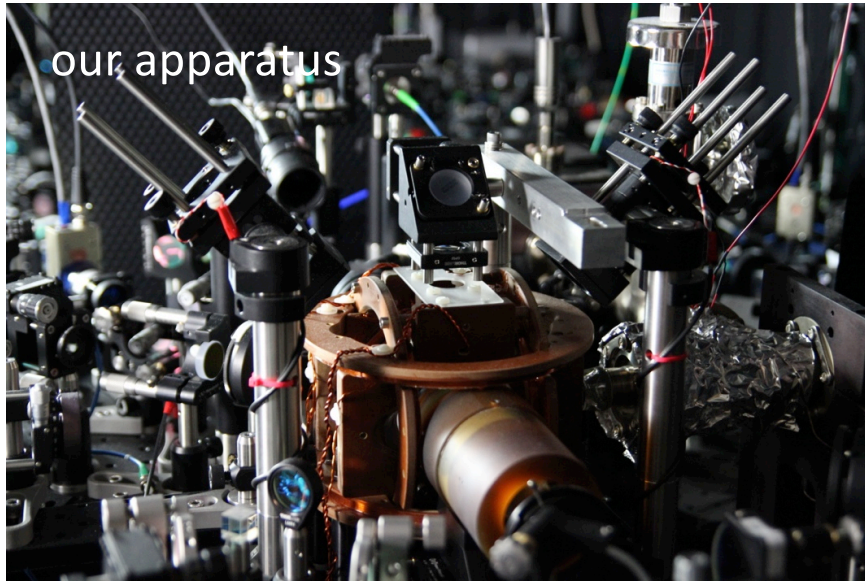
# Quantum gas assembly



Two-atom version

Olshanii *et al.*, PRL (2002)  
Weiss *et al.*, PRA (2004)

# Single neutral atoms in optical tweezers

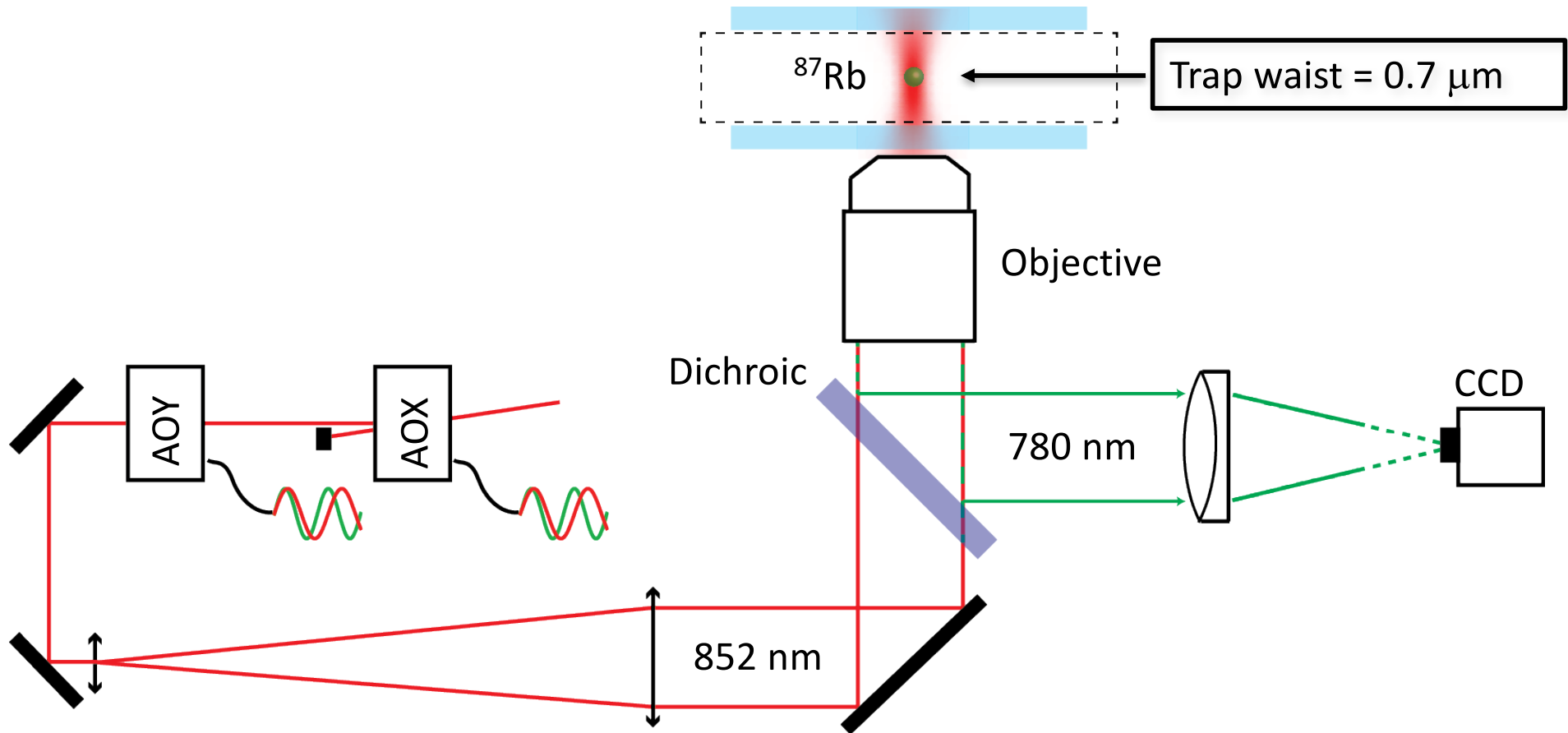


## Sub-poissonian loading of single atoms in a microscopic dipole trap

Nicolas Schlosser, Georges Reymond, Igor Protsenko  
& Philippe Grangier

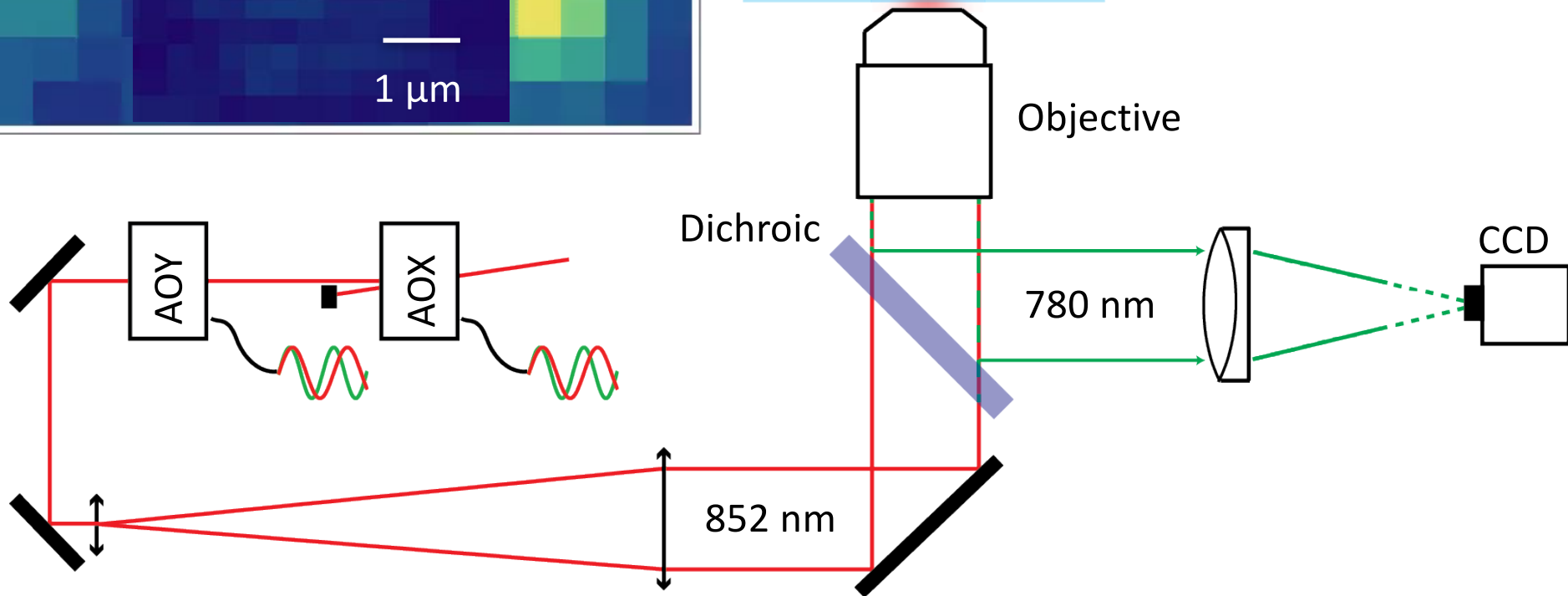
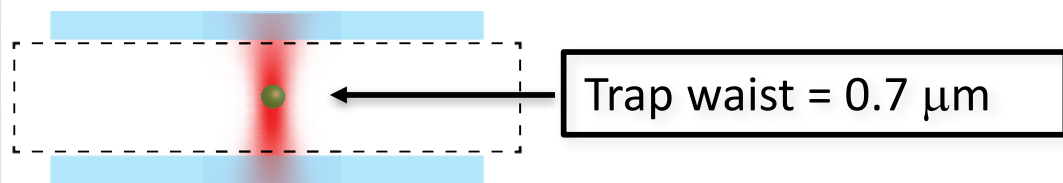
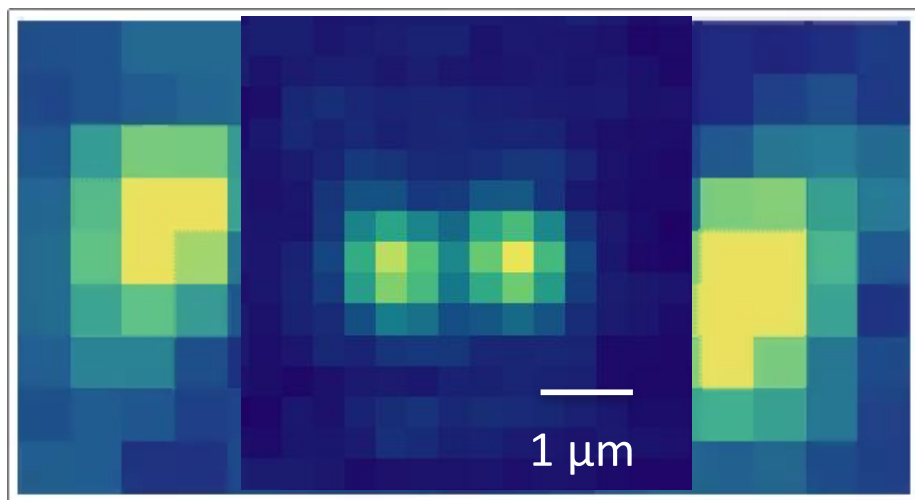


# Single neutral atoms in optical tweezers

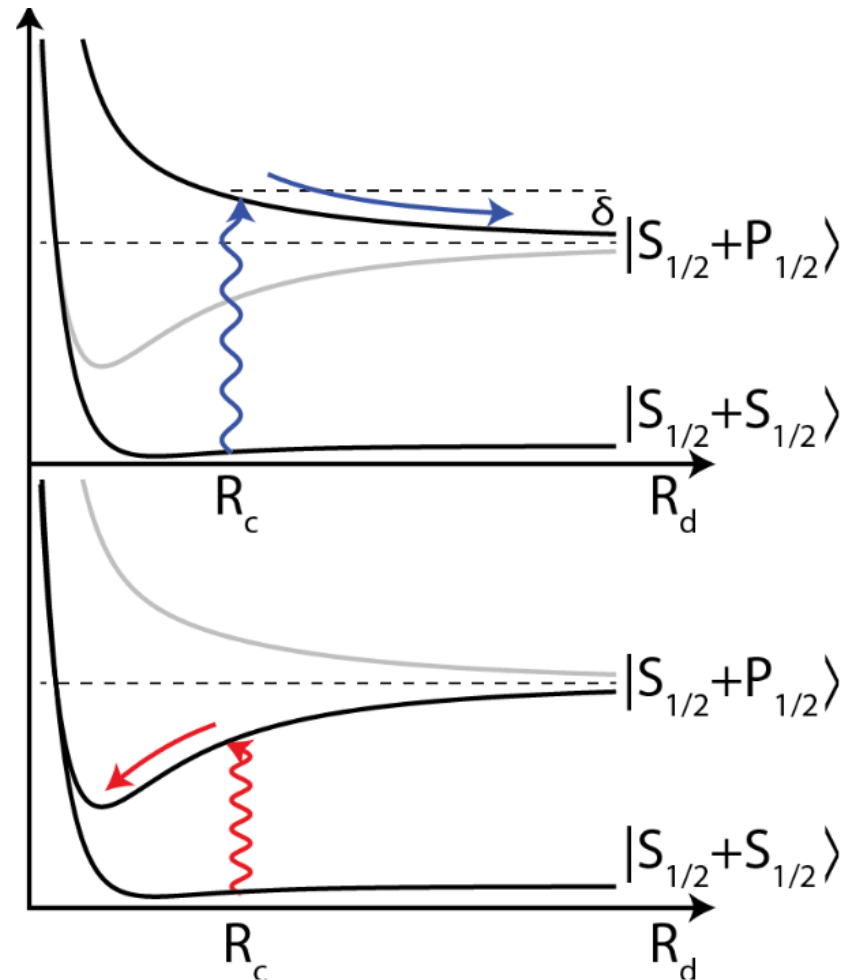
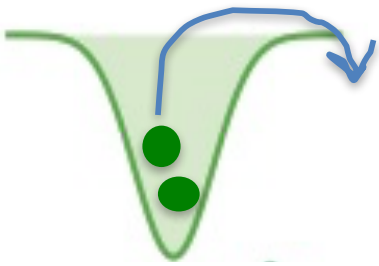


# Single neutral atoms in optical tweezers

Atom images

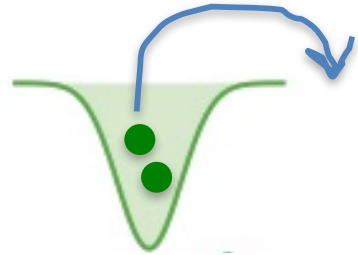


# Tailor light-assisted collisions

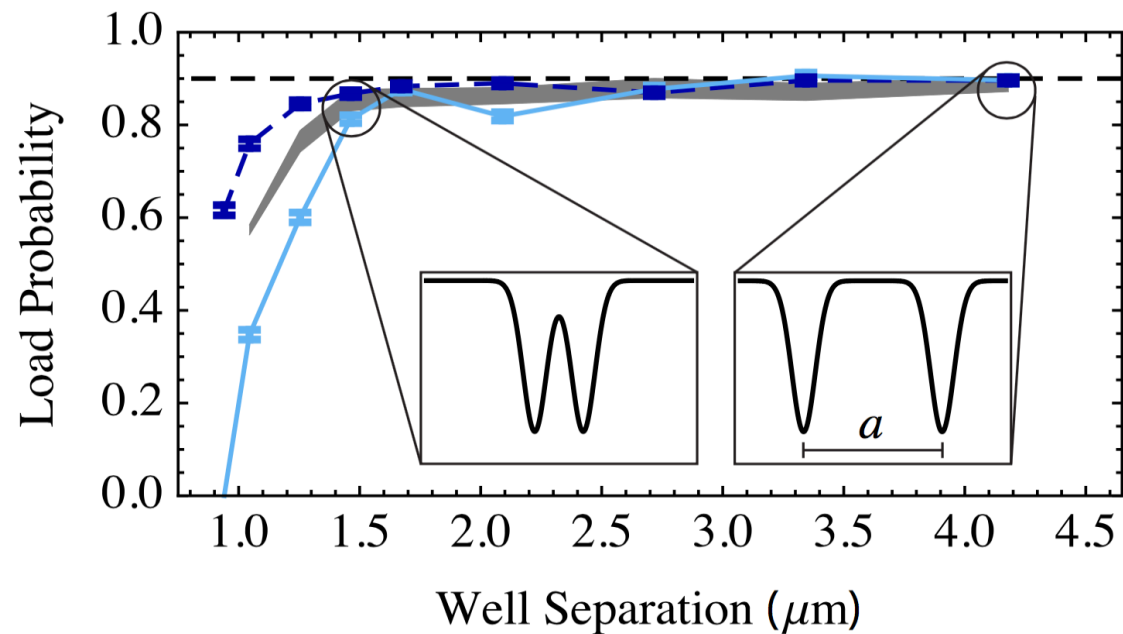
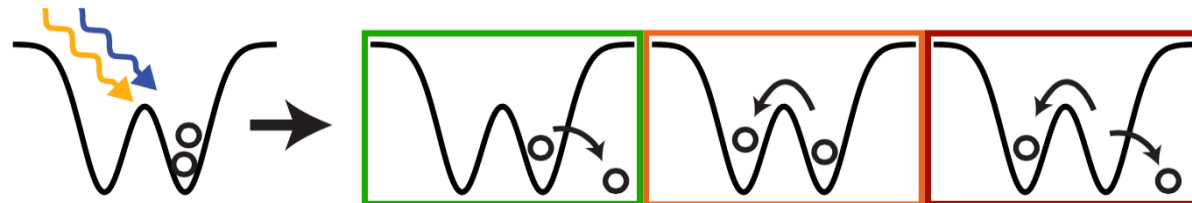


Mikkel Andersen Group  
New Zealand  $^{85}\text{Rb}$

# Near-deterministic loading of single atoms



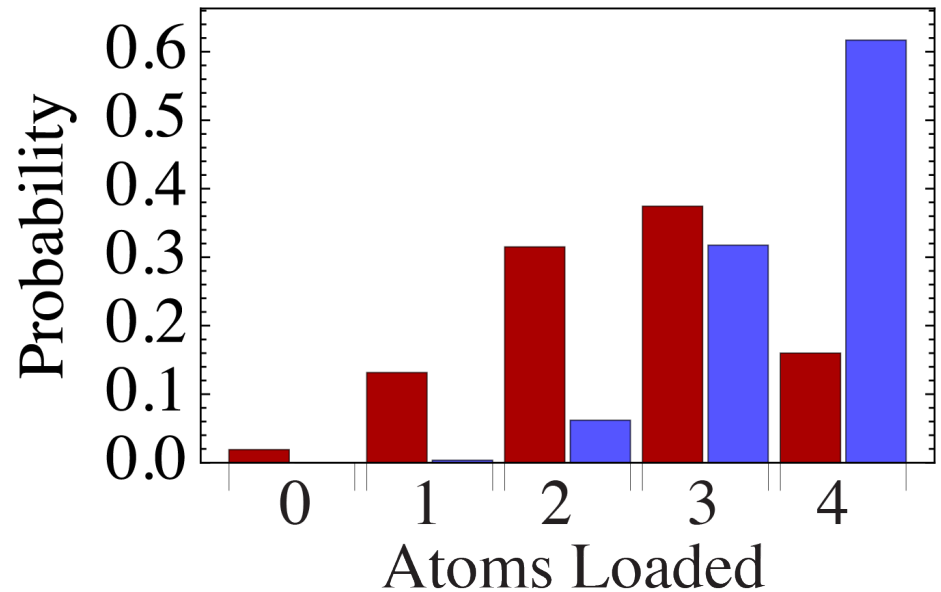
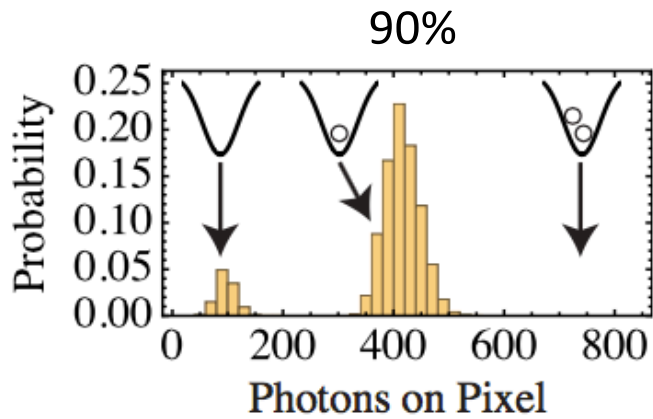
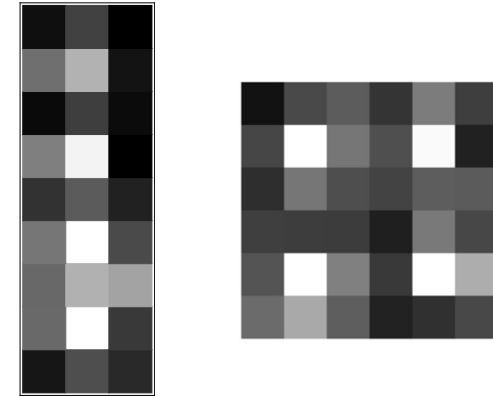
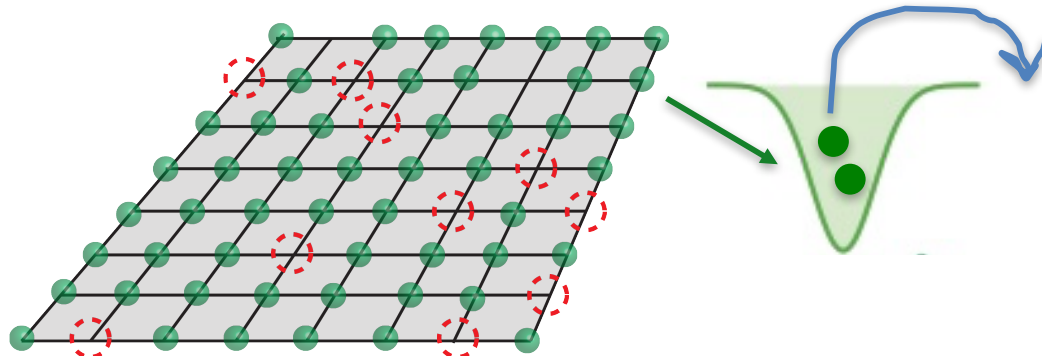
- Smaller volume traps (light applied during MOT loading)
- Understand spacing scaling



Grunzweig *et al.*, Nature Phys. (2010)

B. J. Lester *et al.*, PRL (2015)

# Loading arrays of atoms

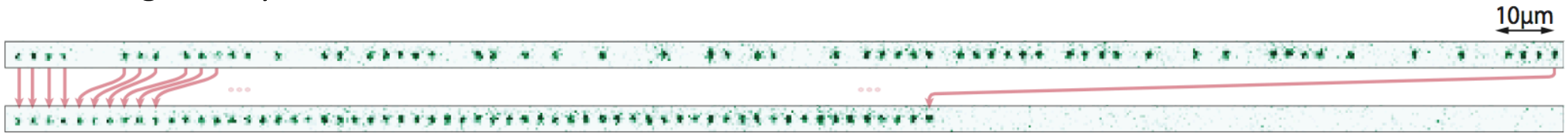


Many more traps

Grunzweig *et al.*, Nature Phys. (2010)  
B. J. Lester *et al.*, PRL (2015)

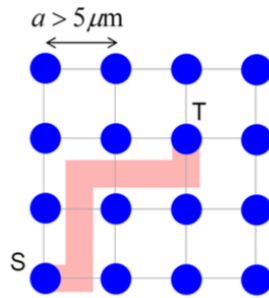
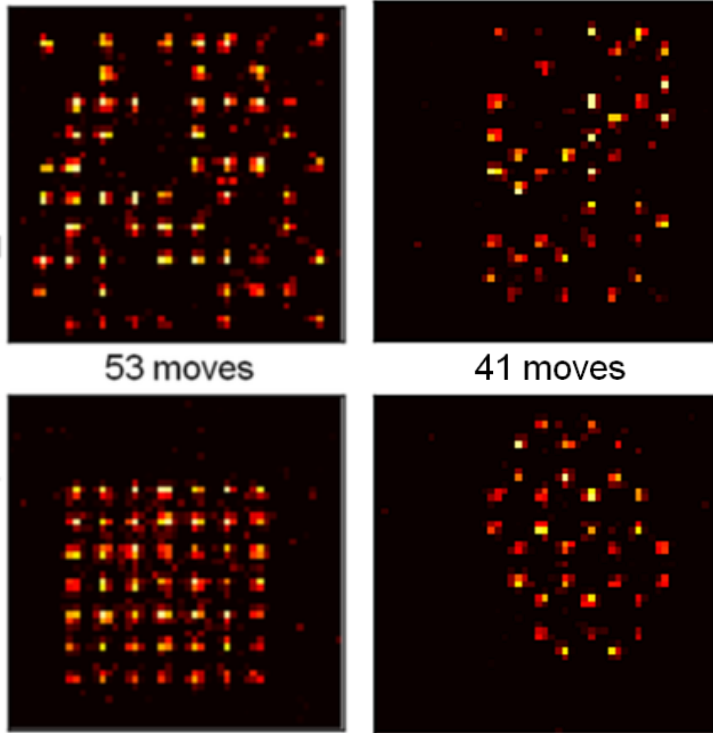
# Moving larger arrays

Rearrange many atoms: Paris and Harvard



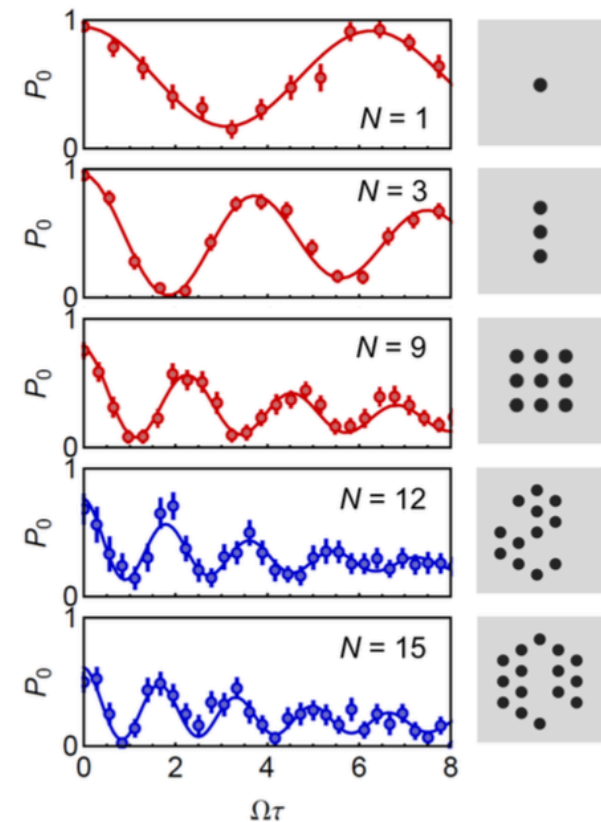
Endres, *et al.*, arXiv:1607.03044 (2016)

Barredo, *et al.*, arXiv:1607.03042 (2016)



Rydberg physics in arrays

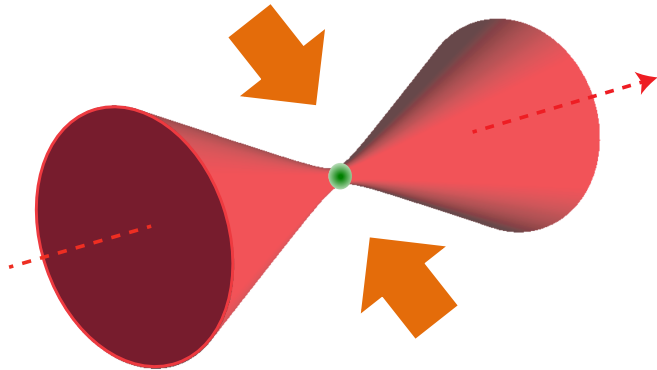
LaBuhn *et al.*, arXiv:1509.04543



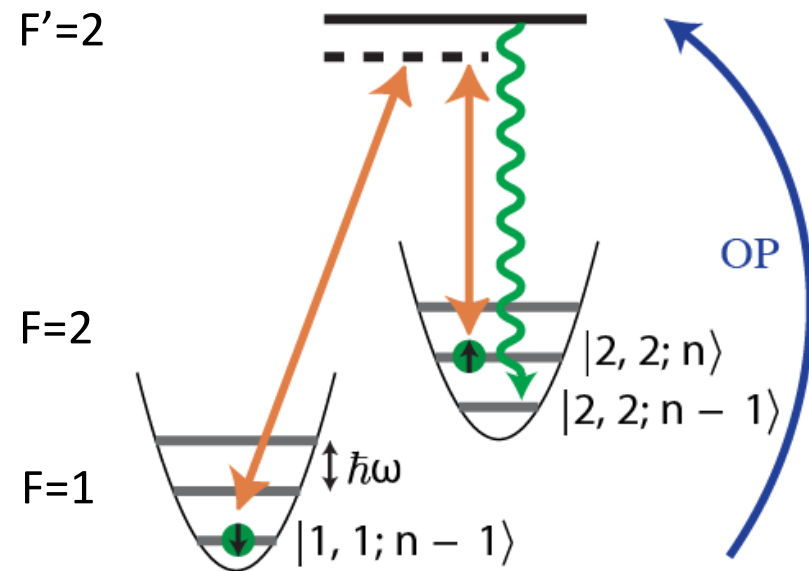
First atom sorting machine: Meschede group, 2006

See also Wilk *et al.* PRL (2010); Zhang *et al.*, PRL (2010)

# Raman sideband cooling single neutral atoms



External cooling beams



Alternate **coherent** and **dissipative** steps

Requirements and challenges:

- Large trap frequency  $\omega$ 
  - small Lamb-Dicke parameter
  - larger Rabi rate possible
- Good precooling via PGC
- Consider effects of non-paraxial focus

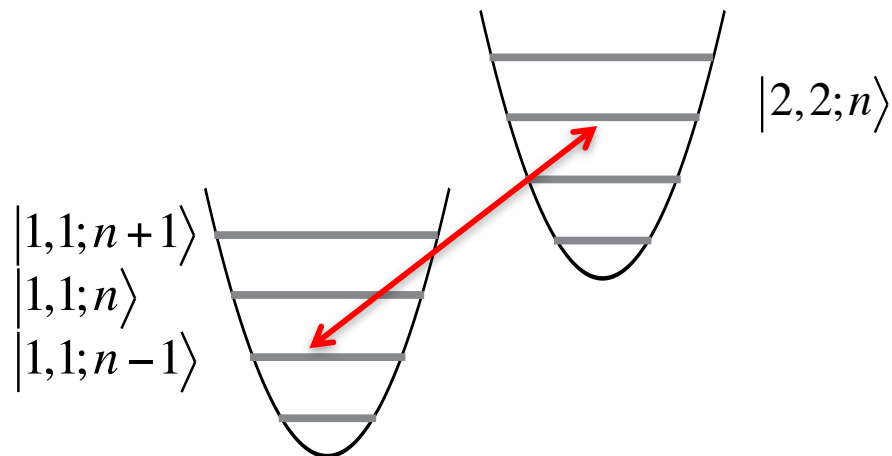
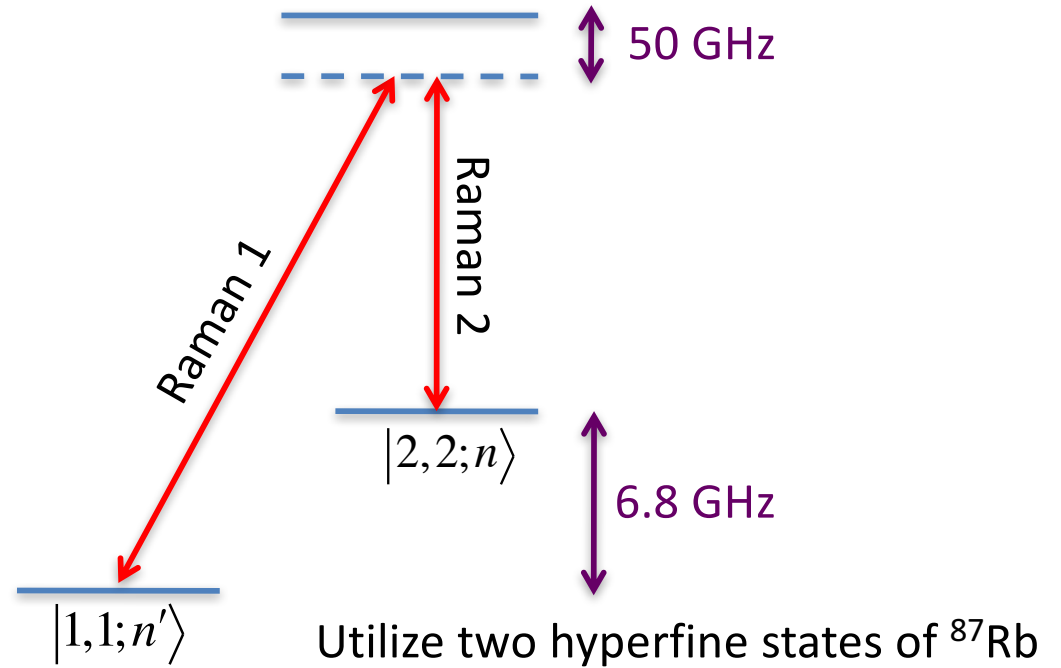
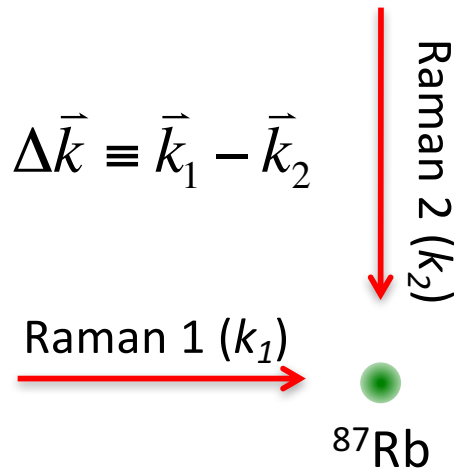
Monroe *et al.*, PRL (1995)

H. Perrin *et al.*, Europhys. Lett. (1998)

S. Hamman *et al.*, PRL (1998)

V. Vuletic *et al.*, PRL (1998)

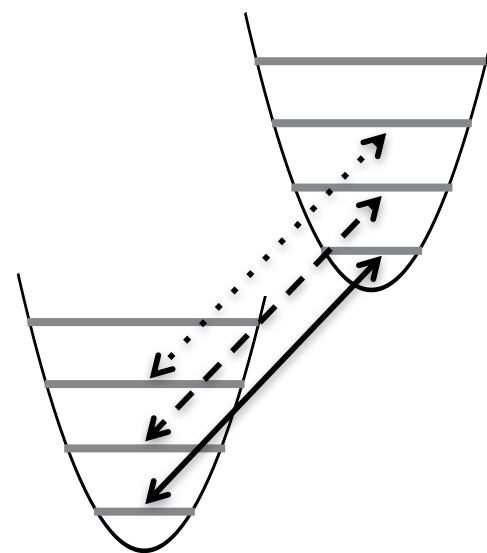
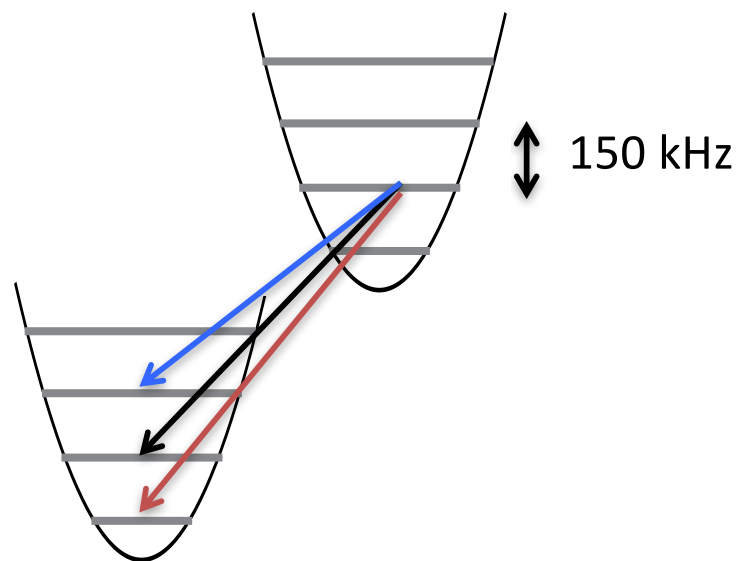
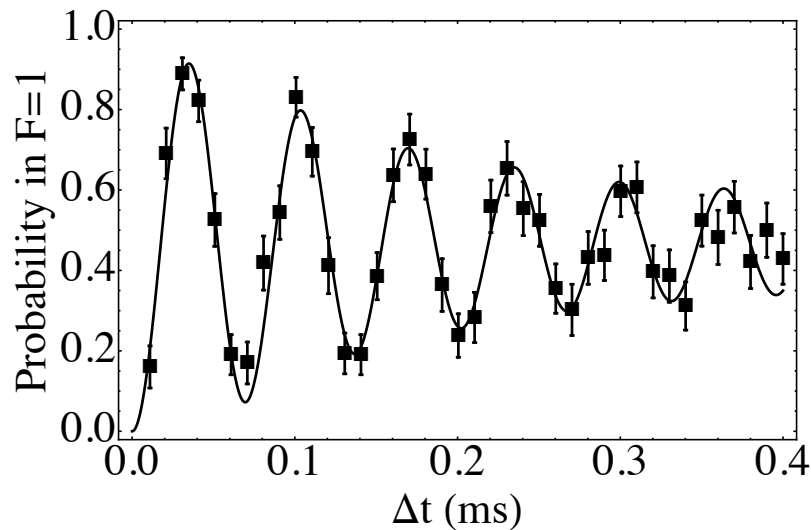
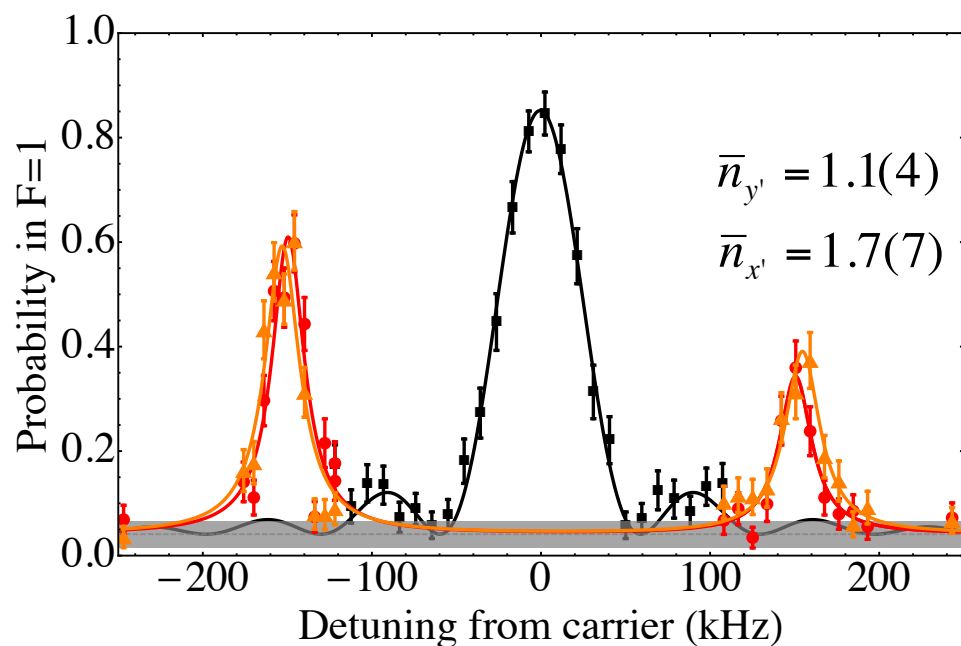
# Raman sideband transitions





# Spectroscopic measurement of precooling

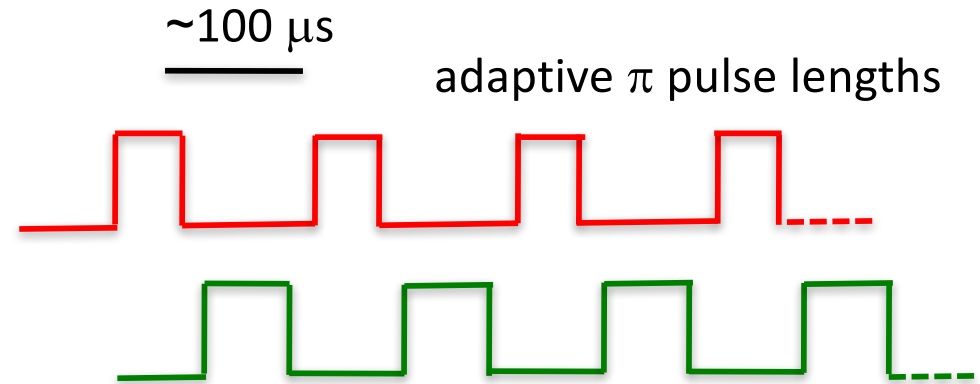
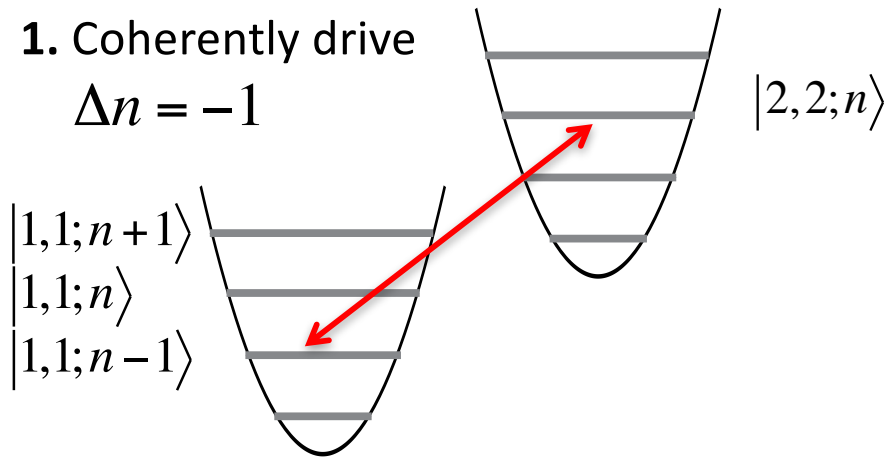
## Motional spectroscopy



# Cooling sequence

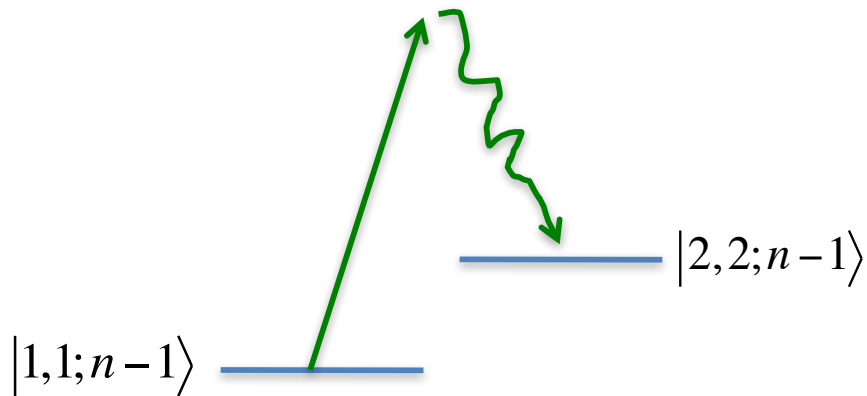
1. Coherently drive

$$\Delta n = -1$$



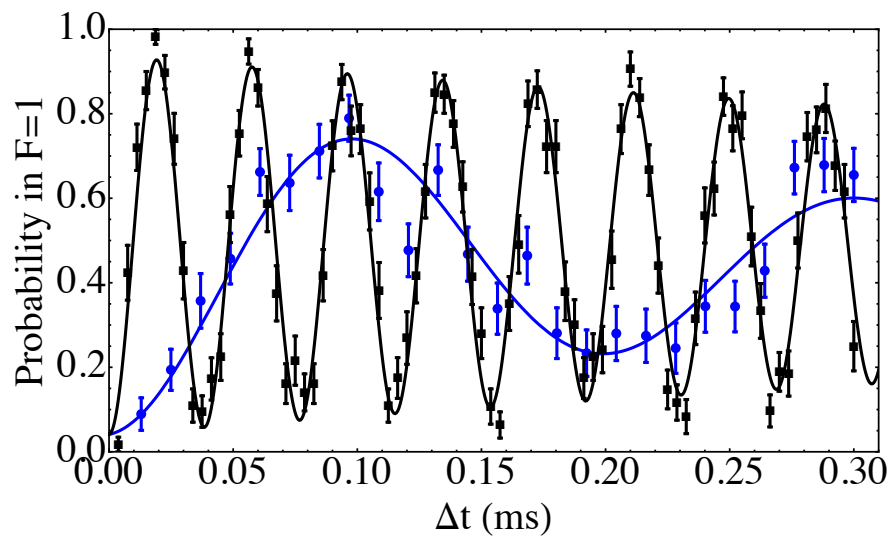
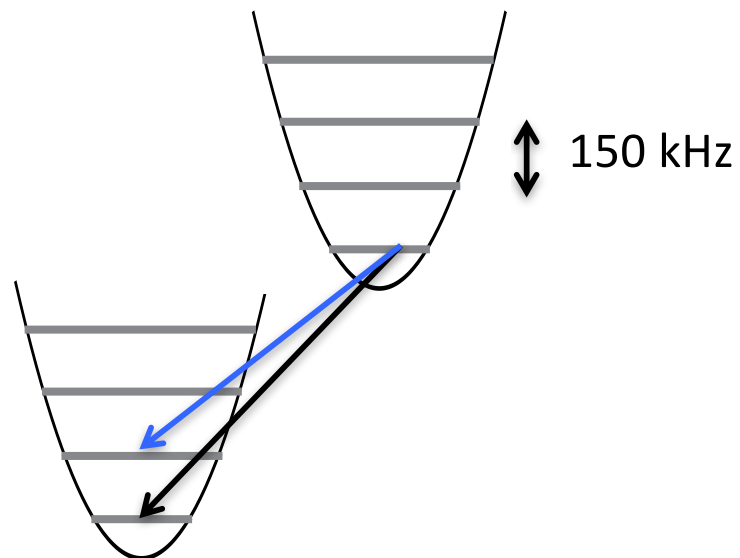
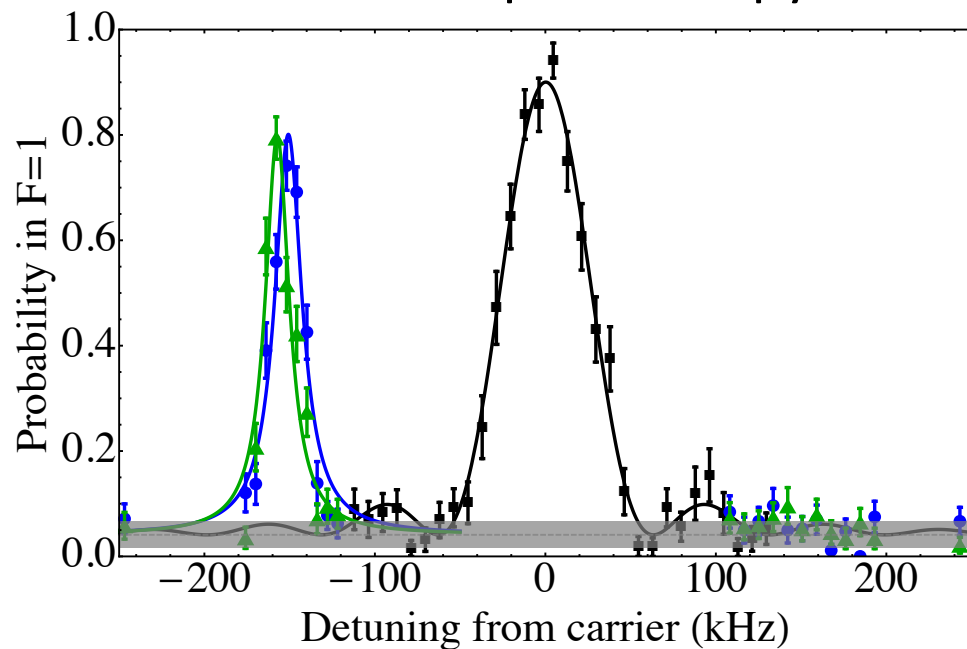
2. Pump back to  $|2,2;n-1\rangle$  state: cool efficiently in Lamb-Dicke regime

$$P_{\text{return}} \sim 1 - (2\bar{n} + 1)\eta_{OP}^2$$

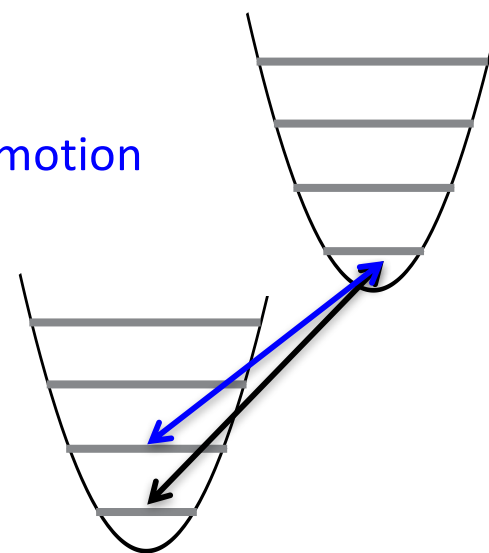


# Radial ground state cooling

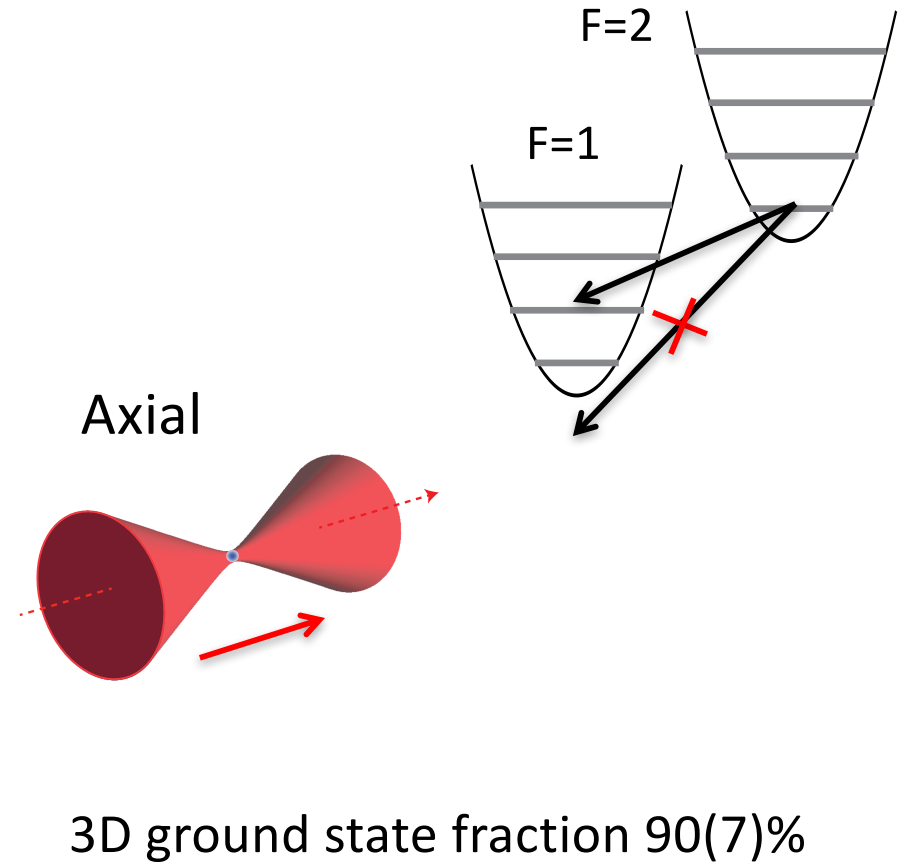
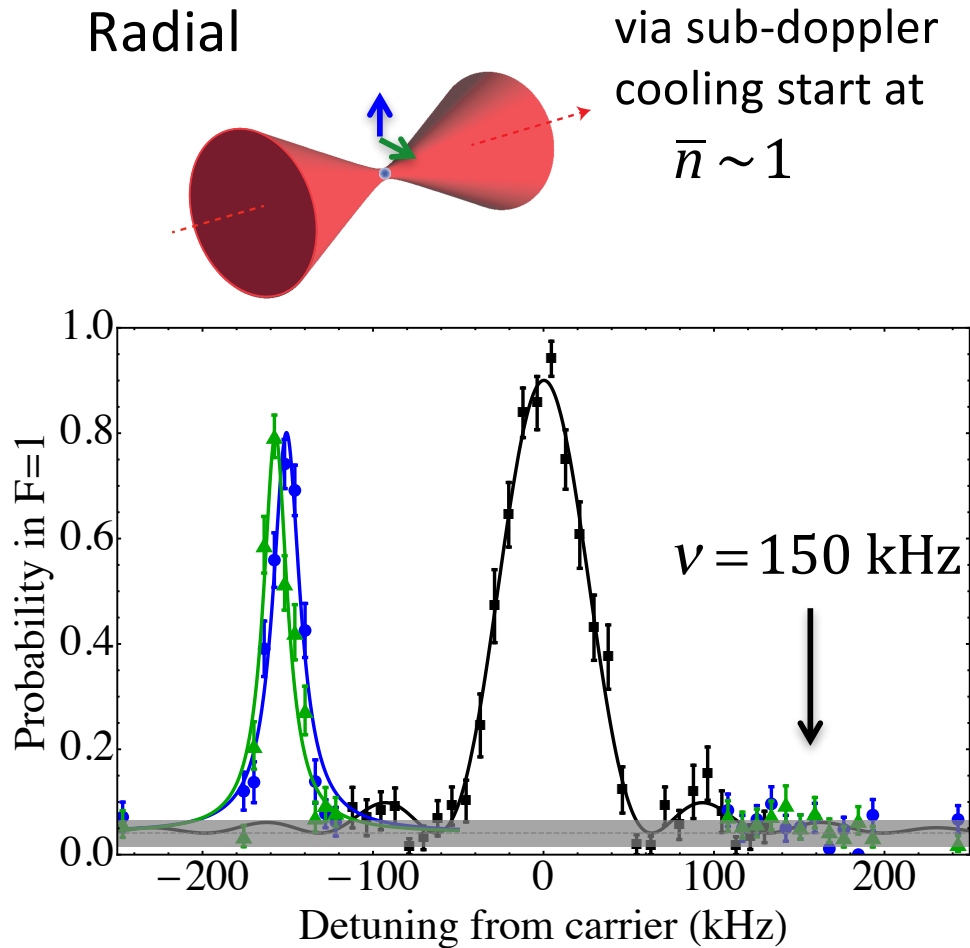
## Motional spectroscopy



Coherent  
control of motion

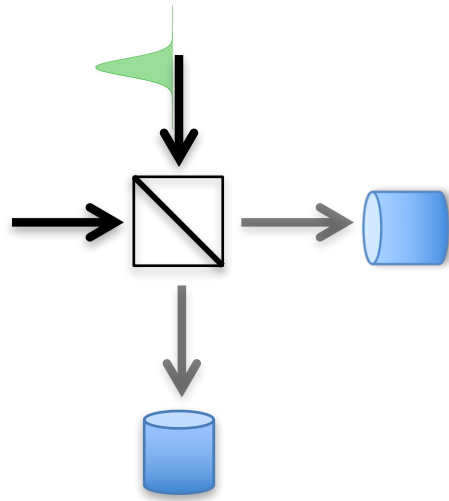


# 3D ground state cooling in an optical tweezer



Kaufman *et al.*, PRX (2012); Thompson *et al.*, PRL (2013);  
cold fermions in tweezers: Serwane *et al.*, Science (2011)


# Hong-Ou-Mandel with photons




$$|1,0\rangle \rightarrow \frac{1}{\sqrt{2}}(|1,0\rangle + |0,1\rangle)$$


# Hong-Ou-Mandel interference of photons

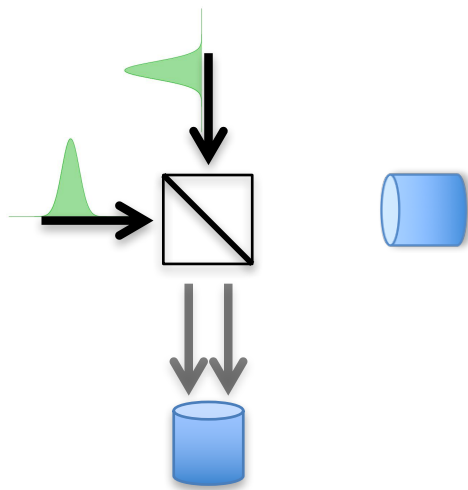
Spontaneous emission

$|e\rangle$  

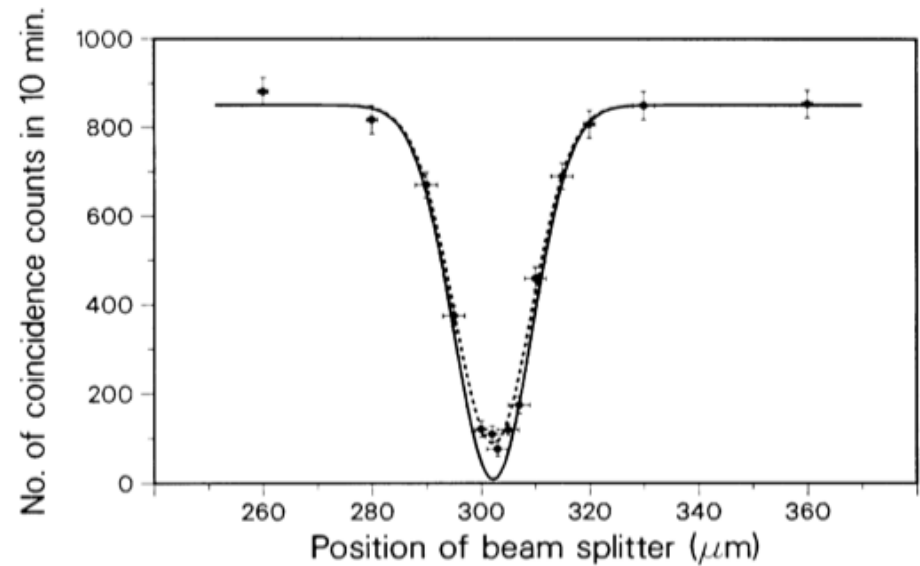
$|g\rangle$  

$|e\rangle$  

$|g\rangle$  



$$|1,1\rangle \rightarrow \frac{1}{\sqrt{2}} (|2,0\rangle + |0,2\rangle)$$



C. K. Hong, Z. Y. Ou, and L. Mandel, Phys. Rev. Lett. (1987).

For example: Beugnon...Grangier, Nature (2006)

M. Tichy *et al.*, J. Phys. B (2011)

# Hong-Ou-Mandel interference of photons

## Measurement of Subpicosecond Time Intervals between Two Photons by Interference

C. K. Hong, Z. Y. Ou, and L. Mandel

*Department of Physics and Astronomy, University of Rochester, Rochester, New York 14627*

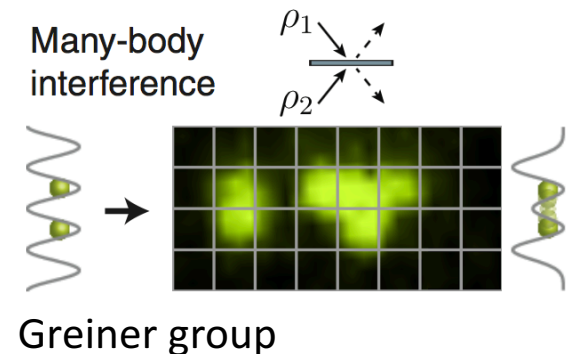
(Received 10 July 1987)

A fourth-order interference technique has been used to measure the time intervals between two photons, and by implication the length of the photon wave packet, produced in the process of parametric down-conversion. The width of the time-interval distribution, which is largely determined by an interference filter, is found to be about 100 fs, with an accuracy that could, in principle, be less than 1 fs.

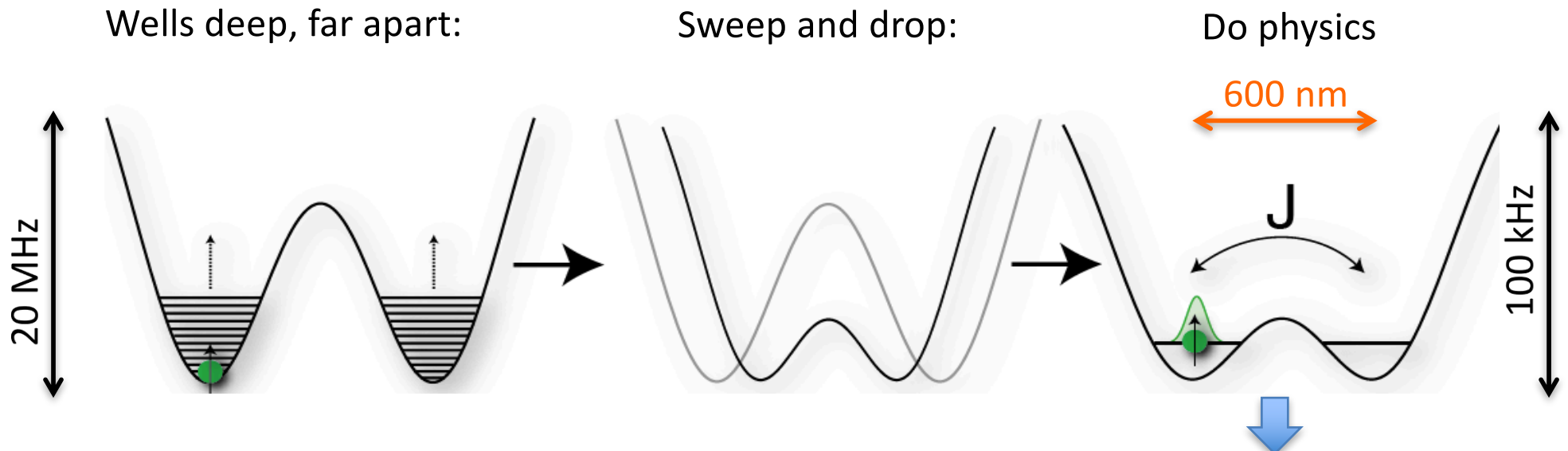
In analogy to original HOM, two-particle quantum interference can diagnose our state purity



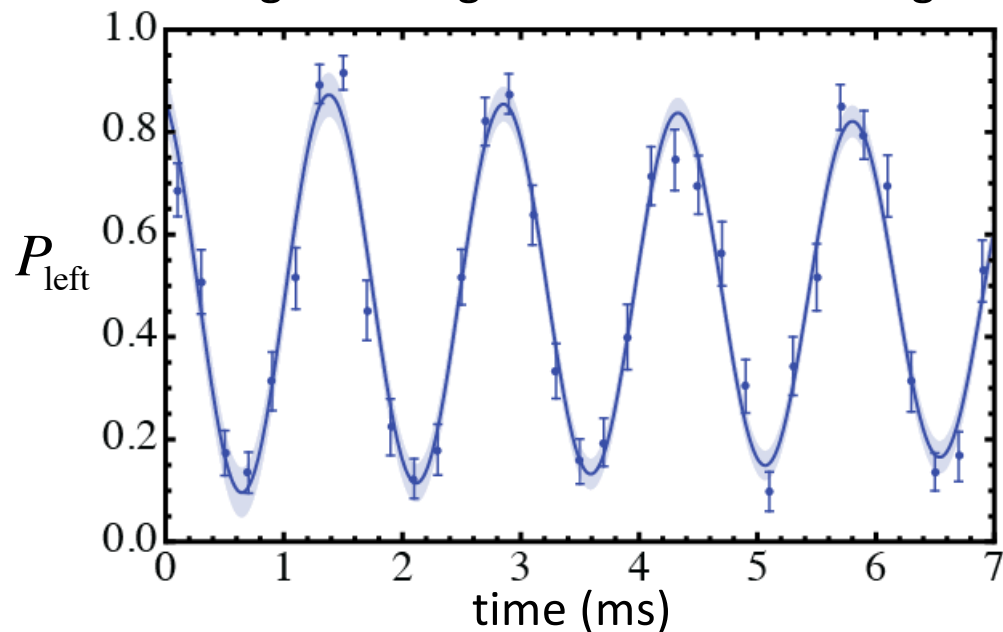
And in QGM experiments now diagnosing many-body states...



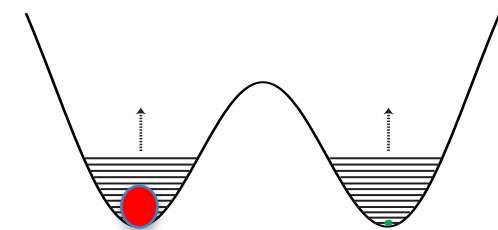
# Our beamsplitter: Tunneling



Single-atom ground-state tunneling



Rapidly pin for imaging



Bias tuned to 0

$$J / 2\pi = 340 \text{ Hz}$$

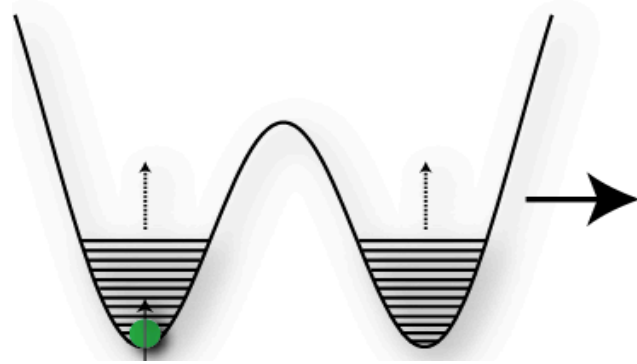
$$U = 0.2J$$



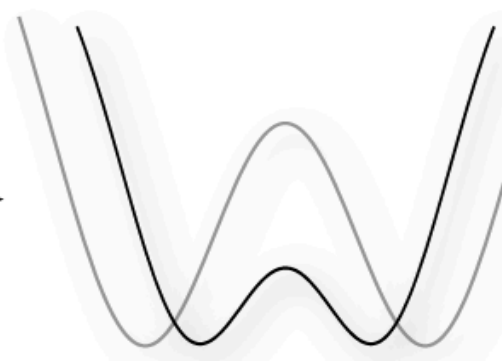
# Initiate tunneling experiments

Wells deep, far apart:

20 MHz



Sweep and drop:

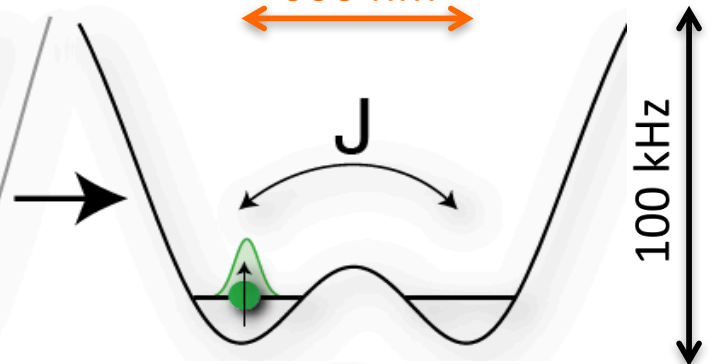


Do physics

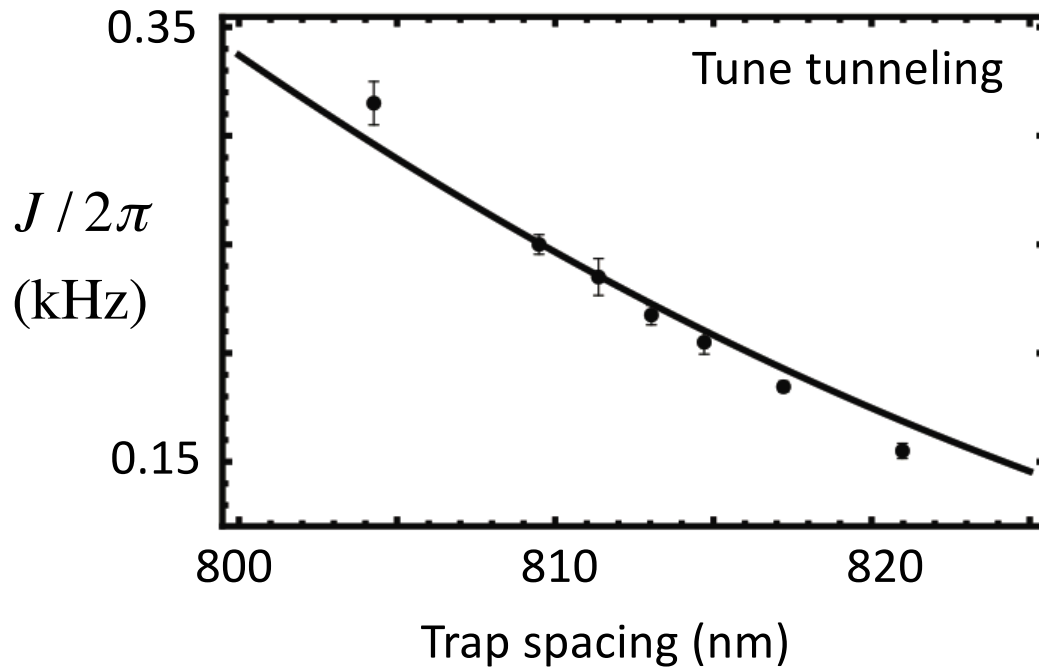
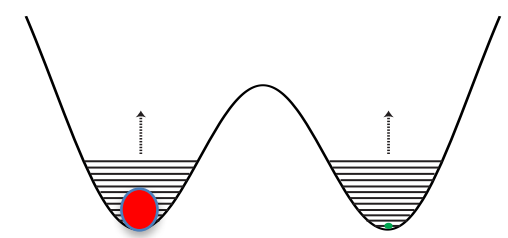
600 nm

J

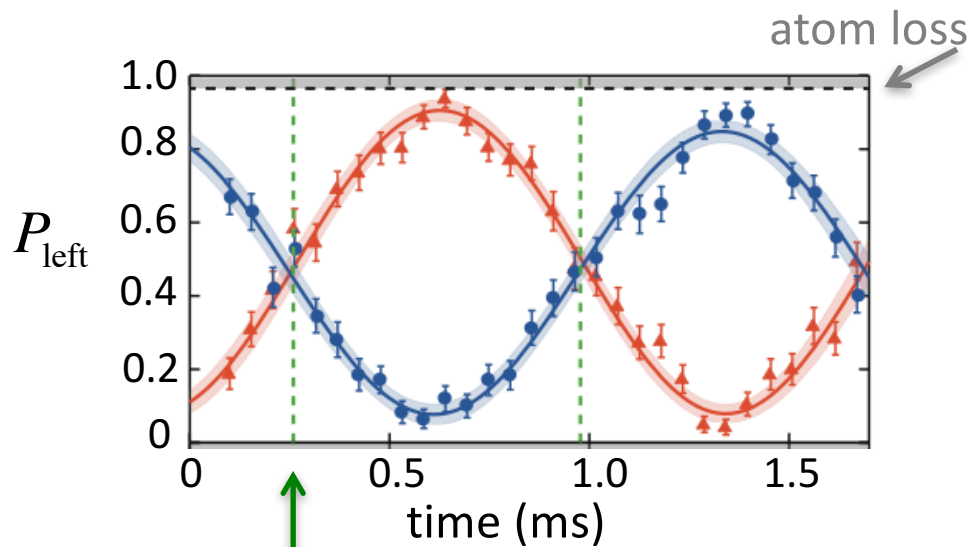
100 kHz



Rapidly pin for imaging

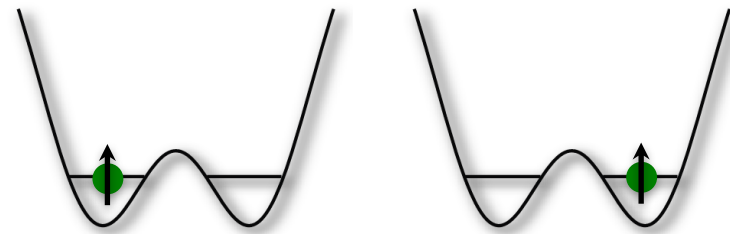


# Tunneling as a beamsplitter

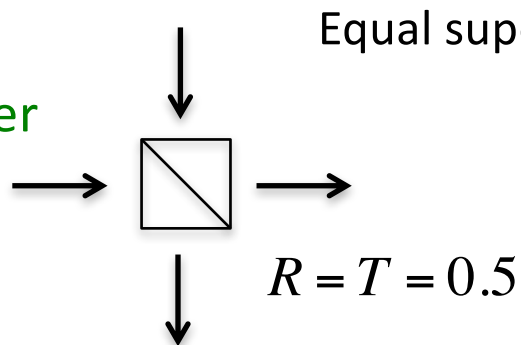


starting on left

starting on right



balanced  
beamsplitter

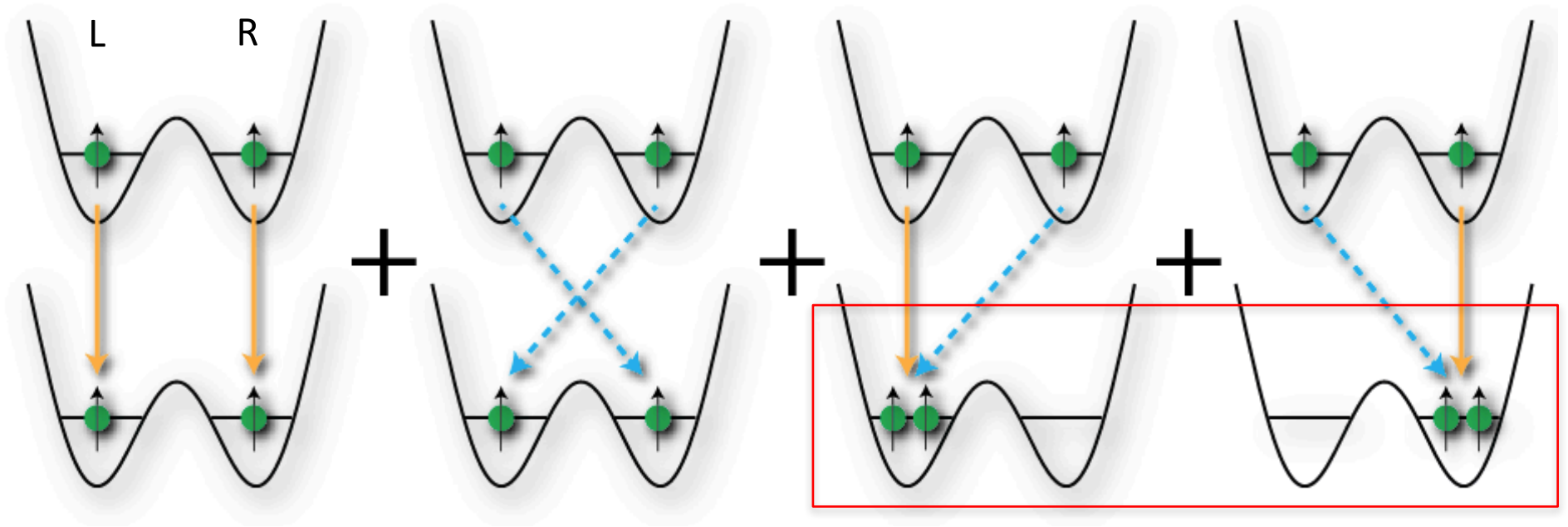


Note:

- identical input and output ports
- $R, T$  vary with tunneling time

# Quantum statistics in atom equivalent

initial:  $\hat{a}_L^\dagger \hat{a}_R^\dagger |0,0\rangle = |1,1\rangle$



Bunching / Bose enhancement

final:  $\frac{1}{2} (\cancel{\hat{b}_L^\dagger \hat{b}_R^\dagger} - \cancel{\hat{b}_R^\dagger \hat{b}_L^\dagger} + i(\hat{b}_L^\dagger)^2 + i(\hat{b}_R^\dagger)^2) |0,0\rangle$

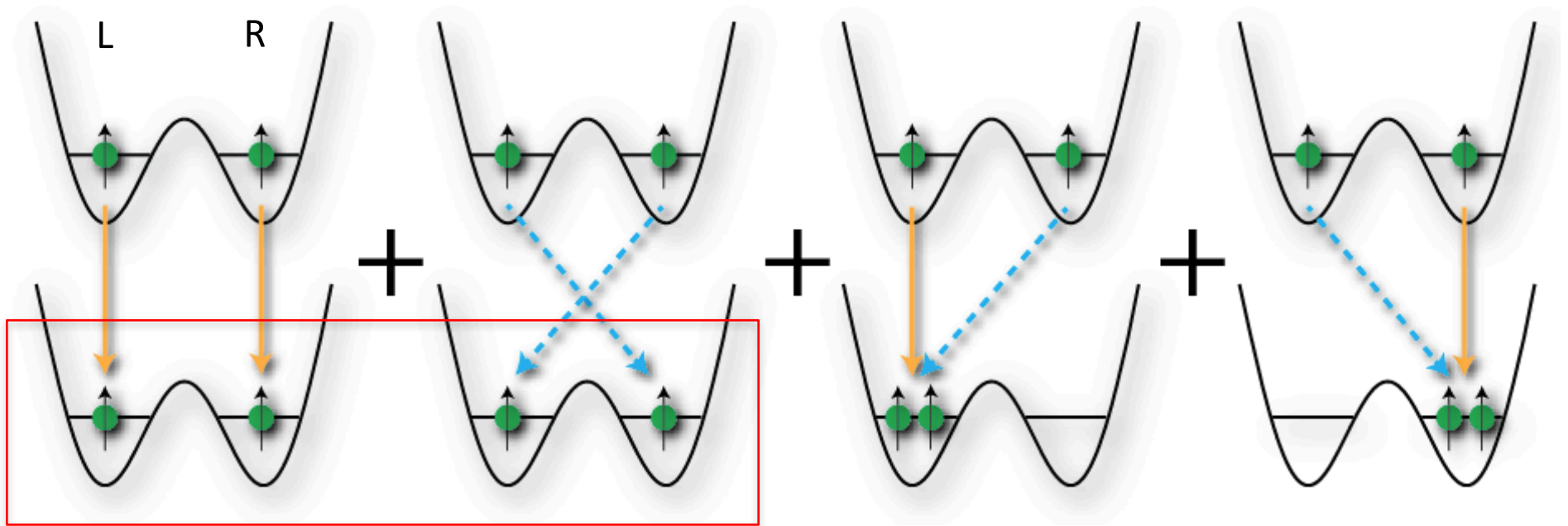
**Bosons**

$\sqrt{2} |2,0\rangle + \sqrt{2} |0,2\rangle$

$P_{11} = 0$

# Quantum statistics in atom equivalent

initial:  $\hat{a}_L^\dagger \hat{a}_R^\dagger |0,0\rangle = |1,1\rangle$



Antibunching / Pauli blocking

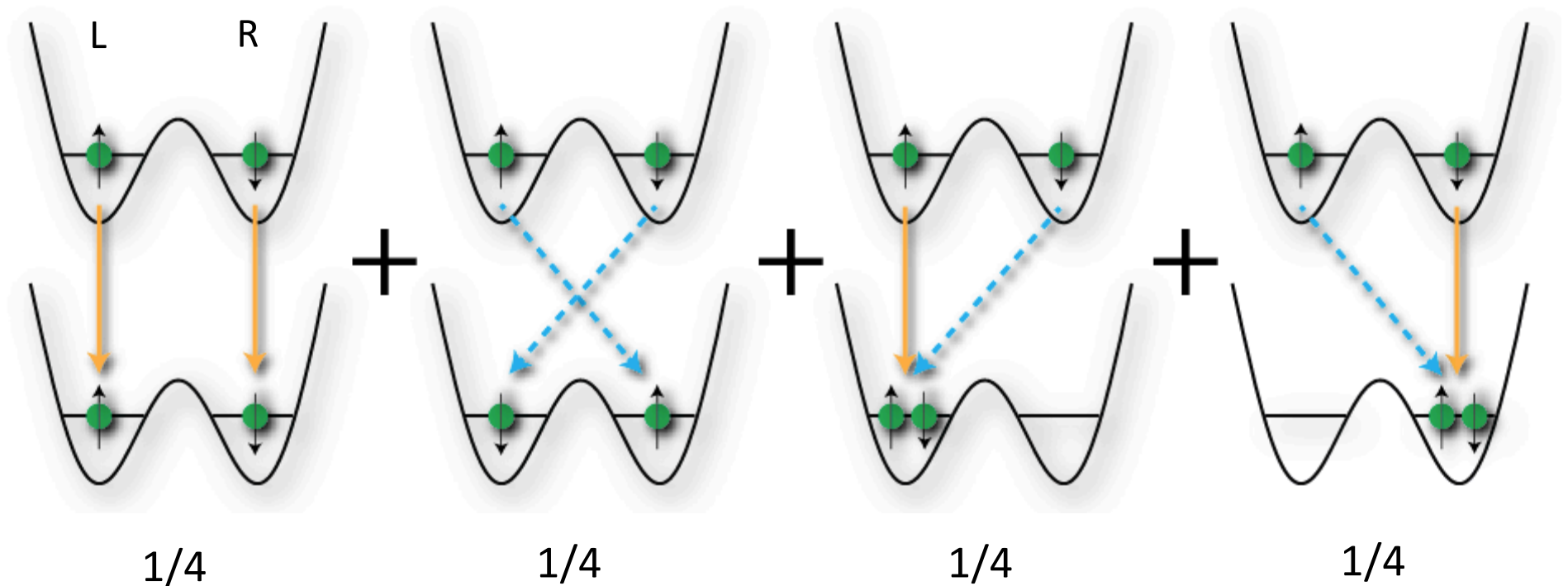
final:  $\frac{1}{2} (\hat{b}_L^\dagger \hat{b}_R^\dagger - \hat{b}_R^\dagger \hat{b}_L^\dagger + i \cancel{(\hat{b}_L^\dagger)^2} + i \cancel{(\hat{b}_R^\dagger)^2}) |0,0\rangle$

$\downarrow$   
 $+ \hat{b}_L^\dagger \hat{b}_R^\dagger$

**Fermions**

$P_{11} = 1$

# Quantum statistics in atom equivalent



flip two independent coins

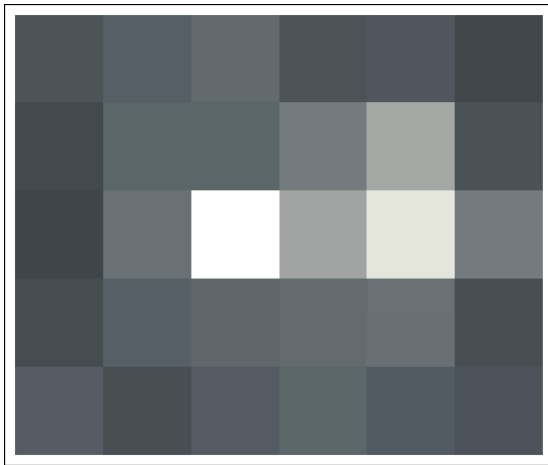
**Distinguishable particles**

(in some other degree of freedom)

$$P_{11} = 0.5$$

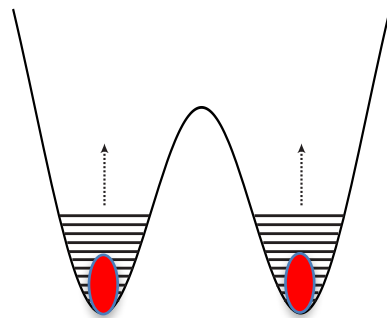
# The experiment: Follow the atoms

set of single-atom images



This measurement used 60% stochastic loading

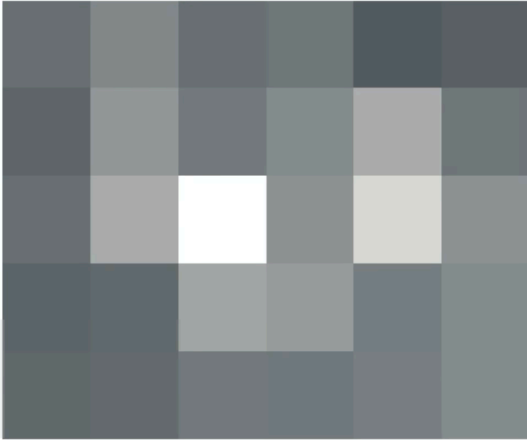
..but ability to follow initial and final states can remove entropy



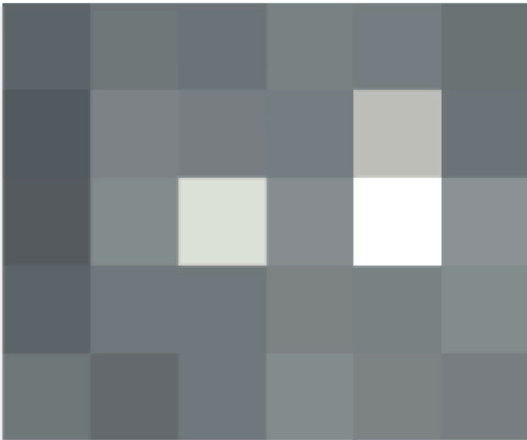
1.6  $\mu\text{m}$

Images: Thermal atoms in deep, separated traps

# The experiment: Follow the atoms



**Image 1**  
(before tunneling)



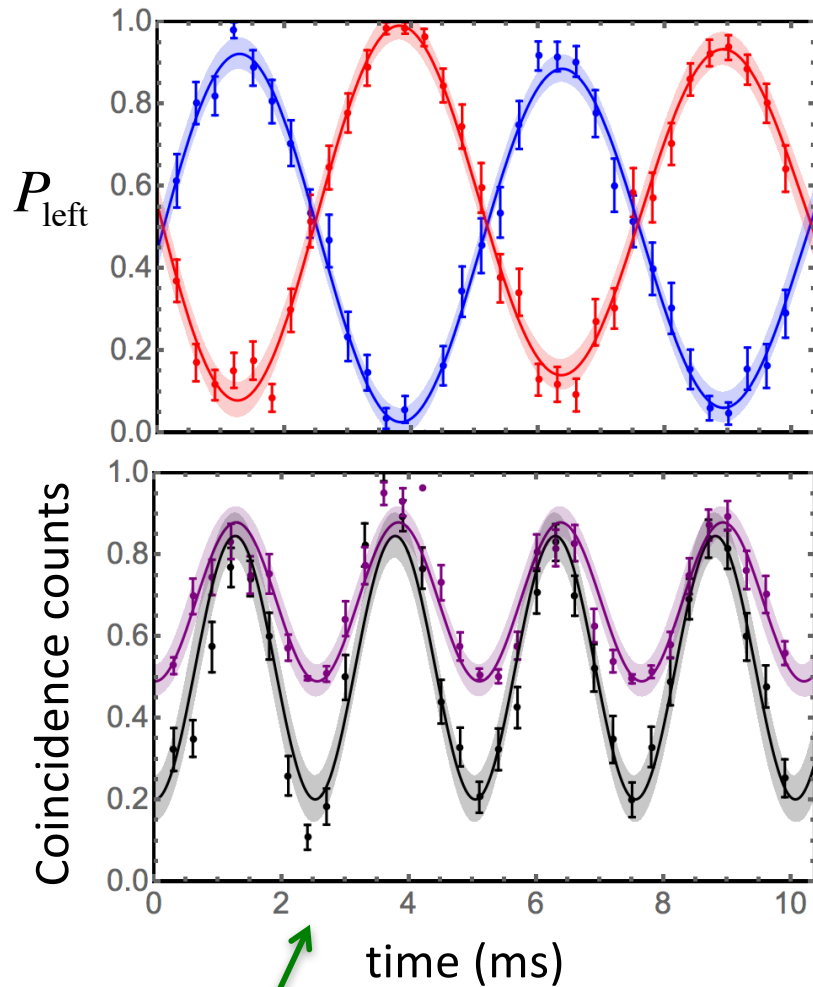
**Image 2**  
(after tunneling)  
(still see only 0 or 1  
light-assisted collisions)

Coincidence count:

Expectation:

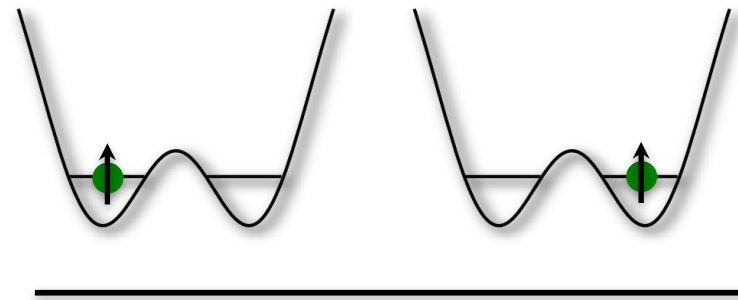
- 0 for bosons
- 50% of time for distinguishable particles (flipping coin)

# Coincidence counts below distinguishable expectation

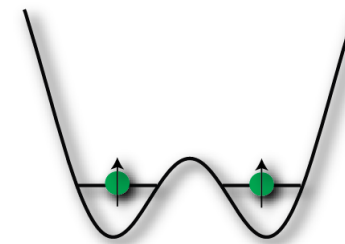


balanced  
beamsplitter

starting on left      starting on right



starting with two atoms

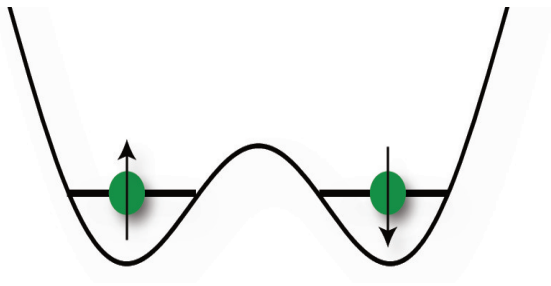


distinguishable  
expectation from  
single-atom data

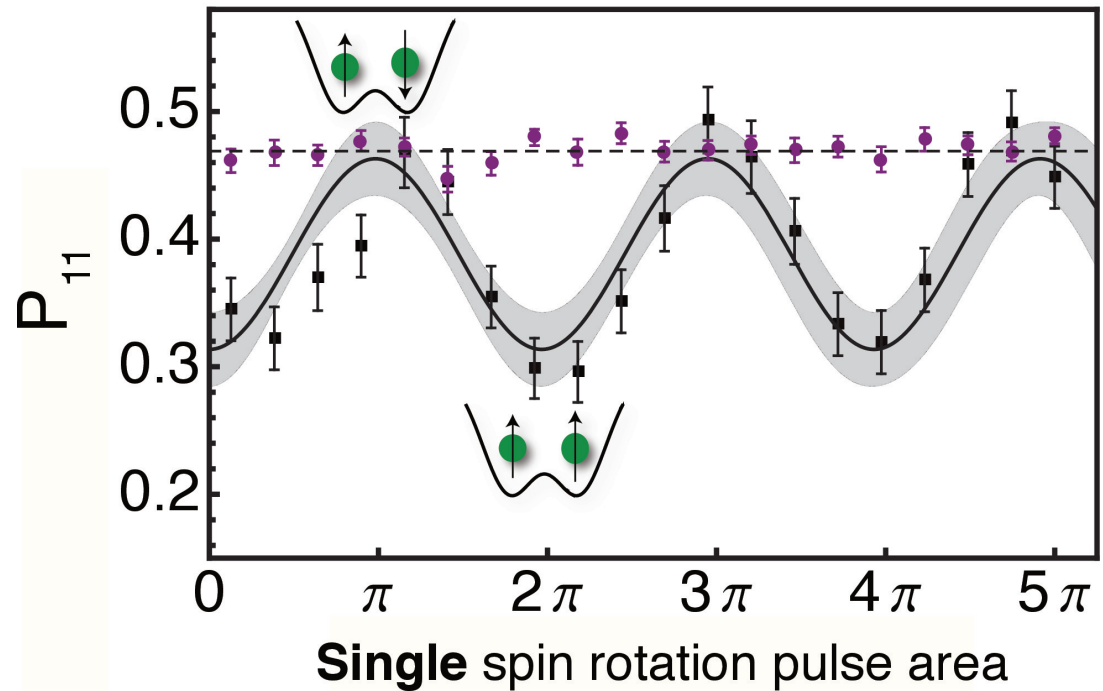


# Tuning distinguishability

Rotate one spin (analogous to polarization with photons)

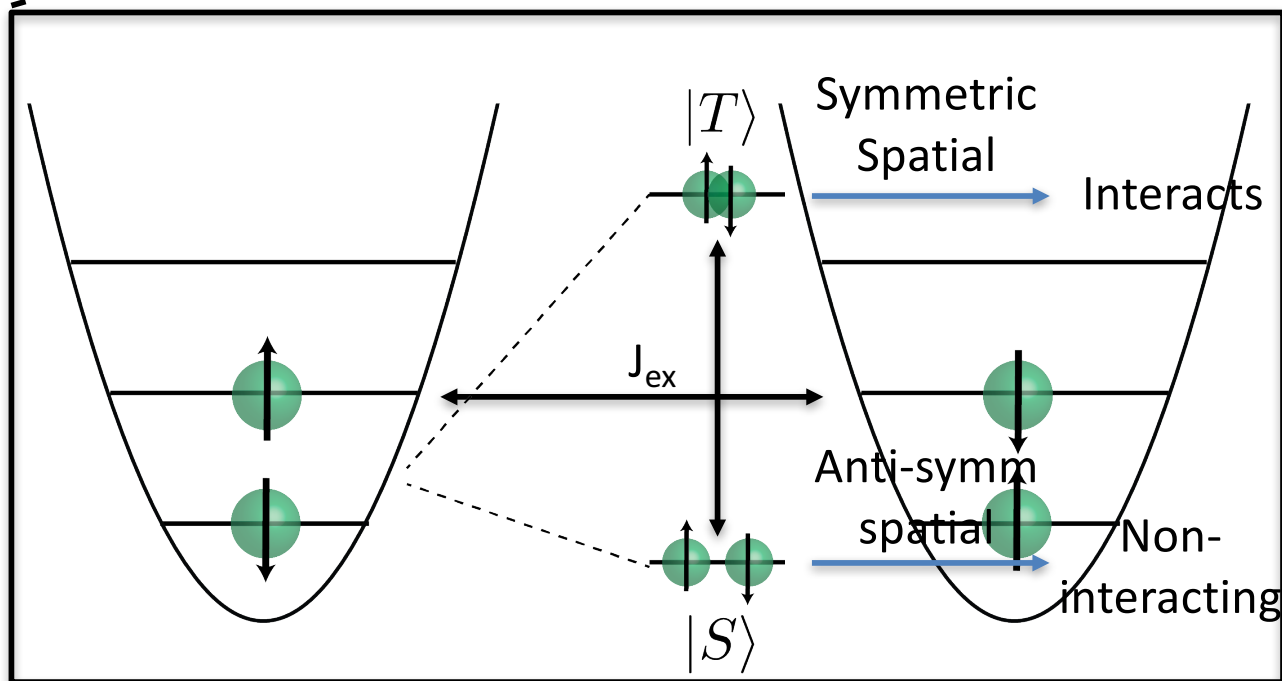
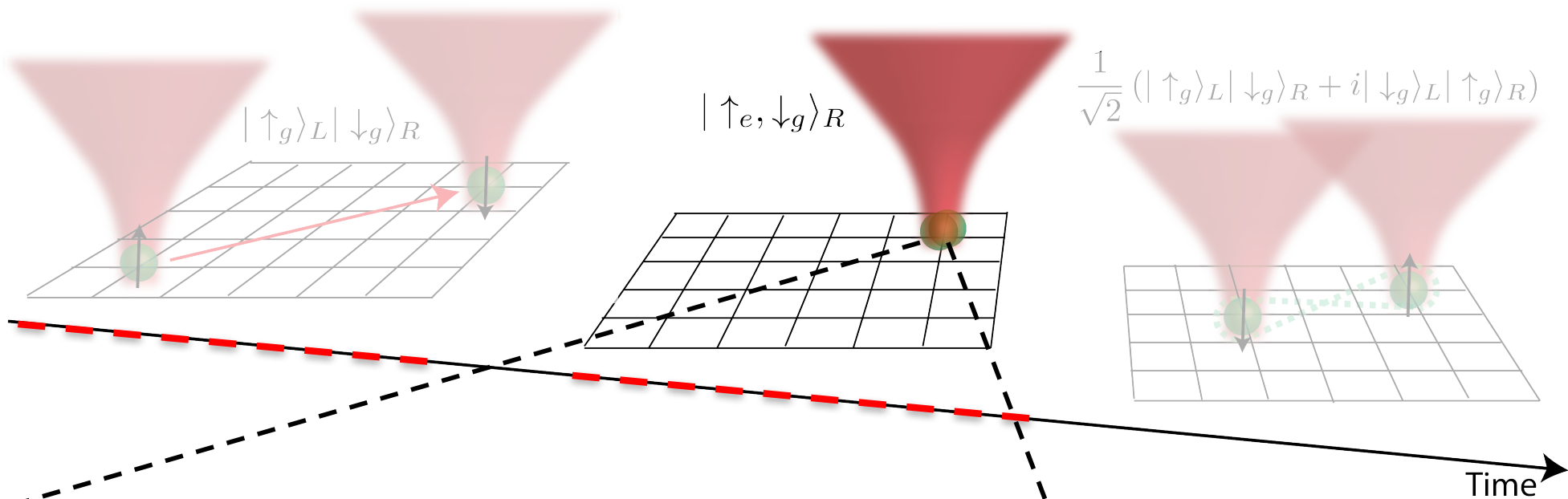


At balanced beamsplitter point



Rabi oscillations on right spin only

# Spin entanglement using spin exchange



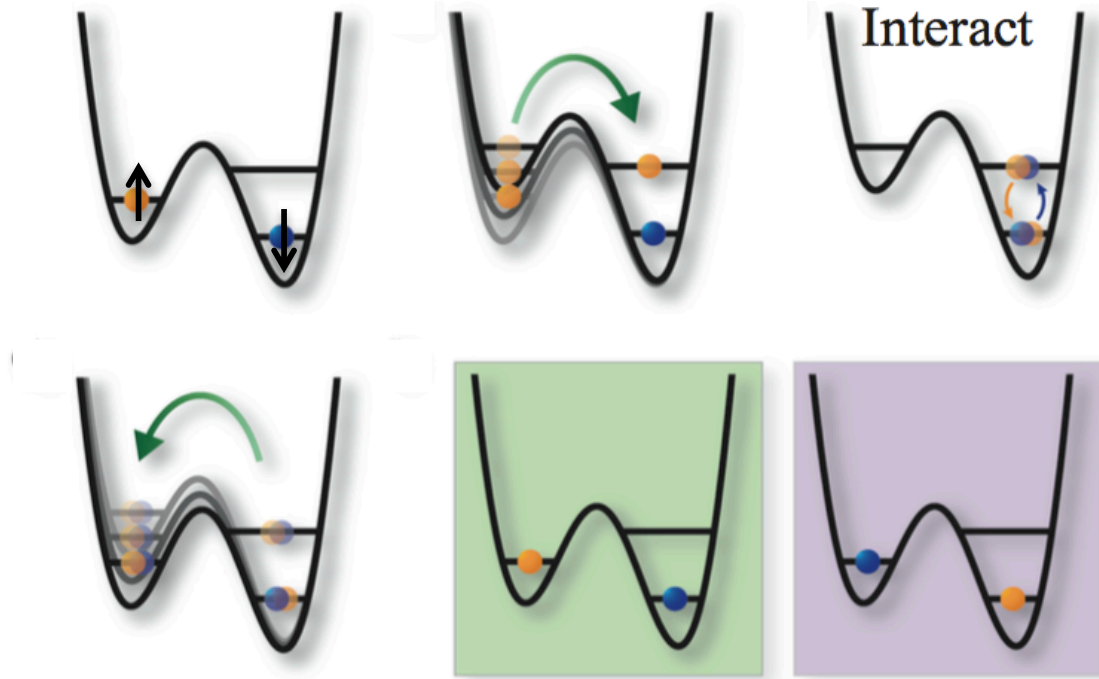
No engineering of spin-dependent interactions required

Energy levels for bosons, but see same dynamics for fermions

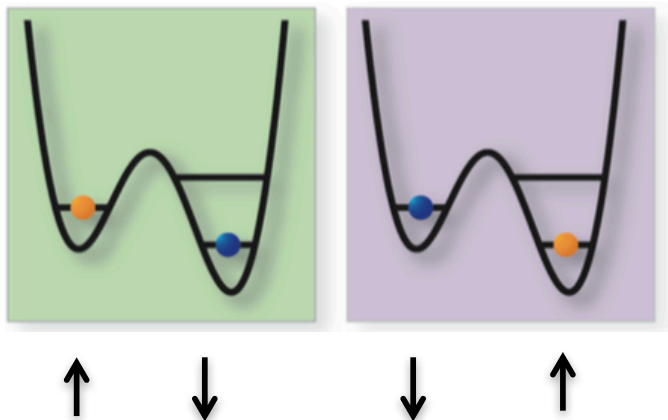
Petta...Goussard, Science (2005)  
 Anderlini...Porto, Nature (2007)  
 G. R. Stewart, RMP (1984)

# Protocol for initializing spin exchange and measuring

Create initial state with single tweezer addressing



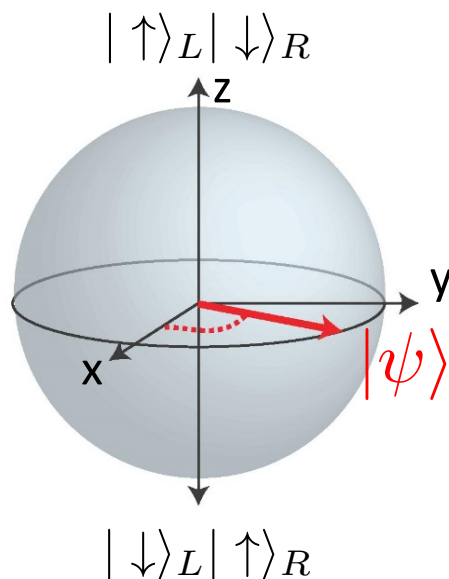
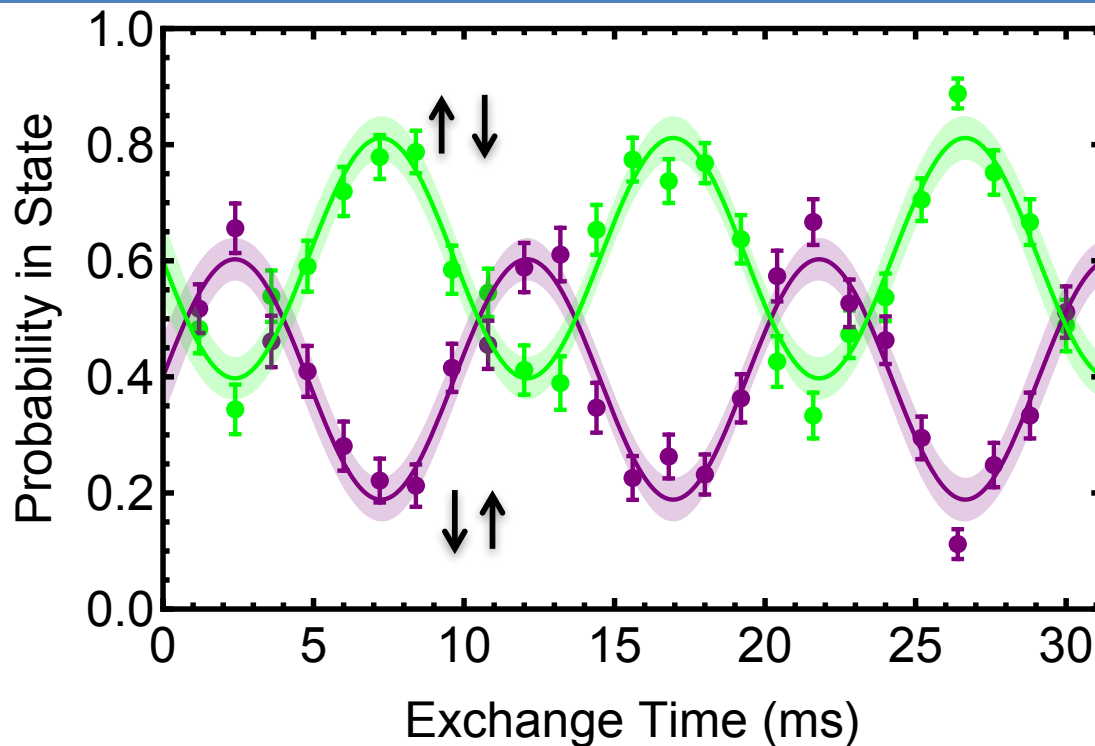
# Spin exchange



Stop at right time to get....

$$\frac{1}{\sqrt{2}}(|\downarrow\rangle_L |\uparrow\rangle_R \pm i |\uparrow\rangle_L |\downarrow\rangle_R)$$

Want to verify phase is preserved upon separating particles



# Observables: Mixing with global microwave rotation



Example:

Singlet maps back to itself

$$\frac{1}{\sqrt{2}} (|\uparrow\rangle_L |\downarrow\rangle_R - |\downarrow\rangle_L |\uparrow\rangle_R) \rightarrow \frac{1}{\sqrt{2}} (|\uparrow\rangle_L |\downarrow\rangle_R - |\downarrow\rangle_L |\uparrow\rangle_R)$$

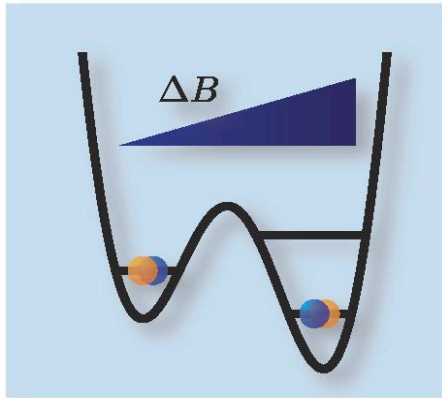
Triplet does not

$$\frac{1}{\sqrt{2}} (|\uparrow\rangle_L |\downarrow\rangle_R + |\downarrow\rangle_L |\uparrow\rangle_R) \rightarrow \frac{1}{\sqrt{2}} (|\uparrow\rangle_L |\uparrow\rangle_R + |\downarrow\rangle_L |\downarrow\rangle_R)$$

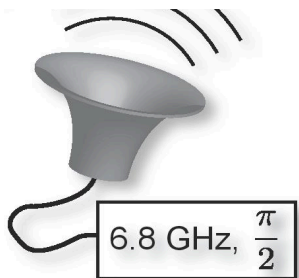
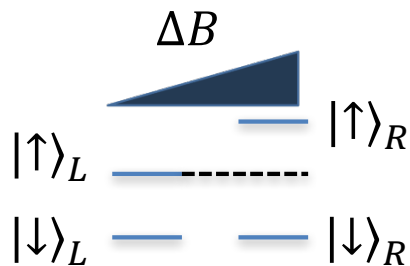
Map to parity (spins same minus spins different)

# Verifying entanglement

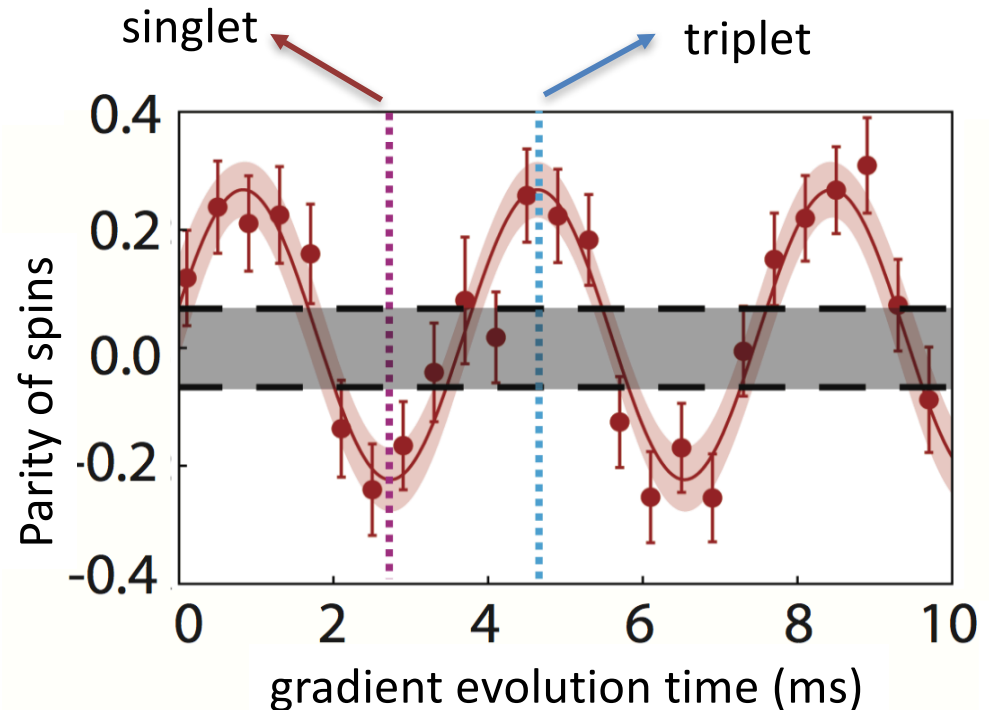
$$\frac{1}{\sqrt{2}}(|\downarrow\rangle_L|\uparrow\rangle_R \pm i|\uparrow\rangle_L|\downarrow\rangle_R)$$



Magnetic field  
breaks degeneracy  
- rotates through  
singlet and triplet



Read out parity with global  
microwave pulse



Spatially resolved entanglement of ultracold atoms:

M. Endres *et al.*, PRL (2015); A. M. Kaufman *et al.*, Nature (2015)

Rydberg atoms: Wilk *et al.* PRL (2010); Zhang *et al.*, PRL (2010)

Entanglement in macroscopic observables:  
for example...

B. Lucke *et al.*, Science 334, 773 (2011)

H. Strobel *et al.*, Science 345, 424 (2014)

# Creating spin entangled state without interaction

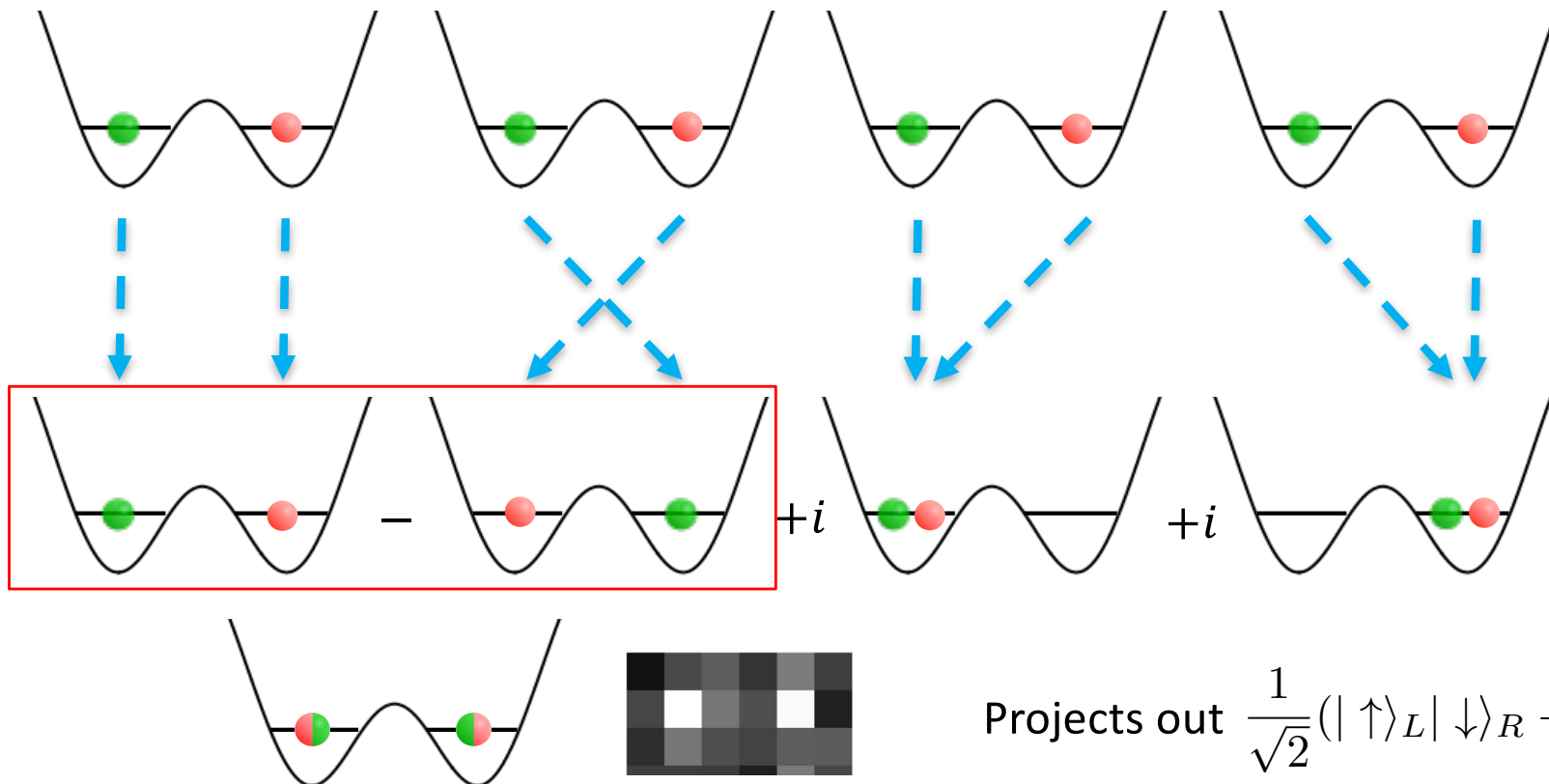
$$\frac{1}{\sqrt{2}}(|\uparrow\rangle_L|\downarrow\rangle_R - |\downarrow\rangle_L|\uparrow\rangle_R)$$

Illustrative thought experiment

Can we achieve this through mode beamsplitter?

No atom interactions...but do have measurement  
(heart of many photon proposals)

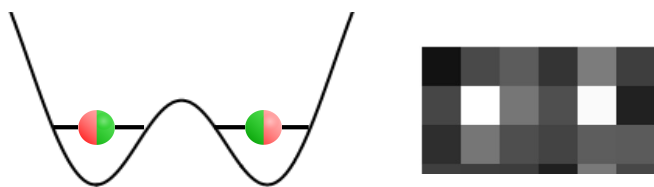
● spin  $|\uparrow\rangle$   
● spin  $|\downarrow\rangle$



Projects out  $\frac{1}{\sqrt{2}}(|\uparrow\rangle_L|\downarrow\rangle_R - |\downarrow\rangle_L|\uparrow\rangle_R)$

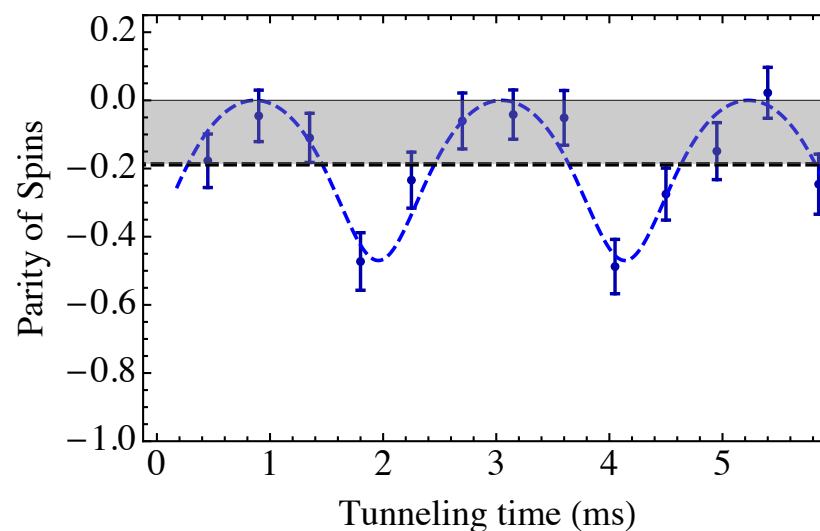
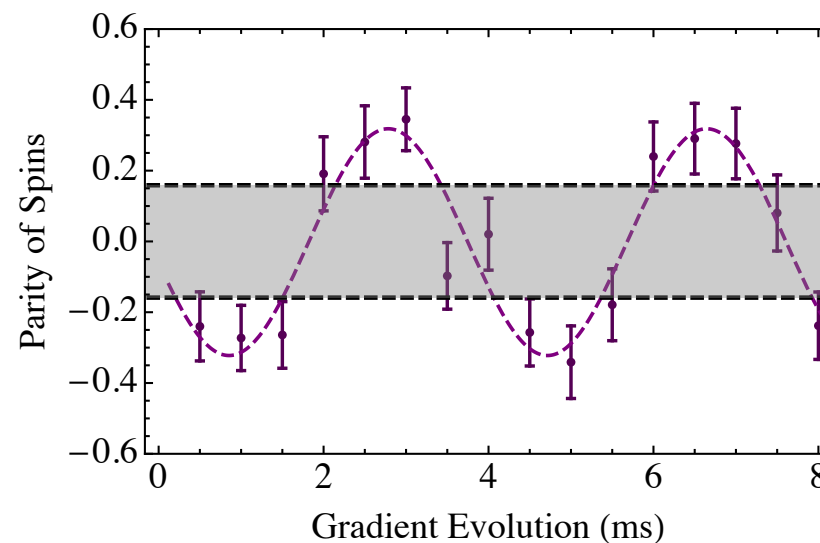
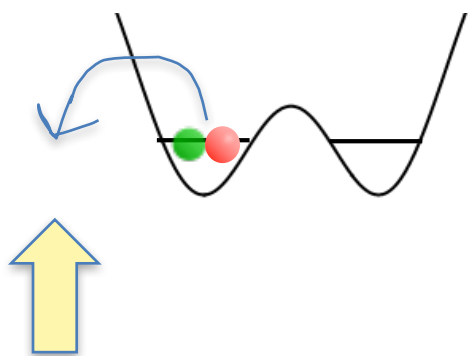
# Creating spin entangled state without interaction

$$\frac{1}{\sqrt{2}}(|\uparrow\rangle_L|\downarrow\rangle_R - |\downarrow\rangle_L|\uparrow\rangle_R)$$



Postselect on

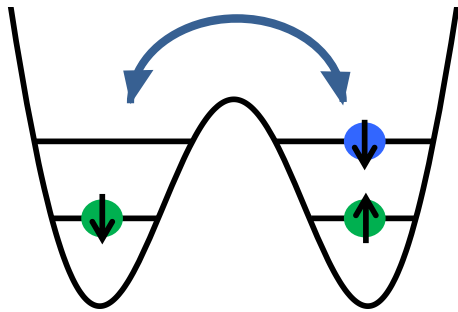
Heralding could make useful....



Preliminary data; more statistical significance required

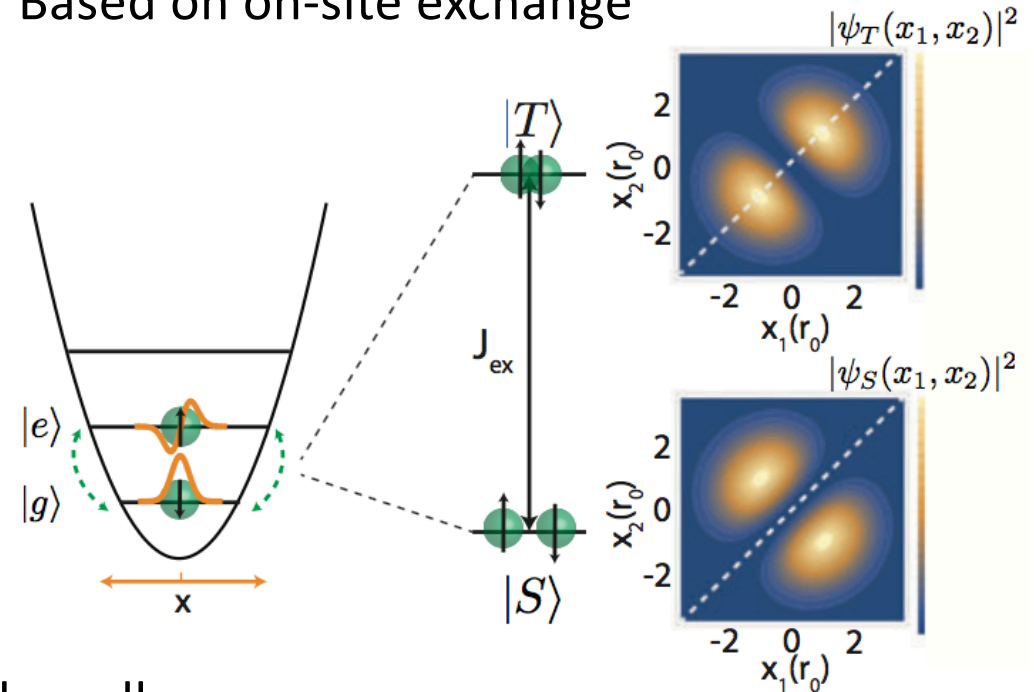


# A 3-atom configuration

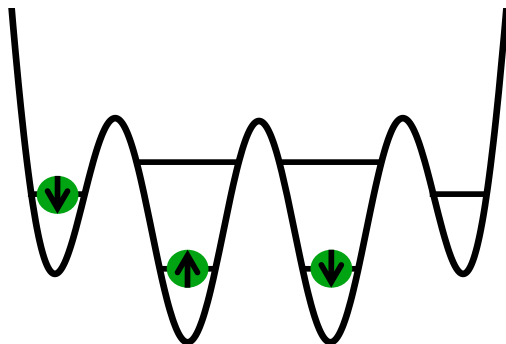


Kondo physics

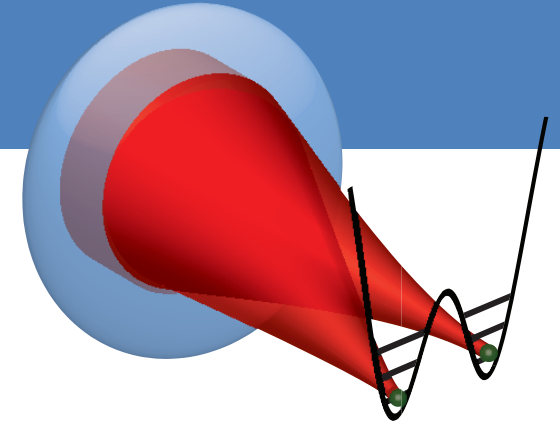
Based on on-site exchange



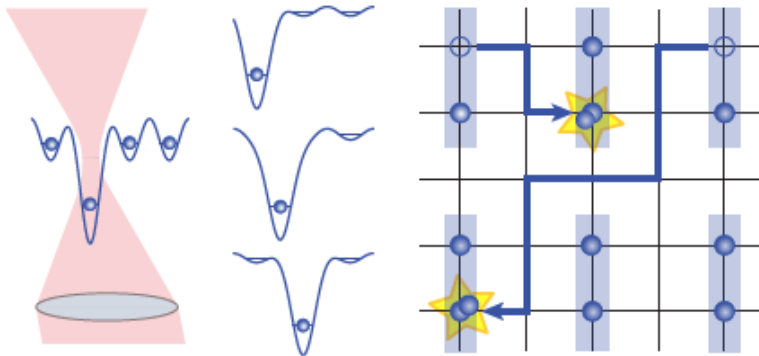
Read out multiple bands with multiple wells



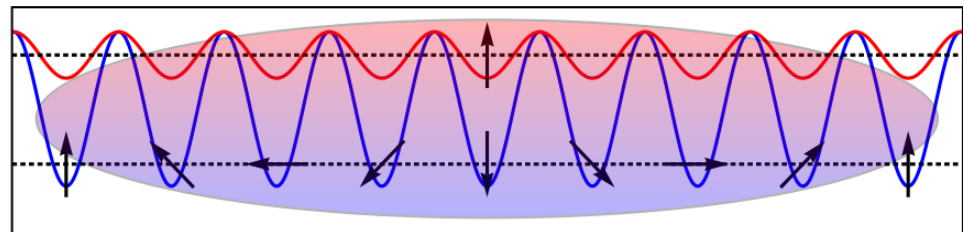
# Conclusions



- Single neutral atoms
  - “single-atom optics” (noninteracting atoms)
  - Extensions to cascaded beamsplitters with boson inputs
  - Use local spin-exchange and movable atoms (interacting atoms)
  - Basic spin-motional coupling has interesting implications even at few-atom level



Weitenberg et al., PRA (2011)



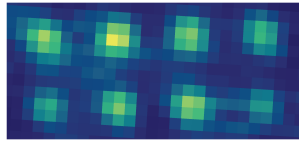
Rey group

# Revisit outline

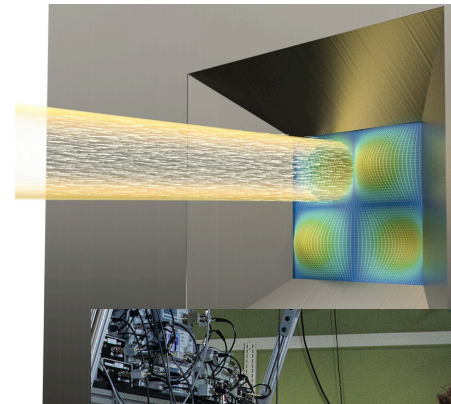
- To consider in context of few-body group
  - New probes and initialization
  - Collisional physics for state preparation
  - While this talk dwells on 2 atoms, 10 - 100 is natural goal
  - Rb – proof of concepts – real gains yet to come with *alkaline earth atoms, molecules, fermions...*
  - More exotic traps with atom spacings 100 nm scale?
  - Adiabatically connect to ground state of less confining trap for delocalized states?
  - Here scattering length small (sometimes effectively zero); could combine with Feshbach resonance
  - Precise measurements that avoid inhomogeneous broadening?

# Our group

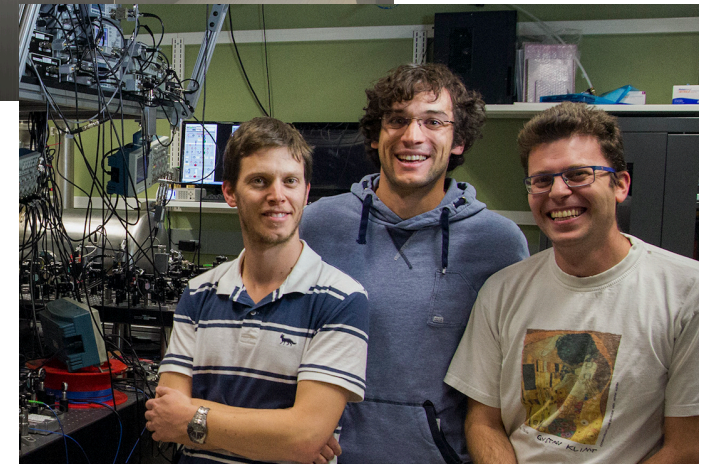
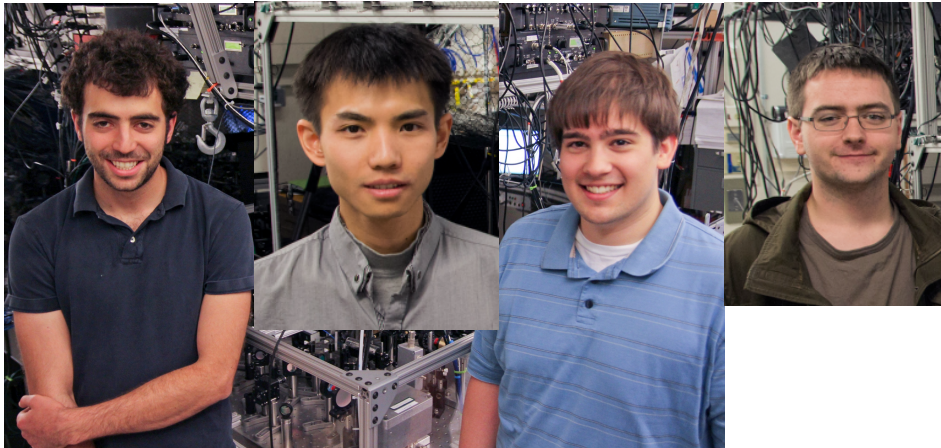
Experiments harnessing control of motion at quantum limits....



...from single neutral atoms



...to mm-scale membrane



Adam Kaufman   Brian Lester   Mark Brown  
Yiheng Lin   Niclas Luick