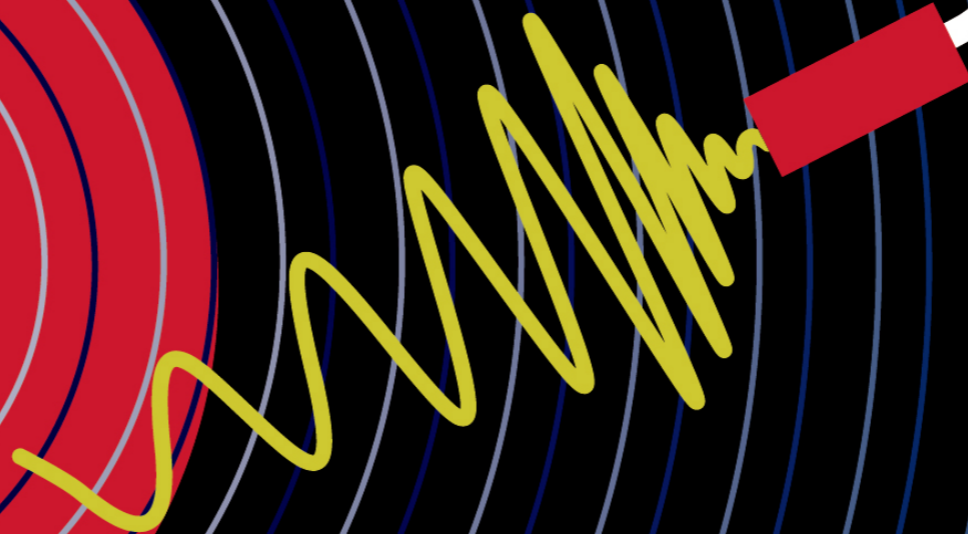
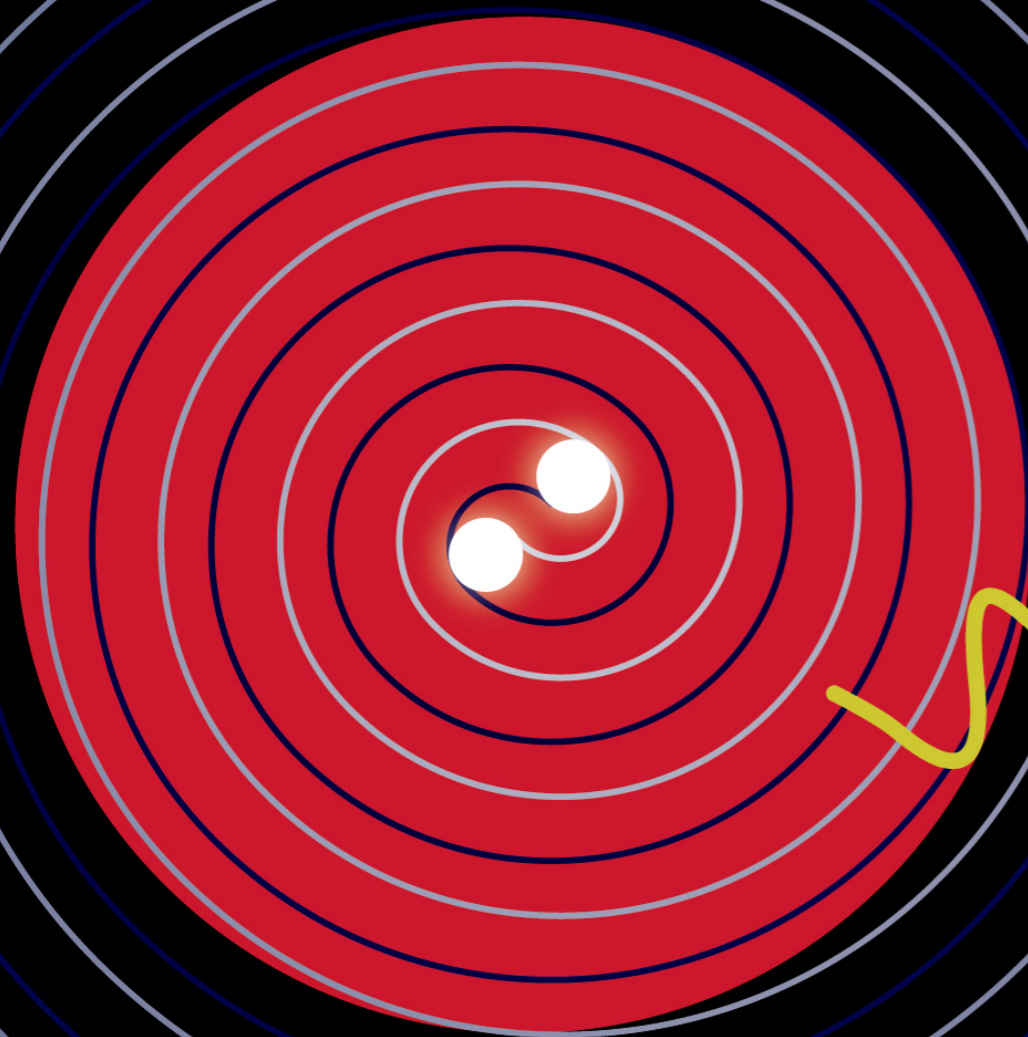


Cosmology with ground-based gravitational-wave detectors

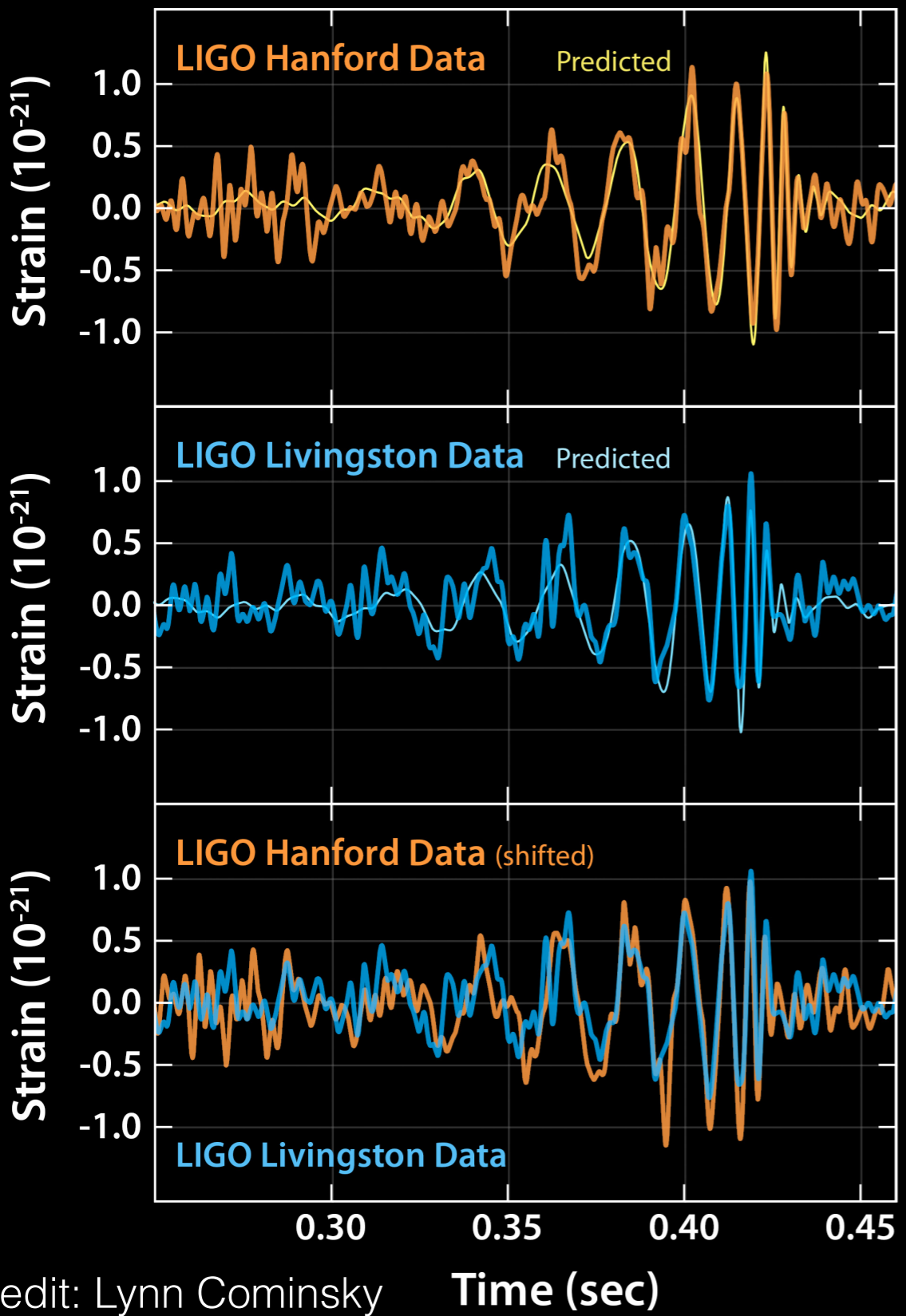


Hsin-Yu Chen

(Black Hole Initiative Fellow, Harvard University)

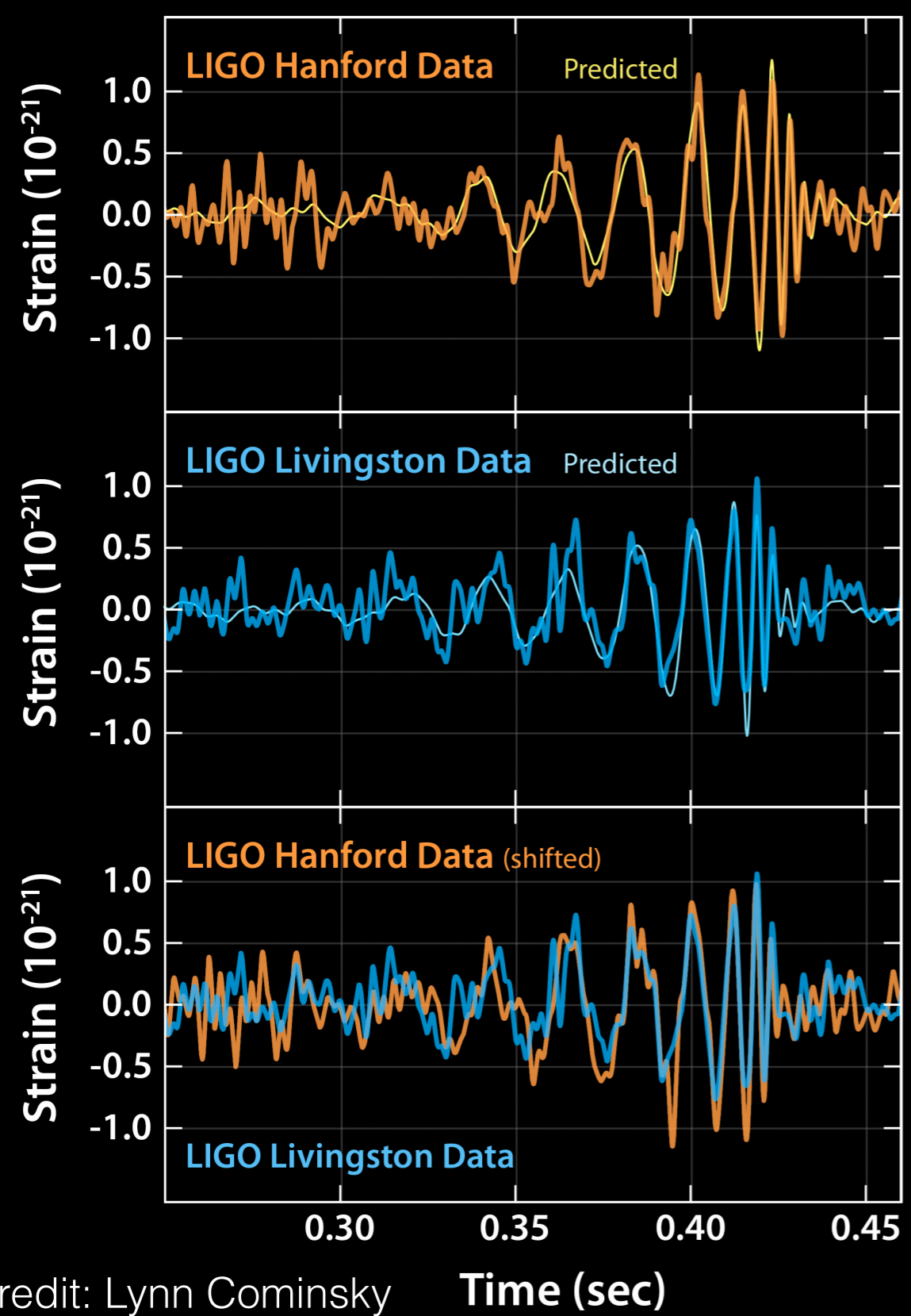
KITP, June 2019

Direct measurement of the luminosity distance



Luminosity Distance $\propto 1/\text{Amplitude}$

Direct measurement of the luminosity distance



Luminosity Distance $\propto 1/\text{Amplitude}$

-Mass, sky location, and binary orientation also affect the amplitude, however these parameters can either be determined independently or marginalized out.

Direct measurement of the luminosity distance

Luminosity Distance $\propto 1/\text{Amplitude}$

-Constrain the cosmological parameters with the redshift and luminosity distance:

$$D_L = c(1+z) \int_0^z \frac{dz'}{H(z')}$$

$$H(z) = H_0 \sqrt{\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda(1+z)^{3(1+w_0+w_a)} e^{-3w_a z/(1+z)}}$$

Direct measurement of the luminosity distance

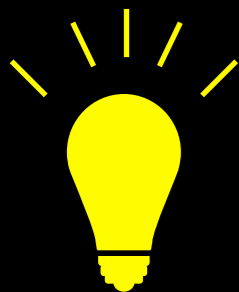
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Different methods for gravitational-wave cosmology



Electromagnetic counterpart

Without electromagnetic counterpart

Unique redshift

Multiple possible redshifts

No redshift

●
 z_{\star}

●
 z_1

●
 z_2

●
 z_3

●
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●
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●
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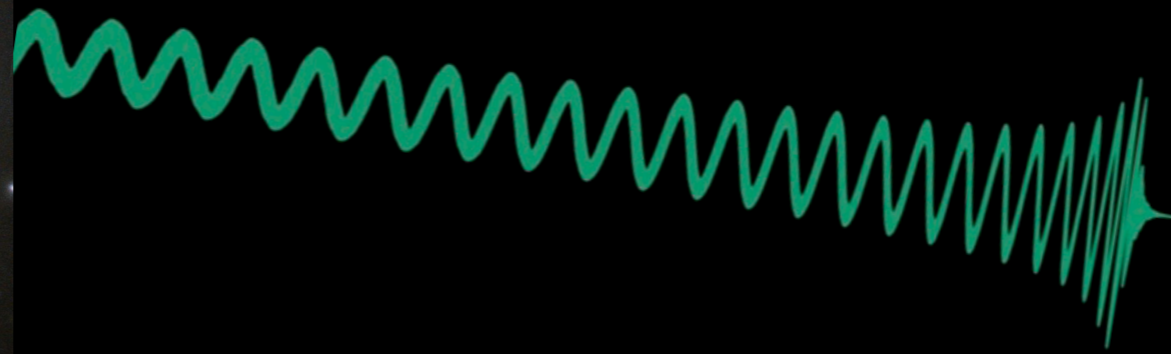
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z_5

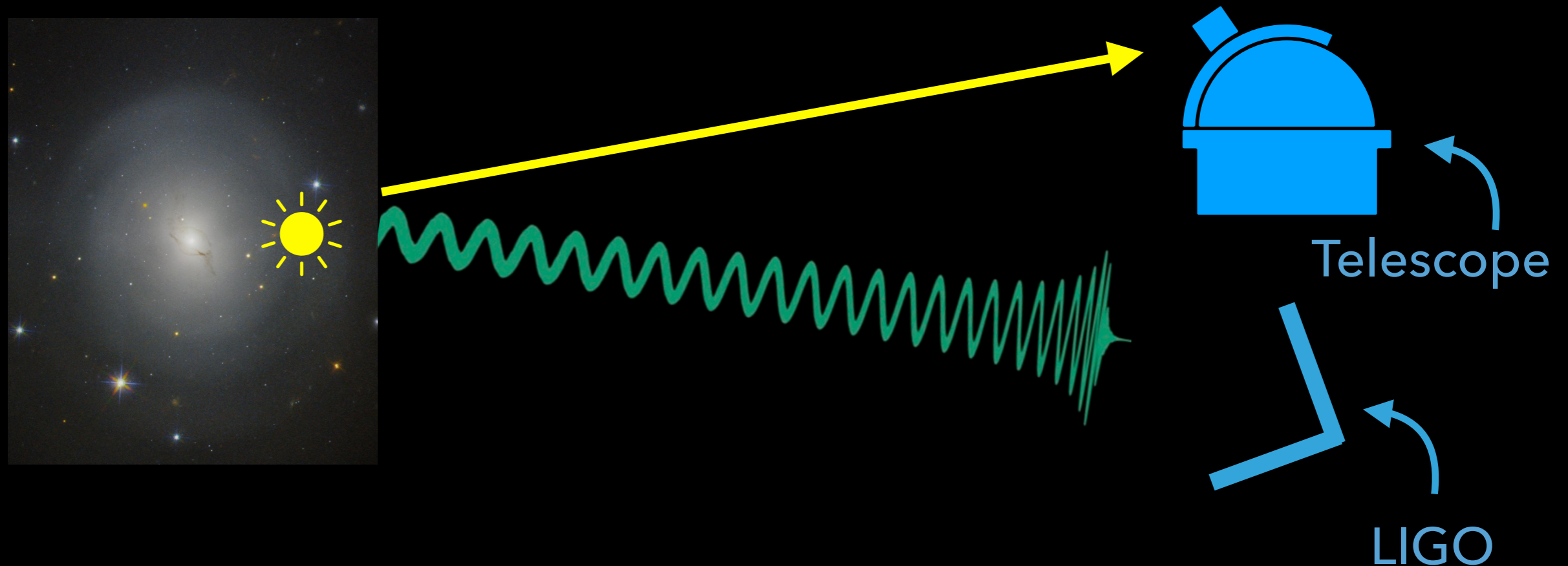
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Determine the redshift of gravitational-wave source with the host galaxy ["Standard Siren"]



Determine the redshift of gravitational-wave source with the host galaxy ["Standard Siren"]



Counterpart method:

Find the host galaxy of the electromagnetic counterpart.

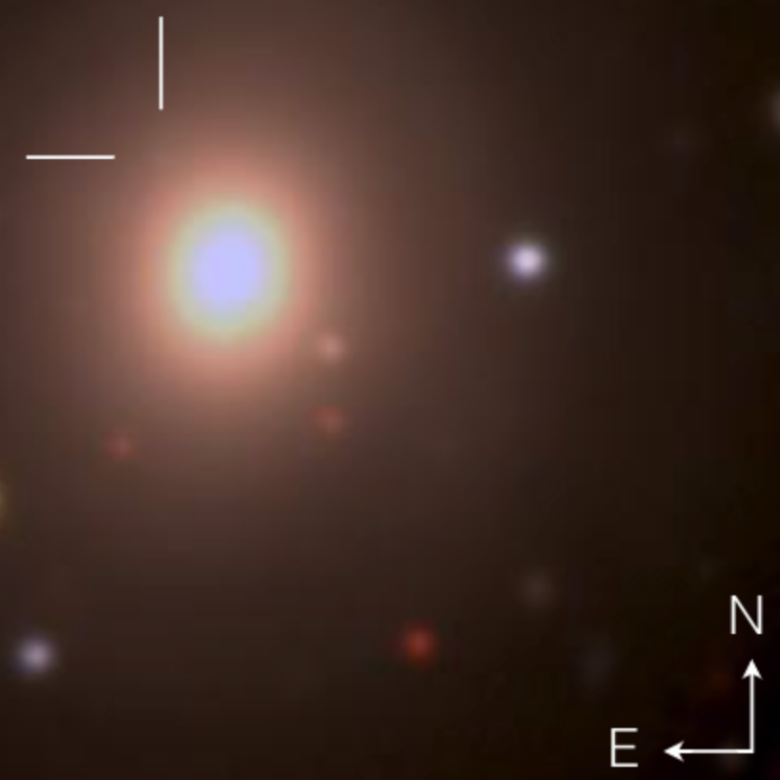
Schutz, Nature, 1986 / Holz & Hughes, ApJ, 2005

The first standard siren measurement with an electromagnetic counterpart

GW170817
DECam observation
(0.5–1.5 days post merger)



GW170817
DECam observation
(>14 days post merger)



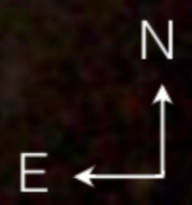
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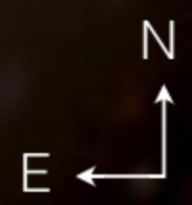


From LIGO-Virgo:

$$D_L = 43^{+2.9}_{-6.9} \text{ Mpc}$$



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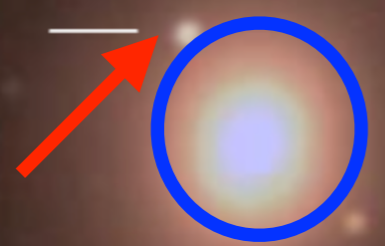


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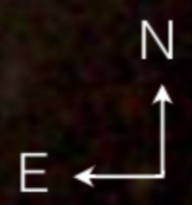
From electromagnetic:

$$v = 3017 \pm 166 \text{ km/s}$$

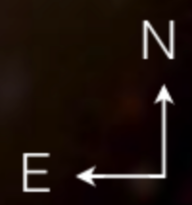


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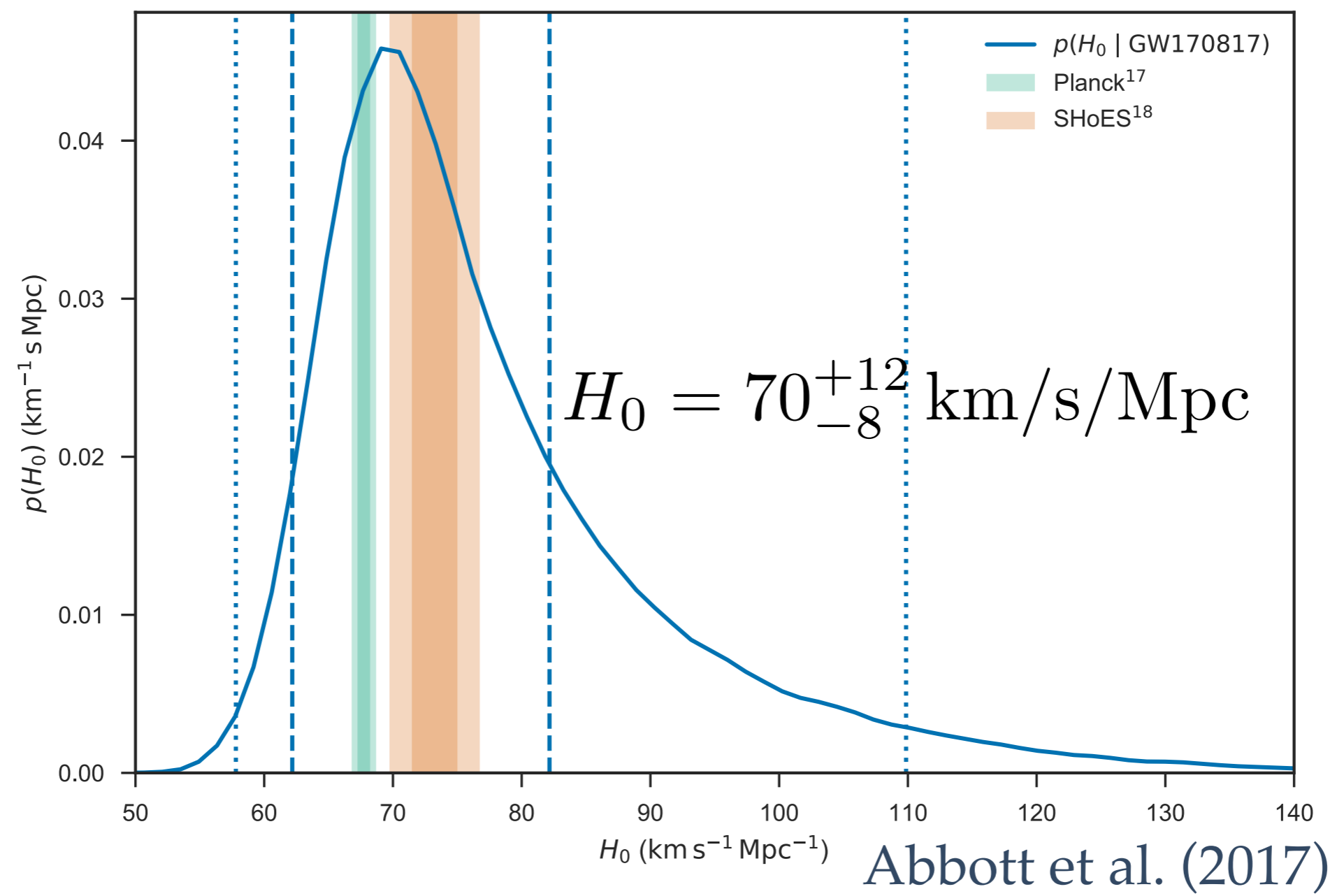


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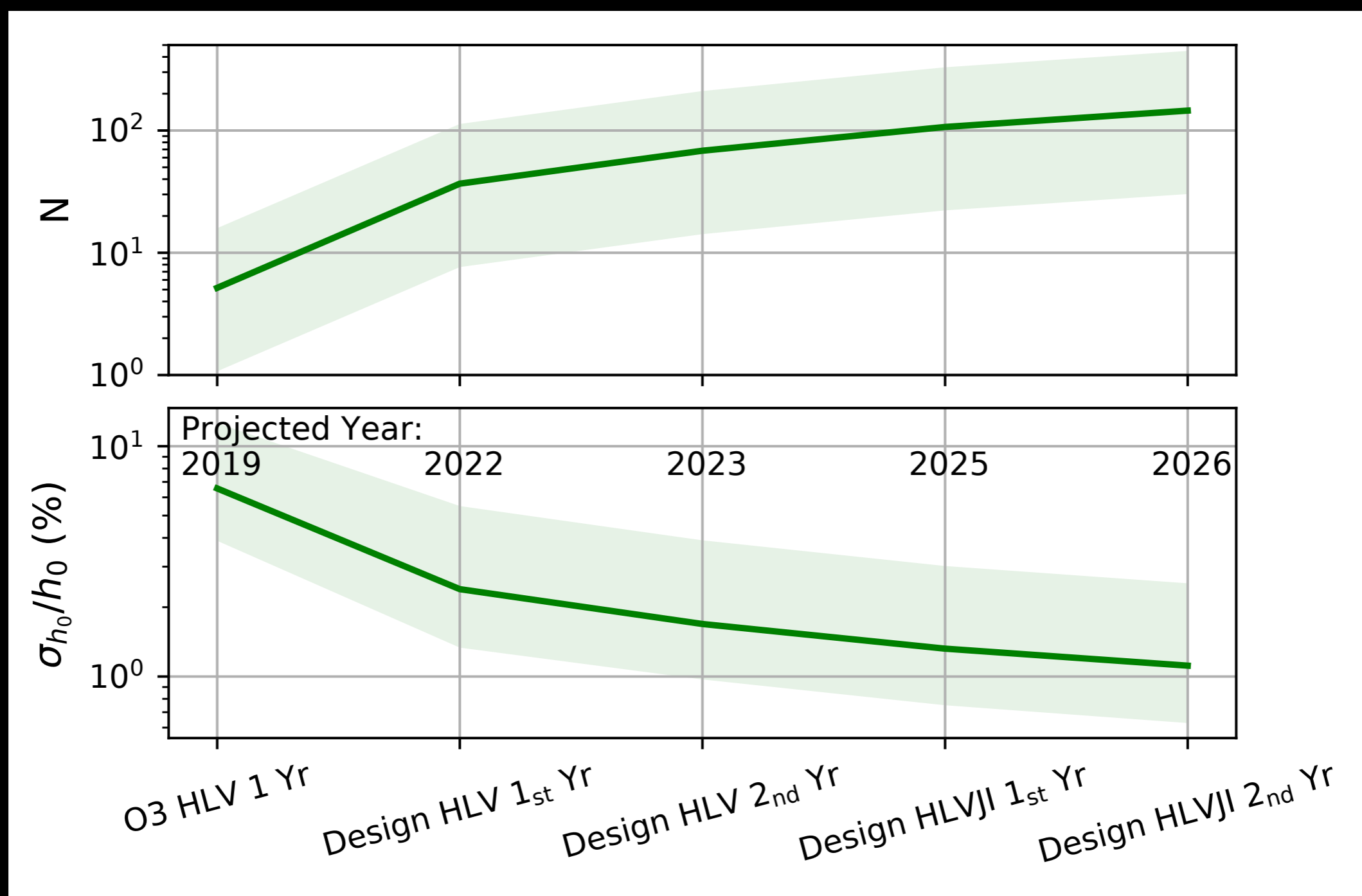
GW170817
DECam color
(0.5–1.5 μm)

From

$D_L =$

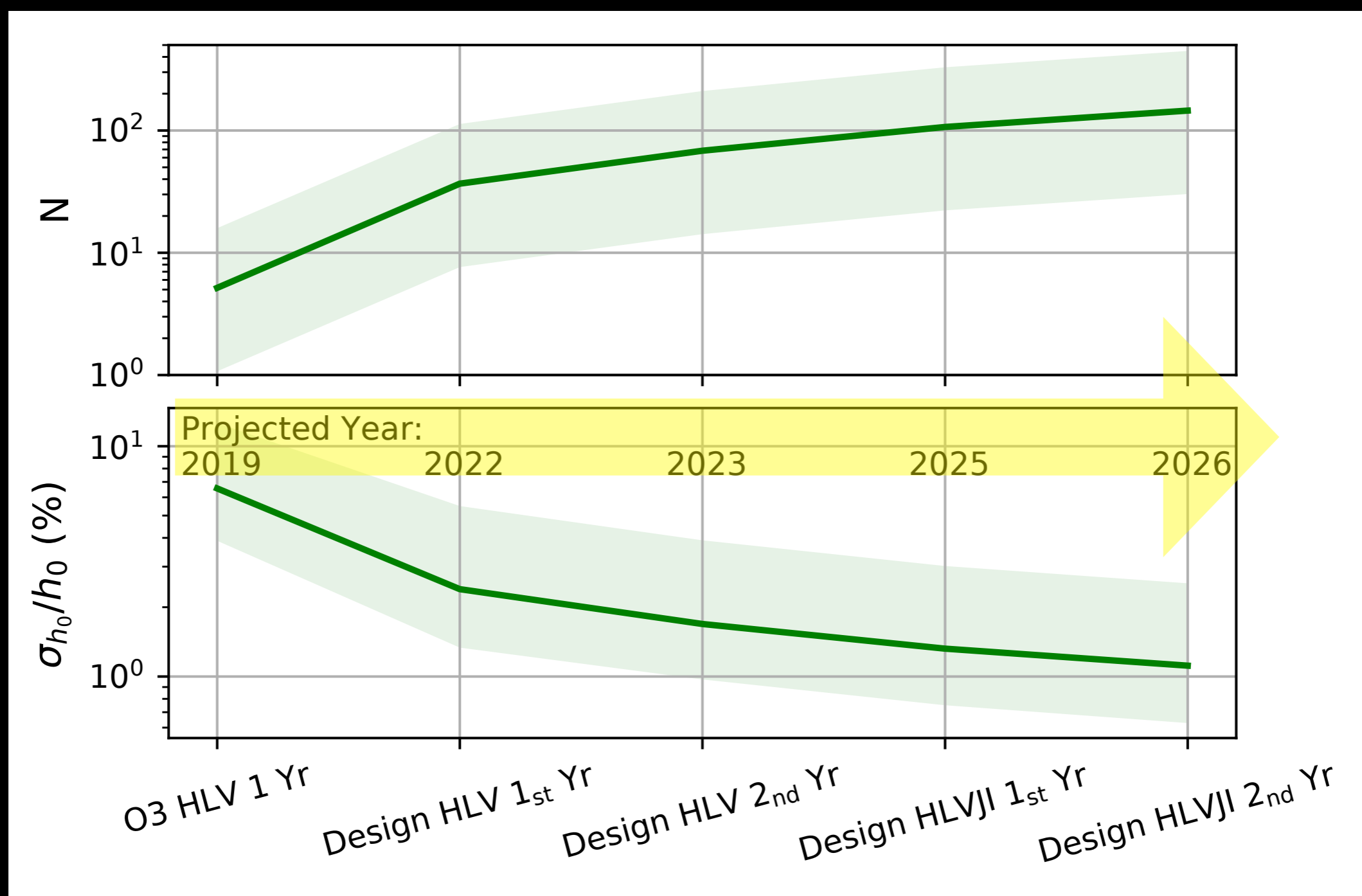


2% Hubble constant measurement within five years



Chen, Fishbach, Holz , Nature, 2018

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Chen, Fishbach, Holz, Nature, 2018

2% in five years

8

- **Realistic distance posteriors were used.**

Chen & Holz (2016) / Chen et al. (2018)

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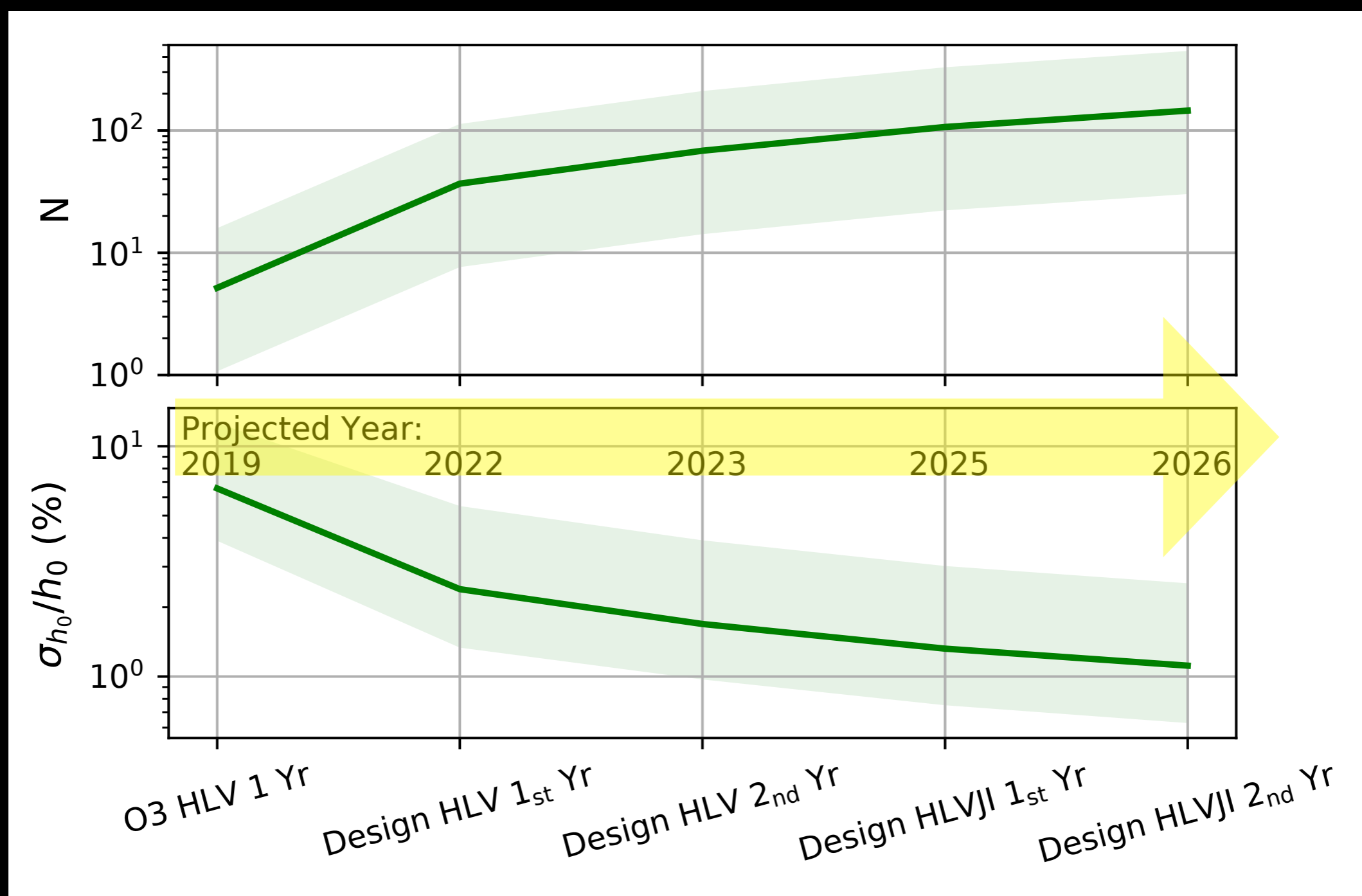
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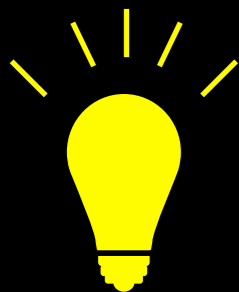
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2% Hubble constant measurement within five years



Chen, Fishbach, Holz, Nature, 2018

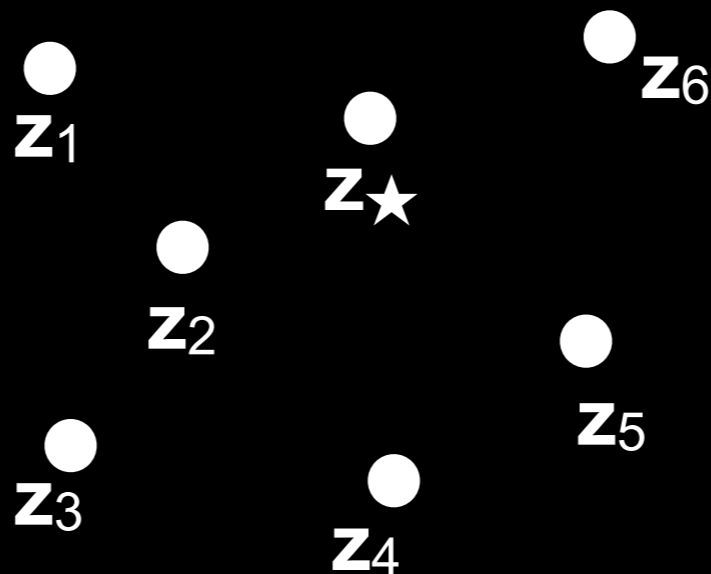
Different methods for gravitational-wave cosmology



Electromagnetic counterpart

Without electromagnetic counterpart

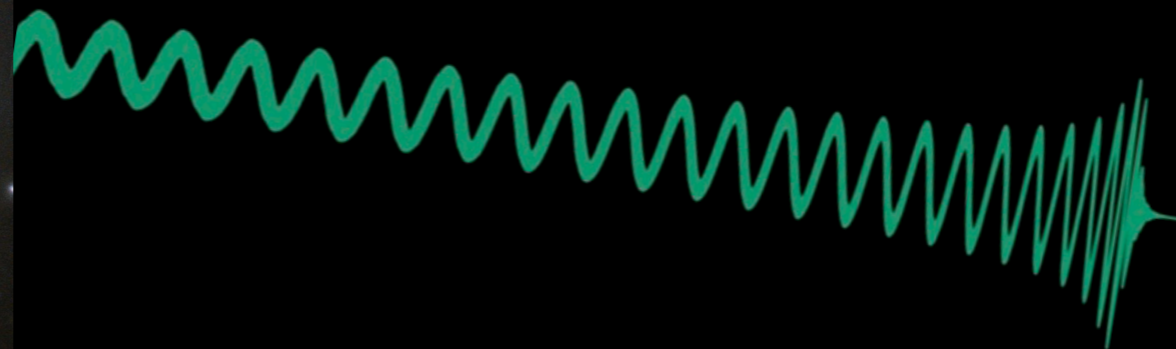
Multiple possible redshifts



No redshift

$z = ??$

Determine the redshift of gravitational-wave source with the host galaxy ["Standard Siren"]

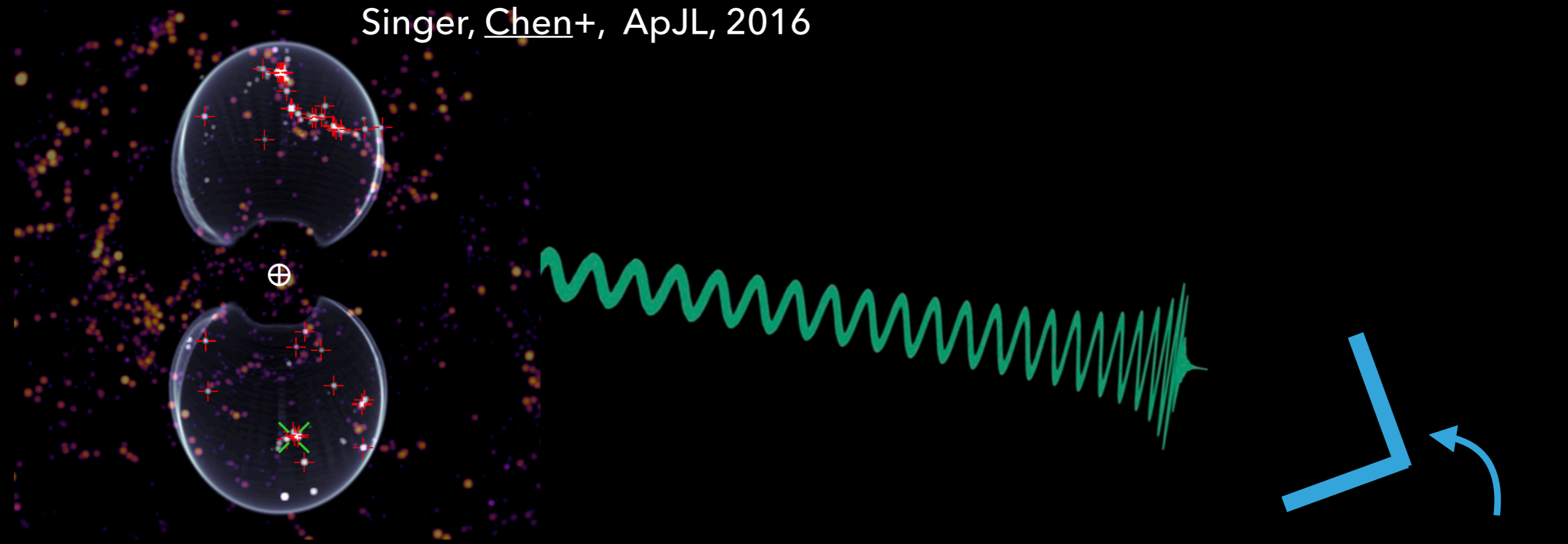


Statistical method: Schutz, Nature, 1986/ Del Pozzo, PRD, 2011

Combine the redshifts of all possible host galaxies.

Determine the redshift of gravitational-wave source with the host galaxy ["Standard Siren"]

Singer, Chen+, ApJL, 2016



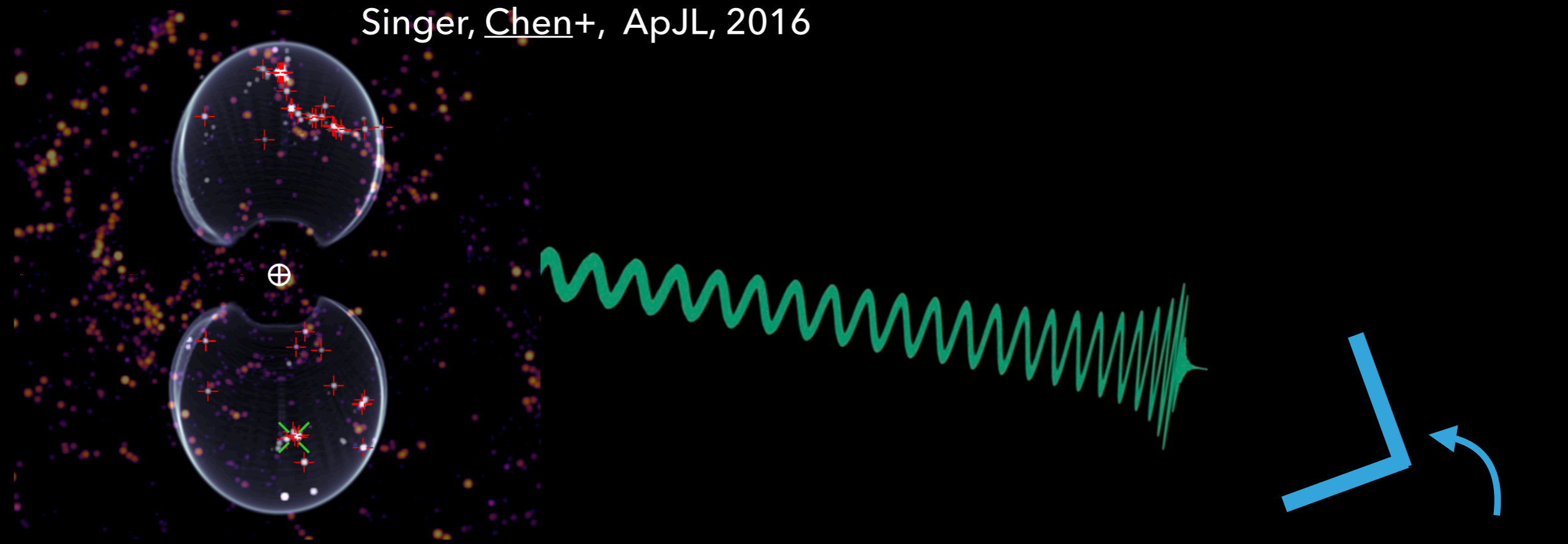
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LIGO

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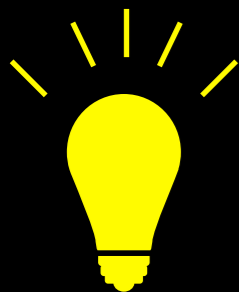
-GW170814: $H_0 = 75.2^{+39.5}_{-32.4}$ km/s/Mpc
(Dark Energy Survey Year 3 data)

DES & LVC, 2019

-GW170817: $H_0 = 76^{+48}_{-23}$ km/s/Mpc

Fishbach, ~Chen et al., ApJL, 2019

Different methods for gravitational-wave cosmology



Electromagnetic counterpart

Without electromagnetic counterpart

Unique redshift

z_{\star}

Multiple possible redshifts

z_1

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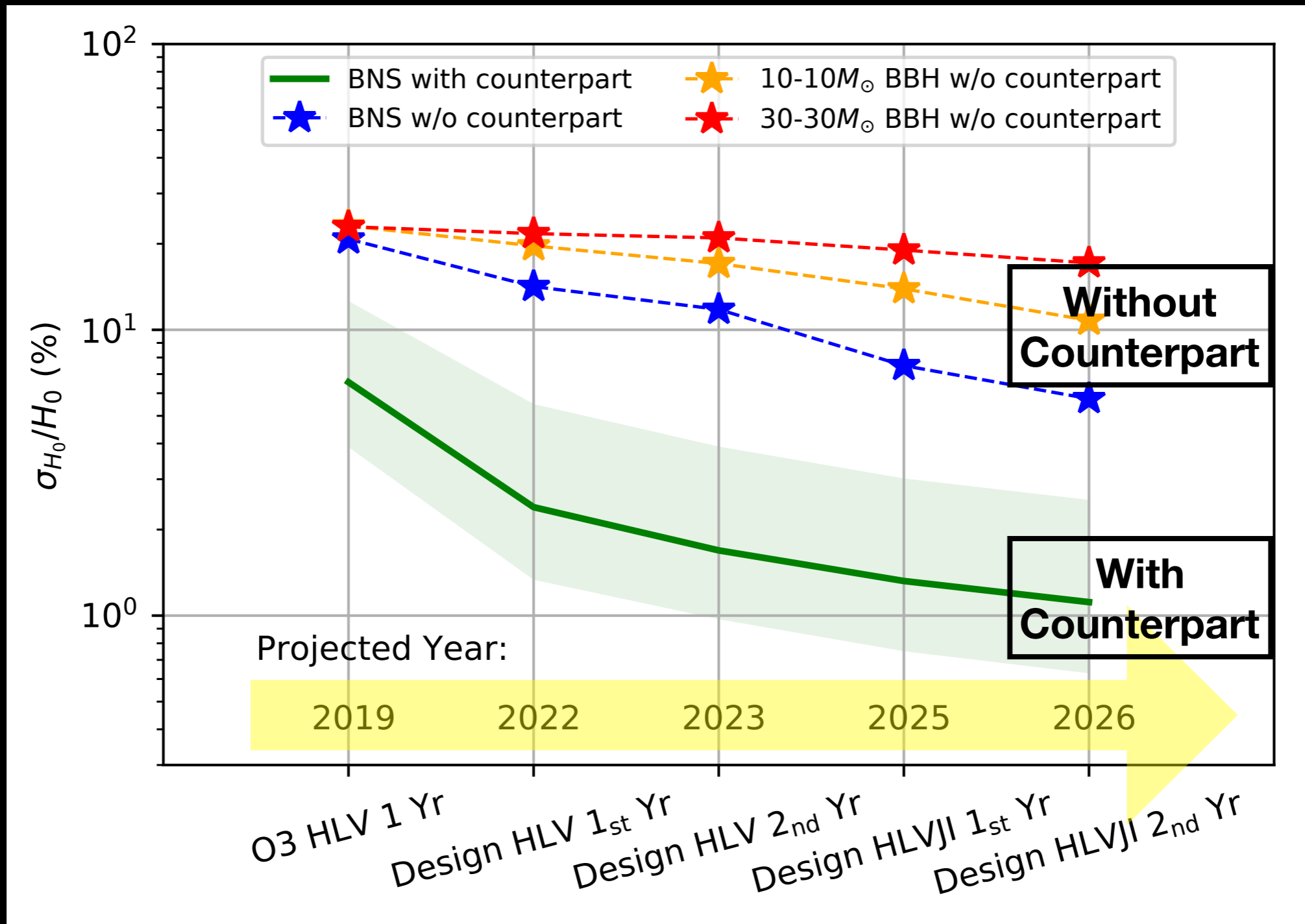
z_6

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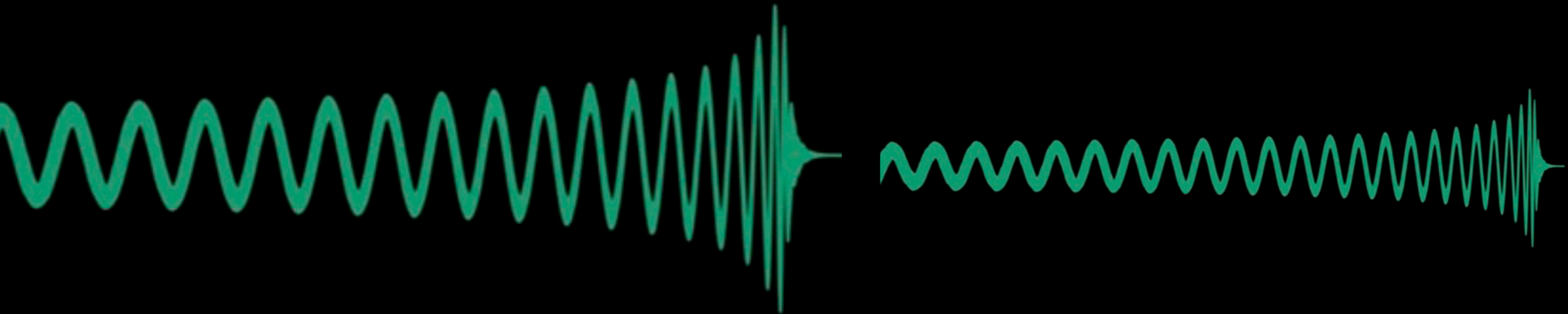
Finding the electromagnetic counterpart is critical



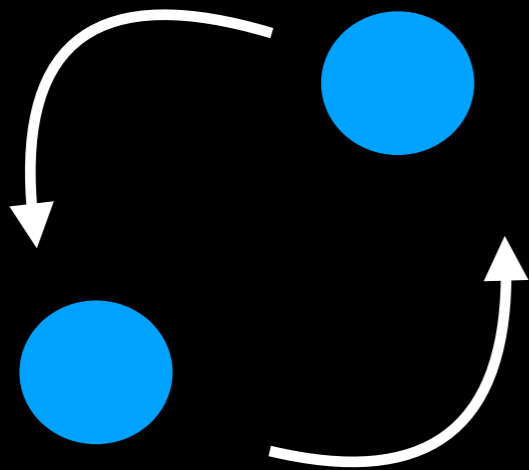
Statistical Method

- **Most of the BBHs can not be localized well.**
 - *They do not contribute to the H_0 measurement.*
- **Complete galaxy catalog was assumed.**
 - *This is not true for most of the cases.*

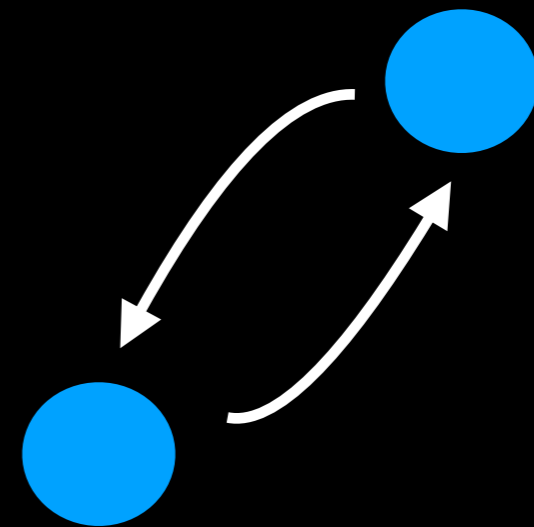
**Improve the H_0 measurement precision:
Break the distance-inclination degeneracy**



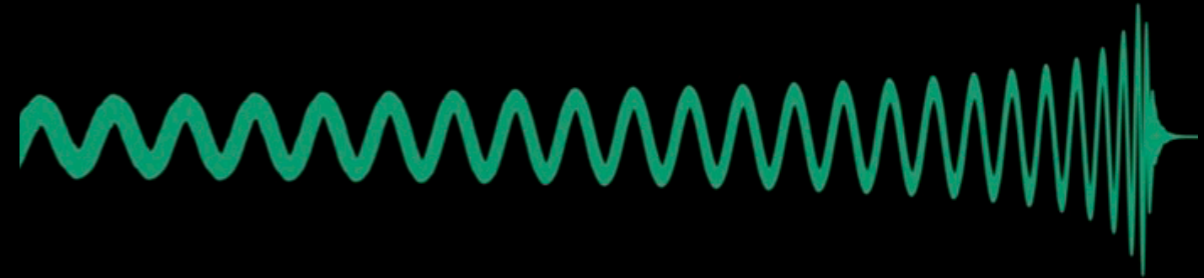
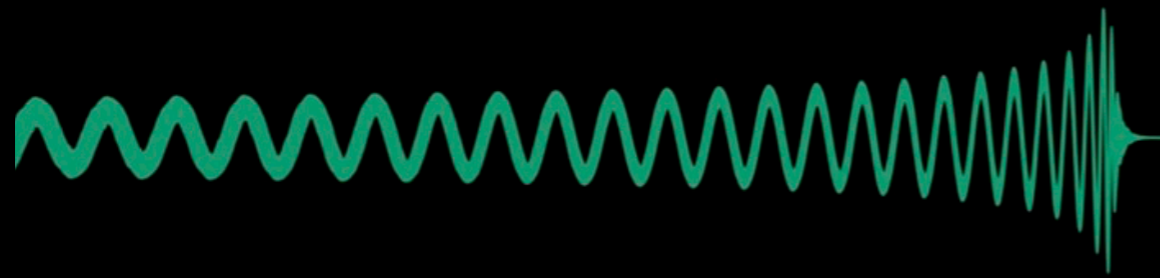
Face-on binary



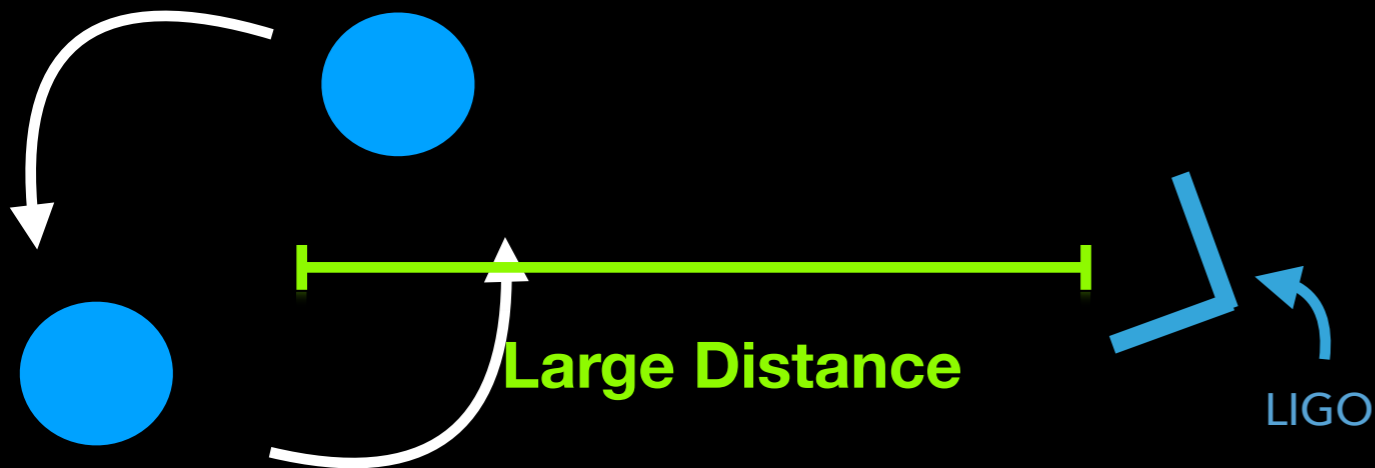
Edge-on binary



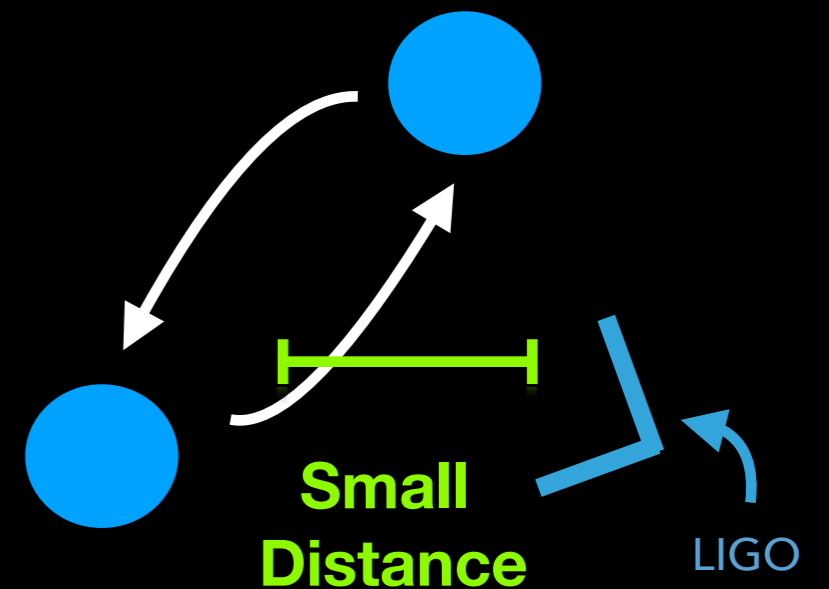
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Face-on binary

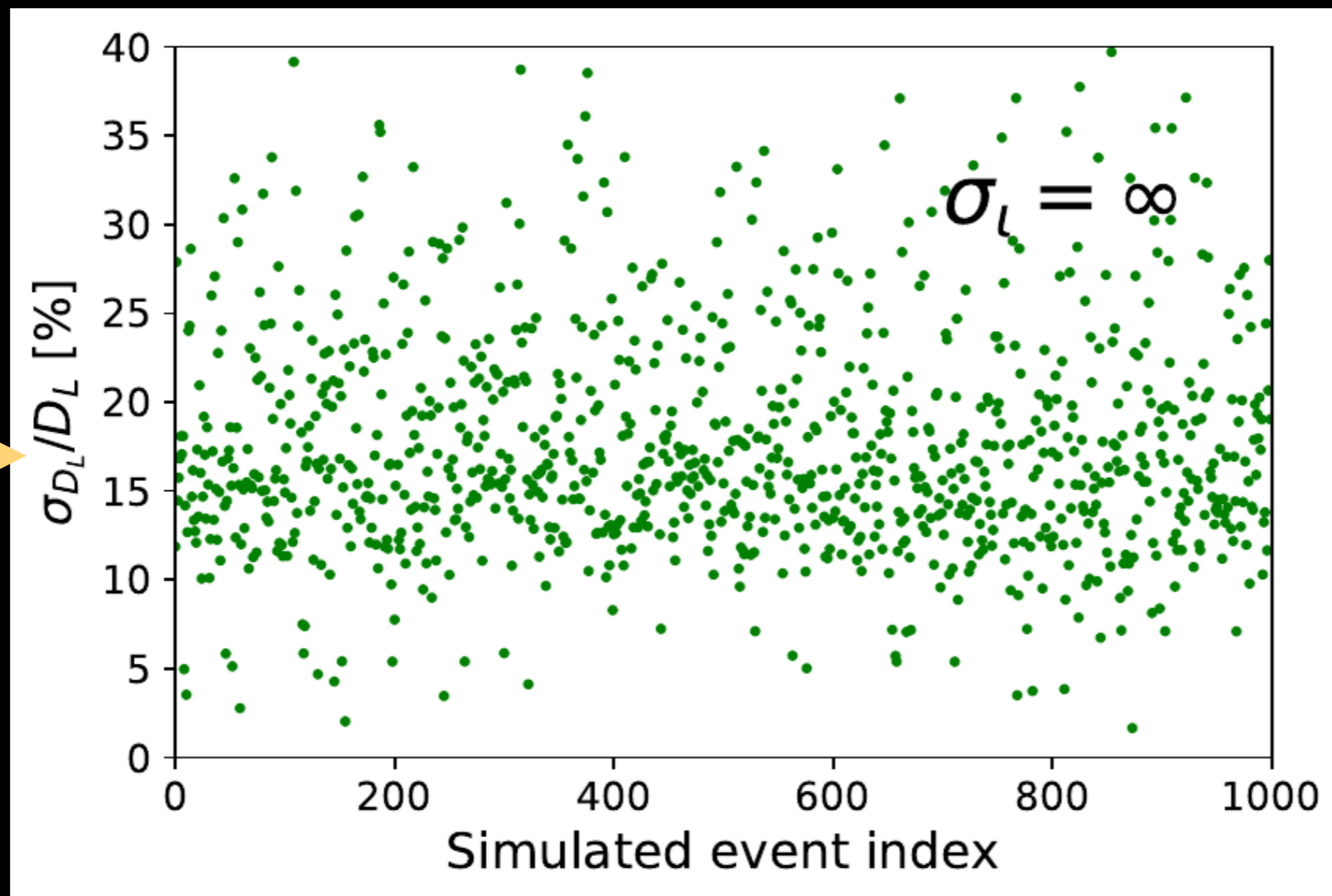


Edge-on binary



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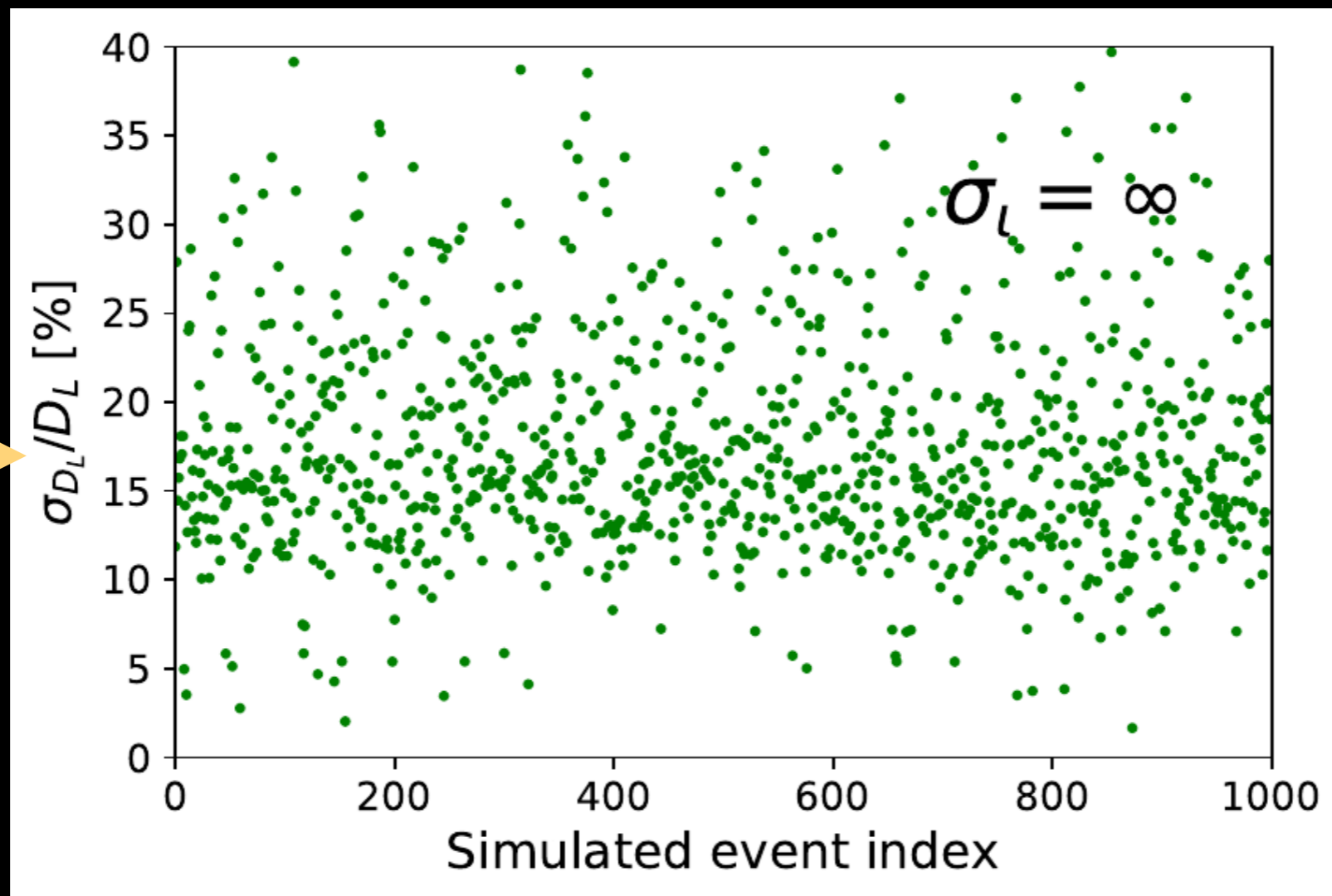
-Neutron star mergers with **viewing angles constrained by electromagnetic emission.**



Can be viewed
as
H0 uncertainty

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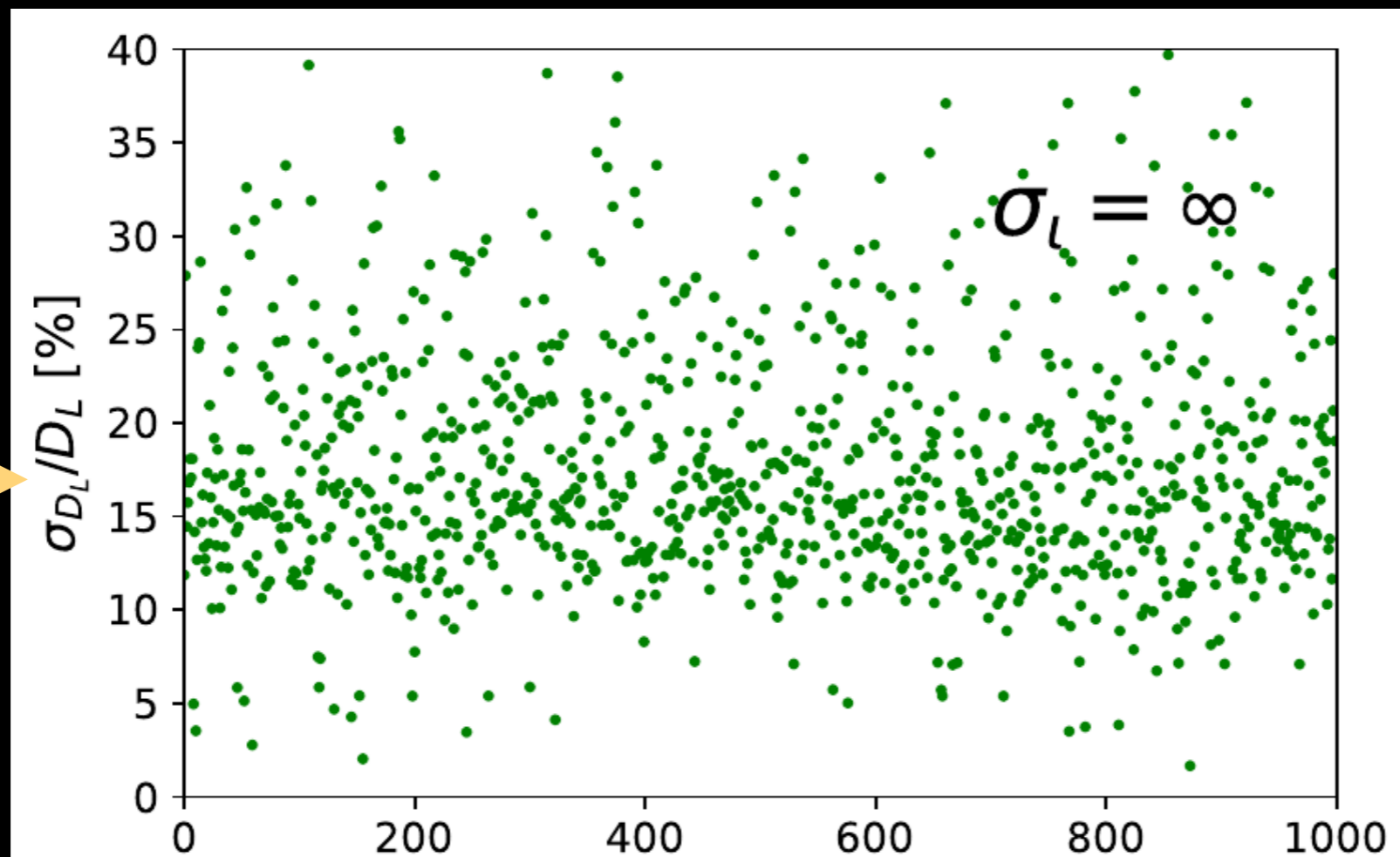


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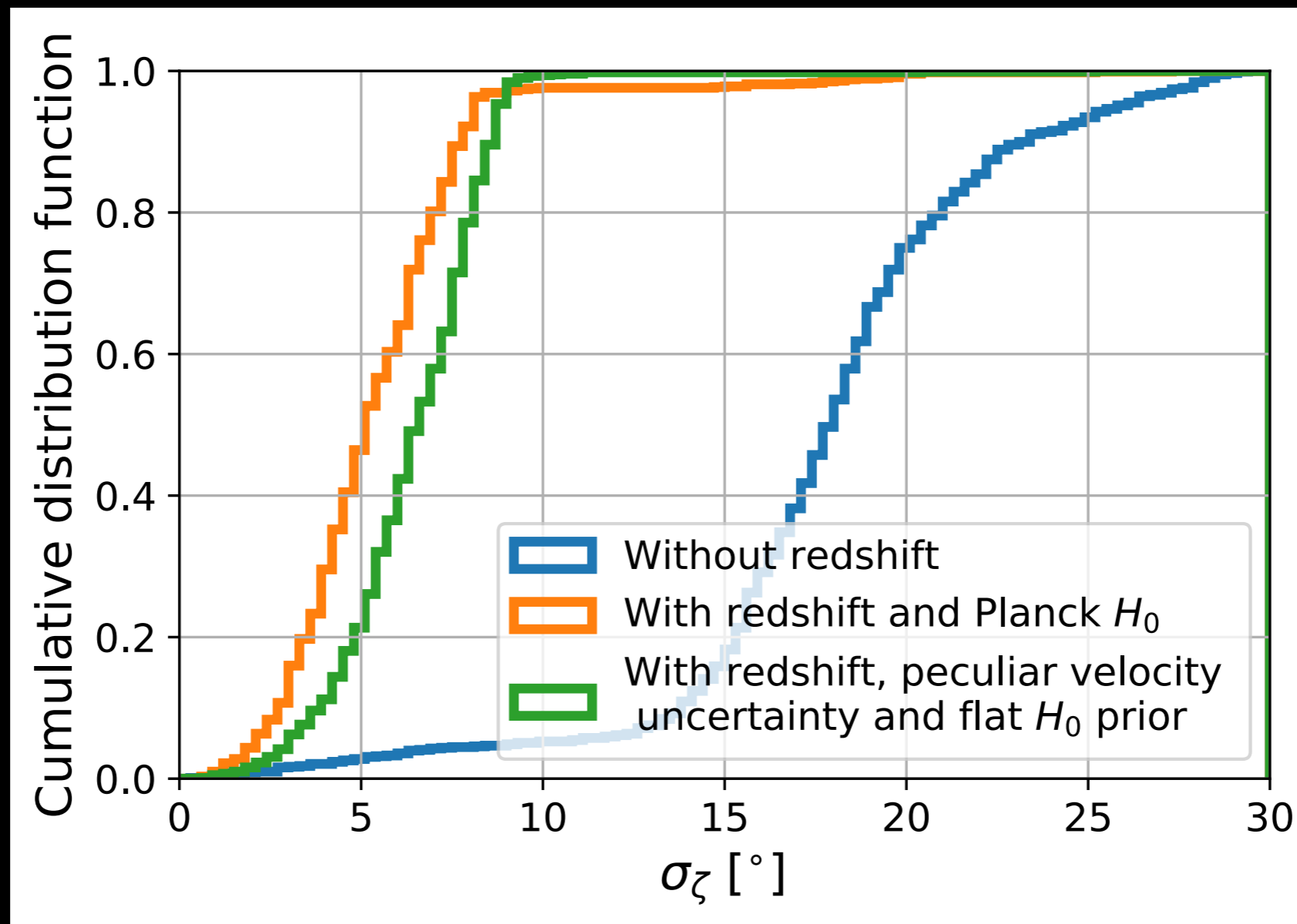
Can be viewed
as
H0 uncertainty →



A factor of 5 to 10 fewer events are required to reach the same Hubble Constant precision if the viewing angle is constrained.

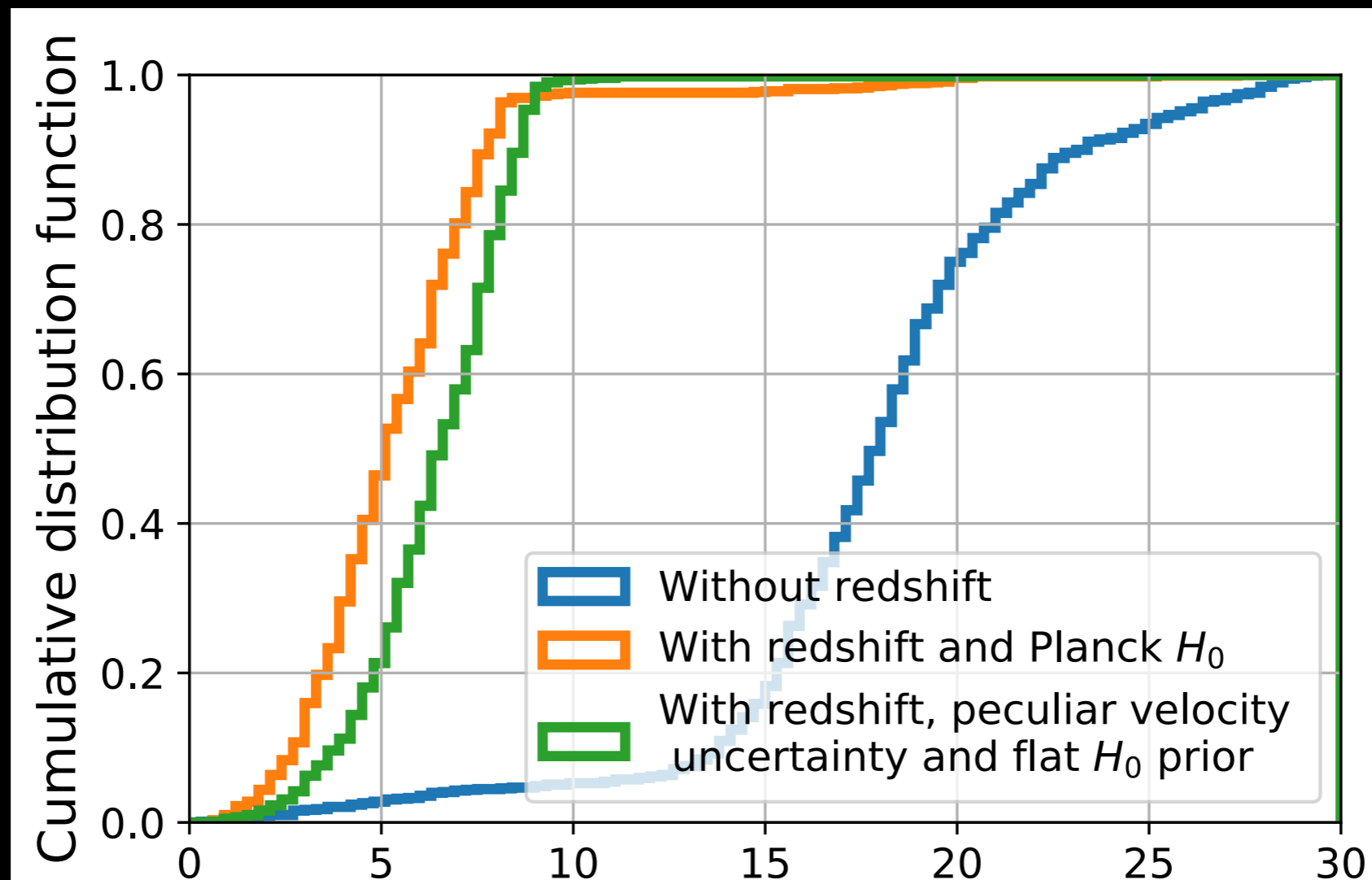
How well can GW detectors constrain the viewing angle?

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Redshift measurement makes a factor of ~3 difference.

What is special about neutron star-black hole merger?

-Electromagnetic and neutrino emissions could be powered by tidal disruption of the neutron star and the resulting accretion disk.

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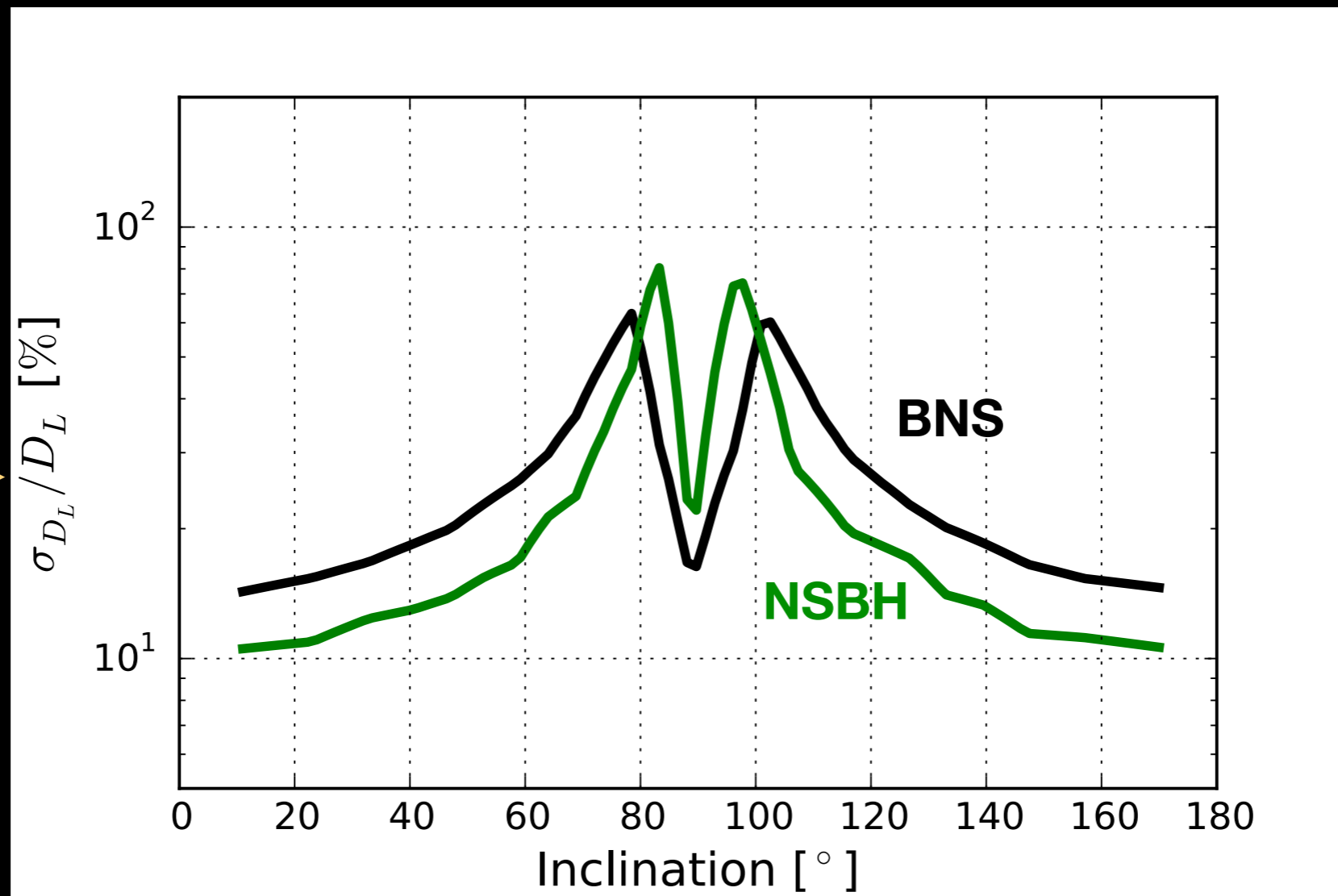
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- At 2G design sensitivity the average detectable redshift is ~ 0.1 ($10-1.4 M_{\odot}$). The measurement of redshift is less affected by peculiar velocity and other local velocity fields.*
- The distance-inclination degeneracy can be broken by the observation of merger-ringdown and precession.*

Improve the H_0 measurement precision: Break the distance-inclination degeneracy

Vitale & Chen, PRL, 2018

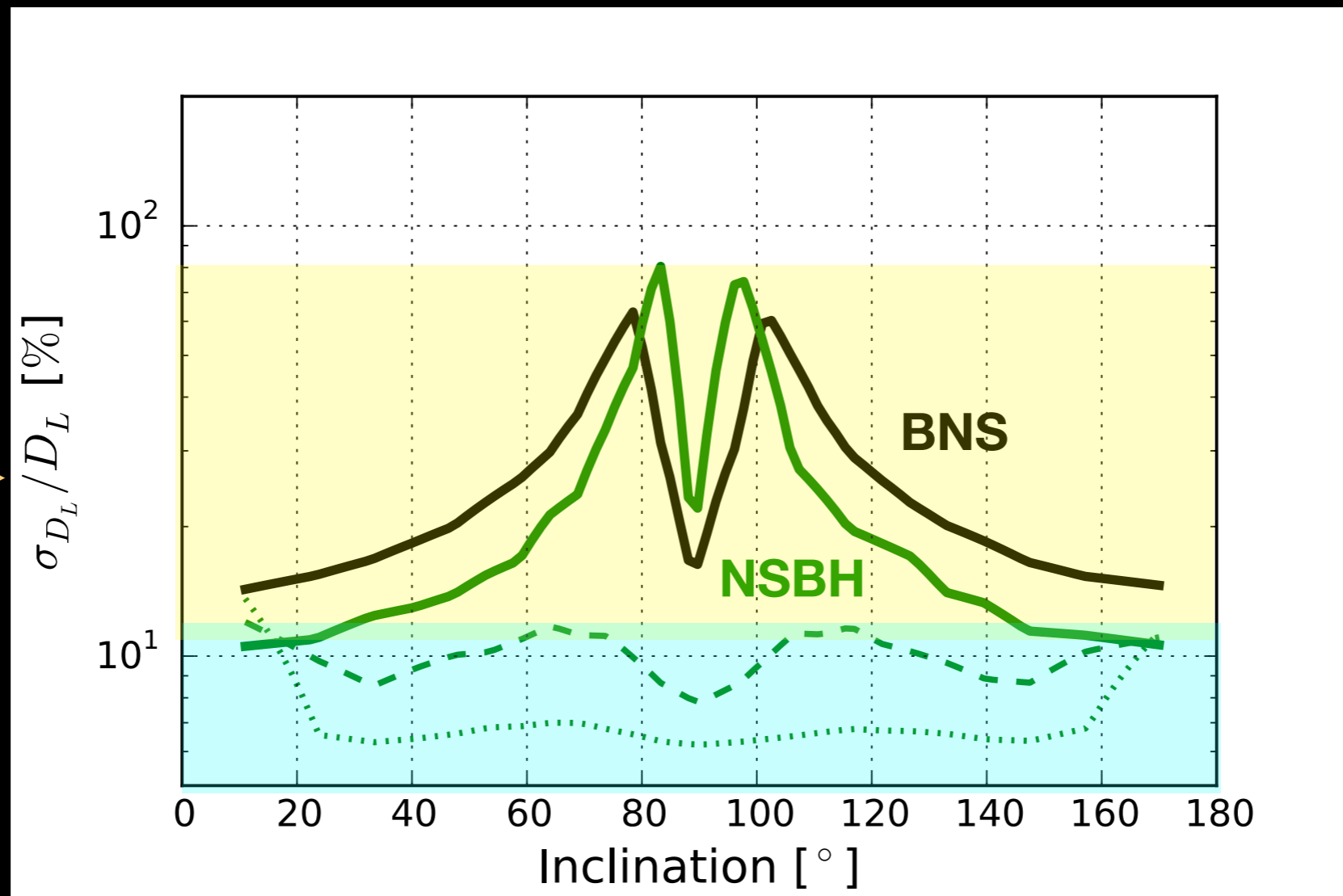


Can be viewed
as →
 H_0 uncertainty

The difference between BNS and NSBH is mainly due to the observation of merger-ringdown.

Improve the H_0 measurement precision: Break the distance-inclination degeneracy

Vitale & Chen, PRL, 2018



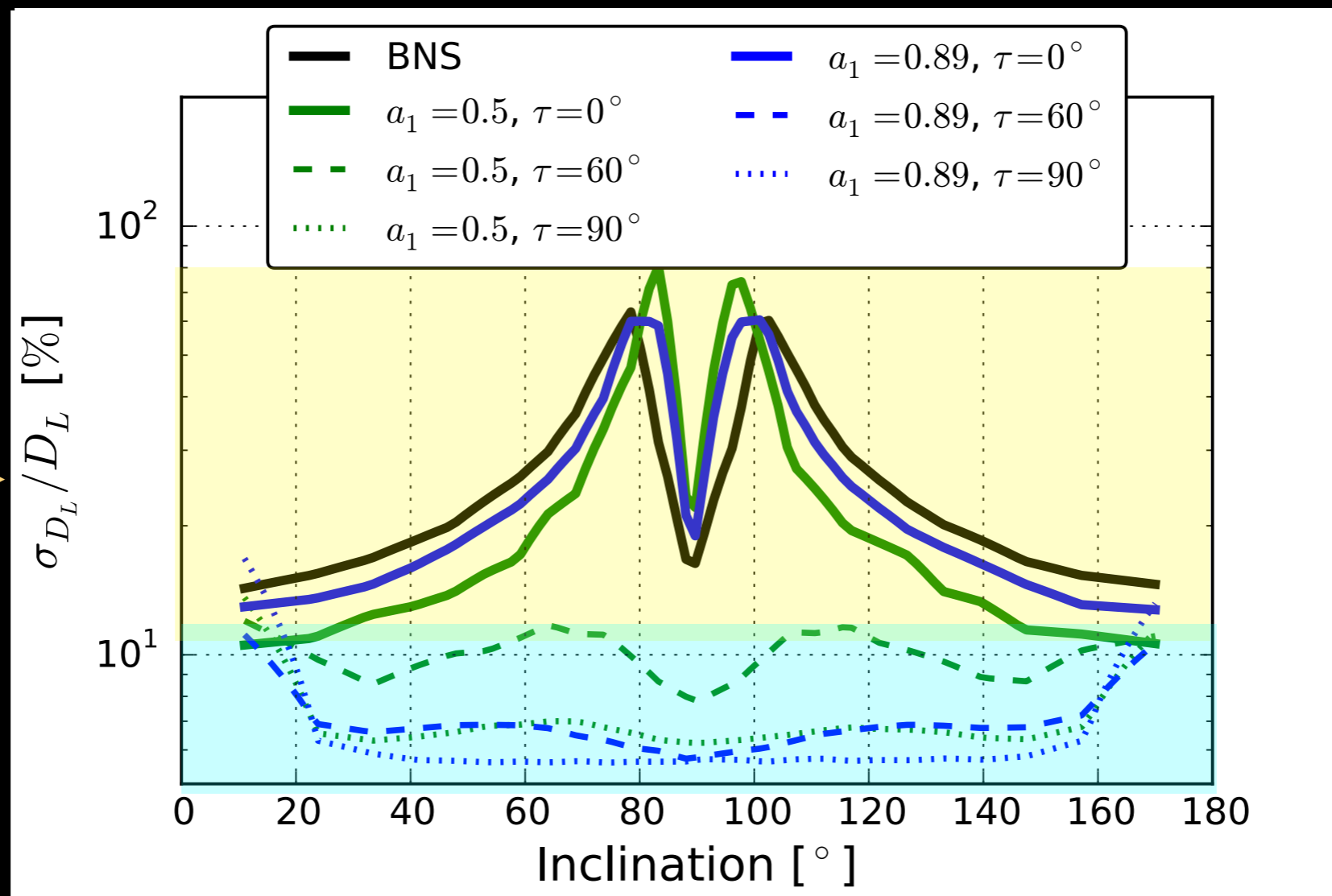
Can be viewed
as \rightarrow
 H_0 uncertainty

Without
Precession

With
Precession

Improve the H_0 measurement precision: Break the distance-inclination degeneracy

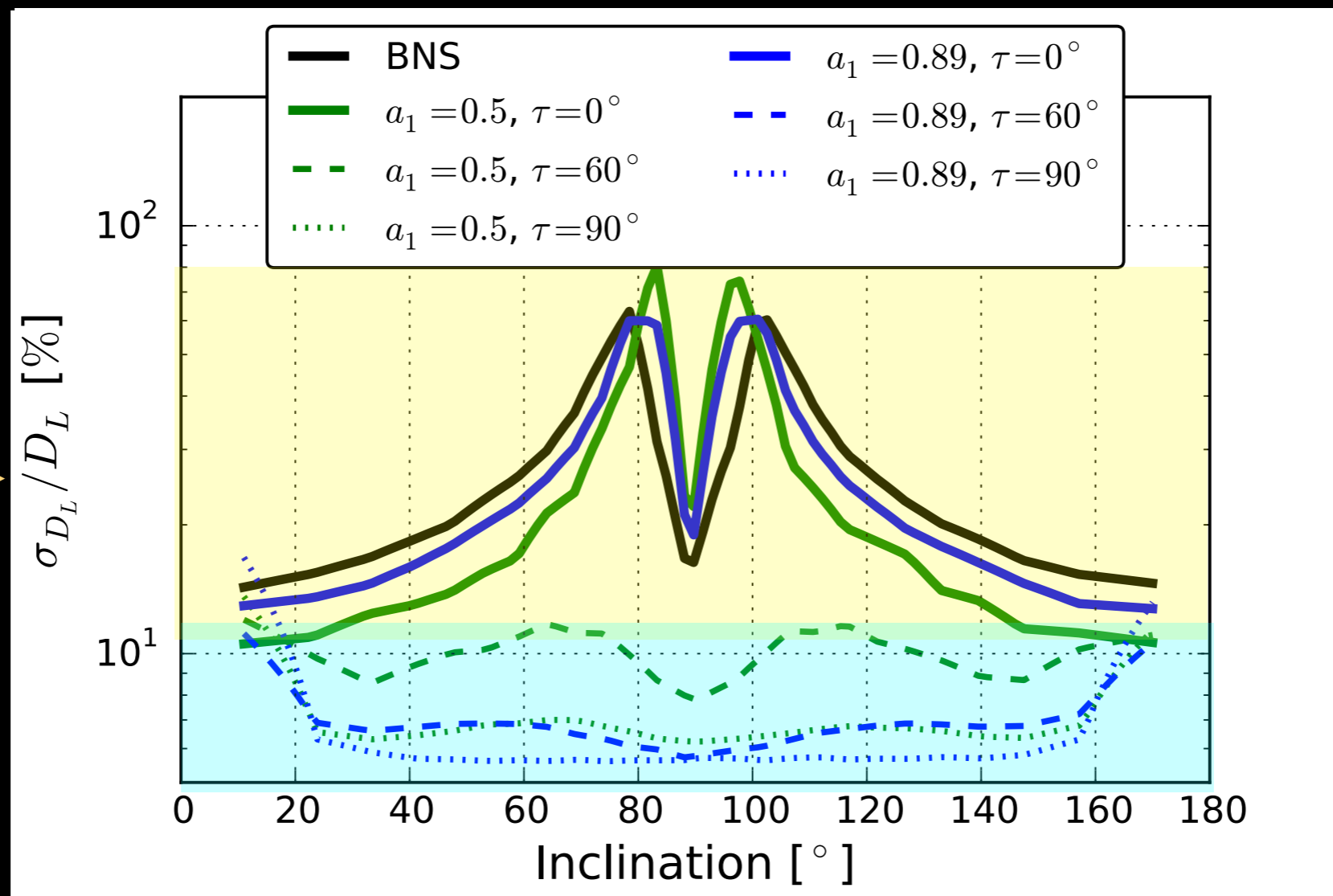
Vitale & Chen, PRL, 2018



A large and misaligned black hole spins results in a significant waveform amplitude modulation, which entirely breaks the degeneracy.

Improve the H_0 measurement precision: Break the distance-inclination degeneracy

Vitale & Chen, PRL, 2018



Can be viewed
as \rightarrow
 H_0 uncertainty

Without
Precession

With
Precession

NSBHs can provide more precise Hubble Constant measurement if its astrophysical rate is larger than 1/10 of binary neutron star mergers.

What has not been discussed?

Systematics error of gravitational wave distance measurement

- Calibration errors, waveform

Electromagnetic observation selection effects

- Mass, spin

- Viewing angle

Beyond 2G, beyond H_0

Summary

-Gravitational waves can serve as an independent probe to the Universe. The Hubble constant uncertainty is expected to reduce to two percent in five years.

-In addition to capturing the EM counterpart, we also need to address various possible systematics and selection effects carefully to ensure an accurate H_0 measurement.