

Physics of collisionless shocks in SN and GRBs: Weibel Instability

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Many thanks to:

Christian Hedeland,

Troels Haugboelle,

Aake Nordlund (Niels Bohr Institute,
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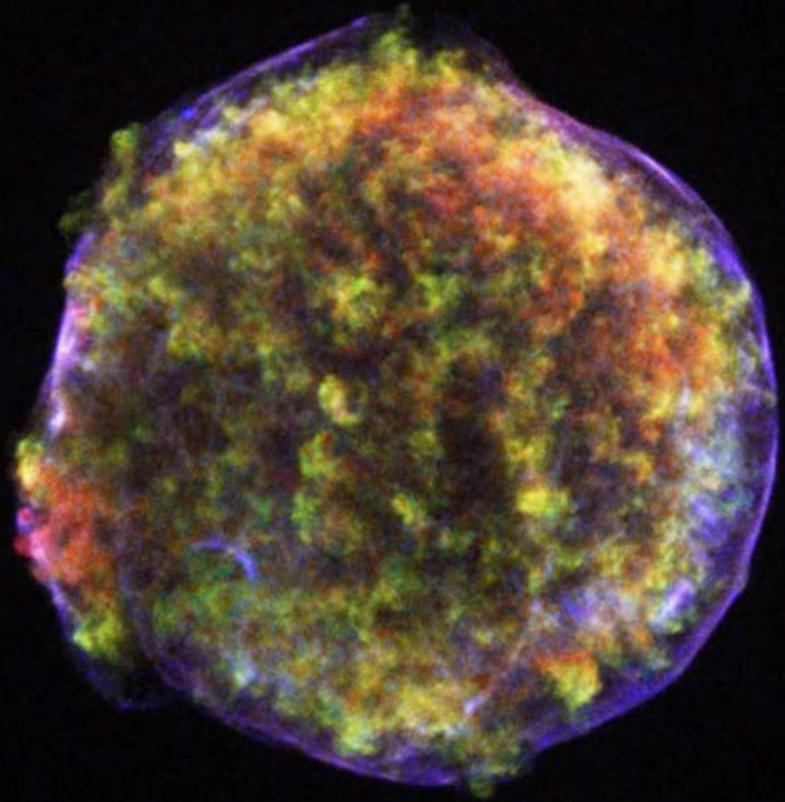
Outline

Collisionless shocks:
GRB/SN “Standard Model”

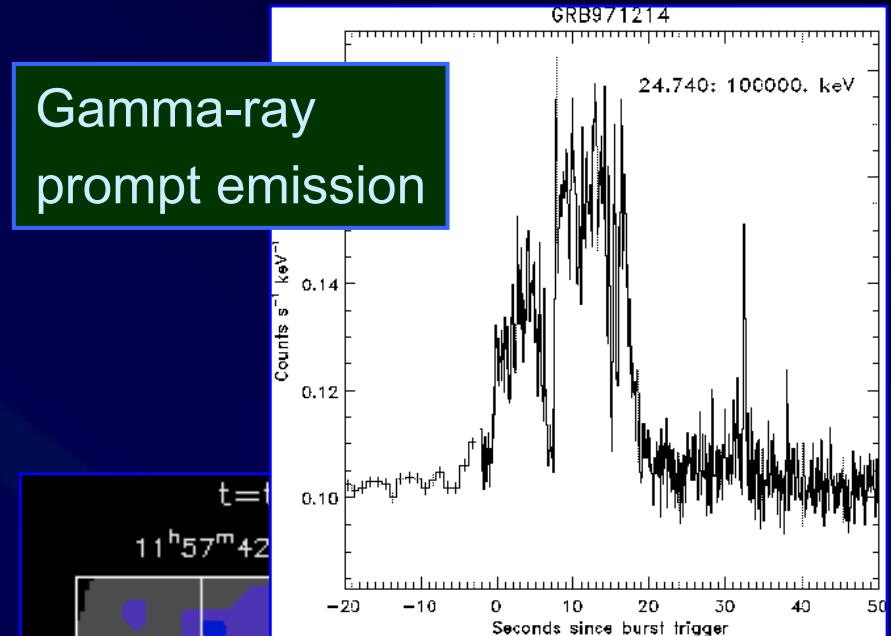
- ♦ Introduction
- ♦ Microphysics of collisionless relativistic unmagnetized shocks
- ♦ Realistic modeling of shocks
- ♦ Particle acceleration...
- ♦ Can the produced fields really populate large volumes?
- ♦ How do the shocks shine?
- ♦ Spectral variability
- ♦ Polarization of radiation
- ♦ Summary

Collisionless shocks DO exist

Tycho supernova



Gamma-ray
prompt emission



X-ray delayed
afterglow emission

How a collisionless shock can form?

Collisionless shock → NO COLLISIONS

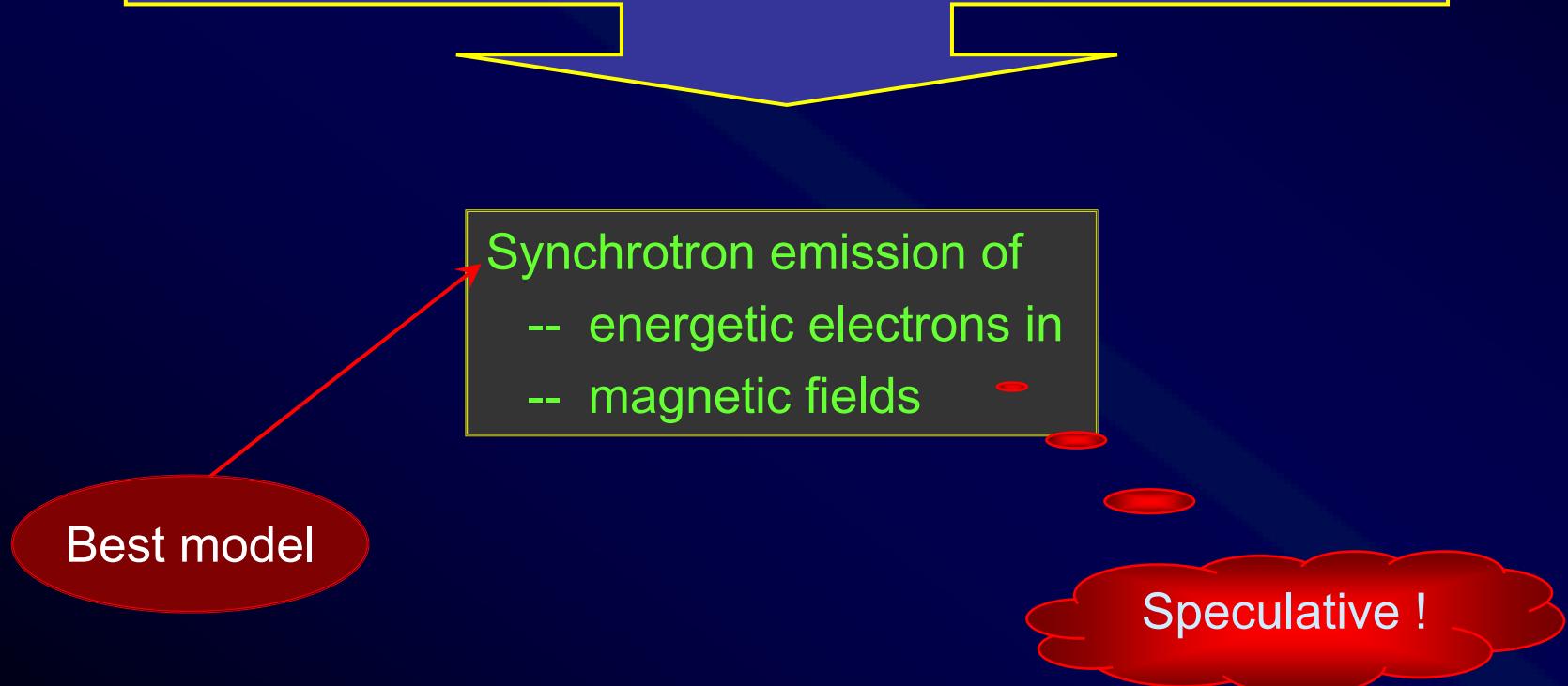
which transport momentum
from downstream to upstream

Electromagnetic fields can mediate
interactions between plasma particles

Why collisionless shocks radiate?

➤ *Shock jump conditions*

- *Strong magnetic fields in the shock*
- *Very efficient particle acceleration*

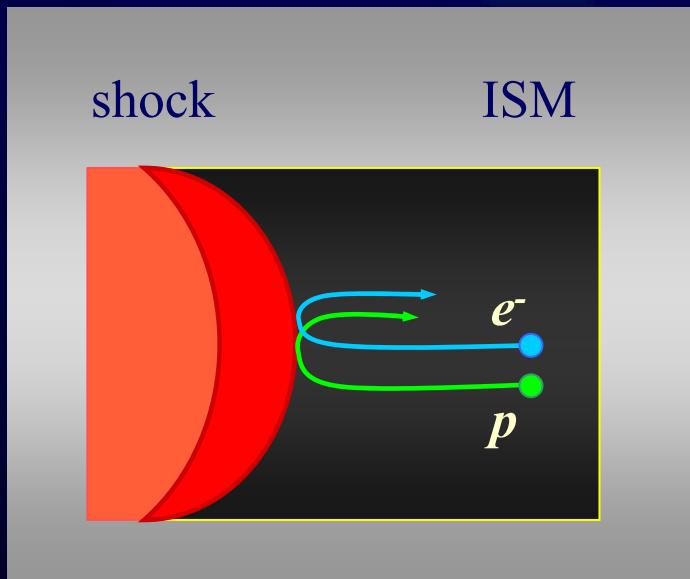


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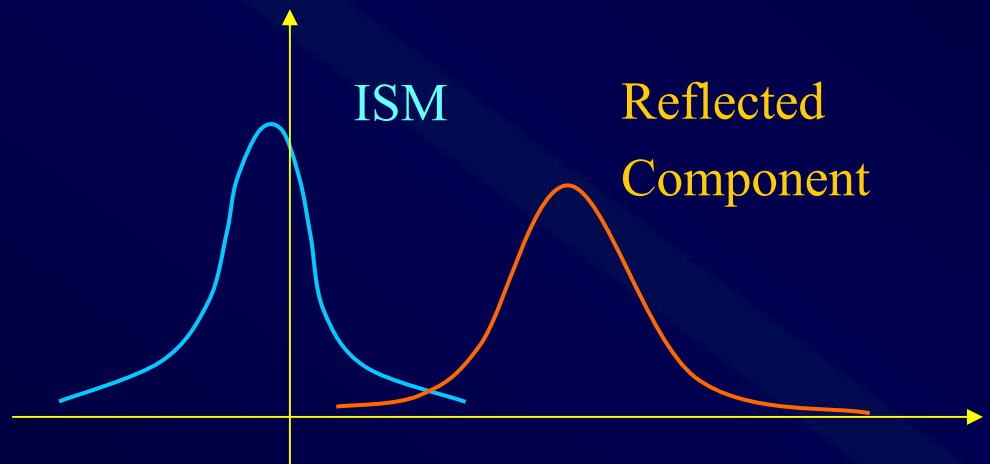
Starting from the first principles

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Conditions at a shock



Anisotropic distribution of particles (counter-propagating streams) at the shock front



General description

Anisotropy: $\varepsilon_{\parallel} > \varepsilon_{\perp}$ characteristic energies (e.g., T) in the directions parallel and perpendicular to the shock propagation direction

Introduce: plasma frequency
anisotropy parameter

$$\omega_{p(e,p)} = \sqrt{4\pi e^2 n / m_{(e,p)}} \sim 10^{(4.7, 3)} n^{1/2}$$

$$A = (\varepsilon_{\parallel} - \varepsilon_{\perp})/\varepsilon \sim (\mathcal{M}-1)/(\mathcal{M}+1)$$

Growth rate

Field scale

Field strength

$$\gamma \sim (v/c) \omega_p A$$

$$1/k \sim c/(\omega_p A)$$

$$B^2/8\pi \sim (\varepsilon_{\parallel} - \varepsilon_{\perp}) \eta$$

efficiency (from simulations)

Outline

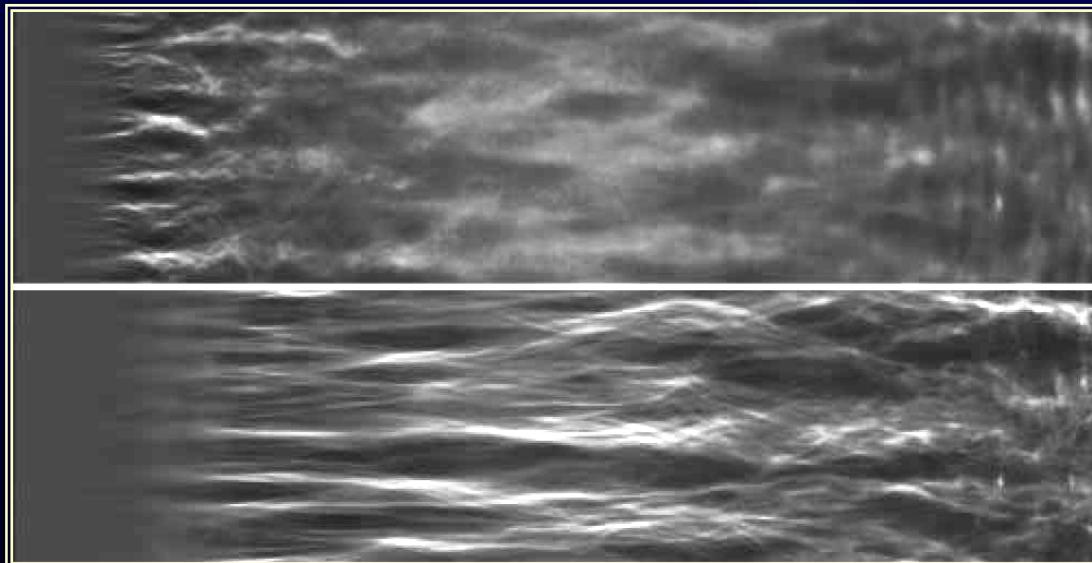
3D relativistic plasma PIC simulations

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Relativistic $e\text{-}p$ shock (GRB)



Proton density

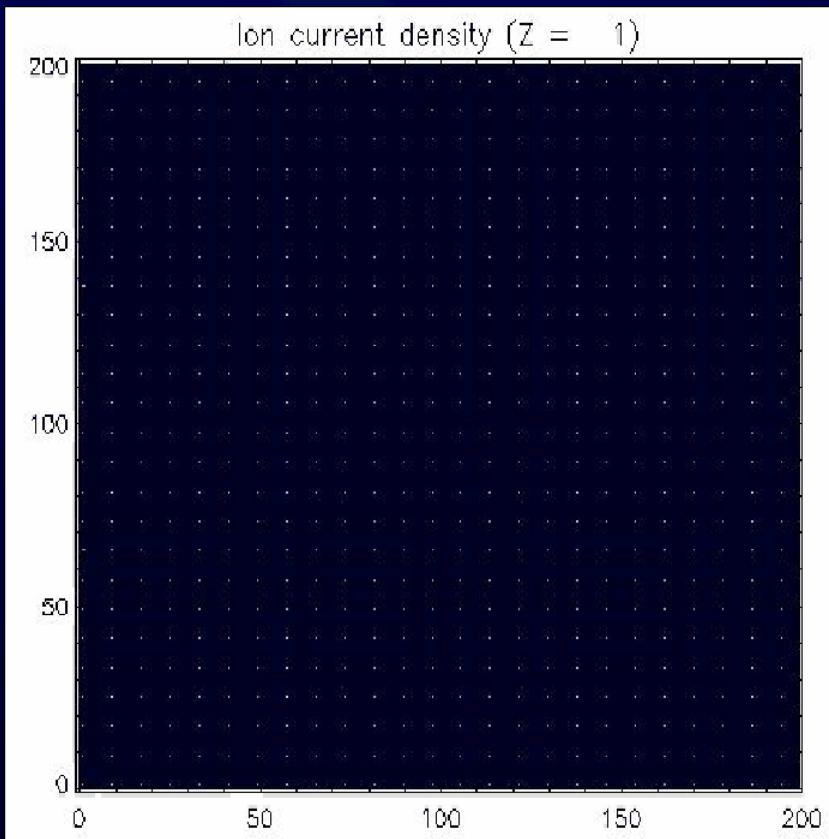


Electron currents

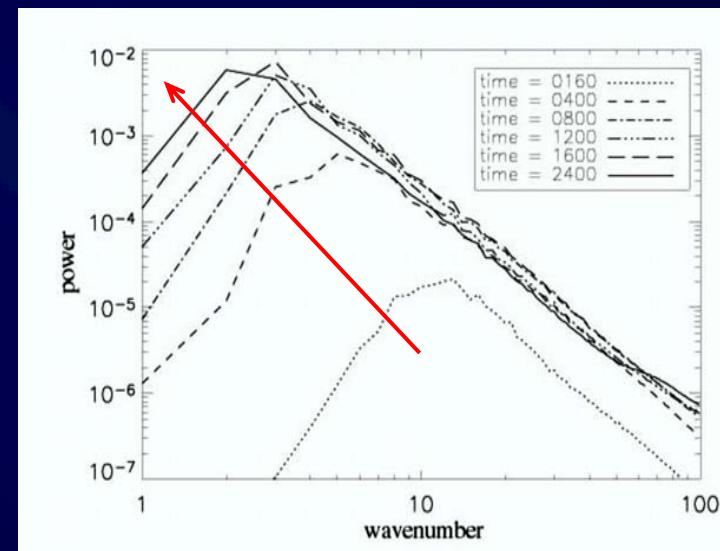
Proton currents

(Frederiksen, et al., 2003)

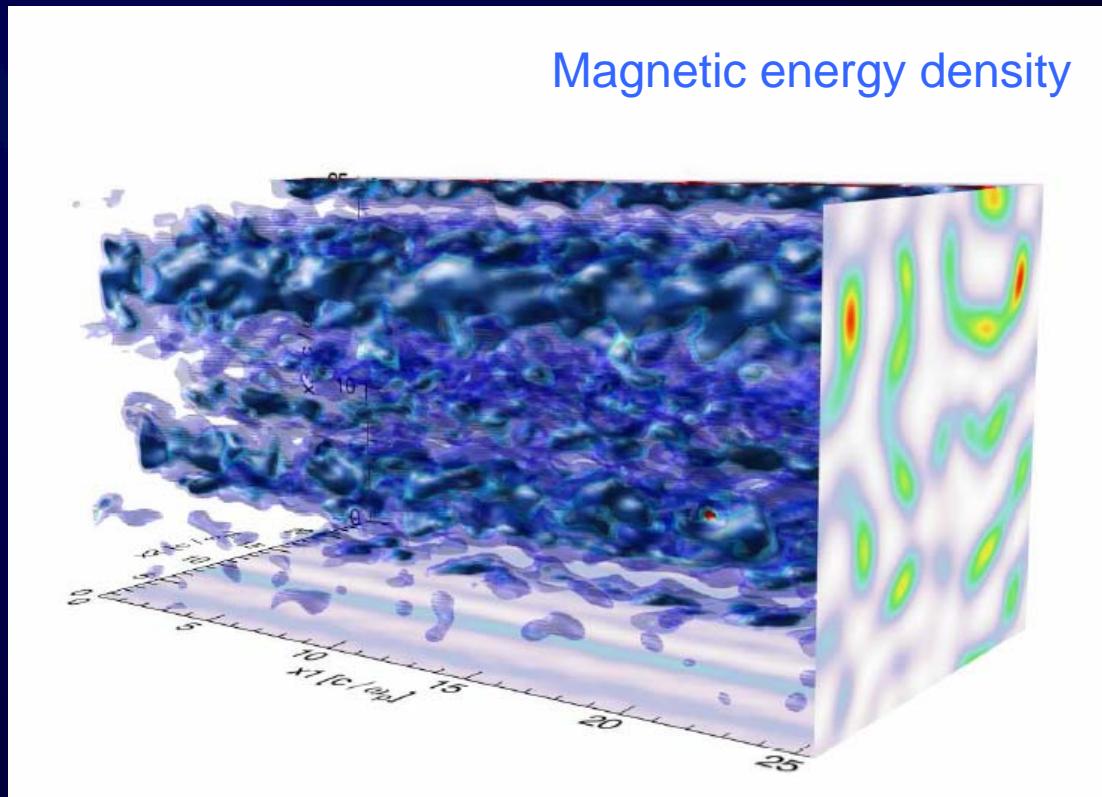
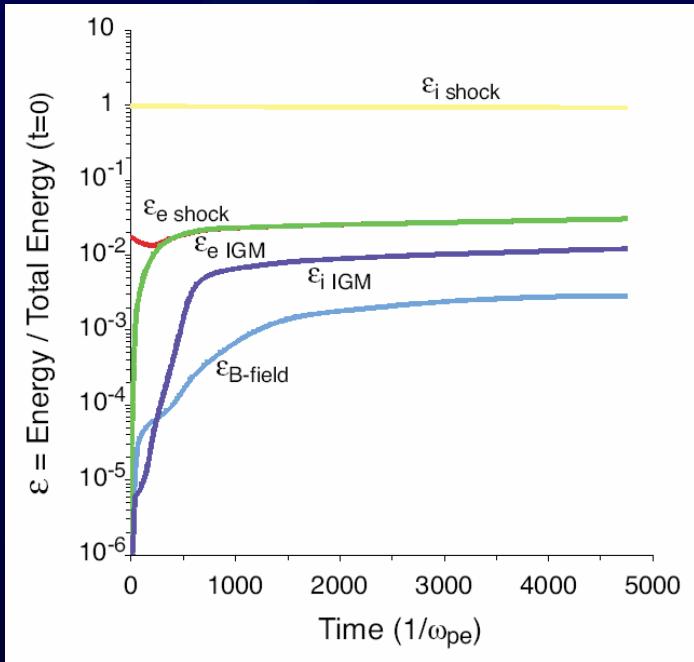
Currents and fields



*B-field scale grows downstream,
where $\varepsilon_B \sim \text{constant}$*



Nonrelativistic $e\text{-}p$ shock (SN)



(Medvedev, Silva, Kamionkowski, 2005)

Rule of thumb

Magnetized vs. Unmagnetized external medium

Critical parameter: *magnetization* σ

$< 1\% = \text{unmagnetized} \rightarrow \text{Weibel}$

$> 1\% = \text{magnetized} \rightarrow \text{no Weibel}$

+ shock front \sim Larmor

+ field amplification is still possible
via Alfvénic-type instability

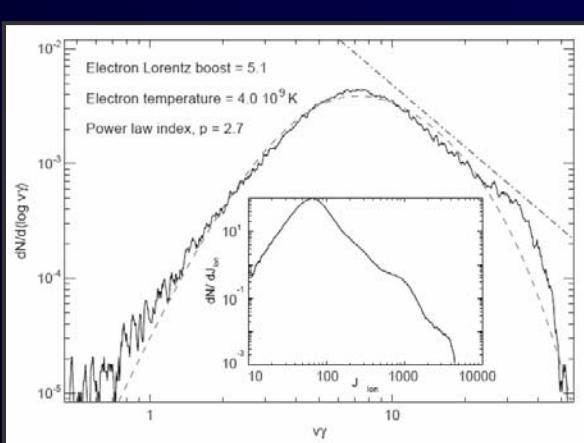
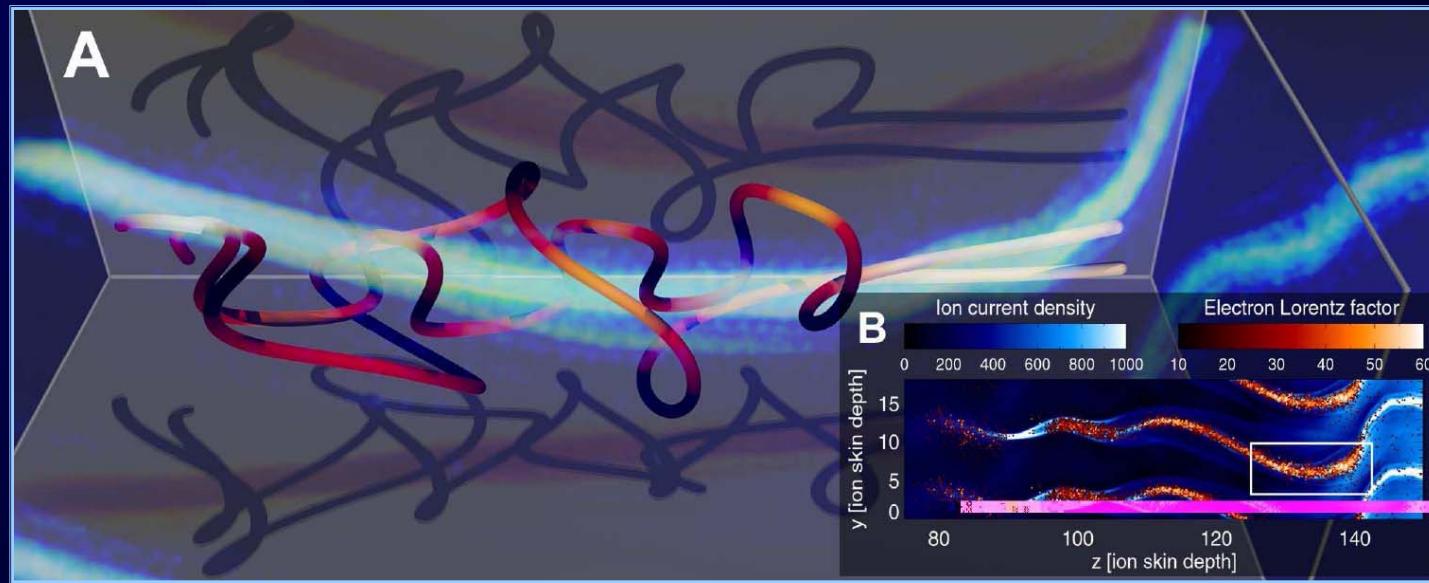
[talk by *Jacco Vink*,
poster by *Malkov & Diamond*]

Outline

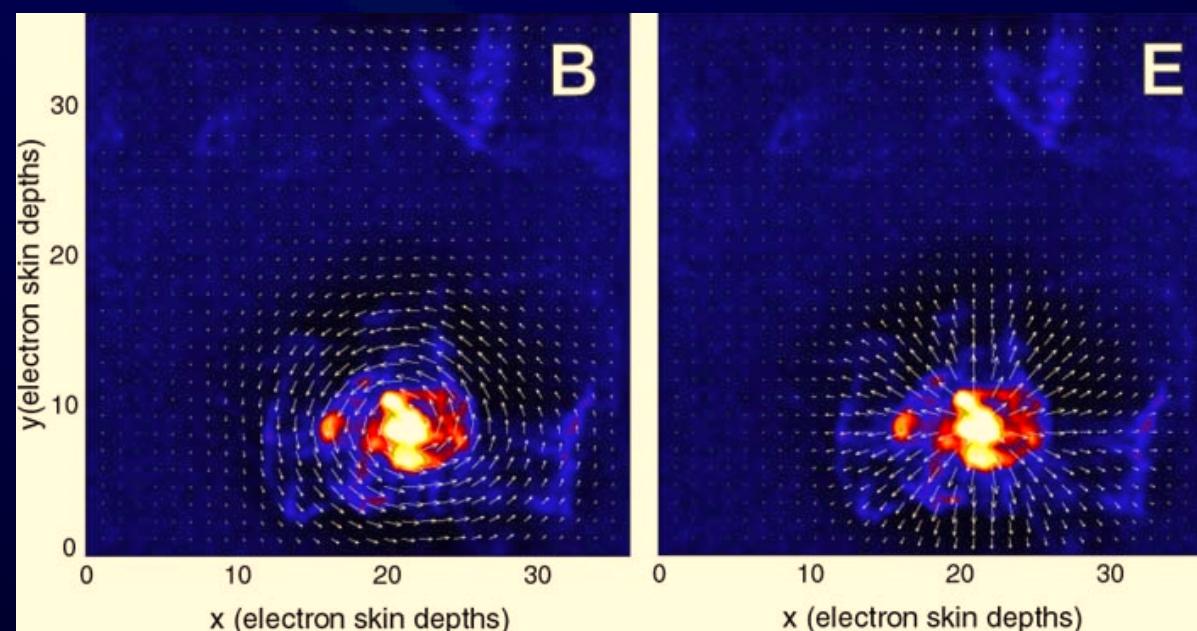
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A hint...
More: talk by Matthew Baring

Particle acceleration e^-p



(Hedgedal, et al, 2005, PhD)



Outline

Fields must populate large volumes downstream in order to explain observations:

Synchrotron-type radiation from shocks

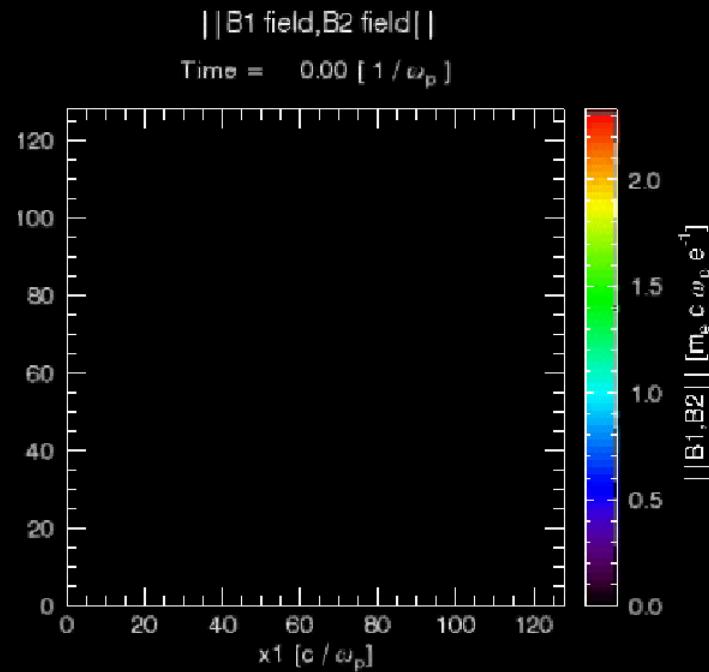
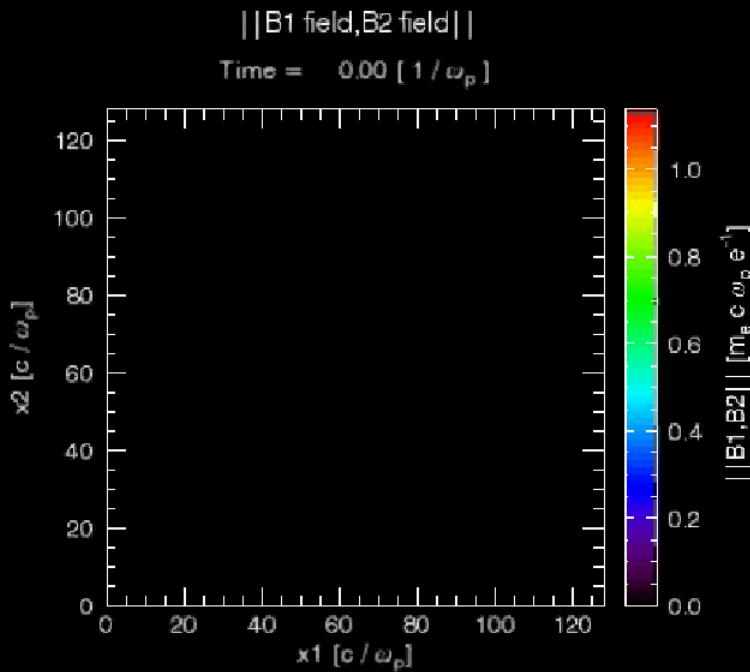
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Evolution of B_{\perp}

Electron-positron simulations

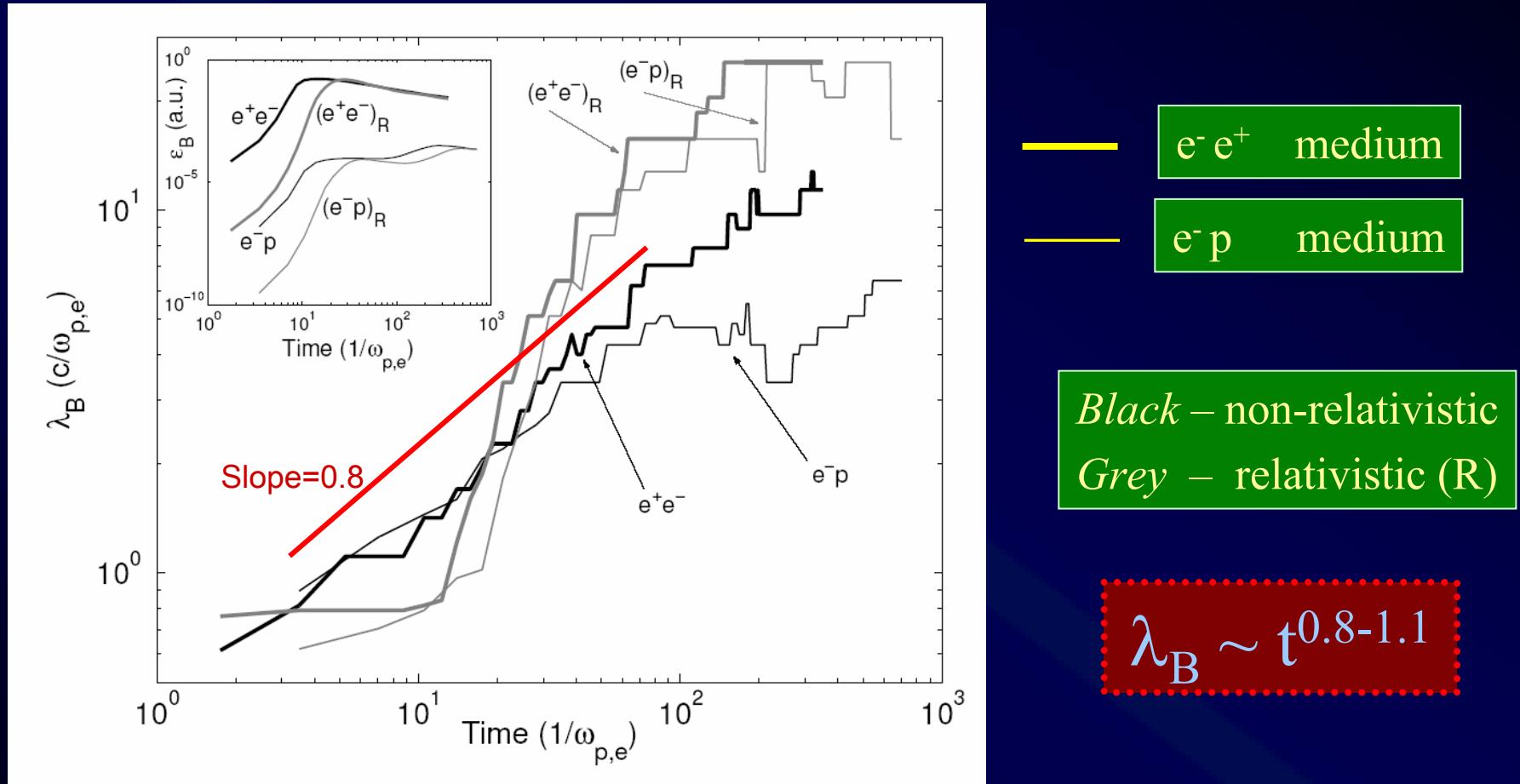
Electron-proton simulations

$$m_p/m_e = 1860$$



(Silva, et al 2005)

The evolution of λ_B



As the spatial scale grows “super-diffusively”,
the standard (diffusive) dissipation quenches

Field dissipation

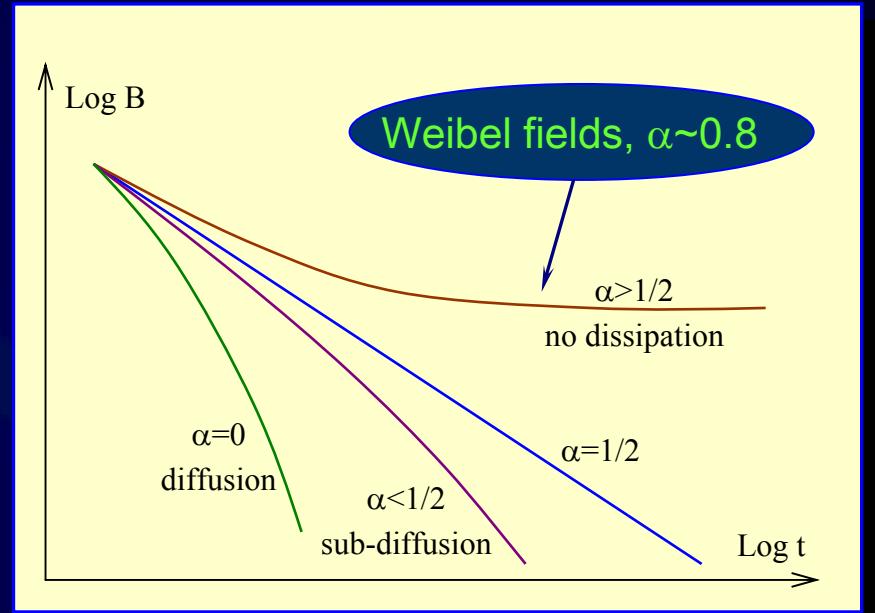
Diffusive dissipation:

$$\frac{\partial B}{\partial t} = -\kappa \frac{\partial^2 B}{\partial x^2} \sim -\frac{\kappa}{\lambda_B^2} B$$

Field scaling:

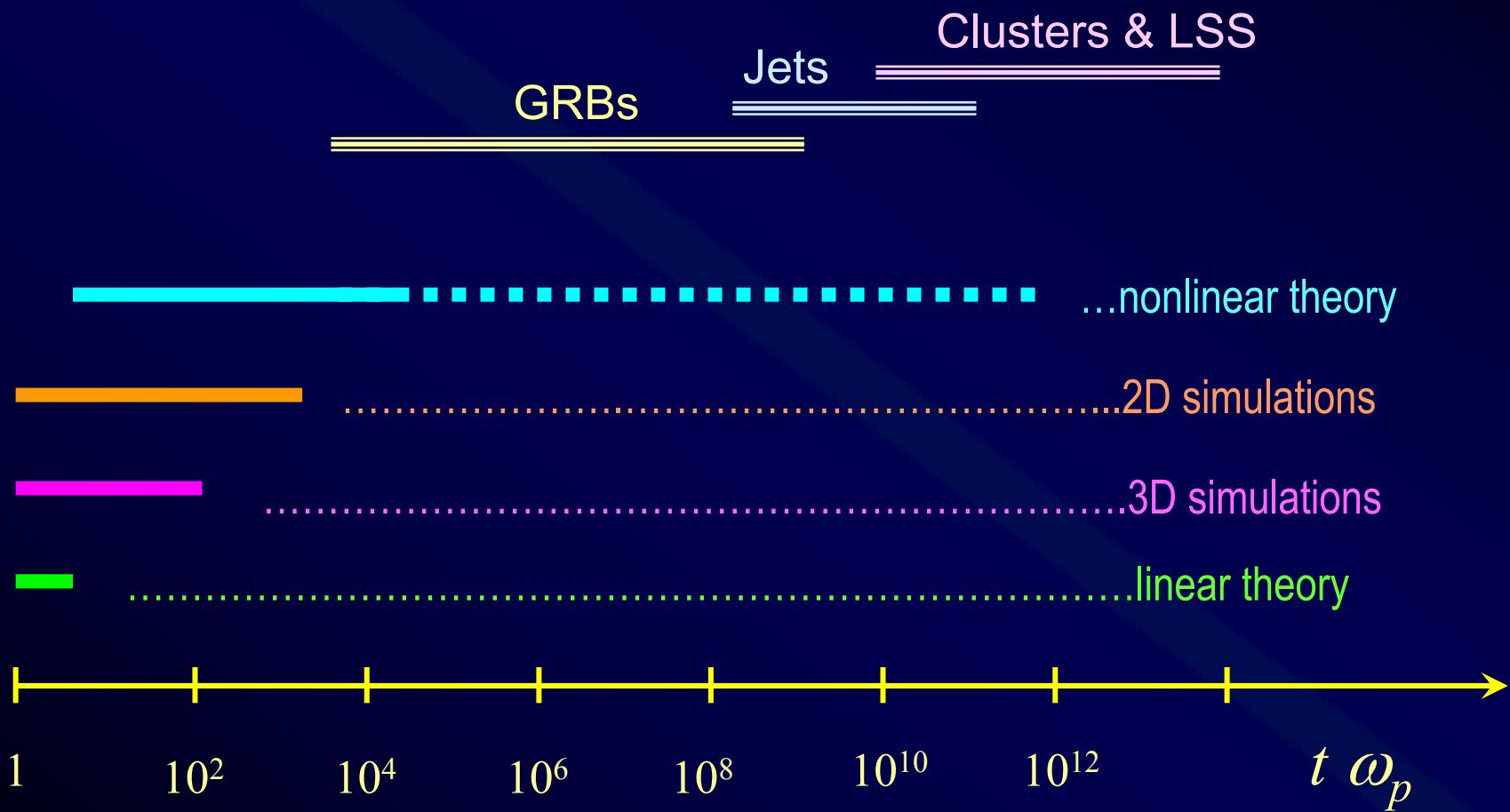
$$\lambda_B \propto t^\alpha$$

Solution:



$$B \propto \exp\left[-\int \lambda_B^{-2}(t) dt\right] \propto \begin{cases} \exp(-t^{1-2\alpha}), & \text{if } \alpha < 1/2 \\ t^{-4}, & \text{if } \alpha = 1/2 \\ \exp\left(\frac{1}{t^{2\alpha-1}} - \frac{1}{t_0^{2\alpha-1}}\right), & \text{if } \alpha > 1/2 \end{cases}$$

Science vs. Nature



Outline

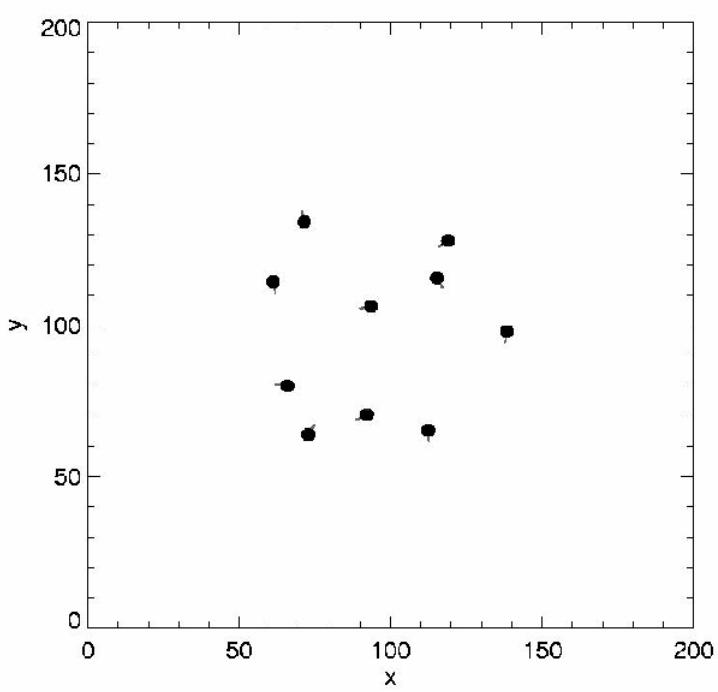
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Radiation from small-scale random fields

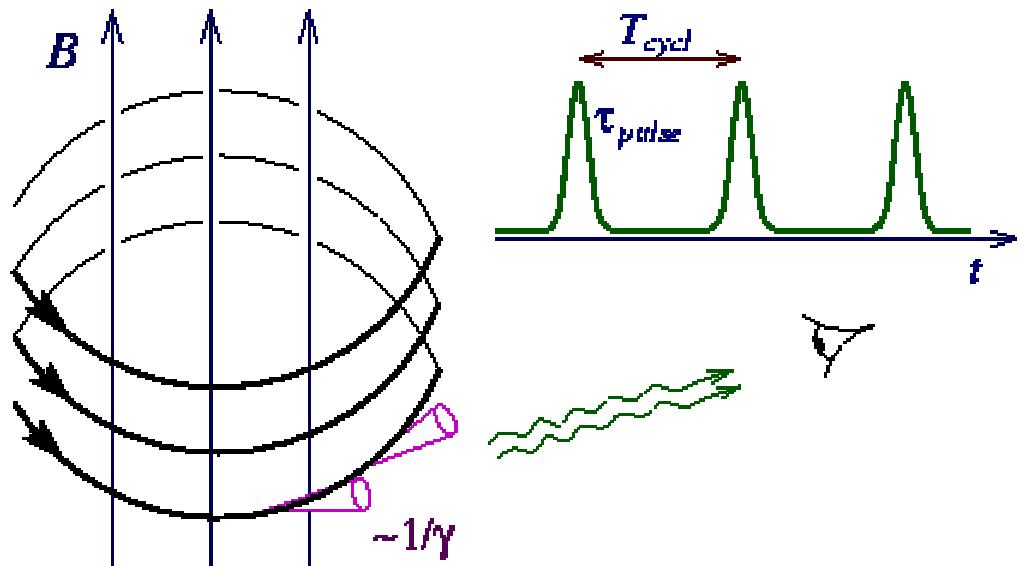
Synchrotron Radiation

$$B(r)=B_0=\text{const}$$

(homogeneous)



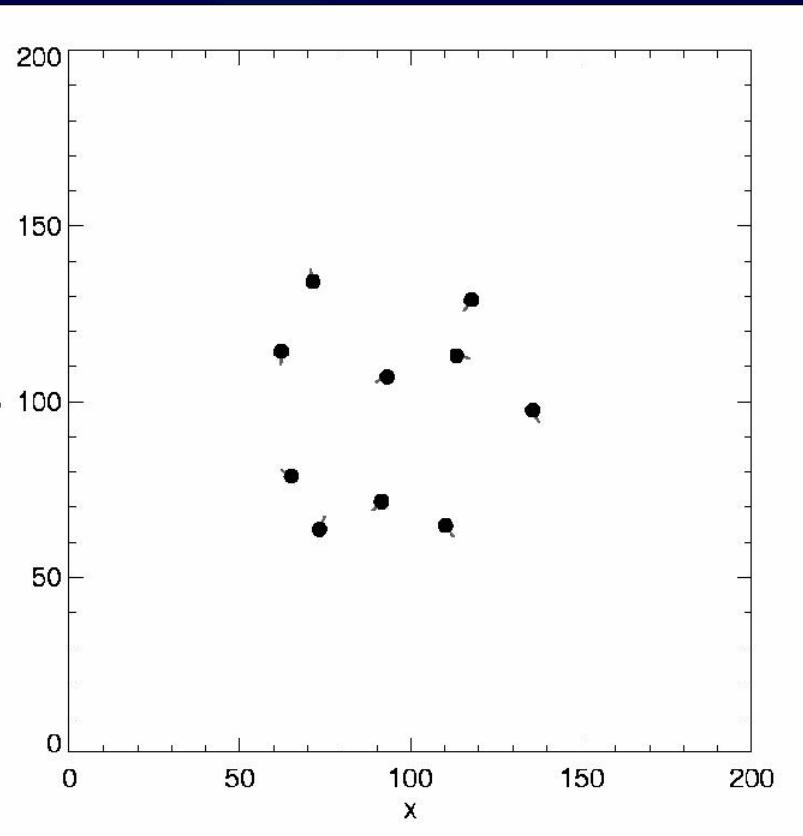
Homogeneous Magnetic Field



$$\text{Synchrotron Radiation: } \omega_s \sim 1/\tau_{pulse} \sim \gamma^2 \omega_H$$

(Frederiksen, 2005, PhD thesis)

Synchrotron Vs. Jitter Radiation

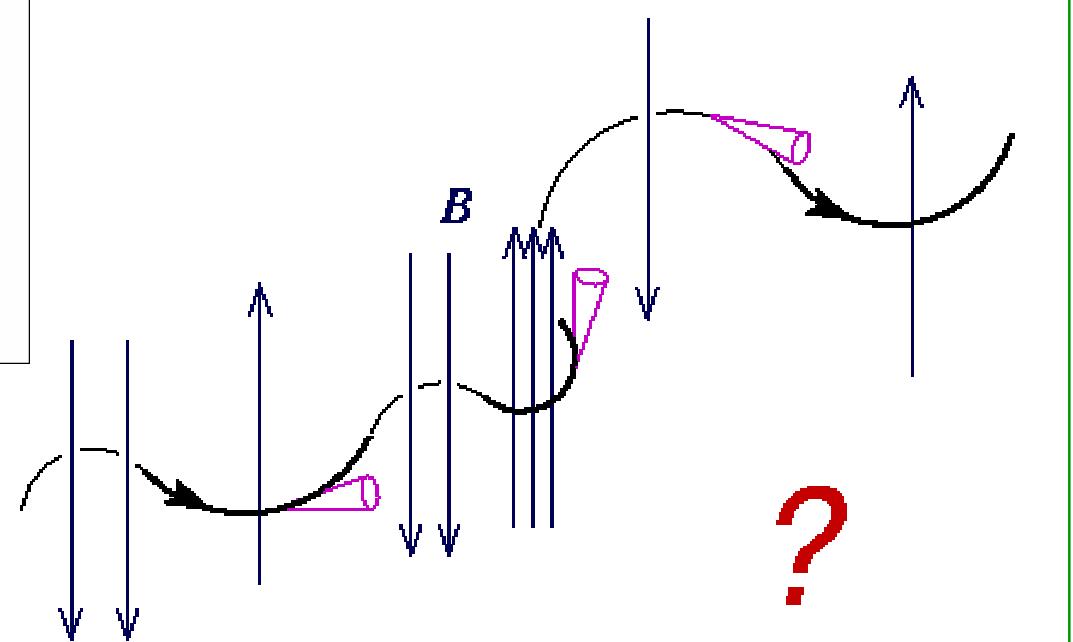


(Frederiksen, 2005, PhD thesis)

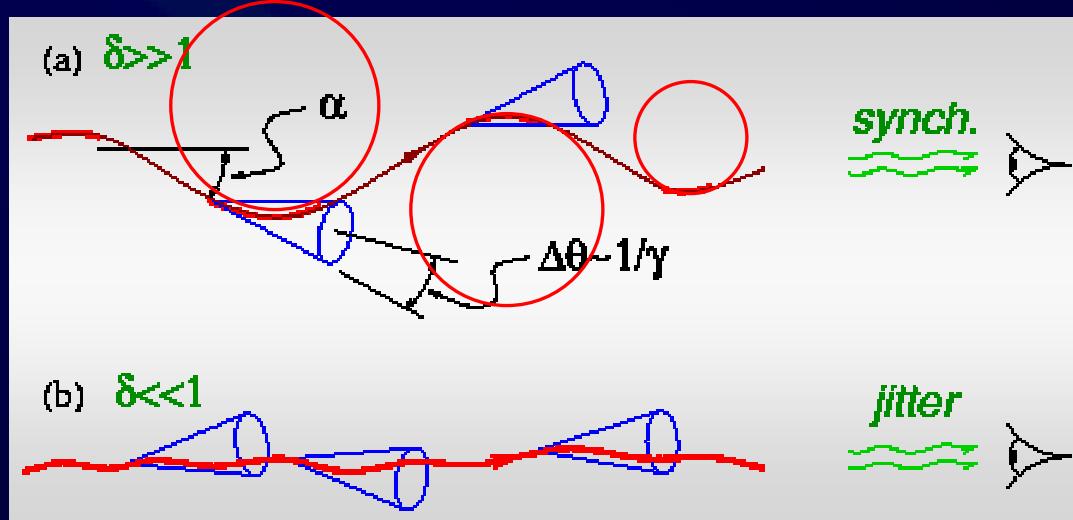
(Medvedev 2000, ApJ)

$$B(r) = B_1(r) , \quad B_0 = 0$$

(highly inhomogeneous, random)



Regimes



$$\omega_s \sim \gamma^2 \omega_H$$

$$\omega_j \sim \gamma^2 c/\lambda$$

Deflection parameter:

$$\delta = \frac{\alpha}{\Delta\theta} = \frac{eB\lambda}{mc^2}$$

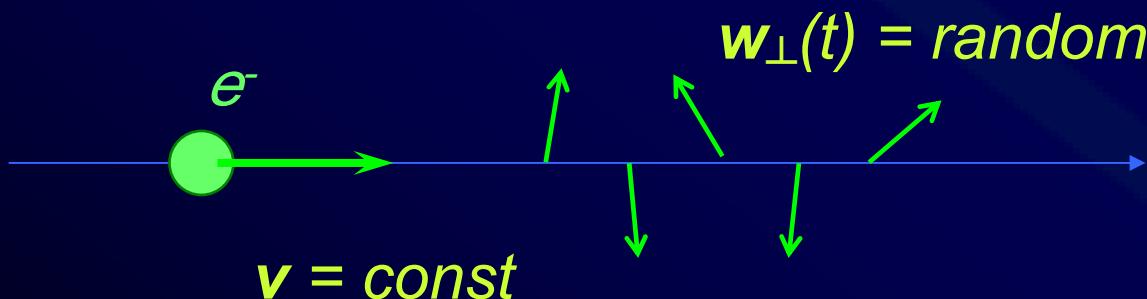
... independent of γ !

(Medvedev, 2000, ApJ)

Jitter regime

When $\delta \ll l$, one can assume that

- particle is highly relativistic $\gamma \gg 1$
- particle's trajectory is *piecewise-linear*
- particle velocity is nearly constant $\mathbf{r}(t) = \mathbf{r}_0 + \mathbf{v} t$
- particle experiences random acceleration $\mathbf{w}_\perp(t)$



Jitter radiation. Theory

Lienard-Wichert
potentials

$$dW = \frac{e^2}{2\pi c^3} \left(\frac{\omega}{\omega'}\right)^4 \left| \mathbf{n} \times \left[\left(\mathbf{n} - \frac{\mathbf{v}}{c} \right) \times \mathbf{w}_{\omega'} \right] \right|^2 d\Omega \frac{d\omega}{2\pi}$$

where $\mathbf{w}_{\omega'} = \int \mathbf{w} e^{i\omega' t} dt$ is the Fourier component of the particle's acceleration, $\omega' = \omega(1 - \mathbf{n} \cdot \mathbf{v}/c)$, and \mathbf{n} is the unit vector pointing toward the observer.

Small-angle
approximation

The dominant contribution
to the integral comes from
small angles

$$\theta \sim 1/\gamma$$

$$\begin{aligned}\omega' &\simeq \omega(1 - v/c + \theta^2/2) \\ &\simeq \omega/2(1 - v^2/c^2 + \theta^2) \\ &= \omega/2(\theta^2 + \gamma^{-2})\end{aligned}$$

$$\frac{dW}{d\omega} = \frac{e^2 \omega}{2\pi c^3} \int_{\omega/2\gamma^2}^{\infty} \frac{|\mathbf{w}_{\omega'}|^2}{\omega'^2} \left(1 - \frac{\omega}{\omega'^2} + \frac{\omega^2}{2\omega'^2\gamma^4} \right) d\omega'$$

Spectral power

Jitter radiation. Theory (cont.)

Fourier image of the particle acceleration from the 3D “(vxB) acceleration field”

We need to express the temporal Fourier component of the acceleration $\mathbf{w} \equiv F_L/\gamma m$ taken along the particle trajectory in terms of the Fourier component of the field in the spatial and temporal domains. Taking the Fourier transform of $\mathbf{w}(\mathbf{r}_0 + \mathbf{v}t, t)$, we have

$$\begin{aligned}\mathbf{w}_{\omega'} &= (2\pi)^{-4} \int e^{i\omega' t} dt \left(e^{-i(\Omega t - \mathbf{k} \cdot \mathbf{r}_0 - \mathbf{k} \cdot \mathbf{v}t)} \mathbf{w}_{\Omega, \mathbf{k}} d\Omega d\mathbf{k} \right) \\ &= (2\pi)^{-3} \int \mathbf{w}_{\Omega, \mathbf{k}} \delta(\omega' - \Omega + \mathbf{k} \cdot \mathbf{v}) e^{i\mathbf{k} \cdot \mathbf{r}_0} d\Omega d\mathbf{k},\end{aligned}$$

where we used that $\int e^{i\omega t} dt = 2\pi\delta(\omega)$. In a statisti-

$$\mathbf{w} = (e/\gamma mc)\mathbf{v} \times \mathbf{B}$$

$$w_\alpha = (e/\gamma mc) \frac{1}{2} e_{\alpha\beta\gamma} (v_\beta B_\gamma - v_\gamma B_\beta).$$

$$|\mathbf{w}_{\Omega, \mathbf{k}}|^2 = (ev/\gamma mc)^2 (\delta_{\alpha\beta} - v^{-2} v_\alpha v_\beta) \overline{B_{\Omega, \mathbf{k}}^\alpha B_{\Omega, \mathbf{k}}^{*\beta}}$$

$$\overline{B_{\Omega, \mathbf{k}}^\alpha B_{\Omega, \mathbf{k}}^{*\beta}} = C(\delta_{\alpha\beta} - n_\alpha n_\beta) f_z(k_{\parallel}) f_{xy}(k_{\perp}),$$

Lorentz force

Ensemble-averaged acceleration spectrum

B-field spectrum

Jitter Spectra: F_ν (1D)

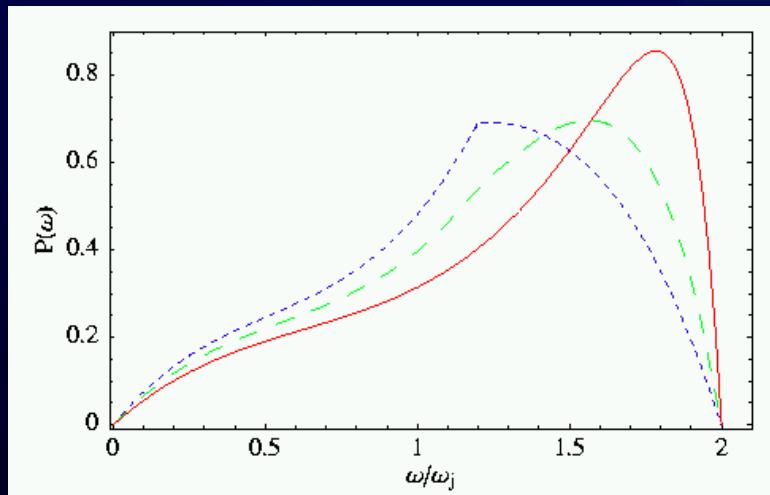
Weibel instability:

$$0 < k < k_{\max} \sim \omega_{p,e}/c$$

Assume, for illustration:

$$\langle B_k^2 \rangle \sim k^{2\mu}, \mu > 1$$

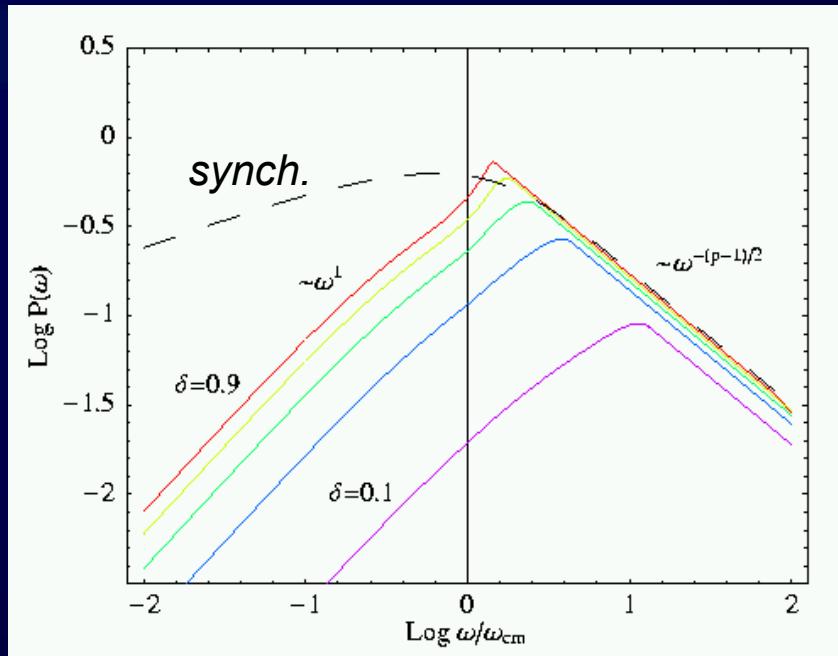
Single electron



$$N(\gamma) \sim \gamma^{-p}, \quad \gamma > \gamma_{\min}$$

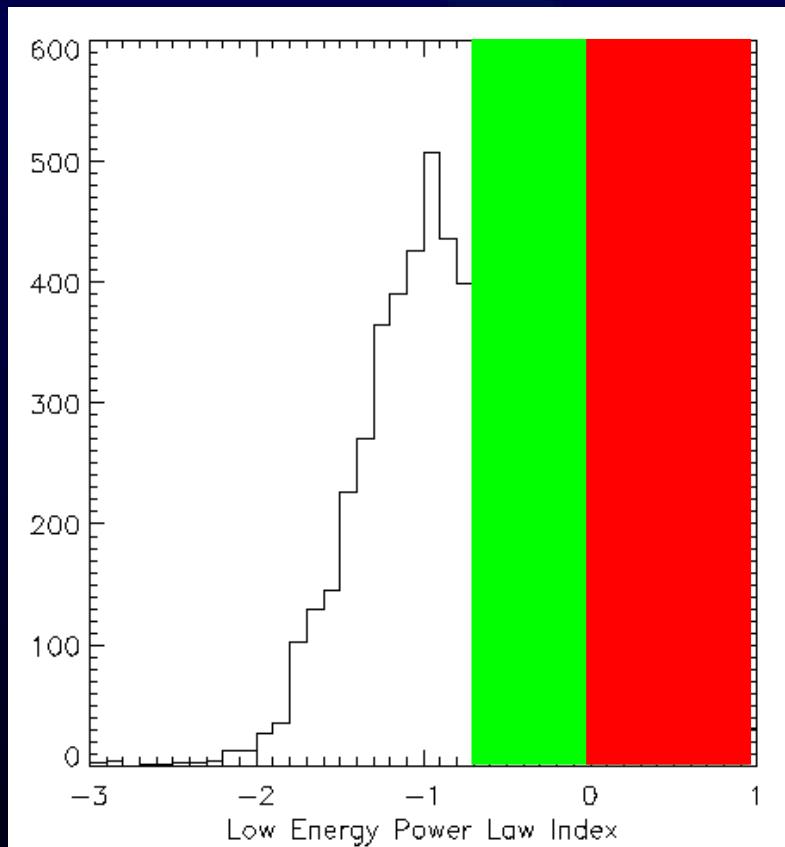
(Medvedev, ApJ, 2000)

Power-law electrons



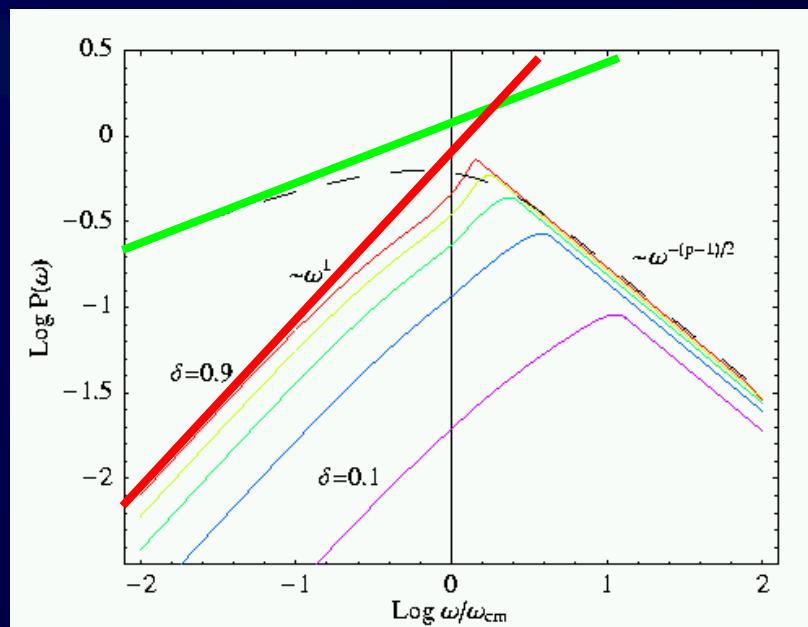
Synchrotron "Line of Death"

About 30% of BATSE GRBs and 50% of BSAX GRBs have photon soft indices α greater than $-2/3$, inconsistent with optically thin Synchrotron Shock Model



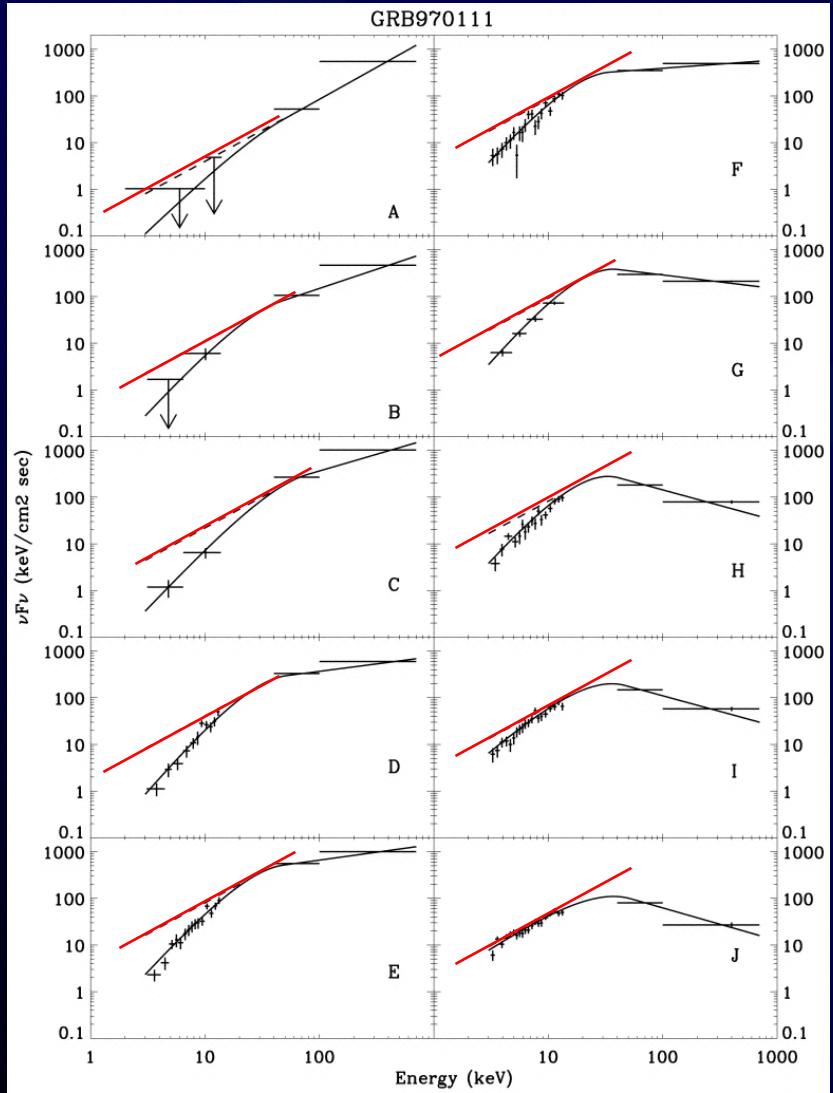
$$F_v \sim v^{\alpha+1}$$

(Medvedev, 2000)



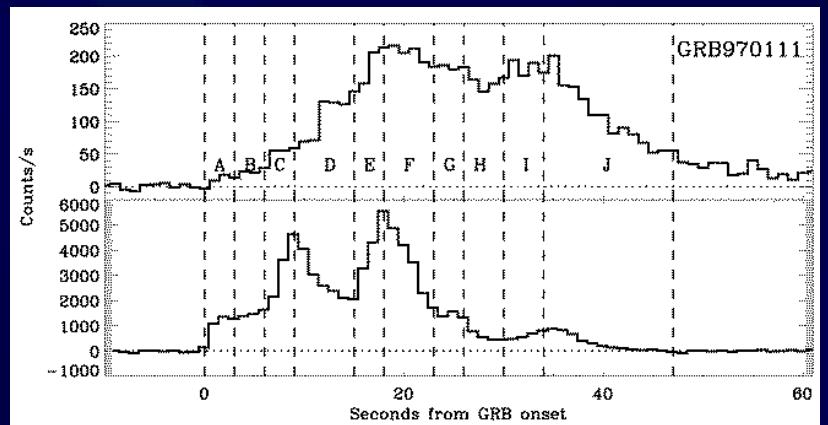
(Preece, et al., ApJS, 2000)

Beppo-SAX spectra



In a sample of 8 GRBs (2-700keV)
50% violate synchrotron limit

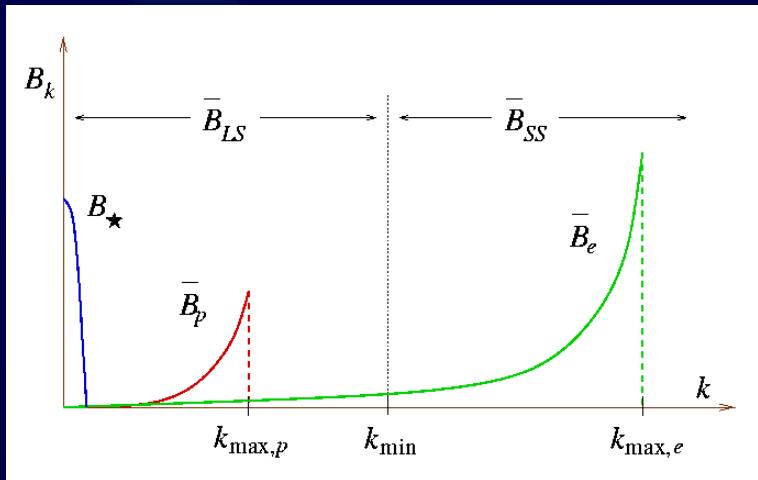
GRB 970111
soft photon index violates
synchrotron limit for the entire burst



(Frontera, et al., ApJ, 2000)

Composite Model of Spectra

(Medvedev, ApJ, 2000)



Frequencies

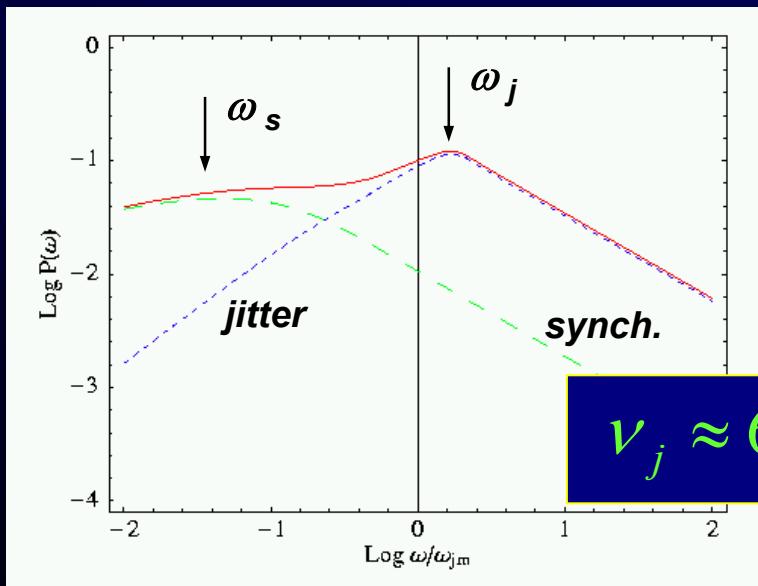
$$\frac{\omega_s}{\omega_j} = \frac{3}{2} \frac{B_{LS}}{B_{SS}} \delta$$

Fluxes

$$\frac{F_{J,\max}}{F_{S,\max}} = f(p, \mu) \delta^2$$

$$\delta \approx \sqrt{(m_p / m_e) \epsilon_B}$$

Break

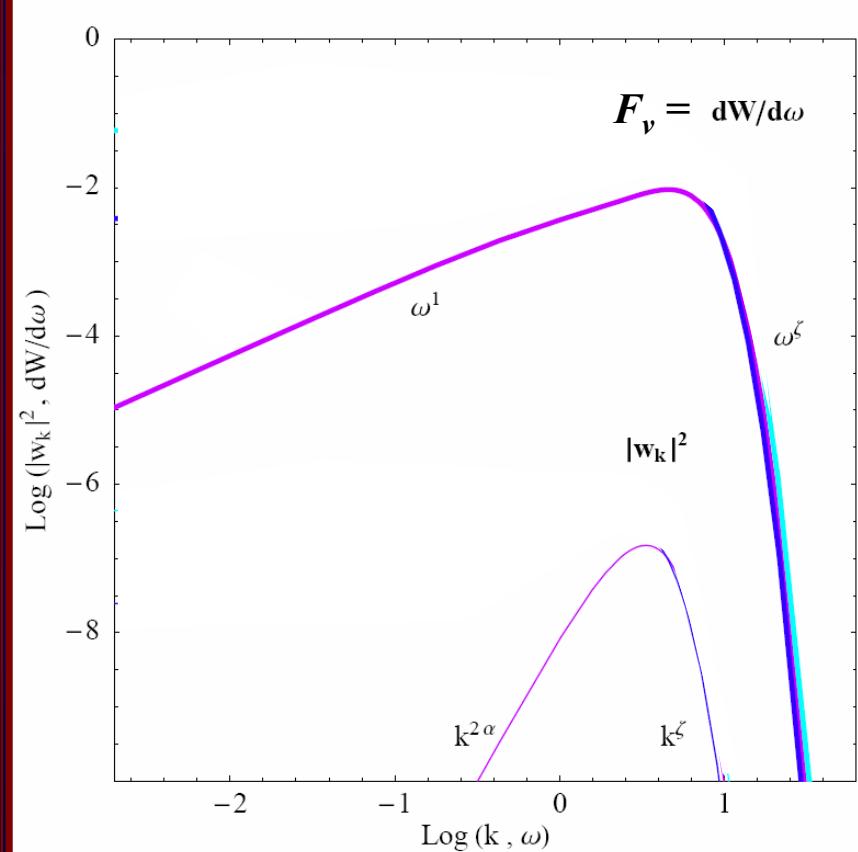


$$\nu_j \approx 6 \times 10^9 \gamma_{\min}^2 \Gamma_{\text{sh}} \Gamma_{\text{int}} \bar{\gamma}_e^{-1/2} n_{e,10}^{1/2} \text{ Hz}$$

Jitter does not work?

Fleishman, ApJ, astro-ph/0502145

- a low-frequency spectrum, $dI_\omega/d\omega \propto \omega^1$, valid in the presence of *ordered* small-scale magnetic field fluctuations, does not occur in the general case of small-scale *random* magnetic field fluctuations,



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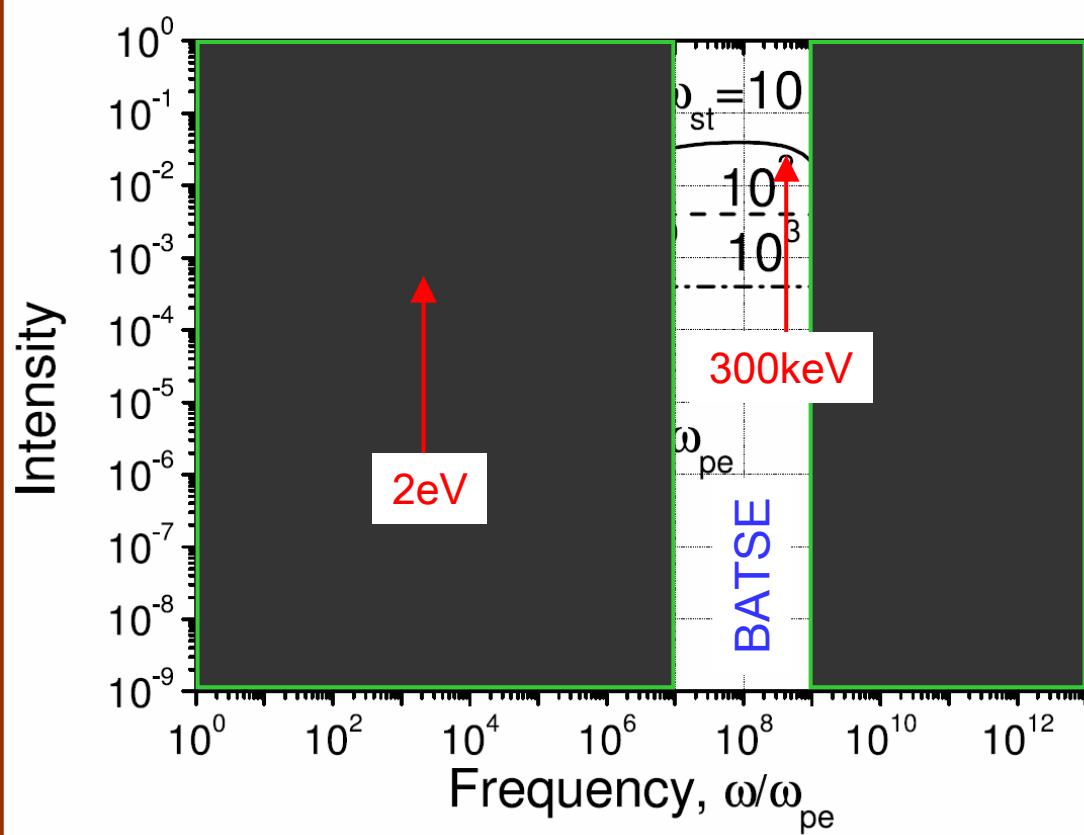
- diffusive synchrotron radiation arising from the scattering of fast electrons on small-scale *random* magnetic or/and electric fields produces a broad variety of low-frequency spectral asymptotes – from $dI_\omega/d\omega \propto \omega^0$ to $\propto \omega^2$ – sufficient to interpret the entire range of low energy spectral indices observed from GRB sources, while the high-frequency spectrum $dI_\omega/d\omega \propto \omega^{-\nu}$ may affect the corresponding high energy spectral index distribution.

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All “diffusive synchrotron” calculations

(perturbative and non-perturbative)

assume isotropic (!) field distribution.

→→ irrelevant for Weibel turbulence !!!

"Jitter" vs. "Diffusive Synchrotron"

No difference:
Same physical mechanism !

Mon. Not. R. Astron. Soc. 000, 1–6 (2005) Printed 11 November 2005 (MNRAS style file v2.2)

Diffusive synchrotron radiation from extragalactic jets

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Accepted 2005 October 13. Received 2005 October 13; in original form 2005 September 20

ABSTRACT

Flattened nonthermal radiation spectra observed from knots and interknot locations of the jets 3C273 and M87 in UV and X-ray bands are discussed within modern models of magnetic field generation in the relativistic jets. Specifically, we explicitly take into account the effect of the small-scale random magnetic field, probably present in such jets, which gives rise to emission of Diffusive Synchrotron Radiation, whose spectrum deviates substantially from the standard synchrotron spectrum, especially at high frequencies. The calculated spectra agree well with the observed ones if the energy densities contained in small-scale and large-scale magnetic fields are comparable. The implications of this finding for magnetic field generation, particle acceleration, and jet composition are discussed.

Key words: acceleration of particles – shock waves – turbulence – galaxies: jets – radiation mechanisms: non-thermal – magnetic fields

1 INTRODUCTION

Relativistic extragalactic jets are known to provide very efficient acceleration of relativistic electrons up to Lorentz-factors $\gamma \sim 10^4 - 10^5$ or higher (Hevens & Meisenheimer 1987). Quasi-exponential cut-offs found in many synchrotron sources in the infrared (IR), optical, or ultraviolet (UV) bands (Rieke et al. 1982; Röser & Meisenheimer 1986; Meisenheimer & Hevens 1986; Kedz 1988) are in a good agreement with the idea of a maximum energy of accelerated electrons, which results from the balance between the efficiency of the acceleration mechanism and synchrotron losses.

The presence of a high-energy cut-off in the energetic spectrum of relativistic electrons results naturally in a progressive spectral softening as the frequency increases in the region of the synchrotron cut-off, which indeed has been observed. However, recent observations (Jester et al. 2005) of the spectrum of the jet 3C273 performed with the highest angular resolution achieved so far ($0''.3$) revealed significant flattening of the radiation spectra in the UV band from most of the jet locations, including both knots and inter-knot regions.

This finding of a non-thermal UV spectral component cannot be easily accommodated within models of synchrotron emission produced by a single population of relativistic electrons (Jester et al. 2005) and requires either a distinct secondary component of relativistic particles,

We will refer the synchrotron radiative process in the presence of small-scale magnetic fields as *Diffusive Synchrotron Radiation* (DSR),

The second component is DSR (called also “3D jitter radiation”, Hededal (2005)) resulting from the interaction of the ultrarelativistic electrons with small-scale random fields.

(Fleishman, 2005, MNRAS (in press), astro-ph/0511353)

$$t_s = \frac{mc^2}{eB} = \frac{c}{\omega_{BS}}$$

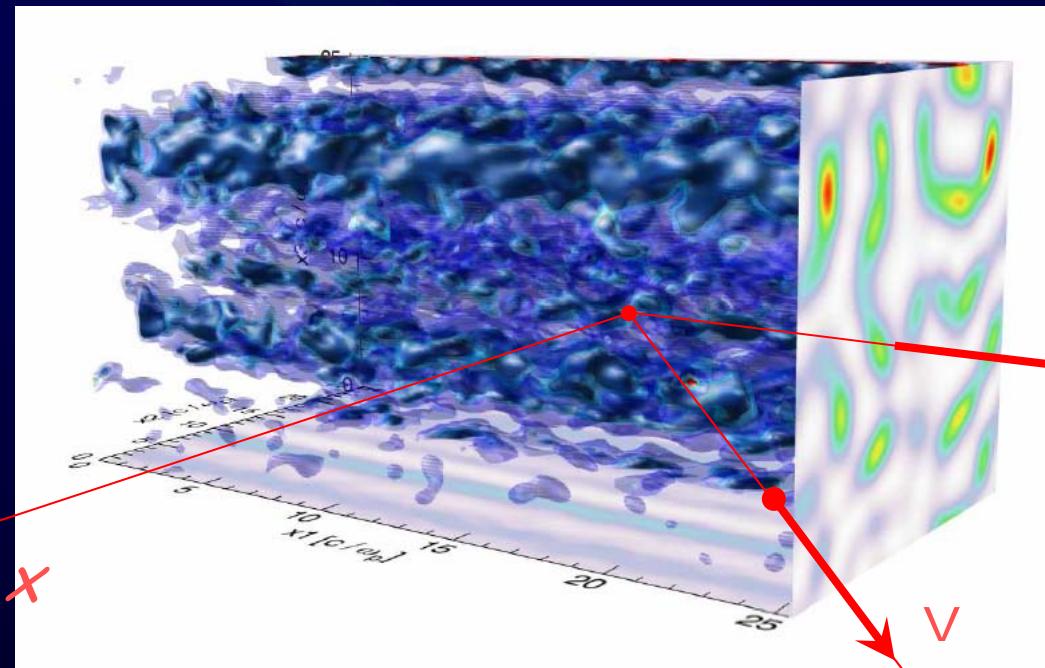
* E-mail: gregory@sun.ioffe.ru

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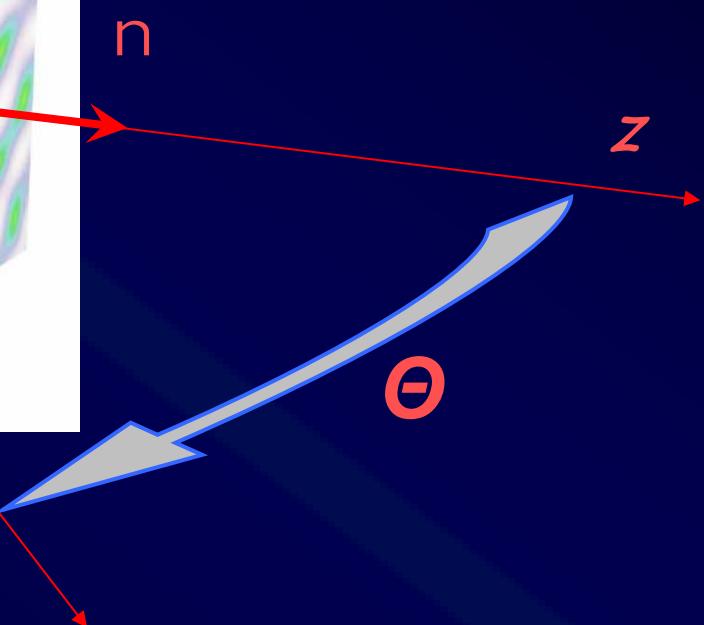
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Viewing angle effect

Radiation vs Θ



B-field is anisotropic:
 $\mathbf{B}_\perp = (B_x, B_y)$ is random,
 $B_z = 0$



Jitter + Weibel theory -- summary

Spectral power of radiation

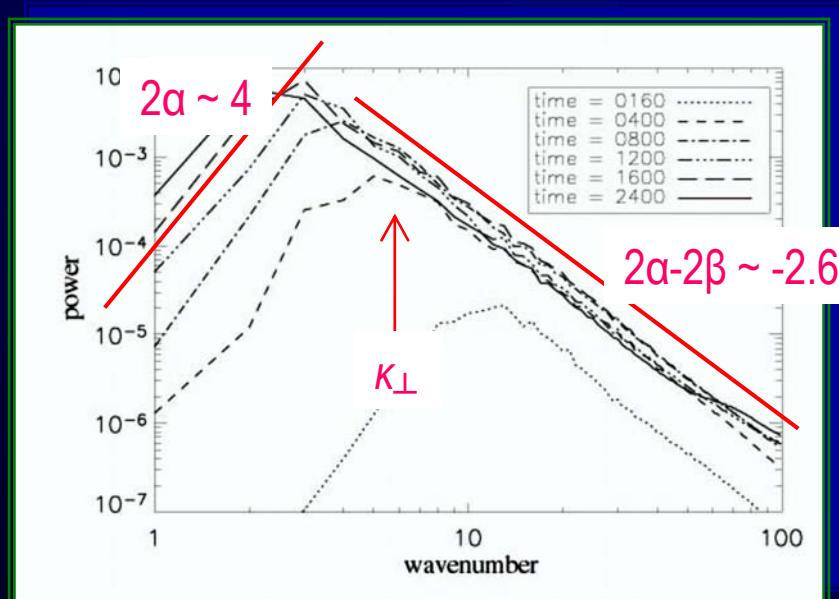
$$\frac{dW}{d\omega} = \frac{e^2 \omega}{2\pi c^3} \int_{\omega/2\gamma^2}^{\infty} \frac{|\mathbf{w}_{\omega'}|^2}{\omega'^2} \left(1 - \frac{\omega}{\omega' \gamma^2} + \frac{\omega^2}{2\omega'^2 \gamma^4}\right) d\omega',$$

Electron's acceleration
spectrum

$$\langle |\mathbf{w}_{\omega'}|^2 \rangle = \frac{C}{2\pi} (1 + \cos^2 \Theta) \int f_z(k_{\parallel}) f_{xy}(k_{\perp}) \delta(\omega' + \mathbf{k} \cdot \mathbf{v}) dk_{\parallel} d^2 k_{\perp}.$$

Models of field spectra,
independent in z and xy (!)

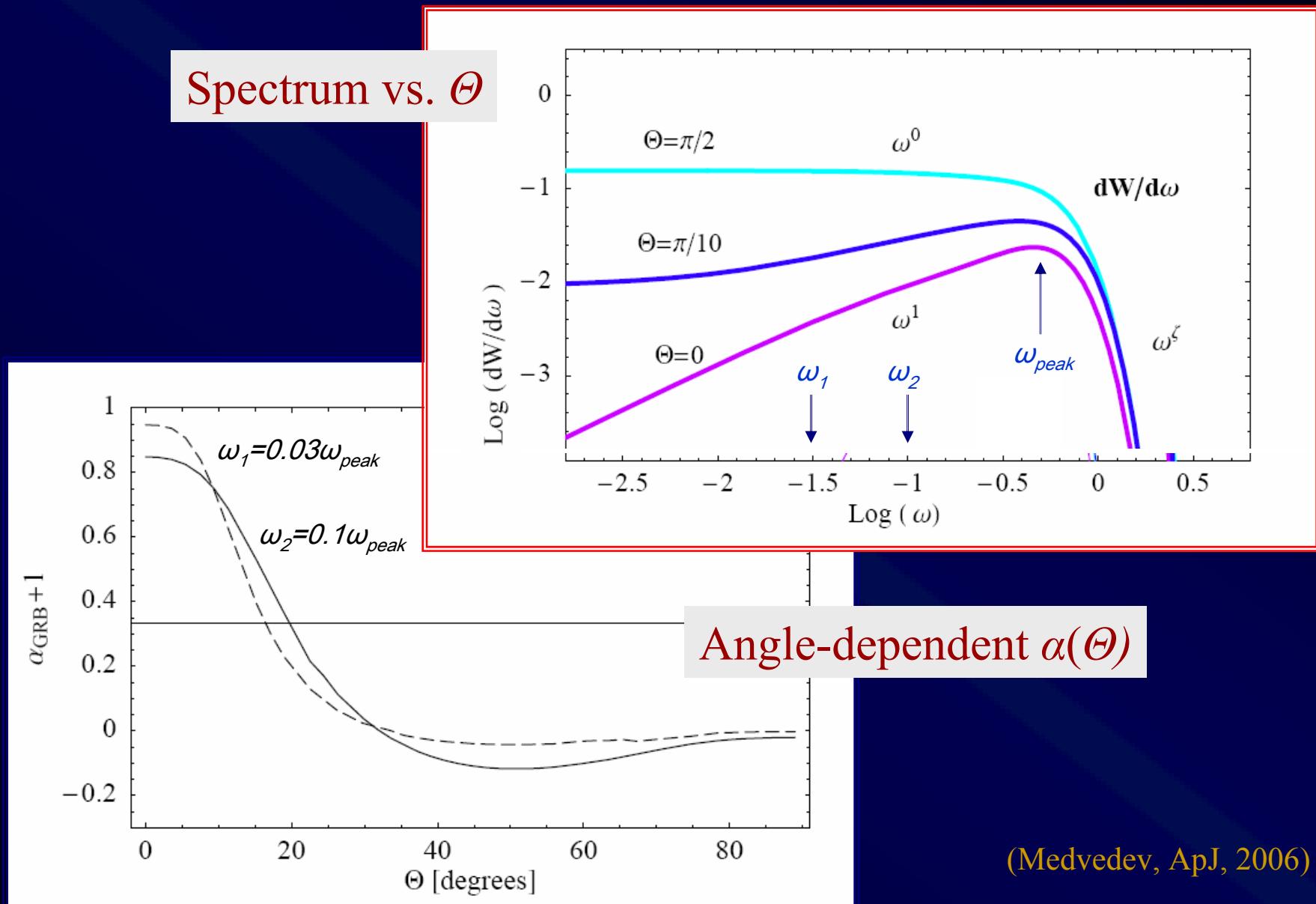
$$f_z(k_{\parallel}) = \frac{k_{\parallel}^{2\alpha_1}}{(\kappa_{\parallel}^2 + k_{\parallel}^2)^{\beta_1}}, \quad f_{xy}(k_{\perp}) = \frac{k_{\perp}^{2\alpha_2}}{(\kappa_{\perp}^2 + k_{\perp}^2)^{\beta_2}},$$



$$\begin{aligned} \alpha_2 &\sim 2 \\ \beta_2 &\sim -3.3 \\ K_{\perp} &\sim \text{const. } (\omega_{p,e}/c) \end{aligned}$$

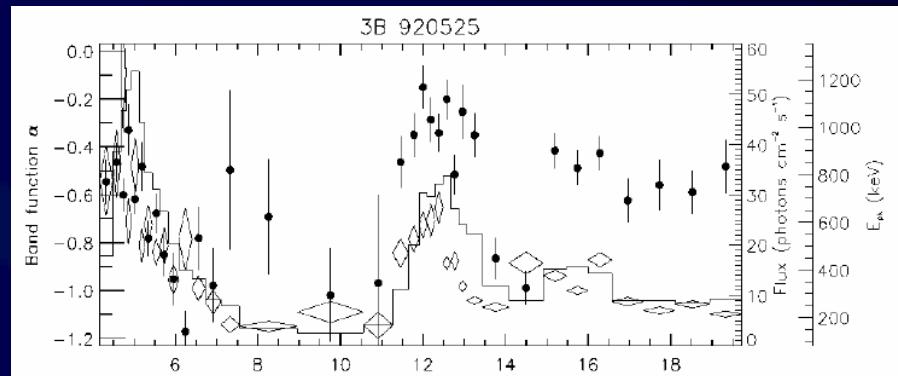
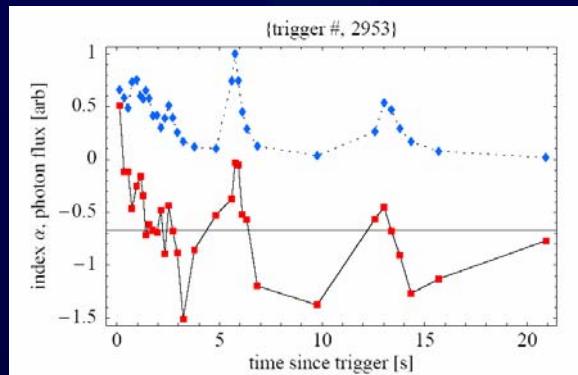
(Frederiksen, ApJL, 2004)

Spectrum vs. viewing angle

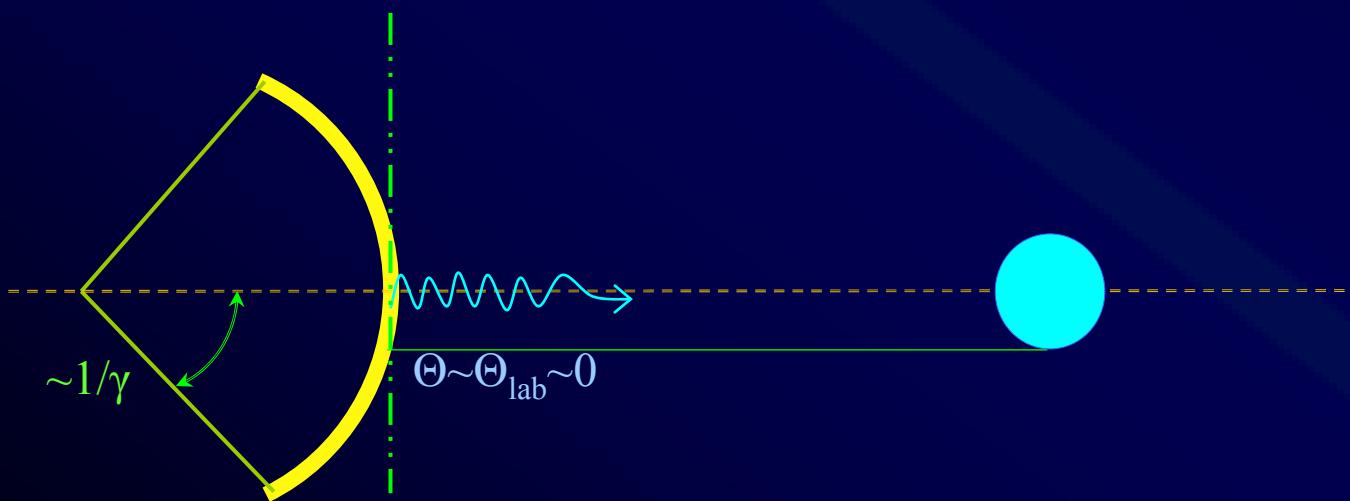


"Tracking" GRBs

Also, "hardness – intensity" correlation ; Also, "tracking behavior"



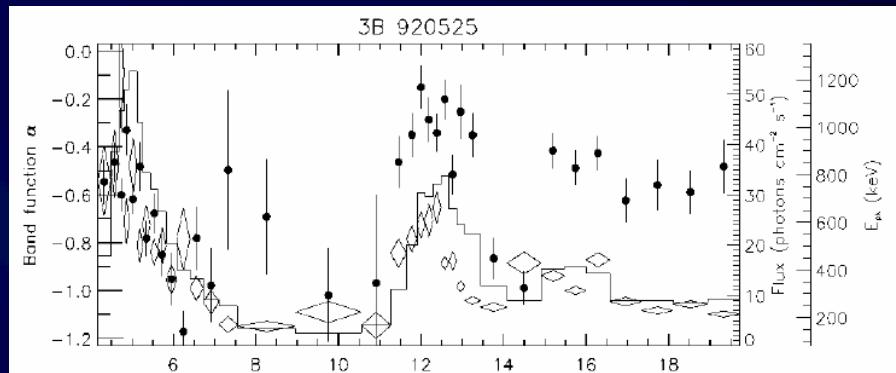
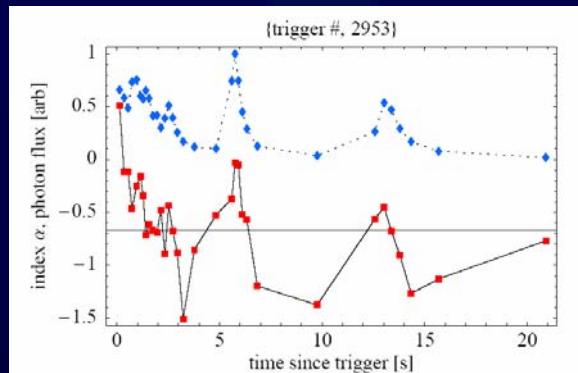
- = α
- ◇ = E_{peak}
- = Flux



t_1 , bright,
high E_{peak} ,
 $\alpha \sim 0$

"Tracking" GRBs

Also, "hardness – intensity" correlation ; Also, "tracking behavior"



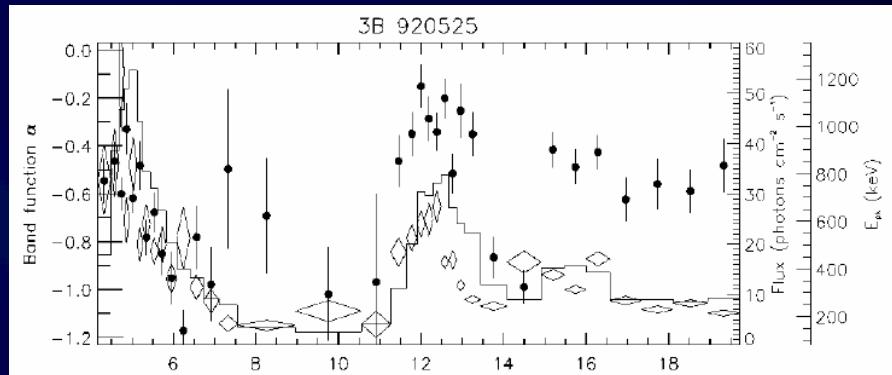
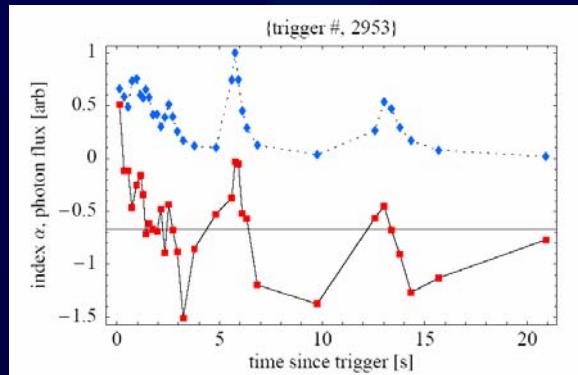
- = α
- ◇ = E_{peak}
- = Flux



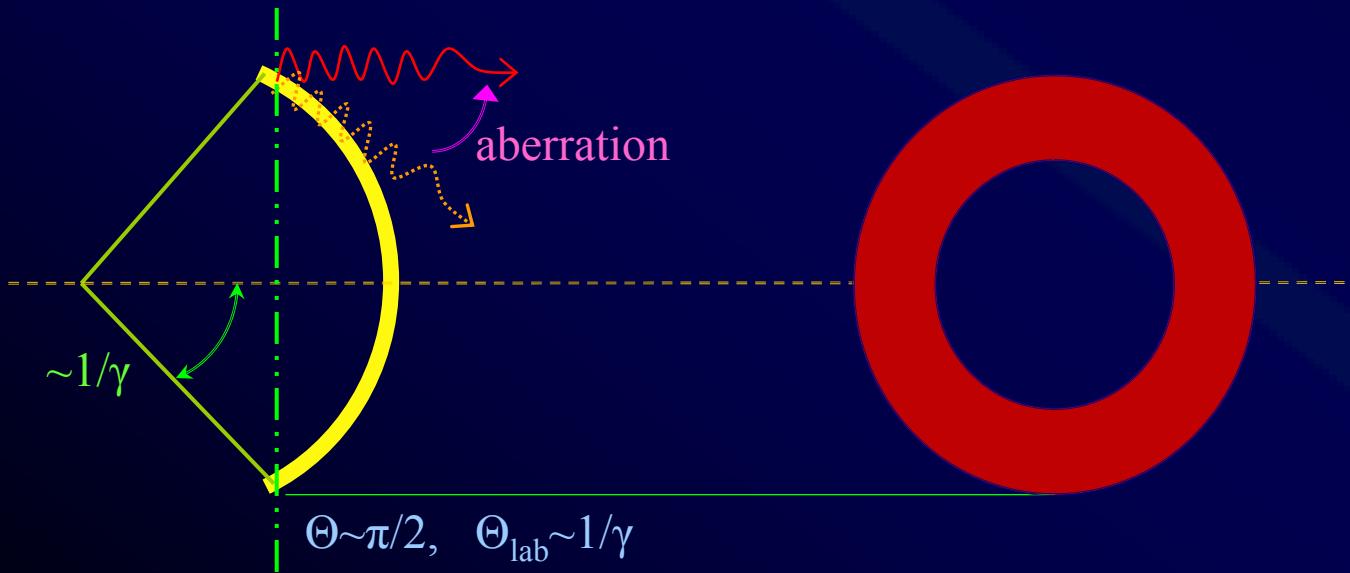
t_2 , intermediate
 $\alpha \sim -2/3$

“Tracking” GRBs

Also, “hardness – intensity” correlation ; Also, “tracking behavior”



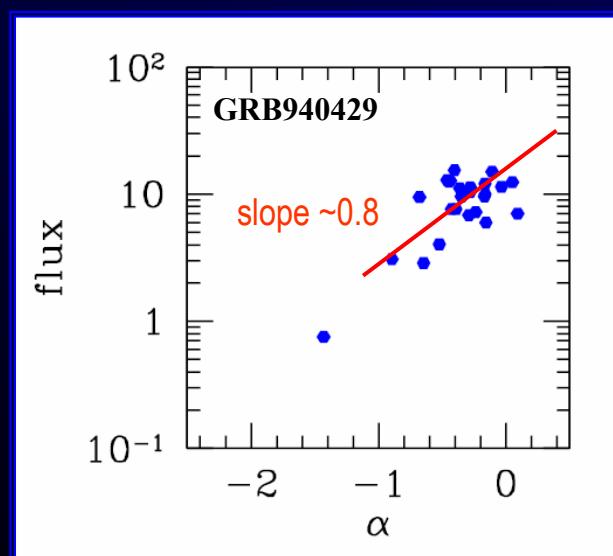
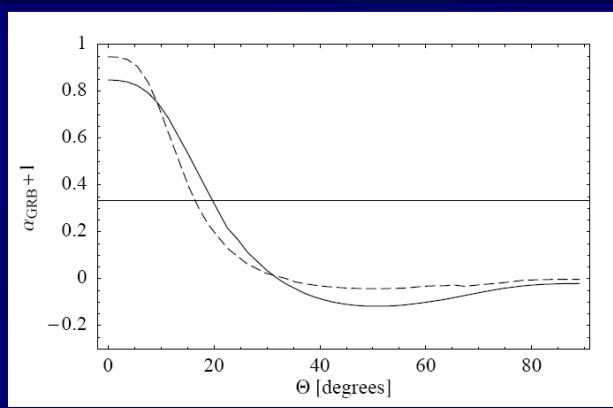
- = α
- ◇ = E_{peak}
- = Flux



t_3 , faint,
low E_{peak} ,
 $\alpha \sim -1$

Flux – α correlation

Also, “hardness – intensity” correlation ; Also, “tracking behavior”

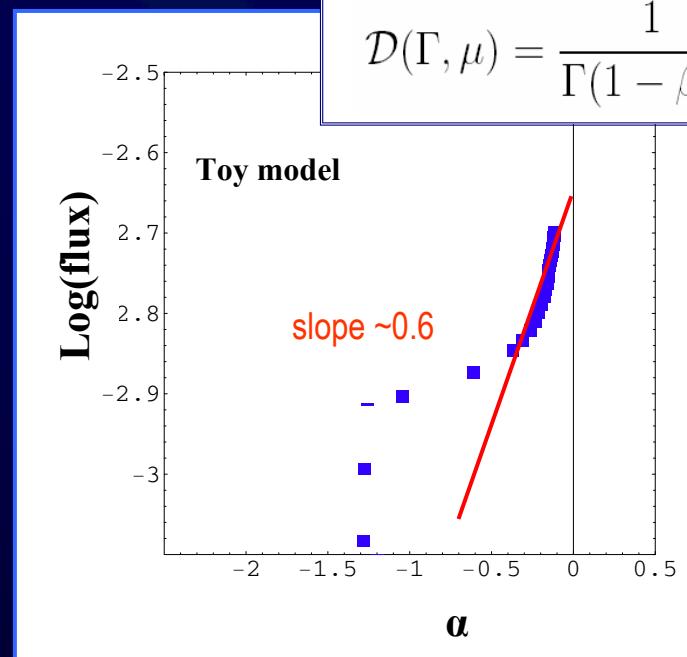


index α depends on Θ
bolometric flux depends on Θ

$$F_{\text{bol}}(t) = F_0 \mu \mathcal{D}^2(\mu) / \Gamma^2,$$

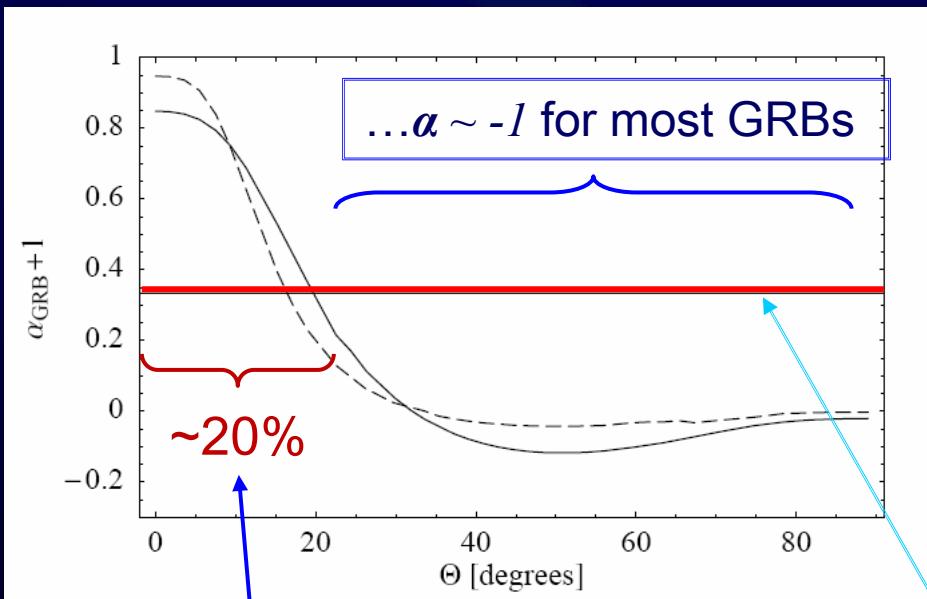
where the Lorentz boost is Θ -dependent

$$\mathcal{D}(\Gamma, \mu) = \frac{1}{\Gamma(1 - \beta\mu)} \quad \mu = \cos\theta$$

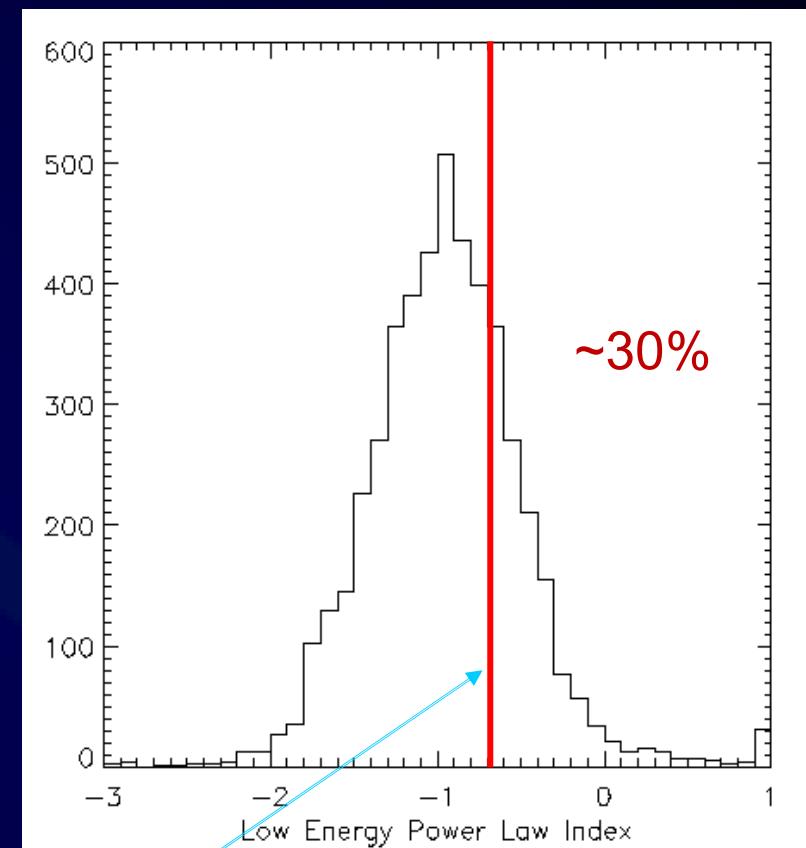


Statistics of α

index α depends on Θ



...of GRB spectra violate SLoD



Synchrotron “Line of Death”

Summary

- shock theory & simulations:
 - magnetic field generation
 - shock formation and evolution
 - e^+e^- and e^-p plasmas
 - particle acceleration (*heating*)
 - long-term evolution of the fields
- radiation production
 - jitter radiation
 - violation of the Synchrotron LoD
 - sharp spectral peaks
 - flux- α correlation (*hardness-intensity* correlation)
 - peak of α distribution at $\alpha \sim -1$
 - spectral variability (+ “*tracking*” behavior)
 - net polarization
 - polarization scintillations