

### **Stefano Profumo**

### University of California, Santa Cruz





### KITP, Santa Barbara (CA), February 4, 2020



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rapidly spiral inward due to the emission of gravitational radiation and ultimately will merge. Uncertainties in the rate for such events arise from our imprecise knowledge of the phase-space structure of galactic halos



- Why it is interesting to consider PBH as Dark Matter
- > Where it is interesting to look for PBH as Dark Matter
- ...some "NO-SEE-UMS" AND "SPACE COWS"

### First question: Can there be enough PBH around to be the DM?

What is the maximal fraction of dark matter in PBH?



Carr et al, 2017

### The fraction of PBH that could be the dark matter depends on the mass function!



...what is the mathematical function that maximizes the mass fraction of primordial black holes compatibly with constraints?

Carr et al, 2017

### The Maximal-Density Mass Function for Primordial Black Hole Dark Matter



 $\infty$ 

#### Benjamin V. Lehmann, Stefano Profumo and Jackson Yant

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**Abstract.** The advent of gravitational wave astronomy has rekindled interest in primordial black holes (PBH) as a dark matter candidate. As there are many different observational probes of the PBH density across different masses, constraints on PBH models are dependent on the functional form of the PBH more function. This complicates proved statements about

# Answer: with N independent constraints, the optimal function is a linear combination of N delta functions with calculable relative weights

 $\min \{ \|\mathbf{x}\| \mid \mathbf{x} \in \operatorname{conv} \{ \mathbf{g}(M) \mid M \in U \} \}$ 



### Answer: with N independent constraints, the optimal function is a linear combination of N delta functions with calculable relative weights

### **Numerical validation**

![](_page_11_Figure_1.jpeg)

![](_page_12_Figure_0.jpeg)

\* Lehmann, Profumo and Yant, JCAP 2018

	$f_{ m mono}$	$f_{ m max,all}$	$f_{ m max,GW}$	$\sigma[\psi]/M_{\odot}$	$\langle M/M_{\odot} \rangle$
Α	27.17	27.25	2.580	2.259	31.09
AB	1.372	1.965	5.139	0.162	0.009
AC	1.371	1.443	0.566	7.294	1.807
ABC	1.371	1.402	2.936	0.220	0.015
Ā	0.991	1.502	2.171	4.827	1.492
ĀΒ	0.991	1.437	11.07	0.221	0.017
ĀC	0.330	0.484	0.364	7.963	5.430
ĀBC	0.330	0.405	0.982	0.741	0.182

### So YES, depending on the constraints choice, PBH can be 100% of the dark matter!

Is there a **goldilocks** signature of **PBH**?

Yes! BH merger with a sub-Chandrasekhar mass (1.4 M<sub>sun</sub>)

LIGO search results are out\* (thanks Sarah!)

### Is there a **goldilocks** signature of **PBH**?

C. Talbot,<sup>6</sup> D. B. Tanner,<sup>30</sup> D. Tao,<sup>1</sup> M. Tápai,<sup>132</sup> A. Tapia,<sup>27</sup> J. D. Tasson,<sup>98</sup> R. Taylor,<sup>1</sup> R. Tenorio,<sup>102</sup> L. Terkowski,<sup>135</sup> M. Thomas,<sup>7</sup> P. Thomas,<sup>47</sup> S. R. Thondapu,<sup>60</sup> K. A. Thorne,<sup>7</sup> E. Thrane,<sup>6</sup> Shubhanshu Tiwari,<sup>118,119</sup> Srishti Tiwari,<sup>136</sup> V. Tiwari,<sup>107</sup> K. Toland,<sup>46</sup> M. Tonelli,<sup>20,21</sup> Z. Tornasi,<sup>46</sup> A. Torres-Forné,<sup>190</sup> C. I. Torrie,<sup>1</sup> D. Töyrä,<sup>13</sup> F. Travasso,<sup>29,41</sup> G. Traylor,<sup>7</sup> M. C. Tringali,<sup>74</sup> A. Tripathee,<sup>138</sup> A. Trovato,<sup>26</sup> L. Trozzo,<sup>191,21</sup> K. W. Tsang,<sup>37</sup> M. Tse,<sup>14</sup> R. Tso,<sup>48</sup> L. Tsukada,<sup>82</sup> D. Tsuna,<sup>82</sup> T. Tsutsui,<sup>82</sup> D. Tuyenbayev,<sup>109</sup> K. Ueno,<sup>82</sup> D. Ugolini,<sup>192</sup> C. S. Unnikrishnan,<sup>136</sup> A. L. Urban,<sup>2</sup> S. A. Usman,<sup>93</sup> H. Vahlbruch,<sup>10</sup> G. Vajente,<sup>1</sup> G. Valdes,<sup>2</sup> M. Valentini,<sup>118,119</sup> N. van Bakel,<sup>37</sup> M. van Beuzekom,<sup>37</sup> J. F. J. van den Brand,<sup>75,37</sup> C. Van Den Broeck,<sup>37,193</sup> D. C. Vander-Hyde,<sup>42</sup> L. van der Schaaf,<sup>37</sup> J. V. VanHeijningen,<sup>66</sup> A. A. van Veggel,<sup>46</sup> M. Vardaro,<sup>53,54</sup> V. Varma,<sup>48</sup> S. Vass,<sup>1</sup> M. Vasúth,<sup>50</sup> A. Vecchio,<sup>13</sup> G. Vedovato,<sup>54</sup> J. Veitch,<sup>46</sup> P. J. Veitch,<sup>57</sup> K. Venkateswara,<sup>179</sup> G. Venugopalan,<sup>1</sup> D. Verkindt,<sup>34</sup> F. Vetrano,<sup>63,64</sup> A. Viceré,<sup>63,64</sup> A. D. Viets,<sup>24</sup> S. Vinciguerra,<sup>13</sup> D. J. Vine,<sup>133</sup> J.-Y. Vinet,<sup>65</sup> S. Vitale,<sup>14</sup> T. Vo,<sup>42</sup> H. Vocca,<sup>40,41</sup> C. Vorvick,<sup>47</sup> S. P. Vyatchanin,<sup>61</sup> A. R. Wade,<sup>1</sup> L. E. Wade,<sup>122</sup> M. Wade,<sup>122</sup> R. Walet,<sup>37</sup> M. Walker,<sup>27</sup> L. Wallace,<sup>1</sup> S. Walsh,<sup>24</sup> H. Wang,<sup>13</sup> J. Z. Wang,<sup>138</sup> S. Wang,<sup>19</sup> W. H. Wang,<sup>109</sup> Y. F. Wang,<sup>94</sup> R. L. Ward,<sup>8</sup> Z. A. Warden,<sup>35</sup> J. Warner,<sup>47</sup> M. Was,<sup>34</sup> J. Watchi,<sup>103</sup> B. Weaver,<sup>47</sup> L.-W. Wei,<sup>9,10</sup> M. Weinert,<sup>9,10</sup> A. J. Weinstein,<sup>1</sup> R. Weiss,<sup>14</sup> F. Wellmann,<sup>9,10</sup> L. Wen,<sup>66</sup> E. K. Wessel,<sup>19</sup> P. Weßels,<sup>9,10</sup> J. W. Westhouse,<sup>35</sup> K. Wette,<sup>8</sup> J. T. Whelan,<sup>62</sup> B. F. Whiting,<sup>30</sup> C. Whittle,<sup>14</sup> D. M. Wilken,<sup>9,10</sup> D. Williams,<sup>46</sup> A. R. Williamson,<sup>143,37</sup> J. L. Willis,<sup>1</sup> B. Willke,<sup>10,9</sup> W. Winkler,<sup>9,10</sup> C. C. Wipf,<sup>1</sup> H. Wittel,<sup>9,10</sup> G. Woan,<sup>46</sup> J. Woehler,<sup>9,10</sup> J. K. Wofford,<sup>62</sup> J. L. Wright,<sup>46</sup> D. S. Wu,<sup>9,10</sup> D. M. Wysocki,<sup>62</sup> S. Xiao,<sup>1</sup> R. Xu,<sup>110</sup> H. Yamamoto,<sup>1</sup> C. C. Yancey,<sup>77</sup> L. Yang,<sup>121</sup> Y. Yang,<sup>30</sup> Z. Yang,<sup>43</sup> M. J. Yap,<sup>8</sup> M. Yazback,<sup>30</sup> D. W. Yeeles,<sup>107</sup> Hang Yu,<sup>14</sup> Haocun Yu,<sup>14</sup> S. H. R. Yuen,<sup>94</sup> A. K. Zadrożny,<sup>109</sup> A. Zadrożny,<sup>157</sup> M. Zanolin,<sup>35</sup> T. Zelenova,<sup>29</sup> J.-P. Zendri,<sup>54</sup> M. Zevin,<sup>58</sup> J. Zhang,<sup>66</sup> L. Zhang,<sup>1</sup> T. Zhang,<sup>46</sup> C. Zhao,<sup>66</sup> G. Zhao,<sup>103</sup> M. Zhou,<sup>58</sup> Z. Zhou,<sup>58</sup> X. J. Zhu,<sup>6</sup> A. B. Zimmerman,<sup>194</sup> M. E. Zucker,<sup>1,14</sup> and J. Zweizig<sup>1</sup>

(LIGO Scientific Collaboration and the Virgo Collaboration)

![](_page_15_Picture_3.jpeg)

Is there a **goldilocks** signature of **PBH**?

Yes! BH merger with a sub-Chandrasekhar mass (1.4 M<sub>sun</sub>)

### Given a mass function, one can calculate:

1. Rate of "goldilocks events"

$$R(\psi) = \int dm_1 \, dm_2 \, \mathcal{R}(\psi; \ m_1, m_2) V_{\text{eff}}(m_1, m_2)$$

### 2. Mass fraction of light+detectable BHs

$$p_{\rm LD} = \frac{\int_{M_{\rm LD,min}}^{M_{\rm LD,max}} \mathrm{d}M \,\psi(M)}{\int_0^\infty \mathrm{d}M \,\psi(M)}$$

### We can numerically compute the maximal possible "goldilocks event rate"

Maximum merger rate (discovery potential)

![](_page_17_Figure_2.jpeg)

\* Lehmann, Profumo and Yant, in progress

### ...but given a light+detectable fraction, and a total mass fraction, a minimal rate also exists!

Minimum merger rate (constraint potential)

![](_page_18_Figure_2.jpeg)

\* Lehmann, Profumo and Yant, in progress

### ...and we can calculate an "optimal" mass fraction

![](_page_19_Figure_1.jpeg)

### PRELIMINARY

\* Lehmann, Profumo and Yant, in progress

### Besides the mass, LIGO informs us about the spin of BHs...

### Besides the mass, LIGO informs us about the spin of BHs...

LIGO/Virgo Collaboration arXiv:1811.12940

Event	$m_1/{ m M}_{\odot}$	$m_2/M_{\odot}$	$\mathcal{M}/M_{\odot}$	$\chi_{ m eff}$	$M_{\rm f}/{ m M}_{\odot}$	$a_{\mathrm{f}}$	$E_{\rm rad}/({\rm M}_{\odot}c^2)$	$\ell_{peak}/(ergs^{-1})$	$d_L/Mpc$	z	$\Delta\Omega/deg^2$
GW150914	$35.6^{+4.8}_{-3.0}$	$30.6^{+3.0}_{-4.4}$	$28.6^{+1.6}_{-1.5}$	$-0.01^{+0.12}_{-0.13}$	$63.1^{+3.3}_{-3.0}$	$0.69^{+0.05}_{-0.04}$	$3.1^{+0.4}_{-0.4}$	$3.6^{+0.4}_{-0.4}\times10^{56}$	$430^{+150}_{-170}$	$0.09\substack{+0.03 \\ -0.03}$	180
GW151012	$23.3^{+14.0}_{-5.5}$	$13.6^{+4.1}_{-4.8}$	$15.2^{+2.0}_{-1.1}$	$0.04^{+0.28}_{-0.19}$	$35.7^{+9.9}_{-3.8}$	$0.67^{+0.13}_{-0.11}$	$1.5^{+0.5}_{-0.5}$	$3.2^{+0.8}_{-1.7} \times 10^{56}$	$1060^{+540}_{-480}$	$0.21\substack{+0.09 \\ -0.09}$	1555
GW151226	$13.7^{+8.8}_{-3.2}$	$7.7^{+2.2}_{-2.6}$	$8.9^{+0.3}_{-0.3}$	$0.18^{+0.20}_{-0.12}$	$20.5^{+6.4}_{-1.5}$	$0.74\substack{+0.07 \\ -0.05}$	$1.0^{+0.1}_{-0.2}$	$3.4^{+0.7}_{-1.7}\times10^{56}$	$440^{+180}_{-190}$	$0.09\substack{+0.04 \\ -0.04}$	1033
GW170104	$31.0^{+7.2}_{-5.6}$	$20.1^{+4.9}_{-4.5}$	$21.5^{+2.1}_{-1.7}$	$-0.04^{+0.17}_{-0.20}$	$49.1^{+5.2}_{-3.9}$	$0.66\substack{+0.08\\-0.10}$	$2.2^{+0.5}_{-0.5}$	$3.3^{+0.6}_{-0.9}\times10^{56}$	$960^{+430}_{-410}$	$0.19\substack{+0.07 \\ -0.08}$	924
GW170608	$10.9^{+5.3}_{-1.7}$	$7.6^{+1.3}_{-2.1}$	$7.9^{+0.2}_{-0.2}$	$0.03^{+0.19}_{-0.07}$	$17.8^{+3.2}_{-0.7}$	$0.69\substack{+0.04\\-0.04}$	$0.9^{+0.05}_{-0.1}$	$3.5^{+0.4}_{-1.3}\times10^{56}$	$320^{+120}_{-110}$	$0.07\substack{+0.02 \\ -0.02}$	396
GW170729	$50.6^{+16.6}_{-10.2}$	$34.3^{+9.1}_{-10.1}$	$35.7^{+6.5}_{-4.7}$	$0.36^{+0.21}_{-0.25}$	$80.3^{+14.6}_{-10.2}$	$0.81\substack{+0.07 \\ -0.13}$	$4.8^{+1.7}_{-1.7}$	$4.2^{+0.9}_{-1.5}\times10^{56}$	$2750^{+1350}_{-1320}$	$0.48\substack{+0.19 \\ -0.20}$	1033
GW170809	$35.2^{+8.3}_{-6.0}$	$23.8\substack{+5.2\\-5.1}$	$25.0^{+2.1}_{-1.6}$	$0.07^{+0.16}_{-0.16}$	$56.4^{+5.2}_{-3.7}$	$0.70\substack{+0.08\\-0.09}$	$2.7^{+0.6}_{-0.6}$	$3.5^{+0.6}_{-0.9}\times10^{56}$	$990^{+320}_{-380}$	$0.20\substack{+0.05 \\ -0.07}$	340
GW170814	$30.7^{+5.7}_{-3.0}$	$25.3\substack{+2.9\\-4.1}$	$24.2^{+1.4}_{-1.1}$	$0.07^{+0.12}_{-0.11}$	$53.4^{+3.2}_{-2.4}$	$0.72\substack{+0.07 \\ -0.05}$	$2.7^{+0.4}_{-0.3}$	$3.7^{+0.4}_{-0.5}\times10^{56}$	$580^{+160}_{-210}$	$0.12\substack{+0.03 \\ -0.04}$	87
GW170817	$1.46^{+0.12}_{-0.10}$	$1.27^{+0.09}_{-0.09}$	$.186^{+0.00}_{-0.00}$	$0.00^{+0.02}_{-0.01}$	≤ 2.8	$\leq 0.89$	$\geq 0.04$	$\geq 0.1 \times 10^{56}$	$40^{+10}_{-10}$	$0.01\substack{+0.00\\-0.00}$	16
GW170818	$35.5^{+7.5}_{-4.7}$	$26.8^{+4.3}_{-5.2}$	$26.7^{+2.1}_{-1.7}$	$-0.09^{+0.18}_{-0.21}$	$59.8^{+4.8}_{-3.8}$	$0.67\substack{+0.07 \\ -0.08}$	$2.7^{+0.5}_{-0.5}$	$3.4^{+0.5}_{-0.7}\times10^{56}$	$1020^{+430}_{-360}$	$0.20\substack{+0.07 \\ -0.07}$	39
GW170823	$39.6^{+10.0}_{-6.6}$	$29.4_{-7.1}^{+6.3}$	$29.3^{+4.2}_{-3.2}$	$0.08^{+0.20}_{-0.22}$	$65.6^{+9.4}_{-6.6}$	$0.71\substack{+0.08\\-0.10}$	$3.3^{+0.9}_{-0.8}$	$3.6^{+0.6}_{-0.9}\times10^{56}$	$1850^{+840}_{-840}$	$0.34\substack{+0.13 \\ -0.14}$	1651

### Masses

Spin

![](_page_21_Picture_5.jpeg)

![](_page_21_Picture_6.jpeg)

# Effective Spin

 $\vec{J} = \vec{L} + \vec{S}$ 

 $=\vec{S_1}+\vec{S_2}$ 

 $heta_{
m LS}$ 

 $\vec{L}$ 

 $\chi_{ ext{eff}}$ 

![](_page_22_Figure_1.jpeg)

Dimensionless spin parameter

$$\chi_{\rm eff} = \frac{m_1 \chi_1 \cos \theta_1 + m_2 \chi_2 \cos \theta_2}{m_1 + m_2}$$

Information about:

- Direction. +++
- Spin magnitude. ++
- masses. +

# Effective Spin = 1

![](_page_23_Figure_1.jpeg)

Most black holes from stellar binaries probably start off with their spins aligned

![](_page_24_Figure_0.jpeg)

Spins are essentially isotropic in the dynamical formation scenario. Binary was probably formed in a cluster

![](_page_25_Figure_0.jpeg)

Spin magnitudes are close to zero (expected from PBHs).

![](_page_26_Figure_0.jpeg)

Both spins are anti-aligned with its orbit (rare)

### **Magnitude Spin Priors**

![](_page_27_Figure_1.jpeg)

# Model Selection

- Spin magnitude: Low (L), Flat (F), High (H) and PBH
- Spin orientations: Isotropic (I) and Aligned (A)

Example:

FI = Flat spin magnitude and isotropic spins (LIGO)FA = Flat spin magnitude and align spins

### **Effective Spin Priors**

![](_page_29_Figure_1.jpeg)

![](_page_30_Figure_0.jpeg)

## Evolution of the Odds ratios

![](_page_31_Figure_1.jpeg)

# Evolution of the Odds ratios

![](_page_32_Figure_1.jpeg)

**Truth: Low-isotropic** 

### What about mixed models?

### What about mixed models?

![](_page_34_Figure_1.jpeg)

![](_page_35_Figure_1.jpeg)

# Assuming an initial spin and alignment distribution, one can compute the "best-fit" axion mass

Similarly, spin measurements can put constraints on axion-like particles

![](_page_36_Figure_1.jpeg)

### **Regge** plot (effective spin vs mass) assuming Flat priors for both mass and spin\*

\*Fernandez, Ghalsasy, Profumo, 1911.07862

![](_page_37_Figure_1.jpeg)

\*Fernandez, Ghalsasy, Profumo, 1911.07862

![](_page_38_Figure_1.jpeg)

### **Posterior Probability for ALP mass**

\*Fernandez, Ghalsasy, Profumo, 1911.07862

![](_page_39_Figure_0.jpeg)

<sup>9</sup>There have been suggestions that the actual energy loss is much greater than given by the dynamical friction formula when the sum over modes is taken into account [74], due to generation of surface waves. See, however, Ref. [98], who find a much smaller surface wave contribution. We have done our own derivation of Eq. (13) of Ref. [98] using Fourier (definite  $k_x$  and  $k_y$ ) instead of cylindrical modes, and find the same result.

![](_page_40_Figure_0.jpeg)

### SUBARU HSC microlensing, 1701.02151 VERSION 1

![](_page_41_Figure_0.jpeg)

### SUBARU HSC microlensing, 1701.02151 VERSION 2: wave effects

\* Katz et al, 1807.11495

![](_page_42_Figure_1.jpeg)

SUBARU HSC microlensing, VERSION 3: finite source AND wave effects

...but assuming all stars have  $R = R_{sun}$  !

...but are these bounds robust?

A few (worrisome) assumptions:

> All stars are at the same distance

> All stars have the same size (1 R<sub>sun</sub>)

DM is completely smooth

\* Smyth, Profumo et al, 1910.01285, PRD

![](_page_43_Picture_6.jpeg)

### Sun-like stars are however too dim for HSC!

![](_page_44_Figure_1.jpeg)

### \* Smyth, Profumo et al, 1910.01285, PRD

![](_page_44_Picture_3.jpeg)

![](_page_45_Figure_0.jpeg)

\* Smyth, Profumo et al, 1910.01285, PRD

# ...even if PBH are NOT the dark matter, they can PRODUCE the dark matter via Hawking evaporation!

![](_page_46_Picture_1.jpeg)

### John Tamanas

Country	WCA ID	Gender	Competitions
United States	2007TAMA02	Male	41

#### **Current Personal Records**

Event	NR	CR	WR	Single	Average
3x3x3 Cube	330	424	1485	8.16	10.13
2x2x2 Cube	195	265	901	1.55	3.49
4x4x4 Cube	1115	1644	7465	51.91	58.40
5x5x5 Cube	1654	2403	9997	2:28.52	2:43.81
C 3x3x3 Blindfolded	666	900	4609	5:47.28	

![](_page_46_Picture_6.jpeg)

ro-ph

# ...even if PBH are NOT the dark matter, they can PRODUCE the dark matter via Hawking evaporation!

Mass (g)	$T_H (\text{GeV})$	au (s)	$T_{\rm evap} = T(\tau) \; ({\rm GeV})$
$5M_P \simeq 10^{-4}$	$1.7 \times 10^{17}$	$10^{-41}$	$2 \times 10^{17}$
1	$1.7 \times 10^{13}$	$4 \times 10^{-29}$	$2 \times 10^{11}$
$10^{3}$	$1.7 \times 10^{10}$	$4 \times 10^{-20}$	$6 \times 10^6$
$10^{6}$	$1.7 \times 10^7$	$4 \times 10^{-11}$	200
$10^{9}$	$1.7  imes 10^4$	0.04	0.006
$10^{12}$	17	$4 \times 10^7 \sim 1 \text{ yr}$	$\sim 1 \ {\rm keV}$

#### \* Morrison, Profumo and Yu (JCAP, 2019)

![](_page_48_Figure_0.jpeg)

# Dark Matter can be a mix of Planck-scale relics from PBH evaporation, and stuff the PBH evaporated into!

![](_page_49_Figure_1.jpeg)

#### \* Morrison, Profumo and Yu (JCAP, 2019)

As BH approach the Planck scale, they can acquire a significant relic electric charge

(under simple assumptions)  $P(Q) \sim \exp(-4\pi\alpha(Q/e)^2)$ the relic charge is approximately Gaussian\*  $(8\pi\alpha)^{-1/2} \approx 2.34$ 

If evaporation stops around the Planck scale (because of extremality, or because of quantum gravity) we are left with a population of charged, Planck-scale relics!

\* Page, 1977

\*\* Lehmann, Johnson, Profumo and Schwemberger, 1906.06348

![](_page_51_Figure_0.jpeg)

\* Lehmann, Johnson, Profumo and Schwemberger, 1906.06348

![](_page_52_Figure_0.jpeg)

\* Gaspari, Lehmann, Profumo, in preparation

![](_page_53_Figure_0.jpeg)

 ✓ Microlensing a lot trickier than previously thought!
 ✓ Detection strategies? PTA?

![](_page_54_Figure_0.jpeg)

✓ Decays can produce DM,
 BAU, Planck relics

![](_page_55_Figure_0.jpeg)

# ✓ Likely (partly) charged✓ Detectable!

In the era of gravitational wave astronomy, the physics of macroscopic DM candidates offers many opportunities for the ingenuity of theorists and the craft of observers

![](_page_56_Figure_1.jpeg)

![](_page_58_Figure_0.jpeg)