

# An overview of evidence for a quantum critical point underlying the high-temperature superconducting dome

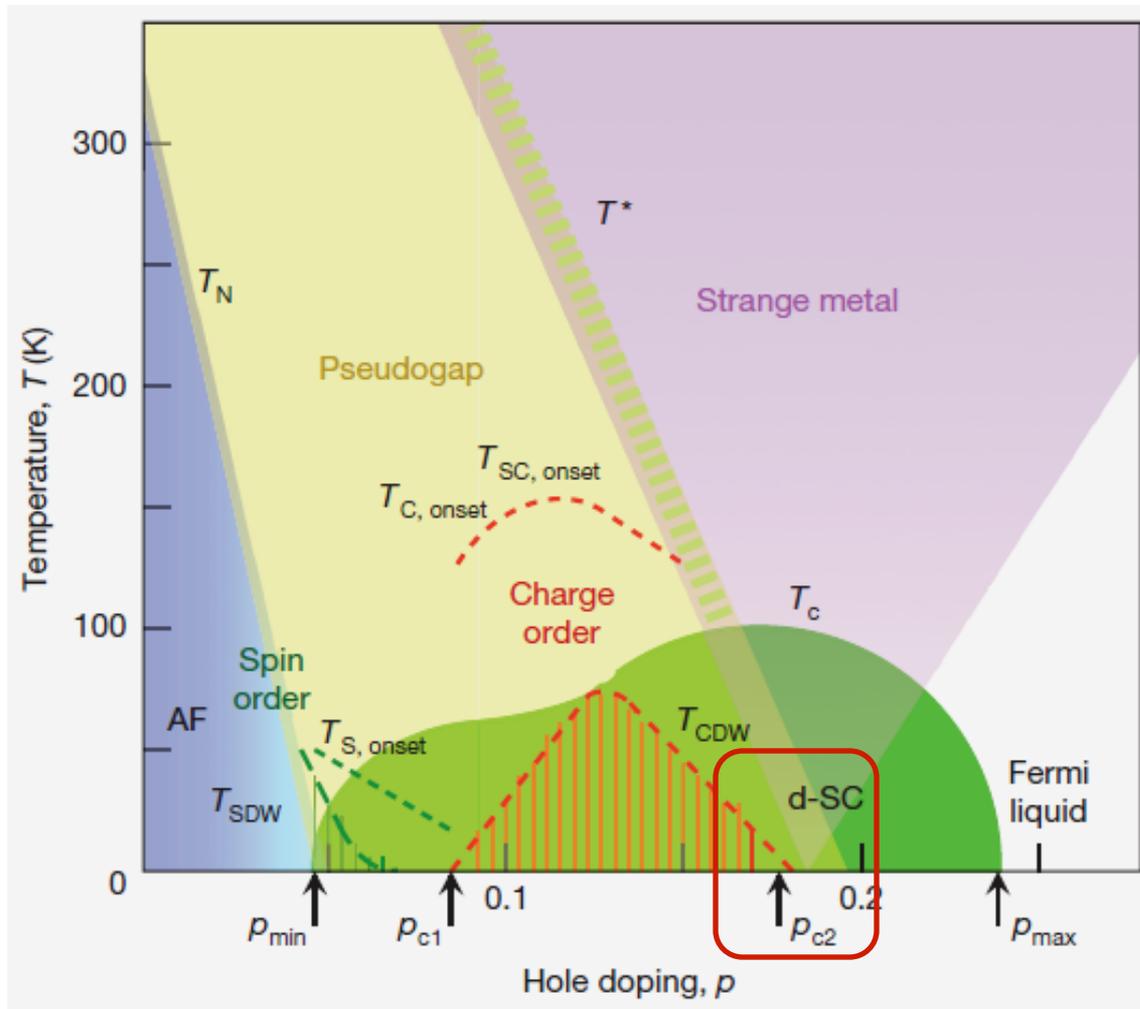
## Important new Probes for high magnetic field research

- A. Using **Focused Ion Beam Sample-Shaping** ...pioneered by Philip Moll... to acquire High-Precision Magnetotransport in a Cuprate Superconductor
- B. Using **Specific Heat** to measure Total Electronic Density of States that participates in superconductivity in a Pnictide Superconductor

## Phenomena near optimum doping....

1. Evidence for **Peak in the “Hall Number”**: non-monotonic evolution of Hall effect
2. Evidence for **Linear-in-T resistivity in the low temperature limit**
3. Evidence for **Linear-in-H resistivity in the low-temperature limit**
4. Evidence for **Quasiparticle Mass Divergence** ...from YBCO quantum oscillations
5. Evidence for **Quasiparticle Mass Divergence**...from specific heat in a pnictide

# The Phase Diagram in 2015:



B. Keimer, S.A. Kivelson, M.R. Norman, S. Uchida, J. Zaanen  
Nature 518, 179 (2015).

*“From quantum matter to high-temperature superconductivity in copper oxides.”*

# Thank You

## Linear magnetoresistance in LSCO thin films grown by MBE



Paula Gallo, J.A. Galvis, Z. Stegen, K.A. Modic, F.F. Balakirev, J.B. Betts, X. Lian, C. Moir, S.C. Riggs, B.J. Ramshaw, R.D. McDonald, GSB, A. Shekhter

J. Wu, A.T. Bollinger, X. He, I. Božović



## Linear magnetoresistance in LSCO single crystals



Xiujun Lian, R.D. McDonald, B.J. Ramshaw, F. Weickert, J.B. Betts, GSB, A. Shekhter

S. Ono



## Mass divergence approaching critical doping in BaFe<sub>2</sub>(As,P)<sub>2</sub>



Camilla Moir, J.A. Galvis, P. P. Giraldo-Gallo, X. Lian, A. Shekhter, GSB

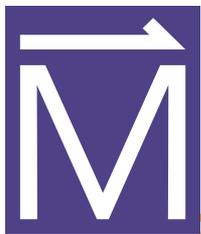
P. Walmsley, J-H Chu, I.R. Fisher



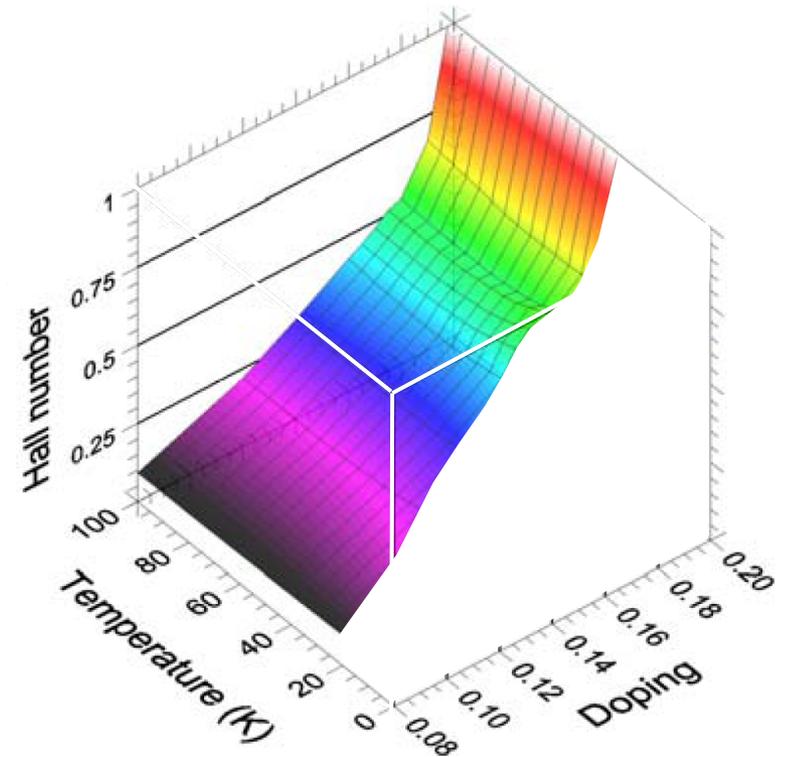
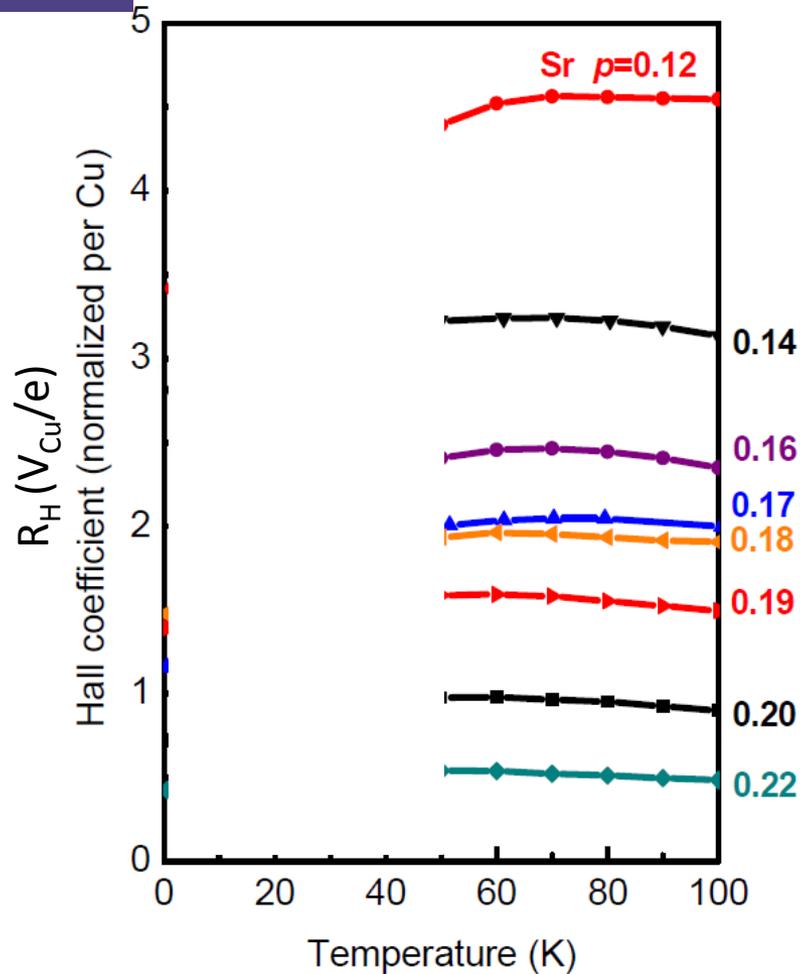
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**Direct Evidence of a Quantum Phase Transition near Optimum T<sub>c</sub>:  
Peak in “Hall Number” in LSCO and Bi2201  
Peak in “Hall Number” as a General Phenomenon?**

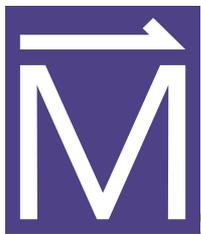


# The Hall Coefficient, $R_H$ , of the Normal State of LSCO in the Zero-Temperature Limit

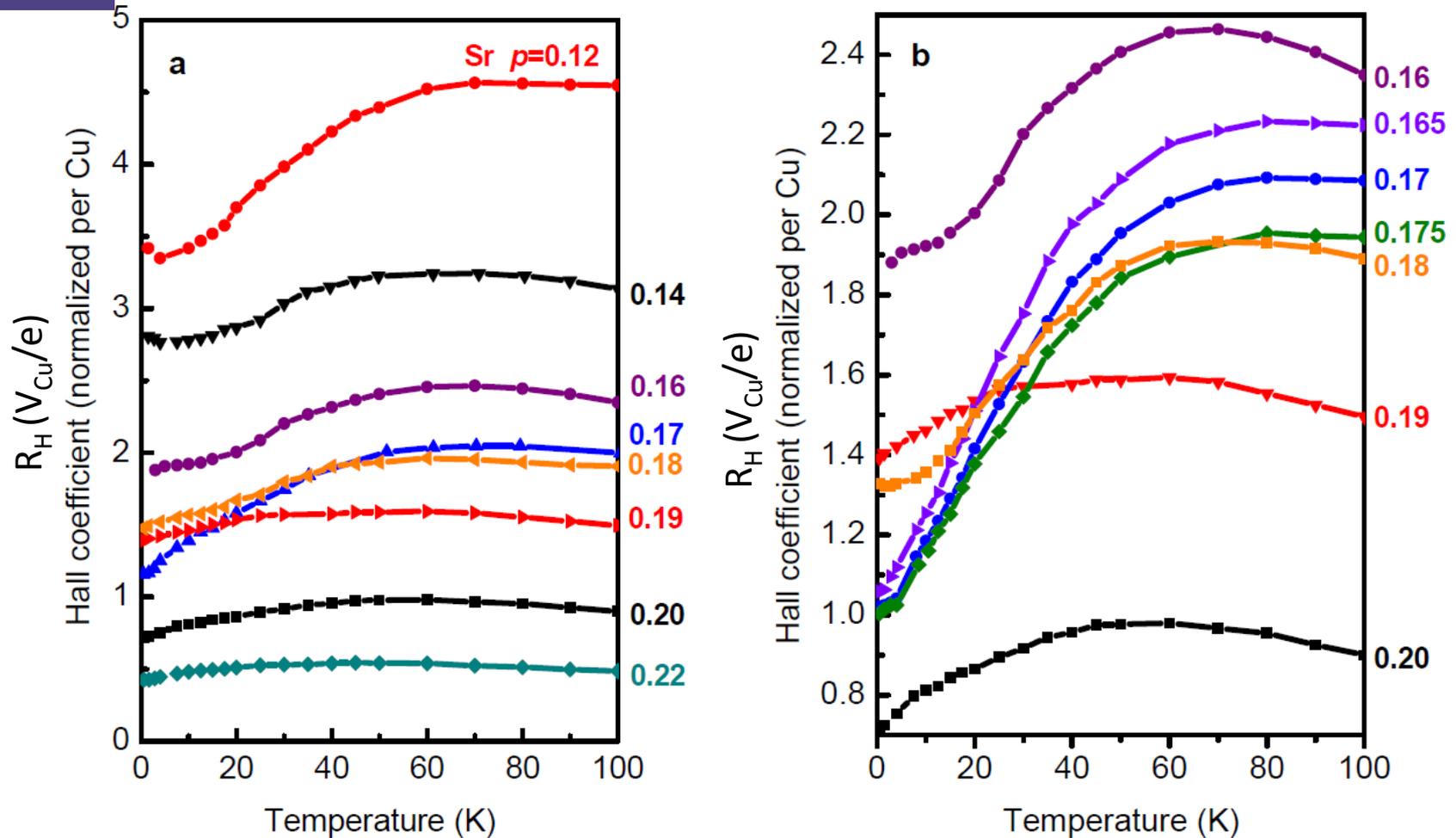


F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger,  
Phys.Rev.Lett. 102, 017004 (2009).

“Quantum Phase Transition in the Normal State of High- $T_c$  Cuprates at Optimum Doping.”

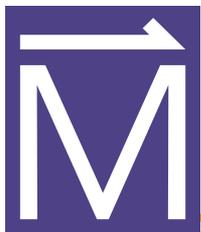


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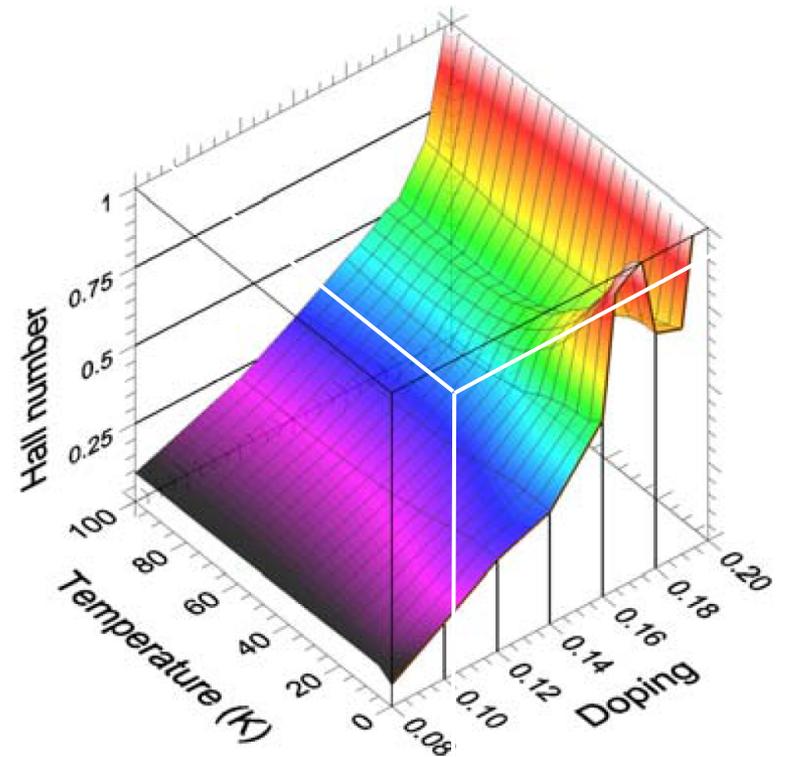
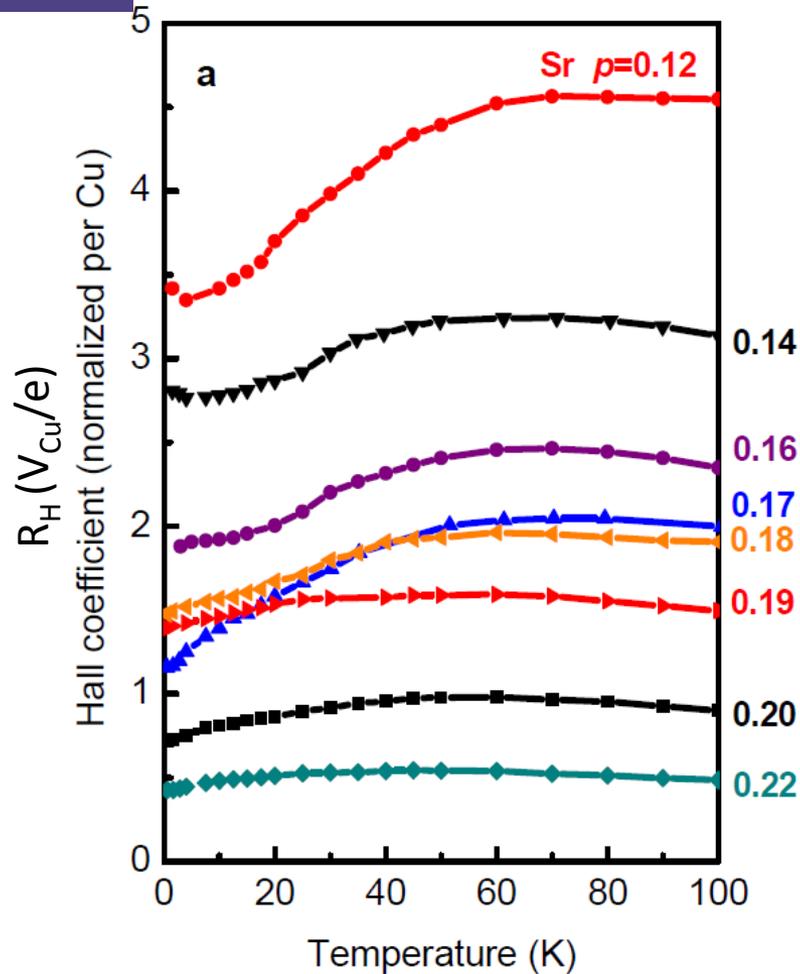


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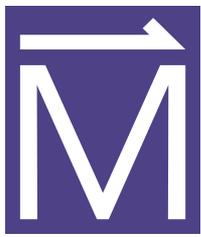


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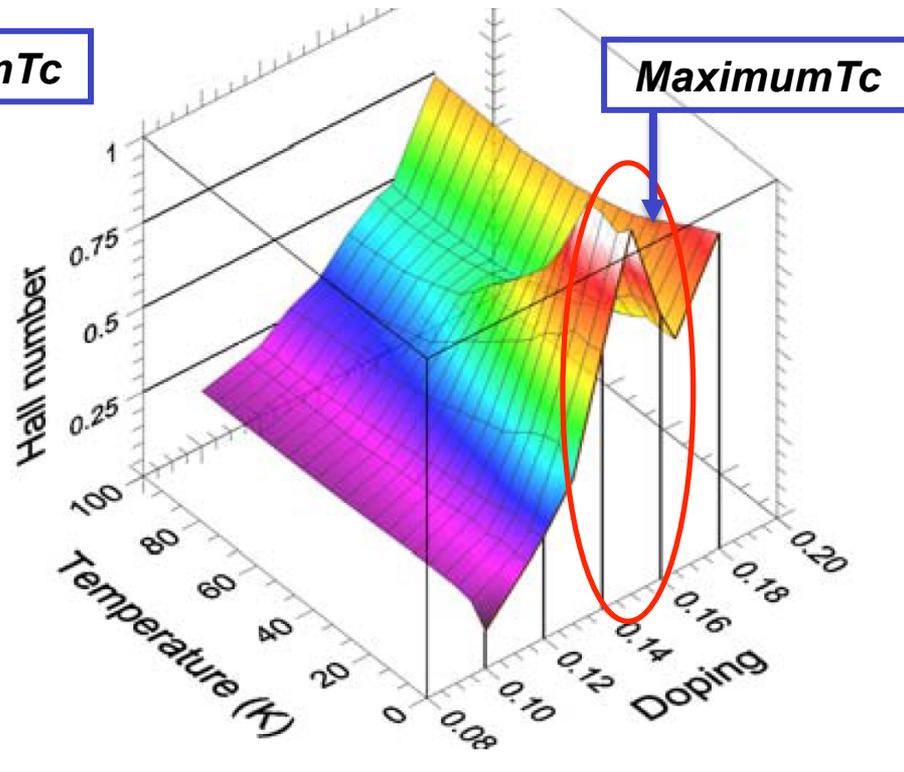
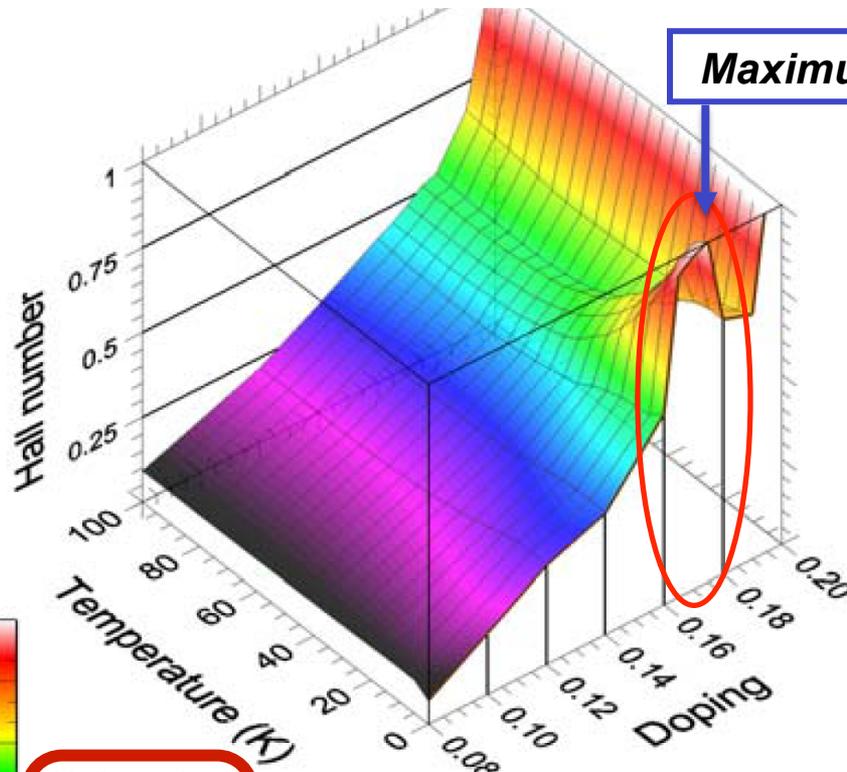
# Peak in Hall Number near Optimum $T_c$ seen in two systems

Reported in LSCO thin films in 2009...

F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger, *Phys.Rev.Lett.* 102, 017004 (2009).  
“Quantum Phase Transition in the Normal State of High- $T_c$  Cuprates at Optimum Doping.”

...but first observed in Bi-2201 single crystals in 2003

Fedor F. Balakirev, Jonathan B. Betts, Albert Migliori, S. Ono, Yoichi Ando & Gregory S. Boebinger, *Nature* 424, 912 (2003).  
“Signature of optimal doping in Hall-effect measurements on a high-temperature superconductor”



“Hall number”  
( $\equiv 1/R_{\text{hall}}$ )  
in units of  
carriers per  
Cu atom

*In electron-doped PrCeCuO4, evidence of phase transition (kink and change in sign of Hall coefficient)*

W. Yu, J.S. Higgins, P. Vach & R.L. Greene, *PRB* (RC) 020503 (2007).

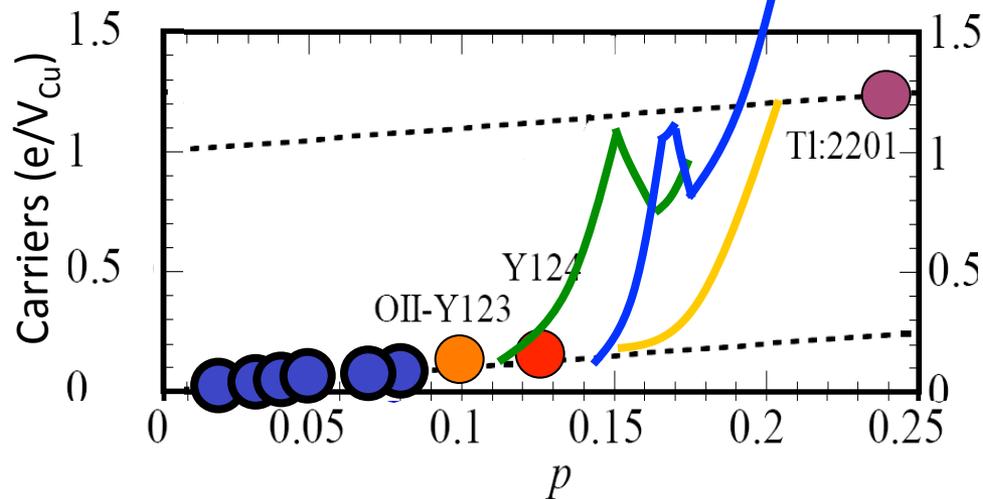
# Number of Carriers versus Doping: Peak or No Peak?

## Hall Effect in BSLCO to 60T

F. F. Balakirev, J. B. Betts, A. Migliori,  
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*Phys.Rev.Lett.* **102**, 017004 (2009)



## Quantum Oscillations in TI-2201

Hussey et al,  
*Nature* **425**,  
814 (2003)

## Hall Effect in LSCO

Y. Ando, *et al.*, PRL **92**  
197001 (2004)

## Quantum Oscillations in Ortho-II YBCO

N. Doiron-Leyraud, *et al.*, *Nature* **447** 565 (2007)

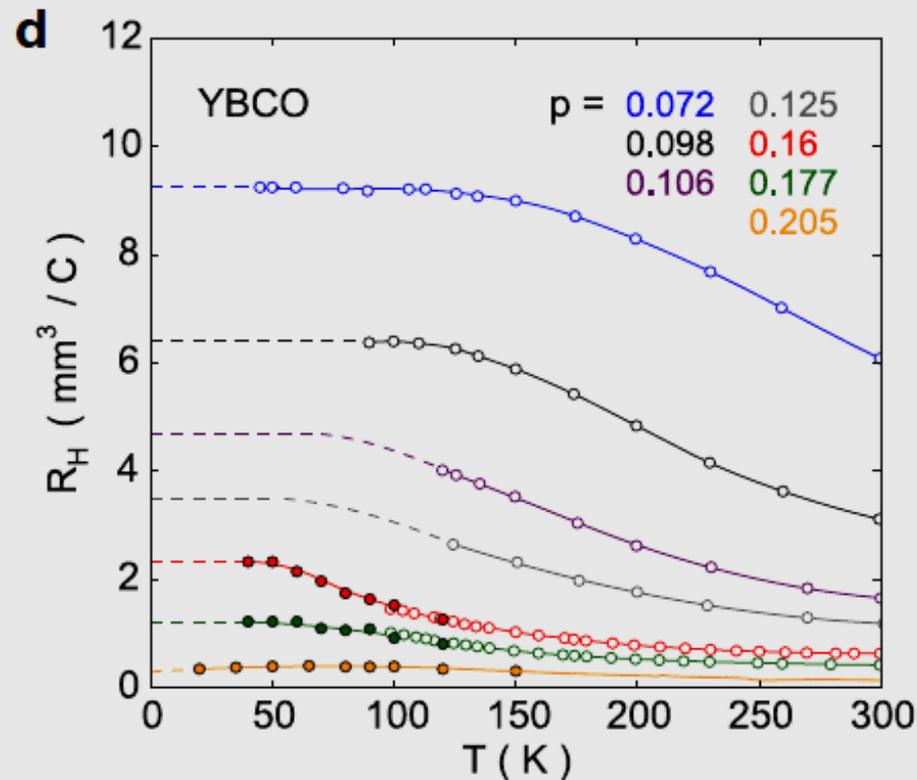
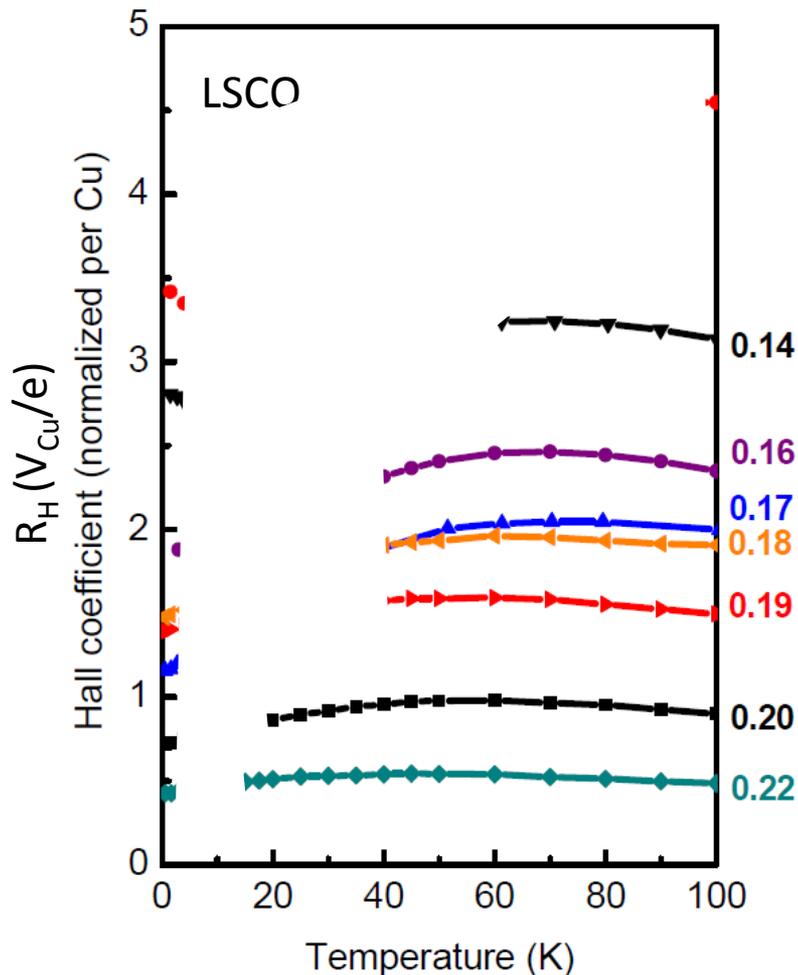
## Quantum Oscillations in YBCO124

Yelland *et al.*, PRL **100**, 047003 (2008)

## Hall Effect in YBCO to 88T

S. Badoux, W. Tabis, F. Laliberte, G. Grissonnanche,  
B. Vignolle, D. Vignolles, J Beard, D.A. Bonn, W.N.  
Hardy, R. Liang, N. Doiron-Leyraud, Louis Taillefer &  
Cyril Proust, *Nature* **531**, 210 (2016)

# Number of Carriers versus Doping: Peak or No Peak?



S. Badoux, W. Tabis, F. Laliberte, G. Grissonnanche, B. Vignolle, D. Vignolles, J Beard, D.A. Bonn, W.N. Hardy, R. Liang, N. Doiron-Leyraud, Louis Taillefer & Cyril Proust, *Nature* 531, 210 (2016)  
 “Change of carrier density at the pseudogap critical point of a cuprate superconductor.”

F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger, *Phys.Rev.Lett.* 102, 017004 (2009).  
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**CLEARLY: We Need Bigger Magnets!**

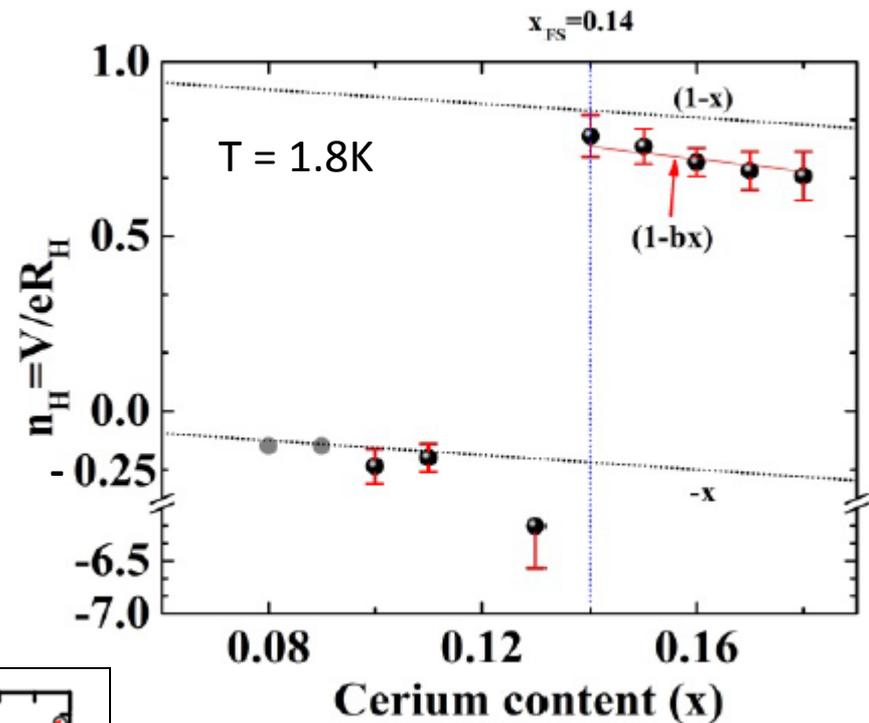
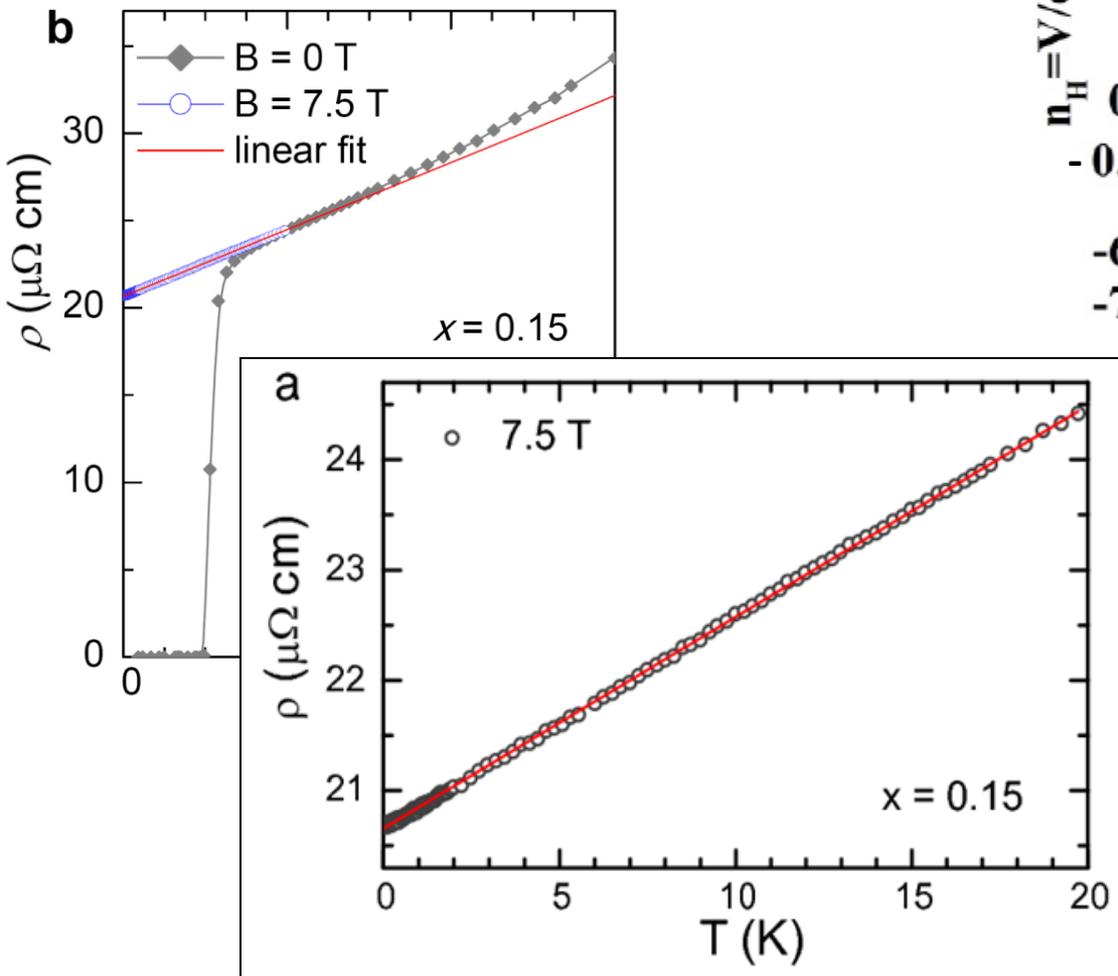
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## Linear-in-T Resistivity as $T \rightarrow 0$ in an Electron-Doped Cuprate

# Evidence for Quantum Criticality in (electron-doped) LCCO

*Linear-in-T Resistivity for  $20\text{mK} < T < 20\text{K}$*



*Low-temperature Hall effect  
changes sign at the quantum  
phase transition*

T. Sarkar, Greene, et al., (UMD)  
arXiv:1706.07836

## Phenomena near optimum doping....

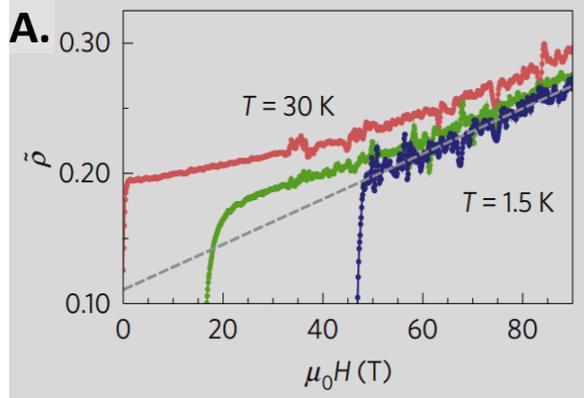
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**Linear Magnetoresistance: New Evidence for Quantum Criticality near Optimum Doping in a Cuprate Superconductor.**

# LINEAR MAGNETO-RESISTANCE: A NEW PHENOMENON, COMMON TO BOTH FAMILIES OF HIGH-TEMPERATURE SUPERCONDUCTORS NEAR CRITICAL

- A. Reported to 90T in an iron-pnictide superconductor last year (Analytis Group)
- B. Now reported to 80T in LSCO MBE-grown films (MagLab Group)

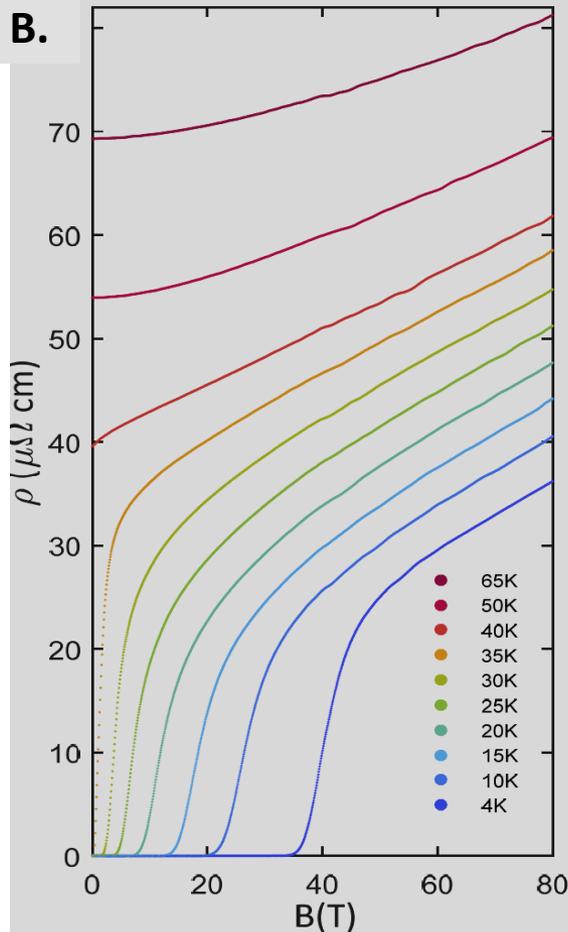
**BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> (x=0.31)**



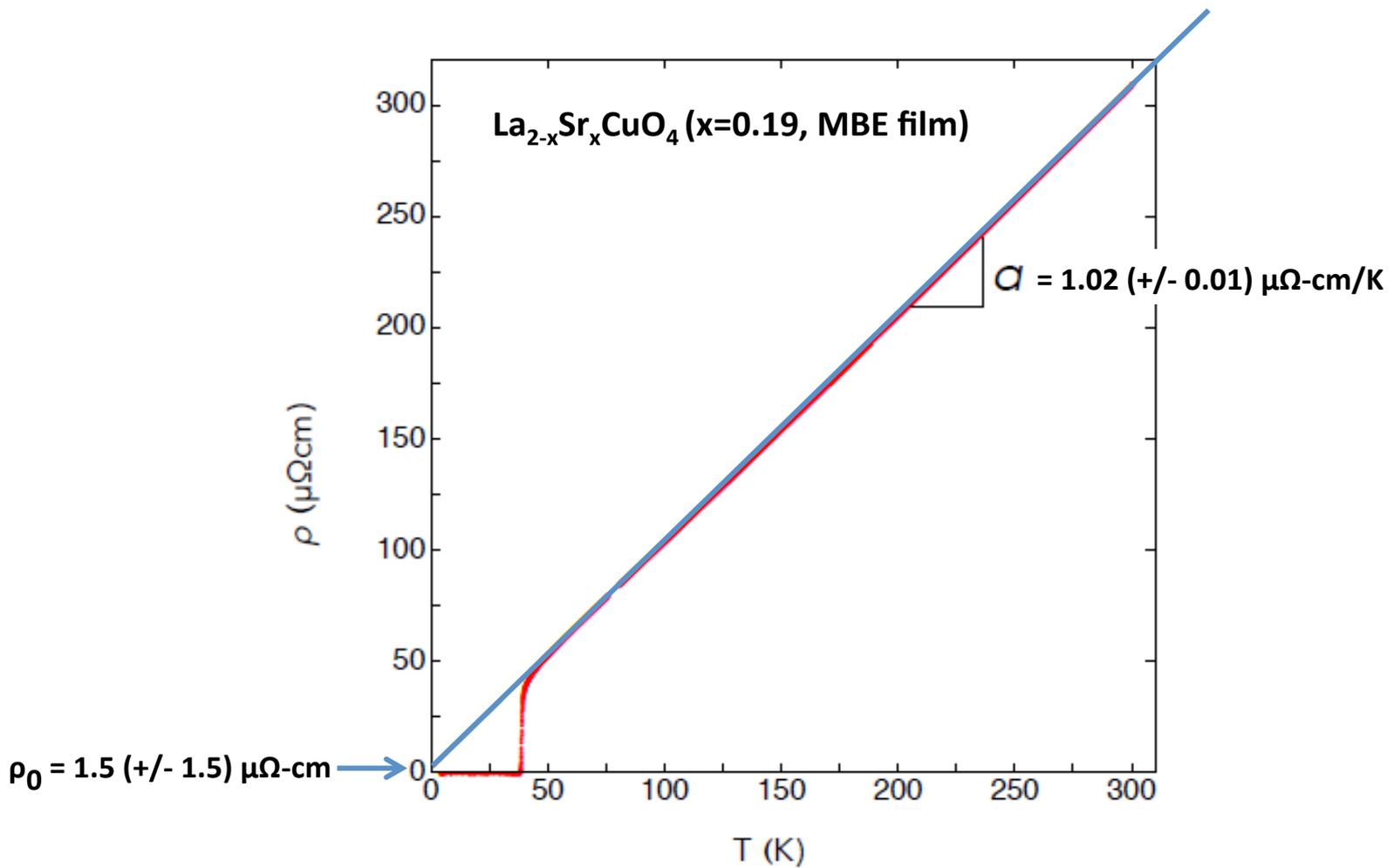
*Ian M. Hayes, et. al. (Analytis Group)*  
*Nature Physics* **12**, 916 (2016)

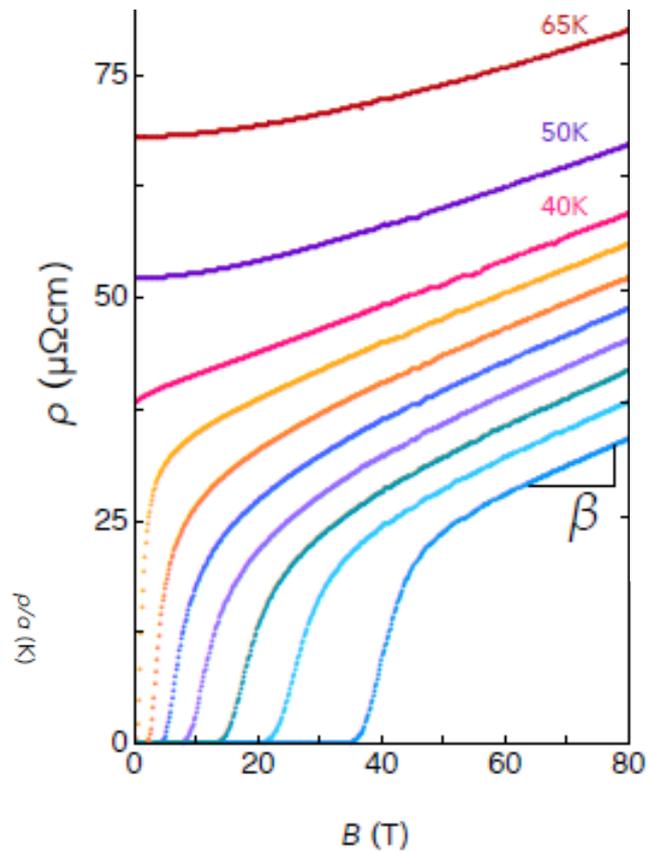
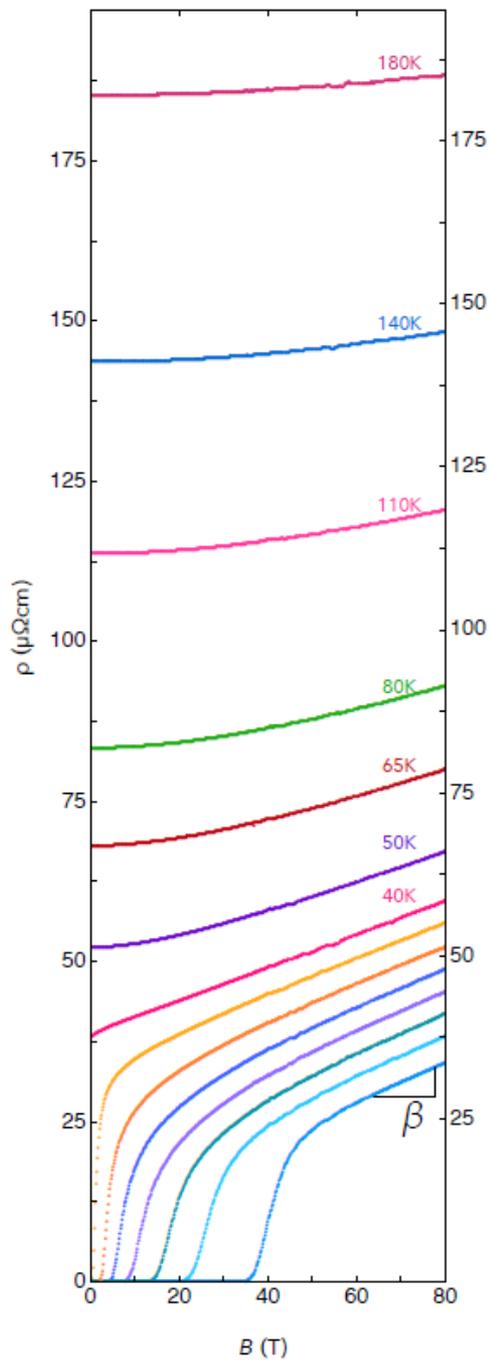
*P. Giraldo-Gallo, et.al.*  
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*arXiv:1705.05806*

**La<sub>2-x</sub>Sr<sub>x</sub>CuO<sub>4</sub> (x=0.19, MBE film)**

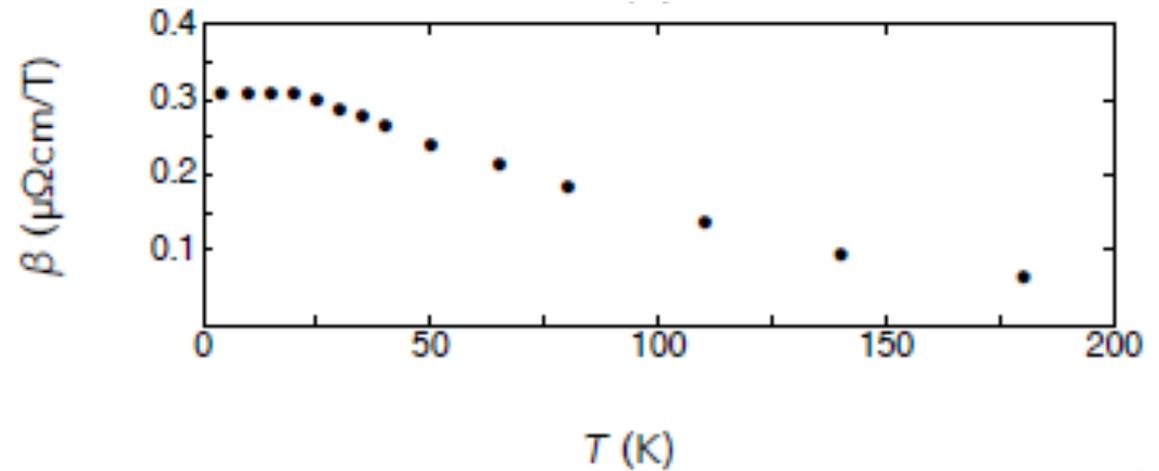


# High Quality Cuprate MBE-Grown Films....Who you gonna call? Ivan Bozovic



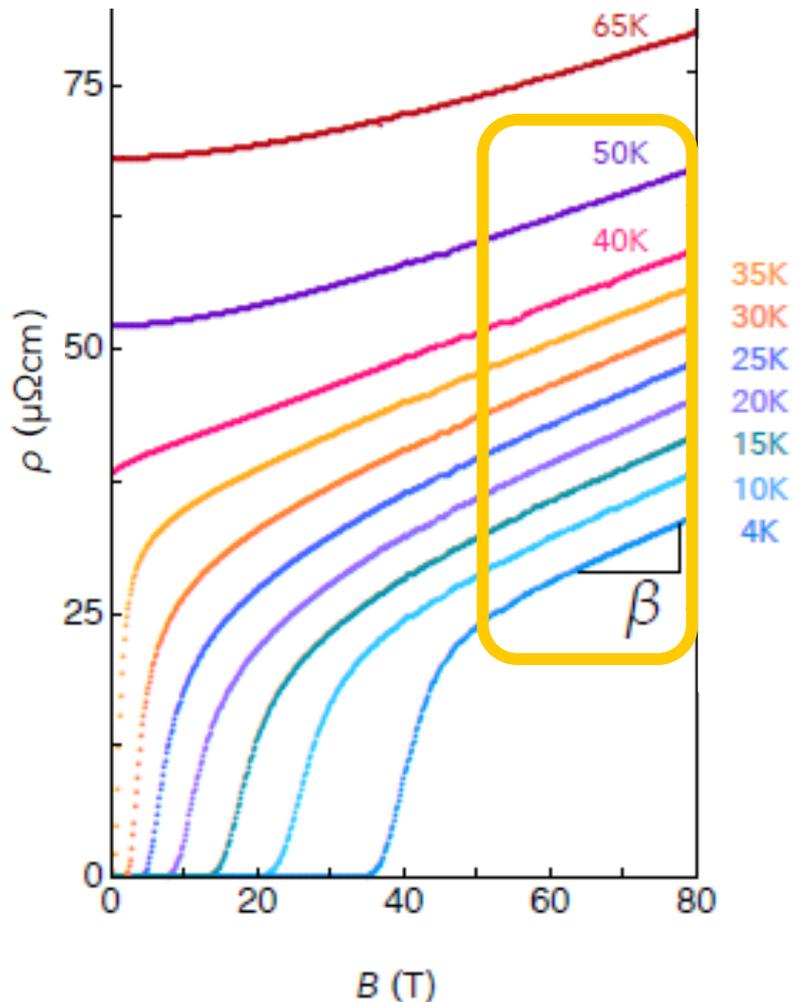


$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$   
 ( $x=0.19$ , MBE film)  
 shows a remarkably  
 linear magnetoresistance

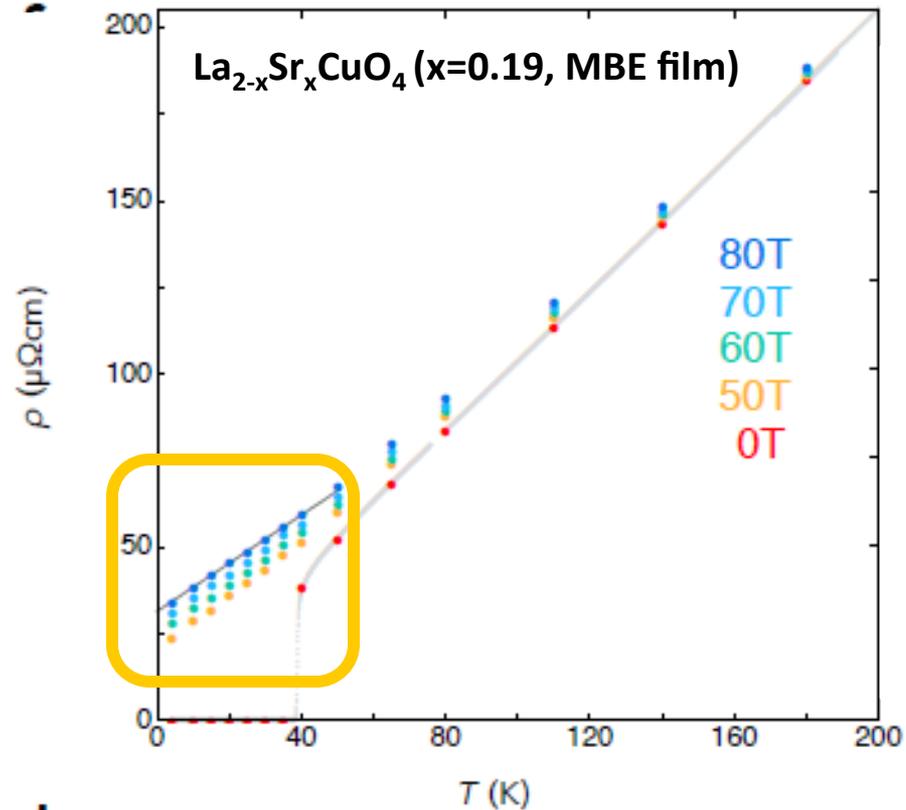


# Linear-in-T and Linear-in-B Regimes Coexist!

For  $T < 50\text{K}$  and  $B > 50\text{T}$ ,  $\rho(B)$  is linear in B



For  $T < 50\text{K}$  and  $B > 50\text{T}$ ,  $\rho(T)$  is linear in T

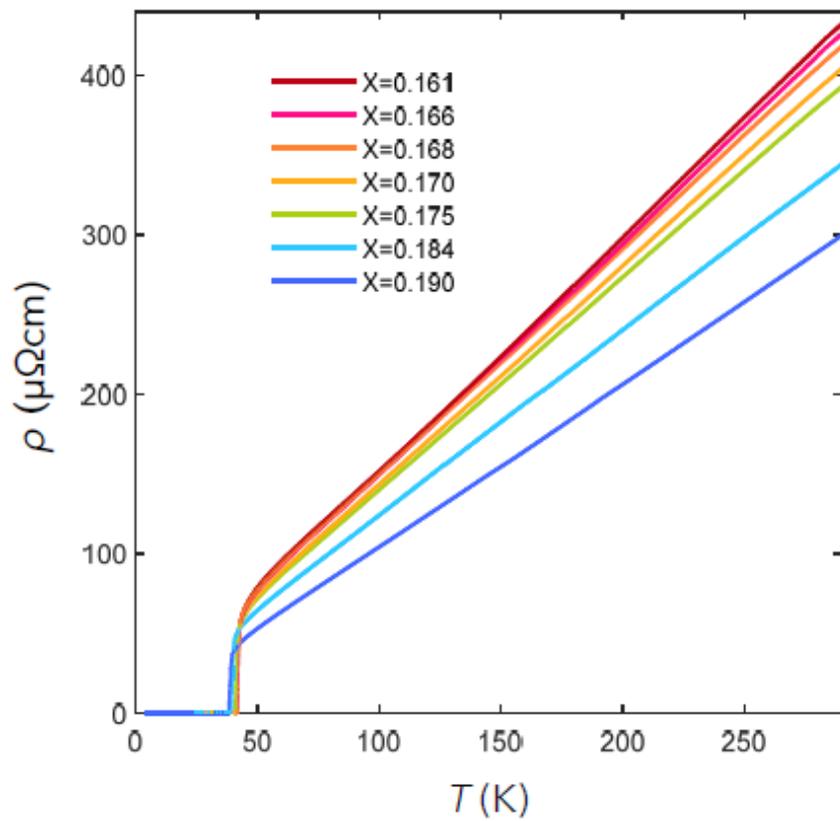


This is inconsistent with the 'quadrature'

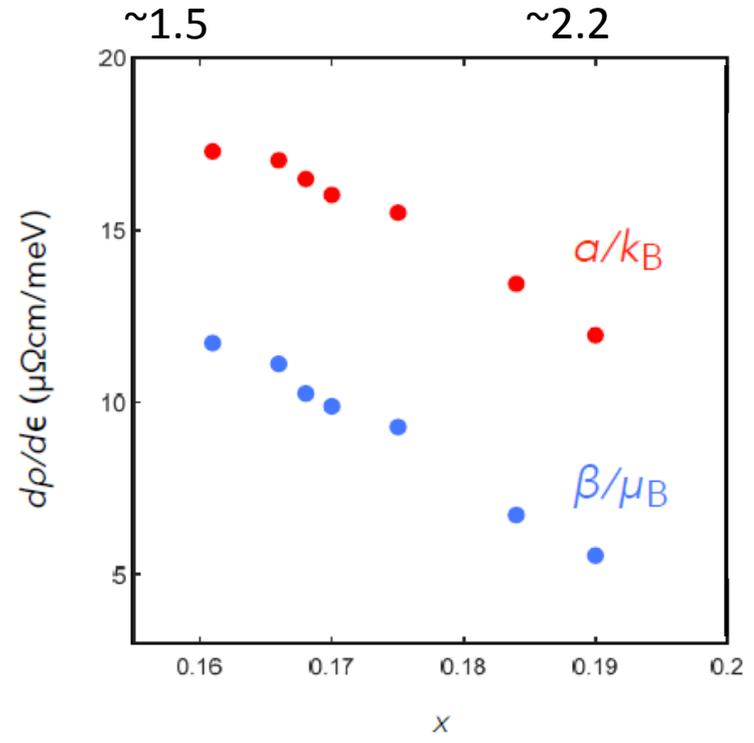
behavior seen in Ba-122:  $\rho(H, T) - \rho(0, 0) \propto \sqrt{(\alpha k_B T)^2 + (\gamma \mu_B \mu_0 H)^2}$

# Doping Dependence of Linear-in-T and Linear-in-B Slopes

$\alpha$  and  $\beta$  track each other with doping



Ratio is  $O(1)$ , but is not a constant:

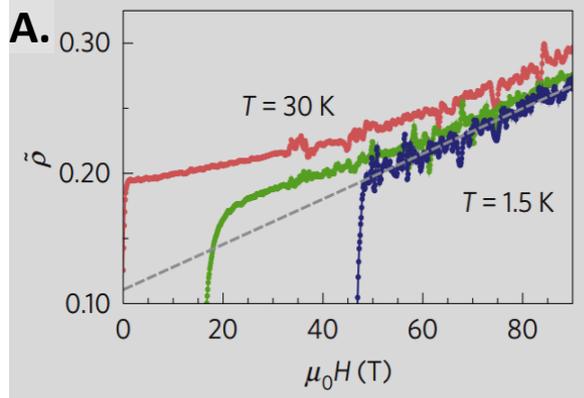


# LINEAR MAGNETO-RESISTANCE: A NEW PHENOMENON, COMMON TO BOTH FAMILIES OF HIGH-TEMPERATURE SUPERCONDUCTORS NEAR CRITICAL

REPORTING

- A. Reported to 90T in an iron-pnictide superconductor last year (Analytis Group)
- B. Now reported to 80T in LSCO MBE-grown films (MagLab Group)
- C. Now reported to 93T in an LSCO bulk sample shaped by Focused Ion Beam (MagLab Group)

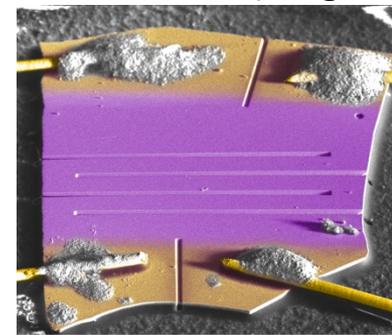
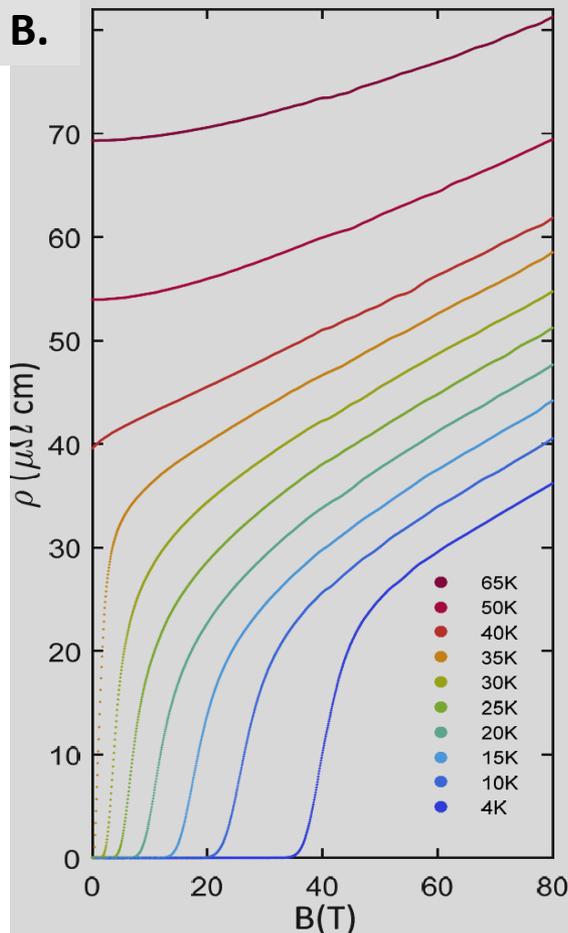
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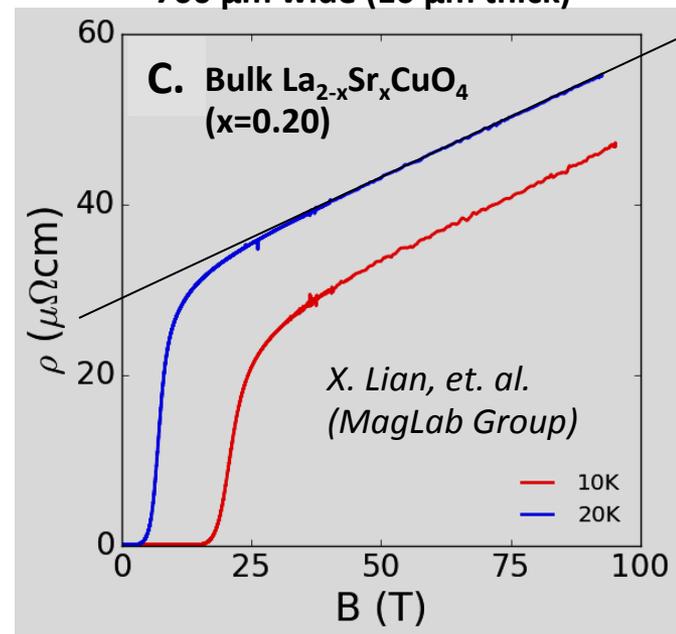
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arXiv:1705.05806

**La<sub>2-x</sub>Sr<sub>x</sub>CuO<sub>4</sub> (x=0.19, MBE film)**



700 μm wide (10 μm thick)



**C. Bulk La<sub>2-x</sub>Sr<sub>x</sub>CuO<sub>4</sub> (x=0.20)**

X. Lian, et. al.  
(MagLab Group)

— 10K  
— 20K

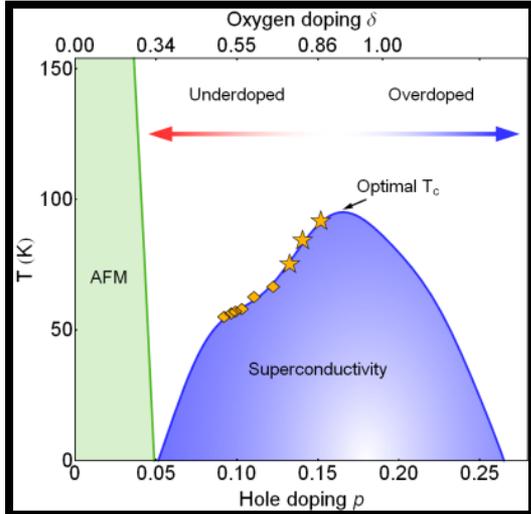
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**Evidence for Enhanced Electron Mass near Optimum Doping in YBCO.**

# A Quantum Critical Point at the Heart of High-Temperature Superconductivity in YBCO

B. Ramshaw, S.E. Sebastian, R.D. McDonald, James Day, B. Tan, Z. Zhu, J.B. Betts, Ruixing Liang, D.A. Bonn, W.N. Hardy, N. Harrison  
 Science (2015) DOI: 10.1126/science.aaa4990

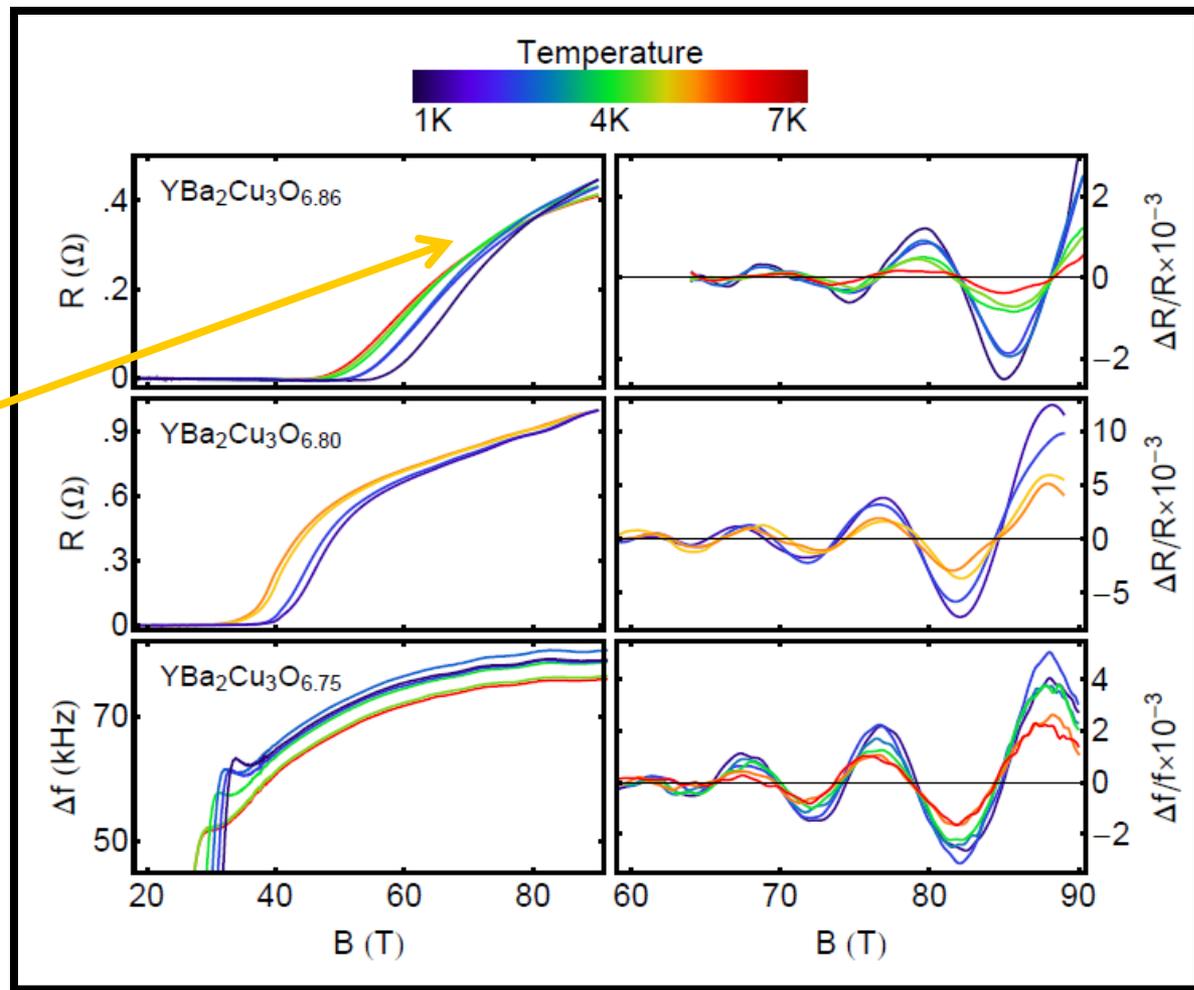


$T_c \sim 91\text{K}$

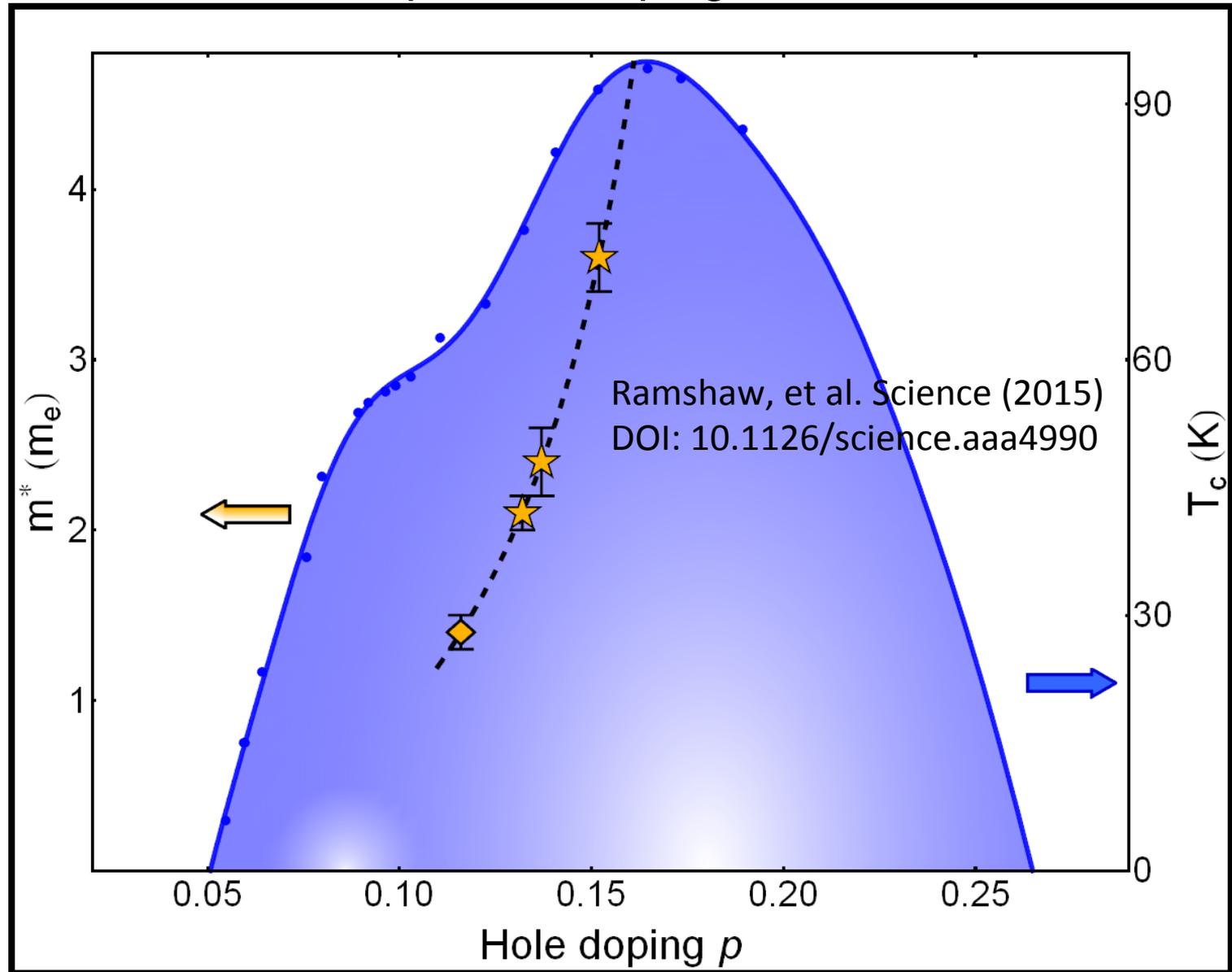
**CLEARLY:** We Need Bigger Magnets!

$T_c \sim 81\text{K}$

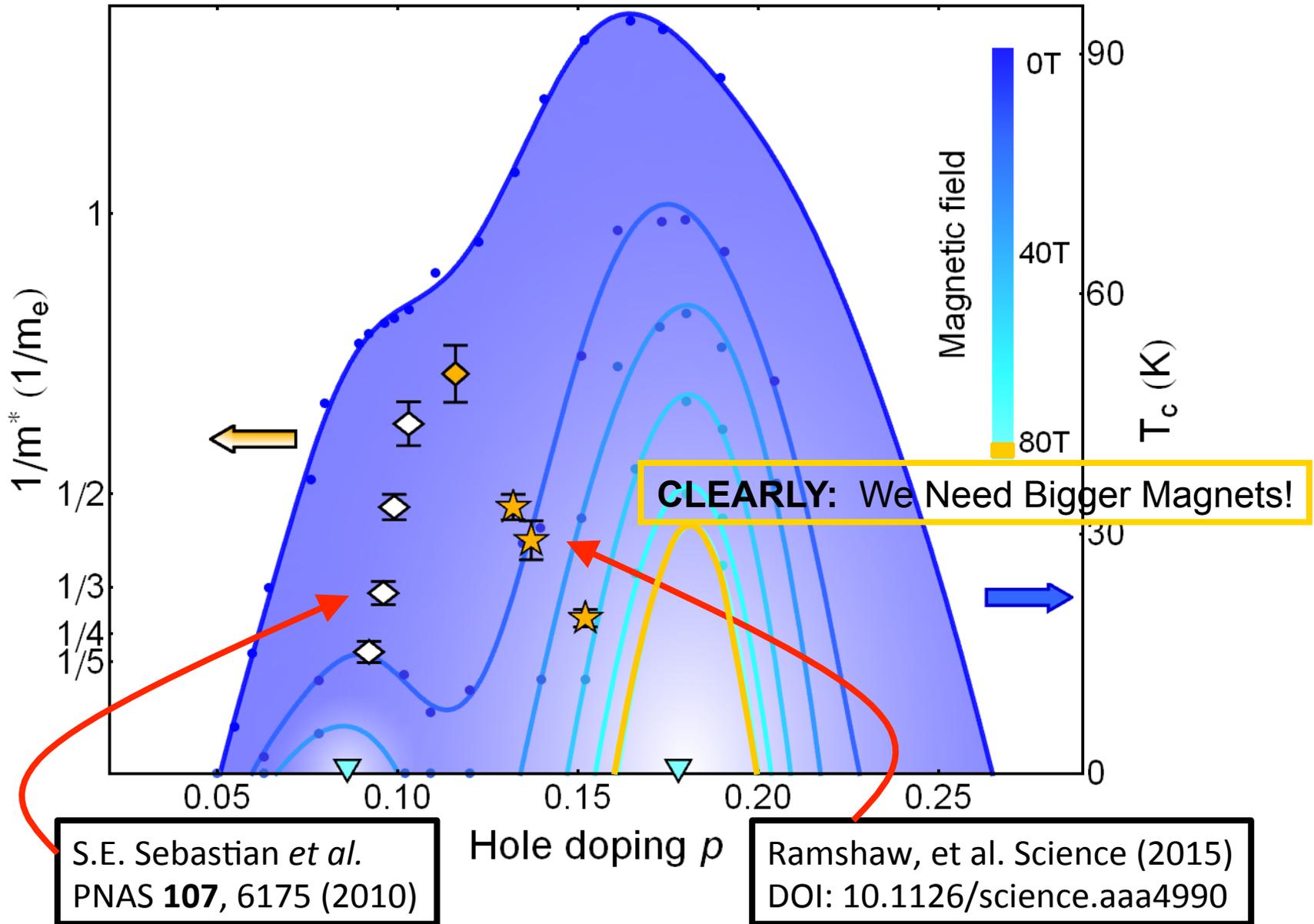
$T_c \sim 75\text{K}$



# Diverging Effective Mass: Evidence of a Quantum Critical Point at Optimum Doping in YBCO



# Diverging Effective Mass: Evidence of a Quantum Critical Point at Optimum Doping in YBCO



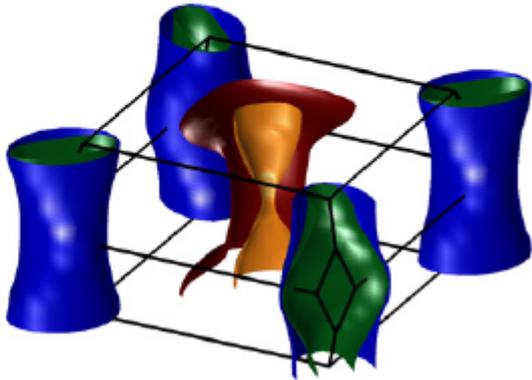
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**Specific Heat to measure Total Electronic Density of States  
that participates in superconductivity:**

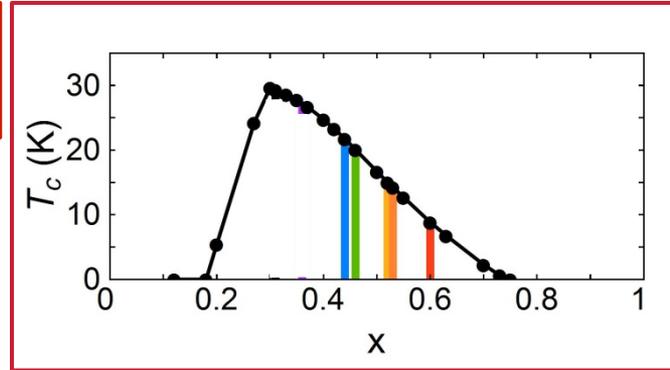
**Evidence for Enhanced Electron Mass near Optimum Doping in a Pnictide.**

# BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> Fermi Surface and Phase Diagram



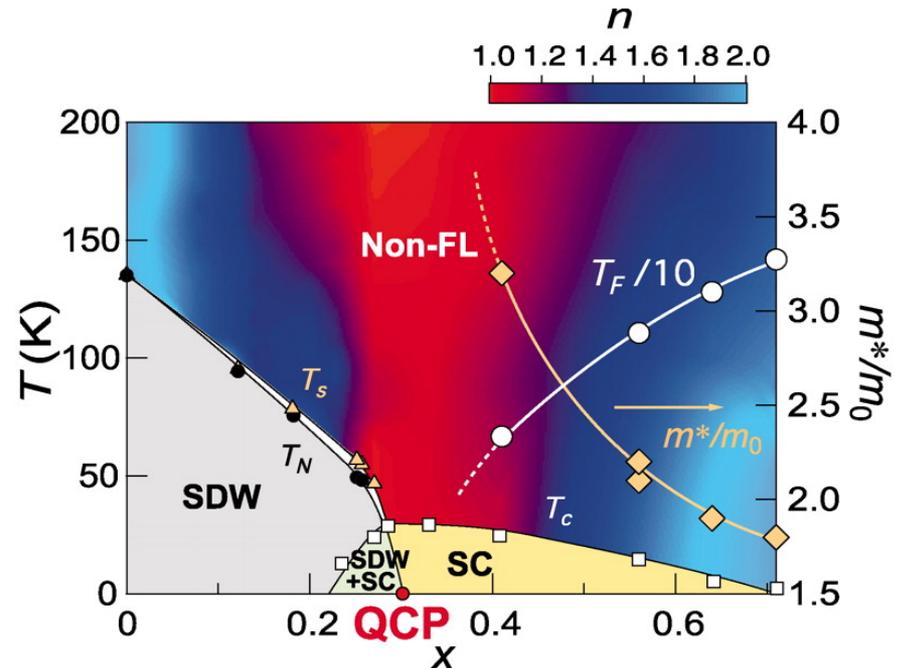
$m^*$  enhancement  
seen in  $\beta$  pocket  
(blue pocket)

We report on  
five dopings:



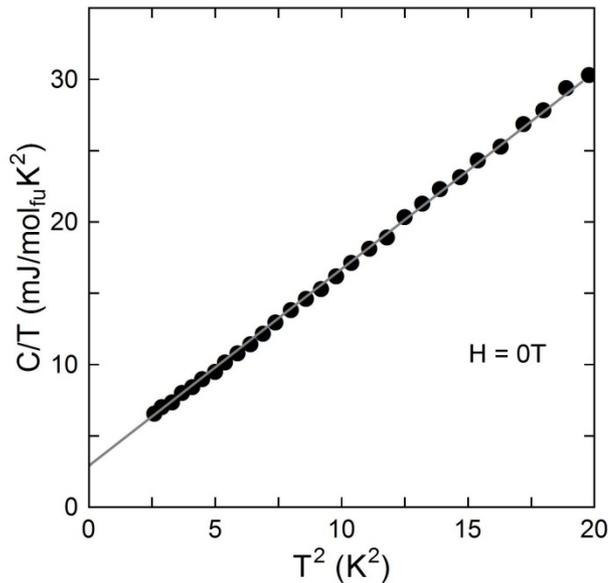
Carrington, A. *Rep. Prog. Phys.* **74**,  
124507 (2011)

K. Hashimoto et al. *Science* 2012;  
**336**:1554-1557

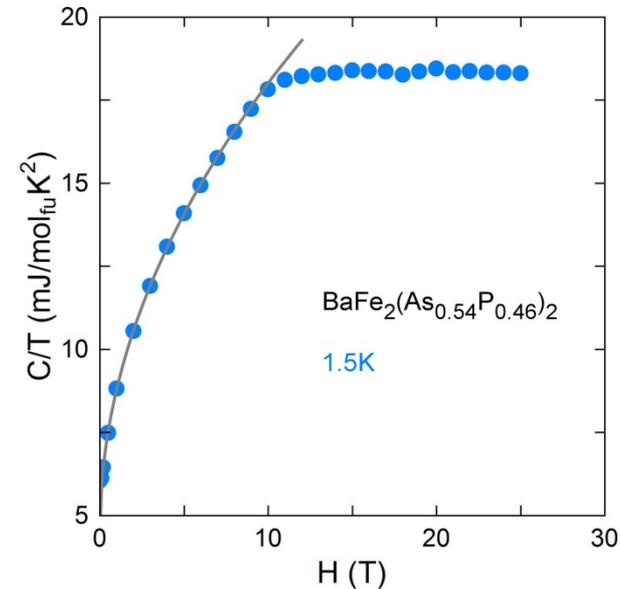


# Our Specific Heat Measurements

The change in the specific heat from zero field to the 'normal state' measures the total normal state electronic density of states of all Fermi surface pockets that take part in superconductivity.



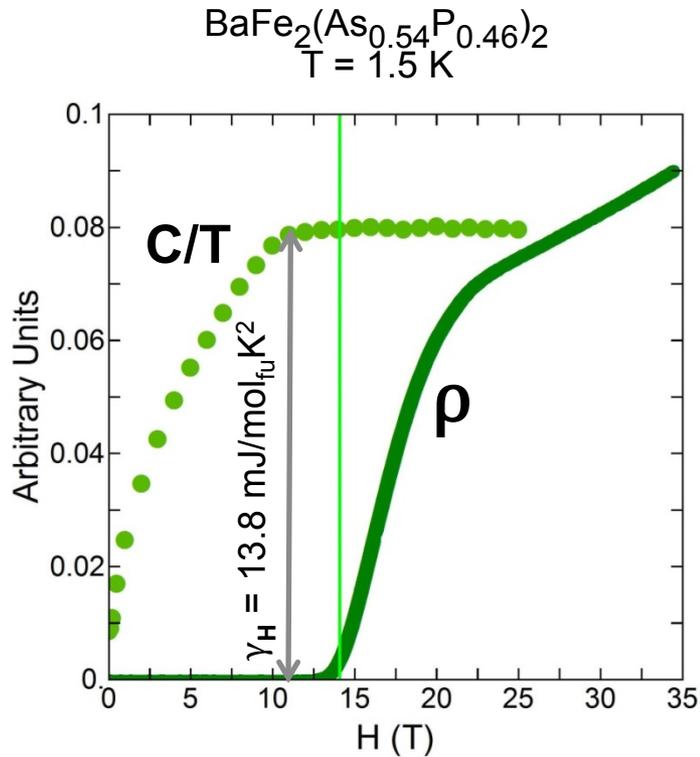
Temperature dependence shows standard linear dependence expected for  $C/T$  versus  $T^2$  ...for  $H=0$ ... and at all magnetic fields.



The  $\sqrt{H}$  dependence indicates nodes in the superconducting gap. The saturation indicates reaching the normal state.

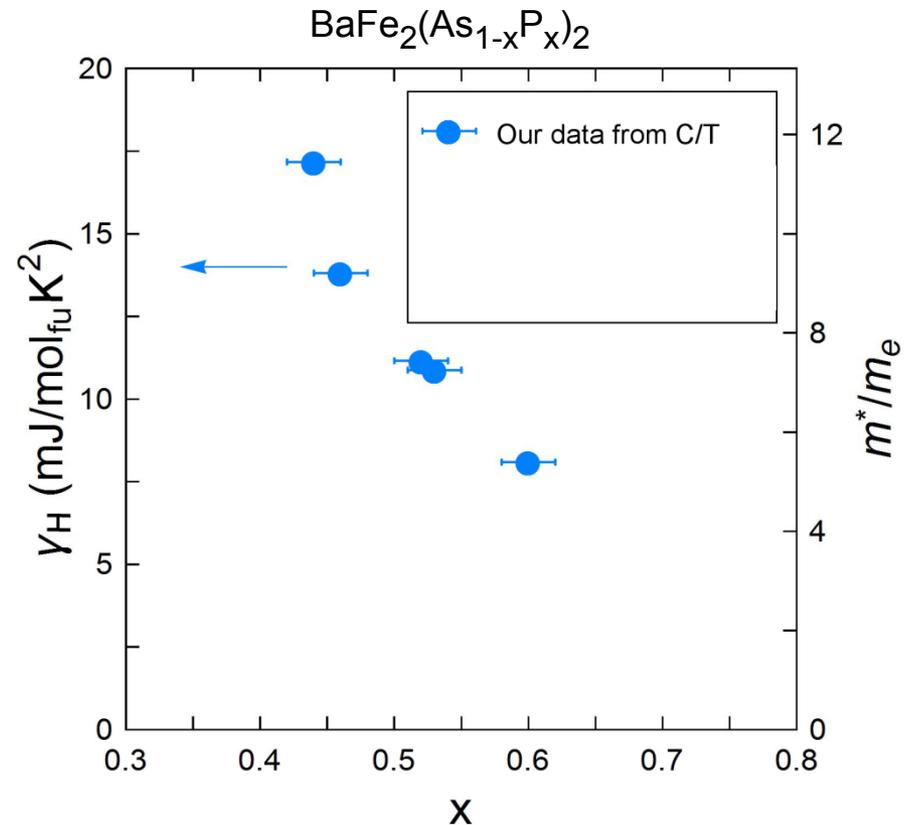


# Phenomenology of the Electronic Specific Heat recovered by Suppressing Superconductivity

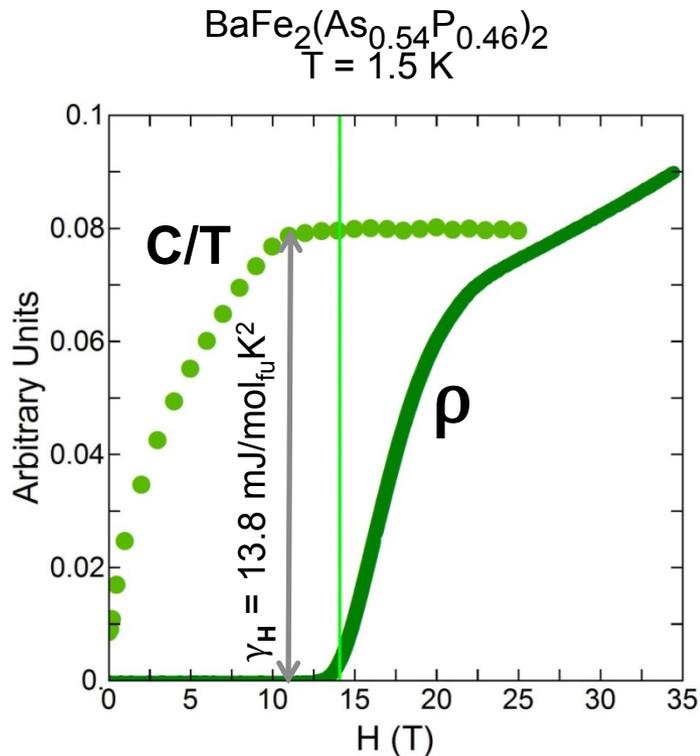


**Saturation of specific heat occurs at the onset of finite resistance**...implies that the bulk of the sample is non-superconducting at the onset of resistance.

Electronic density of states shows enhancement as  $x$  approaches optimum doping,  $x = 0.3$ .

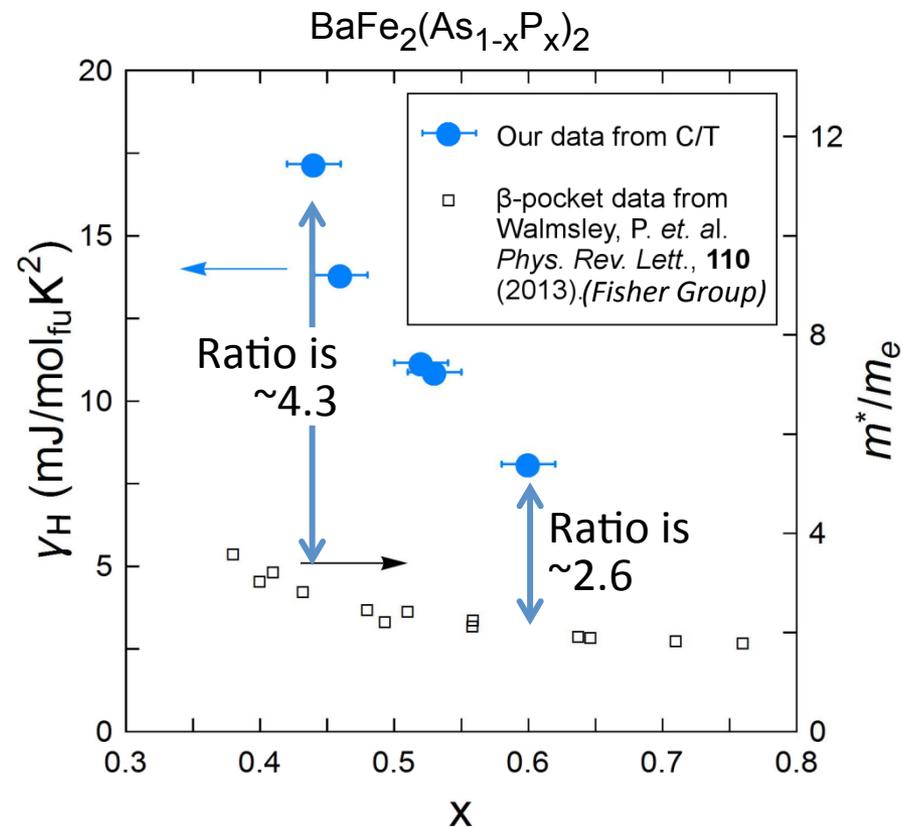


# Specific Heat finds a greater enhancement than seen in the $\beta$ pocket

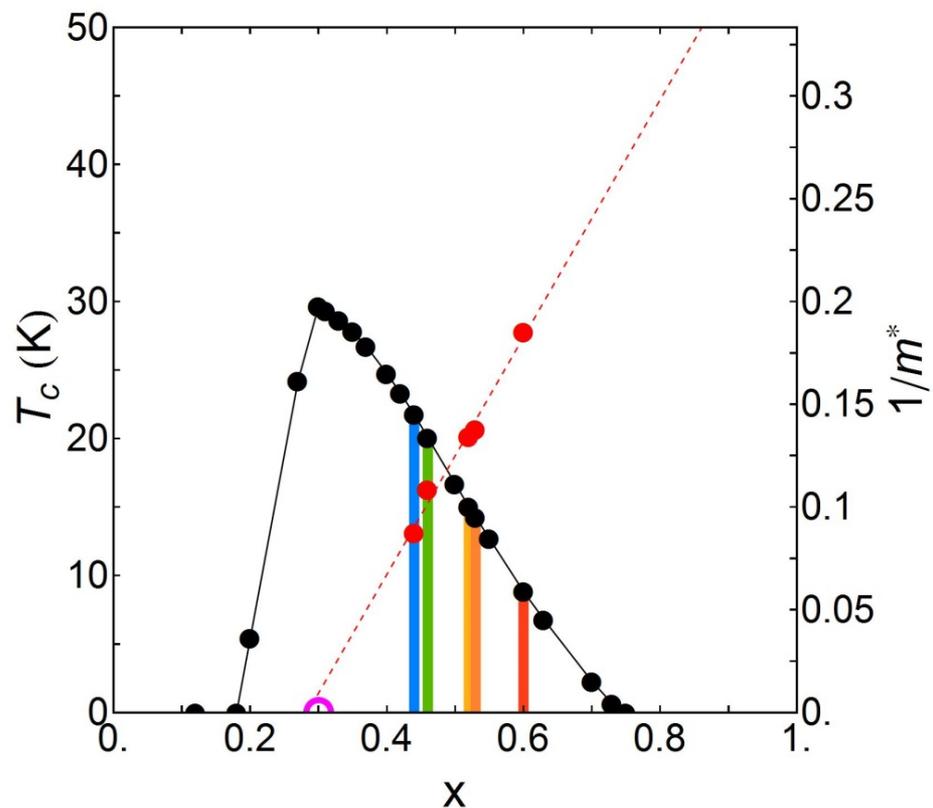
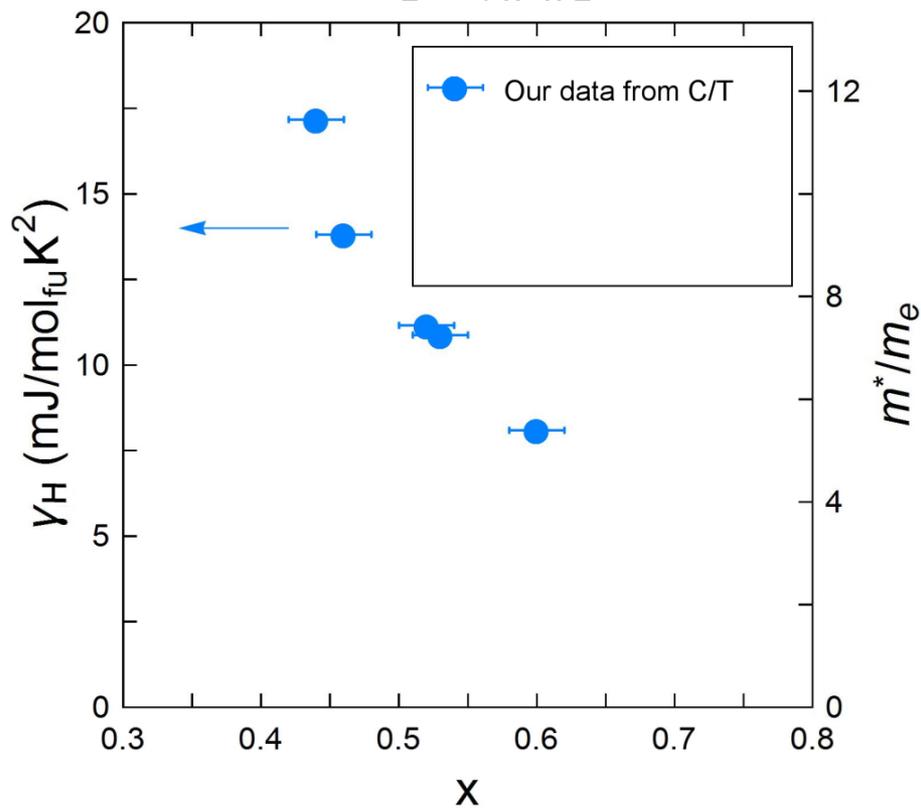
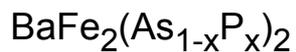


**Saturation of specific heat occurs at the onset of finite resistance**...implies that the bulk of the sample is non-superconducting at the onset of resistance.

Ratio of the two curves increases as doping approaches  $x=0.3$  optimum doping



# Mass Enhancement Appears to Diverge at Optimum Doping



# An overview of evidence for a quantum critical point underlying the high-temperature superconducting dome

## Phenomena near optimum doping....

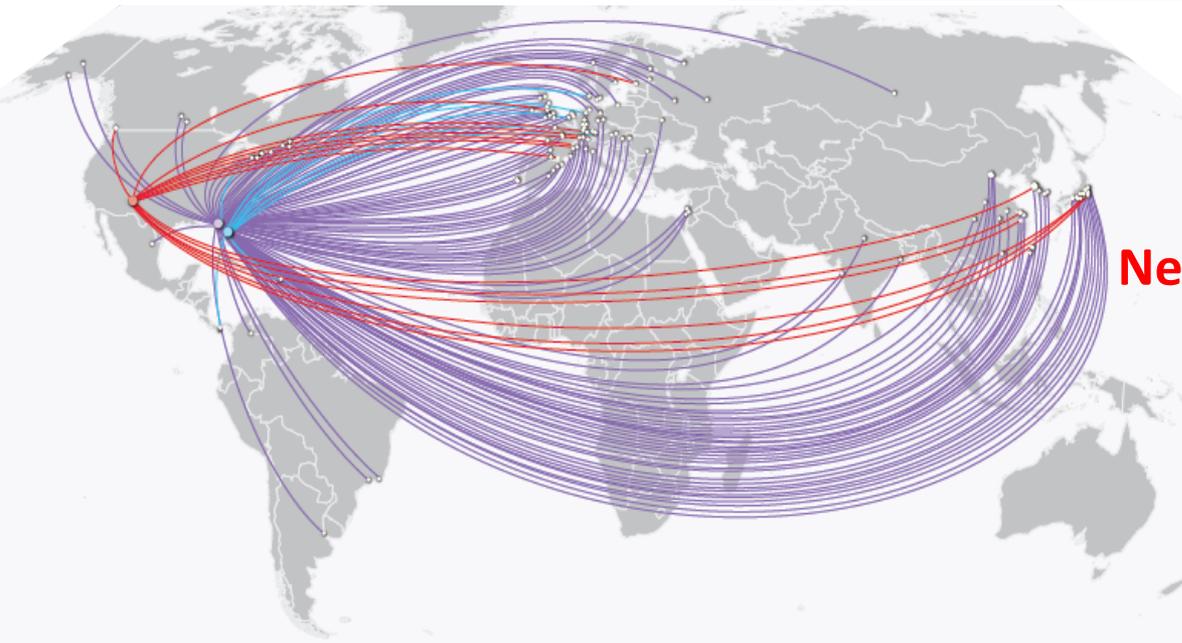
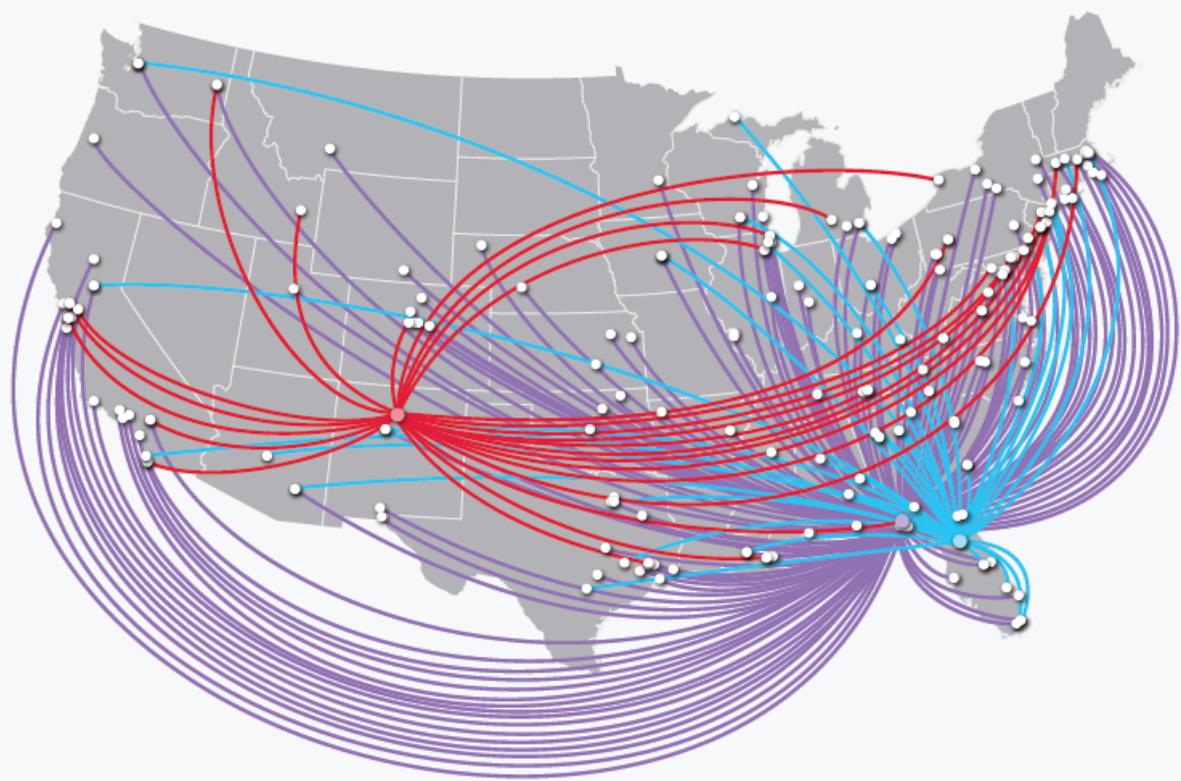
1. **Peak in the “Hall Number”**: non-monotonic evolution of Hall effect evidences a quantum phase transition.

## Phenomena evidencing a quantum critical point near optimum doping...

1. Linear-in-T resistivity in the low temperature limit in electron-doped cuprates, and hole-doped cuprates.
2. Linear-in-H resistivity in the low-temperature limit in both LSCO and Ba122
3. Quasiparticle Mass Divergence from YBCO quantum oscillations
4. Quasiparticle Mass Divergence from Ba122 quantum oscillations
5. Quasiparticle Mass Divergence from Ba122 specific heat

# The MagLab IS Its User Program

In 2016, the MagLab  
hosted experiments  
by **1,778 users**  
from **174 institutions**  
across the **United States...**



...and a total of **321 institutions**  
throughout the world.

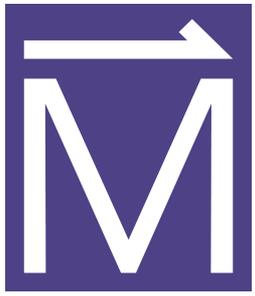
**Newcomers are welcome: in 2016**  
**24% of Principal Investigators**  
**were first-time MagLab PI's**



Thank You

**CLEARLY: We Need Bigger Magnets!**





# Scaling in Ba122 Background Slides

# Scaling between magnetic field and temperature in the high-temperature superconductor

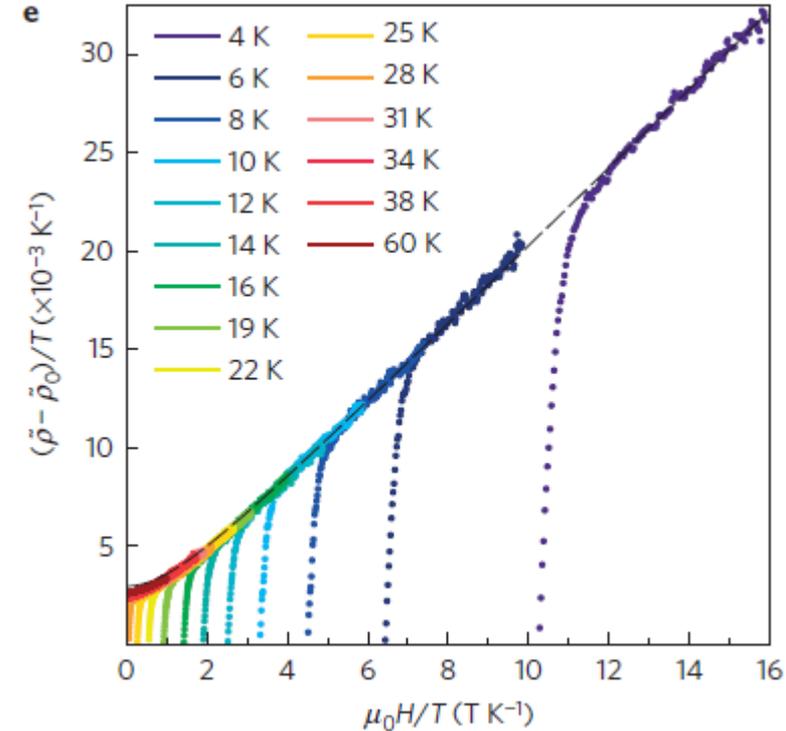
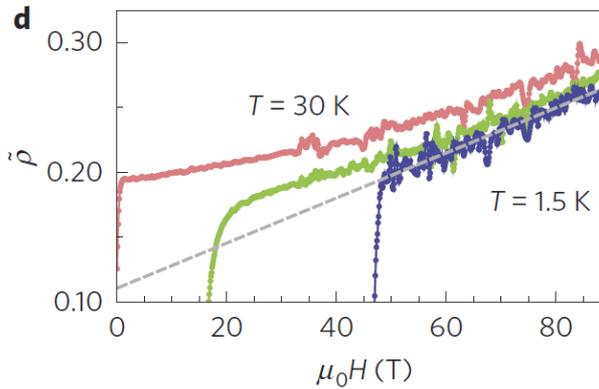
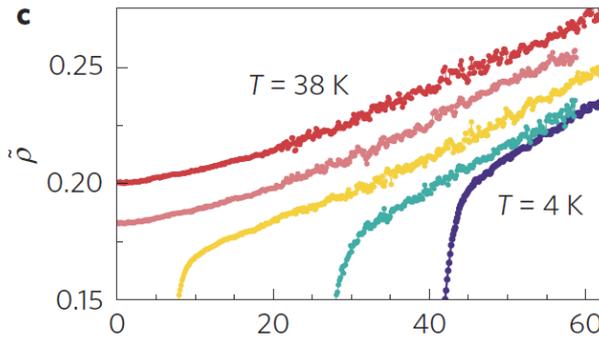
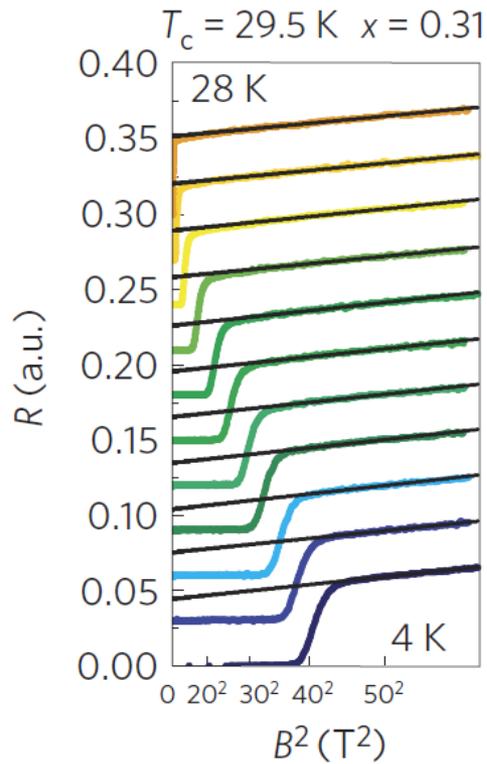
## BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

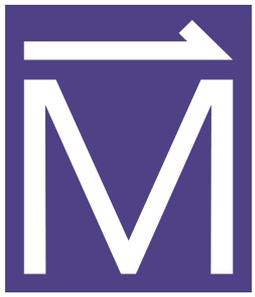
Ian M. Hayes<sup>1,2</sup>, Ross D. McDonald<sup>3</sup>, Nicholas P. Breznay<sup>1,2</sup>, Toni Helm<sup>1,2</sup>, Philip J. W. Moll<sup>1</sup>, Mark Wartenbe<sup>4</sup>, Arkady Shekhter<sup>4</sup> and James G. Analytis<sup>1,2\*</sup>

16 MAY 2016 | DOI: 10.1038/NPHYS3773

$$\rho(H, T) - \rho(0, 0) \propto \sqrt{(\alpha k_B T)^2 + (\gamma \mu_B \mu_0 H)^2} \equiv \Gamma$$

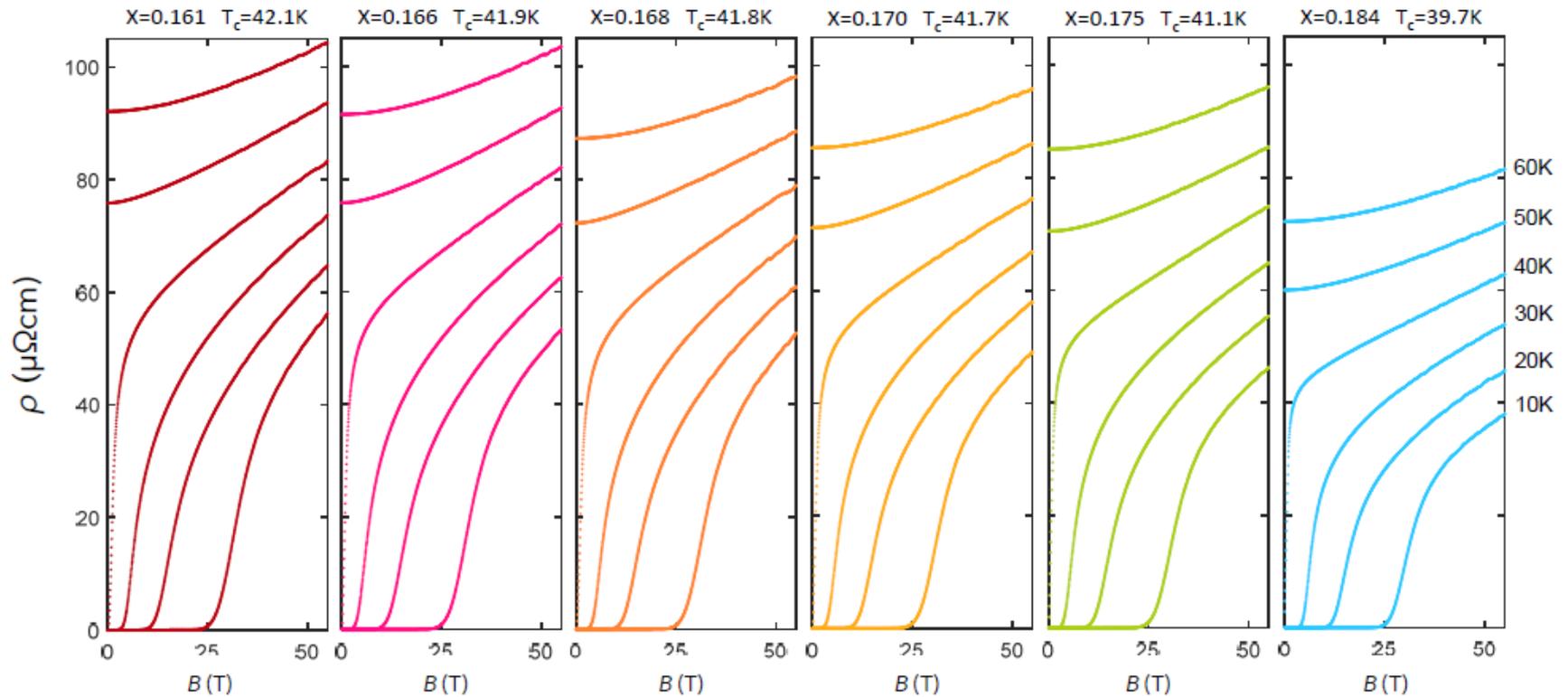
$$\tilde{\rho} = \rho / \rho(300)$$

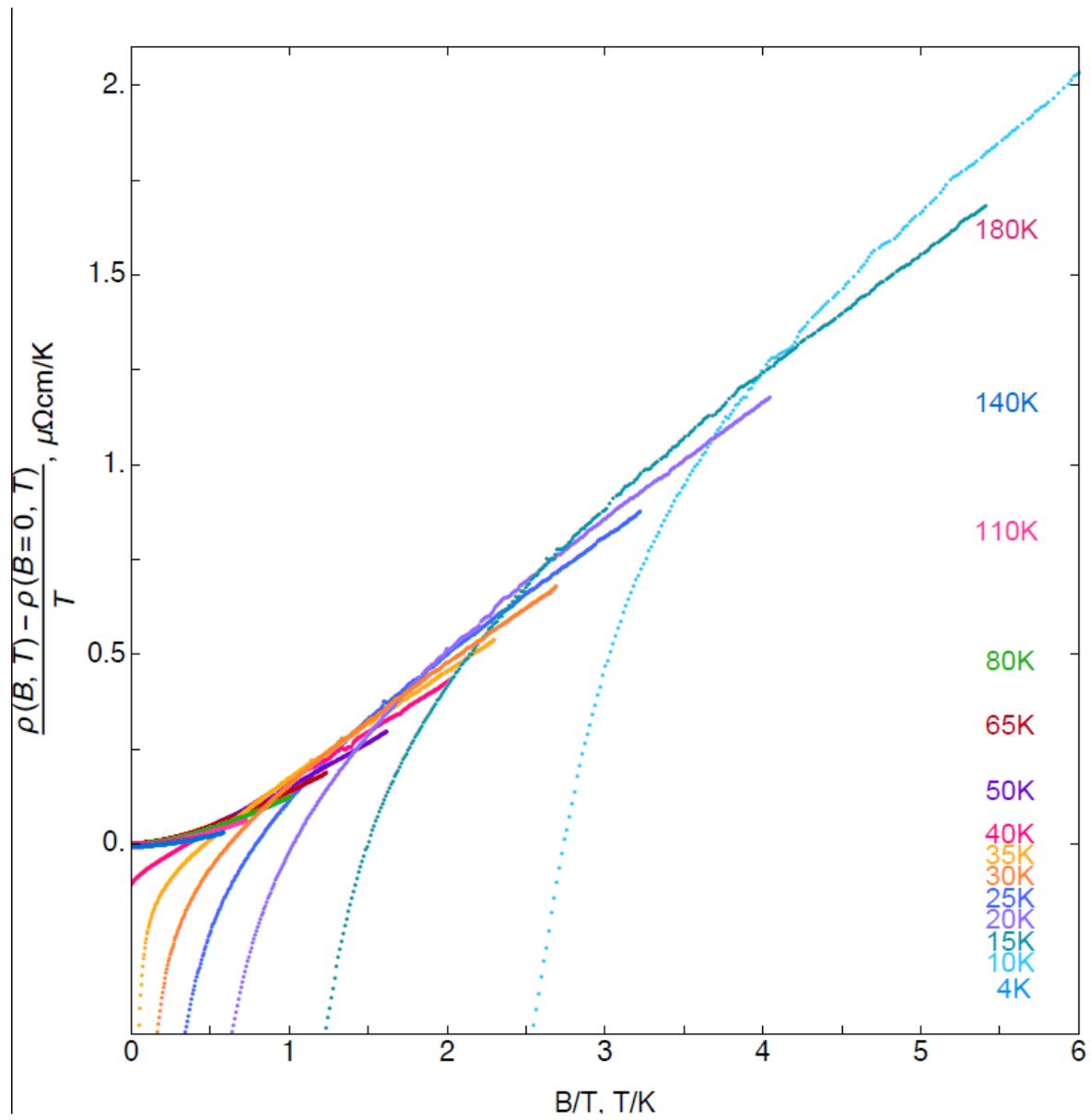


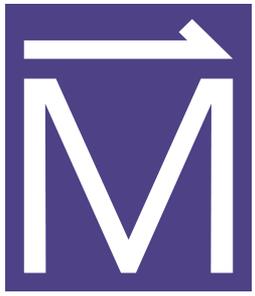


**Linear-in-H in LSCO  
and Scaling in LSCO  
Background Slides**

# Doping Dependence of Linear-in-B Slopes



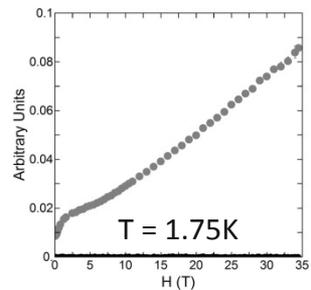




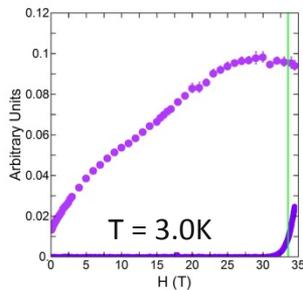
# **Our Specific Heat Measurements Background Slides**

# Comparison of Specific Heat and Resistive Transitions

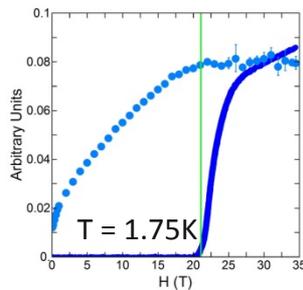
$x = 0.31$



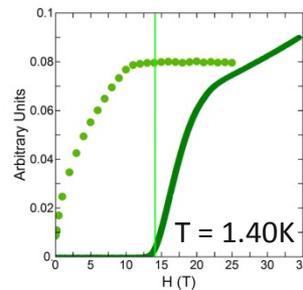
$x = 0.36$



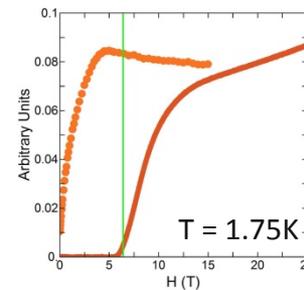
$x = 0.44$



$x = 0.46$



$x = 0.53$



$x = 0.60$

