

# From Perfect Conductor to Perfect Insulator: the Zero-Plateau QH State in Graphene

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(arXiv:0807.2867)

Acknowledgements:

L. Brey, R. Berkovits, M. Goldstein, K. Novoselov, P. Ong

NSF, GIF

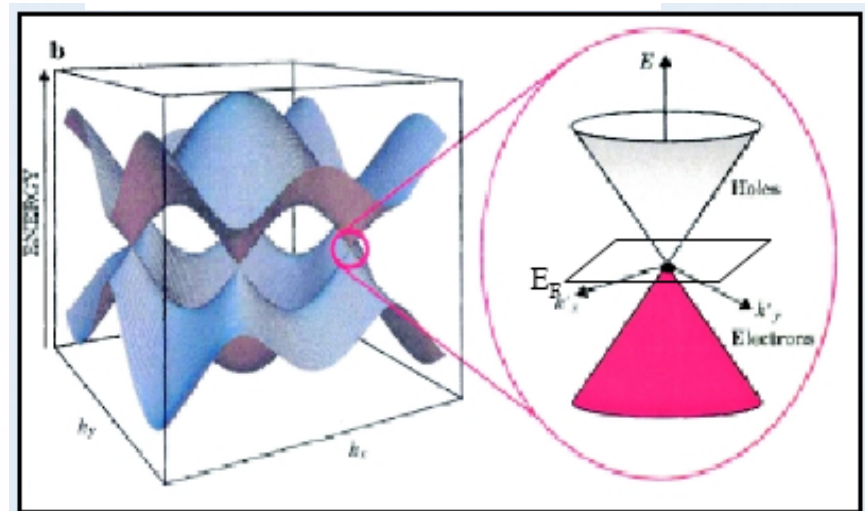
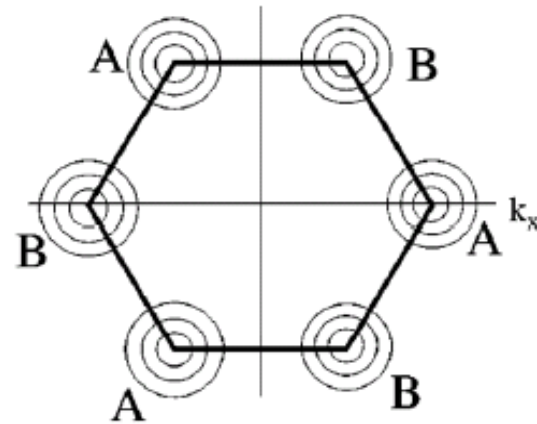
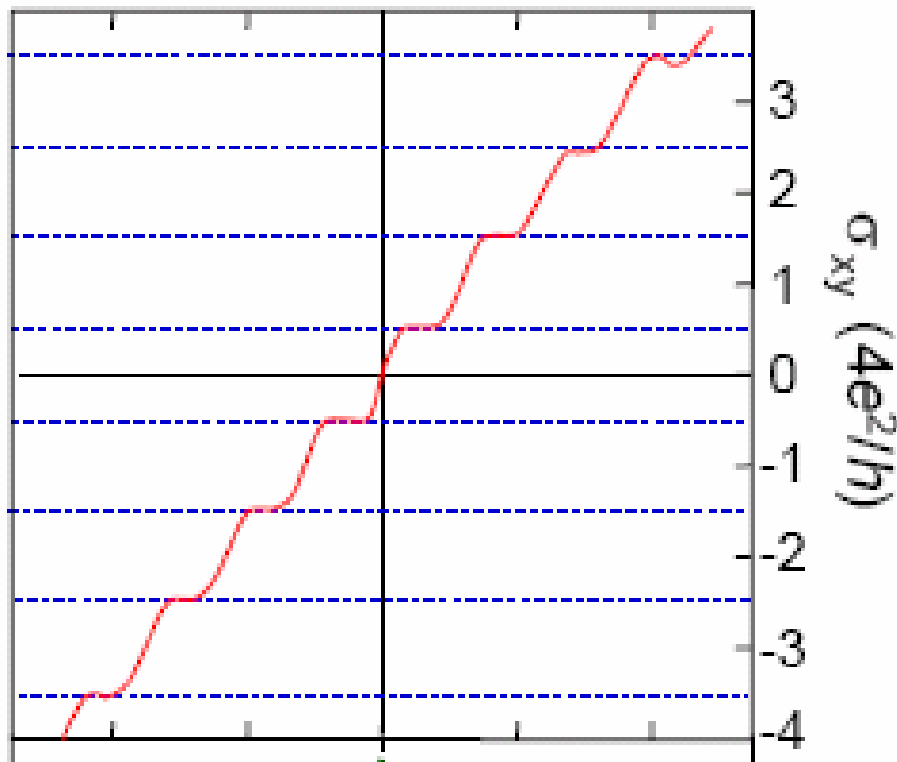
KITP Low Dimensions Conference, Feb 26, 2009

# From Perfect Conductor to Perfect Insulator: the Zero-Plateau QH State in Graphene



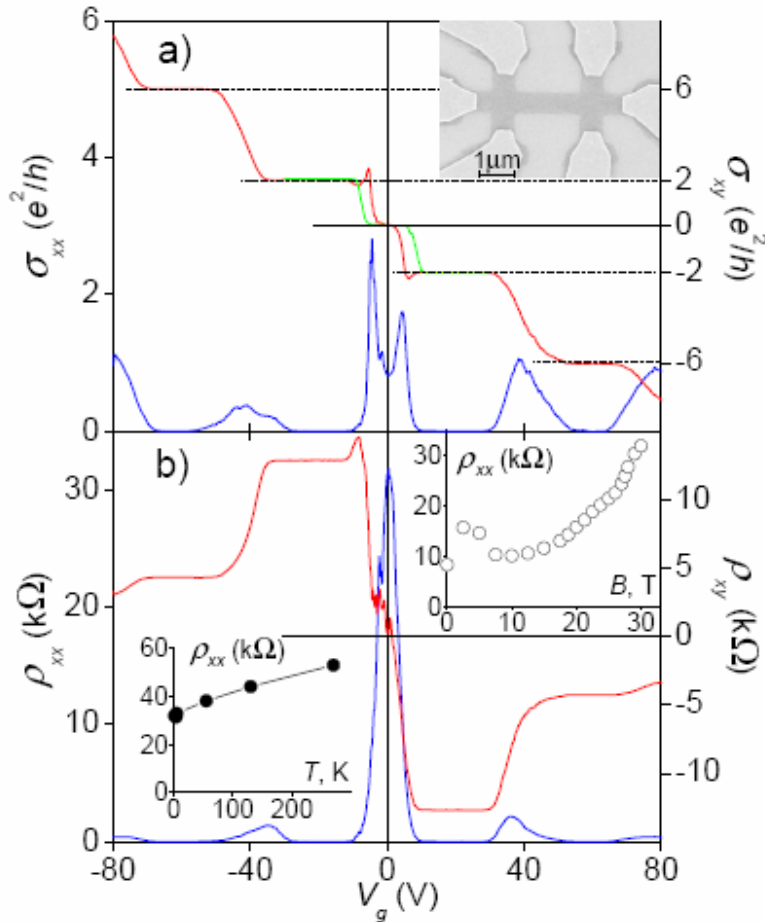
“...Now, **here**, you see, it takes all the running **you** can do, to keep in the same place...” (L. Carroll, from “Alice’s Adventures through the Looking Glass”)

# The Quantum Hall Effect in Graphene



Novoselov, Geim et al., Nature **438**, 197 (05)

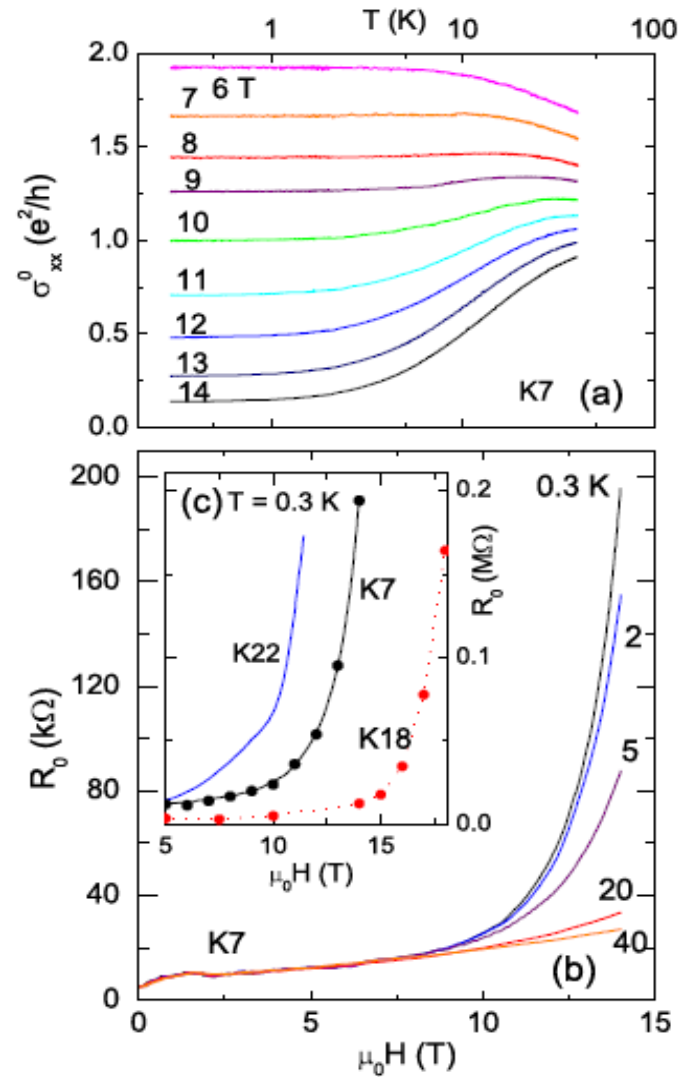
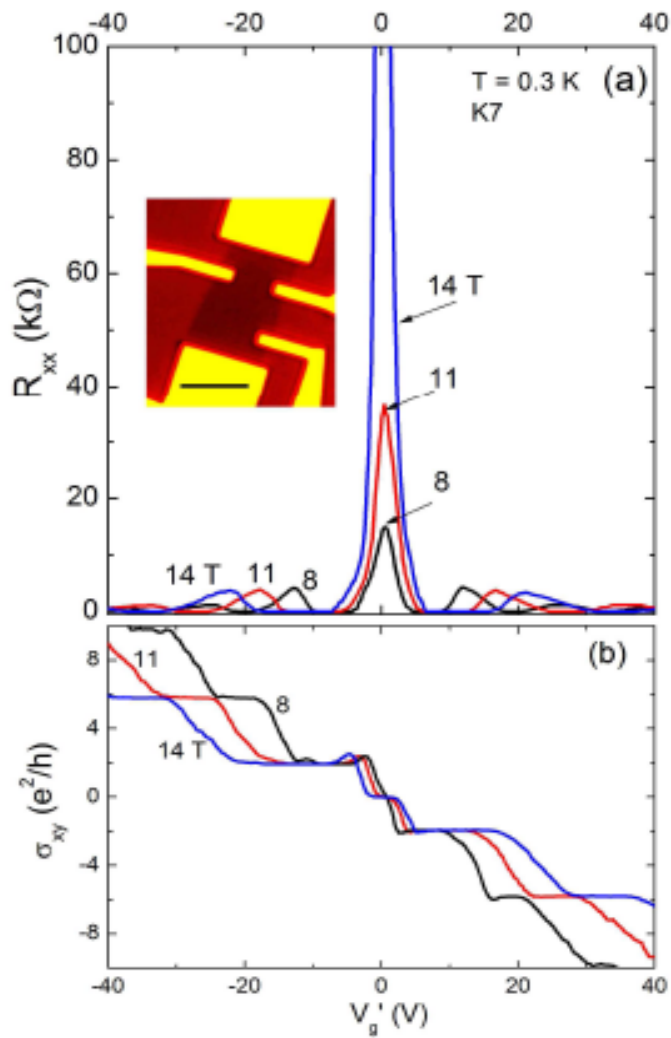
# Stronger B: Dissipative QHE at the Dirac Point



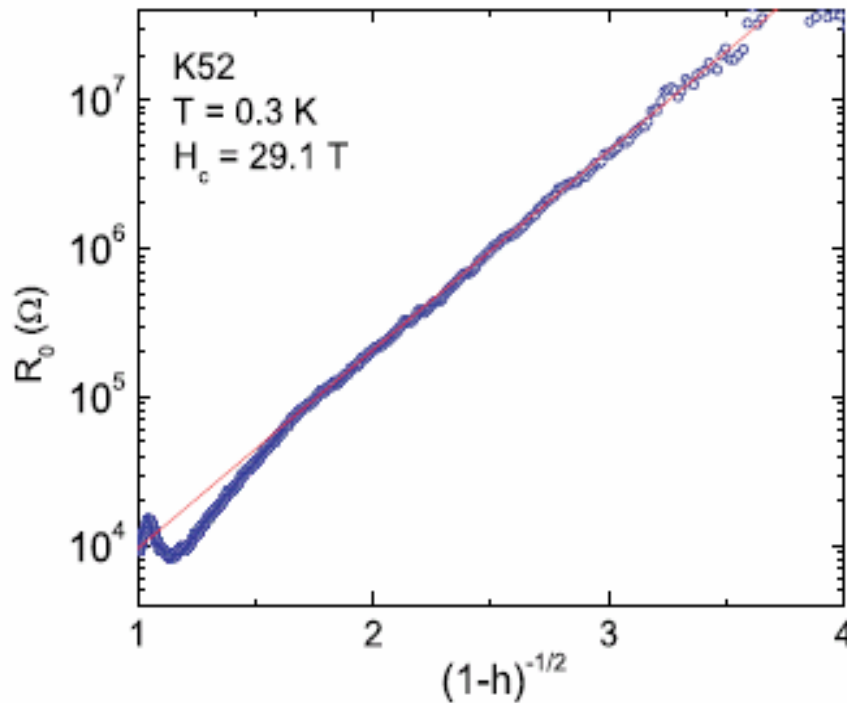
Abanin *et al.* (2007)

- Plateau at  $\nu=0$ , but  $\rho_{xx} \neq 0$ !
- $\rho_{xx}$  increases with  $T \Rightarrow$  **Metal**
- $\rho_{xx}$  increases with  $B$

# Checkelsky, Li and Ong (2007):



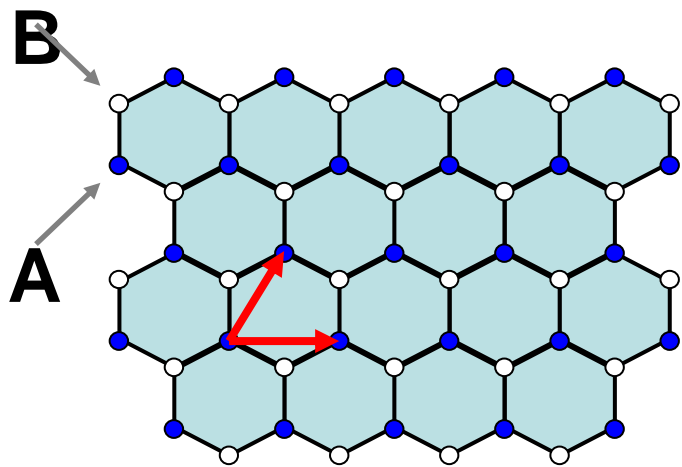
Checkelsky, Li and Ong (2008): more on the “Insulator” -  
Divergence of  $R_0$  at high  $H$



$$R_0 \sim \underbrace{\exp \left\{ \frac{2C}{\sqrt{(H_c - H)}} \right\}}_{\xi_{KT}^2 !!}$$

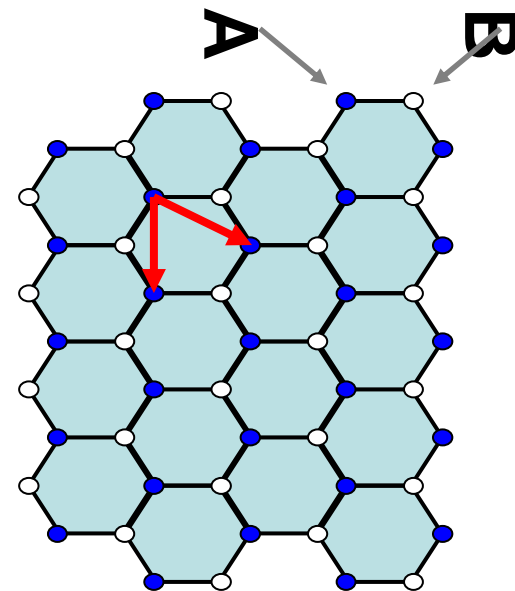
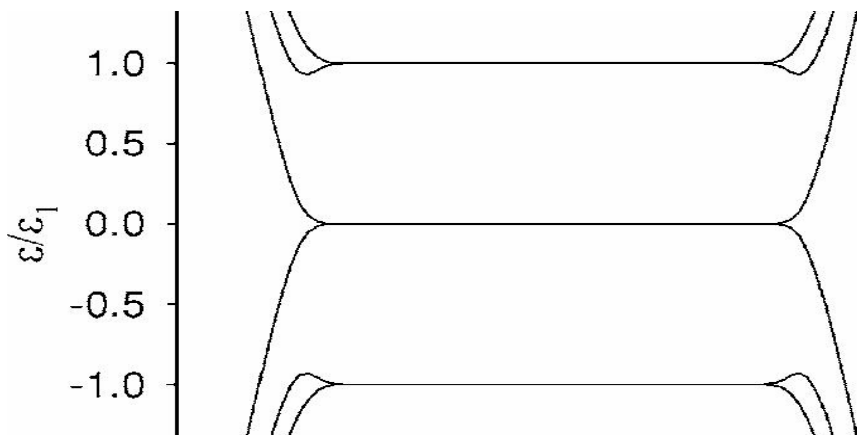
# QH Edge-States in Graphene Ribbons

Brey and Fertig (2006):



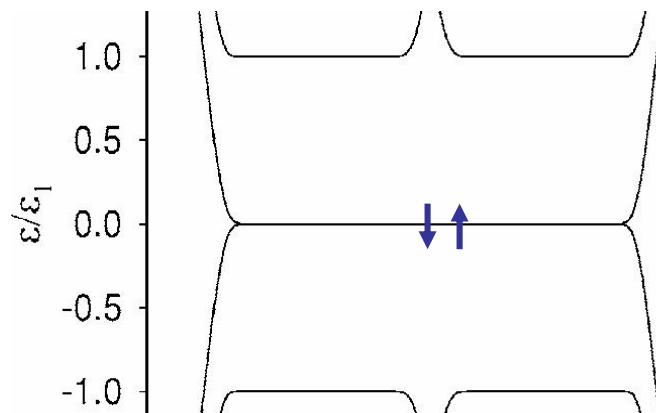
Armchair Edge

Zigzag Edge

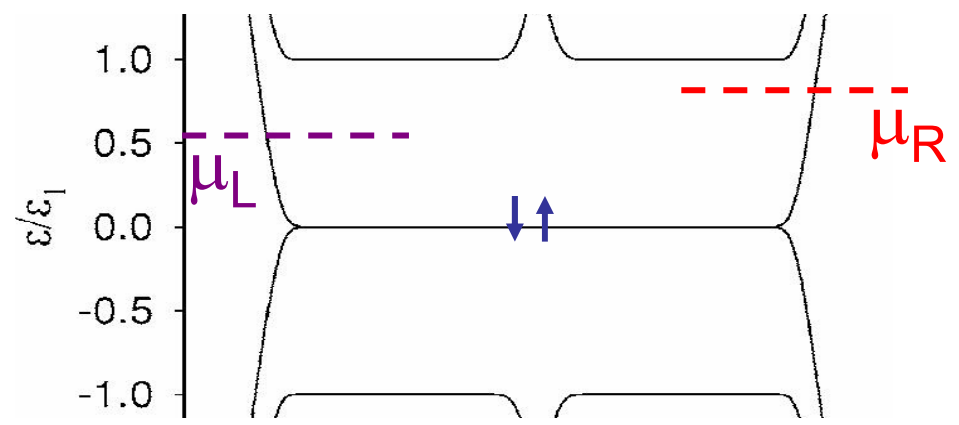
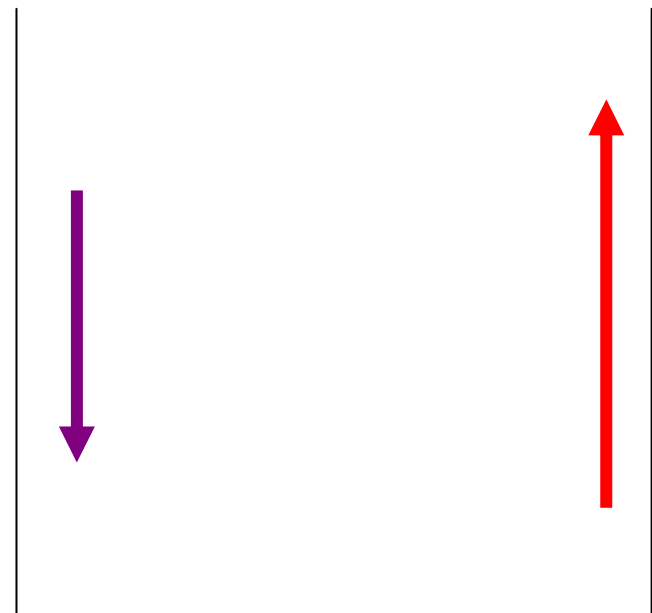
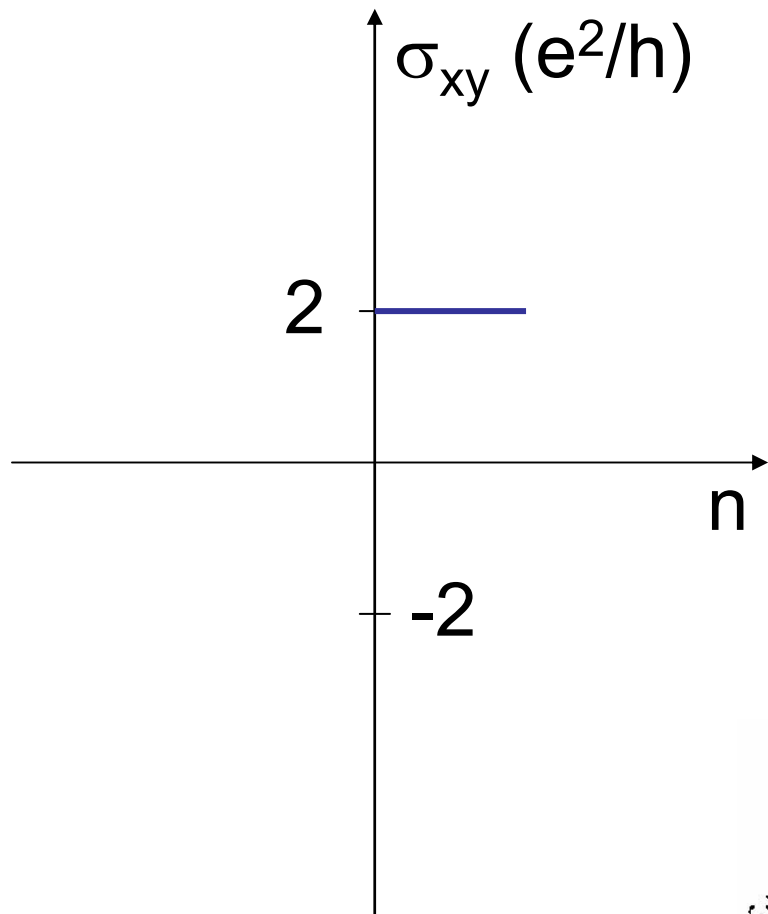


Zigzag Edge

Armchair Edge

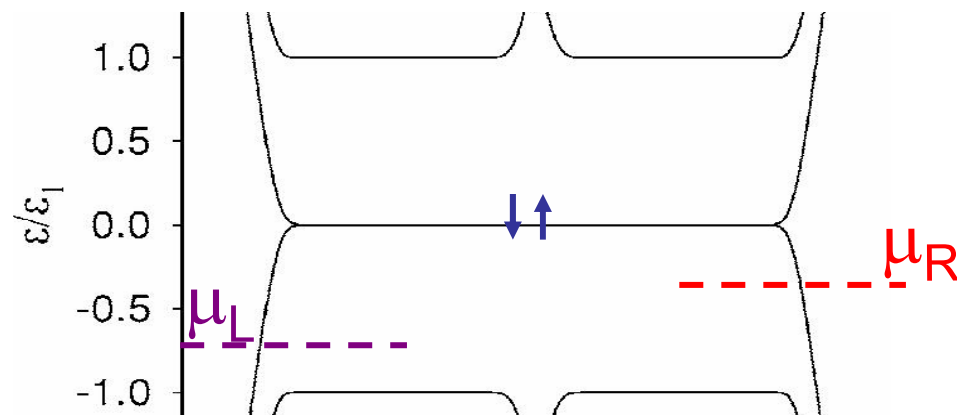
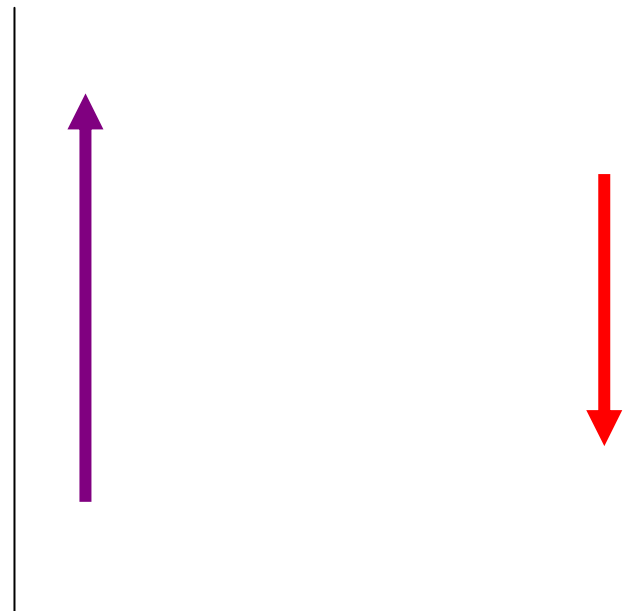
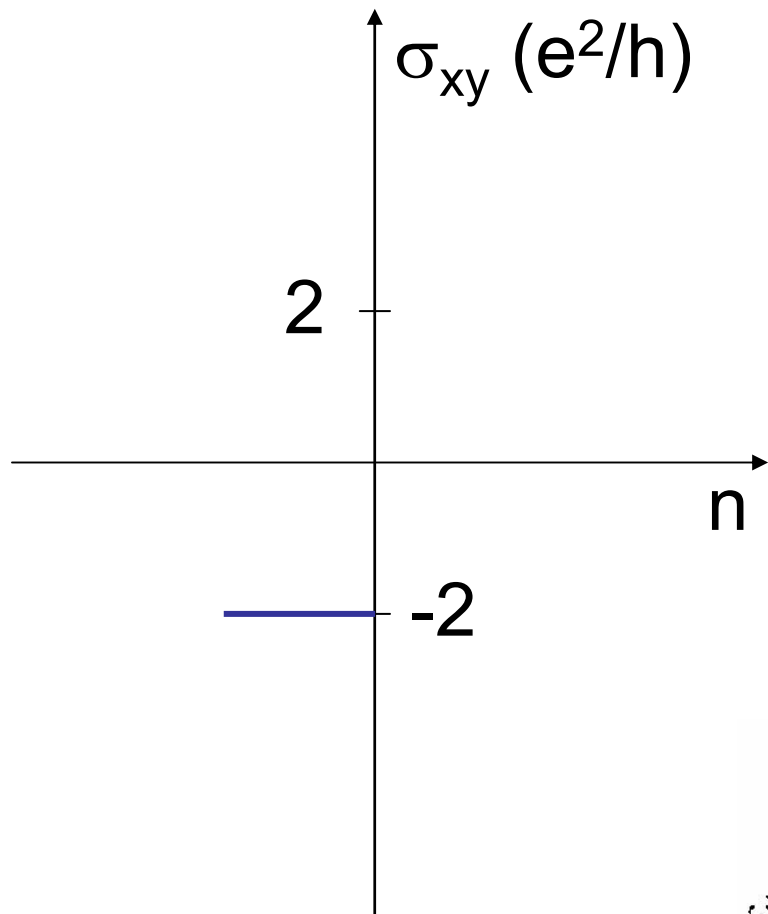


# QH Edge-States in Graphene Ribbons

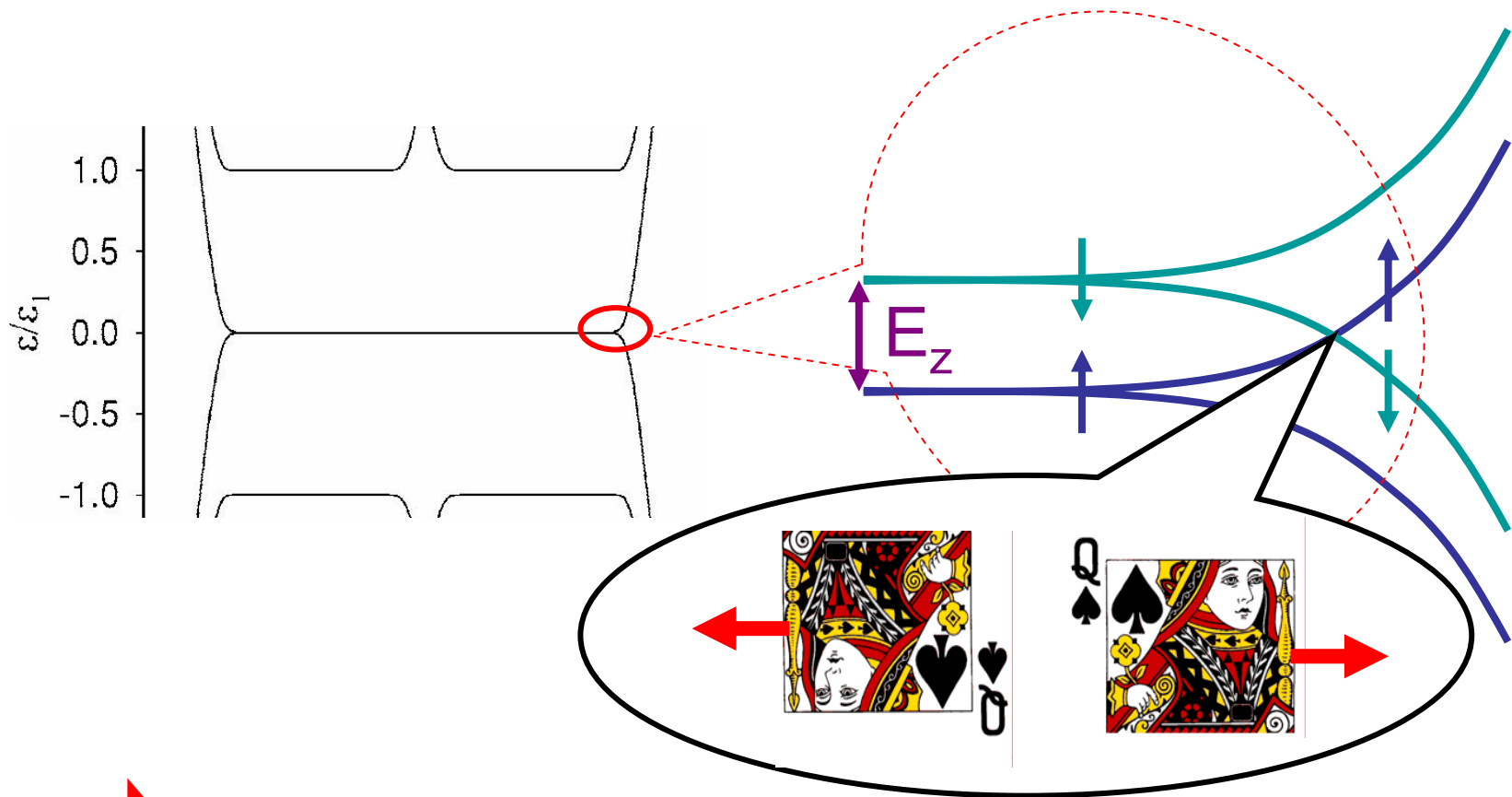




# QH Edge-States in Graphene Ribbons

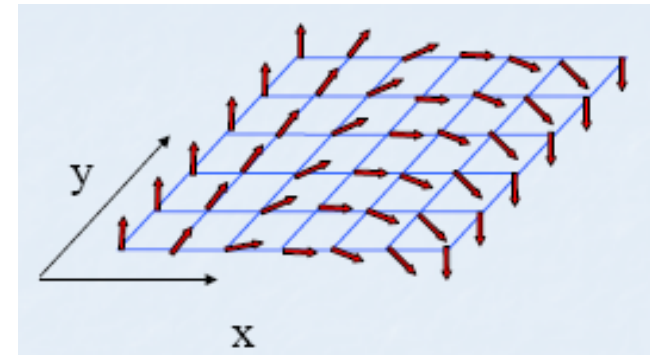
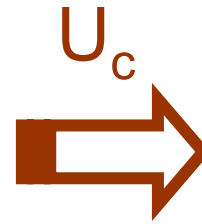
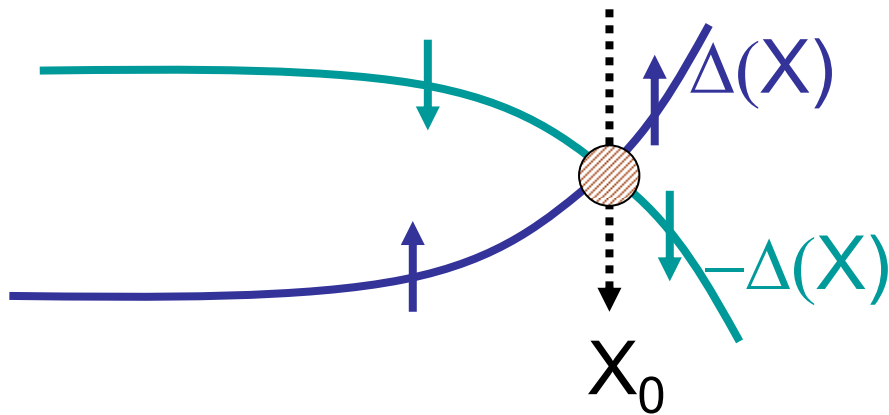


# Origin of $\nu=0$ plateau at high H: Zeeman splitting



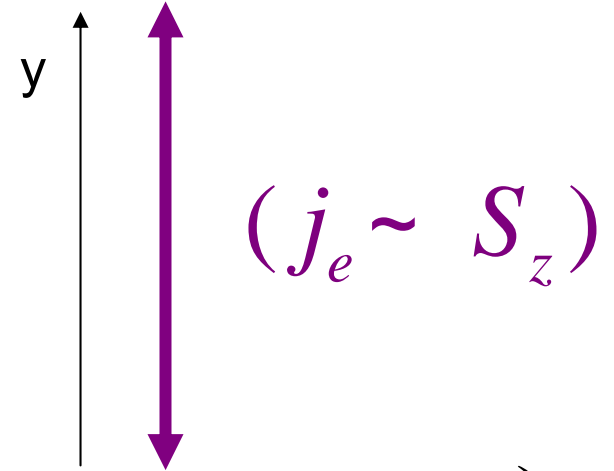
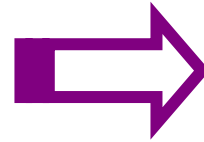
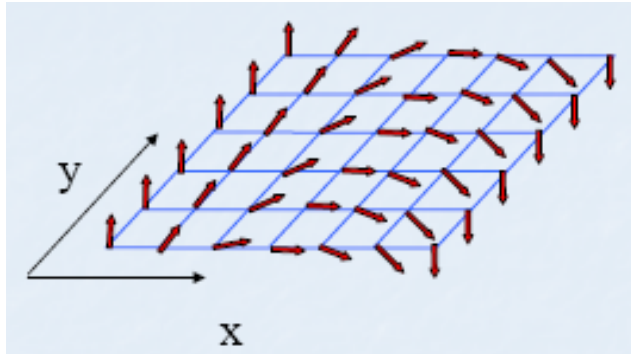
**Spin-flip impurities**  $\rightarrow$  **Finite  $\rho_{xx}$**   
(Abanin, Levitov & Lee)

# Role of Coulomb interactions (Fertig & Brey, 2007):



Finite width Domain Wall

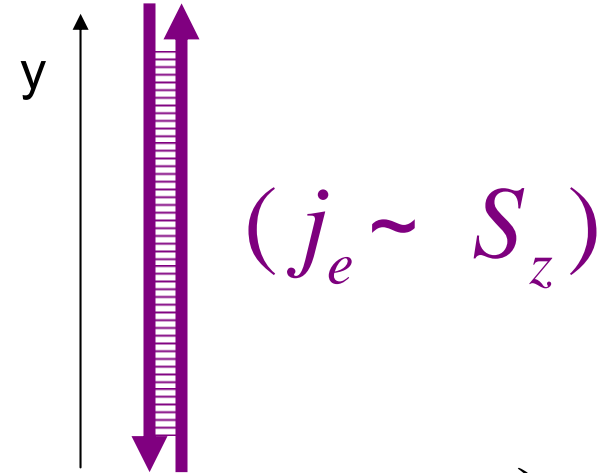
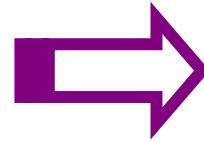
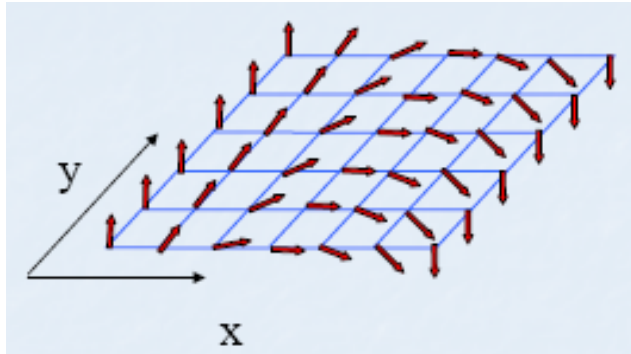
# Our Theory: Effective 1D Model for the Domain Wall



$$H_{DW} = \int \frac{dy}{2\pi} \left( uK (\partial_y \theta)^2 + \frac{u}{K} (\partial_y \phi)^2 - g \cos[4\phi] \right)$$

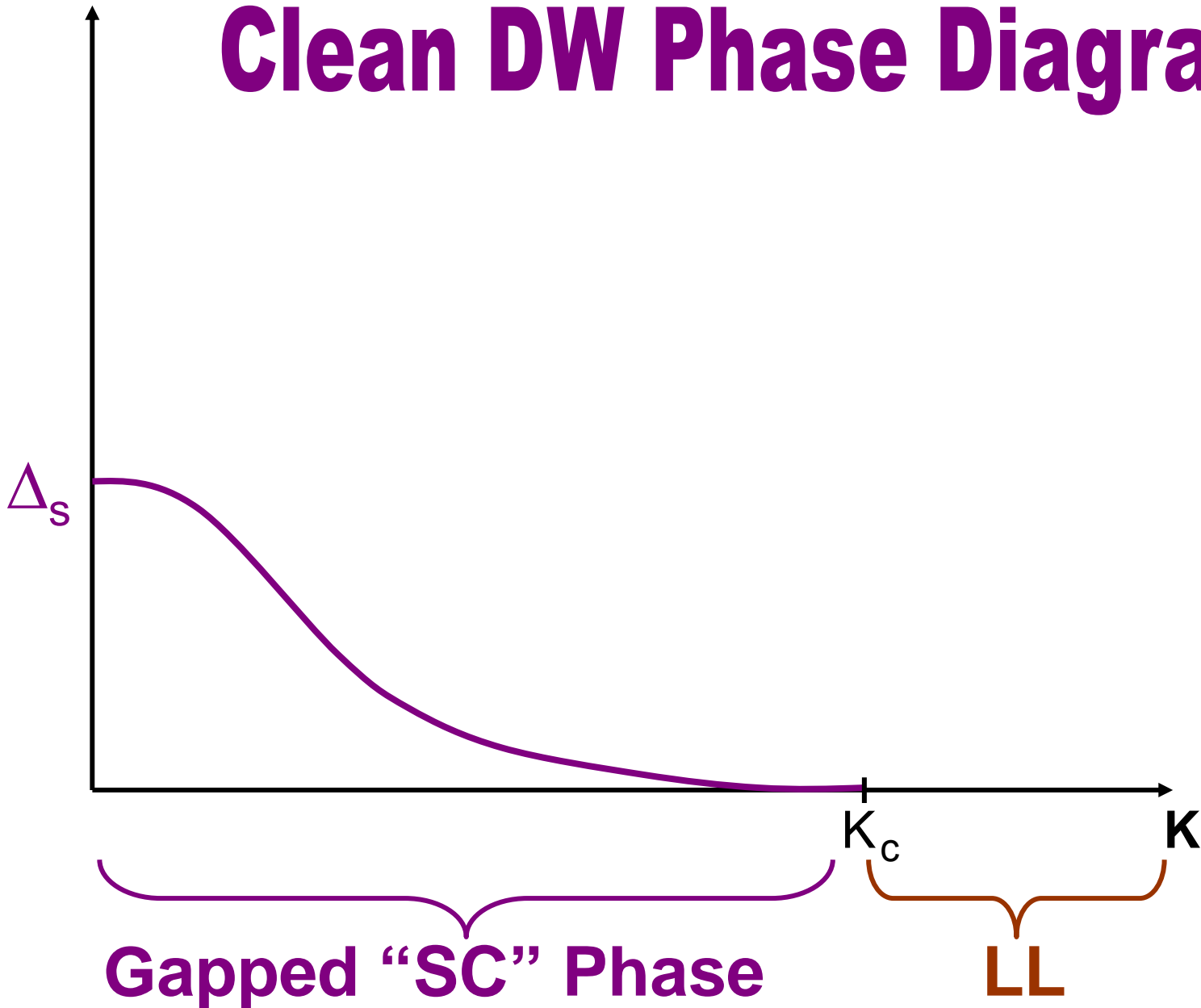
$$K[H, U_c, \Delta'(X_0)], \quad u[H, U_c, \Delta'(X_0)], \quad g[H, U_c, \Delta'(X_0)]$$

# Our Theory: Effective 1D Model for the Domain Wall

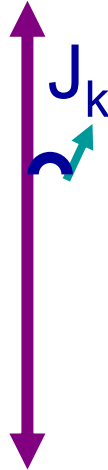
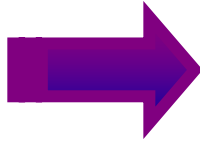
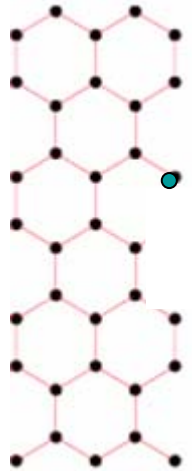


$$H_{DW} = \int \frac{dy}{2\pi} \left( \underbrace{uK (\partial_y \theta)^2}_{\text{"charging energy"}} + \underbrace{\frac{u}{K} (\partial_y \phi)^2}_{\text{"SC stiffness"}} - \boxed{g \cos[4\phi]}_{\text{"Josephson Coupling"}} \right)$$

# Clean DW Phase Diagram



# Theory for Transport: adding Spin-Flip Interaction



$$H = H_{DW} + H_{\sigma} + H_{int}$$

$$H_{\sigma} = \epsilon_z \sigma_z$$

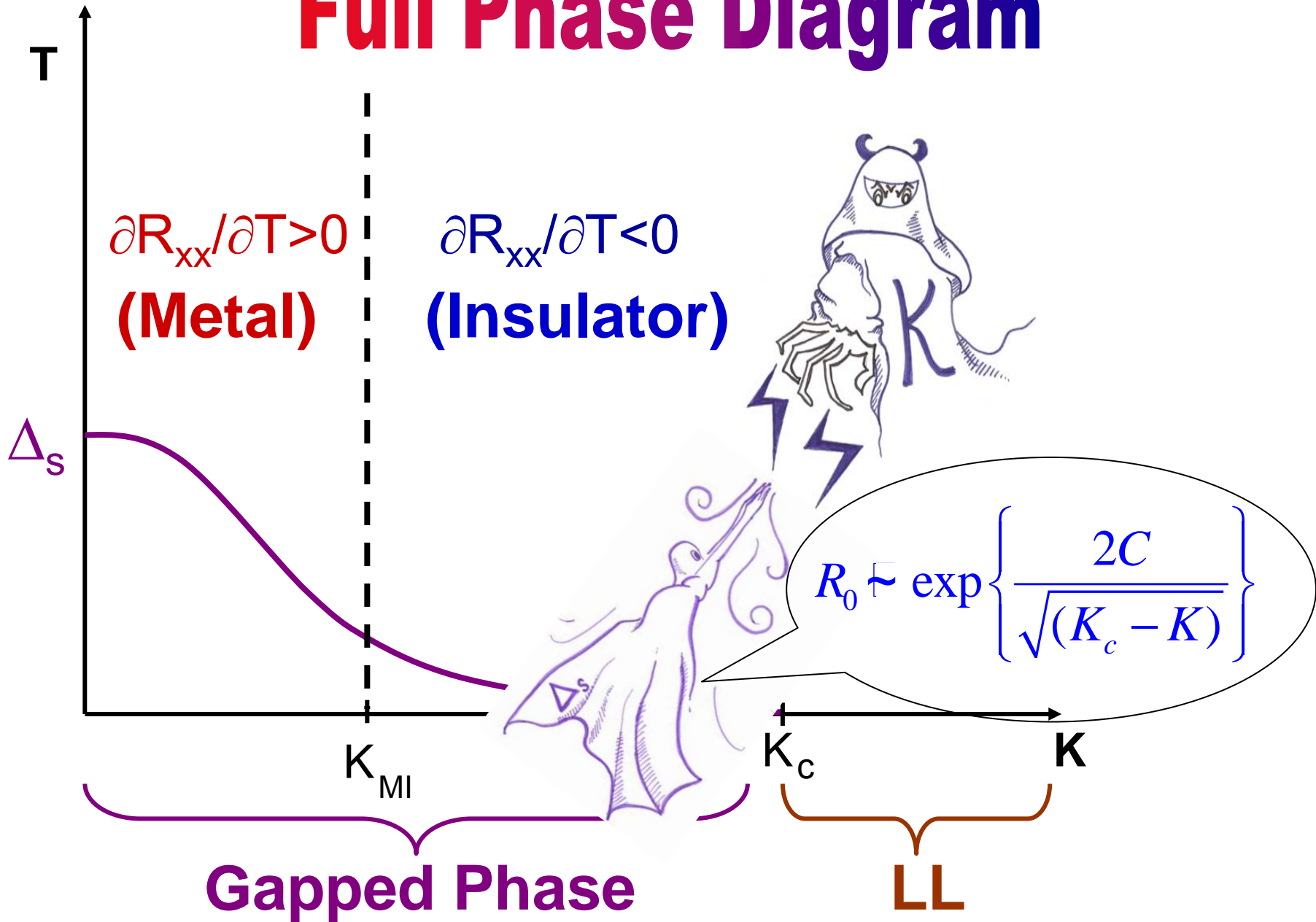
$$H_{int} = J_k \mathbf{S} \cdot \boldsymbol{\sigma}$$

Back-scattering induced resistance for  $T > \Delta_s$ :

$$R_{xx} \approx g^2 T^{\nu(K)} F[\epsilon_z/T] \quad (g \sim J_k)$$

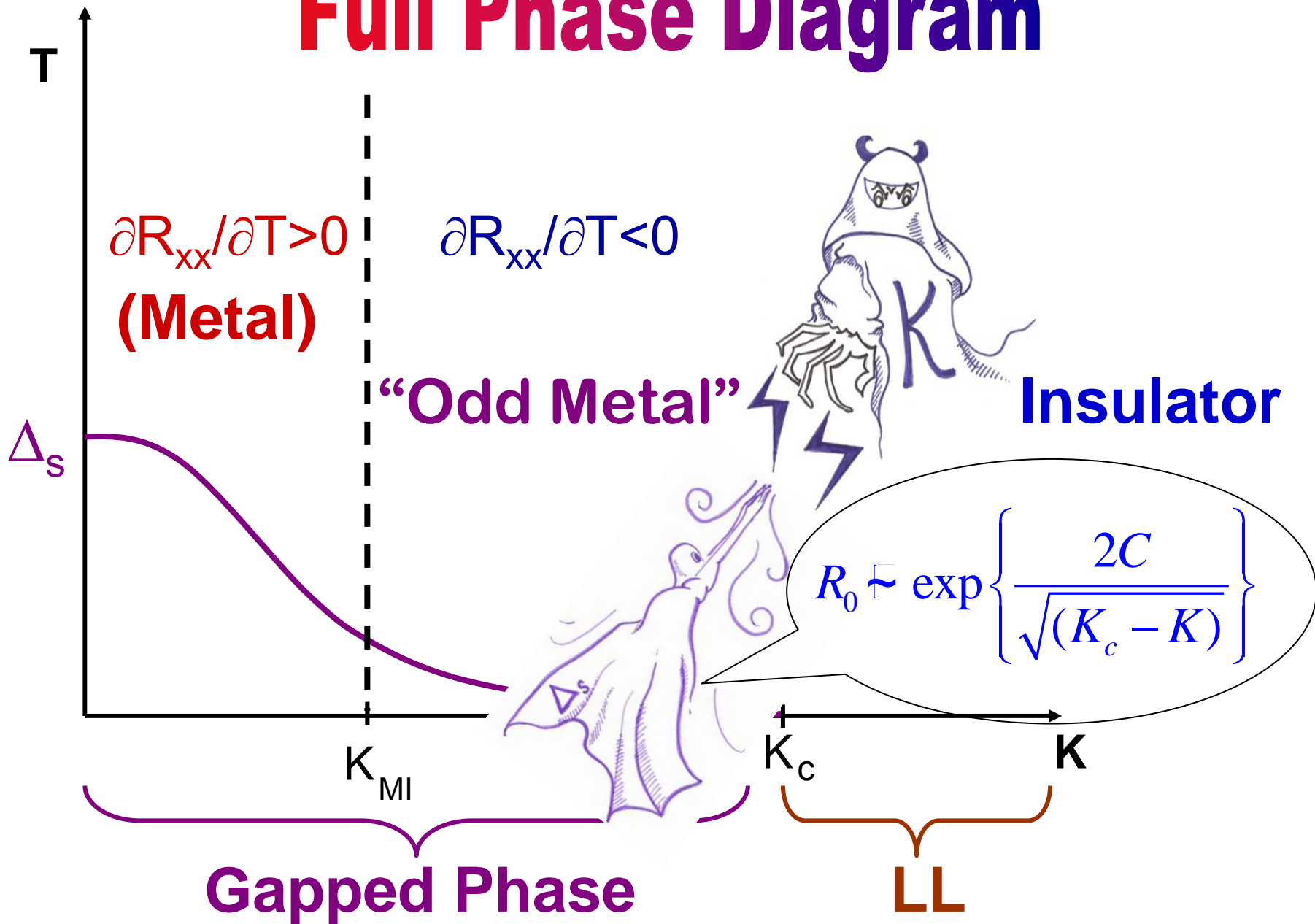
$$\nu(K_{MI}) = 0$$

# Full Phase Diagram





# Full Phase Diagram



# Summary

- ♠ Finite  $R_{xx}$  at the  $\nu=0$  QH state induced by “chiral Kondo effect”: **Spin-flip** = **Charge backscattering**
- ♠ New type of edge state: **spin Domain Wall** = a non-chiral perfect conducting channel
- ♠ Diverse transport phenomena:  $R_{xx}(T)$  is **metallic**, **insulating** or “**odd metal**” depending on  $K$ .  
Divergence of  $R_0 \Rightarrow$  quantum KT-transition (in 1+1d)

