

# Antiferromagnets on the kagomé lattice

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& Institut Universitaire de France



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# Outline

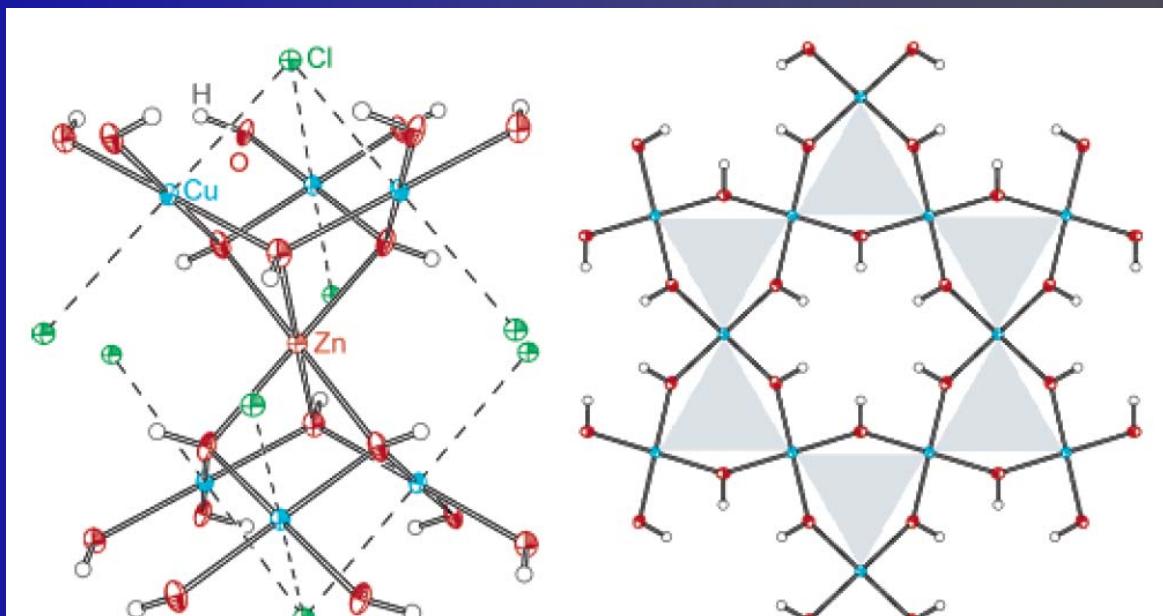
- Spin-1/2 Heisenberg model on kagomé lattice
  - Gap (?) and homogeneous susceptibility: Ph. Sindzingre Paris
  - Dynamical Spin Susceptibility: A. Laeuchli EPFL
- The  $J_1-J_2$  model on the kagomé lattice :
  - a new chiral low temperature phase
  - the role of vortices on the low temp. properties  
J.-C. Dommenga (Rutgers), L. Messio & P. Viot (Paris)

## A Structurally Perfect $S = 1/2$ Kagomé Antiferromagnet

Matthew P. Shores, Emily A. Nytko, Bart M. Bartlett, and Daniel G. Nocera\*

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Cambridge, Massachusetts 02139-4307*

Received June 13, 2005; E-mail: nocera@mit.edu



**Figure 1.** Crystal structure of Zn-paratacamite (**1**),  $Zn_{0.33}Cu_{3.67}(OH)_6Cl_2$ .

**Quantum Magnetism in the Paratacamite Family: Towards an Ideal Kagomé Lattice**

P. Mendels,<sup>1</sup> F. Bert,<sup>1</sup> M. A. de Vries,<sup>2</sup> A. Olariu,<sup>1</sup> A. Harrison,<sup>2</sup> F. Duc,<sup>3</sup> J. C. Trombe,<sup>3</sup>  
J. S. Lord,<sup>4</sup> A. Amato,<sup>5</sup> and C. Baines<sup>5</sup>

**Spin Dynamics of the Spin-1/2 Kagome Lattice Antiferromagnet  $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$** 

J. S. Helton,<sup>1</sup> K. Matan,<sup>1</sup> M. P. Shores,<sup>2</sup> E. A. Nytko,<sup>2</sup> B. M. Bartlett,<sup>2</sup> Y. Yoshida,<sup>3</sup> Y. Takano,<sup>3</sup> A. Suslov,<sup>4</sup> Y. Qiu,<sup>5</sup>  
J.-H. Chung,<sup>5</sup> D. G. Nocera,<sup>2</sup> and Y. S. Lee<sup>1</sup>

**Ground state and excitation properties of the quantum kagomé system  
 $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$  investigated by local probes.**

Oren Ofer and Amit Keren

*Physics Department, Technion, Israel Institute of Technology, Haifa 32000, Israel*

Emily A. Nytko, Matthew P. Shores, Bart M. Bartlett, and Daniel G. Nocera  
*Department of Chemistry, Massachusetts Institute of Technology, Cambridge, MA 02139 USA*

Chris Baines and Alex Amato

*Paul Scherrer Institute, CH 5232 Villigen PSI, Switzerland*

# $^{63}\text{Cu}$ and $^{35}\text{Cl}$ NMR Investigation of the $S = \frac{1}{2}$ Kagomé Lattice System $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

T. Imai<sup>1</sup>, E. A. Nytko<sup>2</sup>, B.M. Bartlett<sup>2</sup>, M.P. Shores<sup>2</sup>, and D. G. Nocera<sup>2</sup>

<sup>1</sup>*Department of Physics and Astronomy, McMaster University, Hamilton, ON L8S4M1, Canada*

<sup>2</sup>*Department of Chemistry, M.I.T., Cambridge, Massachusetts 02139*

(Dated: April 3, 2007)

## Quantum spin liquid states in the two dimensional kagomé antiferromagnets, $\text{Zn}_x\text{Cu}_{4-x}(\text{OD})_6\text{Cl}_2$

S.-H. Lee<sup>\*</sup>, H. Kikuchi<sup>†</sup>, Y. Qiu<sup>‡</sup>, B. Lake<sup>§+</sup>, Q. Huang<sup>‡</sup>, K. Habicht<sup>§</sup> and K. Kiefer<sup>§</sup>

## Low temperature magnetization of the $S=1/2$ kagome antiferromagnet $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

F. Bert,<sup>1</sup> S. Nakamae,<sup>2</sup> F. Ladieu,<sup>2</sup> D. L'Hôte,<sup>2</sup> P. Bonville,<sup>2</sup> F. Duc,<sup>3</sup> J.-C. Trombe,<sup>3</sup> and P. Mendels<sup>1</sup>

<sup>1</sup>*Laboratoire de Physique des Solides, UMR CNRS 8502, Université Paris-Sud, 91405 Orsay, France*

<sup>2</sup>*Service de Physique de l'État Condensé, DSM, CEA Saclay, 91191 Gif-sur-Yvette Cedex, France.*

<sup>3</sup>*Centre d'Élaboration des Matériaux et d'Études Structurales, CNRS UPR 8011, 31055 Toulouse, France*

(Dated: July 16, 2007)



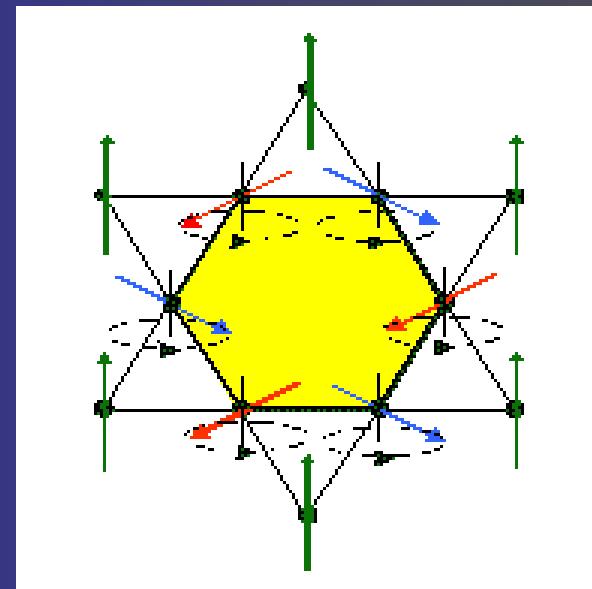
- Curie-Weiss temperature  $\Theta_{\text{cw}} = -300 \text{ K}$ 
  - $J \approx 175 \text{ K}$
- No magnetic order down to 50 mK
- Dynamical features down to 50 mK
- No observable gap down to 0.1 meV
  - No SG transition

A spin liquid phase down to  $T \leq J/1000$

# Classical Heisenberg Hamiltonian on the kagomé lattice

$$H = \sum S_i \cdot S_j$$

$$= \frac{1}{2} \sum_{\alpha} S_{\alpha}^2 + C$$



An infinite number of soft modes, an infinite T=0 degeneracy  
Therm. fluct. select coplanar configurations at very low T  
*J. Chalker, et al 92, Huse & Rutemberg 92 , Reimers & Berlinsky 93*

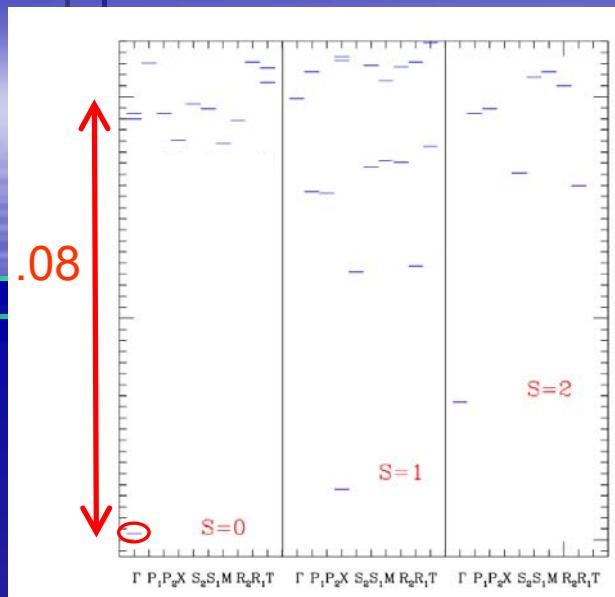
# Quantum Heisenberg Hamiltonian on the kagomé lattice

- V. Elser '89, C. Zeng & V.E. '90, P. Leung & V.E '93
- J. Chalker and J. Eastmond, '92
- P. Chandra & P. Coleman, Rutgers group, '93
- N. Elstner & A.P. Young, '94
- Paris Group: 95, 97, 99... 07

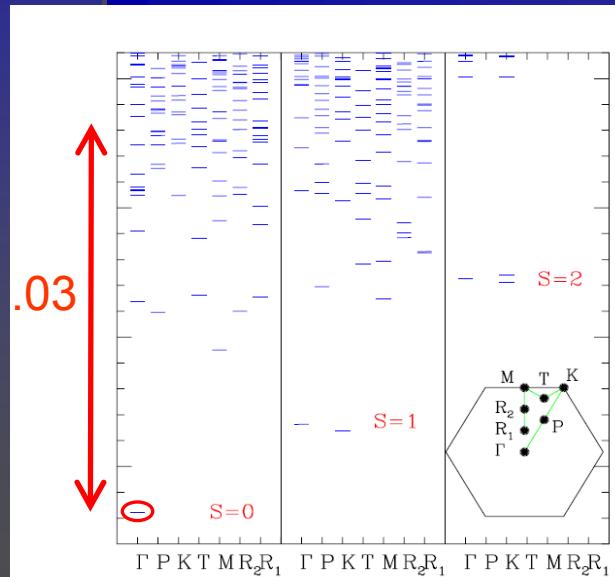
No Local order parameter  
'Short' range correlations

- Dimer approach: Leung & Elser, F. Mila's group '98, '01...

Square N=36

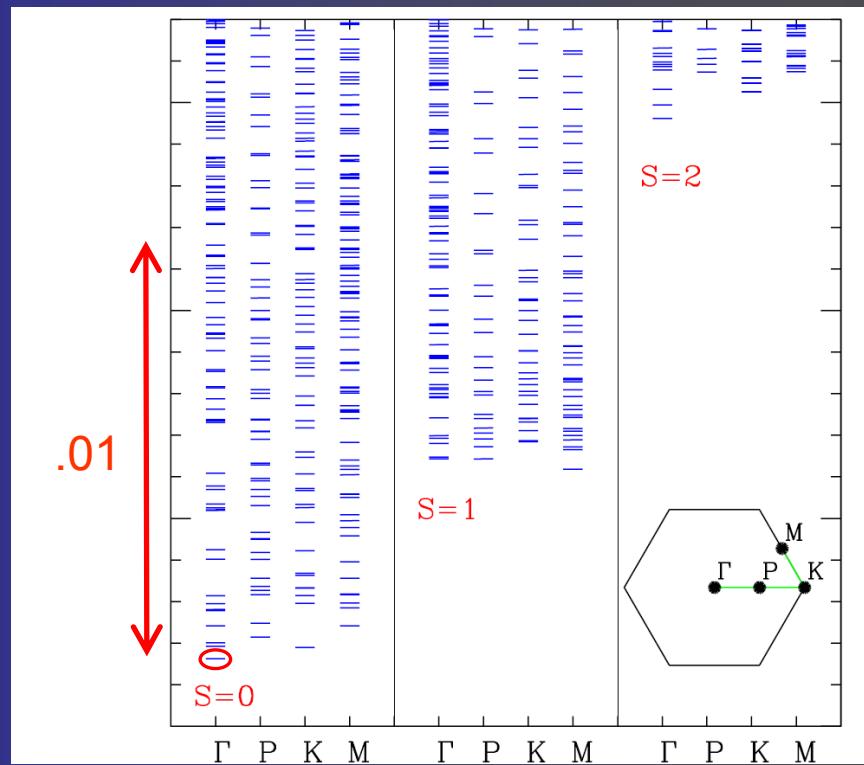


triangular N=36



# Spectra of $H = \sum S_i \cdot S_j$ (per spin)

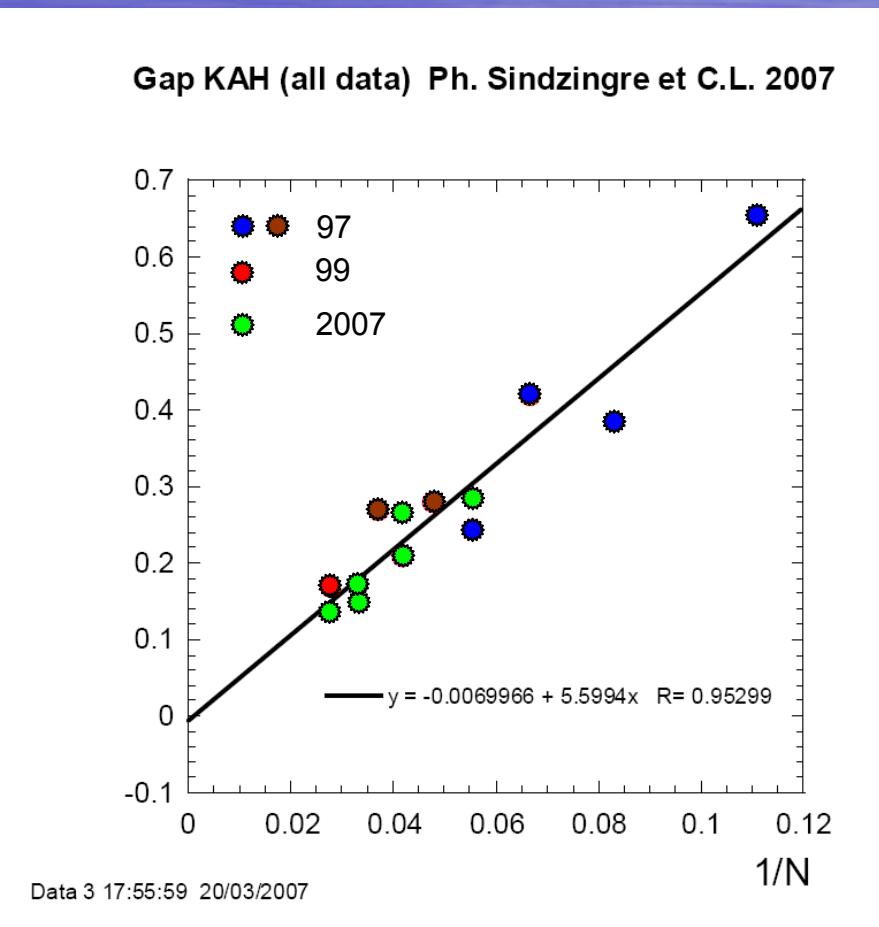
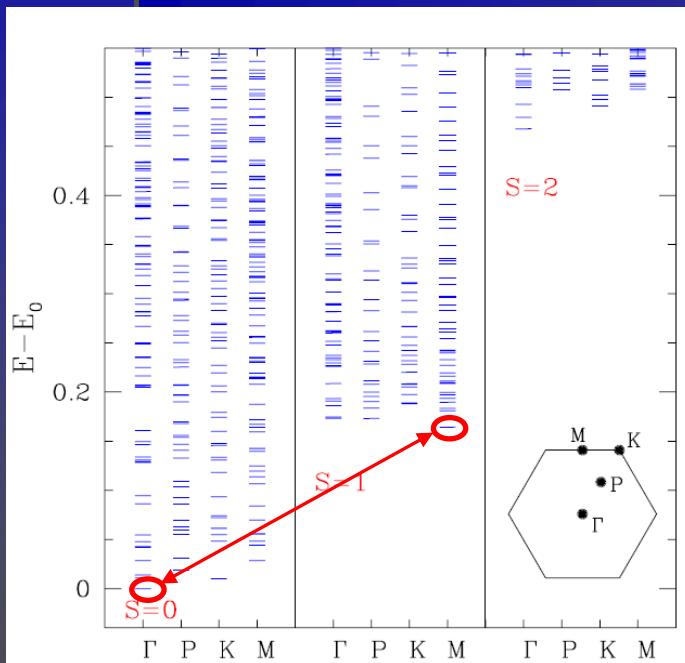
Kagomé N=36



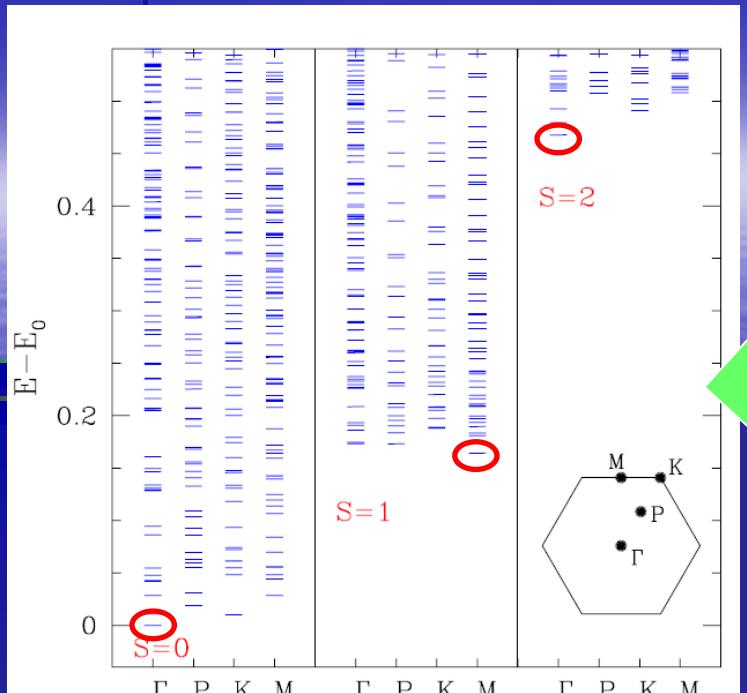
Extremely high density of low lying excitations  
-> Extra low temperature dynamics

# Is the S=1/2 KAH gapped ? (standard analysis)

$$H = \sum S_i \cdot S_j$$

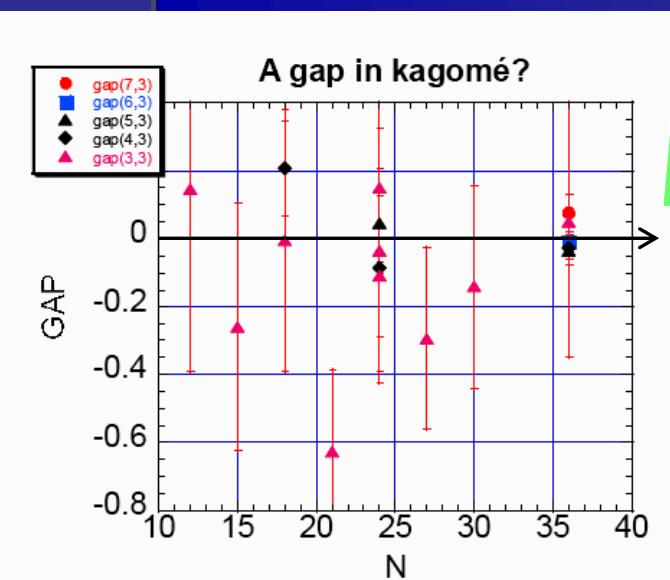
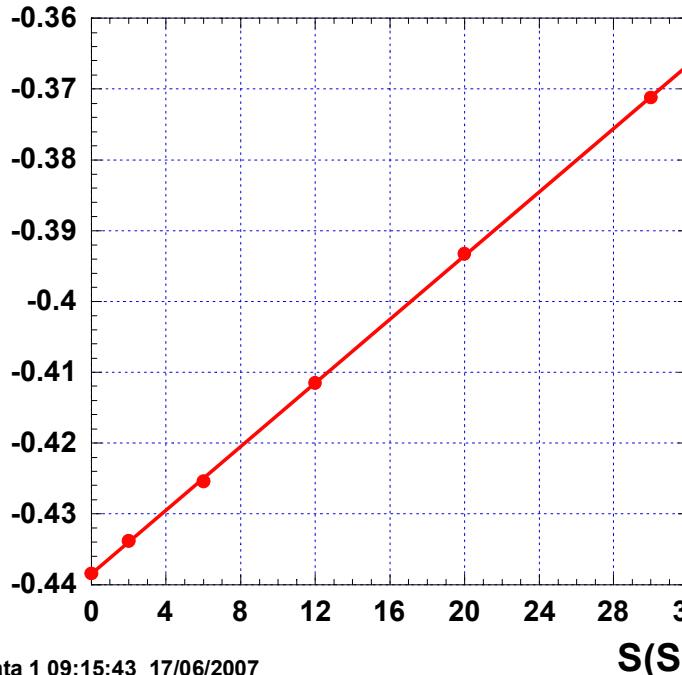


Gap = 0 +/- 0.027



$\langle 2 \mathbf{S}_i \cdot \mathbf{S}_j \rangle$  Kagome symmetric sample  $N = 36$

$$y = -0.43847 + 0.0022471x \quad R = 0.99996$$



Gap = 0 +/- 0.01  
To be read:  
Gap  $\in [0 .. 0.01]$  with proba. 2/3

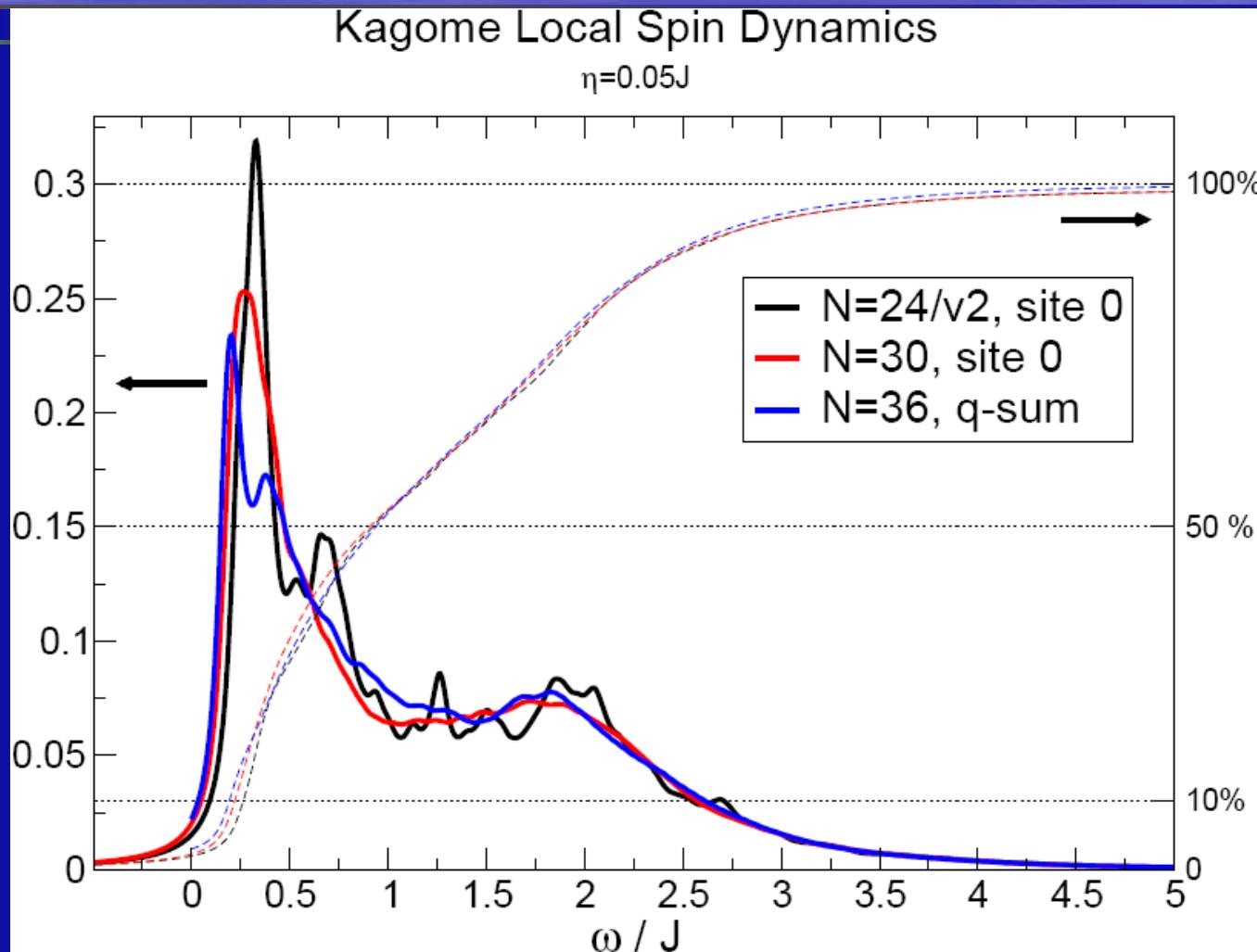
# Is the S=1/2 KAH gapped ? (refined analysis)

- *Spin Gap* ∈ [0 .. 0.01]
- $J\chi(T \sim 0.01J) = 0.09 \pm 0.015$

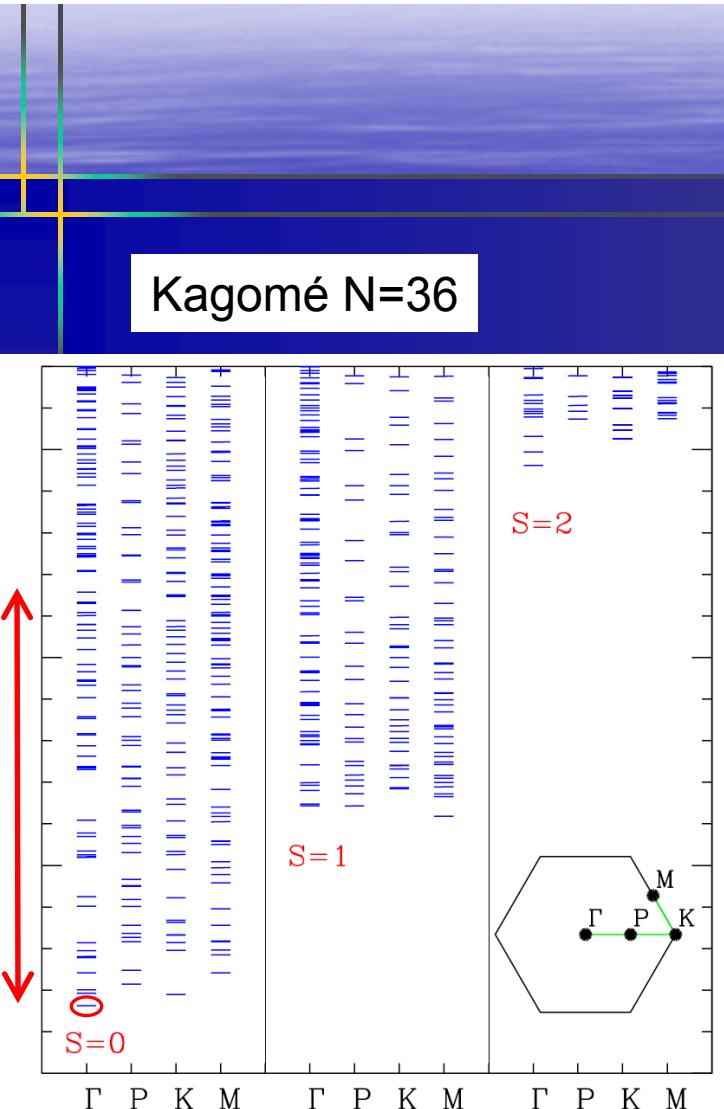
If  $C = 0.5, J = 175 K,$   
 $\chi(T \sim 0.01J) = 0.001 \text{ cm}^3/\text{mole}$

# Dynamical Structure Factor

## Andreas Laeuchli 2007



# Nature of the low temperature phase?

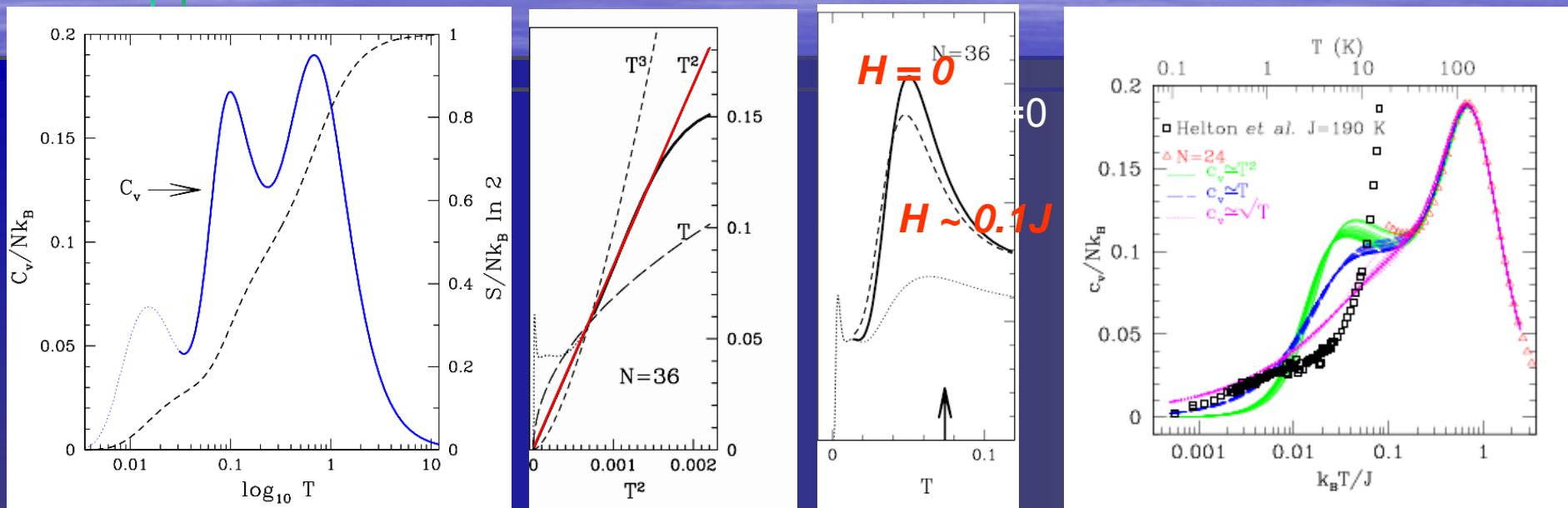


- Valence Bond Crystal ?  
*Zeng & Elser 1990, Syromyatnikov & Maleyev, Nikolic & Senthil, misguich & Sindzingre 2006, Singh & Huse 2007*
- Z2 Spin Liquids?  
*Sachdev 92, Wang & Vishnawath 2006*
- U(1) Spin Liquid ?  
*Hastings 2001,  
Ran, Hermele, Lee & Wen  
Phys Rev. Lett. 98, 117205, 2007*
- Algebraic Vortex liquid ?  
*Ryu, Motrunich, Alicea, M.P.A. Fisher  
Phys Rev. B. 184406 2007*

# Conclusions and open questions?

- Spin  $\frac{1}{2}$  Heisenberg on the kagomé lattice may be gapless:  
Gap = 0 +/- .01,  $J\chi(T=.01K) = .09 +/- .015$
- Continuum of very dense low lying excitations:  
a very good explanation of the ultra-low temperature dynamics of  $ZnCu_3(OH)_6Cl_2$
- Is it a VBC?  
VBC not fully convincing  
Our conclusions would be different for a pyrochlore, or integer spins on a kagome lattice
- A « Critical » Spin or Vortex Liquid?  
May be plausible.. Many features still to be explored

# KHAF specific heat



P. Sindzingre et al.. PRL 00  
Exact diagonalizations

G. Misguich & .Sindzingre  
07 H.T. series

Is it generic for quantum cooperative paramagnets?  
A. Ramirez et al.. PRL 00 (SCGO),  
S. Nakatsuji et al. Science 2005 (  $\text{NiGa}_2\text{S}_4$ )

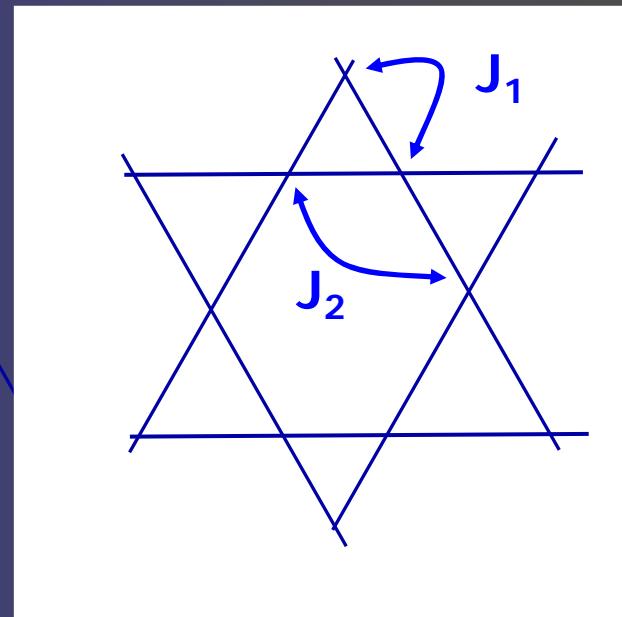
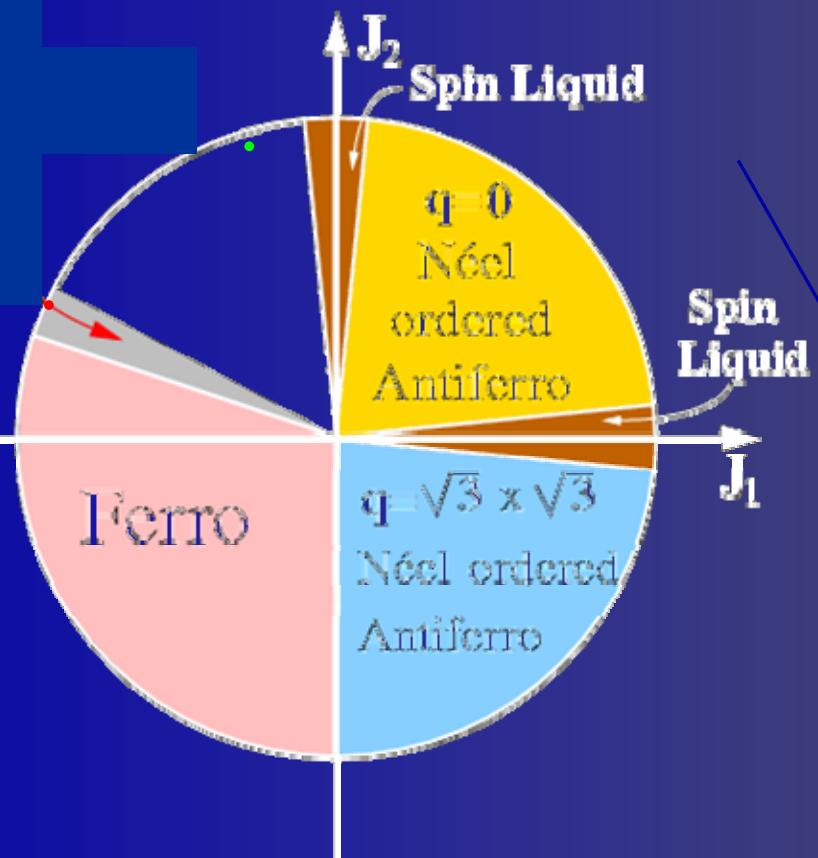
# The $J_1$ - $J_2$ model on the kagomé lat.

a new chiral low temperature phase

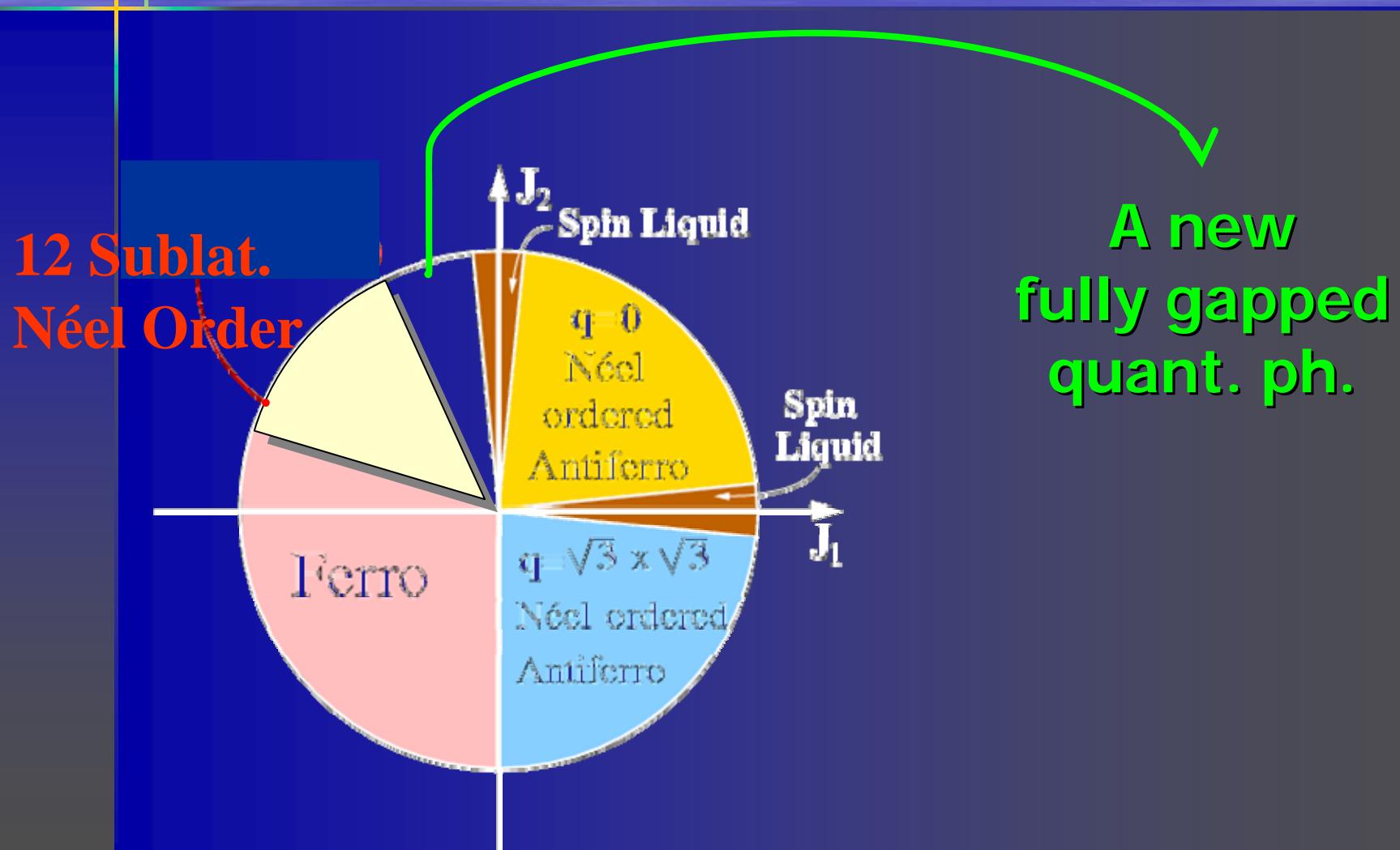
role of thermally activated  $Z_2$  vortices

J.-C. Dommange (Rutgers),  
L. Messio & P. Viot (Paris)

# Quantum phase diagram of the $J_1$ - $J_2$ model on the kagomé latt.

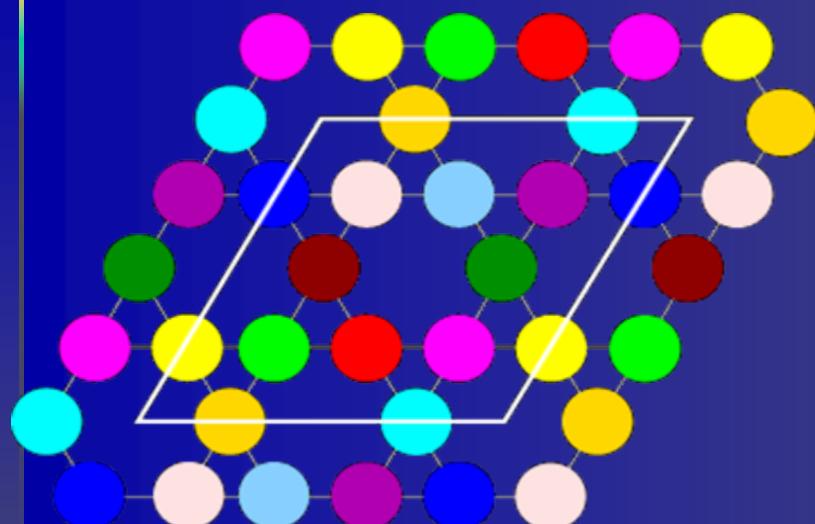


# Spin-1/2 phase diagram of the $J_1$ - $J_2$ model on the kagomé latt.

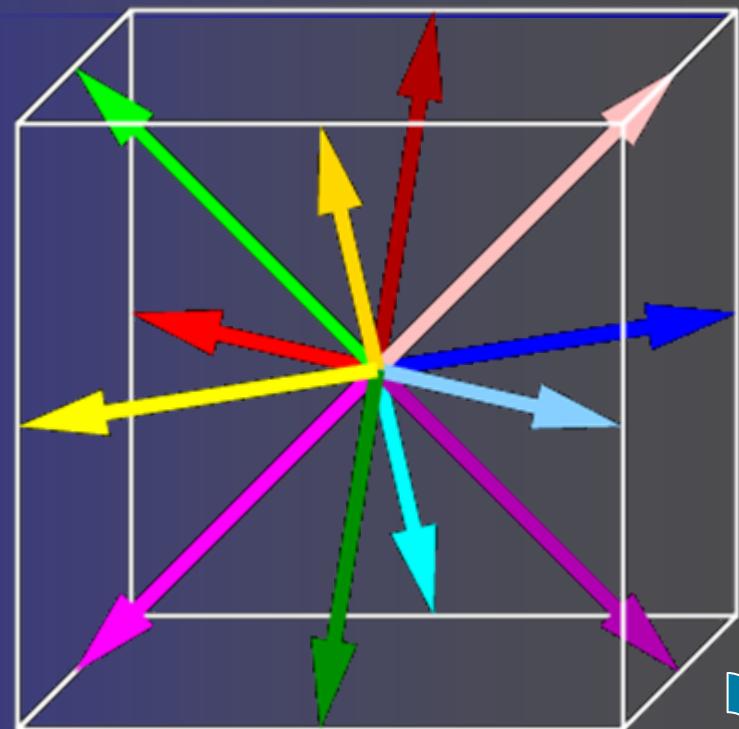


$$J_2/|J_1| < 3$$

T=0 semi classical Néel order



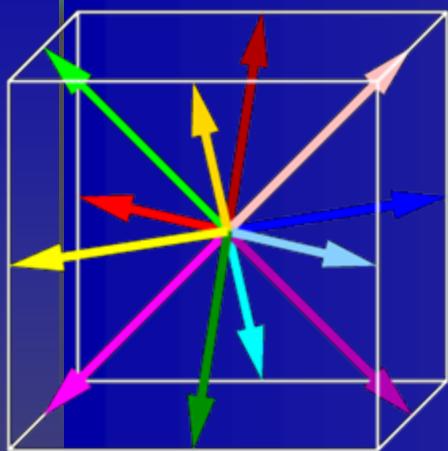
12 sub-lattice Néel order



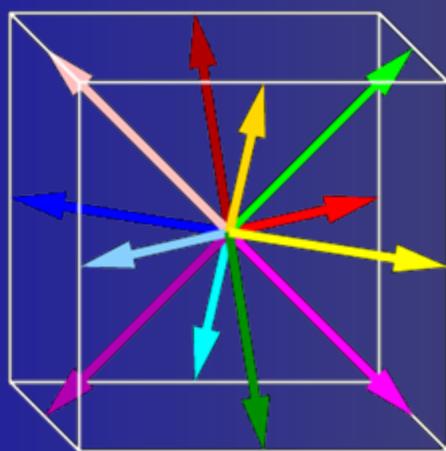
cuboctahedron symmetry of the order parameter

NO LRO in spin-spin correlations at T ≠ 0

# Chiral symmetry breaking (M.C. study - classical spins)

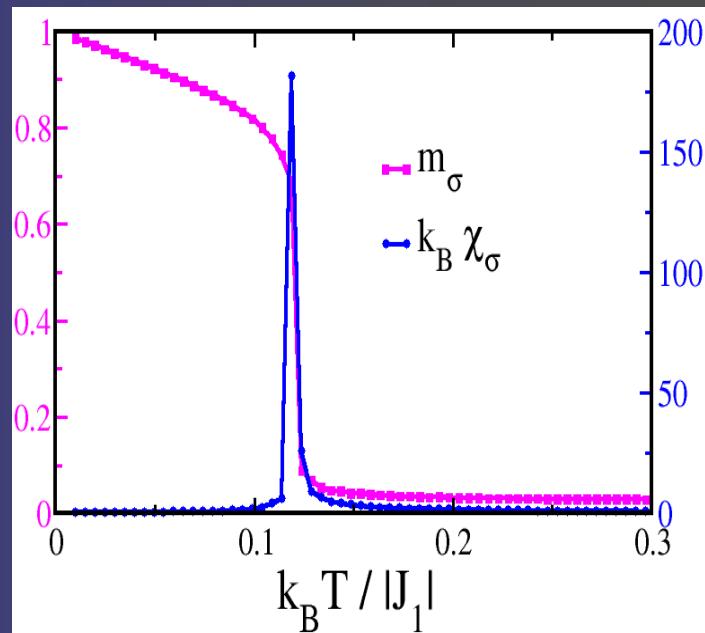


Scalar  
chirality     $\sigma = +1$



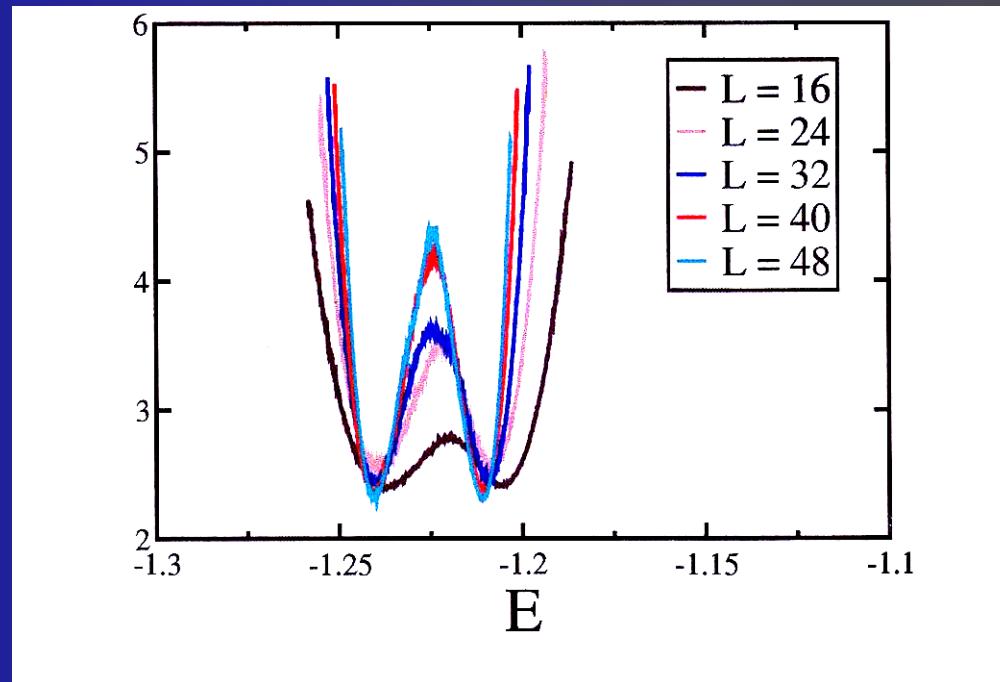
$\sigma = -1$

$N=768, J_2 / |J_1| = 0.38$



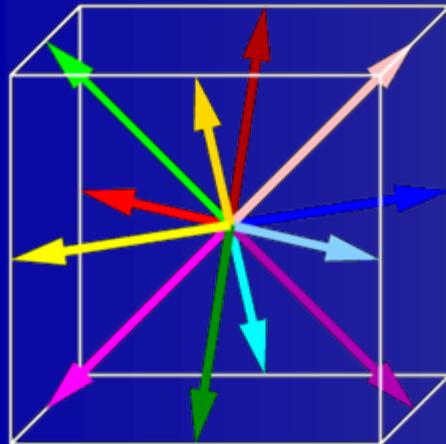
Weak universality (Suzuki 1984) ?

# Free energy histogram

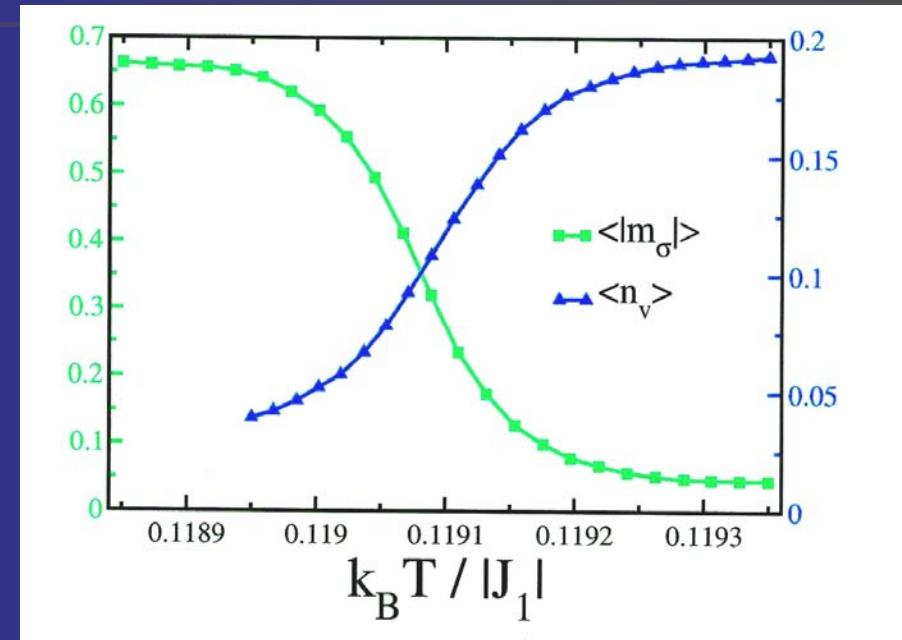
$$J_2 / |J_1| = 0.38$$


A very weak first order phase transition !

# First order chiral phase transition mechanism?



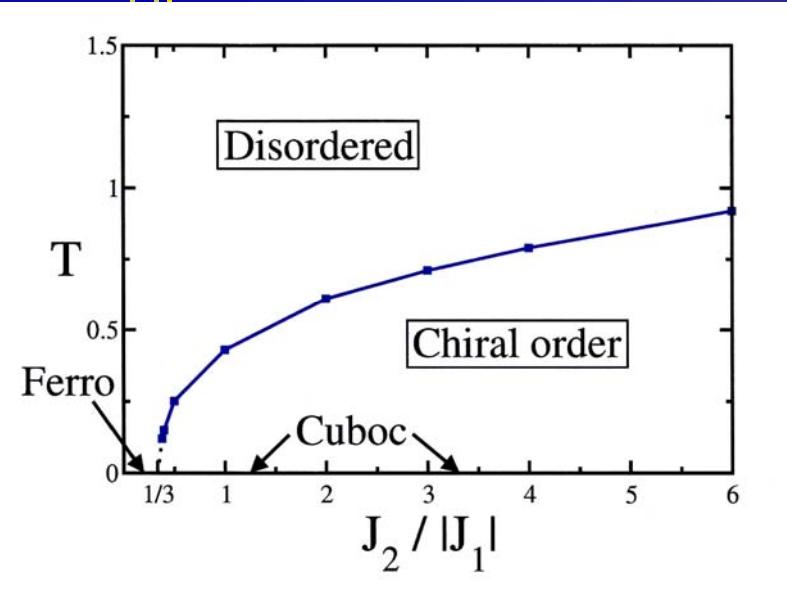
$O_3$  is completely broken  
 $Z_2$  vortices can be present



$$J_2/|J_1| = 0.38$$

At  $T \neq 0$  chirality disappears and  $Z_2$  vortices proliferate

# $T \neq 0$ Phase diagram of the F-AF model



The chiral phase transition:

- ✓ weakly first order at small  $J_2 / |J_1|$
- ✓ due to  $Z_2$  vortices
- ✓ going towards criticality when  $J_2 / |J_1|$  increases
- ✓ cross over from 1<sup>st</sup> to 2<sup>nd</sup> order depends on chem. pot. of vortices

May be not so rare in frustrated magnets (*Momoi et al PRL 97*)

# Conclusion of this 2<sup>nd</sup> part

- 2 new phases in the  $J_1 < 0 - J_2 > 0$  model on the kagomé lattice
  - A semi-classical chiral phase with no LRO in spins, but with chiral order at  $T \neq 0$  and a weekly first order phase transition driven by  $Z_2$  defects
  - A quantum gapped phase

*J.C. Domenge, P. Sindzingre, C. L. & L. Pierre: PRB '05.*

*L. Messio, P. Viot, C.L & L. Pierre (in prep.)*