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WARPED String

Compactifications

w/ Kachru & Polchinski hep-th/0105097

Motivation

- New idea on hierarchies:
different location \leadsto different 4d scales
- New and interesting phenomenology; string experiments?
 - KK modes
 - string scale effects
 - black holes
($\mu\text{grav} \times$)
- Abstract: examples of broad & rich classes of string compactifications

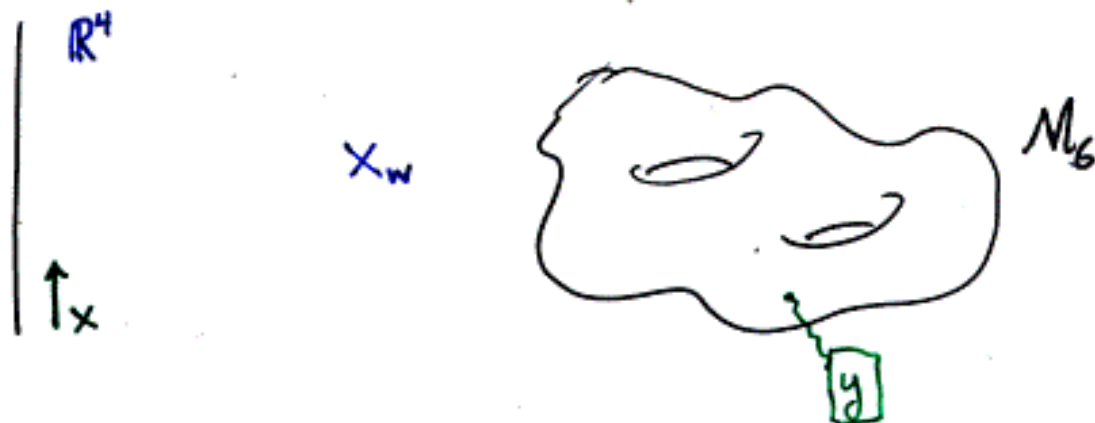
... other possibilities to explore

Outline

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1. Warped compactifications: generalities
2. Evading a no-go theorem
3. String solutions with hierarchies
4. Towards phenomenology
5. Conclusions and questions

1. Warped compactifications: generalities



Poincaré symmetry

$$ds^2 = e^{2A(y)} dx^2 + g_{mn}(y) dy^m dy^n$$

↑
redshift: Varying scale for 4d physics

4d gravity:

$$ds^2 = e^{2A(y)} \tilde{g}_{\mu\nu}(x) dx^\mu dx^\nu + g_{mn} dy^m dy^n$$

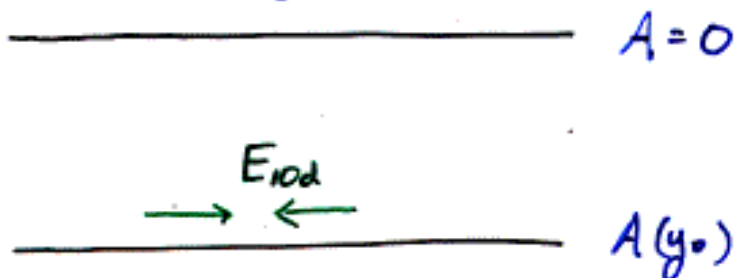
fluctuates

$$S_{10} \sim M_p^8 \int d^{10}x \sqrt{-g} R \sim M_p^8 \int d^6y \sqrt{g_6} e^{2A} \int d^4x \sqrt{-\tilde{g}} \tilde{R}(x)$$

- Measure 4d distances: $ds^2 = \tilde{g}_{\mu\nu} dx^\mu dx^\nu$
- $M_4^2 = M_p^8 \int d^6y \sqrt{g_6} e^{2A}$

↔ Define 4d Planck scale, 4d energies w.r.t. 10d observer at $A=0$

Consider scattering on a brane elsewhere



redshift:

$$E_{4d} = e^{A(y_0)} E_{10d}$$

↑
measure at LHC
TeV

↑
"true" scale for physics
 M_{sb}, M_{pe}

• mechanism for generating hierarchy:

$$m_{30} \sim M_{pe} \rightarrow m_4 \sim e^{A(y_0)} M_{pe}$$

• window to interesting physics @ \sim TeV

- KK modes
- string effects
- black hole creation (cf SGE Katz, th/0009176)

2. Evading a no go theorem

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e.g. IIB (similarly IIA, \dots)

Fields: g_{MN} , $\tau = C_0 + i e^{-\phi}$, $G_3 = F_3 - \tau H_3$, $\tilde{F}_5 = dC_4 + \dots$

Action:
$$S_{\text{IIB}} = \frac{1}{2\kappa_{10}^2} \int d^{10}x \sqrt{-g} \left(R - \frac{\partial_M \tau \partial^M \bar{\tau}}{2(\text{Im}\tau)^2} - \frac{G_3 \cdot \bar{G}_3}{12 \text{Im}\tau} - \frac{\tilde{F}_5^2}{4 \cdot 5!} \right)$$

$+ S_{\text{CS}} + S_{\text{loc}} \leftarrow \text{branes}$

Ansatz:

(Poincaré)

$$ds^2 = e^{2A(y)} \eta_{\mu\nu} dx^\mu dx^\nu + e^{-2A(y)} \tilde{g}_{mn} dy^m dy^n$$

$$\tau = \tau(y)$$

$$G_{(3)mnp} \neq 0$$

$$\tilde{F}_5 = (1 + *) [dx^0 \wedge dx^1 \wedge dx^2 \wedge dx^3]$$

"No go" (Maldacena - Nuñez)

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Einstein's eqn:

$$R_{MN} = \chi_{10}^2 \left(T_{MN} - \frac{1}{8} g_{MN} T \right)$$

$\mu\nu$ (4d):

$$\tilde{\nabla}_6^2 A = \frac{e^{-2A} G \cdot \bar{G}}{48 \text{Im}\tau} + \frac{e^{-6A} (\nabla d)^2}{4} + \frac{\chi_{10}^2 e^{-2A} (T_m^m - T_\mu^\mu)_{loc}}{8}$$

$\forall \quad \forall \quad \forall$
 $0 \quad 0 \quad 0$

positive term
 $p \leq 7$

$\int_{M_6} :$

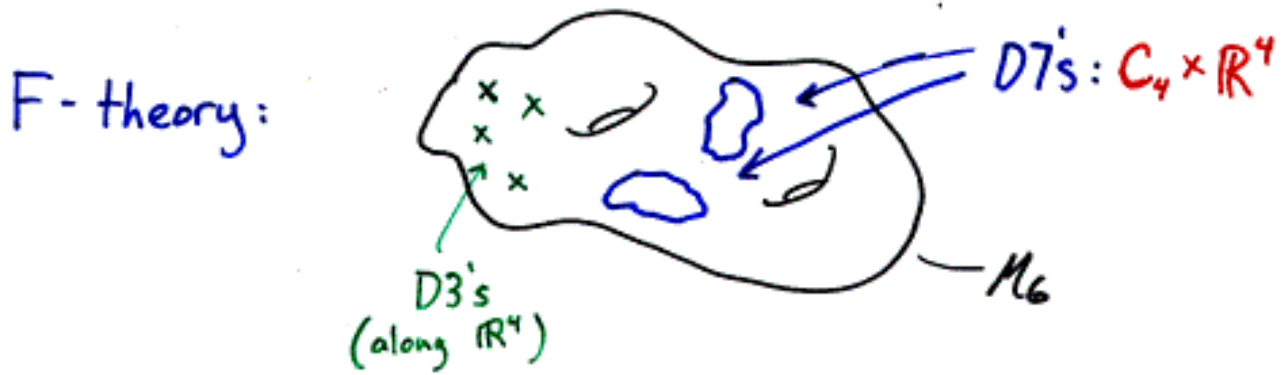
$$0 = \int_{M_6} \text{RHS} \geq 0$$

\Rightarrow each term = 0,
 $A = \text{const}$

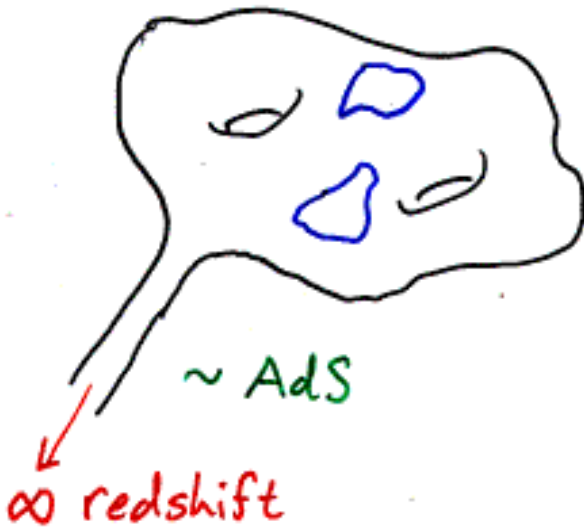
Evasion: String theory has **negative tension objects**

- orientifold planes
- induced -ve D3 tension in F thy.

E.g. Chan, Paul, H. Verlinde



$$S_{D7} = S_{DBI} + \dots - \mu_i(\text{const}) \int_{C_4 \times \mathbb{R}^4} d^4x \sqrt{-g} \text{Tr}(R_\wedge * R)$$

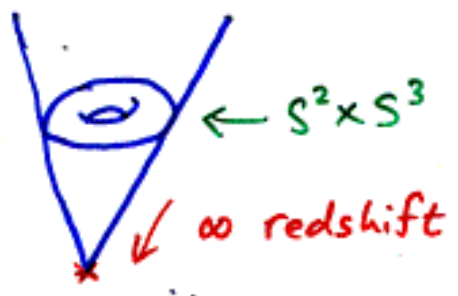


hierarchy -
but arbitrary

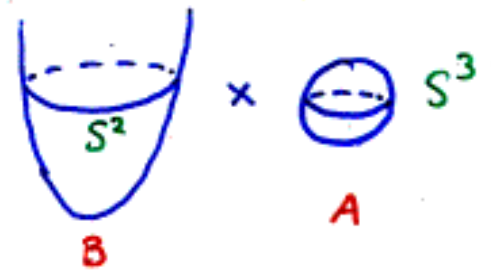
3. String solutions with hierarchies

Klebanov - Strassler:

D3 branes at conifold



↓ deform



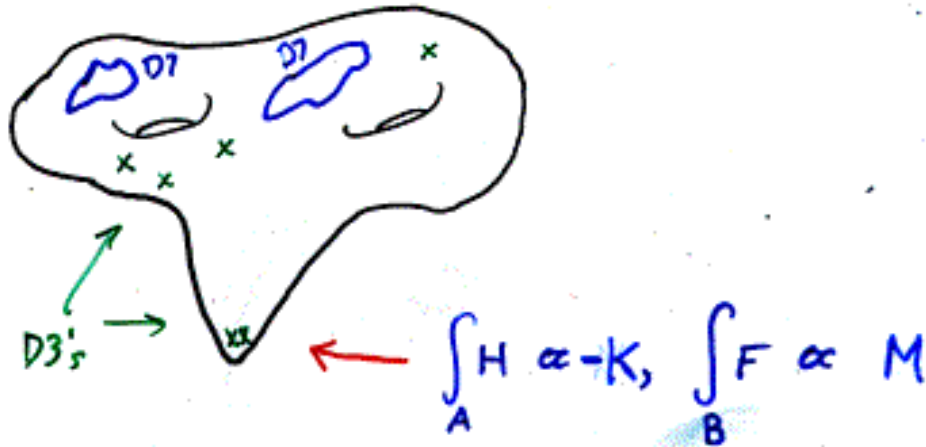
+ Fract. branes

- smooth
- finite & determined redshift
- fluxes replace branes

$$\int_B H_3 = -4\pi^2 \alpha' K \quad \int_A F_3 = 4\pi^2 \alpha' M$$

Branes + fluxes in compact setting?

F-theory (or orientifold):



Constraints:

$$d\tilde{F}_5 = H_3 \wedge F_3 + 2\kappa_{10}^2 T_3 \rho_3^{loc}$$

↔

$$MK + N_{D3} = \frac{\chi(X_8)}{24}$$

Tension ✓

A general class of solutions

(generalizes Graña - Polchinski)

$$ds^2 = e^{2A} dx_4^2 + e^{-2A} \tilde{g}_{mn} dy^m dy^n$$

$$\tilde{F}_5 = (1 + *) d\tilde{y}_\alpha dx^0 dx^1 dx^2 dx^3$$

Einstein + Bianchi:

$$\tilde{\nabla}_6^2 (e^{4A} - \alpha) = \frac{e^{2A}}{6\text{Im}\tau} |iG_3 - *G_3|^2 + e^{-6A} |\partial(e^{4A} - \alpha)|^2$$

$$+ \frac{\kappa_{10}^2 e^{2A}}{2} \left[\underbrace{(T_m^m - T_\mu^\mu)^{\text{loc}} - 4T_3 \rho_3^{\text{loc}}}_{\text{V}}$$

Therefore, if $\underbrace{\quad}_{\text{V}} = 0$ (\sim BPS)

then:

- $= 0$
- $\alpha = e^{4A}$
- $*G_3 = iG_3$

Remaining IB EOM solved w/

- $\tau(y), \tilde{g}_{mn}(y)$ determined by F-thy
- $$\tilde{\nabla}_6^2 e^{-4A} = -e^{2A} \left[\frac{G \cdot \bar{G}}{12 \text{Im}\tau} + \frac{\chi_{10}^2}{2} (T_m^m - T_\mu^\mu)^{loc} \right]$$

$$*G_3 = iG_3 : \quad \epsilon_{123}{}^{123} = -i$$

- implies G_3 is $(0,3)$ or $(2,1)$

- for given $\int_A F \propto M$ $\int_B H \propto -K$

fixes moduli

in particular, \Rightarrow deformation away
from conifold \sim KS

4d, N=1 SUSY thy

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- gravity
- gauge thy. on branes
- light scalar superfields:
 - $h_{1,1}$ Kähler moduli ρ_i
(e.g. take $=1$: scale of M_6)
 - $h_{2,1}$ Complex moduli z^α
 - τ (in orientifold case)

Action: dim. red.

Kähler potential:

$$\chi = -3 \ln(\rho - \bar{\rho}) - \ln(\tau - \bar{\tau}) - \ln \int_{M_6} \Omega_{3^{\wedge}} \bar{\Omega}_3 + \text{const}$$

\uparrow
 $(3,0)$ on CY

Superpotential:

$$W(z^\alpha, \tau) = \int \Omega_{3^{\wedge}} G_3 \quad (\text{Gukov, Vafa, Witten})$$

note: ρ indep.

Check:

$$0 = D_\alpha W = \partial_\alpha W + \partial_\alpha \mathcal{K} W \stackrel{\text{ex.}}{=} \int_{M_6} G_{3\alpha} \chi_\alpha$$

(2,1) forms

$$0 = D_\tau W = \partial_\tau W + \partial_\tau \mathcal{K} W \stackrel{\text{ex.}}{\propto} \int_{M_6} \bar{G}_3 \wedge \Omega$$

$$\Rightarrow G_3 = (2,1) + (0,3) \quad \checkmark$$

F-theory generalization

$$K = -\ln \int_{X_8} \Omega_4 \wedge \bar{\Omega}_4$$

$$W = \int_{X_8} \Omega_4 \wedge G_4$$

w/(locally) $G_4 = -\frac{G_3 d\bar{w}}{\tau - \bar{\tau}}$ + h.c. ← Fiber coord

Can now generate hierarchy:

Near conifold:

$$W_1^2 + W_2^2 + W_3^2 + W_4^2 = Z$$

$$\int_A \Omega = Z$$

$$\int_B \Omega = \mathcal{Y}(z) = \frac{z \ln z}{2\pi i} + \text{holo.}$$

Fluxes:

$$\int_A F \propto +M$$

$$\int_B H \propto -K$$

$$(G_3 = F_3 - \tau H_3)$$

ex

\rightsquigarrow

$$W = \int \Omega \wedge G_3 \propto M \mathcal{Y}(z) - K \tau z$$

$$0 = D_z W \sim \frac{M \ln z}{2\pi} + \frac{K}{g_s}$$

this implies:

$$z \sim e^{-\frac{2\pi K}{M g_s}}$$

(also need to fix τ ; other fluxes $\rightsquigarrow W \rightarrow W + \tilde{W}(\tau)$)

What this means:



$$e^{A_{\min}} \sim z^{1/3} \sim e^{-\frac{2\pi K}{3Mg_s}}$$

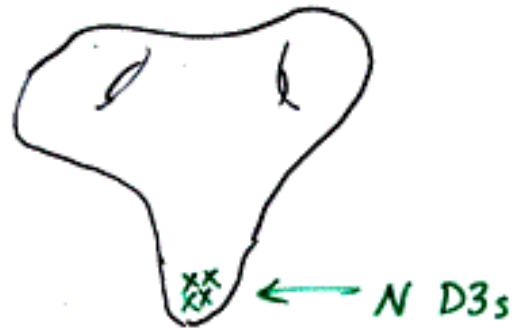
so, by a (discrete!) choice of fluxes,

$$\text{eg. } M=1, \frac{K}{g_s} \sim 8$$

can generate TeV from M_{pl}

4. Towards phenomenology

Gauge dynamics from mobile D3's: (generically required)



4d fields:

- $g_{\mu\nu}$
- A_{μ}^I $SU(N)$
- Z^{α}, τ fixed by flux/pot.
- P, X_m not fixed
 ↗
 brane
 positions

Indeed,

$$\partial_\rho W = 0, \quad \kappa = -3 \ln(\rho - \bar{\rho})$$

gives

$$\mathcal{V} = e^\kappa \left(\underset{\substack{\uparrow \\ z, \tau}}{\kappa^{i\bar{j}} D_i W \bar{D}_{\bar{j}} W} + \kappa^{\rho\bar{\rho}} |D_\rho W|^2 - 3|W|^2 \right)$$

cancel

$$= 0 \quad \text{indep. of } \rho.$$

"No scale" (e.g. also Het, ...)

SUSY broken:

$$0 \neq e^{\kappa/2} W = m_{3/2} \propto \frac{1}{\rho^{3/2}}$$

- α', g_s corrections should fix ρ, X_m
- other branes/fluxes might classically fix all moduli
(SG, SK, & JP in progress)

Conclusion & open questions

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Have constructed a class of classical string solutions corresponding to warped compactifications

- large hierarchies generated by moderate discrete fluxes
- $N=1 \rightarrow N=0$ SUSY
- $\Lambda = 0$

Questions:

- can we fix remaining moduli? (W.I.P.)
- can we build the standard model?
- understanding phenomenological consequences
 - KK, etc. prod
 - (- μ grav)
 - string scale effects
 - black hole production