

Ecosystem Engineers, Landscape Diversity and Species Richness: A Pattern Formation Approach

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Outline

- o Vegetation patterns - mechanisms
- o Mathematical models of vegetation patterns
- o Applying the models to "ecosystem engineers"
- o Relating species richness to pattern formation
- o Conclusion



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Vegetation on hills and semi-arid region is self-organized in the perpendicular to precipitation direction

Vegetation bands on hillsides (Valentin, d'Herbes, 1989)

The mechanism

Precipitation

infiltration

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positive feedback mechanisms between biomass and water

(1) Increased infiltration

Precipitation

infiltration

Biomass ↑

Soil water ↑

Water infiltration ↑

(2) Water up take by roots

Precipitation

Water uptake ↑

Biomass ↑

Root length ↑

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Lefever and Lejeune (1997); Klausmeier, (1999); HilleRisLambers et al. (2000), Okayasu and Aizawa (2001); Rietkerk et al. (2002); Lejeune et al. (2002); Shnerb et al. (2003).

Reproduce observed behaviors

Make predictions

Shed new light on ecological processes

Background equations:
 $\frac{\partial b}{\partial t} = b(1 - \dots)$
 $\frac{\partial w}{\partial t} = 1 - (1 - \rho b)w - w^2n + \delta_1 \nabla^2 w - \delta_2 \nabla^2 n$
 $\frac{\partial h}{\partial t} = \nabla^2 (h^2) + \nabla h \cdot \nabla S$

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Hardenberg, Meron, Shachak, Zarmi, PRL (2001)

$n(x,t)$ - Plant biomass density
 $w(x,t)$ - Soil water density

Positive feedback terms

Biomass growth rate

Maximum standing biomass

Mortality, grazing

$$\frac{\partial n}{\partial t} = \frac{\gamma w}{1 + \sigma w} n - n^2 - \mu n + \nabla^2 n$$

← Seed dispersal

Biomass decrease water loss

Evaporation

Transpiration

Water transport (Darcy's law)

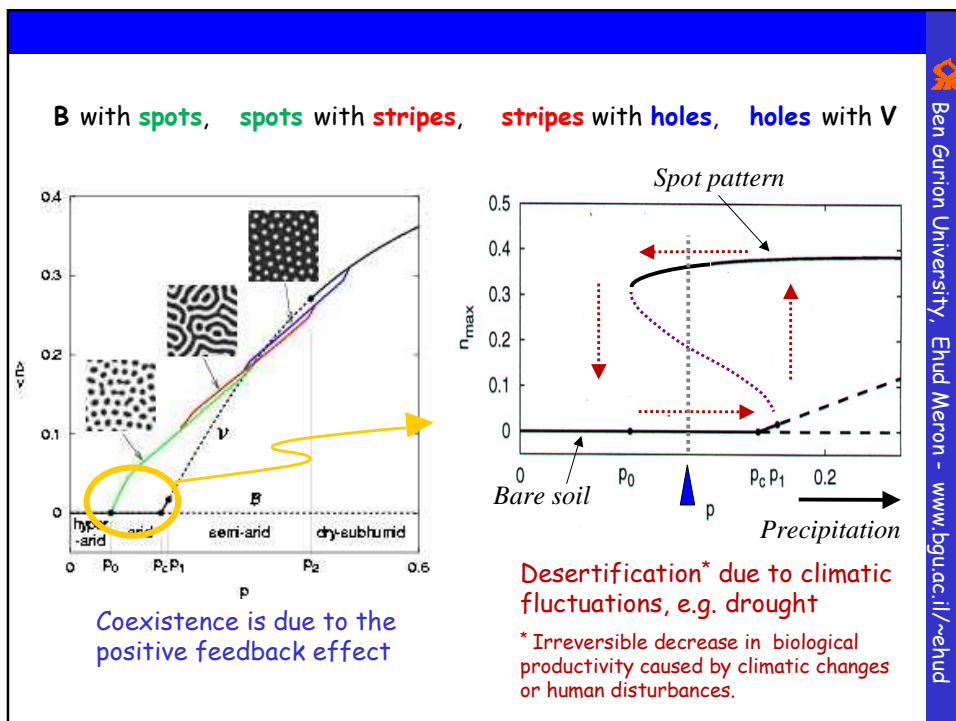
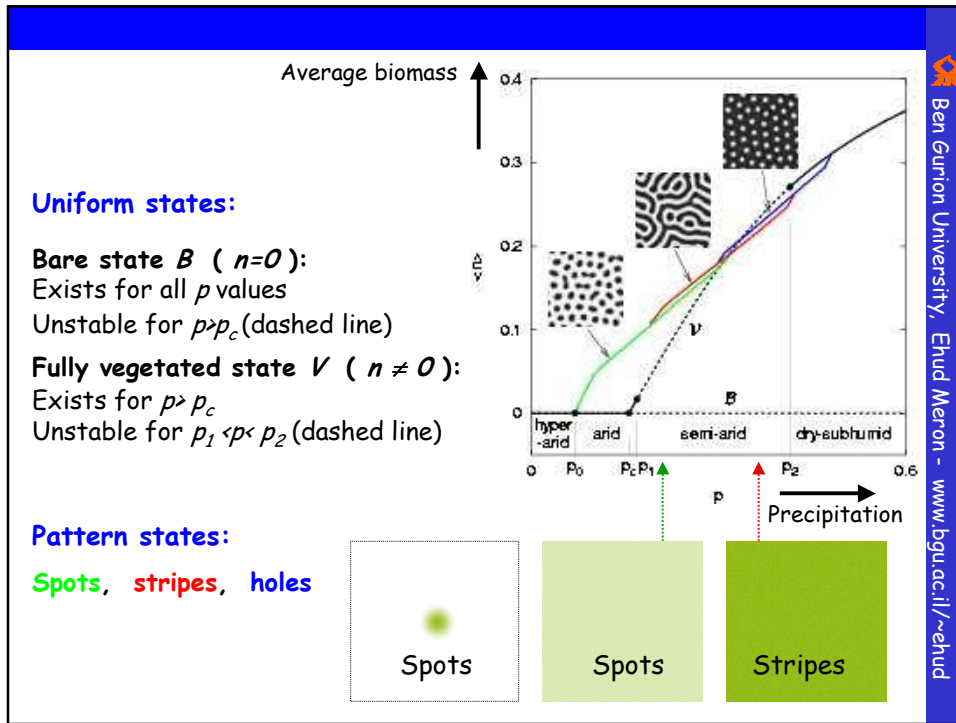
Water uptake by roots

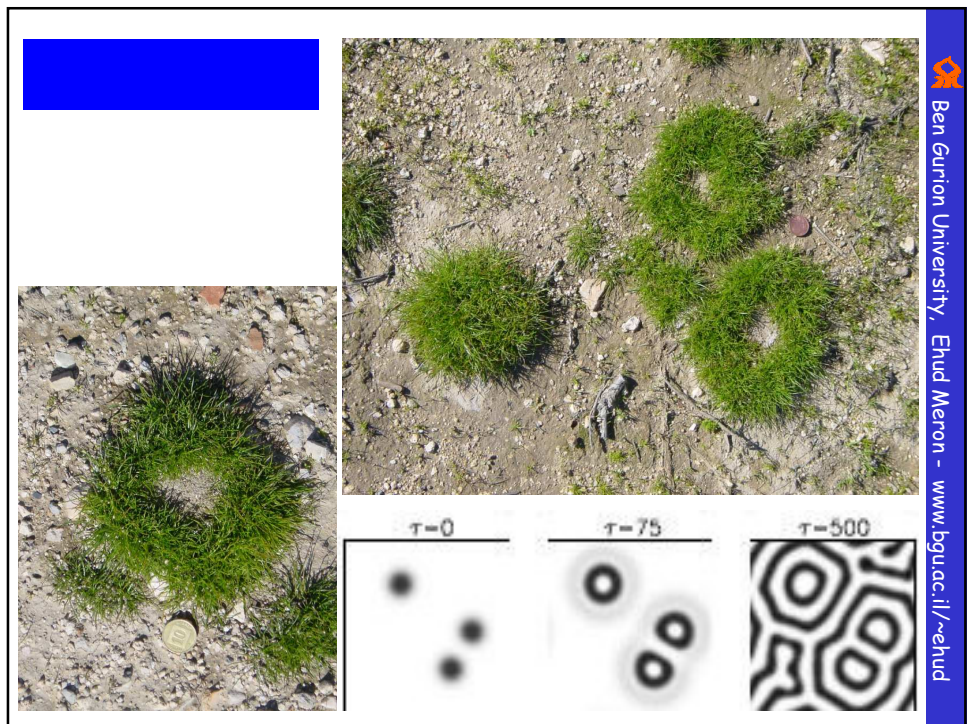
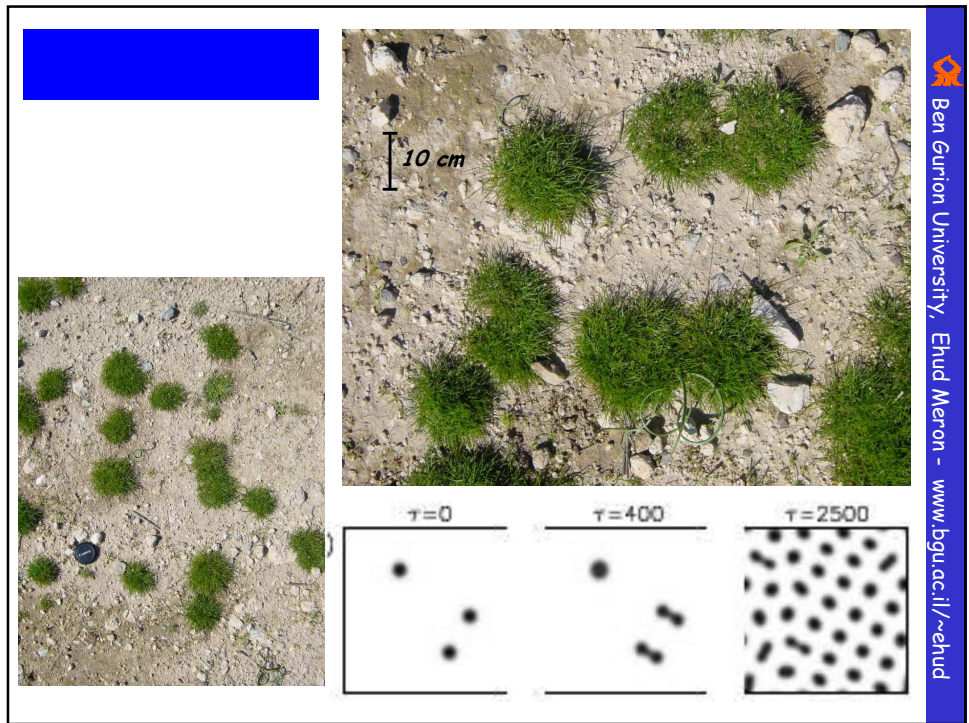
Increased infiltration

Ecological & physical input - small scale

$$\frac{\partial w}{\partial t} = p - (1 - \rho n)w - w^2n + \delta_1 \nabla^2 w - \delta_2 \nabla^2 n$$

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Spots **Stripes** **Holes**

Explicit modeling of the two positive feedback mechanisms

$b(x,t)$ - Plant biomass density
 $w(x,t)$ - Soil water density
 $h(x,t)$ - Surface water height

Okayasu and Aizawa (2001); Rietkerk et al. (2002)

$$\frac{\partial b}{\partial t} = b(1-b) \int_{\Omega} K_b(\vec{r}, \vec{r}') w(\vec{r}') d\vec{r}' - \mu b + \delta_b \nabla^2 b$$

$$\frac{\partial w}{\partial t} = I - (1-\rho b)w - \beta w \int_{\Omega} K_w(\vec{r}, \vec{r}') b(\vec{r}') d\vec{r}' + \delta_w \nabla^2 w$$

$$\frac{\partial h}{\partial t} = p - I + \nabla^2 (h^2) + 2\nabla h \cdot \nabla \zeta + 2h \nabla^2 \zeta$$

$$K_w(\vec{r}, \vec{r}') = \exp\left\{-\frac{|\vec{r}-\vec{r}'|^2}{2\sigma_0[1+\eta b(\vec{r}')]^2}\right\}, \quad K_b(\vec{r}, \vec{r}') = \exp\left\{-\frac{|\vec{r}-\vec{r}'|^2}{2\sigma_0[1+\eta b(\vec{r})]^2}\right\}$$

$I = \alpha h(\vec{r}, t) \frac{b(\vec{r}, t) + \zeta}{b(\vec{r}, t) + k}$

PF 1: Increased infiltration PF 2: Water uptake by roots

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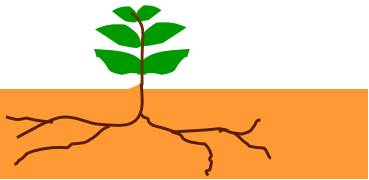
$\eta = dL/db$

– the rate at which the roots extend in response to plant growth

f – parameterizes the dependence of the infiltration rate I on biomass b :

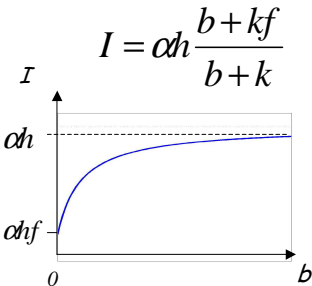
$f=I$ no biomass dependence

$f \ll I$ infiltration rate increases dramatically with biomass \rightarrow



$L = \sqrt{2\sigma_0 [1 + \eta b(\bar{r})]}$

$I = \alpha h \frac{b + kf}{b + k}$



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Uniform states (linear stability analysis):

Bare state ($b=0$):
 Exists for all p values
 Unstable for $p > p_c$ (dashed line)

Fully vegetated state ($b \neq 0$):
 Exists for $p > p_c$
 Unstable for $p_c < p < p_2$ (dotted line)

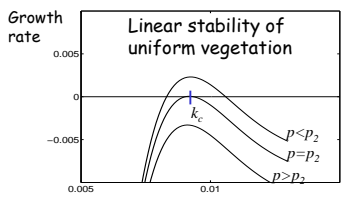
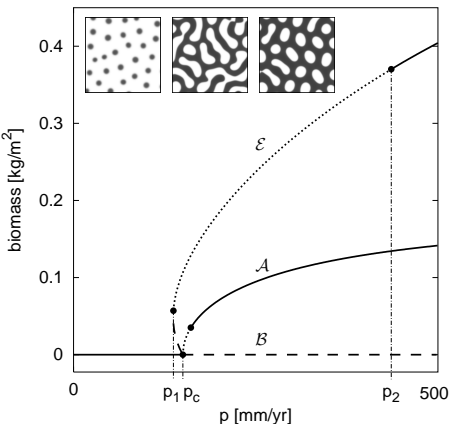
Pattern states (numerical simulations):
 Spots, stripes, holes

Each of the positive feedbacks alone leads to pattern formation

Instability of bare soil becomes subcritical when $R = \frac{2\eta}{1-\rho+\beta} > 1$


Growth rate

Linear stability of uniform vegetation

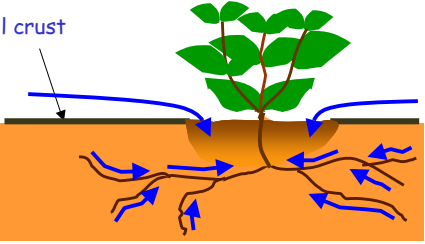
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Ecosystem engineers are key species which modulate the landscape, organize the flow of resources, and strongly affect the number of other species in the ecosystem.




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Engineering:
Cyanobacteria - form soil crusts which reduce infiltration
Shrubs - prevent the growth of soil crusts and increase infiltration



The combined engineering effect - accumulation of soil water. Can it create habitats for other species (e.g. annual plants) ?

Resilience:
Disturbances may destroy the fragile crust. What controls the resilience of the system, is it recoverable ?



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$$\frac{\partial b}{\partial t} = b(1-b) \int_{\Omega} K_b(\bar{r}, \bar{r}') w(\bar{r}') d\bar{r}' - \mu b + \nabla^2 b$$

$$\frac{\partial w}{\partial t} = I - (1-\rho b)w - \beta b \int_{\Omega} K_w(\bar{r}, \bar{r}') b(\bar{r}') d\bar{r}' + \delta_w \nabla^2 w$$

$$\frac{\partial h}{\partial t} = \nabla^2 (h^2) + \nabla h \cdot \nabla \zeta + h \nabla^2 \zeta + p - I$$

$$K_b(\bar{r}, \bar{r}') = \exp\left\{-\frac{|\bar{r}-\bar{r}'|^2}{2\sigma_0[1+\eta b(\bar{r})]^2}\right\}, \quad K_w(\bar{r}, \bar{r}') = \exp\left\{-\frac{|\bar{r}-\bar{r}'|^2}{2\sigma_0[1+\eta b(\bar{r}')]^2}\right\}$$

1. Associate b with the shrub biomass
2. Model the existence of crust by $f \ll 1$

$$I = \alpha h \frac{b + kf}{b + k}$$

η

$\eta = 12 \ (\gg 1)$

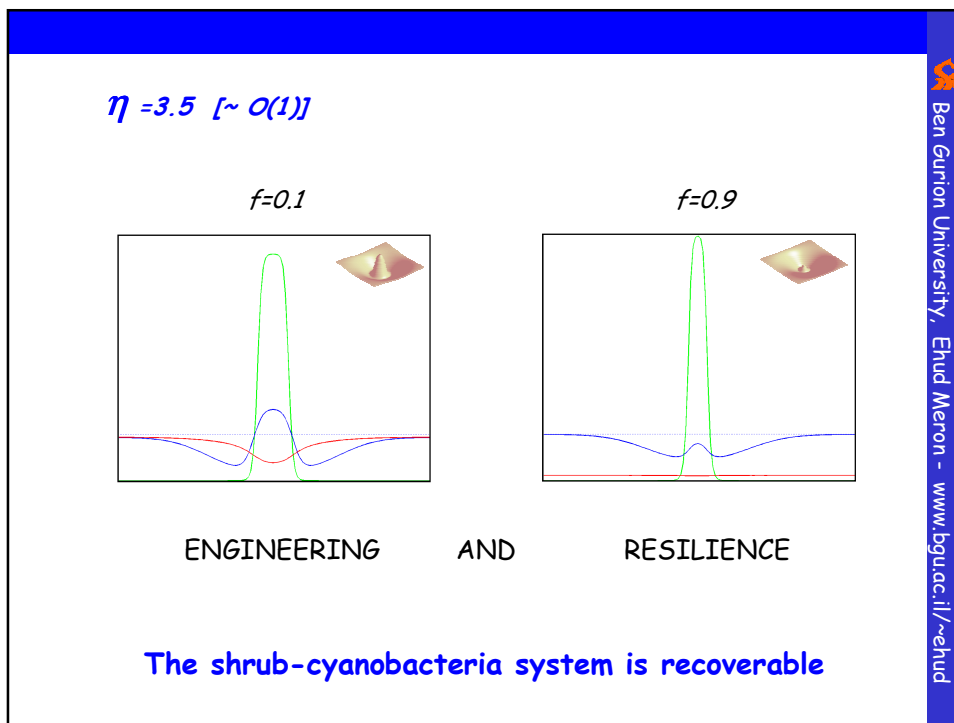
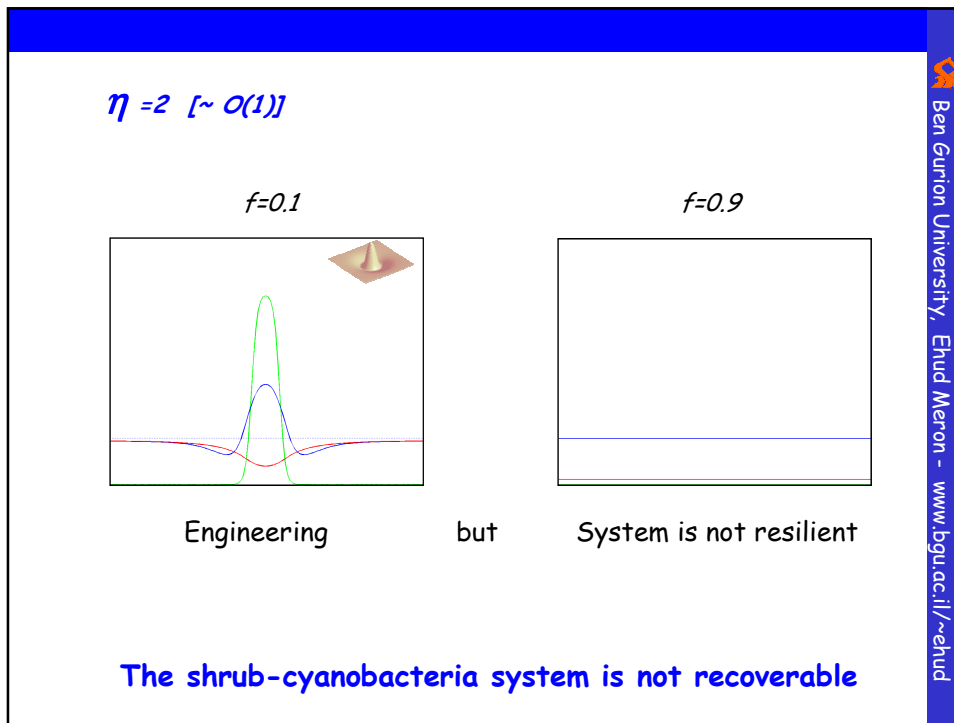
	Biomass
	Soil water
	Surface water

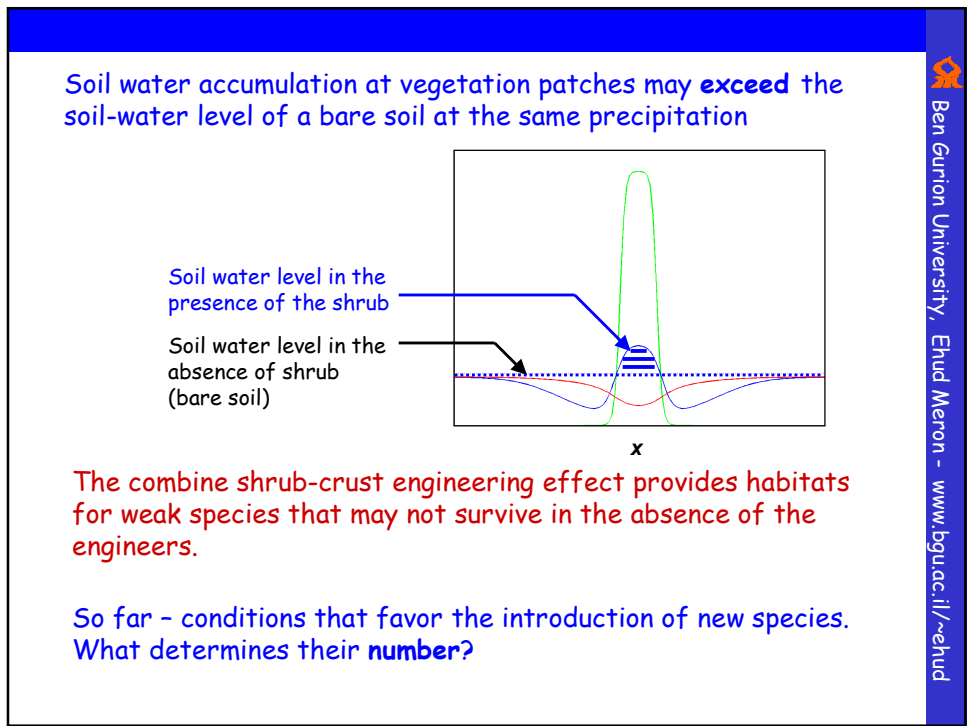
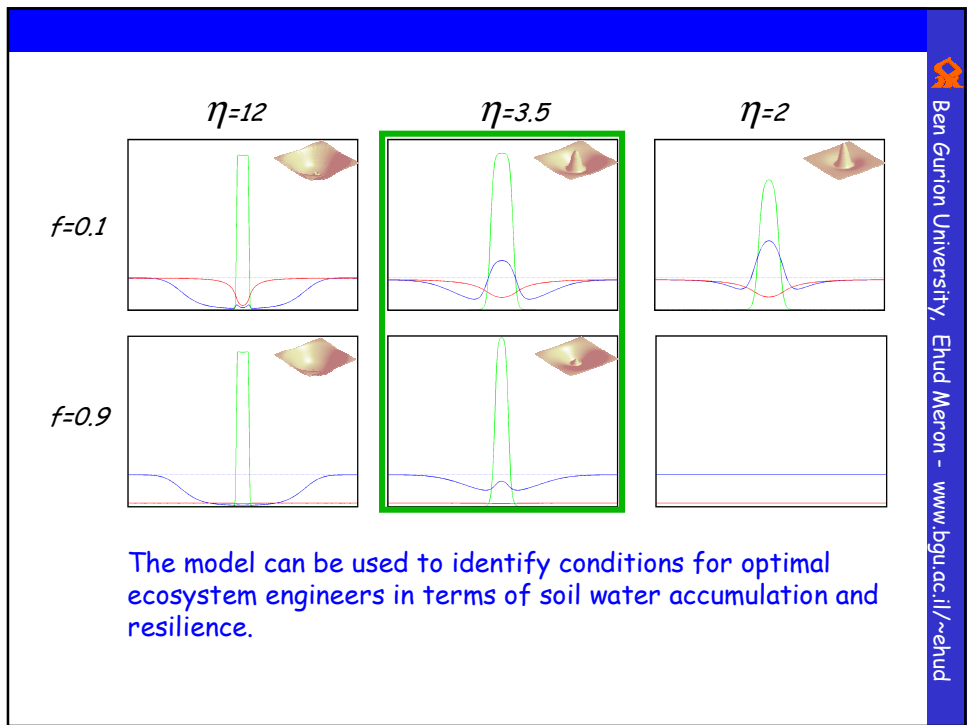
$f=0.1$

No engineering

$f=0.9$

System is resilient





Niche theory in ecology: the more diverse the landscape the more habitats or growth niches it provides and the richer the species that can be accommodated.

Landscape diversity in our case is determined by the spatial patterns the shrub forms.

The model suggests two mechanisms for pattern diversity:

1. Bistability of states:
 - ← Bistability of bare soil and spots
 - ← Bistability of spots and stripes
2. Spatial chaos (yet to be found)

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Ecosystems are going today through unprecedented loss of species and their habitats in response to environmental changes and human disturbances.

The model suggests a new mechanism:

Transitions between states or patterns of the ecosystem engineer that involve habitat loss, induced by climatic changes or human activities.

Example:
Spots → bands
 on a slope

Counterintuitively species loss may result from *increasing precipitation*

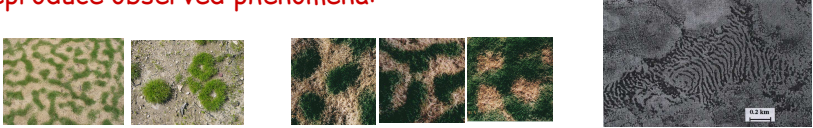
Soil-water redistributions creating habitats →

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Conclusion

The new models:

Reproduce observed phenomena:



Make specific predictions:

- o A universal sequence of states along the rainfall gradient - bare soil, spots, stripes, gaps, uniform vegetation.
- o Bistability ranges.

Shed new light:

- o Desertification & recovery as hysteresis loop
- o A novel mechanism of species loss events - state transitions of the ecosystem engineer

Test predictions in controlled experiments

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