



# Energetic footprints of quantum noise

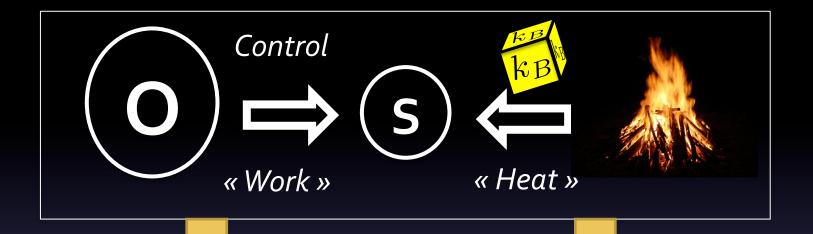
Alexia Auffèves CNRS & Université Grenoble-Alpes

Quantum Thermodynamics conference, KITP, June 25-29, 2018





### Thermodynamics and noise

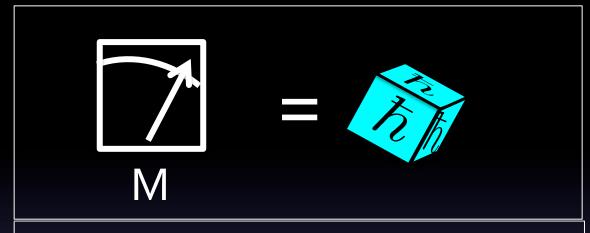


Work extraction from thermal noise => Heat engines

Thermal noise =>
Irreversibility &
Fundamental bounds

- > Thermodynamics = Theory of control against noise
  - > Thermodynamics is based on randomness

### Measurement induced quantum noise

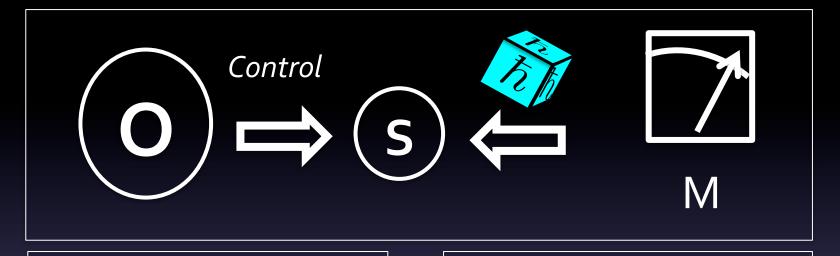


Quantum measurement backaction => Genuine quantum randomness and quantum noise

Quantum time arrow, quantum heat

- > Forget about temperature!
- Rebuild thermodynamics on quantum measurement

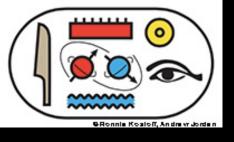
#### Quantum measurement based thermodynamics



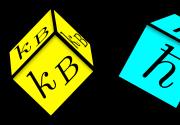
Work extraction from quantum fluctuations?

**Quantum** fundamental bounds?

Energetic and entropic footprints of quantum control?

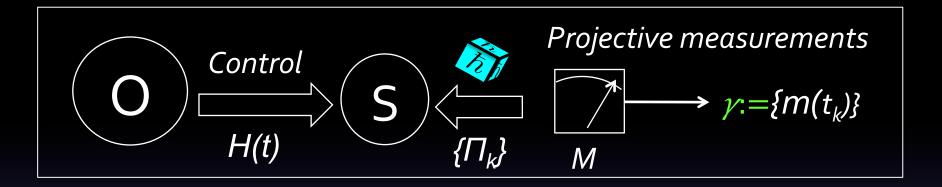


### Outline



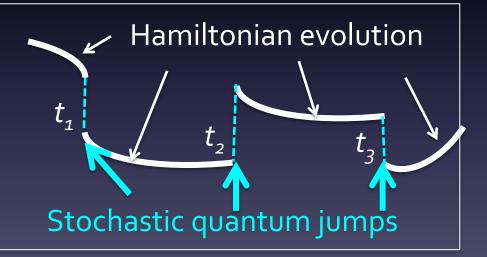
- Introduction: Rebuilding quantum thermodynamics on quantum measurement
- A measurement-powered quantum engine
- Work cost of quantum control
- Conclusion Outlook

### Scenery and definitions



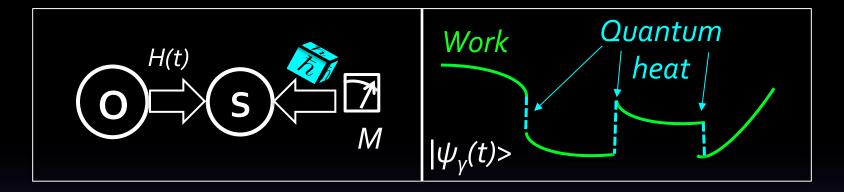
- Pure initial state  $|\psi(t_o)\rangle$
- Read measurement outcomes:

Stochastic quantum trajectory  $|\psi_{\nu}(t)\rangle$ 



- Unread measurement outcomes :
- $|\psi(t_o)\rangle < \psi(t_o)| \rightarrow \rho(t) = \sum_{\gamma} P[\gamma] |\psi_{\gamma}(t)\rangle < \psi_{\gamma}(t)|$

#### First Law



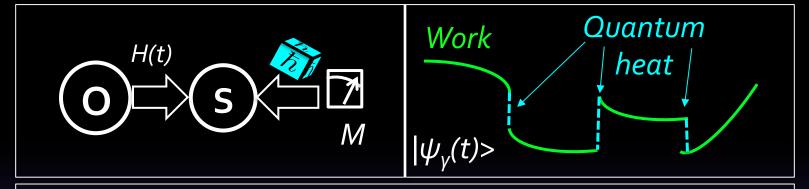
#### Read measurement outcomes

- Internal energy:  $U_{\gamma}(t) := \langle \psi_{\gamma}(t) | H(t) | \psi_{\gamma}(t) \rangle$
- Work:  $W[\gamma](t_k -> t_{k+1}) := U_{\gamma}(t_{k+1} -) U_{\gamma}(t_k)$
- Quantum heat:  $Q_q[\gamma](t_k) := U_{\gamma}(t_k^+) U_{\gamma}(t_k^-)$
- $\Delta U_{\gamma} = W[\gamma] + Q_{q}[\gamma]$

#### **Unread measurement outcomes**

- Work : Energy transfers during unitaries
- Quantum heat: Energy transfers during non-unitaries

#### Second Law



#### Stochastic entropy production

- $\Delta_i S[\gamma] := log(P_F[\gamma]/P_B[\gamma_r])$  with  $\gamma := \{m(t_k)\}$ ,  $\gamma r := \{m(t_{N-k})\}$ 
  - $P_{F}[\gamma] = p_{o}(m(t_{o})) | < m(t_{k+1}) | G | m(t_{k}) > |^{2}$
  - $P_B[\gamma_r] = p_N(m(t_N)) | < m(t_{k+1}) | G^+ | m(t_k) > |^2$
  - ➤ G: propagator

$$=> \Delta_i S[\gamma] = - log(p_N(m(t_N)) + log(p_o(m(t_o)))$$

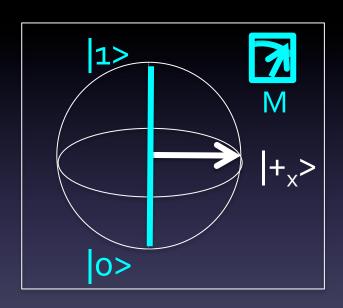
#### Mean entropy production

•  $<\Delta_i S[\gamma]> = \Delta S_{VN}$  with  $S_{VN} = -Tr[\rho \log \rho]$  Von Neumann entropy

### Meet the quantum heat

**System**: a Qubit,  $H=[hv_0/2] \sigma_{Z}$ 

**Transformation:** (i) Preparation in  $|+_x\rangle$  (ii) Measurement of  $M=\sigma_z$ 

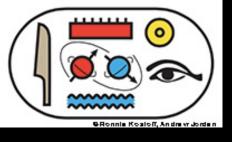


#### 2 stochastic trajectories:

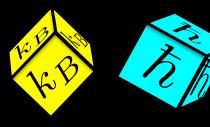
- $\Gamma_1 = [|+_{x}>, |0>]$
- $\bullet \quad \Gamma_2 = [|+_{\times}\rangle, |1\rangle]$

#### **Energetic balance**

- $\triangleright$  Initial energy  $U_i = 0$
- Final energy  $U_f = +/- hv_o/2$
- $\triangleright$   $\Delta U[\gamma] = +/-hv_o/2 = Q_q[\gamma]$
- Energetic footprint of quantum noise: Quantum heat
- A purely quantum term due to measurement backaction



### Outline

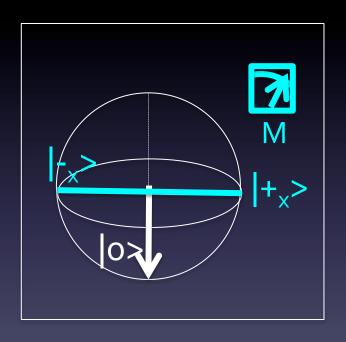


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#### Meet the quantum heat (II)

**System**: a Qubit,  $H=[hv_0/2] \sigma_{Z}$ 

**Transformation:** (i) Preparation in  $|o\rangle$  (ii) Measurement of  $M=\sigma_x$ 



#### 2 stochastic trajectories:

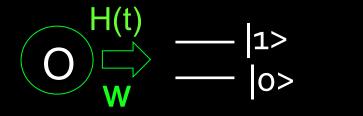
- $\Gamma_1 = [|0\rangle, |+_{\chi}\rangle]$
- $\Gamma_2 = [|0\rangle, |-\chi\rangle]$

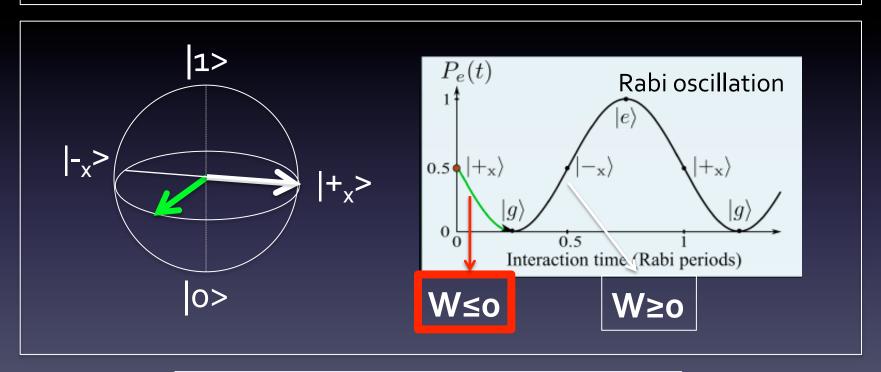
#### **Energetic balance**

- ightharpoonup Initial energy  $U_i = -hv_0/2$
- $\rightarrow$  Final energy  $U_f = o$
- $\rightarrow$   $<\Delta U[\gamma]> = hv_0/2 = <Q_q[\gamma]>$
- [M,H]≠o => Quantum heat is transferred **on average**
- Let us use this property to build a quantum engine

#### Basic mechanism

A qubit exchanges work with a resonant driving field

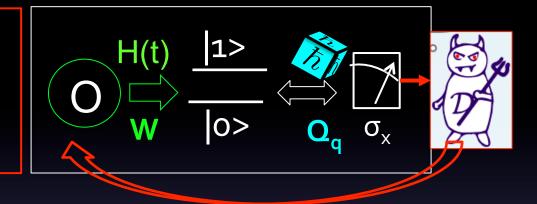




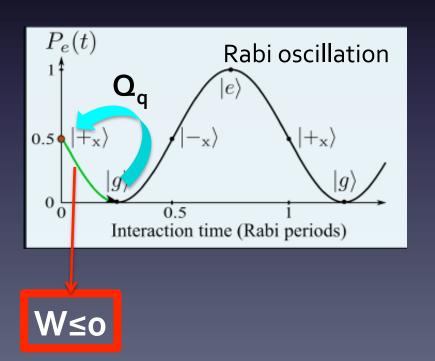
- |+<sub>x</sub>> = good for work extraction ©
- |-x> = bad for work extraction  $\odot$

#### Basic mechanism

- Solution: Stabilize the qubit in |+x>
- $\triangleright$  Measurement of  $\overline{\sigma_X}$
- $\rightarrow$  Feedback in  $|+_{x}>$

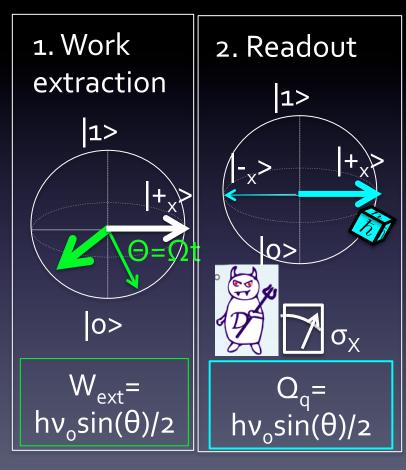


- New quantum Maxwell's demon experiment
- Energy <Q<sub>q</sub>> is extracted from the measurement and converted to work <W>

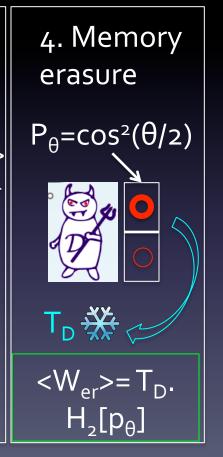


#### Measurement powered engine (MPE)

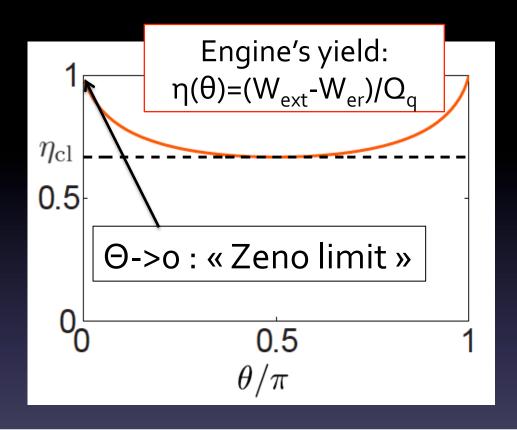
o. Initialize in  $|+_x>$ , couple to a resonant field







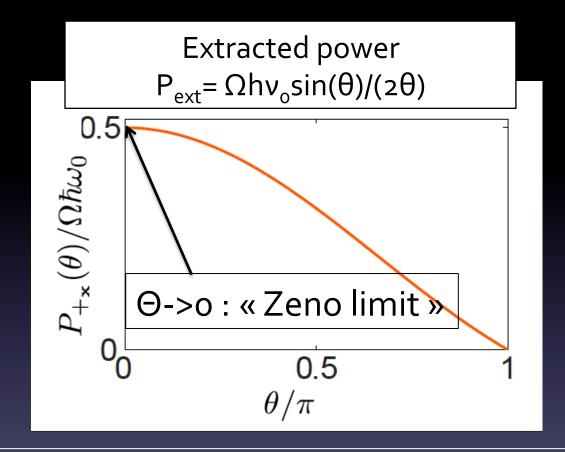
### MPE performances: Yield



#### **Zeno limit:**

- Qubit « frozen » in the |+√> state ☺
- $W_{ext}$  ->h $v_0\theta/2$ ;  $W_{er}\approx\theta^2\ln(\theta)$  => Yield  $\eta$ ->1

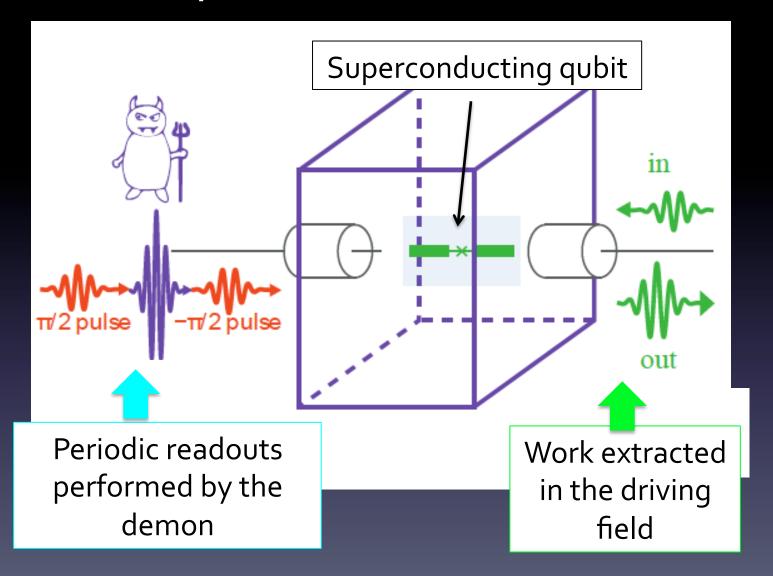
#### MPE performances: Extracted power



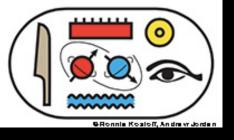
Zeno limit: Qubit « frozen » in the |+,> state

- $W_{\text{ext}}$ -> $h\nu_0\theta/2$ ;  $\theta=\Omega dt$ , P-> $P_{\text{max}} = \Omega h\nu_0/2$
- Power and yield simultaneously optimized

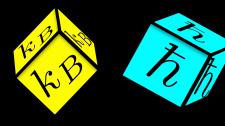
### Proposal for circuit QED



Experiment still to come!

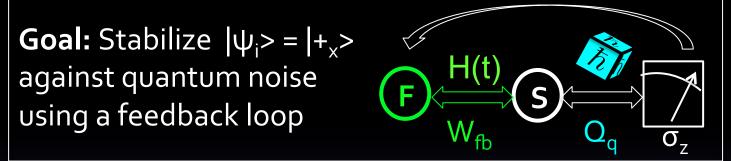


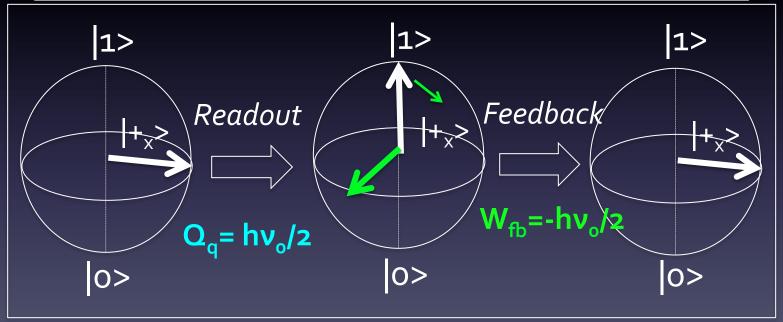
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### « Naïve » feedback stabilizing protocol

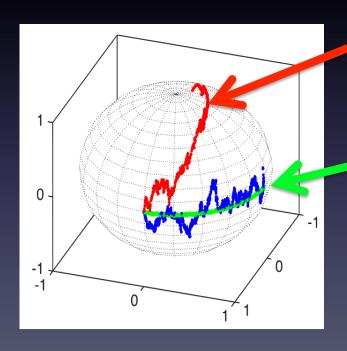




A perfect feedback requires  $W_{fb} [\Gamma] = -Q_{q} [\Gamma]$ 

### A realistic feedback stabilizing protocol

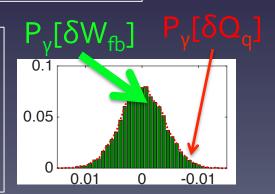
- Generalization of our framework to continuously monitored quantum systems with feedback loop
- > Thermodynamic analysis of a stabilized qubit



No feedback => decoherence: γ converges towards | o> or | 1>

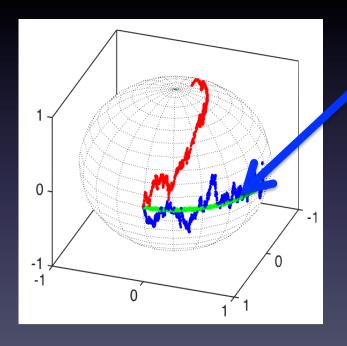
Perfect feedback & stabilization

Histograms of quantum heat and work fluctuations

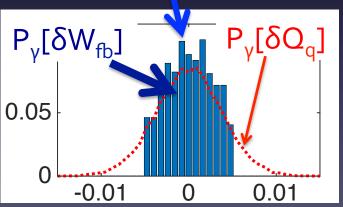


### A realistic feedback stabilizing protocol

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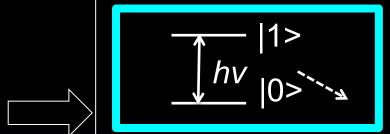
Power bounded feedback => Imperfect stabilization



### Energetic cost of quantum control

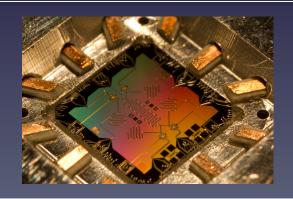


- Thermal noise
- Energy scale of classical control: kT

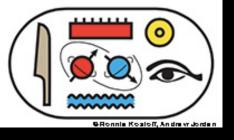


Cryostat

- Quantum noise: Pure dephasing
- kT << hv</li>



Quantum heat: A new energy scale to assess the energetic cost of quantum control



### Outline



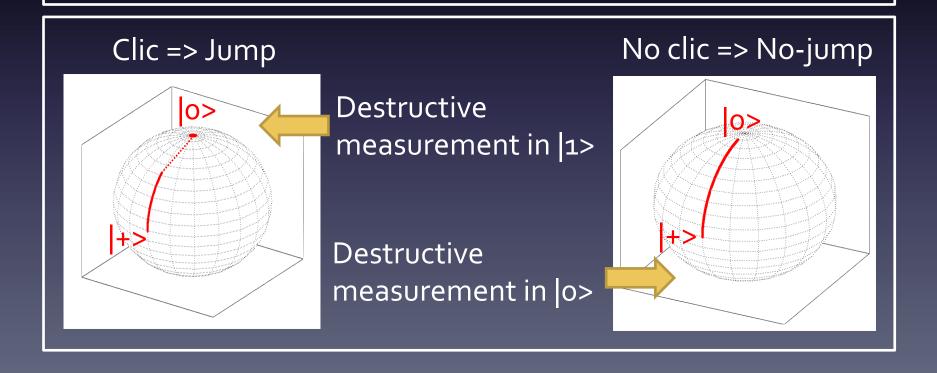


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- > Thermodynamics of spontaneous emission
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### Scenery of spontaneous emission

- A Qubit prepared in |+> and coupled to a T=o bath
- Quantum jump unraveling (Monitored by a photo-counter)





### Thermodynamic analysis



- $<\Delta U[\gamma]> = -hv_0/2$
- No work exchanged

#### > The bath plays a double role

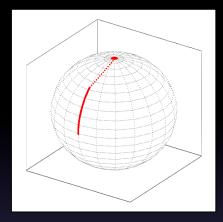
- Exchange of classical heat with the Qubit Q<sub>cl</sub> = o or hν<sub>o</sub>
- Extraction of information on the Qubit's state => Quantum heat component  $Q_{\alpha}$

First Law:  $\langle \Delta U[\gamma] \rangle = -h\nu_0/2 = \langle Q_q[\gamma] \rangle + \langle Q_{cl}[\gamma] \rangle$ 



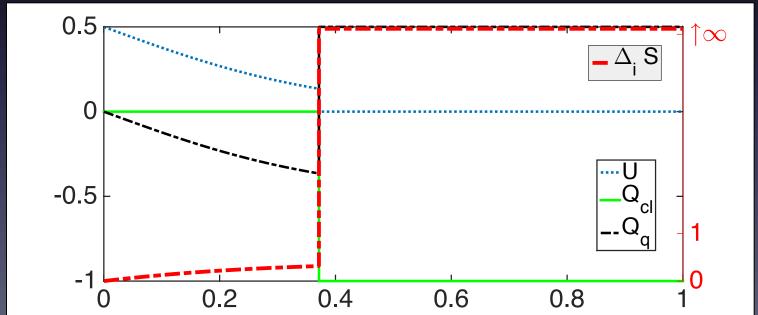
- Jump:  $Q_{cl}[\gamma] = -h\nu_{o}$ ,  $Q_{g}[\gamma] = h\nu_{o}/2$  (measurement in |1>)
- No-Jump:  $Q_{cl}[\gamma] = 0$ ,  $Q_{g}[\gamma] = -hv_{o}/2$  (measurement in  $|o\rangle$ )

### Jump trajectories

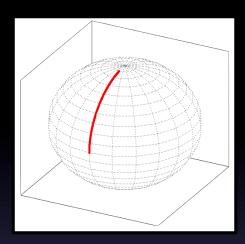


#### After the jump:

- Entropy production diverges
- Classical heat  $Q_{cl} = -h\omega_{o}$
- Quantum heat  $Q_q = h\omega_0/2$

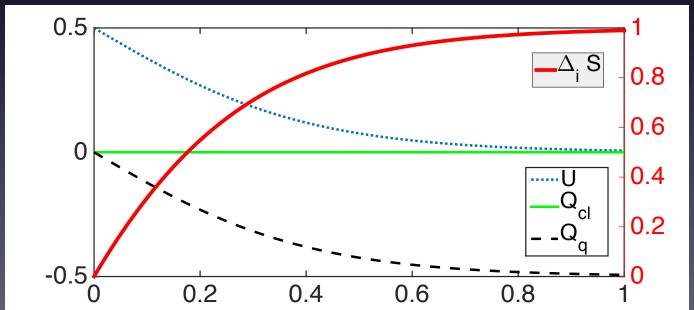


### No jump trajectories

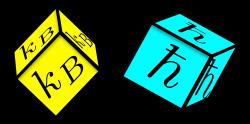


#### For t large

- Classical heat  $Q_{cl} = o$
- Quantum heat  $Q_q = -h\omega_0/2$
- Entropy production  $\Delta_i S = \Delta S_{VN}$
- Entropy of measurement



#### Conclusions



- Energetic footprint of quantum noise:
   Quantum heat => Proper energy scale to assess the work cost of quantum control
- Work extraction from quantum noise instead of thermal noise => Measurement Powered Engine
- Doable with state of the art devices of cQED
- Key role of randomness in the building of thermodynamical concepts



#### Outlooks & collaborations





Quantum engines



M. Richard, Grenoble



B. Huard, Lyon

#### Thdyn of entanglement fluorescence



G. Haack Geneva

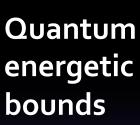
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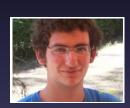


M. Esposito Luxembourg



J. Anders Exeter





C. Elouard Rochester



D. Herrera-Marti Grenoble

#### Thermodynamics of reservoir engineering



M. Santos D. Gerace A. Carvalho Rio Pavia



Brisbane

#### Quantum foundations



P. Grangier, Orsay & N. Farouki, Grenoble



- 25 interdisciplinary PhD scholarships for quantum engineering in Grenoble along 4 calls (2017-2018)
- Next and LAST deadline: October 2018







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