

GUT and Neutrino Mass Models

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Snowmass on the Pacific, KITP, Santa Barbara, CA, May 30, 2013

The 3-Flavor Era in Neutrino Physics!

- Exciting Time in ν Physics: recent hints/evidences of large θ_{13} from T2K, MINOS, Double Chooz, Daya Bay and RENO

- Latest 3 neutrino global analysis:

Fogli, Lisi, Marrone, Montanino, Palazzo, Rotunno (2012)
 [see also, Gonzalez-Garcia, Maltoni, Salvado, Schwetz (2012)]

Parameter	Best fit	1σ range	2σ range	3σ range
$\delta m^2/10^{-5} \text{ eV}^2$ (NH or IH)	7.54	7.32 – 7.80	7.15 – 8.00	6.99 – 8.18
$\sin^2 \theta_{12}/10^{-1}$ (NH or IH)	3.07	2.91 – 3.25	2.75 – 3.42	2.59 – 3.59
$\Delta m^2/10^{-3} \text{ eV}^2$ (NH)	2.43	2.33 – 2.49	2.27 – 2.55	2.19 – 2.62
$\Delta m^2/10^{-3} \text{ eV}^2$ (IH)	2.42	2.31 – 2.49	2.26 – 2.53	2.17 – 2.61
$\sin^2 \theta_{13}/10^{-2}$ (NH)	2.41	2.16 – 2.66	1.93 – 2.90	1.69 – 3.13
$\sin^2 \theta_{13}/10^{-2}$ (IH)	2.44	2.19 – 2.67	1.94 – 2.91	1.71 – 3.15
$\sin^2 \theta_{23}/10^{-1}$ (NH)	3.86	3.65 – 4.10	3.48 – 4.48	3.31 – 6.37
$\sin^2 \theta_{23}/10^{-1}$ (IH)	3.92	3.70 – 4.31	$3.53 - 4.84 \oplus 5.43 - 6.41$	3.35 – 6.63
δ/π (NH)	1.08	0.77 – 1.36	—	—
δ/π (IH)	1.09	0.83 – 1.47	—	—

- Evidence of $\theta_{13} \neq 0$
- hints of $\theta_{23} \neq \pi/4$
- expectation of Dirac CP phase δ

- no clear preference for hierarchy
- Absolute neutrino mass scale?
- Majorana vs Dirac?

Need For Precision Measurements

(i) Absolute mass scale: Why $m_\nu \ll m_{u,d,e}$?

- seesaw mechanism: most appealing scenario \Rightarrow Majorana
 - GUT scale (type-I, II) vs TeV scale (type-II, III, inverse seesaw)
- TeV scale new physics (warped extra dimension, U(1)) \Rightarrow Dirac or Majorana

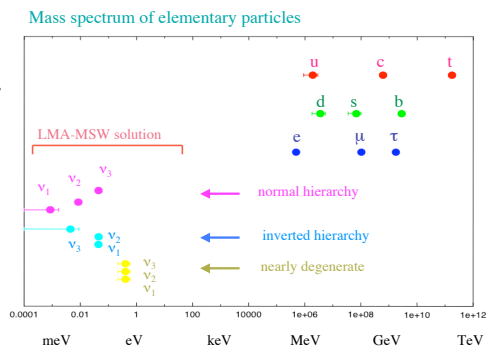
(ii) Flavor Structure: Why neutrino mixing large while quark mixing small?

- neutrino anarchy: no parametrically small number Hall, Murayama, Weiner (2000); de Gouvea, Murayama (2003)
 - near degenerate spectrum, large mixing
 - still alive and kicking de Gouvea, Murayama (2012)
 - heterotic string theory connection
- family symmetry: there's a structure, expansion parameter (~~symmetry effect~~)
 - mixing result from dynamics of underlying symmetry
 - leptonic symmetry (normal or inverted)
 - for quarks and leptons: quark-lepton connection \leftrightarrow GUT (normal)
- Alternative?
- In this talk: assume 3 generations, no LSND/MiniBoone/Reactor Anomaly

Planck 2013 Data Release: $N_{\text{eff}} = 3.26 \pm 0.35 \Rightarrow$ sterile neutrino marginally consistent

Origin of Mass Hierarchy and Mixing

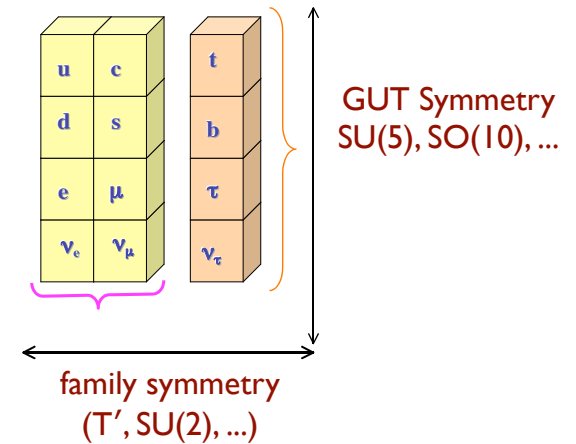
- In the SM: 22 physical quantities which seem unrelated
- Question arises whether these quantities can be related
- **No fundamental reason can be found in the framework of SM**
- less ambitious aim \Rightarrow reduce the # of parameters by imposing symmetries
 - SUSY Grand Unified Gauge Symmetry
 - GUT relates quarks and leptons: quarks & leptons in same GUT multiplets
 - one set of Yukawa coupling for a given GUT multiplet \Rightarrow intra-family relations
 - seesaw mechanism naturally implemented
 - proton decay, leptogenesis, LFV charged lepton decay
 - Family Symmetry
 - relate Yukawa couplings of different families
 - inter-family relations \Rightarrow further reduce the number of parameters



\Rightarrow Experimentally testable *correlations* among physical observables

Origin of Mass Hierarchy and Mixing

- Several models have been constructed based on
 - GUT Symmetry [SU(5), SO(10)] \oplus Family Symmetry G_F
- Family Symmetries G_F based on continuous groups:
 - U(1)
 - SU(2)
 - SU(3)
- Recently, models based on discrete family symmetry groups have been constructed
 - A_4 (tetrahedron)
 - T' (double tetrahedron)
 - S_3 (equilateral triangle)
 - S_4 (octahedron, cube)
 - A_5 (icosahedron, dodecahedron)
 - Δ_{27}
 - Q_4



Motivation: Tri-bimaximal (TBM) neutrino mixing

Discussion on Discrete gauge anomaly:
Araki, Kobayashi, Kubo, Ramos-Sanchez,
Ratz, Vaudrevange (2008)

Tri-bimaximal Neutrino Mixing

- **Tri-bimaximal Mixing Pattern** Harrison, Perkins, Scott (1999)

$$U_{TBM} = \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix}$$

$$\sin^2 \theta_{\text{atm}, TBM} = 1/2 \quad \sin^2 \theta_{\odot, TBM} = 1/3 \quad \sin \theta_{13, TBM} = 0.$$

- **General approach:**
 - **PMNS = LO prediction (TBM, BM, ...) + corrections**
 - **corrections:** $\left\{ \begin{array}{l} \text{higher order terms in super potential (family symmetry)} \\ \text{contributions from charged lepton sector (GUT symmetry)} \end{array} \right.$

Non-Abelian Finite Family Symmetry A_4

- TBM mixing matrix: can be realized with finite group family symmetry based on A_4

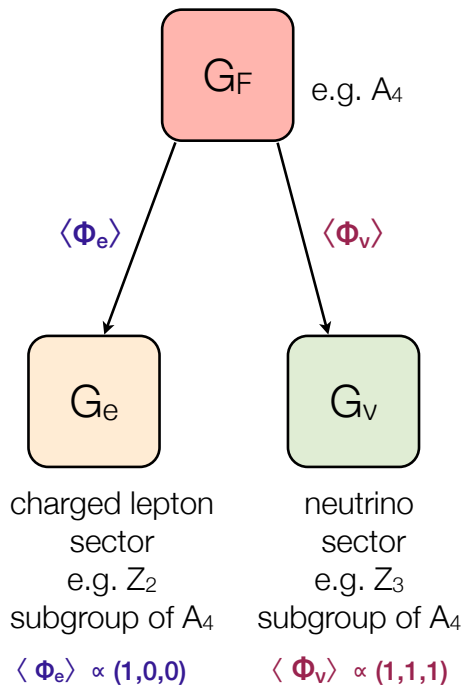
Ma, Rajasekaran (2001); Babu, Ma, Valle (2003); ...

- A_4 : even permutations of 4 objects

$$S: (1234) \rightarrow (4321)$$

$$T: (1234) \rightarrow (2314)$$

- a group of order 12
- Invariant group of tetrahedron
- TBM arises from misalignment of symmetry breaking patterns



An Example: a SUSY $SU(5) \times T'$ Model

M.-C.C, K.T. Mahanthappa
Phys. Lett. B652, 34 (2007);
Phys. Lett. B681, 444 (2009)

- GUT compatible \Rightarrow Double Tetrahedral Group T' [cf. Talk by KT Mahanthappa]
- Symmetries \Rightarrow 10 parameters in Yukawa sector \Rightarrow 22 physical observables
 - neutrino mixing angles from group theory (CG coefficients)
 - TBM: misalignment of symmetry breaking patterns
 - neutrino sector: $T' \rightarrow G_{TST_2}$, charged lepton sector: $T' \rightarrow G_T$
 - GUT symmetry \Rightarrow deviation from TBM related to quark mixing θ_c
- **complex CG's of T' \Rightarrow Novel Origin of CP Violation**
 - CP violation in both quark and lepton sectors entirely from group theory
 - connection between leptogenesis and CPV in neutrino oscillation

M.-C.C, K.T. Mahanthappa,
Phys. Lett. B681, 444 (2009)

before θ_{13} discovery

Sum Rules: Quark-Lepton Complementarity

Quark Mixing

mixing parameters	best fit	3σ range
θ_{23}^q	2.36°	$2.25^\circ - 2.48^\circ$
θ_{12}^q	12.88°	$12.75^\circ - 13.01^\circ$
θ_{13}^q	0.21°	$0.17^\circ - 0.25^\circ$

Lepton Mixing

mixing parameters	best fit	3σ range
θ_{23}^e	42.8°	$35.5^\circ - 53.5^\circ$
θ_{12}^e	34.4°	$31.5^\circ - 37.6^\circ$
θ_{13}^e	5.6°	$\leq 12.5^\circ$

- **QLC-I** $\theta_c + \theta_{sol} \cong 45^\circ$ Raidal, '04; Smirnov, Minakata, '04

(BM) $\theta_{23}^q + \theta_{23}^e \cong 45^\circ$

- **QLC-II** $\tan^2\theta_{sol} \cong \tan^2\theta_{sol,TBM} + (\theta_c / 2) * \cos \delta_e$

Ferrandis, Pakvasa; King; Dutta, Mimura; M.-C.C., Mahanthappa

(TBM) $\theta_{13}^e \cong \theta_c / 3\sqrt{2}$

- testing sum rules: a *more* robust way to distinguish different classes of models

measuring leptonic mixing parameters to the precision of those in quark sector

Intensity Frontier

after θ_{13} discovery

Sum Rules: Quark-Lepton Complementarity

Quark Mixing

mixing parameters	best fit	3σ range
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Lepton Mixing

mixing parameters	best fit	3σ range
θ_{23}^e	38.4° ↓	$35.1^\circ - 52.6^\circ$
θ_{12}^e	33.6°	$30.6^\circ - 36.8^\circ$
θ_{13}^e	8.9° ↑	$7.5^\circ - 10.2^\circ$

- **QLC-I** $\theta_c + \theta_{sol} \cong 45^\circ$ Raidal, '04; Smirnov, Minakata, '04
(BM) $\theta_{23}^q + \theta_{23}^e \cong 45^\circ$ → **inconsistent @ 2σ**

- **QLC-II** $\tan^2\theta_{sol} \cong \tan^2\theta_{sol,TBM} + (\theta_c / 2) * \cos \delta_e$ Ferrandis, Pakvasa; King; Dutta, Mimura; M.-C.C., Mahanthappa
(TBM) $\theta_{13}^e \cong \theta_c / 3\sqrt{2}$ → **Too small**

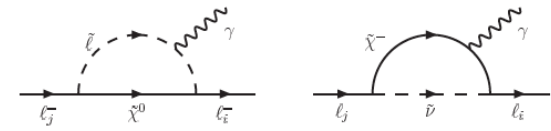
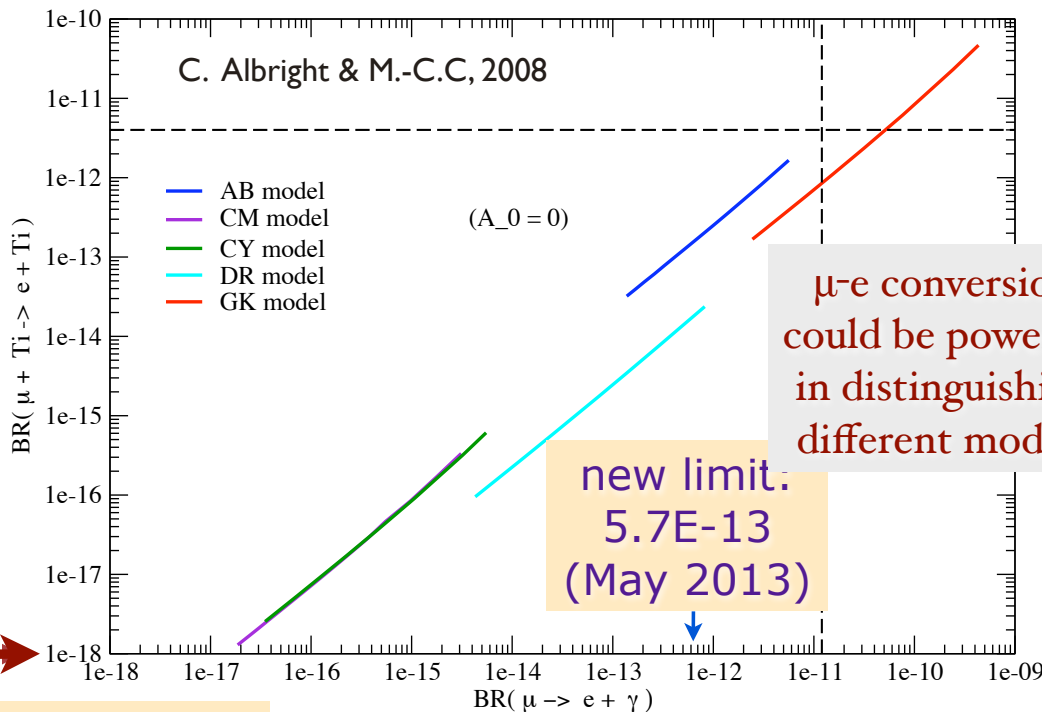
- testing sum rules: a *more* robust way to distinguish different classes of models

measuring leptonic mixing parameters to the precision of those in quark sector

Intensity Frontier

Other Correlations: Rare CLFV Processes

- SUSY GUTs: Lepton flavor violating charged lepton decays [cf. Talk by Andre de Gouvea]
 - five viable SUSY SO(10) models with dark matter constraints in cMSSM:



μ -e conversion could be powerful in distinguishing different models

▶ individual branching fraction: strong dependence on soft SUSY parameters

▶ correlations between branching fractions: **strong dependence on flavor structure**

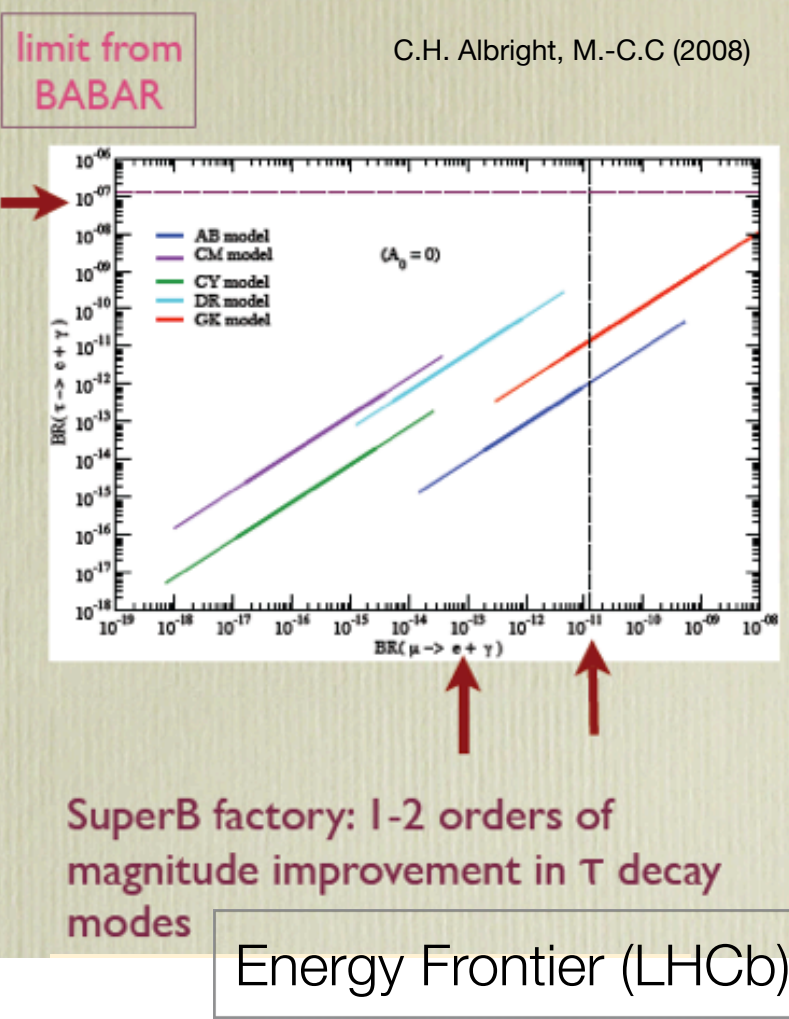
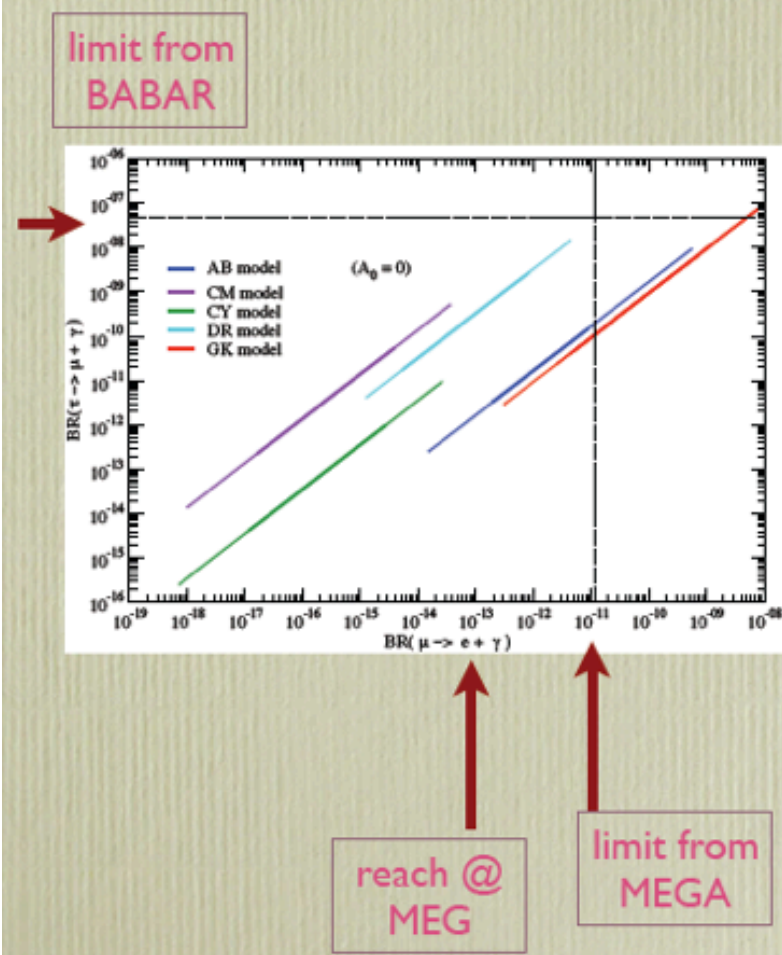
new limit: $5.7E-13$ (May 2013)

sensitivity of proposed Muze exp

reach at MEG

Intensity Frontier ($\mu 2e, \dots$)

Other Correlations: Rare CLFV Processes



Other Possibilities

- Beyond TBM and BM mixing pattern:

- Golden Ratio for solar angle

$$\tan^2 \theta_{\text{sol}} = 1/\Phi^2 = 0.382, \quad (1.4\sigma \text{ below best fit})$$

$$\Phi = (1 + \sqrt{5}) / 2 = 1.62$$

Datta, Ling, Ramond, '03;
 Z2 x Z2: Kajiyama, Raidal, Strumia, '07;
 A5: Everett, Stuart, '08; ...

[cf. Talk by Lisa Everett]

- Dodeca Mixing Matrix from D_{12} Symmetry

J. E. Kim, M.-S. Seo (2010)

leading order:

$$\theta_c = 15^\circ, \theta_{\text{sol}} = 30^\circ, \theta_{\text{atm}} = 45^\circ$$

$$V_{\text{PMNS}} = U_l^\dagger U_\nu = \begin{pmatrix} \cos \frac{\pi}{6} & \sin \frac{\pi}{6} & 0 \\ -\frac{1}{\sqrt{2}} \sin \frac{\pi}{6} & \frac{1}{\sqrt{2}} \cos \frac{\pi}{6} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \sin \frac{\pi}{6} & \frac{1}{\sqrt{2}} \cos \frac{\pi}{6} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$$\left. \begin{array}{l} 12 = 360^\circ / 30^\circ \Rightarrow Z_{12} \\ 15^\circ \Rightarrow Z_2 \end{array} \right\} Z_{12} \times Z_2 = D_{12}$$

$$\theta_c + \theta_{\text{sol}} = 45^\circ \quad (\text{not from GUT symmetry})$$

breaking of D_{12} :

$$\theta_c = 15^\circ \rightarrow 13.4^\circ$$

$$\theta_{\text{sol}} = 30^\circ + O(\epsilon), \theta_{13} = O(\epsilon)$$

Kähler Corrections

Leurer, Nir, Seiberg (1993); Dudas, Pokorski, Savoy (1995); Dreiner, Thomeier (2003);

- Contributions from Supergravity:

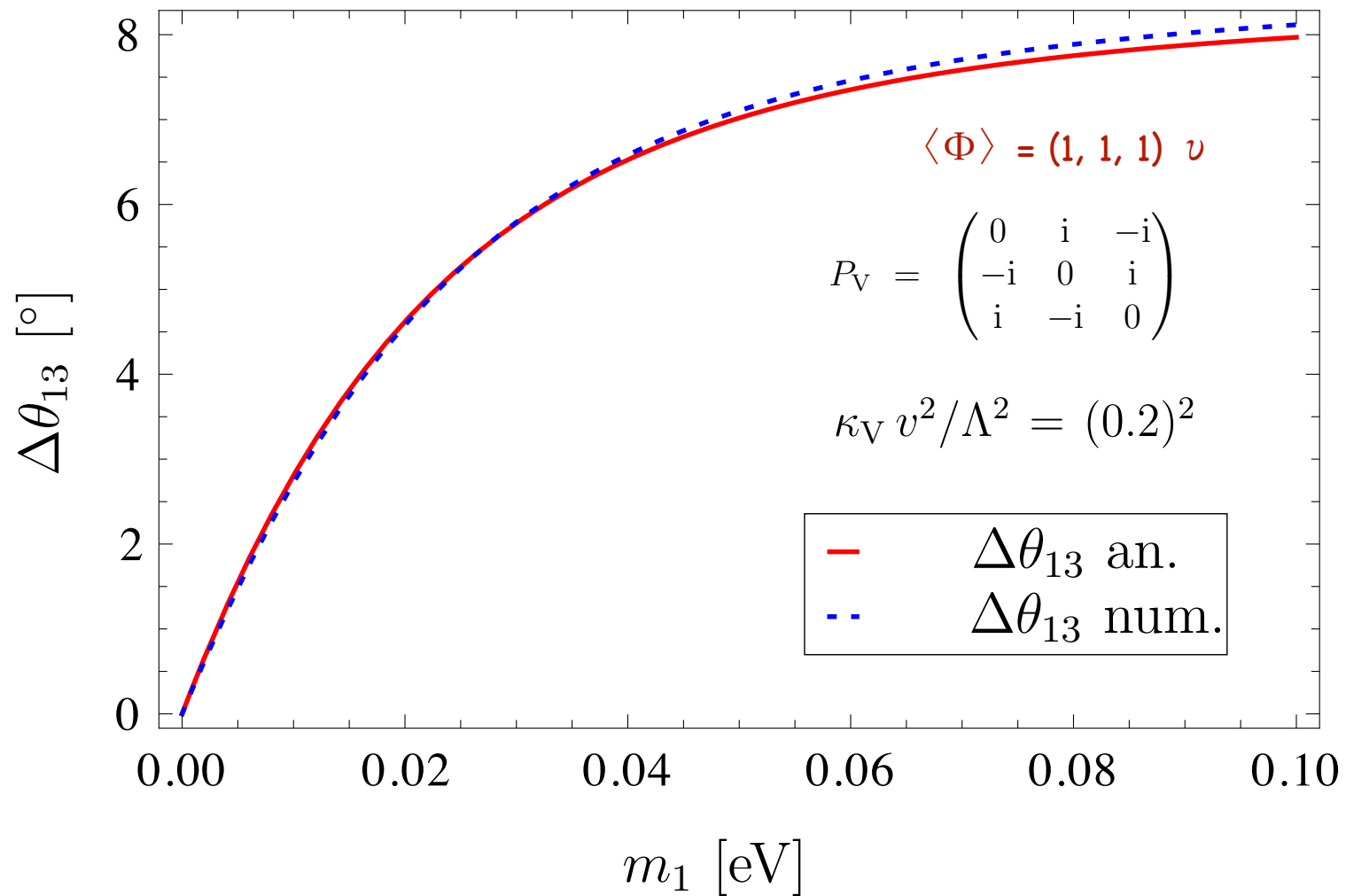
- higher order terms in Kähler potential induced (and determined) by

VEVs of flavon fields (flavor Higgses) $\mathcal{K}_L = 1 - 2xP$

- non-trivial flavor structure in \mathbf{P} can be induced
- can't be forbidden by conventional symmetry
- while similar in structure to RG corrections, can be along different directions than RG
- size of Kähler corrections generically dominate RG corrections (no loop suppression, contributions from copies heavy states)
- non-zero CP phases can be induced

An Example: Enhanced θ_{13} in A4

M.-C.C., Fallbacher, Ratz, Staudt (2012)

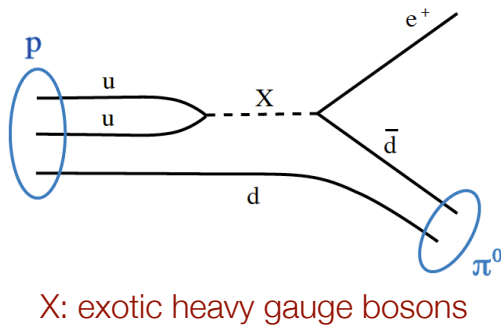


**Theoretical understanding of Kähler
corrections crucial in achieving precision
compatible to experimental accuracy.**

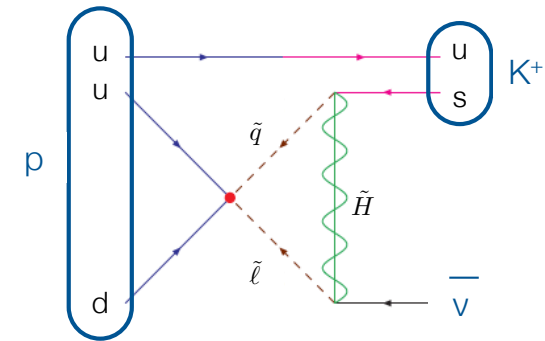
Knowledge Frontier

Proton Decay

- GUT predicts proton decay



SUSY GUTs:
additional
contributions
mediated by
superpartners



\tilde{H} : color-triplet Higgsinos

lifetime: $\tau_p \propto M_X^4$

$$\tau_p \propto M_{\tilde{H}}^2$$

- Experimental Limits

$$\tau(p \rightarrow e^+ \pi^0) > 8.2 \times 10^{33} \text{ years} \quad (90\% \text{ CL, SuperK 2009}) \quad \Rightarrow M_X > 5 \times 10^{15} \text{ GeV}$$

$$\tau(p \rightarrow \bar{\nu} K^+) > 2.3 \times 10^{33} \text{ years} \quad (90\% \text{ CL, SuperK 2005}) \quad \Rightarrow M_{\tilde{H}} > 10^{19} \text{ GeV} \quad !!$$

Dermis k, Mafi, Raby, 2000 **for reasonable soft SUSY masses**

A recent updated study: Babu, Pati, Tavartkiladze (2010)

[cf. Talk by Radovan Dermisek]

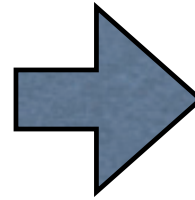
GUTs and doublet-triplet splitting

Review: MCC, Fallbacher, Ratz (212)

Suppressing the mu term in the MSSM

Assumptions:

- Consistency with unification
- Anomaly freedom

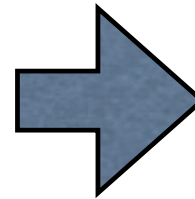


Only R symmetries can forbid the mu term in the MSSM

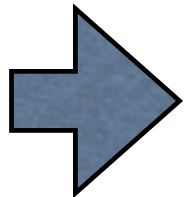
No-Go for R symmetries in 4D GUTs

assumptions:

- GUT model in four dimensions based on $G \supset SU(5)$
- GUT symmetry breaking is spontaneous
- only finite number of fields



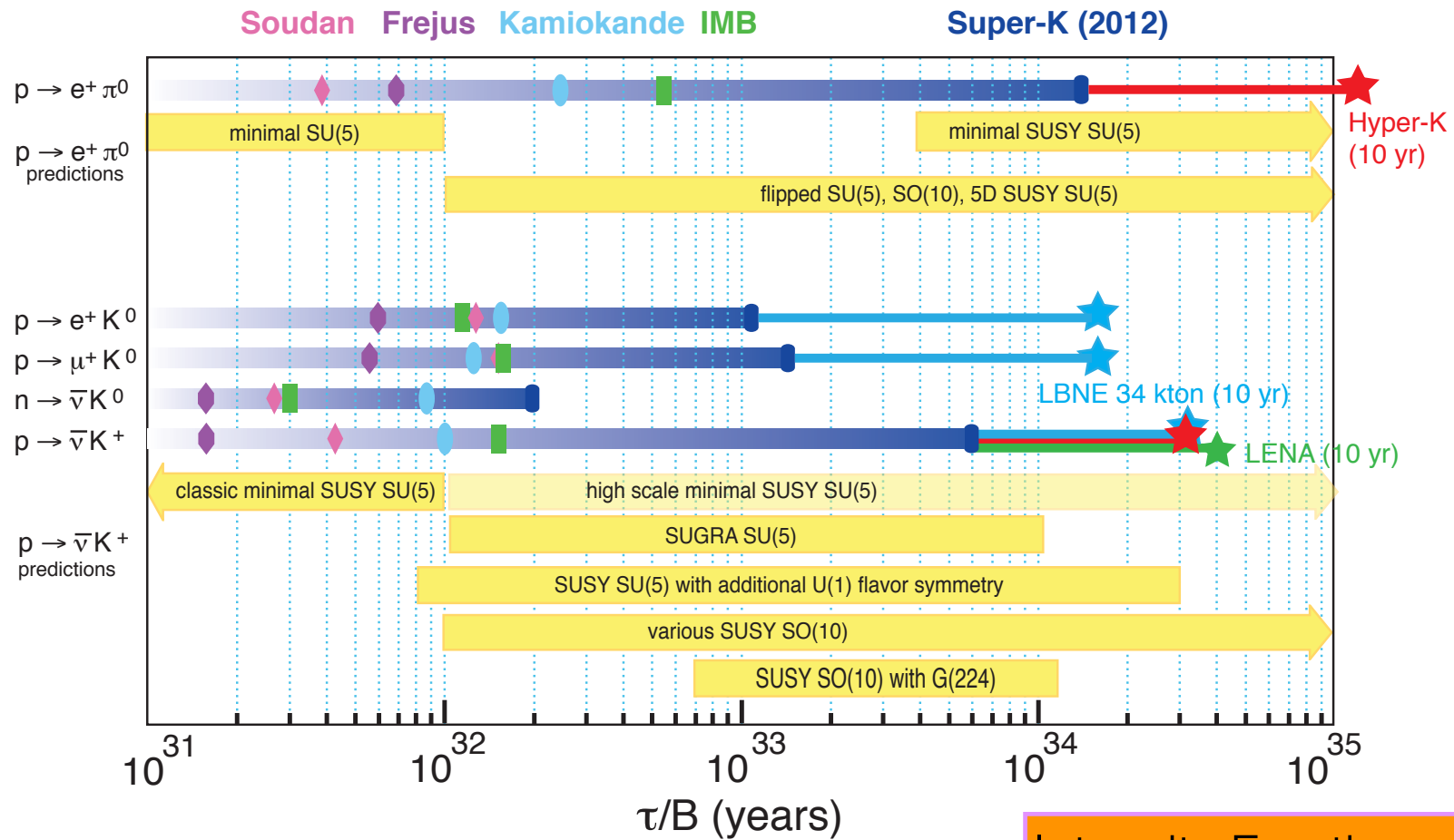
Impossible to have MSSM spectrum (w/o exotics) and residual R symmetries



higher-dimensional models of Grand Unification (dim 5 decay suppressed, dim 6 decay enhanced)

Experimental Limits Confront Theory

Talks by K.S. Babu, E. Kern,
ISOUPS2013



Dirac Neutrino Mass and the μ Term

M.-C. C., Michael Ratz, Christian Staudt,
Patrick Vaudrevange, (2012)

- R-symmetries: Anomaly-free, SU(5)-consistent, allow Yukawa couplings

- ▶ absence of perturbative μ term \Rightarrow constraints on R charges of H_u, H_d

\rightarrow non-perturbative μ term \sim TeV automatically arise

$$\mu \sim \langle \mathcal{W} \rangle / M_{\text{P}}^2 \sim m_{3/2}$$

- ▶ absence of perturbative Weinberg operator \Rightarrow constraints on R charges of leptons

\rightarrow non-perturbative, realistic Dirac neutrino mass automatically arise

$$Y_\nu \sim \frac{m_{3/2}}{M_{\text{P}}} \sim \frac{\mu}{M_{\text{P}}}$$

- ▶ solutions **automatically** forbid dim-4 and suppress dim-5 proton decay of the MSSM

- ▶ all superpotential B and L violating operators to **all orders** with Hilbert basis method

- an example: \mathbb{Z}_8^R symmetry

R. Kappl, M. Ratz, C. Staudt (2011)

\rightarrow $\Delta L = 2$ operators forbidden \Rightarrow no neutrinoless double beta decay

\rightarrow $\Delta L = 4$ operators allowed \Rightarrow new LNV processes

anomaly-free, SU(5) compatible R symmetries simultaneously solve μ problem, naturally small Dirac neutrino masses

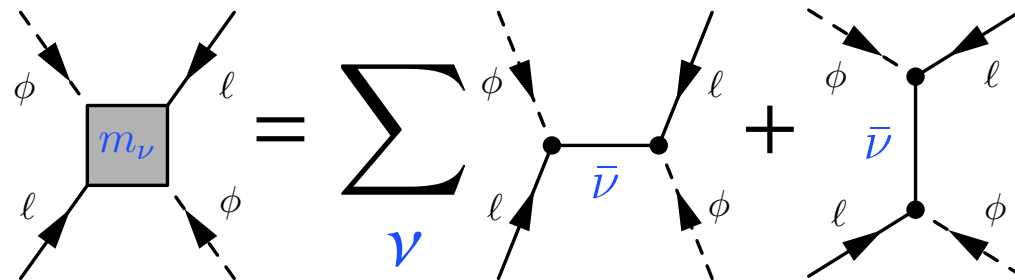
Heterotic Seesaw

Talk by Michael Ratz at BeNE 2012

- heterotic string models: O(100) RH neutrinos

Buchmüller, Hamaguchi, Lebedev, Ramos-Sánchez, Ratz (2007)

- O(100) contributions to the effective neutrino mass operator



- Effective suppression

$$m_\nu \sim \frac{v^2}{M_*}$$

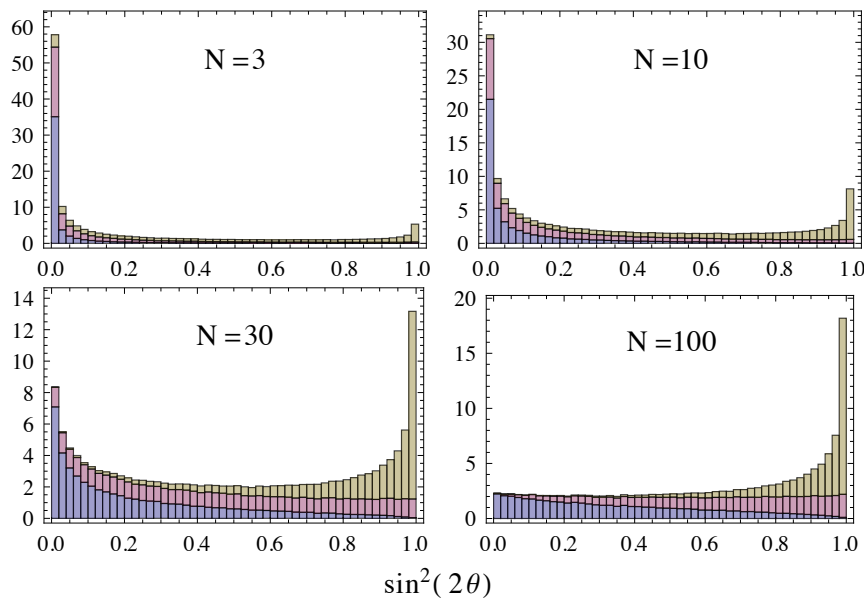
$M_* \sim \frac{M_{\text{GUT}}}{10 \dots 100}$

Heterotic Seesaw

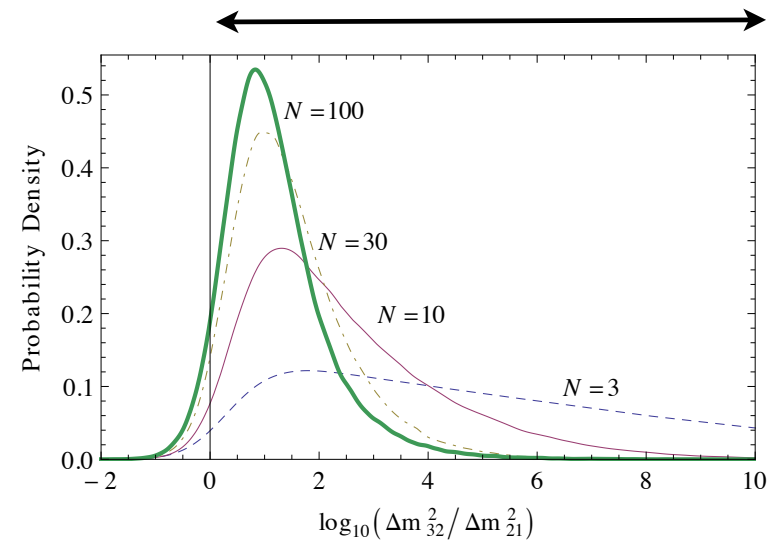
Talk by Michael Ratz at BeNE 2012

- statistical expectations with large N (= # of RH neutrinos)
⇒ anarchy

preference for large mixing angles



preference for normal hierarchy



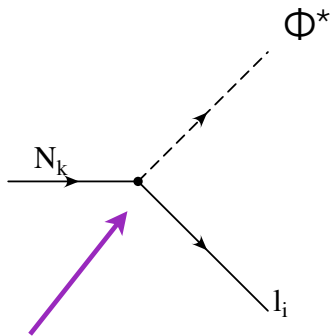
Feldstein, Klemm (2012)

Leptogenesis

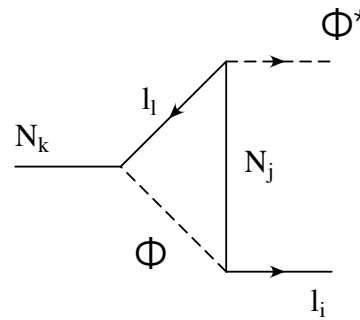
Fukugita, Yanagida, 1986

- RH heavy neutrino decay:

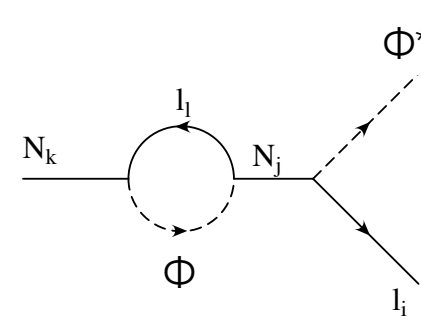
- quantum interference of tree-level & one-loop diagrams \Rightarrow primordial lepton number asymmetry ΔL



neutrino Yukawa interactions



leptons



antileptons

$$\text{Leptonic CP violation} \Rightarrow \Delta L \propto [\Gamma(N_1 \rightarrow \ell_\alpha \Phi) - \Gamma(N_1 \rightarrow \bar{\ell}_\alpha \bar{\Phi})] \neq 0$$

\Leftrightarrow neutrino parameters

Cosmic Frontier

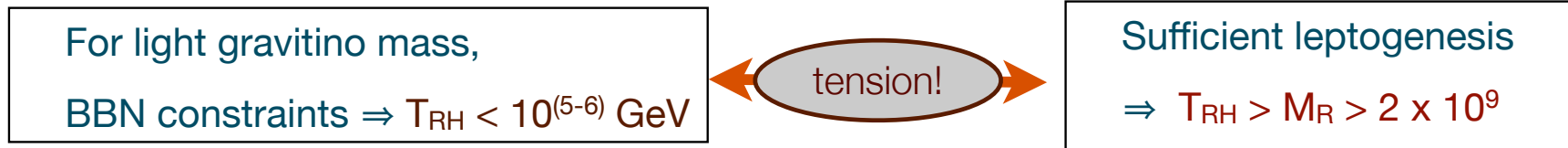
Leptogenesis \Leftrightarrow CPV in Neutrino Oscillation

- models for neutrino masses:
 - additional symmetries
 - reduce the number of parameters \Rightarrow model dependent connection possible
- rank-2 mass matrix (may be realized by symmetry)
 - models with 2 RH neutrinos (2 x 3 seesaw) Kuchimanchi & Mohapatra, 2002
 - sign of baryon asymmetry \leftrightarrow sign of CPV in ν oscillation Frampton, Glashow, Yanagida, 2002
- all CP come from a single source
 - minimal models with spontaneous CP violation:
 - SM + vectorial quarks + singlet scalar Branco, Parada, Rebelo, 2003
 - minimal LR model: only 1 physical leptonic CP phase M.-.C.C, Mahanthappa, 2005
 - SCPV in SO(10): $\langle 126 \rangle_{B-L}$ complex Achiman, 2004, 2008
 - SUSY SU(5) x T' Model: M.-.C.C, Mahanthappa, 2009
 - group theoretical origin of CP violation \Rightarrow only low energy lepton phases $\neq 0$

In all models, non-zero Dirac CP phase required for leptogenesis

“Non-standard” Leptogenesis

- Gravitino problem:



- Possible ways to avoid the tension:

- **resonant leptogenesis** (near degenerate RH neutrinos) Pilaftsis, 1997
 - TeV scale leptogenesis possible
 - possible collider tests Pilaftsis, Underwood, 2003
- **soft leptogenesis** Boubekour, 2002; Grossman, Kashti, Nir, Roulet, 2003; D’Ambrosio, Giudice, Raidal, 2003
 - CP phase in soft SUSY parameters
- **Dirac leptogenesis** K. Dick, M. Lindner, M. Ratz, D. Wright, 2000; H. Murayama, A. Pierce, 2002
 - connections to LFV B. Thomas, M. Toharia, 2006
- **non-thermal leptogenesis**
 - inflaton decay Fuji, Hamaguchi, Yanagida, 2002

N-Nbar Oscillation \Leftrightarrow Leptogenesis Scale

- Neutrino Experiments \rightarrow “archeological” evidence for leptogenesis
- n-nbar oscillation searches \rightarrow complementarity test of leptogenesis (baryogenesis) mechanisms
 - constrain the scale of leptogenesis
- observation of neutron antineutron oscillation K.S. Babu, R.N. Mohapatra, 2012
 - new physics with $\Delta B = 2$ at $10^{(5-6)}$ GeV
 - erasure of matter-antimatter generated at high scale, e.g. standard leptogenesis
- ▶ Low scale leptogenesis scenarios preferred

Toward the Theory of Leptogenesis:

Buchmuller, Fredenhagen, 2000;
Simone, Riotto 2007;
Lindner, Muller 2007

Classical Boltzmann Equations



Quantum Boltzmann Equations

(Closed-time-path formulation for non-equilibrium QFT)

Schwinger, 1961; Mahanthappa, 1962;
Bakshi, Mahanthappa, 1963;
Keldysh, 1965

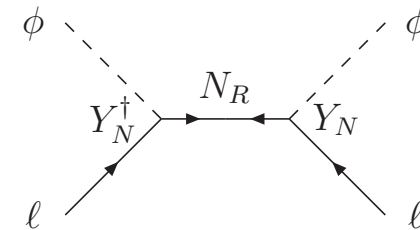
Knowledge Frontier

TeV Scale Seesaw Models

For a recent review:
M.-C. C., J.R. Huang, arXiv:1105.3188

- With new particles:
 - **type-I seesaw**
 - generally decouple from collider physics

Kersten, Smirnov, 2007



- **type-II seesaw** Lazarides, 1980; Mohapatra, Senjanovic, 1980

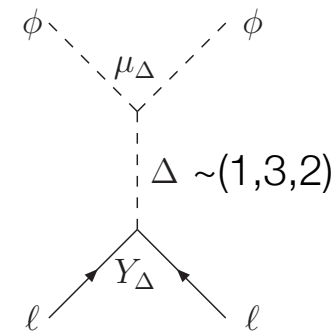
- TeV scale doubly charged Higgs \Leftrightarrow **small couplings**

- unique signatures:

$$\Delta^{++} \rightarrow e^+ e^+, \mu^+ \mu^+, \tau^+ \tau^+$$

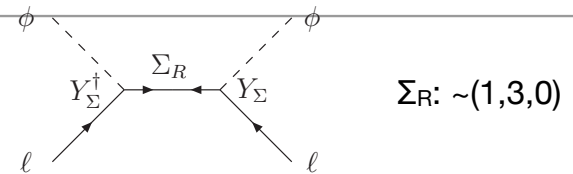
- decay BR \Leftrightarrow mass ordering

Perez, Han, Huang, Li, Wang, '08; Han, Mukhopadhyaya, Si, Wang, '07; Akeroyd, Aoki, Sugiyama, '08; ...



Energy Frontier

TeV Scale Seesaw Models



- With new particles:

- **type-III seesaw** Foot, Lew, He, Joshi, 1989; Ma, 1998

- TeV scale triplet decay : observable displaced vertex

$$\tau \leq 1 \text{ mm} \times \left(\frac{0.05 \text{ eV}}{\sum_i m_i} \right) \left(\frac{100 \text{ GeV}}{\Lambda} \right)^2 \quad \text{Franceschino, Hambye, Strumia, 2008}$$

- neutral component Σ^0 can be dark matter candidate E. J. Chun, 2009

- **Radiative Seesaw**

- Zee-Babu model (neutrino mass at 2 loop) Zee 1986; Babu, 1989

- singly+doubly charged SU(2) singlet scalars

- neutrino mass at higher loops: TeV scale RH neutrinos Krauss, Nasri, Trodden, 2003; E. Ma, 2006; Aoki, Kanemura, Seto, 2009

- loop particles can also have color charges

- enhanced production cross section Perez, Han, Spinner, Trenkel, 2011

TeV Scale Seesaw Models

- With new interactions:

- SUSY LR Model:

- tested via searches for W_R

Azuleos et al 06; del Aguila et al 07, Han et al 07; Chao, Luo, Xing, Zhou, '08; ...

- More Naturally: **inverse seesaw** or **higher dimensional operators** or **Extra Dim**

- **inverse seesaw** Mohapatra, 1986; Mohapatra, Valle, 1986; Gonzalez-Garcia, Valle, 1989

- **non-unitarity effects**

Intensity Frontier

- enhanced LFV (both SUSY and non-SUSY cases)

- correlation

Hirsch, Kernreiter, Romao, del Moral, 2010

$$\frac{\text{BR}(\tilde{\chi}_1^\pm \rightarrow \tilde{N}_{1+2} + \mu^\pm)}{\text{BR}(\tilde{\chi}_1^\pm \rightarrow \tilde{N}_{1+2} + \tau^\pm)} \propto \frac{\text{BR}(\mu \rightarrow e + \gamma)}{\text{BR}(\tau \rightarrow e + \gamma)}$$

SUSY Flavor

- Family symmetry:
 - if symmetry breaking at TeV \Rightarrow signatures at colliders
 - non-anomalous, non-universal $U(1)'$ at TeV M.-C. C., de Gouvea, Dobrescu (2006)
 - probing flavor through Z' decays at colliders M.-C. C., J.-R. Huang (2009)
 - with SUSY: superpartners charged under family symmetry, can probe (indirectly) flavor sector even for high symmetry breaking scale
 - inverse hierarchy for sfermions
 - global $U(2)$ Dine, Leigh, Kagan '93; Pomarol, Tommasini '95; Barbieri, Davali, Hall '96; Barbieri, Hall, Romanino, '97; ...
 - anomalous $U(1)$ Dudas, Pokorski, Savoy '95; Dudas, Grojean, Pokorski, Savoy '96; Nelson, Wright '97;

Correlations among Observables

- Example: MSSM with bi-linear R-Parity Violation

de Campos, Eboli, Hirsch, Margo, Porod,
Restrepo, Valle, 2010

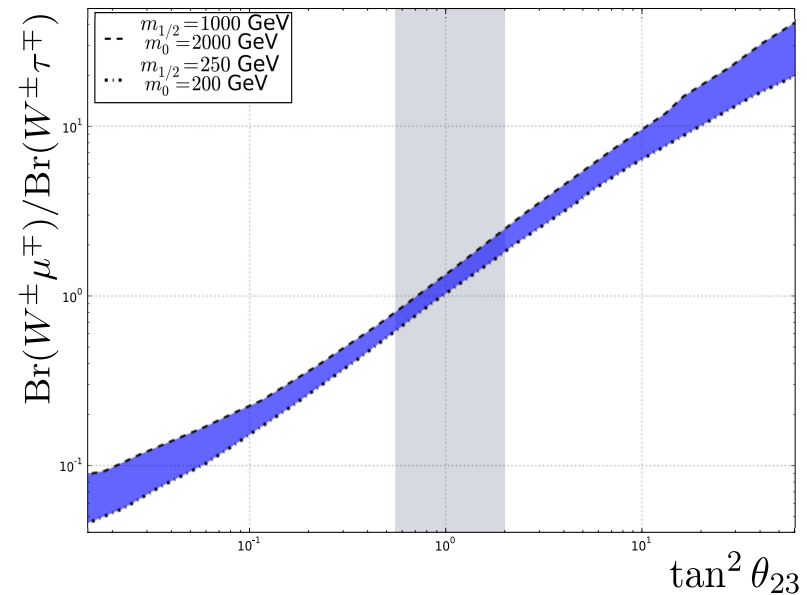
$$\mathcal{W}_R = \epsilon_i \hat{L}_i \hat{H}_u$$

- mixing angle \leftrightarrow neutralino decay

$$\tan^2 \theta_{\text{atm}} \simeq \frac{BR(\tilde{\chi}_1^0 \rightarrow \mu^\pm W^\mp)}{BR(\tilde{\chi}_1^0 \rightarrow \tau^\pm W^\mp)}$$

[cf. Talk by Prashant Sarawat]

Energy Frontier



Curing FCNC Problem: Family Symmetry vs MFV

- low scale new physics severely constrained by flavor violation

$$\psi_{(0)} \sim e^{(1/2-c)ky}$$

- Warped Extra Dimension

- wave function overlap \Rightarrow naturally small Dirac mass

- non-universal bulk mass terms (c) \Rightarrow FCNCs at tree level $\Rightarrow \Lambda > O(10)$ TeV

- fine-tuning required to get large mixing and mild mass hierarchy

- **Minimal Flavor Violation** quark sector: A. Fitzpatrick, G. Perez, L. Randall (2007) lepton sector: M.-C.C., H.B. Yu (2008)

$$C_e = aY_e^\dagger Y_e, \quad C_N = dY_\nu^\dagger Y_\nu, \quad C_L = c(\xi Y_\nu Y_\nu^\dagger + Y_e Y_e^\dagger)$$

- **T' symmetry in the bulk for quarks & leptons:** M.-C.C., K.T. Mahanthappa, F. Yu (2009)
A4 for leptons: Csaki, Delaunay, Grojean, Grossmann (2008)

- TBM mixing: common bulk mass term, no tree-level FCNCs

- TBM mixing and masses decouple: no fine-tuning

- can accommodate both normal & inverted mass orderings

- **Family Symmetry: alternative to MFV to avoid FCNCs in TeV scale new physics**

- many family symmetries violate MFV, possible new FV contributions



Summary & Discussions

- Intensity Frontier: probe high (GUT) scale physics not accessible to collider experiments
 - CP violation (neutrino experiments, ...)
 - Baryon number non-conservation (nucleon decay searches, N - N bar oscillation, ...)
 - Lepton number non-conservation (neutrino-less double beta decay)
 - Charged Lepton flavor violation (CLFV)
 - Majorana vs Dirac (neutrino-less double beta decay)
- Cosmic Frontier
 - N_{eff}
 - absolute mass scale of neutrinos
 - leptogenesis
- Energy Frontier
 - CLFV predictions in GUT flavor models
 - new particles and interactions in TeV scale seesaws
 - correlations in TeV scale (SUSY) seesaws