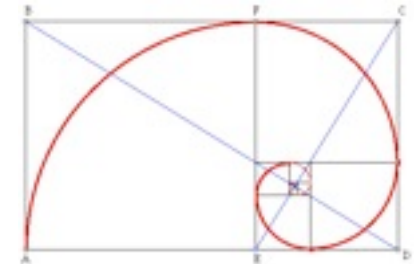
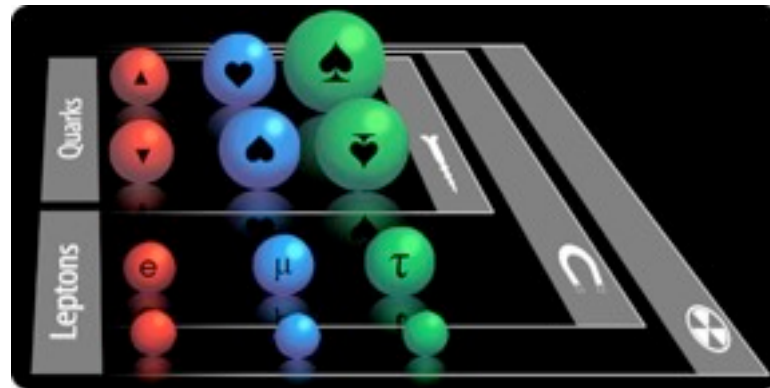
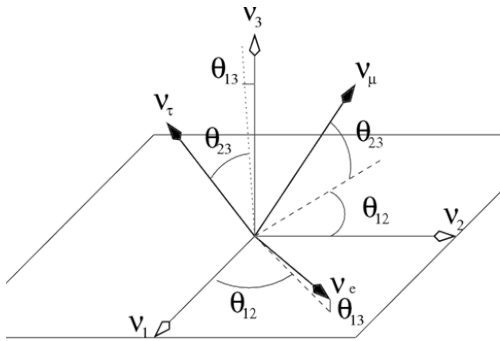


Perspectives on Neutrino Mass Models



Lisa L. Everett
Snowmass on the Pacific, KITP
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The Big Picture -- Many Questions Remain

- How many light neutrinos?

Anomalies: LSND, MiniBooNE, Gallium, Reactor
eV-scale sterile neutrinos? But tension still with all oscillation data
see e.g. Kopp et al., [1303.3011](#), Abazajian et al. [1204.5379](#) (white paper),...

Thus: restrict here to 3-family neutrino models only

SM \longrightarrow ν SM

- Still, many questions:

Nature of neutrino mass suppression? Majorana? Dirac?
Mass hierarchy? **Lepton mixing angle pattern?** CP violation?
Implications for BSM paradigms? Connections to other NP?

The Flavor Puzzle, Rejuvenated

Flavor puzzle of SM is notoriously difficult...

Still difficult in ν SM, but more interesting --

One primary reason: two large mixing angles!

$$\theta_{23} \simeq 45^\circ \pm 5^\circ \quad \theta_{12} \simeq 34^\circ \pm 1^\circ$$

3-family models: handwave a bit (in diagonal charged lepton basis)

3	small angles	\longrightarrow	\sim diagonal \mathcal{M}_ν	} (“easy”)
1	large, 2 small	\longrightarrow	$\sim \text{Rank} \mathcal{M}_\nu < 3$	
3	large angles	\longrightarrow	anarchical \mathcal{M}_ν	} (“harder”)
2	large, 1 small	\longrightarrow	fine-tuning, non-Abelian	

Anarchy vs. Structure

→ The question: is θ_{13} large or small?

$$\theta_{13} \simeq 9^\circ \pm 1^\circ$$

Post-March 2012 case for anarchy: [de Gouvea and Murayama, 1204.1249](#)

some recent explicit realizations: [Bai and Torroba, 1210.2394](#)
[Altarelli et al., 1207.0587,...](#)

Focus here on structure (symmetry):

Paradigm: discrete non-Abelian family symmetry
(subgroup of $SO(3)$ or $SU(3)$, broken
to some appropriate coset space)

Main issue/challenge: many theoretical starting points

Role of Small (Cabibbo-sized?) Corrections

Quark sector:

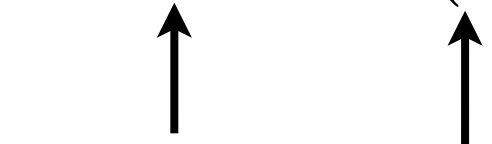
$$\mathcal{U}_{\text{CKM}} \sim 1 + O(\lambda_C)$$

Cabibbo angle λ_C (or some power) as a flavor expansion parameter

Lepton sector:

$$\mathcal{U}_{\text{MNSP}} \sim \mathcal{W} + O(\lambda')$$

“bare” mixing angles $(\theta_{12}^0, \theta_{13}^0, \theta_{23}^0)$ perturbations



choice of bare mixing angles? depends on perturbations

Unification paradigm (broad sense): useful to take

$$\lambda' = \lambda_C$$

ideas of quark-lepton complementarity and “Cabibbo haze”

Raidal '04, Minakata+Smirnov, '04, many others...

Ramond and collaborators (including yours truly...)

Long before 2012, it was conjectured that θ_{13} is a Cabibbo effect

$$\theta_{13} \sim \frac{\lambda_C}{\sqrt{2}} \sim \lambda_C \cos \theta_{23}^0$$

Ramond '03, '04,...

(general idea often called “charged lepton corrections”) $\mathcal{U}_{\text{MNSP}} \sim \mathcal{U}_{\text{CKM}}^\dagger \mathcal{W}$

good fit to data! but nontrivial to implement...

one reason: now $\sim \lambda_C$ corrections floating around

Family Symmetry Model (Broad) Taxonomy

Pre-March 2012 most models: $\theta_{23}^0 = 45^\circ$ $\theta_{13}^0 = 0^\circ$

Choices for “bare” solar angle θ_{12}^0 :

(1) within $\sim \lambda_C^2$ of exp:

tri-bimaximal mixing

$$\tan \theta_{12}^0 = \frac{1}{\sqrt{2}} \quad \theta_{12}^0 = 35.26^\circ$$

“the beautiful matrix
with the ugly name”

Harrison, Perkins, Scott '02

(100s of papers. Key players include
Ma, Chen et al., Altarelli et al.,...)

others, such as **golden ratio** mixing $\phi = (1 + \sqrt{5})/2$

$$\tan \theta_{12} = \phi^{-1} \quad \theta_{12} = 31.72^\circ \quad \text{or} \quad \cos \theta_{12} = \frac{\phi}{2} \quad \theta_{12} = 36^\circ$$

Ramond, Kajiyama et al.,
LE+Stuart (+Ding), Feruglio et al.,...

Rodejohann et al.,...

(2) within $\sim \lambda_C$ of exp:

bimaximal mixing

$$\tan \theta_{12}^0 = 1 \quad (\text{quark-lepton complementarity})$$

Post-March 2012

- **Keep** $\theta_{23}^0 = 45^\circ$ $\theta_{13}^0 = 0^\circ$

(1) within $\sim \lambda_C^2$ of exp:

need to **control corrections** to ensure other angles not shifted out of experimentally allowed ranges

TBM (or other mixing scenarios) as leading order framework
original scenarios need modifying; this however is doable
(CP phases often play a significant role)

Lin 0905.3534 -- anticipated issue and proposed a solution
See also e.g. Ma '12, King+Stuart et al. '12, other talks here,...

(2) within $\sim \lambda_C$ of exp: resurgence?

- **Modify** $\theta_{23}^0 = 45^\circ$ $\theta_{13}^0 = 0^\circ$

θ_{13} numerology

drop maximal θ_{23} (some hints in data)?

Some final thoughts...

- **Exciting times!** Lots of ideas, lots of room for more
- issue of **connection to observations** and **testability**
 → requires NP!
 but NP generically comes with its own flavor puzzle
 how to disentangle?
- role of **CP phases** -- new focus
 connection to **leptogenesis** highly model dependent
 better **soundbite/motivation** for exp program??