

Snowmass on the
Pacific @ KITP

Lattice gauge theories and the composite Higgs

(on behalf of the USQCD BSM group)

Julius Kuti

University of California, San Diego

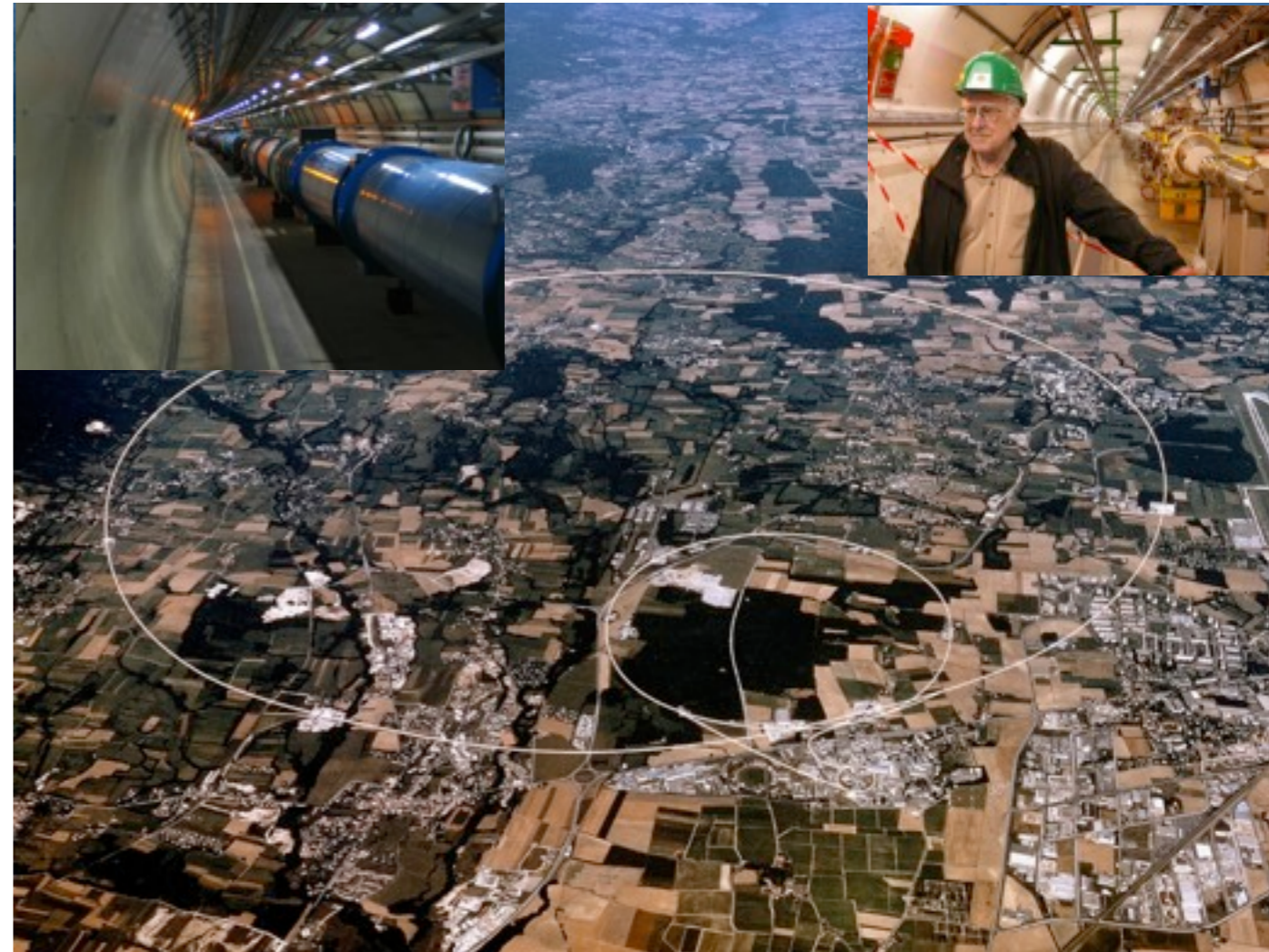
Snowmass on the Pacific @ KITP, May 29-31, 2013

Large Hadron Collider - CERN

primary mission:

- **Search for Higgs particle**
- **Origin of Electroweak symmetry breaking**

- A Higgs-like particle is found
Is it the Standard Model Higgs?
- Or, new strong dynamics?
- Composite Goldstone-like Higgs?
- SUSY?



Large Hadron Collider - CERN

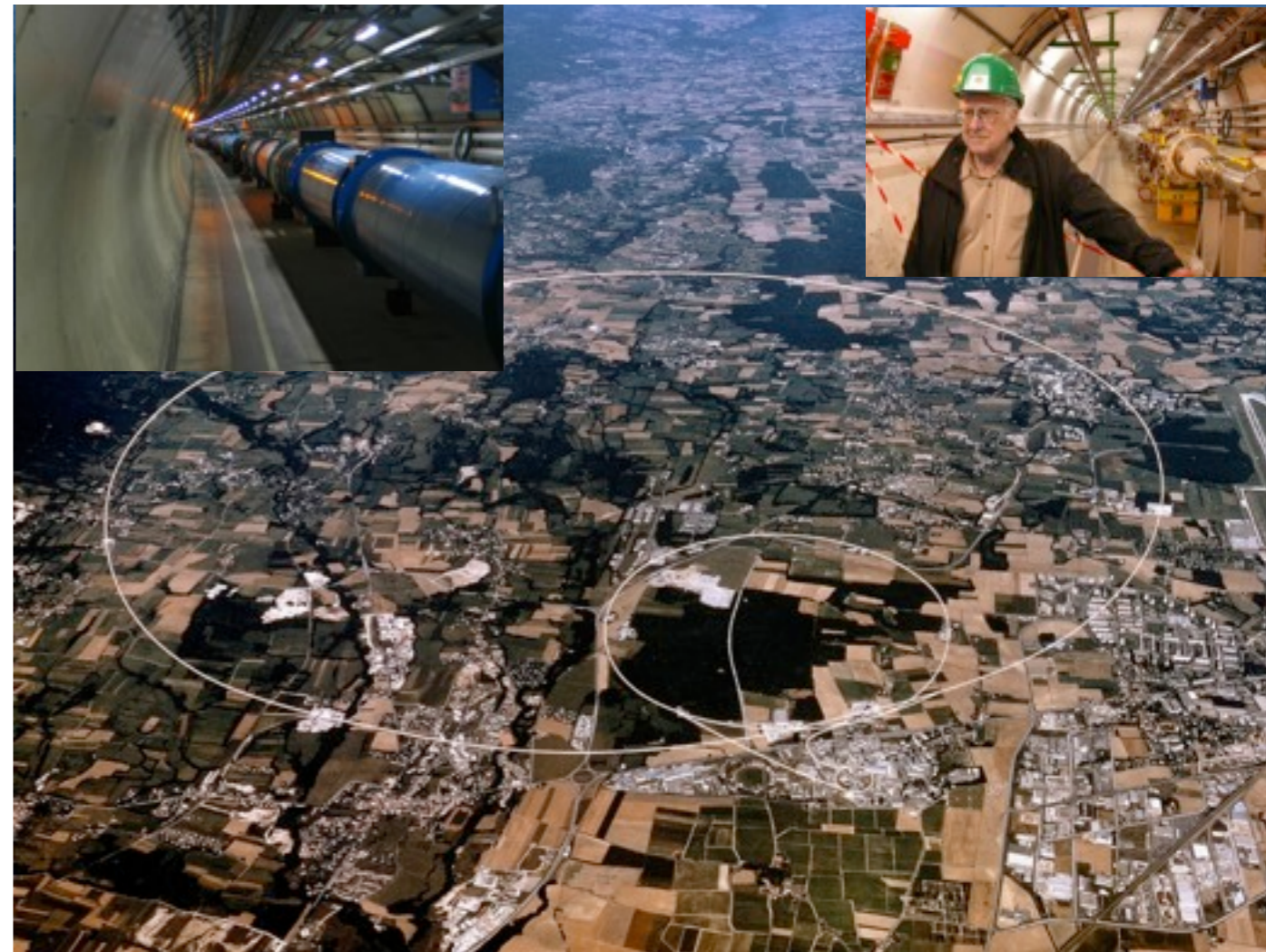
primary mission:

- *Search for Higgs particle*
- *Origin of Electroweak symmetry breaking*

- A Higgs-like particle is found
Is it the Standard Model Higgs?
- Or, new strong dynamics?
- Composite Goldstone-like Higgs?
- SUSY?



Primary focus of USQCD BSM effort and this short talk



LATTICE GAUGE THEORIES AT THE ENERGY FRONTIER

Thomas Appelquist, Richard Brower, Simon Catterall, George Fleming,
Joel Giedt, Anna Hasenfratz, Julius Kuti, Ethan Neil, and David Schaich

(USQCD Collaboration)

(Dated: March 10, 2013)

USQCD BSM White Paper - community based effort:

LATTICE GAUGE THEORIES AT THE ENERGY FRONTIER

Thomas Appelquist, Richard Brower, Simon Catterall, George Fleming,
Joel Giedt, Anna Hasenfratz, Julius Kuti, Ethan Neil, and David Schaich

(USQCD Collaboration)

(Dated: March 10, 2013)

USQCD BSM White Paper - community based effort:

- to identify most significant lattice results of last few years
- to identify major research directions for planning
- to describe BSM lattice toolset with phenomenological applications
- estimate resources needed for the plan

New hardware proposal submitted including USQCD BSM plans

Introducing USQCD BSM groups with highlighted publications:

(approximately 1/5 of USQCD community)

select publications of Lattice Strong Dynamics (LSD) collaboration:

WW Scattering Parameters via Pseudoscalar Phase Shifts

[Thomas Appelquist](#) (Yale U.), [Ron Babich](#), [Richard C. Brower](#) (Boston U.), [Michael I. Buchoff](#), [Michael Cheng](#) (LLNL, Livermore), [Michael A. Clark](#) (Harvard-Smithsonian Ctr. Astrophys.), [Saul D. Cohen](#) (Washington U., Seattle), [George T. Fleming](#) (Yale U.), [Joe Kiskis](#) (UC, Davis), [Meifeng Lin](#) (Yale U.) *et al.*. Jan 2012. 8 pp.
Published in **Phys.Rev. D85 (2012) 074505**

select publication from Lattice Higgs Collaboration (LHC):

Can the nearly conformal sextet gauge model hide the Higgs impostor?

[Zoltan Fodor](#) (Wuppertal U. & IAS, Julich & Eotvos U.), [Kieran Holland](#) (U. Pacific, Stockton), [Julius Kuti](#) (UC, San Diego), [Daniel Nogradi](#) (Eotvos U.), [Chris Schroeder](#) (LLNL, Livermore), [Chik Him Wong](#) (UC, San Diego). Sep 2012.
10 pp.
Published in **Phys.Lett. B718 (2012) 657-666**

select publications of SUSY group:

Phase Structure of Lattice N=4 Super Yang-Mills

[Simon Catterall](#), [Poul H. Damgaard](#), [Thomas Degrand](#), [Richard Galvez](#), [Dhagash Mehta](#). Sep 2012. 28 pp.
Published in **JHEP 1211 (2012) 072**

Neutralino-hadron scattering in the NMSSM

[Sophie J. Underwood](#) (Adelaide U.), [Joel Giedt](#) (Rensselaer Poly.), [Anthony W. Thomas](#), [Ross D. Young](#) (Adelaide U.). Mar 2012. 4 pp.
Published in **Phys.Rev. D86 (2012) 035009**

select publication of Boulder BSM collaboration:

MCRG study of 8 and 12 fundamental flavors

[Gregory Petropoulos](#), [Anqi Cheng](#), [Anna Hasenfratz](#), [David Schaich](#) (Colorado U.).
Dec 2012. 7 pp.
Published in **PoS LATTICE2012 (2012) 051**
To appear in the proceedings of Conference: [C12-06-24 Proceedings](#)
e-Print: [arXiv:1212.0053](#) [hep-lat] | [PDF](#)

select publication of BSM finite temperature studies:

QCD with colour-sextet quarks

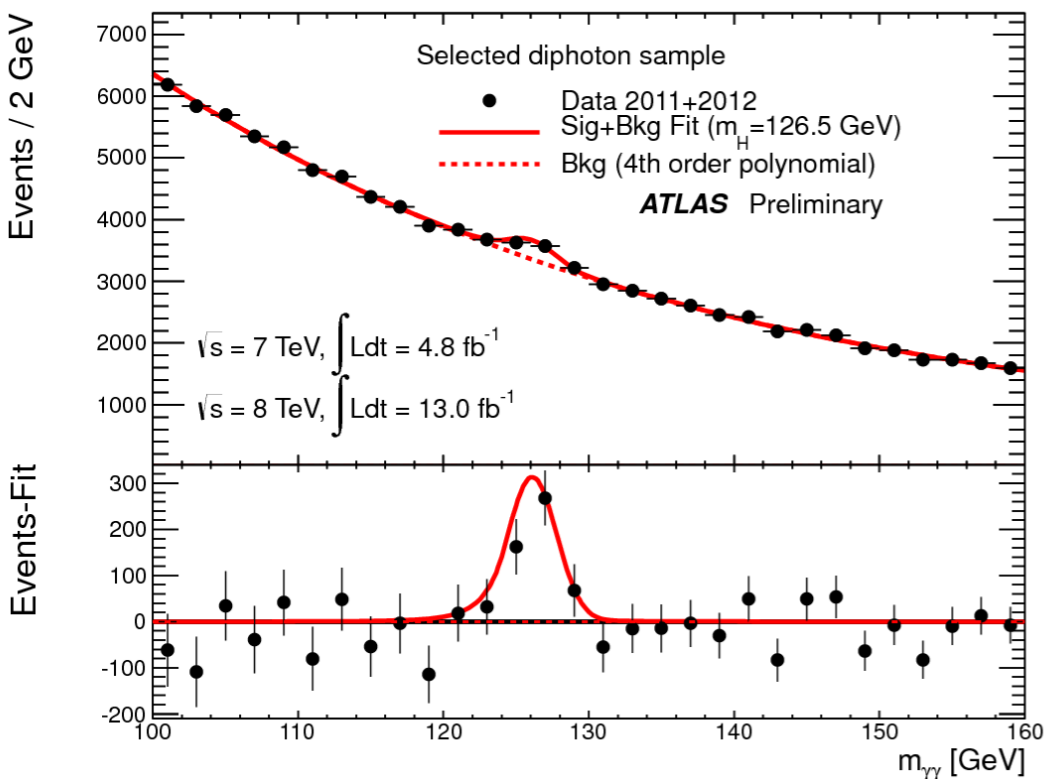
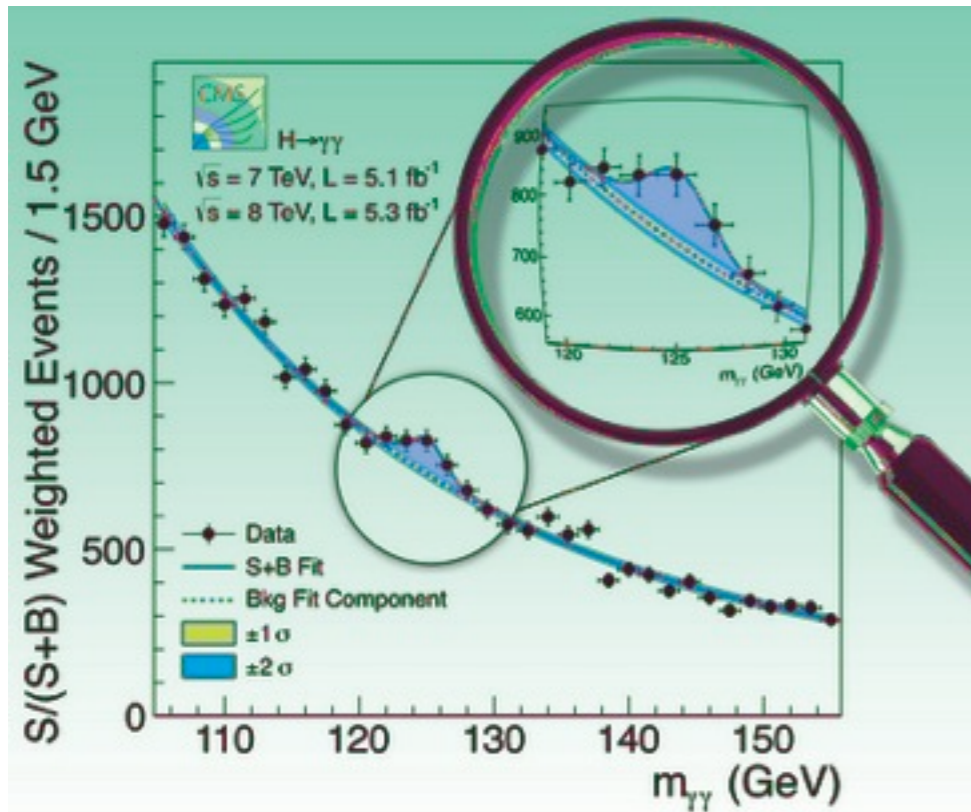
[D.K. Sinclair](#), [J.B. Kogut](#). Nov 2012. 7 pp.
Published in **PoS LATTICE2012 (2012) 026**

Rational for BSM:

voices: a light Higgs-like scalar is found which is consistent with SM within errors and no composite states have been seen below 1 TeV, ergo no need for BSM based compositeness. Besides, how do you get a light Higgs from compositeness?

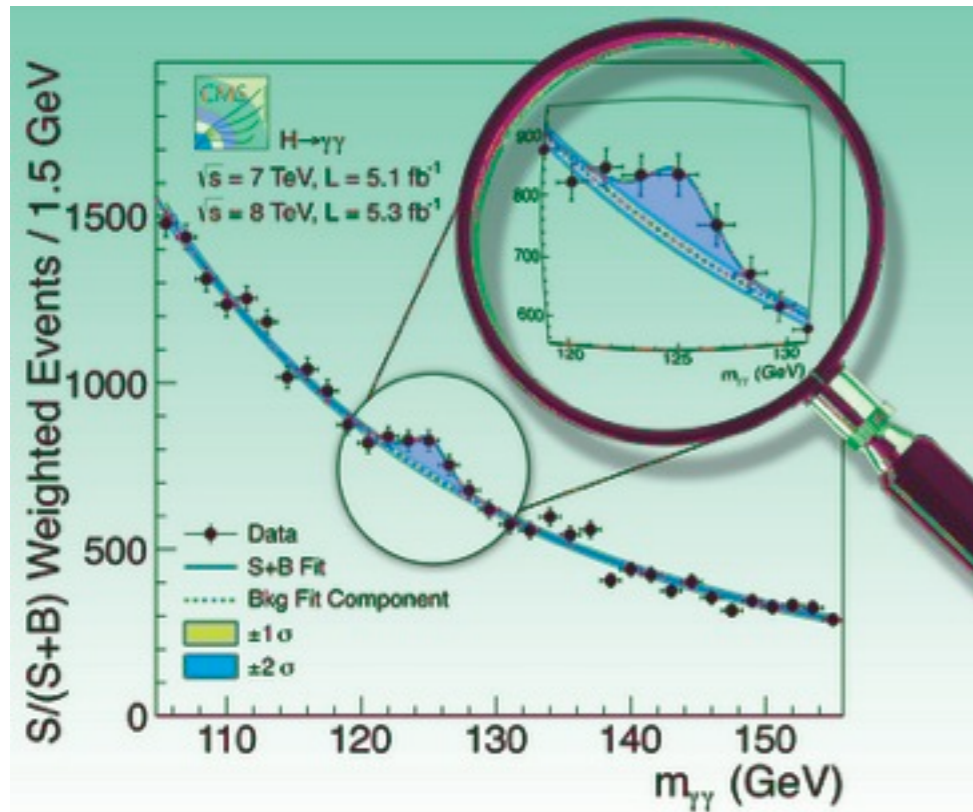
facts: Compositeness and a light Higgs scalar are not incompatible; search for composite states in the LHC7/8 runs was not based on solid predictions but on naively scaled up QCD and on unacceptable old technicolor guessing games. This alone does not make compositeness right!

plans: LHC14 will search for new physics from compositeness and SUSY, and the USQCD BSM group is preparing quantitative lattice based predictions to rule in or rule out



Rational for BSM:

three USQCD BSM directions based on gauge force:

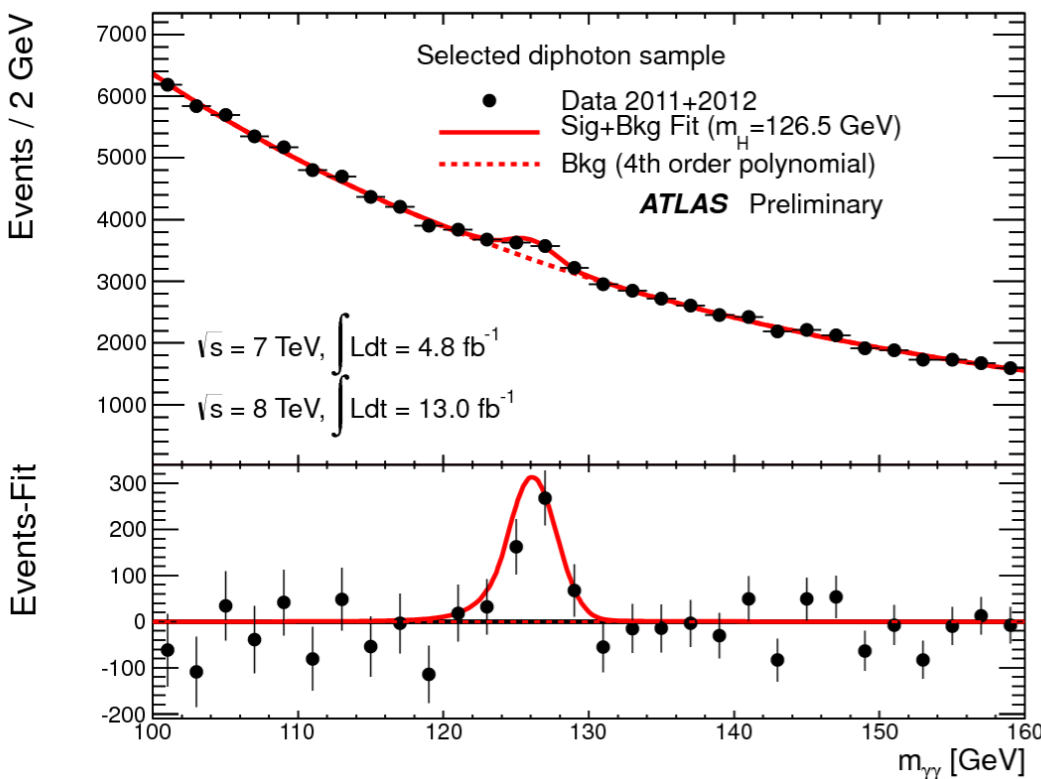


- strongly coupled near-conformal gauge theories
 - light scalar is expected from approximate scale invariance (dilaton, or just light scalar?)
 - QCD is NOT approximately scale invariant making old technicolor guessing games irrelevant

- light pseudo-Goldstone boson (like little Higgs)
 - starts from a scalar massless Goldstone boson
 - expects to make quantitative predictions about composite spectrum above 1 TeV

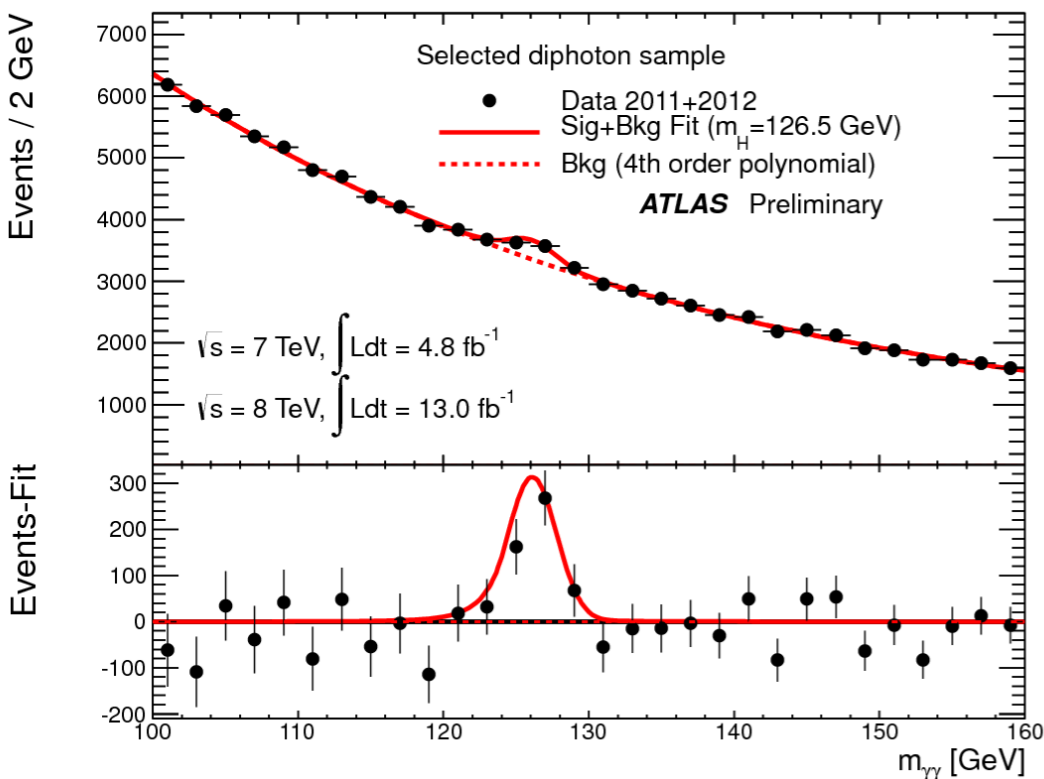
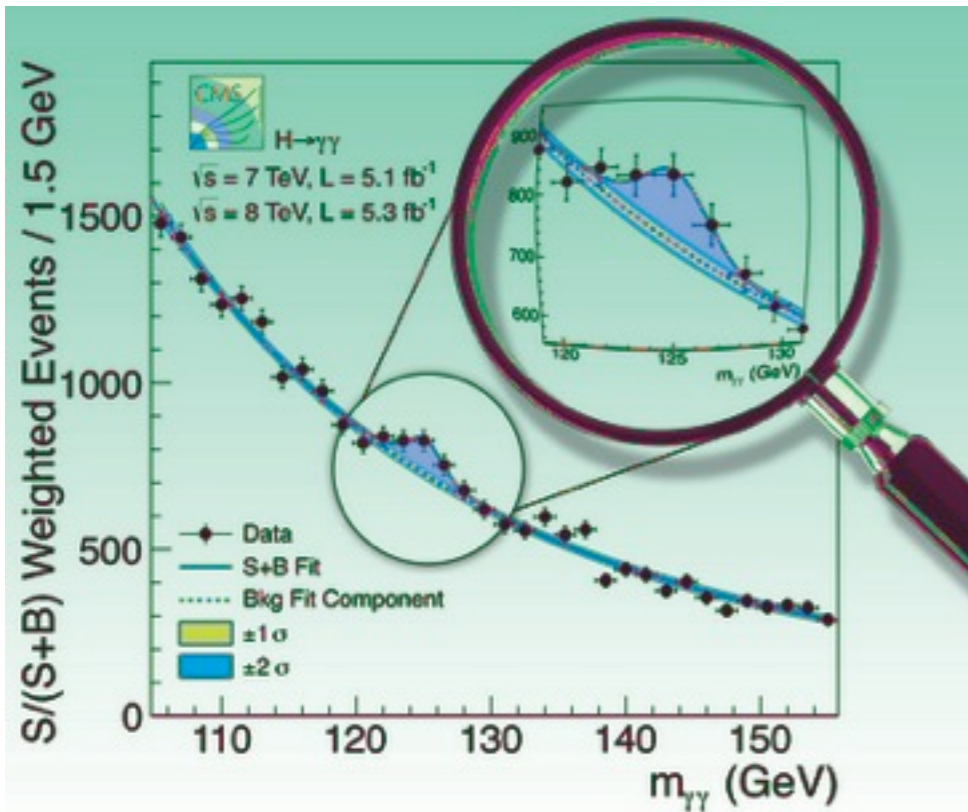
• SUSY

- for better understanding of dynamical symmetry breaking and to explore susy theory scenarios
- We are calculating quantitative predictions for LHC14 (e.g. sextet model)



Rational for BSM:

three USQCD BSM directions based on gauge force:



- strongly coupled near-conformal gauge theories
 - light scalar is expected from approximate scale invariance (dilaton, or just light scalar?)
 - QCD is NOT approximately scale invariant making old technicolor guessing games irrelevant
- light pseudo-Goldstone boson (like little Higgs)
 - starts from a scalar massless Goldstone boson
 - expects to make quantitative predictions about composite spectrum above 1 TeV
- SUSY
 - for better understanding of dynamical symmetry breaking and to explore susy theory scenarios
 - We are calculating quantitative predictions for LHC14 (e.g. sextet model)

Compositeness

Rational for BSM:

three USQCD BSM directions based on gauge force:

- strongly coupled near-conformal gauge theories
 - light scalar is expected from approximate scale invariance (dilaton, or just light scalar?)

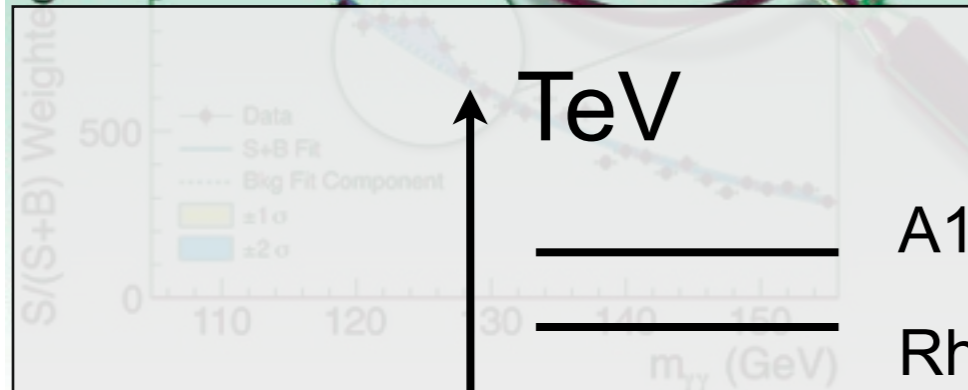
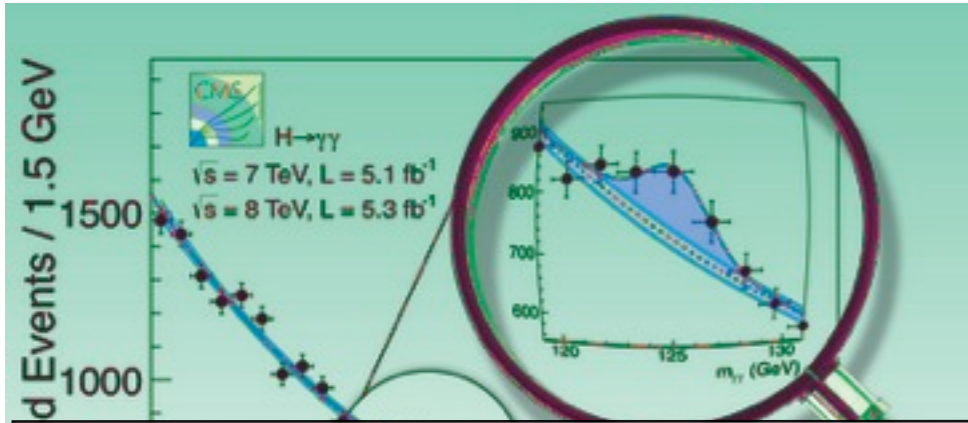
from approximate scale invariance

- QCD is NOT approximately scale invariant
- making old technicolor/guessing games irrelevant

light pseudo-Goldstone boson (like little Higgs)

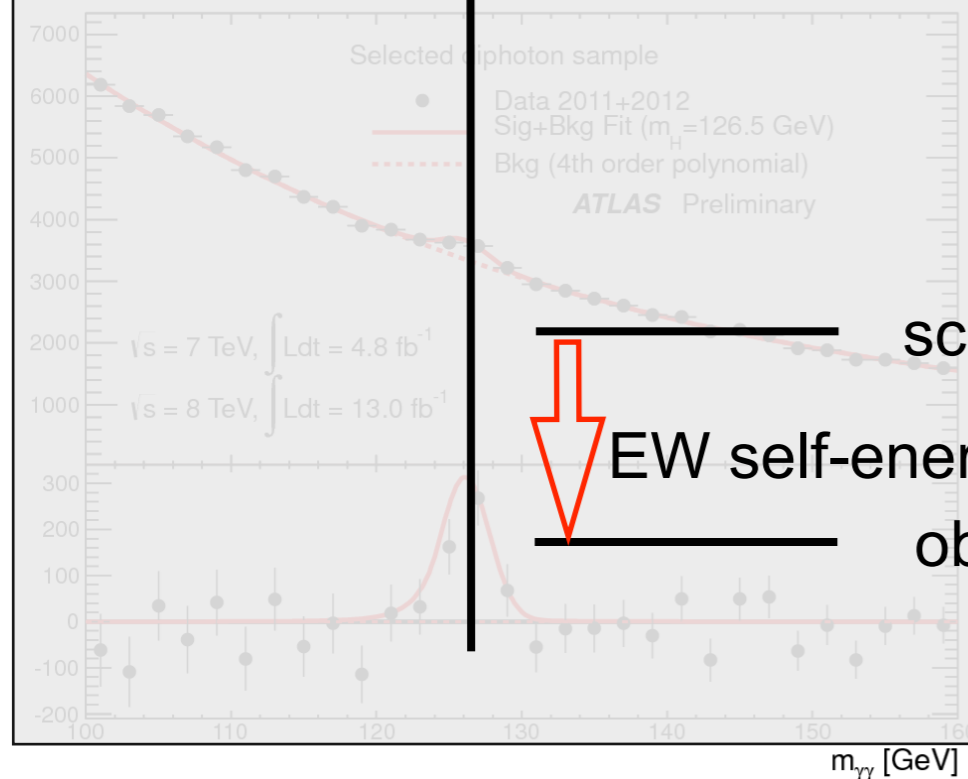
- starts from a scalar massless Goldstone boson

- expects to make quantitative predictions about composite spectrum above 1 TeV



A1 ~ 2.4 TeV

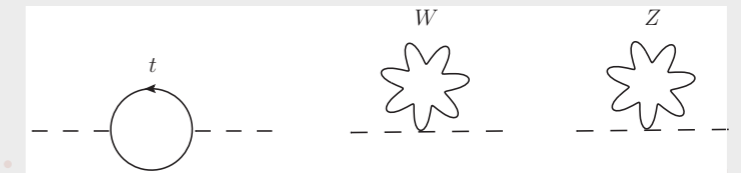
Rho ~ 1.7 TeV



scalar composite at 500 GeV?

EW self-energy

observed Higgs-like

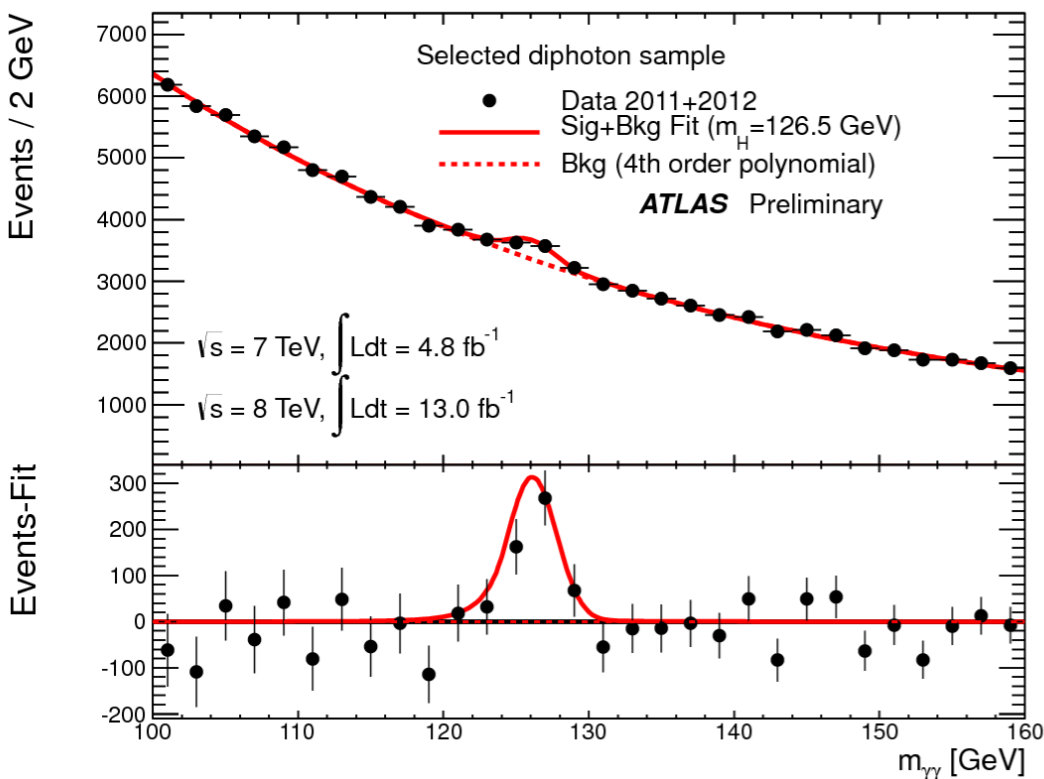
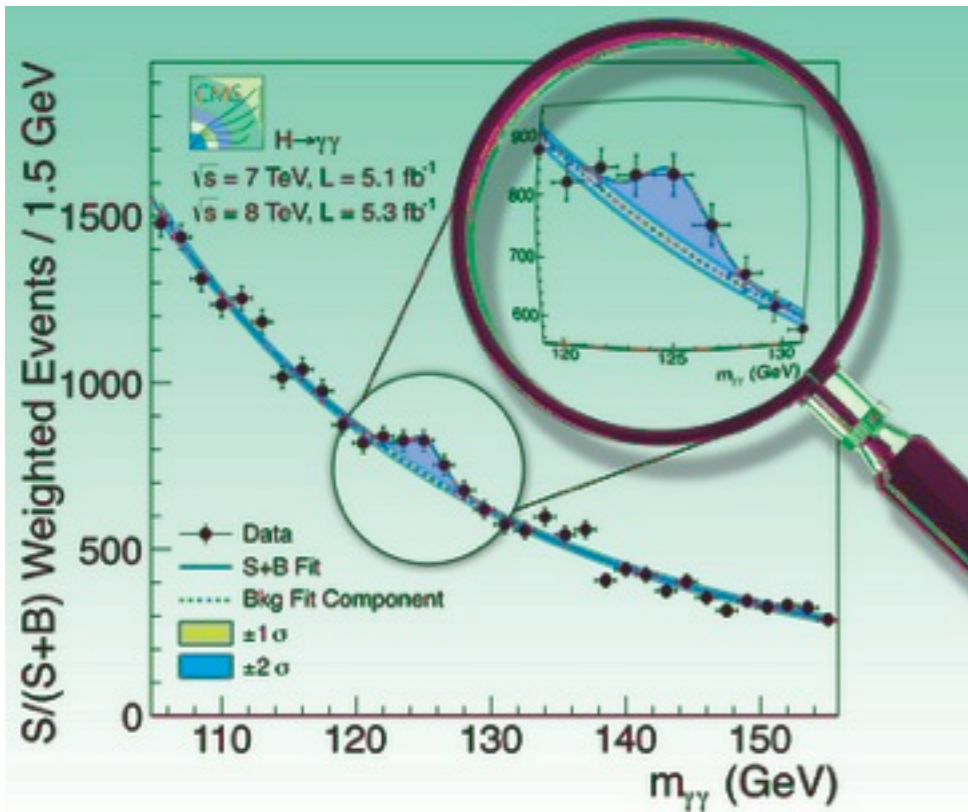


$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

- We are calculating quantitative predictions for LHC14 (e.g. sextet model)

Rational for BSM:

three USQCD BSM directions based on gauge force:



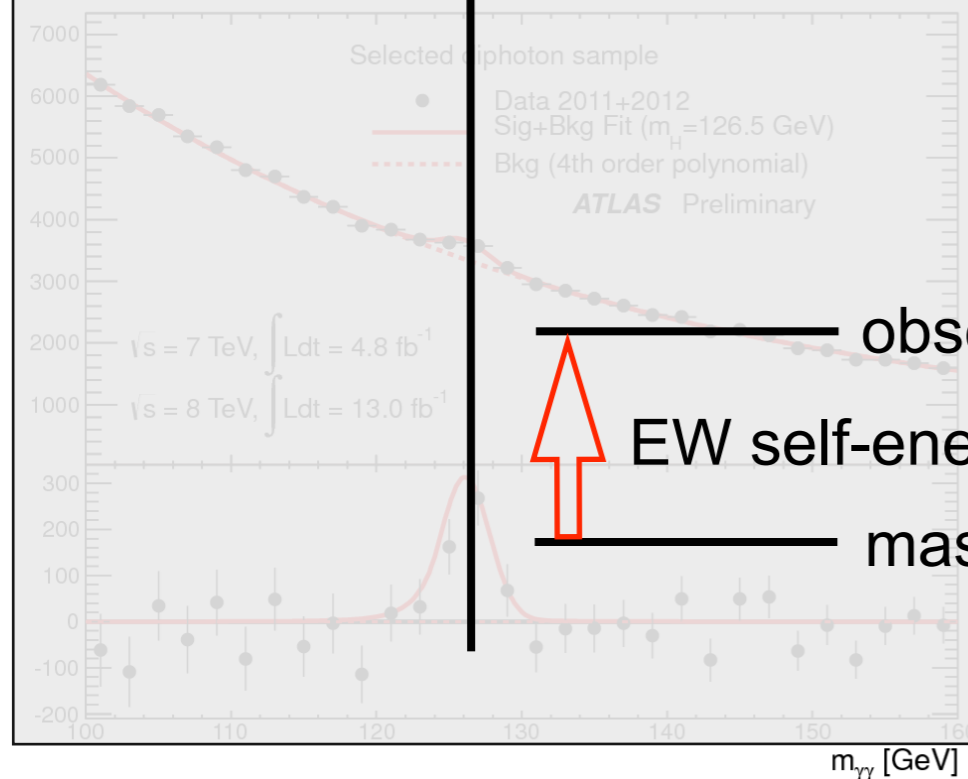
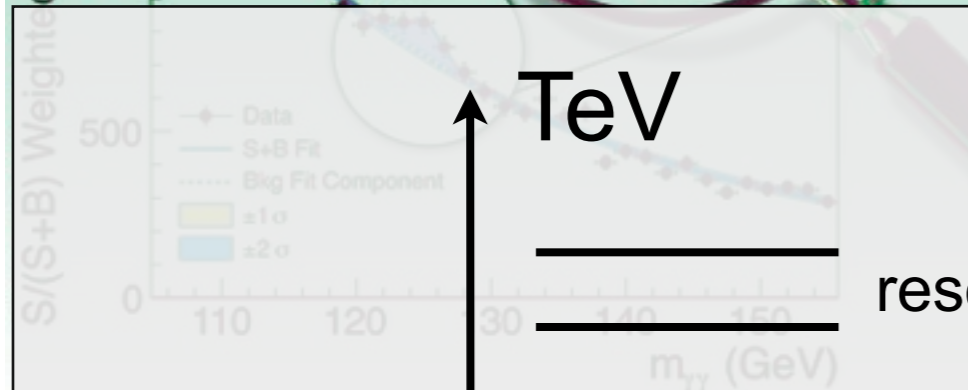
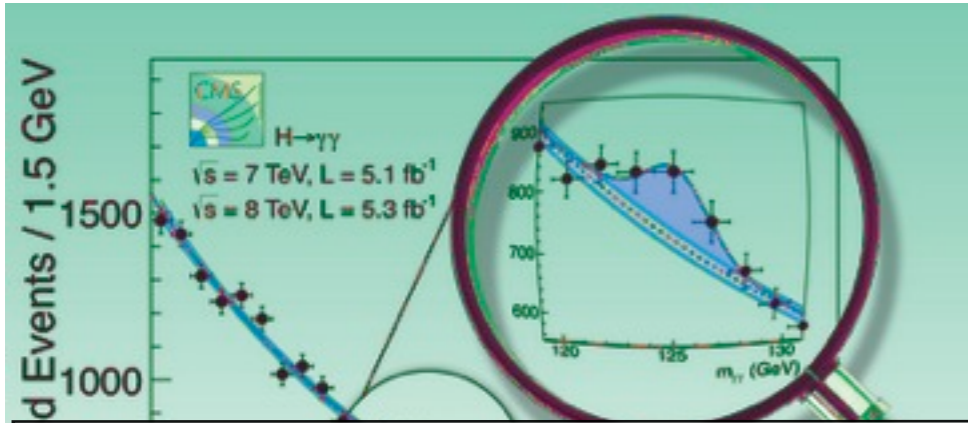
- strongly coupled near-conformal gauge theories
 - light scalar is expected from approximate scale invariance (dilaton, or just light scalar?)
 - QCD is NOT approximately scale invariant making old technicolor guessing games irrelevant
- light pseudo-Goldstone boson (like little Higgs)
 - starts from a scalar massless Goldstone boson
 - expects to make quantitative predictions about composite spectrum above 1 TeV
- SUSY
 - for better understanding of dynamical symmetry breaking and to explore susy theory scenarios
 - We are calculating quantitative predictions for LHC14 (e.g. sextet model)

Compositeness

Rational for BSM:

three USQCD BSM directions based on gauge force:

- strongly coupled near-conformal gauge theories
 - light scalar is expected from approximate scale invariance (dilaton, or just light scalar?)



PNGB (little Higgs) scenario

resonances in 1-2 TeV range

- light pseudo-Goldstone boson (like little Higgs)
 - starts from a scalar massless Goldstone boson

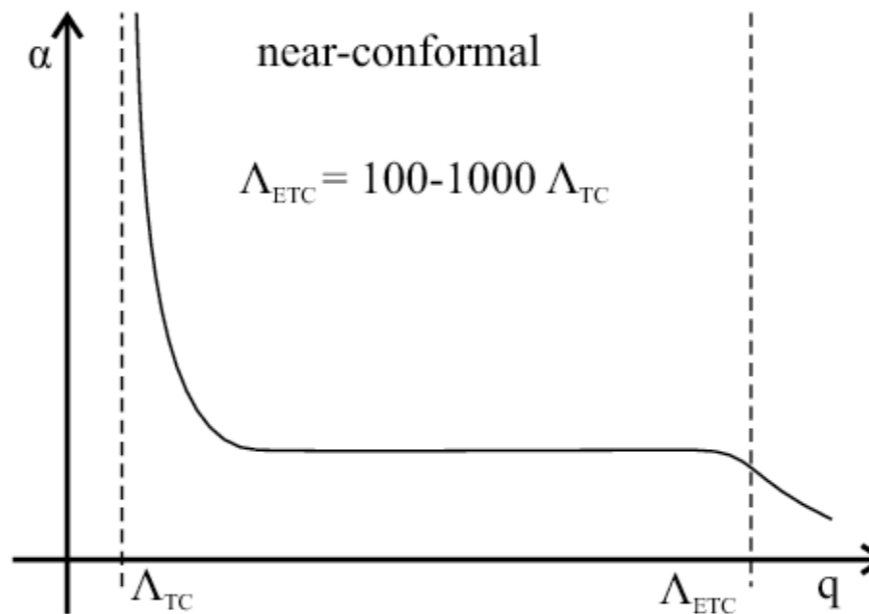
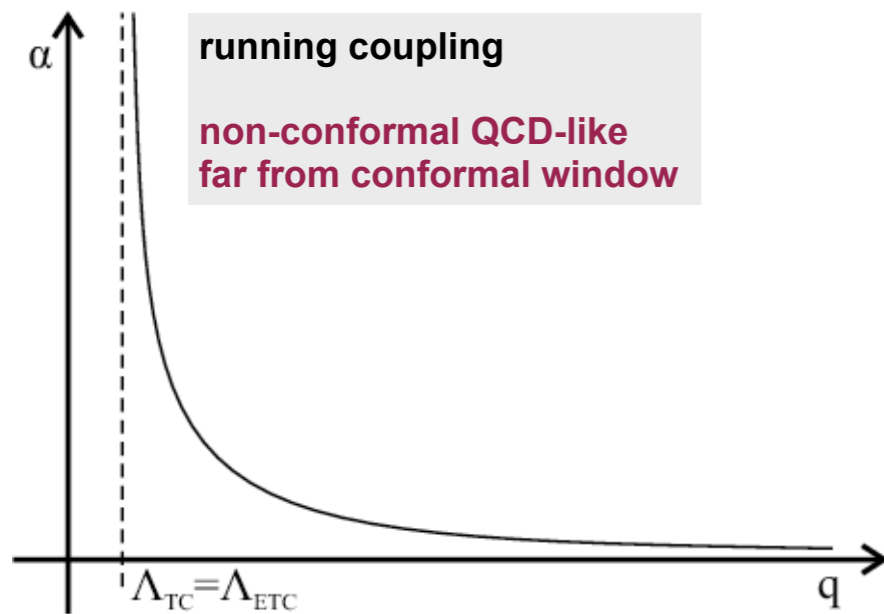
observed Higgs-like at 125 GeV

EW self-energy

massless scalar pseudo-Goldstone

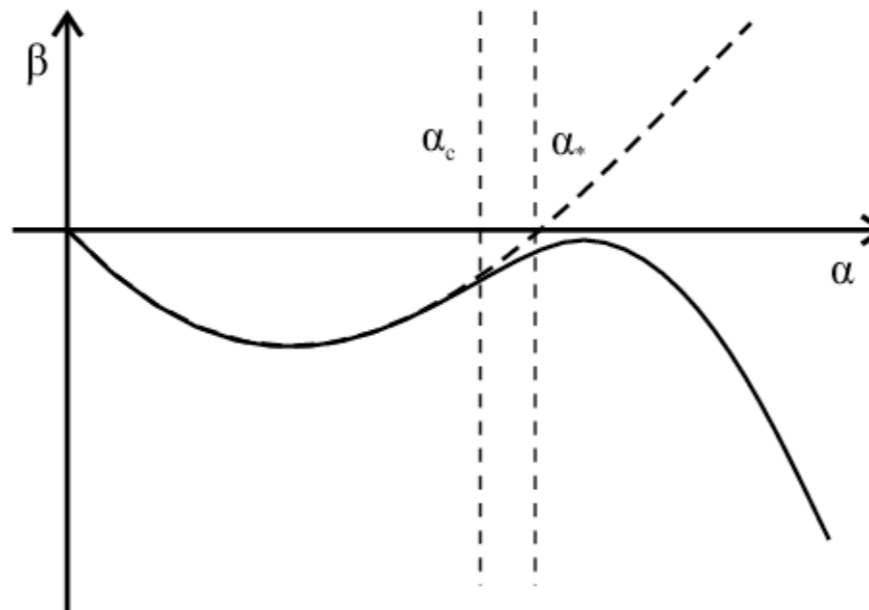
- We are calculating quantitative predictions for LHC14 (e.g. sextet model)

The light Higgs near conformality (dilaton-like?)

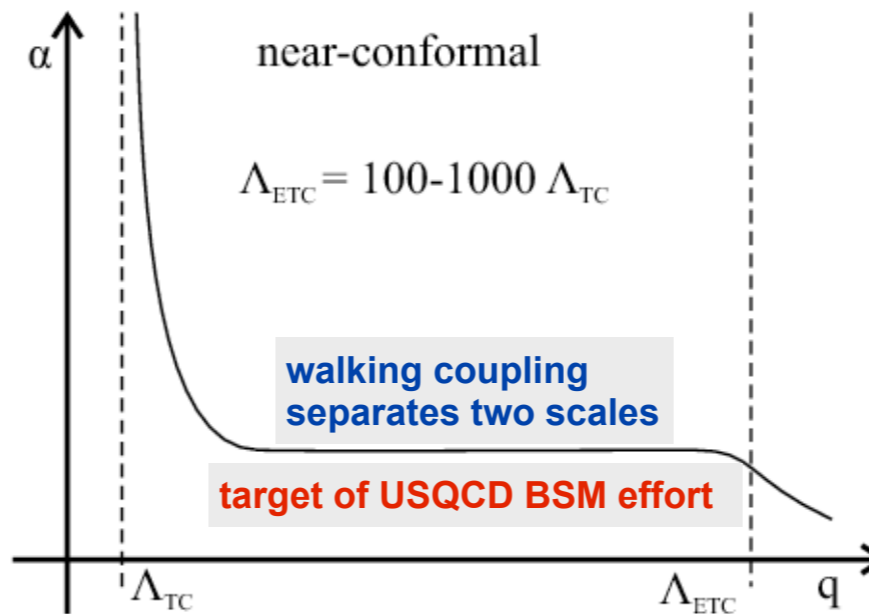
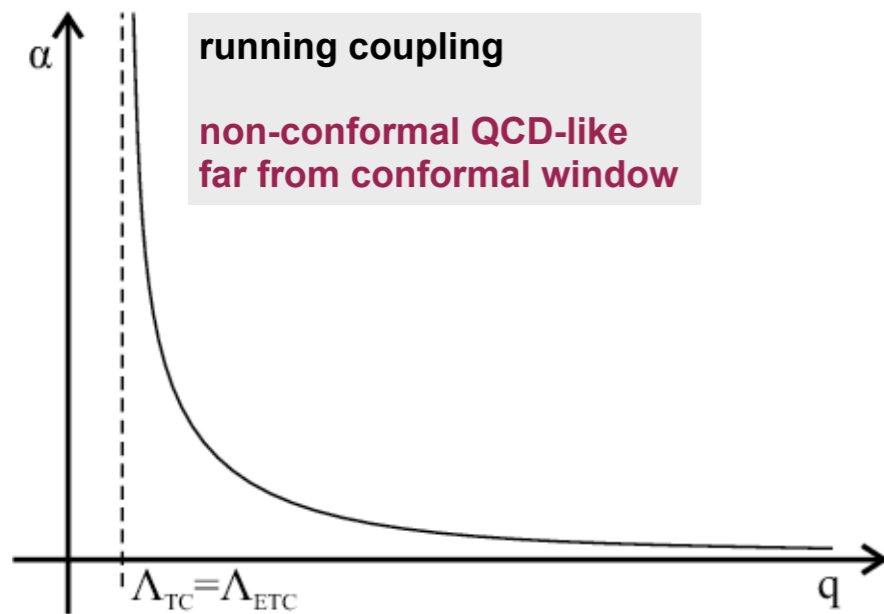


original textbook Technicolor paradigm:

- one massless fermion doublet $\begin{bmatrix} u \\ d \end{bmatrix}$
chiral SB
- three Goldstone pions
- become longitudinal components of weak bosons
- composite Higgs mechanism
scale of Higgs condensate $\sim F=250$ GeV
 $\Lambda_{TC} \sim TeV$
- flavor changing currents and fermion mass generation would be problems
- conflicts with EW precision constraints

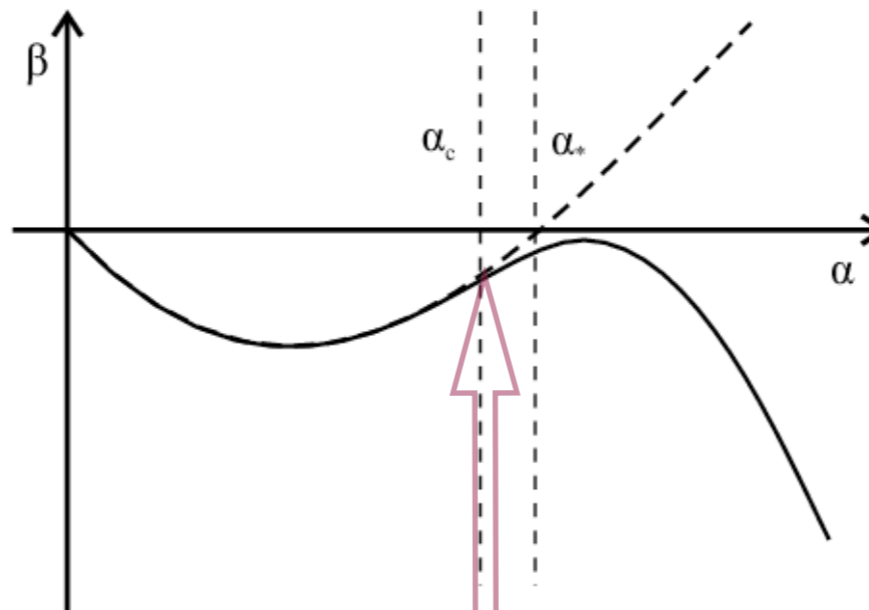


The light Higgs near conformality (dilaton-like?)



original textbook Technicolor paradigm:

- one massless fermion doublet $\begin{bmatrix} u \\ d \end{bmatrix}$ chiral SB
- three Goldstone pions
- become longitudinal components of weak bosons
- composite Higgs mechanism
scale of Higgs condensate $\sim F=250 \text{ GeV}$
 $\Lambda_{TC} \sim \text{TeV}$
- flavor changing currents and fermion mass generation would be problems
- conflicts with EW precision constraints



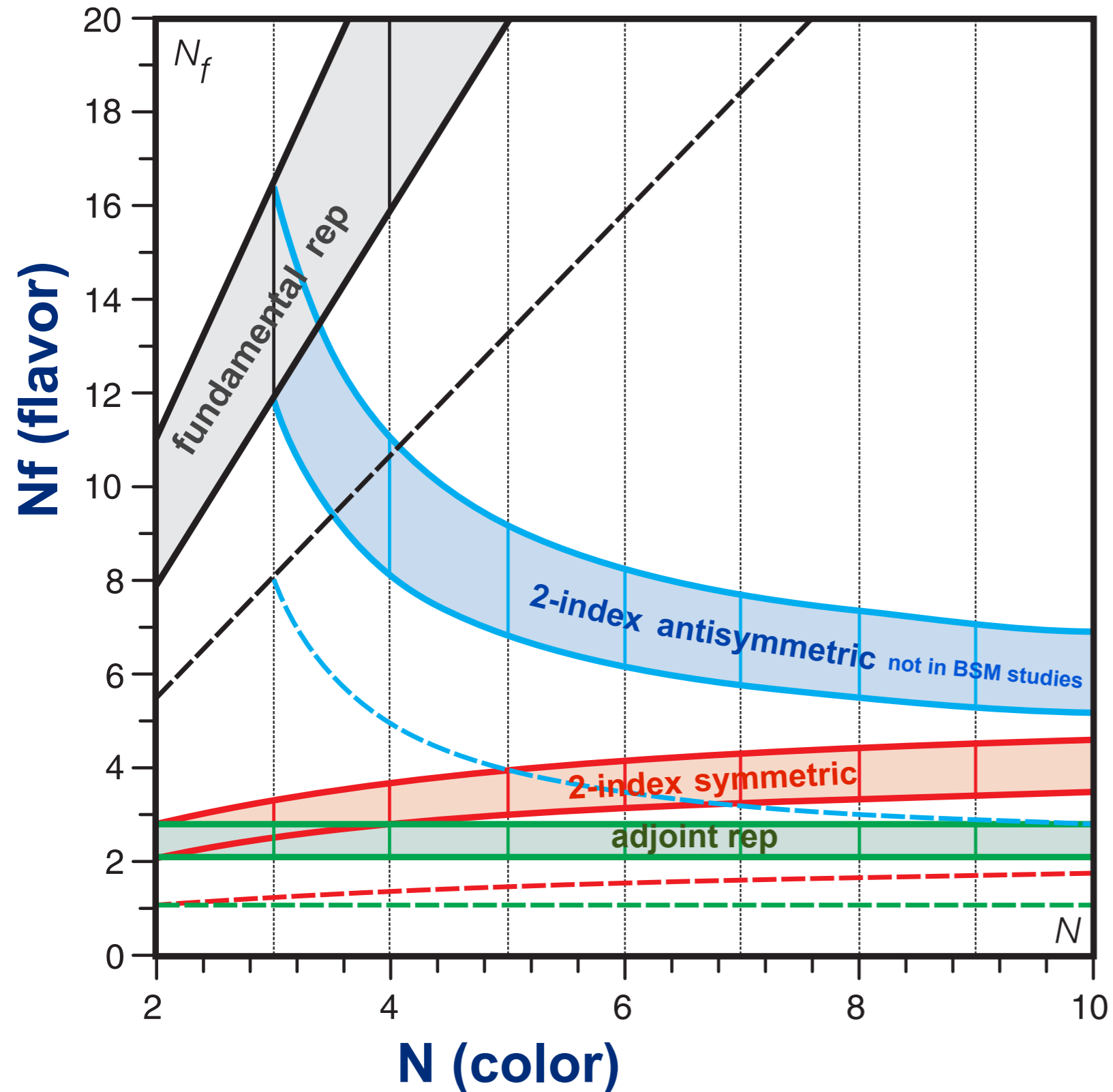
Chiral symmetry breaking
turns conformal FP into
walking

Extended Technicolor paradigm:

- requires walking gauge coupling
chiral SB on $\Lambda_{TC} \sim \text{TeV}$ scale
- fermion mass generation from
scale at $\Lambda_{ETC} \sim 100 - 1000 \Lambda_{TC}$
- can solve problem of flavor changing
currents
- composite Higgs mechanism
- broken Dilaton \rightarrow unusual
composite Higgs particle in BSM ?
- can avoid conflict with EW precision
constraints
- candidate models require non-
perturbative lattice studies

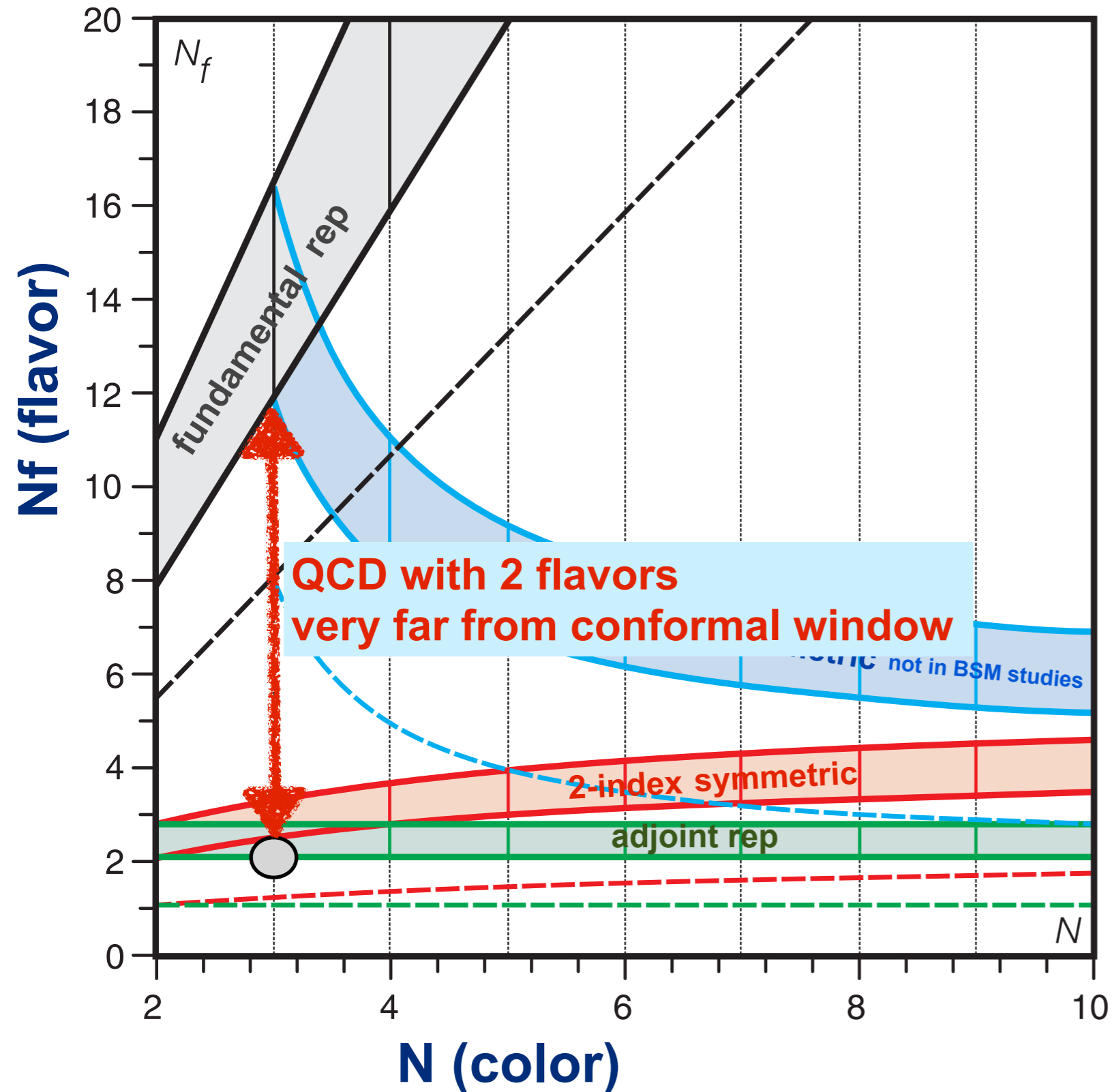
The light Higgs near conformality (dilaton-like?)

theory space and conformal window
color, flavor, and massless fermion representation



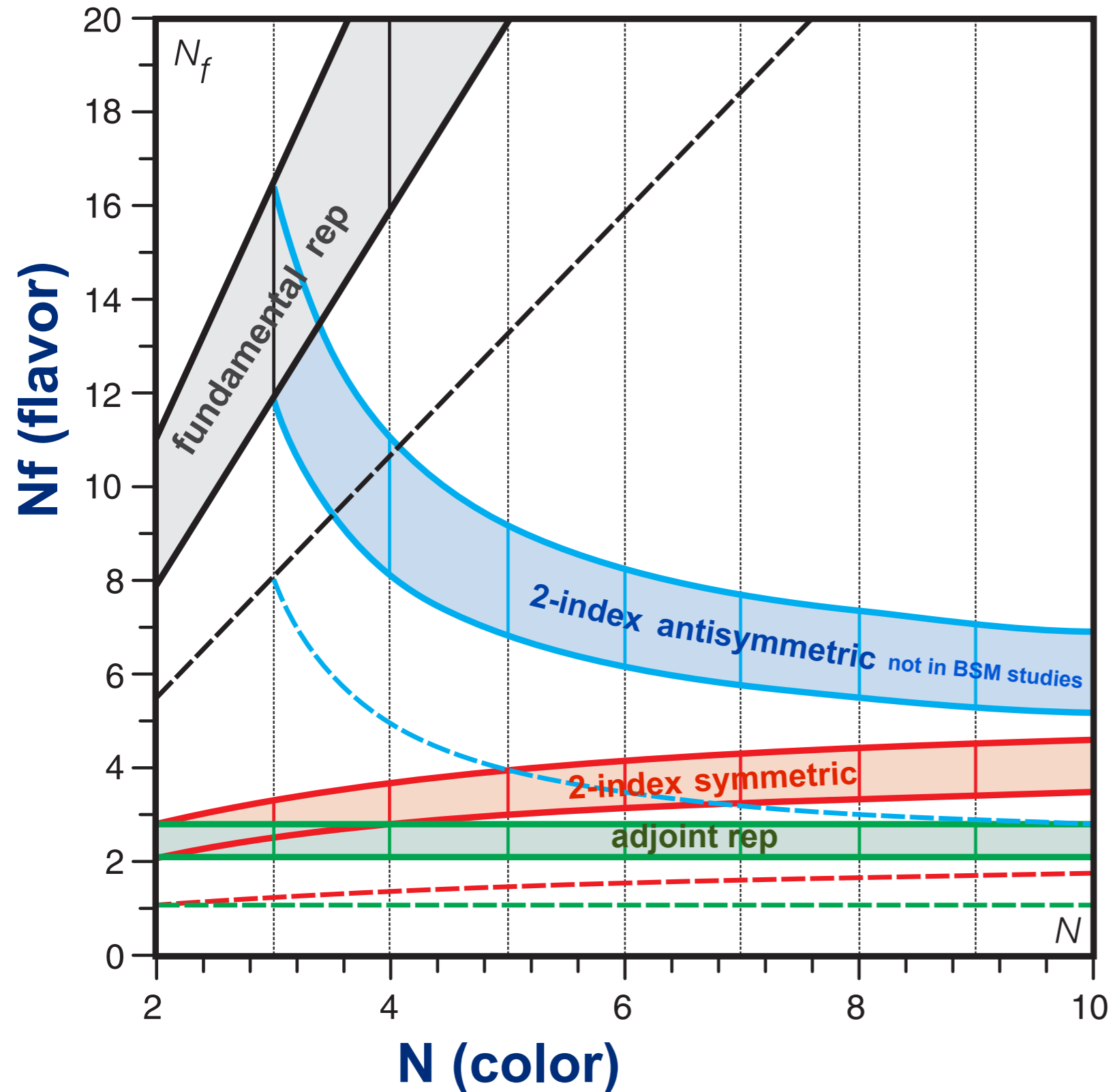
The light Higgs near conformality (dilaton-like?)

theory space and conformal window
color, flavor, and massless fermion representation



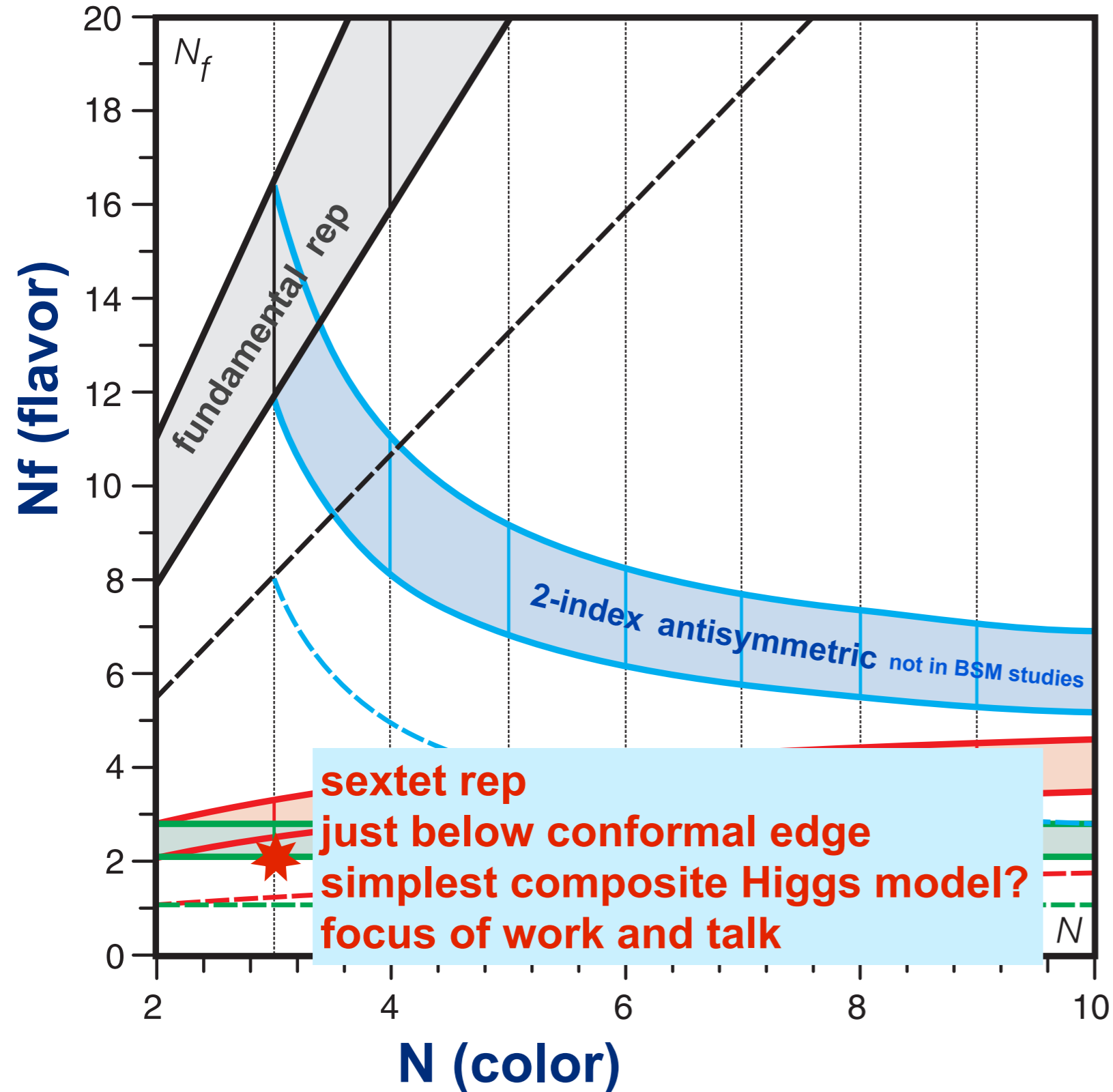
The light Higgs near conformality (dilaton-like?)

theory space and conformal window
color, flavor, and massless fermion representation



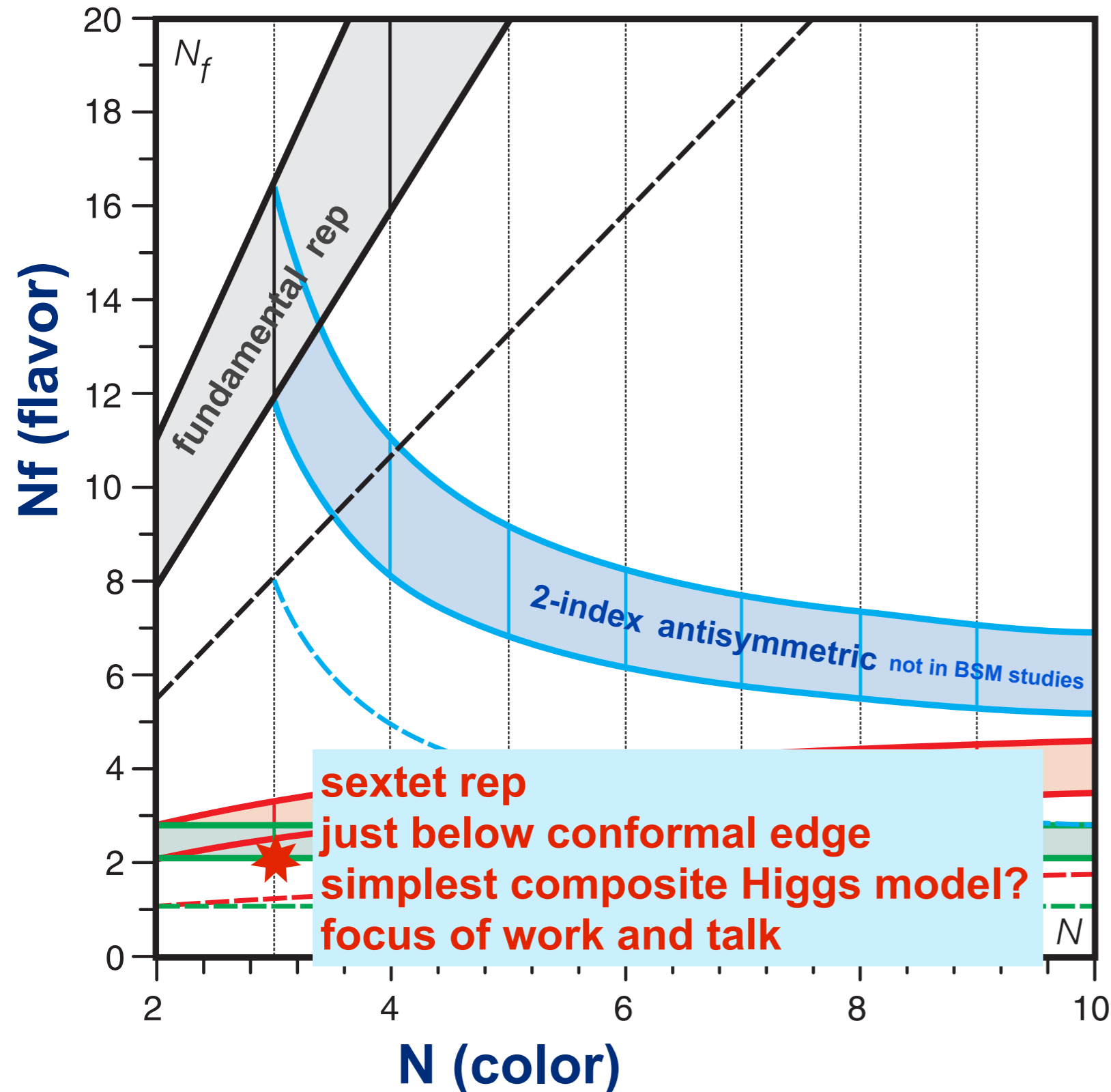
The light Higgs near conformality (dilaton-like?)

theory space and conformal window
color, flavor, and massless fermion representation



The light Higgs near conformality (dilaton-like?)

theory space and conformal window
color, flavor, and massless fermion representation



characteristics of nearly scale invariant gauge theories:

very small beta function with gauge coupling slowly changing with scale

chiral condensate with large B/F

the only input parameter is the gauge coupling which is set by the vev from the condensate

The light Higgs near conformality (dilaton-like?)

$$m_\sigma^2 \simeq -\frac{4}{f_\sigma^2} \langle 0 | [\Theta_\mu^\mu(0)]_{NP} | 0 \rangle \quad \text{Partially Conserved Dilatation Current (PCDC)}$$

there are two different expectations when conformal window is approached: $g(\mu = \Lambda) = g_c$

1. dilaton mass parametrically vanishes $m_\sigma^2 \simeq (N_f^c - N_f) \cdot \Lambda^2 \quad \frac{m_\sigma}{f_\sigma} \rightarrow 0$

2. dilaton mass finite in the limit $f_\sigma \simeq \Lambda \quad \frac{m_\sigma}{f_\sigma} \rightarrow \text{const}$

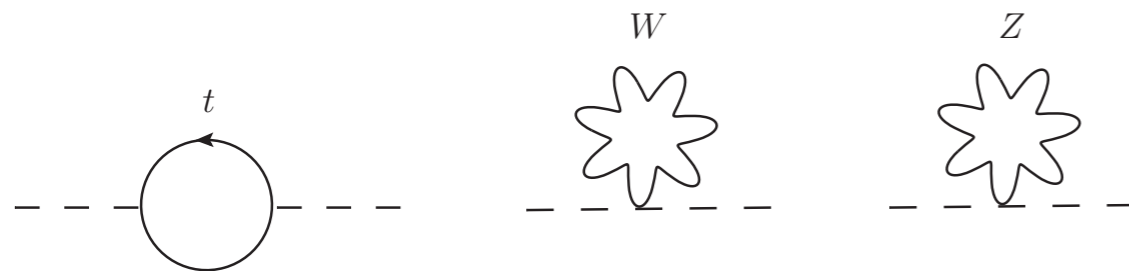
important role of $\frac{f_\pi}{f_\sigma}$ in electroweak phenomenology

both scenarios expect light Higgs-like dilaton

but how light is light ?

400-500 GeV dynamical Higgs as impostor?

Sannino



$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

The light Higgs near conformality (dilaton-like?)

$$m_\sigma^2 \simeq -\frac{4}{f_\sigma^2} \langle 0 | [\Theta_\mu^\mu(0)]_{NP} | 0 \rangle$$

Partially Conserved Dilatation Current (PCDC)

there are two different expectations when conformal window is approached: $g(\mu = \Lambda) = g_c$

1. dilaton mass parametrically vanishes $m_\sigma^2 \simeq (N_f^c - N_f) \cdot \Lambda^2$ $\frac{m_\sigma}{f_\sigma} \rightarrow 0$

2. dilaton mass finite in the limit $f_\sigma \simeq \Lambda$ $\frac{m_\sigma}{f_\sigma} \rightarrow \text{const}$

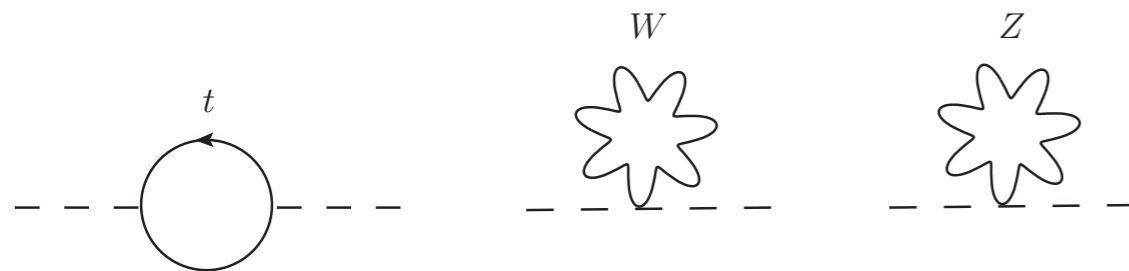
important role of $\frac{f_\pi}{f_\sigma}$ in electroweak phenomenology

both scenarios expect light Higgs-like dilaton

but how light is light ?

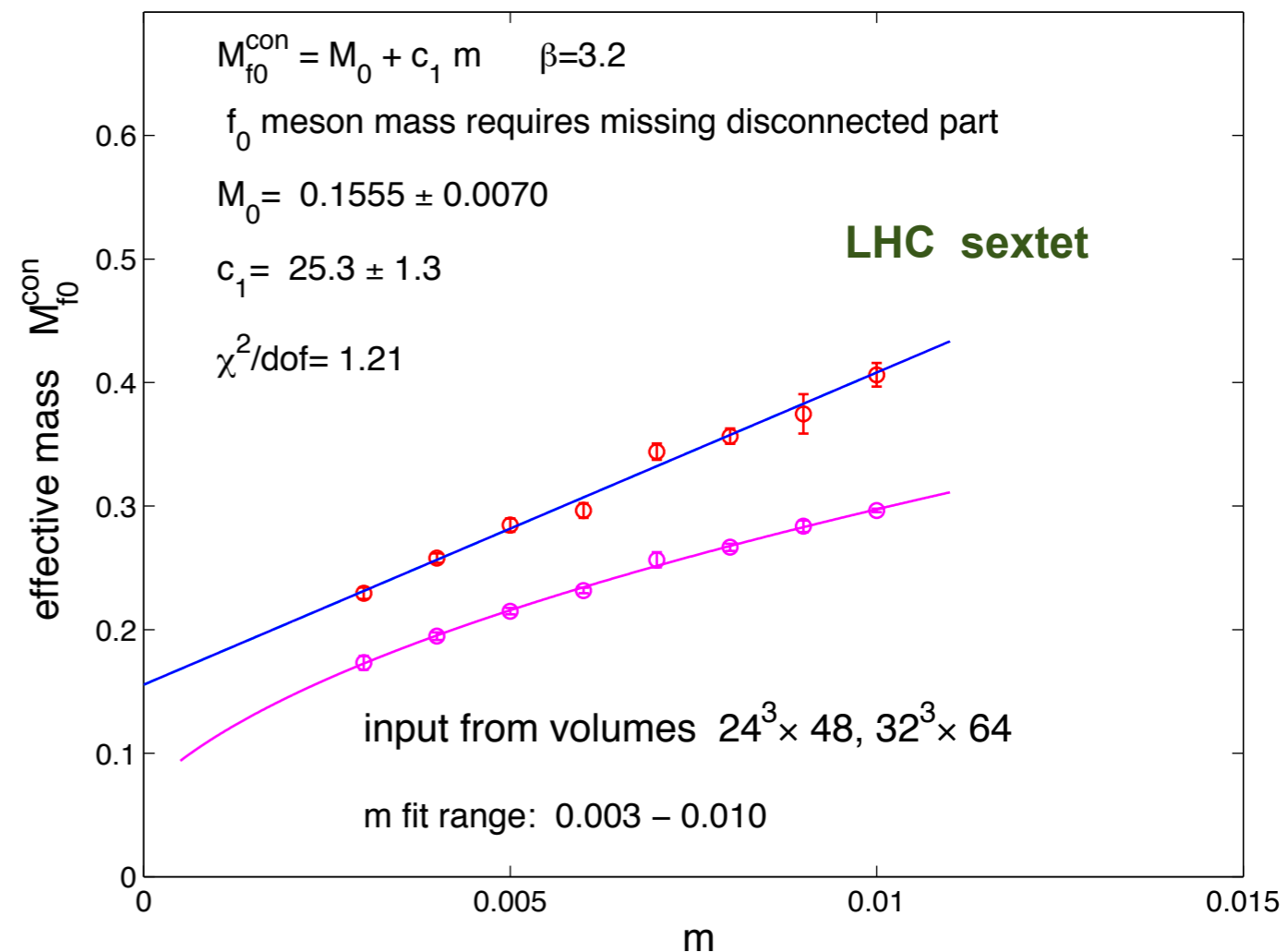
400-500 GeV dynamical Higgs as impostor?

Sannino



$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

effective mass $M_{f_0}^{\text{con}}$ from 0^{++} connected correlator



The light Higgs near conformality (dilaton-like?)

$$m_\sigma^2 \simeq -\frac{4}{f_\sigma^2} \langle 0 | [\Theta_\mu^\mu(0)]_{NP} | 0 \rangle$$

Partially Conserved Dilatation Current (PCDC)

there are two different expectations when conformal window is approached:

$$g(\mu = \Lambda) = g_c$$

1. dilaton mass parametrically vanishes $m_\sigma^2 \simeq (N_f^c - N_f) \cdot \Lambda^2 \quad \frac{m_\sigma}{f_\sigma} \rightarrow 0$

2. dilaton mass finite in the limit $f_\sigma \simeq \Lambda \quad \frac{m_\sigma}{f_\sigma} \rightarrow \text{const}$

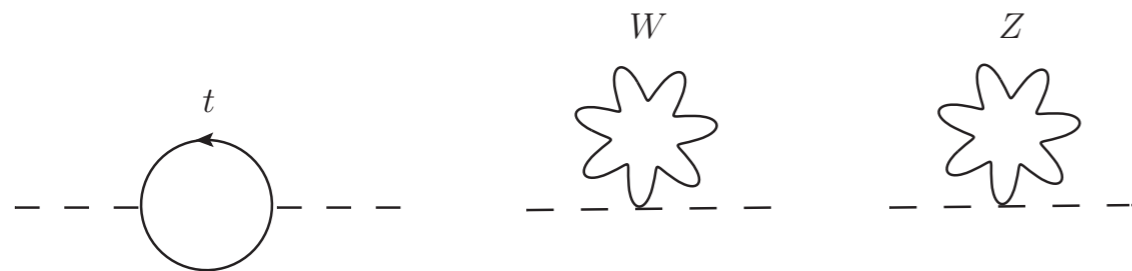
important role of $\frac{f_\pi}{f_\sigma}$ in electroweak phenomenology

both scenarios expect light Higgs-like dilaton

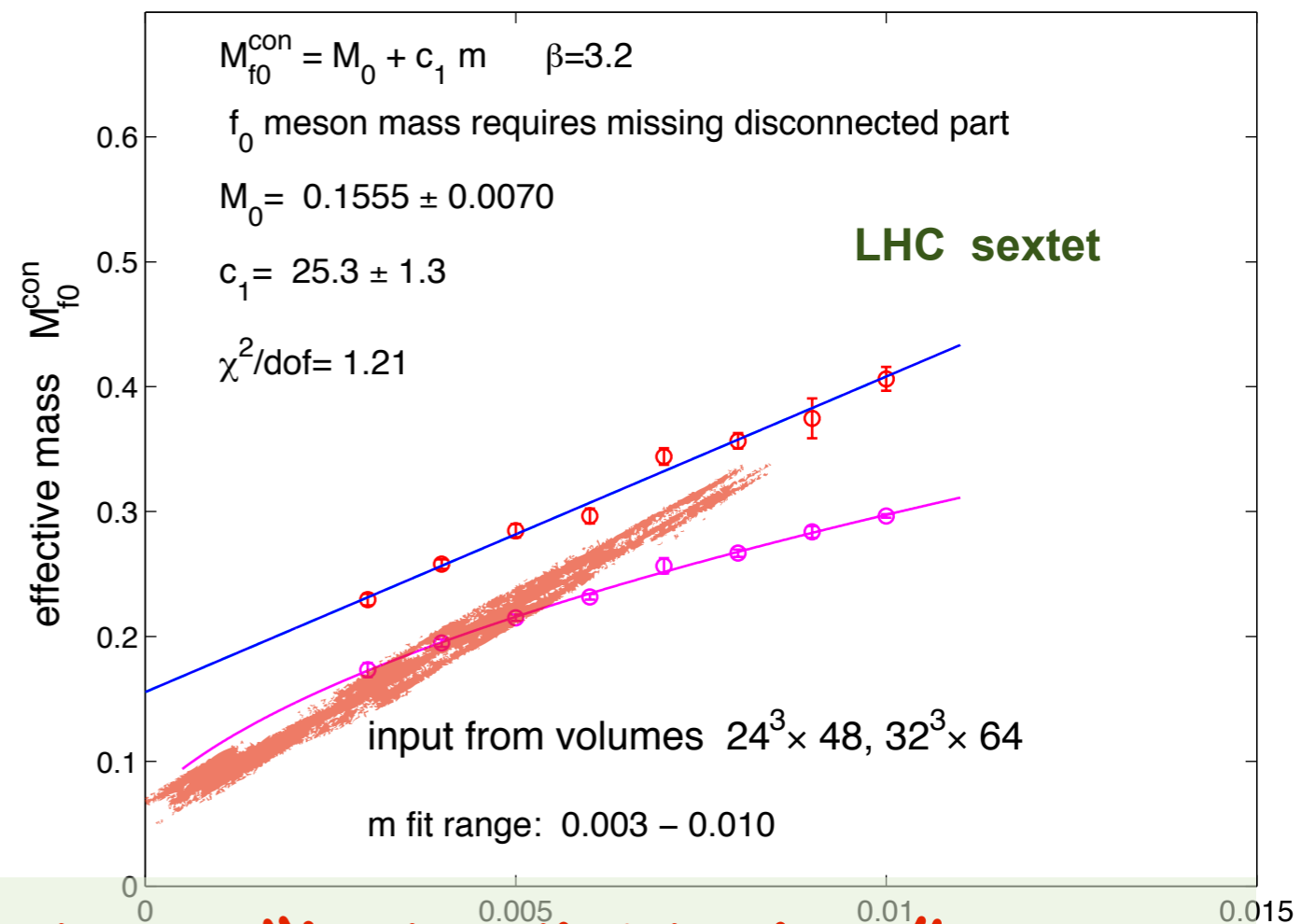
but how light is light ?

400-500 GeV dynamical Higgs as impostor?

Sannino



effective mass $M_{f_0}^{\text{con}}$ from 0^{++} connected correlator



is this SCGT dilaton-like scalar state, or "just a light Higgs" ?

The light Higgs near conformality (dilaton-like?)

$$m_\sigma^2 \simeq -\frac{4}{f_\sigma^2} \langle 0 | [\Theta_\mu^\mu(0)]_{NP} | 0 \rangle$$

Partially Conserved Dilatation Current (PCDC)

there are two different expectations when conformal window is approached: $g(\mu = \Lambda) = g_c$

1. dilaton mass parametrically vanishes $m_\sigma^2 \sim (N_f^c - N_f) \cdot \Lambda^2$ $\frac{m_\sigma}{f_\sigma} > 0$

2. dilaton mass finite in the limit $\frac{m_\sigma}{f_\sigma} \rightarrow 0$ **tunable for light dilaton state close to conformal window?**

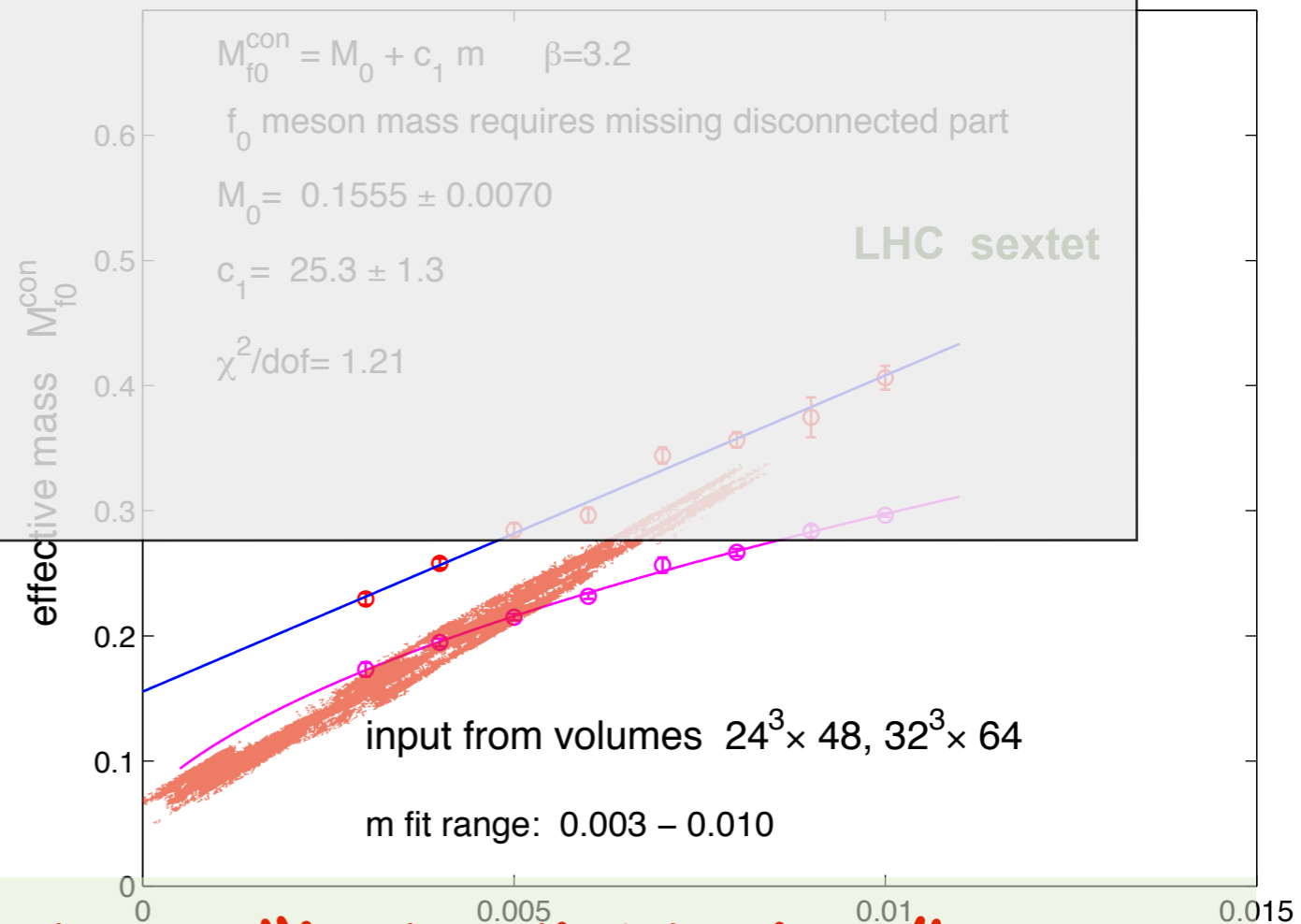
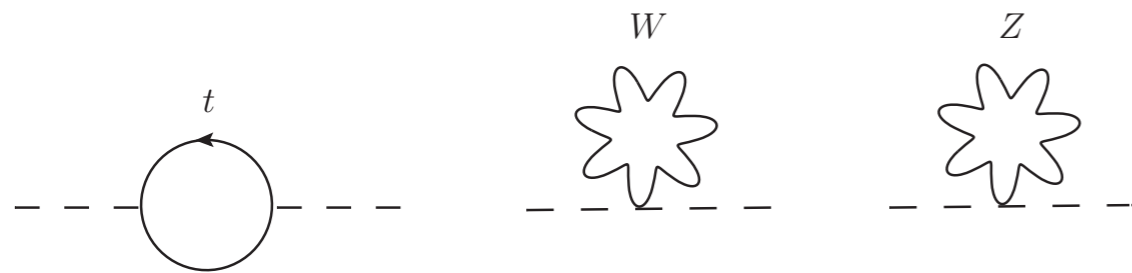
important role of $\frac{m_\sigma}{f_\sigma}$ in electroweak phenomenology
- N_f is not continuously tunable

both scenarios correct light Higgs-like dilaton
- fermion mass term ?

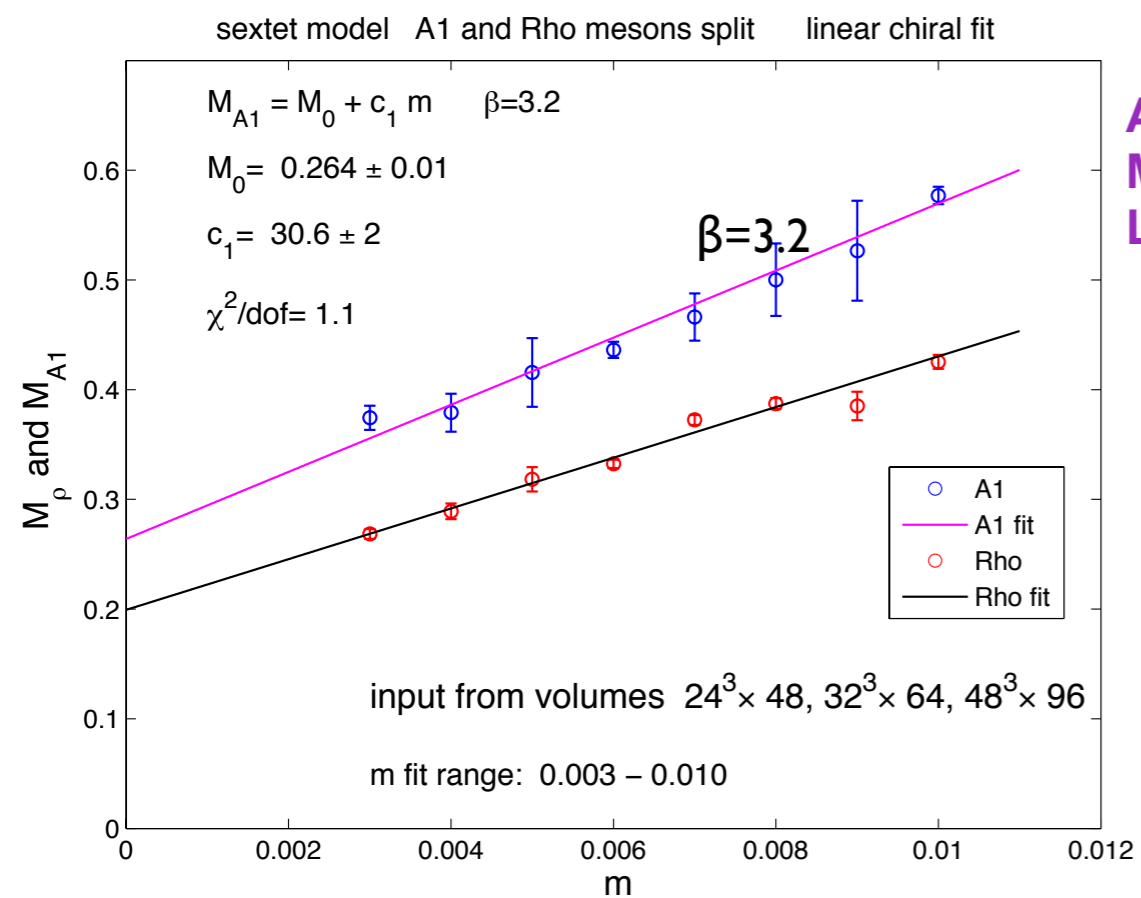
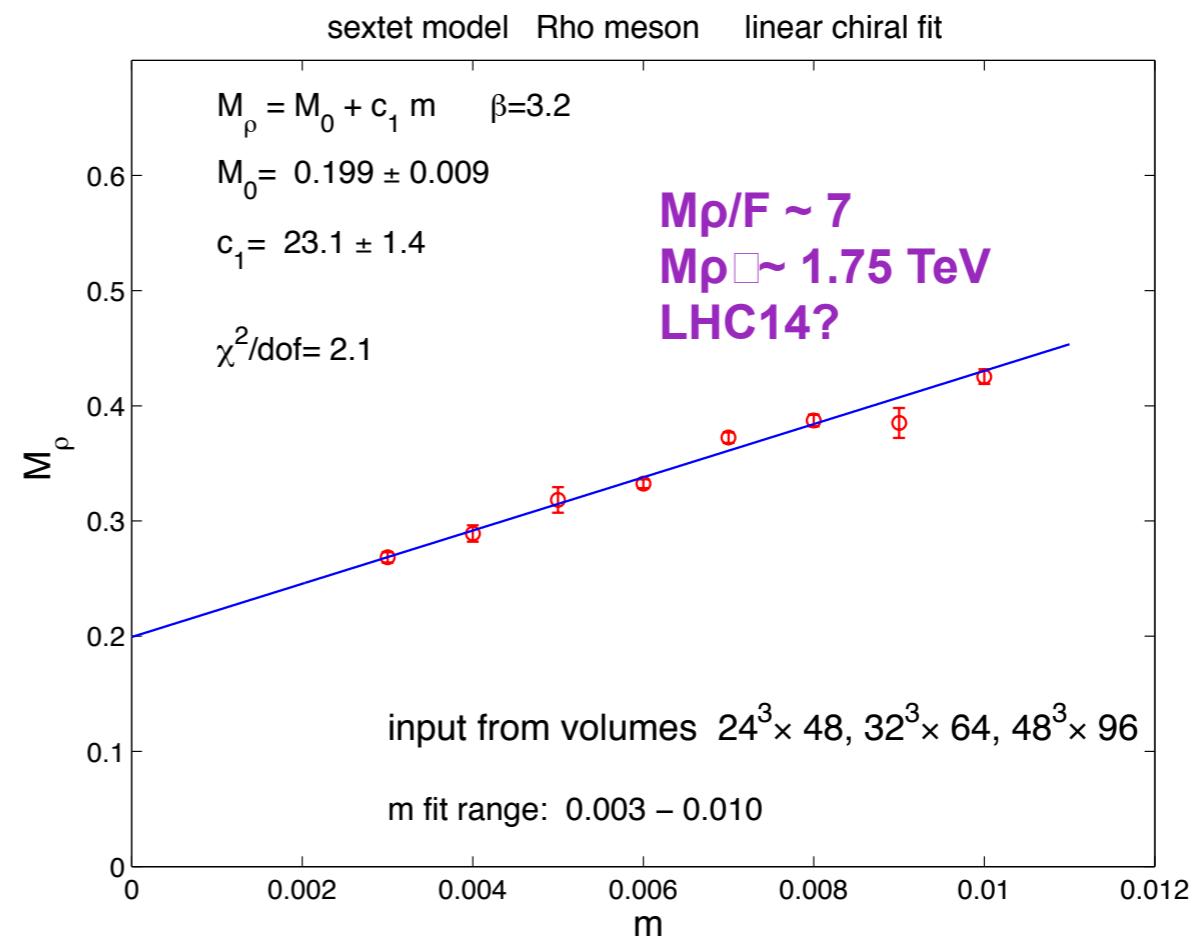
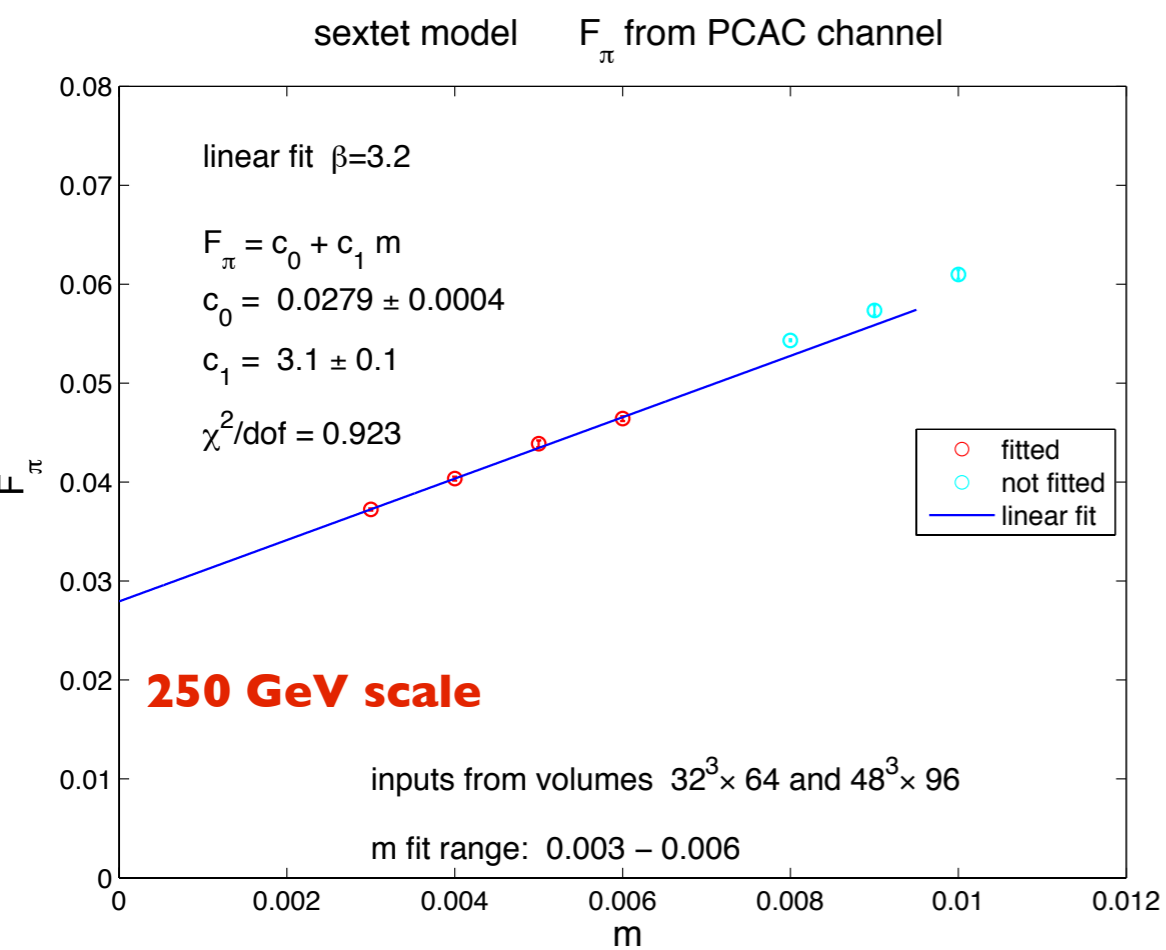
but how light is light?
- four-fermion operators ?

400-500 GeV dynamical Higgs as impostor?

Sanjino



$\delta M_H^2 \sim -12r^2 r_t^2 m_t^2 - r^2 r^2 (600 \text{ GeV})^2$
is this SCGT dilaton-like scalar state, or "just a light Higgs" ?



$A_1/F \sim 9.5$

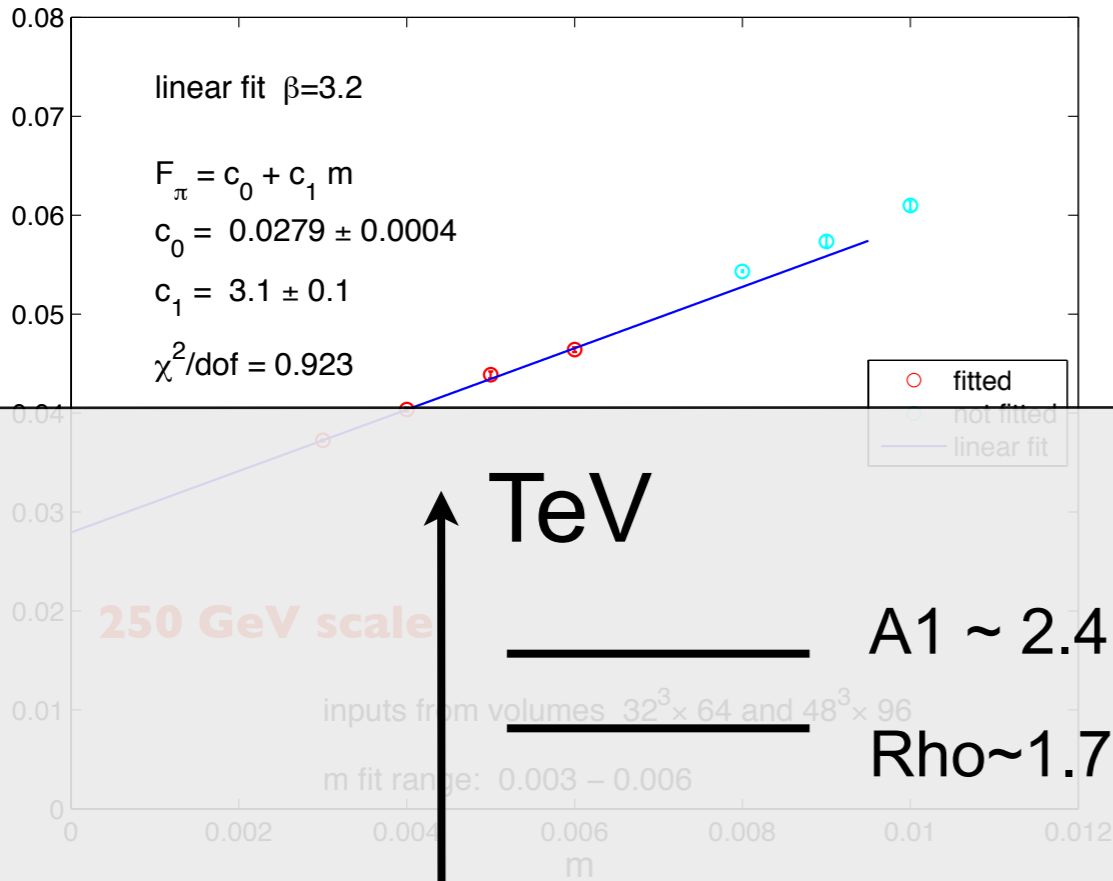
$M_{A_1} \sim 2.37 \text{ TeV}$

LHC14?

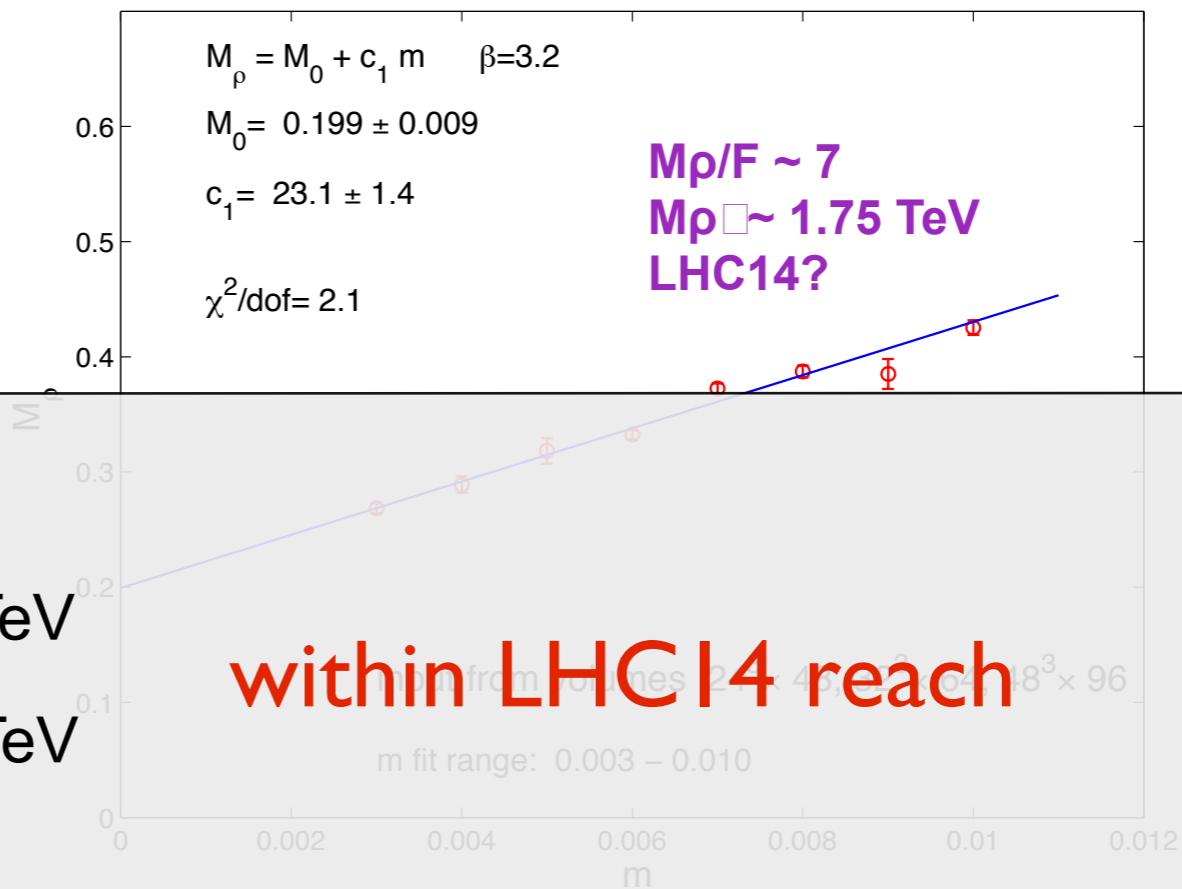
- $N_f=2$ SU(3) sextet M_ρ and $M(A_1)$

- two lowest states above scalar Higgs state

sextet model F_π from PCAC channel



sextet model Rho meson linear chiral fit



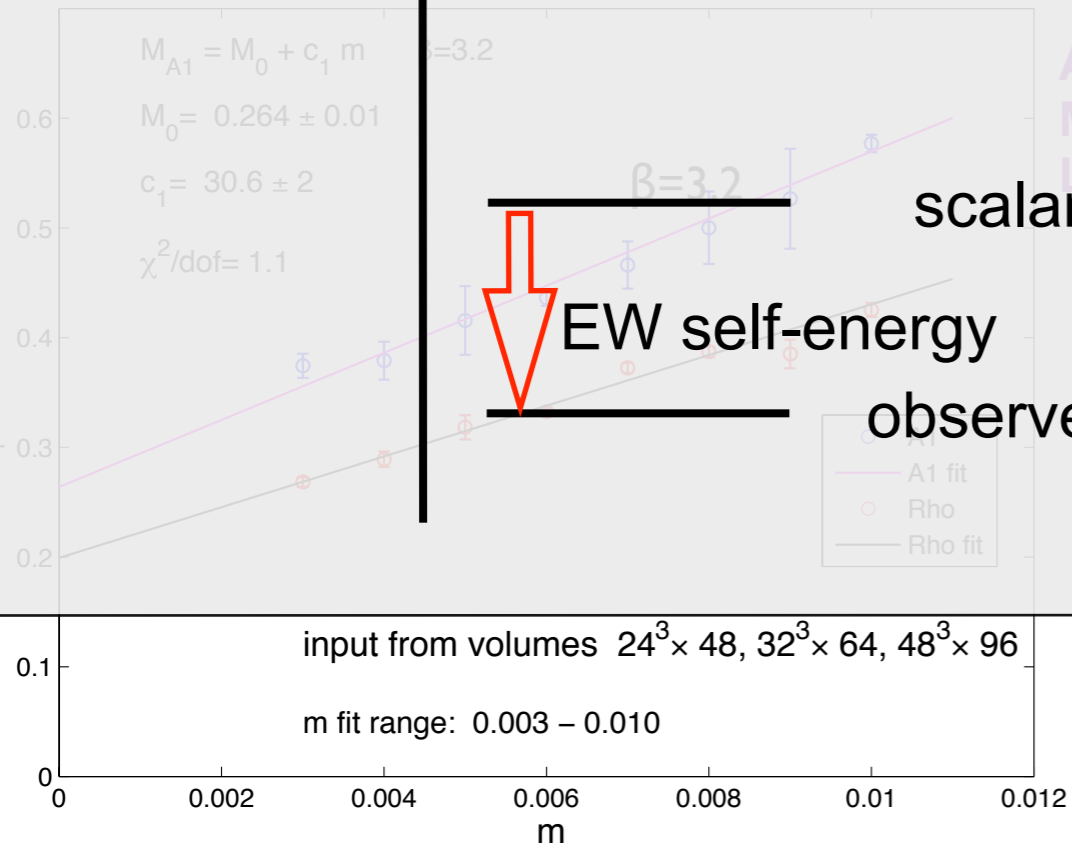
TeV

250 GeV scale

A1 ~ 2.4 TeV

Rho ~ 1.7 TeV

sextet model A1 and Rho mesons split linear chiral fit

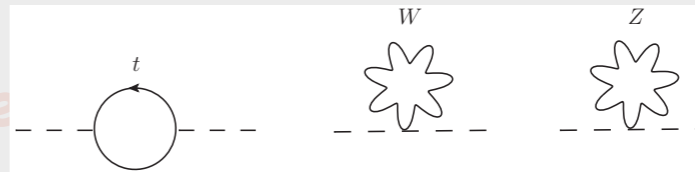


A1/F ~ 9.5
M_A1 ~ 2.37 TeV
LHC14?

scalar impostor 500 GeV?

EW self-energy

observed Higgs-like



$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

- two lowest states above scalar Higgs state

input from volumes $24^3 \times 48, 32^3 \times 64, 48^3 \times 96$

m fit range: 0.003 - 0.010

Higgs as a pseudo-Goldstone boson

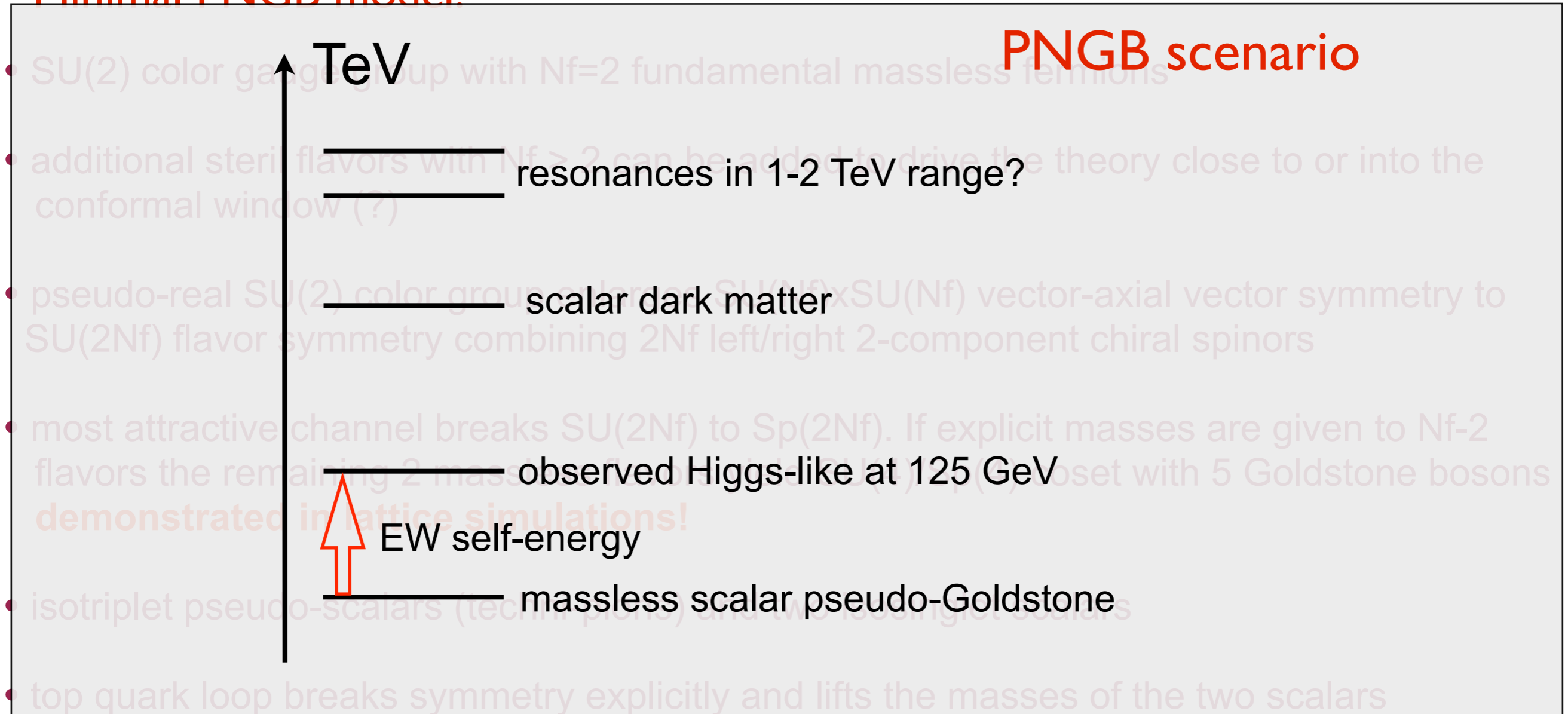
Minimal PNGB model:

- SU(2) color gauge group with $N_f=2$ fundamental massless fermions
- additional sterile flavors with $N_f > 2$ can be added to drive the theory close to or into the conformal window (?)
- pseudo-real SU(2) color group enlarges SU(N_f) \times SU(N_f) vector-axial vector symmetry to SU($2N_f$) flavor symmetry combining $2N_f$ left/right 2-component chiral spinors
- most attractive channel breaks SU($2N_f$) to Sp($2N_f$). If explicit masses are given to N_f-2 flavors the remaining 2 massless flavors yield SU(4)/Sp(4) coset with 5 Goldstone bosons **demonstrated in lattice simulations!**
- isotriplet pseudo-scalars (techni-pions) and two isosinglet scalars
- top quark loop breaks symmetry explicitly and lifts the masses of the two scalars
- the lighter is the composite Higgs (PC=+1)
and heavier is scalar dark matter candidate (PC=-1)

Higgs as a pseudo-Goldstone boson

Minimal PNGB model:

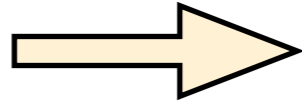
PNGB scenario



- the lighter is the composite Higgs (PC=+1)
and heavier is scalar dark matter candidate (PC=-1)

Studies of supersymmetric theories on the lattice

- New theoretical formulations
- improved algorithms
- increased computer power



studies of N=1 and N=4 super Yang-Mills

N=1 super Yang-Mills is supersymmetric pure gauge QCD

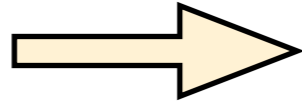
first step to super QCD can play the role of non-perturbative SUSY breaking in high scale hidden sector

SUSY and the LHC

- If SUSY is correct explanation for what we are seeing at LHC, it must be broken.
- That breaking (because of no go theorems etc) must be non-perturbative in character and hence the lattice potentially offers a good tool to understand it.
- Low energy constants that encode the SUSY breaking in any effective low energy SUSY model (e.g. MSSM) are determined by non perturbative quantities in the sector that breaks SUSY (e.g. super QCD).
- Thus measuring these condensates via lattice simulation helps to constrain the parameter space of any BSM SUSY low energy theory. Again this could be the MSSM or something else.

Studies of supersymmetric theories on the lattice

- New theoretical formulations
- improved algorithms
- increased computer power



studies of N=1 and N=4 super Yang-Mills

N=1 super Yang-Mills is supersymmetric pure gauge QCD

first step to super QCD can play the role of non-perturbative SUSY breaking in high scale hidden sector

SUSY and the LHC

- If SUSY is correct explanation for what we are seeing at LHC, it must be broken.
- That breaking (because of no go theorems etc) must be non-perturbative in character and hence the lattice potentially offers a good tool to understand it.
- Low energy constants that encode the SUSY breaking in any effective low energy SUSY model (e.g. MSSM) are determined by non perturbative quantities in the sector that breaks SUSY (e.g. super QCD).
- Thus measuring these condensates via lattice simulation helps to constrain the parameter space of any BSM SUSY low energy theory. Again this could be the MSSM or something else.

Non-perturbative N=4 super Yang-Mills

- holographic dilaton connection in pursuing light Higgs?
 - dilaton is simple to realize (translations along flat directions)
 - N=4 lattice action has flat directions (protected by exact lattice supersymmetry)
- exploring holographic connections between gauge theories and string/gravity theories

Toolset and its phenomenological applications

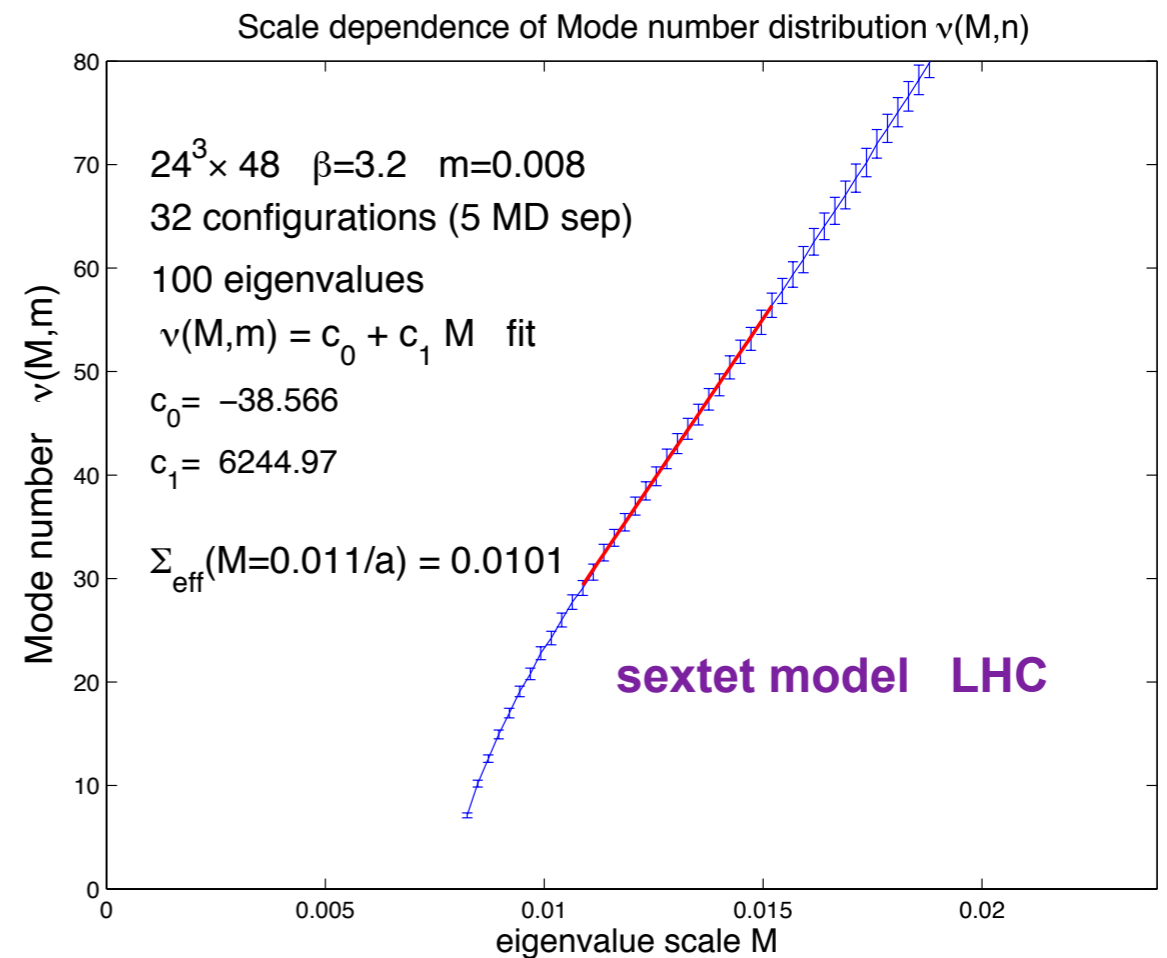
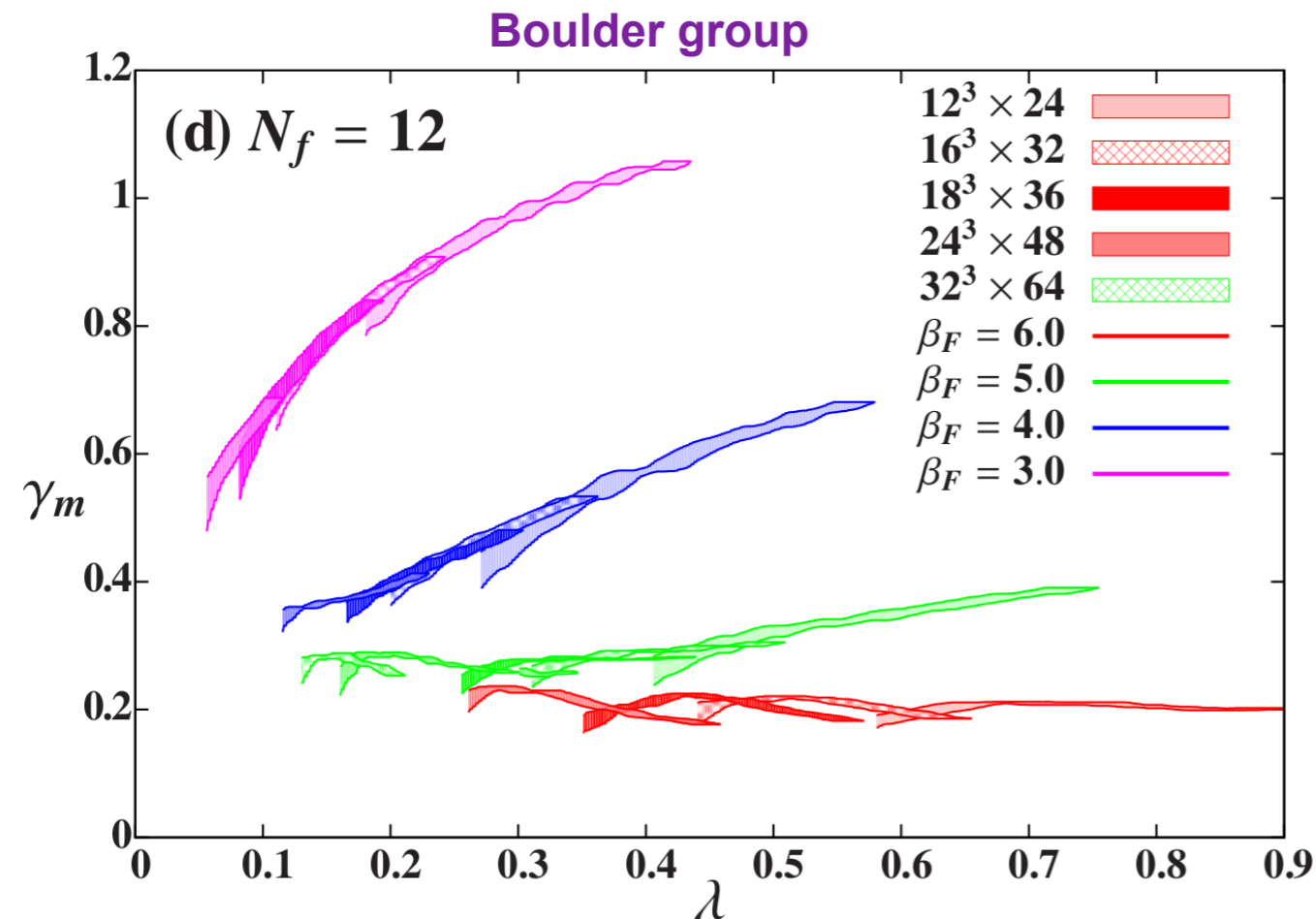
Toolset and its phenomenological applications

chiSB, Dirac spectrum, Anomalous dimension

$$\lim_{\lambda \rightarrow 0} \lim_{m \rightarrow 0} \lim_{V \rightarrow \infty} \rho(\lambda, m) = \frac{\Sigma}{\pi} \quad \text{spectral density}$$

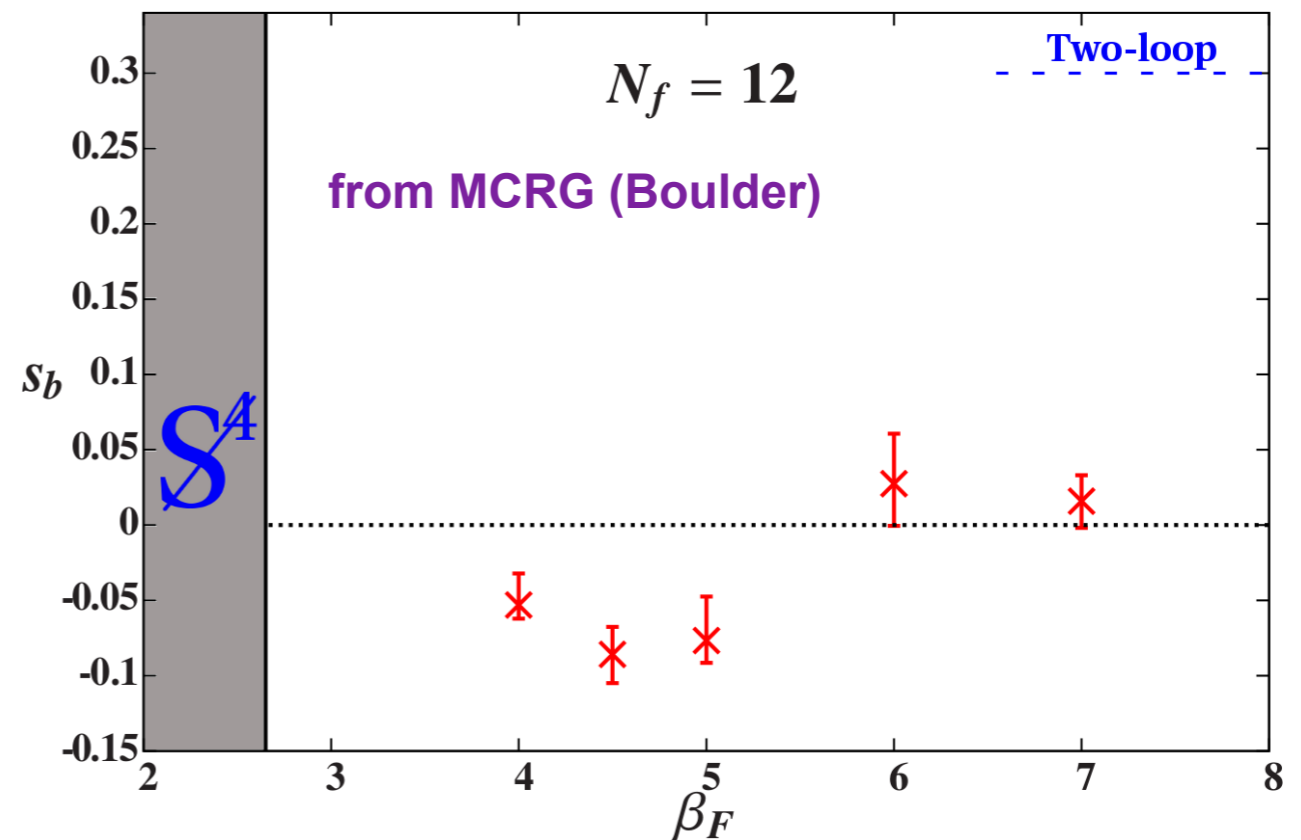
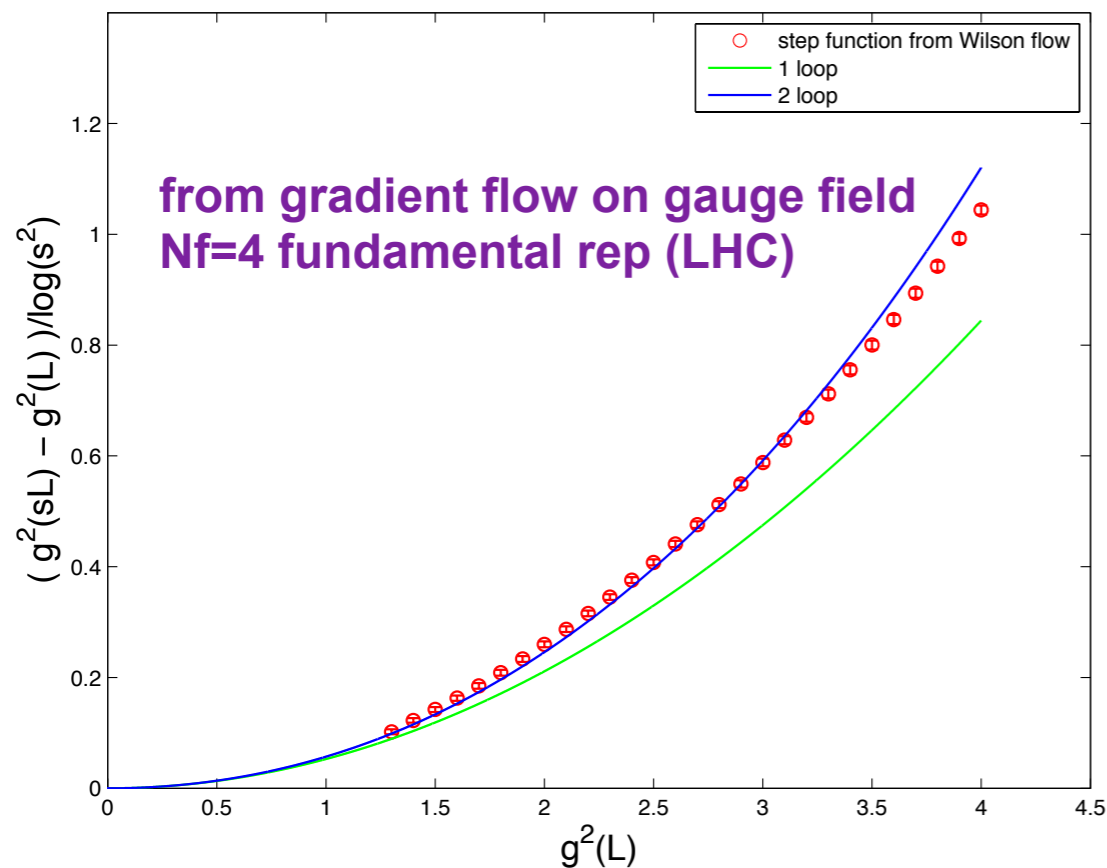
$$\nu(M, m) = V \int_{-\Lambda}^{\Lambda} d\lambda \rho(\lambda, m), \quad \Lambda = \sqrt{M^2 - m^2} \quad \text{mode number density complete UV control}$$

$$\nu_R(M_R, m_R) = \nu(M, m_q) \quad \text{renormalized and RG invariant}$$



Toolset and its phenomenological applications

Running coupling and beta-function (to understand the new gauge force)



gradient flow on gauge field is beautiful realization of
Wilson's exact RG with continuous momentum
integration - Luscher

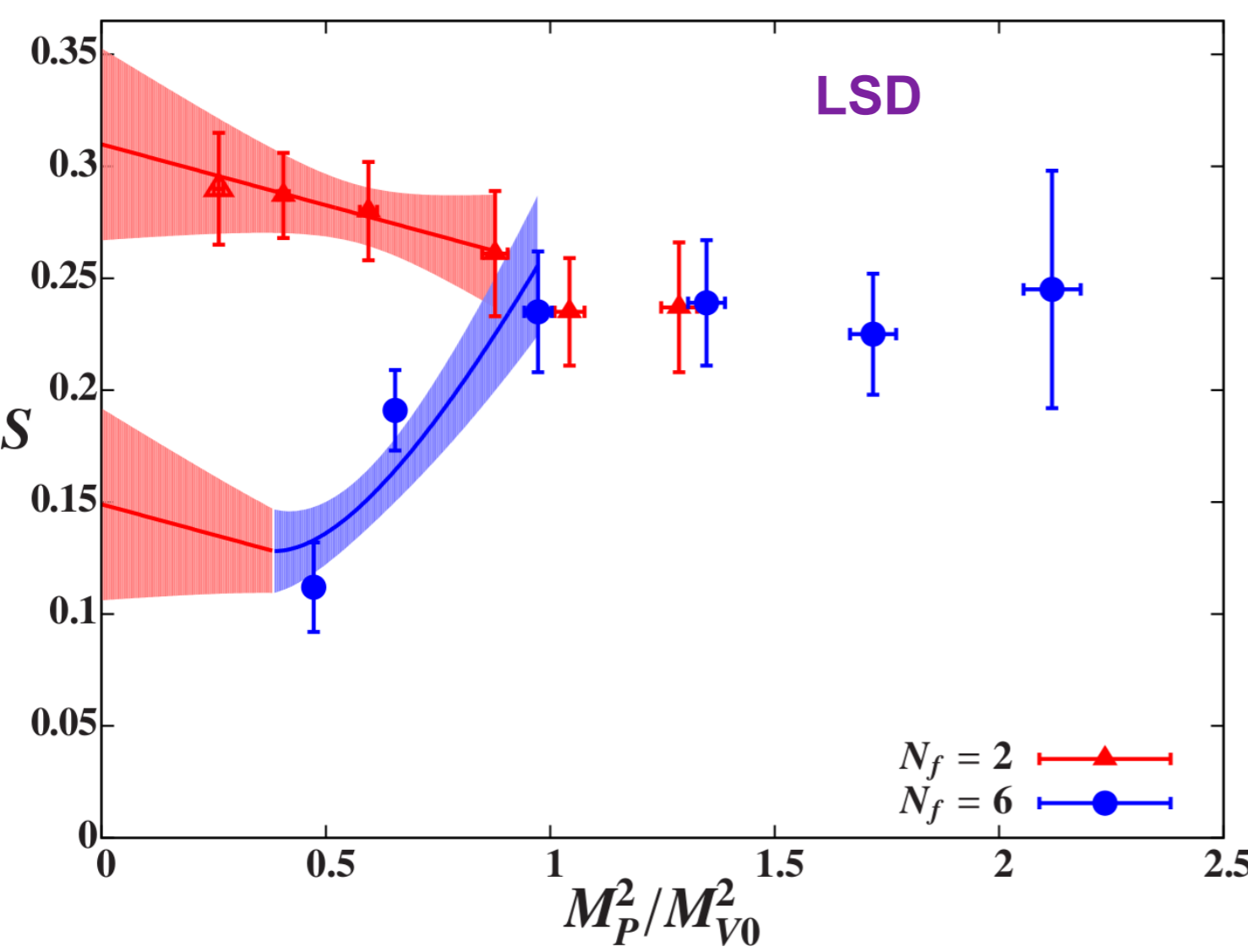
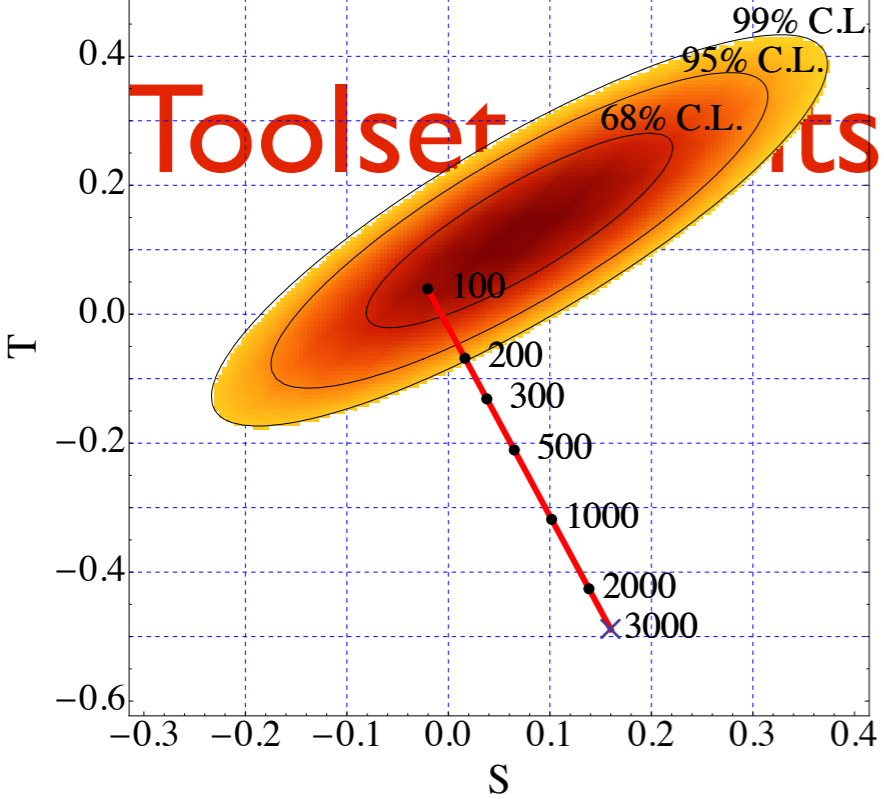
complements Schrodinger functional method (LSD)

Toolset

its phenomenological applications

S-parameter

LSD group with several phenomenological explorations

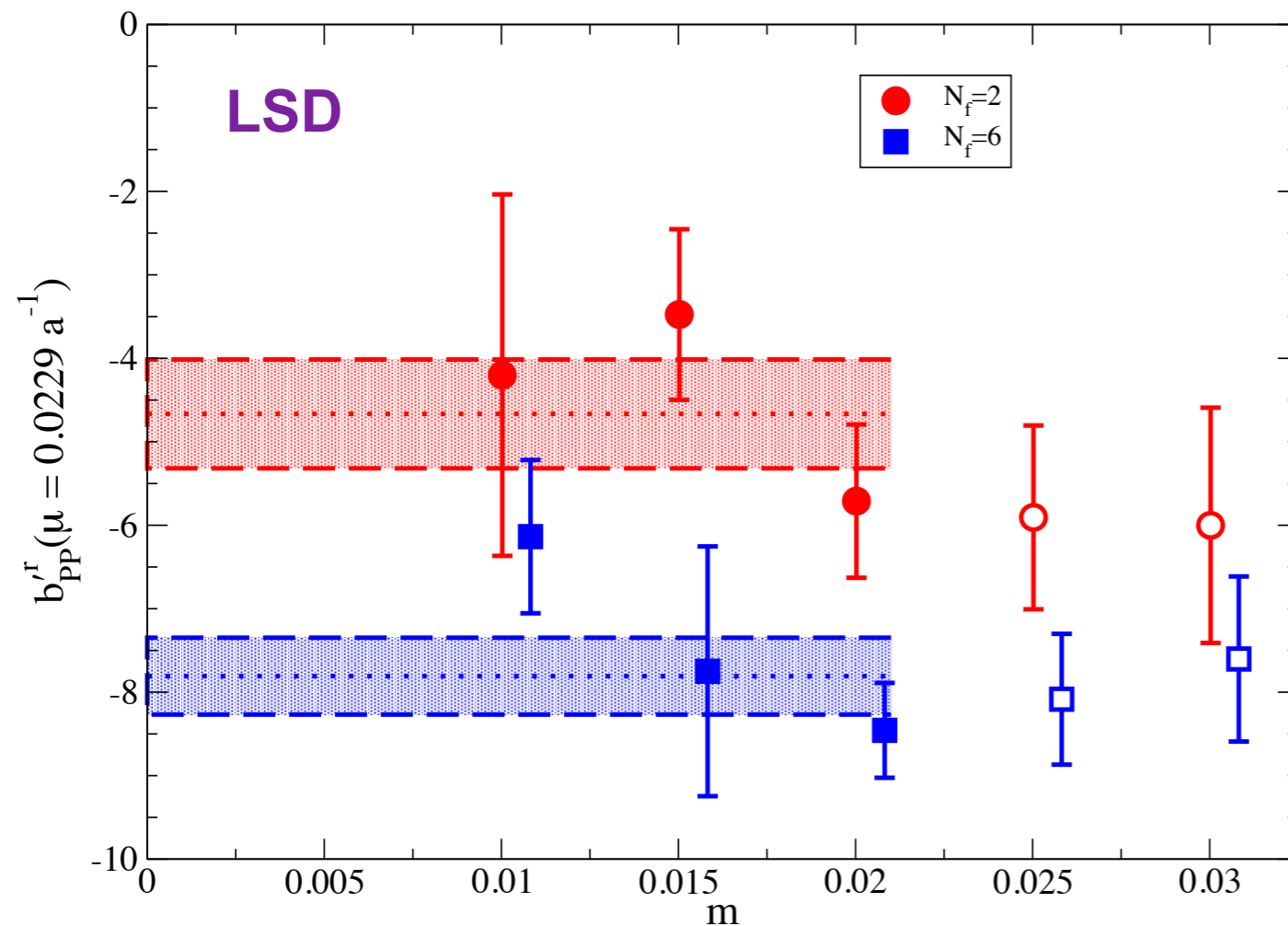


- near CW S-parameter is not increasing according to the naive scaling based on QCD and earlier expected by phenomenologists
- without non-perturbative BSM lattice work phenomenology is misinforming in model building

Toolset and its phenomenological applications

WW scattering

(what if cross section is stronger than expected from weakly coupled SM Higgs?)



- potentially important for LHC14 machine upgrade
- based on equivalence theorem

Toolset and its phenomenological applications

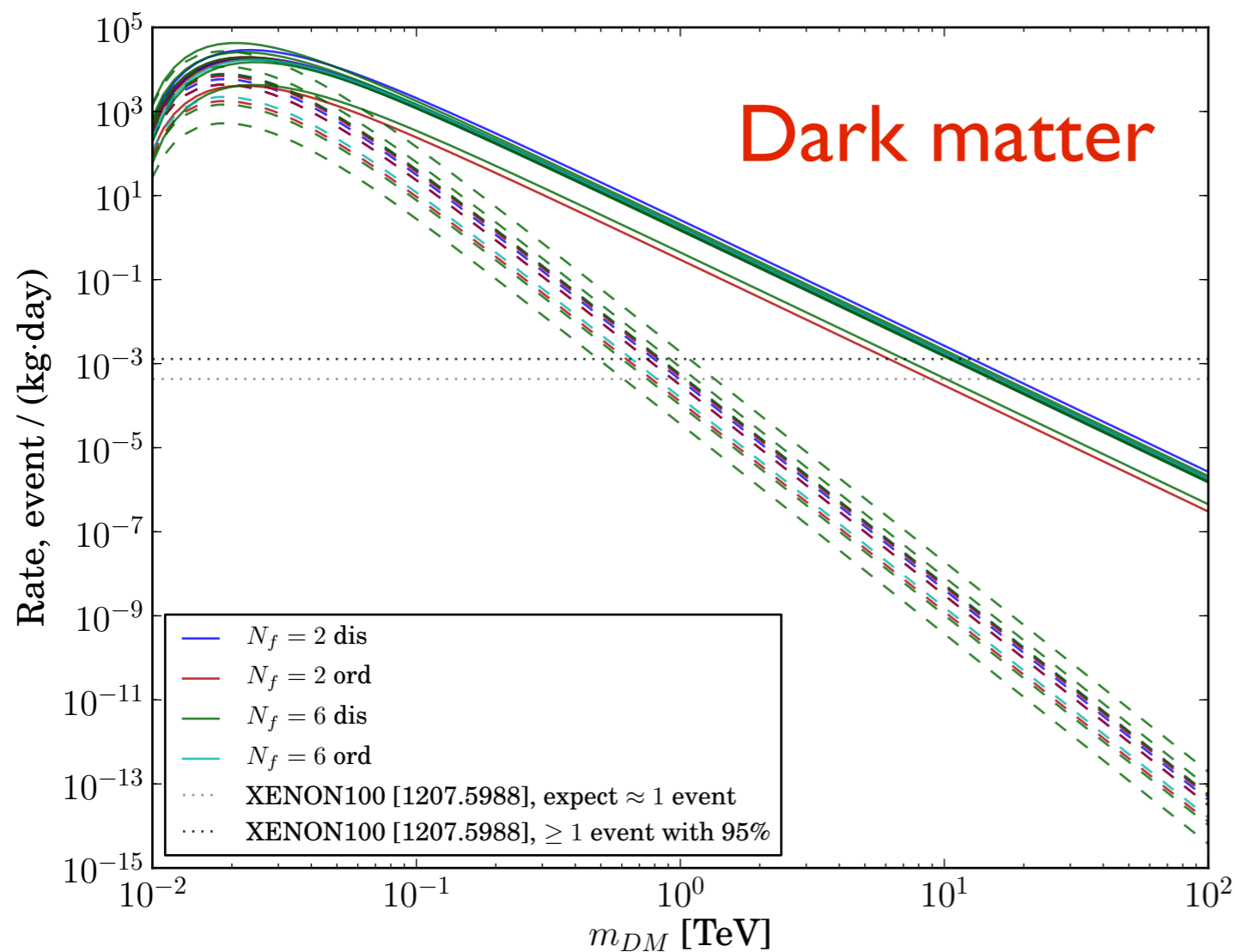
The Total Energy of the Universe:

Vacuum Energy (Dark Energy) $\sim 67\%$

NonBaryonic Dark Matter $\sim 29\%$

Visible Baryonic Matter $\sim 4\%$

Dark matter
self-interacting?



LSD group - first USQCD BSM
paper on dark matter

- dark matter candidates
electroweak active in the application
- there is room for electroweak singlet
dark matter particles

EW phase transition in sextet model - early universe

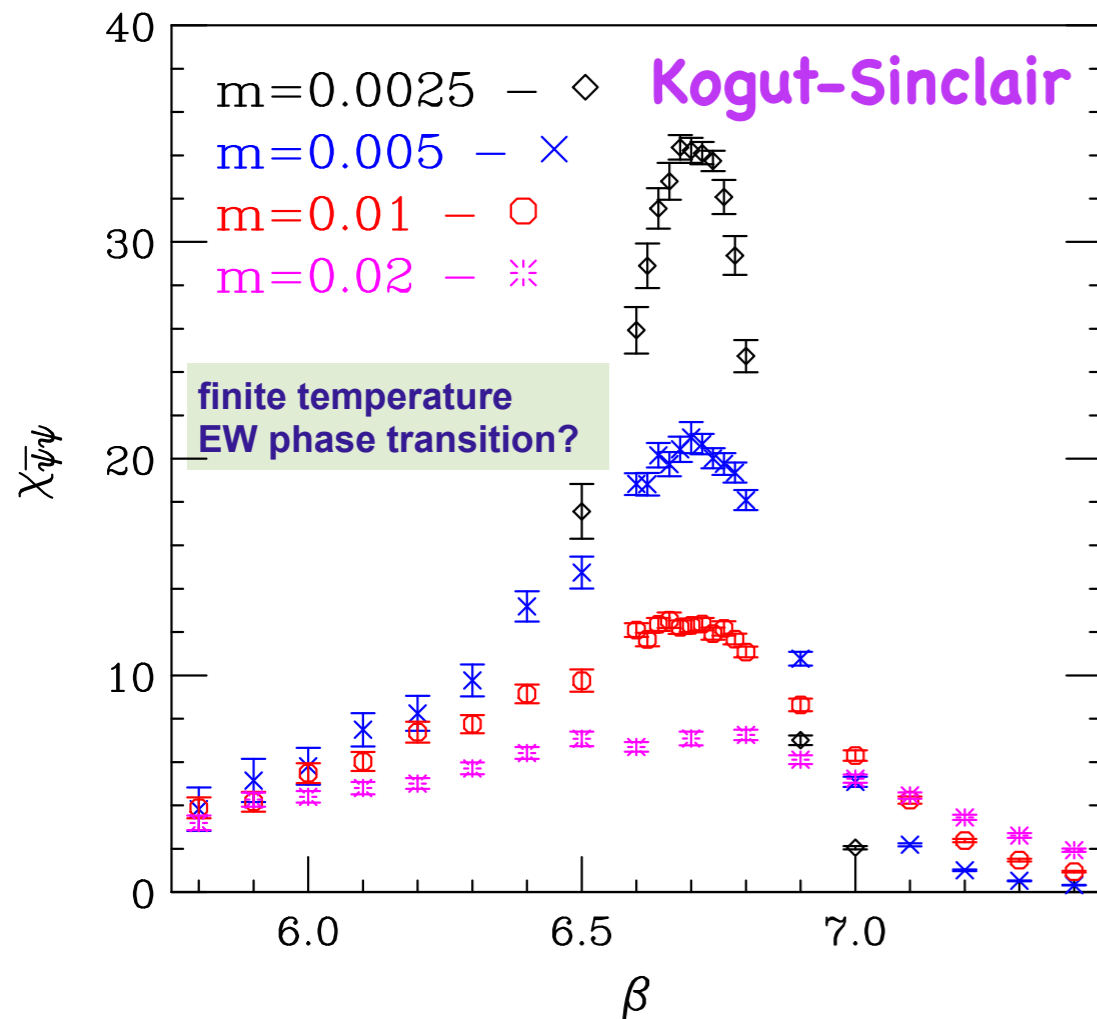
Kogut-Sinclair consistent with χ SB phase at T=0

relevance in early cosmology

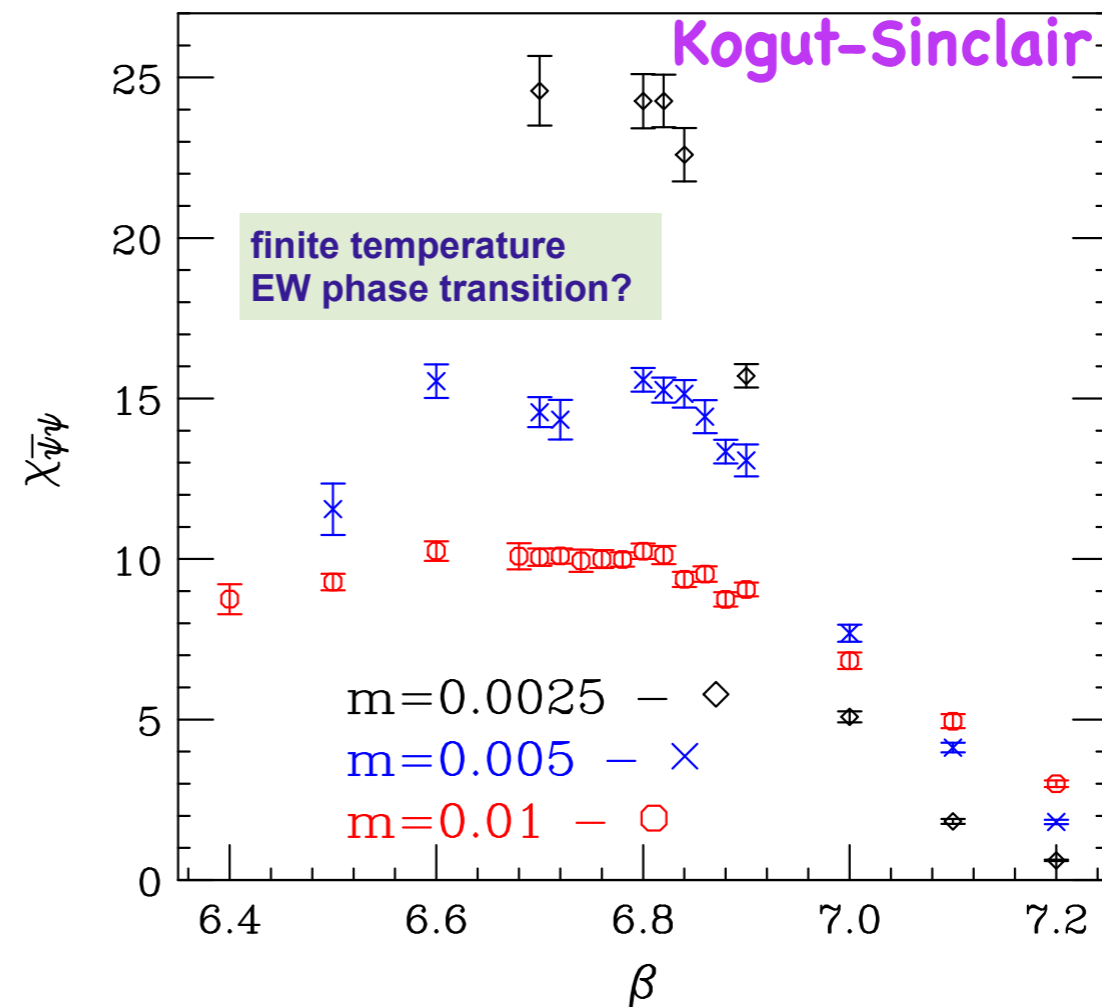
We are planning to run sextet thermo after model passed other tests

Third massive fermion flavor (electroweak singlet) dark matter?

$16^3 \times 8$ lattice



$24^3 \times 12$ lattice



Summary

Computational goals of USQCD BSM program and future plans:

- To determine whether a composite dilaton-like particle or light Higgs can emerge in near-conformal quantum field theories for LHC14 testing
- To investigate strongly coupled gauge theories with a composite Higgs built from a pseudo-Nambu-Goldstone boson
- To investigate the nature of $N=1$ SUSY breaking with matter multiplets targeting super QCD
($N=4$ conformal SUSY remains test bed for AdS/CFT theoretical conjectures)