

Spintronics of Spin-Orbit coupled Systems: Achievements and Challenges

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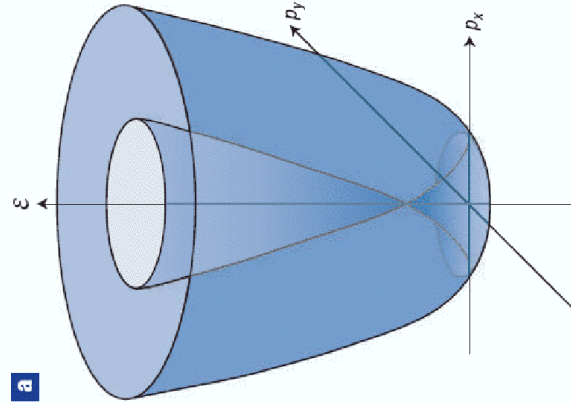
Conference on Spintronics

Kavli Institute for Theoretical Physics
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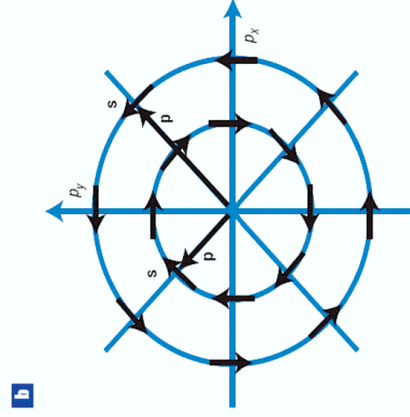
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How spin-orbit coupling changes the spectrum of noncentrosymmetric systems?



It splits the paraboloid $E(p) = p^2/2m$ into two sheets



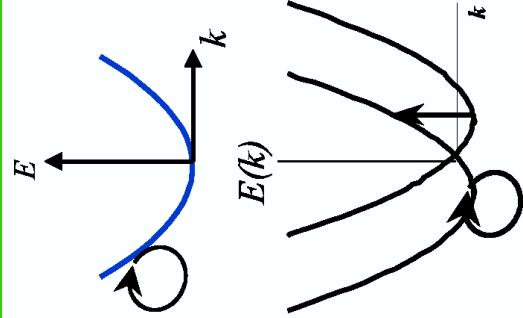
SO coupling establishes a strict connection between the direction of the momentum \mathbf{p} and the direction of the spin \mathbf{S}

Where Spin Coupling to Electric Field comes from?

Oscillator strength for a free electron in a parabolic band:

$$f = m_0 / m$$

m - electron effective mass
 m_0 - electron vacuum mass



Simplest spin-orbit coupling in non-centrosymmetric uniaxial crystals and in quantum wells

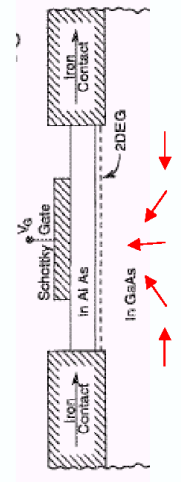
$$H_\alpha = \alpha(\boldsymbol{\sigma} \times \mathbf{k}) \cdot \hat{\mathbf{z}} = \alpha(\sigma_x k_y - \sigma_y k_x)$$

It splits spectrum into two spin branches

Near the spectrum bottom the oscillator strength is divided equally between the intra- and interbranch transitions

f^{inter} **results in spin coupling to ac electric field, and in EDSR (electric dipole spin resonance) in a strong magnetic field**

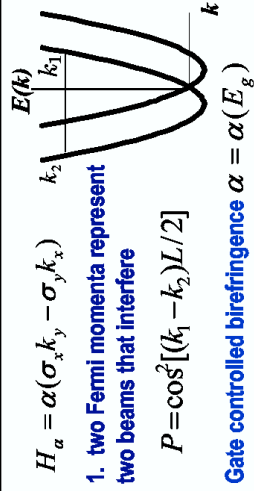
Spin transistor: Ideas encoded



$$H_\alpha = g(\boldsymbol{\sigma} \cdot \mathbf{B}_{in}) / 2, \mathbf{B}_{in} = 2\alpha(\mathbf{k} \times \hat{\mathbf{z}}) / g$$

2. electron spin $\mathbf{s} \parallel \mathbf{k}$ precesses in the effective magnetic field $\mathbf{B}_{in}(\mathbf{k})$

Two equivalent pictures:



- Basic ideas underlying the device:**
- (i) Spin injection from ferromagnetic electrodes,
 - (ii) Gate control of electron spin (SO),
 - (iii) Spin precession in internal magnetic field (SO),
 - (iv) Spin interference (SO).

Spintronics without magnetic elements:
 generating nonequilibrium spin populations electrically via SO coupling

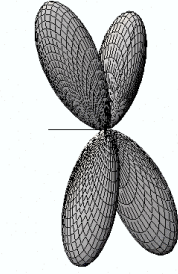
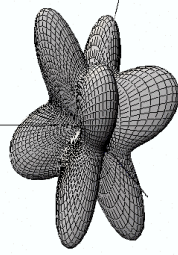
EDSR – Electric Dipole Spin Resonance

$$H_{so} = H_1(\mathbf{k}, \boldsymbol{\sigma}) + H_2(\mathbf{r}, \boldsymbol{\sigma}), \quad g\mu_B B \gg \alpha k_F$$

$H_1(\mathbf{k}, \boldsymbol{\sigma})$ mechanism well known in 3D:

Bell (1962), McCombe et al. (1967), Dobrowolska et al. (1984)

$$H_1(\mathbf{k}, \boldsymbol{\sigma}) : H_\alpha = \alpha(\sigma_x k_y - \sigma_y k_x) \text{ SIA, } H_\beta = \beta(\sigma_x k_x - \sigma_y k_y) \text{ BIA}$$



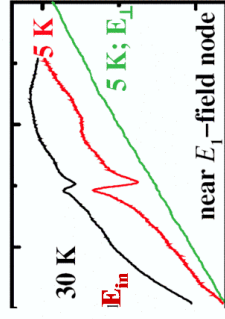
SIA $\hat{\mathbf{E}} \parallel \hat{\mathbf{z}}$ BIA and SIA $\hat{\mathbf{E}} \parallel \hat{\mathbf{z}}$

Ratio of matrix elements: $\ell_\perp / \ell_\parallel \approx \omega_c \omega_s / \omega_0^2$

$$H_2(\mathbf{r}, \boldsymbol{\sigma}) = \mu_B (\boldsymbol{\sigma} \cdot \hat{\mathbf{g}}(\mathbf{r}) \mathbf{B}(\mathbf{r})) / 2$$

With $g \approx 0$, the mechanism proved to be efficient in AlGaAs QWs with $\mathbf{E} \parallel \mathbf{z}$

Kato et al. (2003)



Schulte et al. (2005) AIAs
In narrow QWs, EDSR with in-plane E dominates

$$I_{EDSR} \approx 10^4 I_{EPR}$$

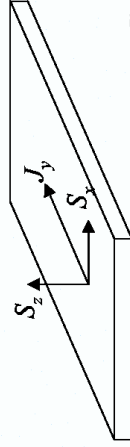
Charge Transport vs Spin Transport

Maxwellian equations include:

E , D , ρ , and J for electric charge and current
 B and H , or $M = (B - H) / 4\pi$ for magnetization

Spin magnetization \mathcal{S} is the only observable quantity.
There is no magnetic charges and currents.

Spin nonconservation makes theory highly sophisticated, cf. AHE



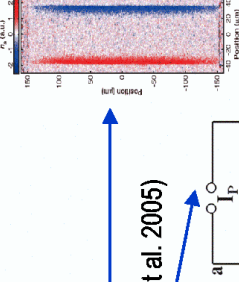
Observing \mathcal{S}_x : Kato et al. (2004),

Silov et al. (2004), Ganichev et al. (2004)

Observing \mathcal{S}_z by optical techniques:

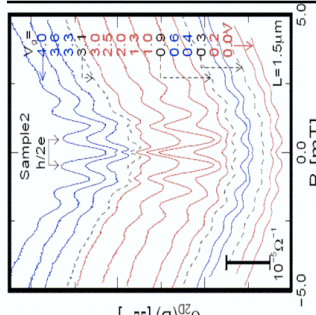
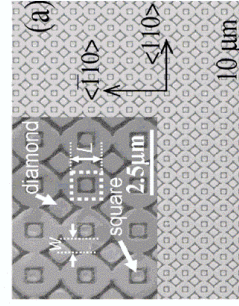
in n -GaAs by Kerr rotation (Kato et al. 2004)

in p -GaAs by polarized emission (Wunderlich et al. 2005)



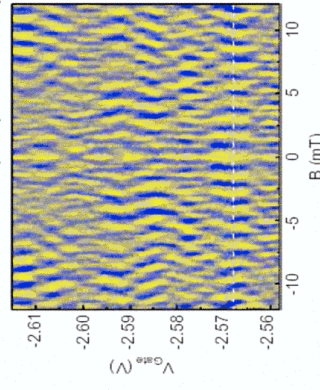
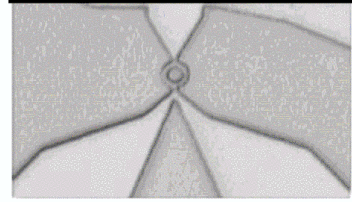
All these observations: generating spin magnetization by electric current due to central symmetry violation (irrespective of detailed mechanisms)

Spin interference in transport experiments



Spin interferometer with square loop array (follow $B=0$ vertical)

InGaAs
Koga et al. (2005)



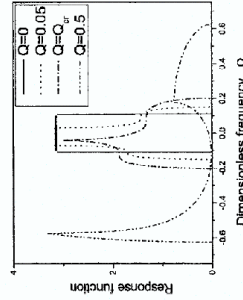
Conductance of a ring controlled by gate voltage (follow vertical sections)

$\leftarrow \alpha=0$ HgTe/HgCdTe
Koenig et al. (2005)

Formalism, spatial scales, and spin currents

Two analytical models: (i) ballistic transport in rings and (ii) diffusive transport

Both result in characteristic length $\ell_\alpha = \hbar^2 / m\alpha \approx L_{\text{sd}}, k_\alpha = m\alpha / \hbar^2$



Response of $\sigma_x(\mathbf{q}, \omega)$ to $\mathbf{E}(\mathbf{r}, t) = E \exp[i(\mathbf{q}\mathbf{r} - \omega t)]$

$$Q = q / 2k_\alpha, \varpi = 2v_F k_\alpha, \Omega = m(\omega - \varpi) / 2\hbar k_F k_\alpha$$



Response diverges for $q \rightarrow 2k_\alpha$ (breakdown when two Fermi surfaces touch)

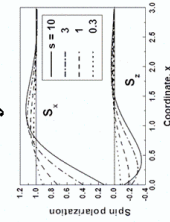
$\alpha \neq 0$ island as spin emitter into $\alpha = 0$ leads; maximum effect at $d \approx \ell_\alpha$

Such spin currents are well defined because they are conserved in $\alpha=0$ regions

Spin currents in $\alpha \neq 0$ regions

$$j_i^s = \frac{1}{2} \langle \sigma_I v_i + v_i \sigma_I \rangle \text{ or } j_i^s = \left\langle \frac{d}{dt} \sigma_I x_i \right\rangle$$

A beautiful playground for different SO coupling mechanisms, but they physical meaning and relation to spin accumulation remain obscure yet



In systems with $j_i^z = 0, S_z \neq 0$ develops when spin leak at or across the edge

Conjecture: spin currents with $q \approx ik_\alpha$ seem more relevant than $q=0$ currents

Nontraditional systems: from graphene to metal surfaces

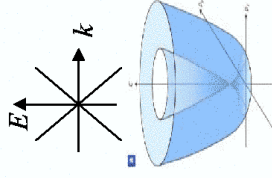
Dispersion law and magnetic quantization in graphene:

$$E(k) = \hbar v_F k, E_n = \text{sign}\{n\} \sqrt{2\hbar v_F^2 B |n|} / c, -\infty < n < \infty$$

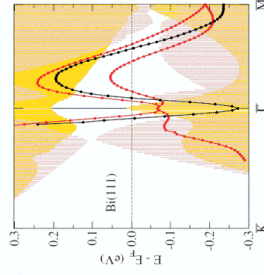
Magnetic quantization with k-linear SO term:

$$E_0 = \hbar \omega_c \delta, E_n^\pm = \hbar \omega_c (n \pm \sqrt{\delta^2 + 2(k_\alpha \ell_B)^2 n}), n \leq 1$$

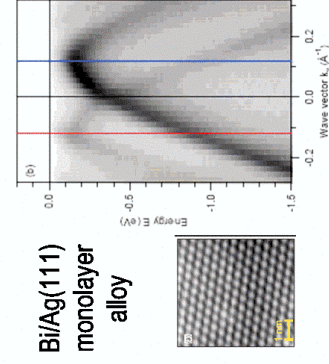
$$\omega_c = eB / \hbar c, \delta = (1 - gm / 2m_0) / 2, k_\alpha = m\alpha / \hbar^2, \ell_B^2 = \hbar^2 / eB$$



Giant SO coupling near surfaces of semimetals and metals



Surface states Bi (111)
Black: without SO coupling
Red: with SO coupling
Koroteev et al. (2004)



Large SO results in ultra-short spin precession lengths

Conclusions:

1. Effect of SO on energy spectrum
2. Ideas underlying SO devices,
3. EDSR in 2D,
4. Electrical generation of spin populations,
5. Discovery of spin interference,
6. Theory: status, characteristic scales, challenges,
7. Nontraditional systems and surfaces