

Physics of Stellar Winds from Hot, Luminous Massive Stars

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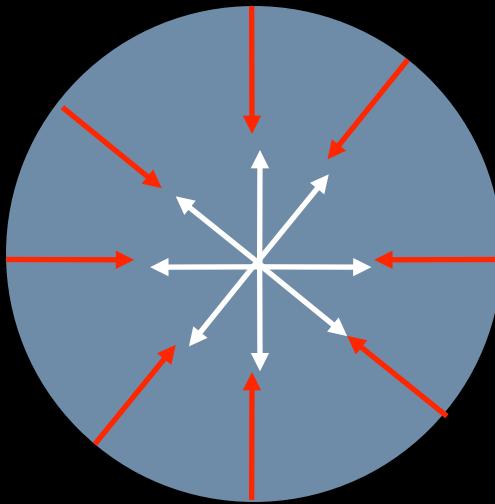
Types of Stellar Winds

- **Solar-type Coronal Winds**
 - Low $M_{\dot{m}} \sim 10^{-14} M_{\text{sun}}/\text{yr}$; $V_{\text{inf}} \sim V_{\text{esc}} \sim 500 \text{ km/s}$
 - Thermally driven with $V_{\text{sound}} \sim V_{\text{esc}}$
- **Cool (super) giant (super)winds**
 - Low $V_{\infty} \sim 10^{\text{'s}}$ of km/s < V_{esc} ; high $M_{\dot{m}} \sim 10^{-4} - 10^{-8} M_{\text{sun}}/\text{yr}$
 - Driven by pulsation and/or dust ?
- **Radiatively driven winds of hot stars (OB, WR, LBV)**
 - High V_{∞} ($\sim 3 V_{\text{esc}} = 2000-3000 \text{ km/s}$) $\gg V_{\text{sound}} \sim 10 \text{ km/s}$
 - High $M_{\dot{m}}$ ($10^{-4} - 10^{-8} M_{\text{sun}}/\text{yr}$)
- LBVs may have superwind phases (up to $1 M_{\text{sun}}/\text{yr}$, e.g. η Car)

Radiative force vs. gravity

Radiative
Force

$$g_{rad} = \int_0^{\infty} dv \frac{K_v F_v}{c}$$



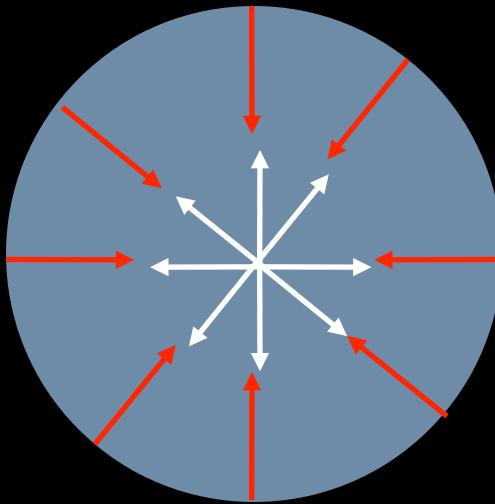
Gravitational
Force

$$\frac{GM}{r^2}$$

Radiative force vs. gravity

Radiative
Force

$$g_{rad} = \int_0^{\infty} dv \frac{\kappa_v F_v}{c}$$



Gravitational
Force

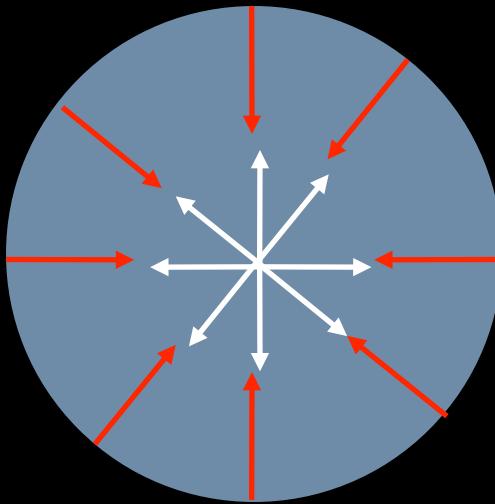
$$\frac{GM}{r^2}$$

$$\Gamma_e \equiv \frac{g_e}{g} = \frac{\kappa_e L / 4\pi r^2 c}{GM / r^2} = \frac{\kappa_e L}{4\pi G M c}$$

Radiative force vs. gravity

Radiative
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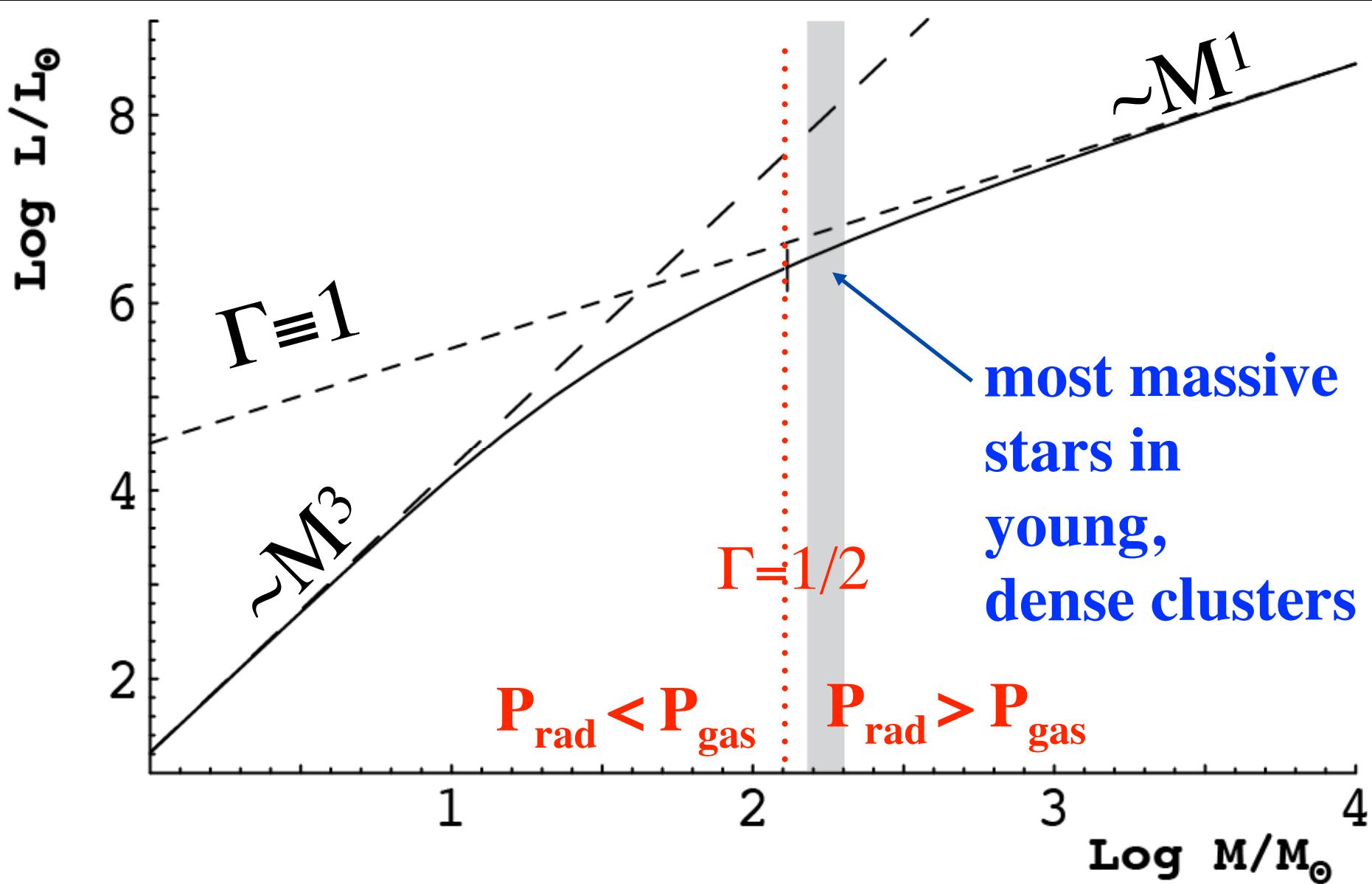
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$$\Gamma \simeq 2 \times 10^{-5} \frac{L / L_\odot}{M / M_\odot} \frac{\overline{\kappa_F}}{\kappa_e}$$

Eddington Standard Model (n=3 Polytrope)



If $\Gamma_F \equiv \Gamma > 1$, steady-state equation of motion (for $v > v_{\text{sound}} \rightarrow 0$):

$$v \frac{dv}{dr} = -\frac{\kappa L}{4\pi r^2 c} - \frac{GM}{r^2}$$

$$v \frac{dv}{dr} = (\Gamma - 1) \frac{GM}{r^2}$$

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$$v_\infty^2 = (\Gamma - 1) v_{esc}^2$$

“anti-gravity”

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$$v \frac{dv}{dr} = (\Gamma - 1) \frac{GM}{r^2}$$

$$4\pi\rho vr^2 dv = \frac{L}{c} \left(\frac{\Gamma - 1}{\Gamma} \right) \kappa \rho dr$$

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“anti-gravity”

$$\dot{M} v_\infty = \frac{\tau L}{c} \left(\frac{\Gamma - 1}{\Gamma} \right)$$

OB : $\tau \leq 1$

WR : $\tau \approx 1 - 10$

“wind momentum”

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OB : $\tau \leq 1$

WR : $\tau \approx 1 - 10$

“wind momentum”

“wind energy”

“photon tiring limit”

$$\dot{M} \frac{v_\infty^2 + v_{esc}^2}{2} = \tau L \frac{v_\infty}{2c}$$

$$\tau < \frac{2c}{v_\infty} \simeq 200$$

For wind, need: $\Gamma > 1 \rightarrow \kappa_F > \kappa_{Edd} \equiv \frac{4\pi GMc}{L}$

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In optically thick star: $\kappa_F \simeq \kappa_R \equiv \frac{\int_0^\infty \frac{\partial B_\nu}{\partial T} d\nu}{\int_0^\infty \frac{1}{\kappa_\nu} \frac{\partial B_\nu}{\partial T} d\nu} \leq few \kappa_e$
Rosseland mean

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Rosseland
mean

In optically thin wind: $\kappa_F \simeq \kappa_P \equiv \frac{\int_0^\infty \kappa_\nu B_\nu d\nu}{\int_0^\infty B_\nu d\nu} \equiv Q \kappa_e$

Planck
mean

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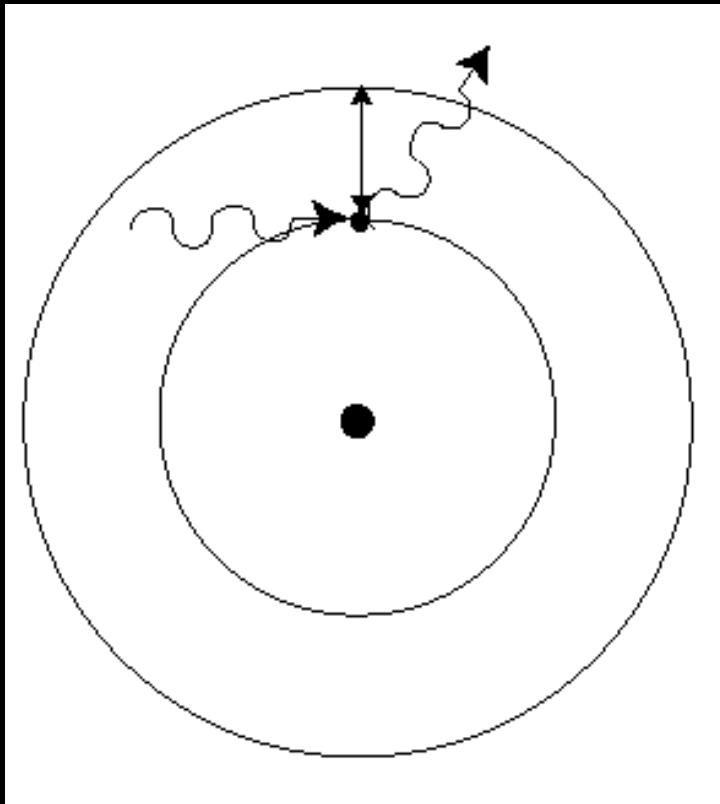
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 Planck mean

from line opacity: $Q \sim 2000 \frac{Z}{Z_\odot}$ cf. Gayley 1995

Driving by Line-Opacity

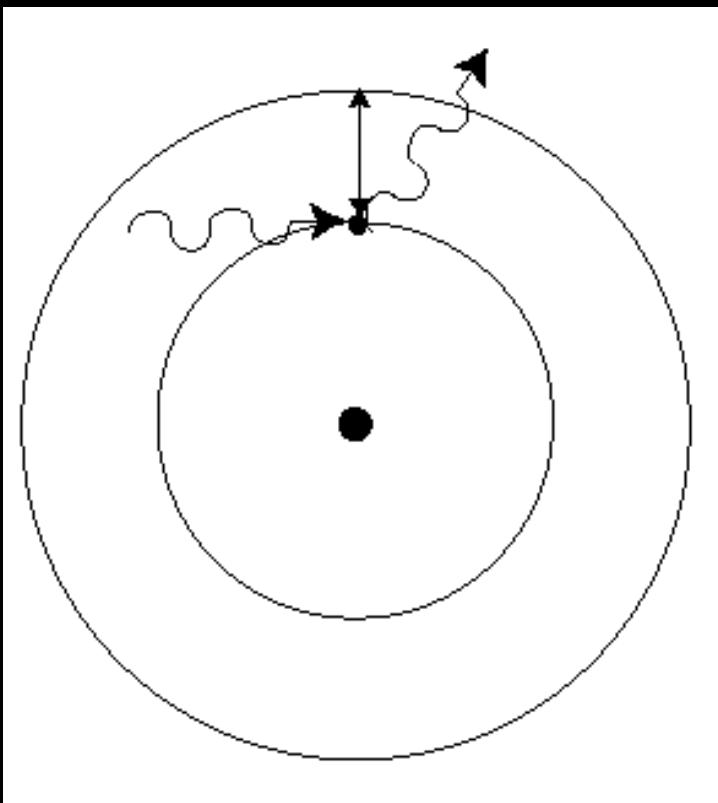
Optically **thin**



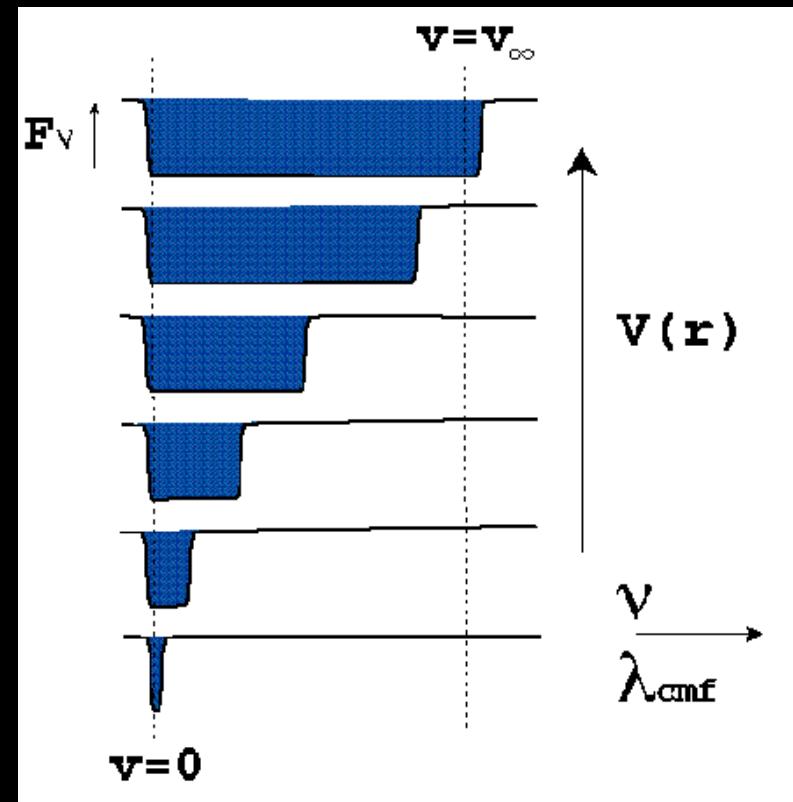
$$\Gamma_{\text{thin}} \sim Q\Gamma_e \sim 1000\Gamma_e$$

Driving by Line-Opacity

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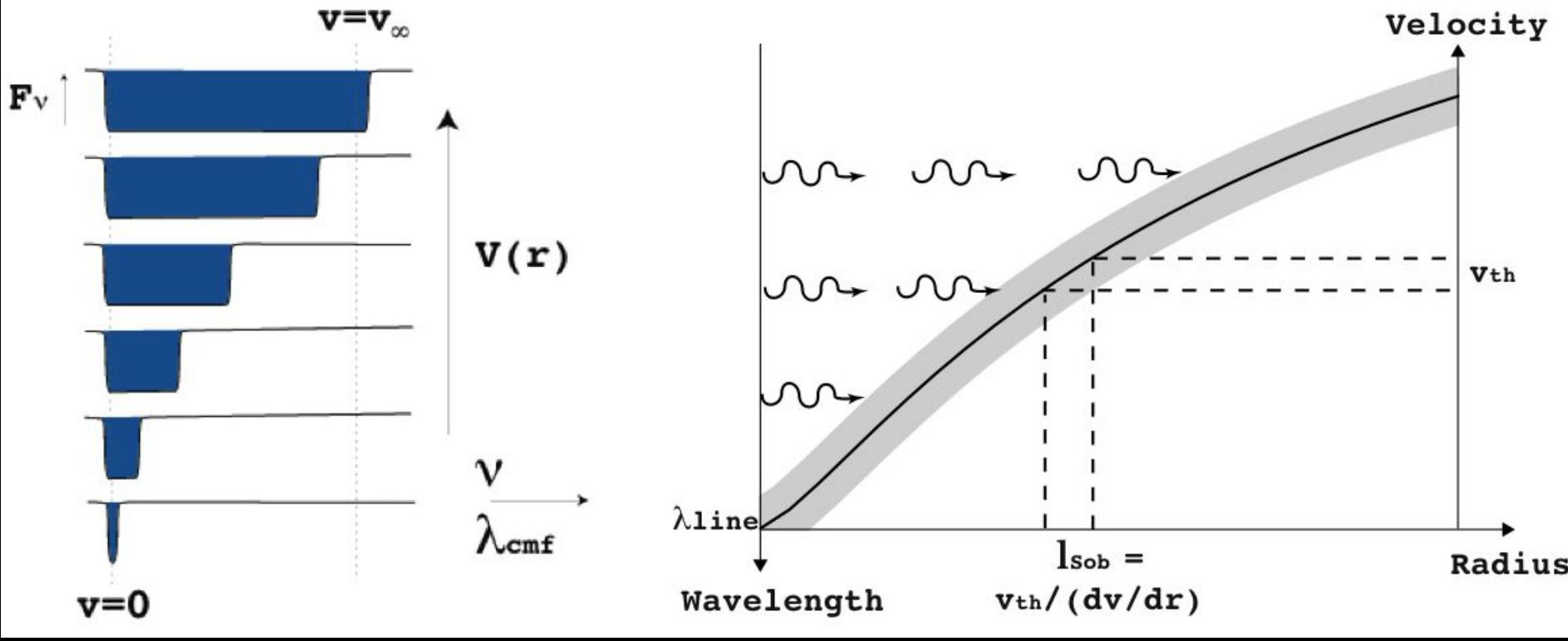
Optically **thick**



$$\Gamma_{\text{thin}} \sim Q\Gamma_e \sim 1000\Gamma_e$$

$$\Gamma_{\text{thick}} \sim \frac{Q\Gamma_e}{\tau} \sim \frac{1}{\rho} \frac{dv}{dr}$$

Line-driving



For strong,
optically thick
lines:

$$g_{thick} \sim \frac{g_{thin}}{\tau} \sim \frac{1}{\rho} \frac{dv}{dr}$$

$$\tau \equiv \kappa \rho \frac{V_{th}}{dv/dr} \sim \frac{V_{th}}{V_\infty} R_*$$

$l_{sob} \ll R_*$

CAK model of steady-state wind

Equation of motion:

$$\mathbf{v}\mathbf{v}' \approx -\frac{GM(1-\Gamma)}{r^2} + \frac{\bar{Q}L}{r^2} \left(\frac{r^2 \mathbf{v}\mathbf{v}'}{\dot{M}\bar{Q}} \right)^\alpha$$

inertia \approx gravity \approx CAK line-force

$0 < \alpha < 1$
 CAK ensemble of
thick & thin lines

$\mathbf{g}_{\text{CAK}} \approx \text{gravity}$

Mass loss rate

$$\dot{M} \approx \frac{L}{c^2} \left(\frac{\bar{Q}\Gamma}{1-\Gamma} \right)^{\frac{1}{\alpha}-1}$$

inertia \approx gravity

Velocity law

$$\mathbf{v}(r) \approx \boxed{\mathbf{v}_\infty} (1 - R_* / r)^\beta \quad \beta \approx 0.8$$

$\sim \mathbf{V}_{esc}$

**Wind-Momentum
Luminosity law**

$$\begin{aligned} \dot{M} \mathbf{v}_\infty &\sim \bar{Q}^{-1+1/\alpha} L^{\frac{1}{\alpha}} & \alpha &\approx 0.6 \\ &\sim Z^{0.6} L^{1.7} & \boxed{\bar{Q} \sim Z} \end{aligned}$$

$$\dot{M}_{cak} \approx \frac{L}{c^2} \left(\frac{Q\Gamma_e}{\Gamma_e - 1} \right)^{-1+1/\alpha}$$

Define $\dot{M}_{-6} \equiv \frac{\dot{M}}{10^{-6} M_{\odot}/yr}$ $L_6 \equiv \frac{L}{10^6 L_{\odot}}$

Then for $Q = 1000$:

$$\dot{M}_{-6} \approx 2L_6 \left(\frac{\Gamma_e}{1 - \Gamma_e} \right)^{1/2}; \quad \alpha = 2/3$$

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$\therefore \dot{M}_{cak}$ very sensitive to value of α !

NLTE Wind models

- To compute line opacity, need **atomic physics** and **NLTE** wind code
 - WM-basic: Pauldrach + ~1985- pres.
 - POWR: Hamman+ ~1990-pres.
 - CMFGEN: Hiller+ ~1990-pres.
 - FastWind: Puls+ ~2000-pres.

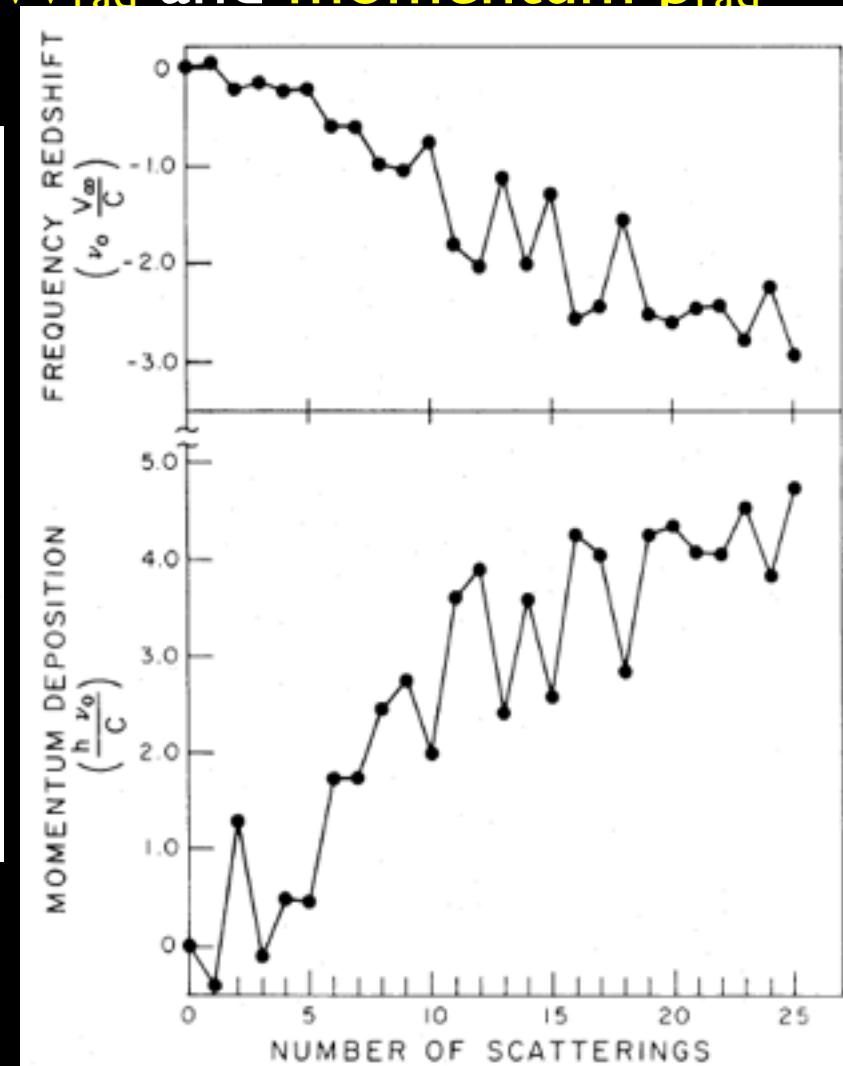
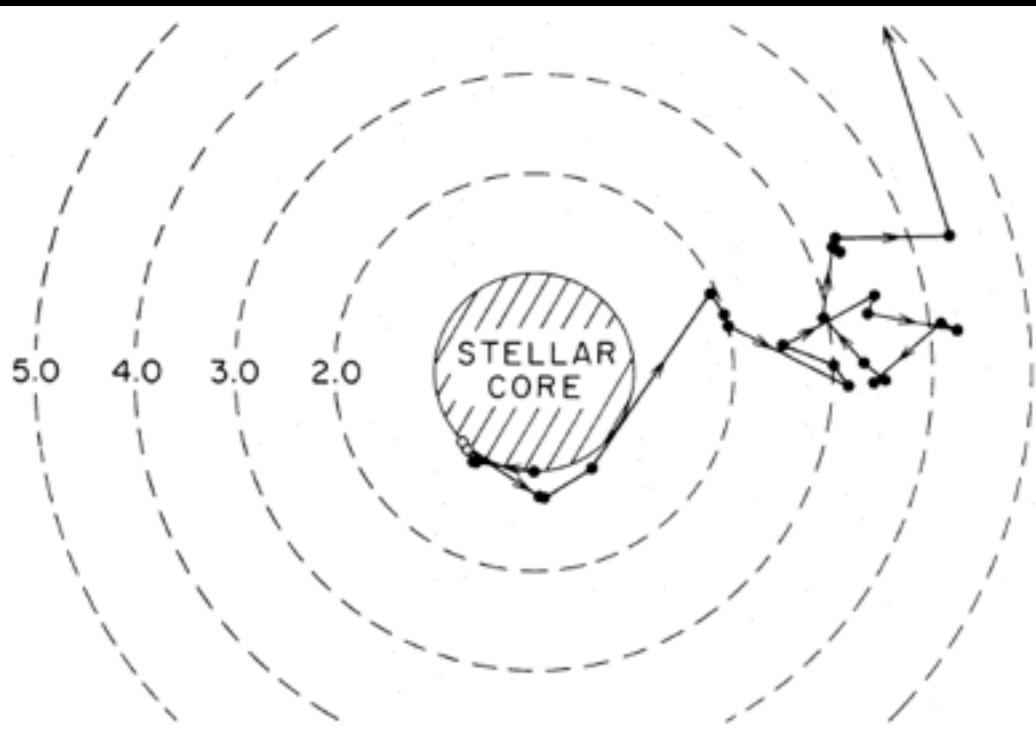
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 - WM-basic: Pauldrach + ~1985- pres.
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 - CMFGEN: Hiller+ ~1990-pres.
 - FastWind: Puls+ ~2000-pres.
- Solve with wind dynamics
 - Vink+ 2001-present: **Monte Carlo** + ISA NLTE
 - => recipe for $M_{\dot{d}o}$ & V_{inf}
 - Graefener 2005-present: CMF + NLTE

Monte-Carlo models

Abbott & Lucy 1985; LA 93; Vink et al. 2000

Assume velocity law + V_{inf} , use MC transfer through line list to compute global radiative work W_{rad} and momentum D_{rad}

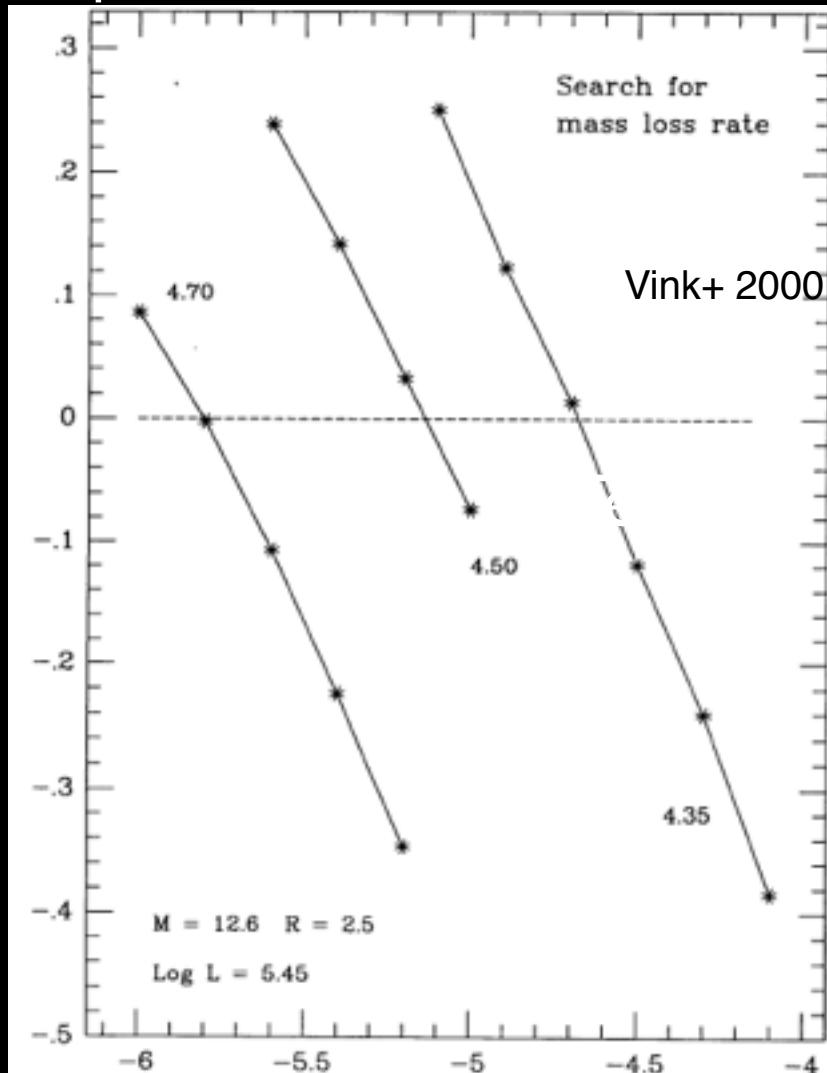


Monte-Carlo models

Compute mass loss rate from:

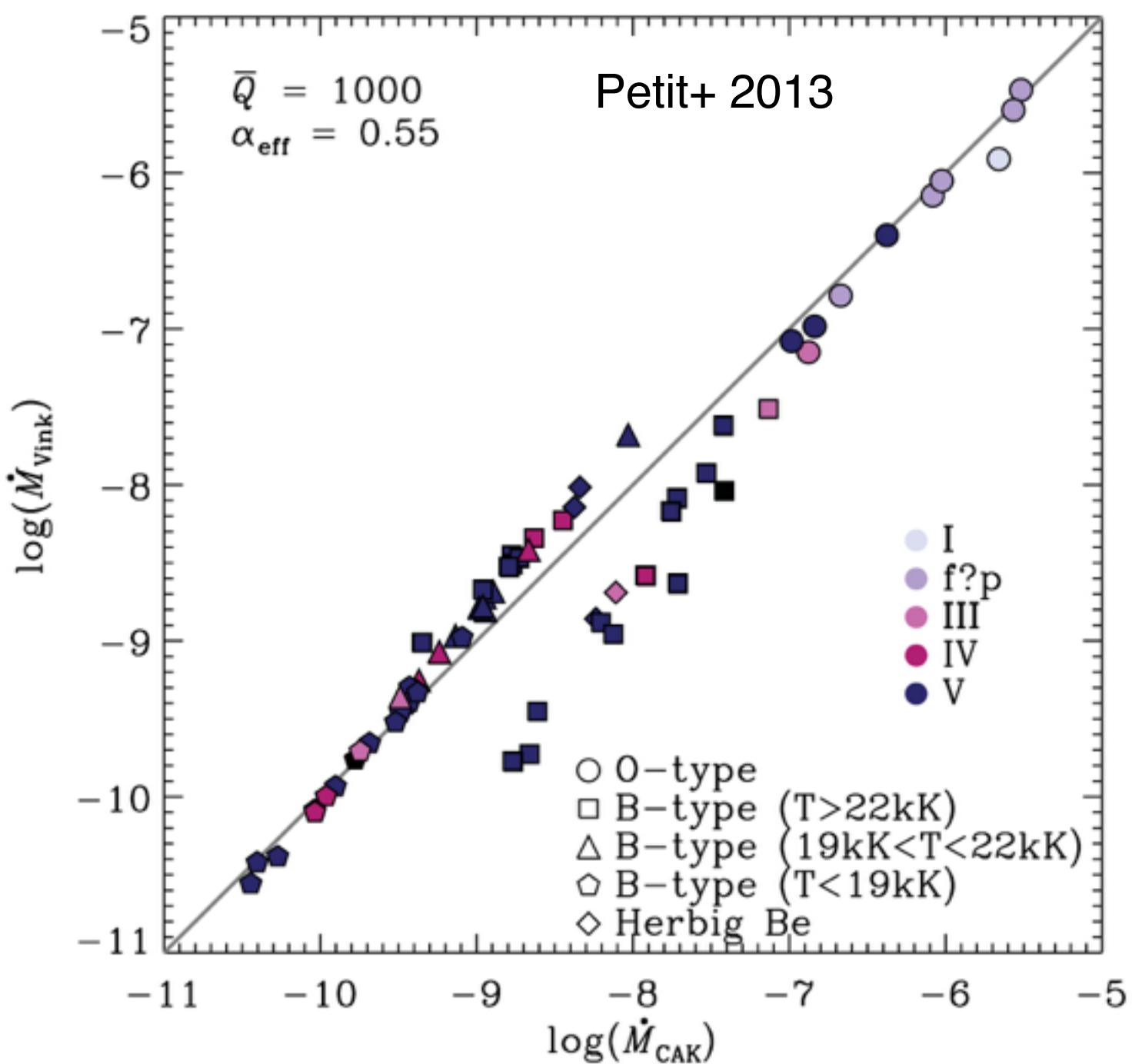
$$\dot{M} \approx \frac{2 W_{rad}}{V_{esc}^2 + V_\infty^2}$$

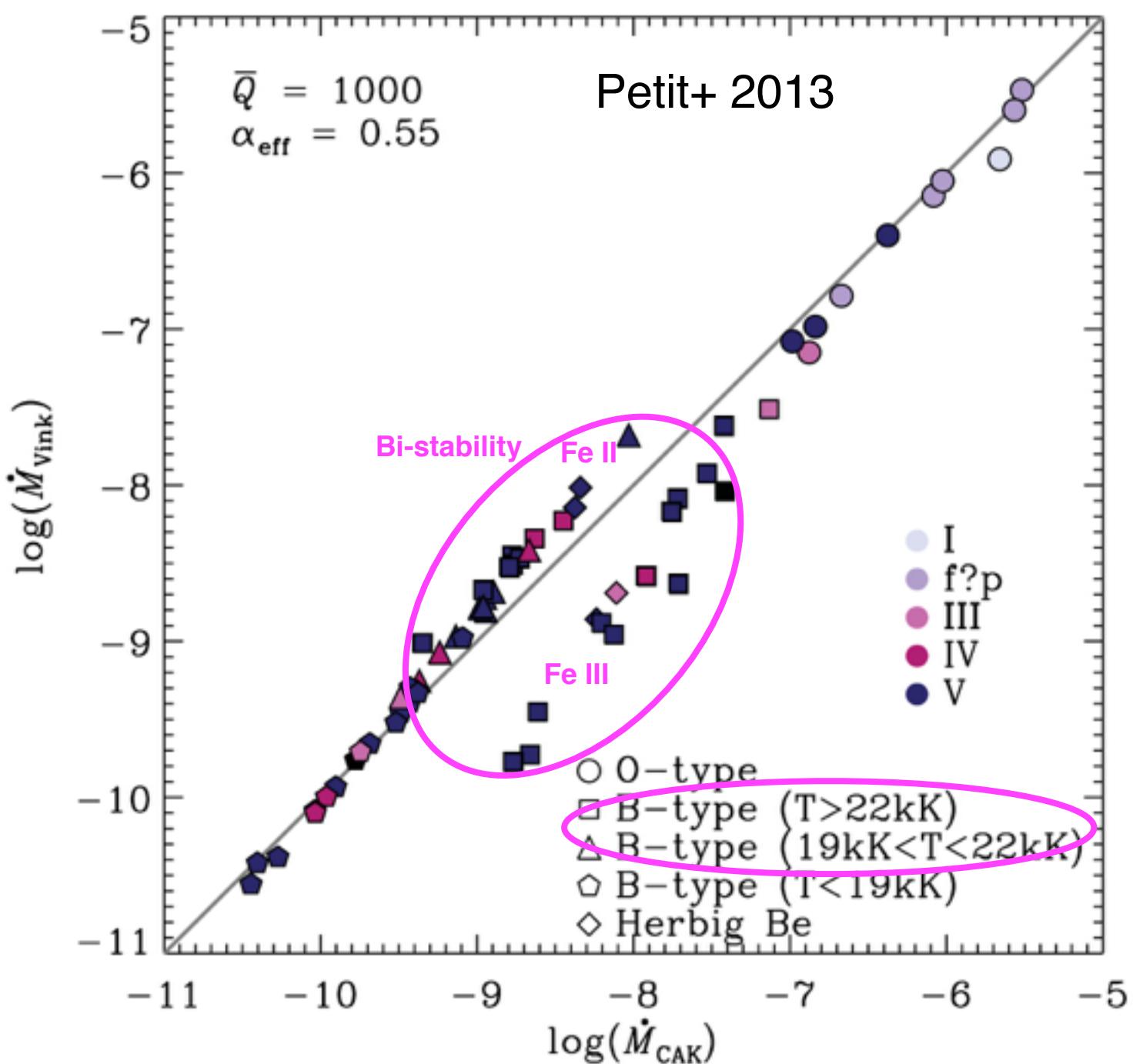
$$\log \frac{\dot{W}_{rad}}{E_{wind}}$$



Muller & Vink 2008:
can also infer V_{inf}

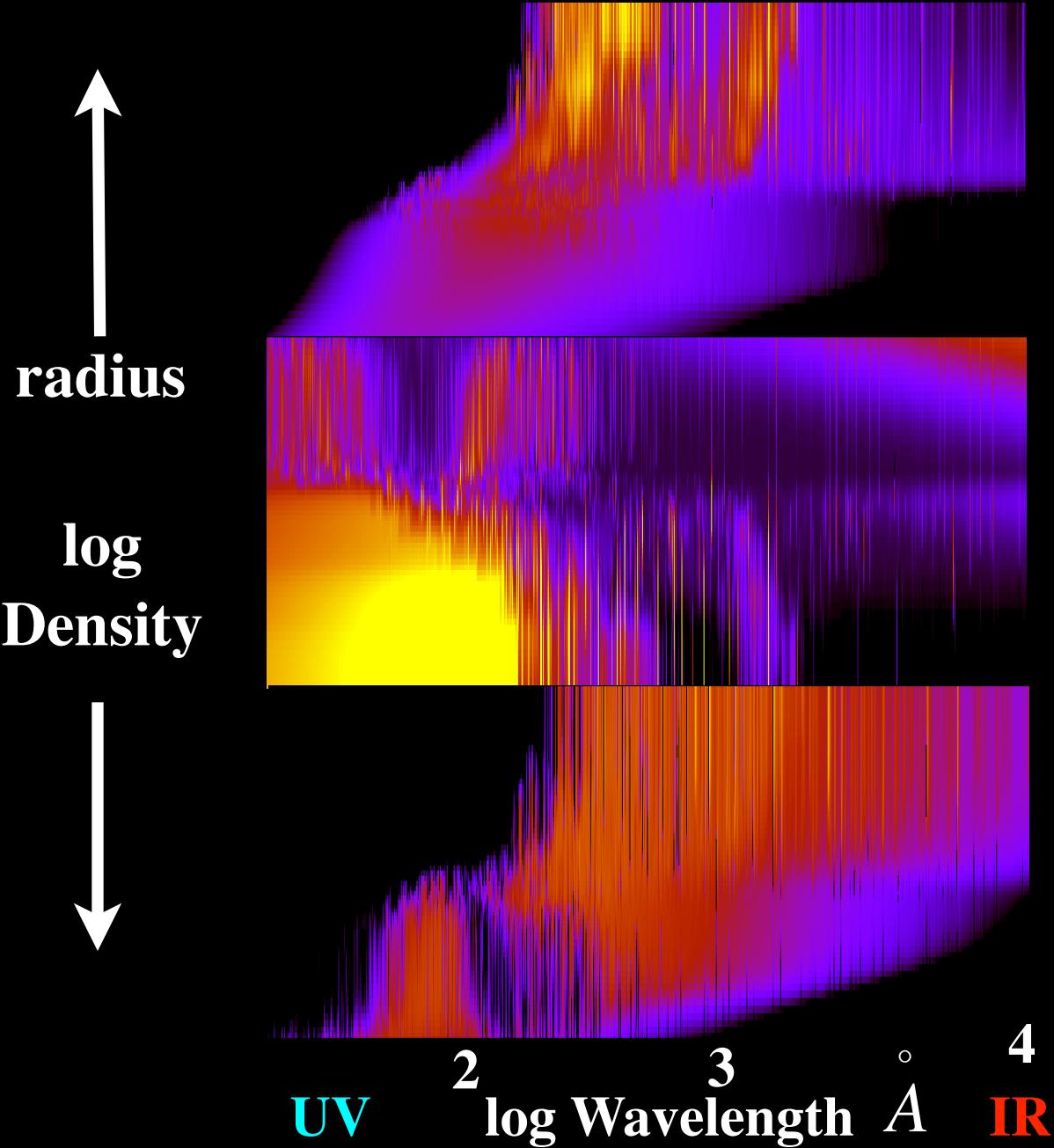
$$\log \dot{M}$$





Wolf-Rayet Wind Driving

courtesy
G. Graefener



Radiative
acceleration

=

Opacity

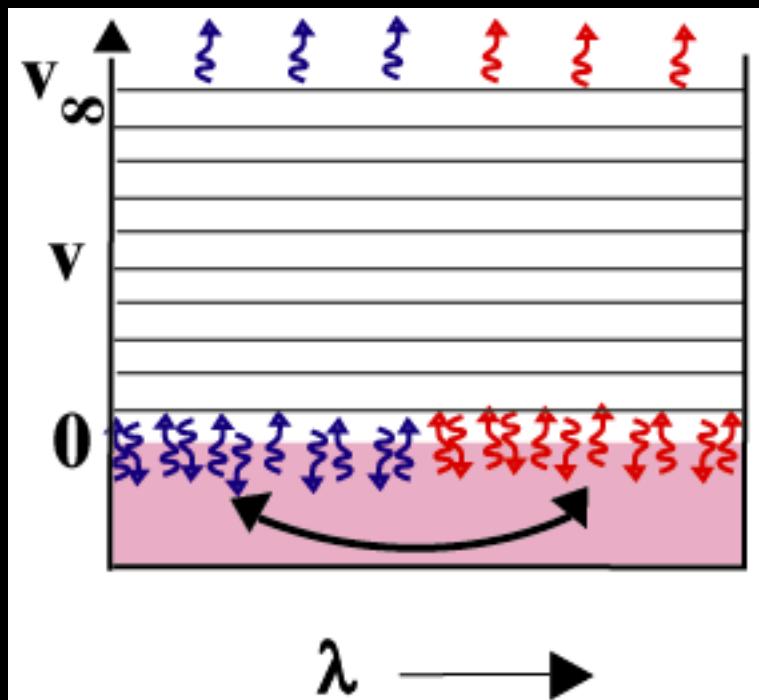
X

Flux

Multi-line scattering

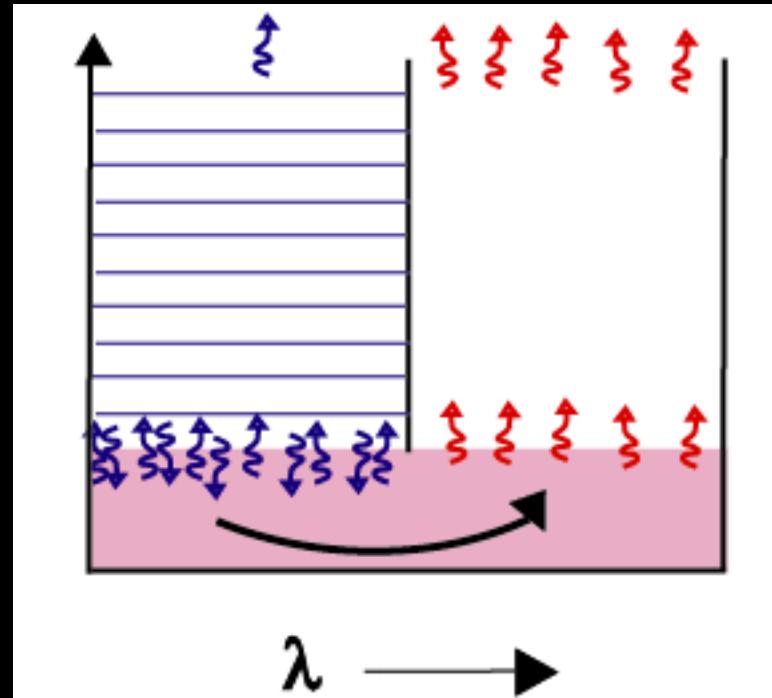
$$\Delta V = 10V_\infty$$

photon “leakage”



“Effectively gray” line-distribution

Friend & Castor 1982; Gayley et al. 1995

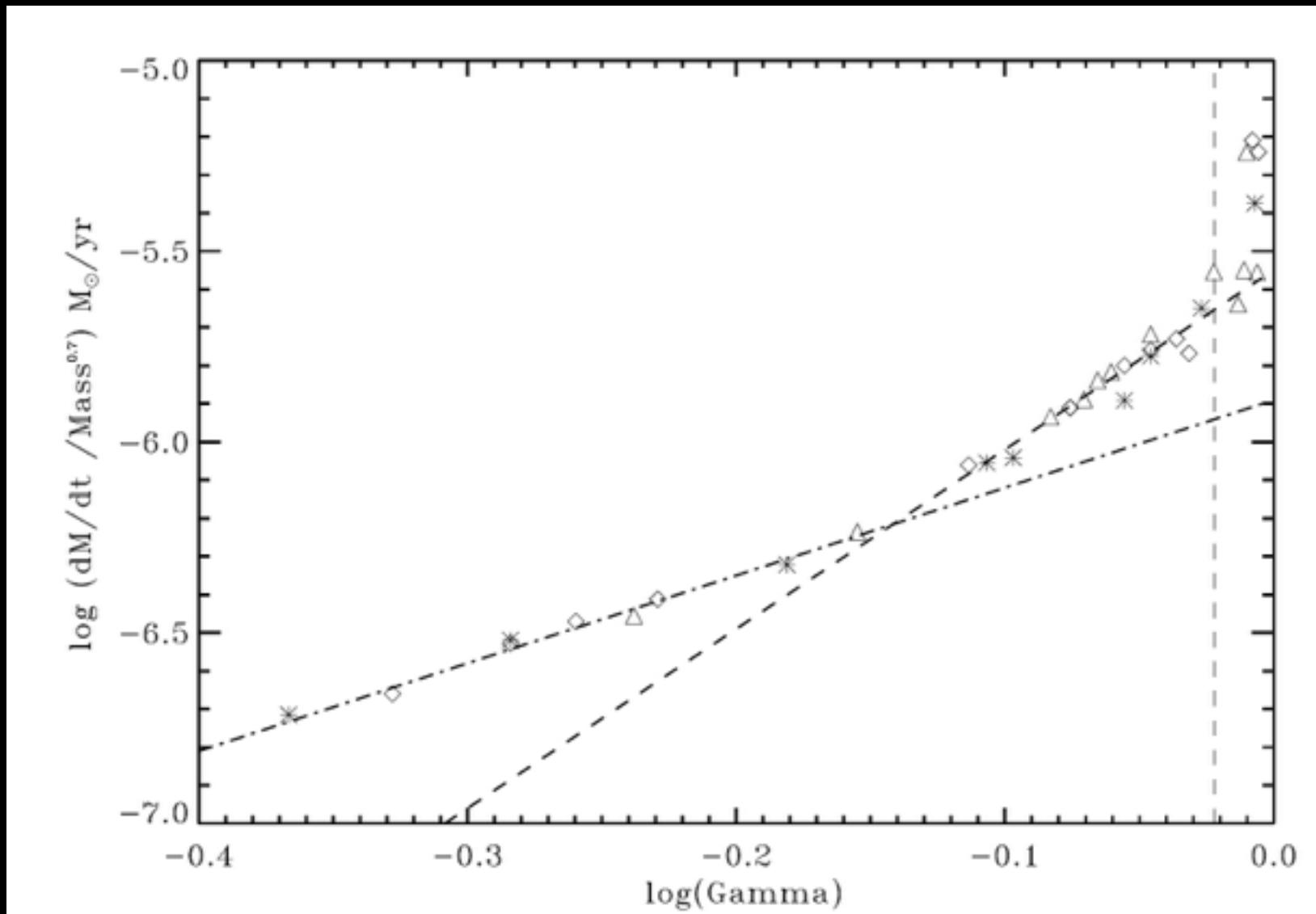


“Bunched” line-distribution

Onifer & Gayley 2006

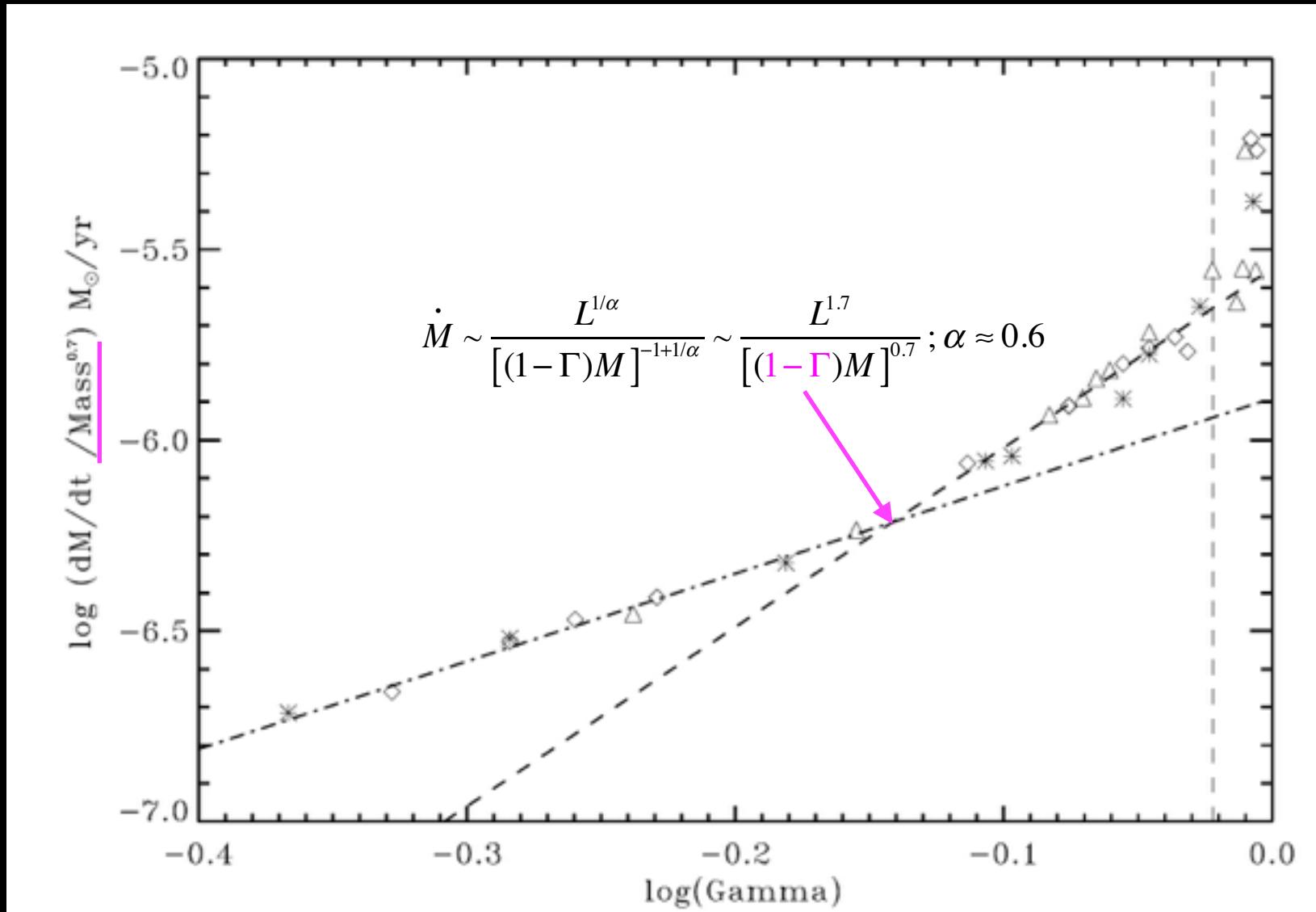
Line-Driven Mass Loss near Edd. limit

Vink+ 2011



Line-Driven Mass Loss near Edd. limit

Vink+ 2011



$P_{\text{rad}}/P_{\text{gas}}$ at sonic base of optically thick wind

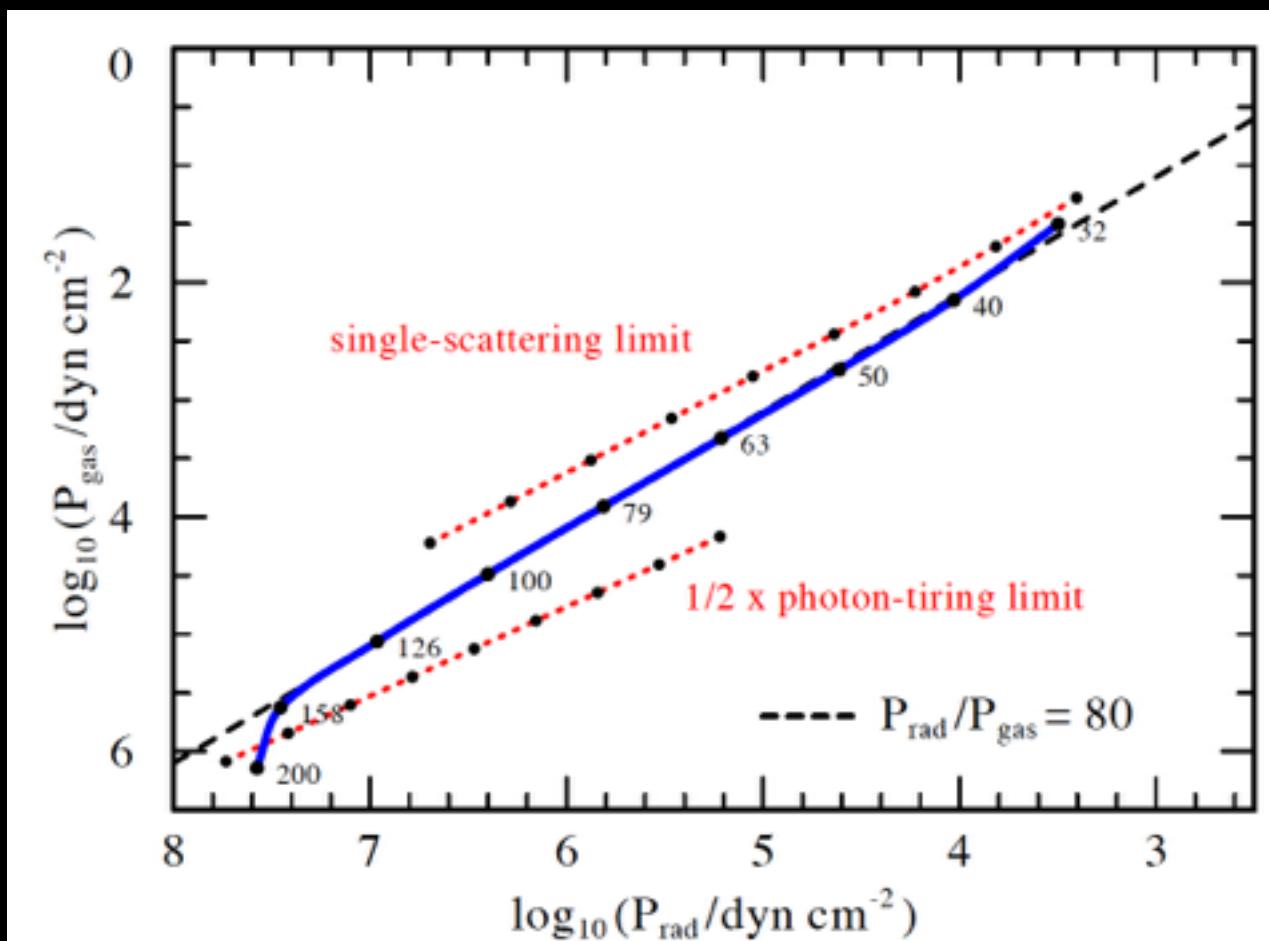
at sonic radius R :

$$P_{\text{gas}} = \rho a^2 = \frac{\dot{M} a}{4\pi R^2} = \tau \frac{F}{c} \left(\frac{\Gamma - 1}{\Gamma} \right) \frac{a}{v_\infty}$$

$$P_{\text{rad}} = \frac{F}{c} (\tau + 2/3)$$

$$\boxed{\frac{P_{\text{rad}}}{P_{\text{gas}}} = \frac{v_\infty}{a} \left(\frac{\tau + 2/3}{\tau} \right) \left(\frac{v_\infty^2}{v_{\text{esc}}^2} + 1 \right)}$$

Graefener & Vink 2013

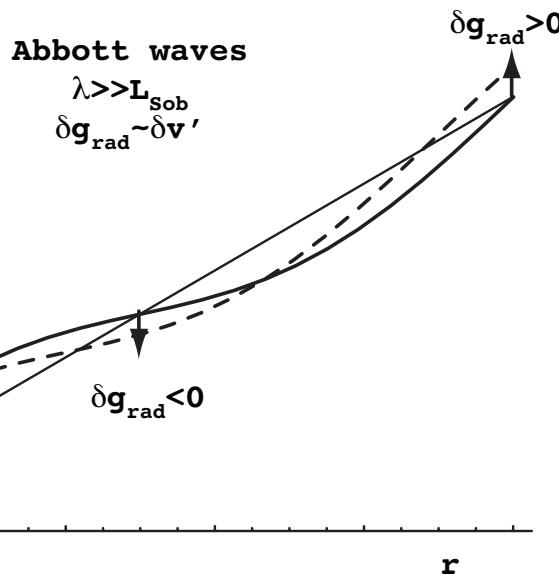


Is line-driving stable?

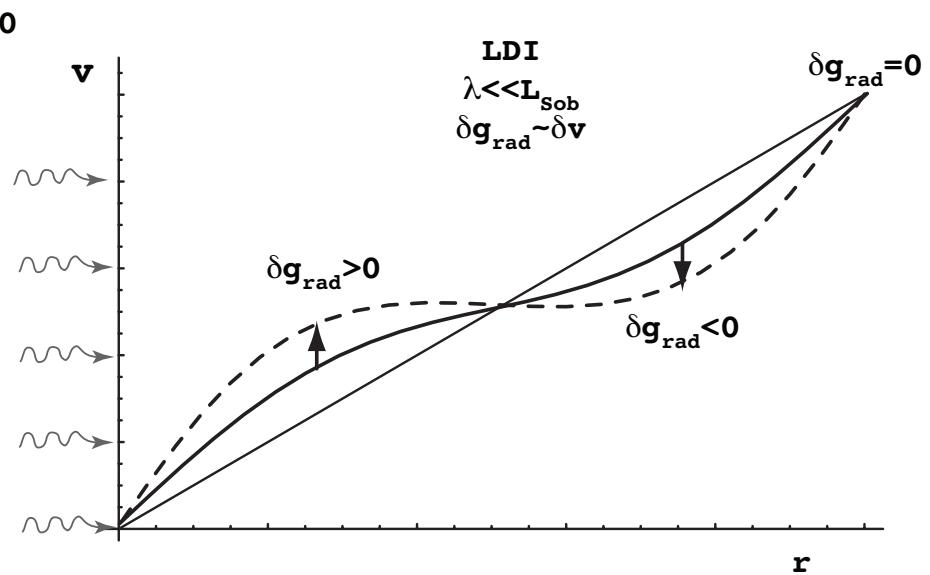
Carry out linear stability
analysis

Response to small-amp. perturbation

Stable



Unstable



Abbott speed
 $\delta g_{rad}/\delta v' = -U \approx -v$

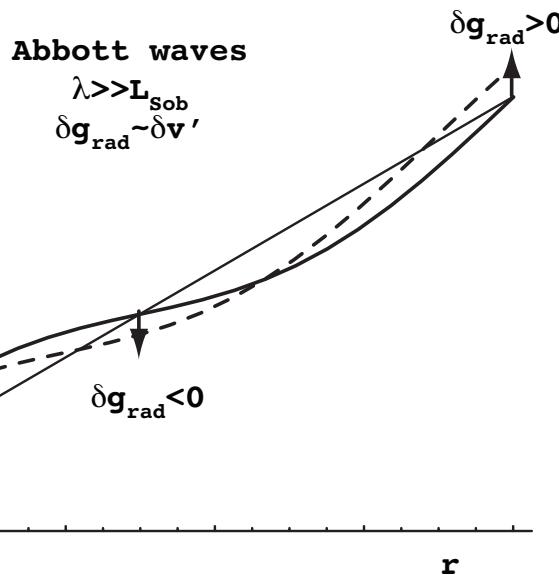
Abbott 1980

Instability growth rate

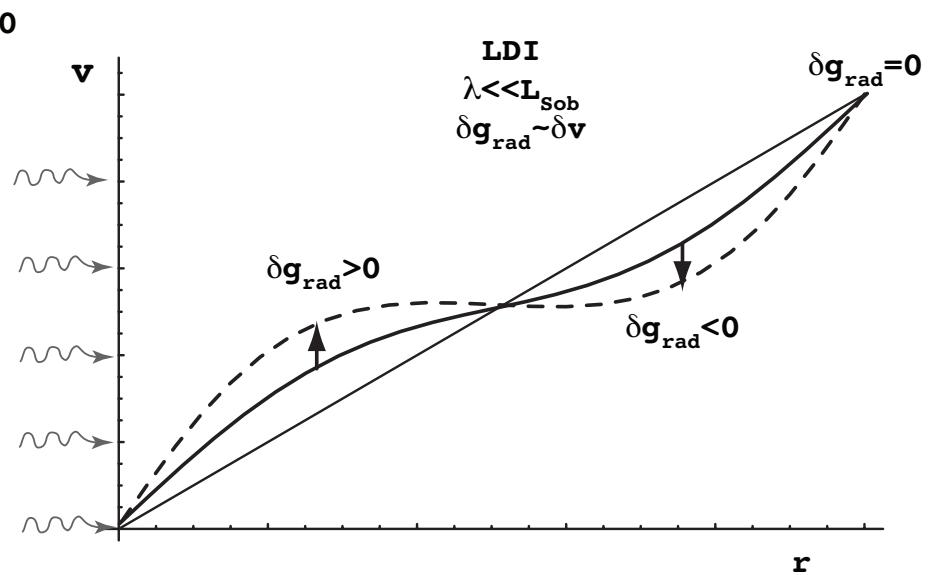
$$\begin{aligned}\delta g_{rad}/\delta v &= \Omega \\ &\sim g_0/v_{th} \sim vv'/v_{th} \sim v/L_{sob} \sim 100 v/R \\ &\Rightarrow e^{100} \text{ growth!}\end{aligned}$$

Response to small-amp. perturbation

Stable



Unstable



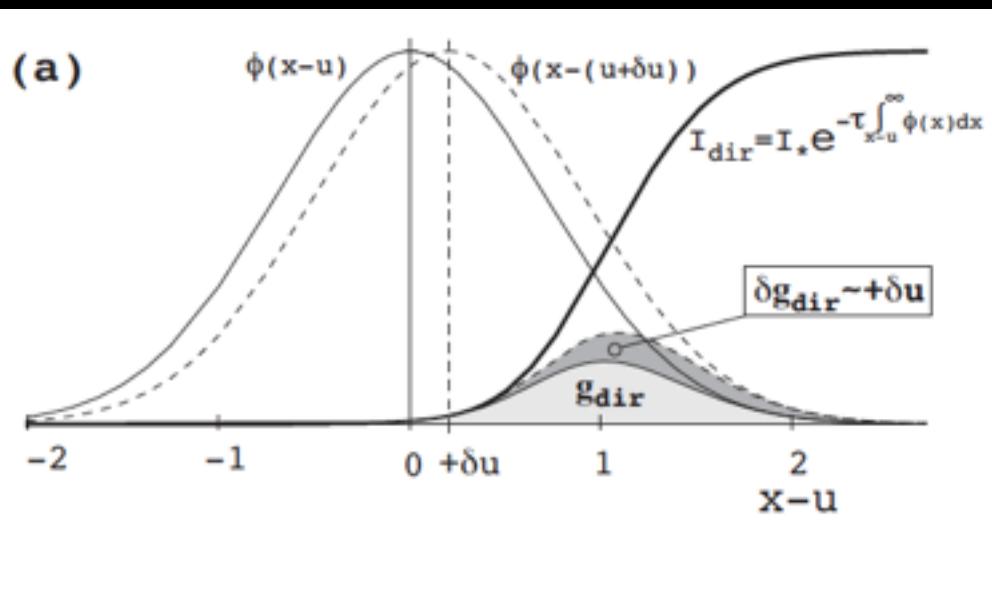
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Line-Deshadowing Instability



for $\lambda < L_{\text{sob}}$:

$$i\omega = \delta g / \delta v = +g_o / v_{\text{th}} = \Omega$$

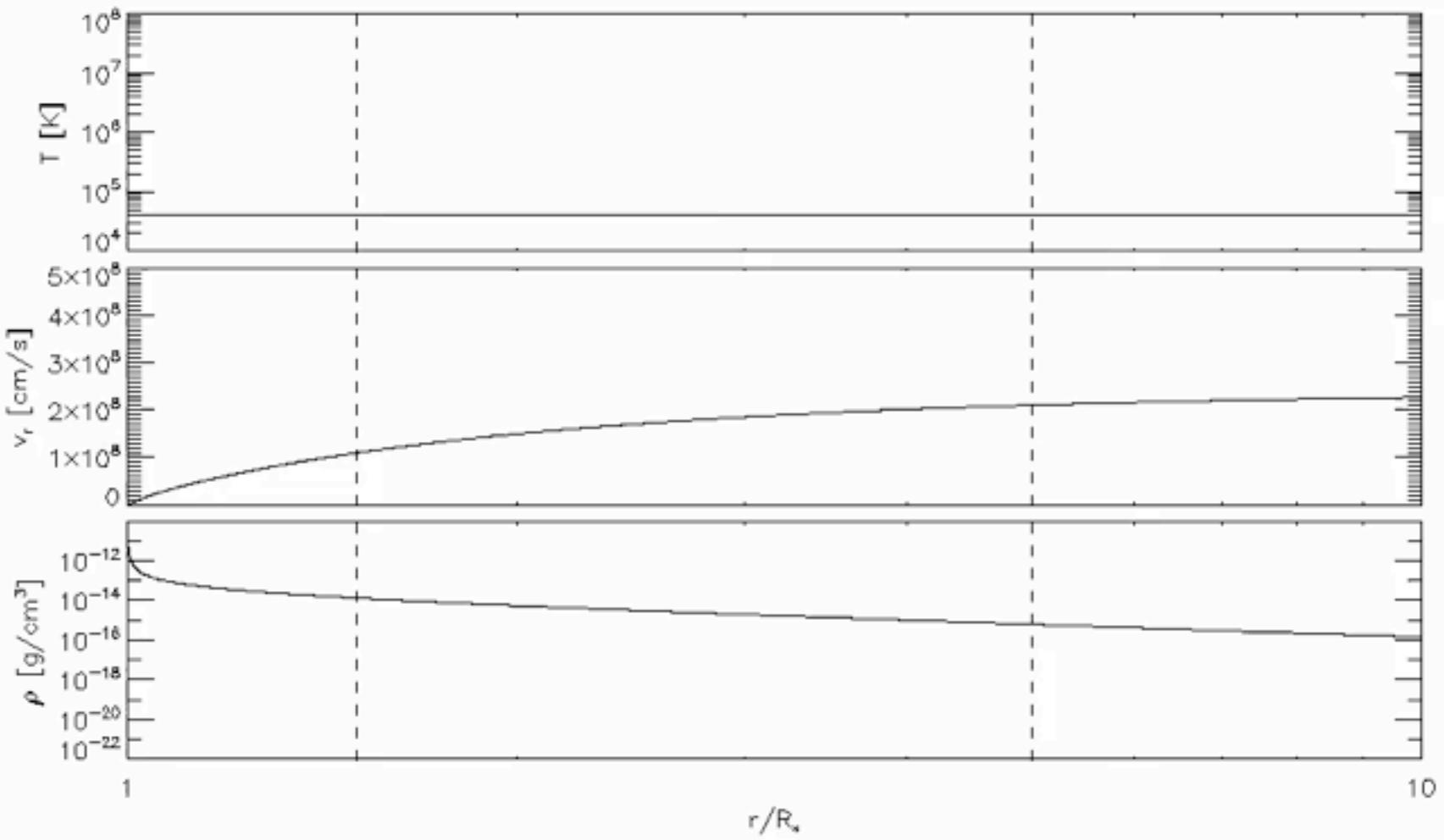
Instability with growth rate

$$\Omega \sim g_o / v_{\text{th}} \sim v v' / v_{\text{th}} \sim v / L_{\text{sob}} \sim 100 v / R$$

$\Rightarrow e^{100}$ growth!

1D SSF sim of LDI

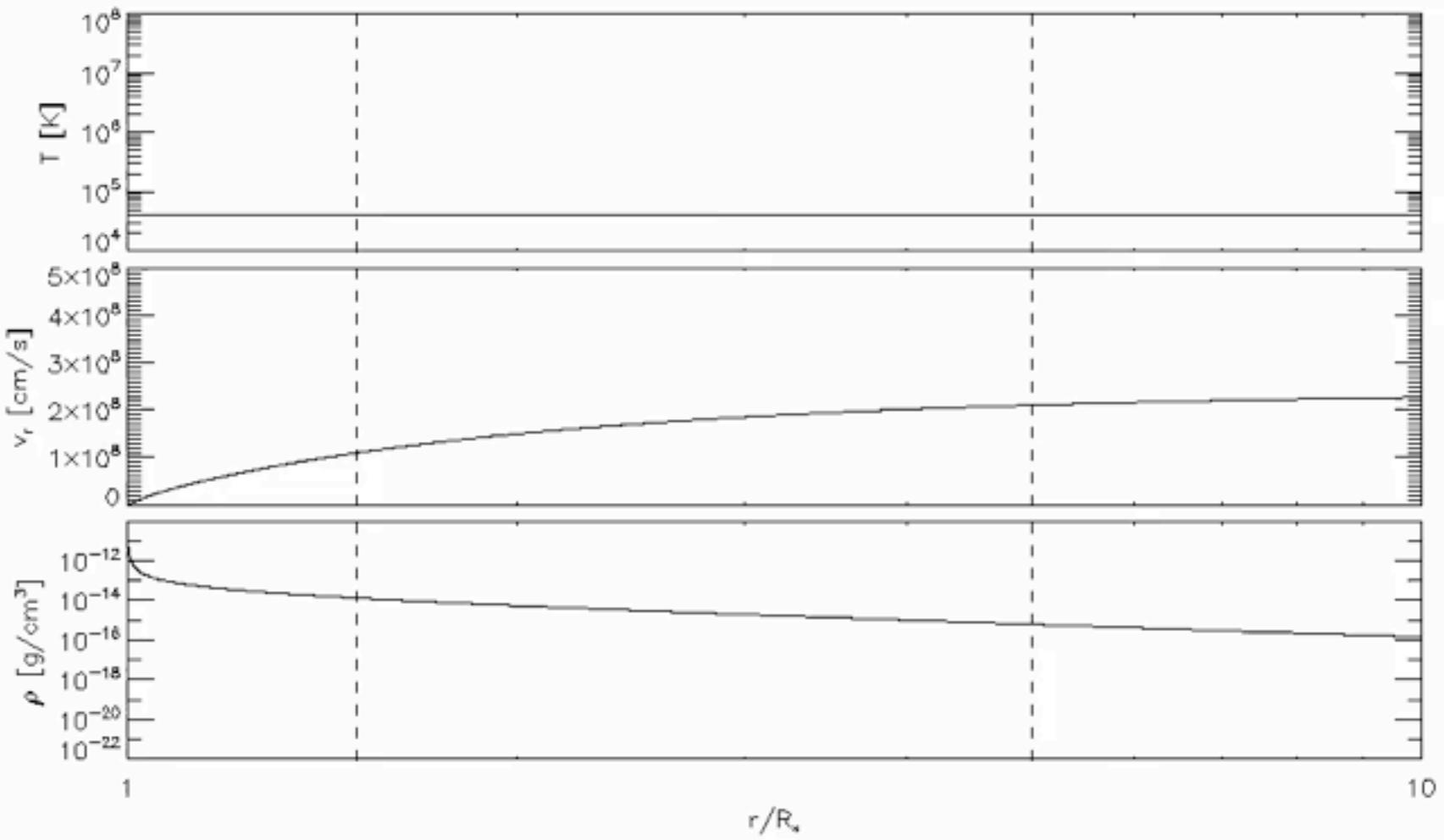
Smooth Source Function



courtesy J. Sundqvist

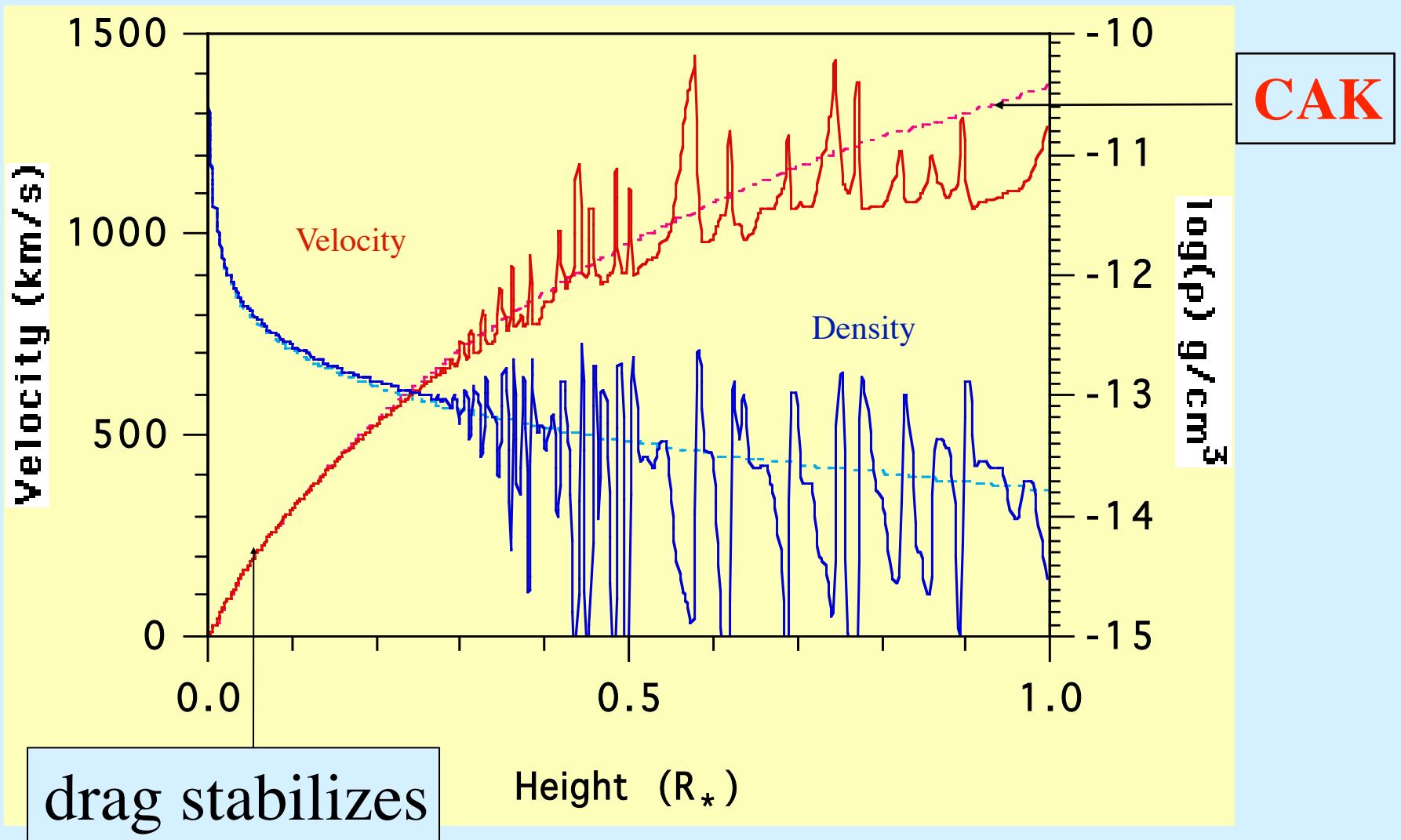
1D SSF sim of LDI

Smooth Source Function



courtesy J. Sundqvist

Time snapshot of SSF instability simulation



but back-scattering also self-excites!

Hydro sims, 2D-R

The **radial** line-force drives the wind outflow. But in 2-D (or 3-D), you can also have a non-zero **lateral** radiation force, which may then affect the scales and shapes of clumps.

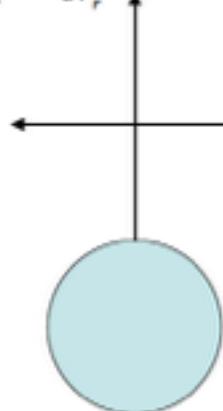
Lateral line-drag

Owocki+ 90

$$\frac{\delta g_r^{dir}}{\delta v_r} + \frac{\delta g_r^{diff}}{\delta v_r} \approx (100 - 50) \frac{v}{r}$$

net **radial instability** for:

$$\lambda_r \leq L_r = \frac{v_{th}}{dv/dr} = \frac{v_{th}}{v} r$$



$$\frac{\delta g_\phi^{dir}}{\delta v_\phi} = 0$$
$$\frac{\delta g_\phi^{diff}}{\delta v_\phi} = -50 \frac{v}{r}$$

lateral damping for:

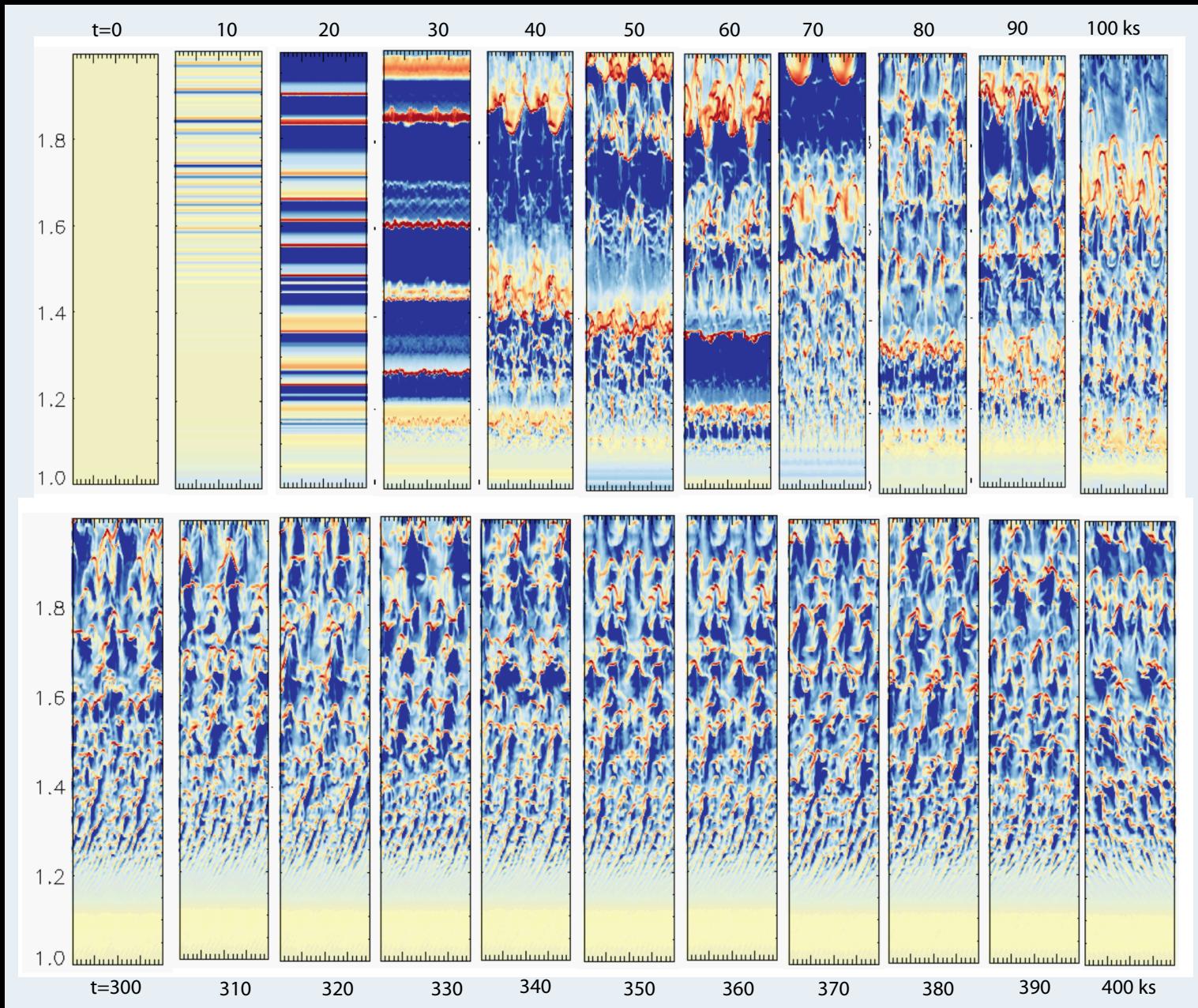
$$\lambda_\phi = r d\phi \leq L_\phi = \frac{v_{th}}{v/r}$$

$$d\phi \leq \frac{v_{th}}{v} = \frac{1}{100} = 0.6^\circ$$

2D-H + 2D-R planar LDI sims

Sundqvist+ in prep.

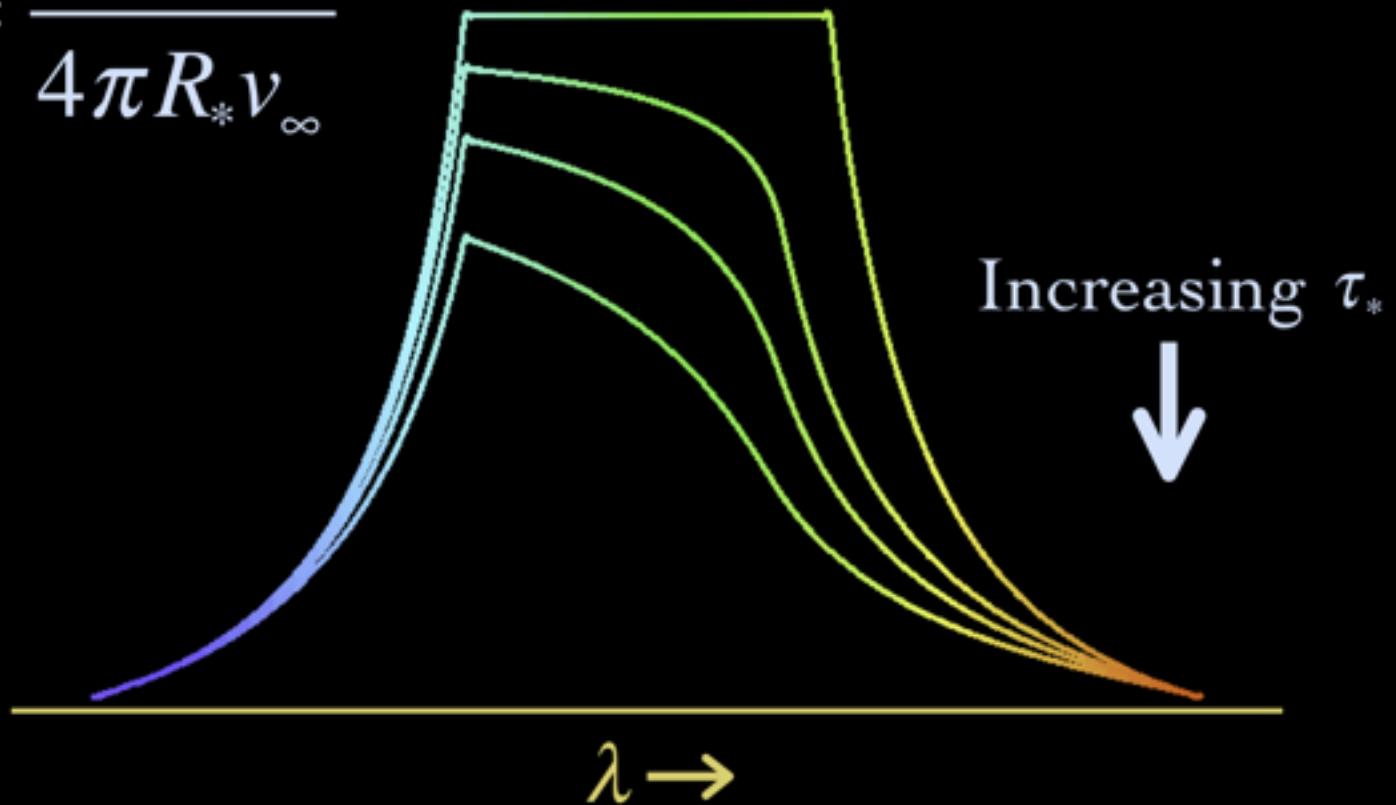
↑ — r=1 to 2 Rstar —→



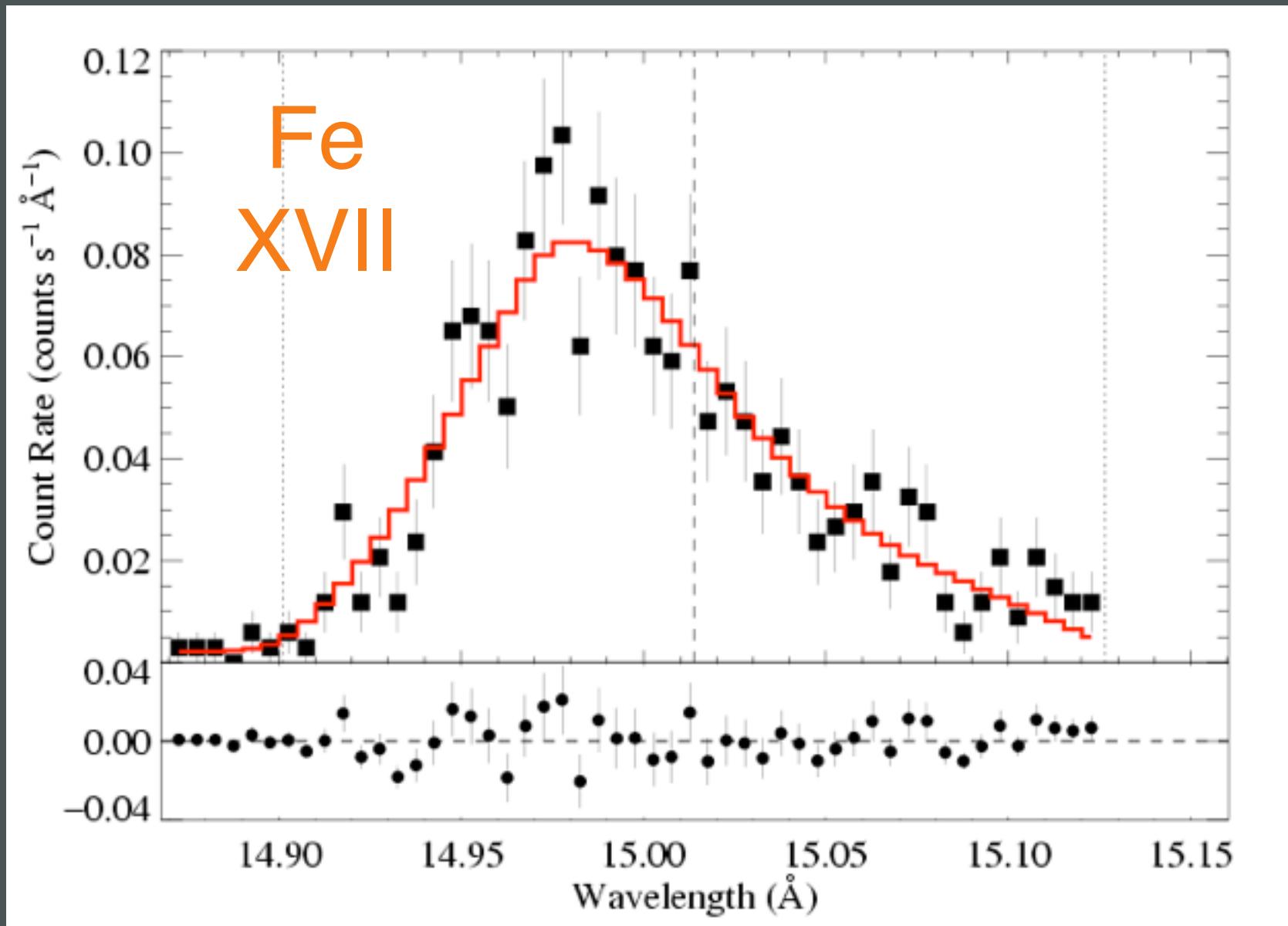
$$\frac{\delta\rho}{\langle\rho\rangle}$$

X-ray emission line-profile

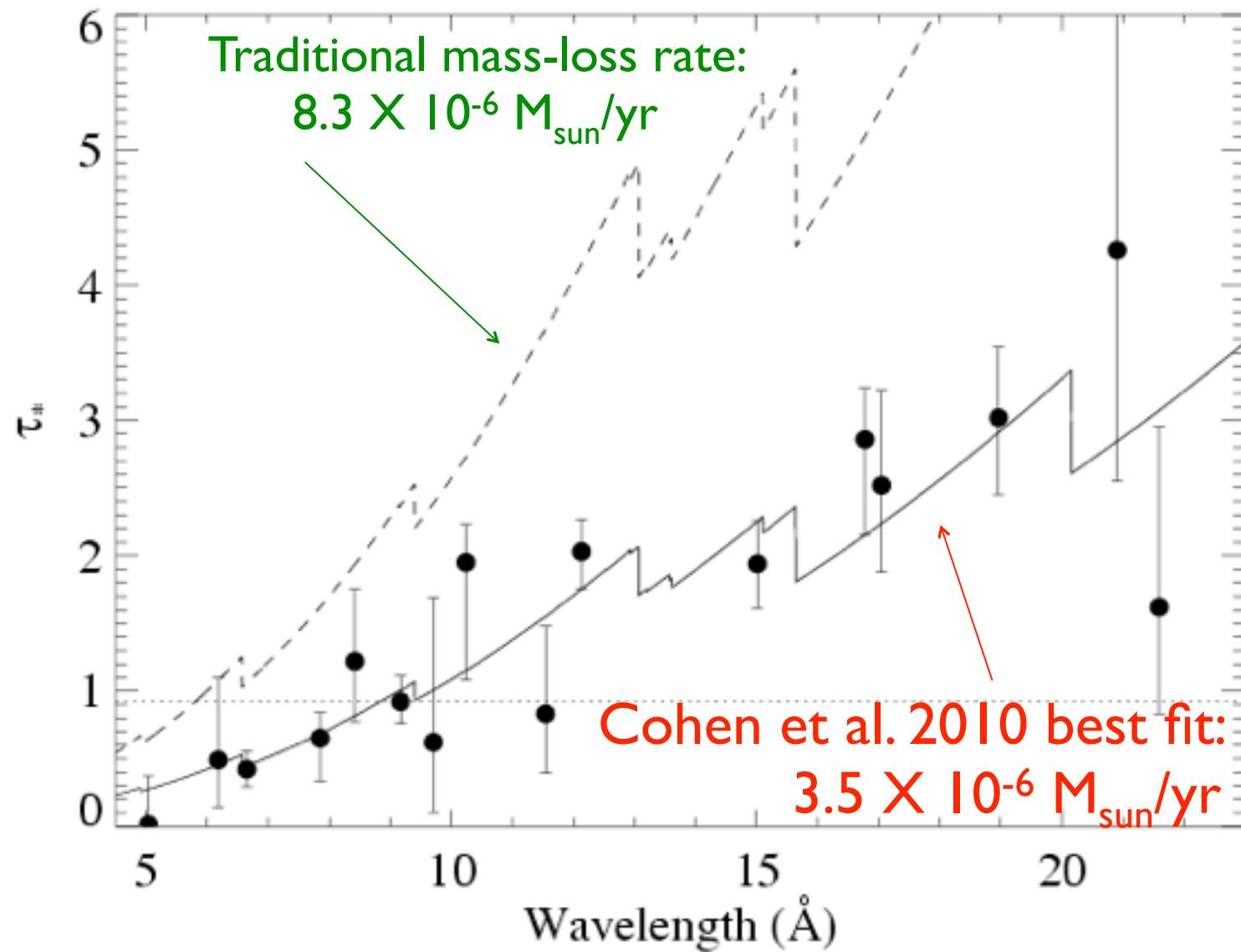
$$\tau_* = \frac{\kappa \dot{M}}{4\pi R_* v_\infty}$$



Chandra X-ray line-profile for ZPup



Inferring ZPup M_{dot} from X-ray lines



How are such winds
affected by (rapid)
stellar rotation?

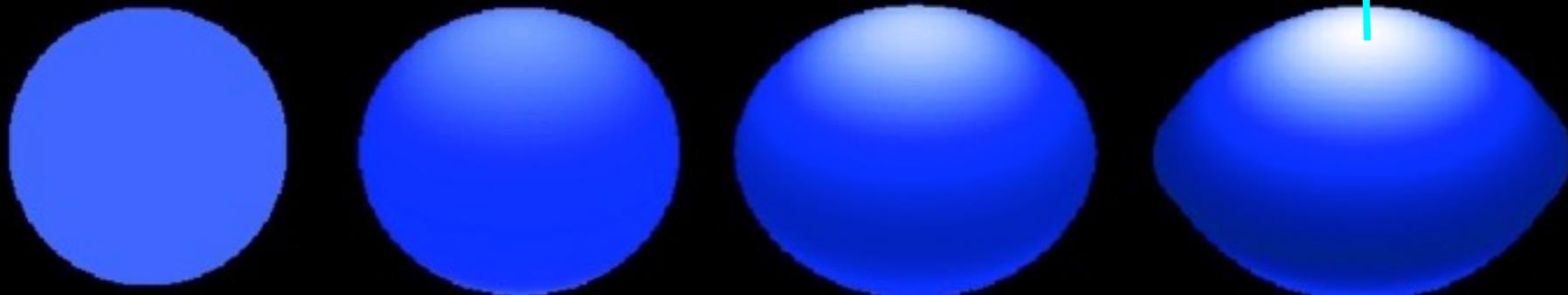
Gravity Darkening

$$\dot{M} \sim F(\theta)$$

$$F(\theta) \sim g_{eff}(\theta)$$

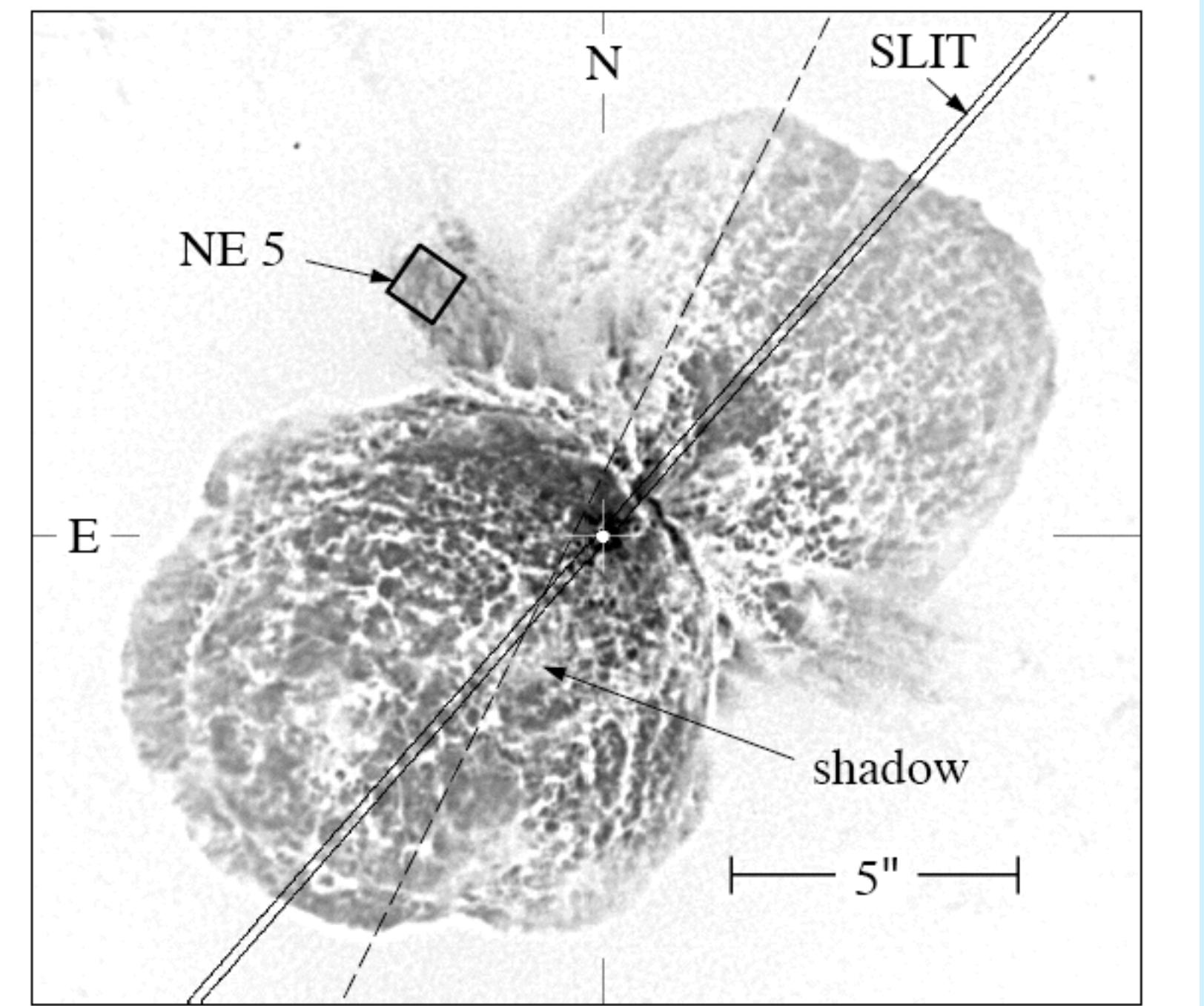
$$V_\infty \sim \sqrt{g_{eff}(\theta)}$$

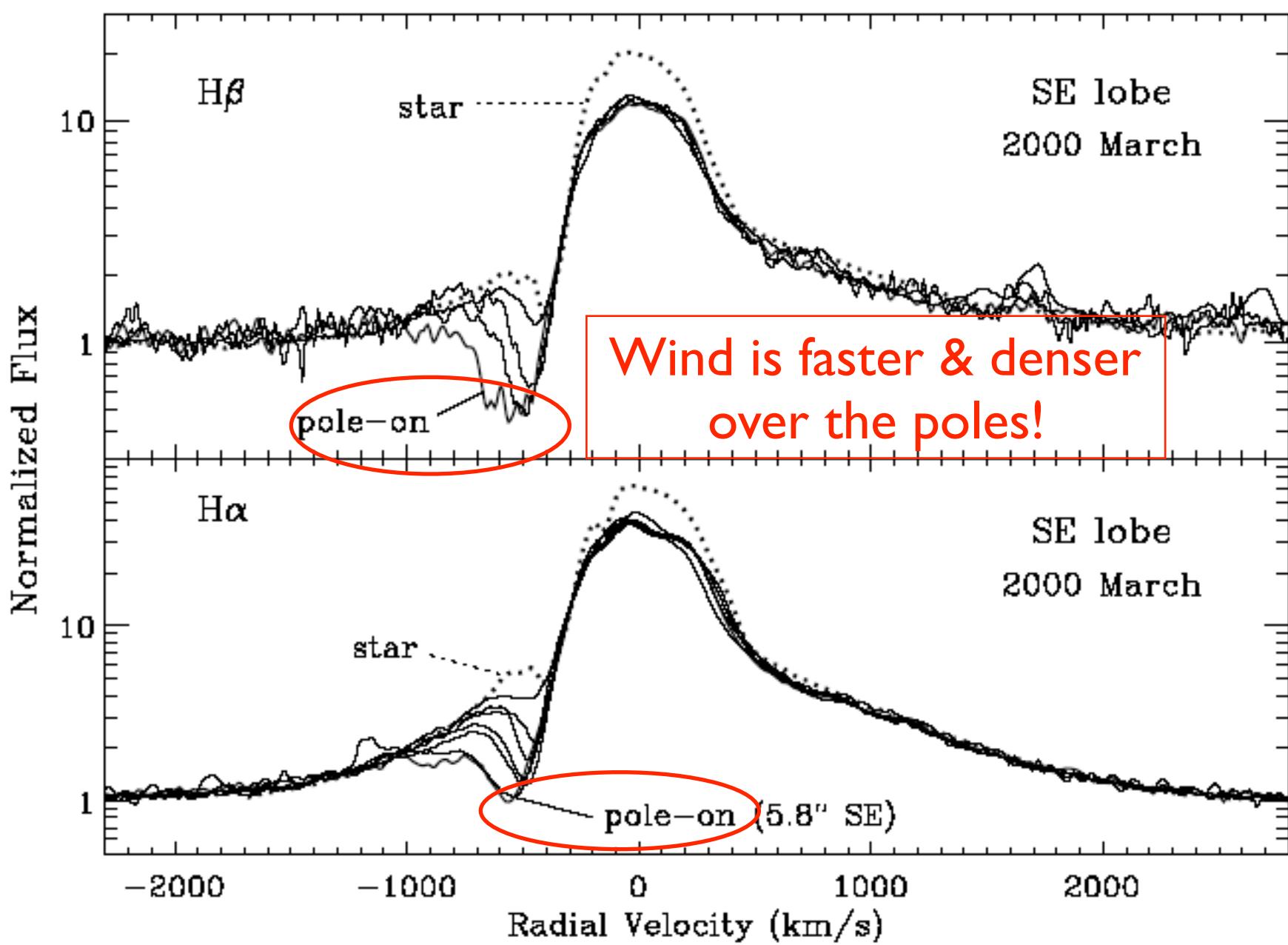
higher at pole!



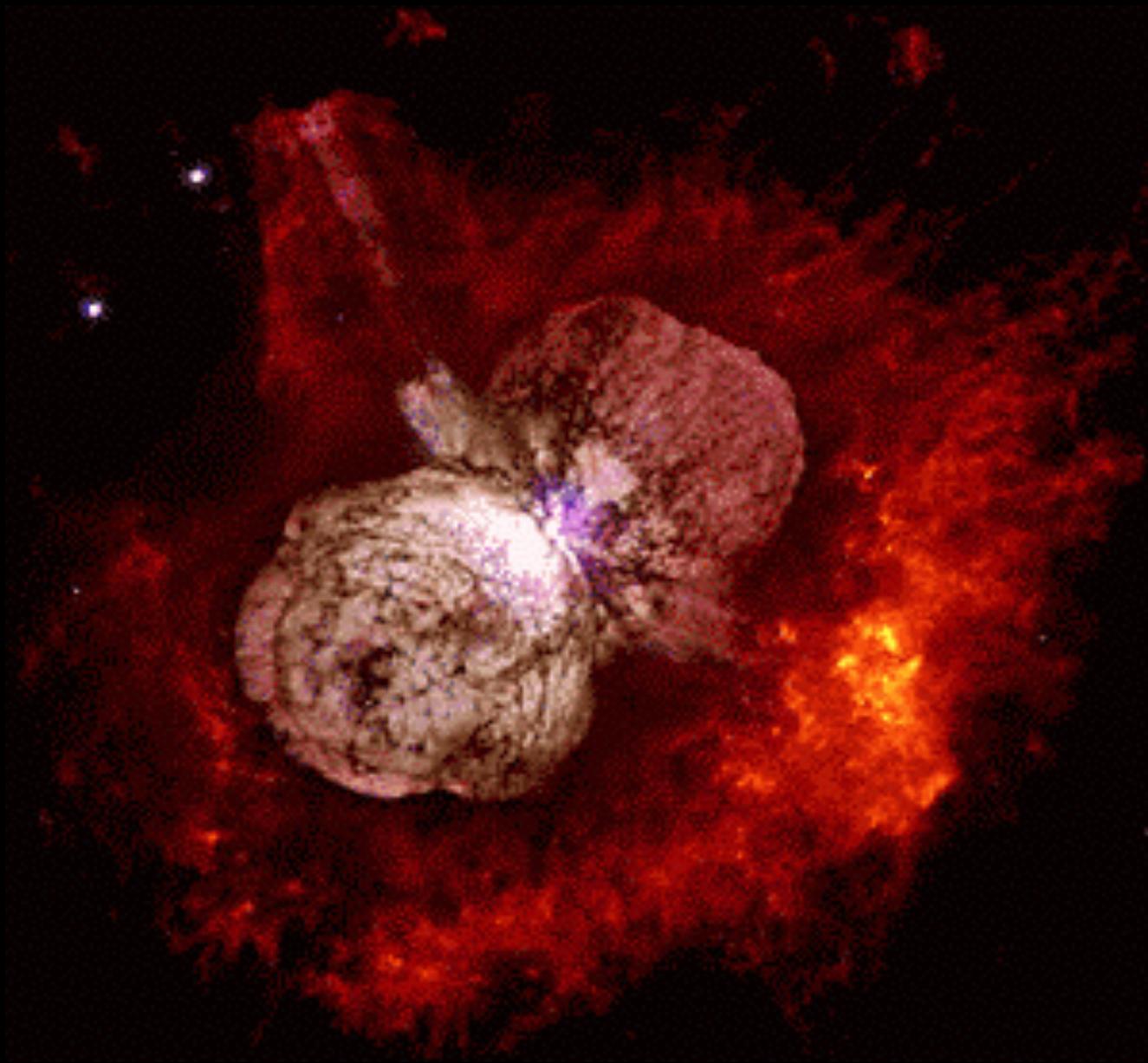
increasing stellar rotation







Eta Carinae



Massive, Luminous stars:

Several M_{\odot} of circumstellar matter resulting from brief eruptions, expanding at about 50-600 km/s.

VY CMa



IRC+10420



P Cygni



SN1987A
(courtesy P. Challis)



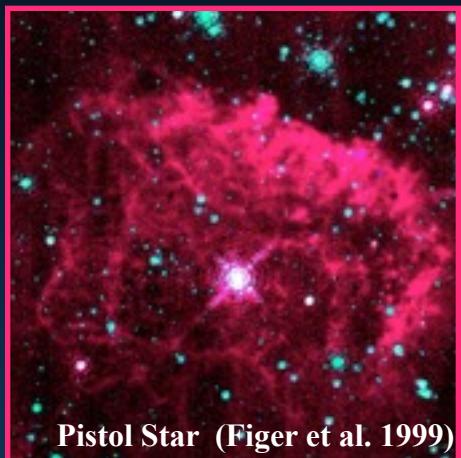
HD 168625
(Smith 2007)



Sher 25
(Brandner et al. 1997)



Eta Car



Pistol Star (Figer et al. 1999)

3 Key points about η Car's eruption

1. $M_{\dot{m}} > 10^3 M_{\dot{m}}(\text{CAK})$

=> can **NOT** be line-driven!

2. $L_{\text{obs}} > L_{\text{Edd}}$

=> “super-Eddington” (by factor $> 5!$)

3. $L_{\text{obs}} \approx M_{\dot{m}} V^2 / 2$

=> $M_{\dot{m}}$ limited by energy or “photon-tiring”

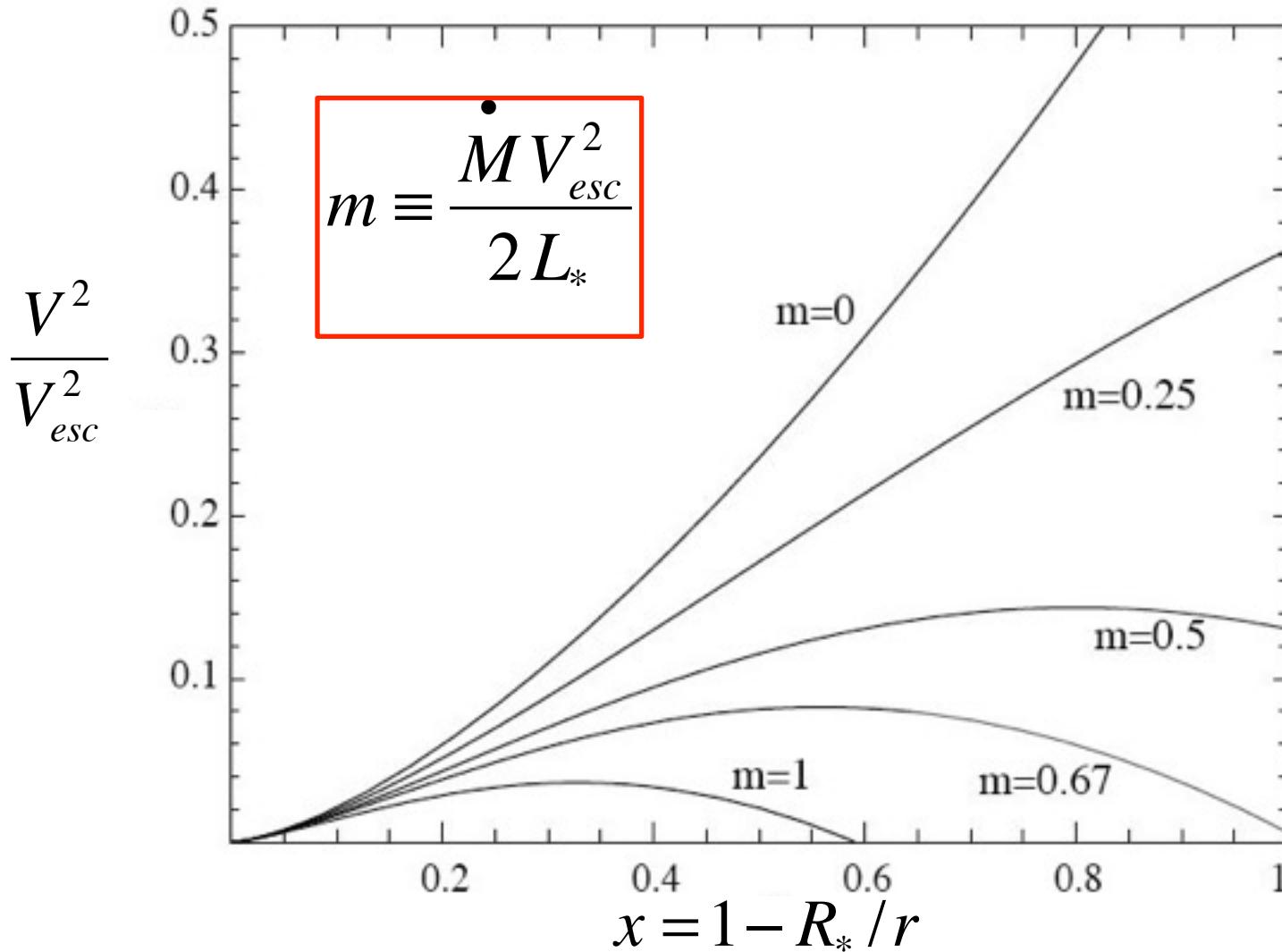
super-Eddington continuum-driven wind

- Quataert+ 2016
 - add energy $E_{\dot{m}} > L_{\text{Edd}}$ at some R_h in envelope
 - $\tau \gg 1 \Rightarrow F_{\text{rad}} \rightarrow 0$, so $E_{\dot{m}} \Rightarrow$ rad. enthalpy $h = 4P_{\text{rad}}/\rho$
 - leads to $\gamma = 4/3$ polytropic wind
 - But(!), also need to ensure $E_{\dot{m}} > M_{\dot{m}} GM/R_h$
- Owocki & Gayley 1997, Owocki, Gayley & Shaviv 2004
 - continuum flux-driven wind with photon tiring

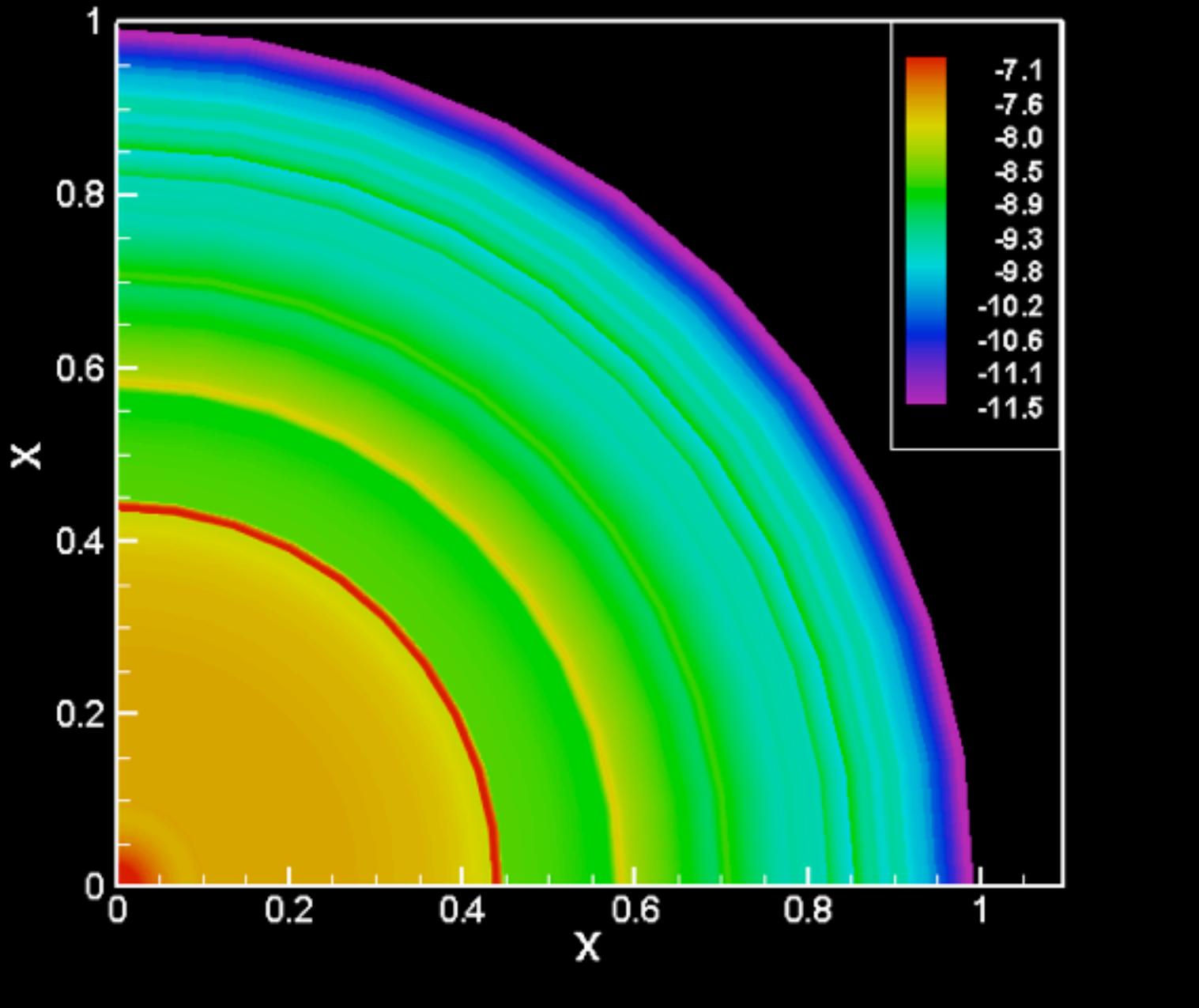
Stagnation of photon-tired outflow

$$\frac{\kappa}{\kappa_{Edd}} = 1 + \sqrt{x}$$

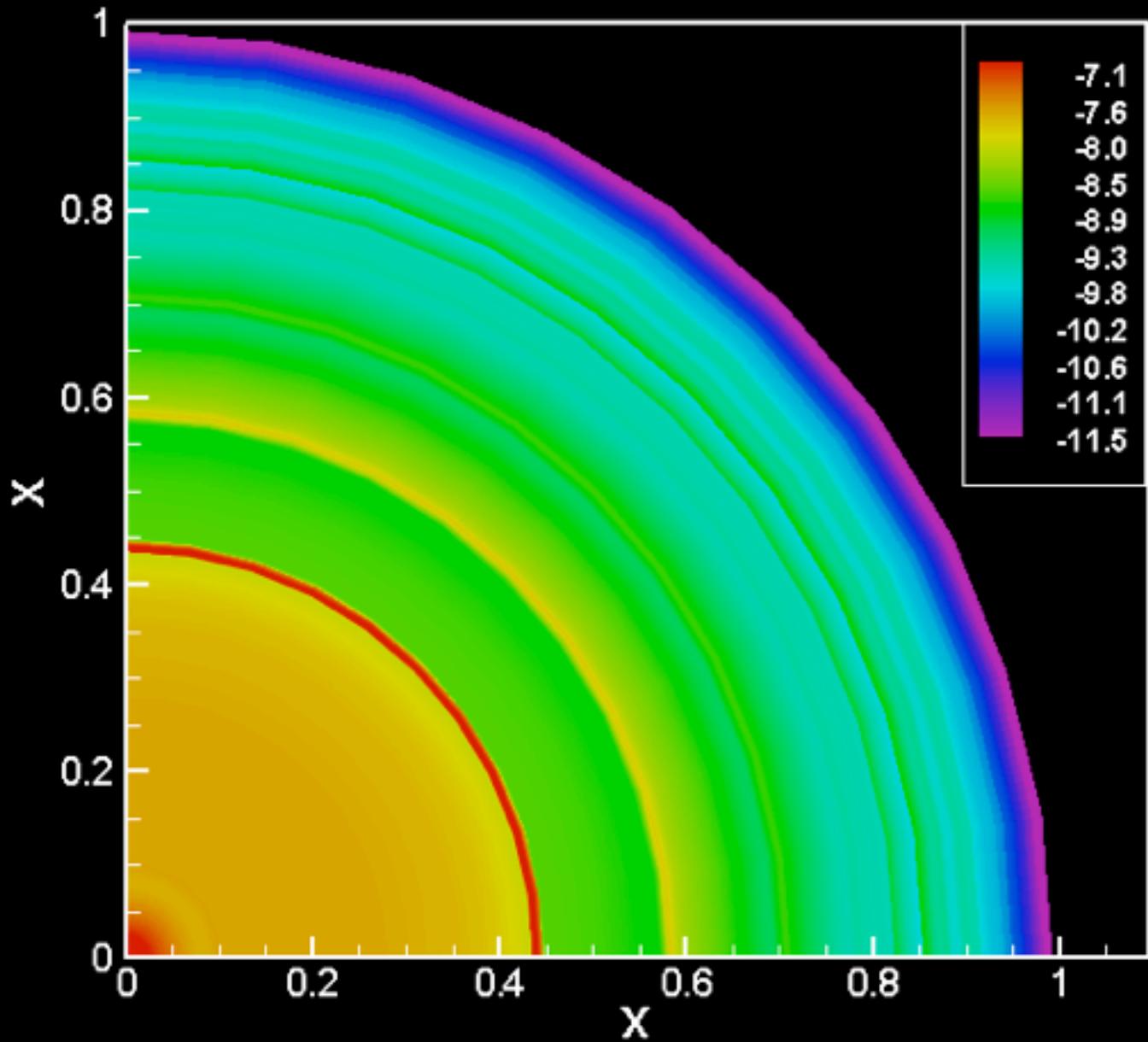
$$L(r) = L_* - \dot{M} \left[\frac{V^2}{2} + \frac{GM}{R} - \frac{GM}{r} \right]$$



Density after 0.0000E+00 seconds



Density after 0.0000E+00 seconds

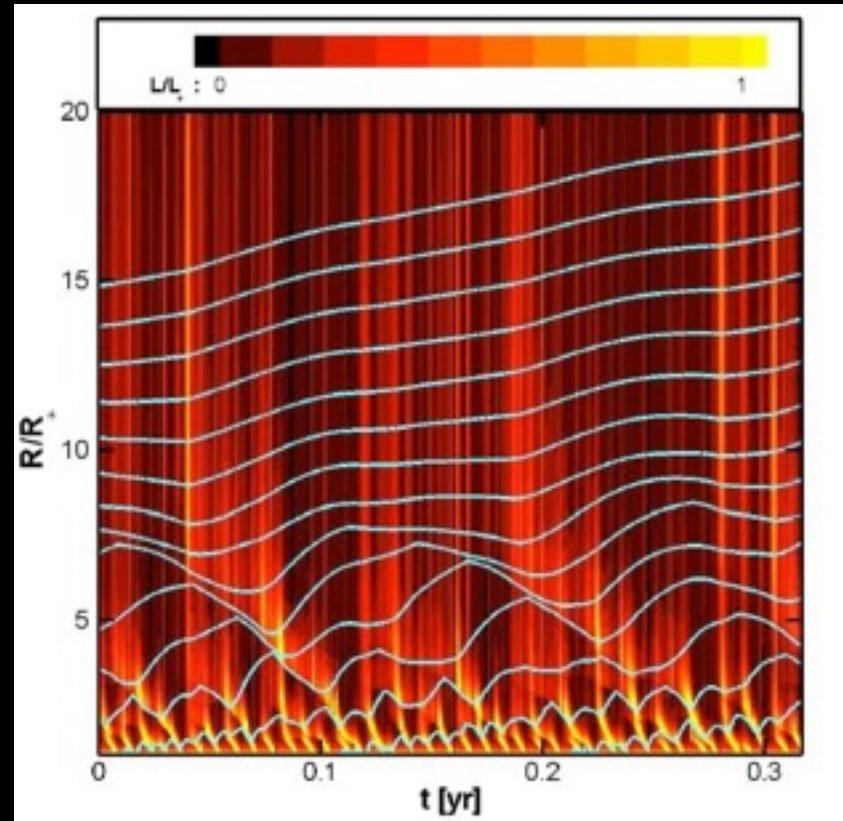
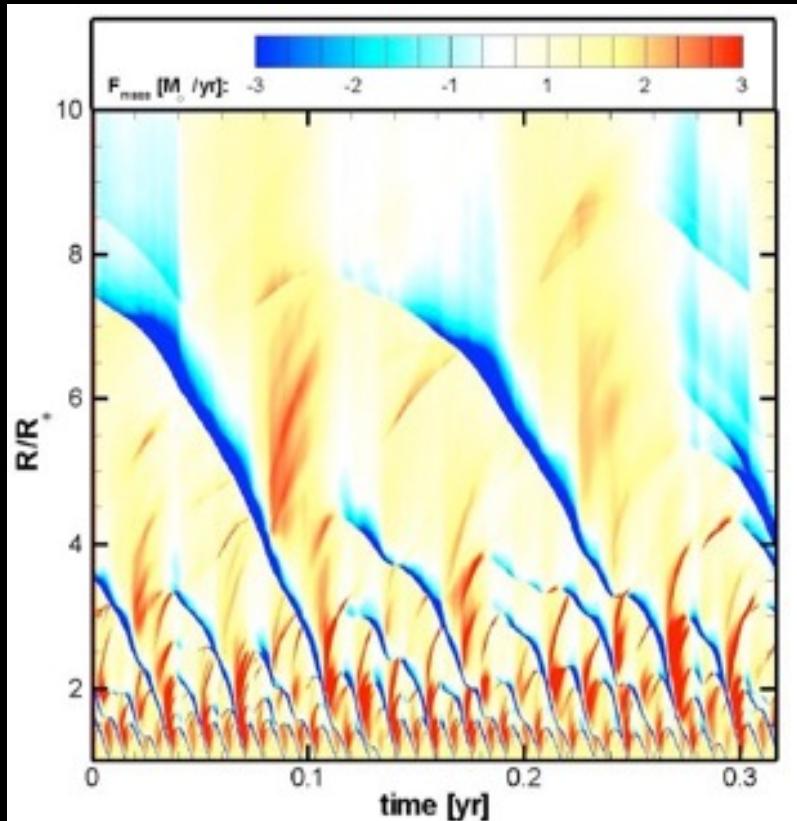


1D Sim of Photon Tiring & Flow Stagnation

van Marle, Owocki & Shaviv 2009

$$\dot{M}(r,t)$$

$$L(r,t) / L_*$$



$$\left\langle \dot{M}_\infty \right\rangle \approx \frac{L_*}{V_{esc}^2 / 2}$$

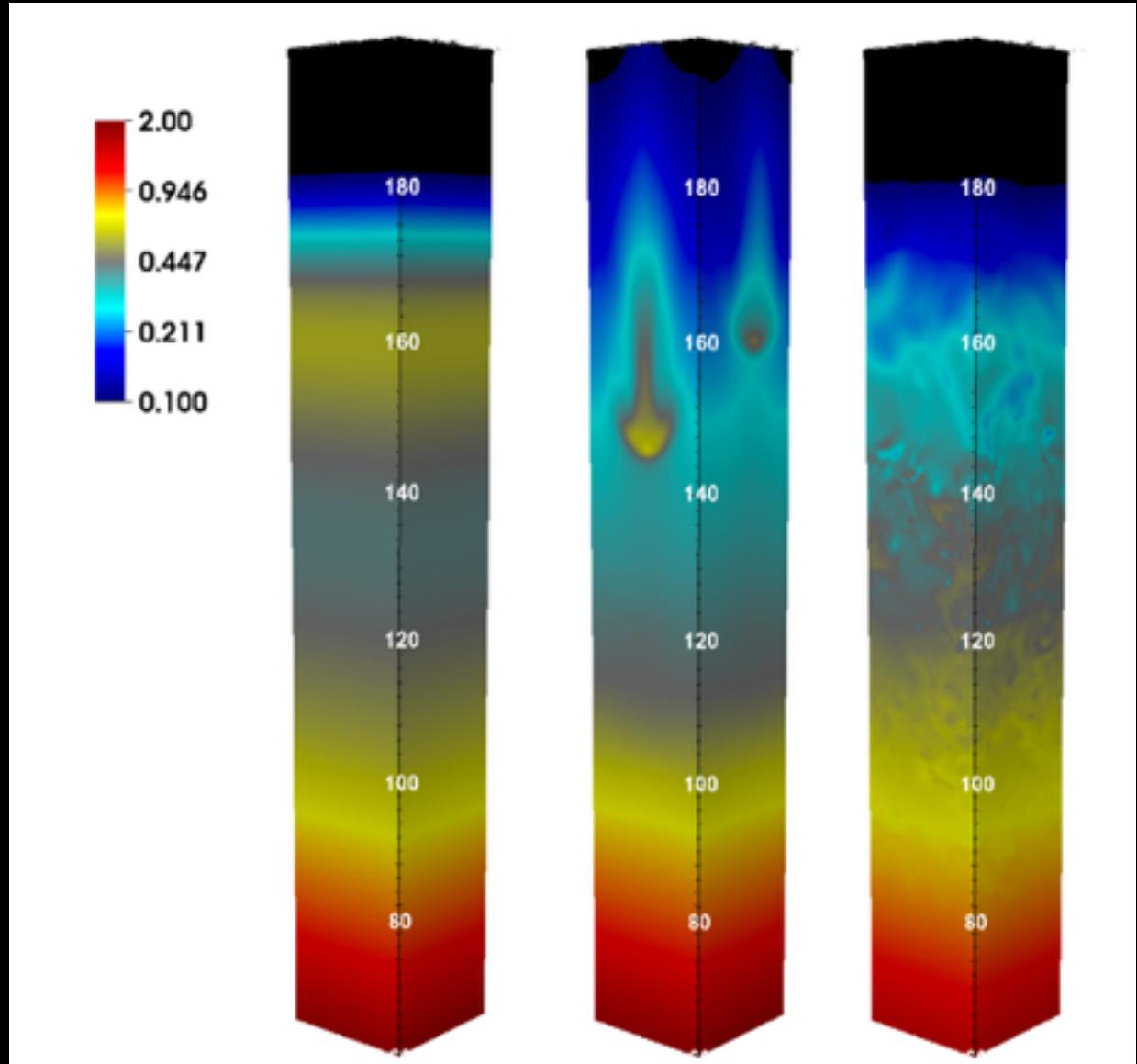
$$V_\infty \ll V_{esc}$$

$$L_{obs} = L_\infty \ll L_*$$

“Local Radiation Hydrodynamics Simulations of Massive-Star Envelopes
at the Iron Opacity Peak”

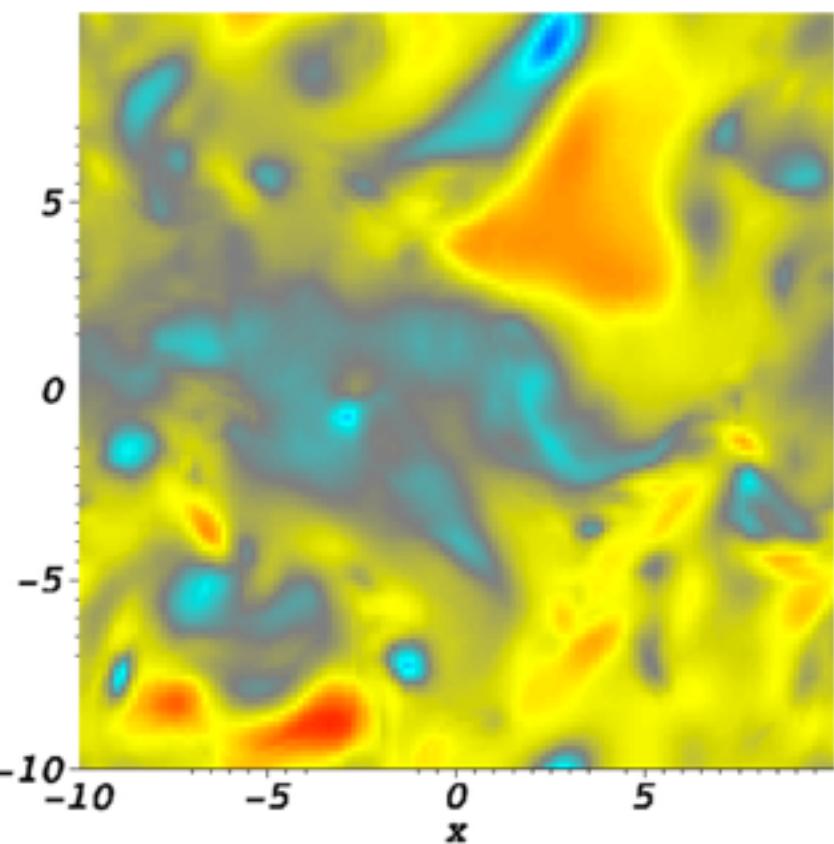
Clump
structure
from
instabilities
at Iron opacity
bump

<https://goo.gl/3kYbtg>



density

0.200 0.263 0.346 0.456 0.600



radiative flux

-0.000150 -7.50e-05 0.00 7.50e-05 0.000150

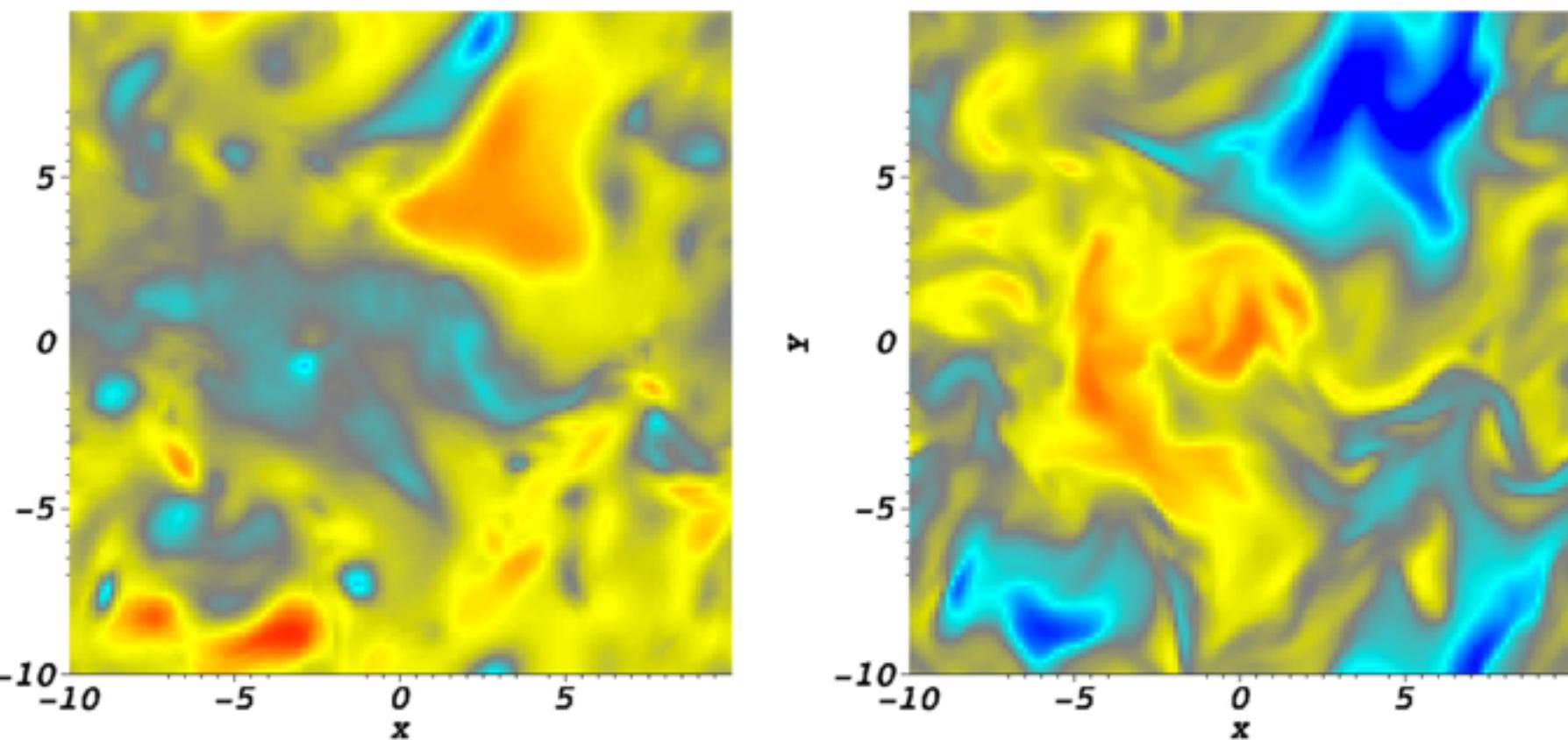
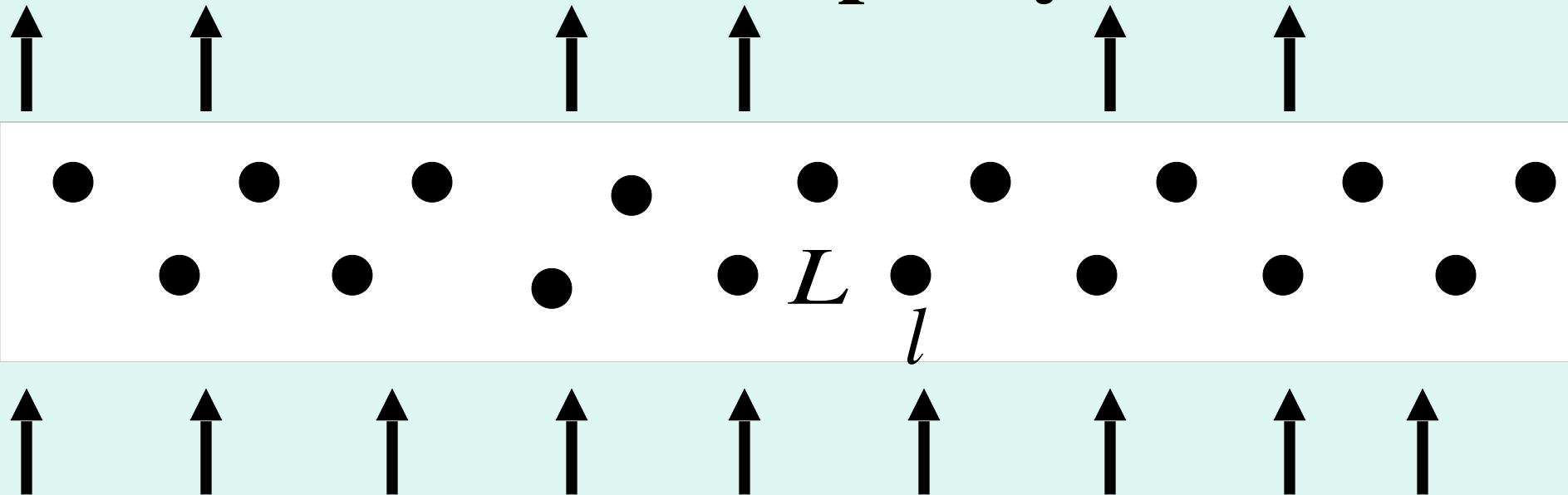


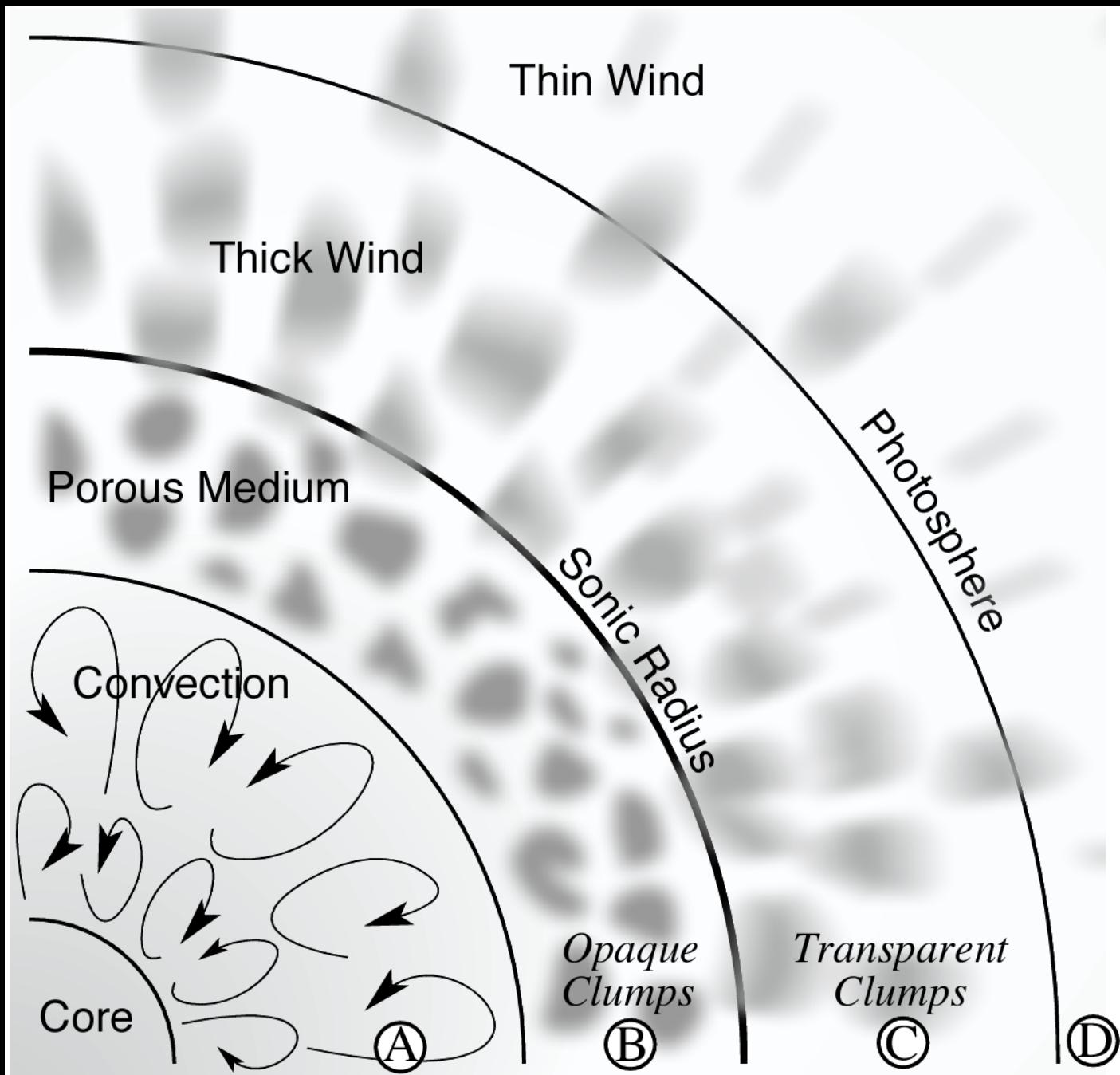
figure 8. Horizontal slices of density ρ (left) and vertical component of the radiation flux $F_{r,z}$ (right) at $z = 140R_{\odot}$ for the run

Porous opacity

Shaviv 98-03



$$K_{eff} \approx \frac{l^2}{m_b} = \frac{\kappa}{\tau_b} \quad \tau_b \equiv \kappa \rho_b l \gg 1$$
$$= K \frac{1 - e^{-\tau_b}}{\tau_b}$$



A POROSITY-LENGTH FORMALISM FOR PHOTON-TIRING-LIMITED MASS LOSS FROM STARS ABOVE THE EDDINGTON LIMIT

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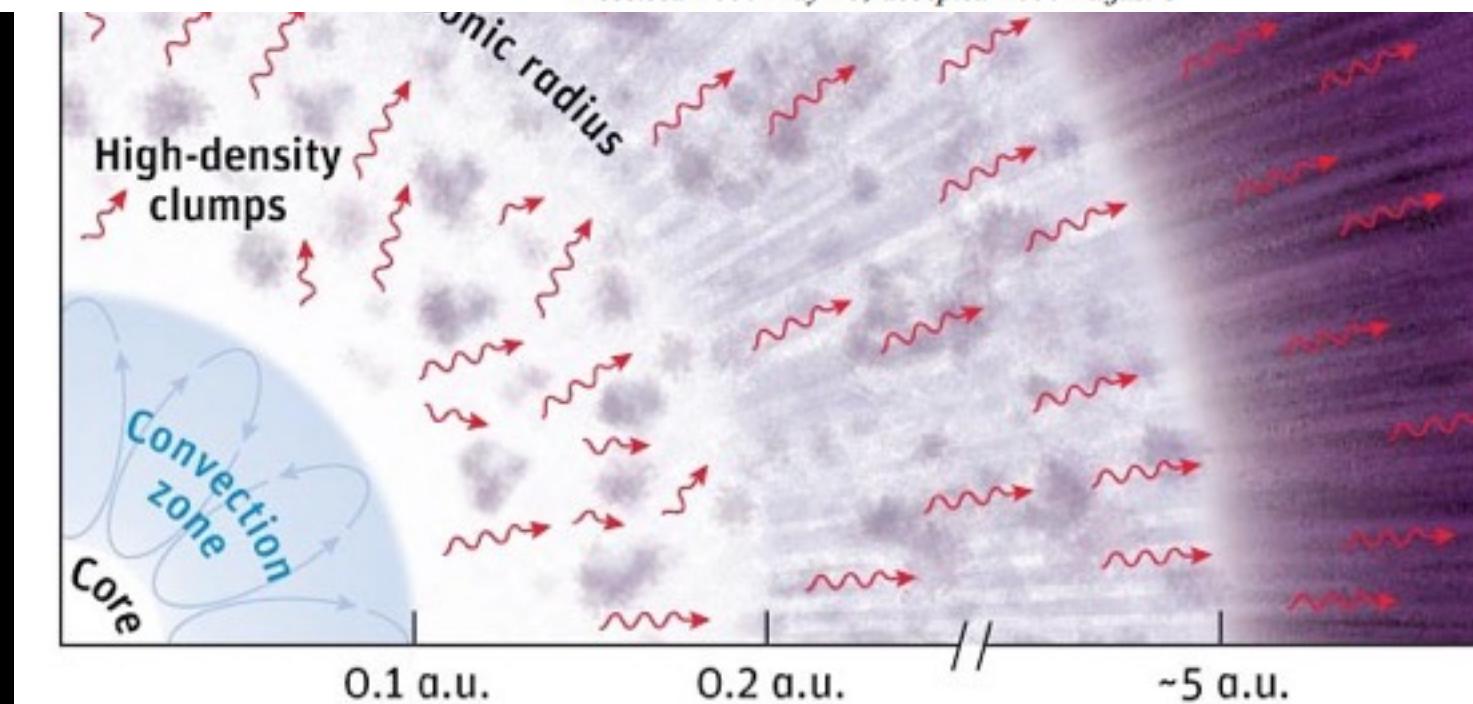
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Received 2004 May 10; accepted 2004 August 3



Turbulent Porosity

from LDI sims:

$$\frac{K_{eff}}{K} \approx \frac{1}{\sqrt{1 + \tau_h}} \quad \tau_h \equiv \kappa \rho h$$

$$h = (f_{cl} - 1)\ell$$

“porosity length”

$$f_{cl} \equiv \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2}$$

clumping factor

ℓ density auto-correlation length

Porosity regulated mass loss

Porosity reduced
Eddington factor

$$\Gamma_{eff} \equiv \frac{\Gamma}{\sqrt{1 + \tau_h}} = 1 \quad \Rightarrow \quad \dot{m}_{por} \equiv \frac{\dot{M}_{por}}{\dot{M}_{tir}} \simeq \frac{\Gamma^2 - 1}{\Gamma} \frac{R}{h} \frac{v_s}{c}$$

to keep below
tiring limit

requires

$$\dot{m}_{por} \leq 1$$

\rightarrow

$$\frac{h}{R} \geq \frac{\Gamma^2 - 1}{\Gamma} \frac{v_s}{c}$$

Some questions for workshop

- How to unify our understanding of
 - Explosive vs. Eruptive vs. Steady-wind mass loss
 - Failed explosions, failed winds
 - Dynamical vs. Diffusive time scales
 - Energy sources
 - Pre-SN LBVs: nuclear or waves
 - etaCar LBVs: binary merger &/or common env.
 - Momentum transfer
 - via $P_{\text{rad}} \gg P_{\text{gas}}$; optically thick to thin: $g_{\text{rad}} = \kappa F_{\text{rad}}/c$
 - What determines partition of escape energy?
 - Radiative vs. kinetic vs. potential
 - How different in 3D vs. 1D?
 - Rayleigh-Taylor, porosity

Summary

- Massive star winds driven by line-scattering
 - $\dot{M}_{\text{dot}} V_{\text{inf}} \sim \tau L/c$
 - OB winds $\tau \sim < 1$; WR winds $\tau \sim 1-10$
 - \dot{M}_{dot} very sensitive to CAK alpha (thin/thick lines)
 - $V_{\text{inf}} \sim \text{few } V_{\text{esc}}$
- Strong Line-Deshadowing Instability
 - small-scale clumping & embedded soft X-rays
- Eddington limit \Rightarrow LBV's & Eruptions?
 - energy limited, super-Edd, continuum-driven wind
 - failed wind \Rightarrow porosity \Rightarrow regulates \dot{M}_{dot}
- Explosion vs. wind