

# The Randall-Sundrum Model in string theory and throat field mediated SUSY breaking

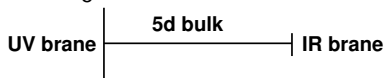
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# Motivation and overview

The **Randall-Sundrum 1 model**:  $ds^2 = e^{2k|y|} \eta_{\mu\nu} dx^\mu dx^\nu + dy^2$   
— a "slice of  $AdS_5$ " between two 4d branes: ( $\rightarrow$  Randall/Sundrum '99)



- Interesting for particle physics and cosmology model building: Hierarchy problem / Compositeness / Sequestering / ...
- **How can such models be realized in string compactifications?**
- Type IIB compactifications with branes and fluxes may develop a **"warped throat"** which looks like a RS background (plus 5 compact extra dimensions)  $\rightarrow$  Verlinde '99, Giddings/Kachru/Polchinski '01

In this context, we will investigate:

- 1 the 5d description of 10d **hierarchy stabilization** by fluxes
- 2 the role of the universal **unstabilized Kähler modulus** in 5d
- 3 how **SUSY breaking** can be mediated from the IR to the UV brane

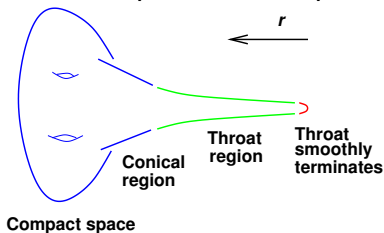
# Review: The warped deformed conifold

Example of a **warped compactification** of **10d IIB supergravity** with **fluxes** → Klebanov/Strassler '00, GKP:

- spacetime is **warped product** of 4d Minkowski space with 6d CY manifold (actually CY orientifold or  $F$  theory base)
- in some “warped throat” region geometry is approximately  **$\text{AdS}_5 \times T^{1,1}$**  (where  $T^{1,1} \simeq S^2 \times S^3$  is a 5d Einstein space)
- have  **$M$  units of RR 3-form flux** on the  $S^3$
- Radius  $R$  of  $T^{1,1}$  and AdS **varying slowly** along AdS radial direction  $r$ :
  - $R_{\text{eff}}(r)^4 \sim (\alpha')^2 g_s N_{\text{eff}}(r)$
  - $N_{\text{eff}}(r) \sim g_s M^2 \log \frac{r}{r_s}$
- have  $N_{\text{eff}}(r)$  units of  **$\tilde{F}_{(5)}$  flux through  $T^{1,1}$**  at  $r$ , where  $\tilde{F}_{(5)} = F_{(3)} \wedge B_{(2)} + \dots$  (compare this with D3 brane metric!)

# 10d vs. 5d geometry

This "warped throat" is part of some compact CY space:



UV brane



- throat terminates smoothly at small  $r$ : RS **IR brane**
- throat becomes conical for large  $r$ . Compact CY + conical region: RS **UV brane**
- throat itself: RS **bulk**, approximately  $\text{AdS}_5 (\times T^{1,1})$

# 1. 10d vs. 5d radius stabilization

Fluxes can **stabilize complex structure moduli**, governing the hierarchy between IR and UV end. **5d mechanism?**

Recall that interval length/hierarchy is modulus in pure RS 1!

Deviation from AdS geometry in throat: parametrized by **one scalar degree of freedom**,  $N_{\text{eff}}(r) \sim \int_{T^{1,1}} \text{at } r \tilde{F}_{(5)}$ , **with fixed boundary values**  $N_{\text{UV}}, N_{\text{IR}}$ :

- $N_{\text{UV}}$  fixed by branes and fluxes on UV manifold (tadpole condition)
- $N_{\text{IR}} = g_s M^2$

Compare this with **Goldberger-Wise mechanism** for radius stabilization in RS I:

- field content = gravity + **1 scalar  $H$**  with **boundary values fixed** by steep potentials on boundaries  $\rightarrow$  Goldberger/Wise '99
- **Bulk profile + boundary values determine interval length.**
- Here: Can determine bulk potential from requiring that **backreaction gives rise to correct deformation of AdS background.**
- Result:  $V_{\text{bulk}}(H) \sim M_5^7 R_{\text{eff}}(r_s)^{-2} H^{-8/3}$

## 2. The universal Kähler modulus

- Complex structure moduli can be stabilized by fluxes
- but Kähler moduli remain massless (at this stage...)
- $\exists$  always at least a "universal" Kähler modulus which in unwarped compactifications governs the size of the internal manifold.

Geometrical significance of the UKM? (see also  $\rightarrow$  S. Giddings' talk)

Throat metric:

$$ds^2 = h(r)^{-1/2} \eta_{\mu\nu} dx^\mu dx^\nu + h(r)^{1/2} (dr^2 + r^2 ds_{T^{1,1}}^2), \quad h(r) = 1 + \frac{R_{\text{eff}}(r)^4}{r^4}$$

UKM : can change  $h(r) \rightarrow T + R_{\text{eff}}(r)^4/r^4$  ( $\rightarrow$  Giddings/Maharana '05)

- For large  $T$  ( $T$  dominant in  $h$ ):
  - $T \leftrightarrow$  overall rescaling of internal manifold as in unwarped case
  - 5d picture not valid (no throat)
- For small  $T$ :
  - $T$  rescales only UV manifold + conical region
  - throat length and shape unaffected
  - $T$  is a UV brane field in the 5d picture

### 3. SUSY breaking mediation by throat fields

Assume now ( $\rightarrow$  KKLT '04):

- $T$  is stabilized nonperturbatively
- SUSY is broken in the IR (e.g. by  $\overline{D3}$ s), vacuum dS or Minkowski and
- Standard Model fields  $Q$  live somewhere on the UV manifold

No direct coupling between ~~SUSY~~ sector and SM sector: **sequestering**  
( $\rightarrow$  Randall/Sundrum '98)

How can ~~SUSY~~ be mediated from the IR to the UV?

- Dominant in this framework: mixed modulus-anomaly mediation  
( $\rightarrow$  Choi/Falkowski/Nilles/Olechowski '05, H.-P. Nilles' talk)
- **Other equally important contributions?** (see also  $\rightarrow$  Choi/Jeong '06)

### 3. SUSY breaking mediation by throat fields

Effective 4d theory: Model ~~SUSY~~ sector as **F term breaking** by chiral superfield  $X$ . All heavy (flux-stabilized) moduli integrated out.

Minimal scenario (modulus-anomaly mediation):

$$\mathcal{L} \supset \int d^4\theta \bar{\varphi} \varphi \Omega + \int d^2\theta \varphi^3 W + \text{h.c.}$$

$$\Omega = -(T + \bar{T}) + \omega^2 \tilde{\Omega}(X, \bar{X}), \quad W = W_0 + e^{-T} + \omega^3 \tilde{W}(X)$$

- $\omega \ll 1$  is the warp factor in the IR
- $T$  is UV brane field  $\Rightarrow$  sequestering in  $\Omega$
- $e^{-T}$  term from nonperturbative stabilization,  $W_0$  from heavy fields

For Minkowski (or dS with small  $\Lambda$ ) uplift: need  $W_0 \sim \omega^2$ ,  $F_X \sim \omega$   
 $\Rightarrow F_\varphi \sim \omega^2$

- Add visible sector in the UV:
- $\Rightarrow$  soft scalar masses  $m^2 \sim \omega^4$  for visible sector fields.



### 3. SUSY breaking mediation by throat fields

Warped deformed conifold scenario:

More fields!

In particular have **vector superfields**  $V$  from  $SO(4)$  symmetry of Klebanov-Strassler throat.

- $SO(4)$  broken by UV manifold  $\Rightarrow V$  gets UV-scale mass.
- expect  $X$  to be charged under  $V$  (e.g.  $\overline{D3}$ s at tip of throat break  $SO(4)$ , hence they must couple to  $V$ )

$$\Omega = -(T + \overline{T}) + \omega^2 \tilde{\Omega}(X, e^V \overline{X}) \quad W = W_0 + e^{-T} + \omega^3 \tilde{W}(X) + V^2$$

This gives a  $D$  term for  $V$ ,  $D \sim \omega^4$ .

- Add visible sector fields  $Q$  with coupling  $Qe^V \overline{Q}$
- $\Rightarrow$  scalar soft mass  $m^2 \sim \omega^4$  induced.
- **Comparable with modulus-anomaly mediation.**

# Summary and outlook

- The throat looks like a **RS 1 model** with extra fields from the 5d perspective.
- **Radius stabilization by fluxes** in 10d becomes **Goldberger-Wise stabilization** in 5d. The potential of the Goldberger-Wise scalar can be inferred from its backreaction on the geometry.
- The **universal Kähler modulus** is a **brane field** in the 5d picture.
- Sequestering between the IR and UV ends may be violated by **massive vector fields** coming from broken isometries of the throat.

- Next steps:

## Apply:

- Build a model in which throat field mediation is realized.

## Understand:

- Find the 5d SUGRA theory that describes the Klebanov-Strasser throat.
- Find its coupling to the  $X$  sector and to fields on the UV manifold.