

# DYNAMICS OF MASSIVE BLACK HOLE BINARIES IN GALACTIC MERGERS

MONICA COLPI

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**MASSIVE BLACK HOLES: BIRTH, GROWTH AND IMPACT**

KAVLI INSTITUTE, SANTA BARBARA, 6 August 2013

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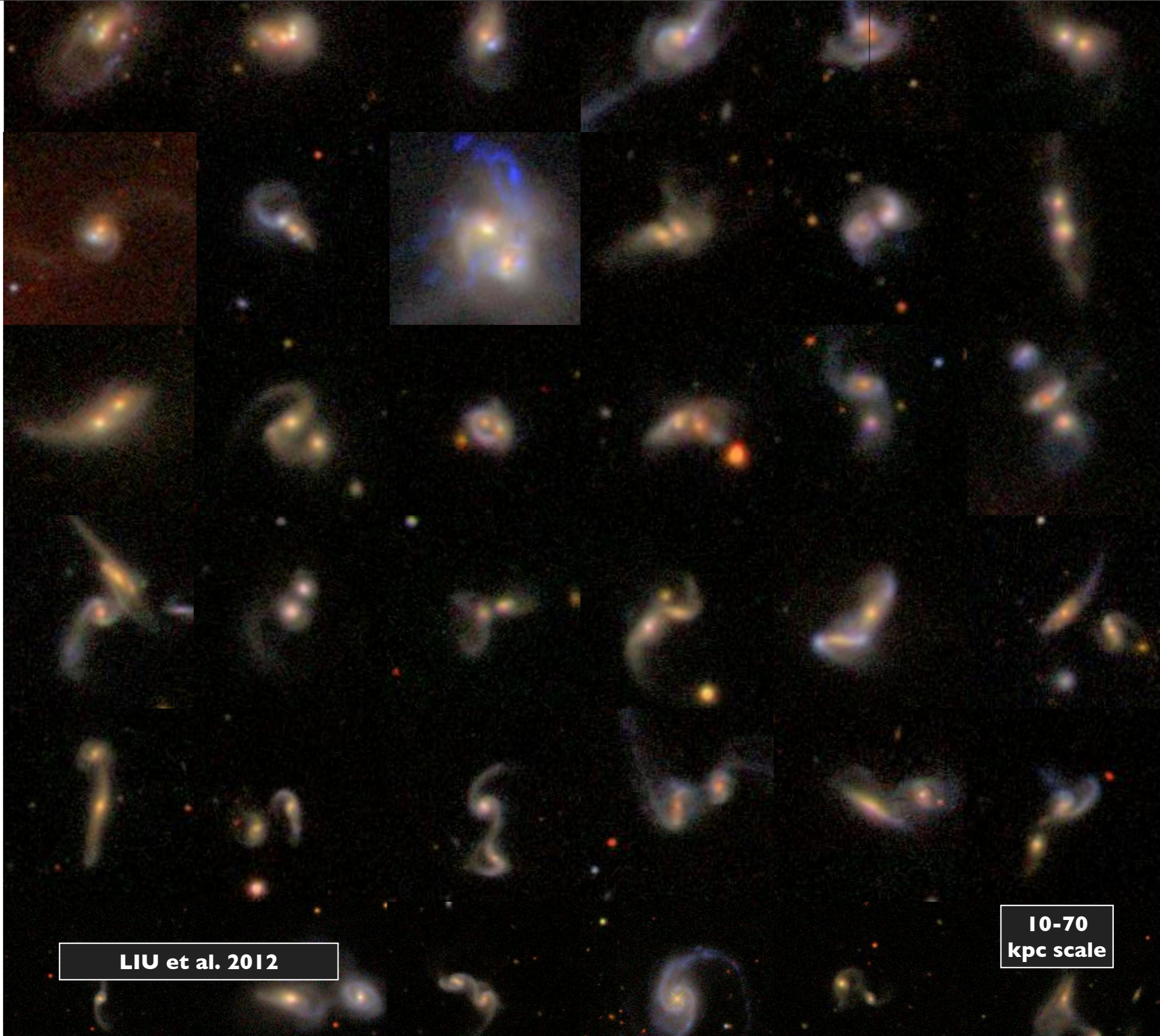
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acknowledge the collaboration

Simone Callegari (Zurich) Massimo Dotti (Milano Bicocca)  
Davide Fiacconi (Zurich) Francesco Haardt (Insubria)  
Lucio Majer (Zurich) Carmen Montuori (Haifa)  
Marta Volonteri (Paris)

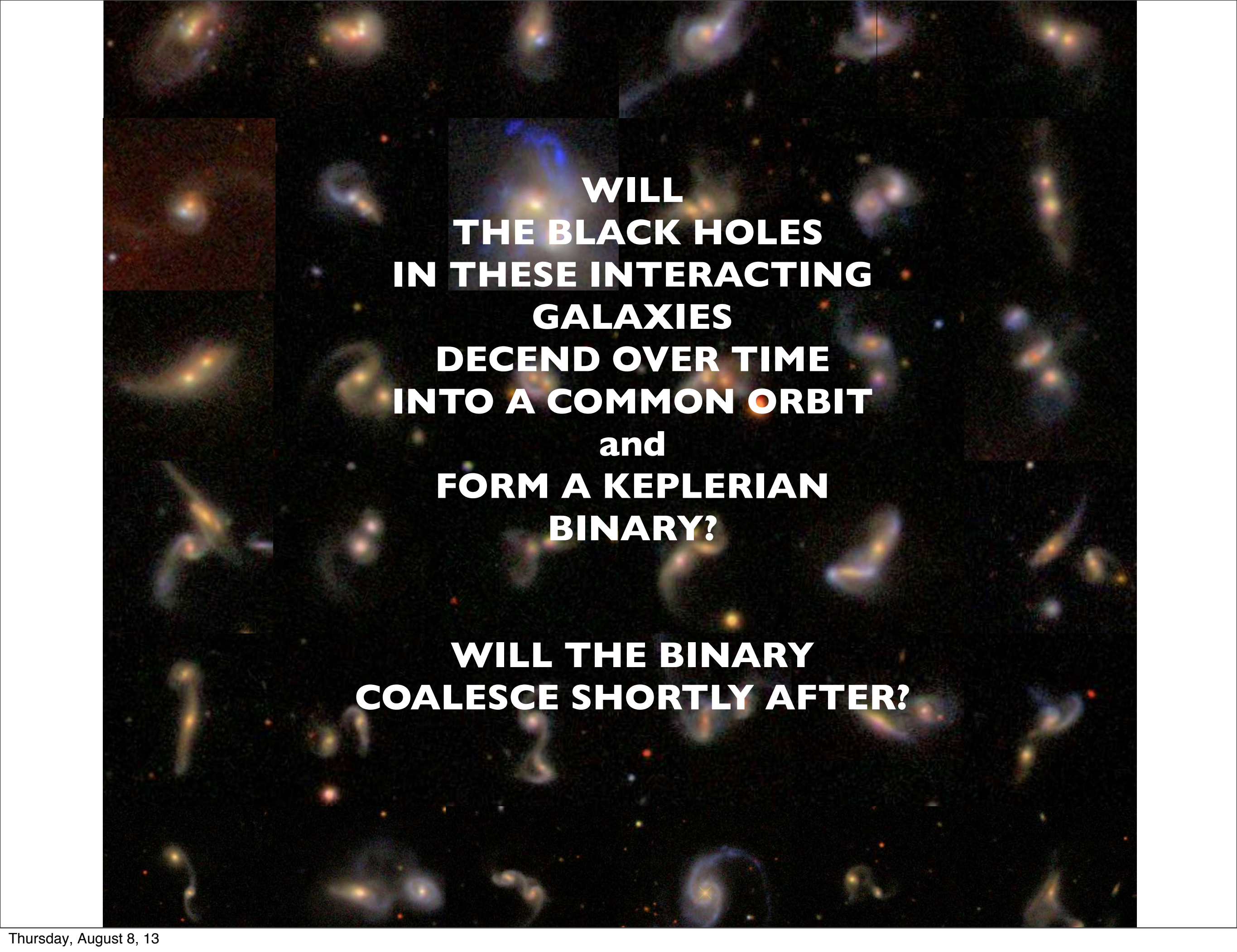




**LIU et al. 2012**

**10-70  
kpc scale**





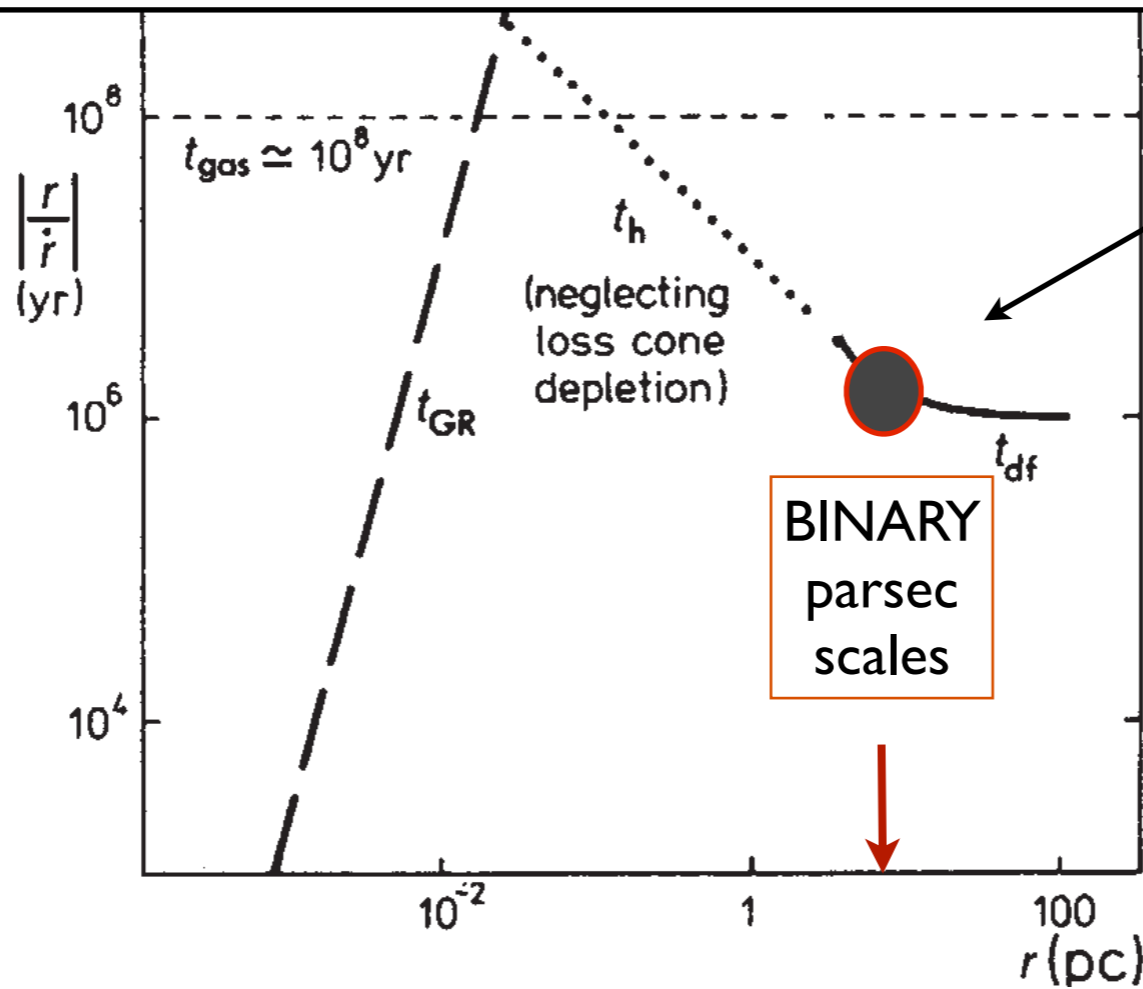
**WILL  
THE BLACK HOLES  
IN THESE INTERACTING  
GALAXIES  
DECEND OVER TIME  
INTO A COMMON ORBIT  
and  
FORM A KEPLERIAN  
BINARY?**

**WILL THE BINARY  
COALESCE SHORTLY AFTER?**



**PHASE I  
PAIRING**

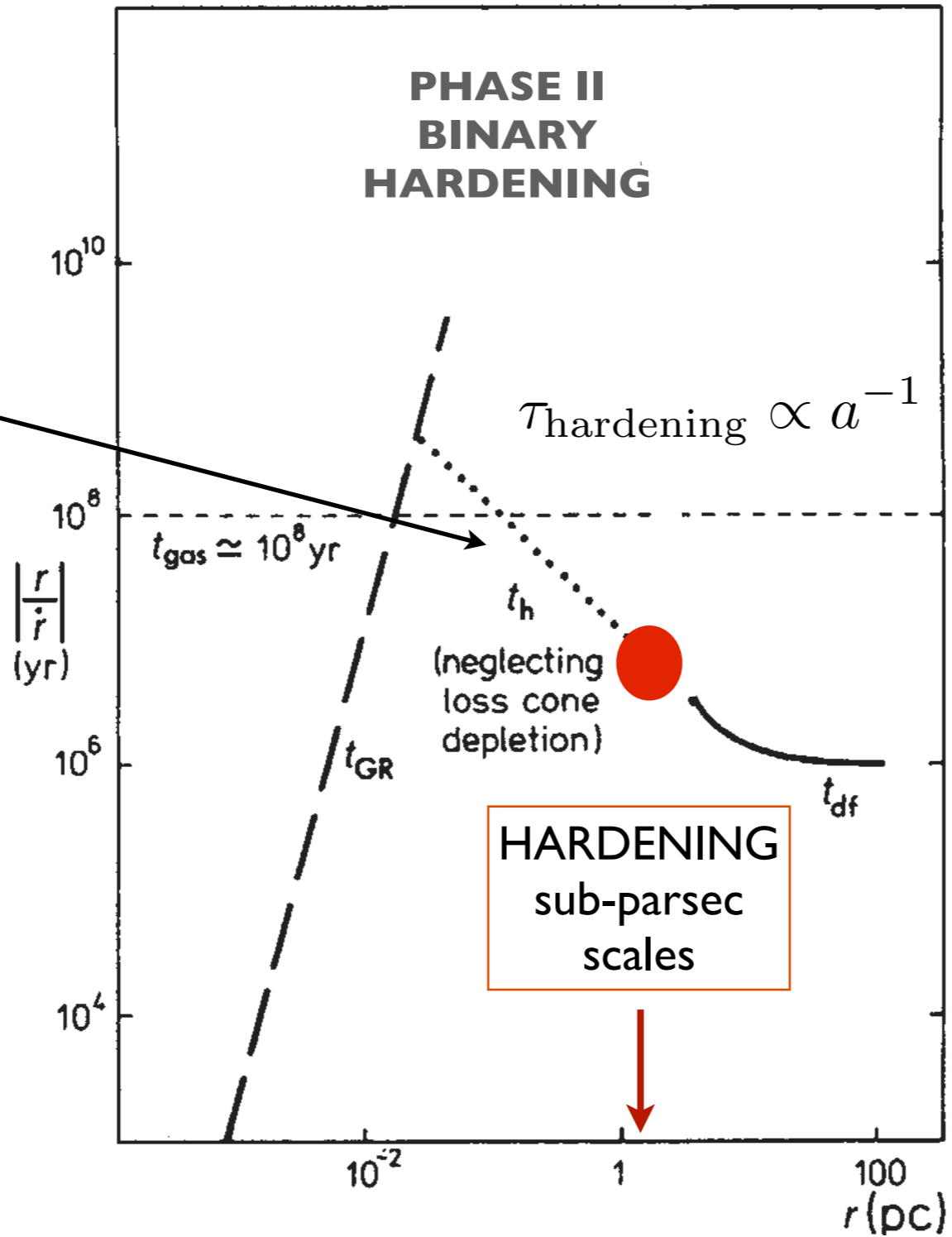
$$a_{\text{Binary}} \sim \frac{GM_{\text{BH,T}}}{\sigma^2} \sim 10 \left( \frac{M_{\text{BH,T}}}{10^8 M_{\odot}} \right) \left( \frac{200 \text{ km s}^{-1}}{\sigma} \right)^2 \text{ pc}$$



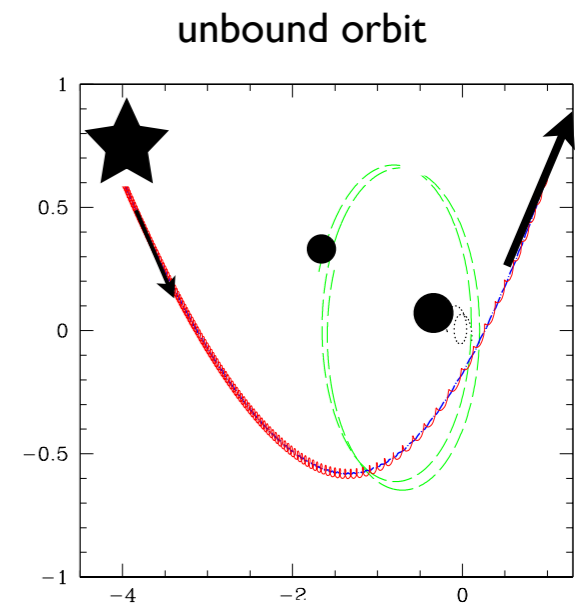
**DYNAMICAL  
FRICTION  
AGAINST  
THE  
STARS  
CONTROLS  
THE  
PAIRING  
in the  
“spherical”  
galaxy**

Diagram of the timescales in the approach and eventual coalescence of a supermassive binary

HARDENING THROUGH  
**SCATTERING OFF SINGLE STARS**  
 PLUNGING FROM NEARLY RADIAL ORBITS



$$\frac{G\mu_{\text{BH}}}{2a_{\text{Hard}}} > \frac{3}{2}\sigma^2$$



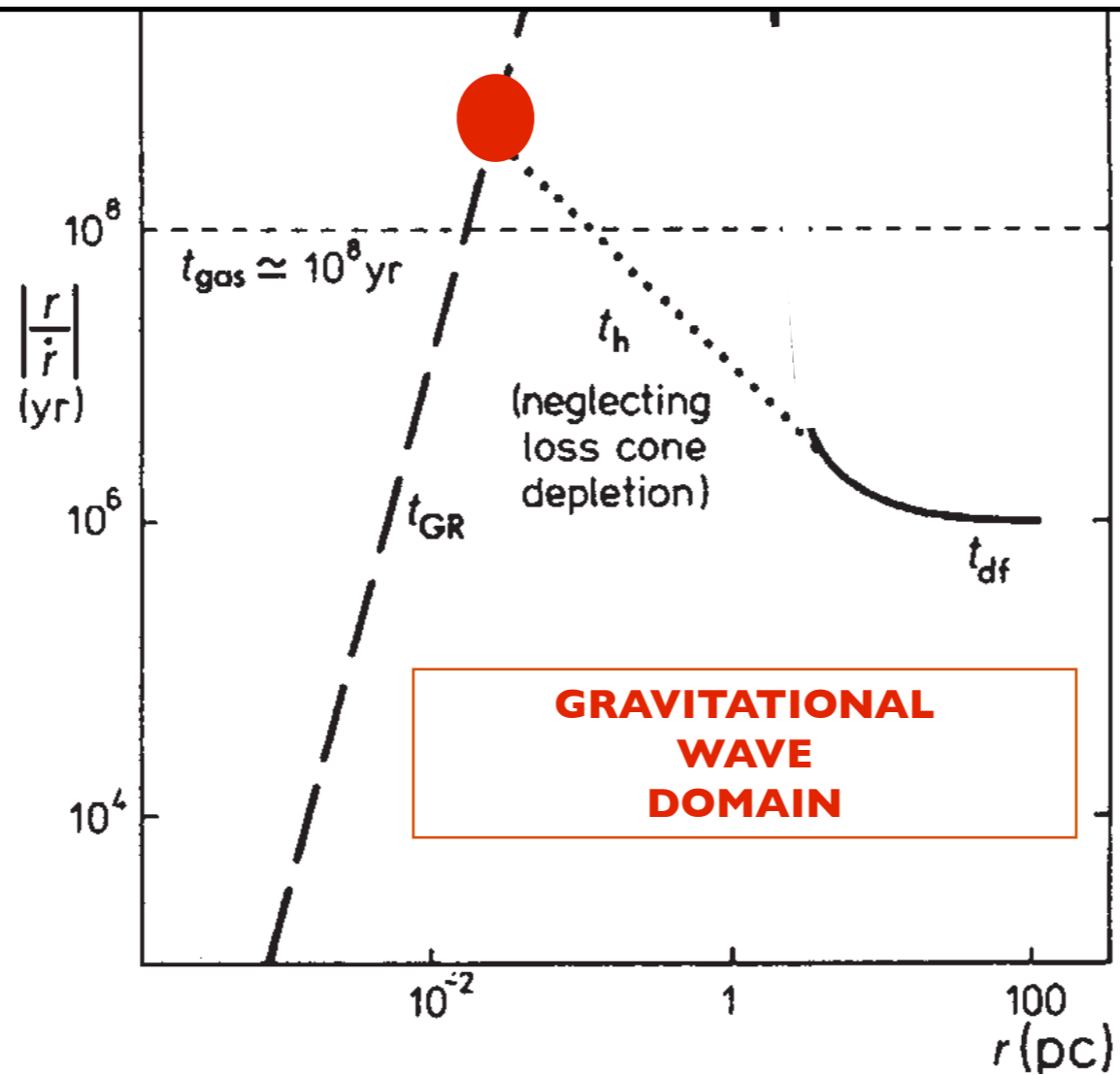
QUINLAN 1996, YU 2002

$$a_{\text{Hard}} \sim \frac{G\mu_{\text{BH}}}{3\sigma^2} \sim 3 \frac{q_{\text{BH}}}{(1+q_{\text{BH}})^2} \frac{M_{\text{BH,T}}}{10^8 M_{\odot}} \left( \frac{200 \text{ km s}^{-1}}{\sigma} \right)^2 \text{ pc}$$

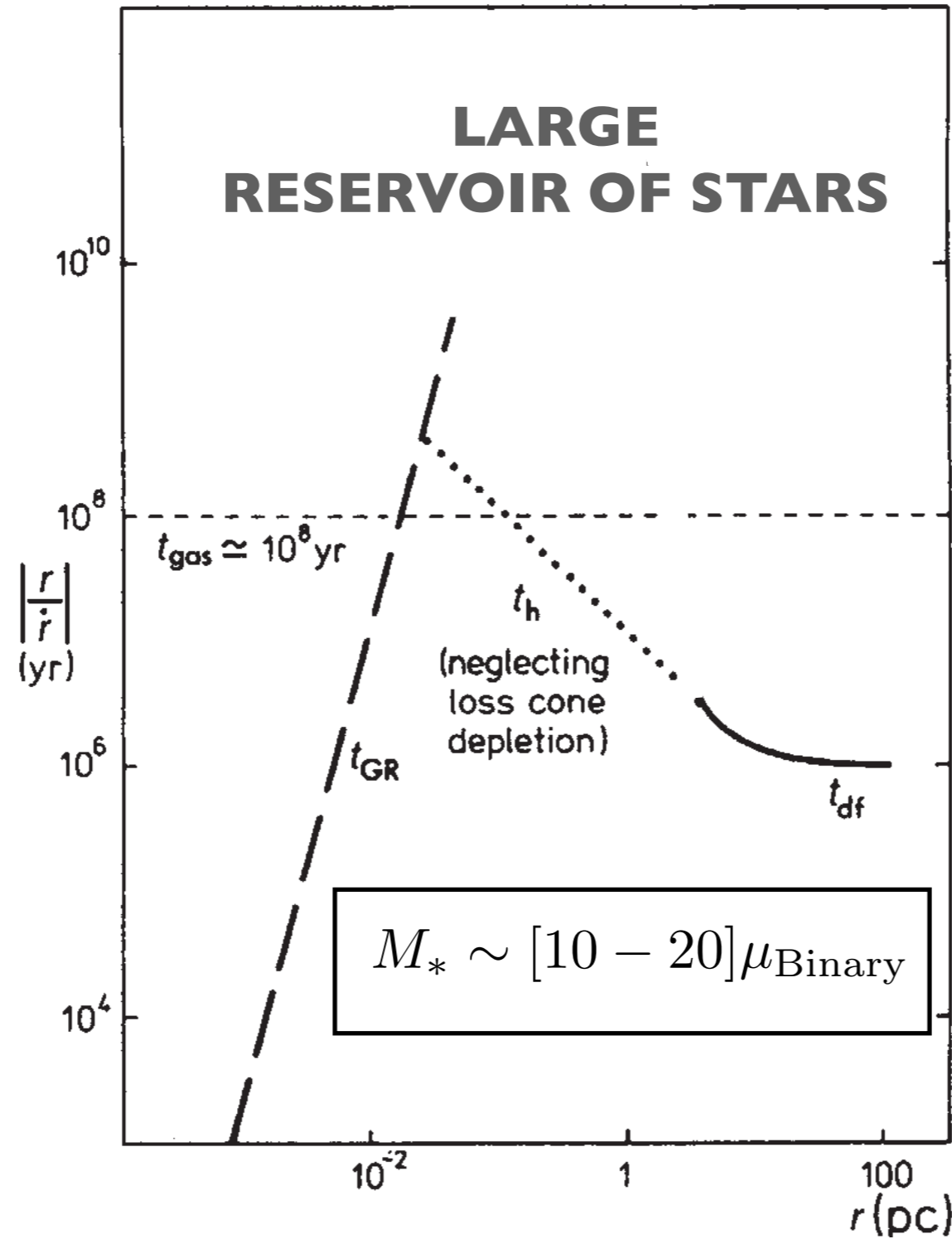


$$P(a_{\text{GW}}) \sim 16 \left( \frac{M_{\text{BH,T}}}{10^8 M_{\odot}} \right)^{5/8} \left( \frac{t_{\text{GW}}}{10^9 \text{yr}} \right)^{3/4} \text{yr}$$

$$V_{\text{cir}}(a_{\text{GW}}) \sim 4130 \left( \frac{M_{\text{BH,T}}}{10^8 M_{\odot}} \right)^{1/8} \left( \frac{t_{\text{GW}}}{10^9 \text{yr}} \right)^{-1/8} \text{km sec}^{-1}$$



$$a_{\text{GW}} \sim 25 \cdot 10^{-3} \left( \frac{M_{\text{BH,T}}}{10^8 M_{\odot}} \right)^{3/4} \left( \frac{t_{\text{GW}}}{10^9 \text{yr}} \right)^{1/4} \text{pc}$$



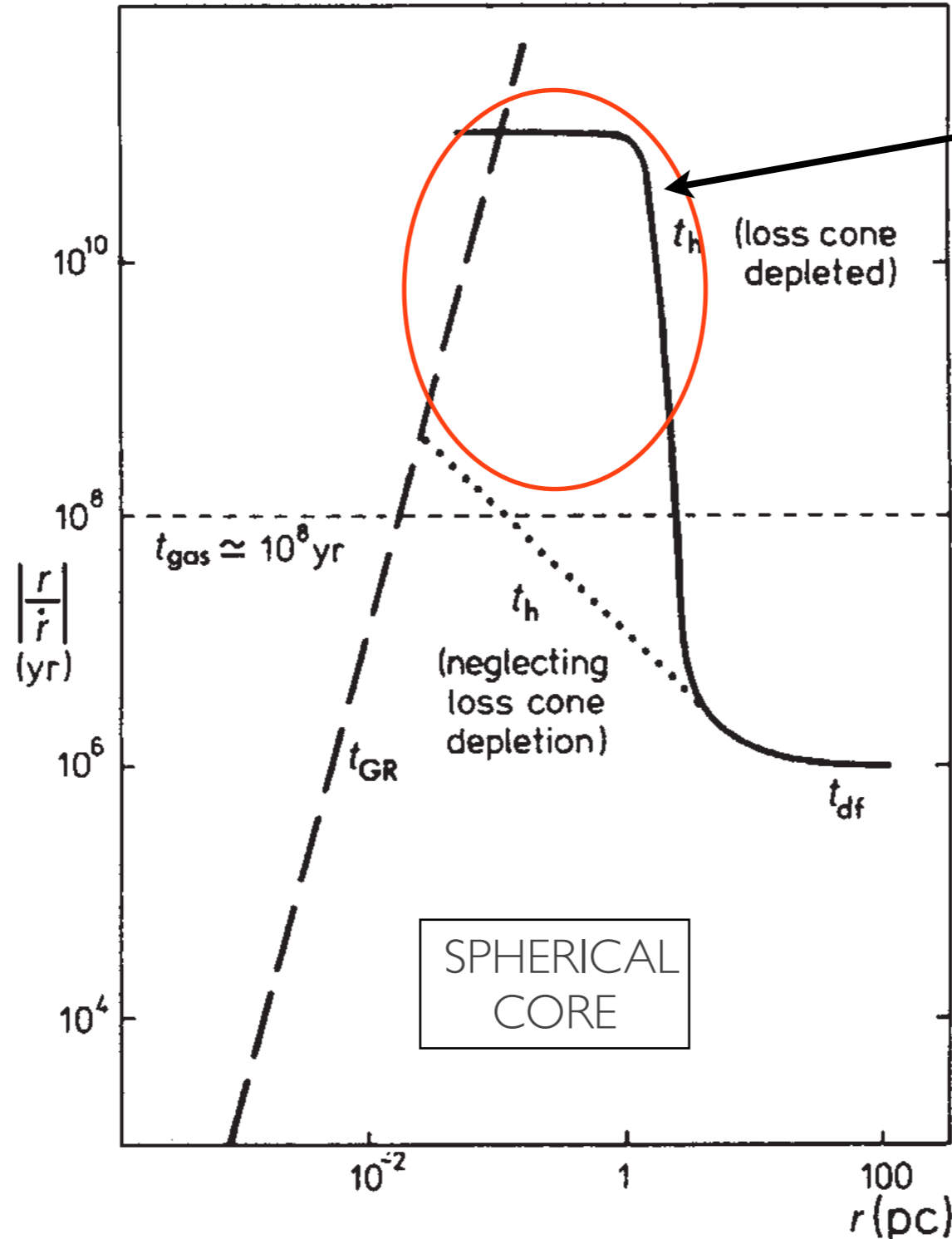
to transit  
from hardening  
to  
GW phase

massive  
ejection of stars

Diagram of the timescales in the approach and eventual  
coalescence of a supermassive binary  
from Begelman, Blandford & Rees

# THE LAST PARSEC PROBLEM

**star's ejection implies DEPLETION OF THE LOSS CONE the region in the phase space of low-J orbits**



**REFILLING OF THE LOSS-  
CONE  
ON THE RELAXATION  
TIMESCALE**

$$\tau_{\text{relaxation}} \propto N$$

**IN GALAXIES  
RELAXATION  
TIMESCALE  
LONGER  
HUBBLE TIMES**

## STALLING OF THE BINARY - NO FURTHER DYNAMICAL EVOLUTION

SLOW DIFFUSIVE REFILLING OF THE BINARY LOSS CONE WAS OBSERVED IN N-BODY STUDIES IMPLYING LOW HARDENING RATES

Milosavljevic & Merritt 2005

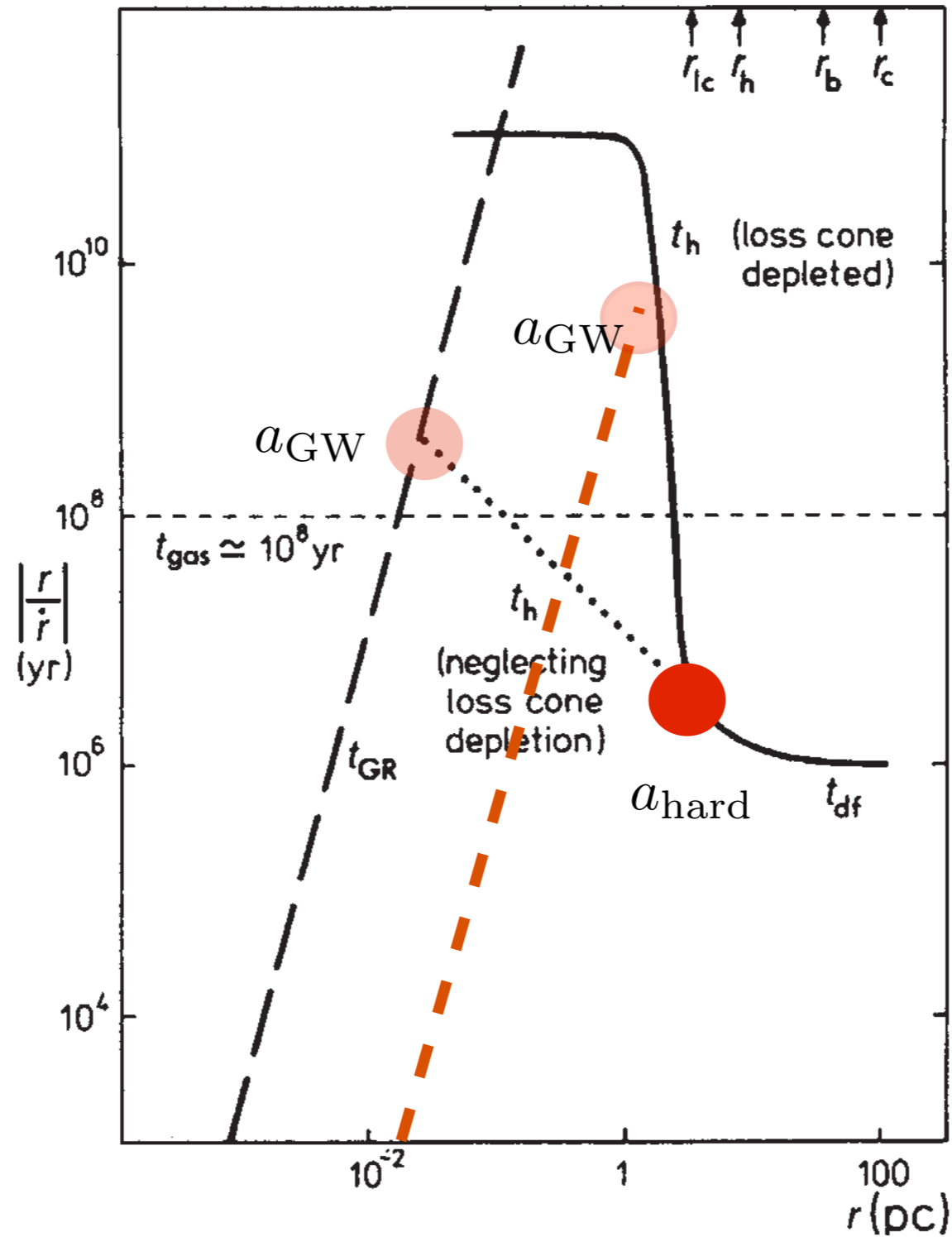


**HOW CAN WE SOLVE THE LAST-PARSEC PROBLEM ?**

**minimal hypothesis**

**RUNAWAY INCREASE OF THE ECCENTRICITY with minor loss of binding energy ?**

**this reduces the mismatch between  $a_{hard}$   $a_{GW}$**

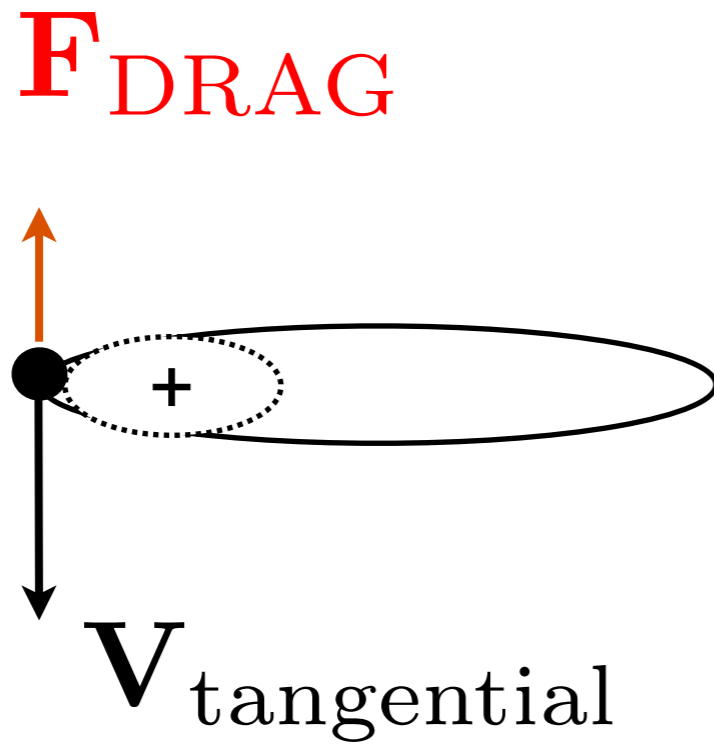


$$t_{GW} \propto (1 - e^2)^{7/2} \frac{a^4}{M_{BH,T}^3}$$

$$a_{GW}(e = 0.9999) \sim 2500 a_{GW}(e = 0)$$

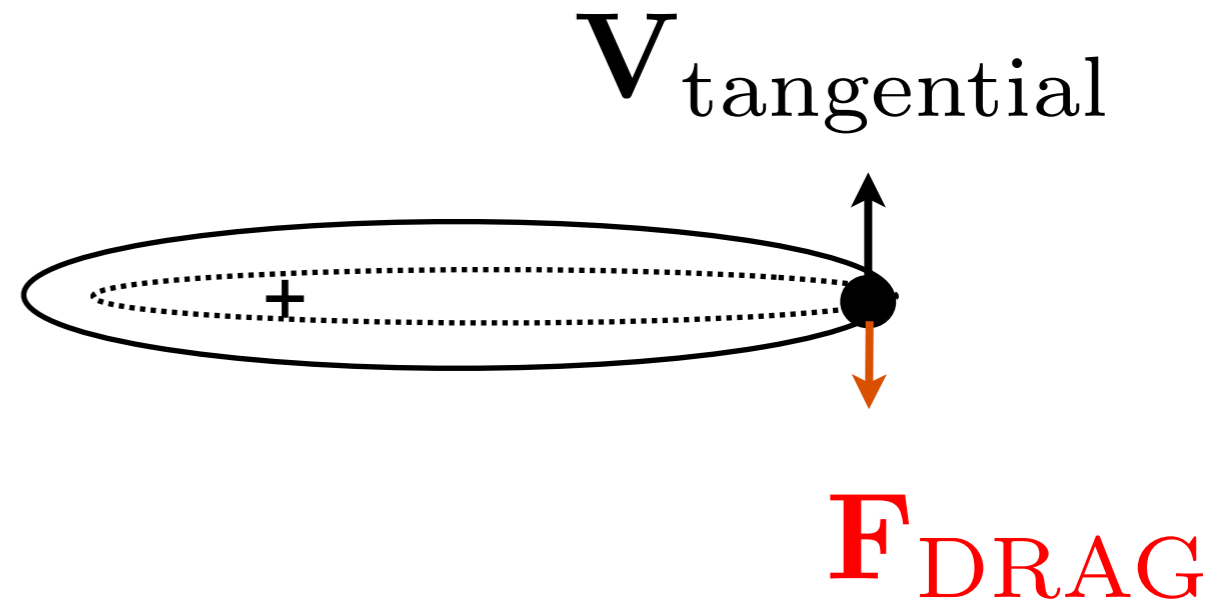
..focus on the orbit of one black hole

**ECCENTRICITY DECREMENT**



drag force  
@  
pericenter

**ECCENTRICITY INCREASE**



the action of the drag force  
mostly confined  
@  
apocenter

## **HARDENING PHASE: SLING-SHOT MECHANISM**

the binary is a “source”  
of angular momentum

the tendency is to “deposit”  
angular momentum  
into the stellar “bath”  
... high eccentricity

QUINLAN 1996, MILOSAVLJEVIC & MERRITT 2001, HEMSENDORF ET AL. 2002, BAUMGARDT et al. 2006, AMARO SEOANE et al. 2009,  
MERRITT et al. 2007, SESANA et al. 2010, SESANA 2010



NEED OF A RAPID REFILLING OF THE LOSS CONE

... in reality ....

GALAXIES ARE NOT “SPHERICAL” BEING RELIC OF A  
MERGER

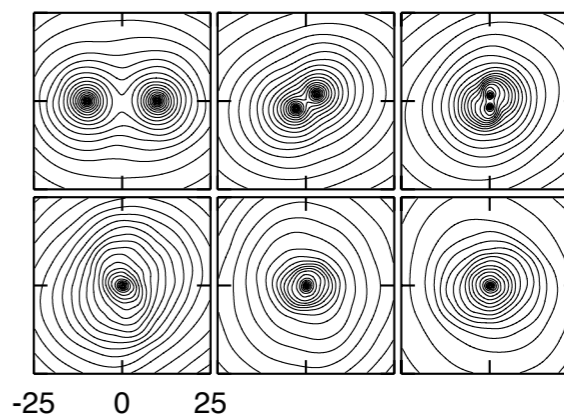
... a degree of triaxiality/axisymmetry

Khan, Just & Merritt 2011; Khan et al. 2012  
Khan & Holley Bockelmann 2013  
Preto et al. 2011  
Berentzen et al. 2009  
Preto et al. 2011,  
Berczik, Merritt, Spurzem, Bischof, 2006

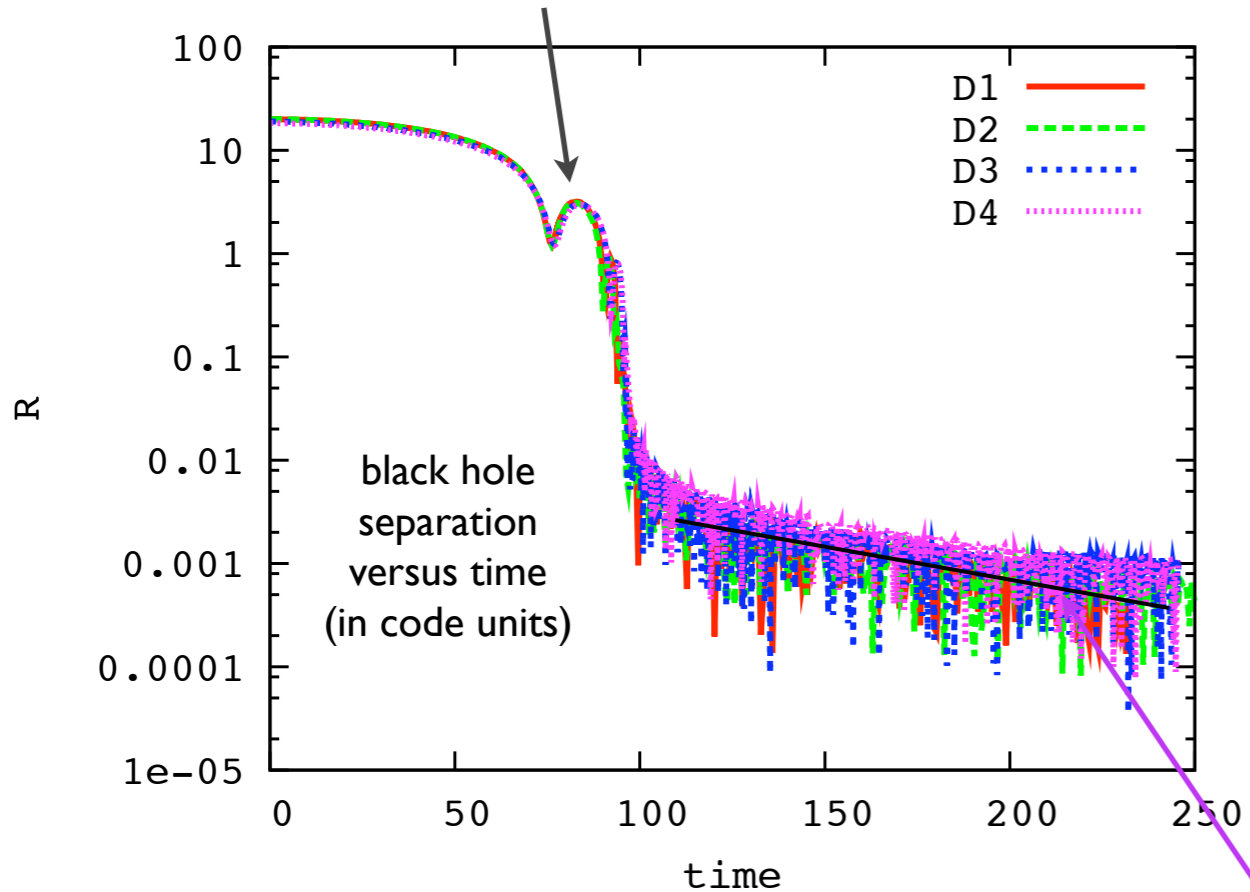
..... KHAN' S TALK

collisionless merger  
between two Hernquist's spheres  
on an initially bound eccentric orbit

**TRIAXIAL GALAXY REMNANT**

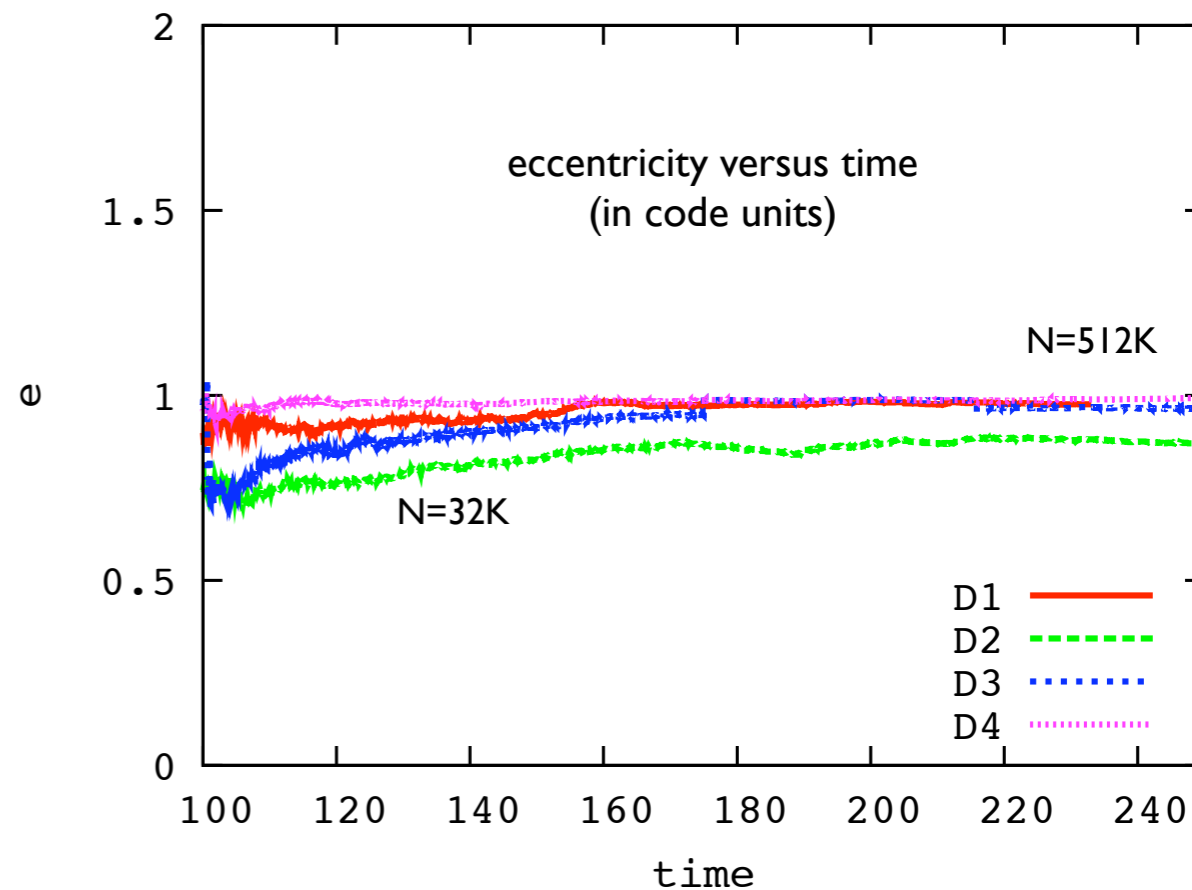


HARDENING BY  
DYNAMICAL FRICTION



HARDENING BY  
3-BODY INTERACTIONS

$$\frac{M_{\text{BH}}}{M_{\text{galaxy}}} = 0.01$$

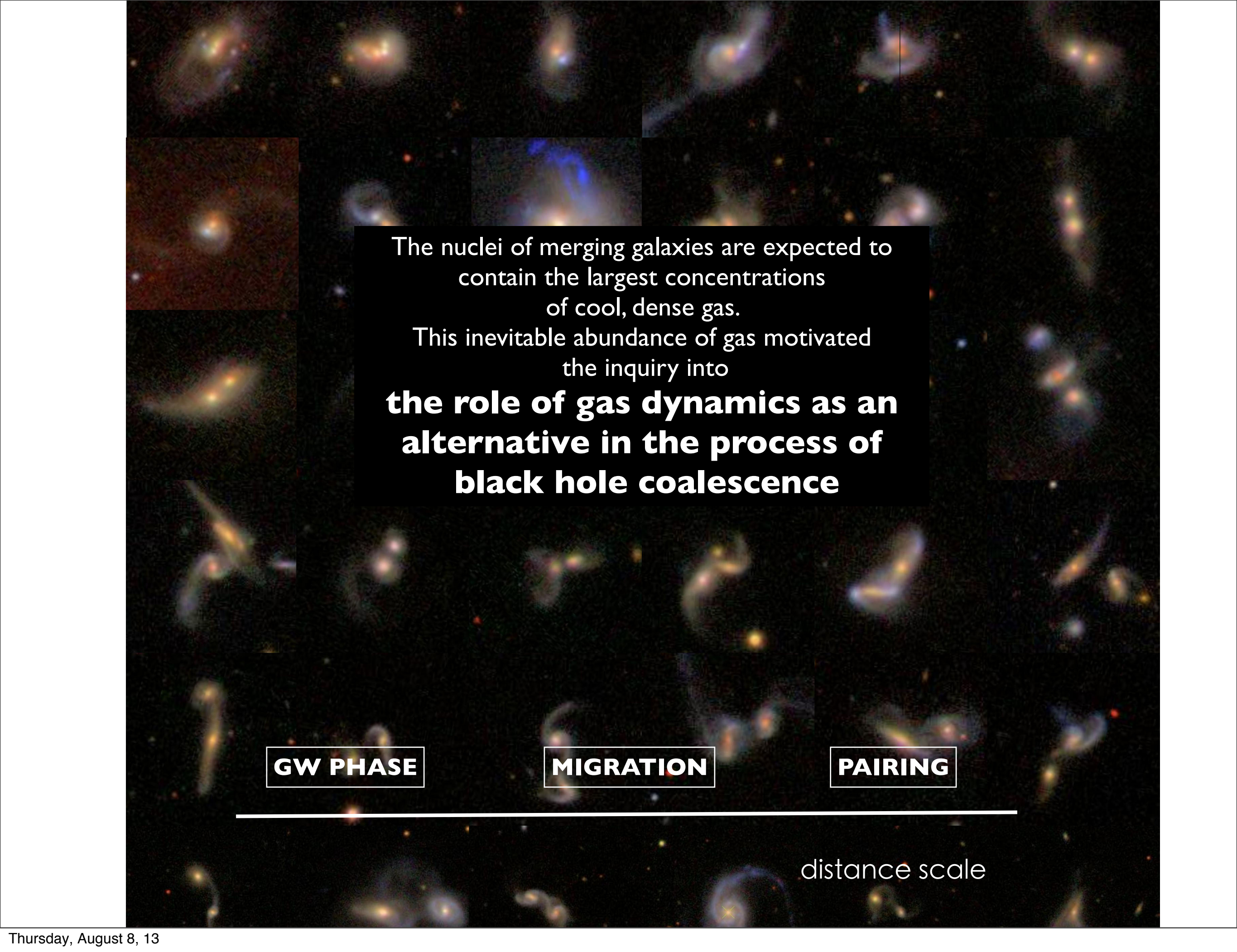


KHAN, JUST & MERRITT 2011

## IN COLLISIONLESS MERGERS

- the “**LAST PARSEC PROBLEM**” as artificial product of the spherical approximation
- hardening rates in SPHERICAL MERGERS are much higher than in spherical isolated models
- coalescence times around 1 Gyr from the time of formation of the binary
- LESSON TO LEARN: **attack the problem “ab initio”**





The nuclei of merging galaxies are expected to contain the largest concentrations of cool, dense gas.

This inevitable abundance of gas motivated the inquiry into

**the role of gas dynamics as an alternative in the process of black hole coalescence**

**GW PHASE**

**MIGRATION**

**PAIRING**

---

distance scale

- major merger of gas-rich Milky Way like galaxies

COPLANAR  
PROGRADE  
PARABOLIC  
ENCOUNTER  
OF TWO  
MILKY WAY  
LIKE GALAXIES



SPH SIMULATION  
COURTESY:  
SANDOR VAN  
WASSENHOVE

ENCOUNTER STARTS  
several Gyears  
BEFORE CONTACT

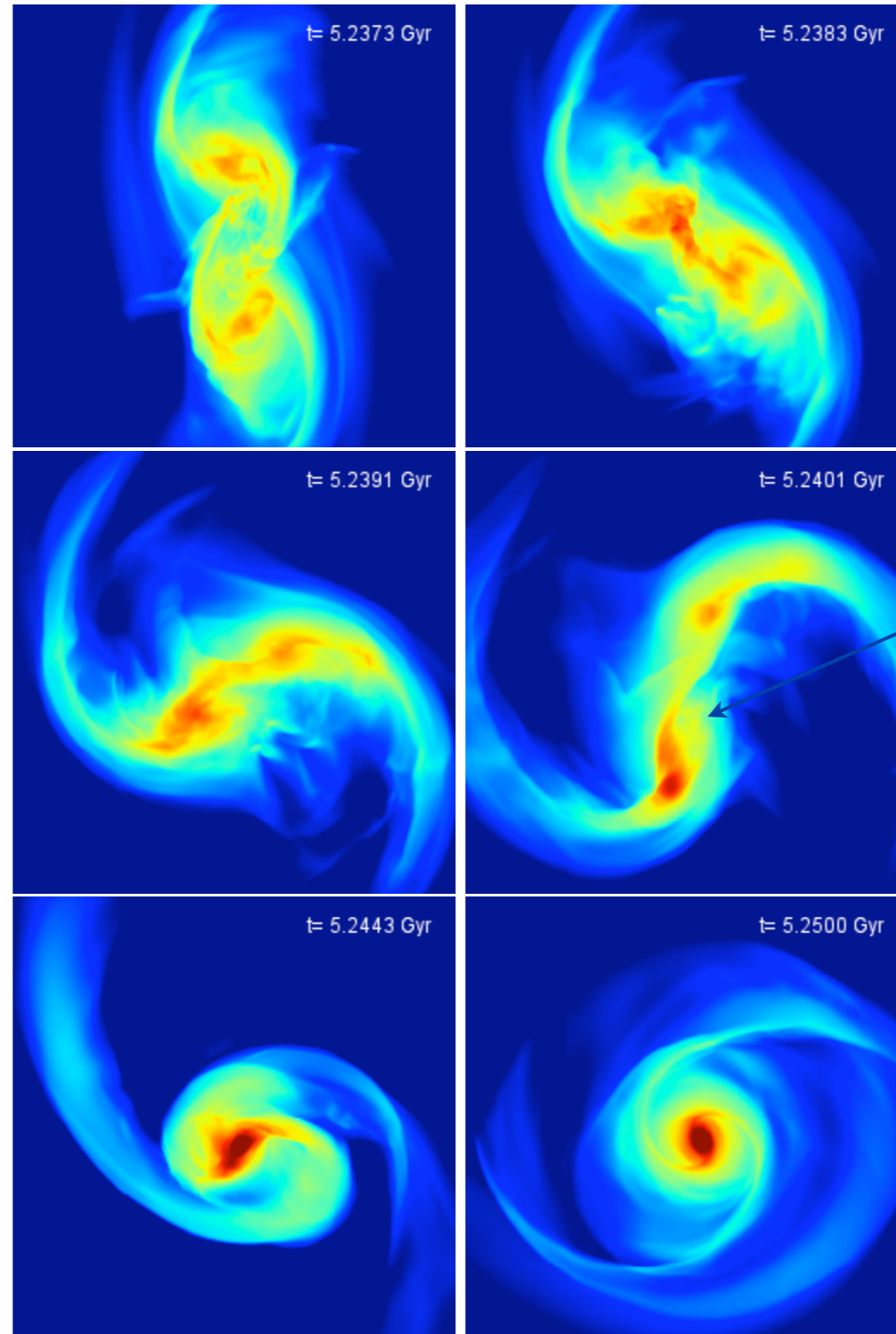
- trace self-consistently the sinking of the stellar and gaseous discs by dynamical friction against the dark matter background of the merging halos
- later, trace self-consistently the dynamics of the black holes in the time varying gravitational potential of the forming galaxy
- 1:1 merger has been tested against both SPH and AMR simulations



# FORMATION OF A MASSIVE NUCLEAR DISC of billion solar masses 200 pc in size 60 pc height

DENSITY MAP  
OF THE GASEOUS  
DISCS DURING THE  
FINAL MERGER

TIDAL TORQUES ARE  
REDISTRIBUTING  
THE ANGULAR  
MOMENTUM OF THE  
TWO INTERACTING  
DISCS



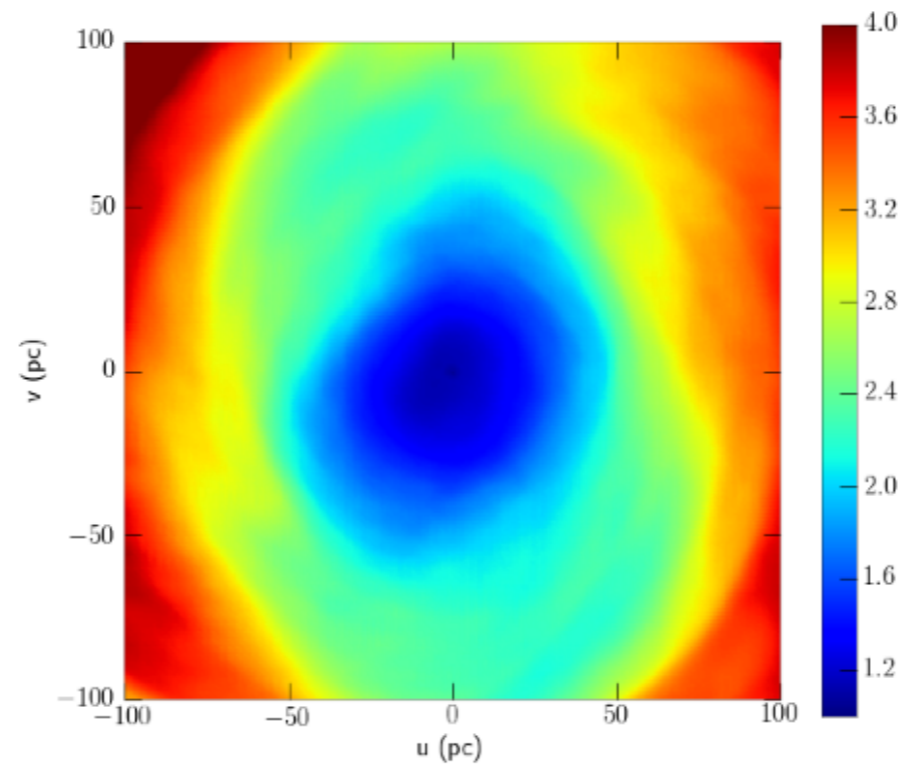
ASYMMETRIC  
SHOCKS DUE  
TO  
TURBULENCE

AMR SIMULATION BY CHAPON, MAYER, TEYSSIER, 2011

PRESSURIZED NUCLEAR DISC  
ONE-PHASE GAS WITH POLYTROPIC EQUATION OF STATE INDEX  
 $\Gamma=7/5$

MAP OF THE LOCAL TOOMRE PARAMETER  
CRITICAL FOR SMALL-SCALE FRAGMENTATION INTO STARS IF  $< 1$

$$Q = \frac{C_{\text{sound}} K_{\text{epicyclic}}}{\pi G \Sigma}$$

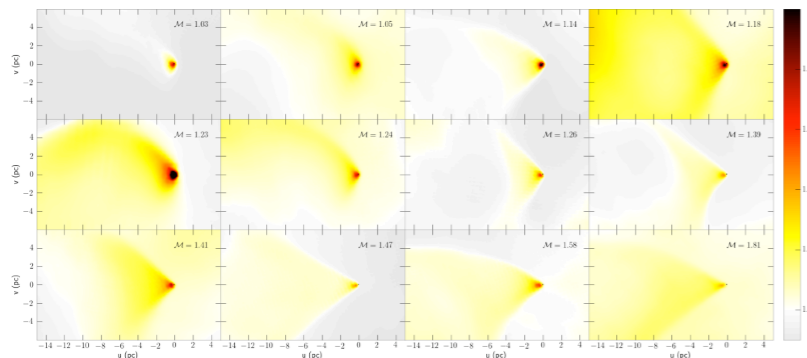
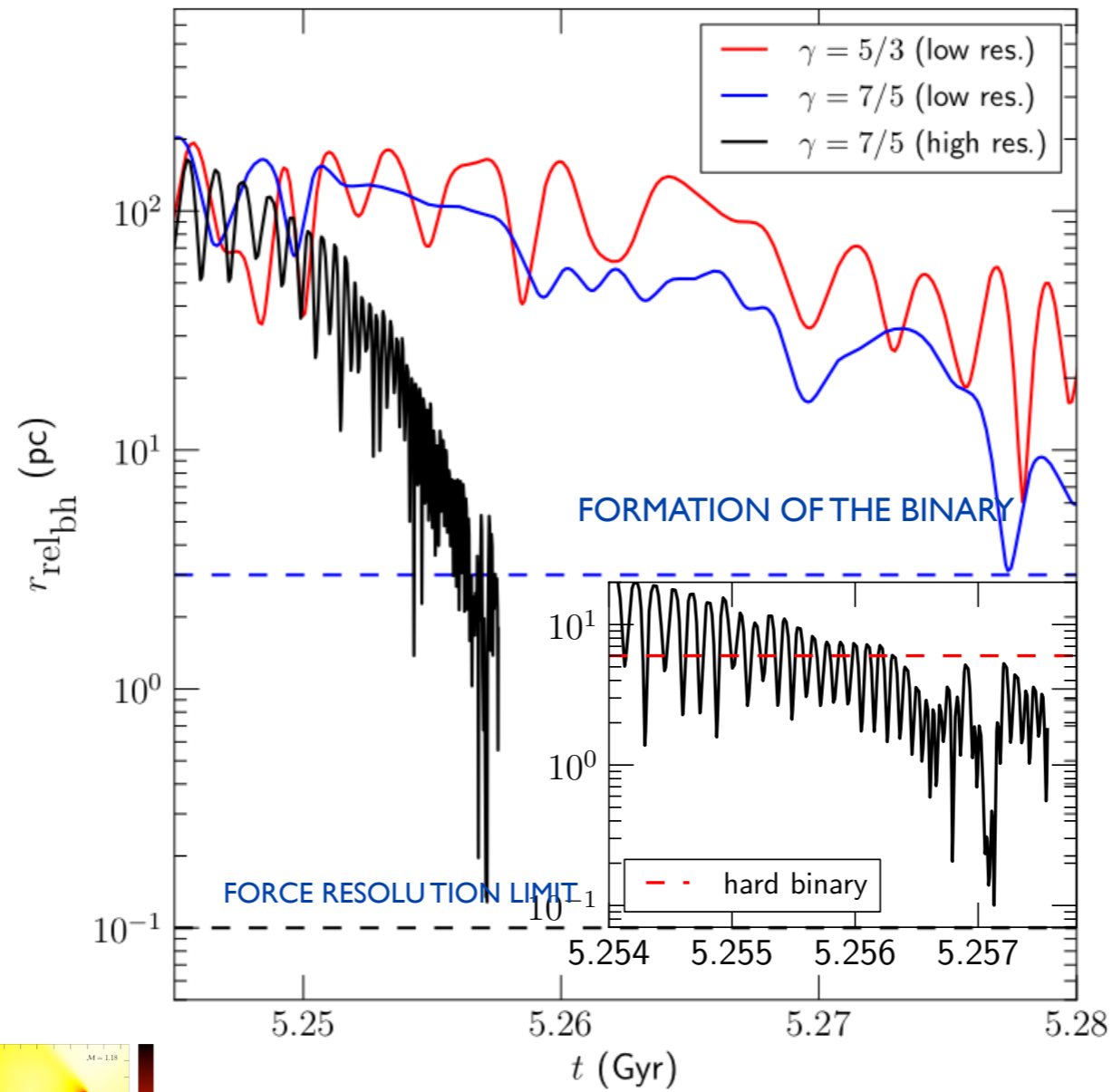


FACE ON VIEW

CHAPON, MAYER, TEYSSIER, 2011



rapid binary formation  
 few million years after the formation of the disc

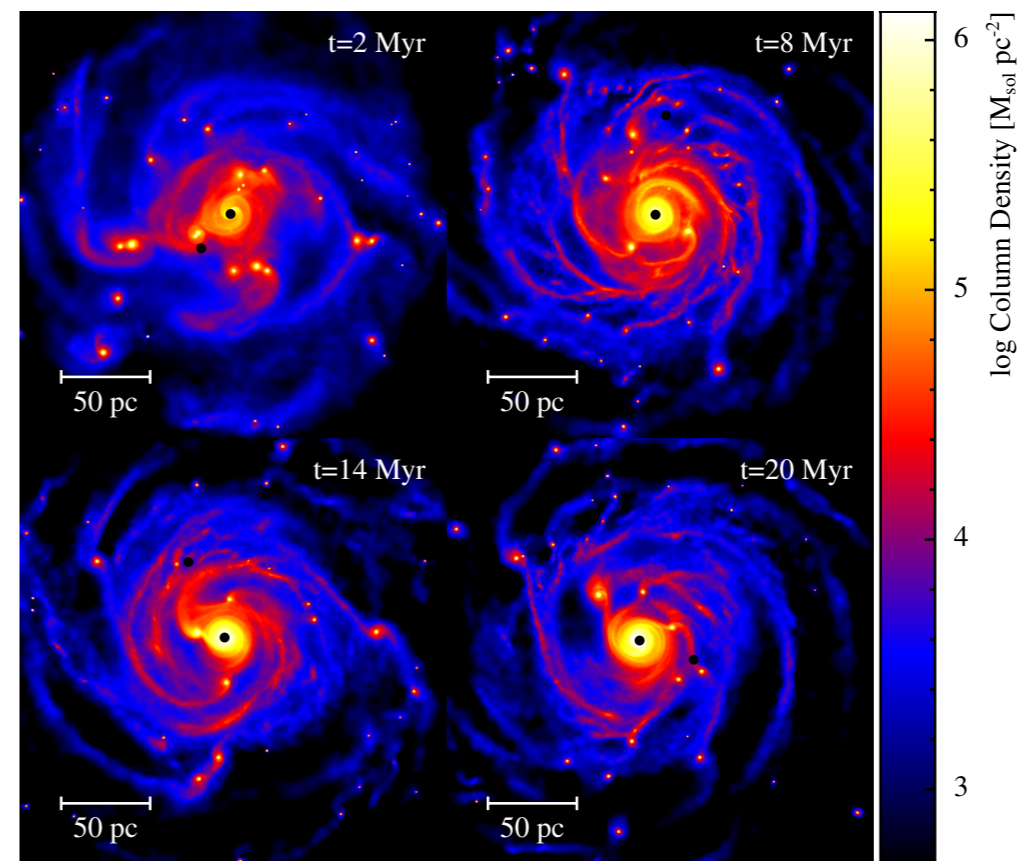


CHAPON, MAYER, TEYSSIER, 2011  
 MAYER et al. 2007  
 COLPI & DOTTI 2011 for a review

# caveats

- THE ISM IS MULTI PHASE
- CIRCUM-NUCLEAR DISCS ARE UNSTABLE TO FRAGMENTATION- STAR FORMATION

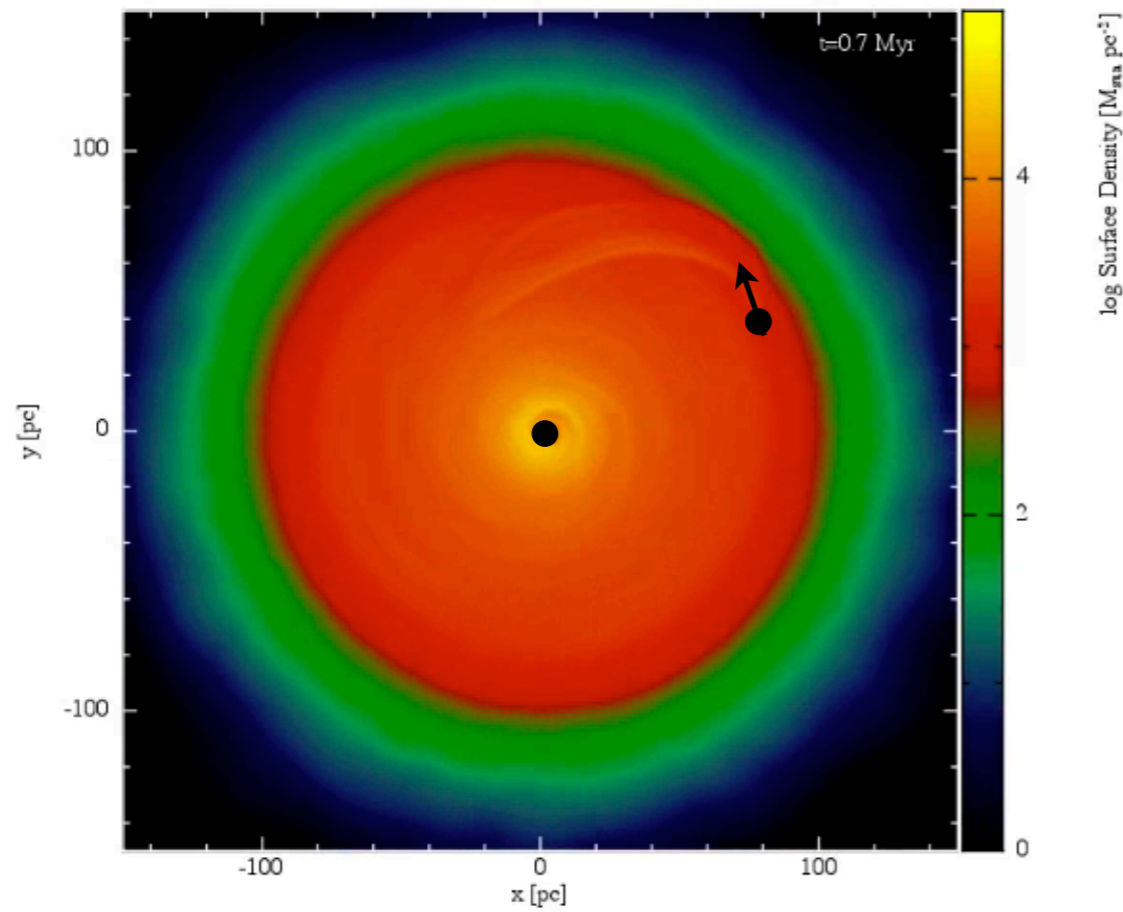
.....FIACCONI's TALK



- black hole dynamics in massive circum-nuclear discs

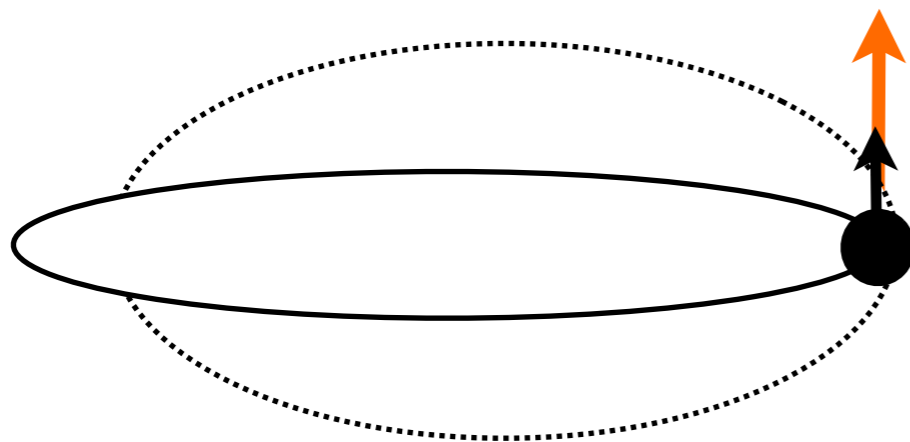
DEDICATED HIGH-RESOLUTION SIMULATIONS  
OF THE BLACK HOLE EVOLUTION IN  
ROTATIONALLY SUPPORTED NUCLEAR DISCS  
MESTEL PROFILE

$$M_{\text{disc}} = 10^8 M_{\odot} \quad M_{\text{BH}} = 10^6 M_{\odot}$$

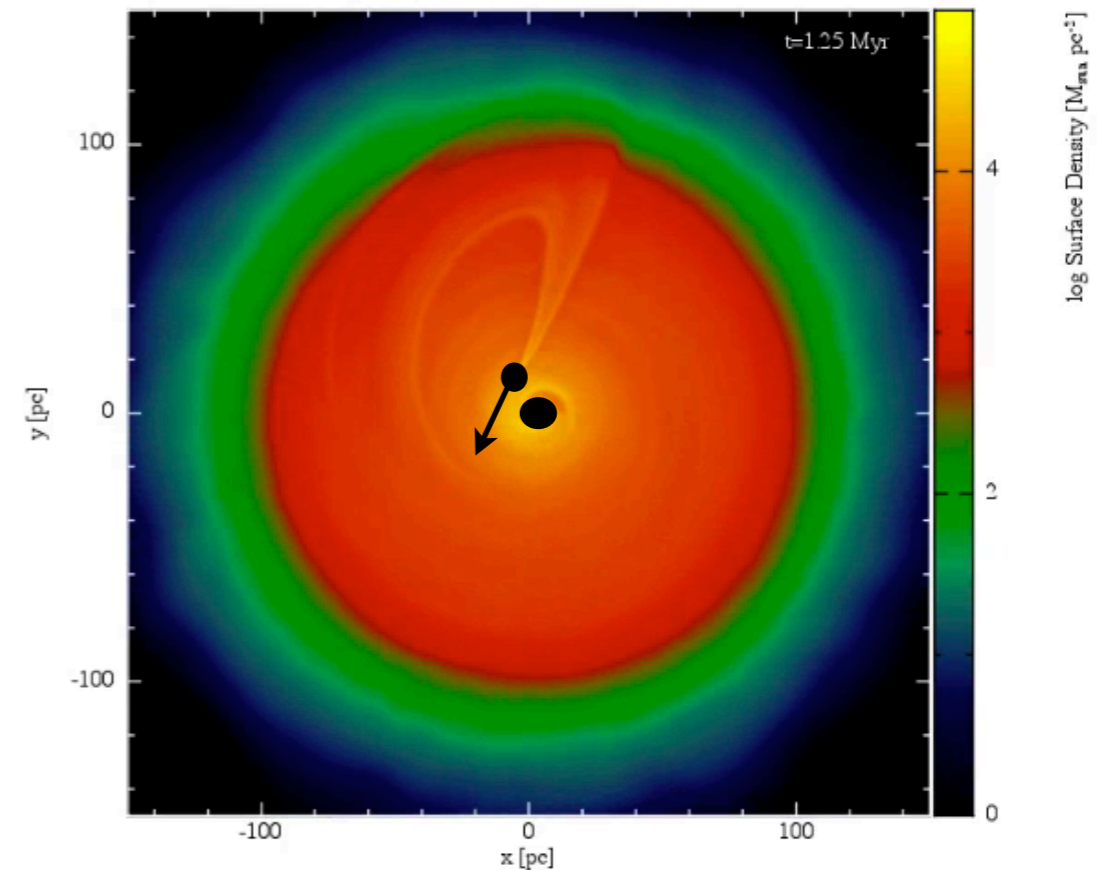


THE ROTATING GASEOUS BACKGROUND  
FORCES THE SECONDARY BLACK HOLE TO  
**CO-ROTATE** WITH THE DISC  
(even counter-rotating orbits get corotating)  
MEMORY LOSS OF THE INITIAL  
ECCENTRICITY  
the drag force is mostly acting at peri-  
center where the wake lags behind

$$\dot{E}_{\text{bin}}/E_{\text{bin}} > \dot{J}_{\text{bin}}/J_{\text{bin}}$$



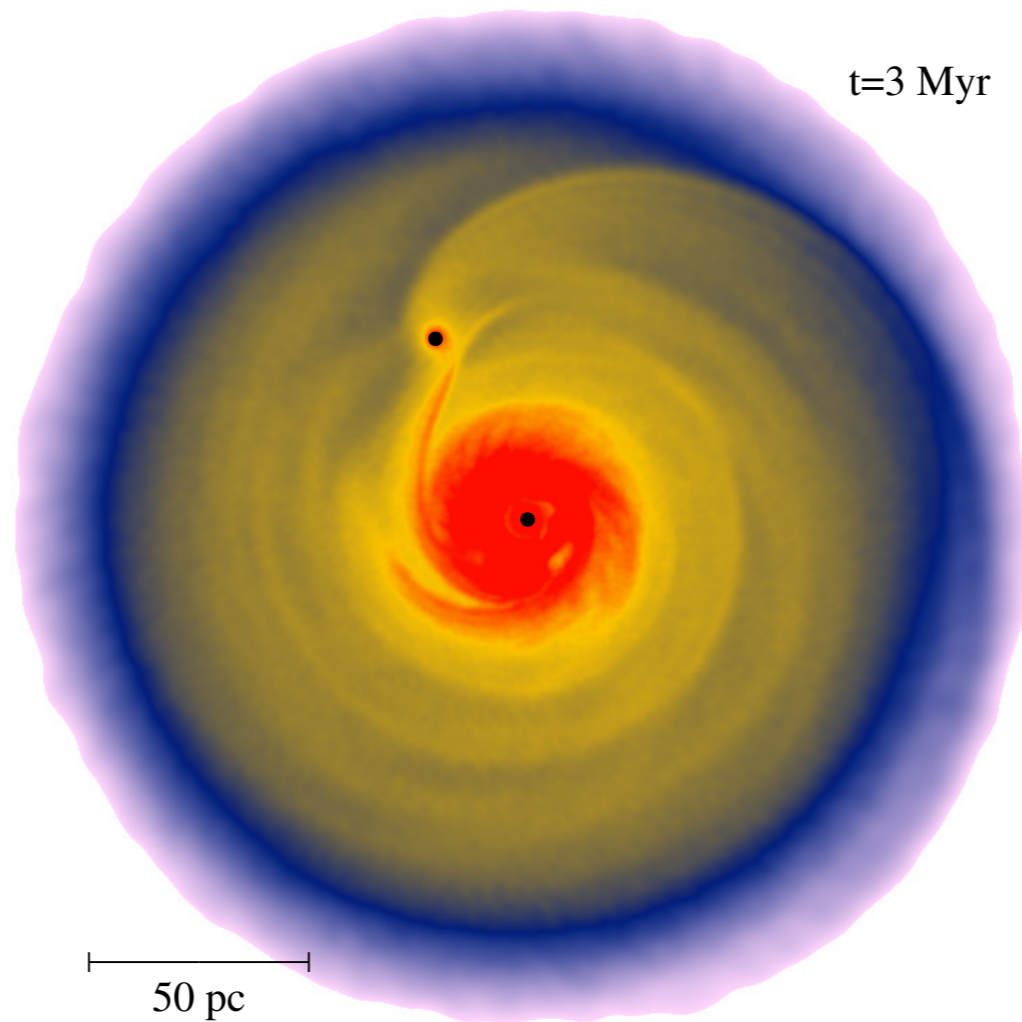
DOTTI et al. 2006,2007,2009a,b  
PEREGO et al. 2009  
COLPI & DOTTI, 2011  
FIACCONI et a. 2013 SUBMITTED



after circularization  
... torques on the secondary black hole  
reminiscent Type I planet migration

$$\frac{t_{\text{migration}}}{t_{\text{dyn-friction}}} \approx 2\pi \ln \Lambda h$$

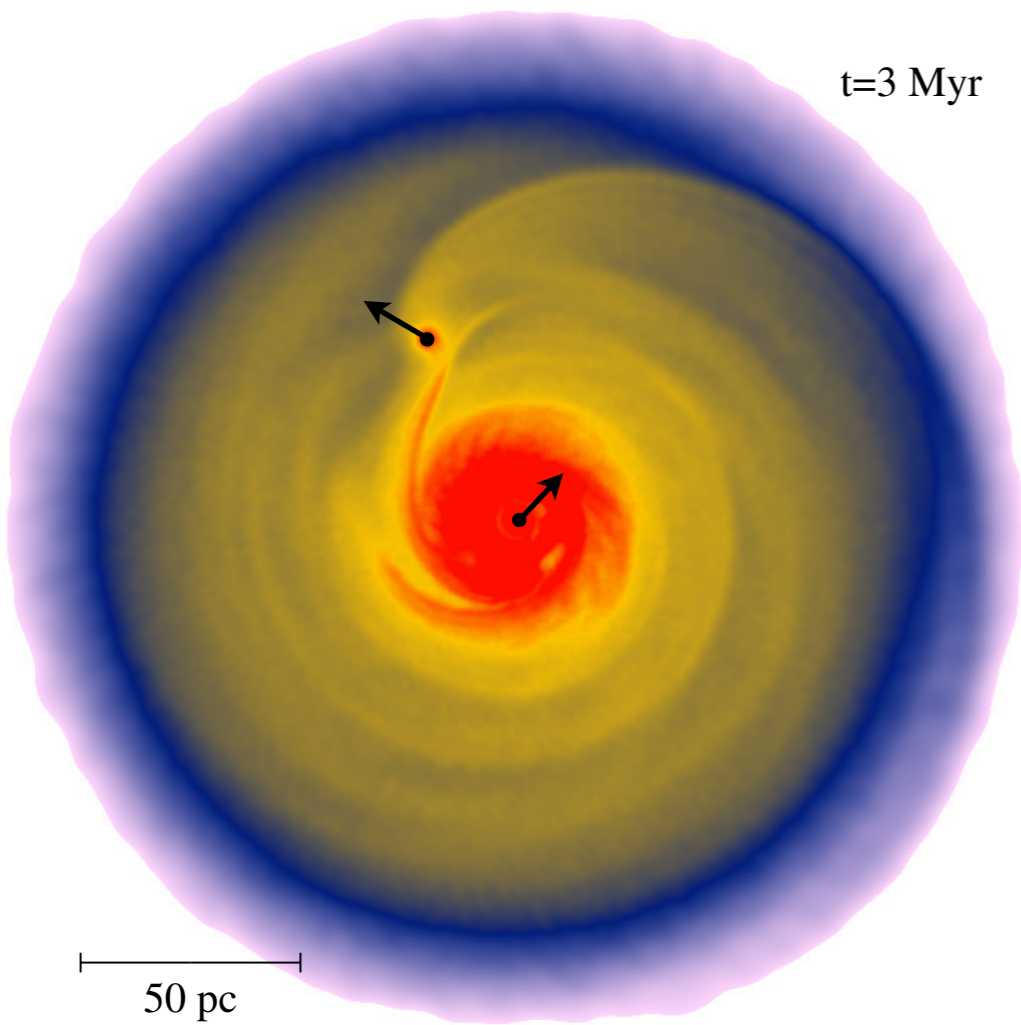
FIACCONI et al. 2013



$$M_{\text{disc}} > M_{\text{BH},2}$$

MAYER, 2013arXiv1308.0431



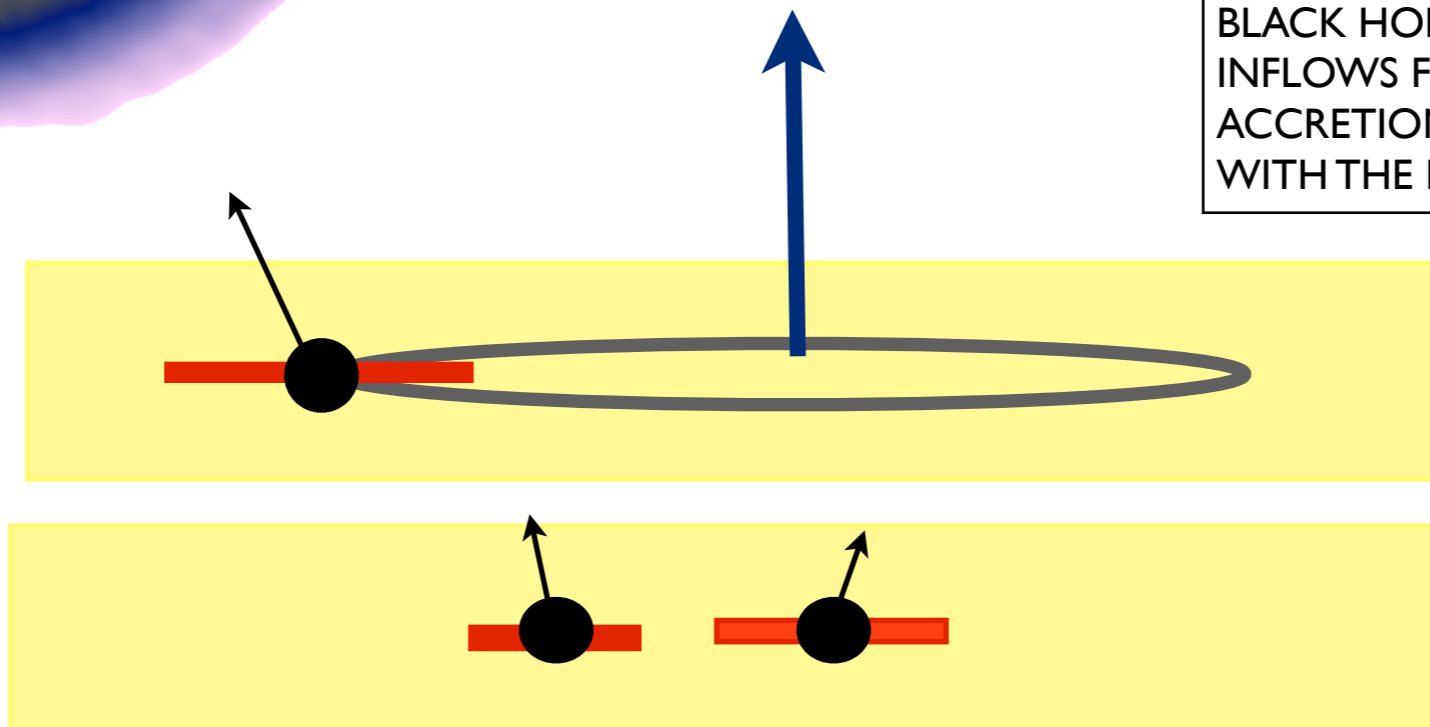


BLACK HOLE  
SPIN - ORBIT ALIGNMENT  
even before  
BINARY FORMATION

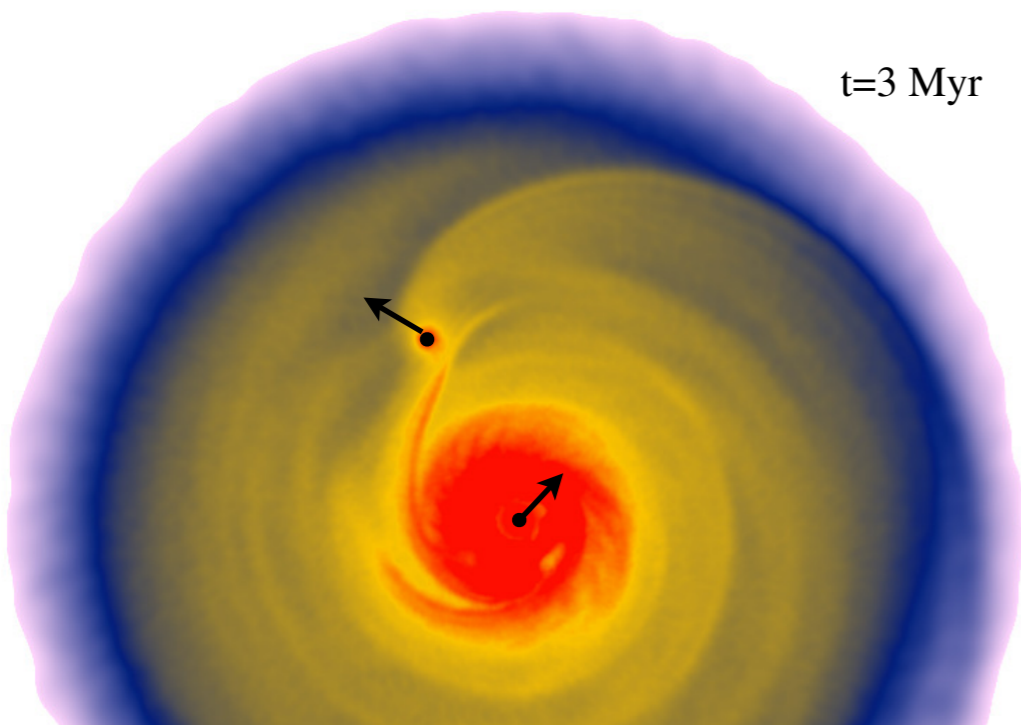
$$\tau_{al} \sim 10^5 a^{5/7} M_{BH,6}^{-2/35} \alpha_{0.1}^{58/35} \left( \frac{f_E}{\eta_{0.1}} \right)^{-32/35} \text{ yr}$$

ORBITAL ANGULAR MOMENTUM

BLACK HOLES ARE FED BY GAS  
INFLOWS FORMING  
ACCRETION DISCS COPLANAR  
WITH THE NUCLEAR DISC



BARDEEN 1970; BARDEEN & PETERSON 1975; BOGDANOVIC et al. 2007; PEREGO et al. 2009; DOTTI et al. 2009, MILLER & KROLIK 2013



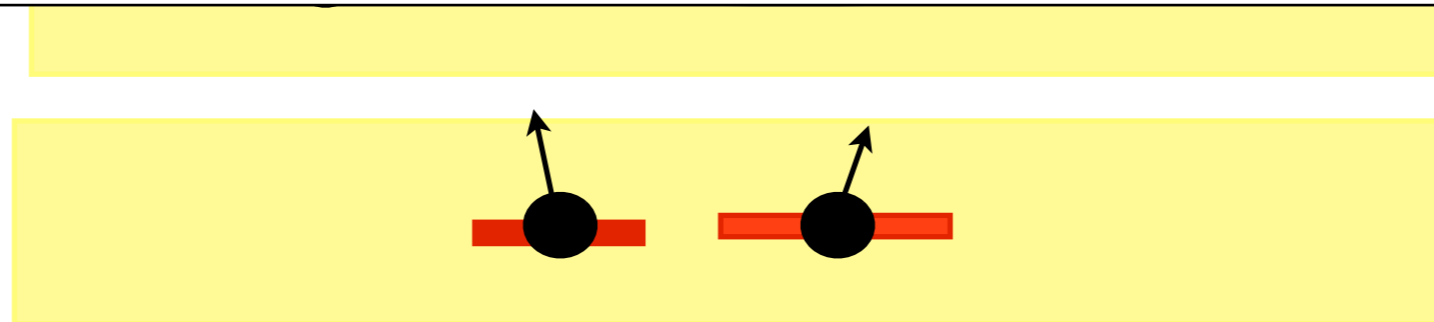
t=3 Myr

BLACK HOLE  
SPIN - ORBIT ALIGNMENT  
BEFORE BINARY FORMATION

if the spin configuration is maintained down to  
coalescence

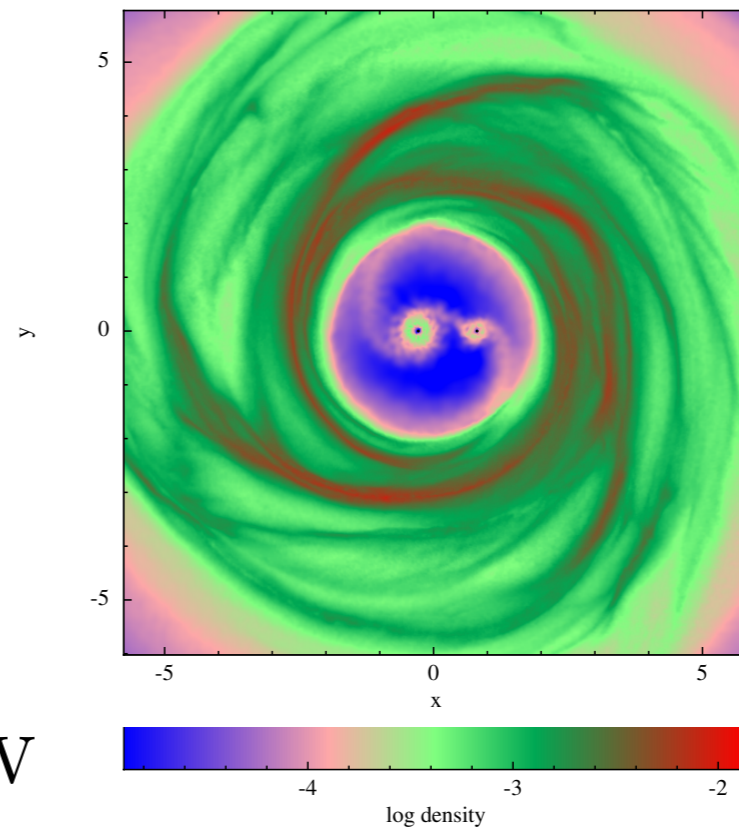
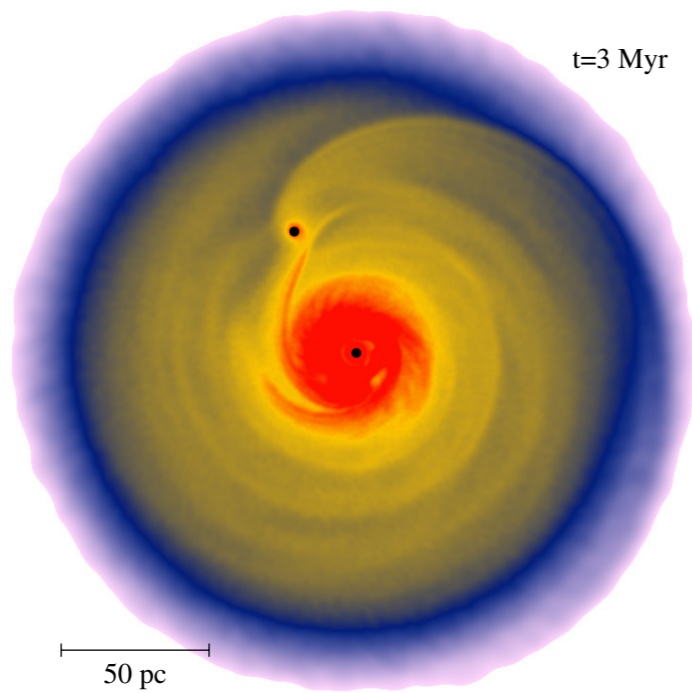
recoil velocities  $< 100$  km/s

anchoring the new black hole to the parent galaxy



BARDEEN 1970; BARDEEN & PETERSON 1975; BOGDANOVIC et al. 2007; PEREGO et al. 2009; DOTTI et al. 2009,2010, MILLER & KROLIK 2013  
COLPI & DOTTI 2011 for a review

# GAP FORMATION ?



$$a_{\text{gap}} > a_{\text{GW}}$$

$$t_{\text{migration}} ?$$

del VALLE & ESCALA 2013

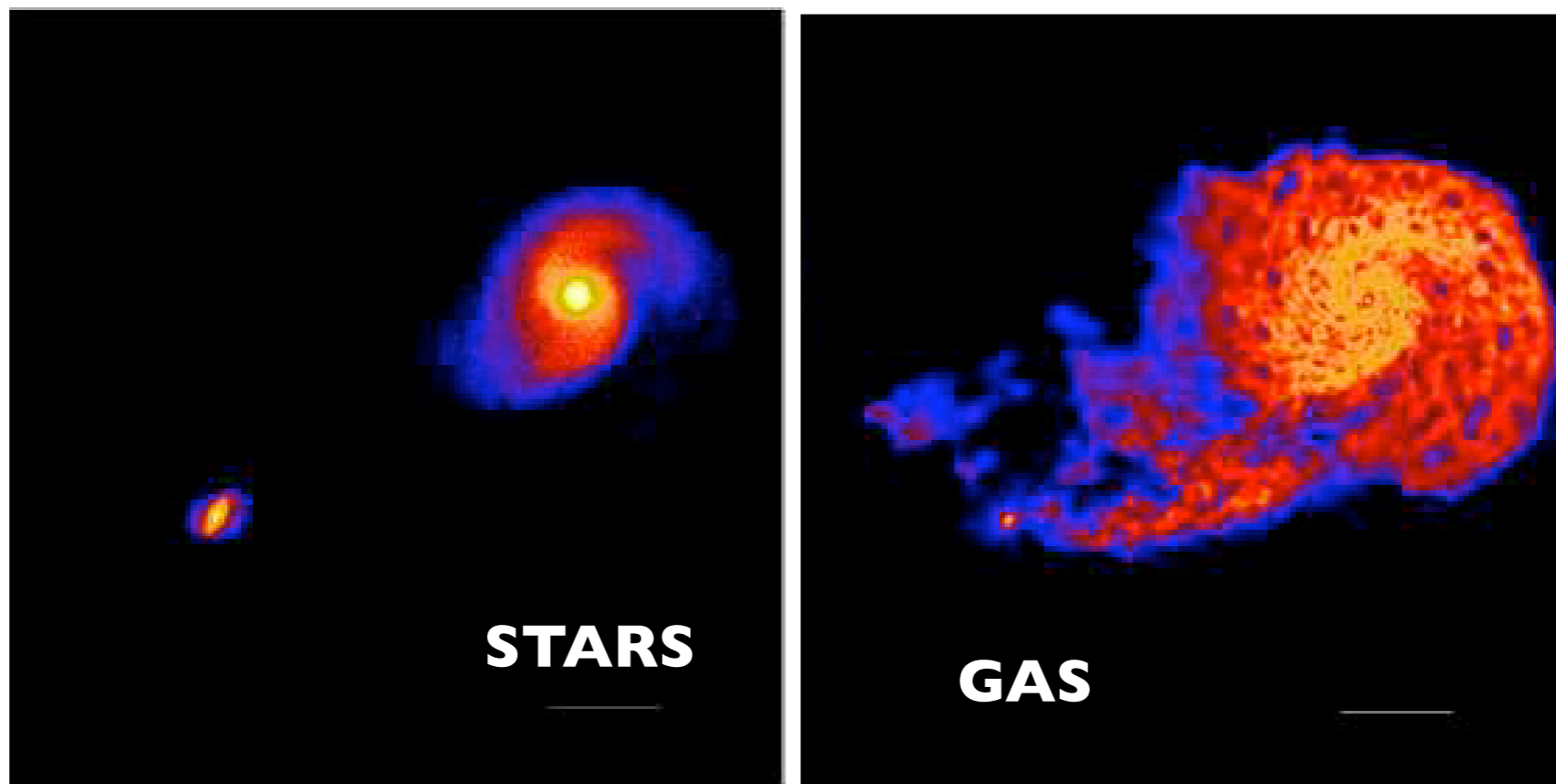
.... **CUADRA's TALK**

when and where the gap forms ?..... here are the most interesting observational signatures

## IN DISSIPATIVE MERGERS

- rapid sinking of the black hole pair by dynamical friction and type I migration against the gas
- multi phase medium ...
- circularization of the orbit
- accretion - spin orbit alignment
- migration in circumbinary disc
- competitive shrinking from stellar interactions

- black hole dynamics in unequal mass merger (1:4, 1:10)

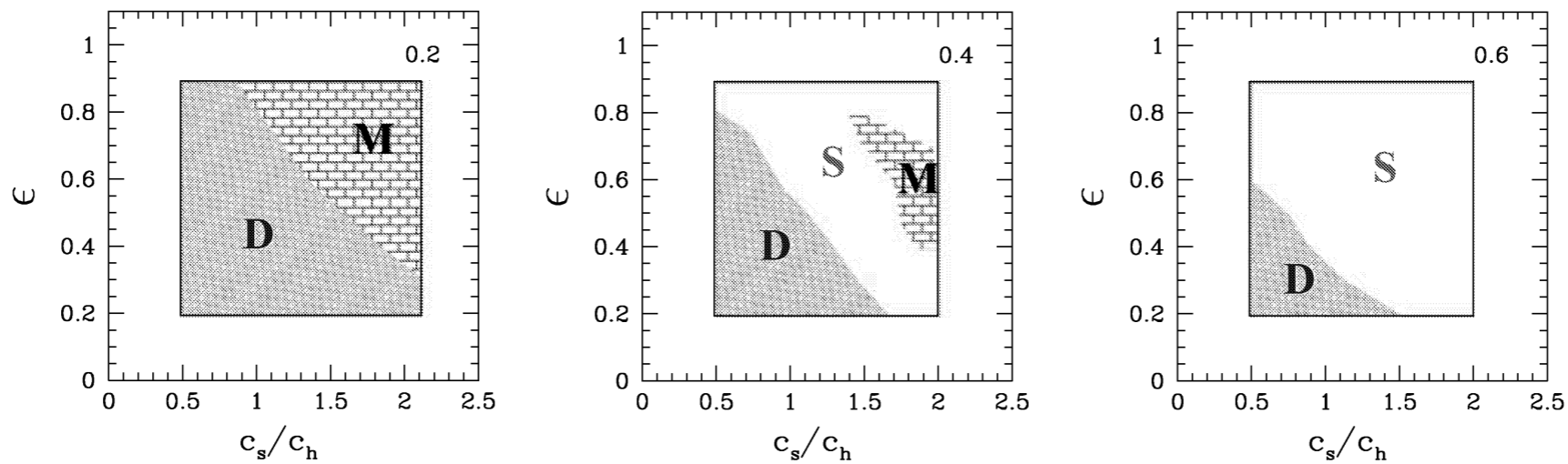
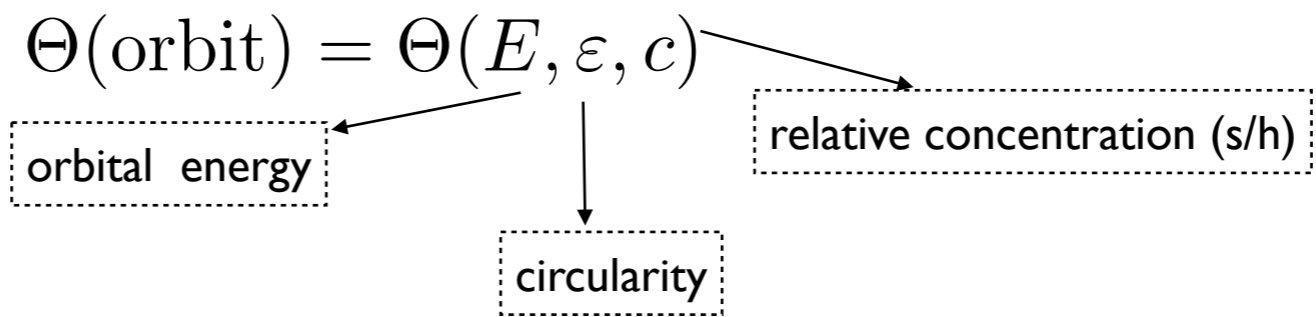




# SINKING OF DARK MATTER SATELLITES IN LARGER DARK MATTER HALOS NFW

$$\frac{t_{\text{merging}}}{t_{\text{dyn}}}\Big|_{\text{vir}} \approx \frac{\Theta(\text{orbit})}{\ln(1 + M_{\text{host}}/M_{\text{sat}})} \frac{M_{\text{host}}}{M_{\text{sat}}}$$

live satellites

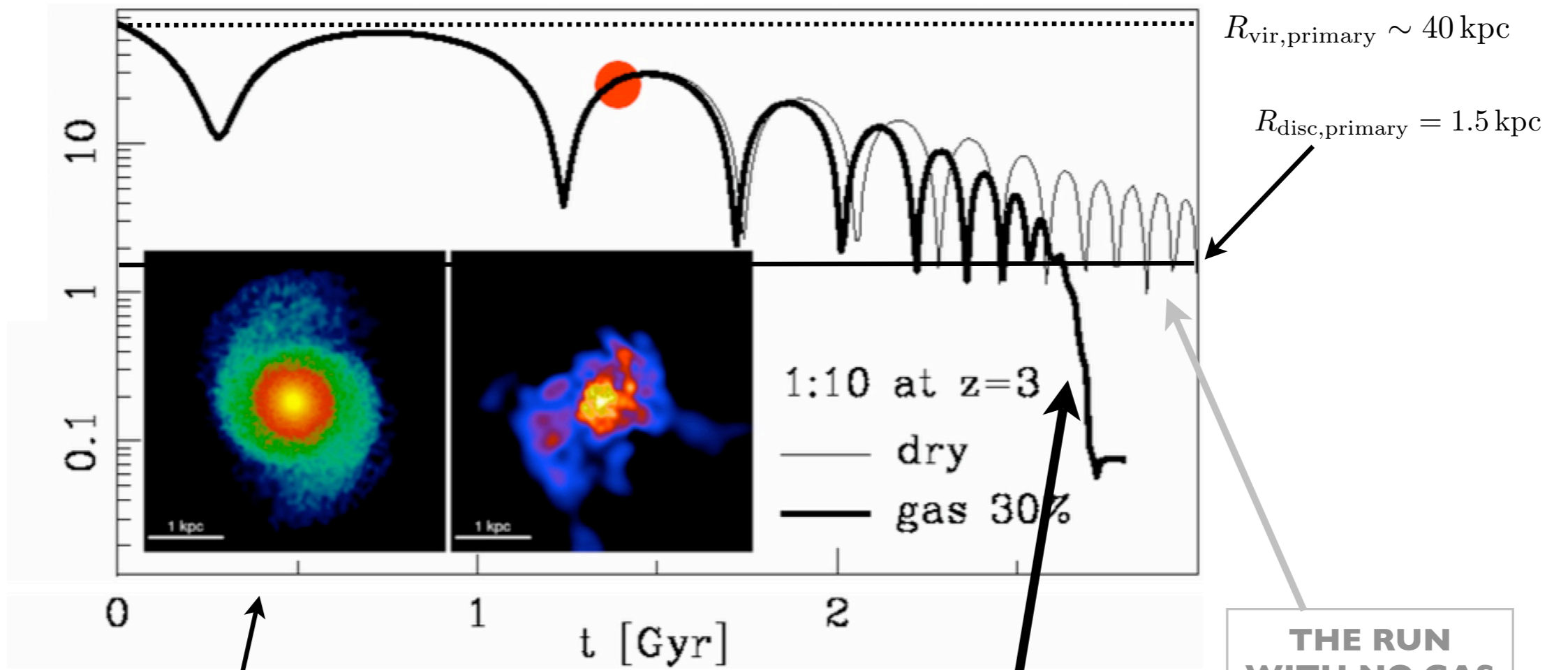


GOVERNATO, COLPI MARASCHI 1994, COLPI, MAYER GOVERNATO 2000, TAFFONI et al. 2002, BOYLAN-KOLCHIN 2008

# BLACK HOLE PAIRING ?

## 30% GAS-RICH COPLANAR PROGRADE PARABOLIC ENCOUNTER

BLACK HOLE SEPARATION (kpc)

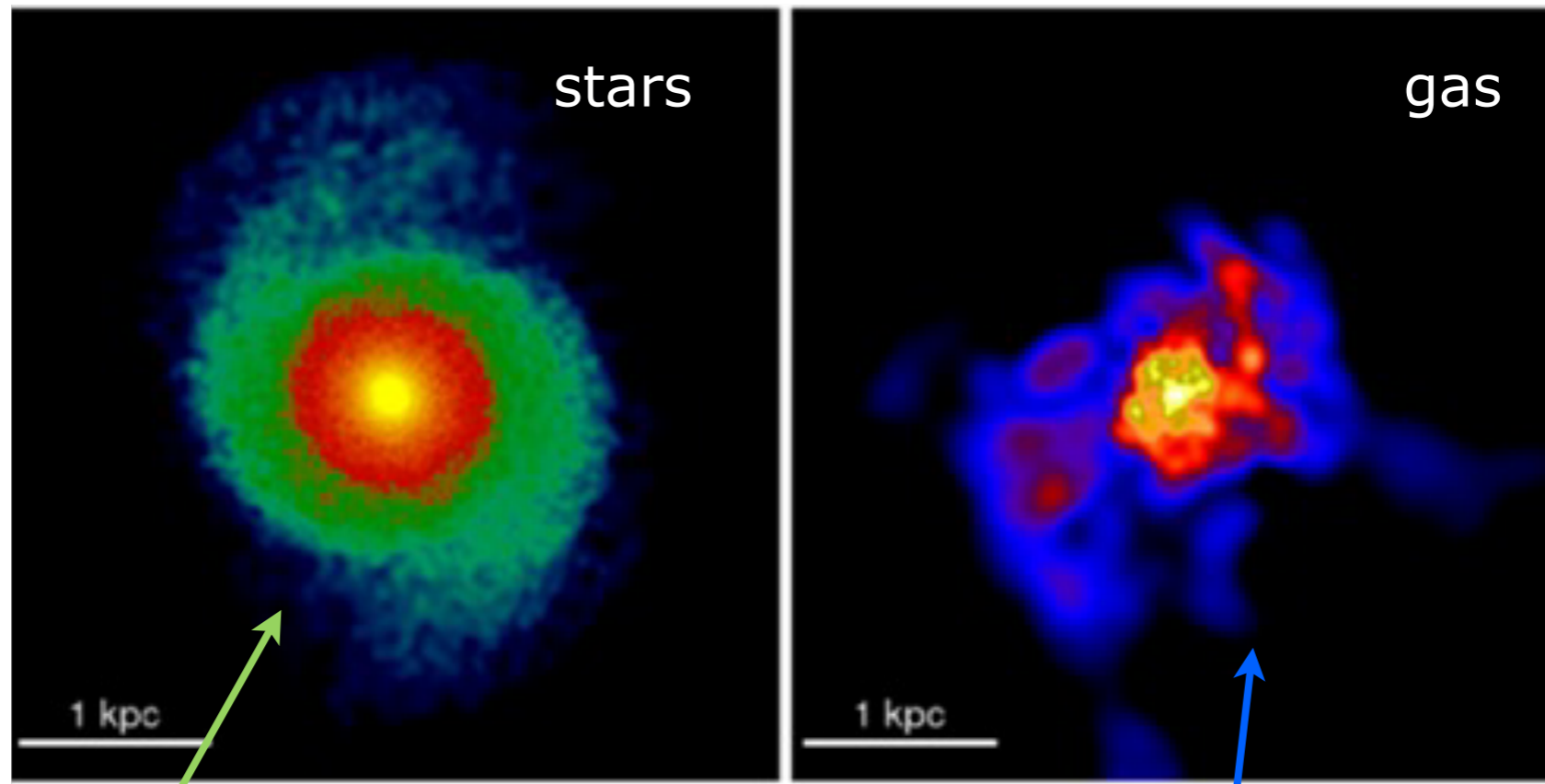


THE BLACK HOLE IS AT THE CENTER OF THE COMPACT CORE

THE RUN WITH NO GAS WANDERING BLACK HOLE

IN GAS-RICH ENVIRONMENT THE SECONDARY BLACK HOLE REACHES A SEPARATION OF 100 pc

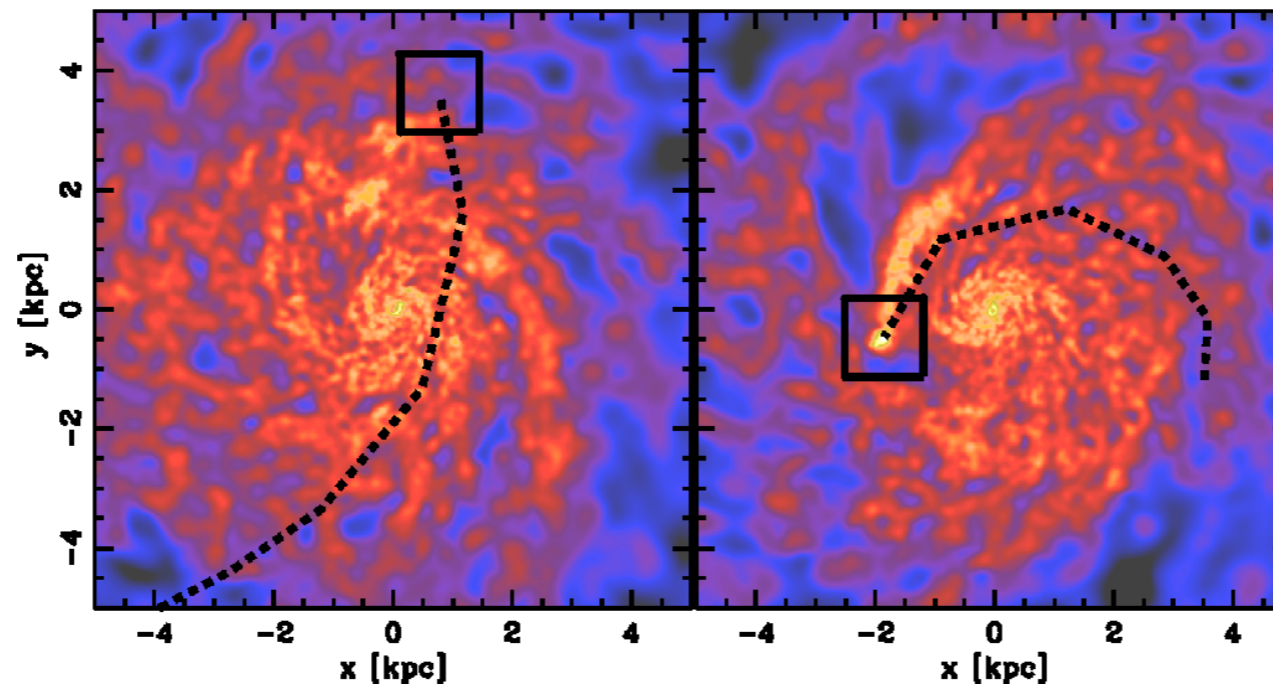
IMAGE @ II PERI-GALACTIC APPROACH



**CONCENTRATED STAR FORMATION EPISODE  
DUE TO INFLOWS BY COMPRESSIVE TIDES**

THE **GALACTIC DISC** DEVELOPS A CLUMPY IRREGULAR  
STRUCTURE  
MOST OF THIS GAS WILL BE RAM-PRESSURE STRIPPED  
WHEN PLUNGING INTO THE DISC OF THE PRIMARY GALAXY

ACCRETION FOLLOWING THE  
**CIRCULARIZATION**  
OF THE BLACK HOLE ORBIT

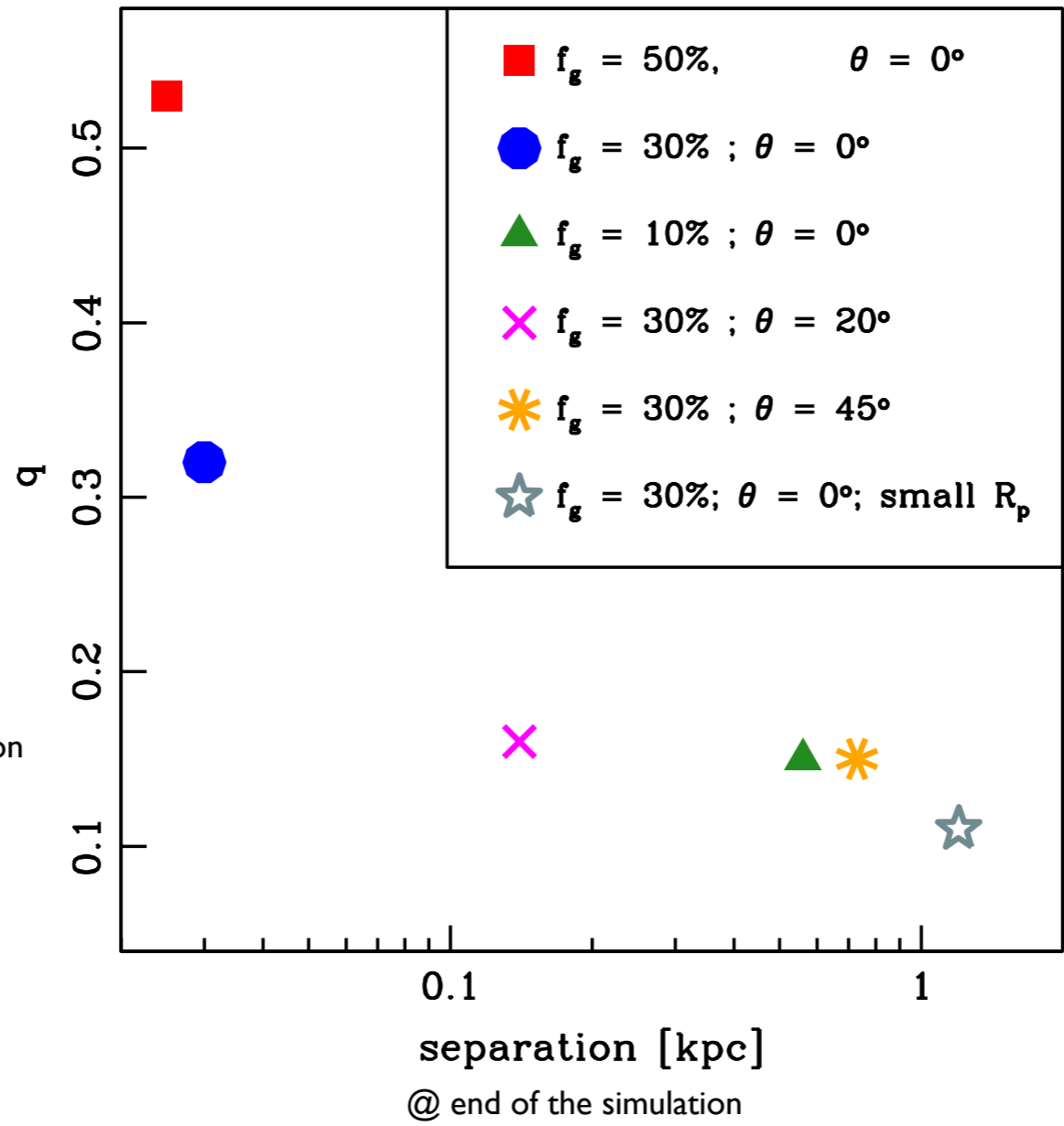


$$\dot{M}_{\text{BHL}} \sim 4\pi \frac{G^2 M_{\text{BH}}^2(t) \rho_{\text{gas}}(t)}{[c_{\text{sound}}^2(t) + V_{\text{rel}}^2(t)]^{3/2}}$$

correlating  
PAIRING versus BLACK HOLE MASS RATIO

$$\frac{M_{\text{BH},2}}{M_{\text{BH},1}}$$

end of the simulation



the ability of pairing depends on the strength of torques in creating a dense cuspy stellar core around the secondary black hole + accretion

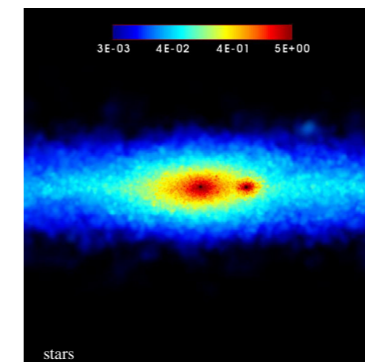
BARYONIC PHYSICS + COSMOLOGICAL ORBITAL PARAMETERS DETERMINE THE OUTCOME OF A MERGER



## BOTTLENECK minor mergers

- the bottleneck is in the pairing phase
- baryonic physics + cosmological parameters determine the outcome of the merger
- existence of a limiting  $q$  (0.1) below which coalescence is aborted or delayed

KHAN et al. 2012a,b



after 30 years...

there has been a number of advances

all studies have enriched the question  
on whether stars or/and gas disc  
in more realistic environments alleviate the last parsec problem  
still knowledge is fragmented and incomplete  
having explored a relatively small  
parameter space

### WISHFUL LIST FOR FURTHER PROGRESS

- (I) GALAXIES WITH IMPROVED PHYSICS AND IMPROVED  
MODELING OF THE GAS THERMODYNAMICS
- (II) STUDY THE DYNAMICS DURING STRUCTURE FORMATION  
AT LARGE REDSHIFT
- (III) CLOSER INSPECTION OF THE GAP OPENING CONDITIONS