

Convective Dynamics of Icy Ocean Worlds

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Frontiers in Oceanic, Atmospheric & Cryospheric
Boundary Layers

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INSTITUTE FOR GEOPHYSICS
THE UNIVERSITY OF TEXAS AT AUSTIN

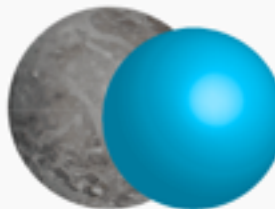
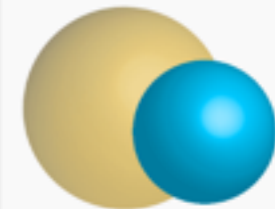
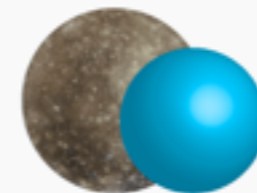
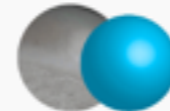
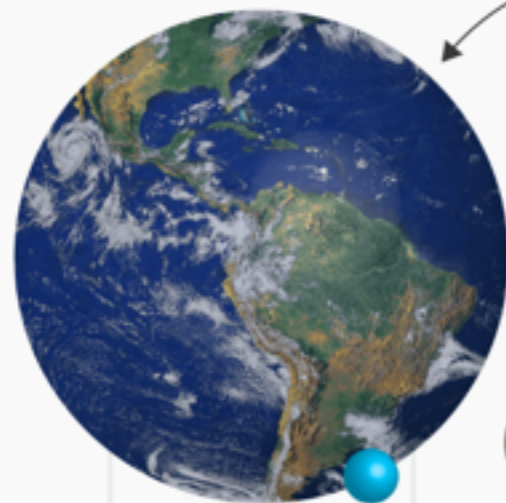


Habitability of Ocean Worlds

- Ocean worlds are exciting prospects for habitability

HOW THE SOLAR SYSTEM'S LARGEST OCEAN WORLDS COMPARE IN SIZE

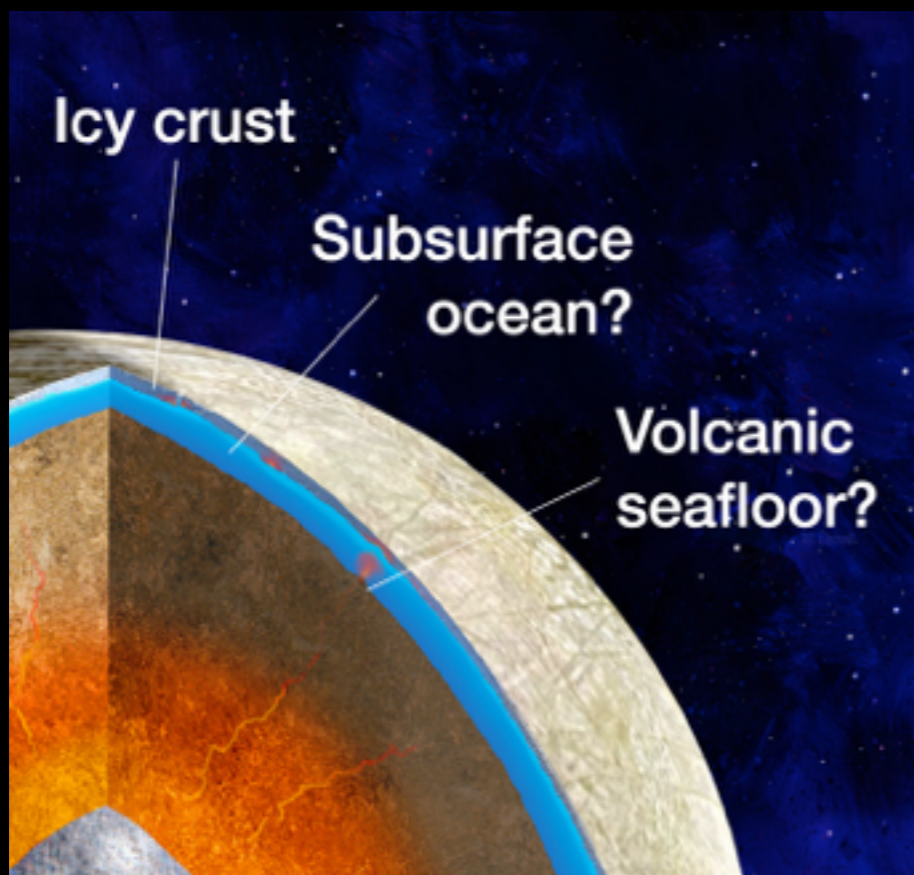
Earth has a surprisingly small amount of water compared to other worlds in the Solar System. Each measurement is the spherical radius of the world and its water (including ice):



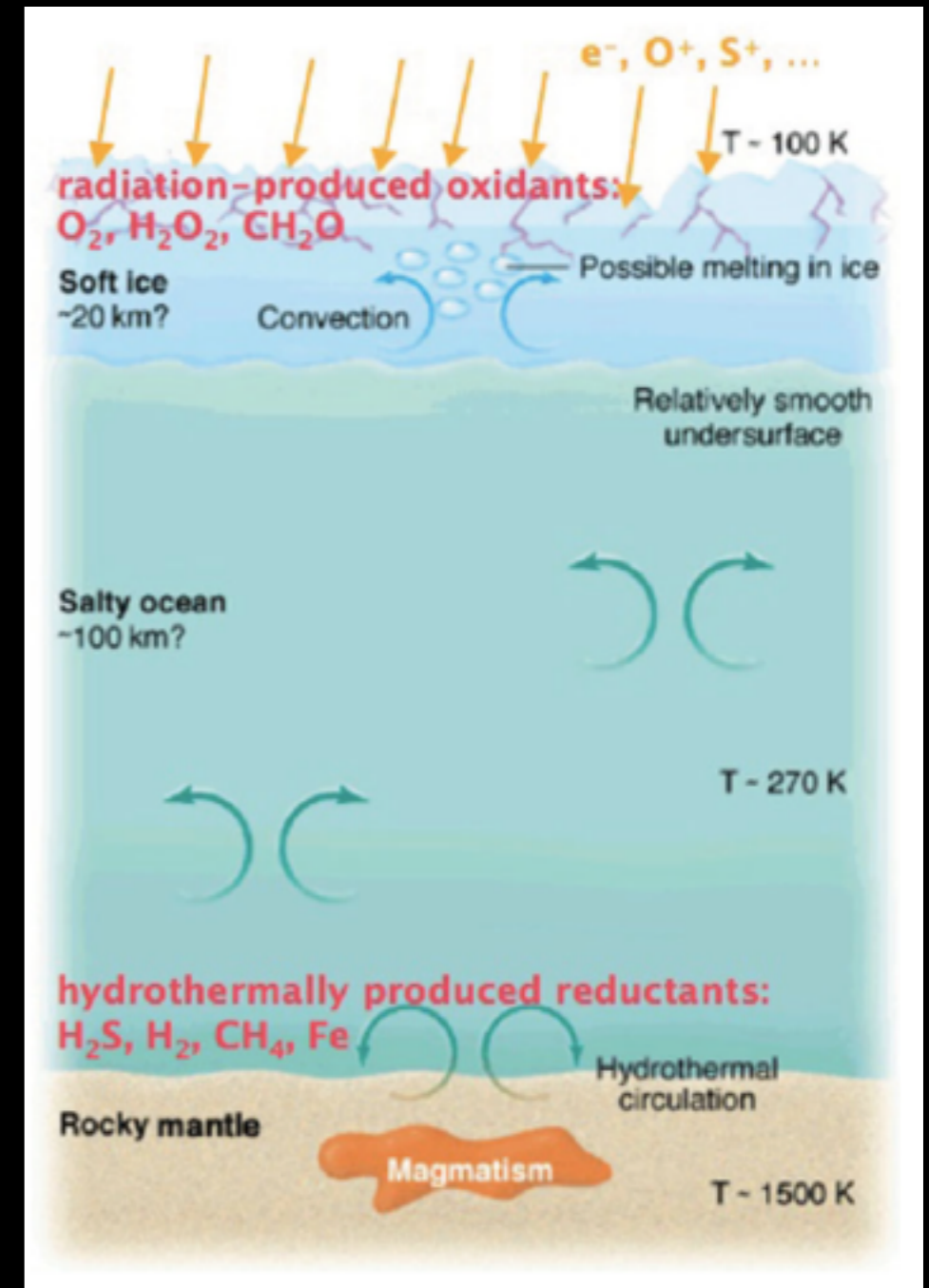
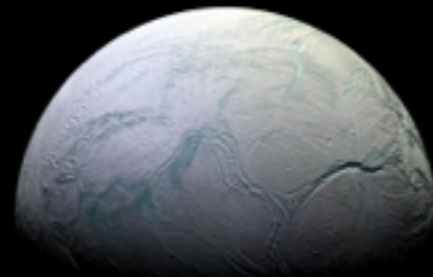
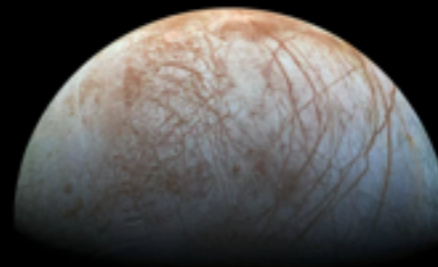
ENCELADUS	DIONE	EARTH	EUROPA	PLUTO	TRITON	CALLISTO	TITAN	GANYMEDE
Water radius: 140 mi./ 220 km.	Water radius: 300 mi./ 480 km.	Water radius: 430 mi./ 690 km.	Water radius: 550 mi./ 880 km.	Water radius: 630 mi./ 1010 km.	Water radius: 730 mi./ 1170 km.	Water radius: 1,120 mi./ 1,800 km.	Water radius: 1,180 mi./ 1,890 km.	Water radius: 1,460 mi./ 2,350 km.
World radius: 157 mi./ 252 km.	World radius: 349 mi./ 561 km.	World radius: 3,959 mi./ 6,371 km.	World radius: 972 mi./ 1,565 km.	World radius: 738 mi./ 1,187 km.	World radius: 840 mi./ 1,352 km.	World radius: 1,498 mi./ 2,410 km.	World radius: 1,601 mi./ 2,576 km.	World radius: 1,635 mi./ 2,631 km.

Habitability of Ocean Worlds

- Oxidants are produced on the surface by ion irradiation
- Reductants might be produced at the seafloor if hydrothermal circulation is present



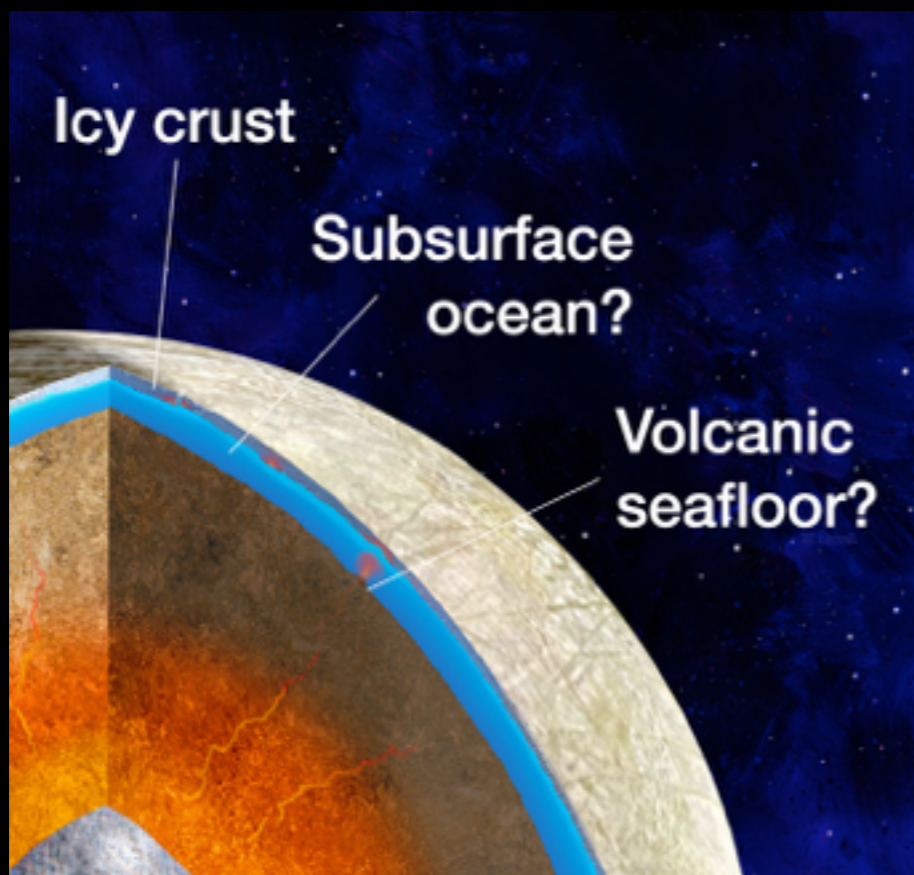
Credit: NASA



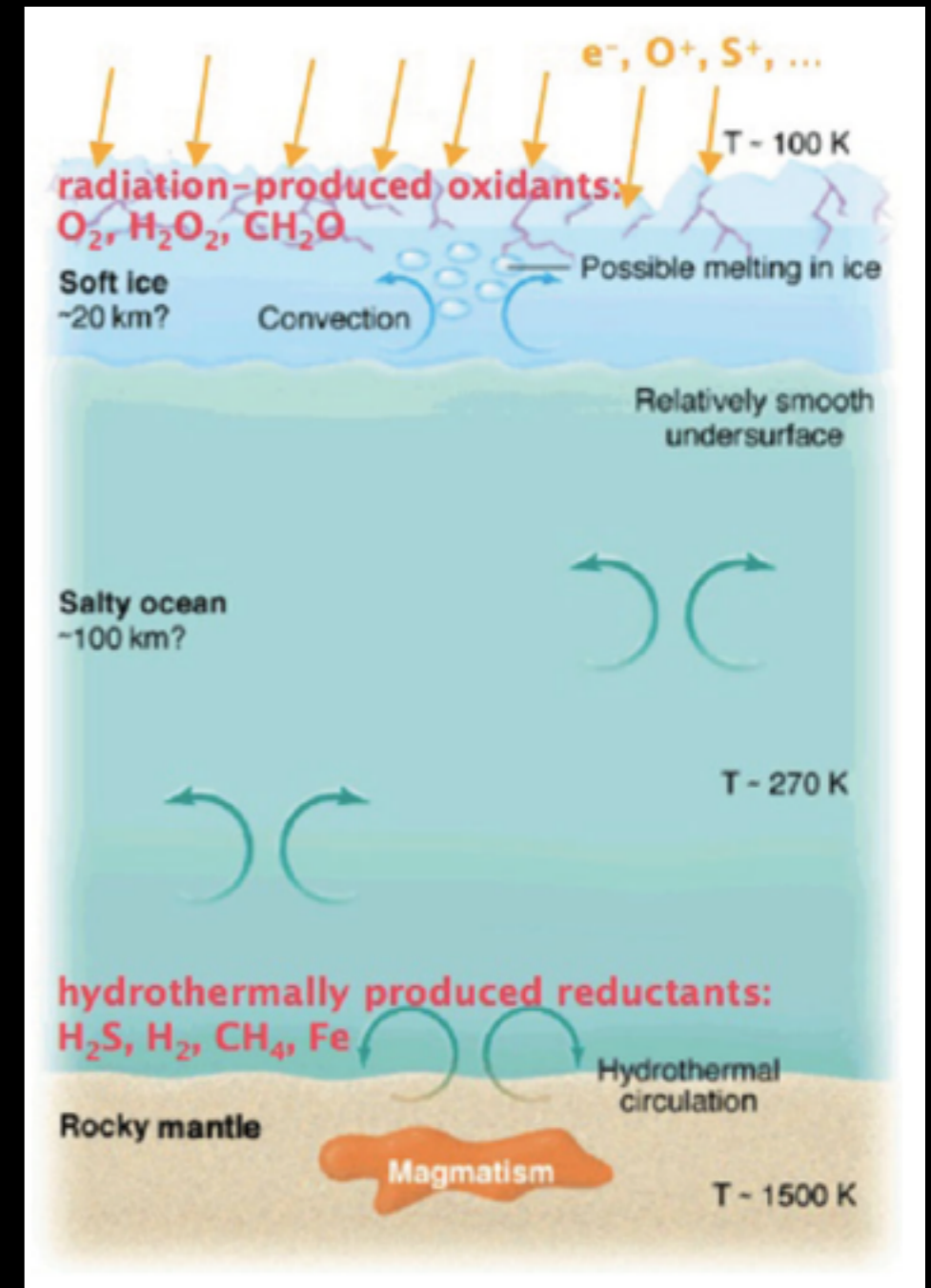
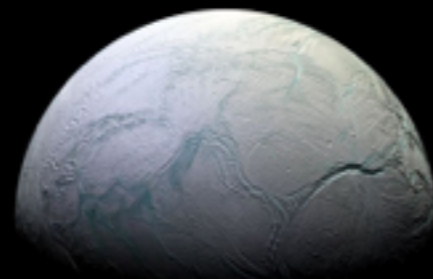
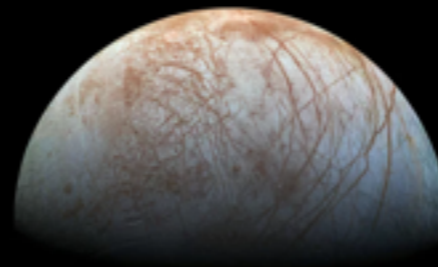
Credit: Pappalardo (2010), after Stevenson (2000)

Habitability of Ocean Worlds

→ How are heat and materials transported across the oceans of icy satellites?



Credit: NASA



Credit: Pappalardo (2010), after Stevenson (2000)

Outline

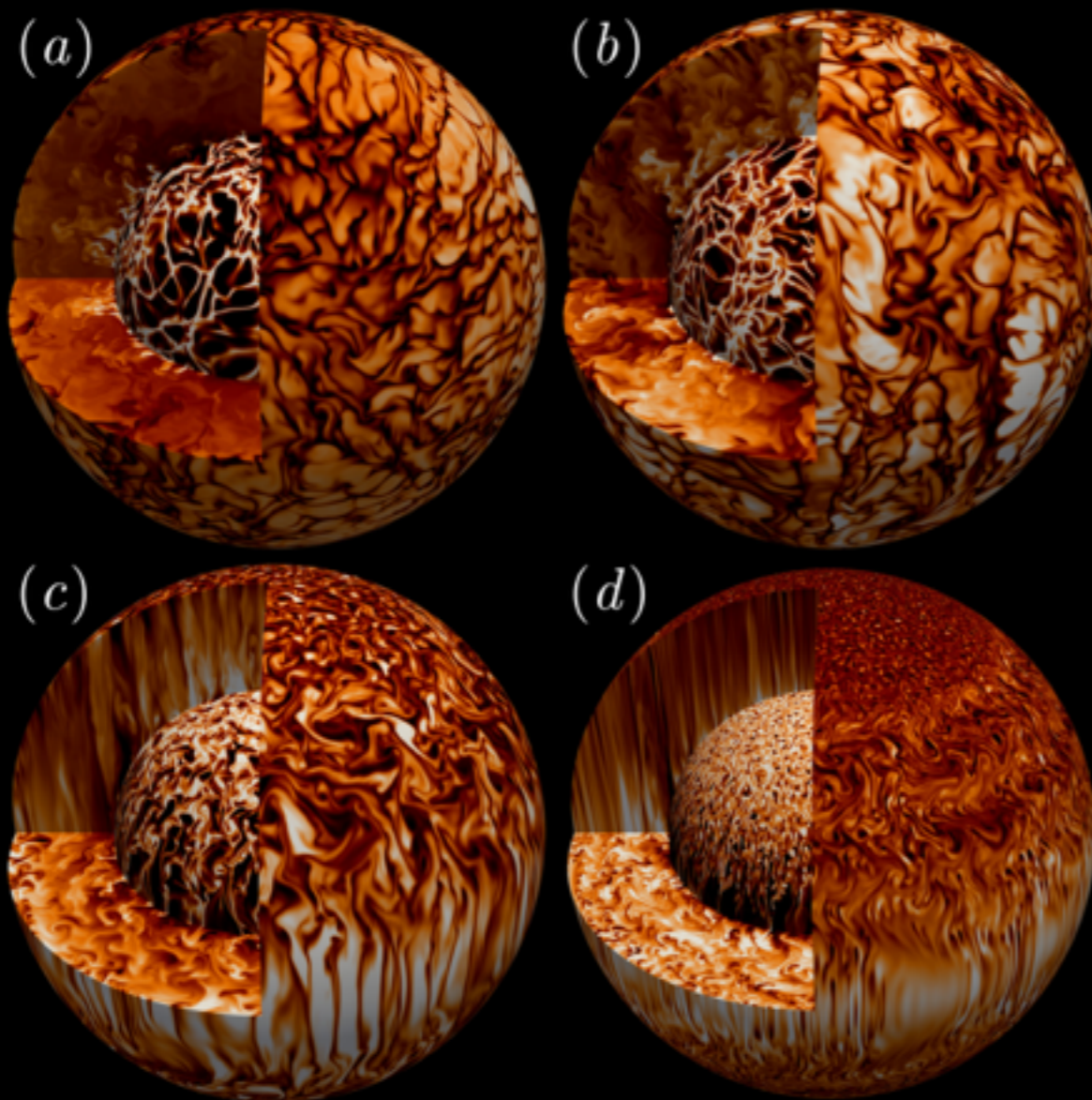
- 1) Theoretical Predictions for Convection
- 2) Numerical Convection Models
- 3) Boundary Layer Implications
- 4) Conclusions

Outline

- 1) Theoretical Predictions for Convection
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Influence of Rotation

- Diversity of dynamical regimes in rotating spherical shell Rayleigh-Bénard convection



- Temperature fluctuations (Gastine et al. 2016)

(a) *Non-rotating*

(b) *Weak rotational influence*

(c) *Moderate rotational influence*

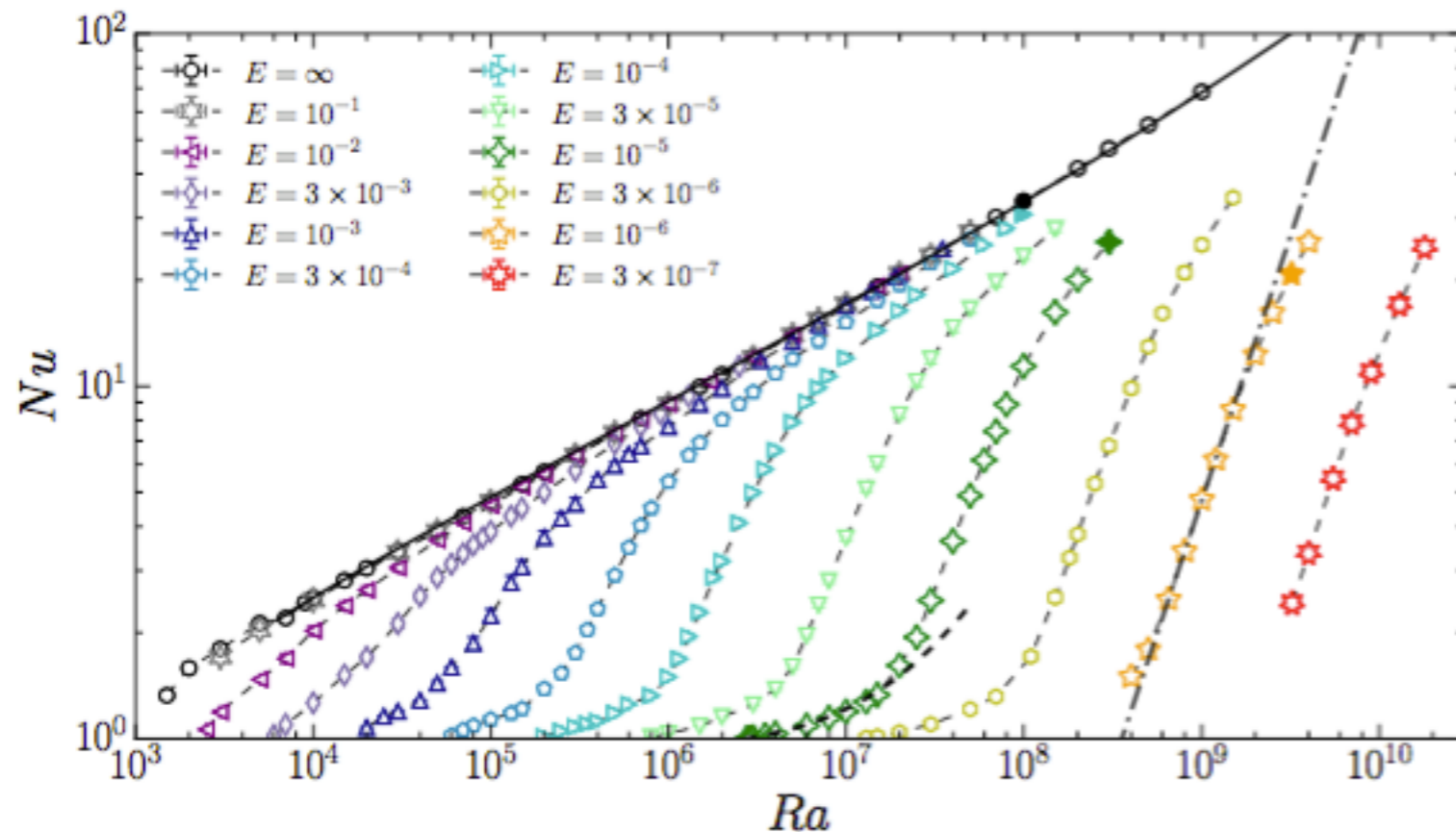
(d) *Stronger rotational influence*

Convective Regimes

- Gastine et al. (2016): Extensive suite of rotating spherical shell RBC models to study scaling behaviors

Convective Regimes

- Gastine et al. (2016): Extensive suite of rotating spherical shell RBC models to study scaling behaviors
 - Heat transfer efficiency (Nu) as a function of thermal forcing (Ra) and rotation rate (E)



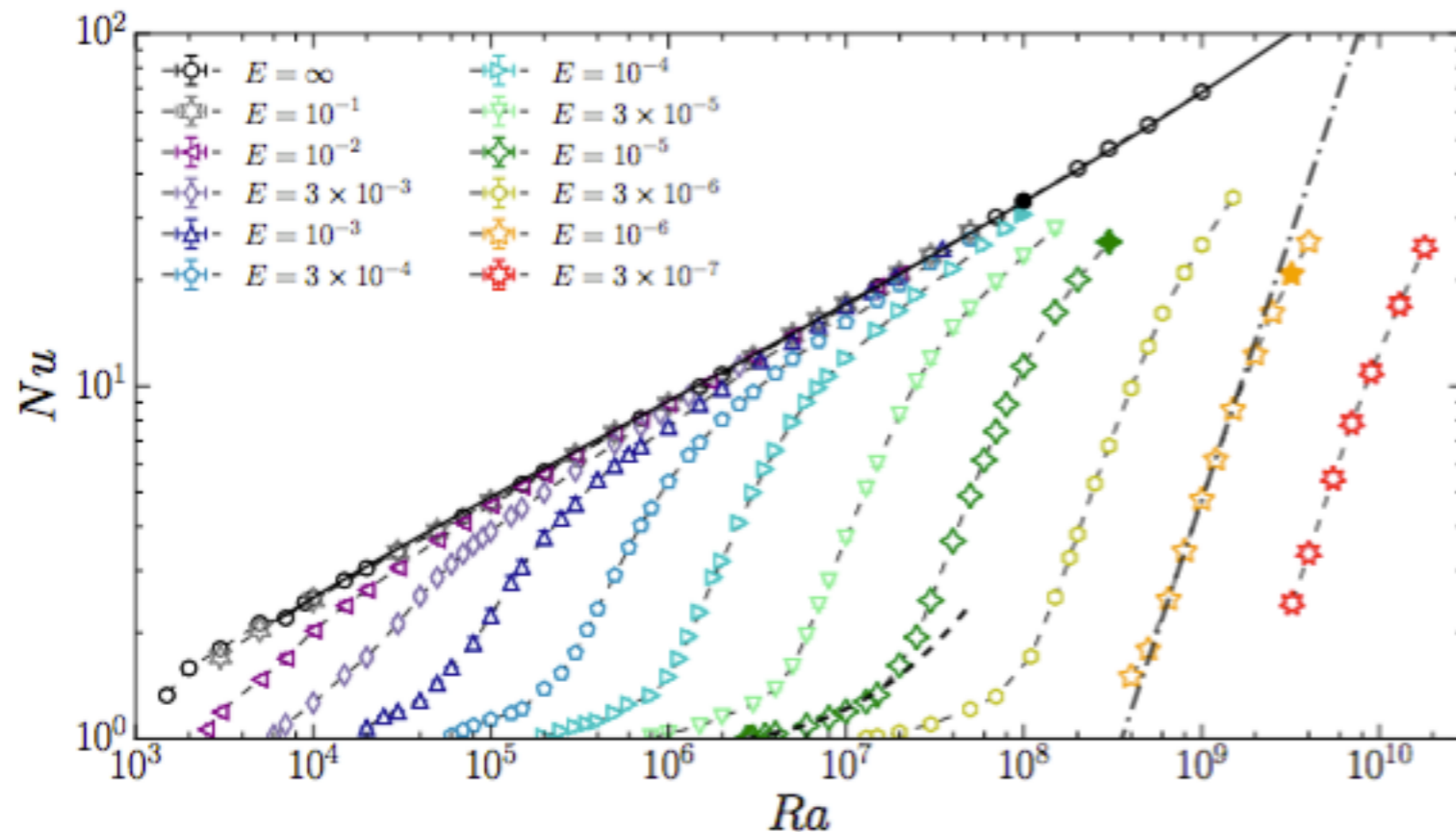
$$Nu = \frac{\text{Total heat flux}}{\text{Conductive heat flux}} = \frac{QD}{\rho C_p \kappa \Delta T}$$

$$Ra = \frac{\text{Buoyancy}}{\text{Diffusion}} = \frac{\alpha g_o \Delta T D^3}{\nu \kappa}$$

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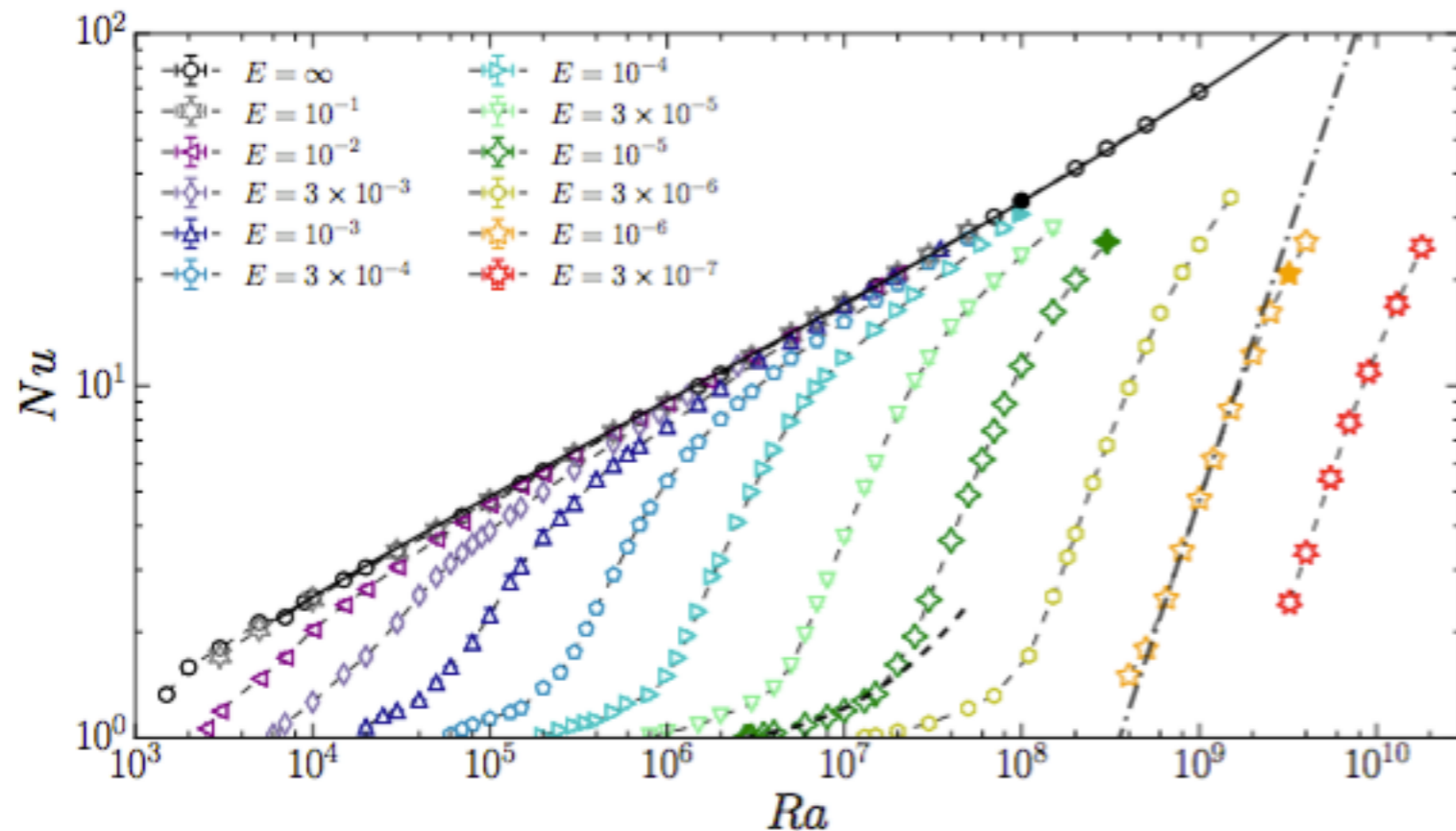
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$$Nu - 1 = 0.08(Ra/Ra_c - 1)$$

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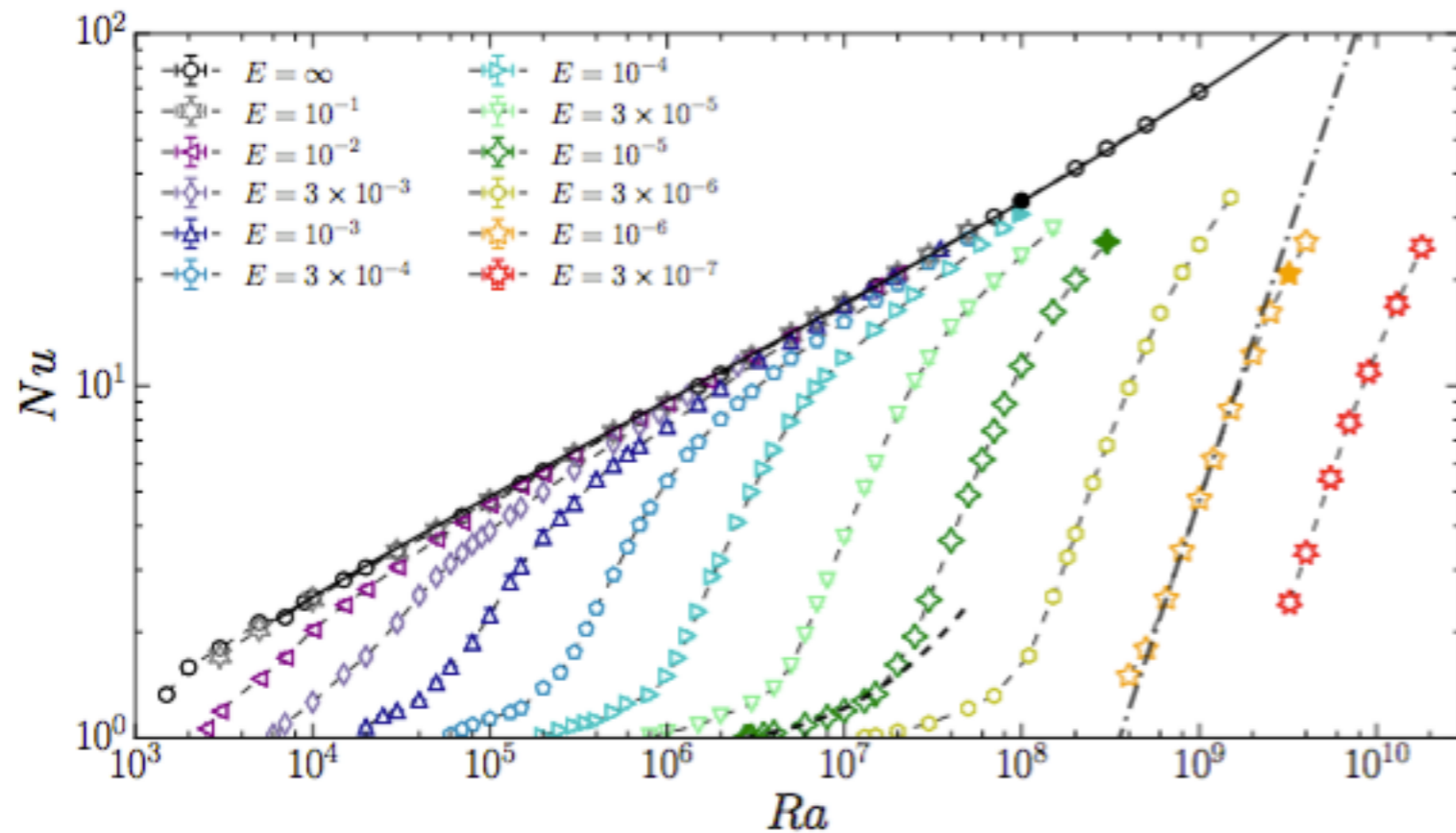
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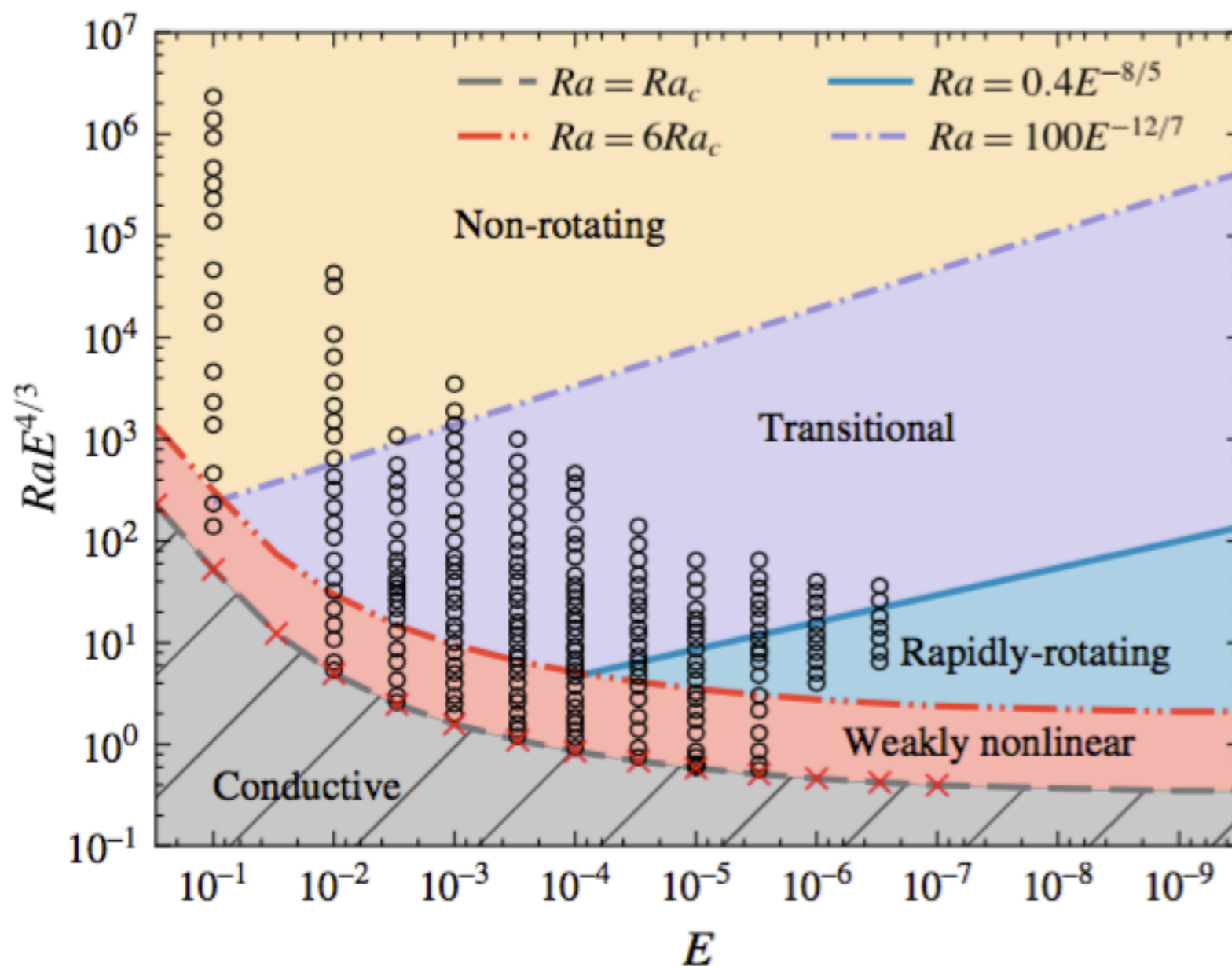
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$$Nu = 0.07 Ra^{1/3}$$

Convective Regime Transitions

- Convective regimes and their predicted boundaries

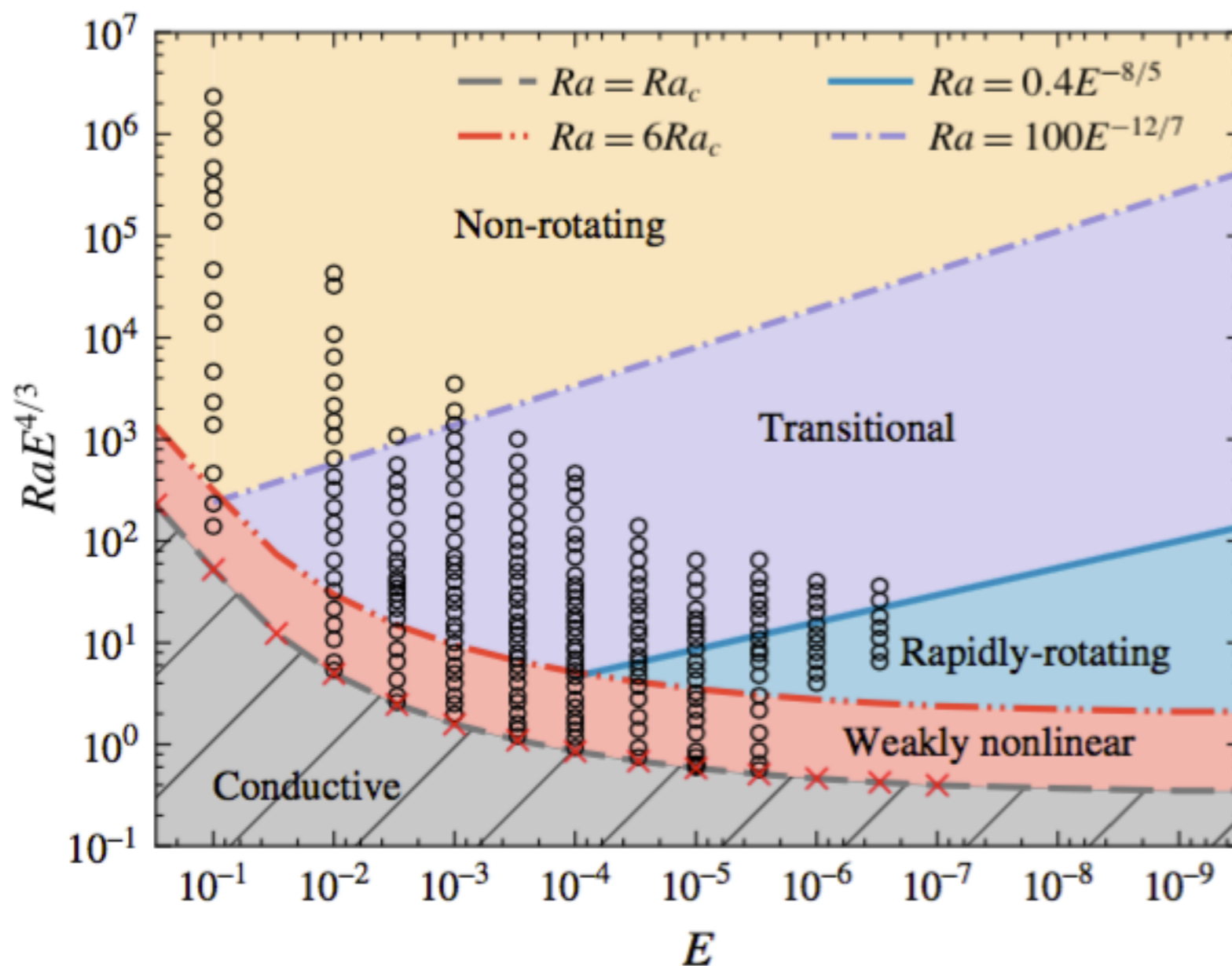


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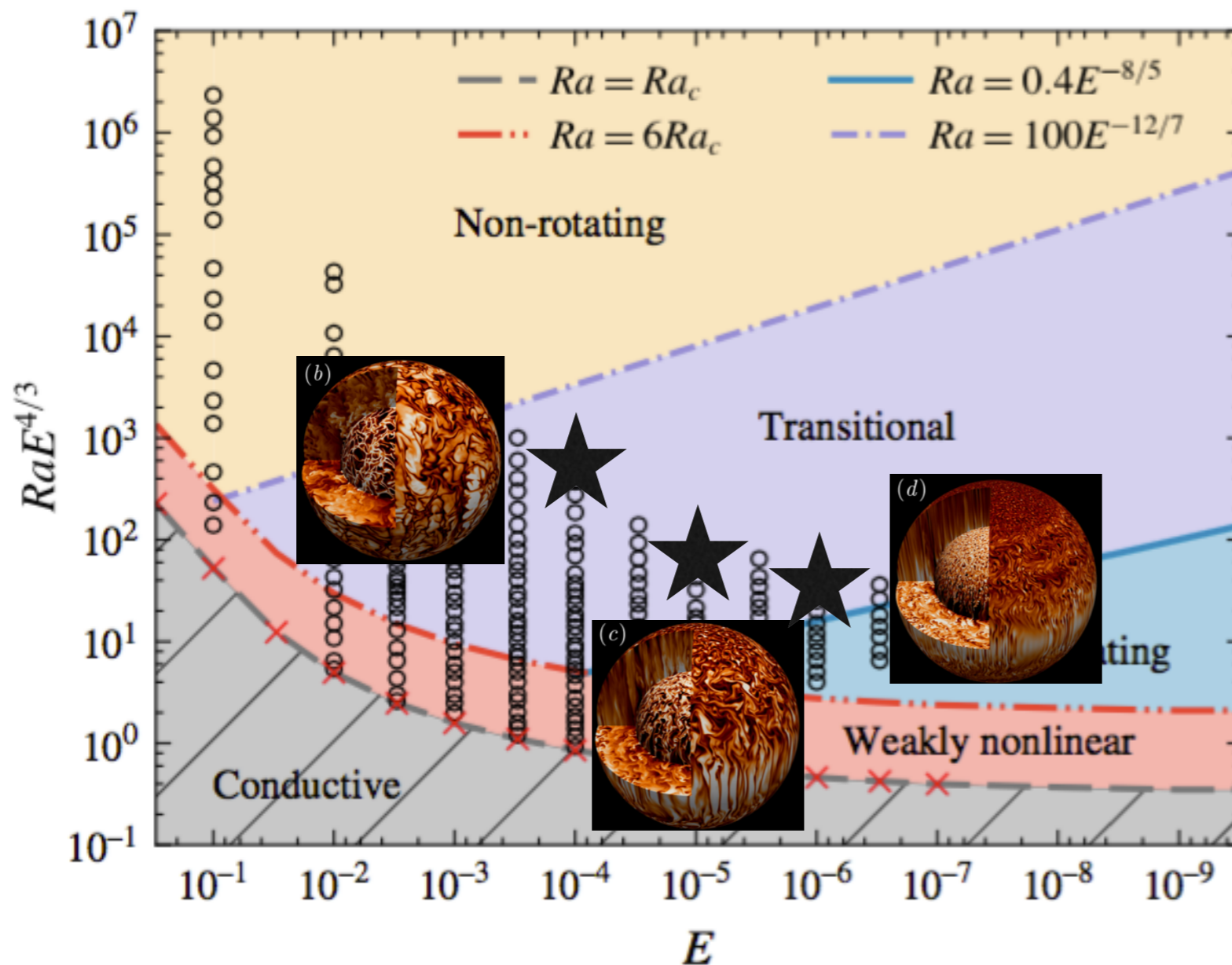
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Intersection between shallow and steep $Nu-Ra$ scalings

Convective Rossby number of the thermal BL is less than unity (Julien et al. 2012)

Convective Regime Transitions

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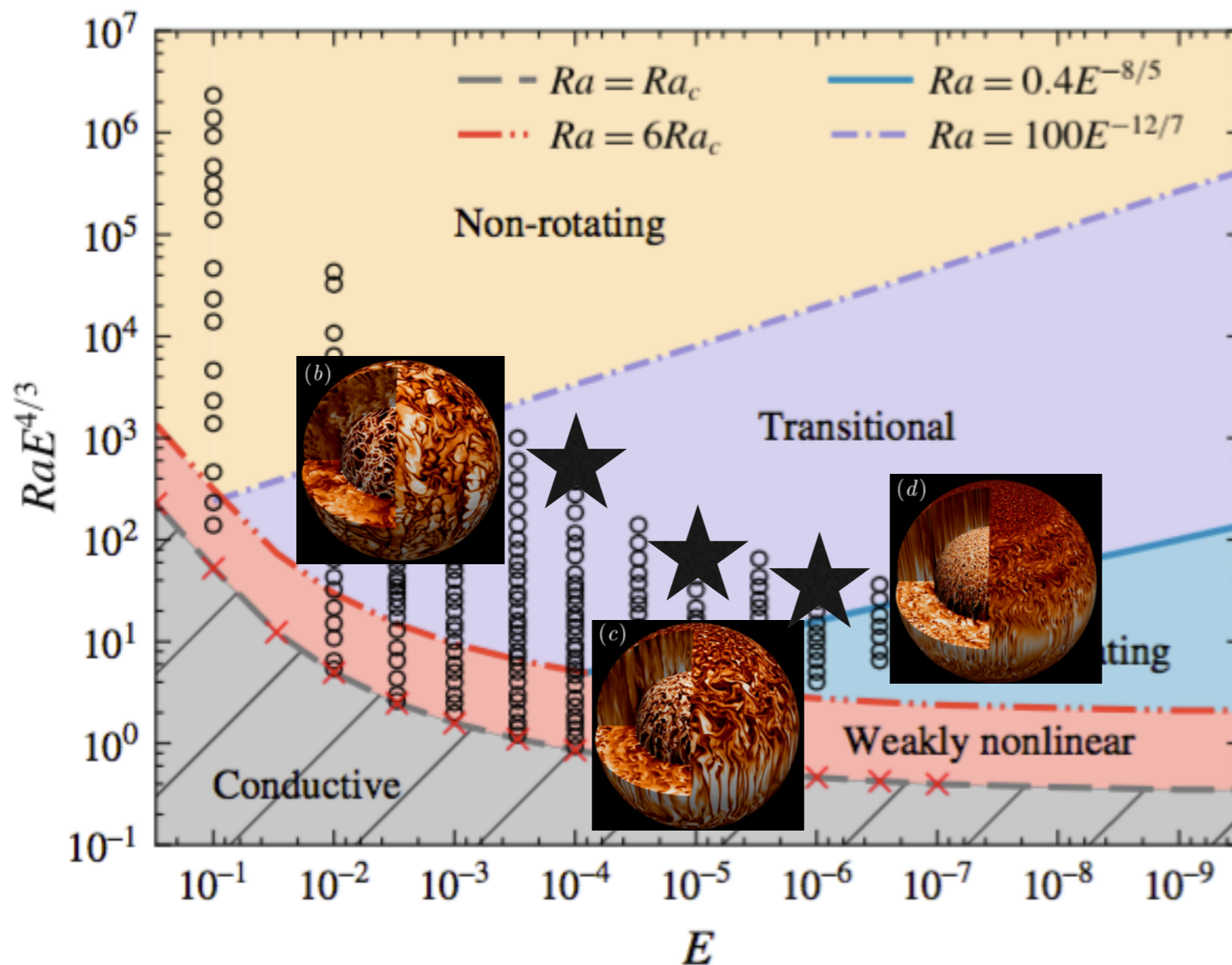
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Convective Regime Predictions

- Application to icy ocean worlds



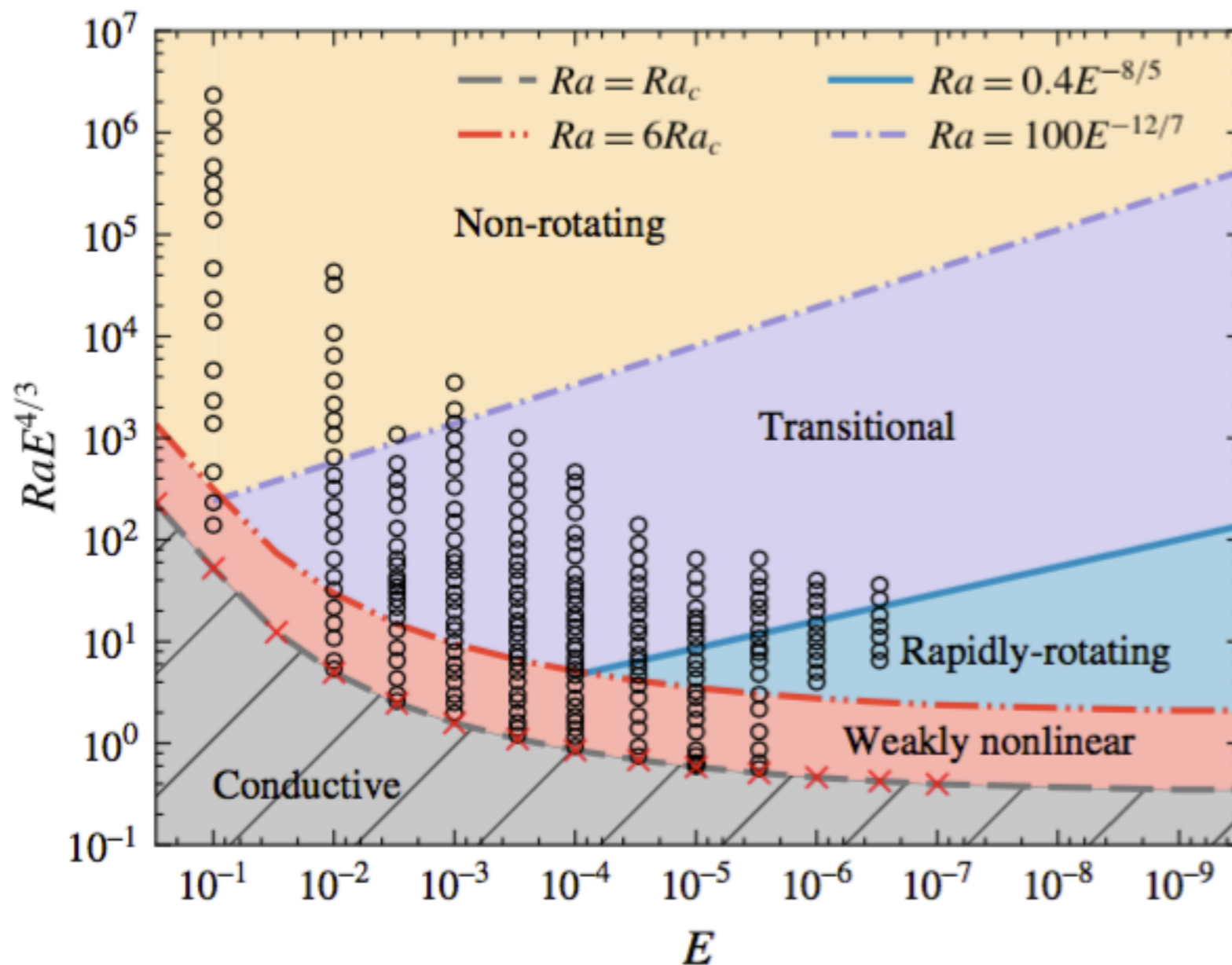
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Ekman number is easy to estimate

Convective Regime Predictions

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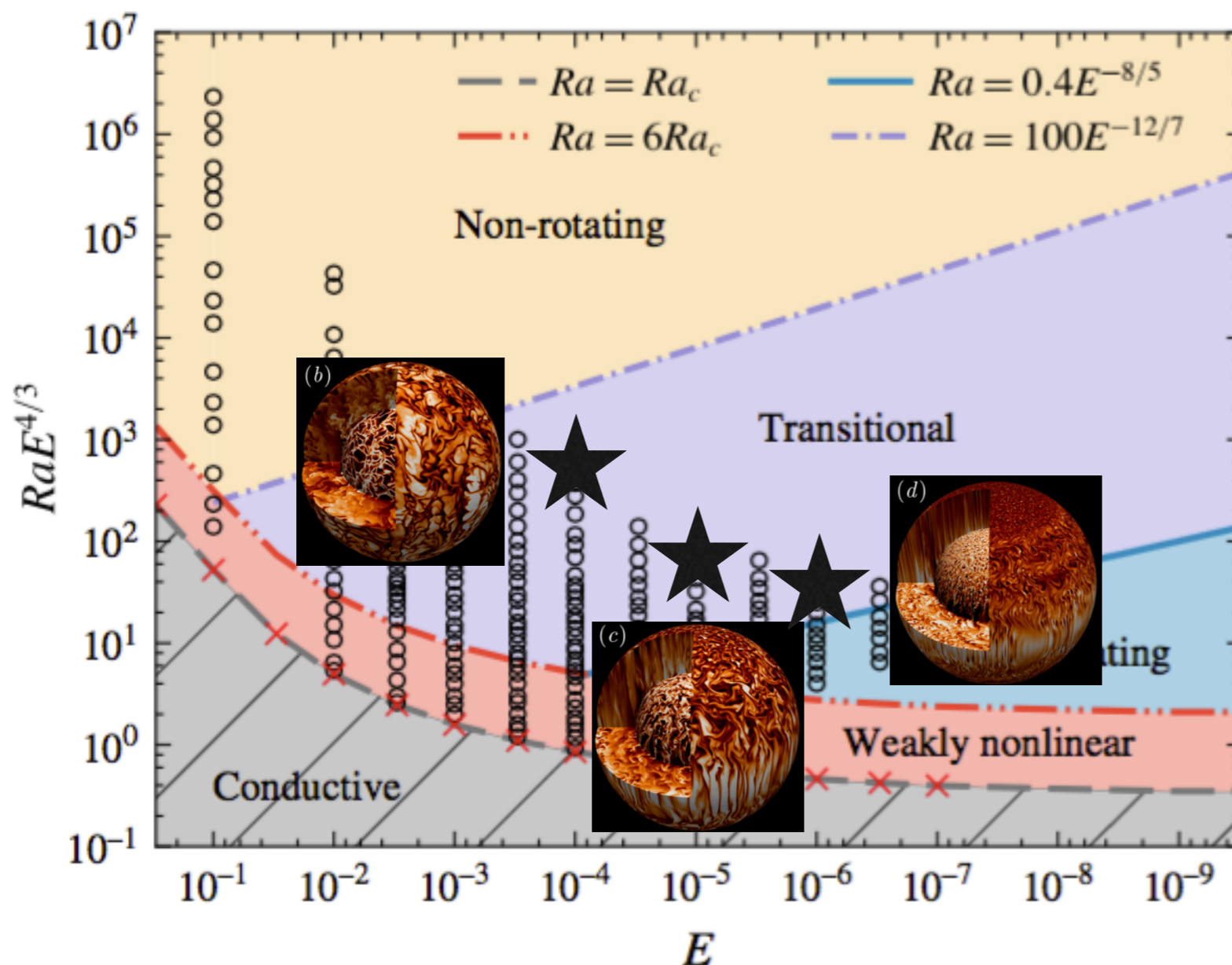
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Rayleigh number is harder to estimate

Convective Regime Predictions

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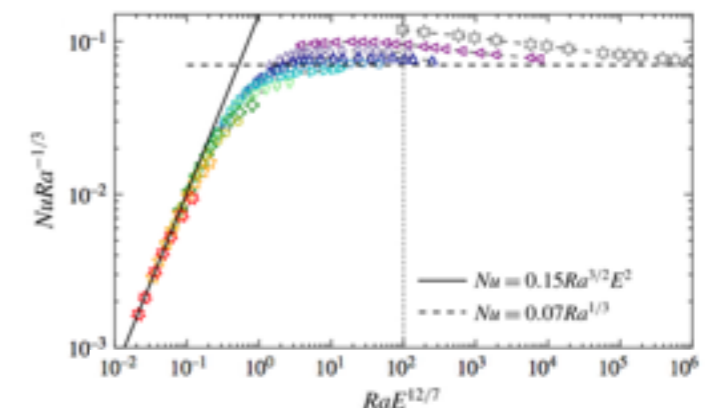


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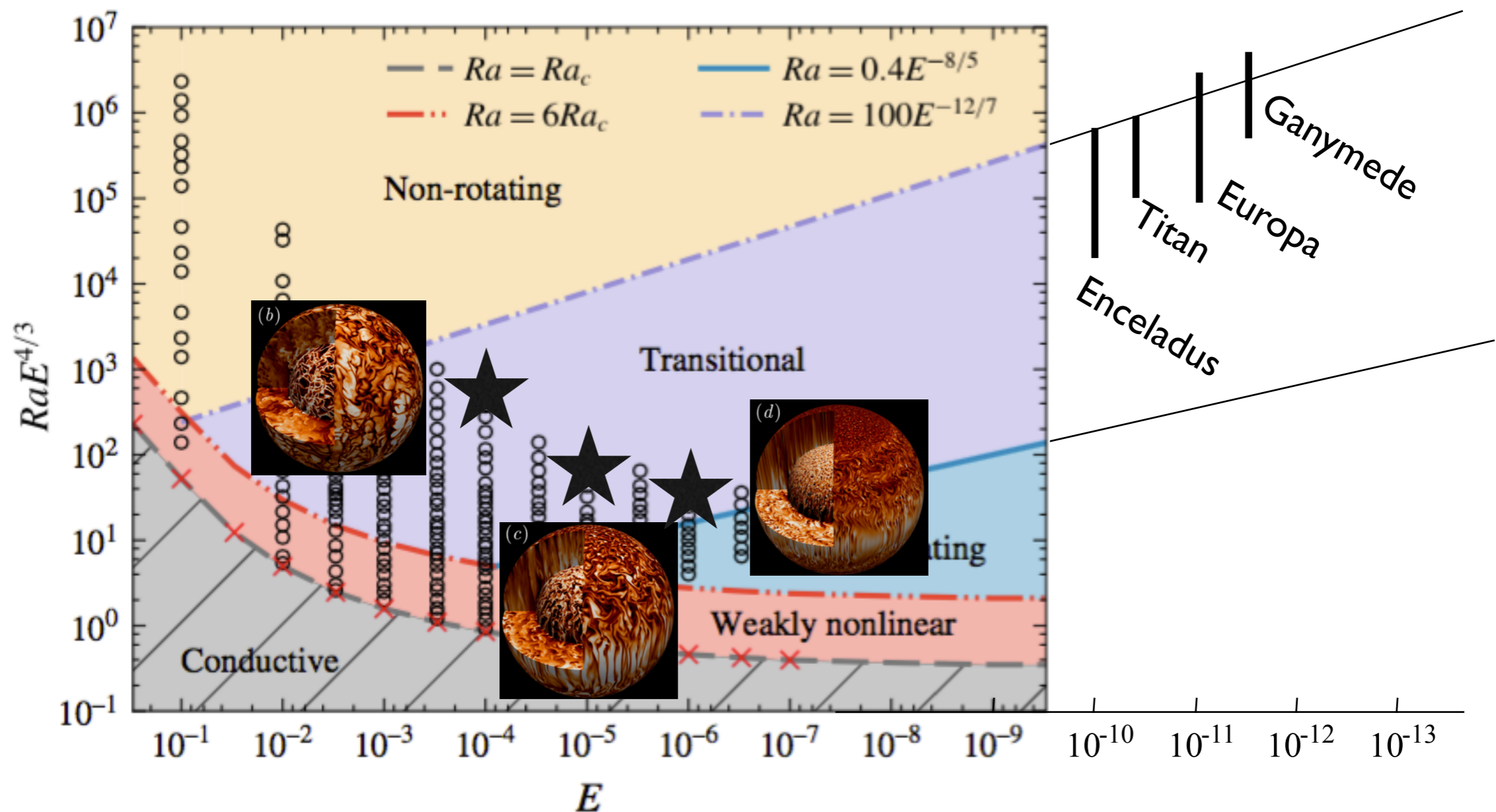
$$Nu = \frac{\text{Total heat flux}}{\text{Conductive heat flux}} = \frac{QD}{\rho C_p \kappa \Delta T}$$

Rayleigh number is harder to estimate, use Nu - Ra scalings



Convective Regime Predictions

- Weak rotational influence predicted for their oceans

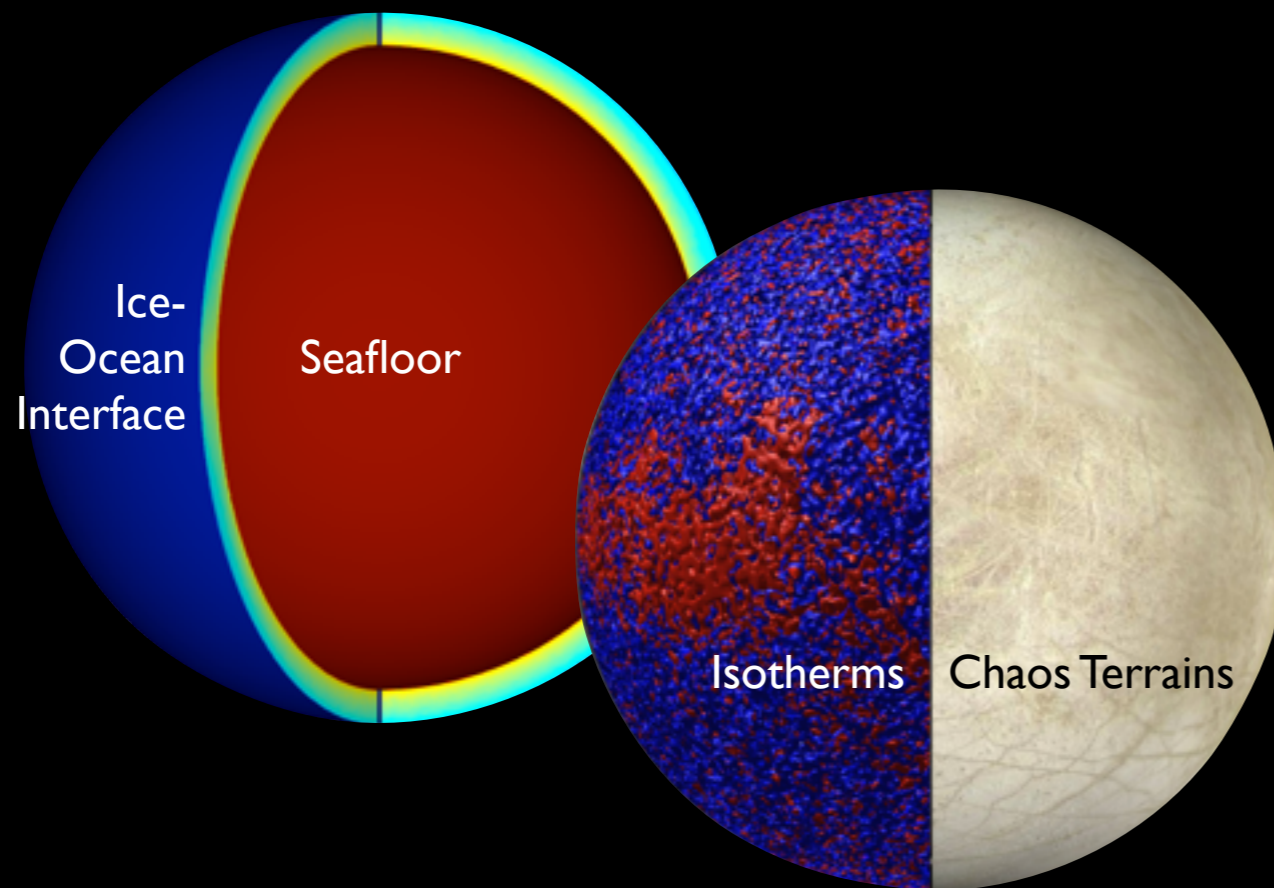


Outline

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Motivation

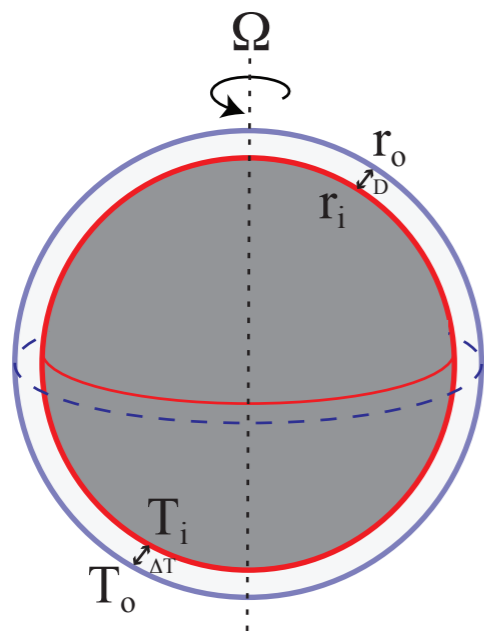
- Numerical models of global ocean convection



- ➔ How does the mantle influence the ocean?
- ➔ How does the ocean influence the ice shell?

Numerical Model: MagIC

- Numerical models of global ocean convection
- Boussinesq thermal convection in a rotating spherical shell (ocean tides and salinity gradients are not considered)

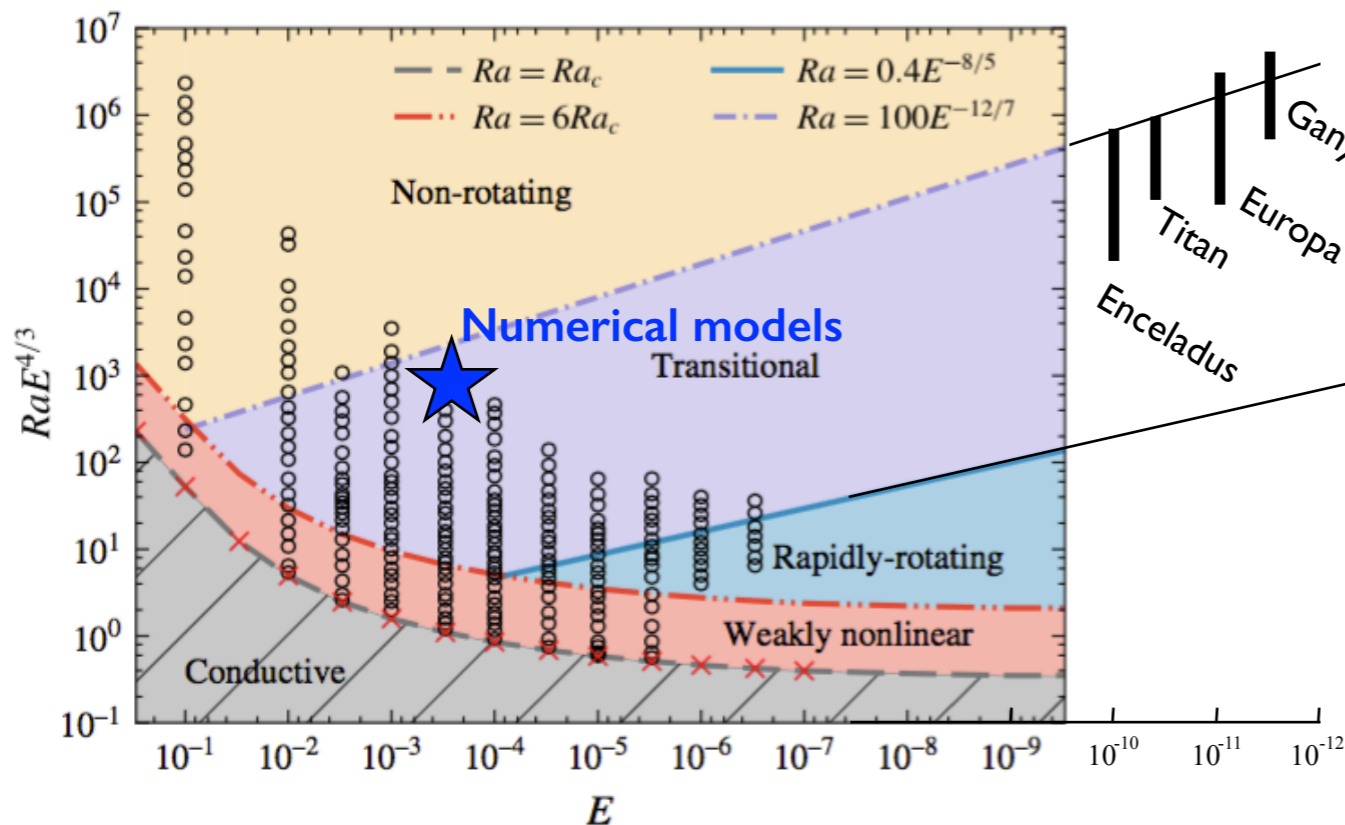


$$E \left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} - \nabla^2 \mathbf{u} \right) + \hat{\mathbf{z}} \times \mathbf{u} + \frac{1}{2} \nabla \Pi = \frac{RaE}{Pr} \frac{\mathbf{r}}{r_o} T$$

$$\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T = \frac{1}{Pr} \nabla^2 T \quad \nabla \cdot \mathbf{u} = 0$$

Numerical Model: MagIC

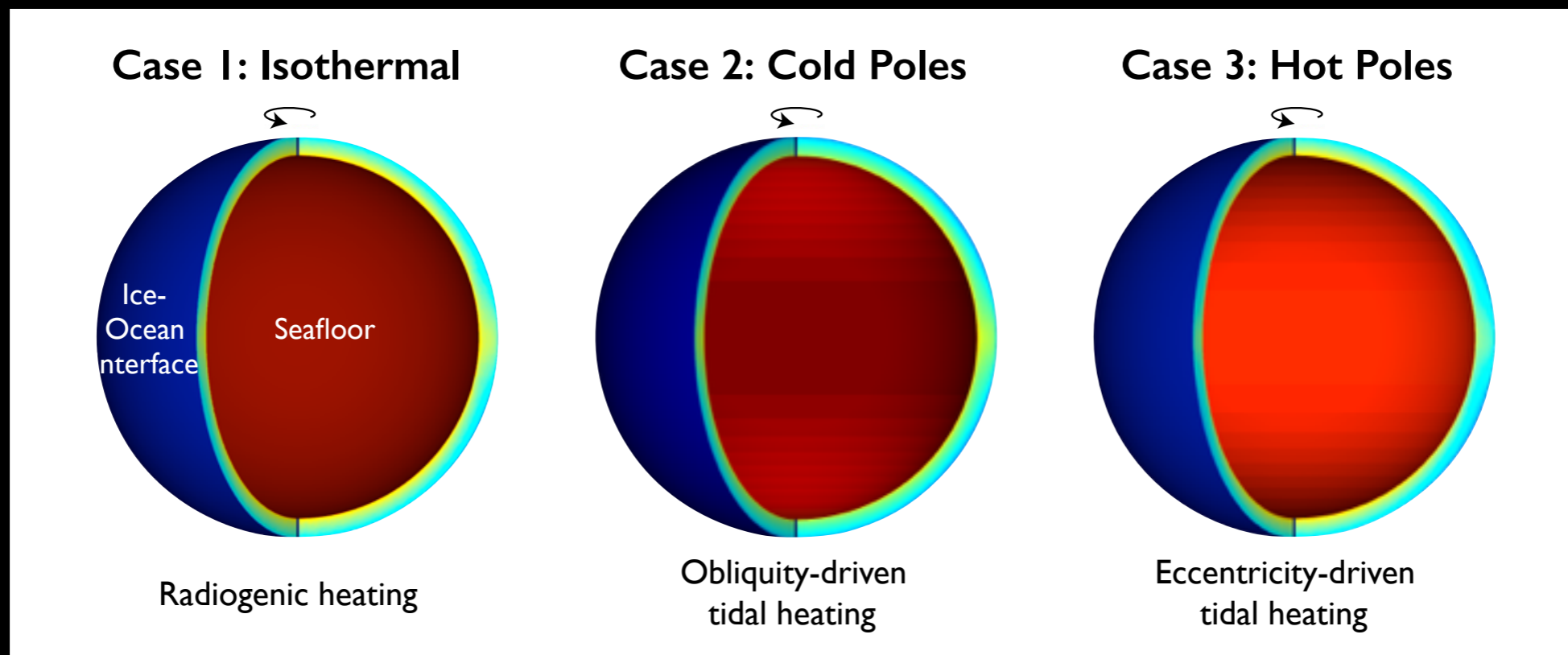
- Numerical models of global ocean convection
 - Boussinesq thermal convection in a rotating spherical shell (ocean tides and salinity gradients are not considered)
 - Transitional regime chosen a priori



Definition	Interpretation	Model
$\chi = r_i/r_o$	Shell geometry	0.9
$E = \frac{\nu}{\Omega D^2}$	$\frac{\text{Viscous force}}{\text{Coriolis force}}$	3.0×10^{-4}
$Pr = \frac{\nu}{\kappa}$	$\frac{\text{Viscous diffusivity}}{\text{Thermal diffusivity}}$	1
$Ra = \frac{\alpha g \Delta T D^3}{\nu \kappa}$	$\frac{\text{Buoyancy}}{\text{Diffusion}}$	3.4×10^7

Numerical Model: MagIC

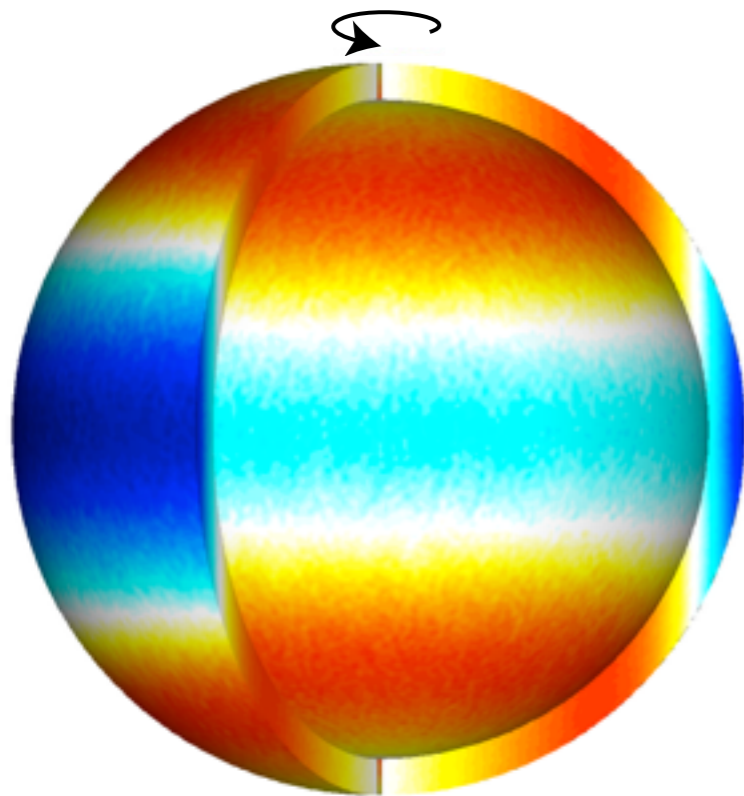
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 - Transitional regime chosen a priori
 - Three mantle heat flow patterns imposed



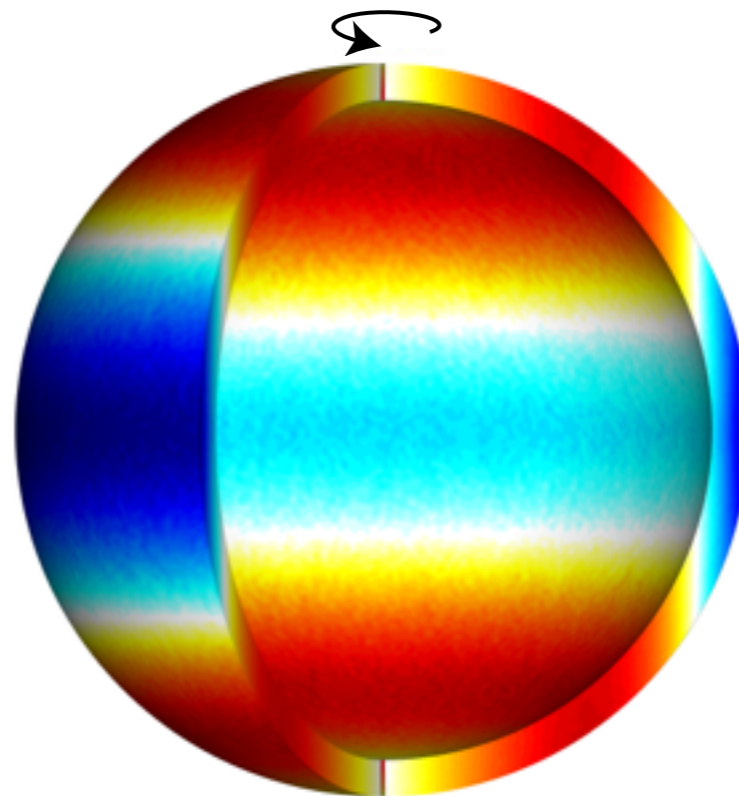
Steady Zonal Ocean Currents

- Three zonal jets develop with retrograde eqtr. flow

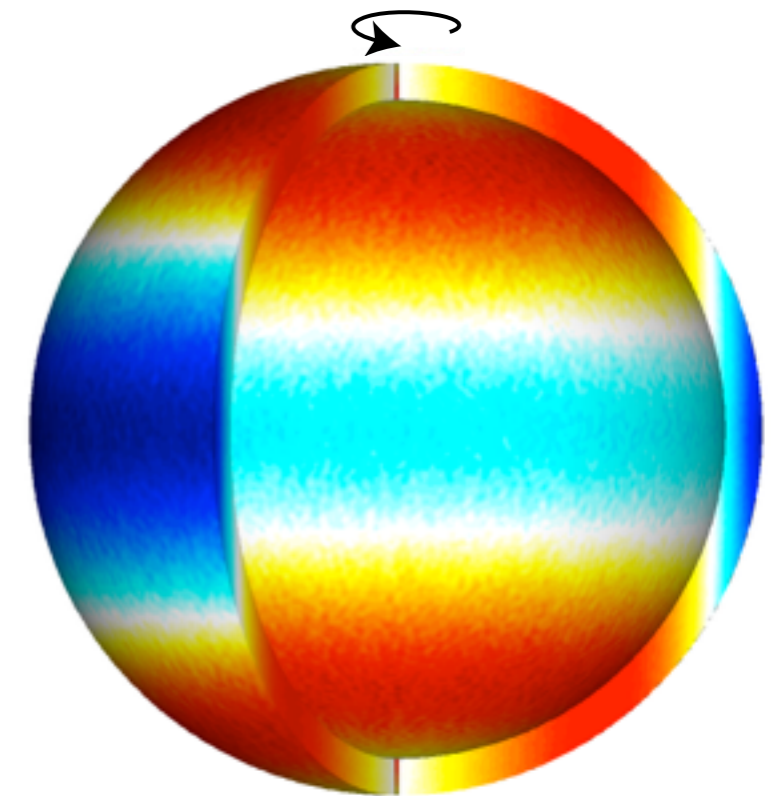
Case 1: Isothermal



Case 2: Cold Poles



Case 3: Hot Poles



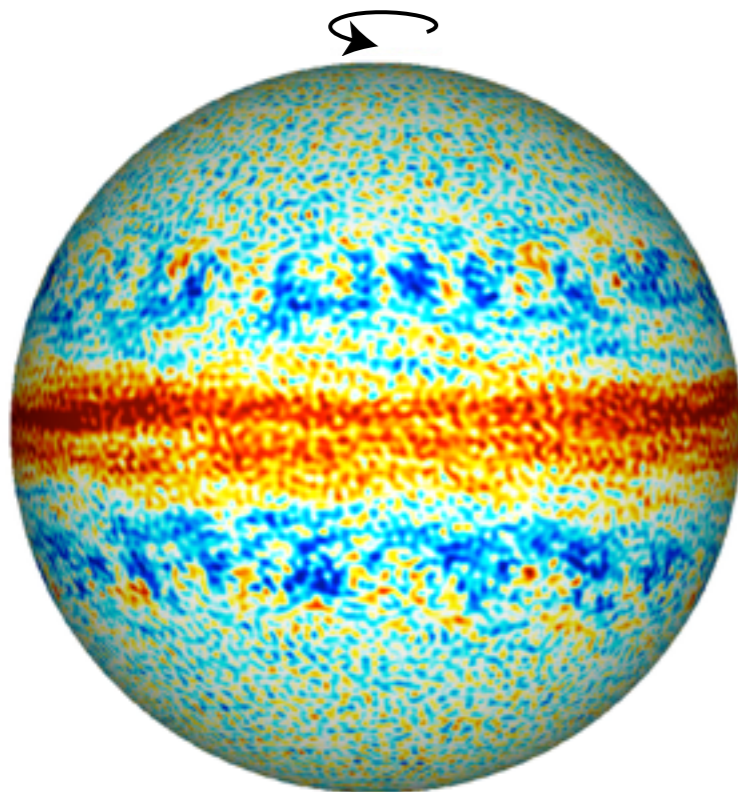
-6000  6000

Reynolds number, $Re = UD/\nu$

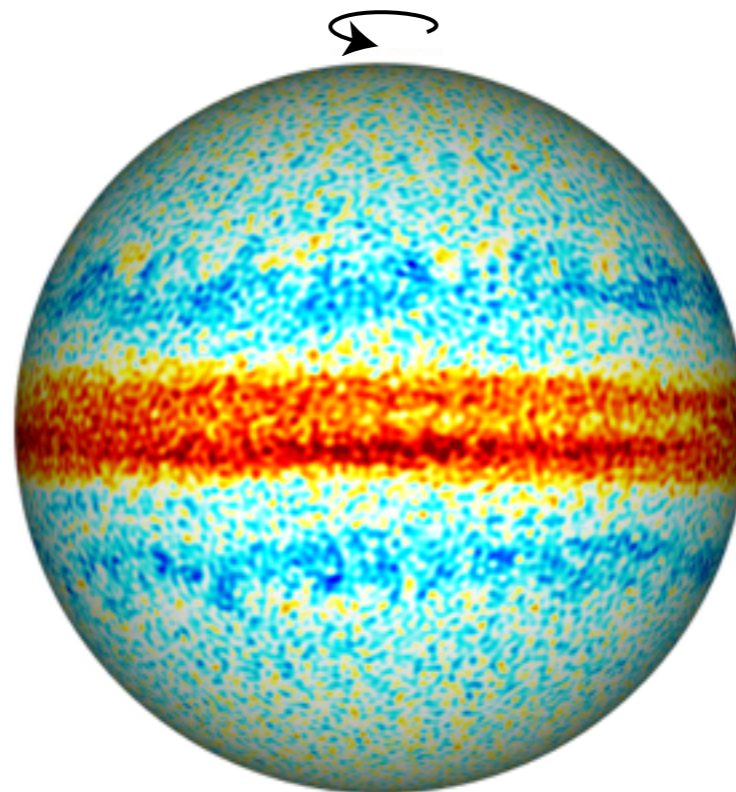
Steady Radial Ocean Currents

- Strong upwelling develops at low latitudes

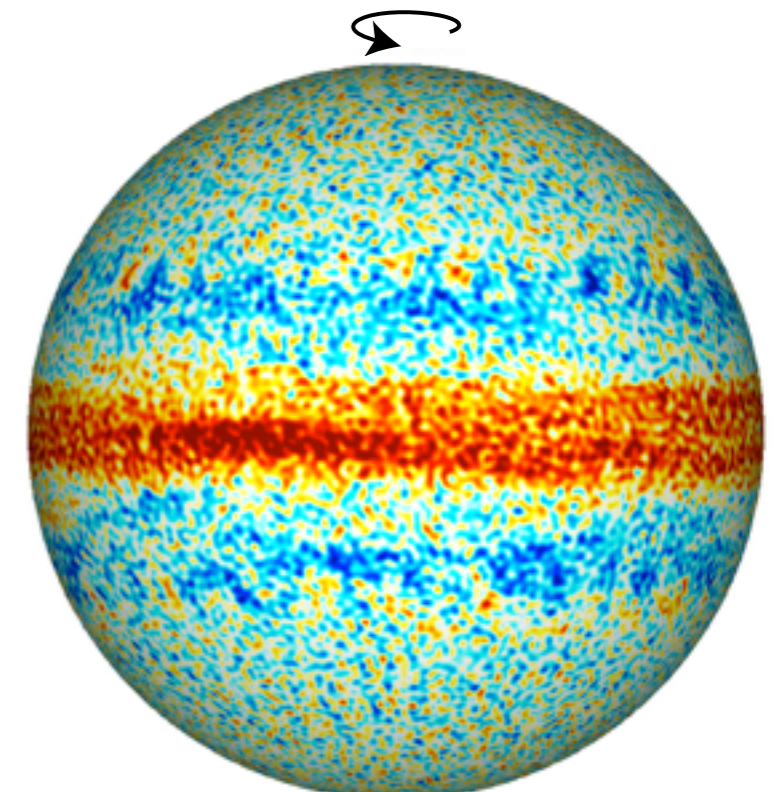
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Case 3: Hot Poles



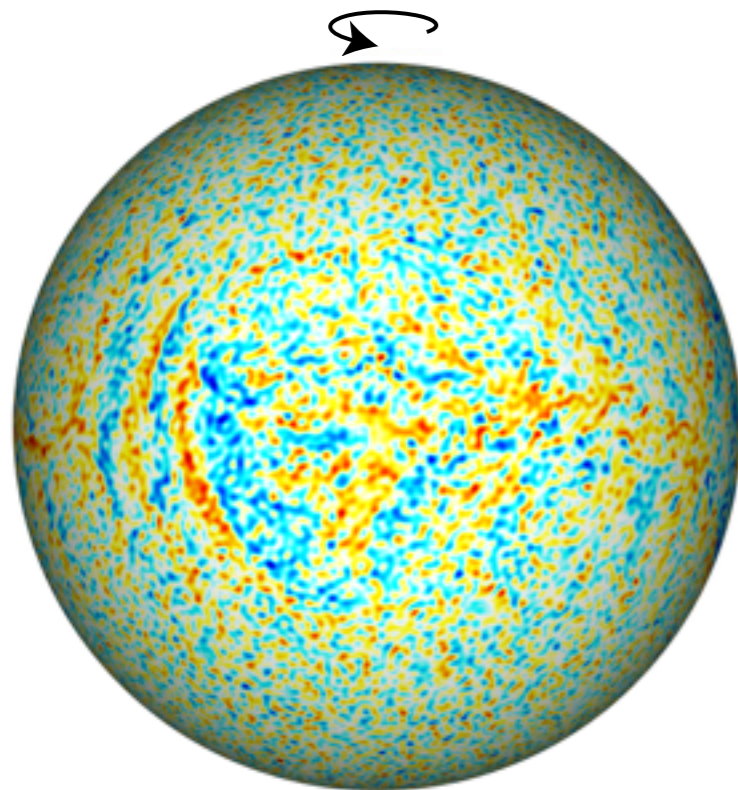
-200  200

Reynolds number, $Re = UD/\nu$

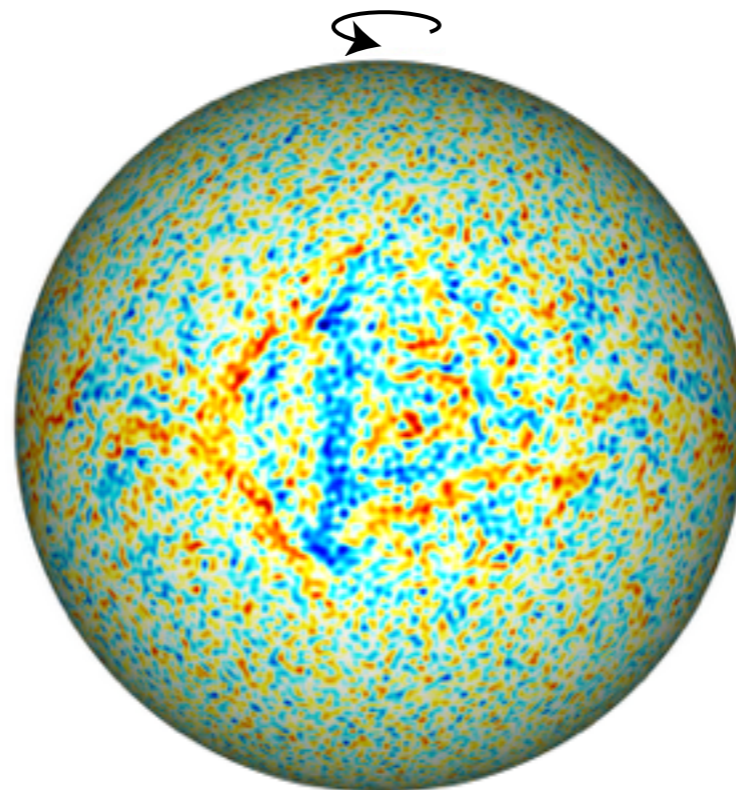
Radial Ocean Currents

- Instantaneous radial velocity is faster, smaller scale

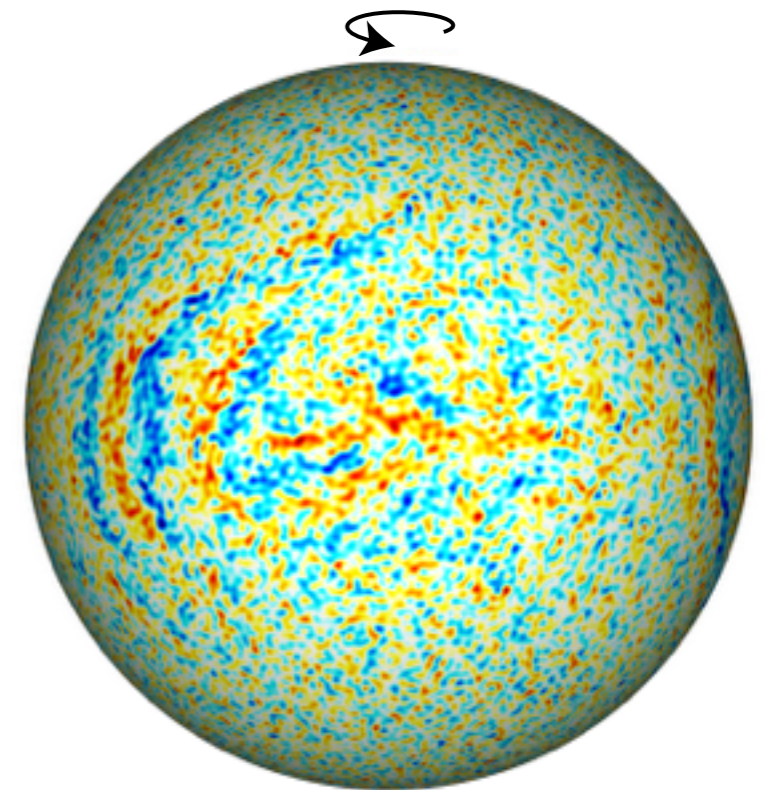
Case 1: Isothermal




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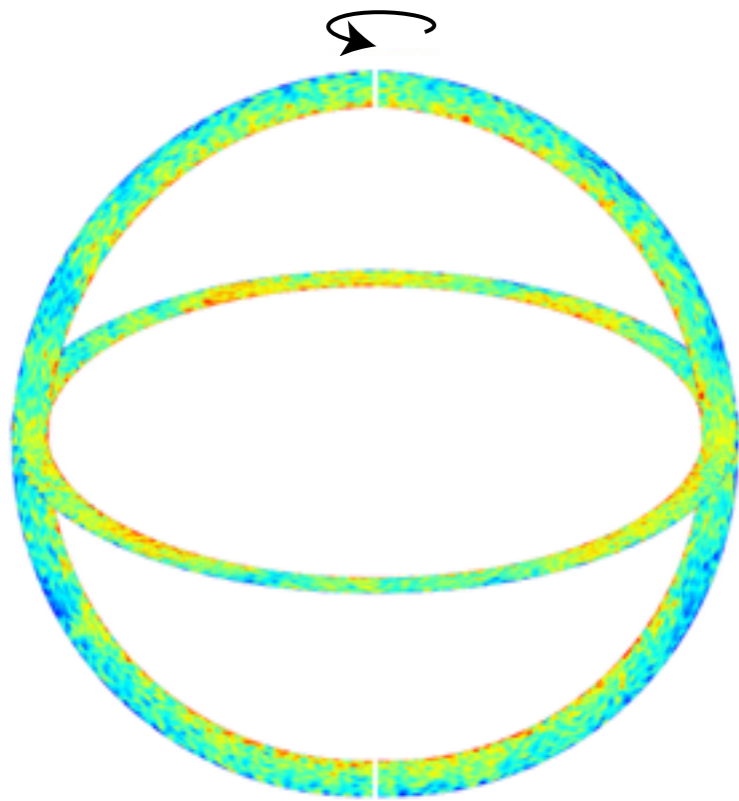
-3000  3000

Reynolds number, $Re = UD/\nu$

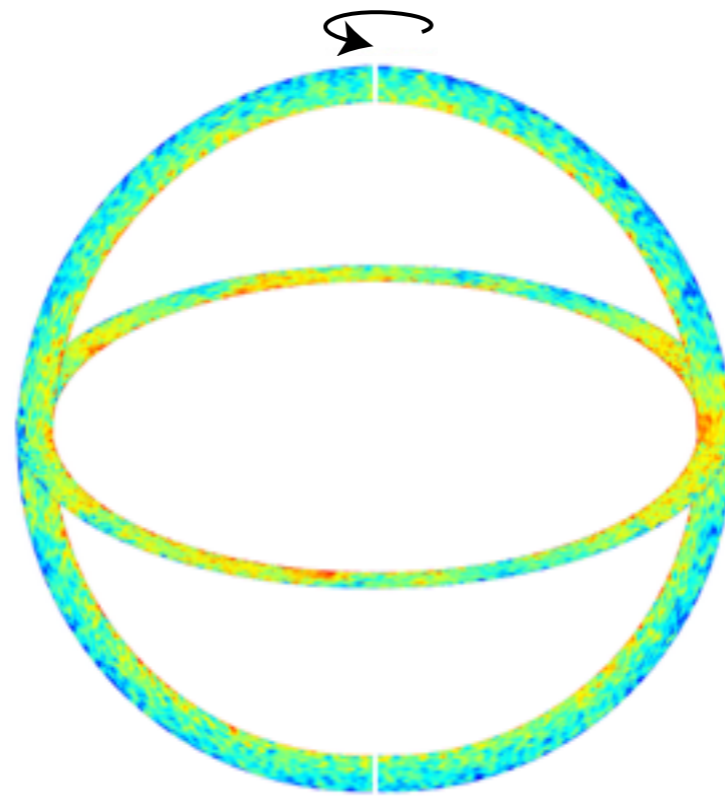
Temperature

- Thermal plumes are mixed into the bulk ocean

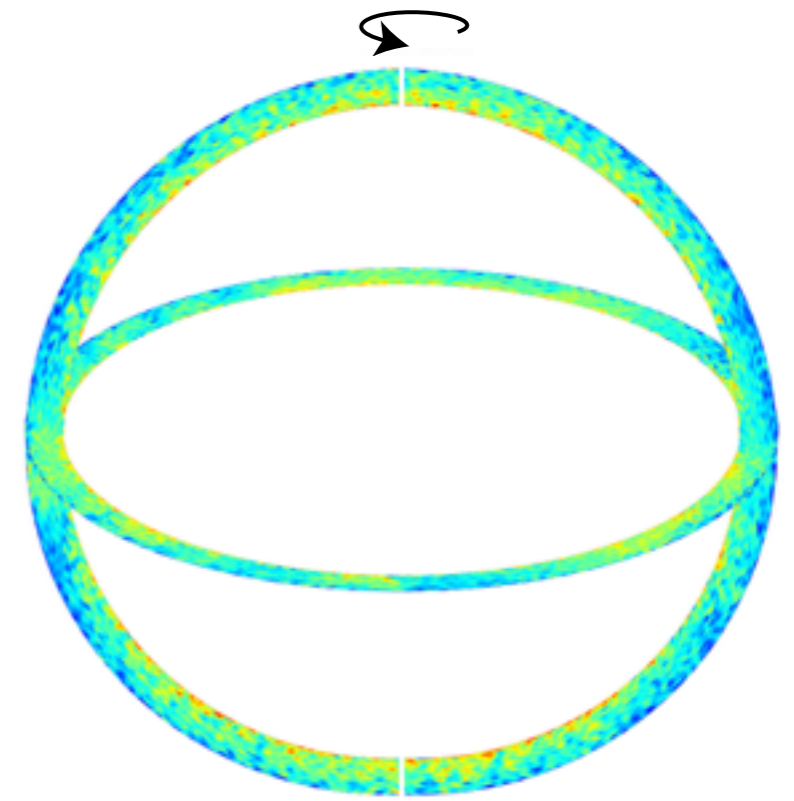
Case 1: Isothermal

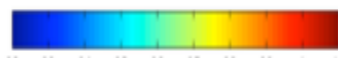


Case 2: Cold Poles



Case 3: Hot Poles

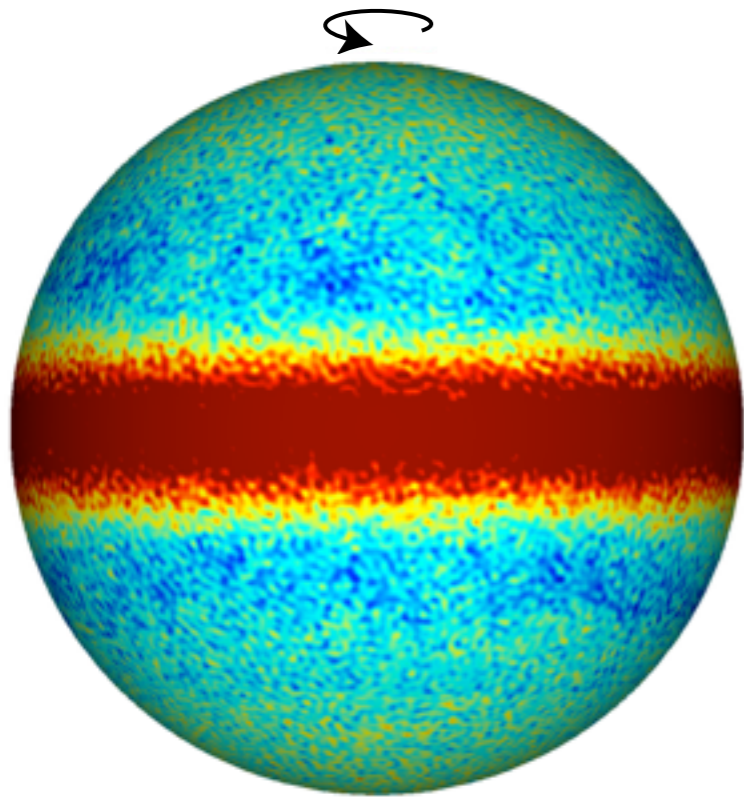


T_0  $T_0 + \Delta T$

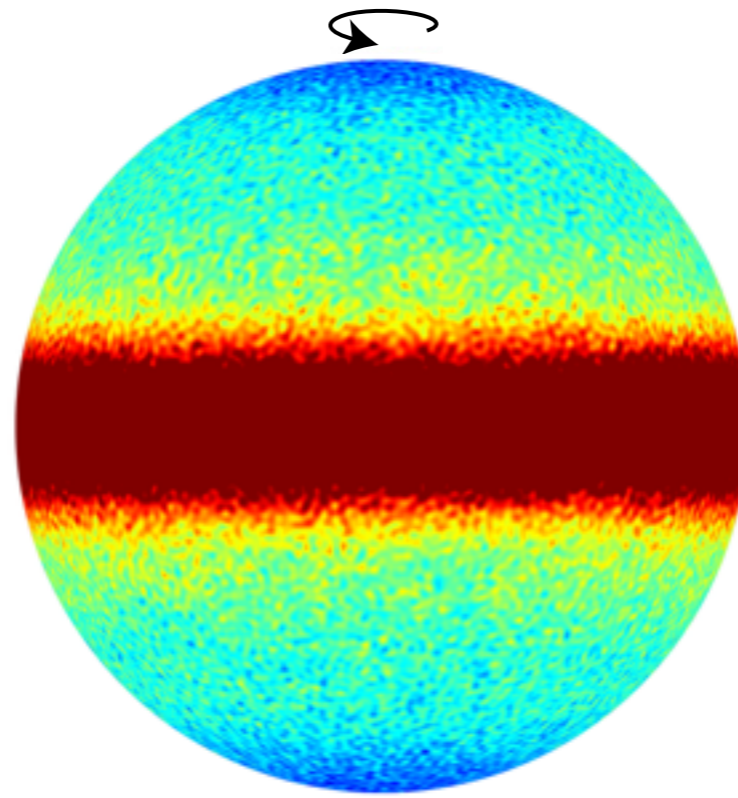
Convective Heat Transfer

- Ice-ocean interface heat flux peaks near equator, pattern mimics the mantle heat flow at high latitudes

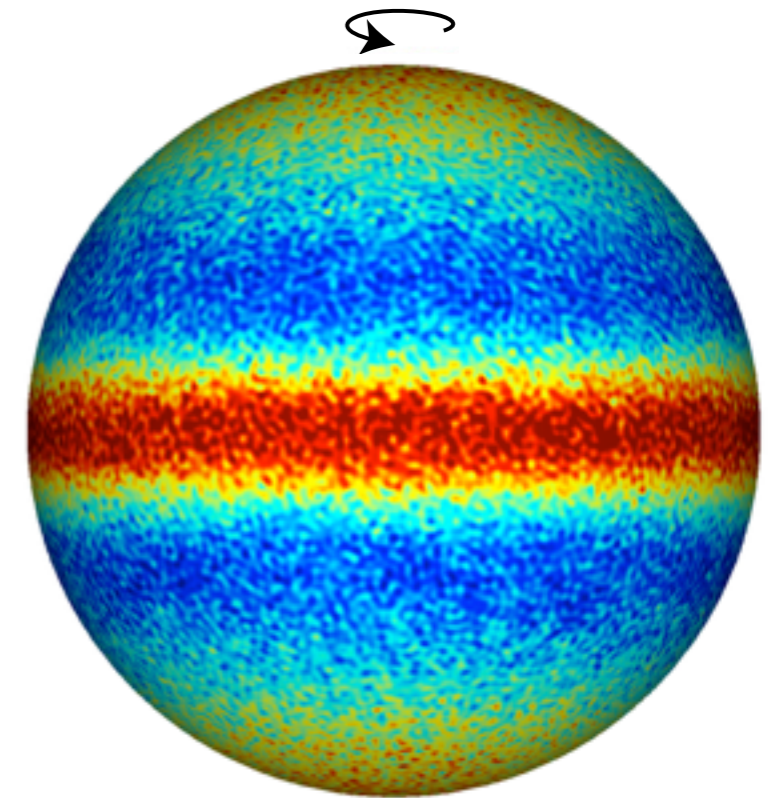
Case 1: Isothermal



Case 2: Cold Poles



Case 3: Hot Poles



0.75  1.25

Convective Heat Transfer

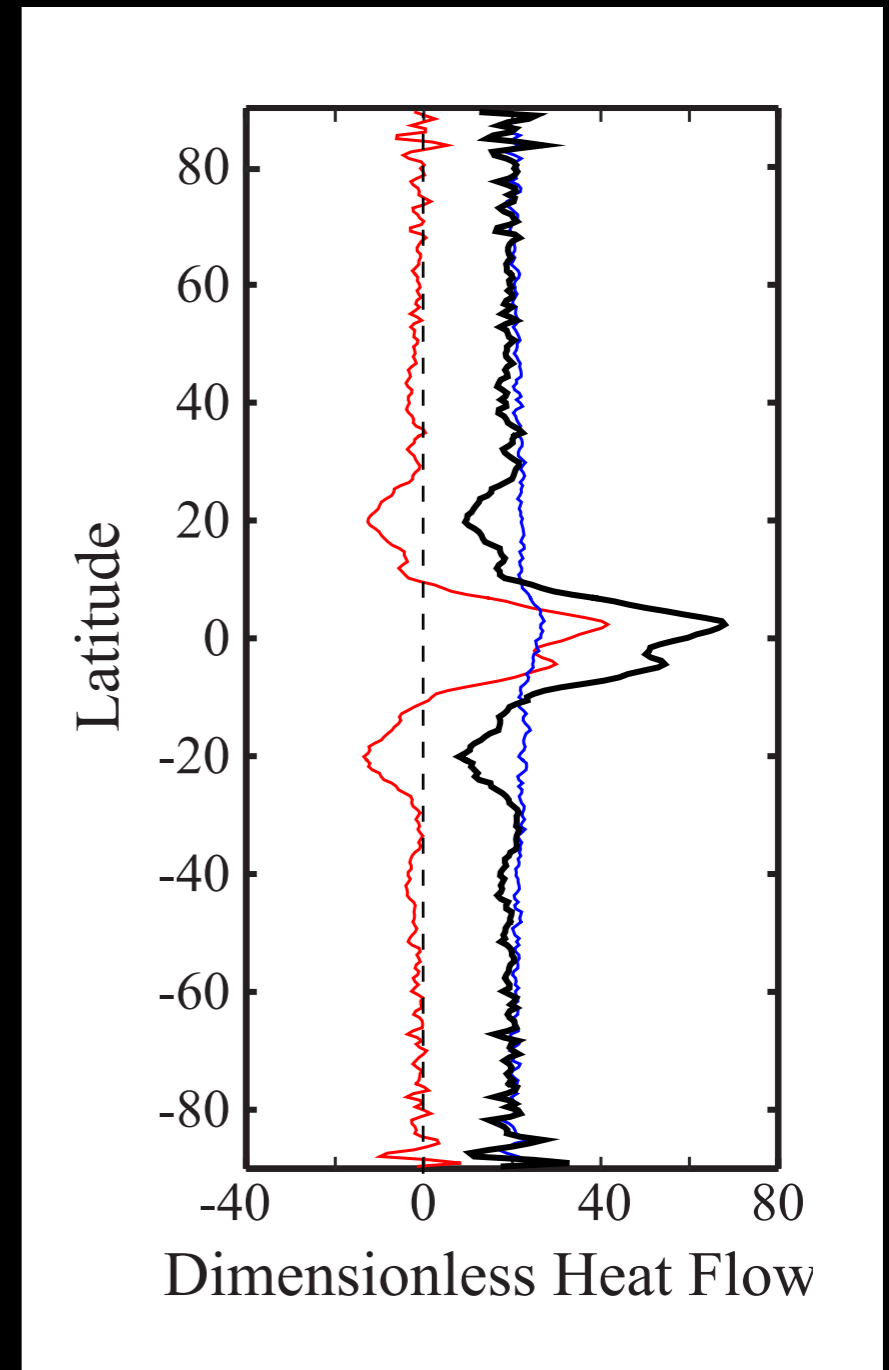
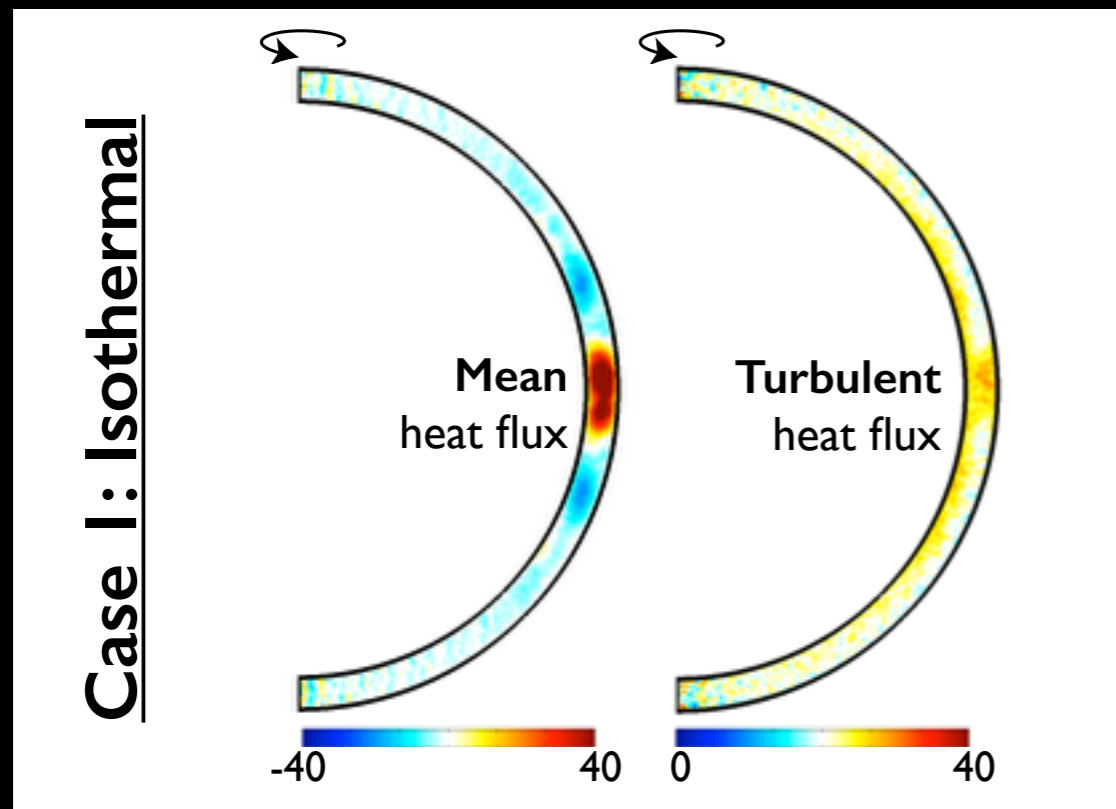
- Heat flux decomposition: total = mean + turbulent
 - *Mean* heat flux due to meridional overturning circulations
 - *Turbulent* heat flux due to fluctuating motions

$$\underbrace{\overline{\langle V_r T \rangle}}_{\text{Total}} = \underbrace{\overline{\langle \bar{V}_r \bar{T} \rangle}}_{\text{Mean}} + \underbrace{\overline{\langle V_r' T' \rangle}}_{\text{Turbulent}} \quad (\text{All variables are dimensionless})$$

(Overbars denote temporal averages; primes denote fluctuations from the mean; brackets denote spatial averages)

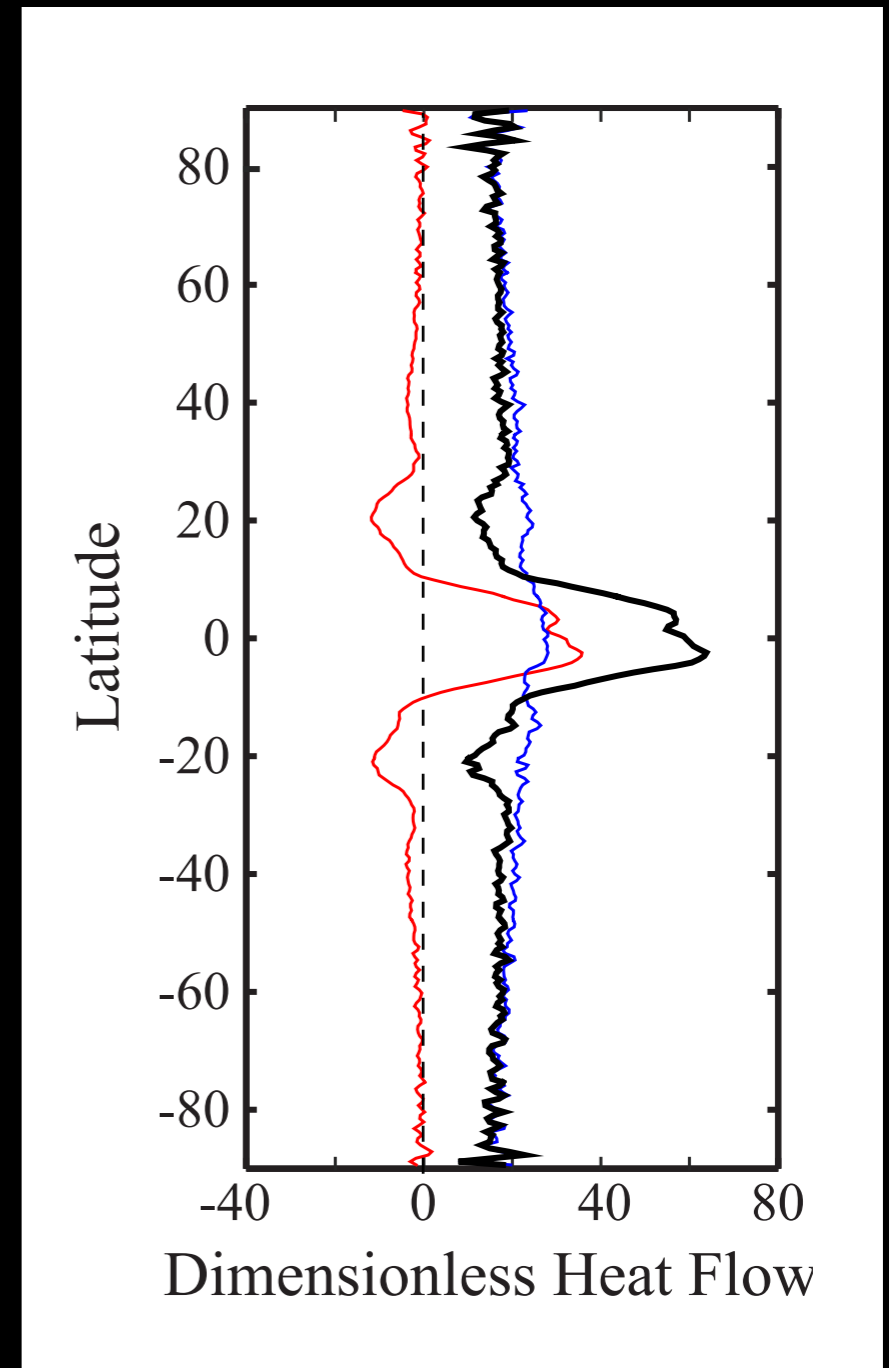
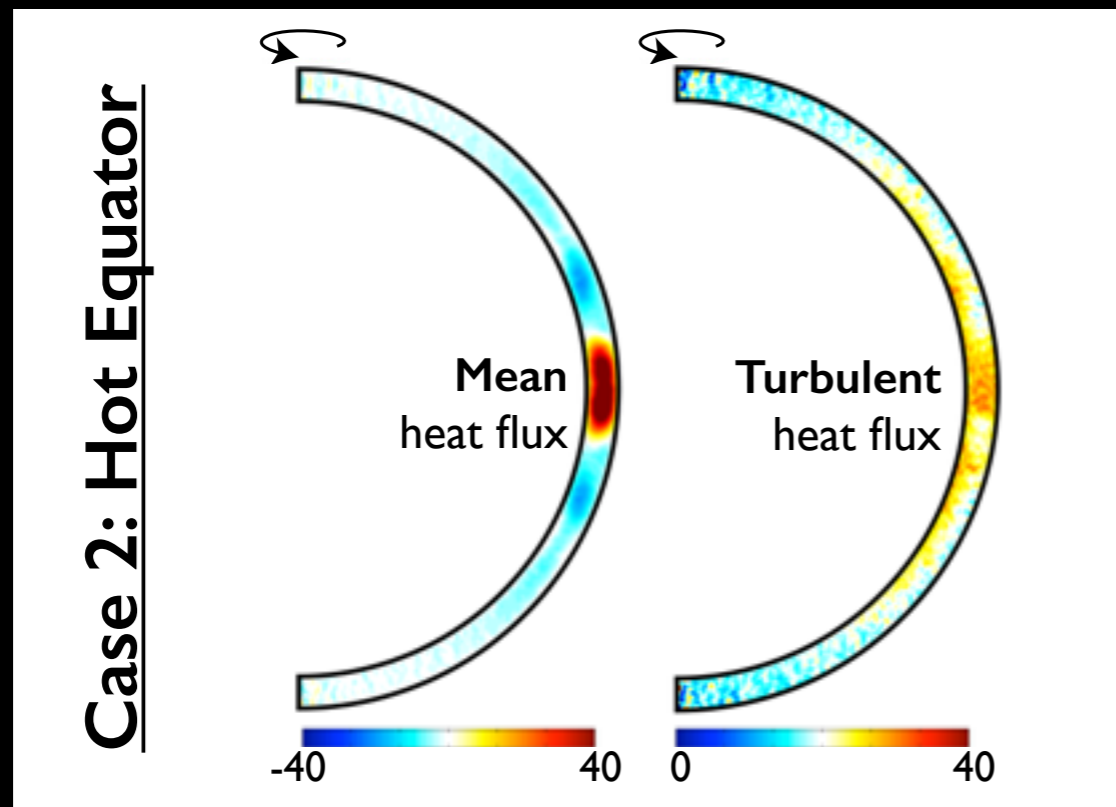
Convective Heat Transfer

- Heat flux decomposition: total = mean + turbulent
- *Mean* heat flux due to meridional overturning circulations (red)
- *Turbulent* heat flux due to fluctuating motions (blue)



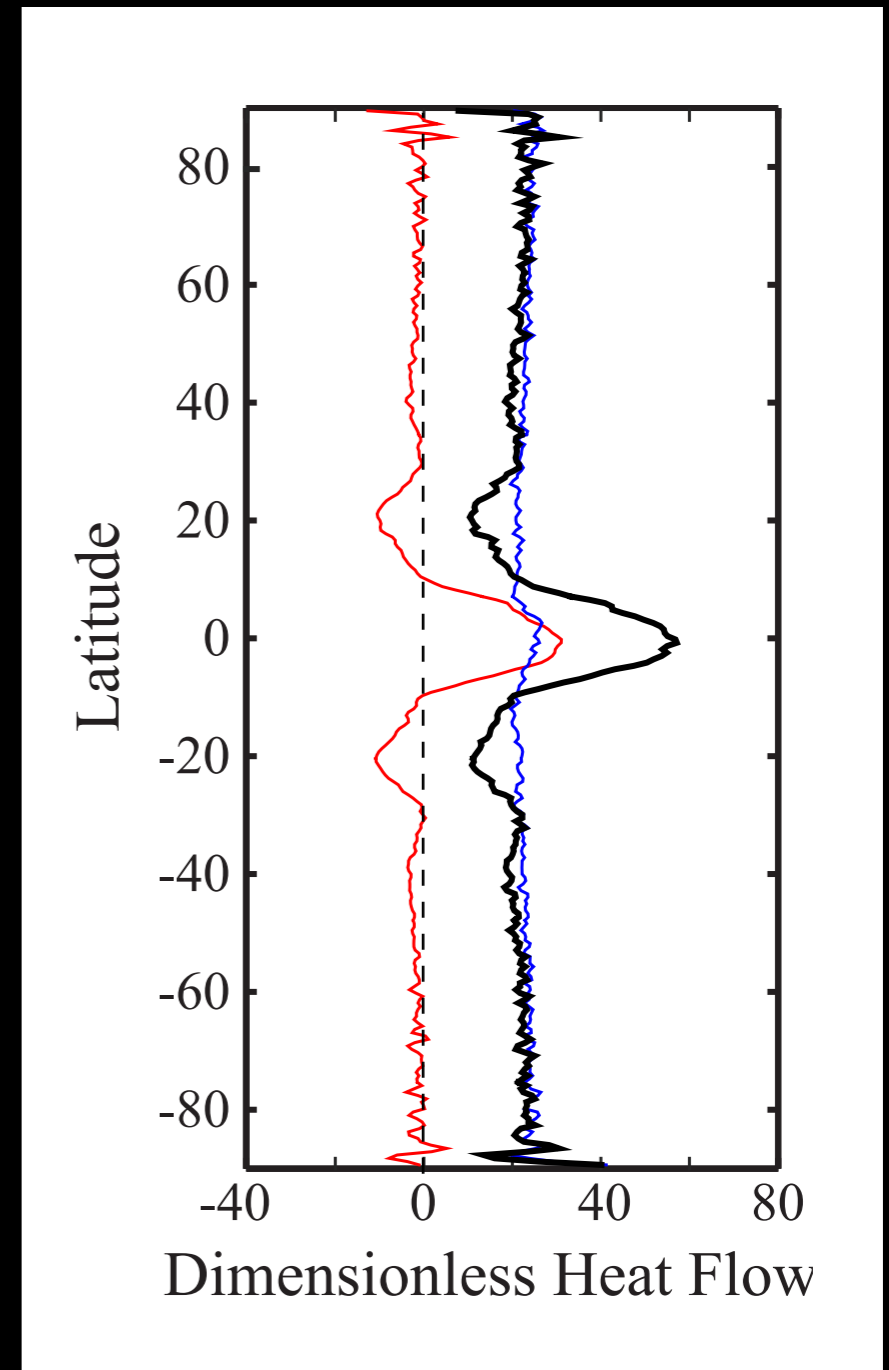
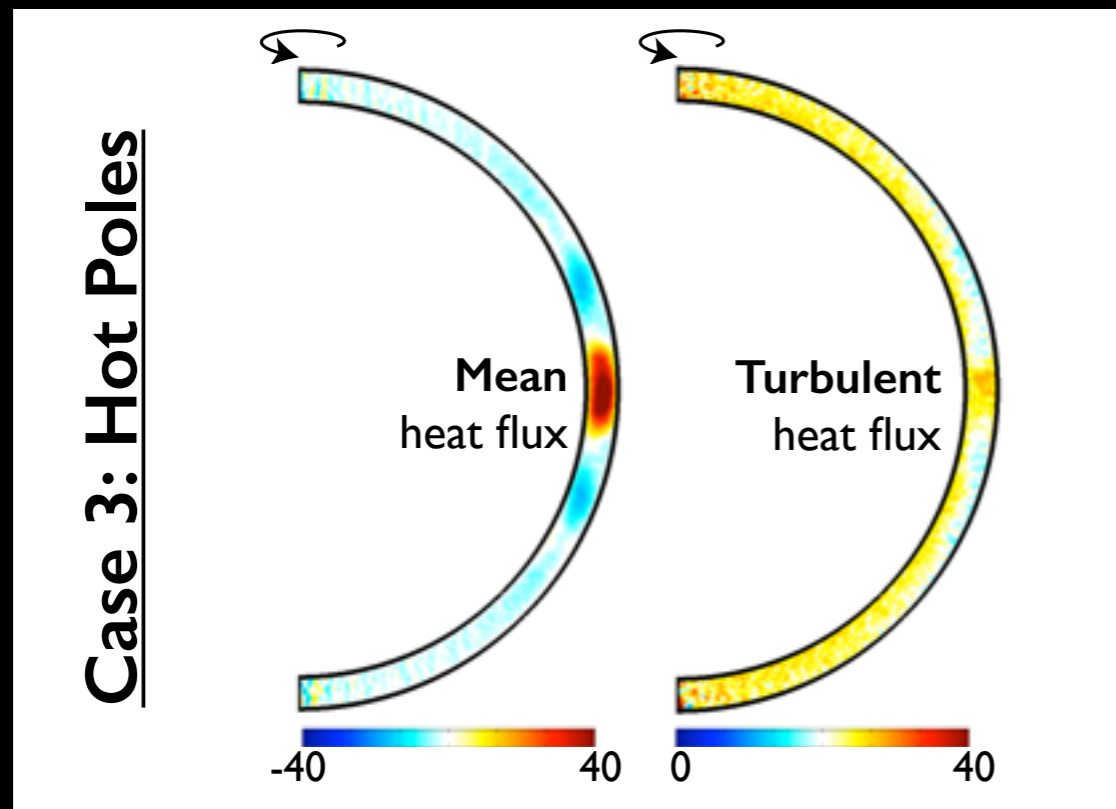
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Global Oceanographic Models

- **Zonal Flows**

- Zonal jets with westward flow near equator, eastward flow at high latitudes are not sensitive to mantle heat flow variations

- **Radial Velocity**

- Mean equatorial upwelling and mid-latitude downwelling are not strongly dependent on mantle heating

- **Convective Heat Transfer**

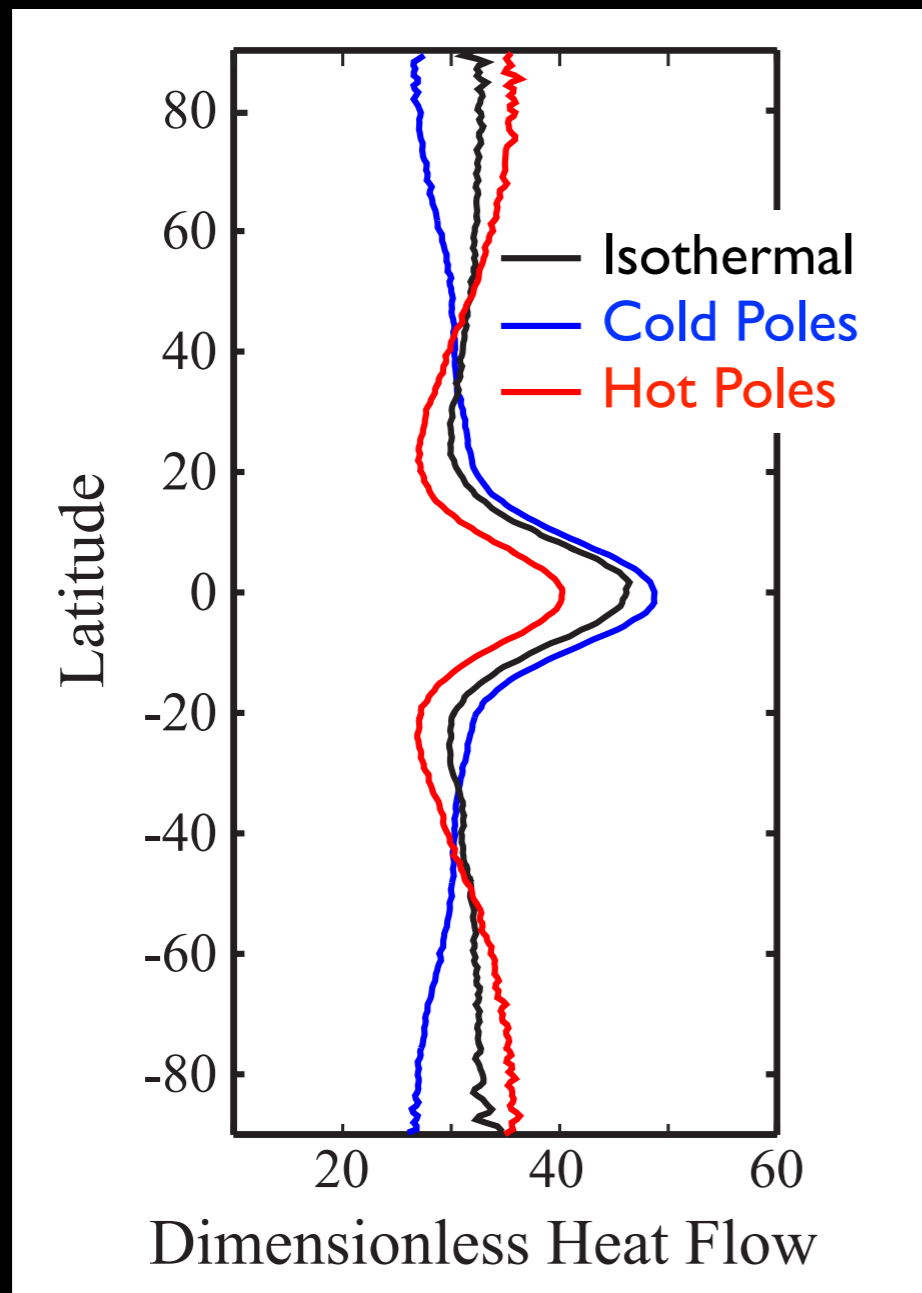
- Heat flux peak at low latitudes is robust to mantle heating heterogeneities
- Polar heat flux behavior depends on mantle heat flow pattern

Outline

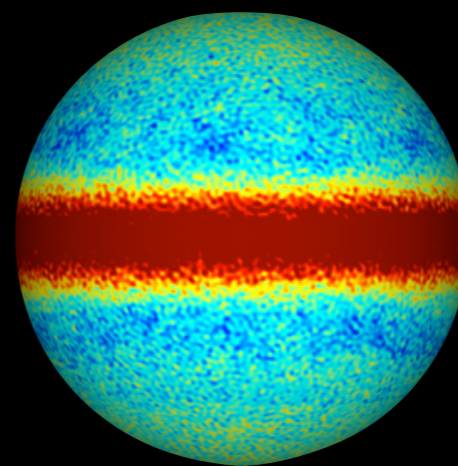
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- 4) Conclusions

Ice Shell Implications

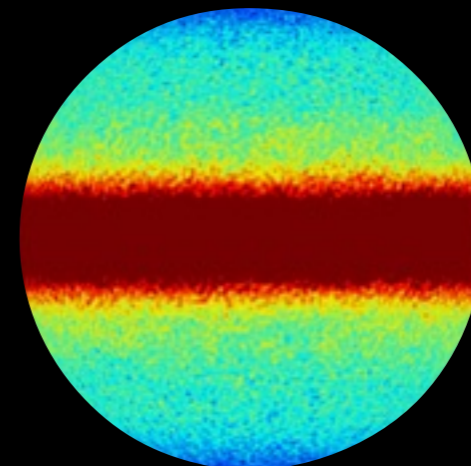
- Oceanic heat transfer may strongly influence any ice-ocean material exchange



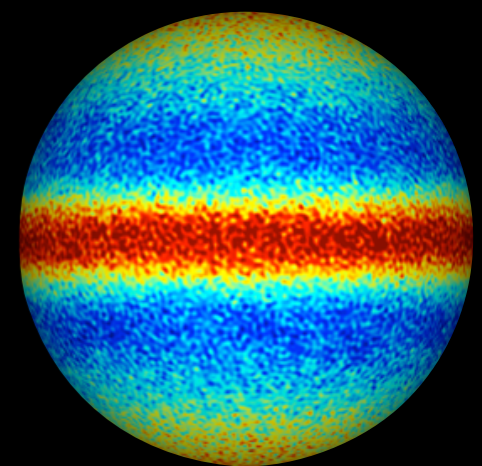
- Ice shell thickness
- Exchange mechanisms
- Geologic activity



Isothermal



Cold Poles

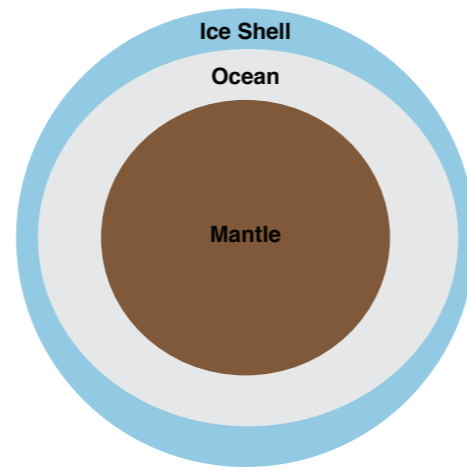
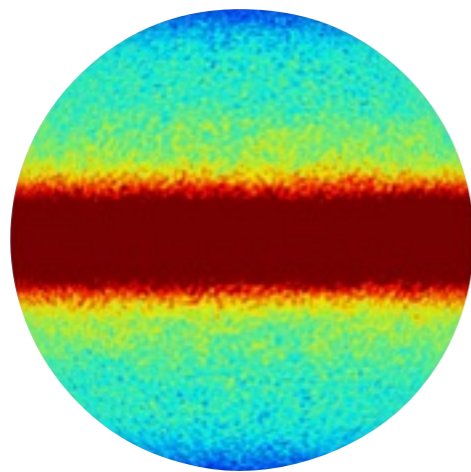


Hot Poles

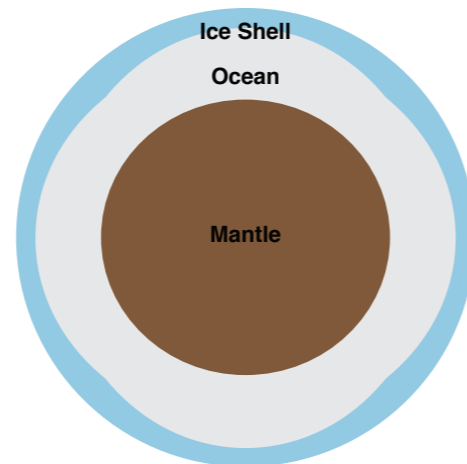
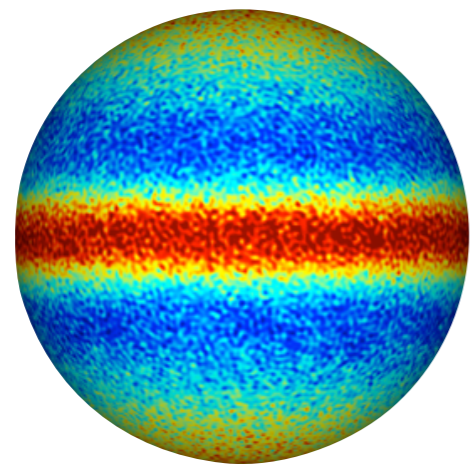
Ice Shell Thickness

- Latitudinal heterogeneity in heat flux should intensify regional melting, reducing ice thickness

Cold Poles

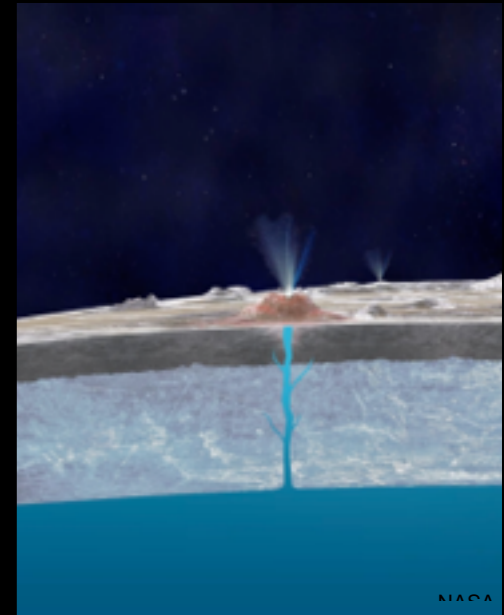


Hot Poles

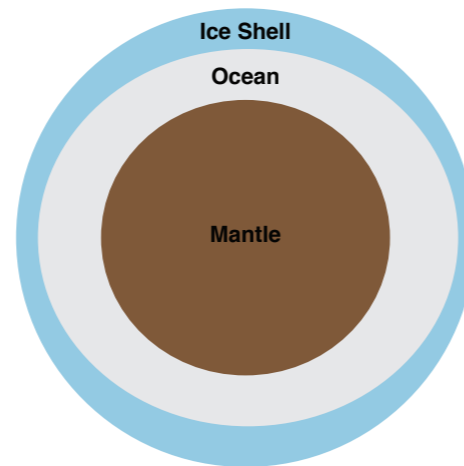
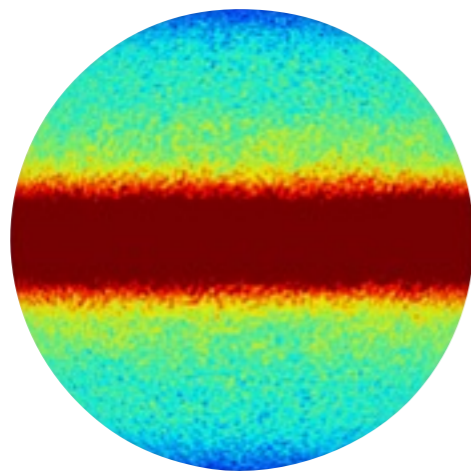


Exchange Mechanisms

- **Thin Ice Shell:** melting of the ice shell may enable direct ocean access through cracks and/or local melt-through events

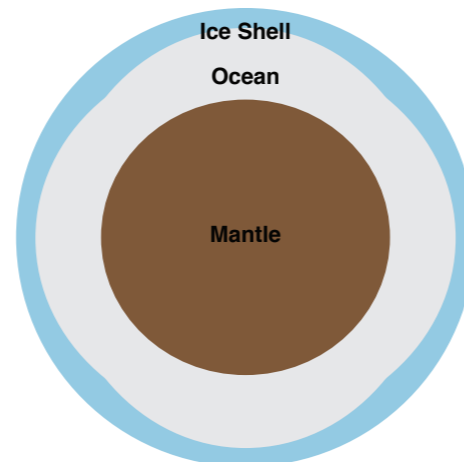
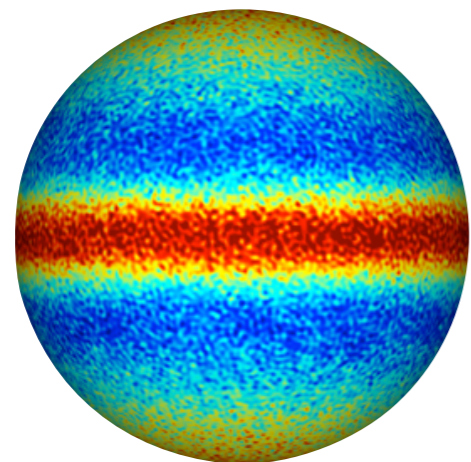


Cold Poles



Cracks / Melt-through
most likely near
equator

Hot Poles

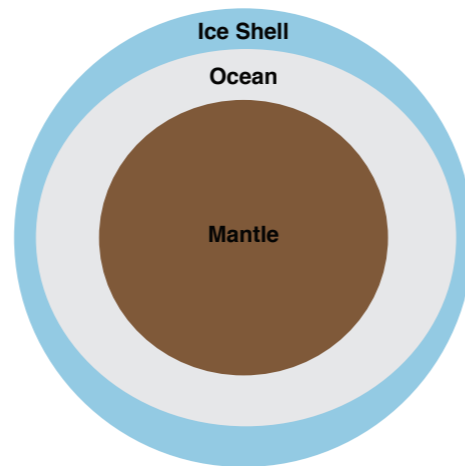
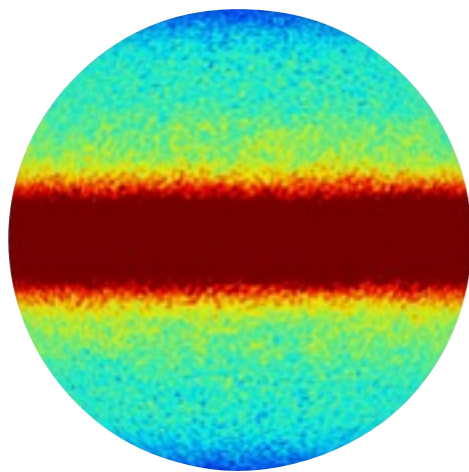


Cracks / Melt-through
most likely near
equator and poles

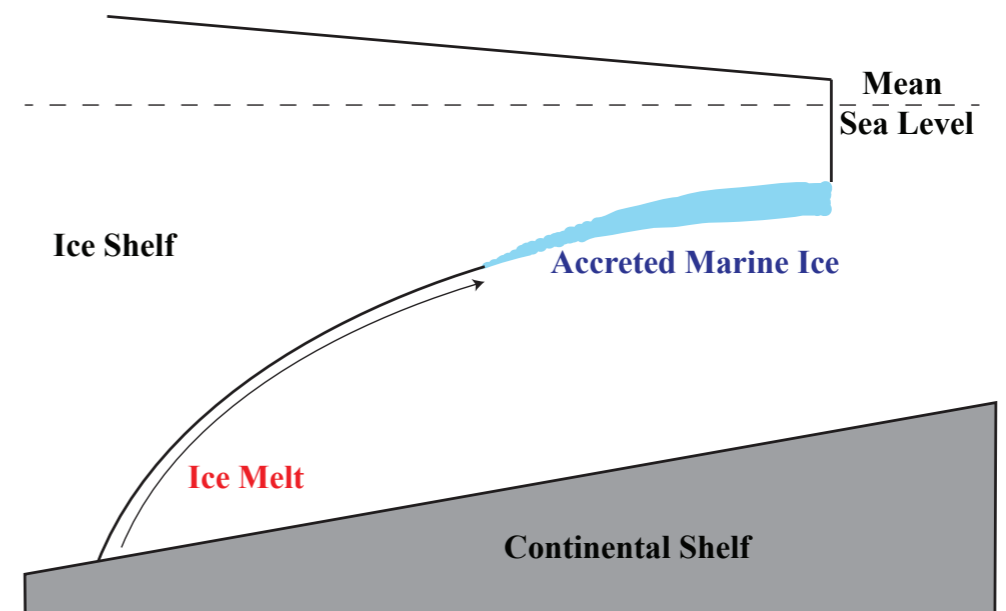
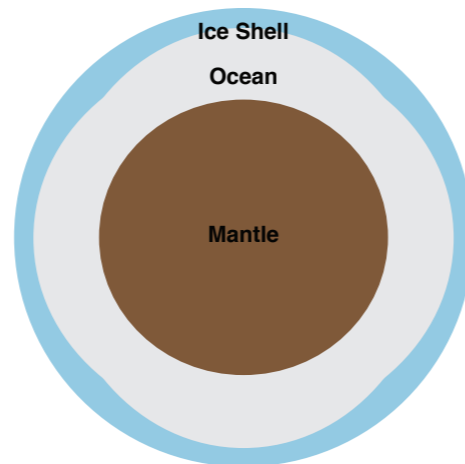
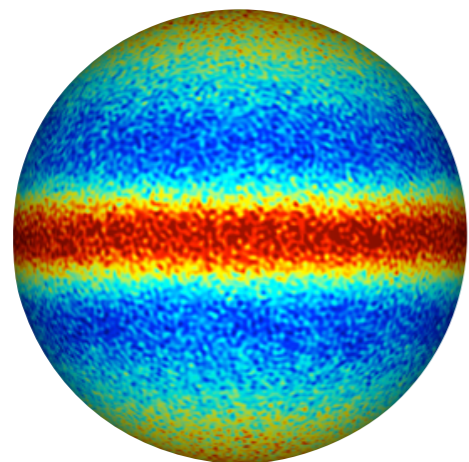
Marine Ice Accretion

- Variations in ice thickness can lead to relatively pure “marine” ice accretion via an ice pump

Cold Poles



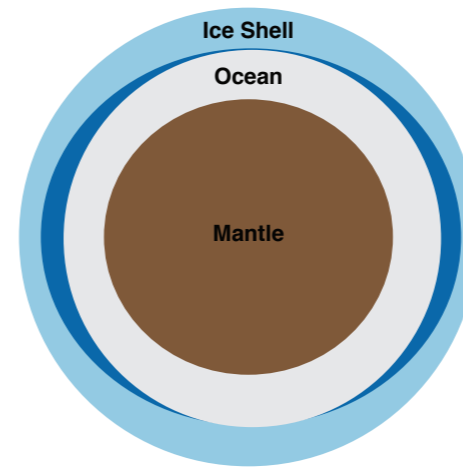
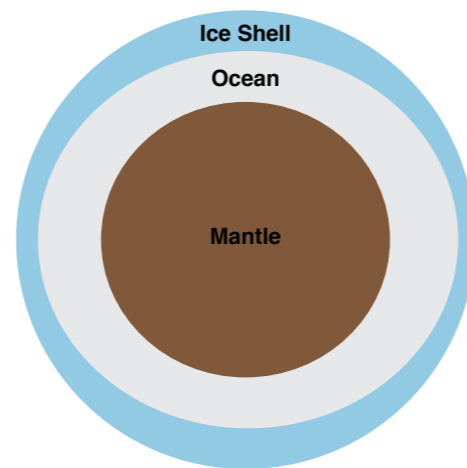
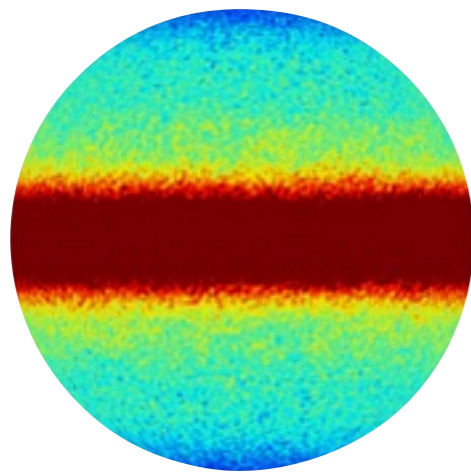
Hot Poles



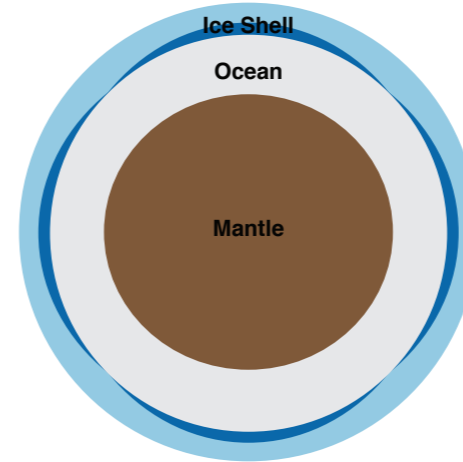
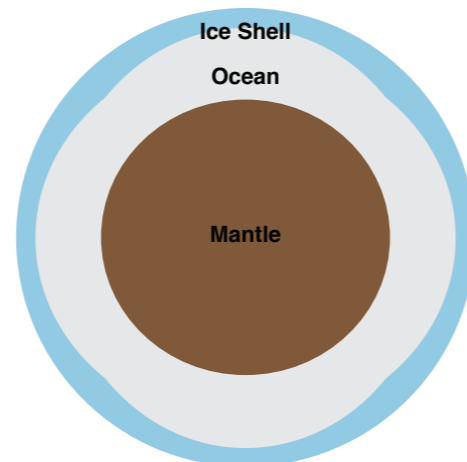
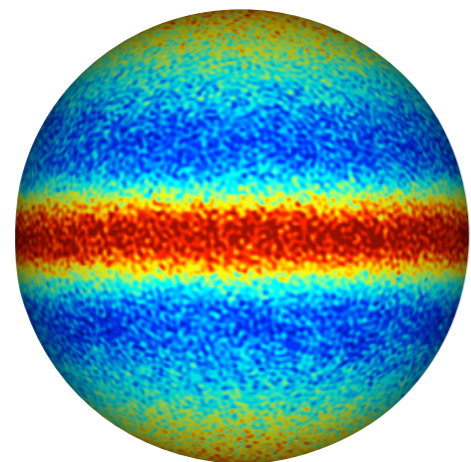
Marine Ice Accretion

- Variations in ice thickness can lead to relatively pure “marine” ice accretion via an ice pump

Cold Poles

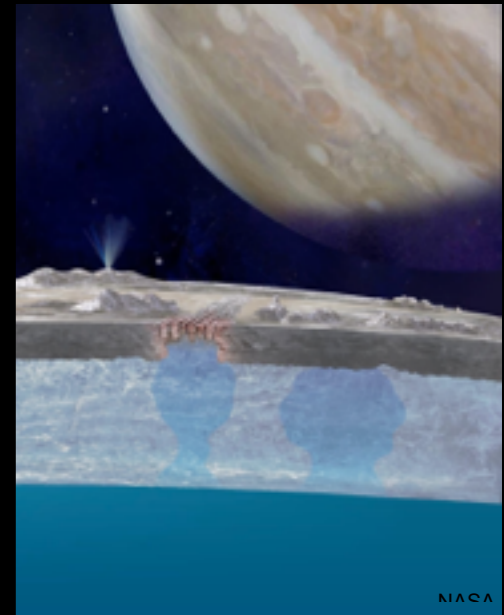


Hot Poles

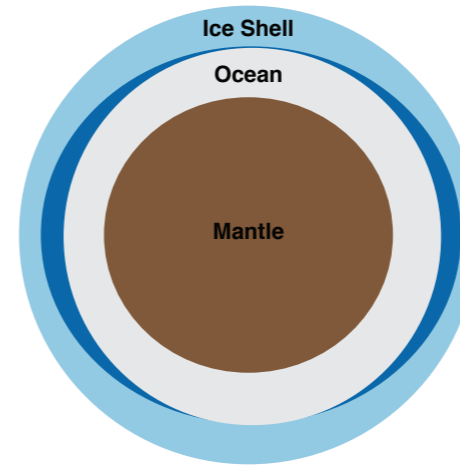
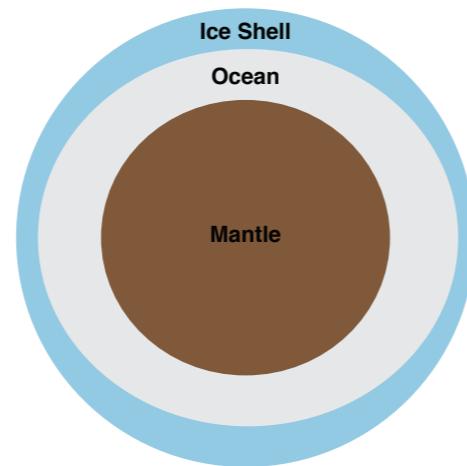
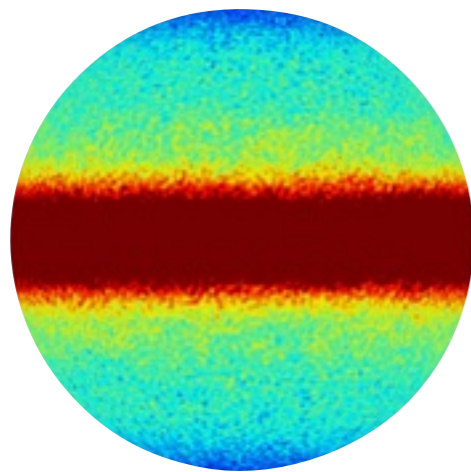


Exchange Mechanisms

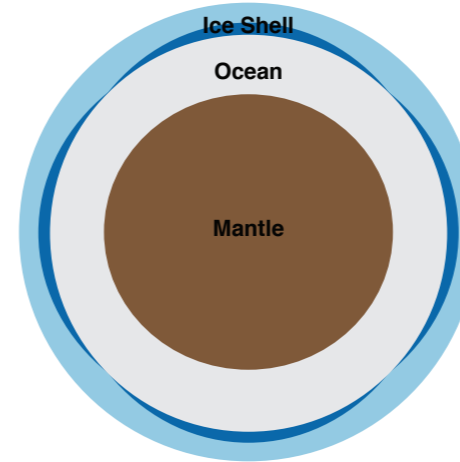
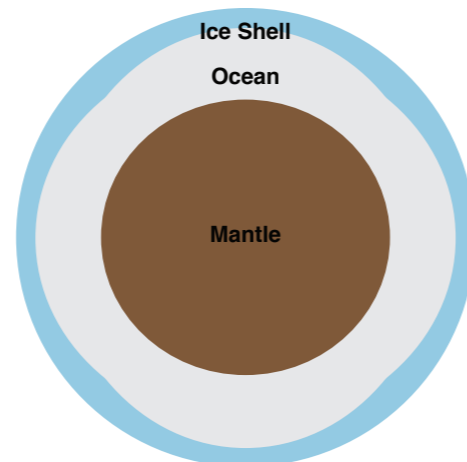
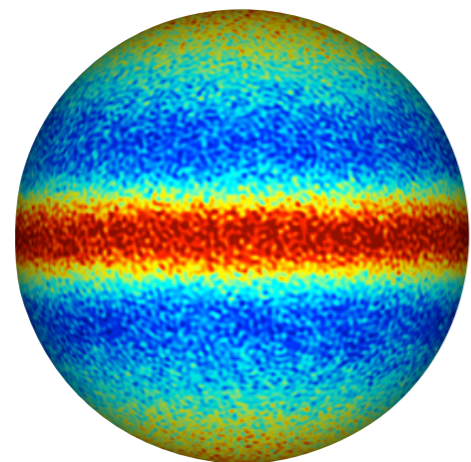
- **Thick Ice Shell:** thermo-compositional diapirism may occur with any substantial thickness of relatively pure marine ice



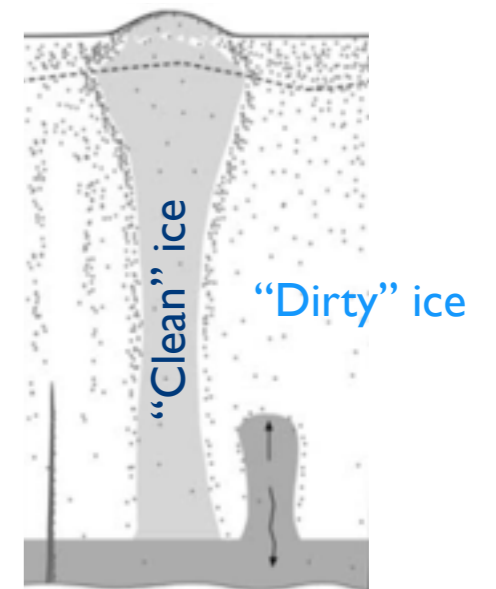
Cold Poles



Hot Poles



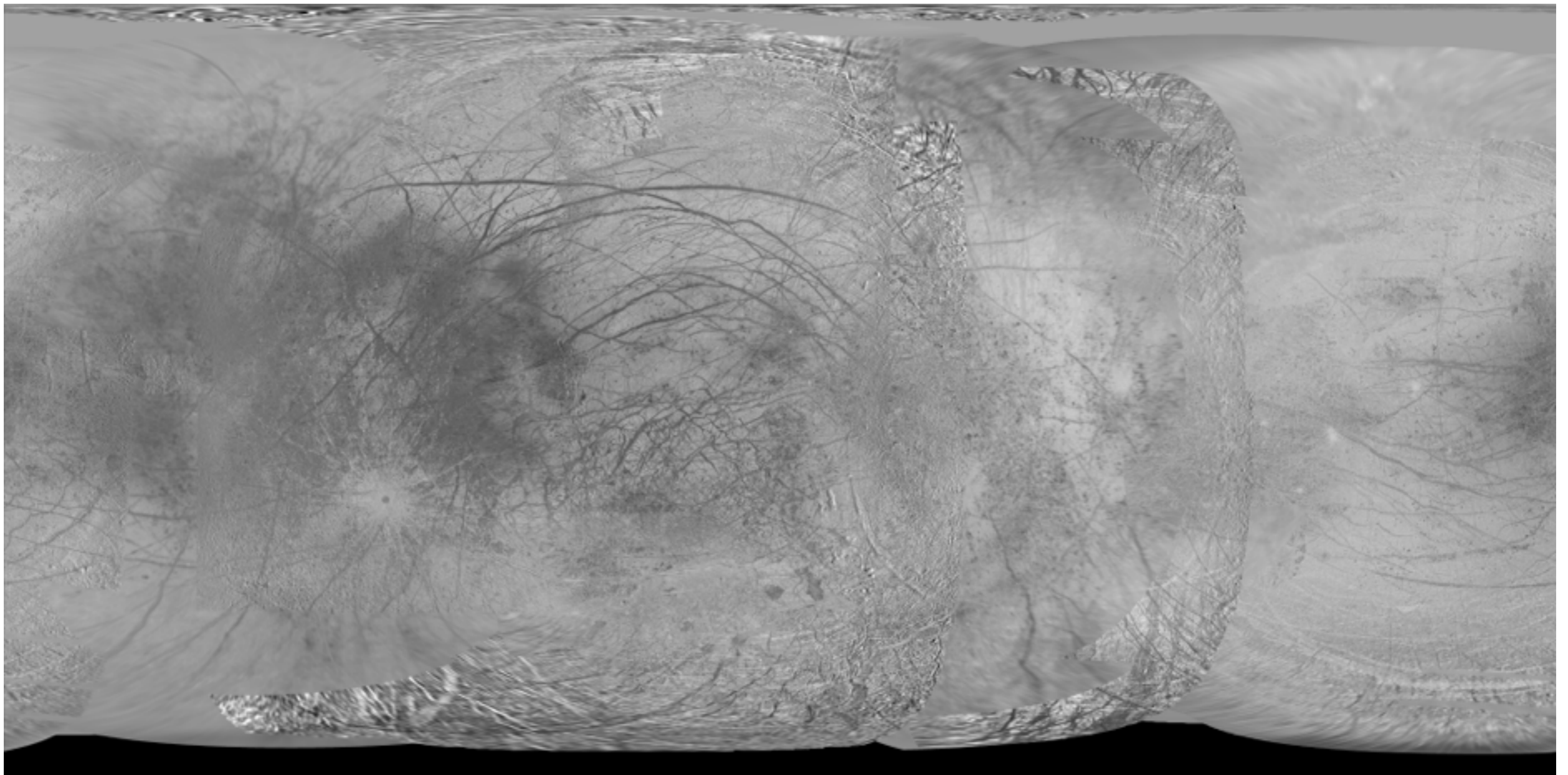
Diapirism most likely near equator



Diapirism most likely near equator and poles

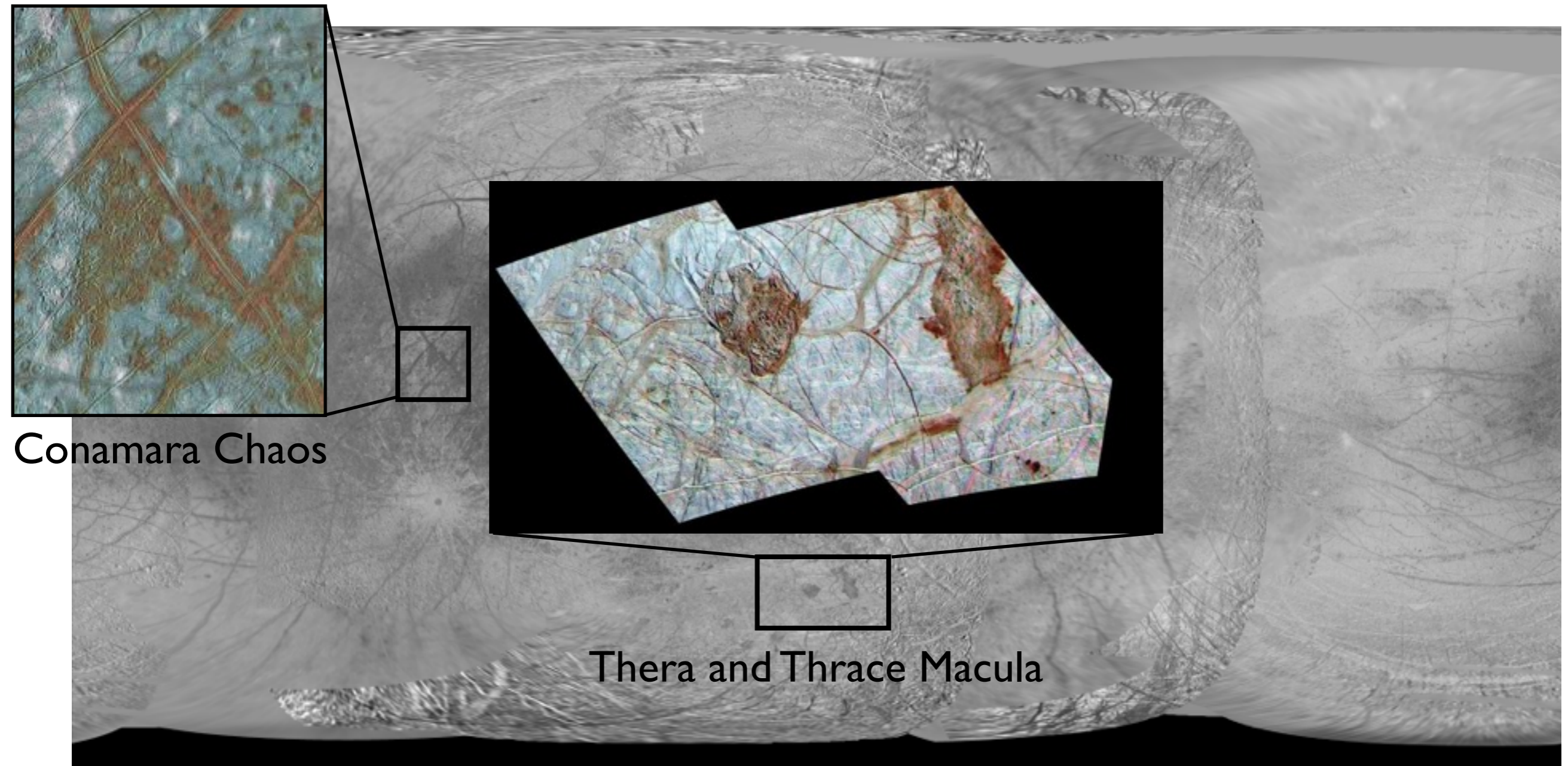
Geologic Activity

- Europa's surface is young and riddled with many unique geologic features



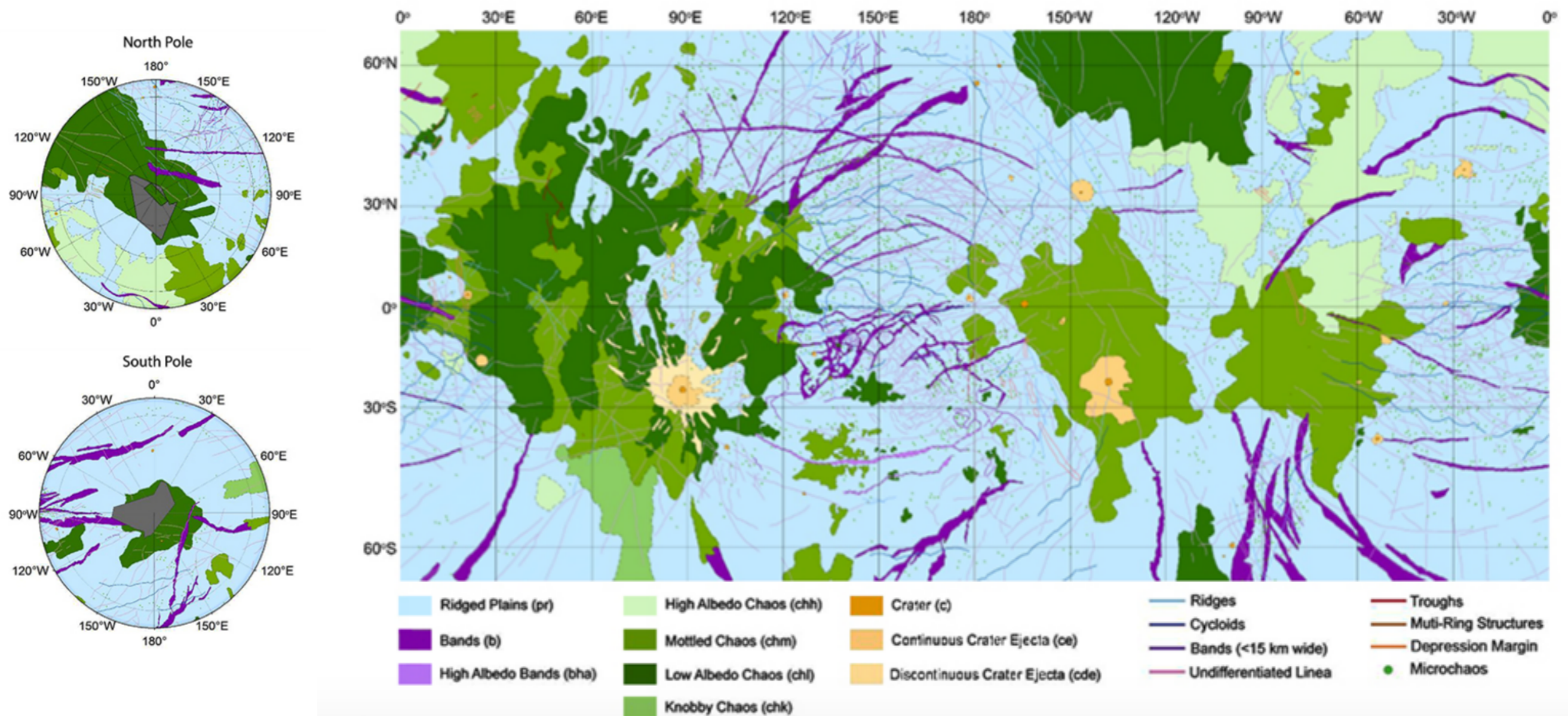
Geologic Activity

- Europa's surface is young and riddled with many unique geologic features, such as chaos terrains



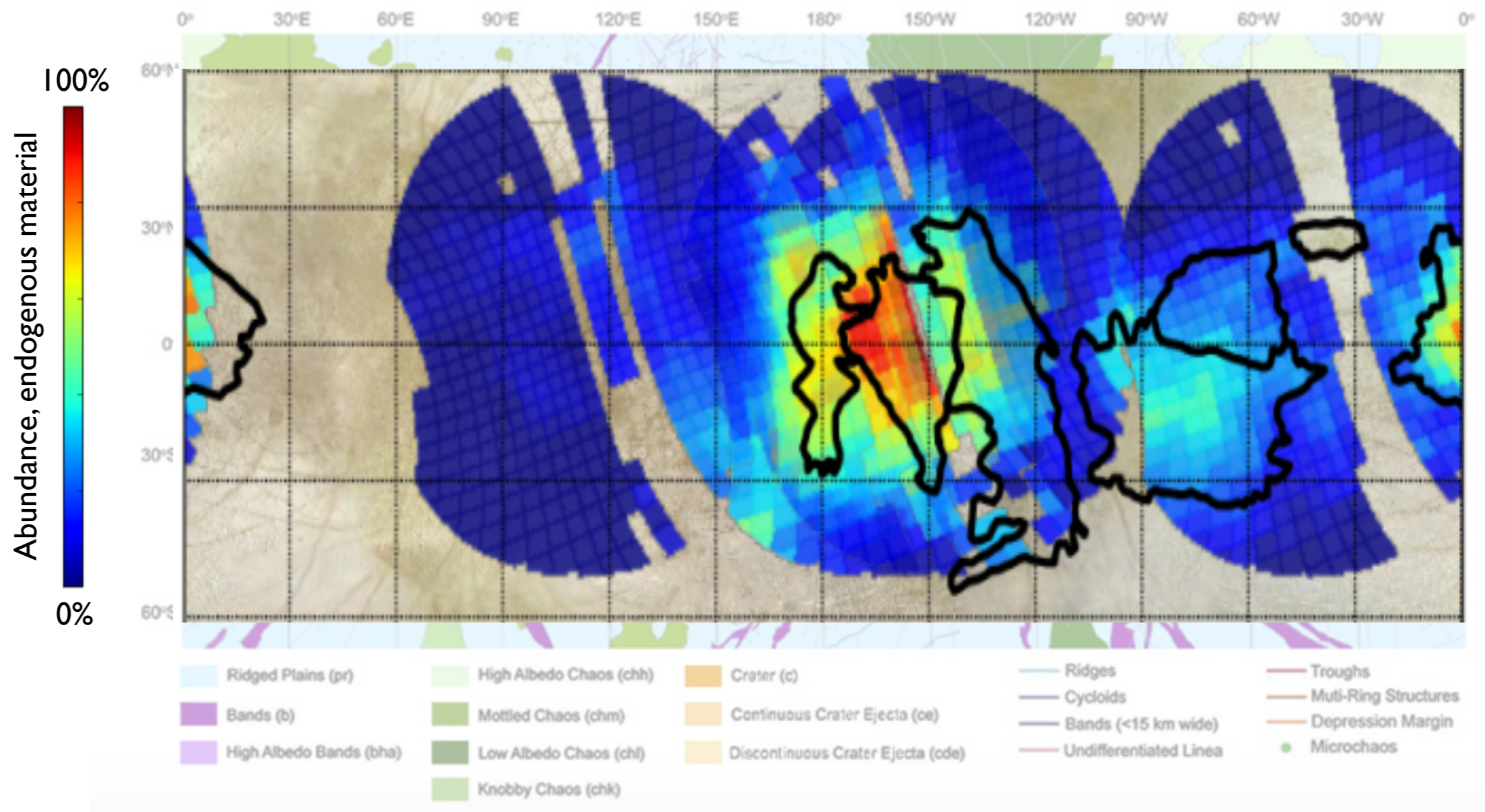
Geologic Activity

- Chaos terrains are most prevalent at low and polar latitudes



Geologic Activity

- Salts with endogenic origin are coincident with leading hemisphere chaos terrains



Implications for Europa

- Heterogeneous heating of the ice shell may promote exchange processes in locally thinned areas
 - Fractures and melt-through (*thin shell*)
 - Diapirism via marine ice accretion (*thick shell*)
 - Chaos terrains suggest eccentricity tidal heating of the mantle (“hot poles” case)

Outline

- 1) Theoretical Predictions for Convection
- 2) Numerical Convection Models
- 3) Boundary Layer Implications
- 4) **Conclusions**

Habitability of Ocean Worlds

- ➔ Oceans of Europa, Ganymede, Enceladus, and Titan predicted to be weakly influenced by rotation
 - 3D turbulence, three zonal jets, and an equatorial upwelling
 - Convective heat transfer has a maxima near the equator; high latitudes are sensitive to mantle heat flow distribution
- ➔ Oceanic heat transfer may strongly influence any ice-ocean material exchange

