



Higgs Physics from the Theoretical Viewpoint

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Collider Physics Conference

January 15, 2004

The Kavli Institute for Theoretical Physics logo, featuring a photograph of a building on the left and the text "Kavli Institute for Theoretical Physics" in a stylized font on the right.

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★ No animals were harmed in the making of this presentation ★

Introduction

The Standard Model is ~35 years old and its essential goal

To describe electroweak interactions with a spontaneously broken $SU(2) \otimes U(1)$ gauge symmetry has been spectacularly confirmed

- Renormalizability
- Discovery of Neutral Currents
- Discovery of W and Z bosons
- Precision test of W and Z properties

But ...

The agent of electroweak symmetry breaking remains elusive

Outline of the talk

I will primarily focus on the LHC. I will mention the possibilities at a linear collider, but I will concentrate on the possibilities for the near future.

My topics will be:

- Introduction
- Higgs Production and discovery
- Precision Measurements

What is the Higgs Boson?

In the minimal Standard Model, Electroweak symmetry breaking is accomplished by a single complex scalar doublet, resulting in the three massive gauge bosons W^\pm , Z , and a single Higgs Boson. The Standard Model Higgs is also responsible for giving mass to quarks and leptons.

In the Supersymmetric Standard Model, there must be at least two scalar doublets resulting in five Higgs scalars: h^0 , H^0 , A^0 , H^\pm

Where is the Higgs?

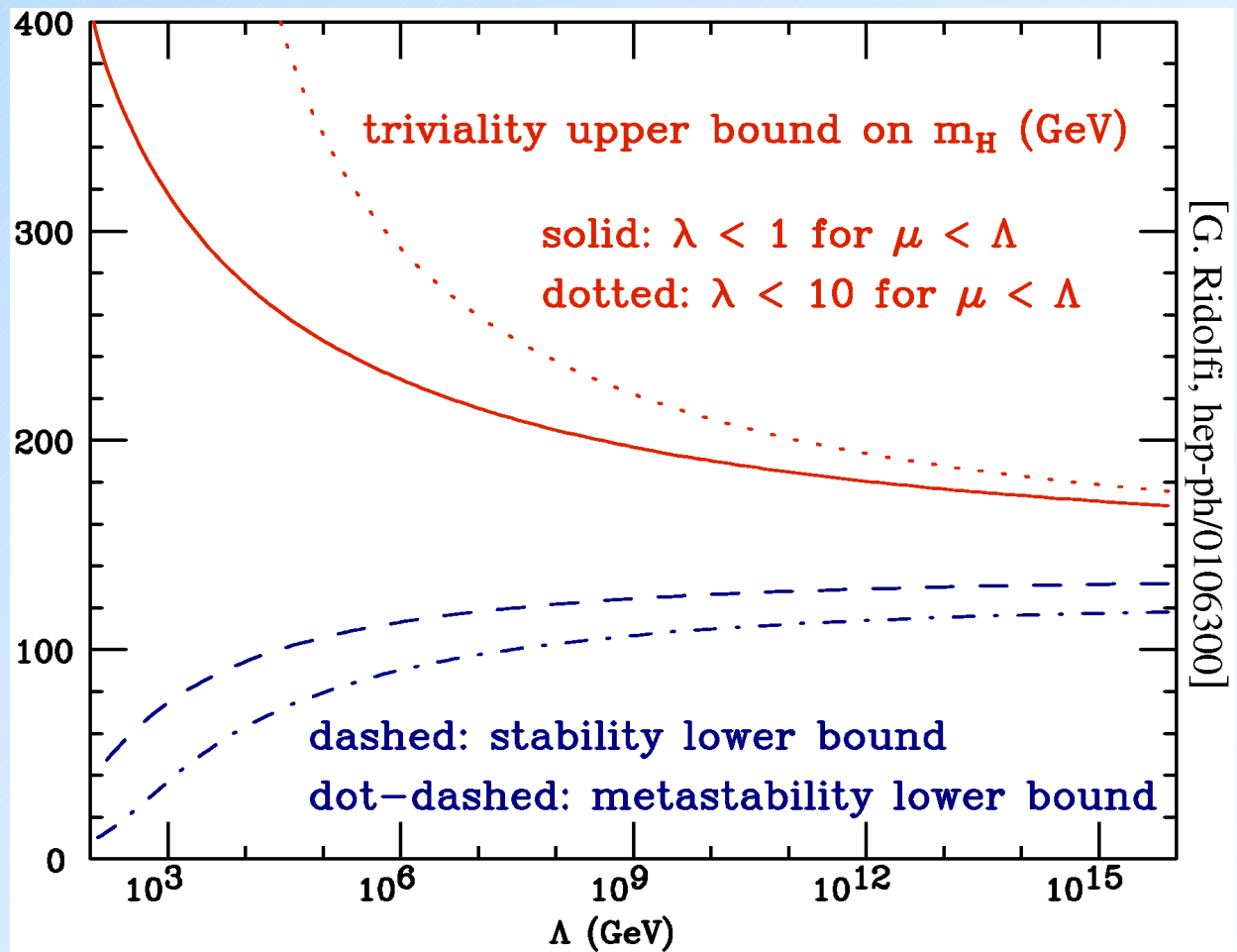
A priori, the mass of the Higgs boson is a free parameter. It can be constrained, however by:

- Theoretical prejudices
- Precision measurements
- Experimental search limits

Theoretical Prejudices

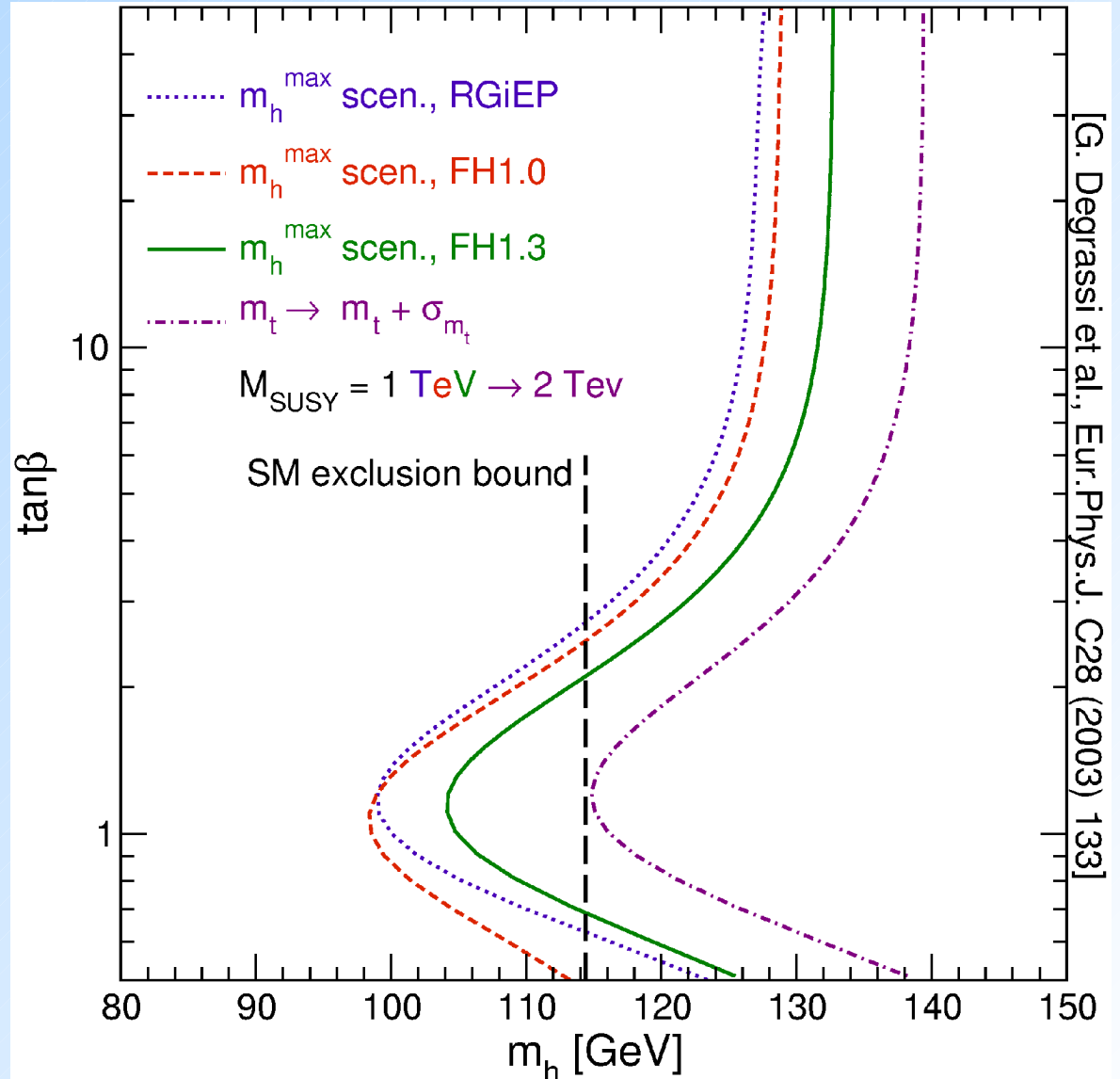
There are three primary considerations determining theoretical prejudices about the mass of the Higgs:

- Vacuum Stability
- Triviality
- Unitarity



Supersymmetric Constraints

In SUSY models, there are further theoretical constraints so that $m_h \leq 135$ GeV.



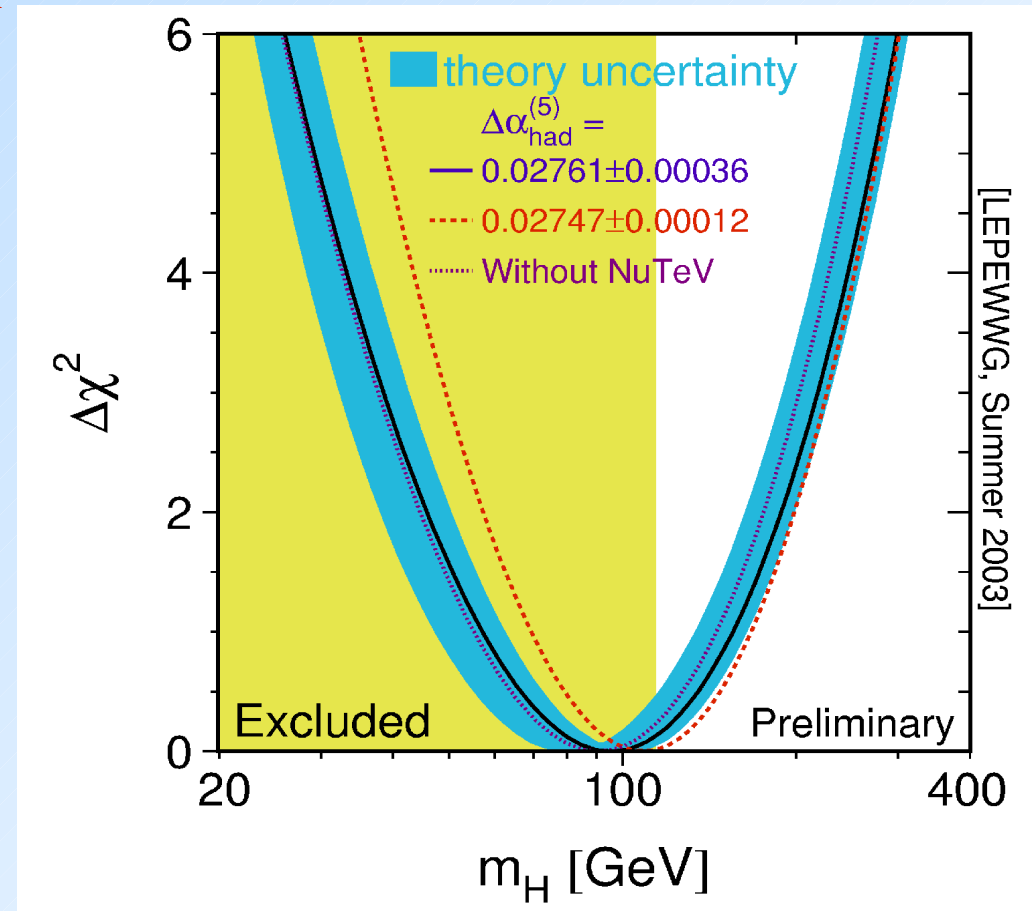
Direct Search / Precision Constraints

LEP Search: $M_H \geq 114.4 \text{ GeV}$

Precision EW Fits: $M_H = 96^{+60}_{-38} \text{ GeV}$

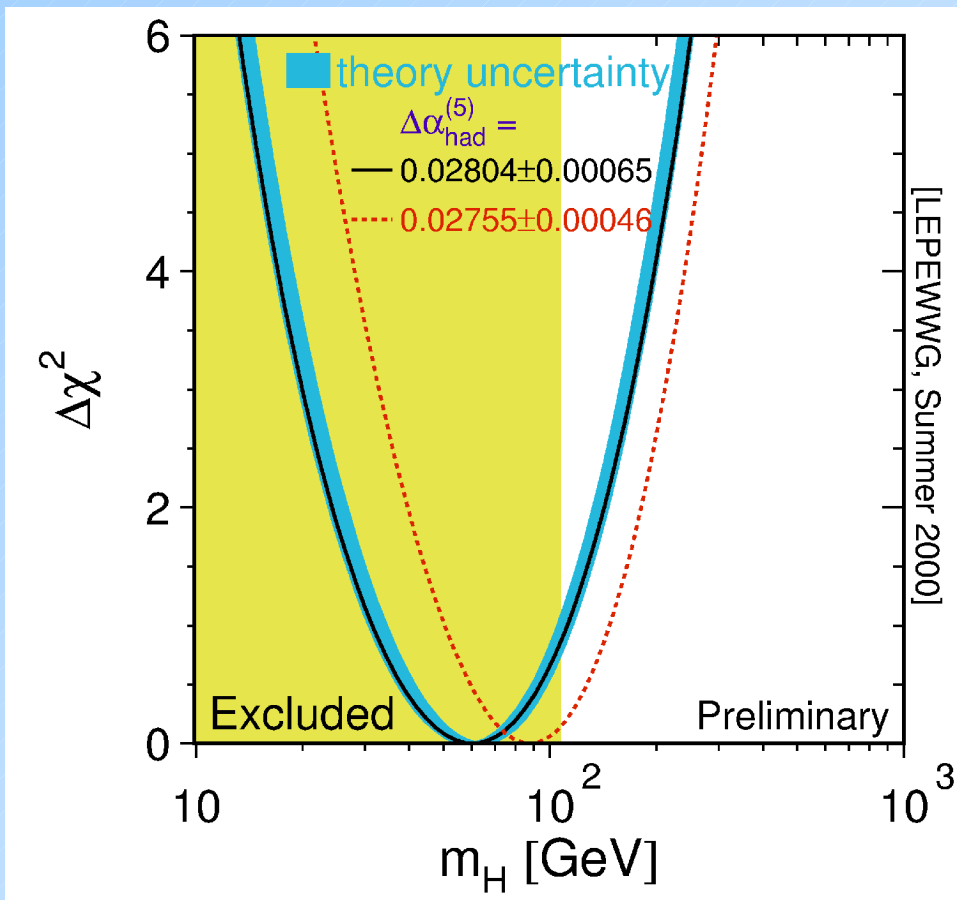
95% CL upper limit: $M_H < 219 \text{ GeV}$

Precision
Measurements from
LEP, SLC, CDF, D0
and NuTeV

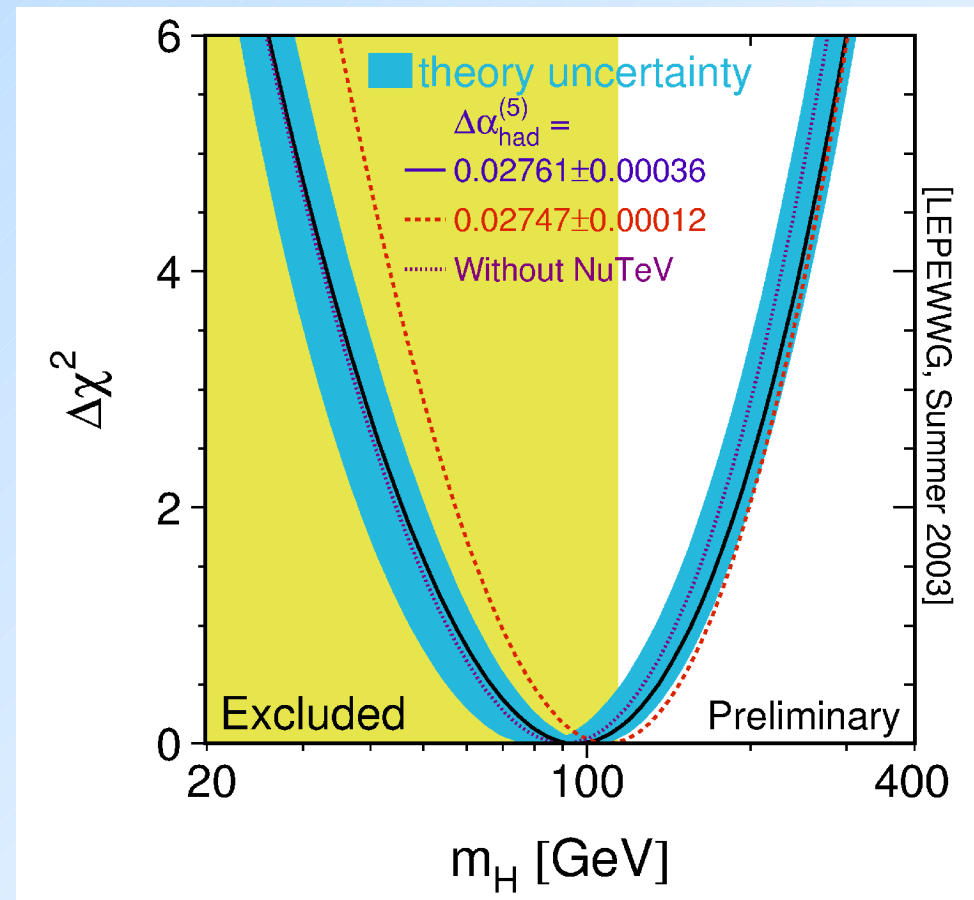


Shifting Blue Bands

Each year the blue band plot seems the same, but there have been shifts!



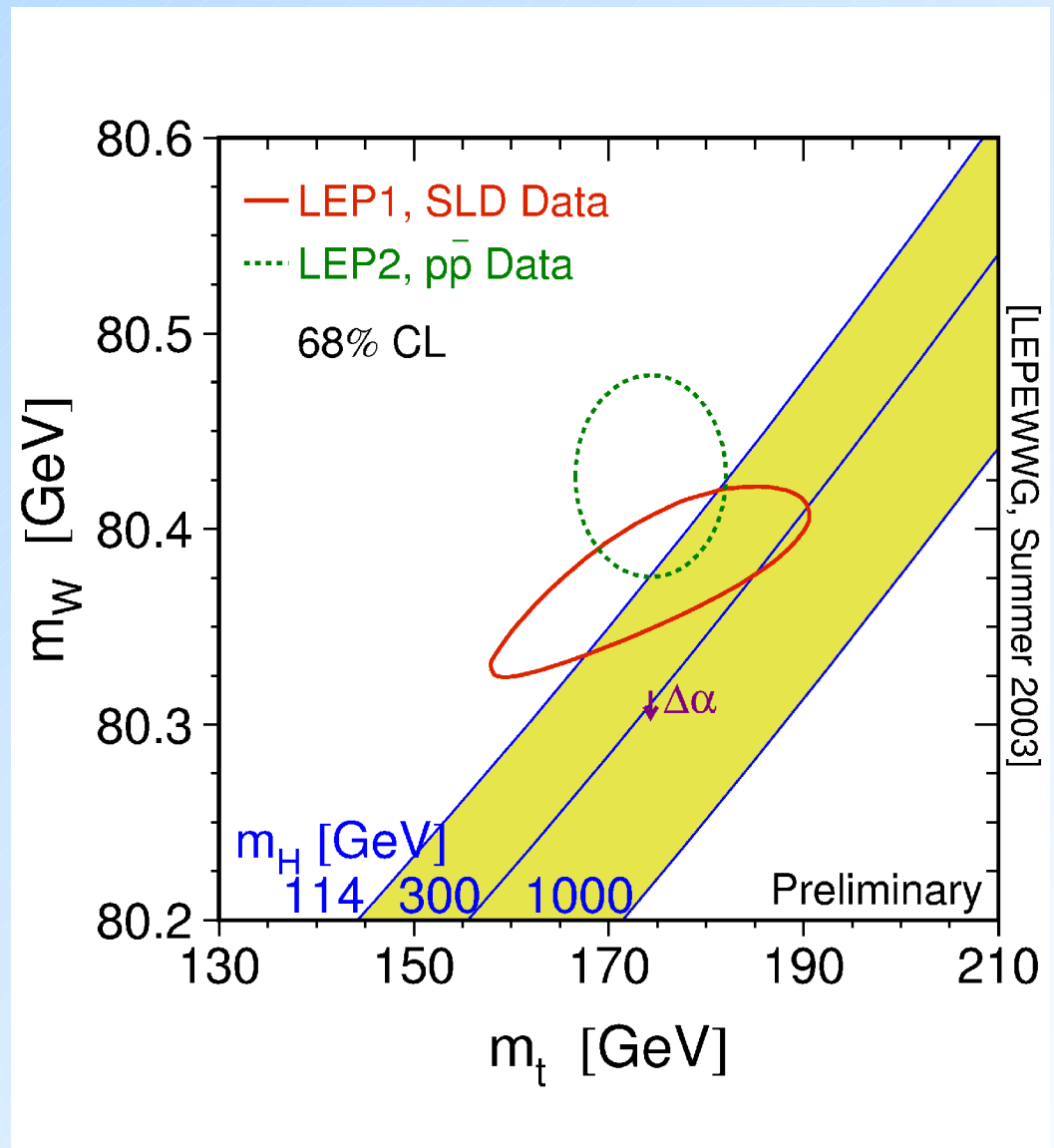
$$m_{h,\text{fit}} = 60 \text{ GeV}$$



$$m_{h,\text{fit}} = 96 \text{ GeV}$$

Some Parameters are More Equal than Others

Changes to m_W and m_t have a strong effect on the m_H fit.

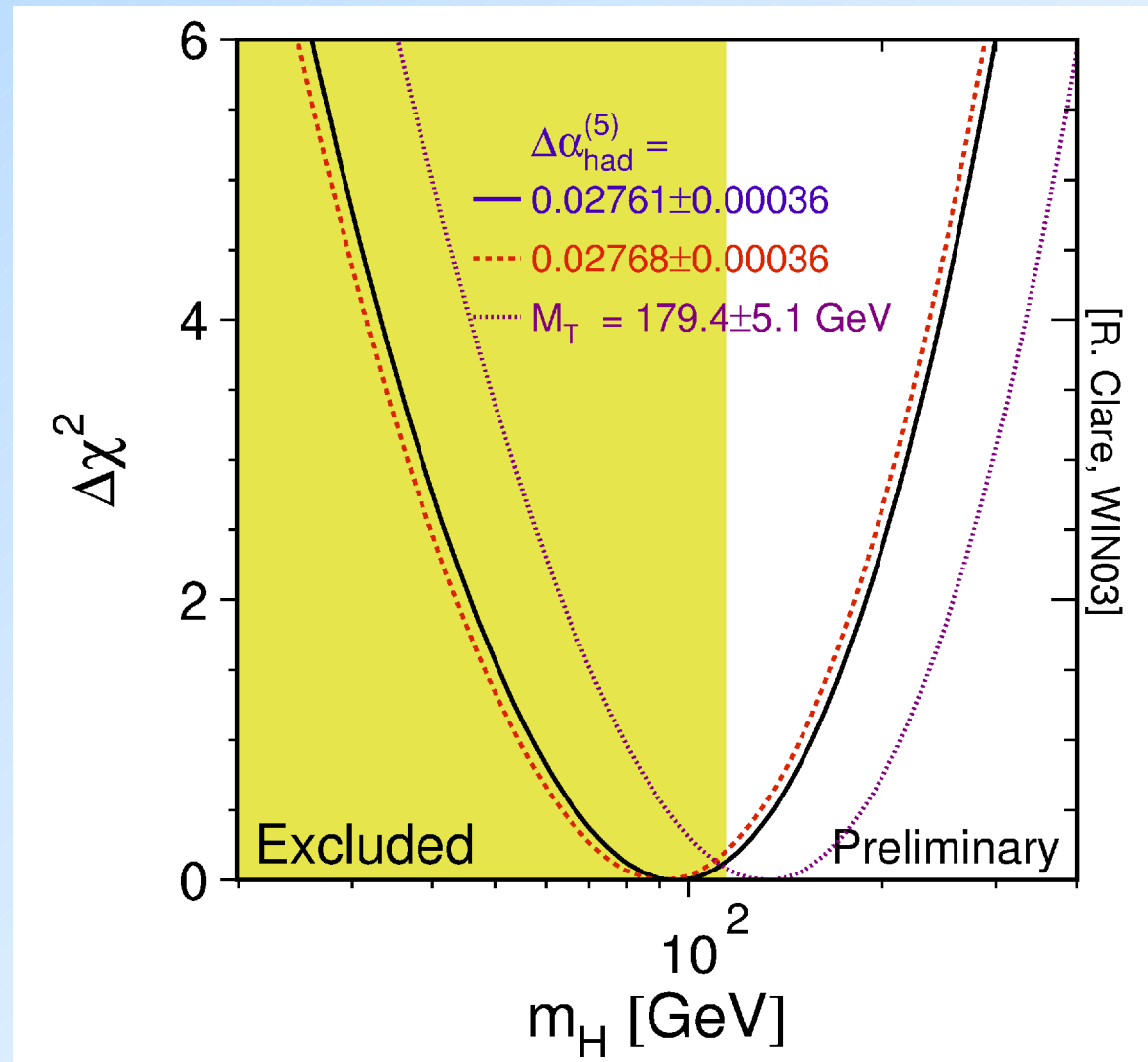


What if m_t moves?

The minimum is broad, and this fact is brought home by considering shifts in crucial parameters.

D. Wood reported that D0's new top mass from Run I data is $m_t = 180.3 \pm 5.1$ GeV.

$$m_{h,\text{fit}} = 126 \text{ GeV} < 283 \text{ GeV}$$

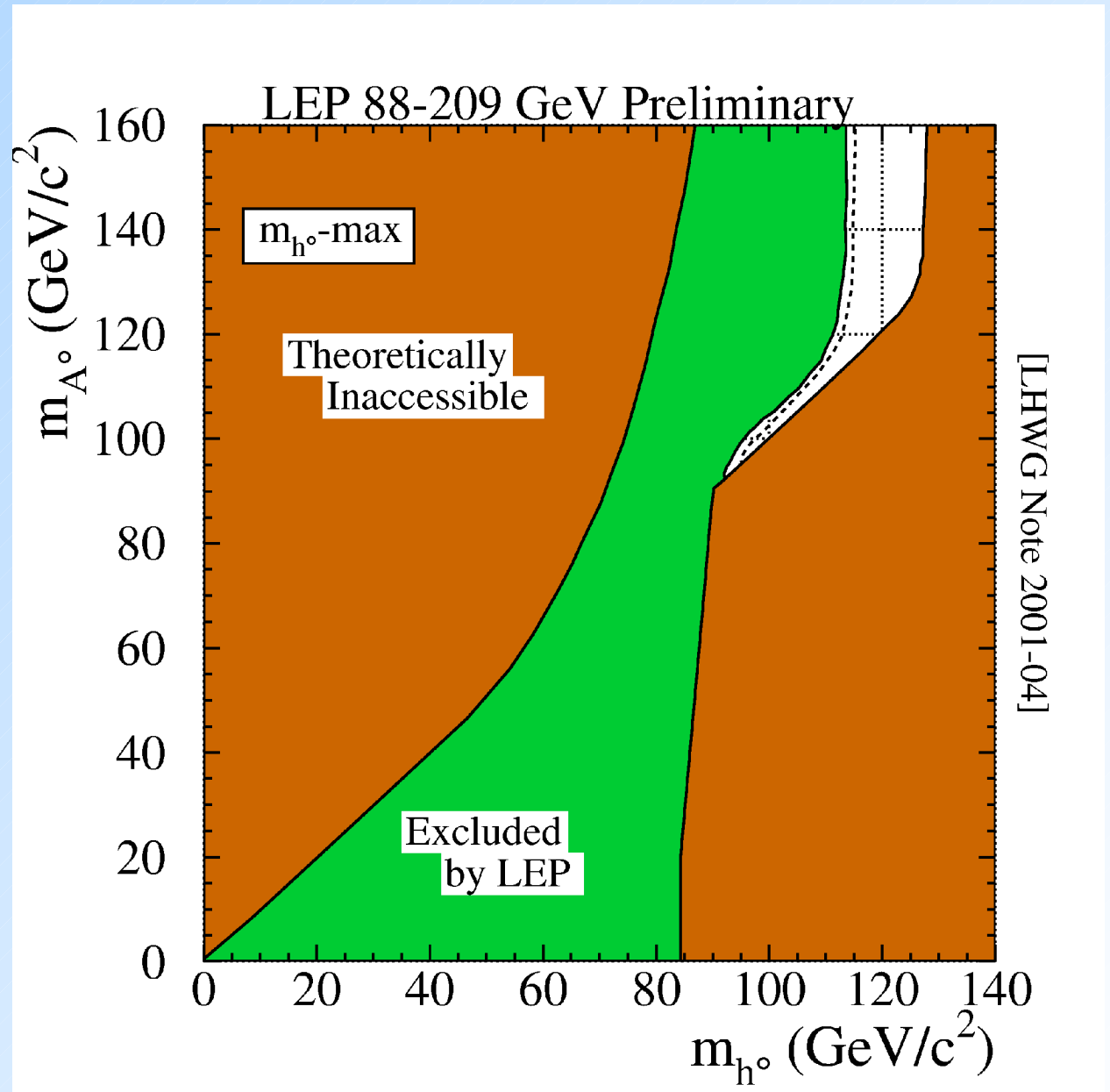


SUSY Higgs Limits

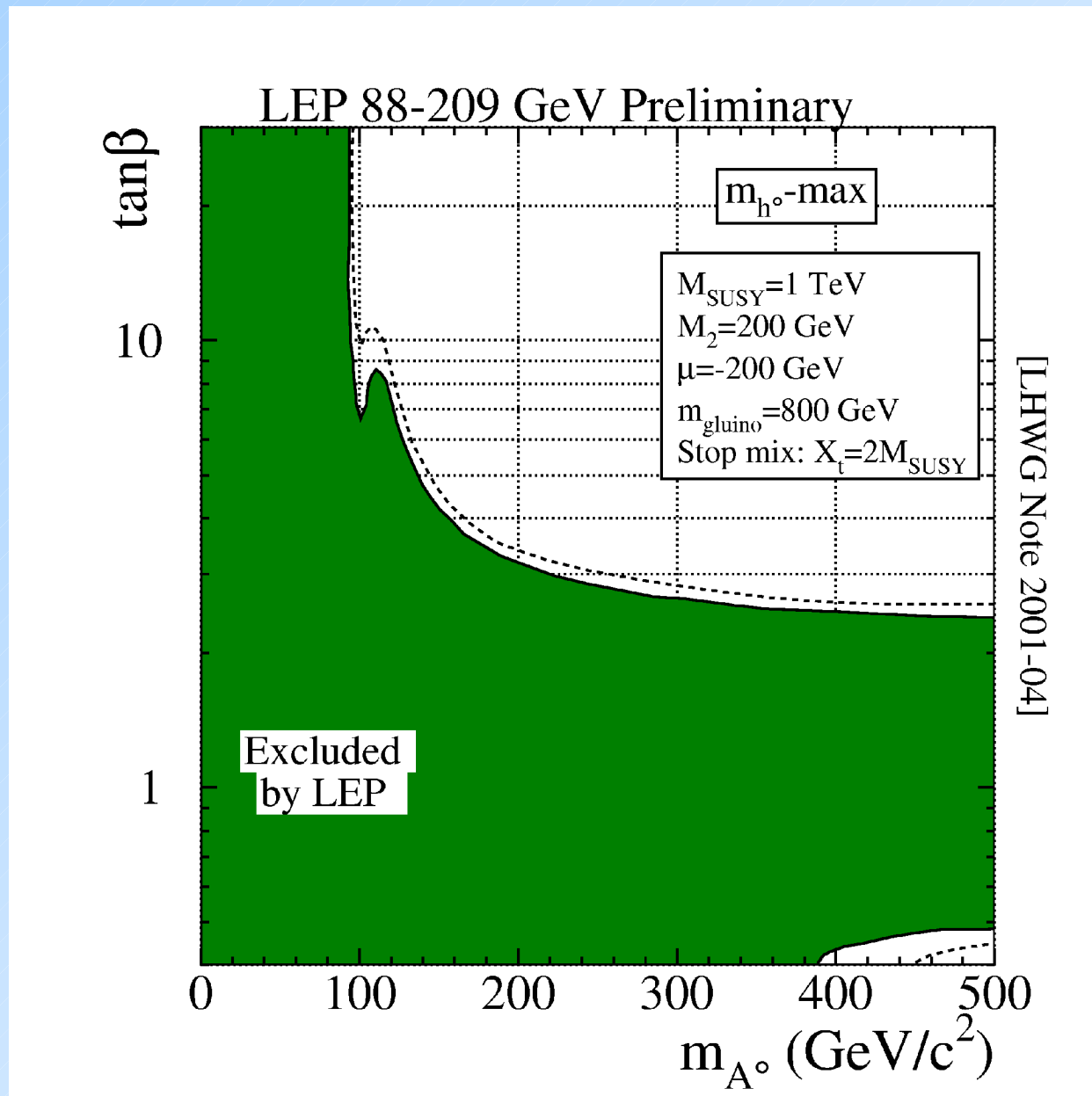
Any limit on SUSY is model dependent.

The most important parameters for the SUSY Higgs sector are m_A , and $\tan\beta$.

In the “ m_h -max” scenario:

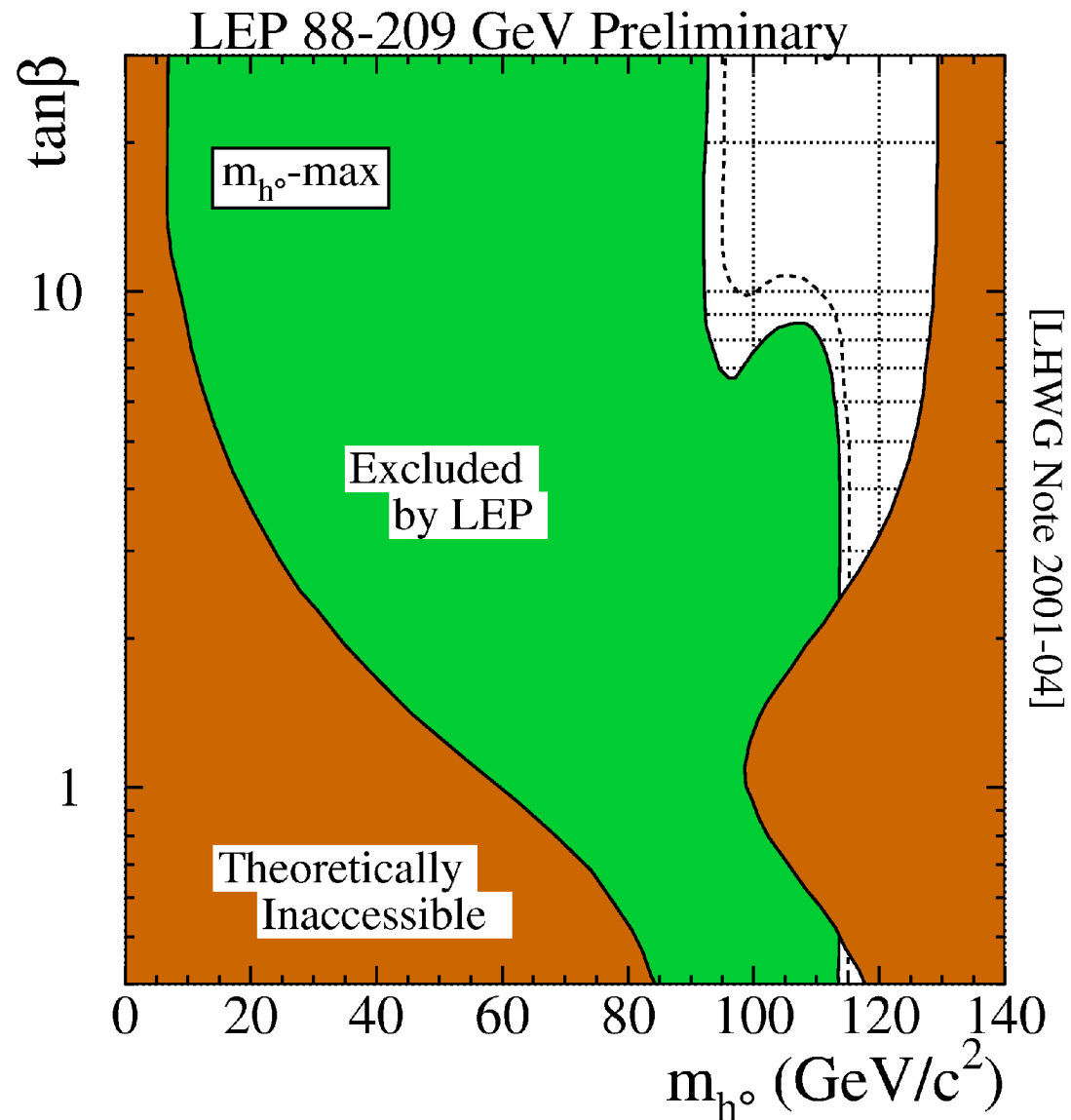


Limits on the Pseudoscalar



SUSY Higgs Limits

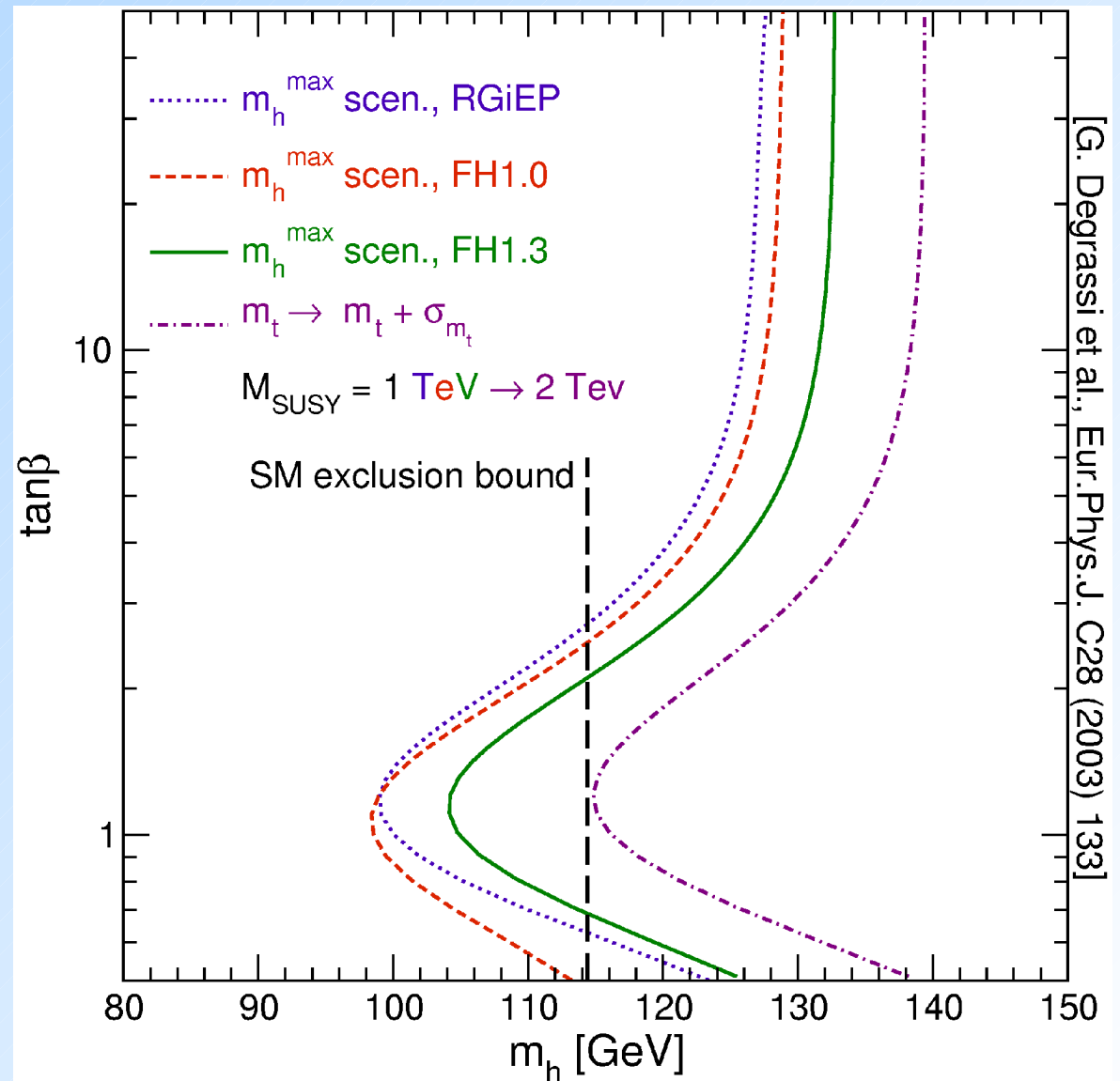
Note the $\tan \beta$ exclusion region.



Higher order corrections weaken the limits!

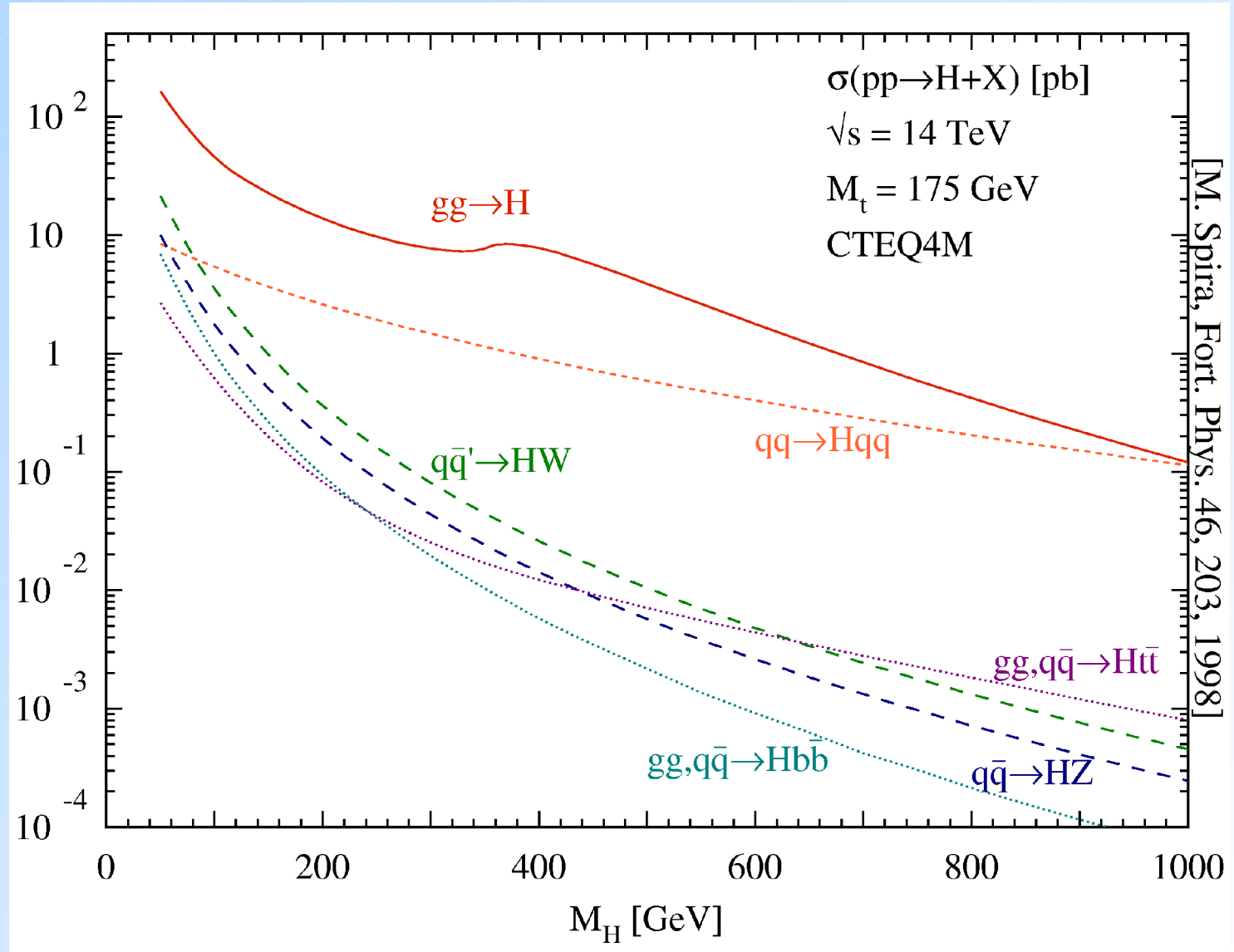
Two-loop corrections to the SUSY Higgs masses weaken the limit from above.

With a shift in the top mass to 179 GeV, the $\tan \beta$ exclusion would completely disappear!

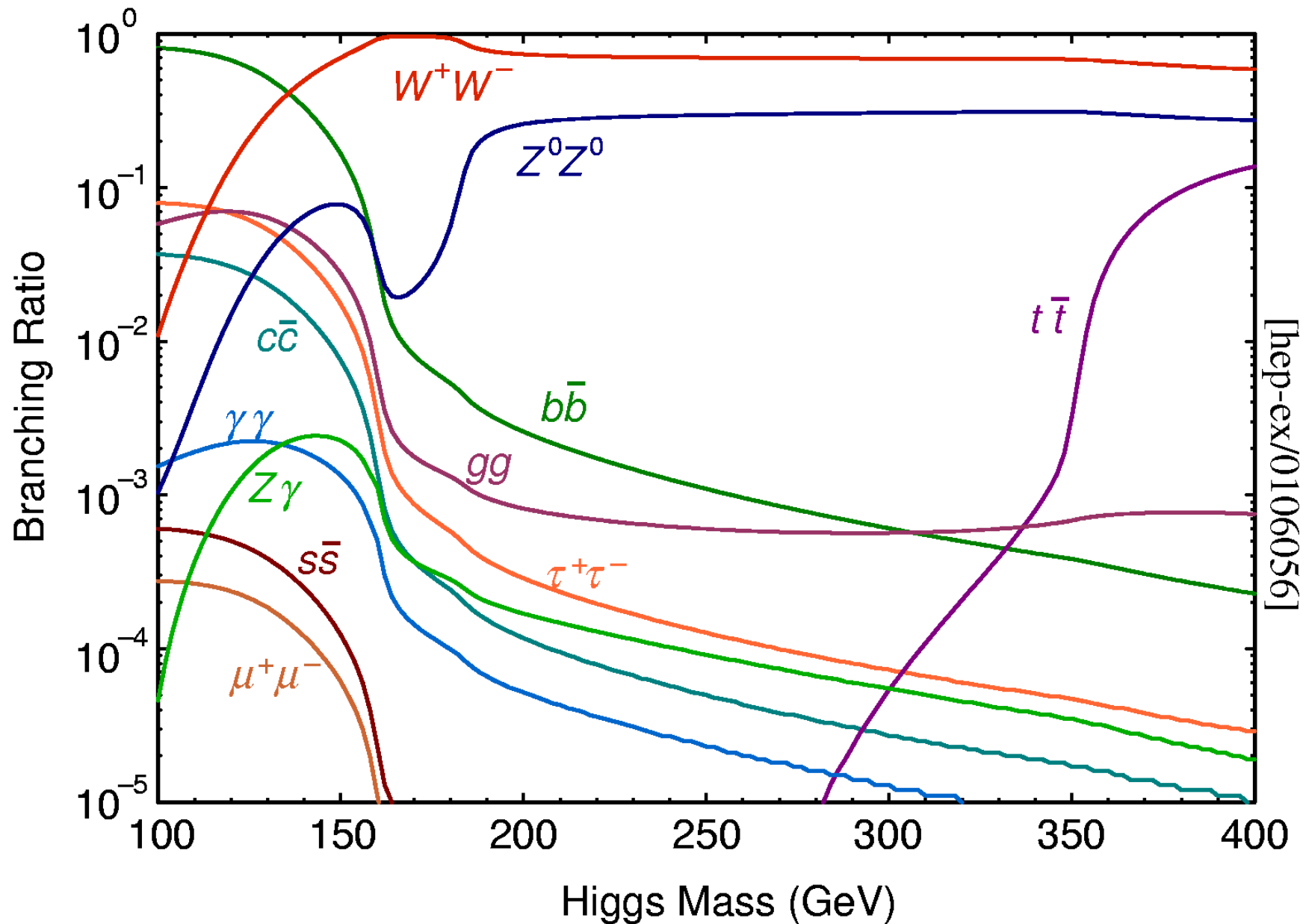


Higgs Production at the LHC

The most important channels are gluon fusion, WBF and $t\bar{t}H$.

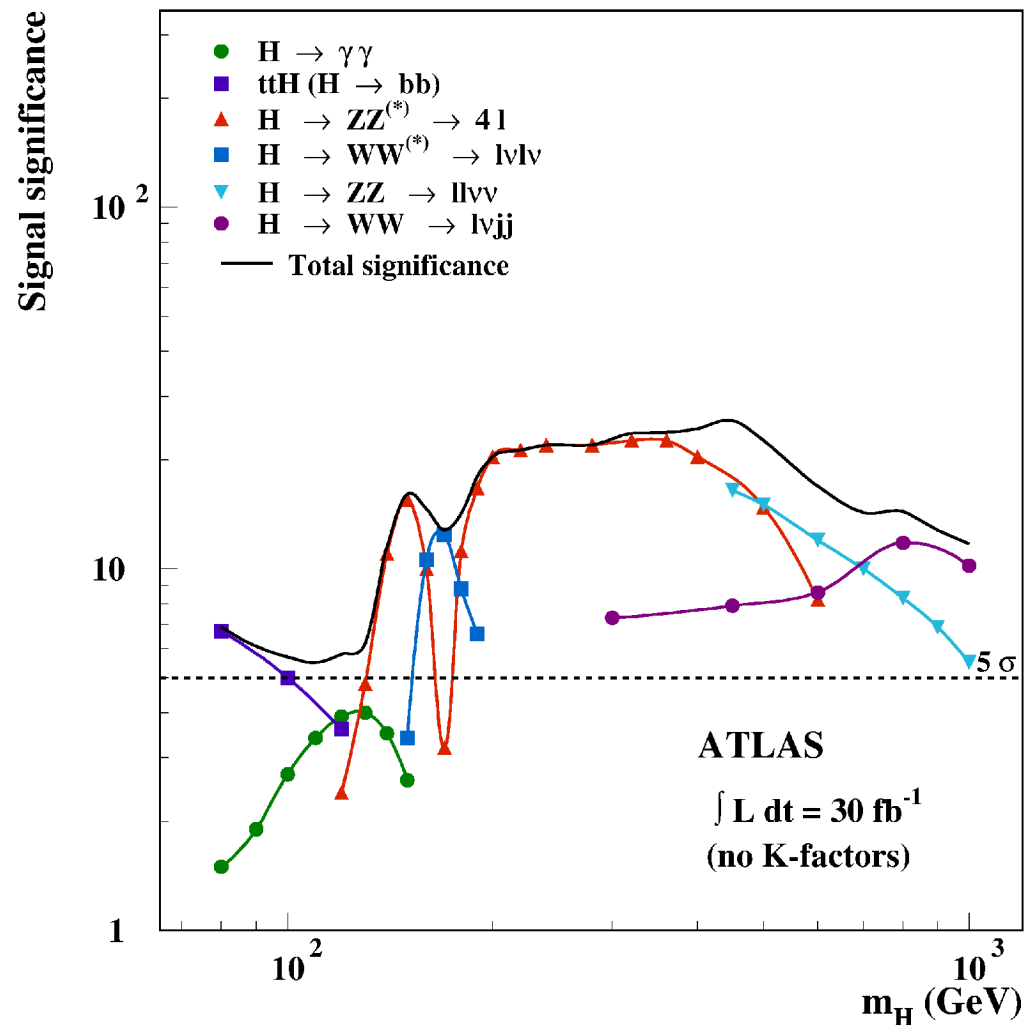


Higgs Branching Ratios



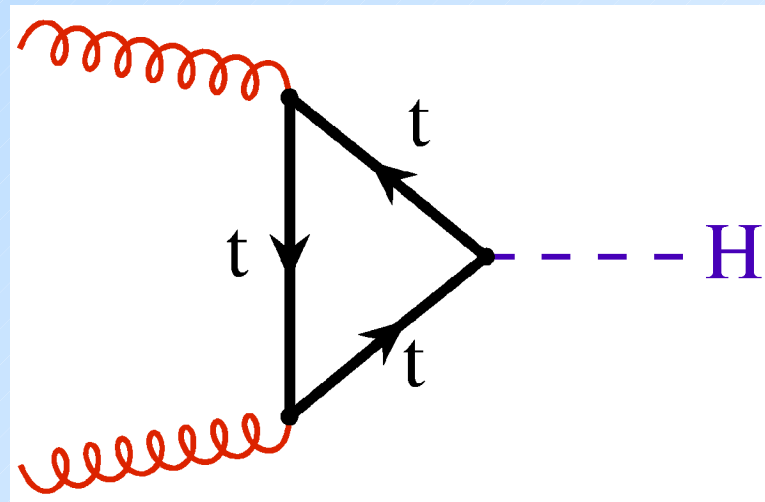
Higgs Discovery requires that you detect the decay products

Inclusive production with decay to $b\bar{b}$ is swamped by QCD production, so we must use rare decays or associated production below the W^+W^- threshold.



Gluon Fusion Dominates Higgs Production

The Higgs boson couples to mass and comes from an electroweak doublet. It seems curious that its production is dominated by gluons, the massless gauge bosons of QCD. The reason: top loops.



The problem for theorists, however, is top loops.

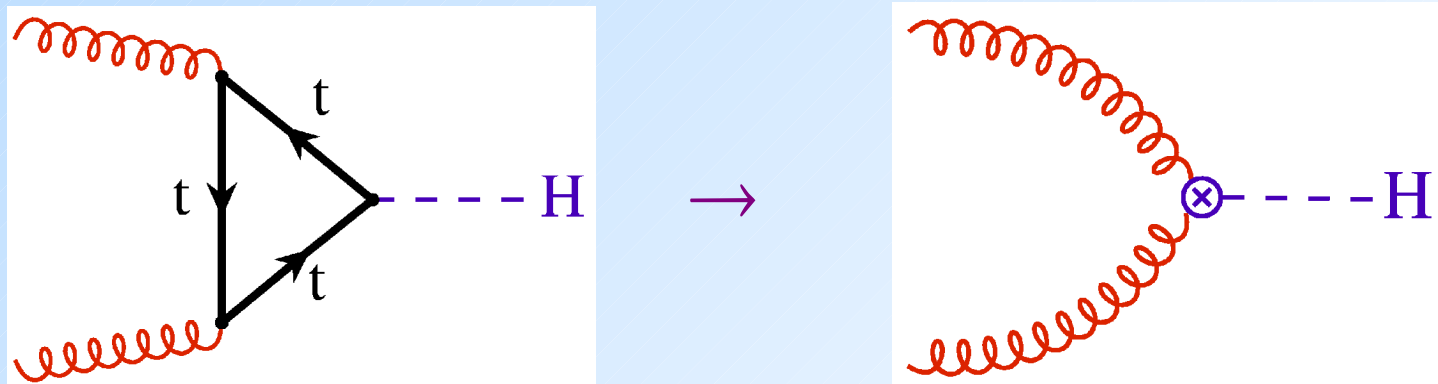
Effective Lagrangian

In the limit that the top quark is very heavy and all other quarks are massless, we can integrate out the top and formulate an effective Lagrangian coupling the Higgs to Gluons.

$$\mathcal{L} = C_1 H G^{\mu\nu} G_{\mu\nu}$$

C_1 has been computed to order α_s^4 ! Chetyrkin, Kniehl, Steinhauser

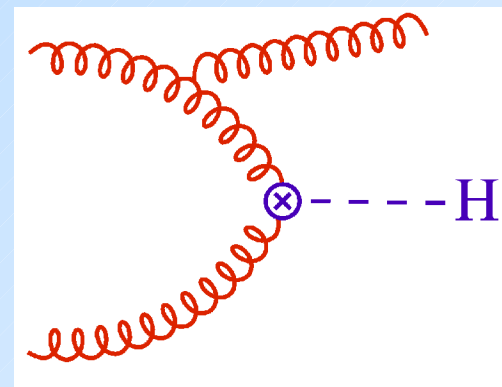
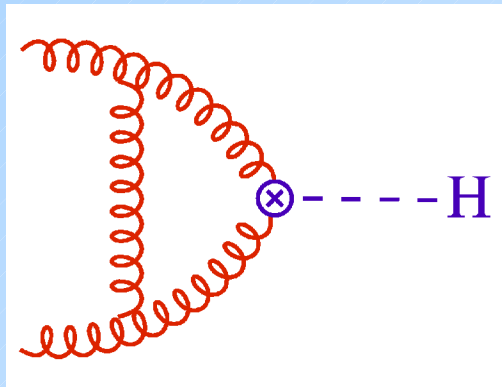
Using the effective Lagrangian greatly simplifies the calculation of radiative corrections.



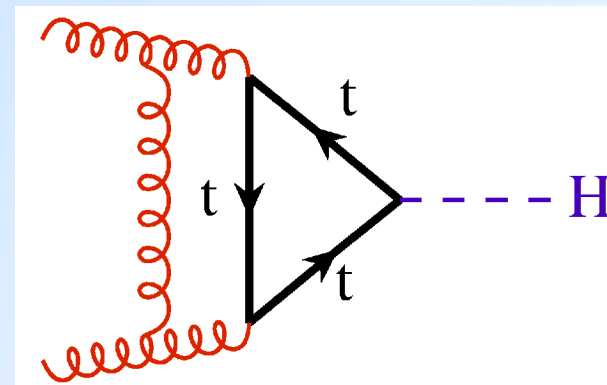
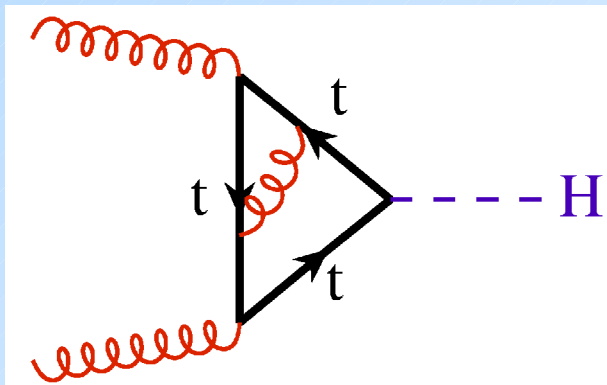
Higher Order Corrections

NLO Corrections have been computed in both the effective Lagrangian

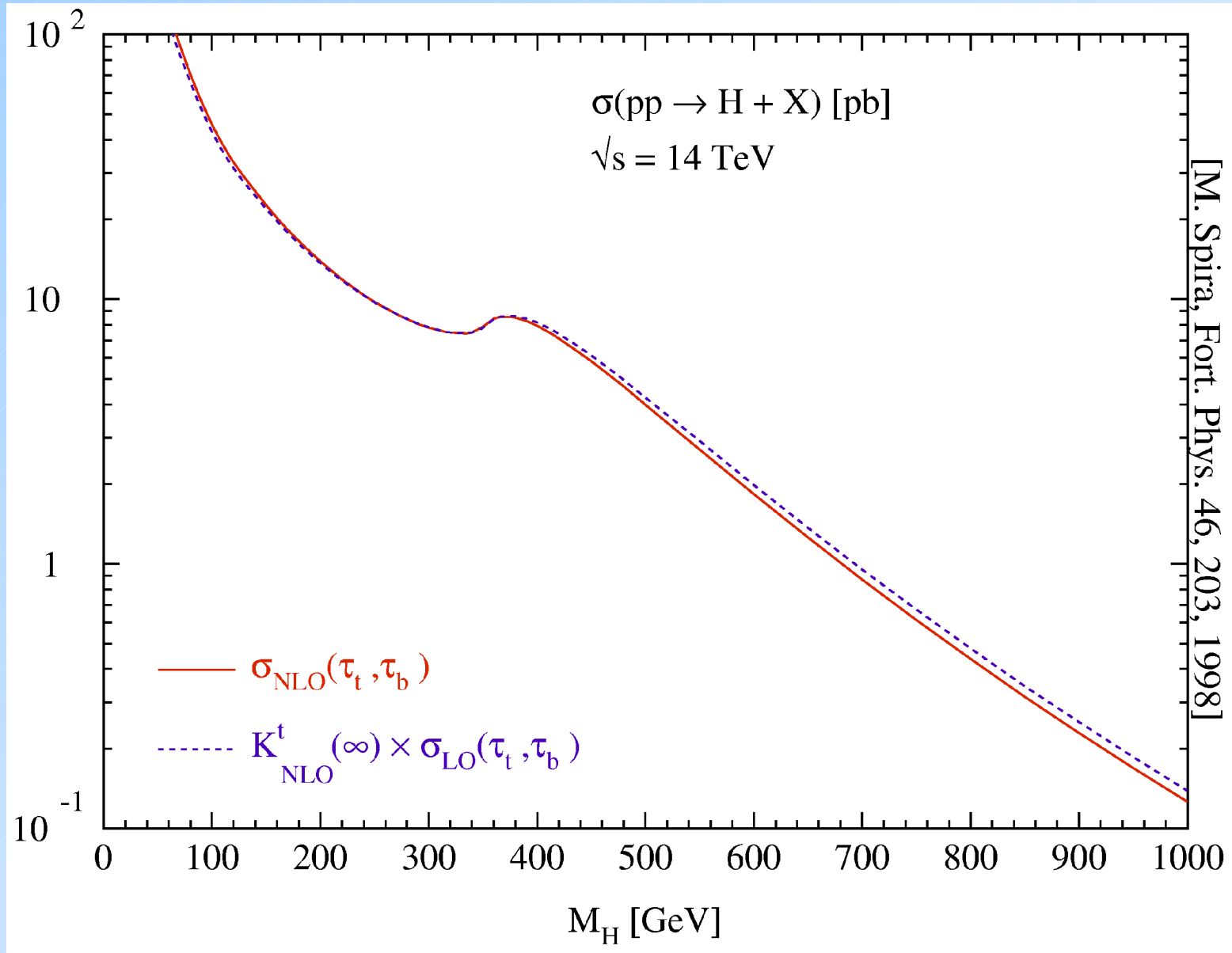
Dawson; Djouadi, Spira, Graudenz, Zerwas



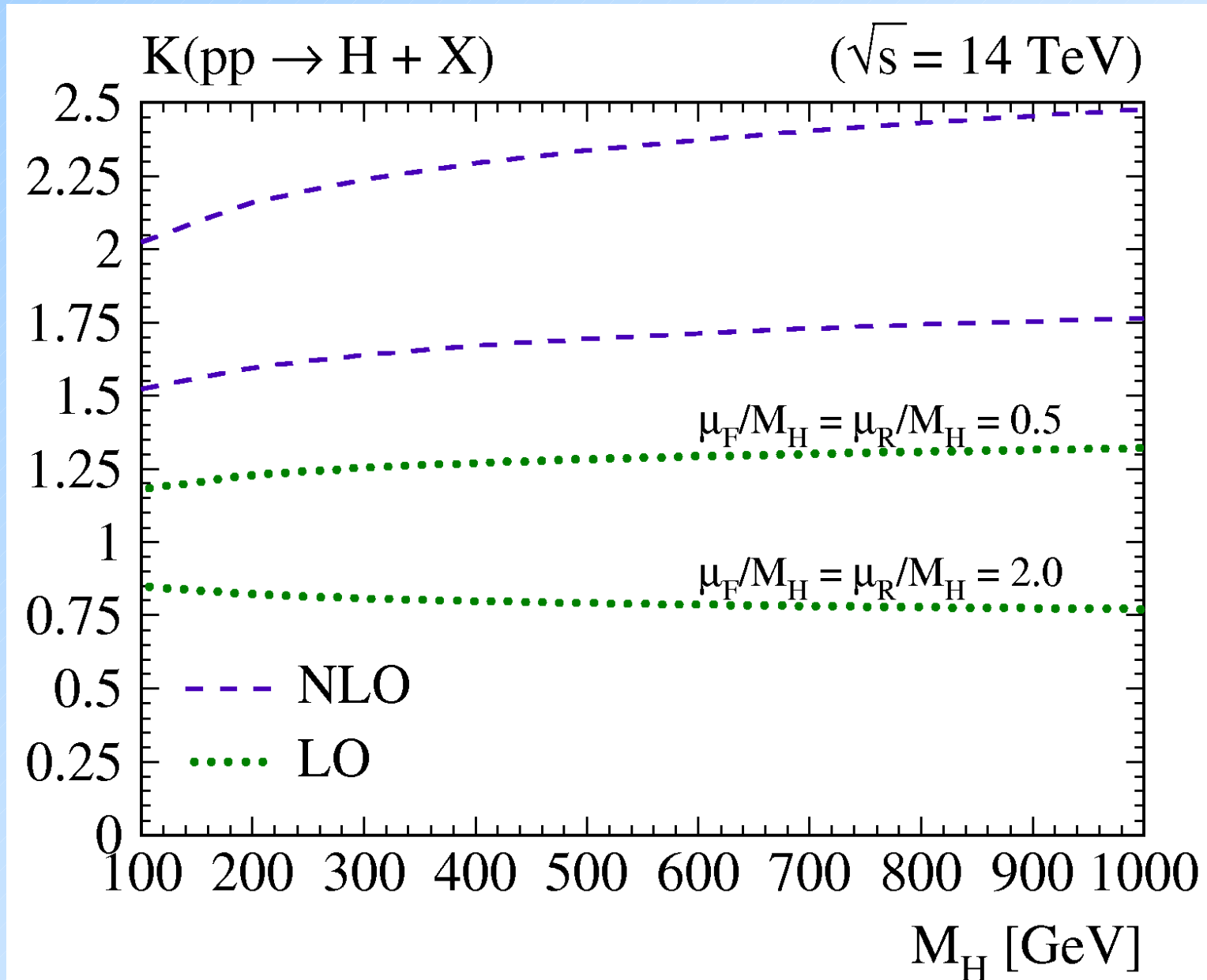
and in the full theory. Djouadi, Spira, Graudenz, Zerwas



They agree extremely well

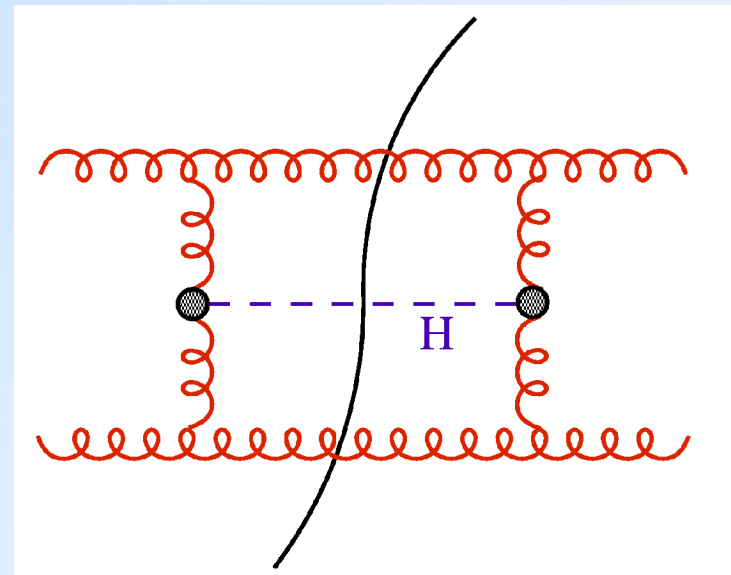
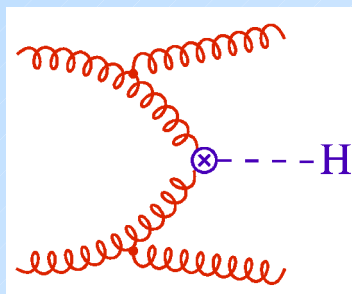
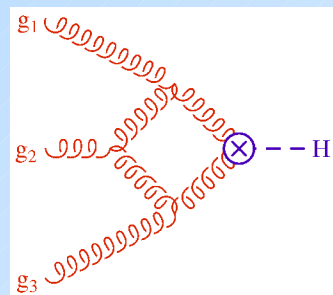
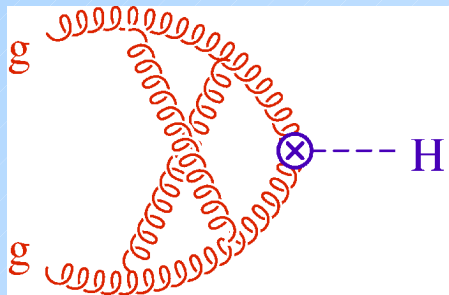


So why do we want NNLO?



Higgs Production at NNLO

In recent years, the Higgs production cross section has been computed to NNLO in the effective theory by three groups using very different methods.



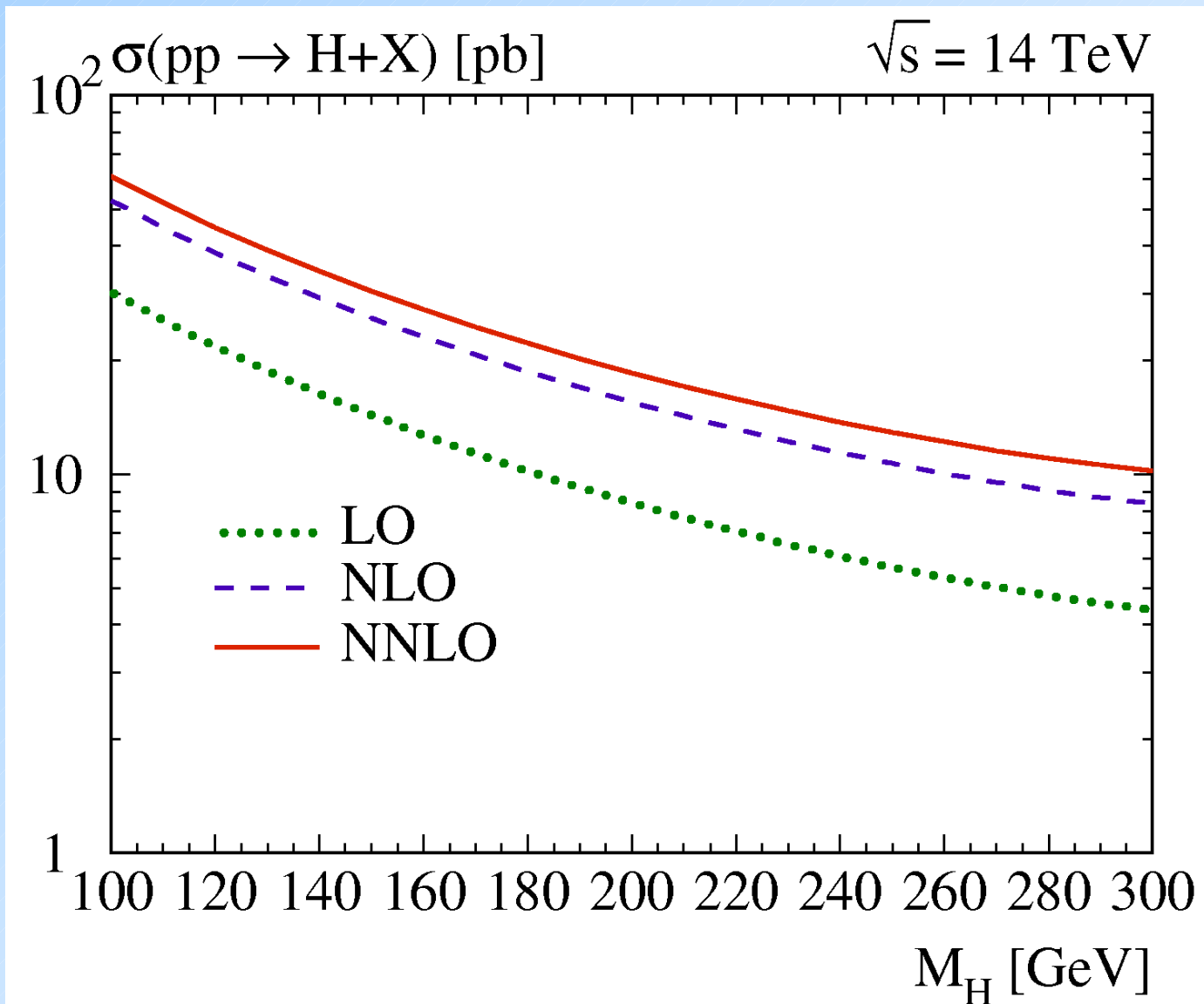
Harlander, WK;
Ravindran, Smith, van Neerven

Anastasiou & Melnikov

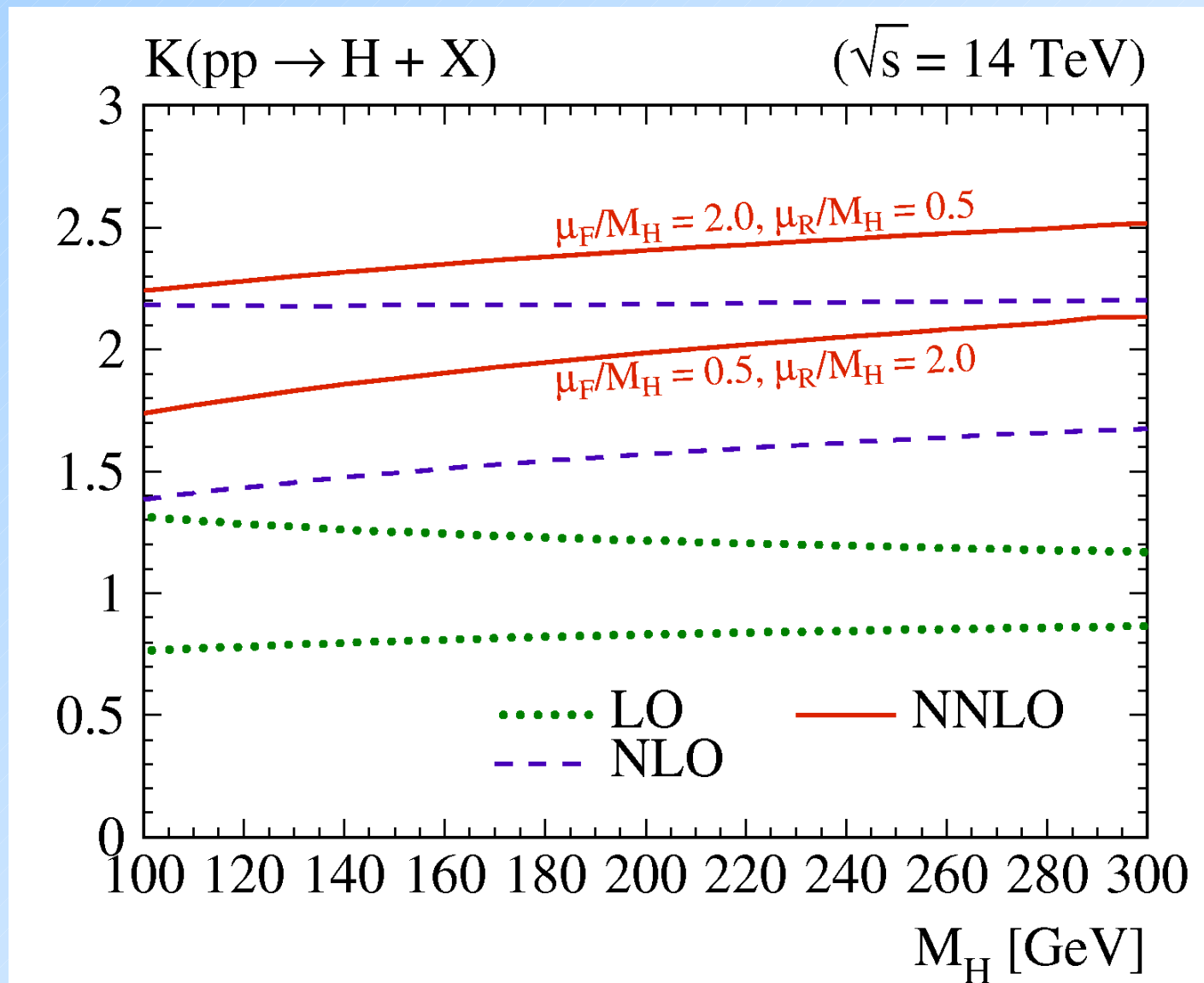
All groups agree exactly

$$\begin{aligned}
 \Delta_{ggA}(x) = & \left[\frac{741}{8} + \frac{139}{2} \zeta_2 - \frac{165}{4} \zeta_3 - \frac{9}{20} \zeta_2^2 \right] \delta(1-x) - \left[\frac{101}{3} - 33 \zeta_2 - \frac{351}{2} \zeta_3 \right] \mathcal{D}_0(x) + [139 - 90 \zeta_2] \mathcal{D}_1(x) - 33 \mathcal{D}_2(x) + 72 \mathcal{D}_3(x) \\
 & - (144x - 72x^2 + 72x^3) \ln^3(1-x) - (297 - 381x + 348x^2 - 330x^3) \ln^2(1-x) - \frac{9(31 - 30x + 93x^2 - 94x^3 + 31x^4)}{2(1-x)} \ln^2(1-x) \ln(x) \\
 & + \left[\frac{(2027 - 2735x + 2182x^2 - 2583x^3)}{4} + (180x - 90x^2 + 90x^3) \zeta_2 \right] \ln(1-x) + 3 \frac{(88 - 211x + 312x^2 - 365x^3 + 187x^4)}{1-x} \ln(1-x) \ln(x) \\
 & + 9 \frac{(7 + 3x + 19x^2 - 3x^3 - 19x^4 + 9x^5)}{1-x^2} \ln(1-x) \ln^2(x) + 36 \frac{(1 - 6x - 13x^2 - 6x^3 + x^4)}{1+x} \ln(1-x) \text{Li}_2(1-x) \\
 & - 18 \frac{(1 + 2x + 3x^2 + 2x^3 + x^4)}{1+x} \ln(1-x) \text{Li}_2(1-x^2) - \frac{9(24 - 38x + 8x^2 + 54x^3 - 19x^4 + 9x^5)}{2(1-x^2)} \text{Li}_3(1-x) \\
 & - \frac{9(27 + 35x + 75x^2 - 29x^3 - 78x^4 + 6x^5)}{2(1-x^2)} \text{Li}_3\left(-\frac{(1-x)}{x}\right) + \frac{9(1 + 2x + 3x^2 + 24x^3 + 16x^4)}{8(1+x)} \text{Li}_3(1-x^2) \\
 & - \frac{9(1 + 2x + 3x^2 - 8x^3 - 8x^4)}{8(1+x)} \text{Li}_3\left(-\frac{(1-x^2)}{x^2}\right) - \frac{9(7 + 14x + 21x^2 + 8x^3 + 4x^4)}{2(1+x)} \left[\text{Li}_3\left(\frac{1-x}{1+x}\right) - \text{Li}_3\left(-\frac{1-x}{1+x}\right) \right] \\
 & - \frac{3(317 - 398x - 87x^2 + 300x^3 - 121x^4)}{4(1-x)} \text{Li}_2(1-x) + \frac{9(11 + 31x + 59x^2 - 25x^3 - 65x^4 + 11x^5)}{2(1-x^2)} \text{Li}_2(1-x) \ln(x) \\
 & + \frac{(42 + 36x - 63x^2 - 33x^3)}{4} \text{Li}_2(1-x^2) + \frac{9(5 + 10x + 15x^2 - 2x^4)}{4(1+x)} \text{Li}_2(1-x^2) \ln(x) + \frac{3(21 + 23x + 41x^2 - 37x^3 - 44x^4 + 4x^5)}{4(1-x^2)} \ln^3(x) \\
 & - \frac{3(154 - 365x + 675x^2 - 827x^3 + 374x^4)}{8(1-x)} \ln^2(x) - \frac{1(2213 - 5599x + 6603x^2 - 7003x^3 + 4342x^4)}{8(1-x)} \ln(x) \\
 & + 9 \frac{(9 - 2x + 27x^2 - 34x^3 + 9x^4)}{1-x} \zeta_2 \ln(x) - \frac{(16309 - 20611x + 23819x^2 - 22749x^3)}{48} + \frac{3}{4} (319 - 277x + 233x^2 - 363x^3) \zeta_2 - \frac{351}{2} (2x - x^2 + x^3) \zeta_3 \\
 & + n_f \left\{ \left[-\frac{689}{72} + l_{Ht} - \frac{5}{3} \zeta_2 + \frac{5}{6} \zeta_3 \right] \delta(1-x) + \left[\frac{14}{9} - 2 \zeta_2 \right] \mathcal{D}_0(x) - \frac{10}{3} \mathcal{D}_1(x) + 2 \mathcal{D}_2(x) - \frac{2}{9} (8 - 12x + 3x^2 - 17x^3) \zeta_2 \right. \\
 & + \frac{2}{9} (8 - 12x + 3x^2 - 17x^3) \ln^2(1-x) + \frac{8}{3} (x + x^2) \ln^2(1-x) \ln(x) - \frac{(922 - 294x + 249x^2 - 1570x^3)}{108} \ln(1-x) \\
 & - \frac{2(17 + 7x + 21x^2 - 61x^3 + 25x^4)}{9(1-x)} \ln(1-x) \ln(x) - \frac{8}{3} (x + x^2) \ln^2(x) \ln(1-x) + \frac{16}{3} (x + x^2) \ln(1-x) \text{Li}_2(1-x) \\
 & - \frac{(2 + 14x + 17x^2)}{6} \text{Li}_3(1-x) - \frac{(2 - 34x - 31x^2)}{12} \text{Li}_3\left(-\frac{(1-x)}{x}\right) + \frac{1}{36} \frac{(68 - 302x + 21x^2 + 227x^3 + 4x^4)}{1-x} \text{Li}_2(1-x) \\
 & + \frac{(2 - 50x - 47x^2)}{12} \text{Li}_2(1-x) \ln(x) + \frac{(2 + 6x + 9x^2)}{72} \ln^3(x) + \frac{1}{72} \frac{(68 + 100x + 69x^2 - 351x^3 + 132x^4)}{1-x} \ln^2(x) \\
 & \left. + \frac{1}{216} \frac{(1282 - 382x + 117x^2 - 3041x^3 + 2384x^4)}{1-x} \ln(x) - \frac{8}{3} (x + x^2) \zeta_2 \ln(x) + \frac{(12707 - 606x + 1641x^2 - 17774x^3)}{1296} \right\}
 \end{aligned}$$

Higgs Cross Section at NNLO

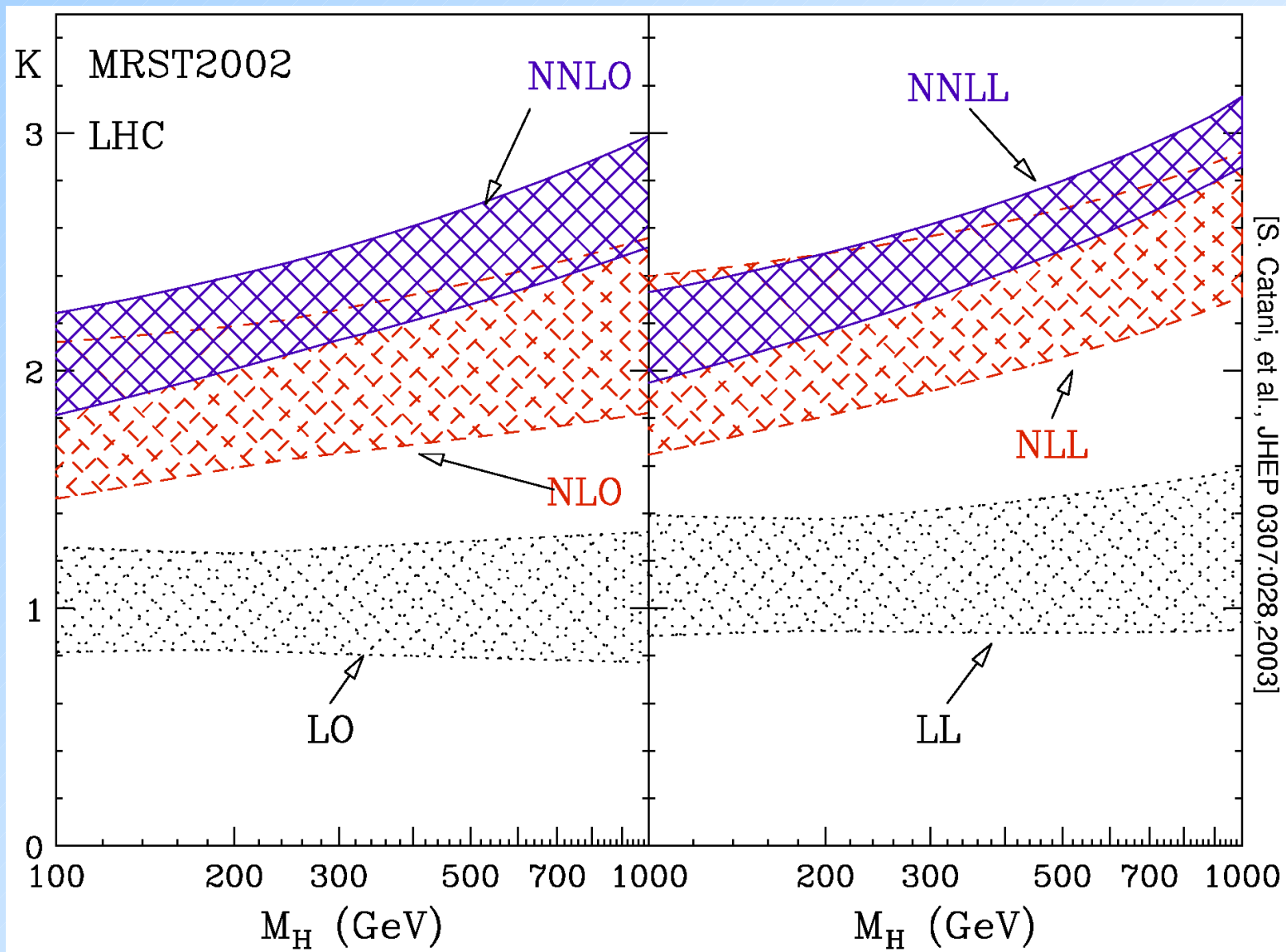


Scale Dependence is still large

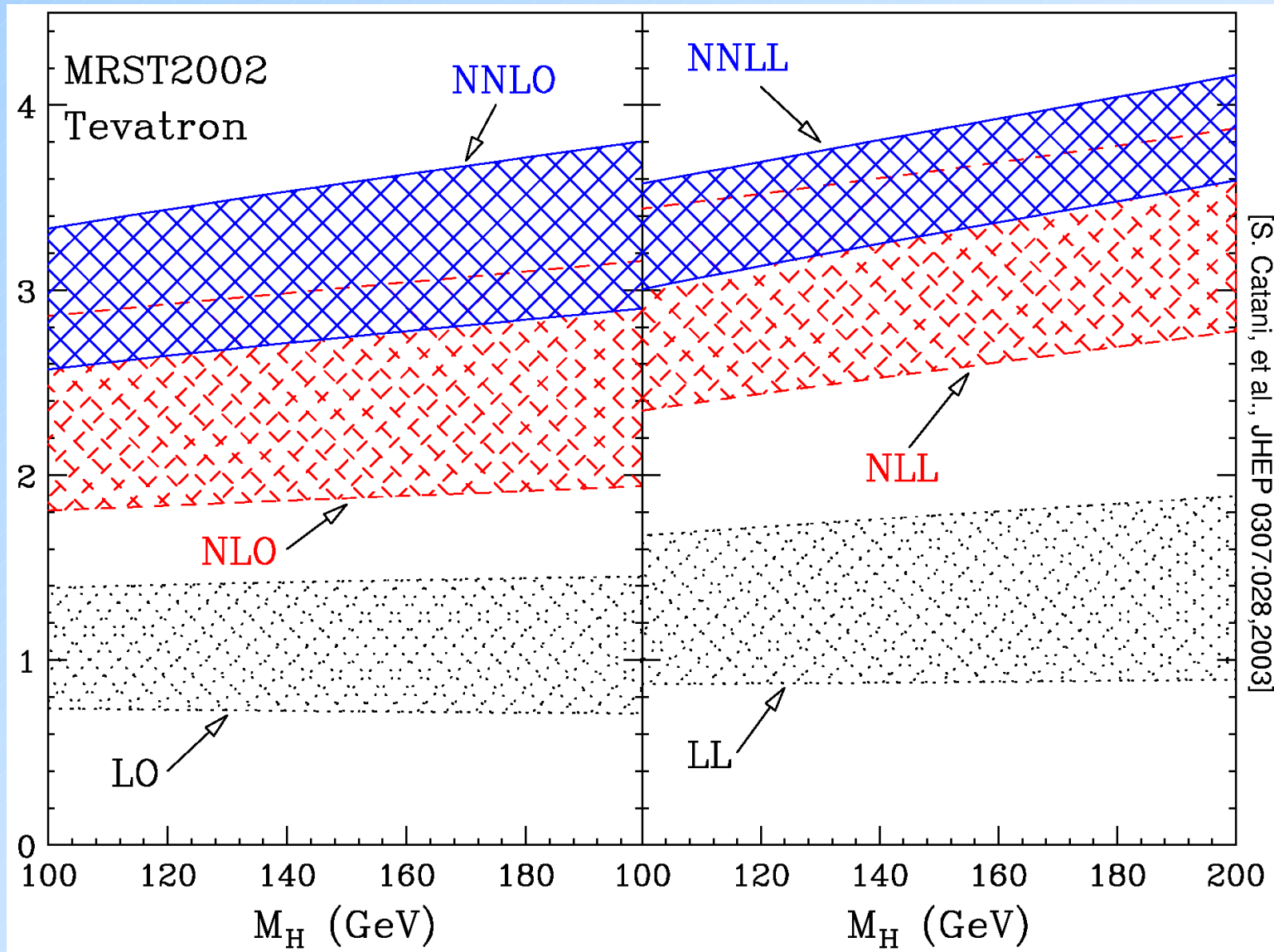


Threshold resummation at the LHC

Catani, de Florian, Grazzini, Nason



Threshold Resummation at the Tevatron

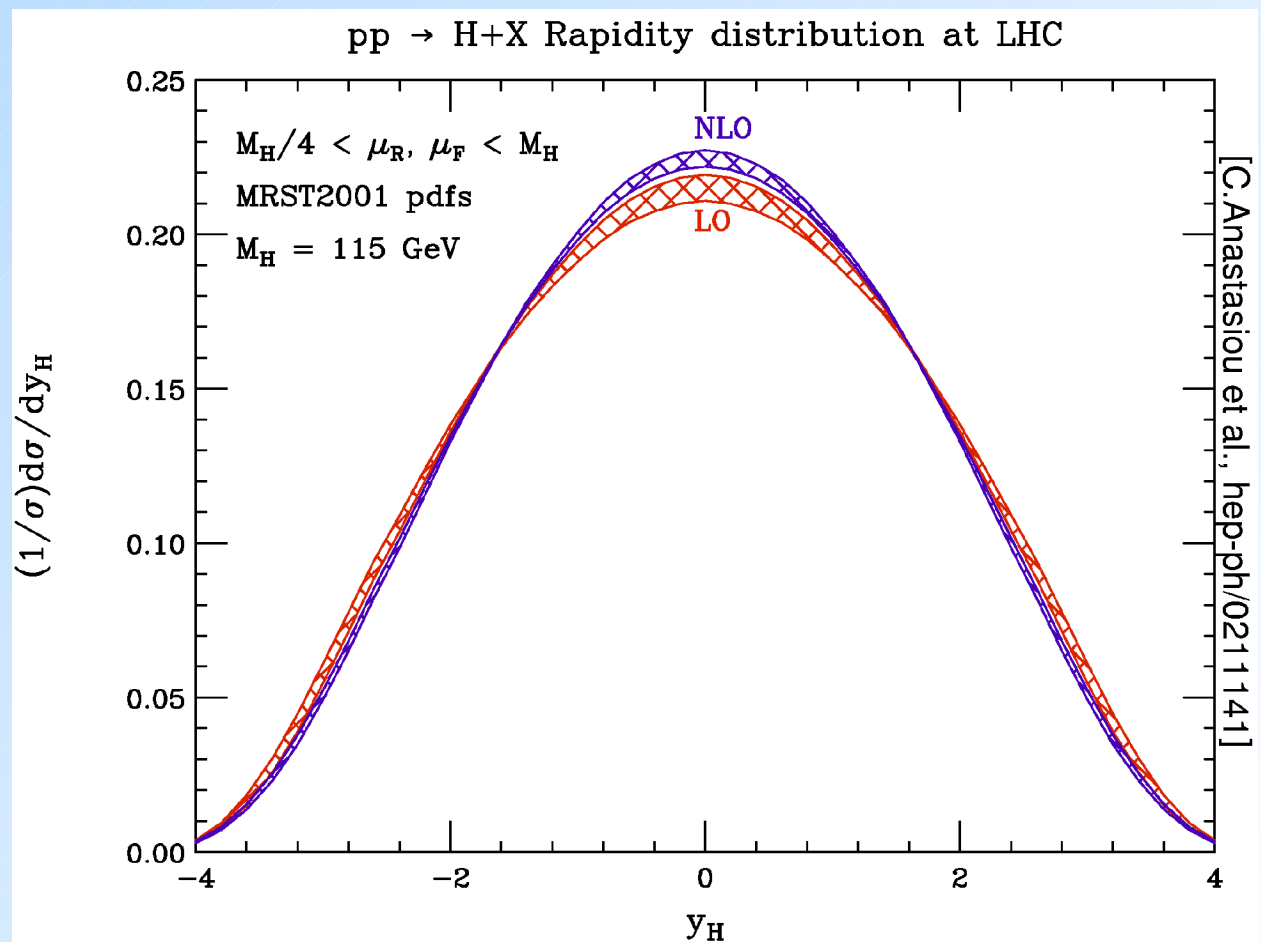


Higgs Distributions at NNLO

Using the cutting method, NNLO distributions can be computed.

Anastasiou, Dixon, Melnikov, Petriello

NNLO distributions
for Drell-Yan exist,
only NLO for Higgs
so far.



Higgs at Finite Q_T

Signal identification as well as the signal to background ratio can be improved by looking at Higgs production at finite Q_T . In the effective theory, this has been computed to NLO.

de Florian, Grazzini, Kunszt; Ravindran, Smith, van Neerven; Glosser, Schmidt

The background process $\gamma\gamma + \text{jet}$ has also been computed to NLO

Del Duca, Maltoni, Nagy, Trócsányi

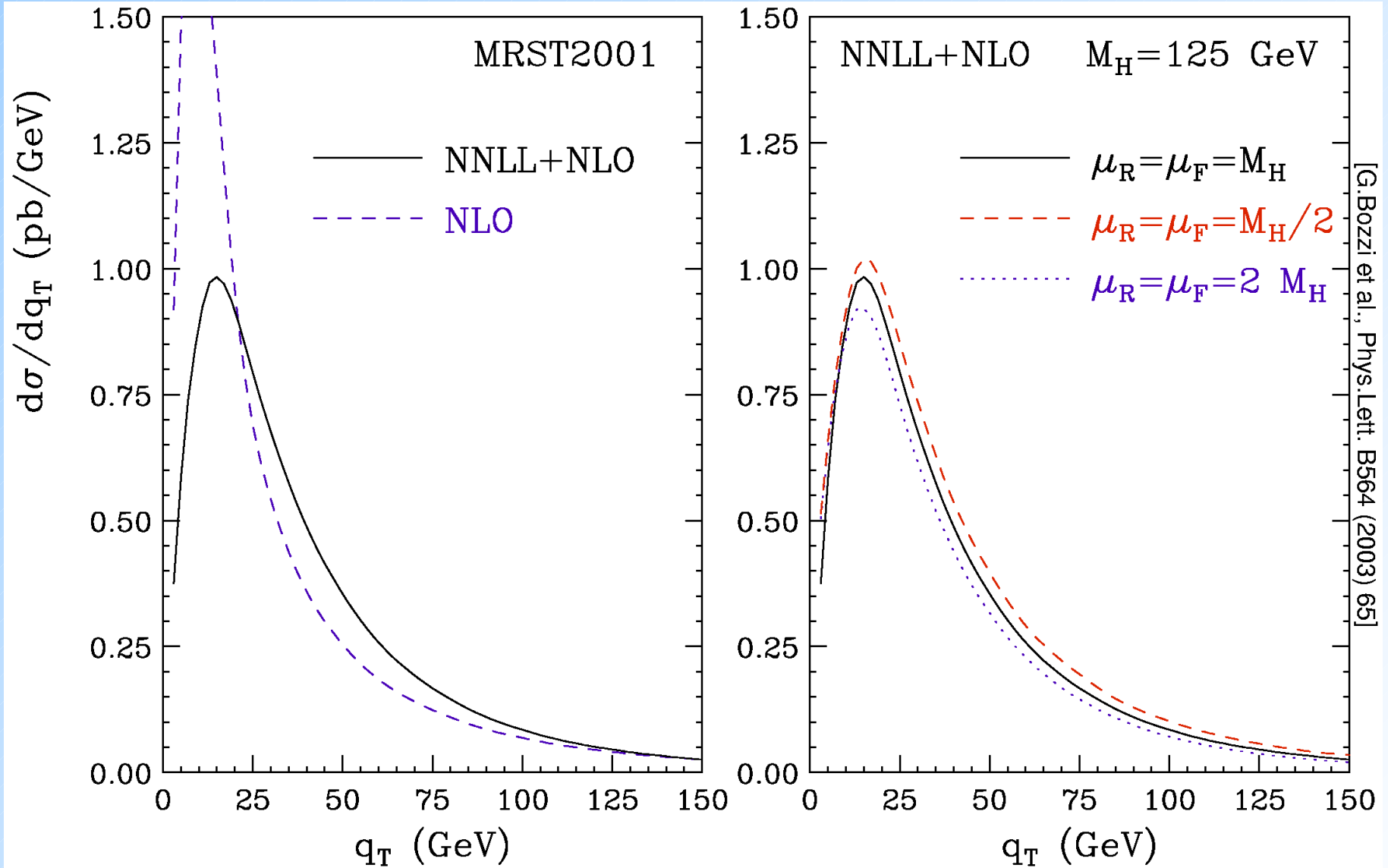
The Higgs Q_T can be resummed alone

Balázs, Yuan; Berger, Qiu; Bozzi, Catani, de Florian, Grazzini

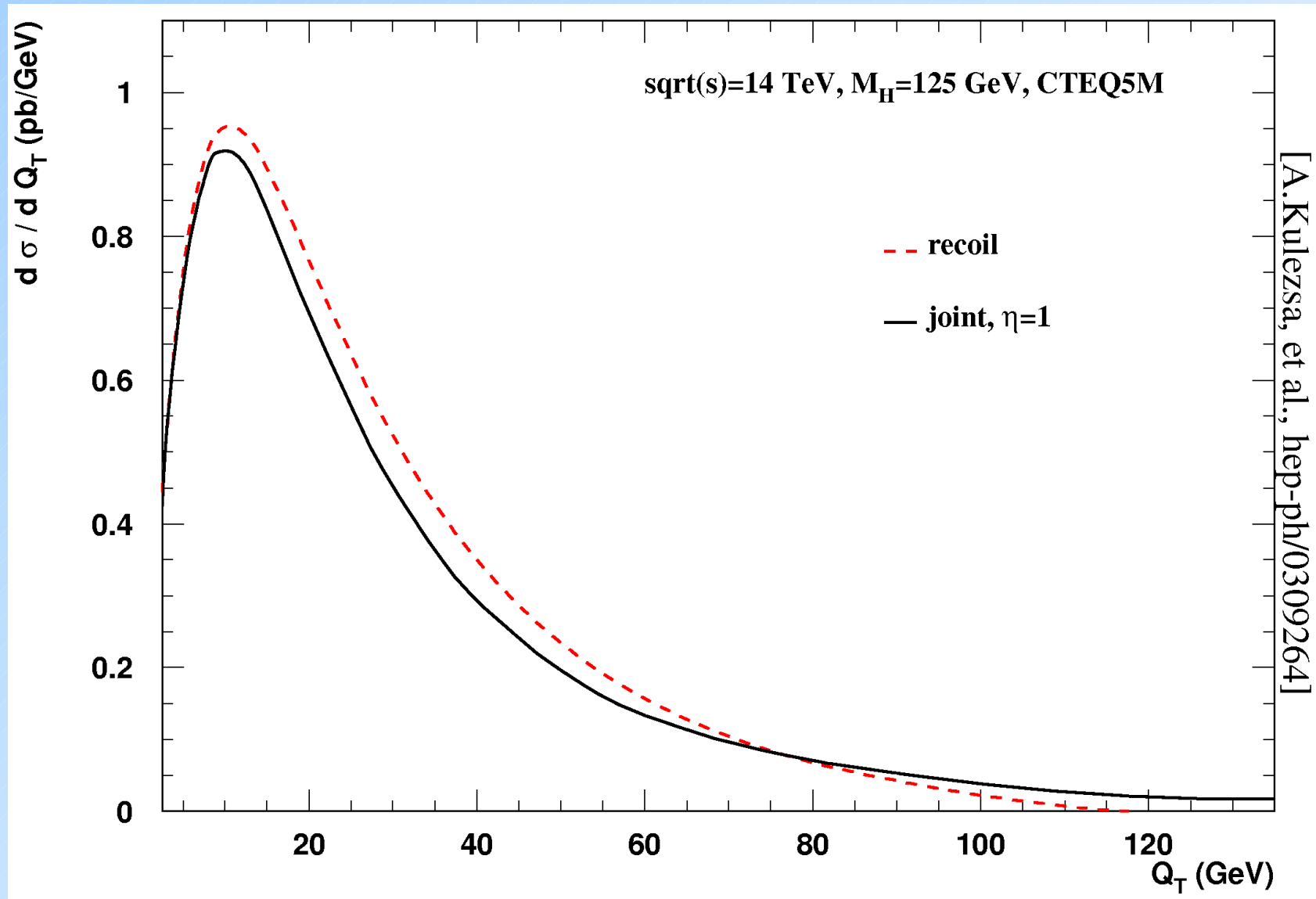
or in conjunction with threshold resummation

Kulesza, Sterman, Vogelsang

Q_T Resummation



Joint Threshold and Q_T Resummation



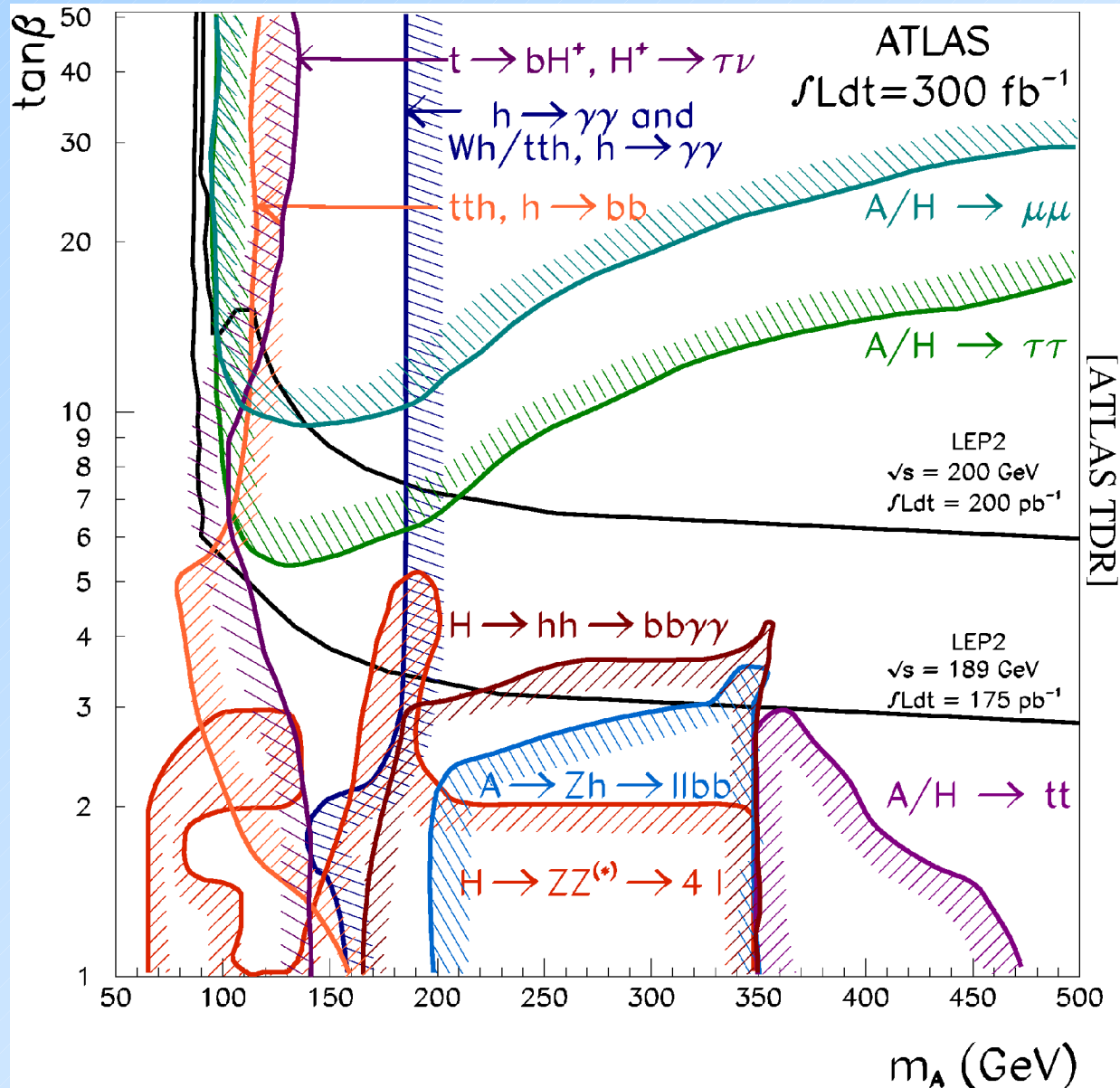
Supersymmetric Higgs Boson Production

In the Minimal Supersymmetric Standard Model (MSSM) there are two Higgs doublets, with vacuum expectation values v_u, v_d . After symmetry breaking, there are 5 physical Higgs Scalars:

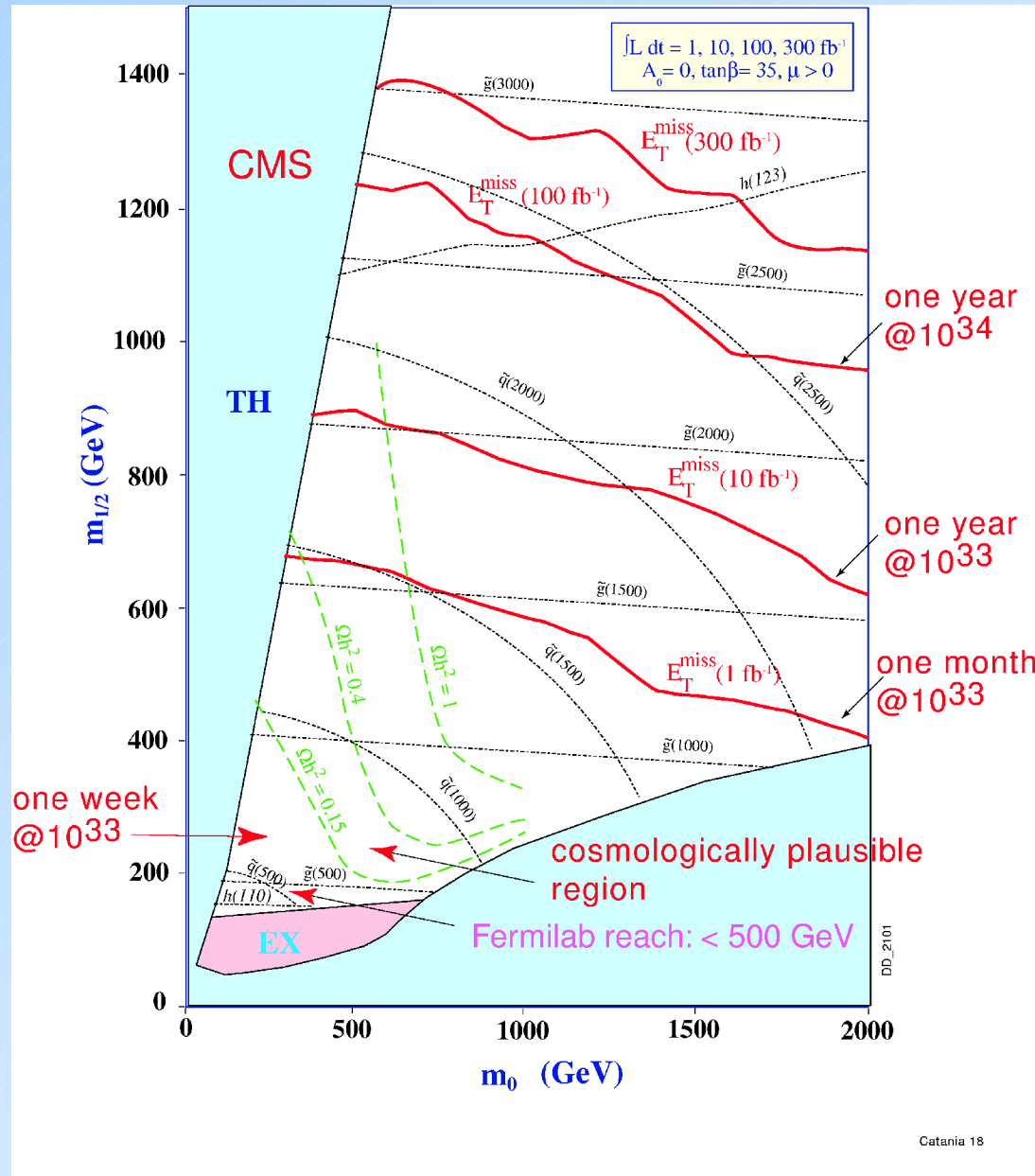
$$h^0, H^0, A^0, H^\pm$$

In the "decoupling" limit, the light neutral scalar, h^0 , has properties almost identical to the Standard Model Higgs. The heavy scalar, H^0 , and the pseudoscalar, A^0 , have very different interactions.

Finding SUSY Higgs 'at LHC



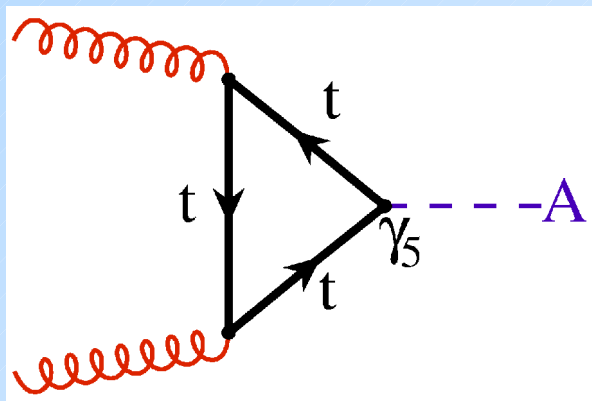
We will likely see super-partners first



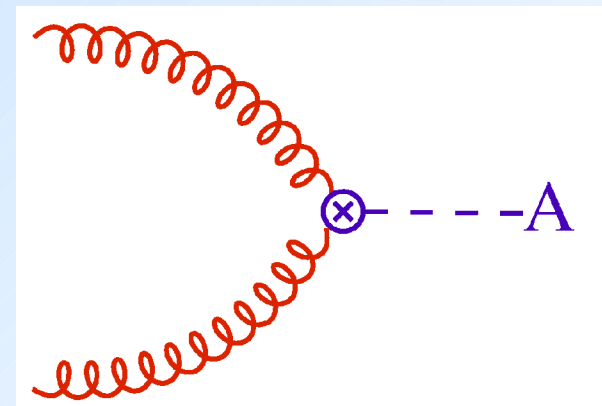
Pseudoscalar Production

Gluon fusion is also very important to pseudoscalar production and can also be described by an effective Lagrangian in which the top quark is integrated out. This effective Lagrangian coupling the pseudoscalar to gluons is:

$$\mathcal{L} = C_1 A \varepsilon_{\alpha\beta\mu\nu} G^{a\alpha\beta} G^{a\mu\nu} + \dots$$



\rightarrow



SUSY Higgs Production

SUSY Higgs production has also been computed using massive fermions to NLO.

Spira, Djouadi, Graudenz, Zerwas

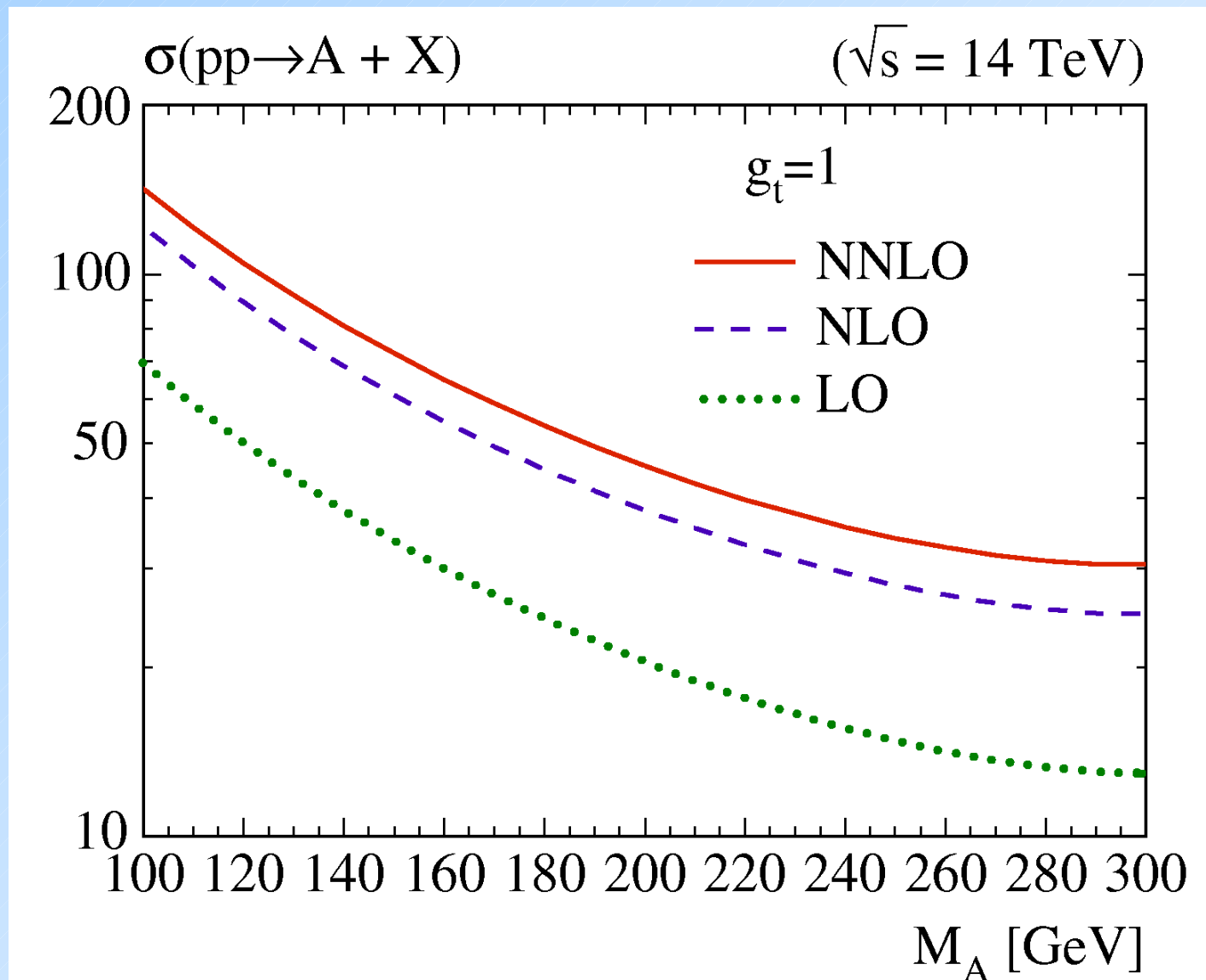
NNLO Pseudoscalar production is computed in the same way as scalar production. But the effective Lagrangians are only valid for top quark loops! The same three groups again obtained exact analytic agreement.

Harlander, WK; Anastasiou, Melnikov; Ravindran, Smith, van Neerven

For scalar Higgs production in SUSY, you can also add squark/gluino effects.

Harlander, Steinhauser; Dawson, Djouadi, Spira

Pseudoscalar Production in Gluon Fusion



H/A Couplings

For the pseudoscalar (and for H^0 in the decoupling limit) the couplings to "up-type" fermions are suppressed by $\tan \beta \equiv v_u/v_d$ while those to "down-type" fermions are enhanced by $\tan \beta$. This presents a problem for gluon fusion calculations:

For $\tan \beta$ significantly larger than 1, b-quark interactions are important. But ... one cannot formulate an effective Lagrangian by integrating out the b-quark to produce ~ 100 GeV Higgs bosons! An NNLO calculation would require massive 3-loop diagrams.

A new production mode at large $\tan \beta$

The importance of b-quark couplings at large $\tan \beta$ suggests a new inclusive production mechanism:

$$b\bar{b} \rightarrow H$$

Since b-quark distributions are generated by gluon splitting the true parent process is

$$gg \rightarrow b\bar{b}H$$

The b-quark distribution resums large logs associated with the gluon splitting, but is fully consistent only if calculated to high enough order to include the parent process.

In this case, one must compute to NNLO.

$b\bar{b} \rightarrow H/A$ at NNLO

We ignore the b-quark mass in our calculation, except where it enters into the Yukawa couplings. Other b-quark mass effects are suppressed by factors of m_b^2/M_H^2 .

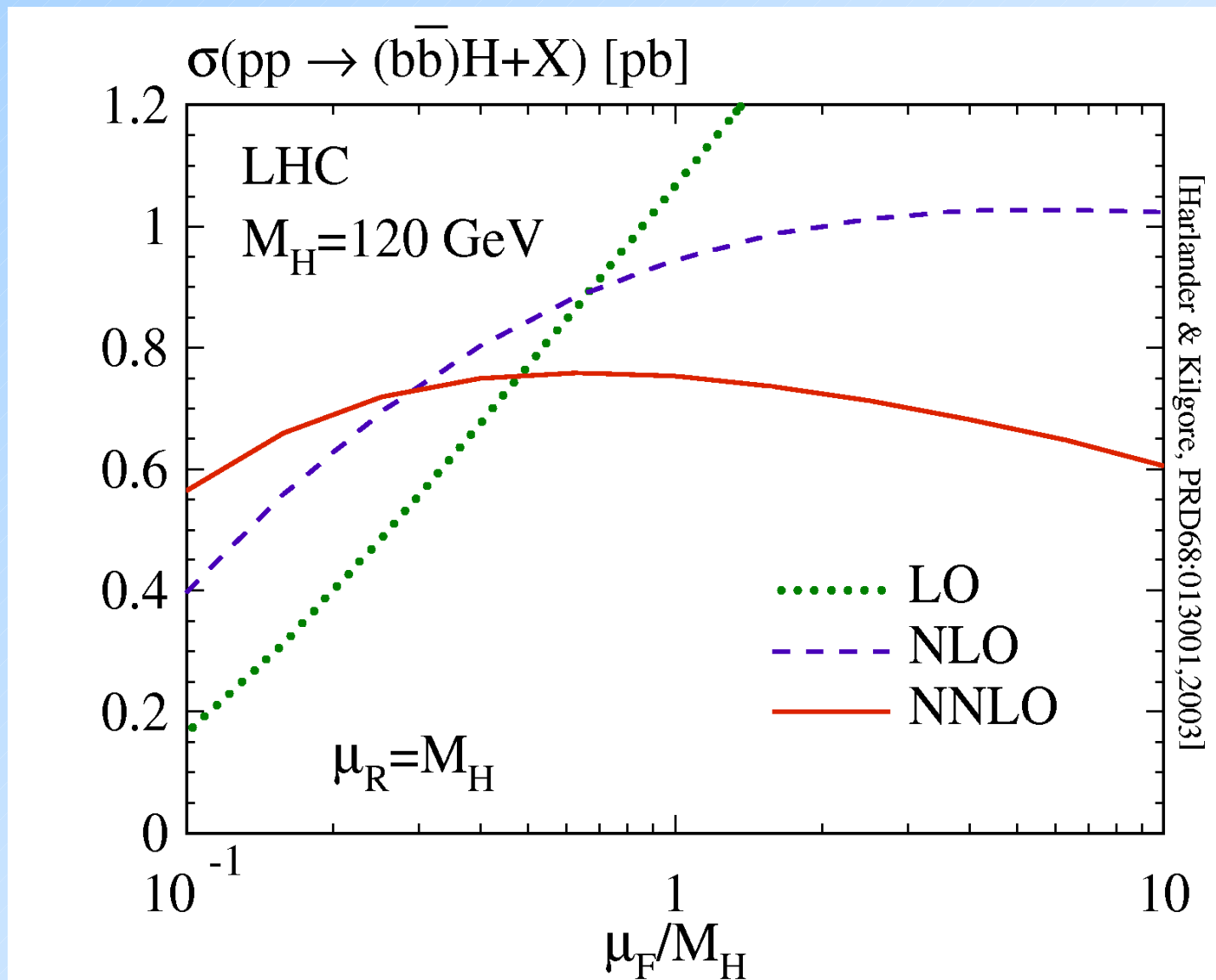
In the $m_b \rightarrow 0$ limit, the partonic cross sections for $b\bar{b} \rightarrow H$ are identically equal to those for $b\bar{b} \rightarrow A$.

$b\bar{b} \rightarrow H/A$ can dominate at large $\tan \beta$ because

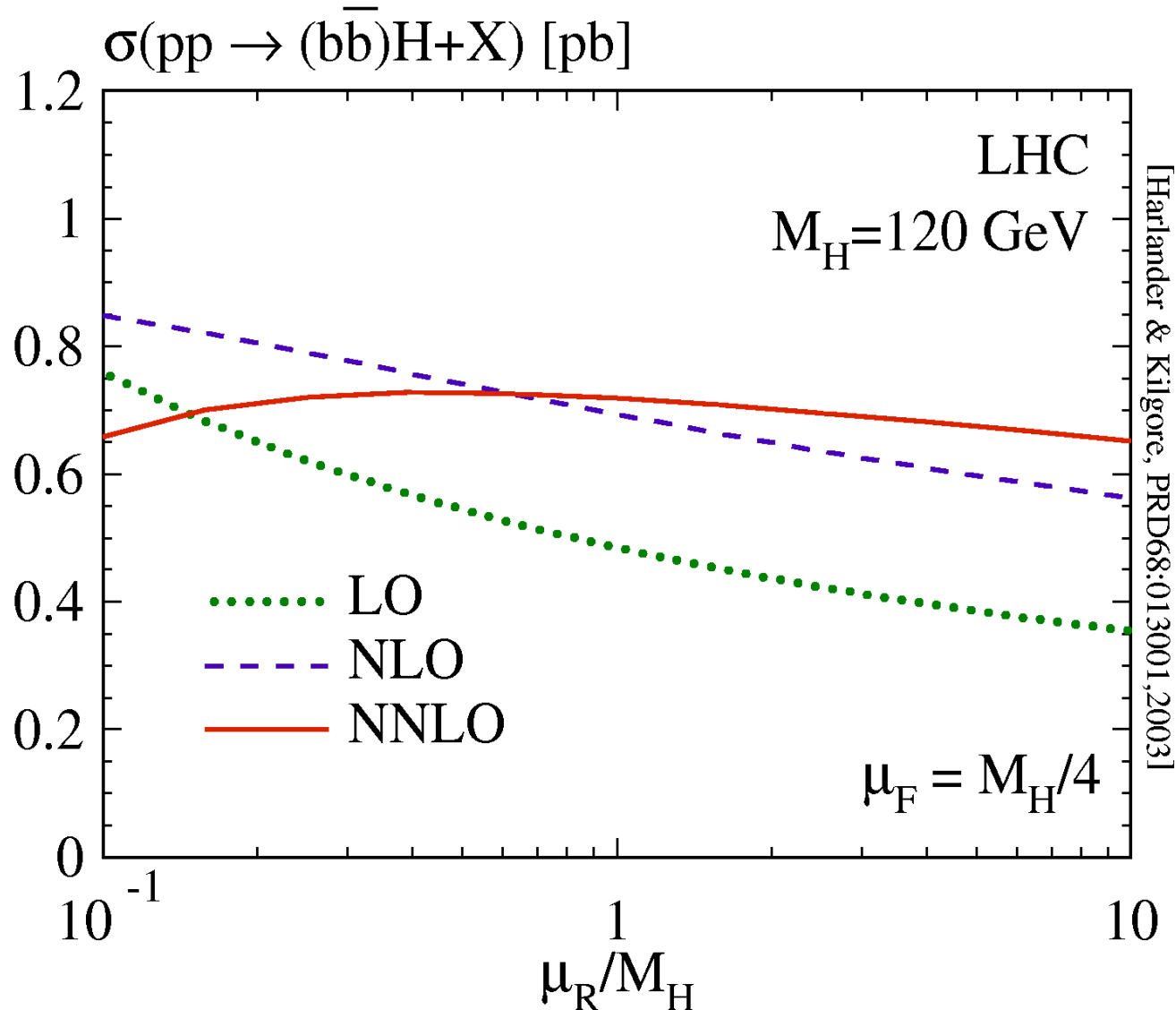
$$\sigma_{bb} \sim m_b^2/M_H^2 \tan^2 \beta \quad \text{while}$$

$$\sigma_{gg} \sim A \cot^2 \beta + B m_b^2/M_H^2 + C m_b^4/M_H^4 \tan^2 \beta$$

Factorization Scale Dependence of $b\bar{b} \rightarrow H/A$ at LHC



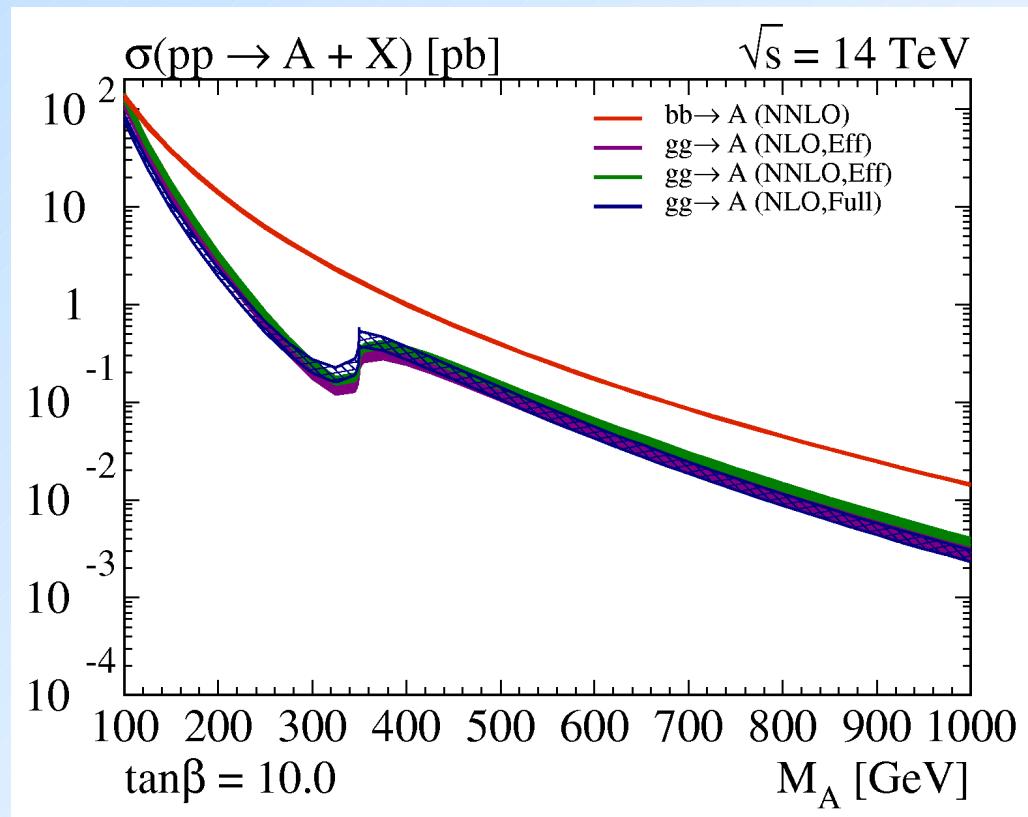
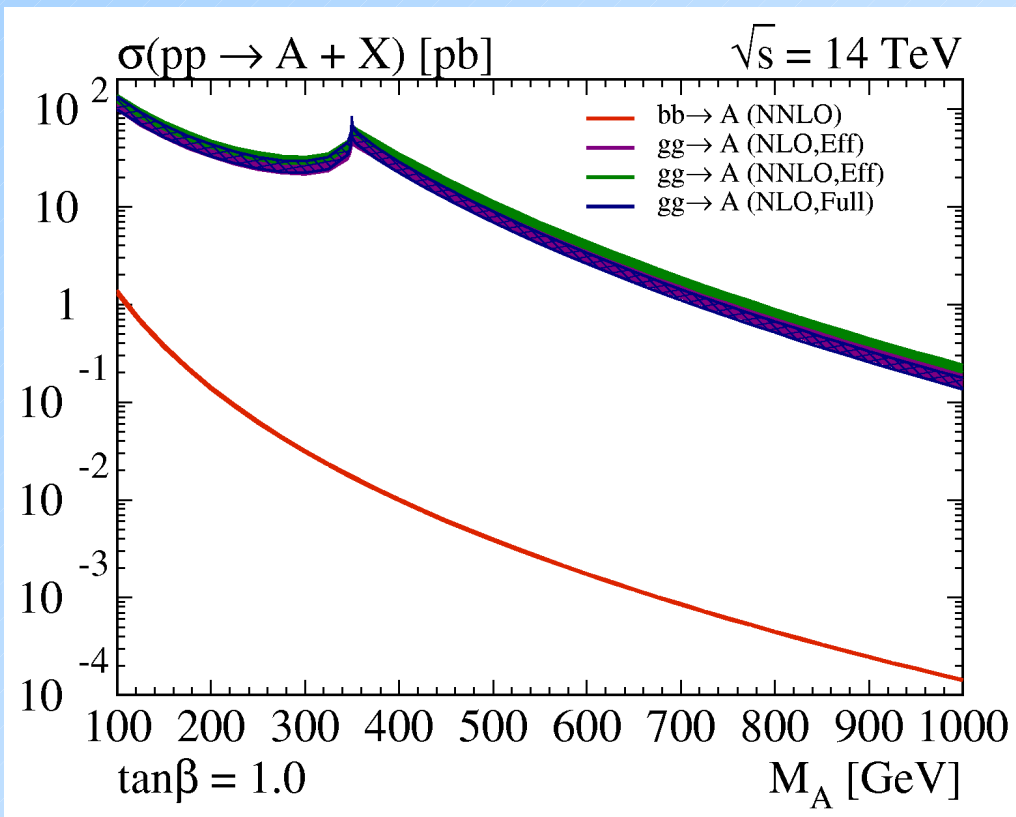
Renormalization Scale Dependence of $b\bar{b} \rightarrow H/A$ at LHC



$b\bar{b} \rightarrow A$ versus $gg \rightarrow A$

At small $\tan \beta$, b quark fusion is tiny.

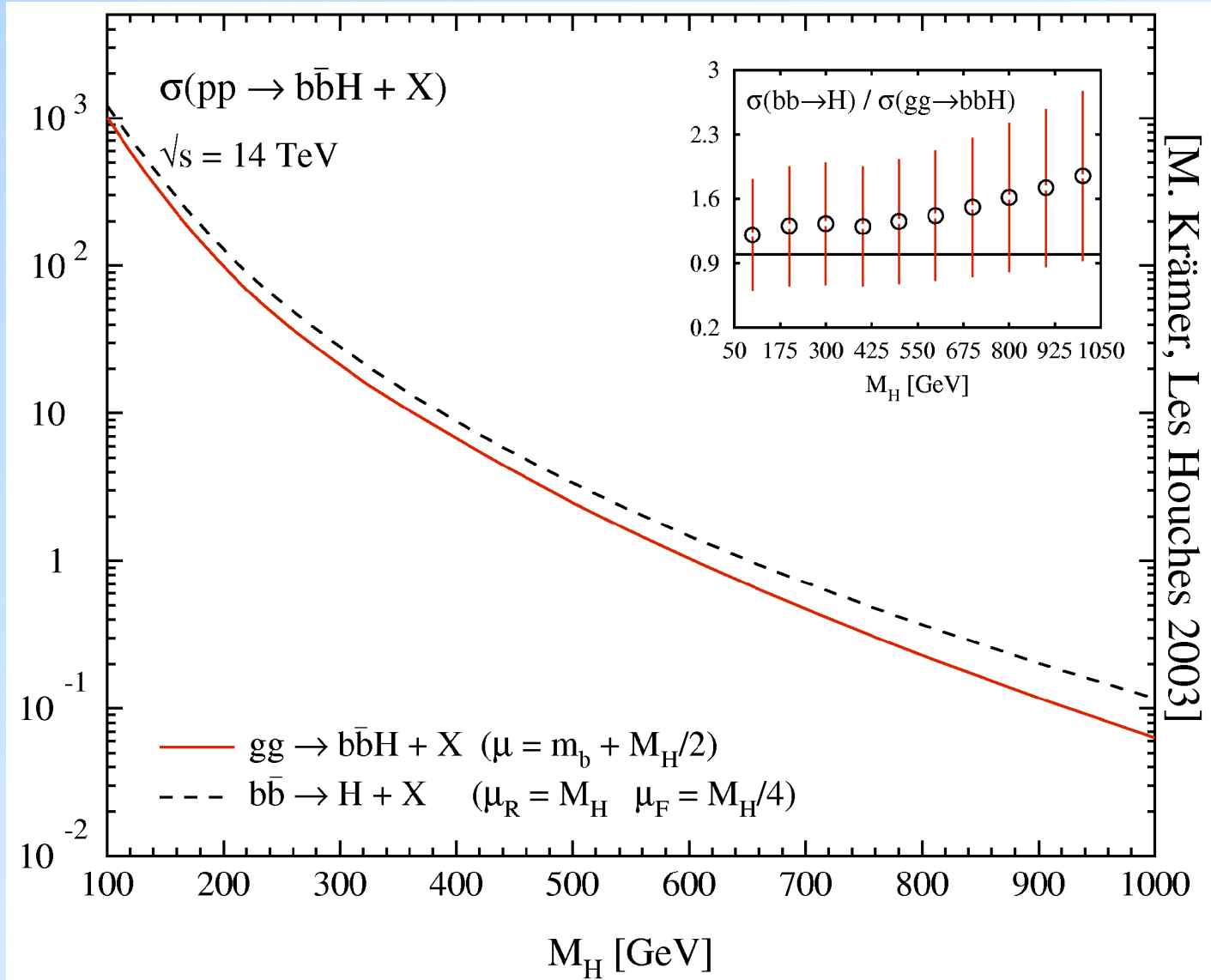
At large $\tan \beta$, it dominates.



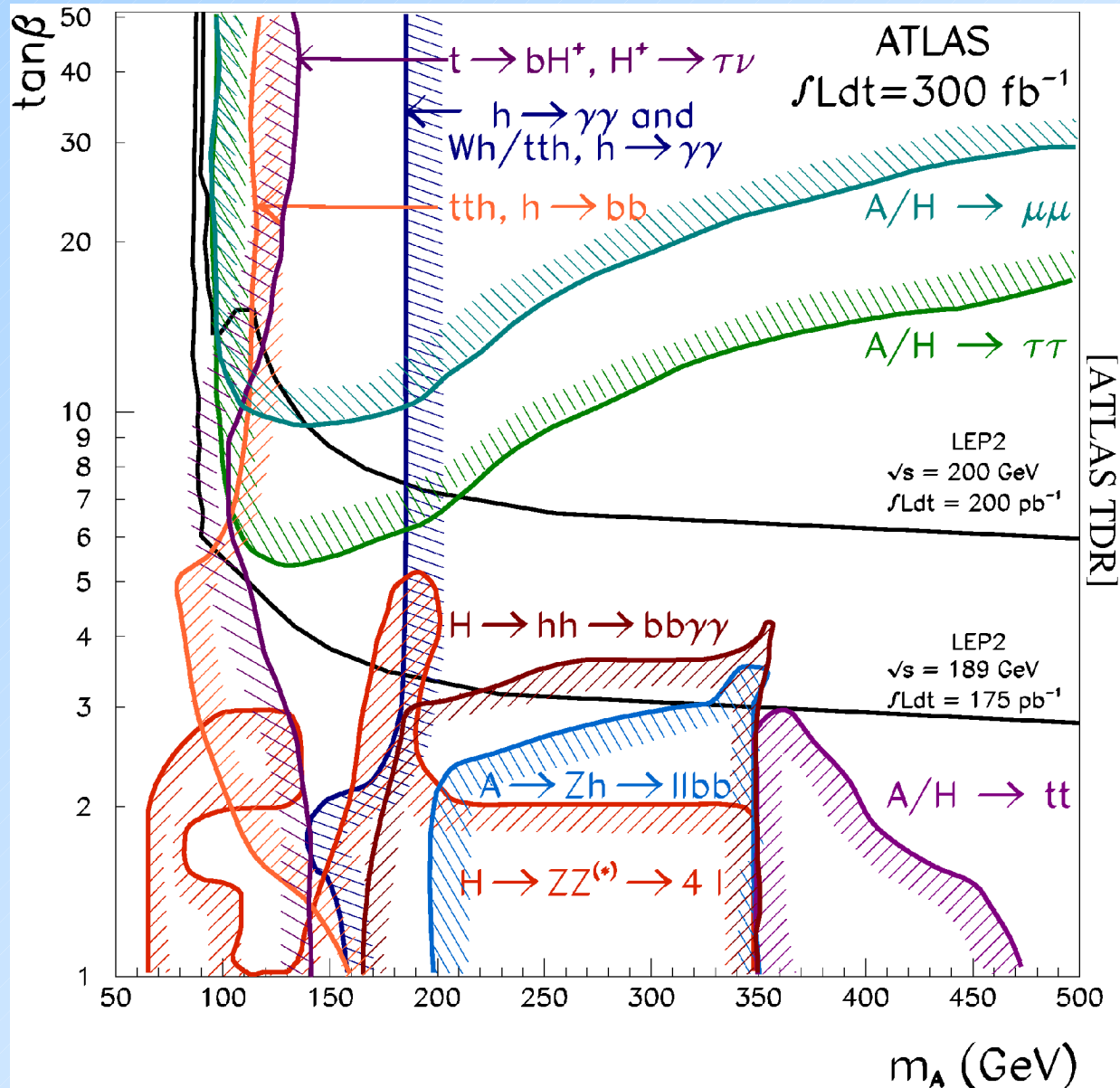
Compare $b\bar{b} \rightarrow H$ (NNLO) to $gg \rightarrow b\bar{b}H$ (NLO)

Dittmaier, Krämer, Spira; Dawson, Jackson, Reina, Wackerroth

The good behavior of $b\bar{b} \rightarrow H$ and the favorable comparison to $gg \rightarrow b\bar{b}H$ largely settles the controversy over b parton distributions.



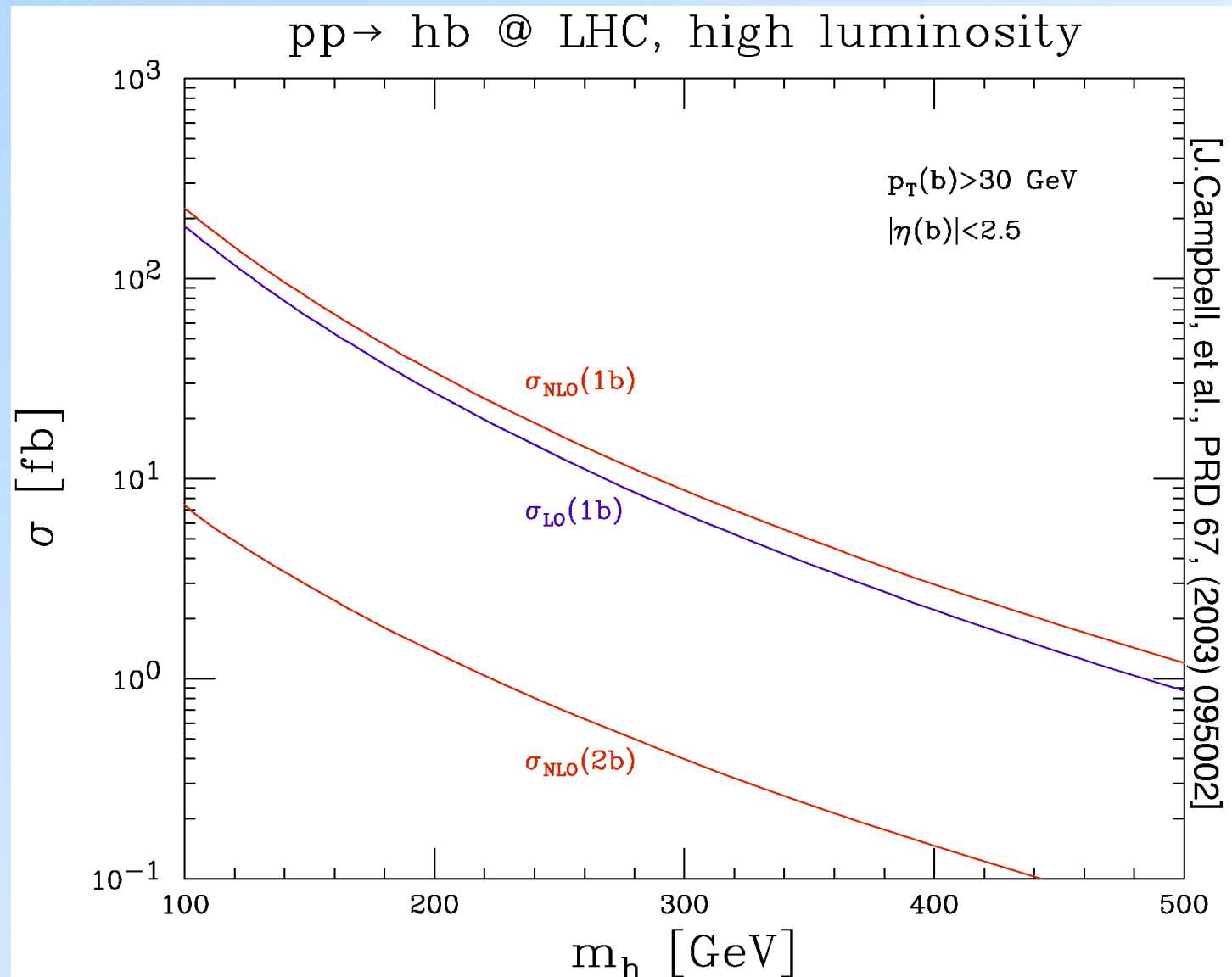
Finding SUSY Higgs 'at LHC



Higgs + b quark Production

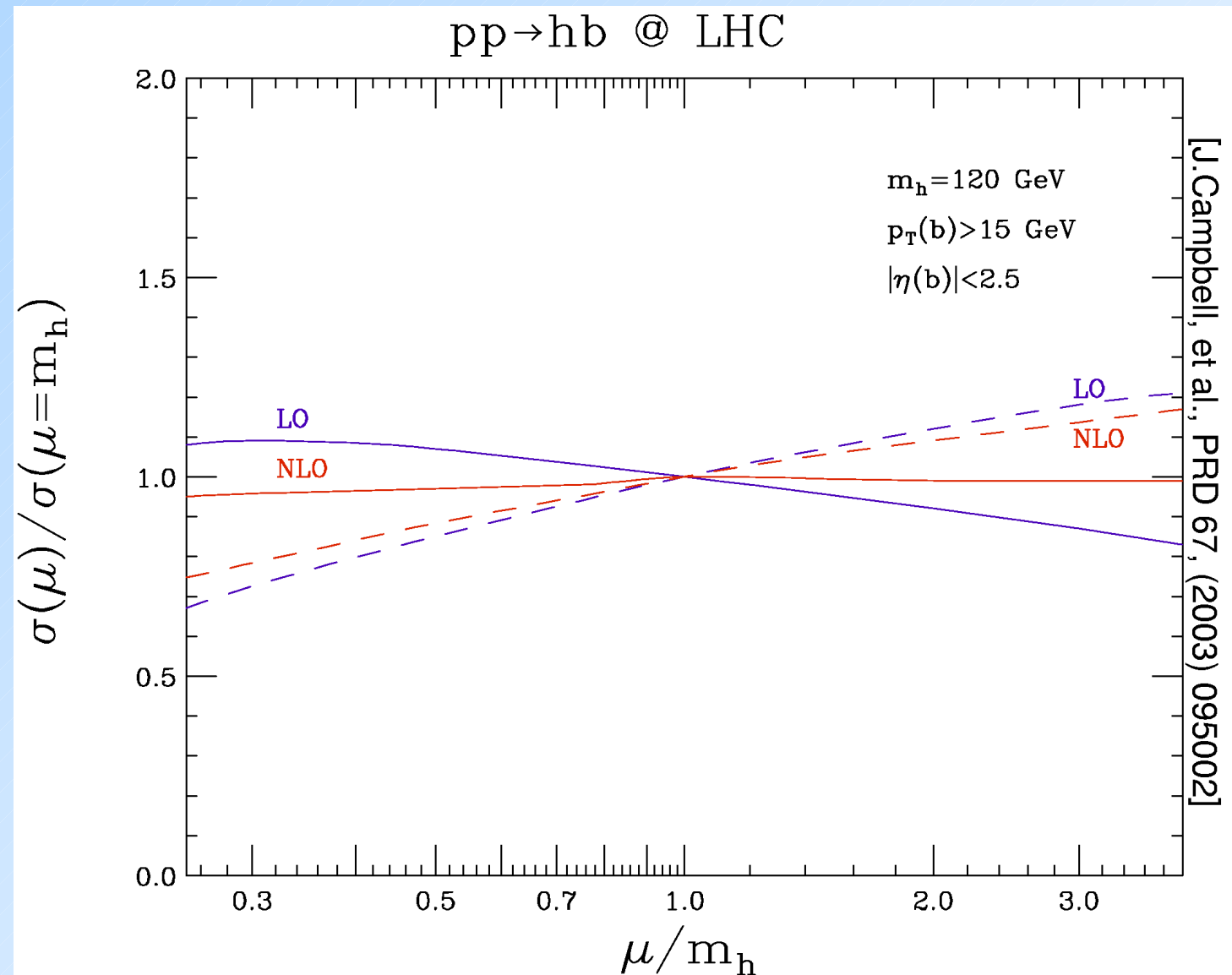
Campbell, Ellis, Maltoni, Willenbrock

A more promising channel may be H+b production. The extra b tag and the Higgs transverse momentum greatly improve detection efficiency.



H + b Scale Dependence

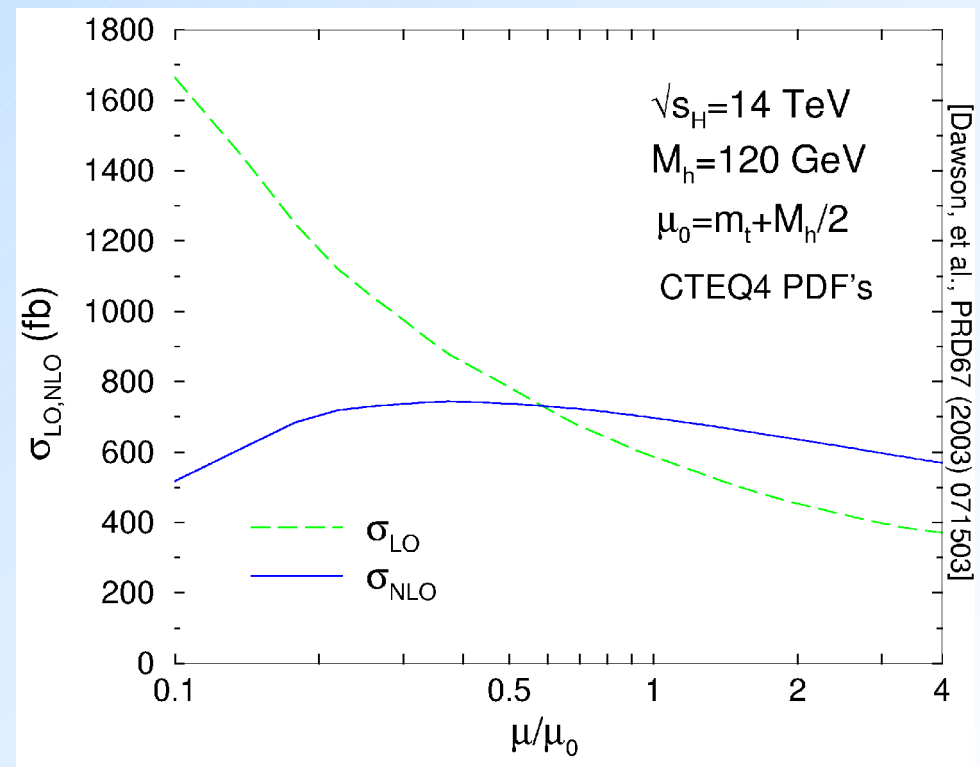
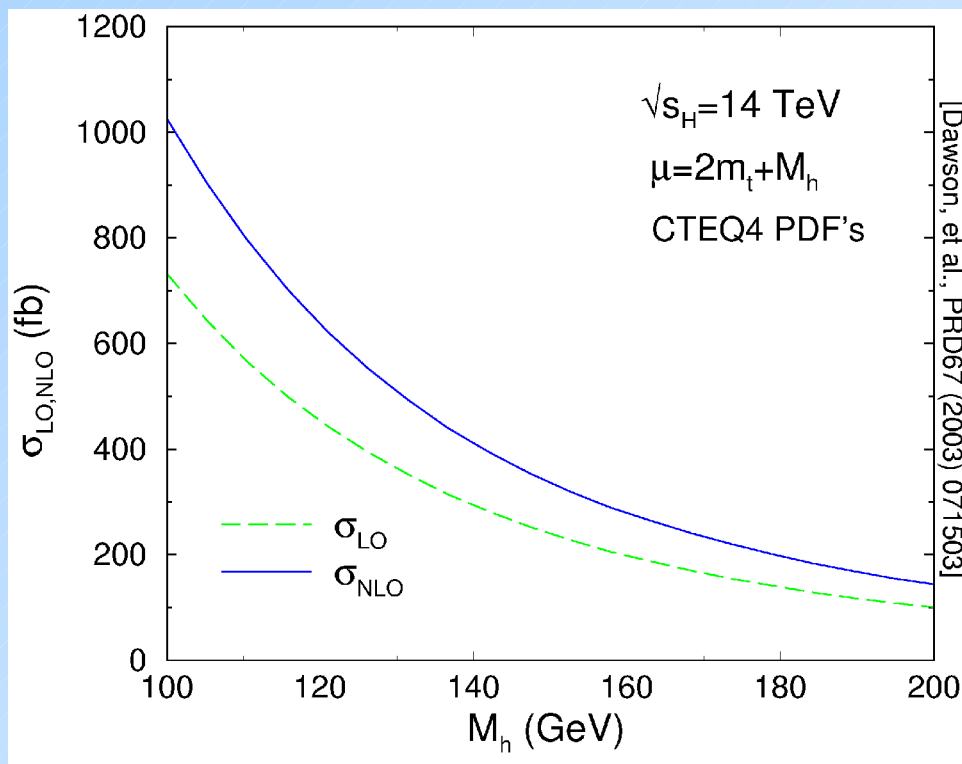
With only one b quark in the initial state, NLO is sufficient to obtain a reliable result.



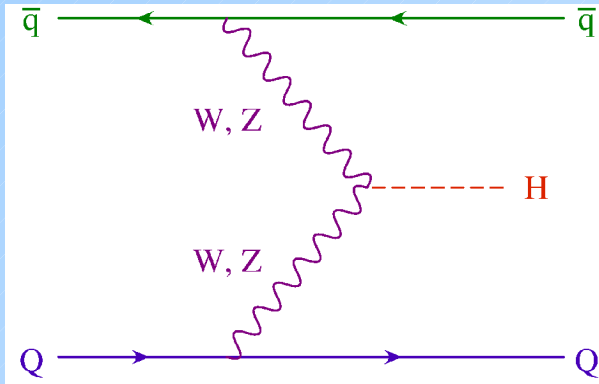
$t\bar{t}H$ production at NLO

This process serves as a discovery mode for a light Higgs and gives information on the top Yukawa coupling.

Beenakker, Dittmaier, Krämer, Plümper, Spira, Zerwas;
Dawson, Jackson, Orr, Reina, Wackerath



Weak Boson Fusion



NLO corrections have been known for some time.

Han, Willenbrock

Recently implemented in multi-purpose Monte-Carlo calculation.

Figy, Oleari, Zeppenfeld

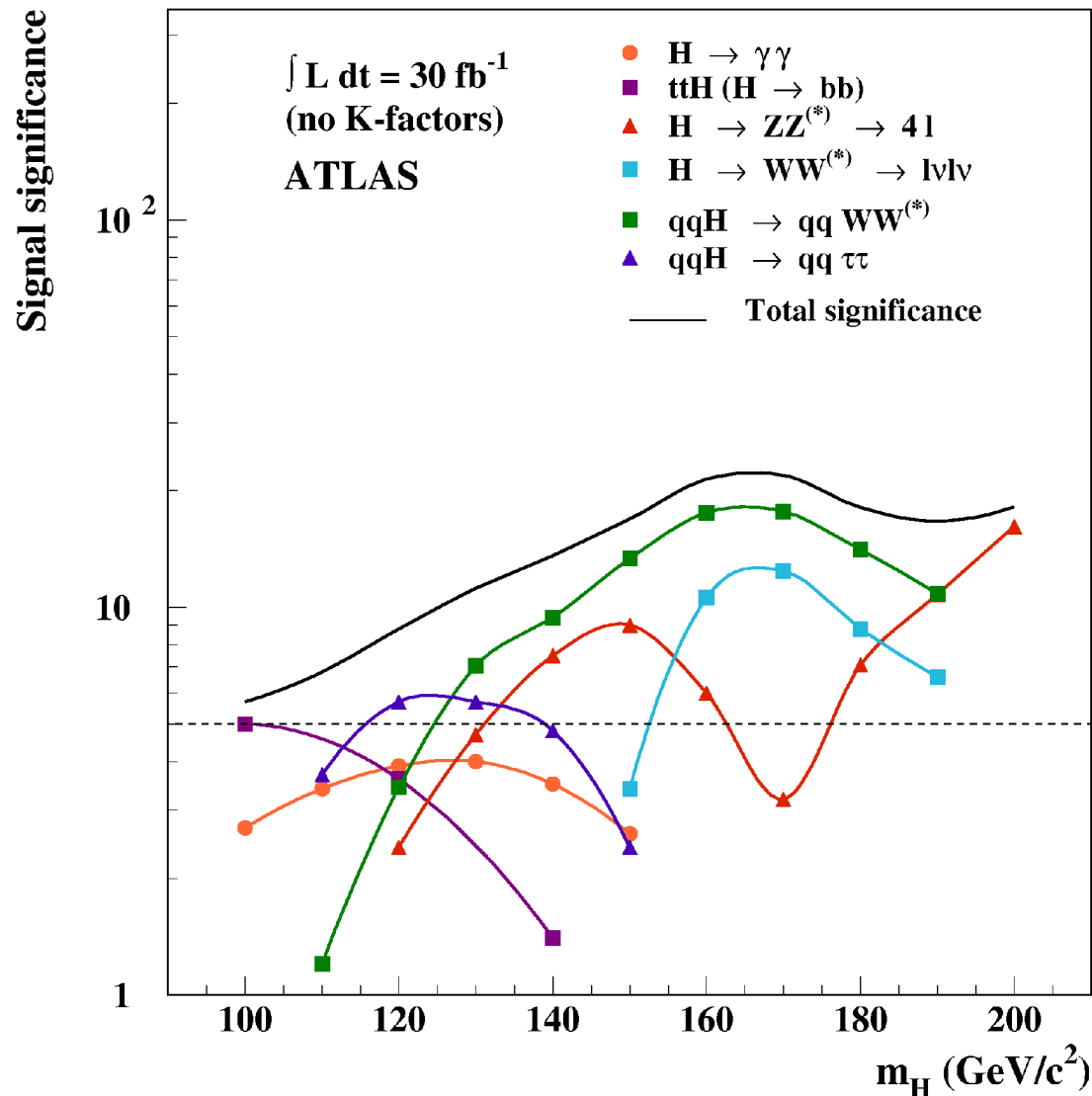
Offers discovery potential in the intermediate mass range and gives a good handle on measuring couplings.

Hagiwara, Kauer, Plehn, Rainwater, Zeppenfeld

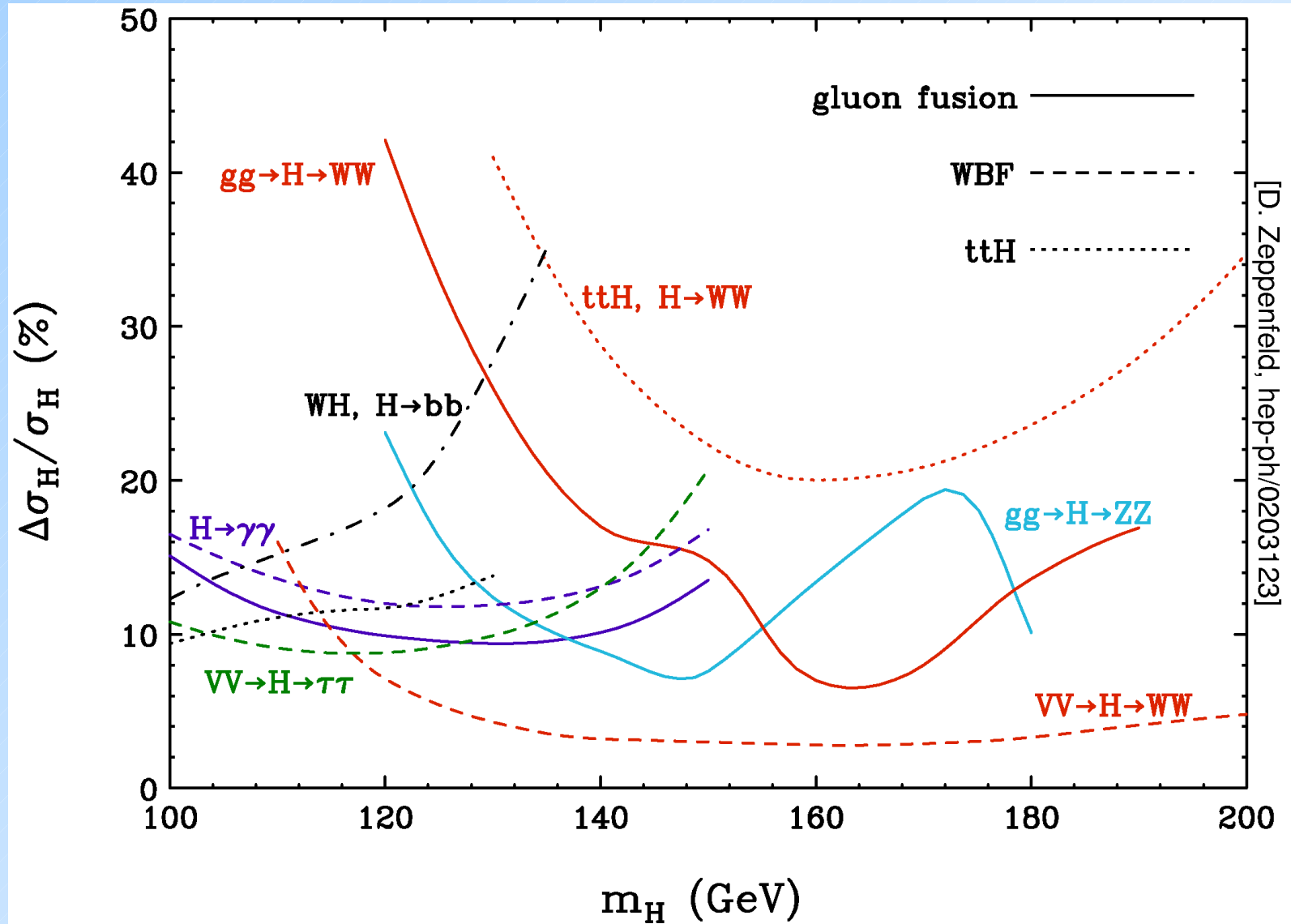
$gg \rightarrow H + 2j$ background computed in full theory.

Del Duca, Kilgore, Oleari, Schmidt, Zeppenfeld

Discovery through Weak Boson Fusion

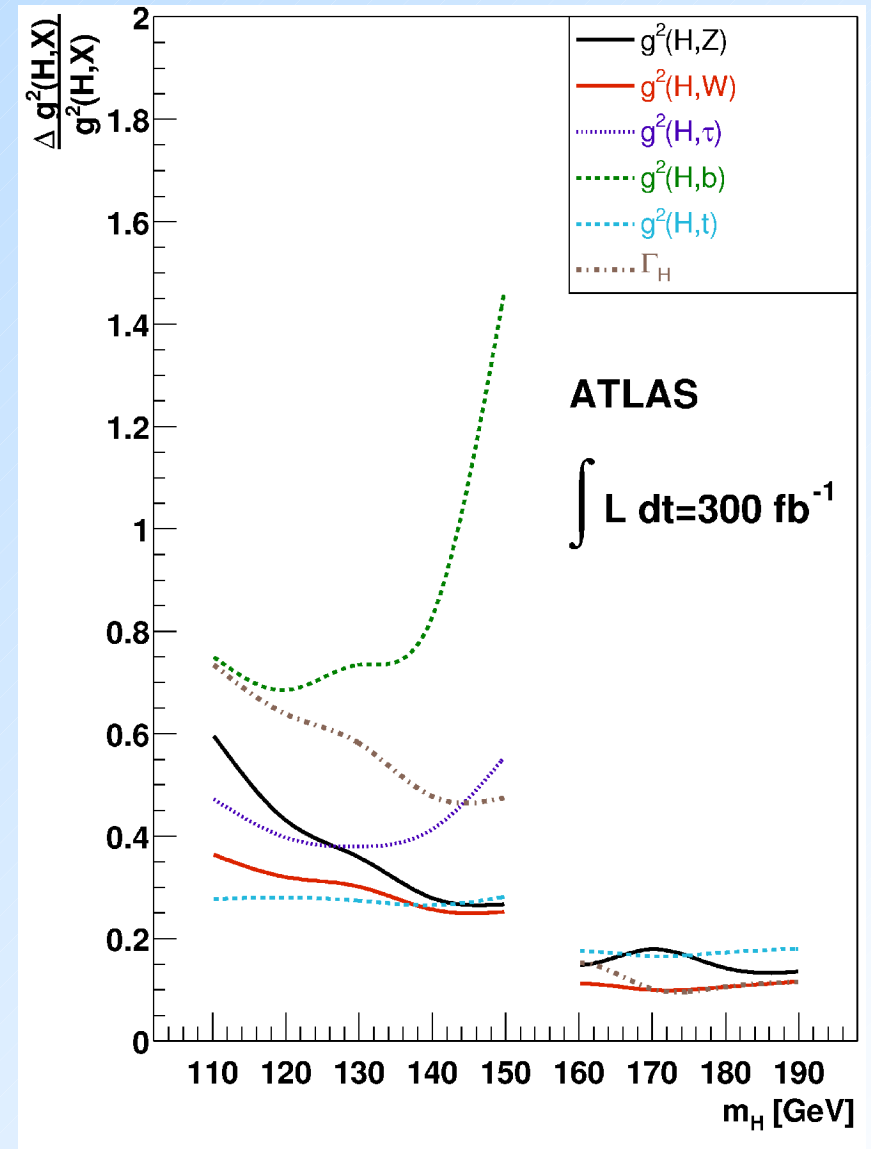
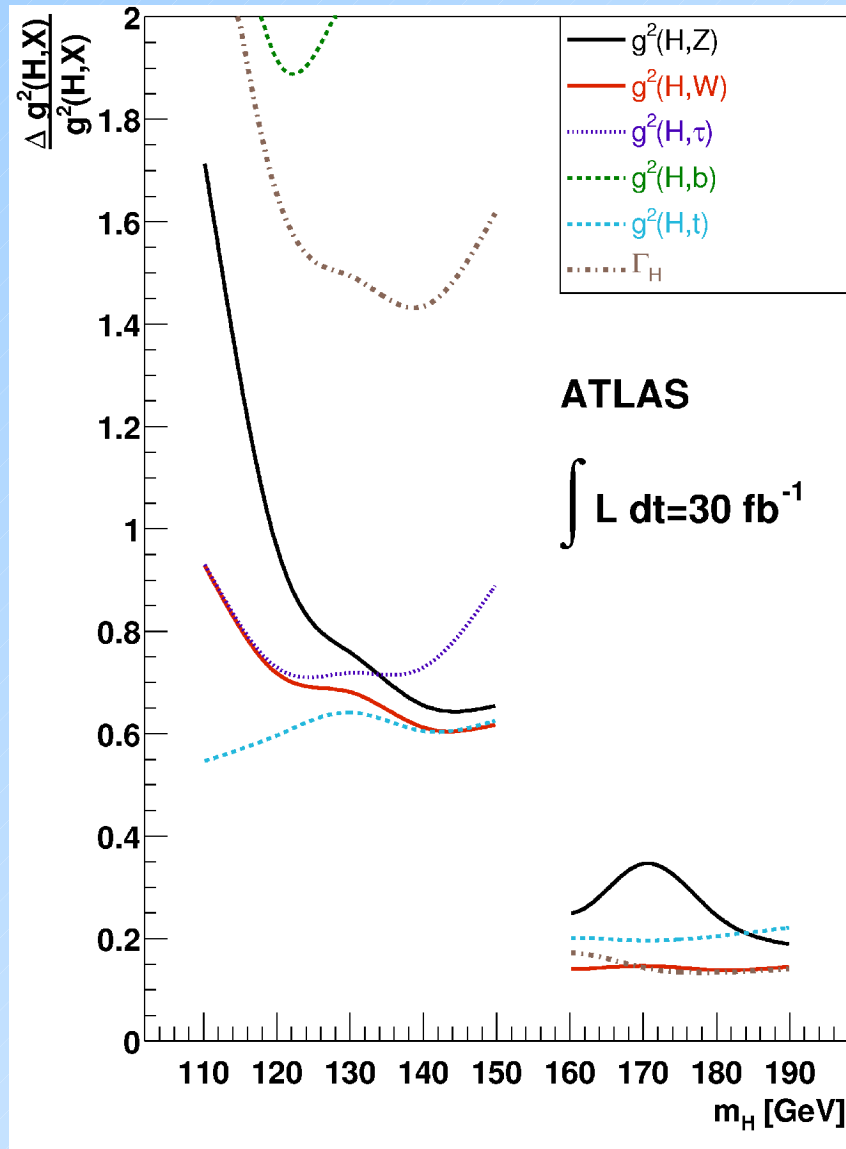


Expected precision in $\sigma \cdot \text{BR}$



[D. Zeppenfeld, hep-ph/0203123]

Expected Precision of Absolute couplings



LHC Summary

We are well positioned to discover the Higgs at the LHC. Some signals will take years of running to develop, but we know how to attack the problem.

We will be able to measure couplings and branching ratios with reasonable precision, but hadronic uncertainties in both detection and in the production cross section will limit precision.

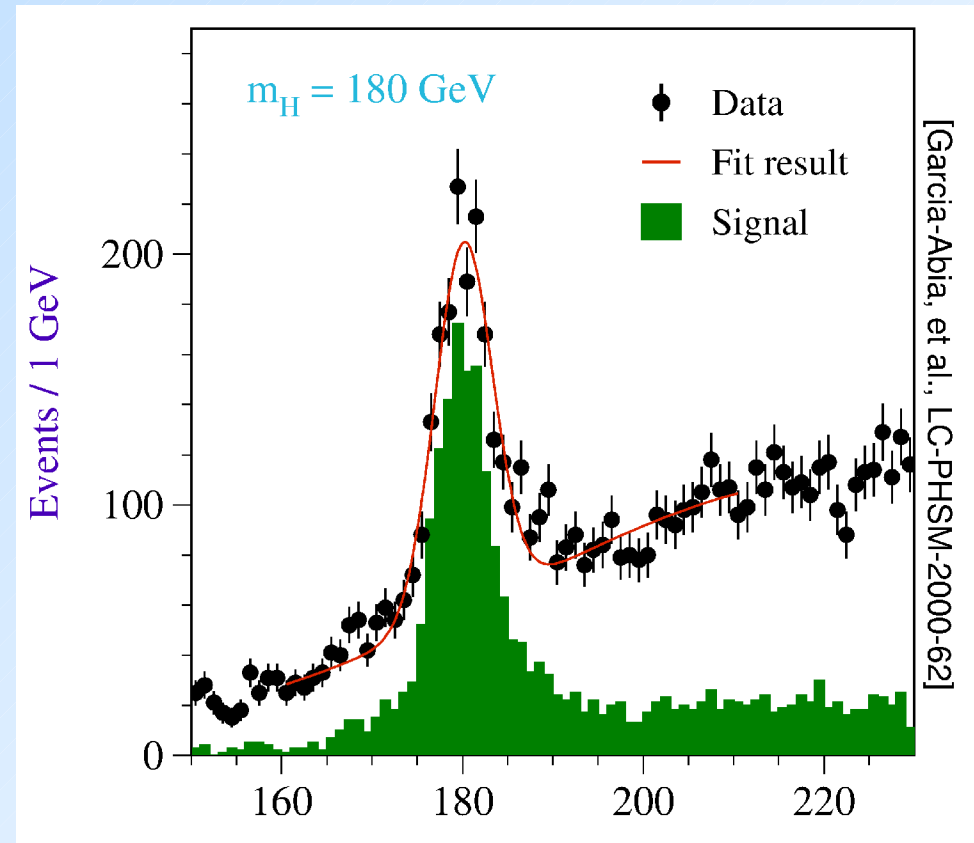
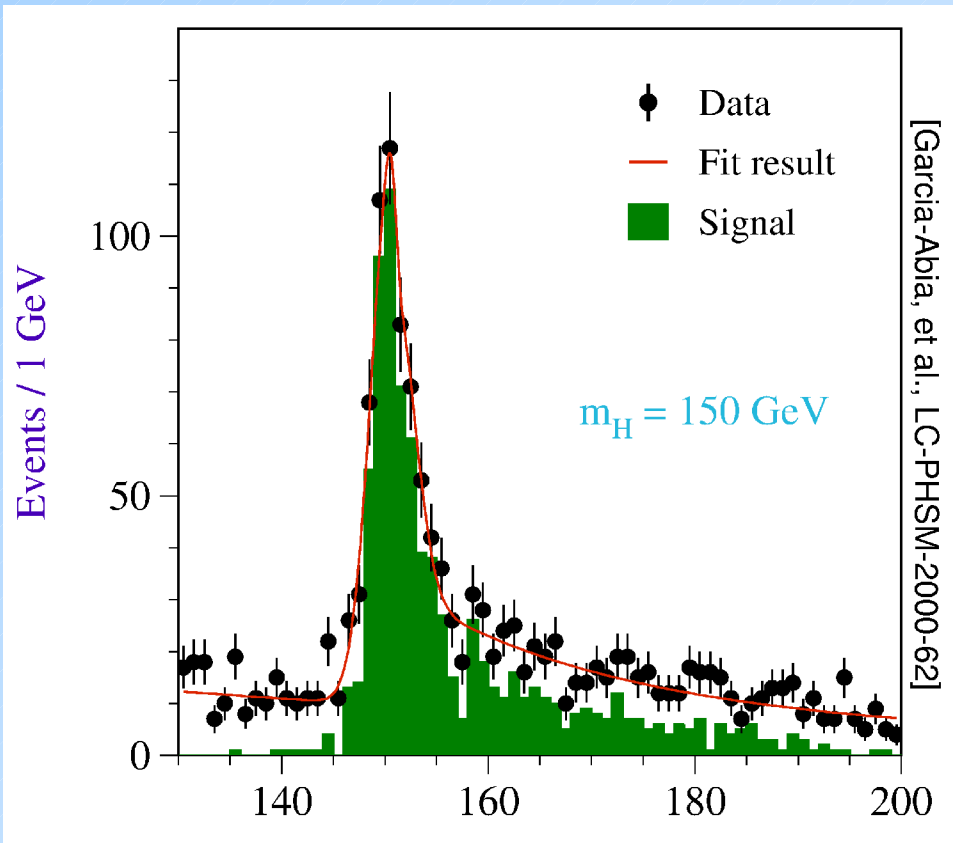
Higgs Bosons at a Linear Collider:

We want to measure all we can at the LHC, but we should remember the importance of the Linear Collider to the program of Higgs studies.

The Linear Collider will be able to measure Higgs properties with phenomenal precision and will allow us to fully understand those components of the symmetry breaking sector that are within its kinematic reach.

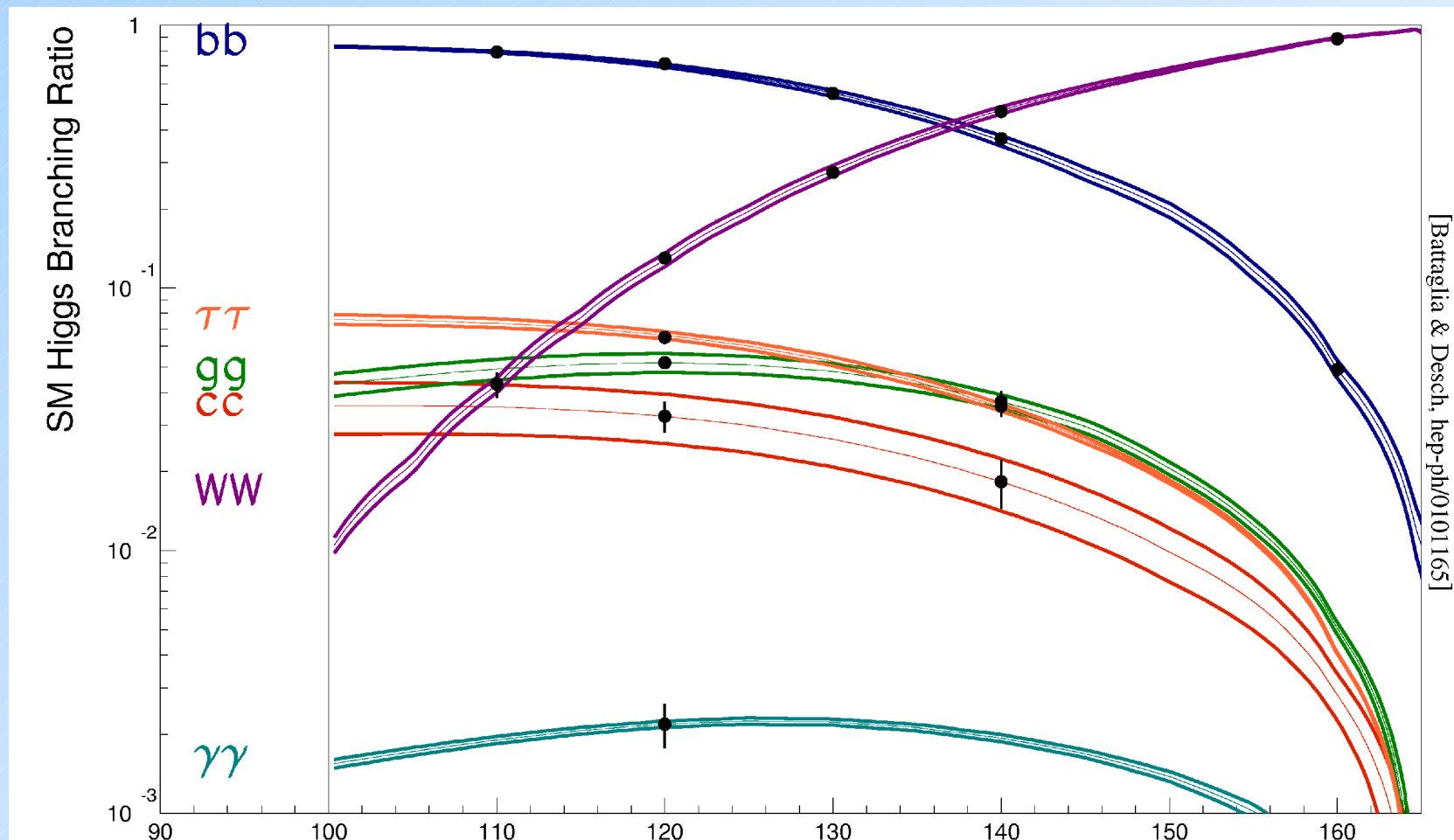
Higgs Discovery at a Linear Collider

The linear collider would be a good discovery machine within its kinematic reach.



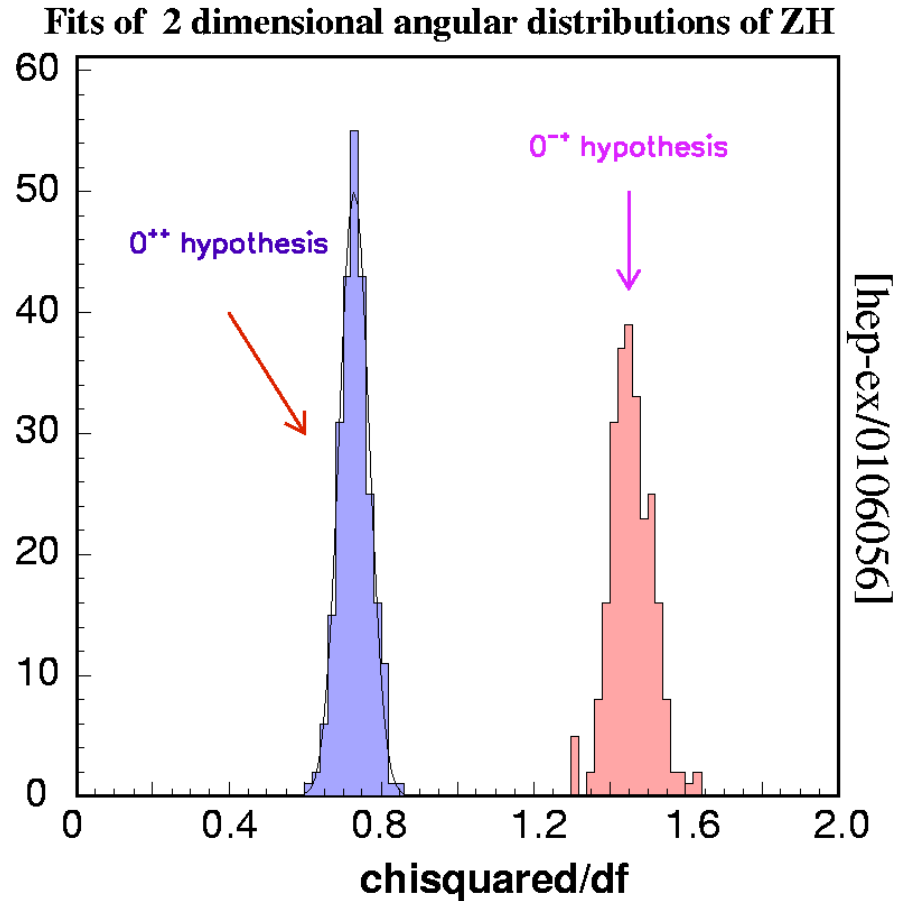
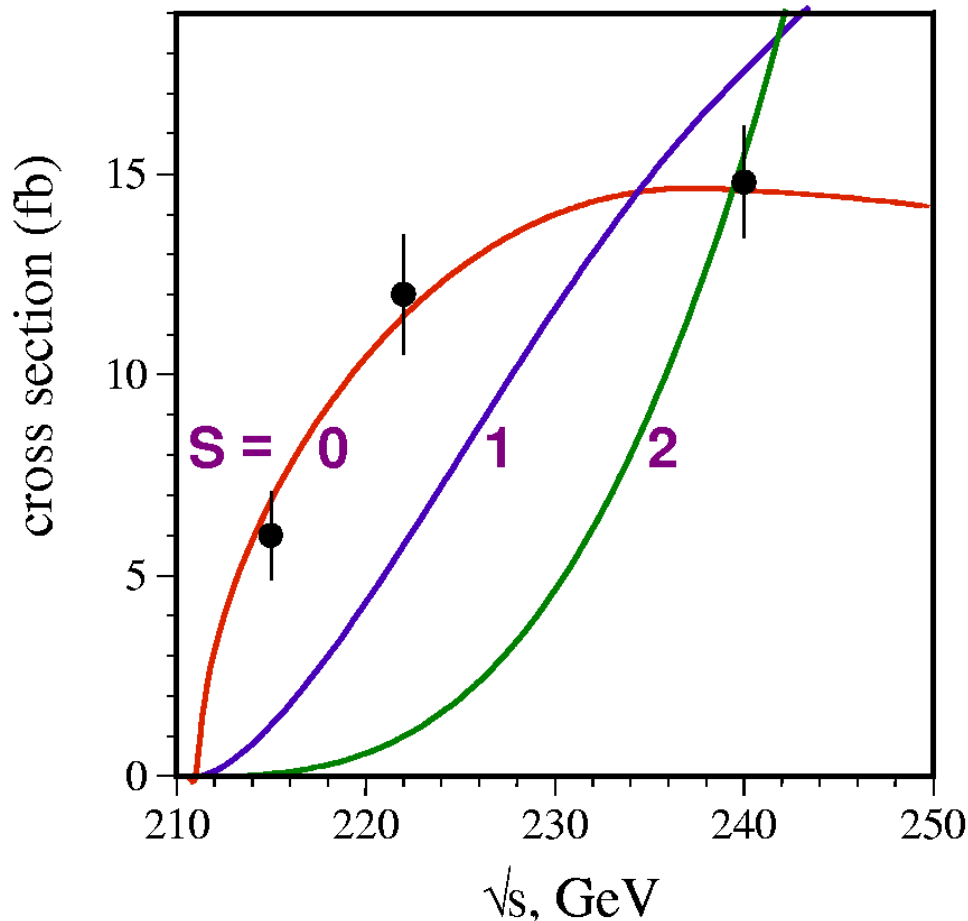
Higgs Couplings at Linear Collider

If the Higgs mass is below ~ 160 GeV, many branching ratios can be precisely measured.



Spin and CP at Linear Collider

The spin and CP quantum numbers can also be definitively measured at the linear collider



Summary

There has been great progress in Higgs physics in the last few years.

- Inclusive production is known to NNLO.
- Some distributions at NNLO are coming.
- b quark distributions established as consistent.
- Associated production processes known to NLO.
- Backgrounds also known to NLO.

What is still needed?

- **Full H + jet at NLO**
double boxes with masses?
- **NNLO Monte Carlo Calculations**
With such simple kinematics, do we need to wait for a general purpose algorithm?
- **Greater understanding of Forward Jet tagging and jet vetoes for WBF**
Are these signals robust enough?
- **Signal Recognition**
Can energy flow algorithms identify color singlets more effectively than traditional jet algorithms?