

The background of the slide is a blue warp tunnel from Star Trek. A dark Starship Enterprise is seen from a rear-quarter perspective, flying away from the viewer into the center of the tunnel. The tunnel walls are composed of many thin, parallel lines that create a sense of depth and motion. The lighting is a cool, blueish-white, with a bright circular glow at the end of the tunnel.

# A Theoretical Trek Into Darkness....

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# collaborators

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- 1112.4849, 1303.2384, 1305.1611, 13xx.xxxx, 13xx.xxxx



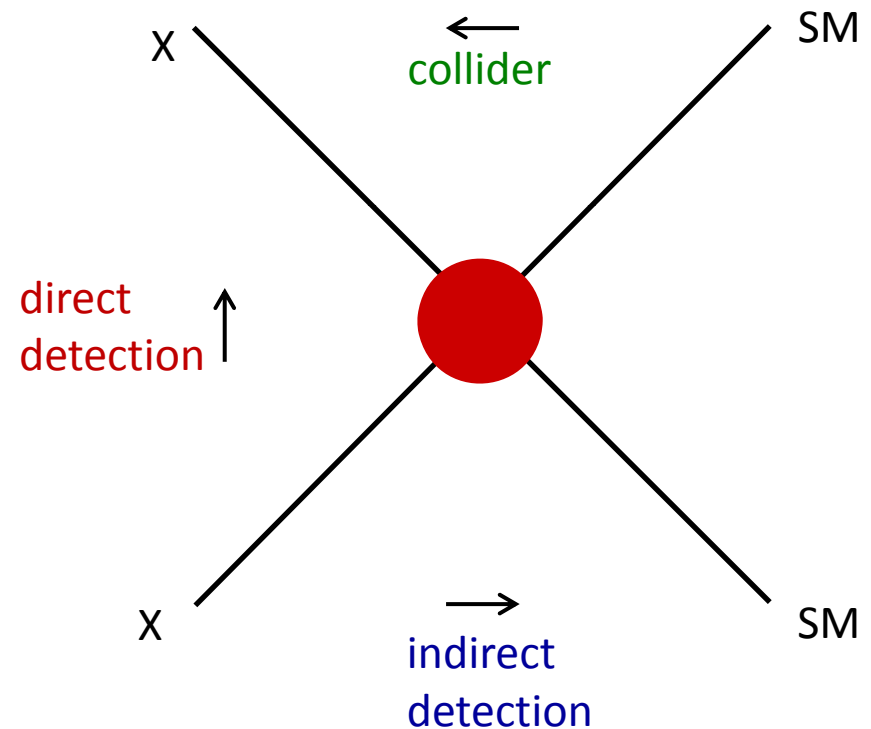
# searching for dark matter....

- usually start with some standard assumptions about **dark matter interactions**
  - single particle candidate (Majorana fermion)
  - **elastic scattering**
  - **contact interaction**
  - **isospin-invariant**
- main motivations are
  - **simplicity**
  - largely valid for **MSSM WIMP models** (actually, more restricted than that)
- but recent data hints only **marginally** consistent with MSSM WIMP models
  - **not clear whether these assumptions are really desirable**
- basic question: **how do the roles of different detection strategies change once we relax these assumptions?**



# dark matter detection strategies

- **direct detection**
  - measure recoil from dark matter scattering against nuclei
- **indirect detection**
  - dark matter annihilation in sun, Galactic center, satellites, etc.
- **collider search**
  - dark matter produced at the LHC
- **quantum matrix elements** for all three processes **related** by **crossing symmetry**
- allows us to probe dark matter **interaction structure** with **multiple approaches**







# issue: models and searches

- there is already a host of **uncertainties**
  - **astrophysics** → uncertainties in **velocity distribution**
  - **nuclear physics** → uncertainties in **nucleon structure** affect scattering
  - **I'll focus on the remaining particle physics uncertainties...**
- ... arise from the many assumptions usually made about dark matter interactions with Standard Model
  - **mostly based on WIMPs** (MSSM) (actually, usually **CMSSM/mSUGRA**)
- possible **problems**
  - search strategies **may not be optimized** for non-standard dark matter
  - if dark matter is non-standard, data **may not be interpreted correctly**
- our goal... **understand how changes to the standard paradigm can alter our interpretation of data, and give us new detection options**



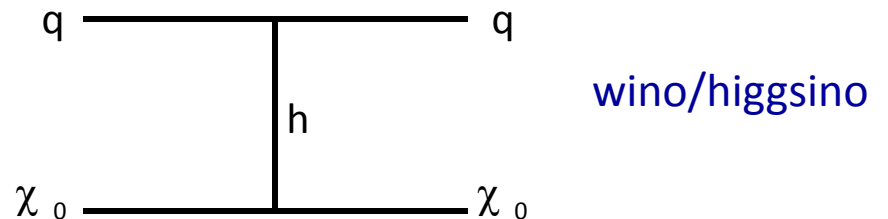
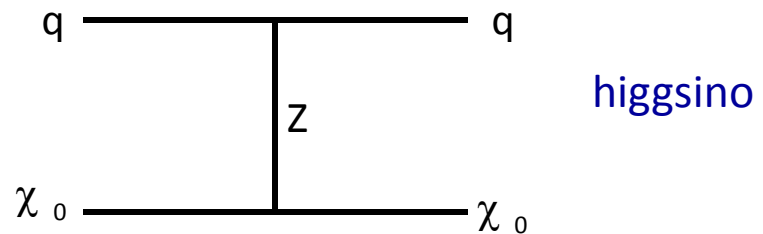
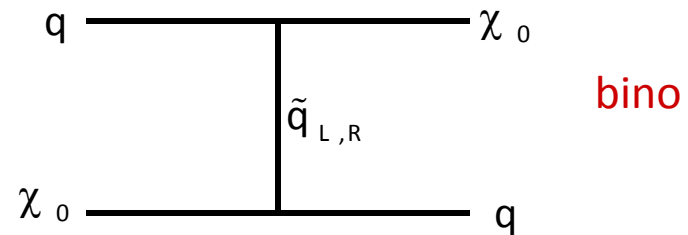
# low-mass dark matter

- hints from DAMA, CoGeNT, CRESST, CDMS-Si could be DM
  - 5-20 GeV
  - light for MSSM WIMPs
- XENON100 is not seeing a signal
  - could be a background....
- experimental issues still under study
  - some will be resolved soon
  - I won't focus on that.....
  - treat low-mass as a test case
- for theory, the question is, how to study low-mass dark matter?
- direct detection
  - low-mass = low recoil energy
  - need  $\mathcal{O}(\text{keV})$  threshold
  - challenging for experiments aimed at WIMPs
  - other detection strategies?
- assumptions play a role in interpretation of the data
  - need to keep track of the options
- start with Isospin-Violating Dark Matter
  - LSP interactions are assumed isospin-invariant, but why?



# why are LSP interactions isospin-invariant?

- if dark matter is mostly **bin**o
  - scatters by squark exchange
  - coupling ( $Y$ ) is isospin-violating
  - **SI term arises from squark-mixing**
    - small for first generation quarks in minimal flavor violation
- if dark matter has some **wino/higgsino** component
  - scatters by Z, higgs exchange
  - $Z \rightarrow$  isospin-violating, but SD or  $v^2$
  - $h \rightarrow$  SI, but isospin-conserving
    - higgs coupling scales with quark mass
    - $m_u \sim m_d \ll m_p$



really needed three fairy  
godmothers!....





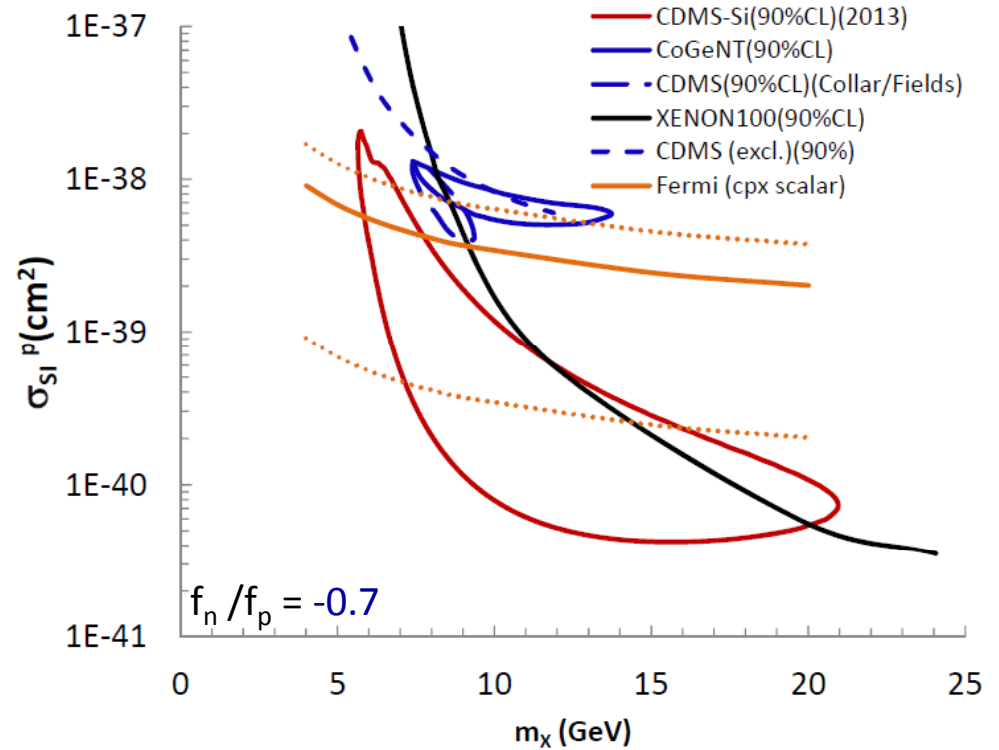
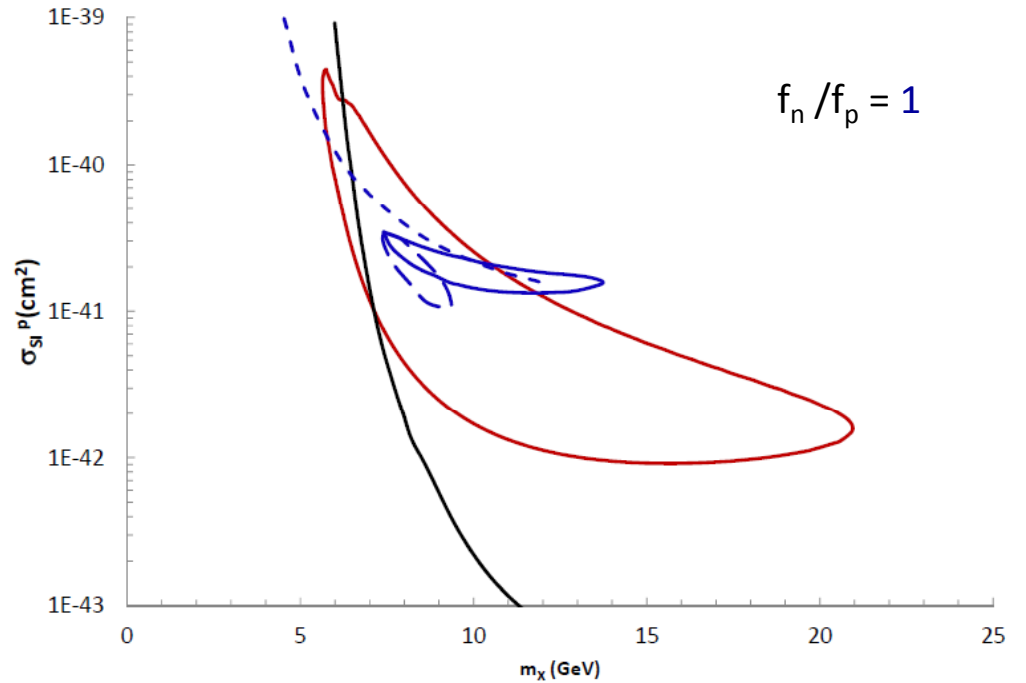
# IVDM

consider low mass as a test case!

- direct detection bounds  
normalized to nucleon ( $f_n / f_p = 1$ )
  - big change if  $f_n / f_p \neq 1$
- consider  $f_n / f_p = -0.7$ 
  - see CLPWY (1004.0697)
  - FKMS (1102.4331)
  - target isotopes, NLO (1205.2695) important
- if  $m_\chi$  small, no reason for  $f_n = f_p$ 
  - must account for this possibility!

$$\sigma_A = \frac{\mu_A^2}{M_*^4} \left[ f_p Z + f_n (A - Z) \right]^2 \times FF$$

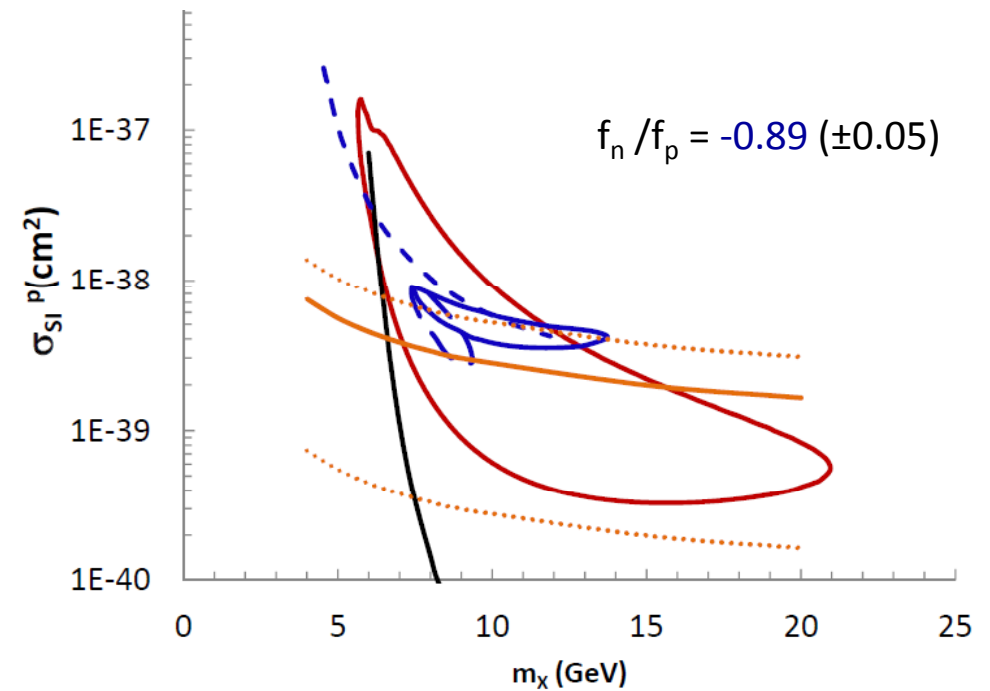
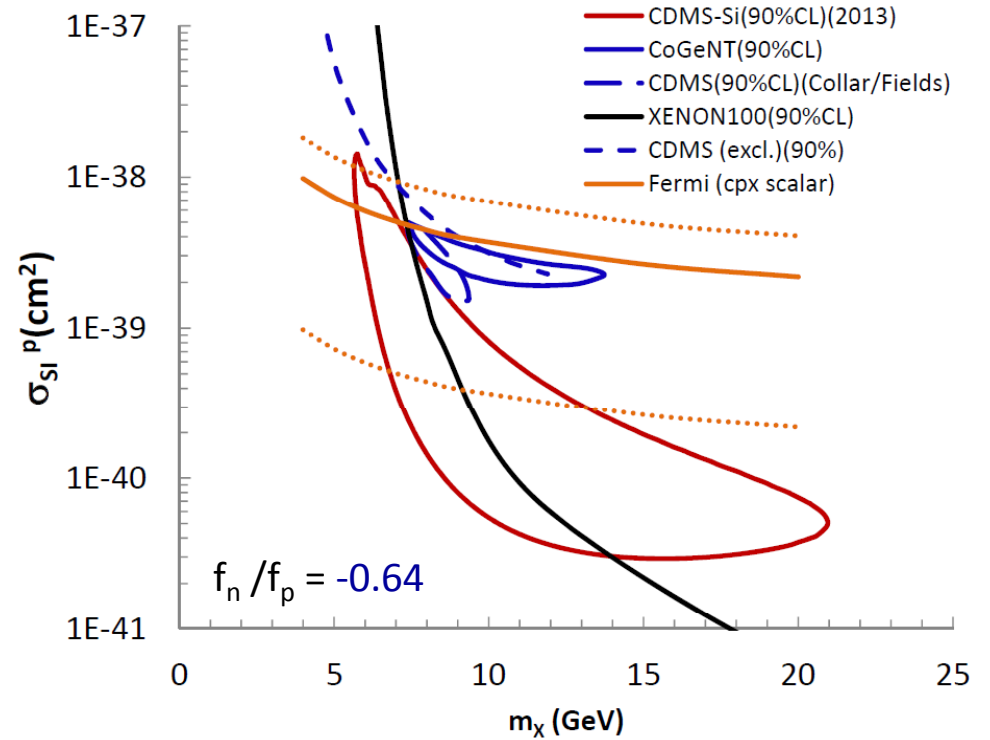
$$\sigma_p = \frac{\mu_p^2 f_p^2}{M_*^4}$$





# multiple experiments

- suppose there is a **real dark matter signal** from multiple experiments with different target
- define
  - $F_Z = \sigma_p / \sigma_N^Z$ ,  $R[Z_1, Z_2] = F_{Z_2} / F_{Z_1}$
  - two signals amount to a **measurement** of  $R[Z_1, Z_2]$
- **quadratic equation** for  $f_n / f_p$
- can determine  $f_n / f_p$  up to a **two-fold ambiguity**
- **need a third target material to resolve the ambiguity**
- **complementary** searches useful
  - need a **framework**





# matrix element approach

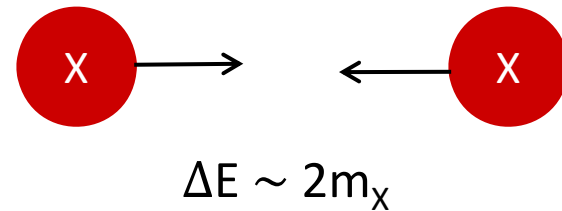
- worth thinking about a **general approach** to dark interactions
- consider a dark matter – Standard Model **interaction structure**
  - $\Gamma_\chi \Gamma_f F(s, t, u)$
  - $\Gamma_\chi$  and  $\Gamma_f$  are **dark matter** and **SM bilinears** (might need a Fierz trans.)
  - $F$  is an interaction form factor ( $F=1$  for a pure contact interaction)
- matrix element for **scattering**, **annihilation** and **production** all arise from this interaction structure
  - all related by **crossing symmetry**
- **what do we want to know about this structure regarding scattering?**
  - **spin-independent** vs. **spin-dependent**
  - $f_n / f_p = ?$
  - suppressed by factors of  $q$  or  $v^\perp$ ?
    - direct detection sensitivity is already very good and getting better, so reasonable models with suppressed scattering are coming into range





# complementary searches

- what can we learn from other search strategies?
- annihilation  $\rightarrow$  s-wave or p-wave?
  - annihilation from L=1 state suppressed by  $v^2 \sim 10^{-6}$
  - higher energy scales
- is pair-creation enhanced?
  - production at LHC occurs at higher energies than annihilation or scattering ( $> 2m_\chi$ )
  - energy enhancement could make LHC searches more promising
  - depends on boson vs. fermion, E dependence of perturbation



$$\begin{aligned}
 |\text{spin} - 0\rangle &\propto 1 \\
 |\text{spin} - 1/2\rangle &\propto \sqrt{E} \\
 &(\phi^* \partial^\mu \phi) \tilde{A}_\mu \\
 &\phi^* \phi \chi \quad \swarrow \sim E
 \end{aligned}$$



# matrix element analysis

also gluon couplings, etc. ....

| Name | Interaction Structure  | $\sigma_{SI}$ suppression   | $\sigma_{SD}$ suppression   | $s$ -wave?            |
|------|--|---|---|-----------------------|
| F1   | $\bar{X} X \bar{q} q$  | 1   | $q^2 v^{\perp 2}$ (SM)  | No                    |
| F2   | $\bar{X} \gamma^5 X \bar{q} q$   | $q^2$ (DM)  | $q^2 v^{\perp 2}$ (SM); $q^2$ (DM)                                | Yes                   |
| F3   | $\bar{X} X \bar{q} \gamma^5 q$   | 0   | $q^2$ (SM)  | No                    |
| F4   | $\bar{X} \gamma^5 X \bar{q} \gamma^5 q$  | 0   | $q^2$ (SM); $q^2$ (DM)  | Yes                   |
| F5   | $\bar{X} \gamma^\mu X \bar{q} \gamma_\mu q$<br>(vanishes for Majorana $X$ )                    | 1   | $q^2 v^{\perp 2}$ (SM)<br>$q^2$ (SM); $q^2$ or $v^{\perp 2}$ (DM) | Yes                   |
| F6   | $\bar{X} \gamma^\mu \gamma^5 X \bar{q} \gamma_\mu q$   | $v^{\perp 2}$ (SM or DM)  | $q^2$ (SM)  | No                    |
| F7   | $\bar{X} \gamma^\mu X \bar{q} \gamma_\mu \gamma^5 q$<br>(vanishes for Majorana $X$ )           | $q^2 v^{\perp 2}$ (SM); $q^2$ (DM)                                | $v^{\perp 2}$ (SM)<br>$v^{\perp 2}$ or $q^2$ (DM)                 | Yes                   |
| F8   | $\bar{X} \gamma^\mu \gamma^5 X \bar{q} \gamma_\mu \gamma^5 q$                                  | $q^2 v^{\perp 2}$ (SM)  | 1   | $\propto m_f^2/m_X^2$ |
| F9   | $\bar{X} \sigma^{\mu\nu} X \bar{q} \sigma_{\mu\nu} q$<br>(vanishes for Majorana $X$ )          | $q^2$ (SM); $q^2$ or $v^{\perp 2}$ (DM)<br>$q^2 v^{\perp 2}$ (SM) | 1   | Yes                   |
| F10  | $\bar{X} \sigma^{\mu\nu} \gamma^5 X \bar{q} \sigma_{\mu\nu} q$<br>(vanishes for Majorana $X$ ) | $q^2$ (SM)  | $v^{\perp 2}$ (SM)<br>$q^2$ or $v^{\perp 2}$ (DM)                 | Yes                   |

a general model can interact through **multiple structures**...  
interference effects for both annihilation and scattering.



# spin-0 and spin-1

|     |  |                                    |  |                         |
|-----|--|------------------------------------|--|-------------------------|
| S1  | $\phi^\dagger \phi \bar{q} q$ or $\phi^2 \bar{q} q$  | 1                                  | $q^2 v^{\perp 2}$ (SM)                                   | Yes                     |
| S2  | $\phi^\dagger \phi \bar{q} \gamma^5 q$ or $\phi^2 \bar{q} \gamma^5 q$  | 0                                  | $q^2$ (SM)   | Yes                     |
| S3  | $\phi^\dagger \partial_\mu \phi \bar{q} \gamma^\mu q$  | 1                                  | $q^2 v^{\perp 2}$ (SM)<br>$q^2$ (SM); $v^{\perp 2}$ (DM) | No                      |
| S4  | $\phi^\dagger \partial_\mu \phi \bar{q} \gamma^\mu \gamma^5 q$   | 0                                  | $v^{\perp 2}$ (SM or DM)                                 | No                      |
| V1  | $B_\mu^\dagger B^\mu \bar{q} q$ or $B_\mu B^\mu \bar{q} q$   | 1                                  | $q^2 v^{\perp 2}$ (SM)                                   | Yes                     |
| V2  | $B_\mu^\dagger B^\mu \bar{q} \gamma^5 q$ or $B_\mu B^\mu \bar{q} \gamma^5 q$   | 0                                  | $q^2$ (SM)   | Yes                     |
| V3  | $B_\nu^\dagger \partial_\mu B^\nu \bar{q} \gamma^\mu q$  | 1                                  | $q^2 v^{\perp 2}$ (SM)<br>$q^2$ (SM); $v^{\perp 2}$ (DM) | No                      |
| V4  | $B_\nu^\dagger \partial_\mu B^\nu \bar{q} \gamma^\mu \gamma^5 q$   | 0                                  | $v^{\perp 2}$ (SM or DM)                                 | No                      |
| V5  | $(B_\mu^\dagger B_\nu - B_\nu^\dagger B_\mu) \bar{q} \sigma^{\mu\nu} q$  | $q^2 v^{\perp 2}$ (SM)             | 1  | Yes                     |
| V6  | $(B_\mu^\dagger B_\nu - B_\nu^\dagger B_\mu) \bar{q} \sigma^{\mu\nu} \gamma^5 q$   | $q^2$ (SM)                         | $v^{\perp 2}$ (SM)                                       | Yes                     |
| V7  | $B_\nu^\dagger \partial^\nu B_\mu \bar{q} \gamma^\mu q$ or $B_\nu \partial^\nu B_\mu \bar{q} \gamma^\mu q$   | $v^{\perp 2}$ (SM); $q^2$ (DM)     | $q^2$ (SM); $q^2$ (DM)                                   | No                      |
| V8  | $B_\nu^\dagger \partial^\nu B_\mu \bar{q} \gamma^\mu \gamma^5 q$ or $B_\nu \partial^\nu B_\mu \bar{q} \gamma^\mu \gamma^5 q$   | $q^2 v^{\perp 2}$ (SM); $q^2$ (DM) | $q^2$ (DM)   | $\propto m_f^2 / m_X^2$ |
| V9  | $\epsilon^{\mu\nu\rho\sigma} B_\nu^\dagger \partial_\rho B_\sigma \bar{q} \gamma_\mu q$ or $\epsilon^{\mu\nu\rho\sigma} B_\nu \partial_\rho B_\sigma \bar{q} \gamma_\mu q$                   | $v^{\perp 2}$ (DM or SM)           | $q^2$ (SM)   | No                      |
| V10 | $\epsilon^{\mu\nu\rho\sigma} B_\nu^\dagger \partial_\rho B_\sigma \bar{q} \gamma_\mu \gamma^5 q$ or $\epsilon^{\mu\nu\rho\sigma} B_\nu \partial_\rho B_\sigma \bar{q} \gamma_\mu \gamma^5 q$ | $q^2 v^{\perp 2}$ (SM)             | 1  | No                      |

for **spin-1** dark matter, **longitudinal polarizations** give **(E / m<sub>X</sub>)** enhancement for collider production



# new frontiers...

- a few unusual things immediately appear from this analysis
- **s-wave annihilation from Majorana fermion dark matter to light SM fermions is **not** always chirality-suppressed**
  - only if interaction is through time-component of pseudovector SM bilinear
  - interesting **IVDM** connection
    - to get SI-scattering from squark exchange, need **sfermion mixing**
    - usually assumed to be proportional to quark mass, but need not be
    - if 1<sup>st</sup> gen. sfermion-mixing sizeable, can get IVDM for Majorana fermion DM
    - also get interaction structure (**F4**) which permit **unsuppressed s-wave annihilation**
- **XX → hh (Majorana fermion) need not be p-wave suppressed**
  - could have s-wave annihilation, but need CP-violation
- for some interactions (pseudoscalar exchange, or pseudovector exchange with spin-0 dark matter), **SI scattering matrix element vanishes**
- **if new physics introduces CP-violation, many new interesting features**



# start of an analysis...?

- for example, suppose we really detected low-mass dark matter...
- we can get a handle on **SI vs. SD**, **couplings** to protons and neutrons from **multiple direct detection experiments**
- with estimate of couplings, **what can we learn about the dark matter candidate?**
- some options arise just from whether or not we see something at **indirect detection searches** or the **LHC**

|             |   |   |                                     |                               |
|-------------|---|---|-------------------------------------|-------------------------------|
| if...?      | <b>collider, indirect</b>                               | <b>collider, indirect</b>   | <b>collider, indirect</b>           | <b>collider, indirect</b>     |
| could be... | Dirac fermion exchanging a "heavy" gauge boson (spin-1) | fermion exchanging heavy spin-0, or spin-0 exchanging heavy gauge boson | spin-0 exchanging a spin-0 mediator | (semi) long-range interaction |

**not complete**, just some options... → in general, need spectral info, etc. ....



# as an example....

suppose we see **spin-independent scattering** with **no momentum or velocity suppression**....

|   | $\sigma_{SD}$    | s-wave? | collider enhancement |
|---|------------------|---------|----------------------|
| $\bar{X}X\bar{q}q$  | $q^2v_{\perp}^2$ | No      | $(E / m_X)^2$        |
| $\bar{X}\gamma^\mu X\bar{q}\gamma_\mu q$                          | $q^2v_{\perp}^2$ | Yes     | $(E / m_X)^2$        |
| $\phi^\dagger\phi\bar{q}q$  | $q^2v_{\perp}^2$ | Yes     | 1                    |
| $i \text{Im}(\phi^\dagger\partial_\mu\phi)\bar{q}\gamma^\mu q$    | $q^2v_{\perp}^2$ | No      | $(E / m_X)^2$        |
| $B_\mu B^\mu\bar{q}q$   | $q^2v_{\perp}^2$ | Yes     | $(E / m_X)^4$        |
| $i \text{Im}(B_\nu^\dagger\partial_\mu B^\nu)\bar{q}\gamma^\mu q$ | $q^2v_{\perp}^2$ | No      | $(E / m_X)^4$        |

combining direct, indirect and collider searches goes a long way towards isolating the interaction structure....



# outlook

- direct detection sensitivity already at levels several orders of magnitude better than the “nominal” WIMP scattering cross-section ( $10^{-40}$  cm<sup>2</sup>)
  - if momentum/velocity-suppressed, just approaching the sensitivity needed
  - structures with SD-scattering can be probed with suppressed SI-scat. as well
  - directional detection may separate momentum and velocity dependence
- **lots of options for dark matter interactions**
  - unless wedded to something very specific (like CMSSM), **no way to choose**
- but we get **complementary information** from **direct detection**, **indirect detection** and **collider searches**
- all data can help **determine structure** of dark matter interactions
- with new data coming and new theory frontiers, **we should be prepared for exciting times ahead...**

...or as Captain Kirk would say...



***“Buckle up!”***

**- Captain James T. Kirk**



***and remember...***



# CosPA 2013

Nov. 12-15, 2013

Honolulu, USA

hosted by  
the University of  
Hawaii



**Aloha!**

<http://www.phys.hawaii.edu/cospa2013>

registration opens July 1....

Back-up slides



# indirect detection

- look for  $\gamma$ ,  $e^\pm$ ,  $p^\pm$ ,  $\nu$  produced by **dark matter annihilation**
- main targets are... anywhere there's a lot of dark matter
- **many techniques and targets**, but upshot is the same
  - rate of annihilations  $\propto \int dV \eta^2 \langle \sigma_{\text{ann.}} v \rangle$
  - estimate  $\int dV \eta^2$  from astrophysics data (with uncertainty!)
  - choice of annihilation products relates number of annihilations to number of particles seen
  - putting the above together with observations yields **a bound on  $\langle \sigma_{\text{ann.}} v \rangle$**
- **since scattering and annihilation matrix elements are related, we probe the matrix element in a different kinematic regime** ( $2m_\chi$  instead of keV)
  - determine matrix element structure and coupling to different SM particles
- **strong signal only if matrix element allows annihilation from s-wave state**
- **good at low mass**, since  $\eta \propto \rho / m_\chi$



# complementary $\gamma$ -ray bounds from dwarf spheroidal galaxies

- **Fermi-LAT** search for photons from **dwarf spheroidal galaxies** (1108.2914,1108.3546)
  - very good at low mass
- very little baryonic matter
  - small background
- **systematic uncertainty** arising from density profile uncertainty
  - can strengthen bounds by  $\times 10$ , but only weaken by  $\times 2$
  - only issue for very steep profiles
- also **anti-proton flux** bounds, but **more uncertain** ( $\times 50$ )
  - 1108.0664

$$\Phi_{pp} \equiv \frac{\langle \sigma_A v \rangle}{8\pi m_X^2} \int_{E_{thr}}^{m_X} \sum_f B_f \frac{dN_f}{dE} dE$$

$$\Phi_{pp} \leq 5.0_{-4.5}^{+4.3} \times 10^{-30} \text{ cm}^3 \text{ s}^{-1} \text{ GeV}^{-2}$$

1108.2914

$$E_{thr} = 1 \text{ GeV}$$

95% CL bound from “**stacked**” analysis of several Milky Way satellites

- cosmic ray propagation
- background
- solar modulation



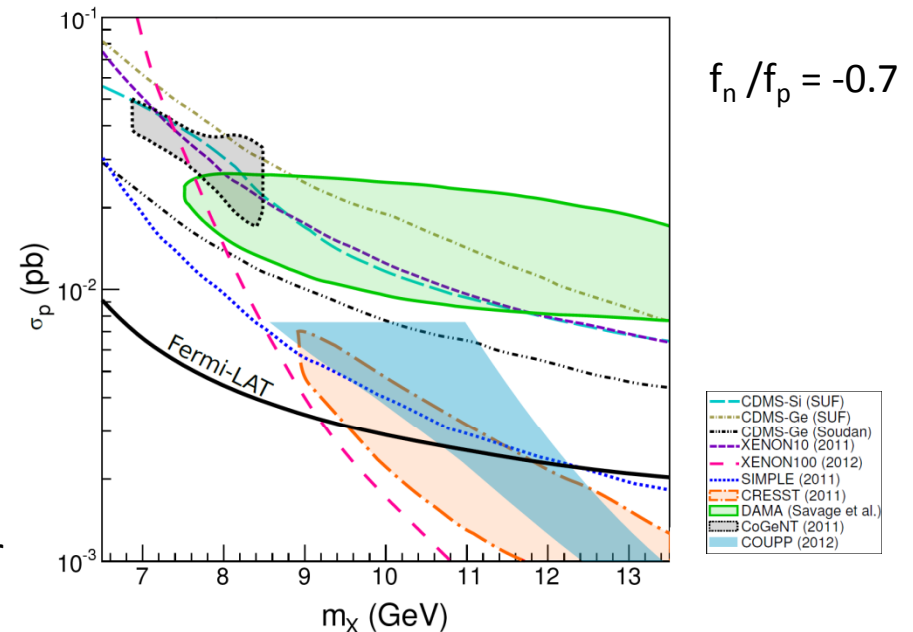
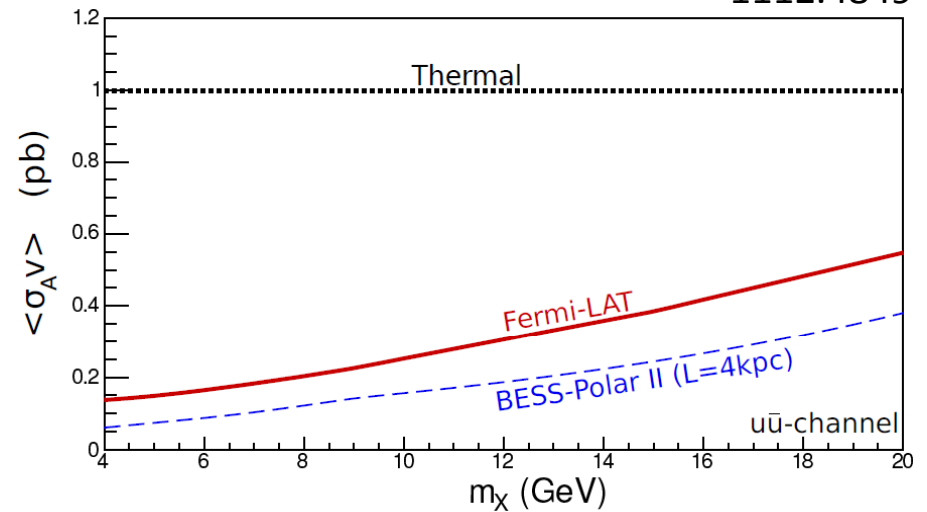


# Fermi-LAT and dwarf spheroidalals

1112.4849

- less astrophysics uncertainty, less background
- for any matrix element, can translate from  $\langle \sigma_{\text{ann.}} v \rangle$  to  $\sigma_{\text{SI}}$
- example  $\rightarrow$  annihilation to  $u/d$ -quarks only, fixed  $f_n/f_p$
- consider elastic contact operators with spin-independent scattering and s-wave annihilation (unique!)
- enhanced  $\sigma_{\text{ann.}}$  if  $f_n/f_p = -0.7$ 
  - tighter bounds
- signal (or lack of it) can point to a model choice....
  - p-wave annihilation?,  $M_* \sim \text{GeV?}$

complex scalar





# models and monojet searches

- compare number of monojets seen to prediction of SM
  - excess could indicate dark matter
- **# of events depends on model**
  - contact operator at LHC energy?
  - energy dependence of matrix element?
  - flavor? → **IVDM could ramp up couplings**
- consider **SI-scattering, s-wave** annihilation, coupling to **u/d**
- **points to a model** in a way **complementary** to direct/indirect detection

| $m_\chi$ (GeV) | $\sigma_p^{(\text{ferm.})}$ (pb) | $\sigma_p^{(\text{scal.})}$ (pb) |
|----------------|----------------------------------|----------------------------------|
| 4              | 0.00079                          | 10.8                             |
| 7              | 0.00092                          | 4.2                              |
| 10             | 0.00097                          | 2.3                              |
| 15             | 0.00106                          | 1.1                              |
| 20             | 0.00107                          | 0.62                             |

$p_T > 350$  GeV,  $\cancel{E}_T > 350$  GeV  
ATLAS monojet search with  $1 \text{ fb}^{-1}$

elastic contact scattering,  $f_n/f_p = -0.7$