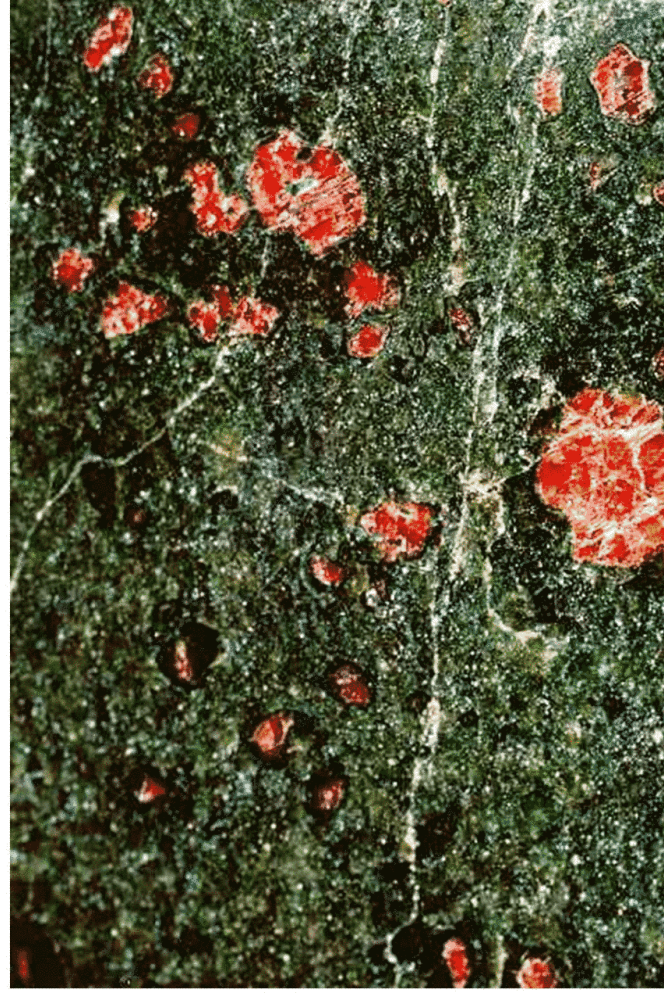
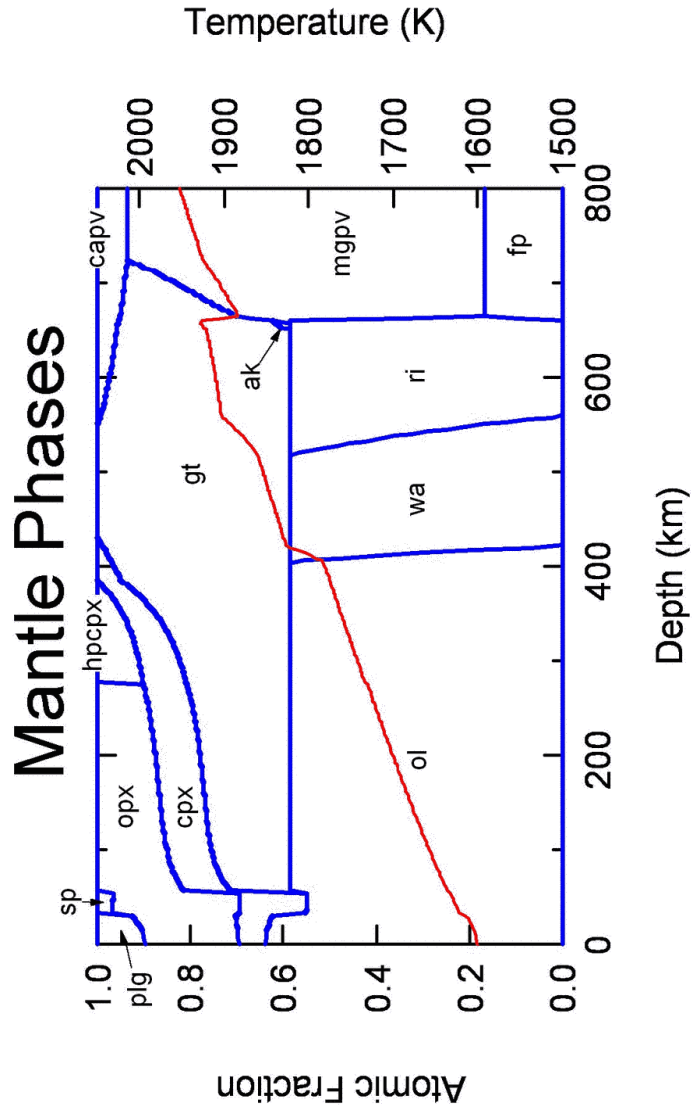


Mineralogy and Crystal Chemistry

Lars Stixrude
University of Michigan

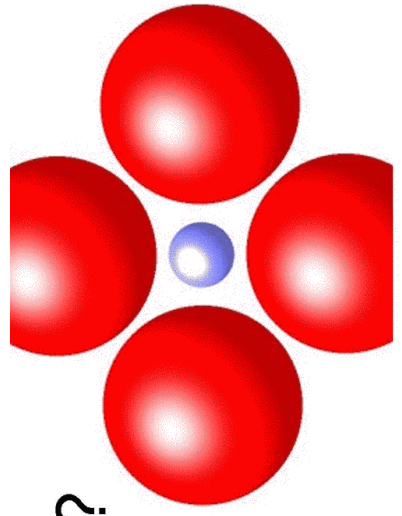
Upper Mantle Xenolith, Depth ~ 100 km
Red=garnet (gt); black=orthopyroxene (opx); green=clinopyroxene (cpx); yellow-
green=olivine (ol)



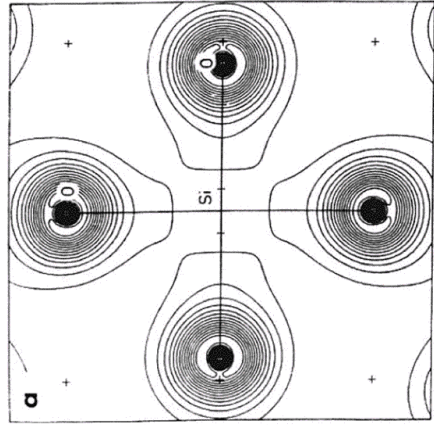


Wadsleyite (wa); Ringwoodite (ri); akimotoite (ak); Mg-perovskite (mgpv);
 Ca-perovskite (capv); Ferropericlase (fp)

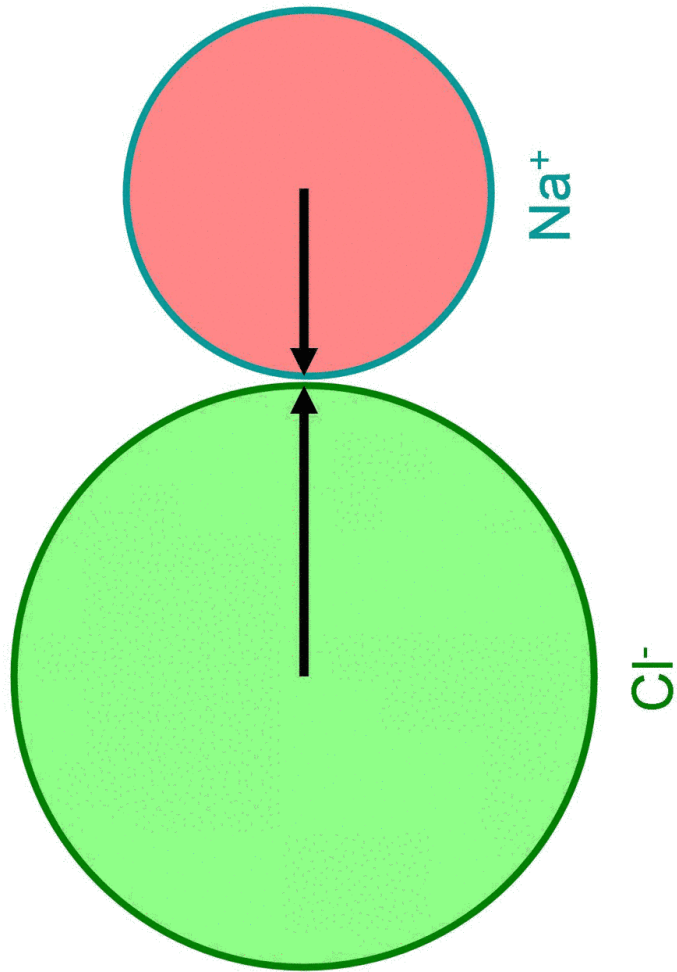
ions or electrons?



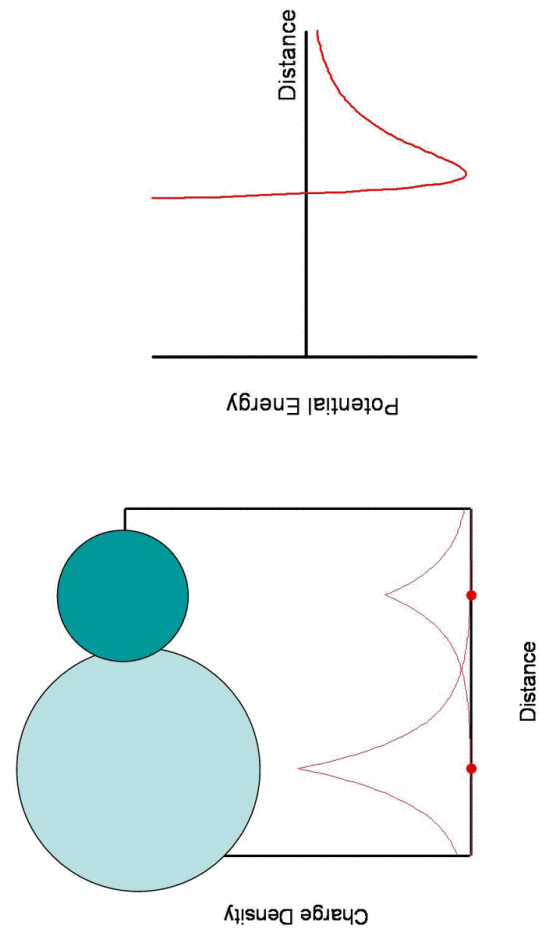
- Pauling/Goldschmidt Model
 - Hard fully charge spheres
 - Rationalize/predict low pressure structures
- High pressure?
 - $P_{\text{bond}} \sim eV/\text{\AA}^3 = 160 \text{ GPa} \sim P_{\text{mantle}}$
 - Ions change
 - Size
 - Shape
 - Charge



Pauling/Goldschmidt Model

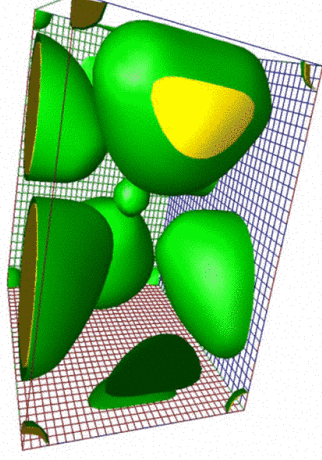


Quantifying the Pauling/Goldschmidt Model



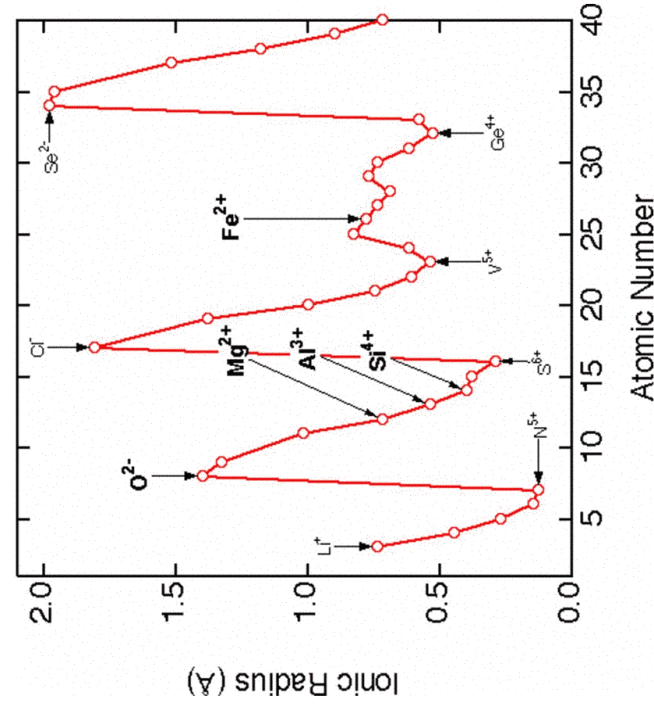
Density functional theory

- No assumption about charge density, type of bonding, ...
- No experimental input, i.e. no free parameters
- Positions and charges of nuclei.
- Assumption of nuclear positions is generally relaxed
- Not exact



Cohen, 1992

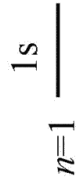
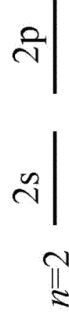
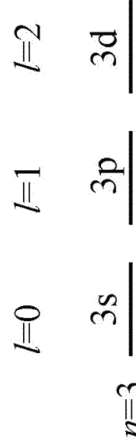
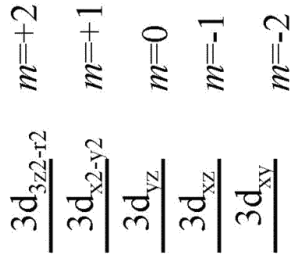
Ionic Radii Shannon and Prewitt



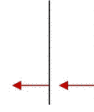
Multi-electron
Atom in a crystal field

Multi-electron
atom

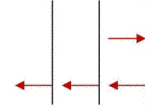
One-electron atom



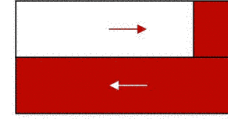
Magnetic Collapse
Origin



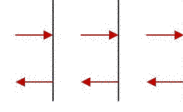
Levels



Low Pressure



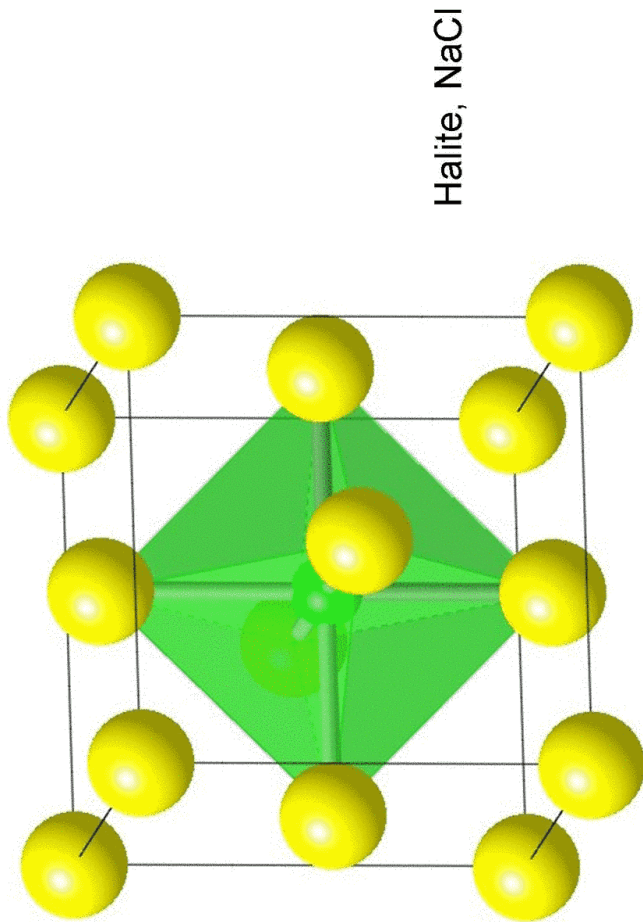
Bands



High Pressure



Coordination Polyhedra

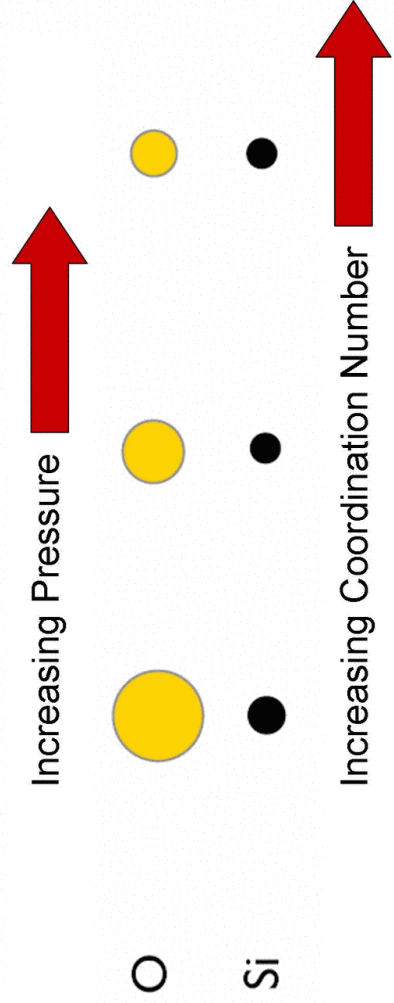


Limiting Radius Ratios

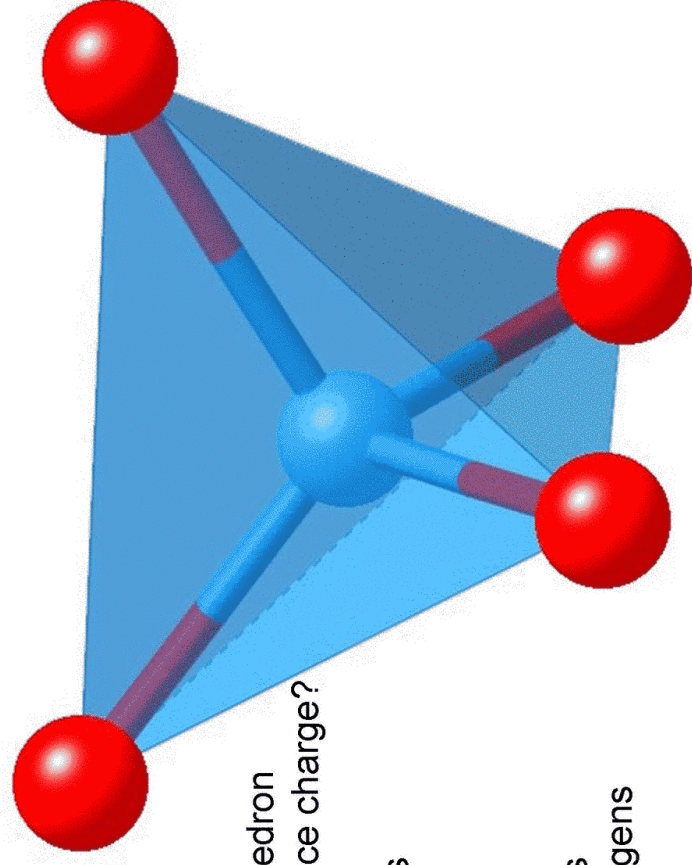
<p>CsCl 8:8</p> <p><i>unit cell</i></p>	<p>NaCl 6:6</p> <p><i>unit cell</i></p>	<p>ZnS 4:4</p> <p><i>1/8th unit cell</i></p>
<p>cell side a</p> <p>$r_c = \frac{1}{2} a \sqrt{3}$ $\frac{1}{2} a \sqrt{2} = r_c \sqrt{2}$</p>	<p>face diagonal $a\sqrt{2}$</p> <p>$\frac{1}{2} a \sqrt{2} = r_c$ $\frac{1}{2} a = r_a$</p>	<p>$\frac{1}{8}$th unit cell</p> <p>$\frac{1}{2} a \sqrt{2} = r_c$ $\frac{1}{4} a = r_a$</p>
<p>$r_u + r_r = r_c \sqrt{3}$ $r_u / r_r = \sqrt{3} - 1$ = 0.732</p>	<p>$r_u + r_r = r_c \sqrt{2}$ $r_u / r_r = \sqrt{2} - 1$ = 0.414</p>	<p>$r_u + r_r = \frac{1}{2} r_c \sqrt{6}$ $r_u / r_r = \frac{1}{2} \sqrt{6} - 1$ = 0.225</p>

Pressure-Induced Coordination Change

- More Efficient Packing
- Ionic Compressibility



Charge Neutrality

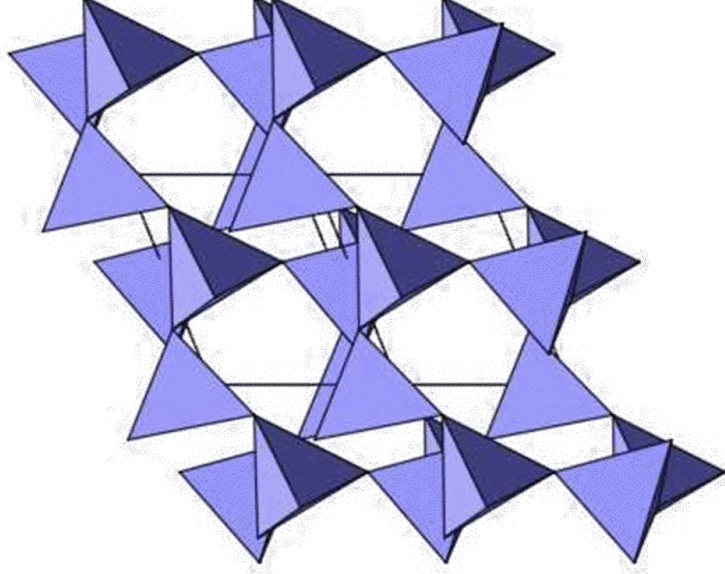


SiO₄⁴⁻ Tetrahedron
How to balance charge?

Orthosilicates
Add cations
e.g. Mg₂SiO₄

Tectosilicates
Share all oxygens
e.g. SiO₂

Charge Neutrality, Sharing of Elements



Quartz, SiO₂
Shared corners

Pauling's Rules 2. Electrostatic Valency

$$e.v. = z/n$$

e.v. electrostatic valency

z = ionic charge

n = coordination number

Electrons Transferred

Cations -> Coordinating Anions

How many electrons? z

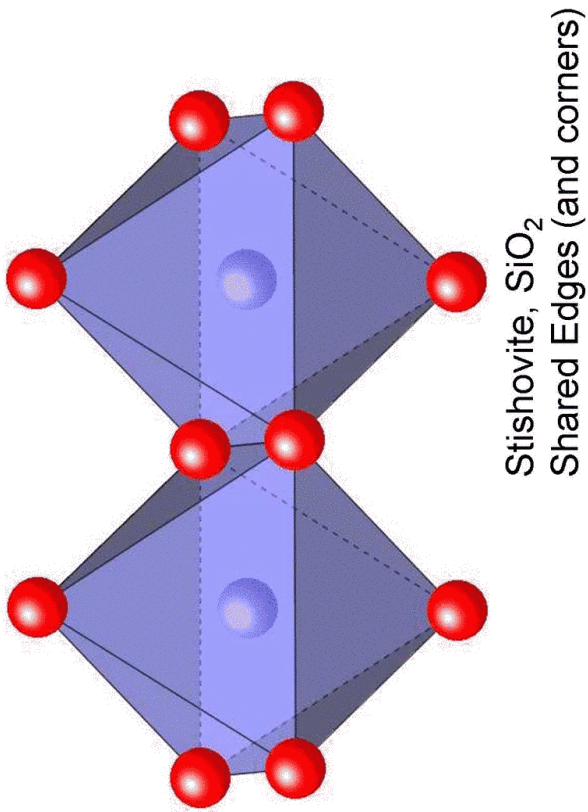
To how many anions? n

e.v. a measure of bond strength

Isodesmic

Anisodesmic

Charge Neutrality, Sharing of Elements



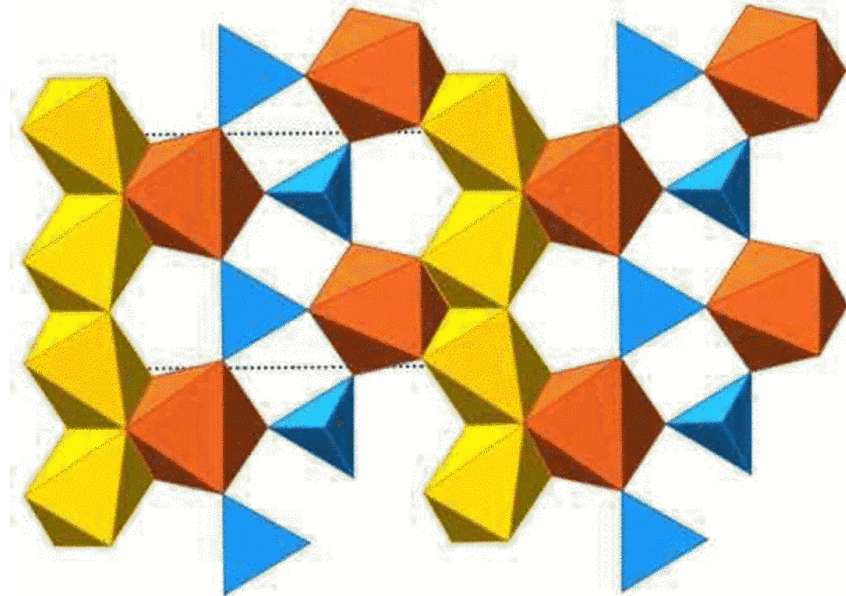
Olivine, Mg_2SiO_4

Mg-octahedra: yellow, orange
Si-tetrahedra: blue

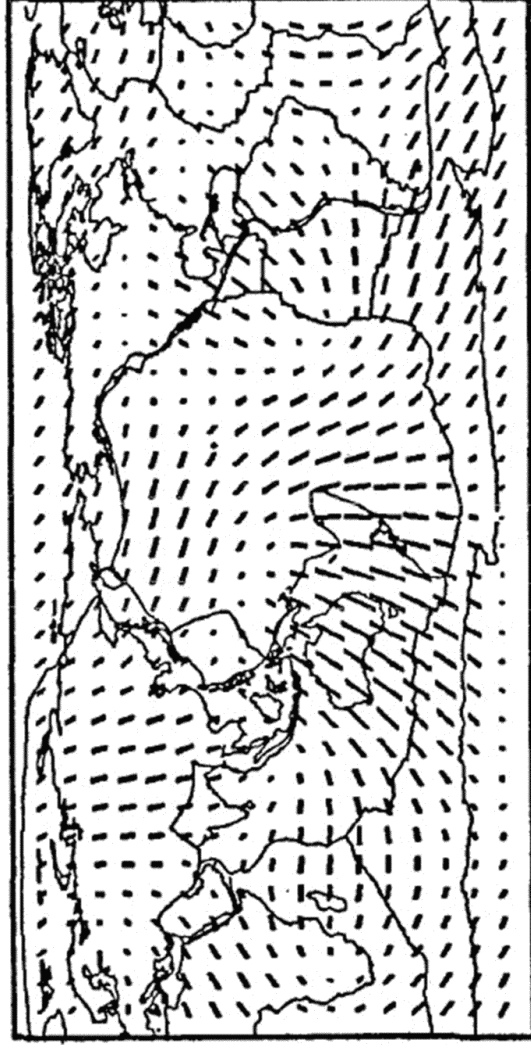
Tetrahedra are isolated, i.e. do not share elements with other tetrahedra

Characteristic of orthosilicates

Also includes garnet



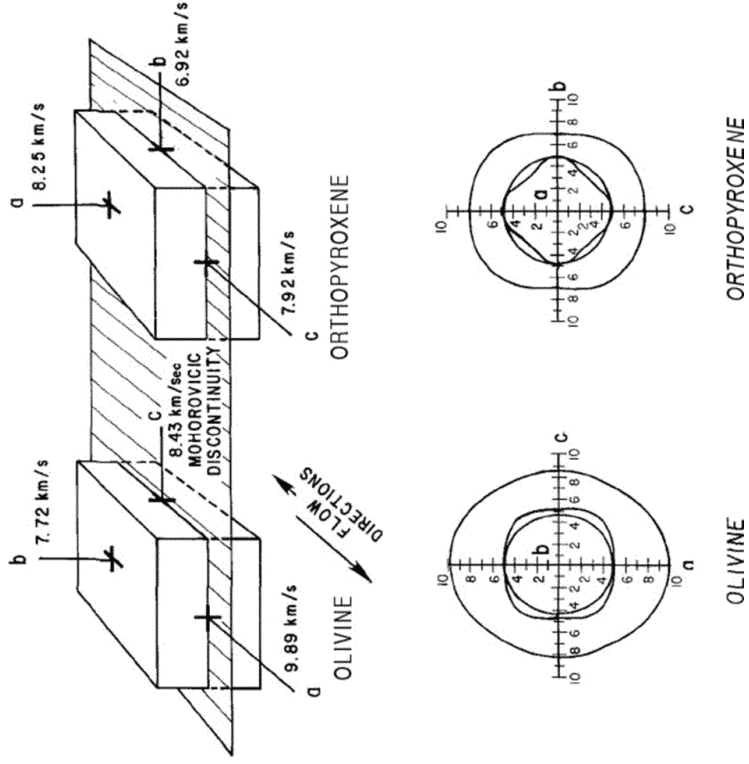
Upper Mantle Azimuthal Anisotropy



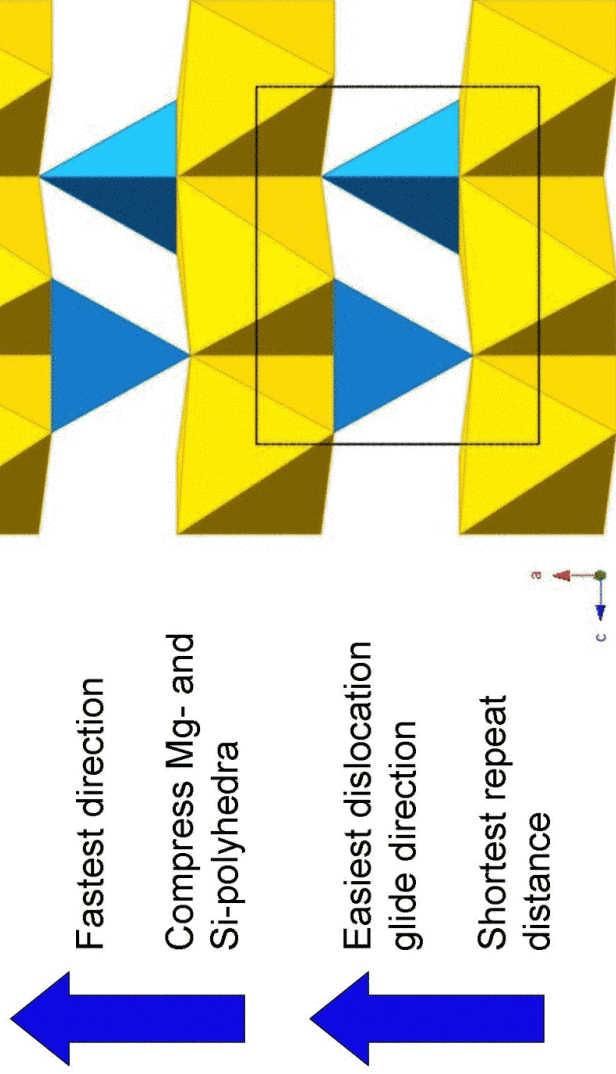
Fast Direction ~ Flow Direction

Tanimoto and Anderson (1984)

Anisotropy and Deformation of Olivine

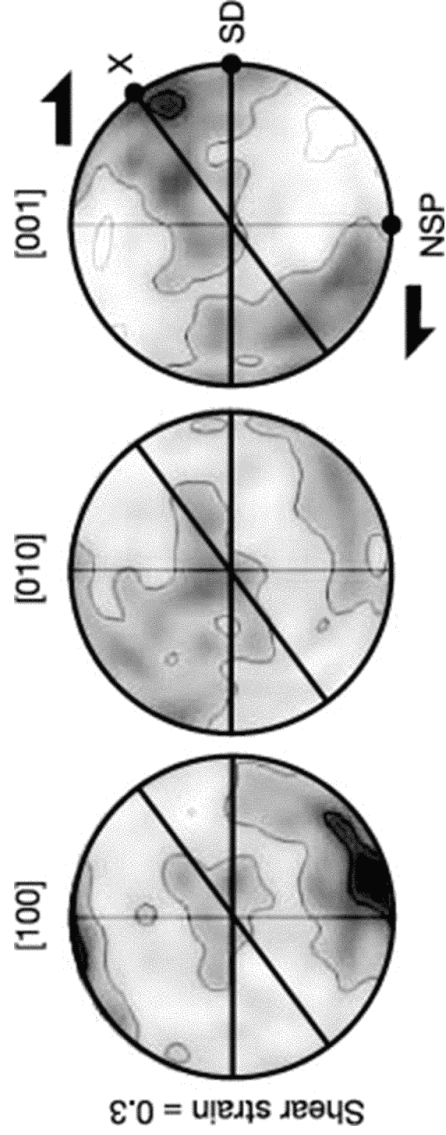


Olivine, Mg_2SiO_4

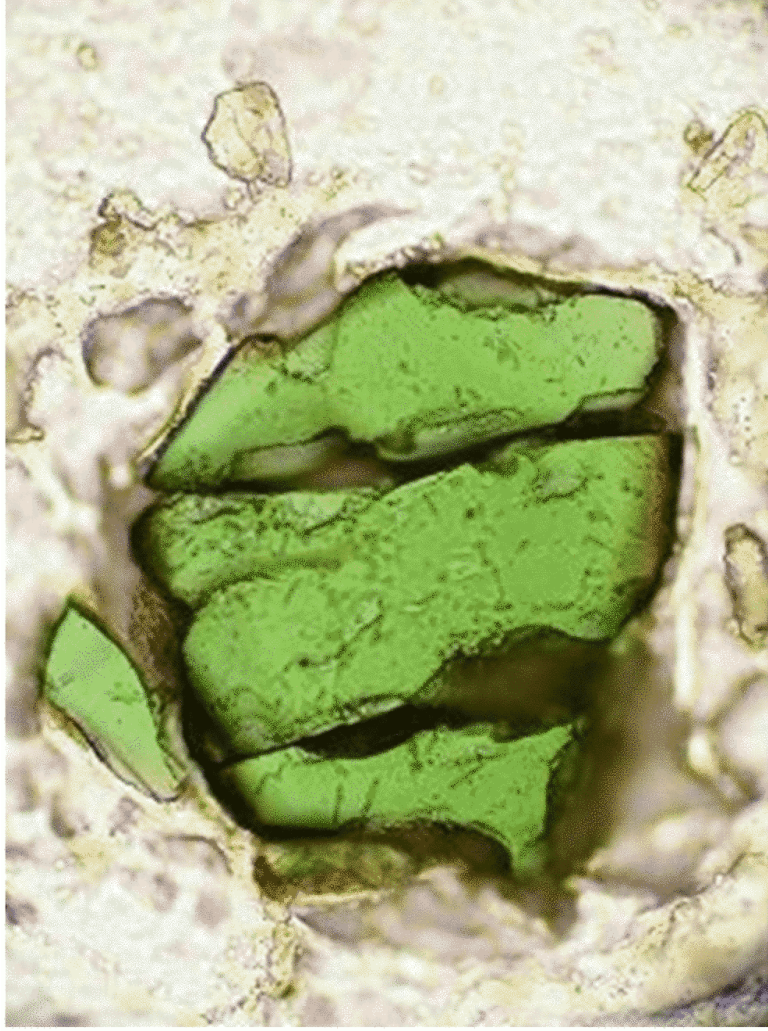


Olivine at 11 GPa (~300 km depth)

Easy slip along c!
Fastest direction perpendicular to flow!



Mainprice et al. (2005)



Synthetic wadsleyite II

Wadsleyite, Mg_2SiO_4

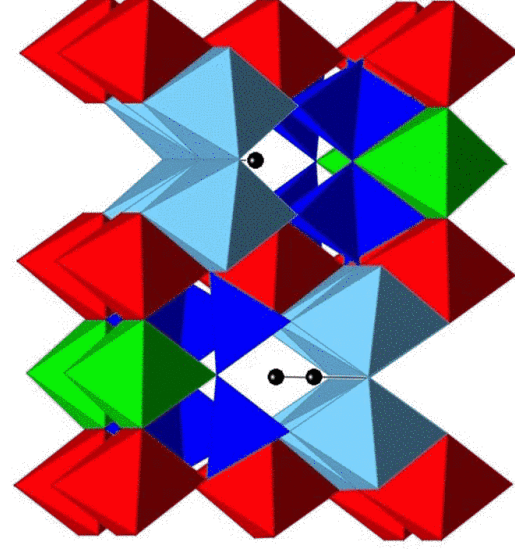
Pairs of tetrahedra share corners

Like sorosilicates (e.g. epidote)
But wrong composition!

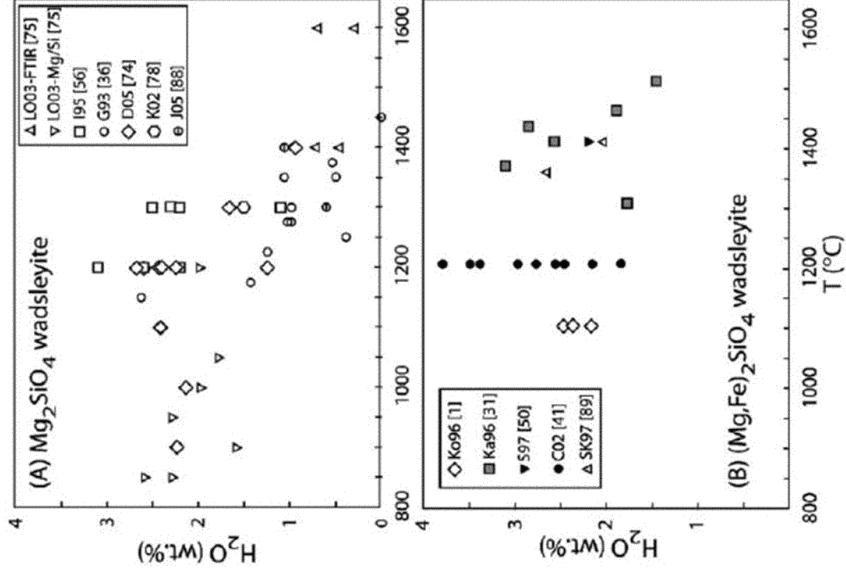
Underbonded oxygen
2/6 electrons from each of five
 $Mg = -5/3 < -2$

Ideal place for a hydrogen
Charge balanced by Mg
vacancies

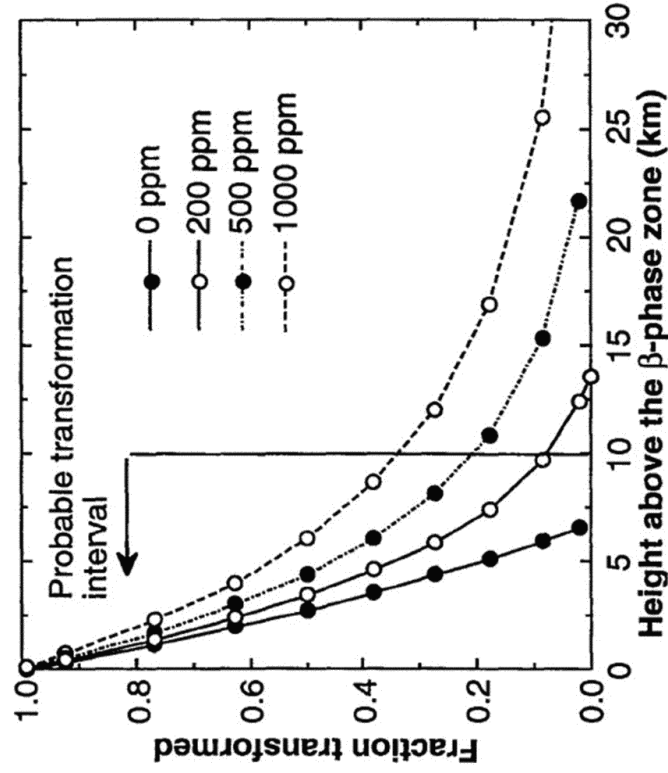
Smyth (1994)



Water solubility in
wadsleyite
Hirschmann et al. (2005)
Several weight %
Several oceans if fully
hydrated



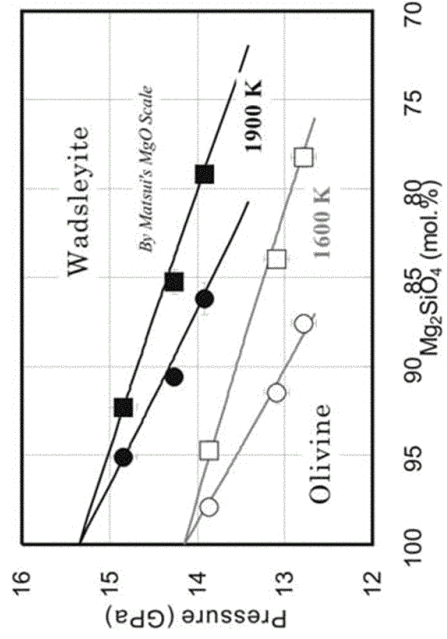
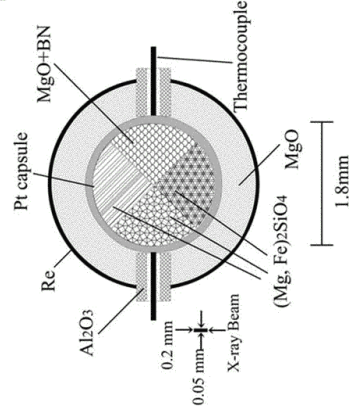
Detection of Water?



Wood (1995)

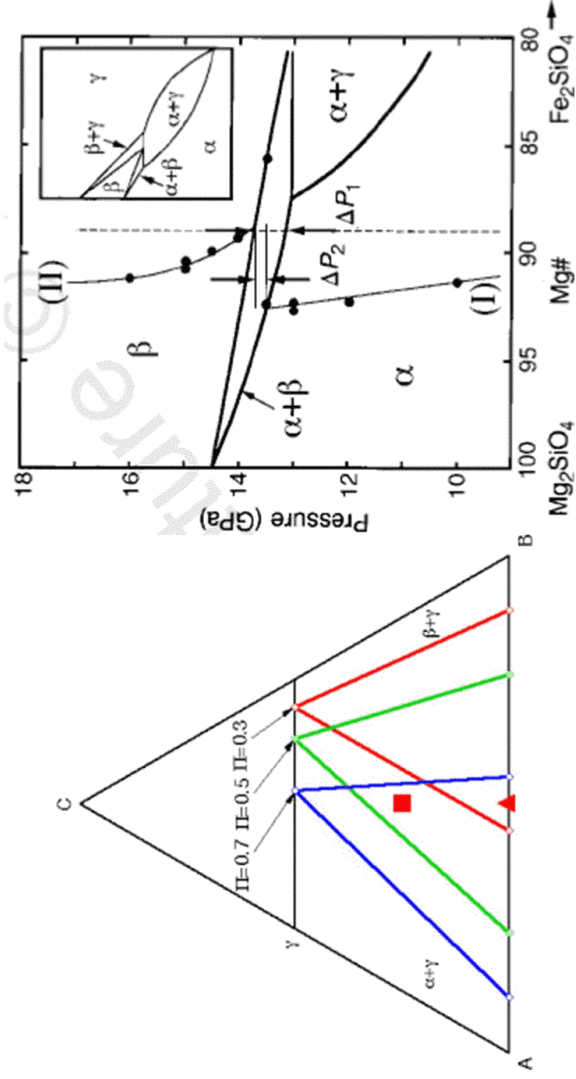
Olivine to Wadsleyite Transition

- Mg_2SiO_4 - Fe_2SiO_4 System



Katsura et al. (2004) GRL

Sharpness of the 410 km discontinuity



Stixrude (1997)

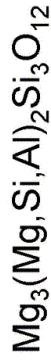
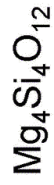
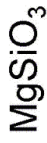
Irifune and Isshiki (1998)

Garnet

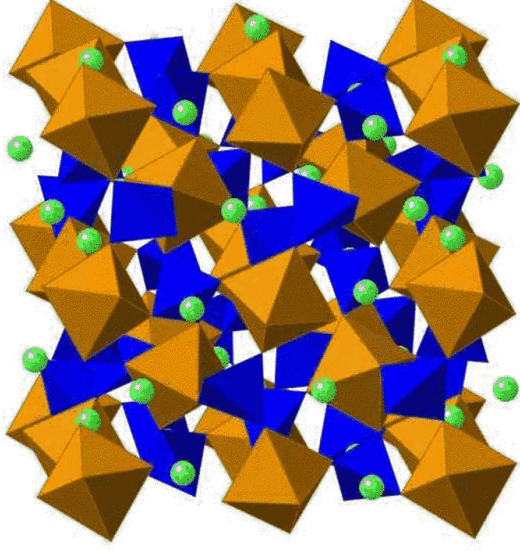


8-, 6-, 4-coordinated sites
Garbage can!

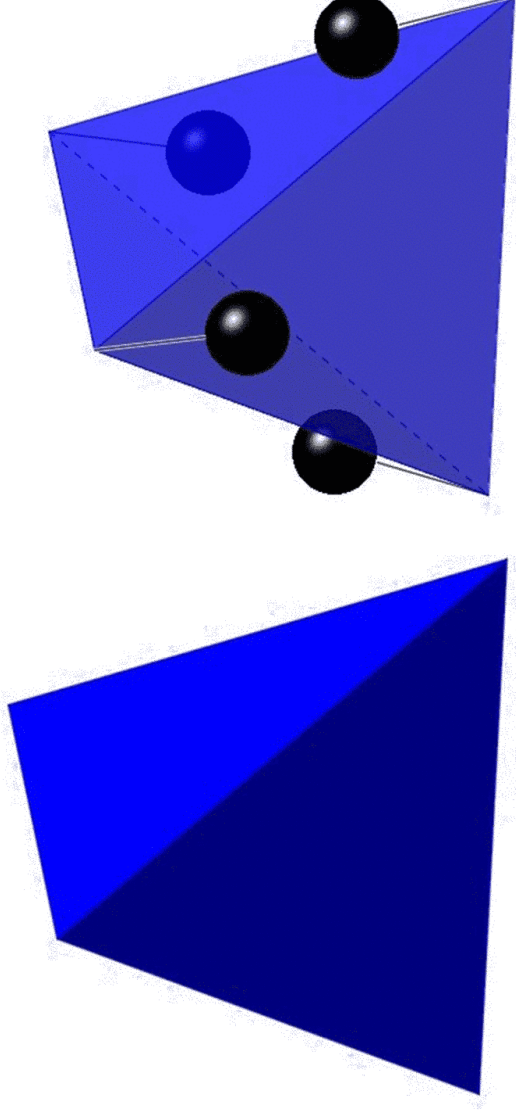
Dissolves pyroxenes



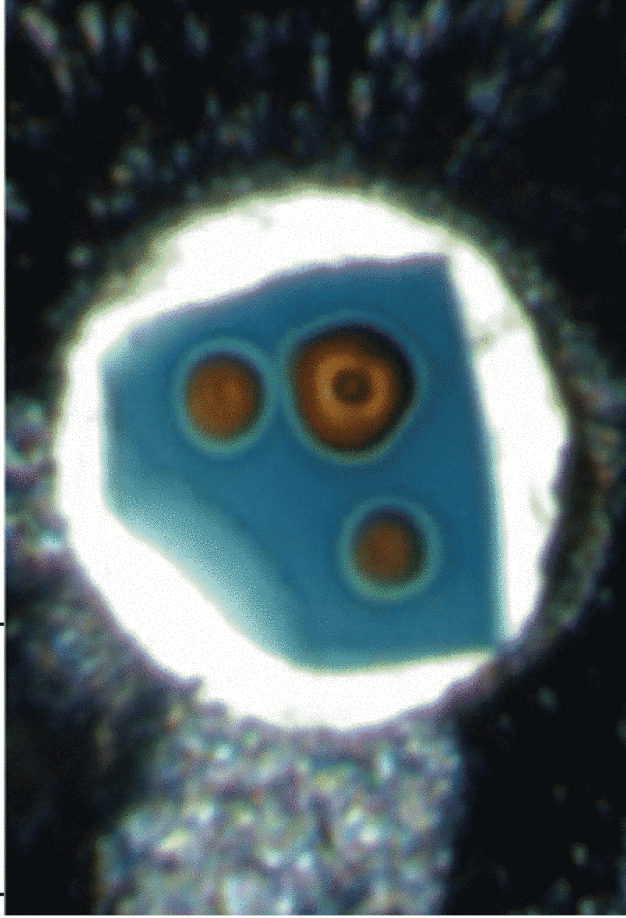
i.e. some Si in 6-fold site



Water in Garnet

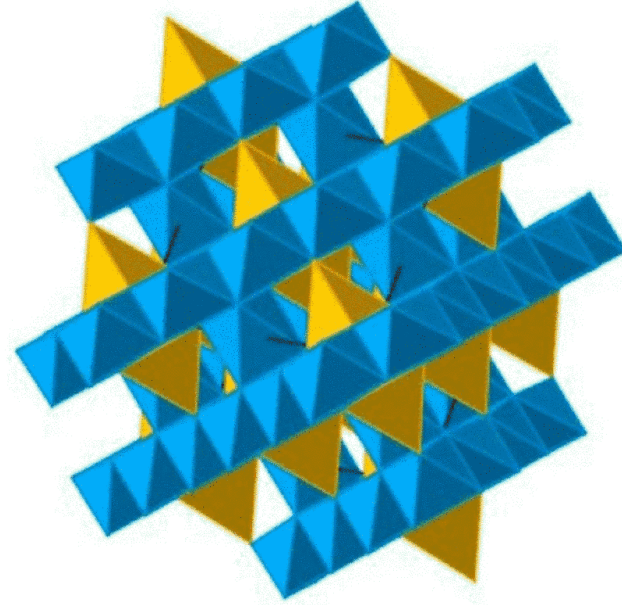


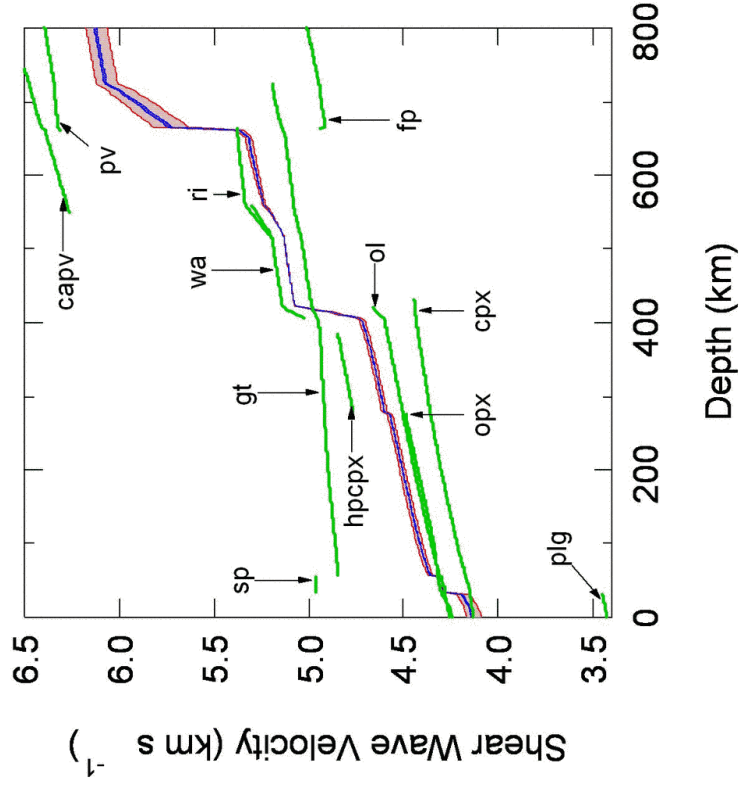
Blue hydrous ringwoodite viewed in situ through the diamond anvil cell, transformed in laser-heated spots to perovskite+ferropericlase



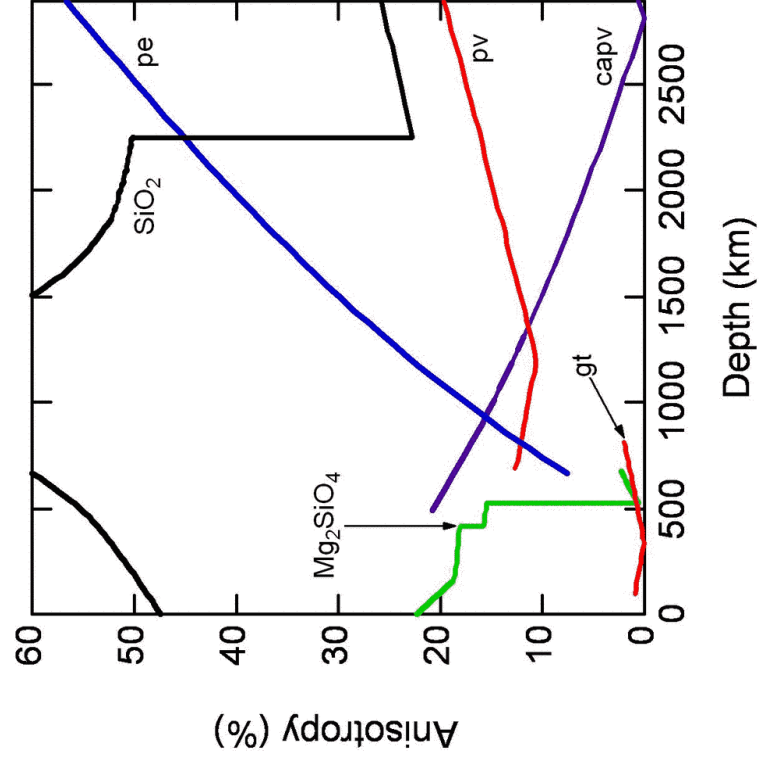
Jacobsen and Lin (2005)

Ringwoodite

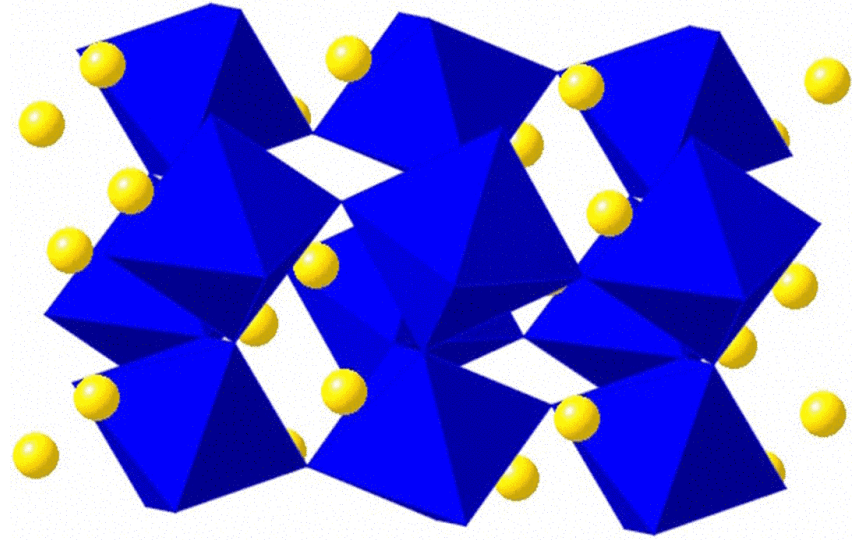
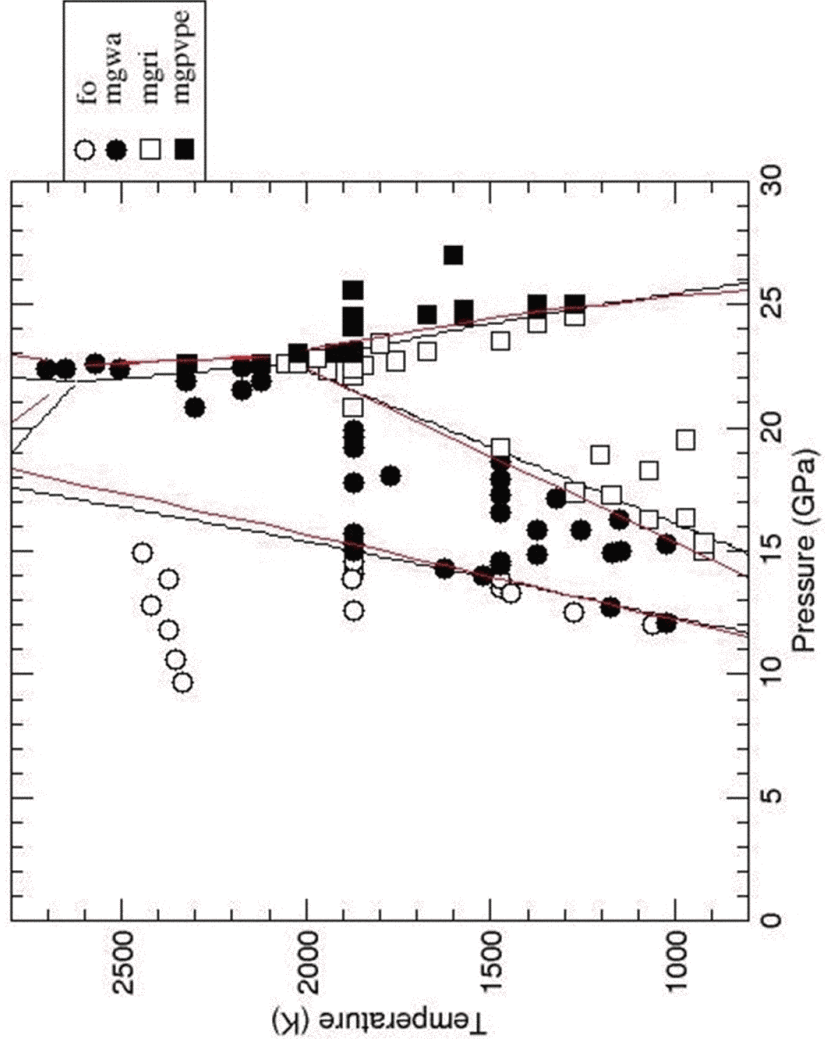




Stixrude (2006) Treatise on Geophysics



Stixrude (2006) Treatise on Geophysics



Pervoskite