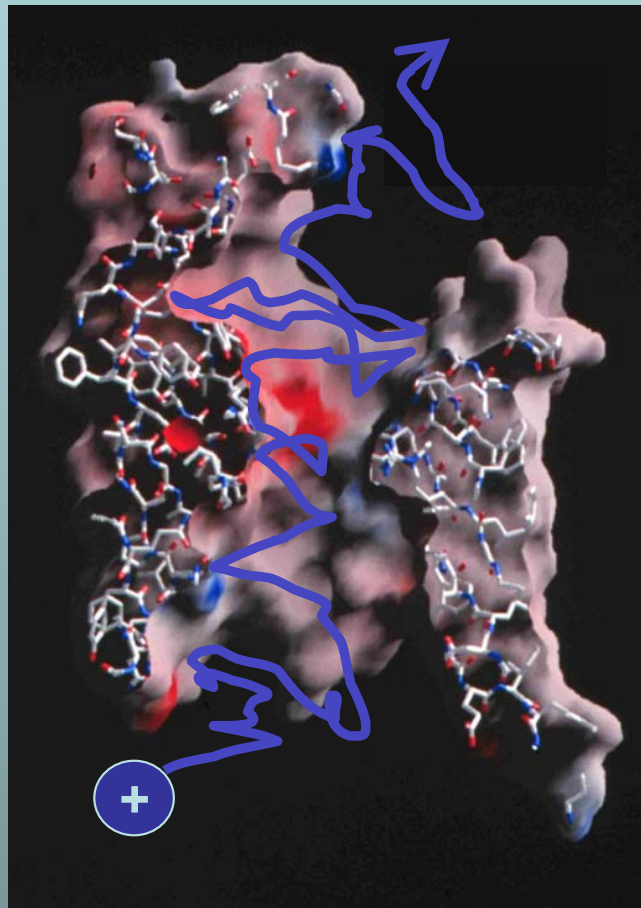
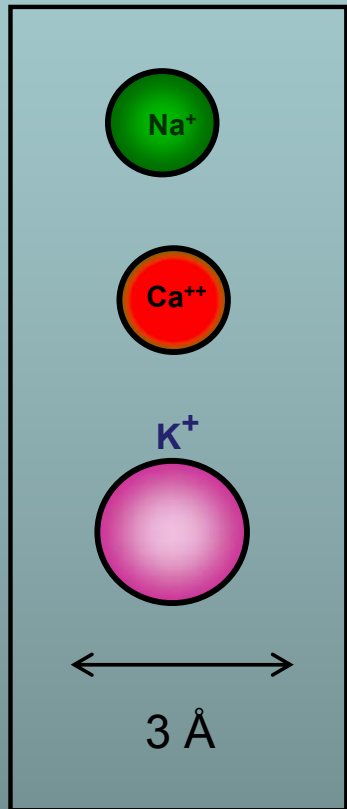


# Ionic Channels are Valves\* of Cells

## Main Controllers of Biological Function



~30 Å

Flow time scale is 0.1 msec to min

*Figure of ompF porin by Raimund Dutzler*

Chemical Bonds are lines  
Surface is Electrical Potential  
Red is negative (acid)  
Blue is positive (basic)

\*Pun:

Valve = Vacuum Tube  
≈ PNP Transistor  
≈ FET Transistor

**BritSpeak**

# Biology and Chemistry are about Chemically Specific Properties

Chemically Specific Properties  
are the same thing as their  
DEVIATION from IDEAL

**Life Occurs in ~130 mM salt solutions**  
*mostly Sodium  $\text{Na}^+$ , Potassium  $\text{K}^+$ , and Calcium  $\text{Ca}^{++}$  Chloride  $\text{Cl}^-$*

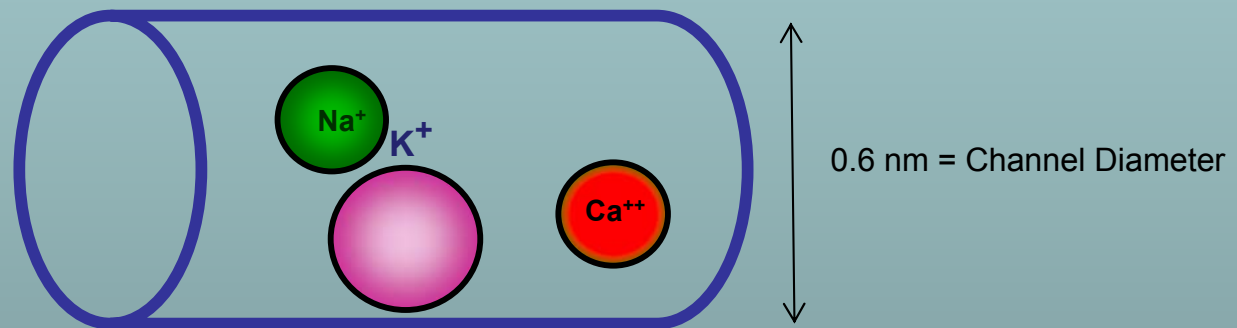
# Ions in Water

are the

## *Liquid of Life*

**Life Occurs in ~130 mM salt solutions**

*mostly  $\text{Na}^+$ ,  $\text{K}^+$ , and  $\text{Ca}^{++}$   $\text{Cl}^-$*



Ions in water and channels are NOT ideal solutions  
because

**Chemically Specific Properties of Ionic solution are their  
DEVIATION from IDEAL**

Molecular Dynamics Force Fields are Calibrated in the ideal in Infinitely Dilute solutions,  
for the most part.

**Biological Theory**  
and  
**Molecular Dynamics Simulations**  
**almost always assume ideal solutions**

*In my opinion*

**New Mathematics**

is needed to deal

**with the INTERACTIONS**

that make ionic solutions non ideal

and that can create the

**CHEMICAL SPECIFICITY**

**of life**

**Biological Theory**  
and  
**Molecular Dynamics Simulations**  
**almost always assume ideal solutions**

*In my opinion*

**New Mathematics**

is needed to deal

**with the INTERACTIONS**

that make ionic solutions non ideal

and that can create the

**CHEMICAL SPECIFICITY**

**of life**

*In my opinion*

**New Mathematics**

is needed to deal

**with the INTERACTIONS**

that make ionic solutions non ideal

and that can create the

**CHEMICAL SPECIFICITY**

**of life**

**No theory is available for properties of mixtures of ions**

**Brownian Motion theory is for UNcharged particles.**

**Brownian Motion theory ignores Interactions**

# **Ion Channels are a good Test Case**

**Simple Physics** (Electrodifffusion)

**Single Structure** (once open)

**Simple Theory is Possible**

and Reasonably Robust

**because Channels are Devices**

with well defined

**Inputs, Outputs and Power Supplies**

*Channels are also Biologically Very Important*

# Ion Channels are Biological Devices

Natural nano-valves\* for atomic control of biological function

Ion channels coordinate contraction in the heart, allowing the heart to function as a pump

Ion channels coordinate contraction in skeletal muscle

Ion channels control all electrical activity in cells

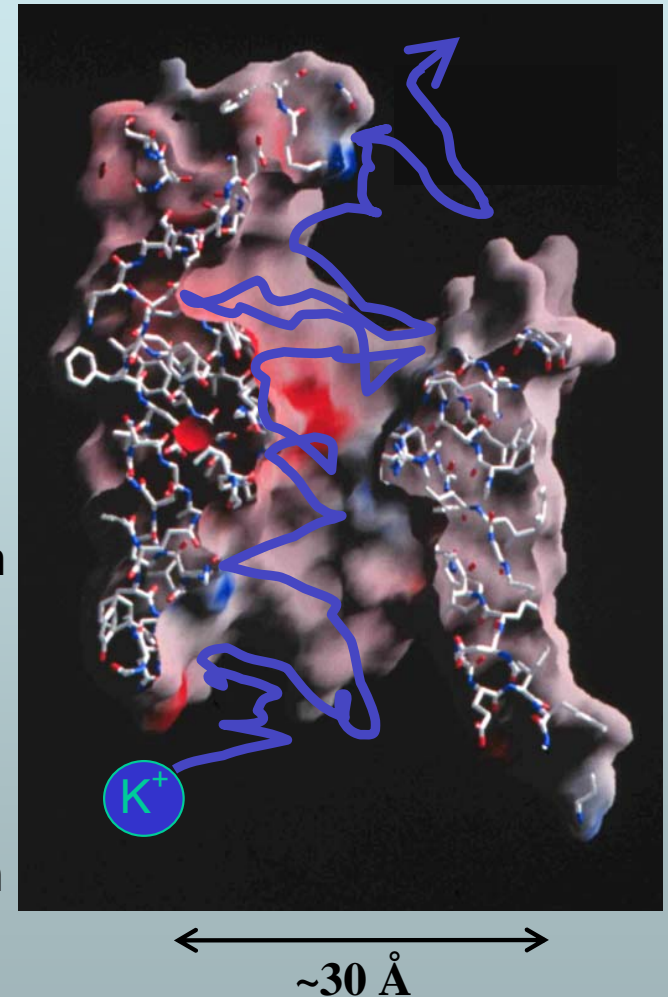
Ion channels produce signals of the nervous system

Ion channels are involved in secretion and absorption in all cells: kidney, intestine, liver, adrenal glands, etc.

Ion channels are involved in thousands of diseases and many drugs act on channels

Ion channels are proteins whose genes (blueprints) can be manipulated by molecular genetics

Ion channels have structures shown by x-ray crystallography in favorable cases.



\*nearly pico-valves: diameter is 400 - 900 pico-meters

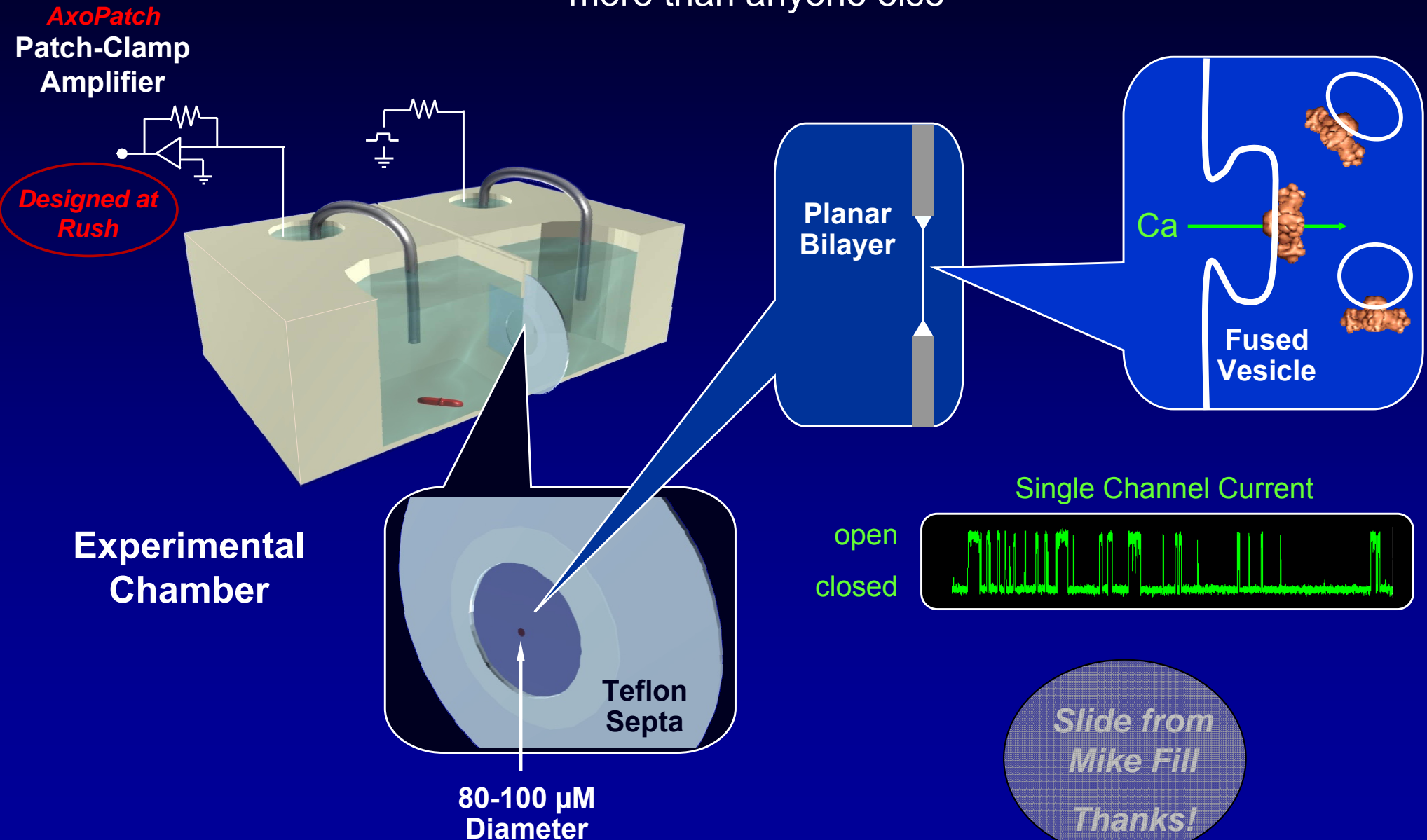
**Ion Channels are studied experimentally  
by thousands of molecular biologists  
every day because they are so important.**

*This number is not an exaggeration.  
We have sold over 10,000 AxoPatch Amplifiers*

# Reconstitution of Single Channels....

## Thanks to Chris Miller !!!

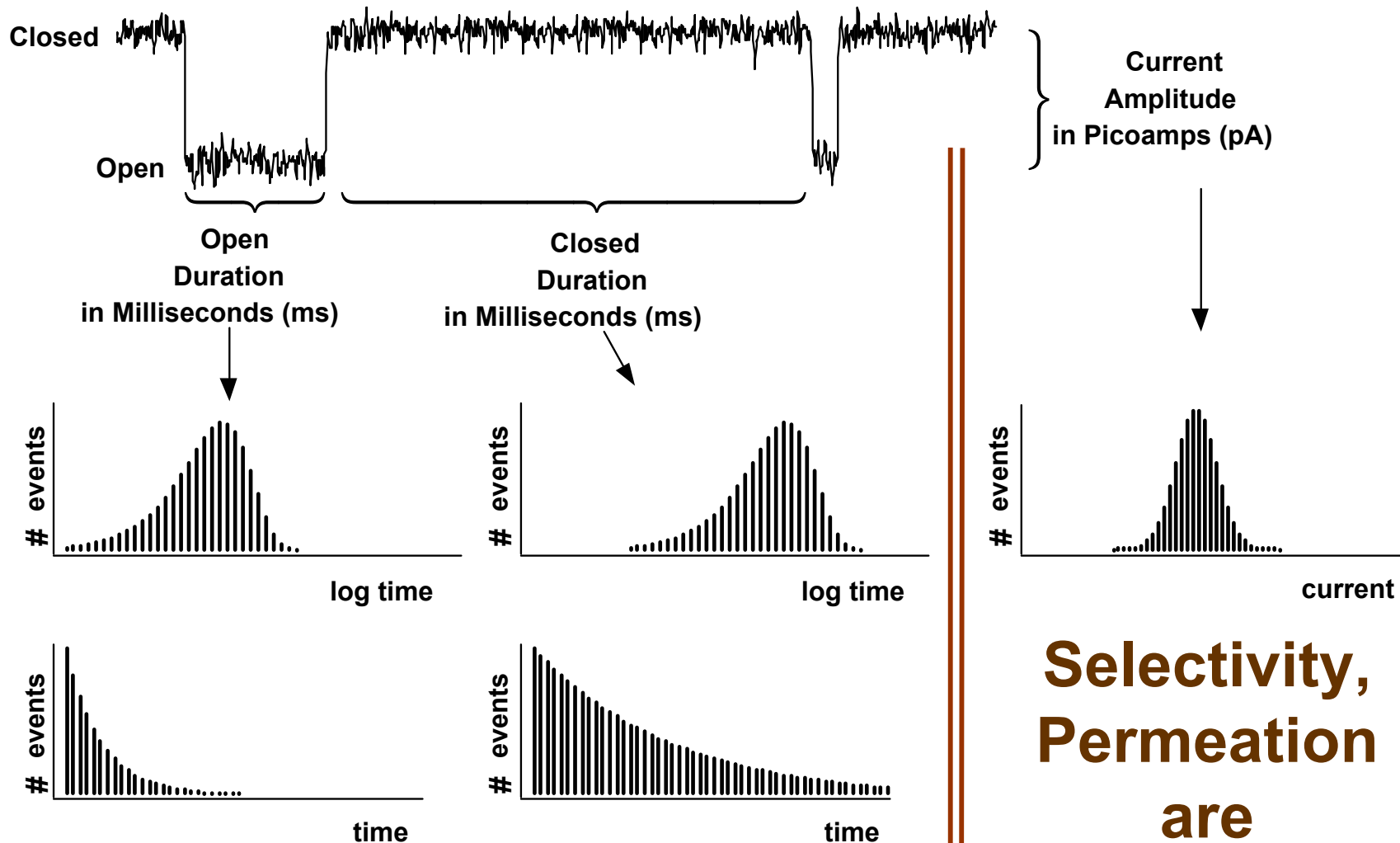
more than anyone else



Slide from  
Mike Fill

Thanks!

# Gating and Permeation



**Gating is Time Behavior**

**Selectivity,  
Permeation  
are  
Amplitude**

***Goal:***  
**Understand Selectivity**

**Selectivity  
Differs  
in Different Types of  
Channels**

**Wolfgang Nonner, Dirk Gillespie, Douglas Henderson, Dezső Boda**

***Goal:***

**Understand the Adaptation that makes Selectivity**

**Selectivity  
is an Adaption  
Necessary for Channels to  
Function**

## Selectivity of Different Channel Types Studied in Many Solutions

<b>RyR Channel</b>	<b>Calcium Channel</b>	<b>Sodium Channel</b>	<b>Synthetic Ca Channel</b>
<b>Selectivity filter</b> <i><b>DDDD</b></i> 4 – charges	<b>Selectivity filter</b> <i><b>EEEE</b></i> 4 – charges	<b>Selectivity filter</b> <i><b>DEKA</b></i> 2 –, 1+ charge	<b>Selectivity filter</b> <i><b>Various</b></i> many – charges
PNP/DFT	PNP/DFT Monte Carlo	Monte Carlo	PNP/DFT

RyR model of Gillespie is best worked out for ~ 120 solutions

Selectivity of K Channel is studied in ~1 solution at infinite dilution

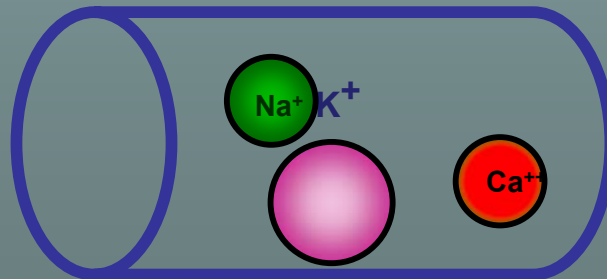
K channel of Roux has atomic detail but is studied at infinite dilution

Quantum /K of Rempe has atomic detail but is studied at infinite dilution

“There is only one word  
that matters in biology  
and that is  
**Specificity** ....”

Aaron Klug

*quoted in the first sentence of H. Pearson, Nature (2008) 455:160 - 164*



**Goal:**

**Understand Selectivity**

well enough to

**Fit Large Amounts of Data\***

and to

**Make a Calcium Channel**

\*from many non-ideal solutions

**Molecular Biologists need a framework  
to interpret their results.**

**Evolutionary Biology, Physics, and Chemistry  
can provide that framework.**

# **Reduced Models**

form the framework for understanding experiments.

Reduced models describe the

## **Input, Output, and Power Supply.**

They describe the essential physics and chemistry.

## **Reduced models are the adaptation**

created by evolution

to perform the biological function of selectivity.

## **Reduced models are the Phenotype**

of the channel

*in my understanding of the meaning of that word*

# **Reduced models are Device Equations**

like Input Output Relations of Engineering Systems.

Finding the reduced model,  
checking its validity,  
estimating its parameters, and their effects,  
are all part of the

**Inverse Problem:**  
**‘Reverse Engineering’ of Selectivity**

In my view,

**Finding the evolutionary adaptation,**

**Finding the underlying physics,**

**Finding the Device equation, and**

**'Reverse engineering' Selectivity**

**are nearly the same things as**

**Understanding Physiology**

**Enough Vague Stuff**

**Goal:**

**Understand Selectivity**

well enough to

**Fit Large Amounts of Data\***

and to

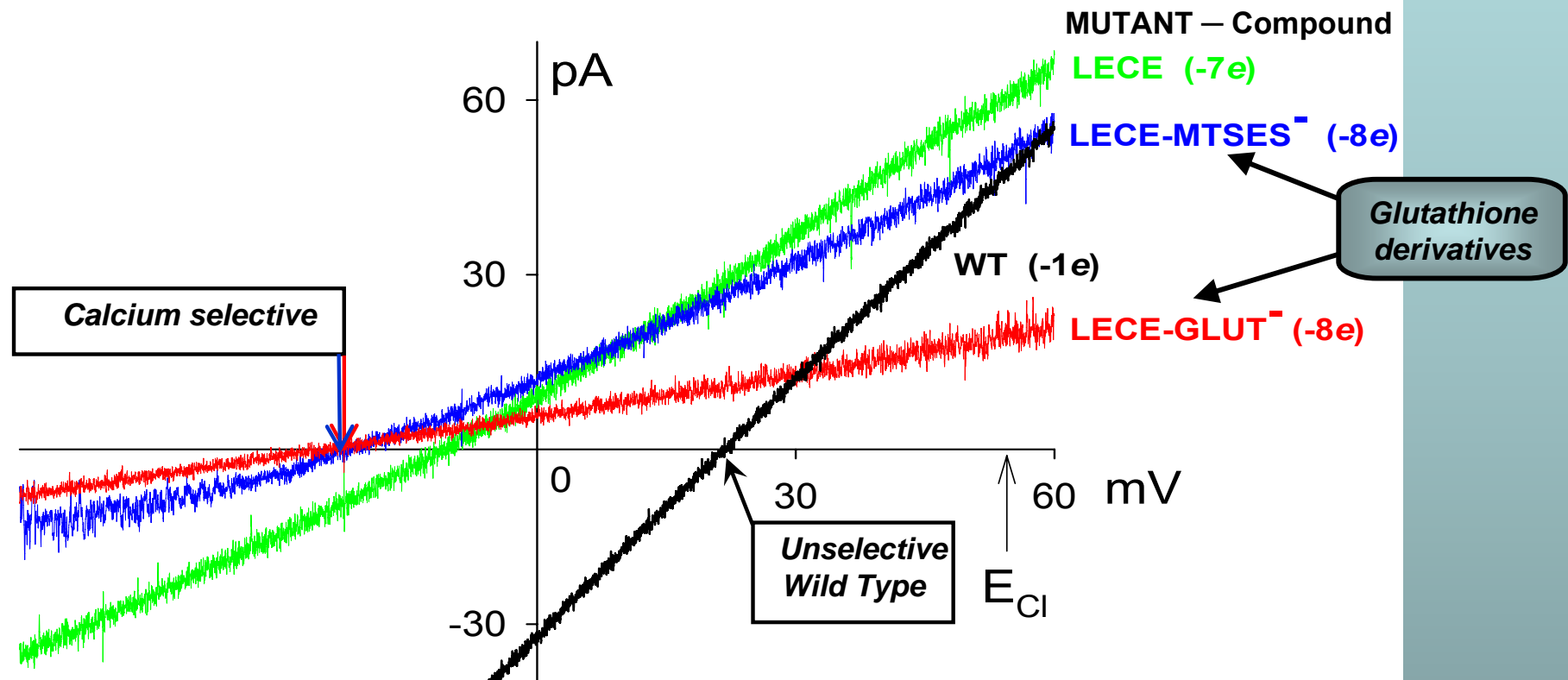
**Make a Calcium Channel**

\*from many non-ideal solutions

# Experiments have built Two Synthetic Calcium Channels

*Designed by Theory*

Mutants of ompF Porin



As density of permanent charge increases, channel becomes calcium selective

$$E_{rev} \rightarrow E_{Ca}$$

*built by Henk Miedema, Wim Meijberg of BioMade Corp., Groningen, Netherlands*

*Miedema et al, Biophys J 87: 3137–3147 (2004)*

# ***Channels are only Holes***

Why can't we understand and build them?

Must have high quality measurements

Must know physical basis of function

## ***Where do we start?***

Not with molecular mythology

Not with gas phase models of traditional channology

*Liquids are not Gases*

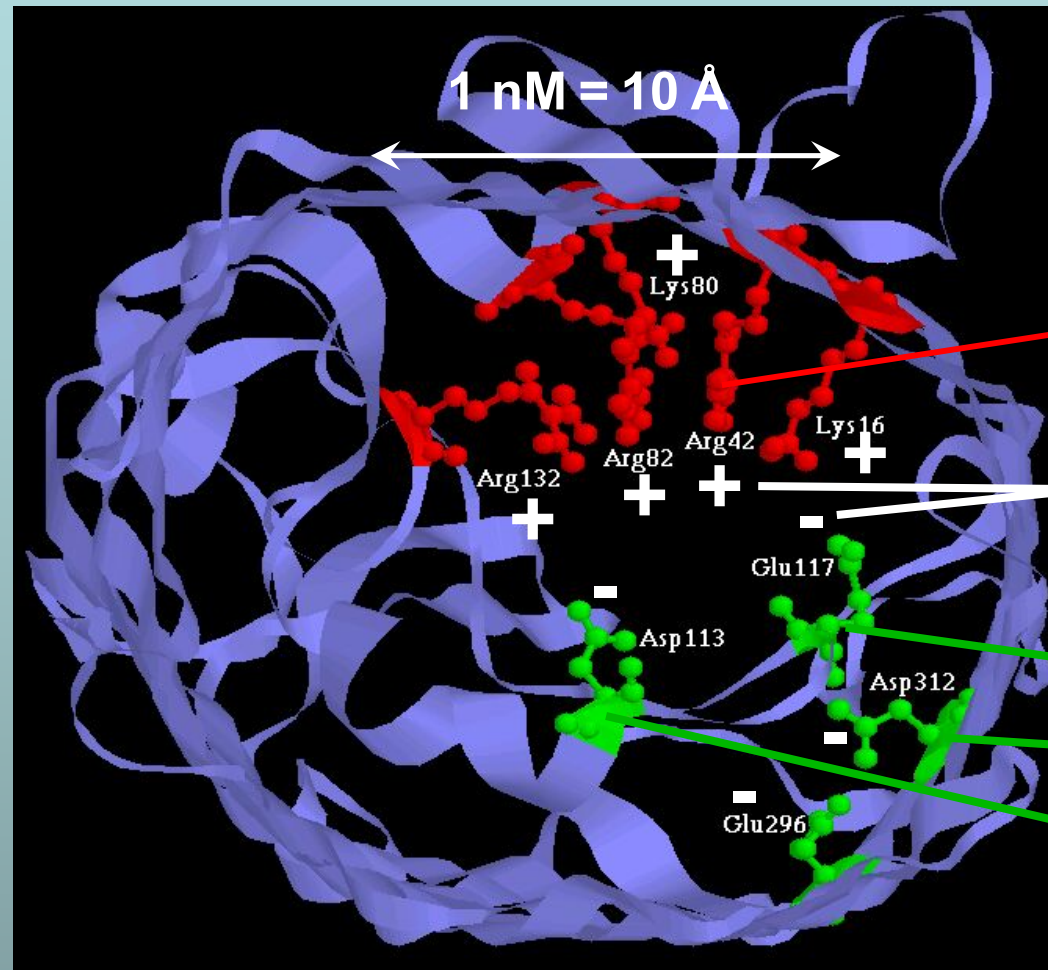
Not with guesses about trajectories of structural biologists

*Counting and Statistics are essential when atomic trajectories are involved*

# Active Sites of Proteins are **Very Charged**

7 charges ~ **20 M net charge** =  $1.2 \times 10^{22} \text{ cm}^{-3}$

Pure water is 55 M



Side Chains  
mix with

Ions are  
**Crowded**

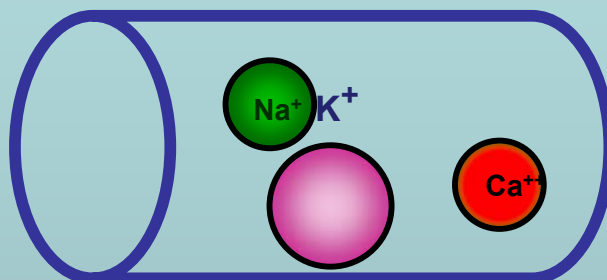
Side  
Chains  
MIX with  
Water, Ions

Selectivity Filters and Gates of Ion Channels  
are  
**Active Sites**

Figure adapted  
from Tilman  
Schirmer 24

# Finite Size Effects

*Working Hypothesis Implicit Solvent Model*



## Chemically Specific Properties

of ions (e.g. activity = free energy per mole)  
come from their

## Diameter and Charge

Atomic Detail



and dielectric ‘constant’ of ionic solution

‘Primitive Implicit Solvent Model’

learned from Doug Henderson, J.-P. Hansen, Stuart Rice, among others... <sup>25</sup>

Thanks!

We need a **model of selectivity** and  
**method of calculation**

to describe the **Reduced Model**,  
which is also **the Evolutionary Adaptation**

that shows how  
**Selectivity arises from Crowding of ions**

At equilibrium,  
we use **Monte Carlo simulations**,  
because they are calibrated.

At nonequilibrium, we have used  
**Density Functional Theory** (of fluids)  
**combined with PNP**

Poisson Nernst Planck theory of drift and diffusion

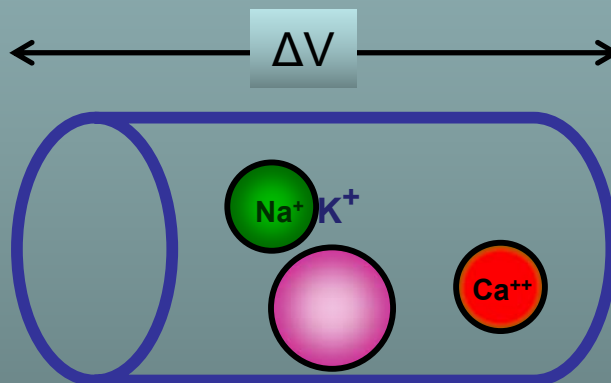
We now introduce the  
**Energy Variational Method**  
of the theory of complex fluids

# Implicit Solvent (“Primitive”) Model of Ionic Solutions

**Almost always an equilibrium theory,**  
*no flows of any kind*

**Usually in the ‘Thermodynamic Limit’**

**No boundary conditions, even for the electric field.**  
*Maxwell died too soon!*



# Energetic Variational Analysis

*EnVarA*

being developed by

Chun Liu,

Yunkyong Hyon, and Bob Eisenberg

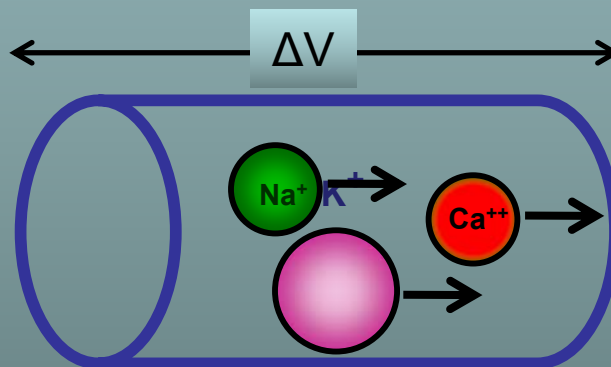
creates a

Field Theory of non-ideal Ionic Solutions

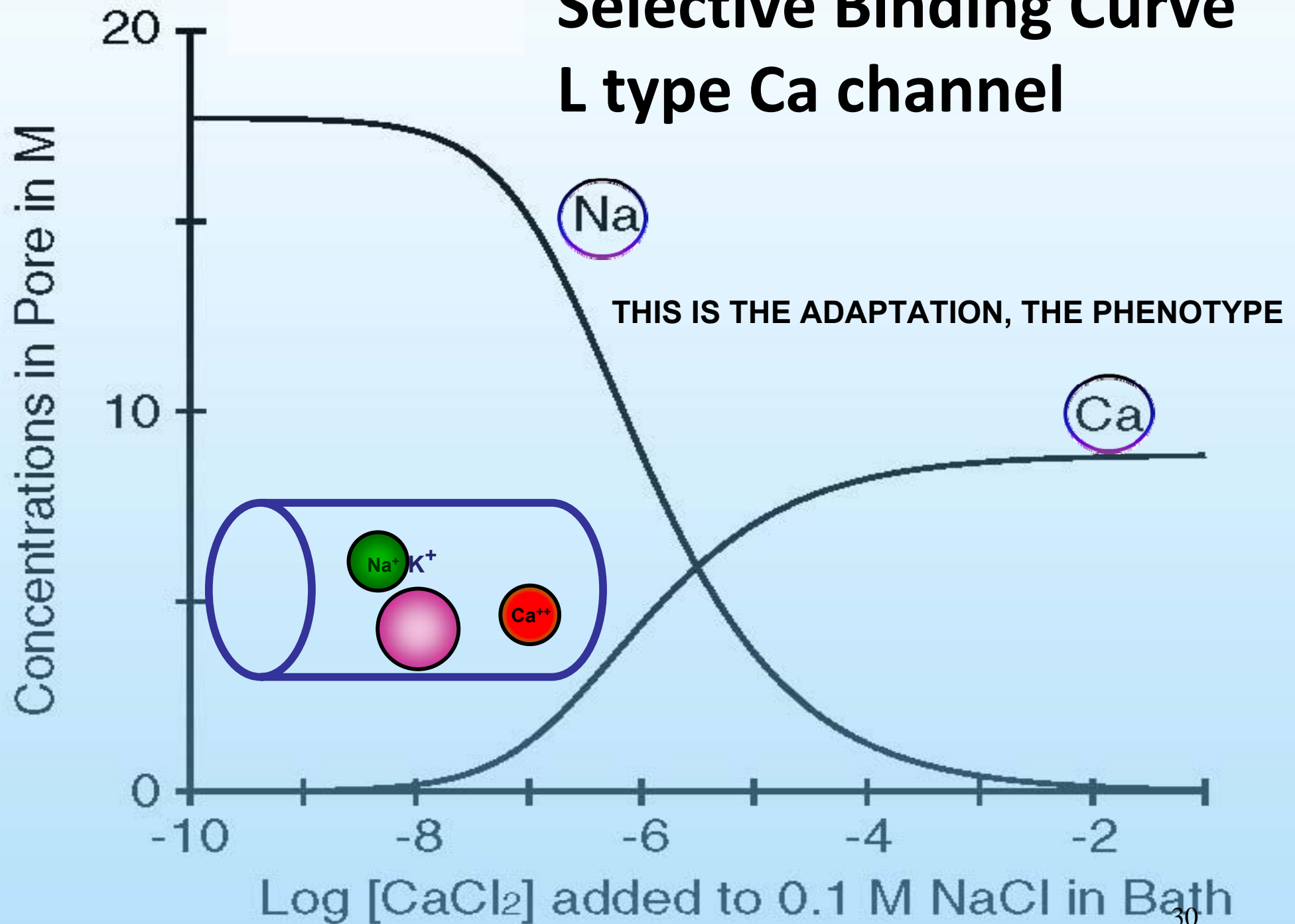
that allows boundary conditions and flow

and deals with

Interactions of Components Self-consistently



# Selective Binding Curve L type Ca channel



# Selectivity Filter

Crowded with Charge

L type Ca Channel

THIS IS THE MODEL

Selectivity  
Filter

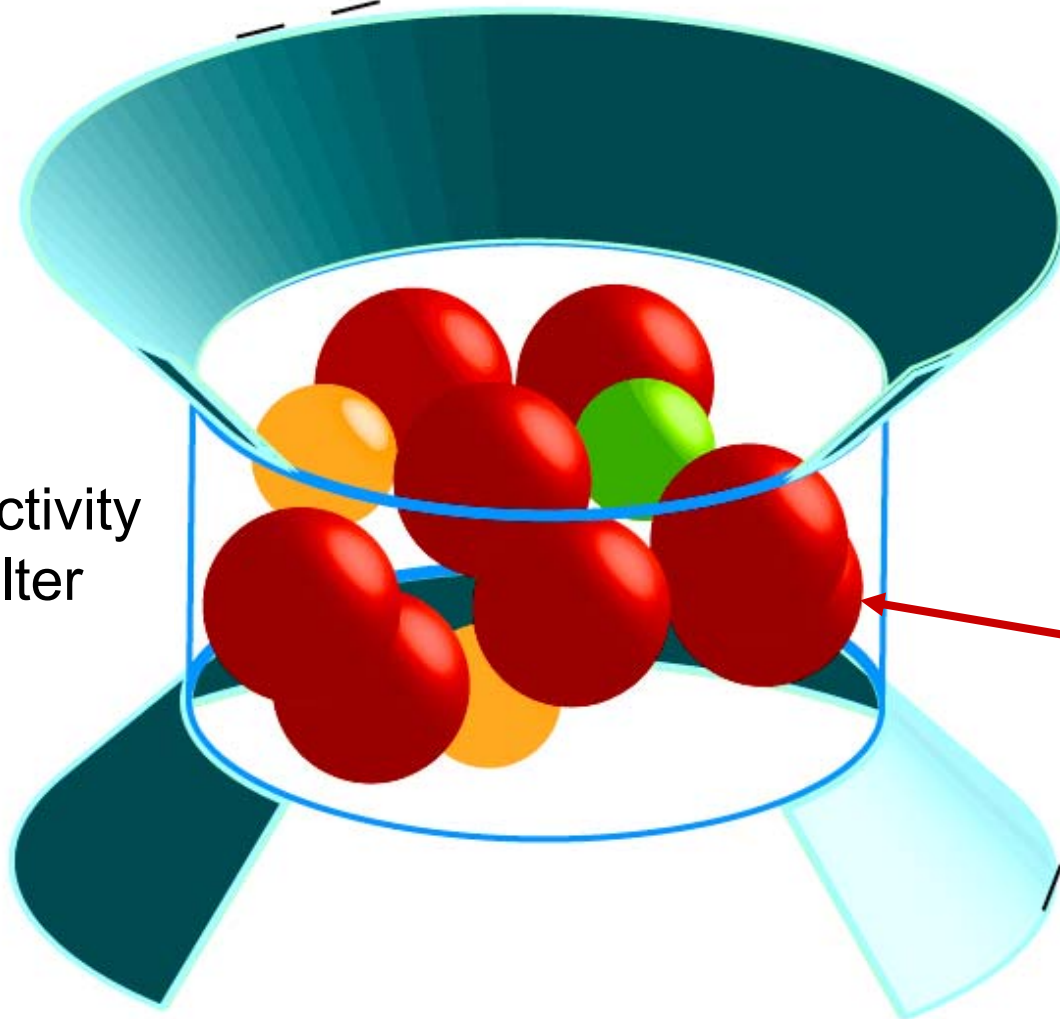
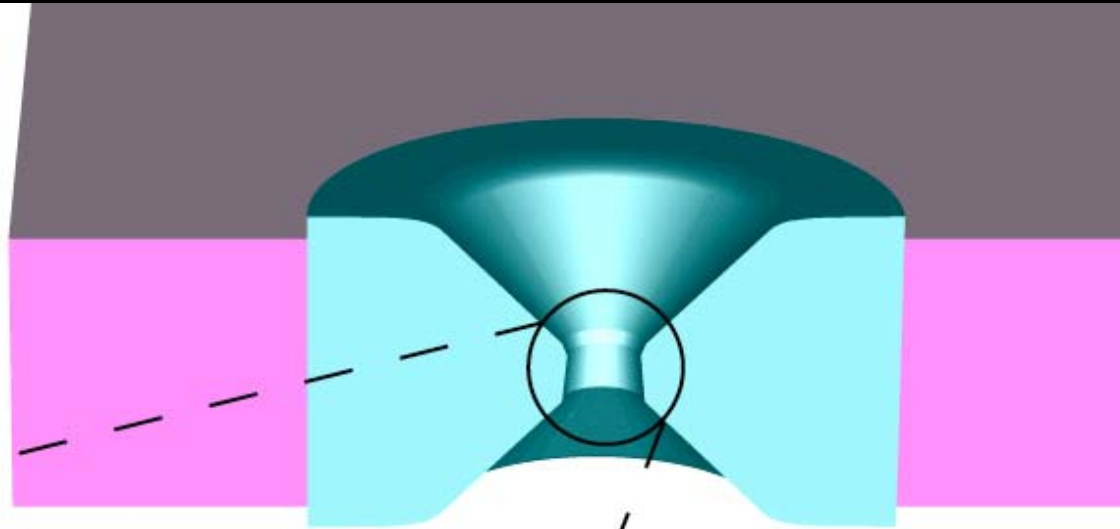
“Side Chains”

$\text{Na}^+$

$\text{Ca}^{++}$

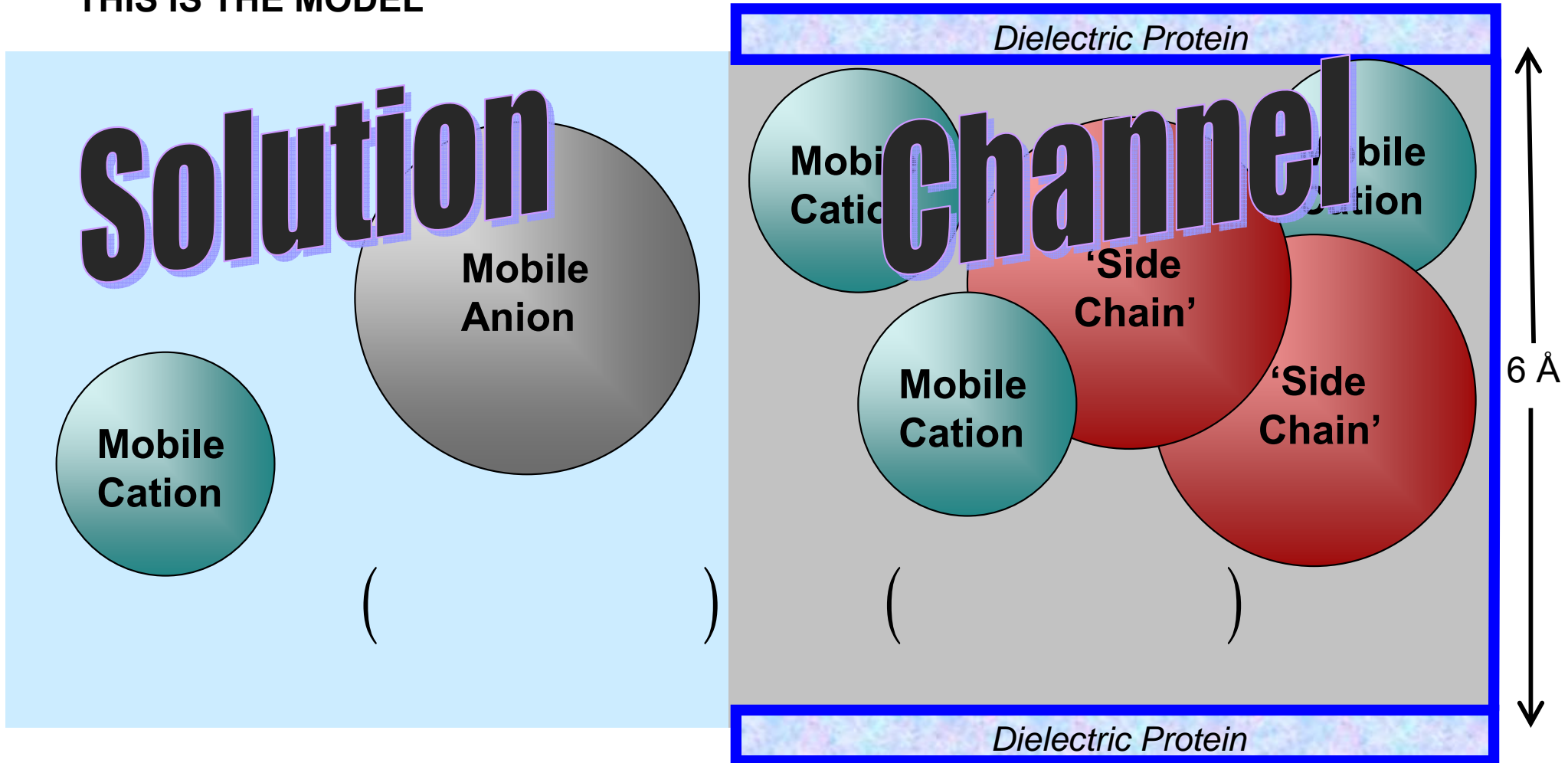
$\text{O}^{-1/2}$

Wolfgang Nonner



# ***Ion 'Binding' in Crowded Channel***

THIS IS THE MODEL



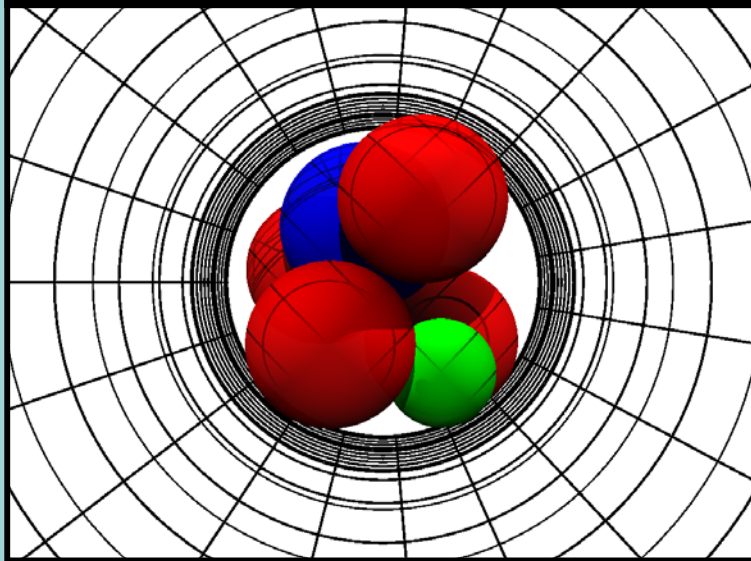
## ***Classical Donnan Equilibrium of Ion Exchanger*** *large mechanical forces*

Side chains move within channel to their equilibrium position of minimal free energy.

We compute the Tertiary Structure as the structure of minimal free energy.

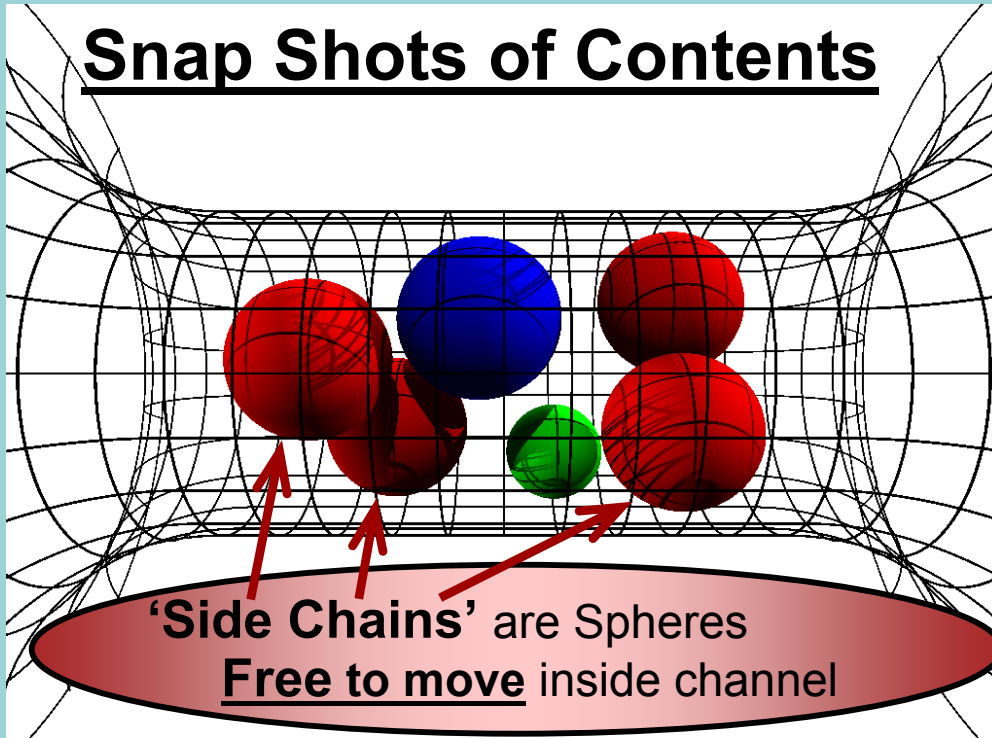
Boda, Nonner, Valisko, Henderson, Eisenberg & Gillespie

### Radial Crowding is Severe



6 Å

### Snap Shots of Contents



'Side Chains' are Spheres  
Free to move inside channel

# Crowded Ions

## *Ion Diameters*

*'Pauling' Diameters*

**Ca<sup>++</sup>**

**1.98 Å**

**Na<sup>+</sup>**

**2.00 Å**

**K<sup>+</sup>**

**2.66 Å**

## *'Side Chain' Diameter*

**Lysine K**

**3.00 Å**

**D or E**

**2.80 Å**

**Channel Diameter 6 Å**

*Parameters are Fixed in all calculations  
in all solutions for all mutants*

Experiments and Calculations done at pH 8

33

## Central Problem\*

**How does the channel control  
selectivity**

**How does the protein produce the  
phenotype?**

**\*an example of “Reverse Engineering”**

# **Most of biology is an Inverse Problem**

How does a biological device work?

How can we make it work better?

**The device equation is the mathematical  
statement of the function.**

**It is the 'slow' variable in the language  
of mathematics of complex system.**

# Inverse Problems

Badly posed,  
simultaneously over and under determined.

**Exact choice of question and data are crucial**

Inverse Problems learned from Heinz Engl and Martin Burger with thanks!

PNP inverse problem (with DFT, noise, systematic error) solved in  
Burger, Eisenberg and Engl (2007) SIAM J Applied Math 67: 960-989

# Inverse Problem for Selectivity

Badly posed,  
simultaneously over and under determined  
with noise and systematic error

**has actually been solved**

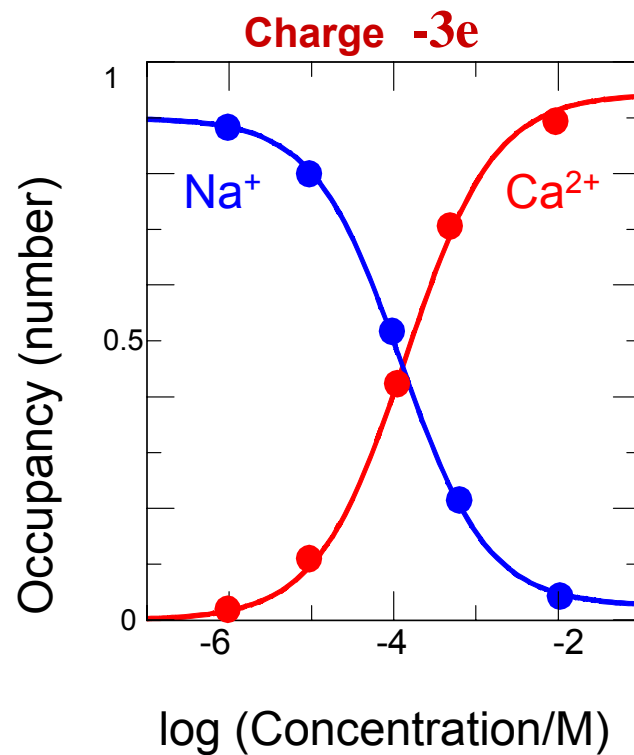
using methods for the

**Inverse Problem of a Blast Furnace.**

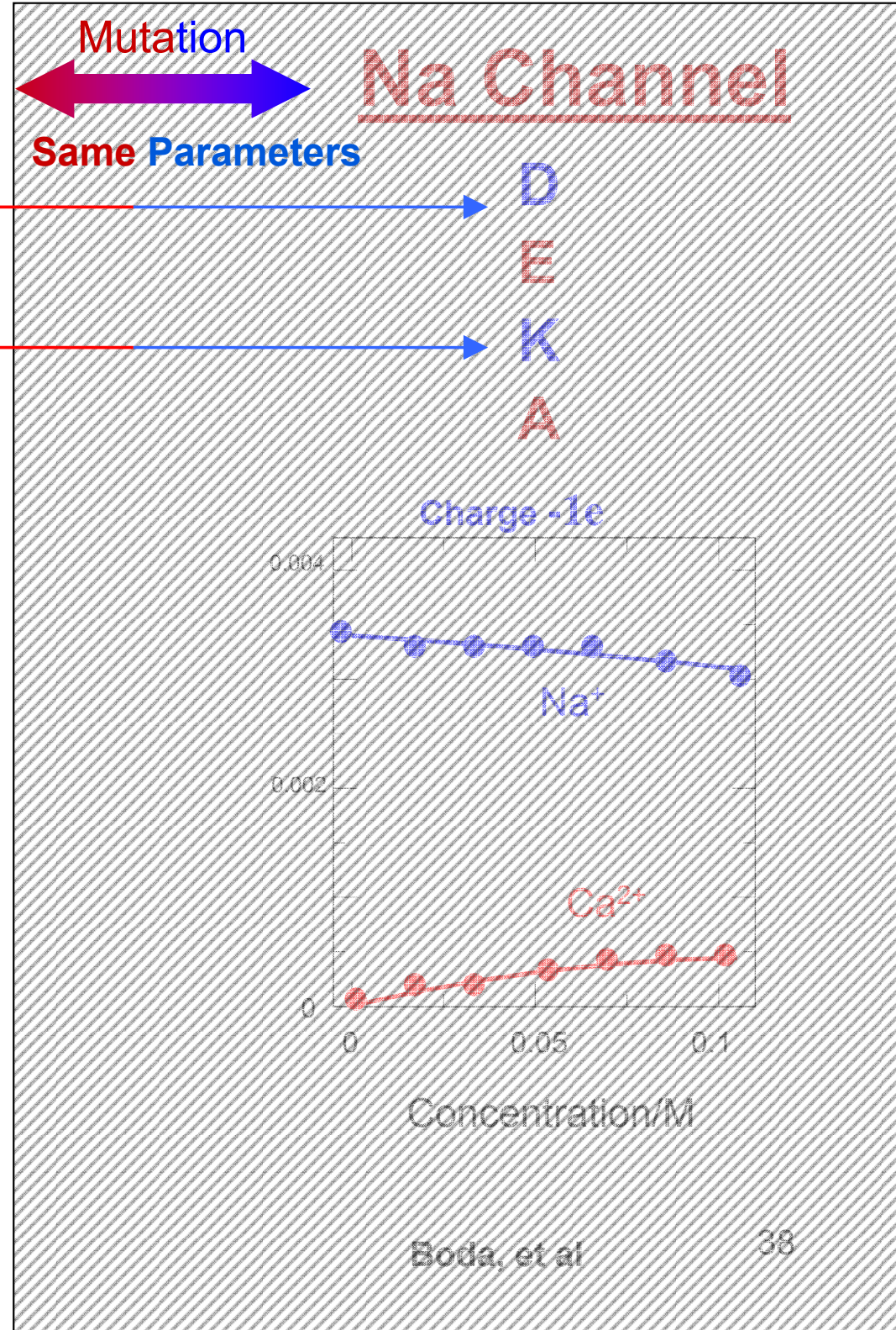
Burger, Eisenberg and Engl (2007) SIAM J Applied Math 67: 960-989

# Ca Channel

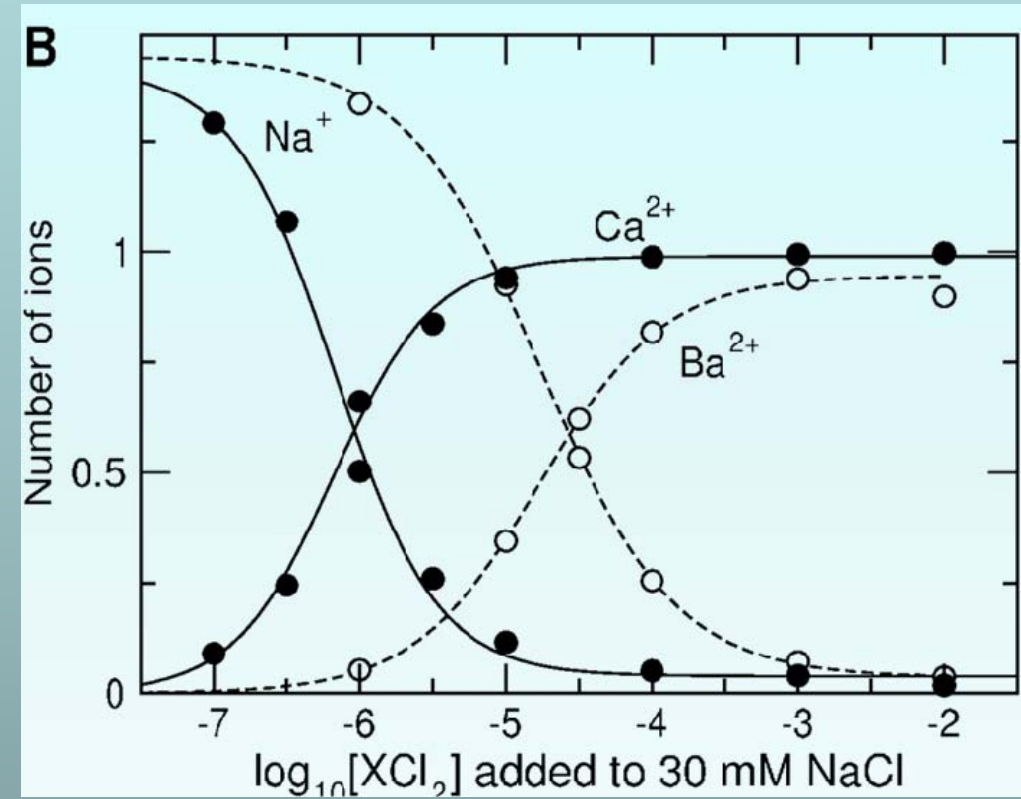
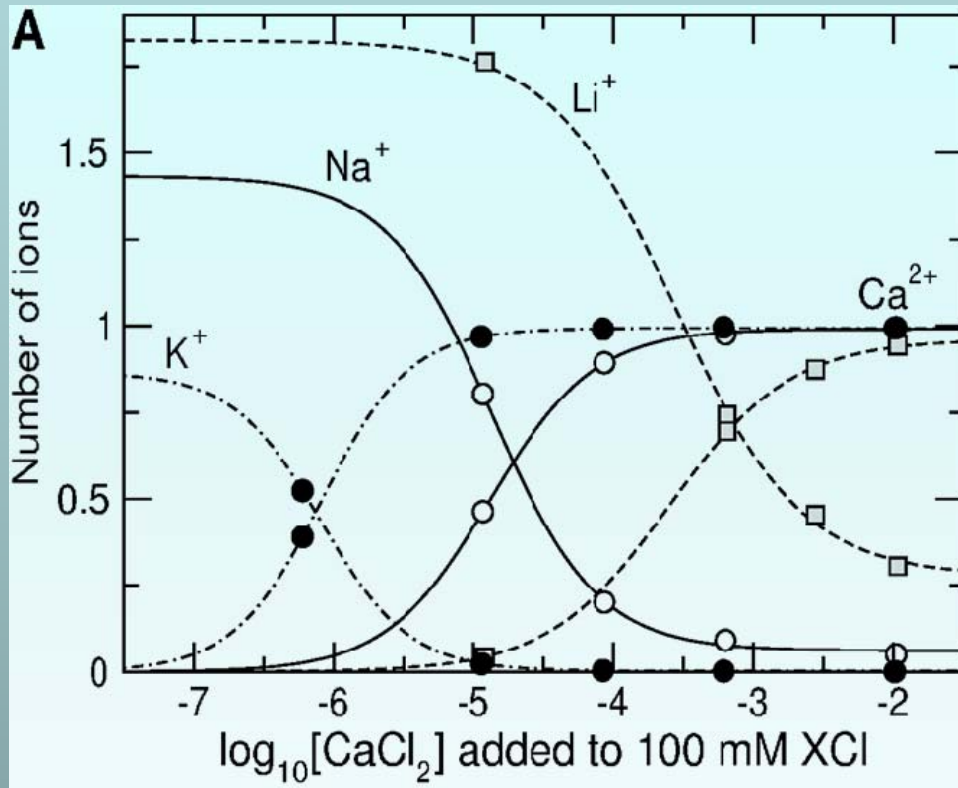
E  
E  
E  
A



EEEE has full biological selectivity  
in similar simulations



# Na, K, Li, Ca, Ba Binding in Calcium Channel



# ***Calcium Channel***

***has been examined in ~35 papers, e.g.,***

- Nonner, W., D. P. Chen, and B. Eisenberg. 1998. Anomalous Mole Fraction Effect, Electrostatics, and Binding in Ionic Channels. *Biophysical Journal* 74:2327-2334.
- Nonner, W., L. Catacuzzeno, and B. Eisenberg. 2000. Binding and Selectivity in L-type Ca Channels: a Mean Spherical Approximation. *Biophysical Journal* 79:1976-1992.
- Nonner, W., D. Gillespie, D. Henderson, and B. Eisenberg. 2001. Ion accumulation in a biological calcium channel: effects of solvent and confining pressure. *J Physical Chemistry B* 105:6427-6436.
- Boda, D., W. Nonner, D. Henderson, B. Eisenberg, and D. Gillespie. 2008. Volume exclusion in calcium selective channels. *Biophys. J.:biophysj*.107.122796.
- Boda, D., M. Valisko, B. Eisenberg, W. Nonner, D. Henderson, and D. Gillespie. 2006. Effect of Protein Dielectric Coefficient on the Ionic Selectivity of a Calcium Channel. *Journal of Chemical Physics* 125:034901.
- Boda, D., T. Varga, D. Henderson, D. Busath, W. Nonner, D. Gillespie, and B. Eisenberg. 2004. Monte Carlo simulation study of a system with a dielectric boundary: application to calcium channel selectivity. *Molecular Simulation* 30:89-96.
- Boda, D., M. Valisko, B. Eisenberg, W. Nonner, D. Henderson, and D. Gillespie. 2007. The combined effect of pore radius and protein dielectric coefficient on the selectivity of a calcium channel. *Physical Review Letters* 98:168102.

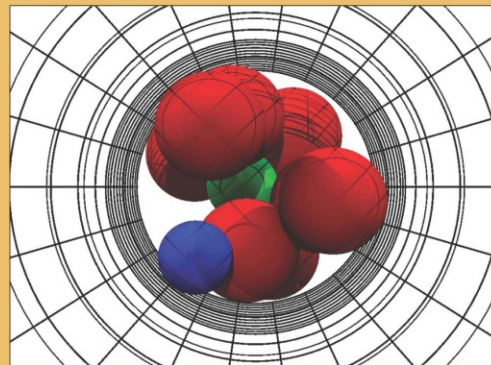
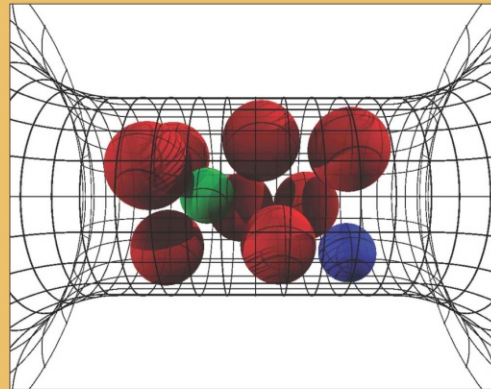
**Most of the papers are available at**  
**<http://www2.phys.rush.edu/RSEisenberg/physioeis.html>**

# ***Calcium Channel***

Summary Simulation Paper (and target for new experiments!) in Experimental Journal

# JGP

The Journal of General Physiology  
Vol 133 • No 5 • May 2009



[www.jgp.org](http://www.jgp.org)

**Next, the Sodium Channel**

# Next, the Sodium Channel

specifically, the

## DEKA Sodium Channel 6 Å

Aspartate  
Glutamate  
Lysine  
Alanine

D  
E  
K  
A

Acid  
Acid  
Basic  
Aliphatic

Negative  
Negative  
Positive  
Neutral

# DEKA Sodium Channel

has very different properties from Ca channel,

e.g., 'binding' curve,  
Na<sup>+</sup> vs Ca<sup>++</sup> selectivity  
Na<sup>+</sup> vs K<sup>+</sup> selectivity

# Challenge

from leading biophysicists

**Walter Stühmer** and **Stefan Heinemann**

Max Planck Institutes, Göttingen, Leipzig

**Can a physical theory explain the mutation  
DEEA into DEKA?**

# Ca Channel

E  
E  
E  
A

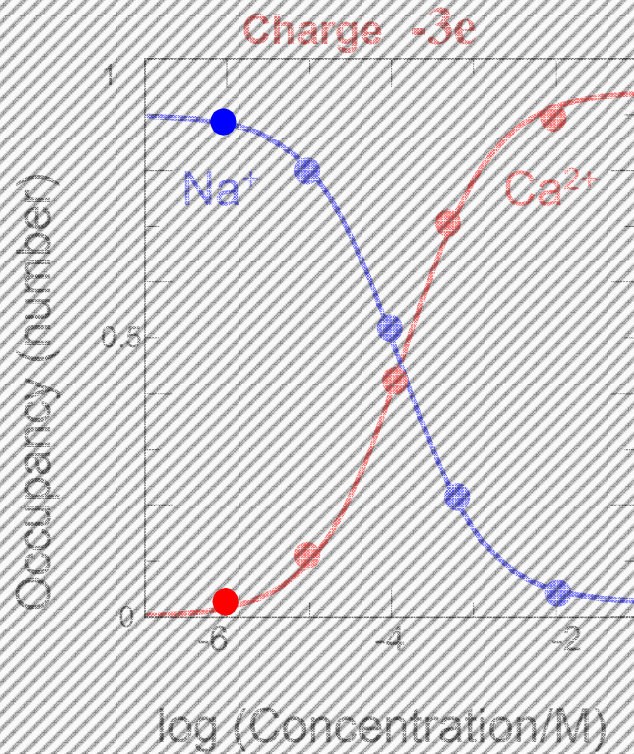
Mutation



Same Parameters

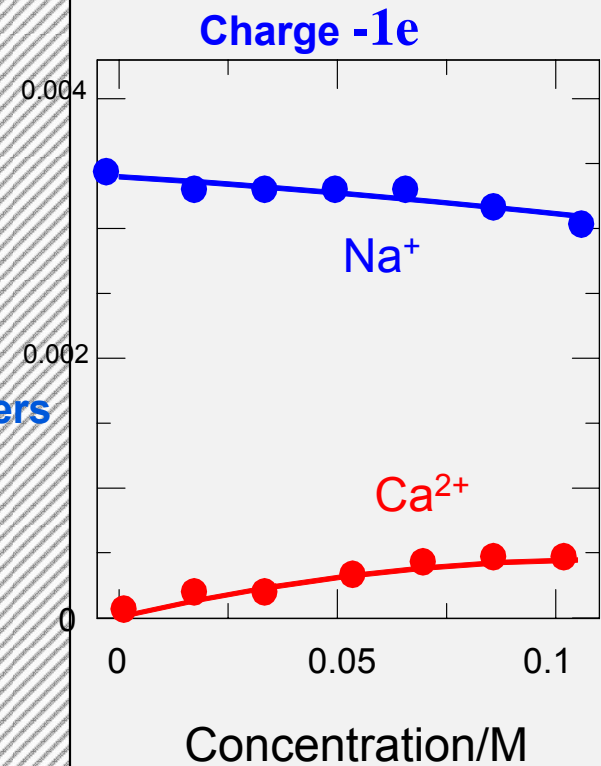
# Na Channel

D  
E  
K  
A



Mutation

Same Parameters



**EEEE** has full biological selectivity  
in similar simulations

Boda, et al

**Nothing was changed**  
*from the*  
*EEEE Ca channel*  
*except the amino acids*

Calculated DEKA Na Channel  
Selects  
 $\text{Ca}^{2+}$  vs.  $\text{Na}^{+}$  and also  $\text{Na}^{+}$  vs.  $\text{K}^{+}$

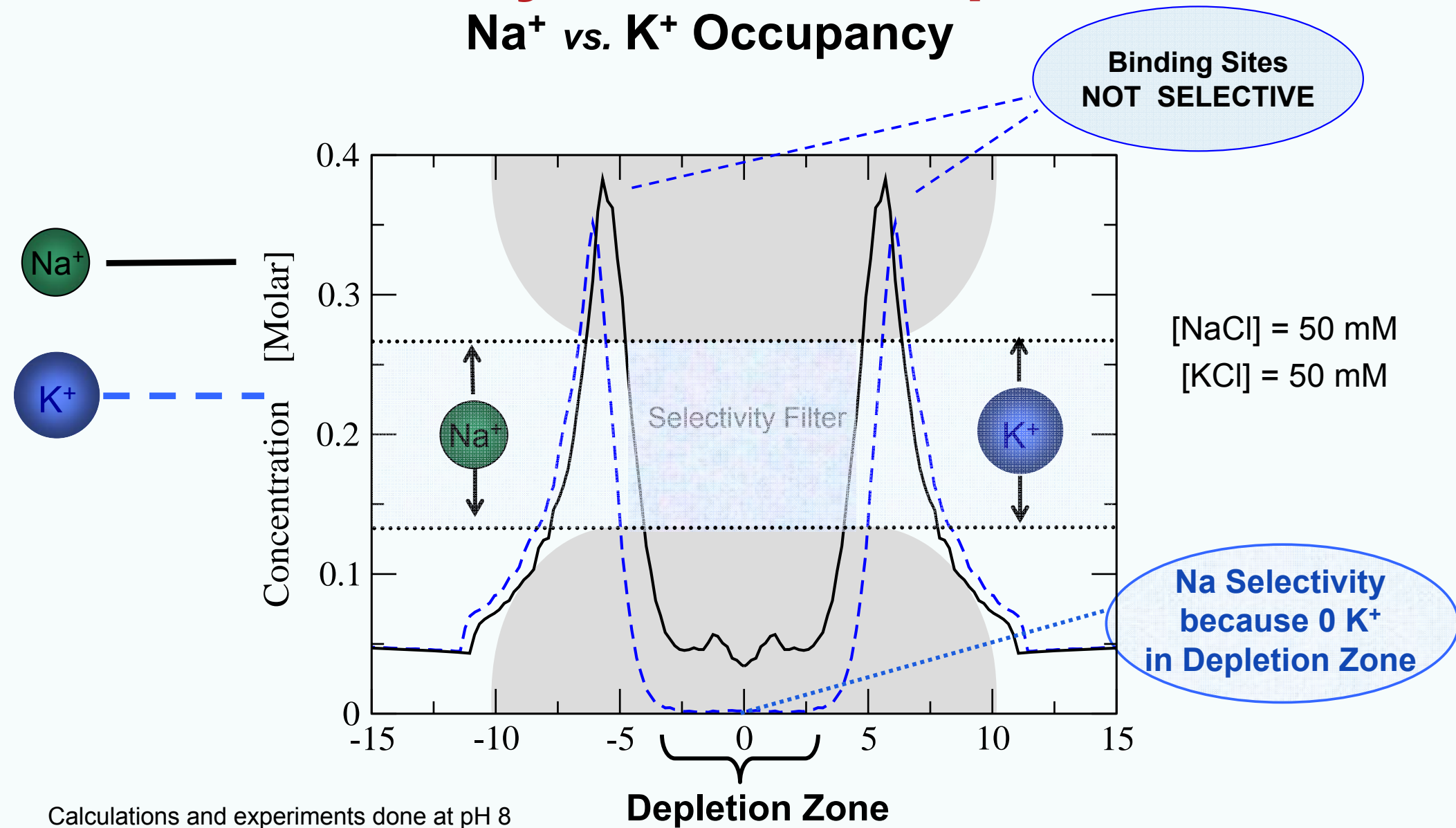
# How?

Does the DEKA Na Channel Select  $\text{Na}^+$  vs.  $\text{K}^+$  ?

**Inverse Problem**  
**“Reverse Engineering”**

# Size Selectivity is in the Depletion Zone

## Na<sup>+</sup> vs. K<sup>+</sup> Occupancy



Calculations and experiments done at pH 8

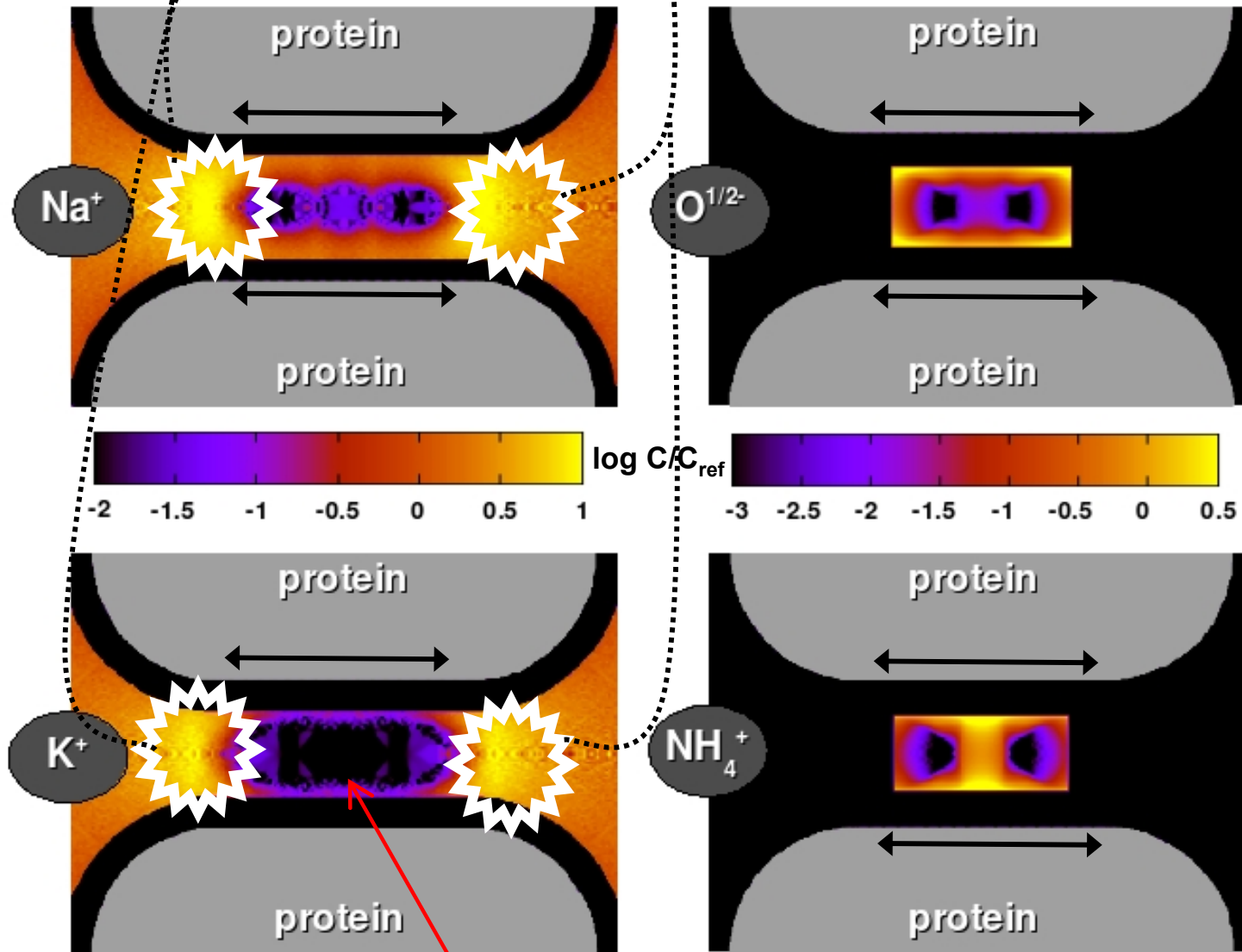
of the **DEKA** Na Channel, 6 Å

**Boda, et al**

# Size Selectivity

## Binding Sites

NOT selective



\*Binding Sites are outputs of our INDUCED FIT

Model of Selectivity, *not* structural inputs

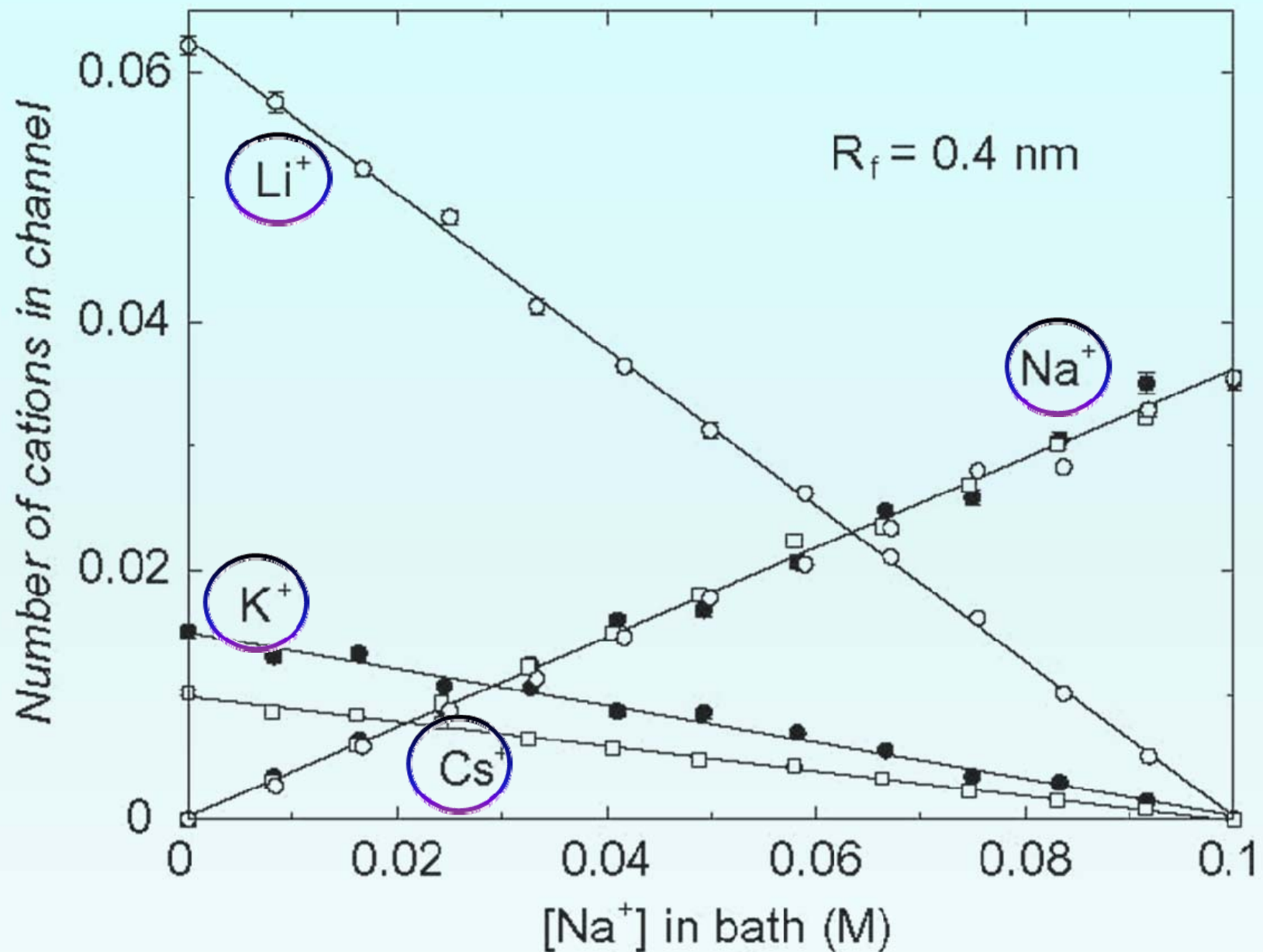
[NaCl] = [KCl] = 50 mM

Ion Diameter	
Ca <sup>++</sup>	1.98 Å
Na <sup>+</sup>	2.00 Å
K <sup>+</sup>	2.66 Å
'Side Chain' Diameter	
NH <sub>4</sub> <sup>+</sup> Lys or K	3.00 Å
O <sup>1/2-</sup> D or E	2.80 Å
Na Channel DEKA 6 Å	

Na vs K Size Selectivity is in  
Depletion Zone

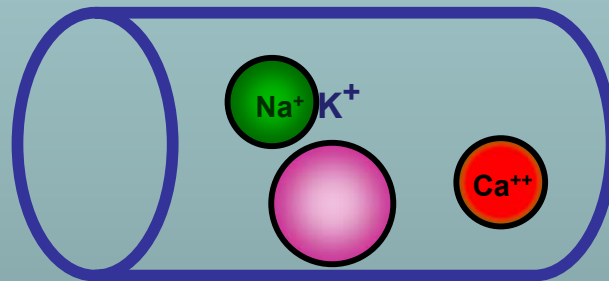
BLACK = Depletion=0

# Na, K, Li, Cs Binding in Sodium channel



# Control Variables

are obvious in simulations of the Na channel,  
but not of the Ca channel\*



# **Control Variables**

in DEKA Na channel

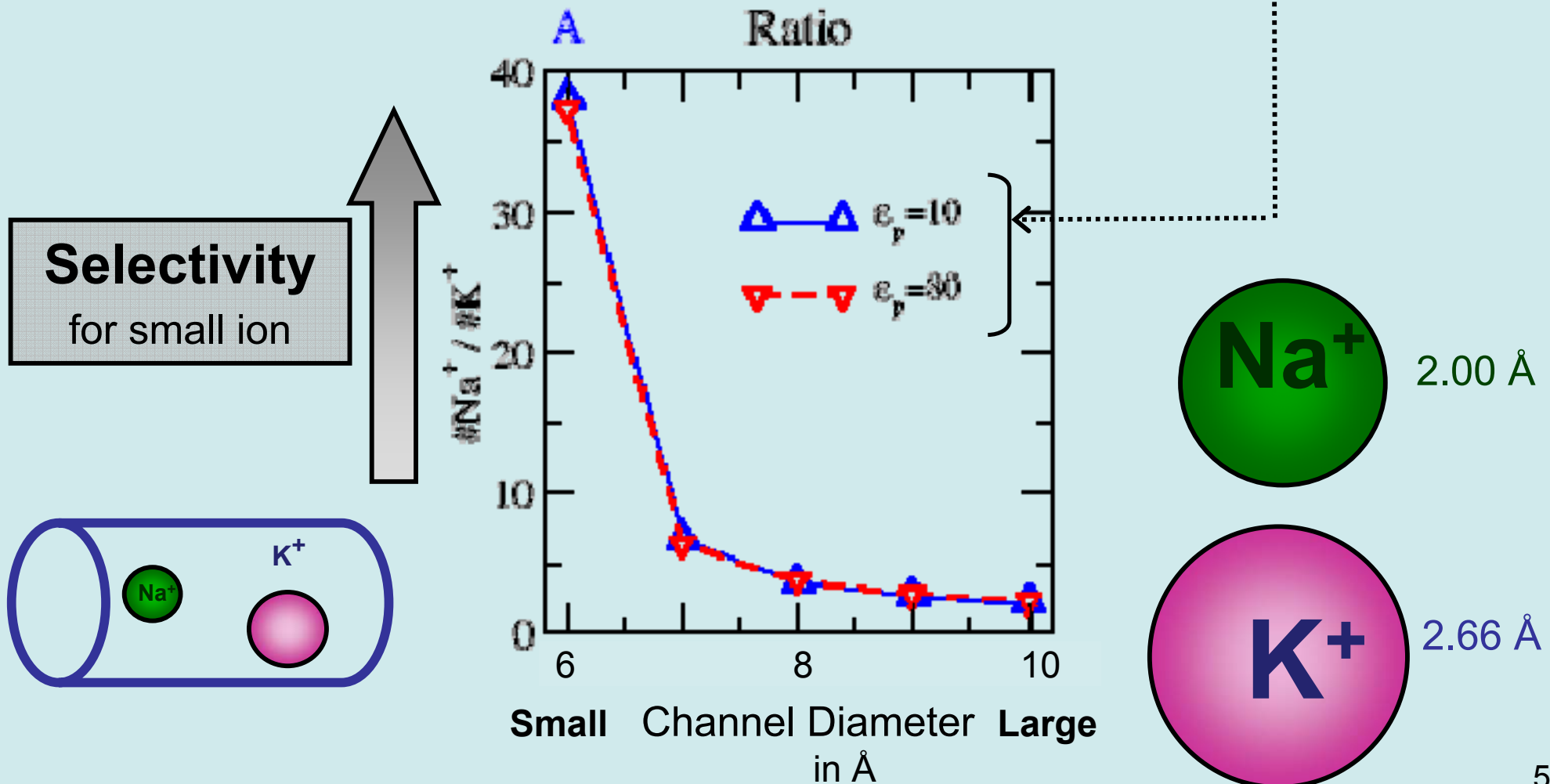
**Selectivity  $Na^+$  vs  $K^+$**   
depends only on channel diameter

**Channel Diameter**  
controls  
**Selectivity**

# $\text{Na}^+$ vs $\text{K}^+$ (size) **Selectivity** (*ratio*)

## **Depends on Channel Size,**

*not* Protein Dielectric Coefficient\*



Boda, et al

\*in DEKA Na Channel

# Control Variables

in DEKA Na channel

- Selectivity  $Na^+$  vs  $K^+$   
depends only on pore diameter
- Conductance\* depends on protein polarization

Protein Dielectric Coefficient  
controls  
Conductance

\* Gillespie & Boda (2008) Biophysical Journal 95:2658

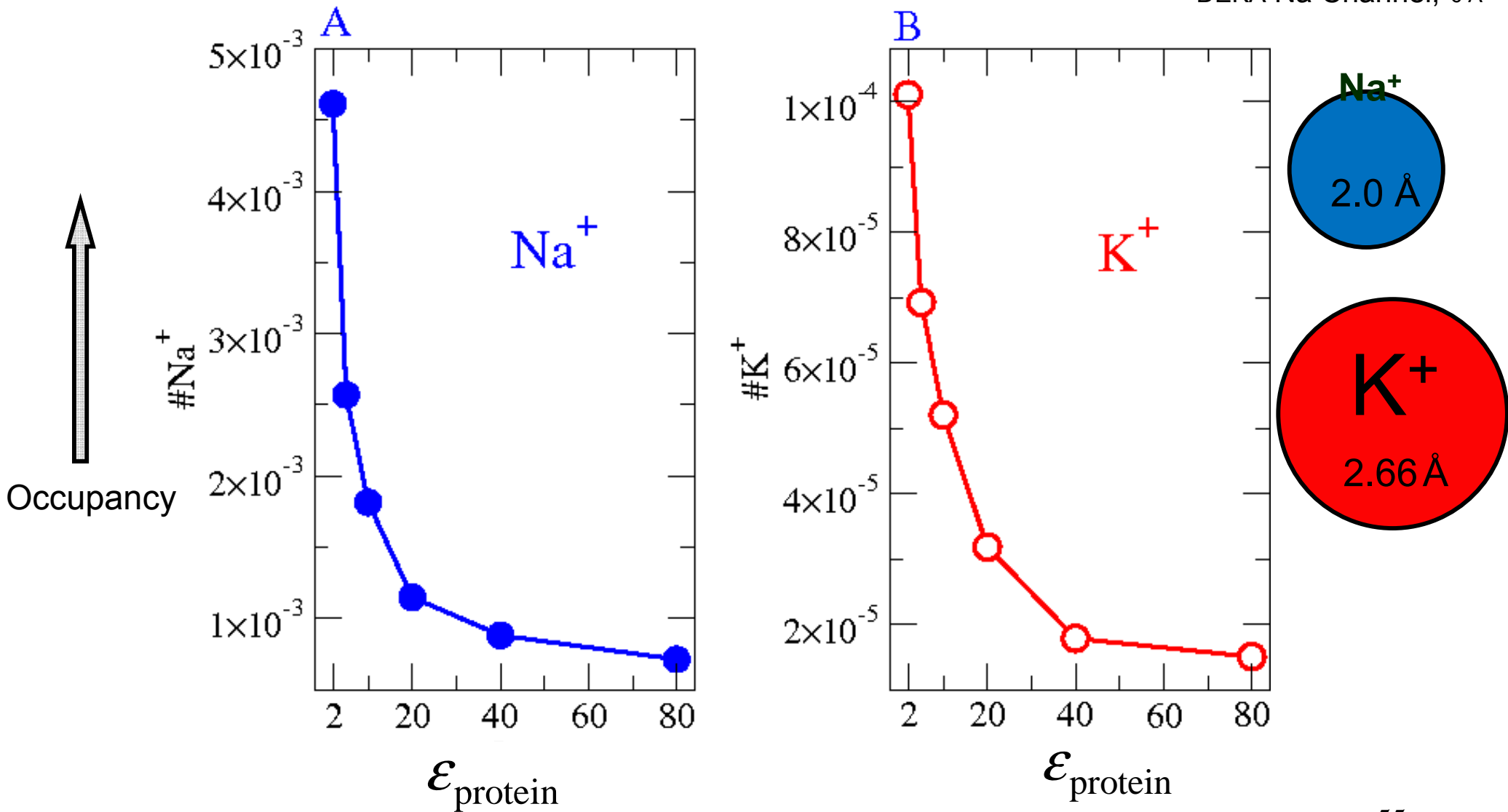
Control Variable

# Occupancy

depends on

## Protein Dielectric

DEKA Na Channel, 6 Å



# Selectivity

comes from

**Electrostatic Interaction**

and

**Steric Competition for Space**



Repulsion

Location and Strength of Binding Sites  
Depend on Ionic Concentration and  
Temperature, etc

***Rate Constants are Variables***

# What does the protein do?

Channel and Contents  
form a

**Self-Organized Structure**

with Side Chains at position of  
Minimum Free Energy

Protein Fits the Substrate

**“Induced Fit Model of Selectivity”**

# What does the protein do?

Certain **MEASURES** of structure are  
Powerful **DETERMINANTS** of Function  
e.g., Volume, Dielectric Coefficient, etc.

Induced Fit Model of Selectivity

Atomic Structure is not pre-formed

Atomic Structure is an important output of the simulation

# What does the protein do?

Protein maintains

Mechanical Forces\*

Volume of Pore

Dielectric Coefficient/Boundary

Permanent Charge

*\* Driving force for conformation changes ??*

Binding Sites\* are **outputs**  
of our Calculations

## **Induced Fit Model of Selectivity**

**Our model has no preformed  
structural binding sites  
but**

**Selectivity is very Specific**

\*Selectivity is in the Depletion Zone,  
NOT IN THE BINDING SITE  
of the DEKA Na Channel

# Specificity

“There is only one word that matters in biology  
and that is specificity.

**The truth is in the details,  
not the broad sweeps.”\***

The detail can be computed  
from the correct broadly applicable physics  
*sometimes*<sup>†</sup>

<sup>†</sup>Bob Eisenberg’s opinion

\*Aaron Klug *quoted in the first sentence of Pearson Nature (2008) 455:160–164*

# Miracle

**We can actually compute the  
Structures that determine Selectivity**

# **Working Hypothesis**

**Selectivity Filter Works because**

it is a

**Self-Organized Structure**

with Side Chains at position of  
Minimum Free Energy

**Protein Fits the Substrate**

*“Induced Fit Model of Selectivity”*

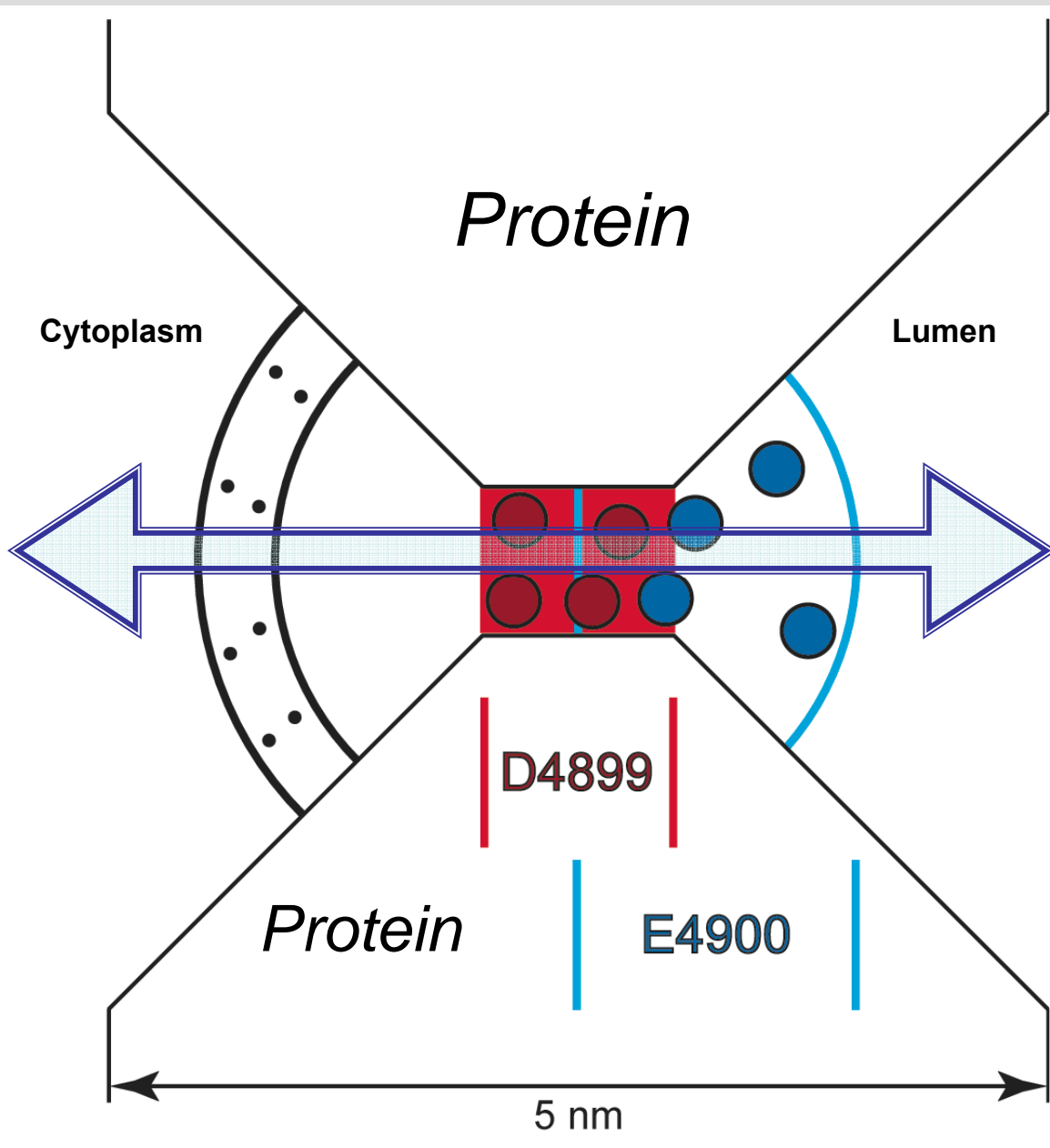


*Best Evidence is from the*  
***RyR Receptor***

**Gillespie, Meissner, Le Xu, et al,**  
*not Bob Eisenberg*

- **More than 120 combinations of solutions & mutants**
- **7 mutants with significant effects fit successfully**

# The Geometry



## **Selectivity Filter**

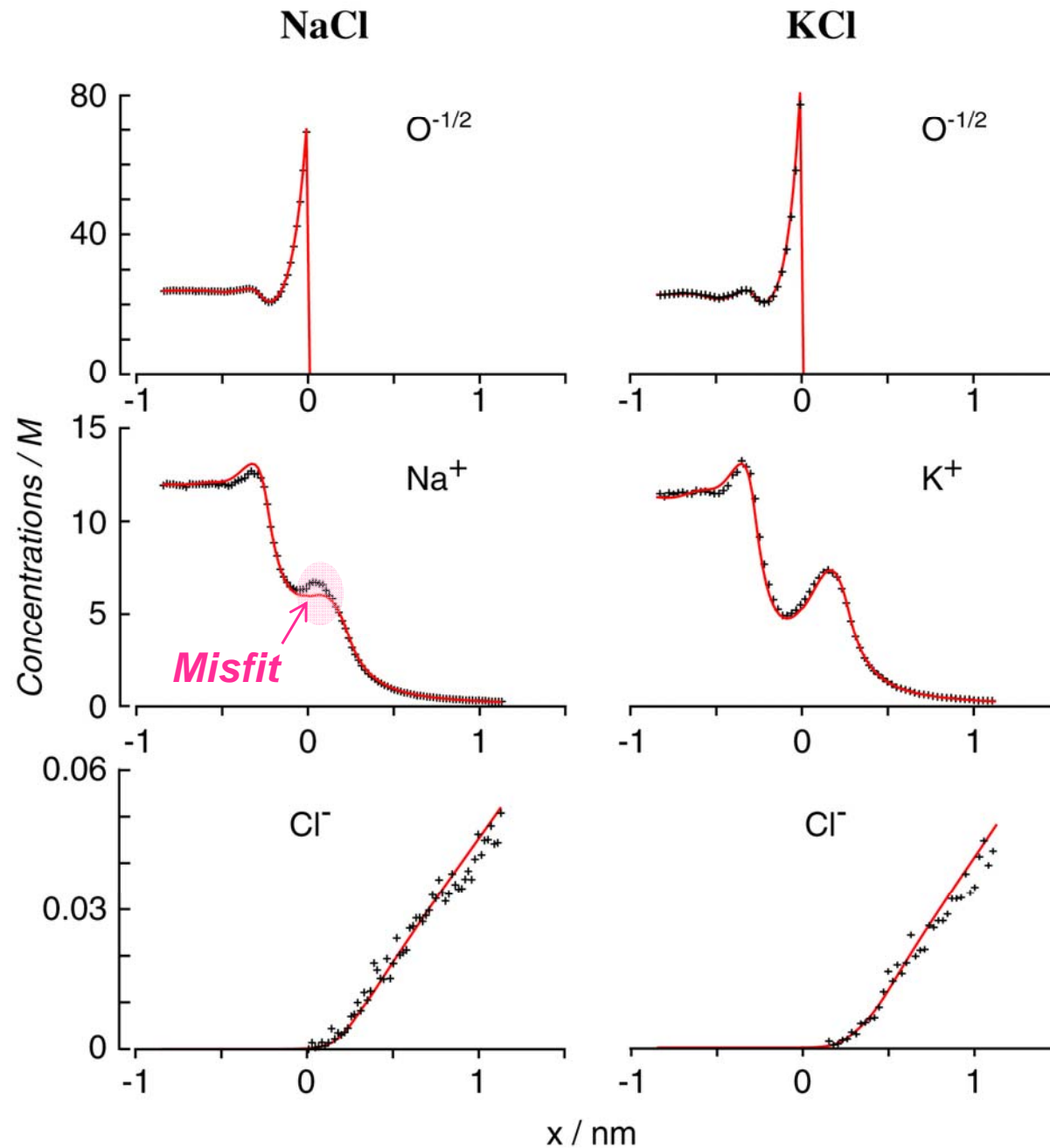
- is 10 Å long and 8 Å in diameter
- confines four **D4899** negative amino acids.

Four **E4900** positive amino acids are on lumenal side, overlapping D4899.

**Cytosolic distributed charge**

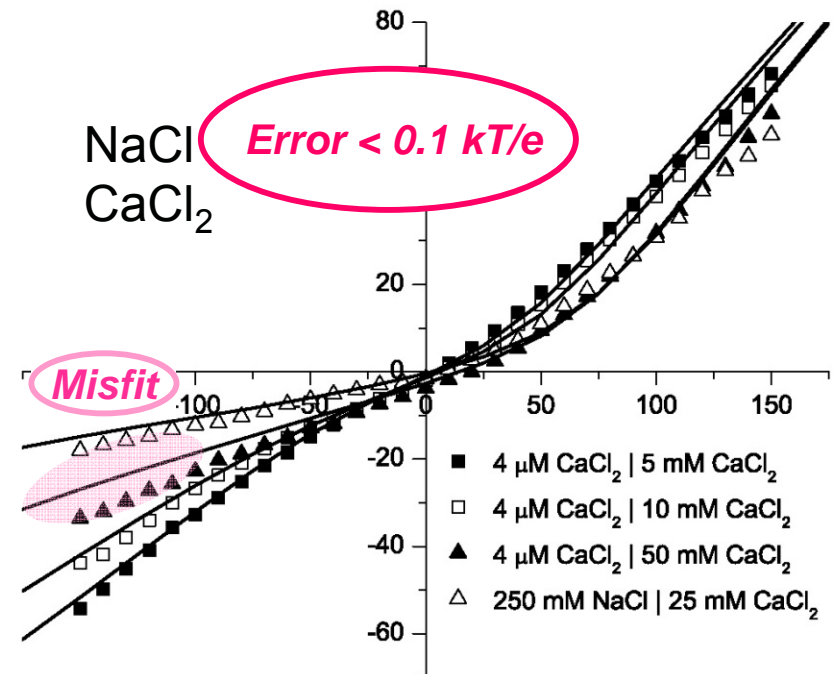
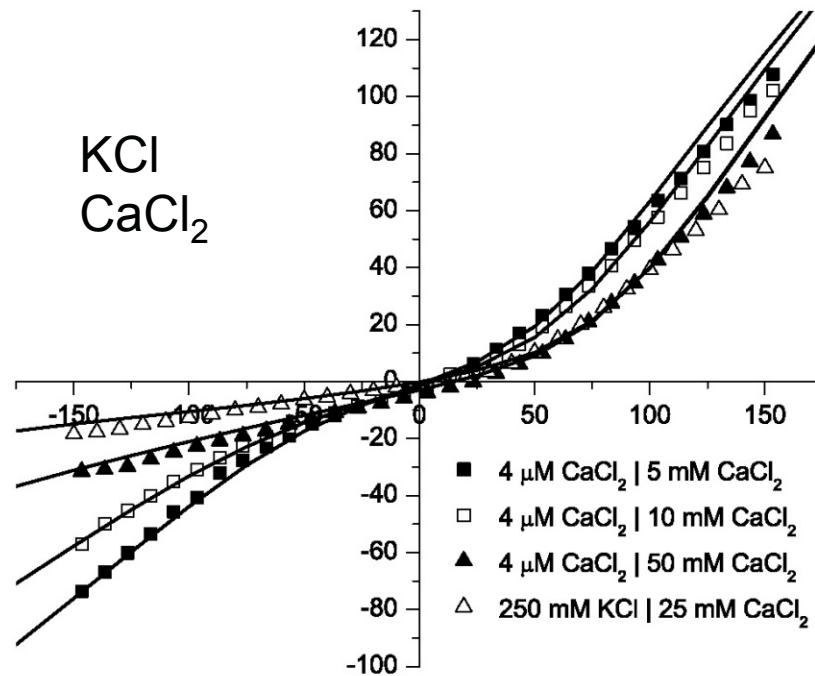
# DFT/PNP vs Monte Carlo Simulations

## Concentration Profiles

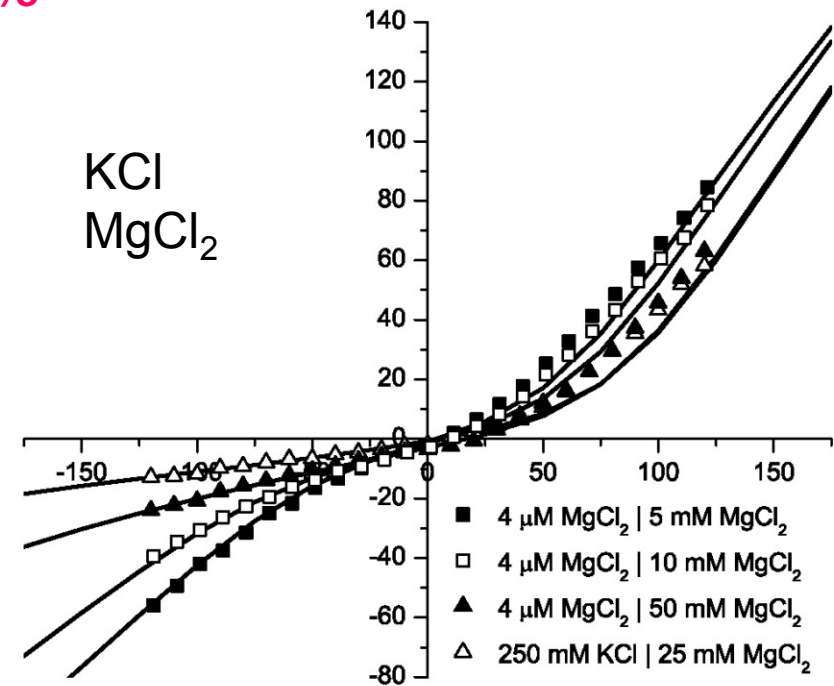
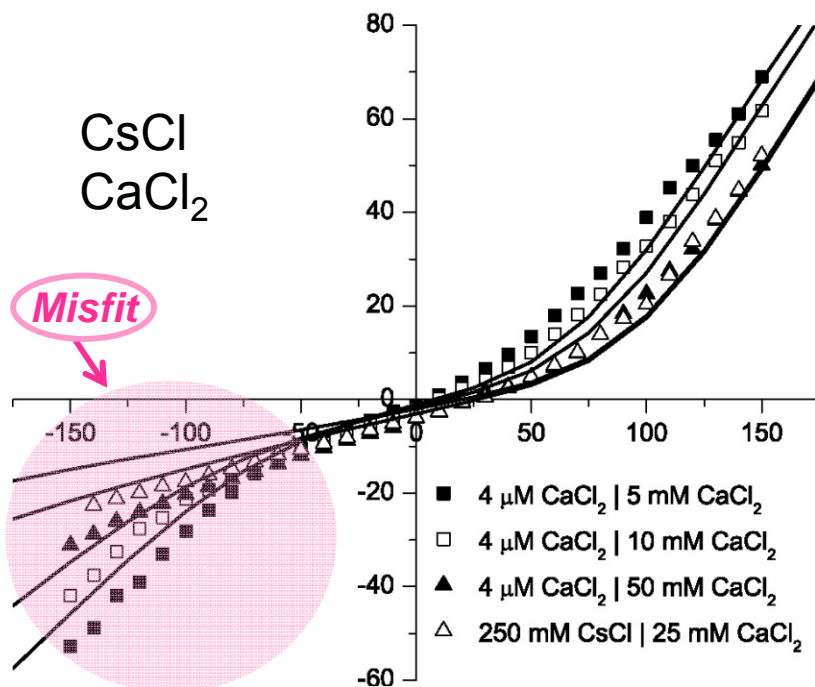


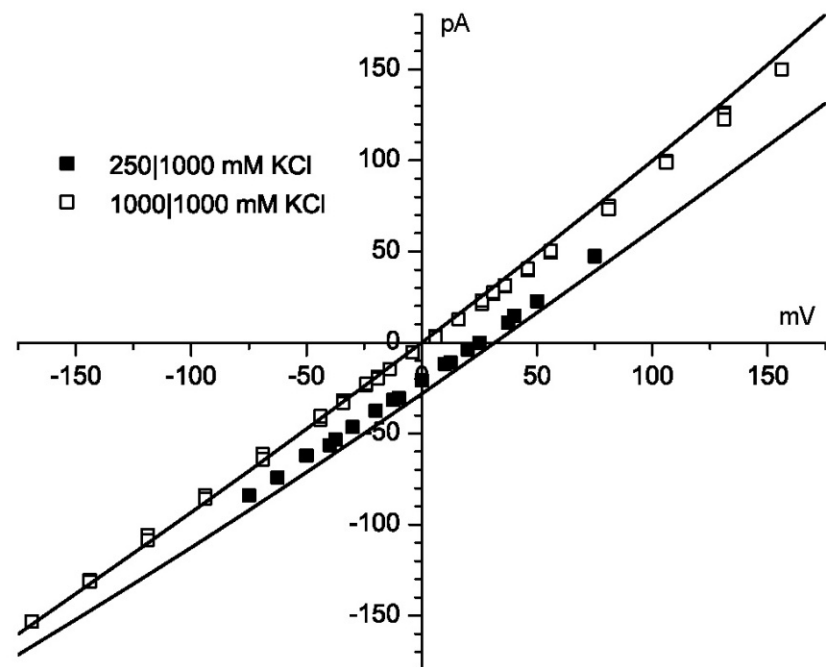
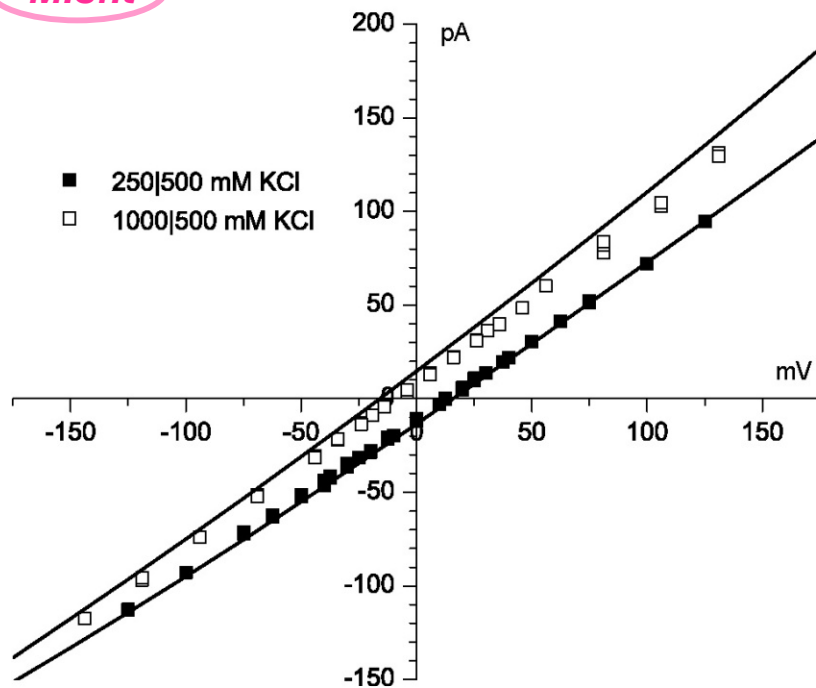
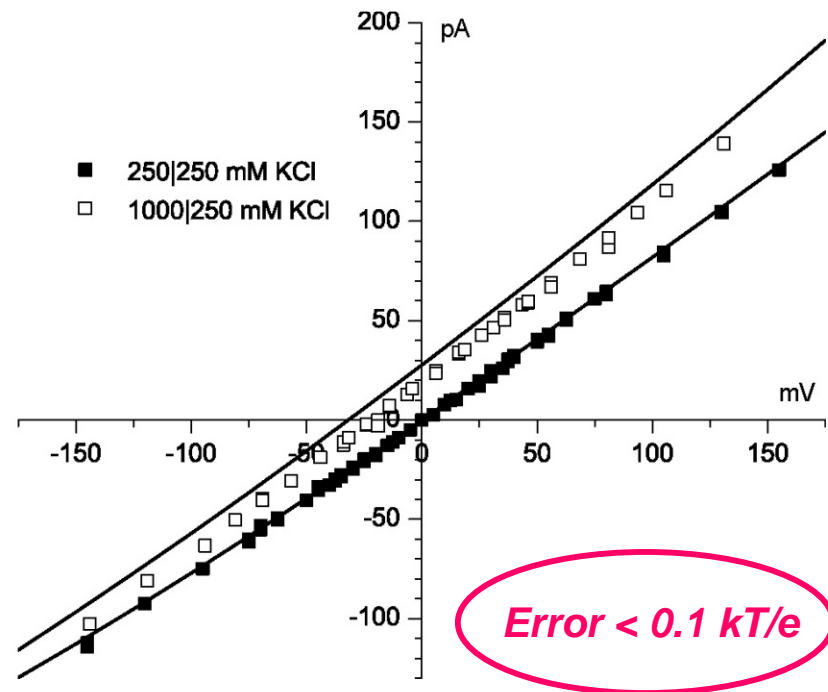
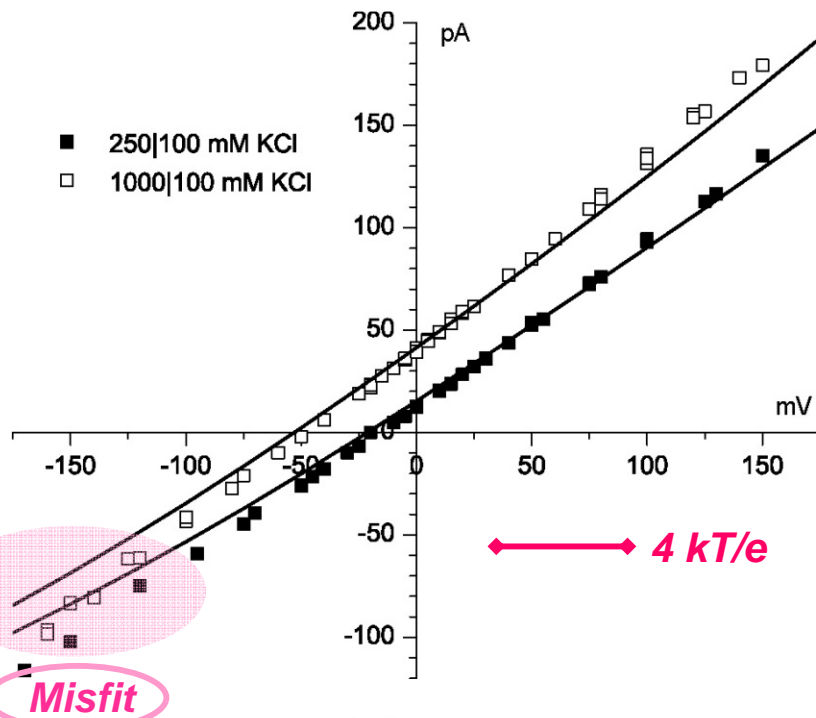
# Divalents

Gillespie, Meissner, Le Xu, et al



2 kT/e

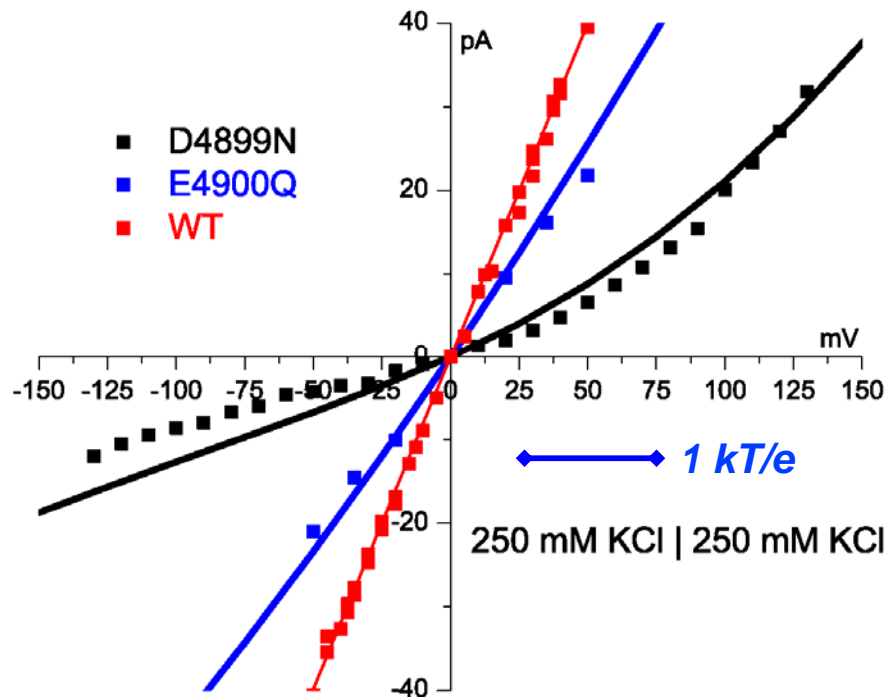




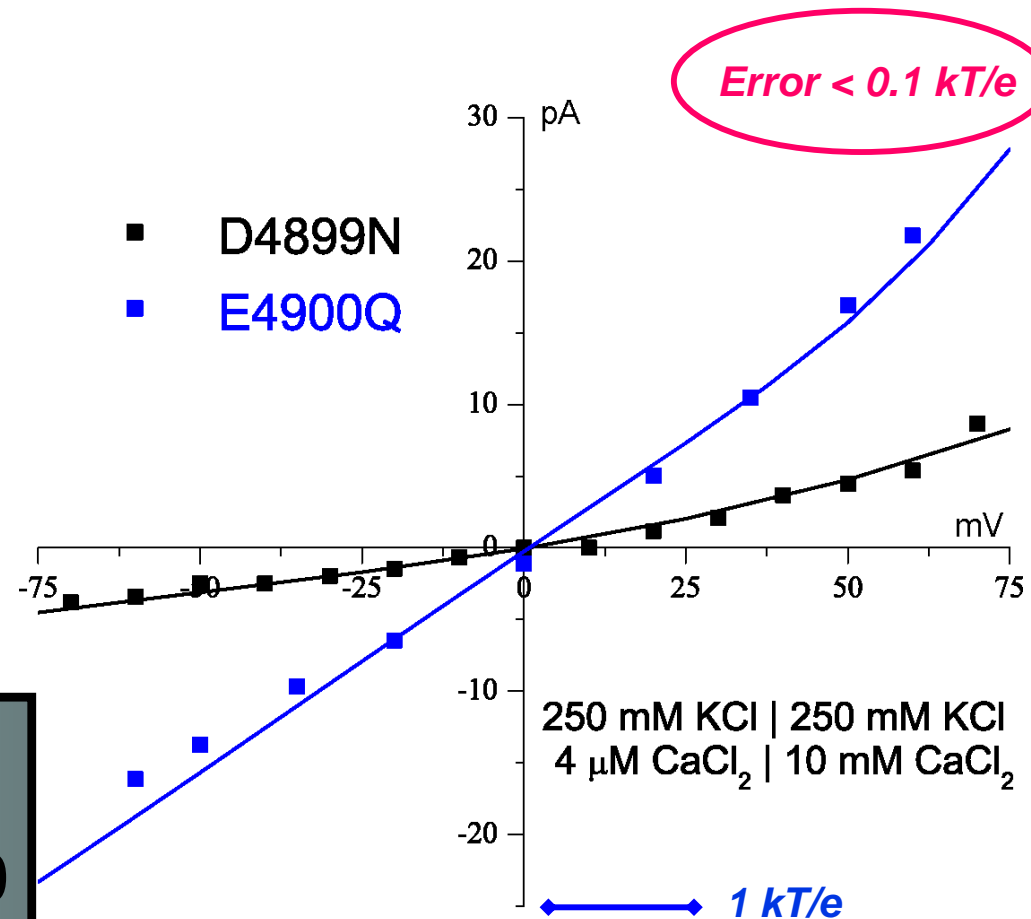
# Theory fits Mutation with Zero Charge

*No parameters adjusted*

## Theory Fits Mutant in K



## Theory Fits Mutant in K + Ca



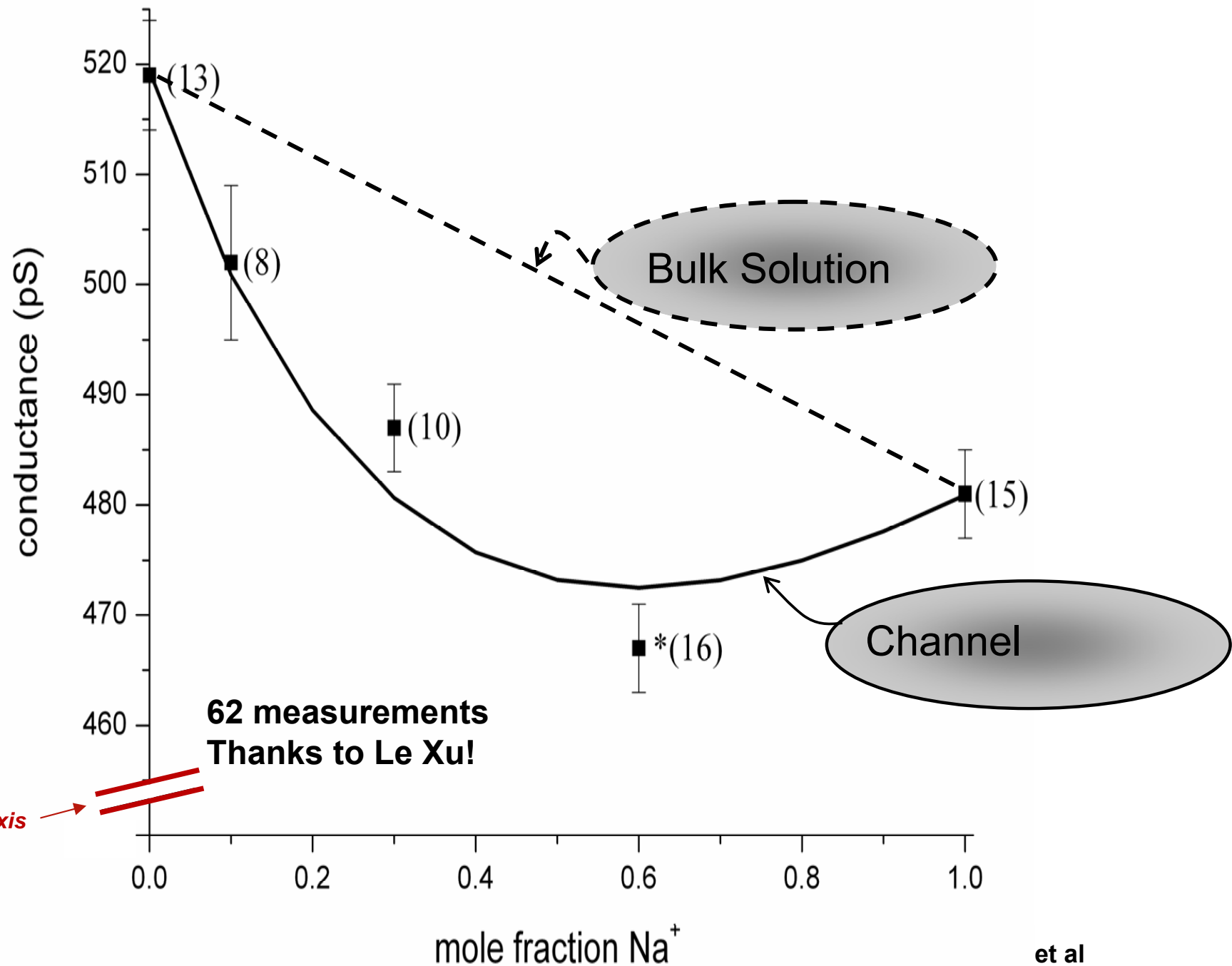
**Protein charge density**  
wild type\*  $13 \text{ M} \Rightarrow 0 \text{ M}$  in D4899

Water is 55 M

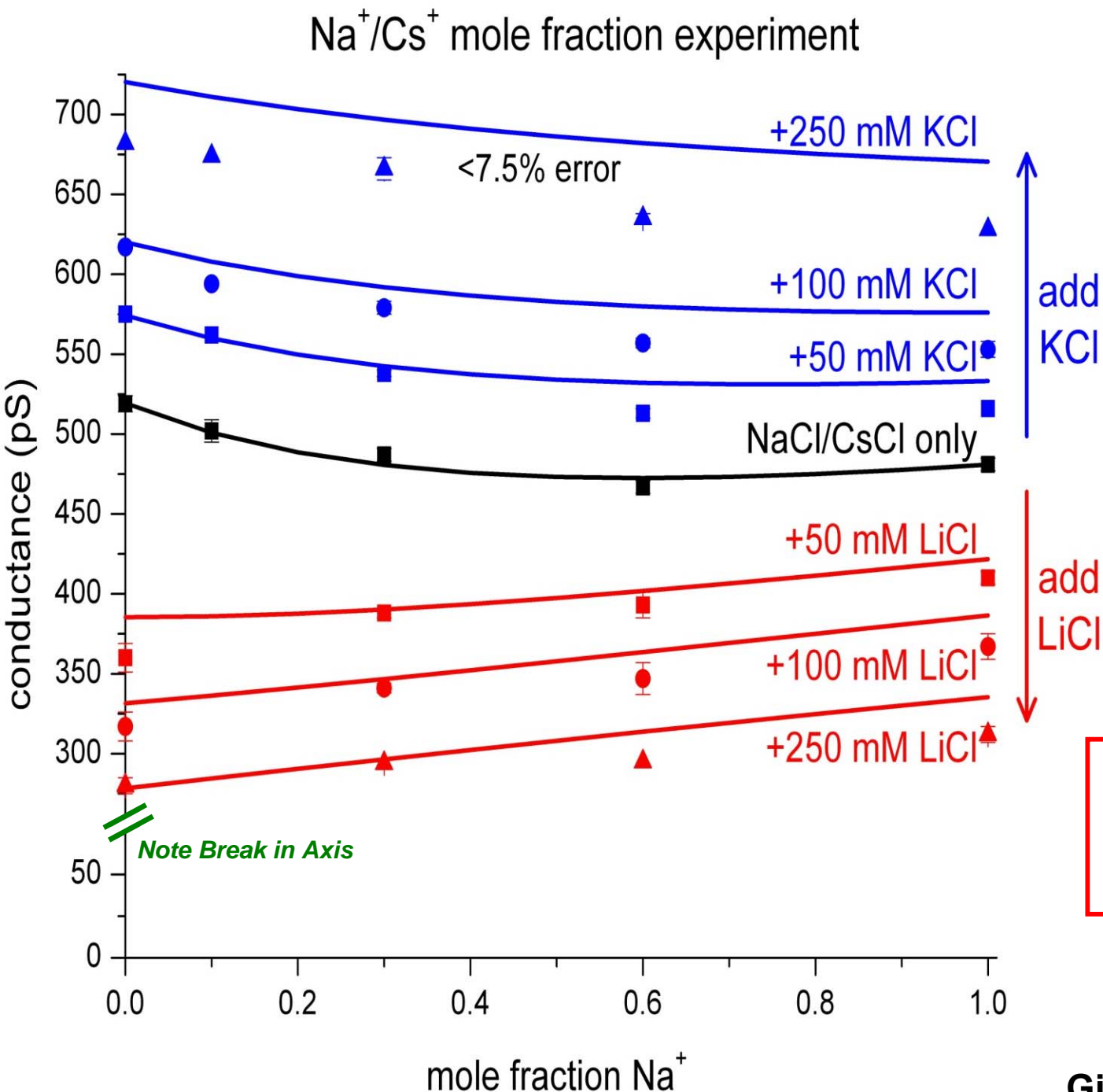
\*some wild type curves not shown, 'off the graph'

Gillespie *et al*  
*J Phys Chem* 109 15598 (2005)

# Model predicted an AMFE for $\text{Na}^+/\text{Cs}^+$ mixtures before it had been measured



# The model predicted that AMFE disappears



The Na<sup>+</sup>/Cs<sup>+</sup> mole fraction experiment is repeated with varying amounts of KCl and LiCl present in addition to the NaCl and CsCl. The model predicted that the AMFE disappears when other cations are present. This was later confirmed by experiment.

**Prediction made without any adjustable parameters.**

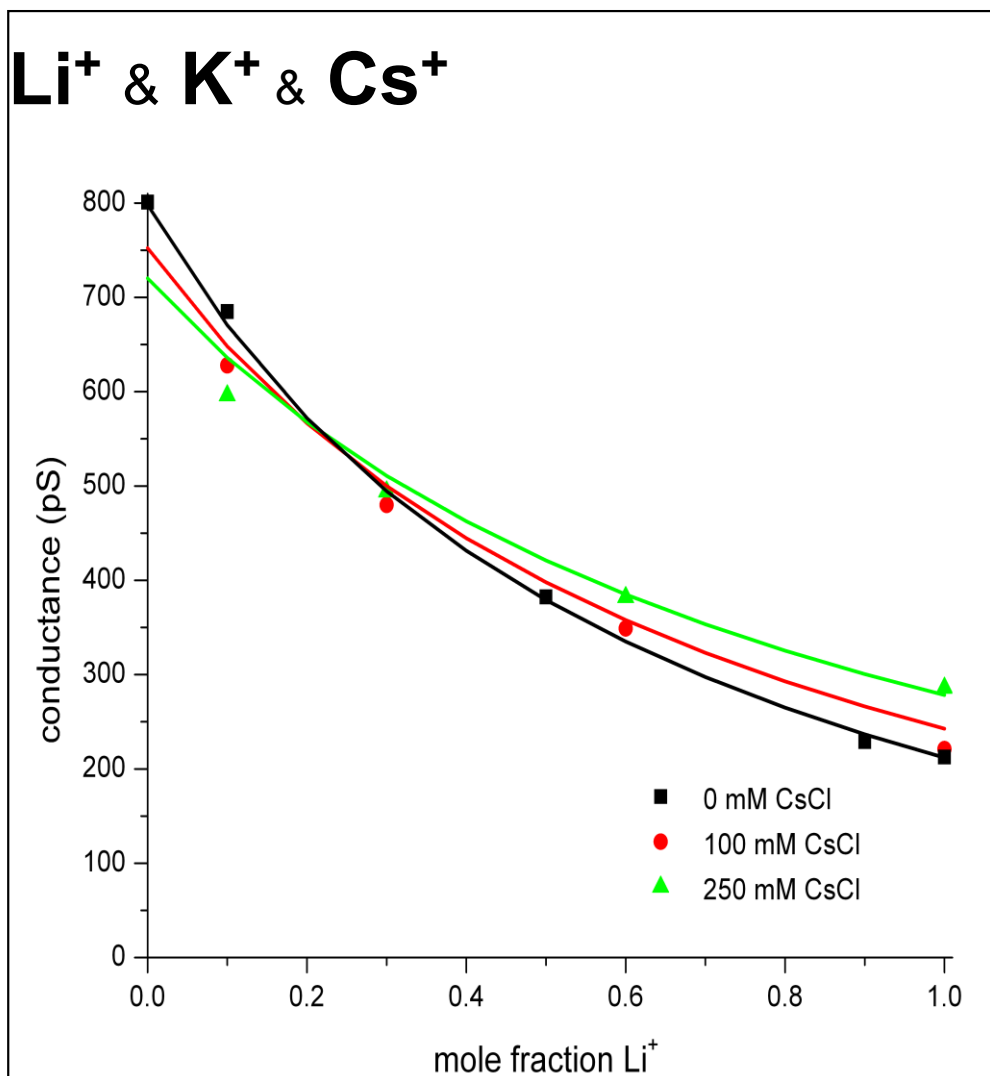
*Error < 0.1 kT/e*

# Mixtures of THREE Ions

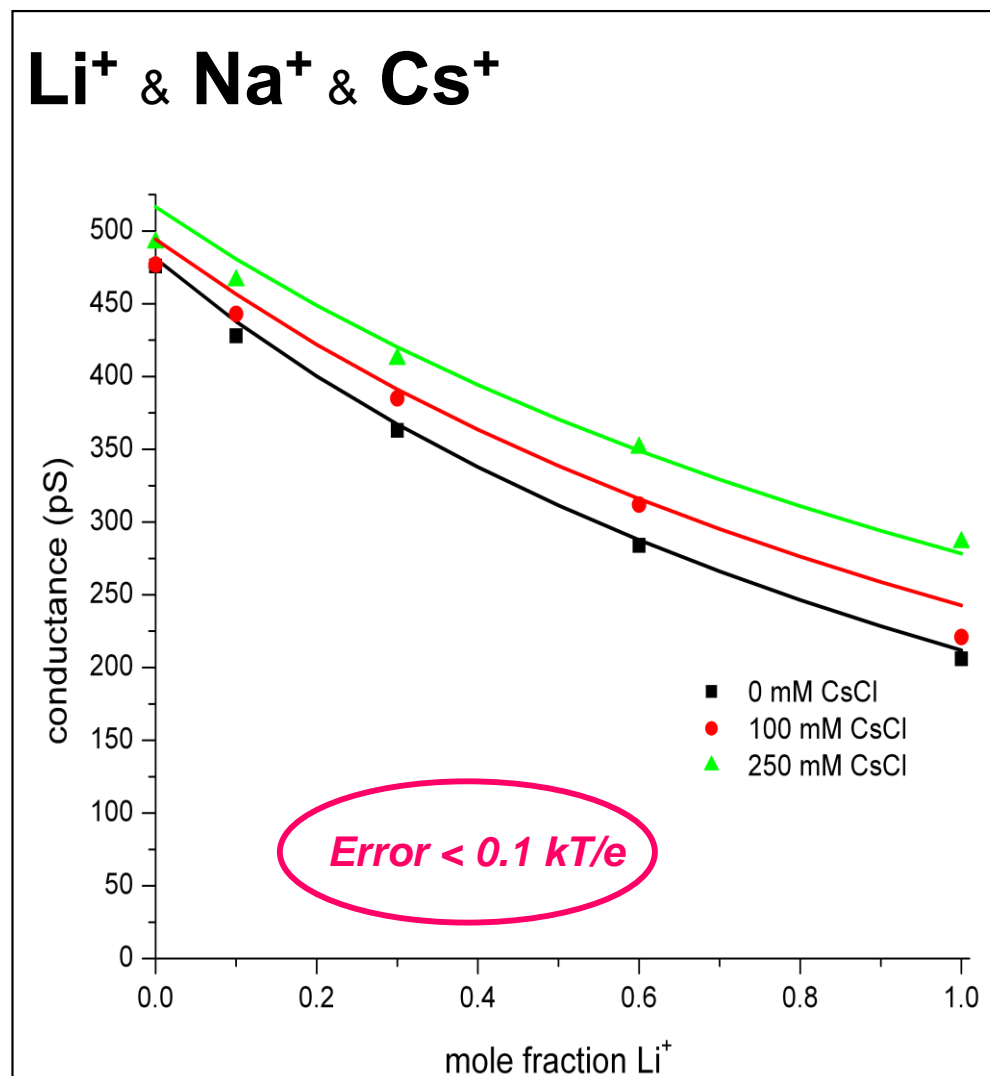
The model reproduced the competition of cations for the pore without any adjustable parameters.

Gillespie, Meissner, Le Xu, et al

## $\text{Li}^+$ & $\text{K}^+$ & $\text{Cs}^+$



## $\text{Li}^+$ & $\text{Na}^+$ & $\text{Cs}^+$





# **Energetic Variational Analysis**

*EnVarA*

being developed by

Chun Liu

Yunkyong Hyon and Bob Eisenberg

creates a

# **Field Theory of Ionic Solutions**

that allows boundary conditions and flow

and deals with

**Interactions of Components Self-consistently**

# Energetic Variational Analysis

## *EnVarA*

Chun Liu, Yunkyong Hyon, and Bob Eisenberg

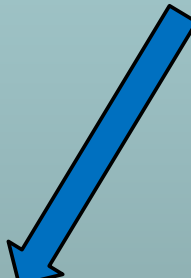
$$\overbrace{\frac{\delta E}{\delta \vec{x}}}^{\text{Conservative 'Force'}} - \overbrace{\frac{1}{2} \frac{\delta \Delta}{\delta \vec{u}}}^{\text{Dissipative 'Force'}} = 0$$

Variational Principle 

# EnVarA

Generalization  
of Chemical Free  
Energy

$$\begin{aligned}
 E(\text{Primitive Phase}; t) = & \int \left[ \underbrace{\left\{ \frac{1}{2} \rho |\vec{u}_{IP}|^2 + w(\rho) \right\}}_{\text{Macroscopic (hydrodynamic)}} \right. \\
 & \left. + \lambda \left[ \underbrace{\frac{1}{2} \epsilon |\nabla \phi|^2}_{\text{Electrostatic}} + \underbrace{k_B T (c_n \log c_n + c_p \log c_p)}_{\text{Entropy}} + \underbrace{E(\text{Solid Spheres})}_{\text{Finite Size Effect}} \right] \right] d\vec{x}
 \end{aligned}$$



# Ionic Solution

## Composite of Water and Ionic Fluids

*Primitive Model Part 1*

### Solvent Water Phase

treated as incompressible conductive dielectric

$$\frac{\partial \rho_f}{\partial t} + \nabla \cdot (\rho_f \vec{u}_f) = 0 \quad \nabla \cdot \vec{u}_f = 0$$

$$\underbrace{\rho_f \frac{\partial \vec{u}_f}{\partial t}}_{\text{Acceleration}} + \underbrace{\rho_f \vec{u}_f \cdot \nabla \vec{u}}_{\text{Convective Acceleration}} + \underbrace{\nabla p_f}_{\text{Pressure Gradient}} = \underbrace{M_f \nabla^2 \vec{u}_f}_{\text{Viscosity}} + \underbrace{k (\vec{u} - \vec{u}_f)}_{\text{Coupling Drag}}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\vec{u} \rho) = 0$$

# Ionic Solution

## Primitive Model Part 2

Macroscopic and atomic scale combined.

Ions in incompressible conductive dielectric

$$\overset{\text{Acceleration}}{\rho} \left( \overset{\text{Convective Acceleration}}{\frac{\partial \vec{u}}{\partial t}} + \vec{u} \cdot \nabla \vec{u} \right) + \overset{\text{Pressure Gradient}}{\nabla p}$$

$$= M \nabla^2 \vec{u} + \overbrace{k(\vec{u} - \vec{u}_f)}^{\text{Coupling Drag}} + \overbrace{(c_n(\vec{x}) - c_p(\vec{x})) \nabla \phi}^{\text{Coulomb Force}}$$

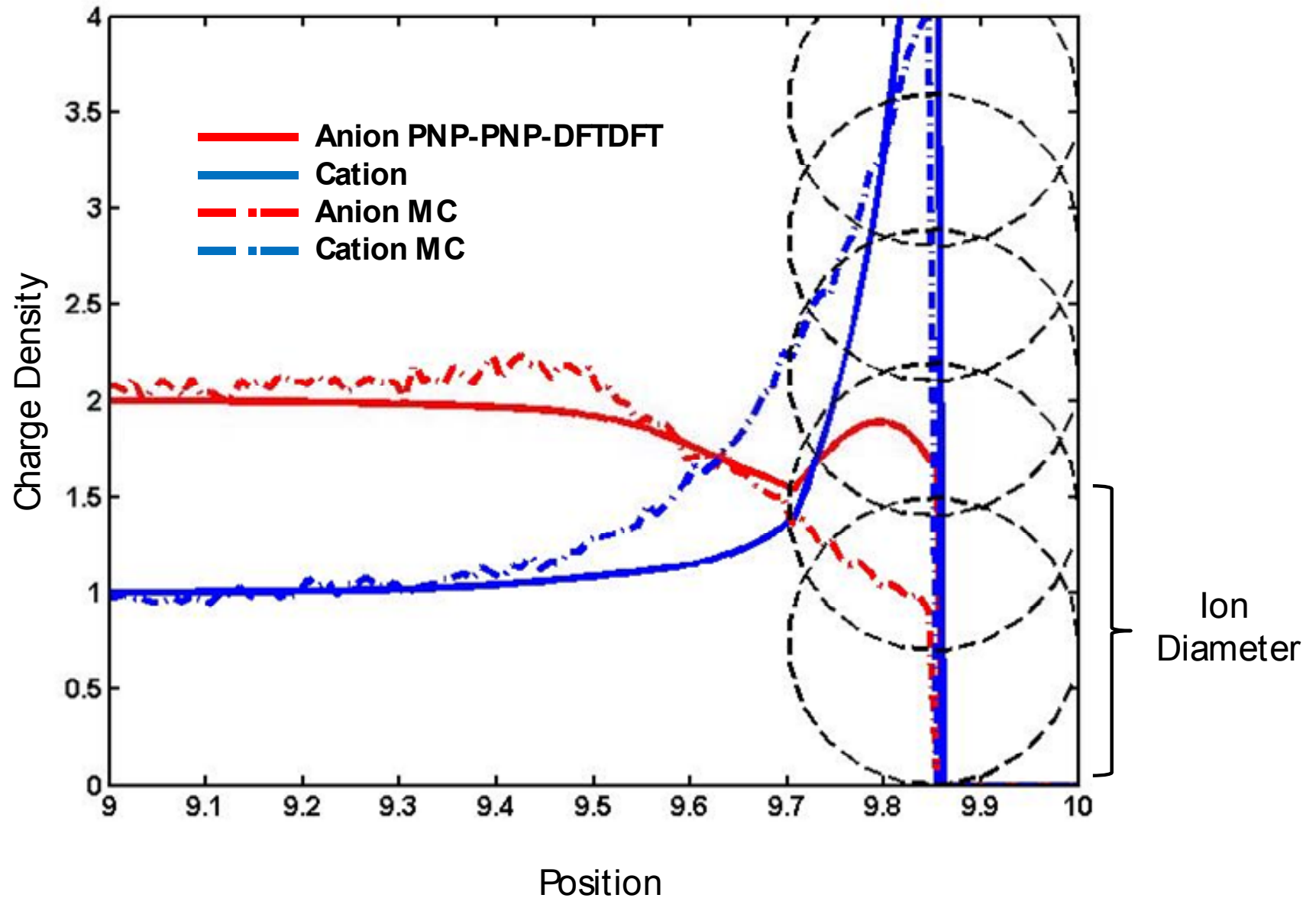
$$\begin{aligned} & -c_n(\vec{x}) \nabla \cdot \int \chi(|\vec{x} - \vec{y}|) (c_n(\vec{y}) + \frac{1}{2} c_p(\vec{y})) d\vec{y} \\ & -c_p(\vec{x}) \nabla \cdot \int \chi(|\vec{x} - \vec{y}|) (\frac{1}{2} c_n(\vec{y}) + c_p(\vec{y})) d\vec{y} \end{aligned}$$

Lennard Jones Solid Sphere

$$c(|\vec{x} - \vec{y}|) = e_{i,j} \frac{a_i + a_j}{|\vec{x} - \vec{y}|} \ddot{\phi}^{12}$$

# Layering: Classical Interaction Effect

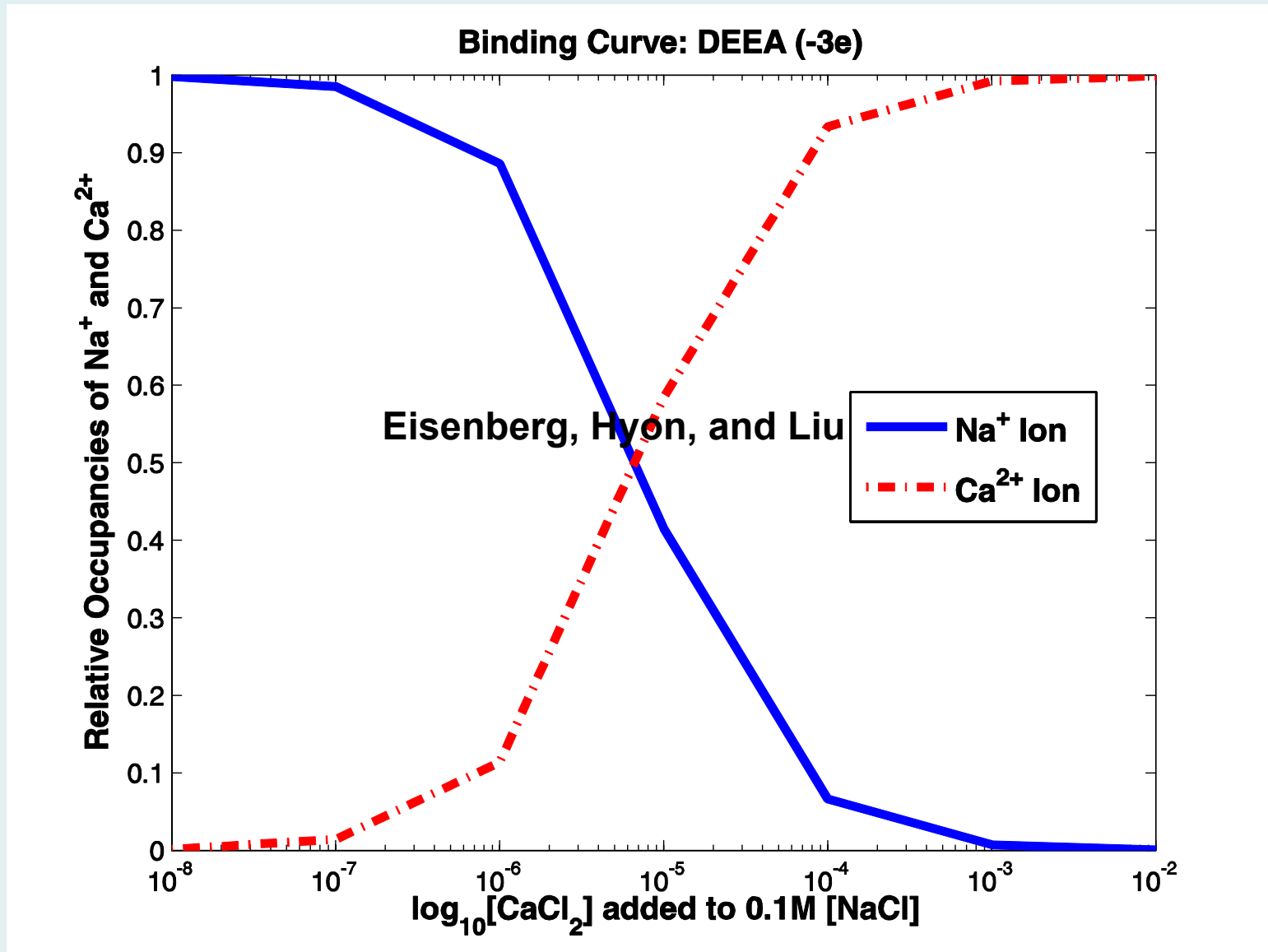
Comparison between PNP-DFT and MC



Eisenberg, Hyon, and Liu

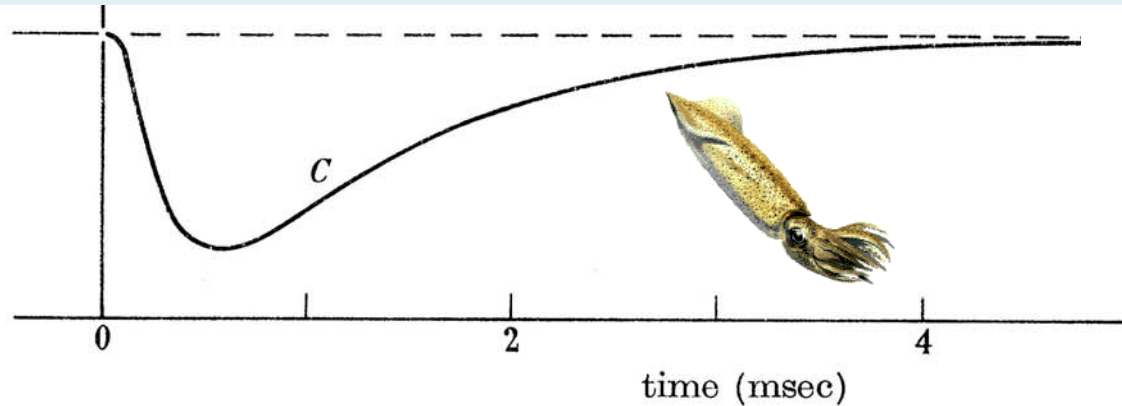
# Ca<sup>2+</sup> and Na<sup>+</sup> Binding Curves

## DEEA Calcium Channel

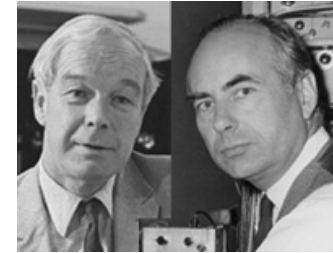


# Sodium Conductance and Inactivation

in Squid Axon (nerve fiber)



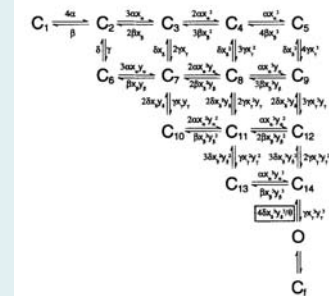
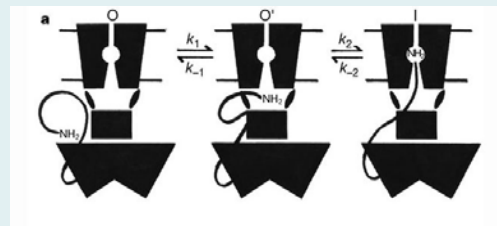
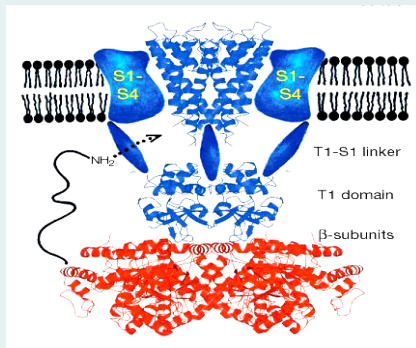
Hodgkin Huxley



J. Physiol (1952)  
116:497

FIGURE 9. Separation of current into components carried by Na and K, from Hodgkin & Huxley (1952*a*, figure 5). A depolarization of 56 mV was applied at  $t = 0$ ; the temperature was 8.5°C. Outward current is shown upwards.

## Conventional Explanation: Elaborate Structural Change



# **Inactivation is Important**

**Many diseases produced by changes in details of inactivation.**

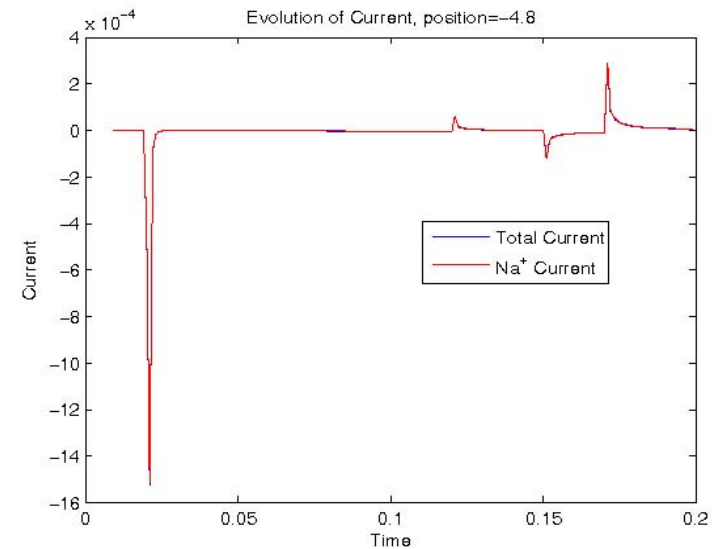
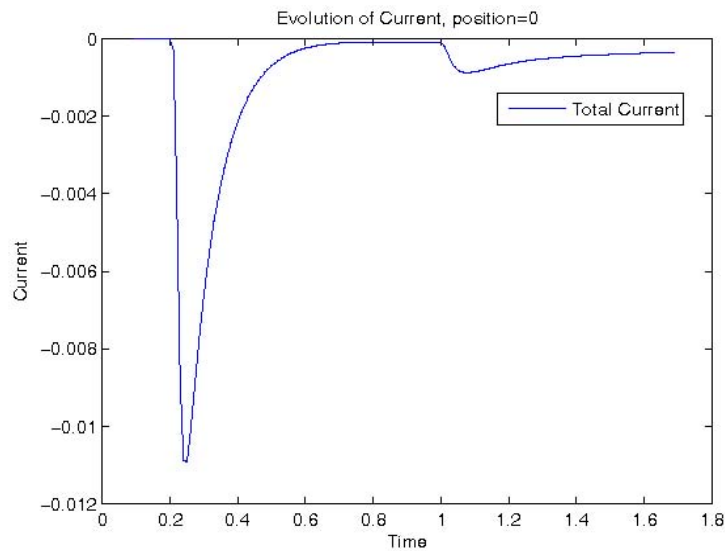
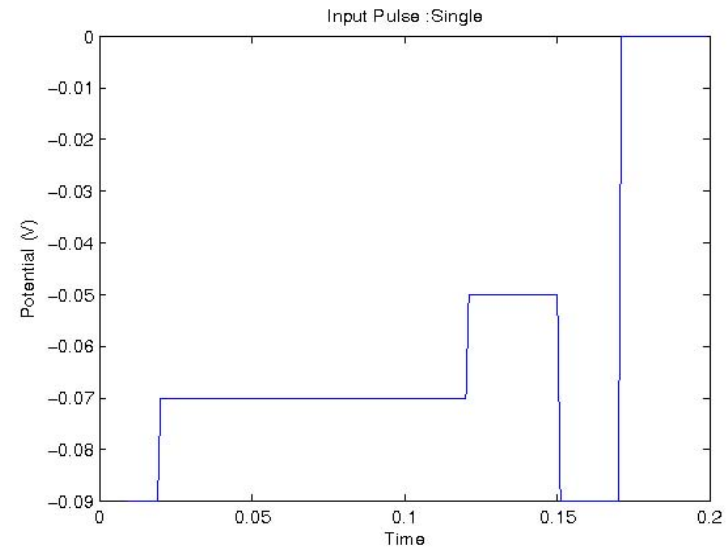
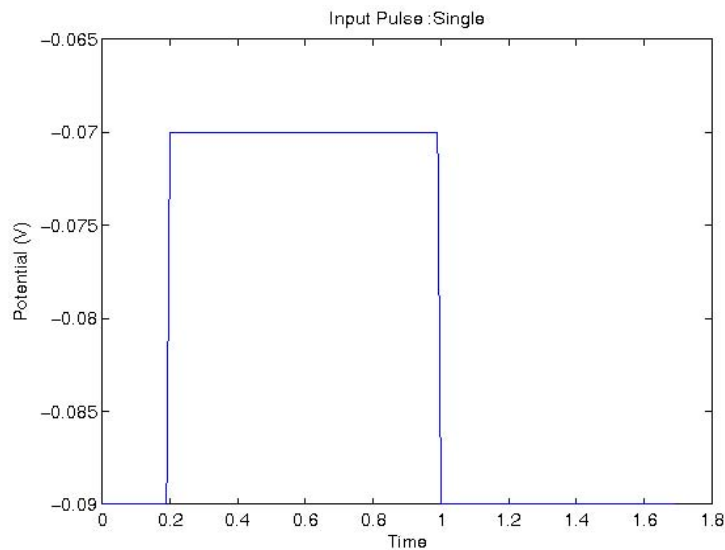
**Energetics of Brain determined by details of inactivation\***

**Energetics determined by time overlap of Na and K currents**

**\*Alle, Roth, and Geiger. Science (2009) 325:1405-8.**

# Sodium Conductance and Inactivation

## Variational Computation in Fixed Structure



# Energetic Variational Analysis

*EnVarA*

Chun Liu, Yunkyong Hyon and Bob Eisenberg

**New Interpretations**

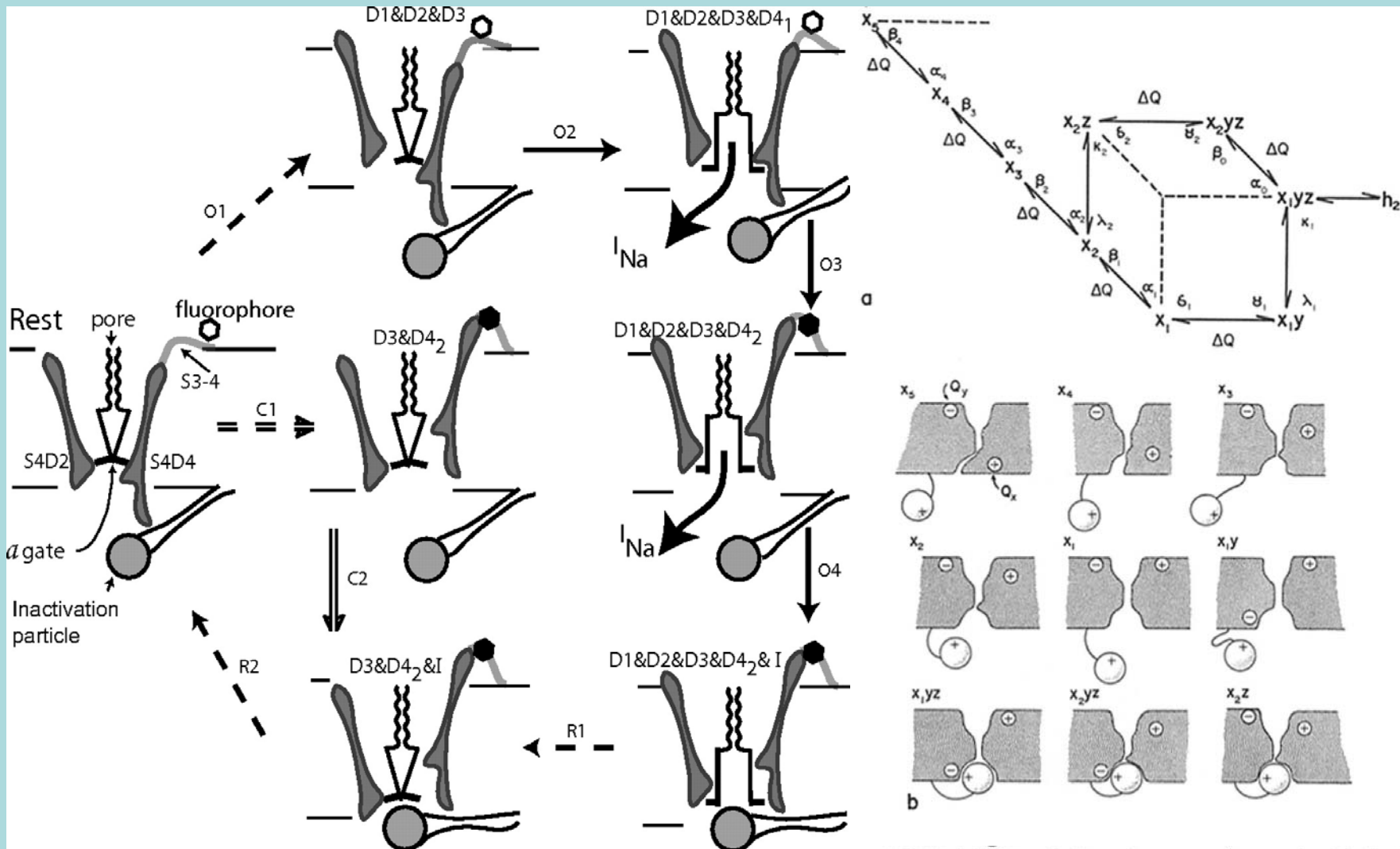
likely to be

**Controversial**

but

**Quantitative and Testable**

# Channel Activation and Inactivation 'Ball and Chain' Model



Armstrong PNAS 2006 103:17991

Armstrong & Bezanilla J Gen Physiol 1977 70:567

Existing Models are Structural and Mechanical  
with no quantitative results

# Energetic Variational Approach *EnVarA*

**New mechanisms\* can be added**

\*if they define an energy and its variation :  
Energy defined by simulations or theories or experiments is OK.

**Full micro/macro treatment  
is needed for an  
Atomic Model,  
with closure.**

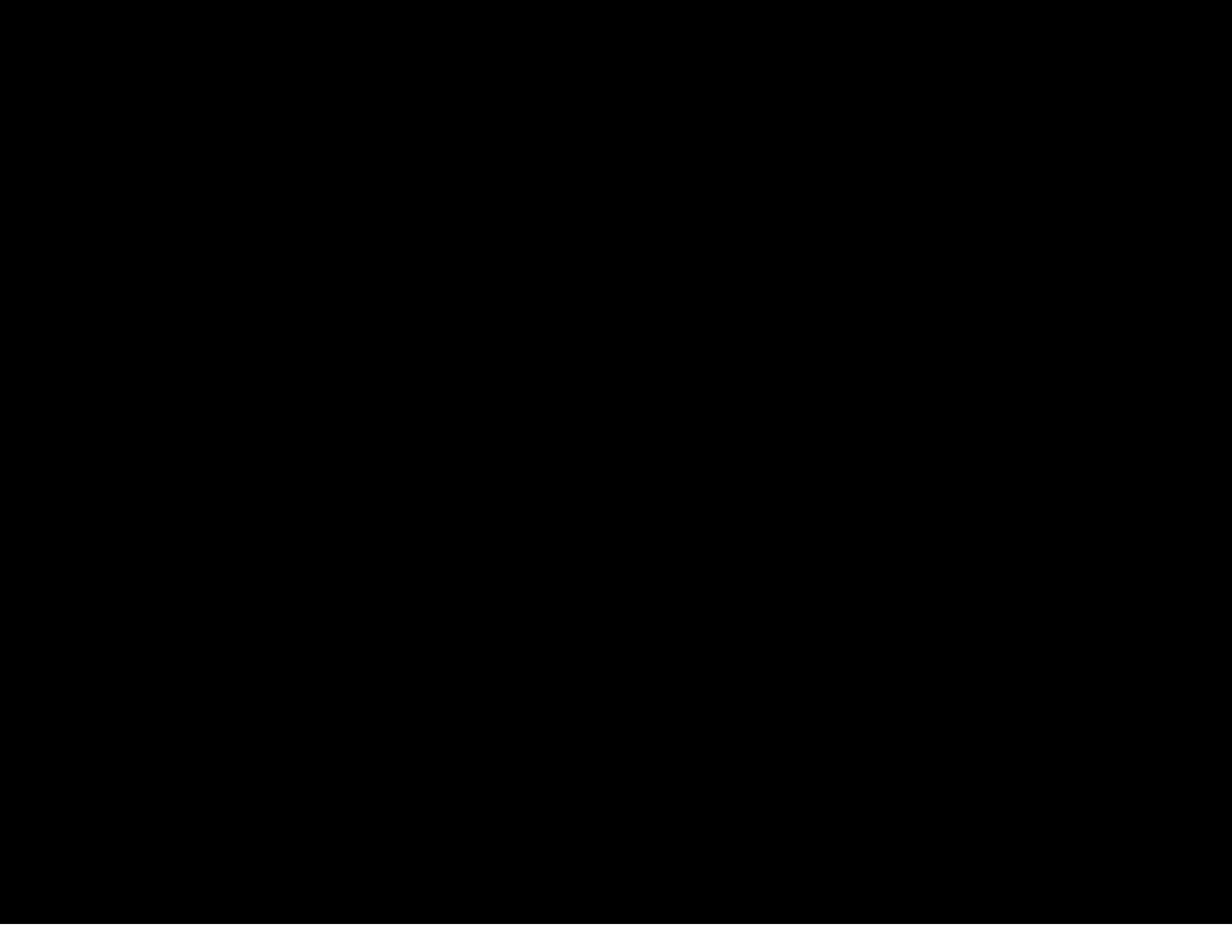
# Can Variational Approach actually calculate Complex\* Biology?

Rolf Ryham and Chun Liu have actually calculated

**\*Movies of Vesicle Fusion**

in preliminary work

with Fred Cohen and Bob Eisenberg





# ***Vaccinations against Traditional Models***

# ***Vaccination 1:***

## **Traditional Biochemistry and Traditional Molecular Dynamics Assume Ideal Solutions**

**Ions in Water and Life are NOT ideal**

**Life Occurs in ~130 mM salt solutions**

**Ions in Water are the Liquid of Life**

## ***Vaccination 2:***

**No gas phase models of  
traditional channel biochemistry**

***Liquids are not Gases***

**No discussions of individual trajectories of  
Structural Biologists**

***Counting and Statistics are essential***

# ***Vaccination 3:***

## **Selectivity**

**Depends Sensitivevely on Self-organized Structure and their Flexibility**

**Induced Structure is Different in Different Solutions**

**so**

# **Structure must be Computed!**

**Rate constants are variables that change dramatically with conditions**

## ***Vaccination 4:***

# **Computation Starts From Crystal Structure *when available* *but***

**Crystal Structures cannot determine Selectivity  
*because***

- 1) Crystal Structures are measured in only one unphysiological solution**
- 2) Crystal Structures are not accurate enough**
- 3) Crystal Structures do not give entropy**

## ***Vaccination 5:***

**Simulations must be calibrated against experimental data.**

**Simulations are not mathematics.**

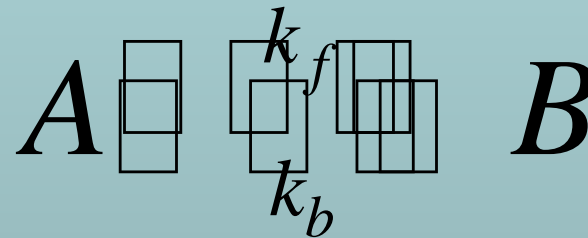
**Molecular Dynamics is science not mathematics.**

## Vaccination 6:

**Law of Mass Action is usually misused.**

**Rate Constants are almost never constant**  
as conditions are changed.

**They often change by factor of  $10^4$  !!**



$$-\frac{d}{dt}[A] = k_f [A]$$

$$J_{A \rightarrow B} = k_f [A]$$

$$-\frac{d}{dt}[B] = k_b [B]$$

$$J_{B \rightarrow A} = k_b [B]$$

Differential equations are almost always solved assuming  $k_f$  and  $k_b$  are constants.

[A] means the concentration of species A, i.e., the number density of A

