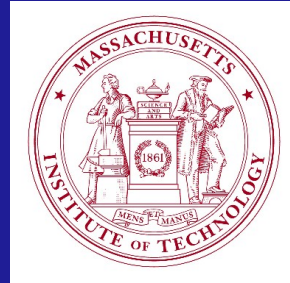


Formation of Close-in Super-Earths and Mini-Neptunes



Hilke E. Schlichting

MIT

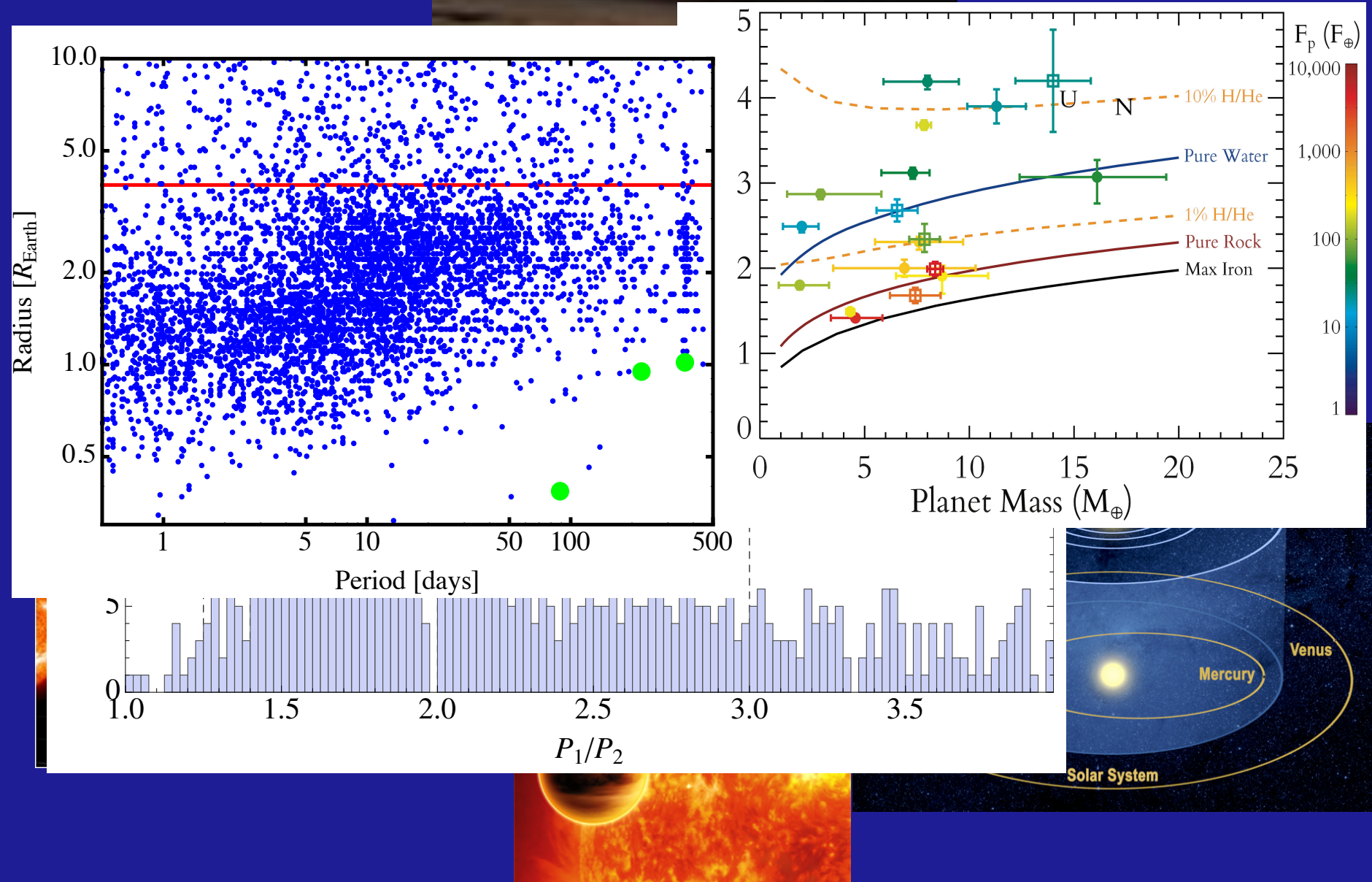
KITP Lunch Seminar

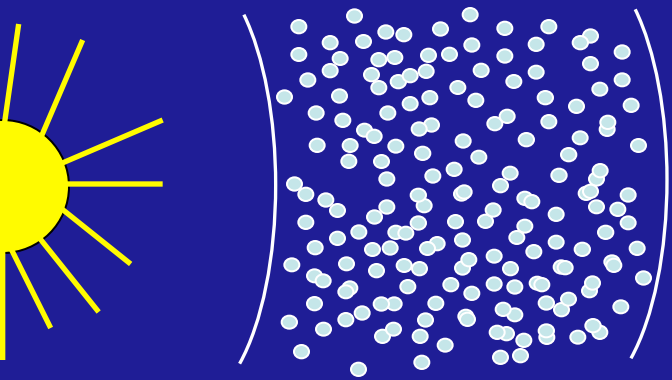
Feb 3th 2015

Collaborators:

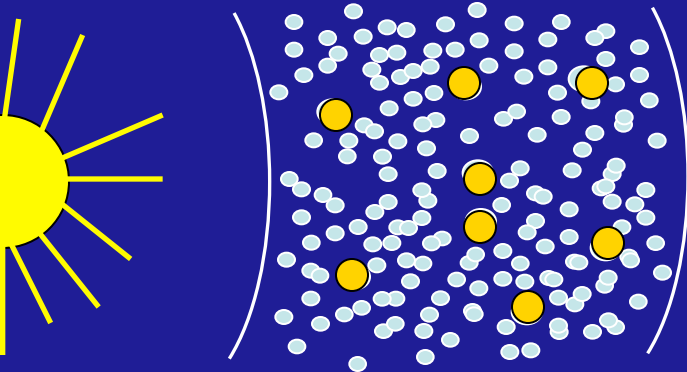
Niraj Inamdar (PhD Student, MIT), Peter Goldreich (Caltech)

From Gas & Dust to Planets





1. Planetesimal formation:

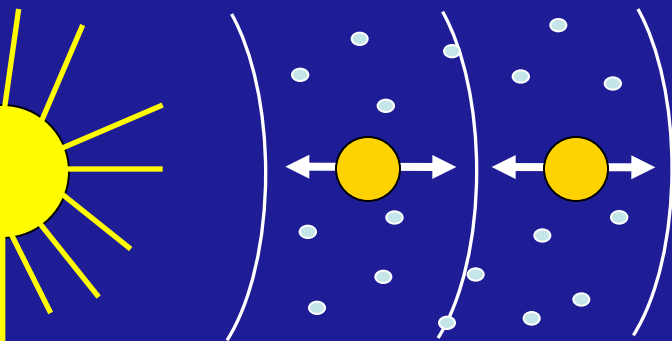


2. Runaway growth:

$$\frac{1}{R_1} \frac{dR_1}{dt} \propto R_1$$

For $v_{\text{esc}} > u$ gravitational focusing enhances the accretion rate

$$\frac{1}{R} \frac{dR}{dt} \sim \frac{\sigma \Omega}{\rho R} \left(\frac{v_{\text{esc}}}{u} \right)^2 \longrightarrow t_{\text{grow}} \sim 10^7 \text{ years}$$



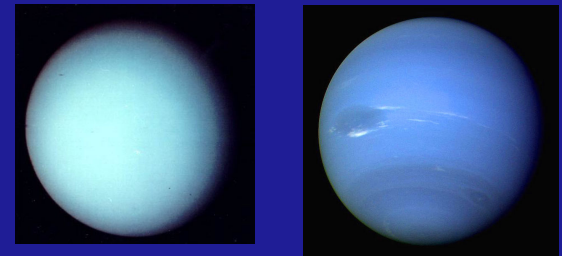
3. Oligarchic growth & Isolation:

$$M_{\text{iso}} \approx 2\pi a (\Delta a_{\text{zone}}) \Sigma \sim M_{\text{Neptune}}$$

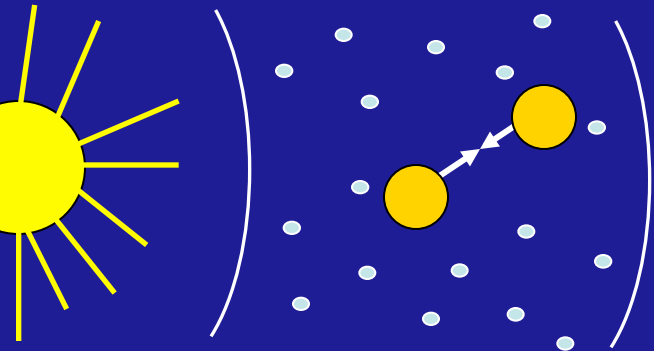
planetesimals protoplanets

$$u, \sigma$$

$$v, \Sigma$$



Last Stages of Terrestrial Planet Formation

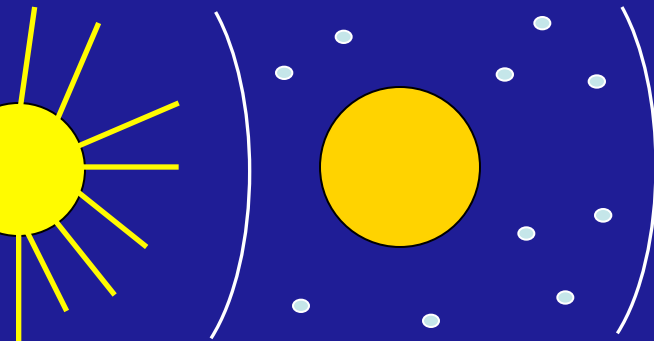


Giant Impacts:

Protoplanets' velocity dispersion increases

→ Giant Impacts

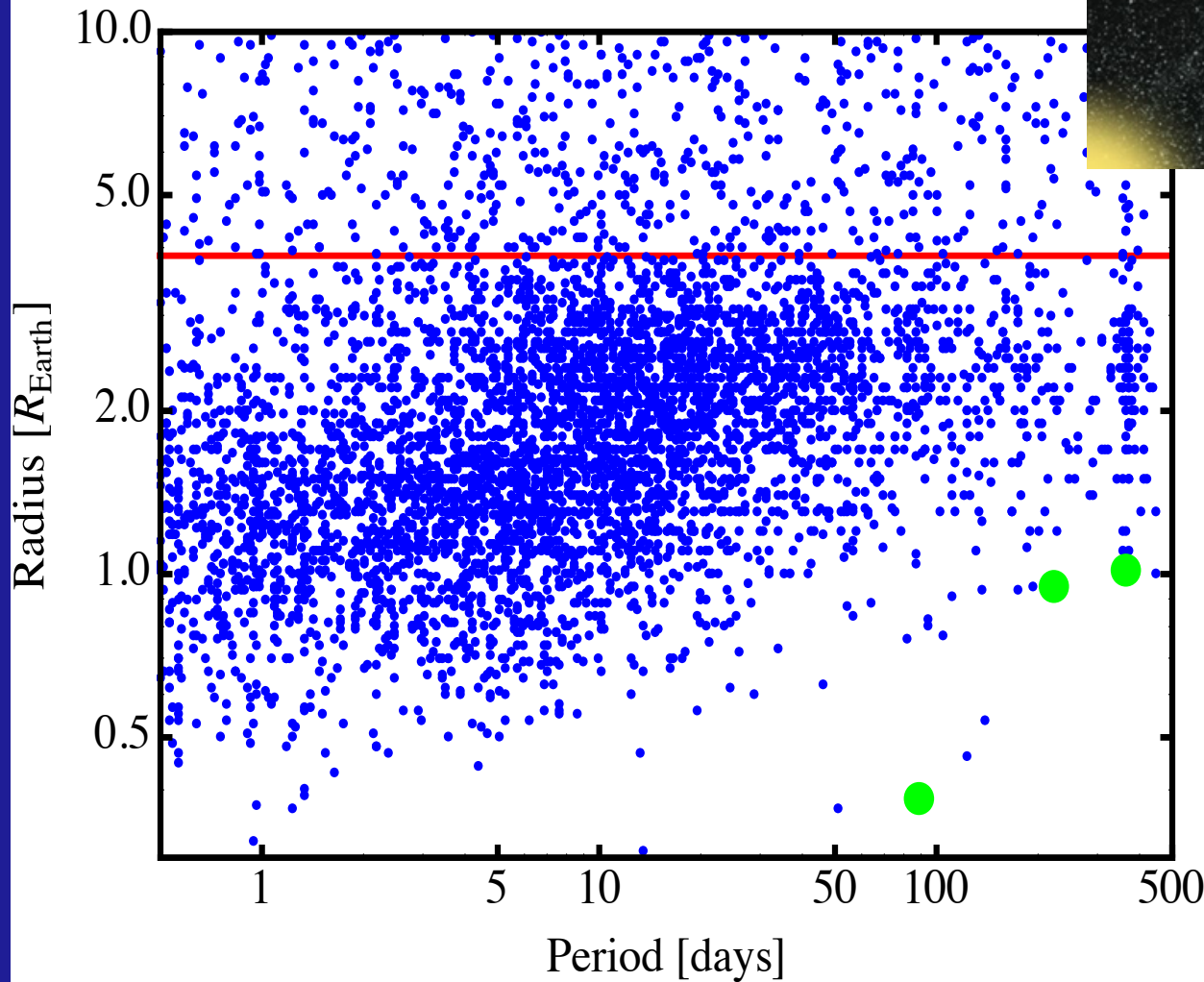
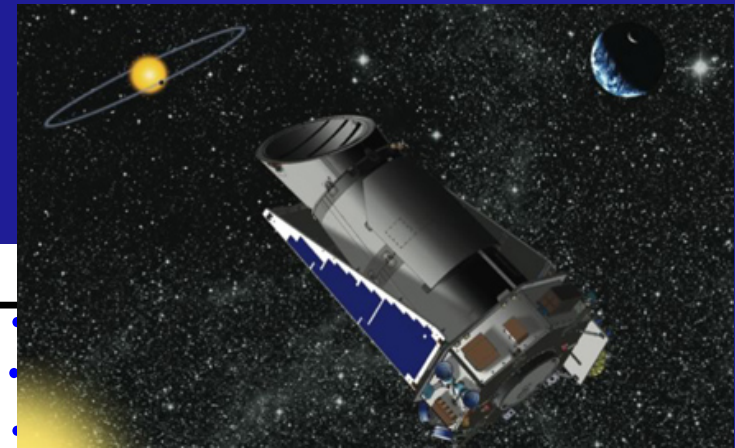
$t_{\text{Giant-Impacts}} \sim 10^8 \text{ years (1AU)}$



Clean up:

- Orbits planar & circular
- Accretion & ejection of remaining planetesimals

Kepler Mission



3538 Planetary
Candidates

1218 Planets in
Multi-Planet Systems

Medium Radius = 2.3

R_{Earth}
Medium Period = 9 days

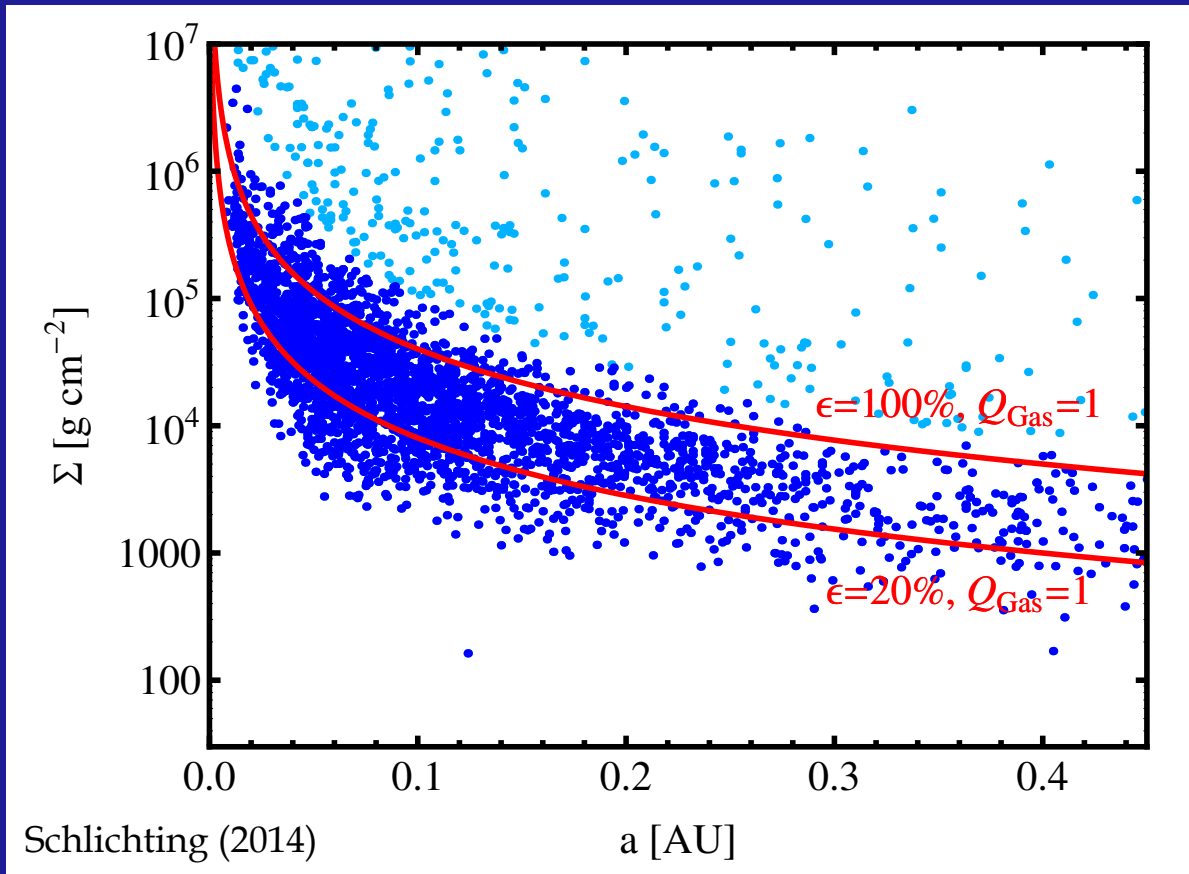
All planetary candidates discovered by Kepler as of Nov. 5th 2013.

Part I

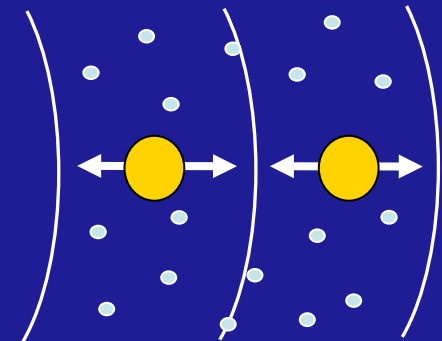
Materials & Supplies



Minimum Disk Masses Required



$$\Delta a \sim 2v_H / \Omega$$

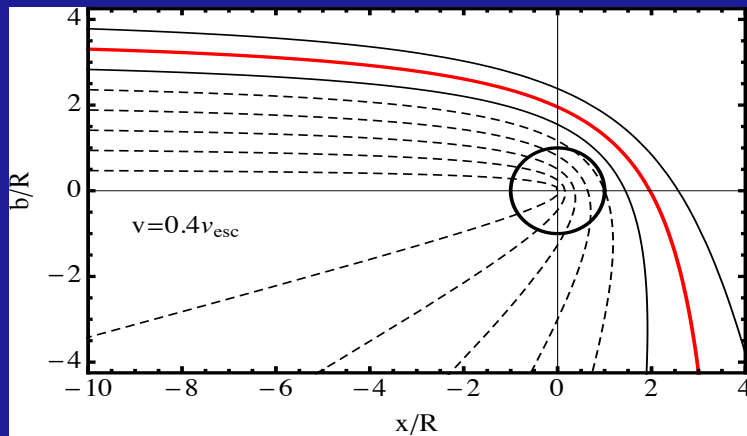


Viscous Stirring

Viscous stirring tends to increase the random kinetic energy all all bodies in the disk

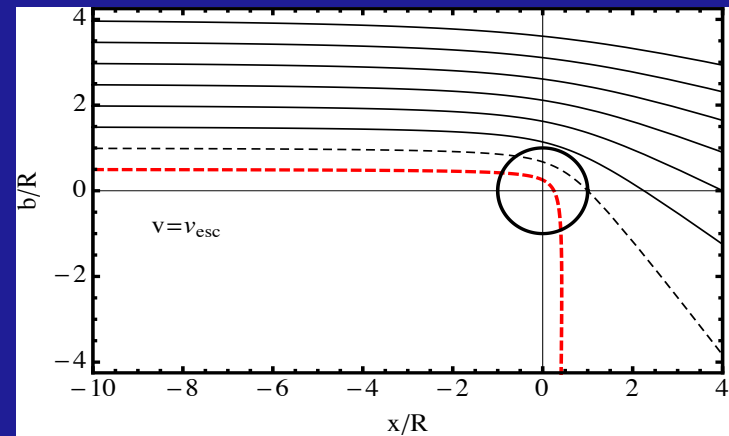
For $v \ll v_{esc}$

$$\sigma_{stirr} \gg \sigma_{coll}$$



For $v \gg v_{esc}$

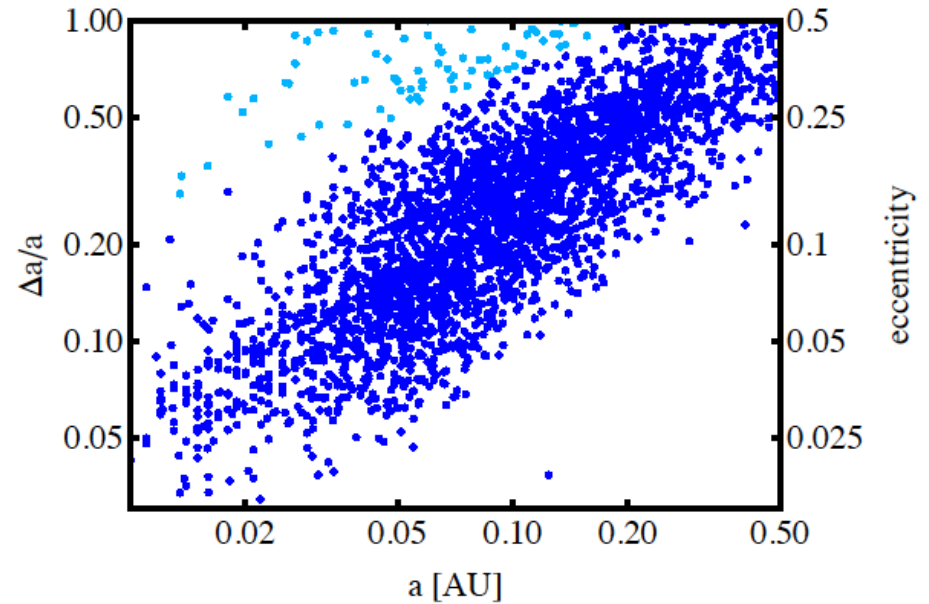
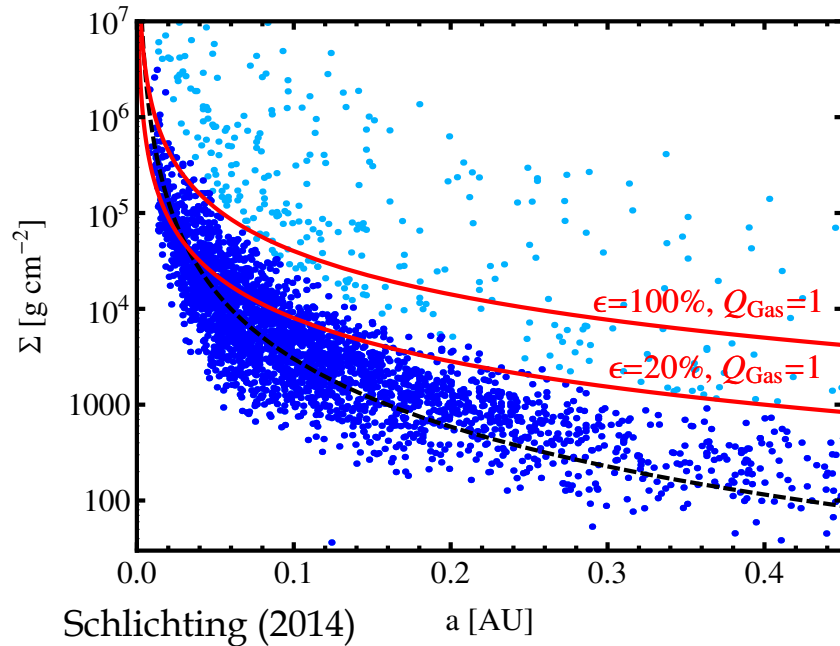
$$\sigma_{stirr} \ll \sigma_{coll}$$



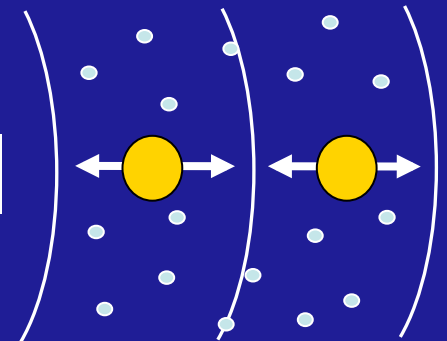
$$\sigma_{stirr} \sim \pi R^2 \left(\frac{v}{v_{esc}} \right)^{-4}$$

$$\sigma_{coll} \sim \pi R^2 \left(1 + \left(\frac{v}{v_{esc}} \right)^{-2} \right)$$

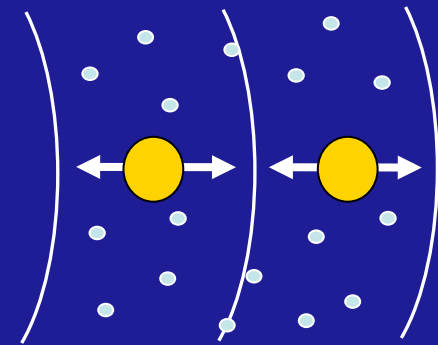
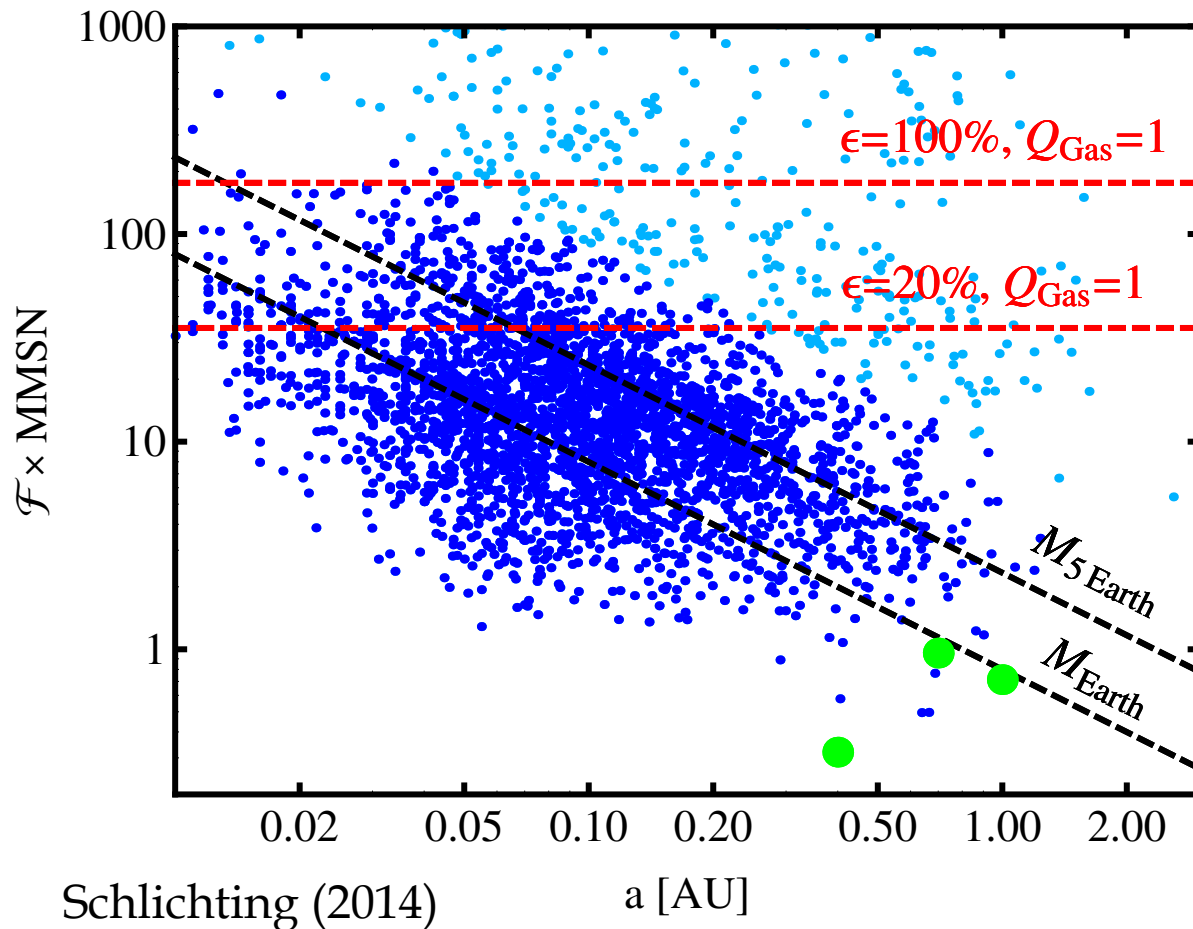
Minimum Disk Masses Required



$$\Delta a \sim 2v_{esc} / \Omega$$



Minimum Disk Masses Required



$$M_{max} \simeq \frac{[2^{5/2} \pi a^2 \Sigma (\rho/\rho_{\odot})^{1/6} (a/R_{\odot})^{1/2}]^{3/2}}{M_{\odot}^{1/2}}$$

Take Home Points I

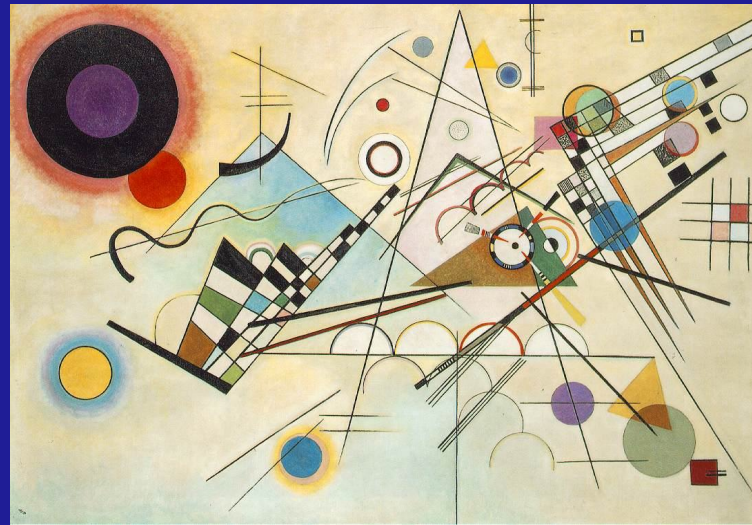
Formation of close in planets as isolation masses unlikely, need very massive inner disks and $\Sigma_{\text{gas}}/\Sigma_{\text{dust}} < 10$ for stability.

Formation of close in planets with Giant Impacts is a possibility, need massive inner disks, typically few tens MMSN.

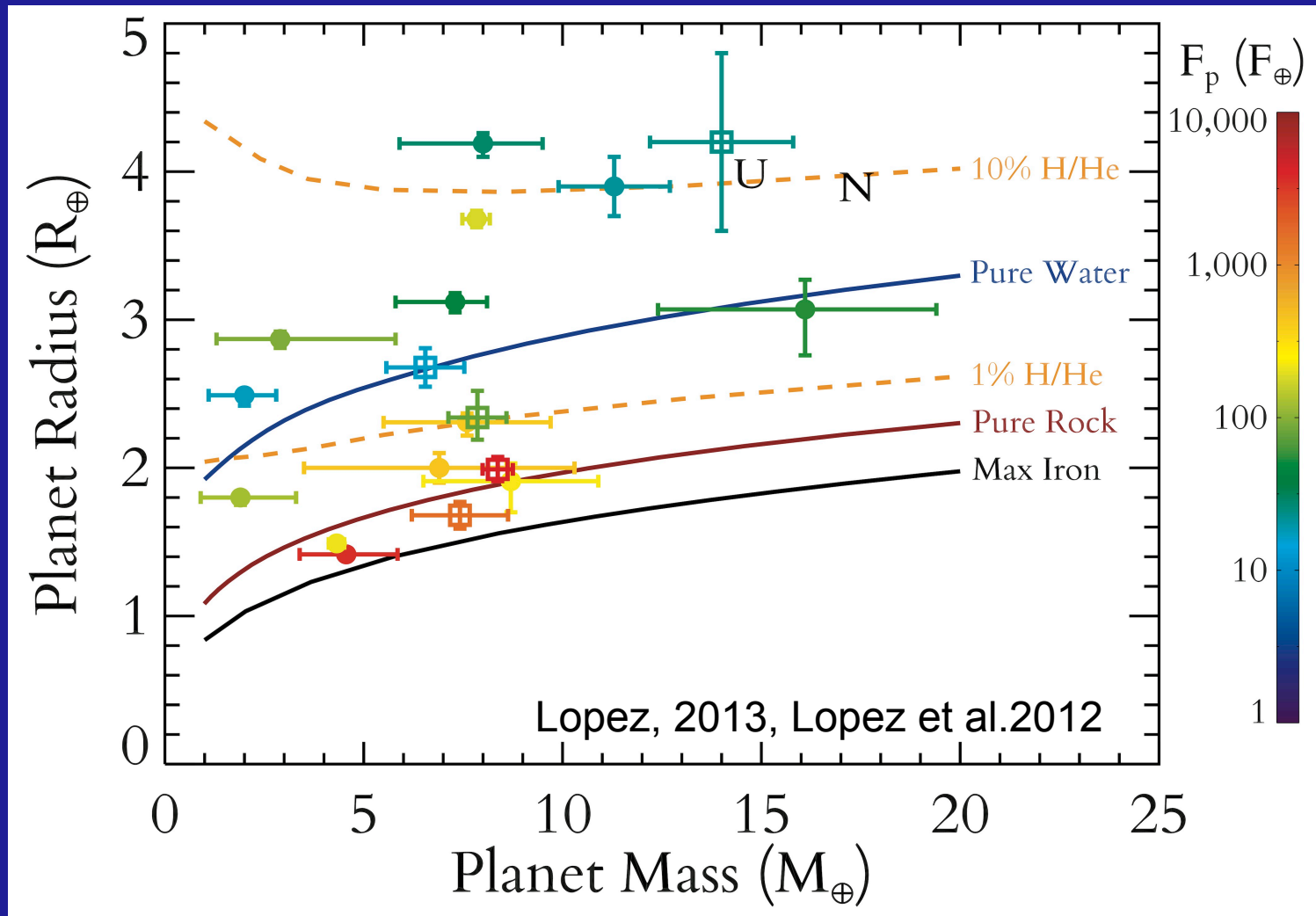
MMSN type disks fully consistent with formation further out and subsequent inward migration and/or radial inward drift of solids and subsequent local assembly.

Part II

Composition & Structure

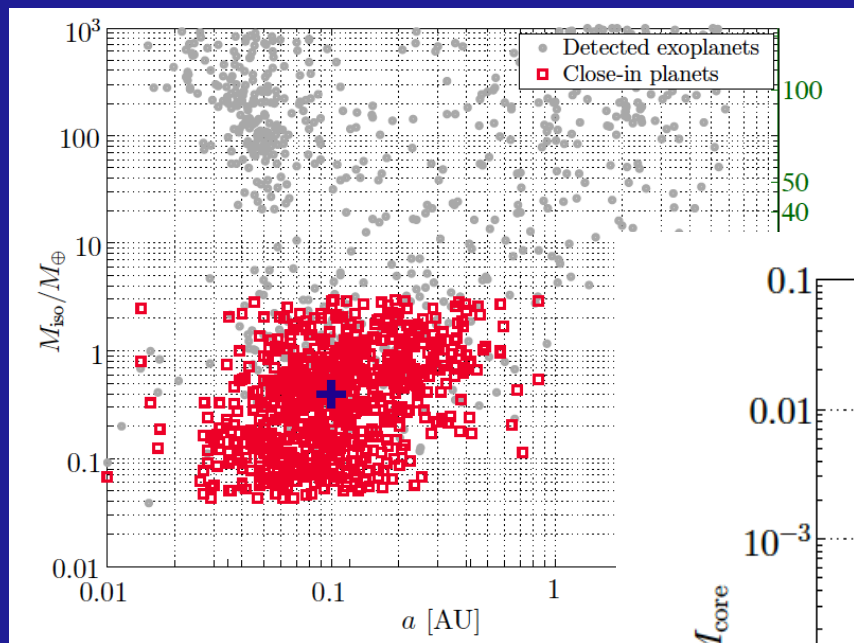


Exoplanet Atmospheres

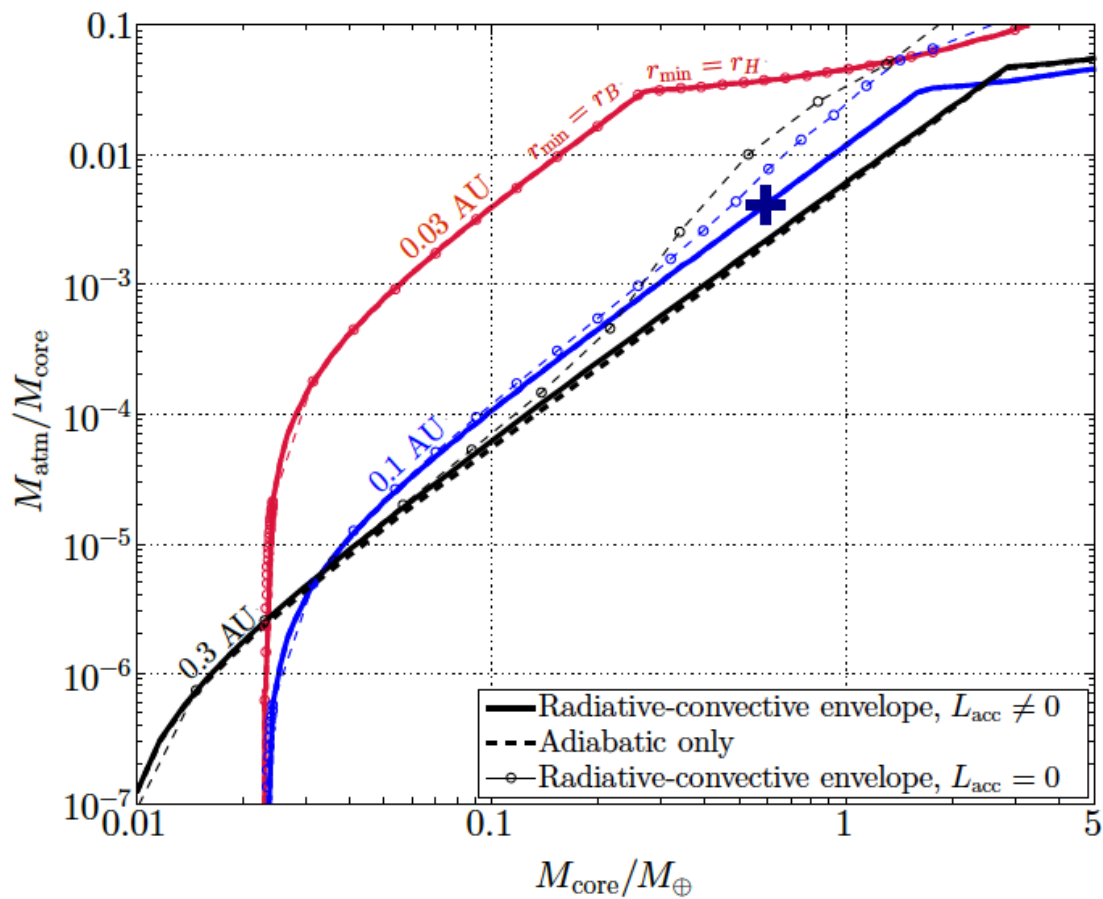


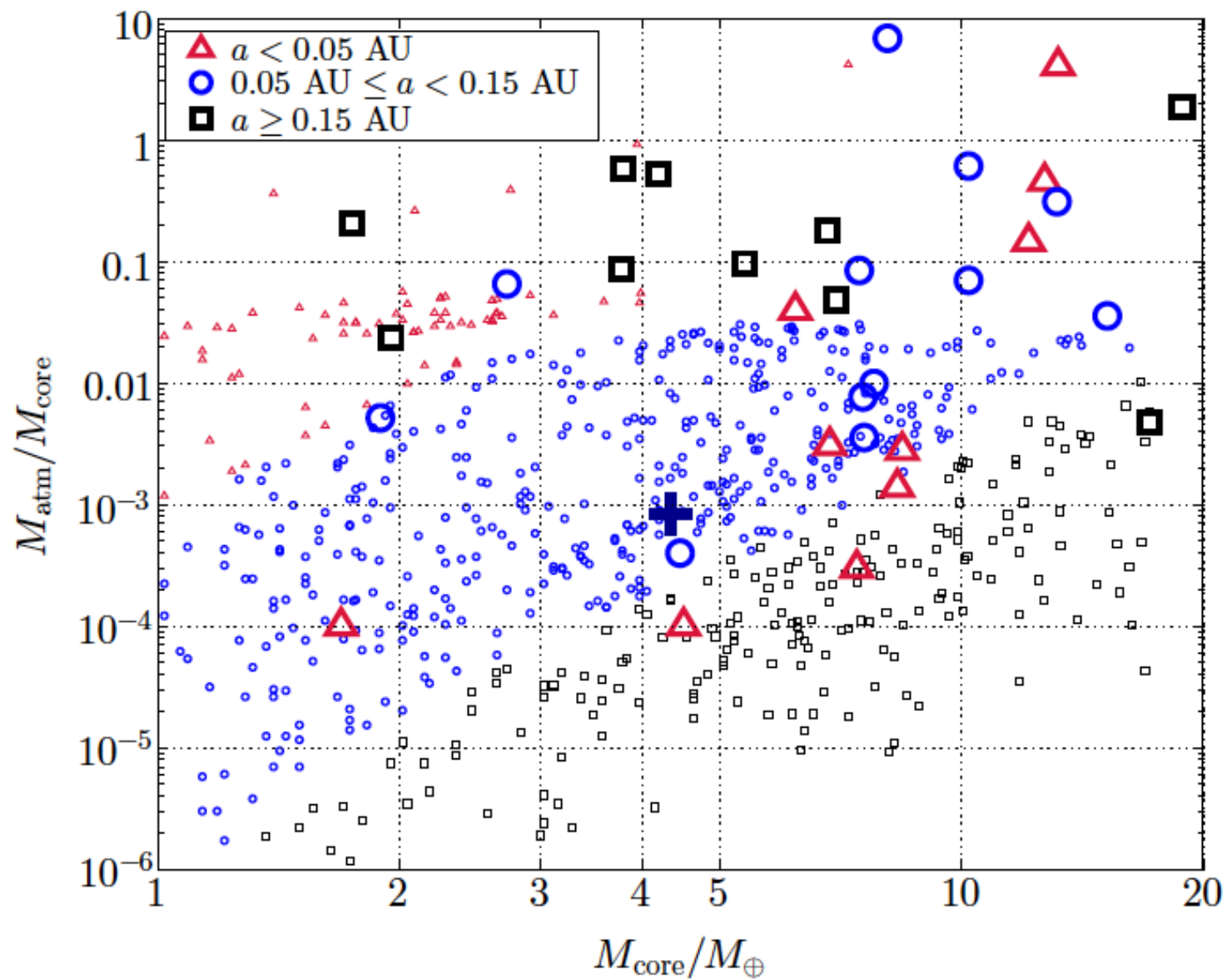
For comparison, the Earth's atmosphere contains less than 10^{-6} of its mass and has an atmospheric scale height that is only $\sim 0.1\%$ of its radius.

Atmospheres of Isolation Masses

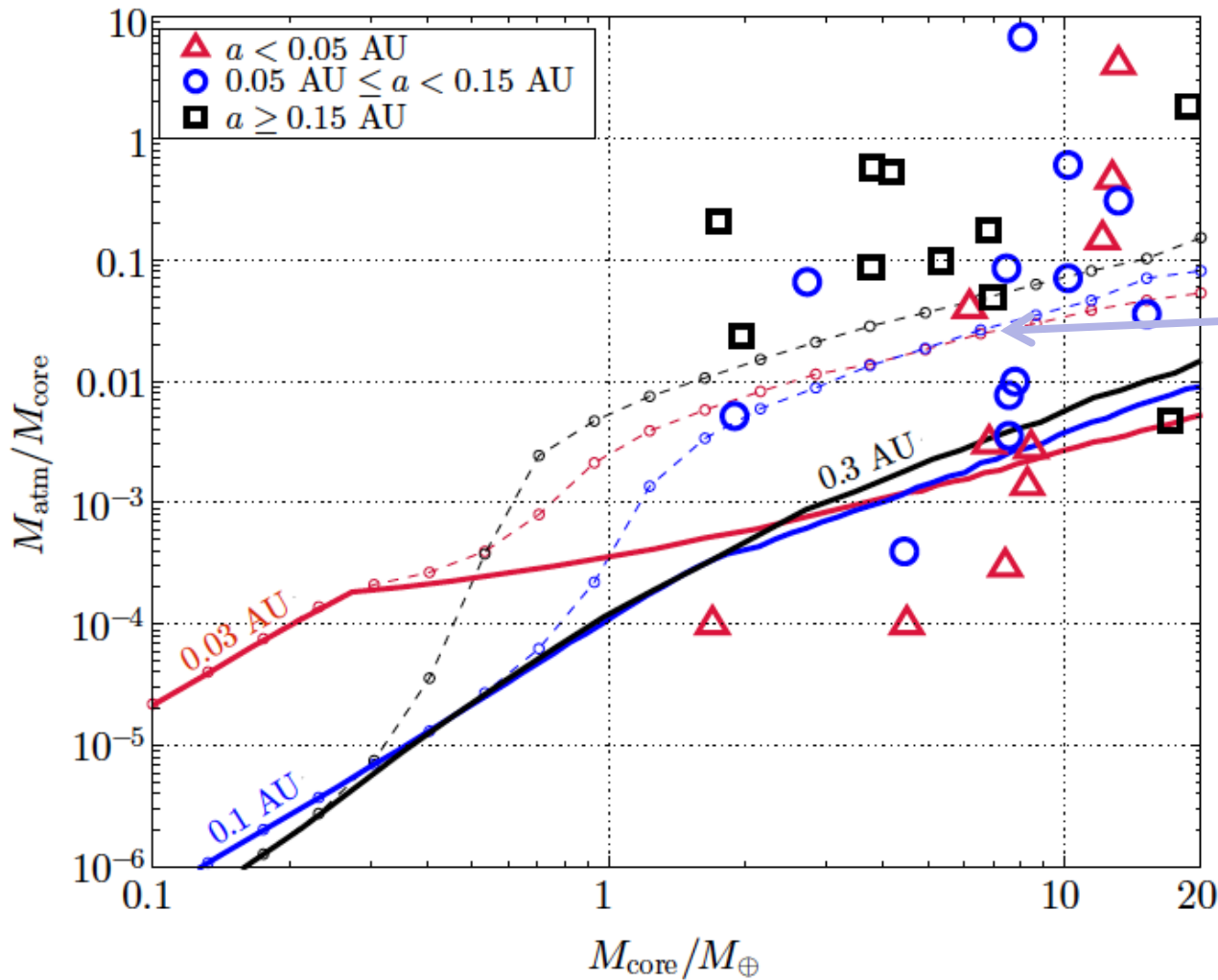


(Inamdar & Schlichting, 2015)





Envelope Accretion After Giant Impacts

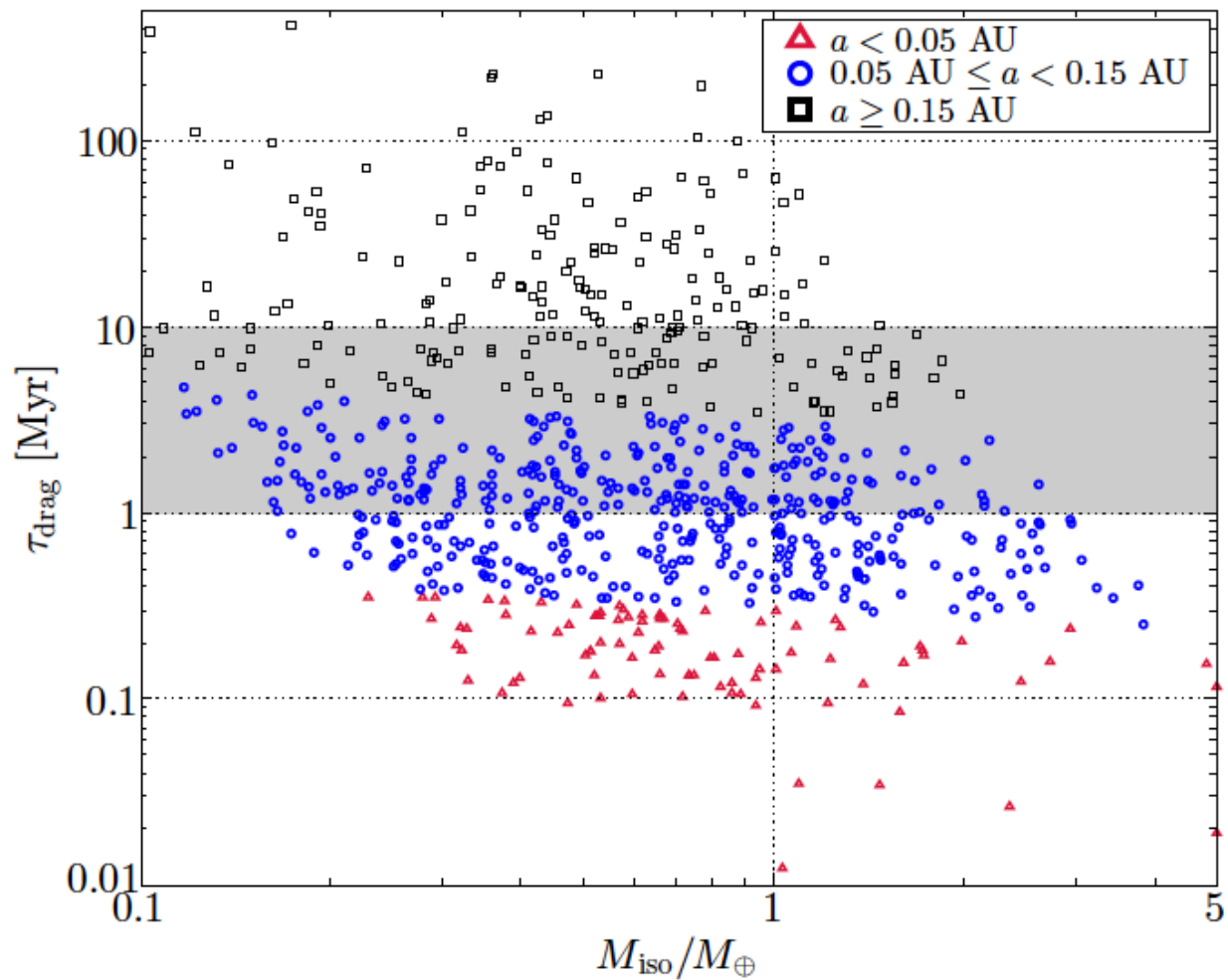


Symbols
from Lopez
& Fortney
(2013)

L=0
(Lee, Chiang &
Ormel 2014)

(Inamdar & Schlichting, 2015)

Radial Drift!



$$R_{\text{core}} \sim M^{1/4}$$

$$\tau_{\text{drag}} = \frac{16}{\pi C_D n^2} \left(\frac{M_p}{R_p^2 \Sigma_g} \right) \left(\frac{a \Omega}{c_s} \right)^3 \frac{1}{\Omega},$$

Take Home Points II

Formation of close in planets as isolation masses challenging, need very massive inner disks and $\Sigma_{\text{gas}}/\Sigma_{\text{dust}} < 10$ for stability and to prevent run-away gas accretion (Lee et al. 2014).

Formation of close in planets with Giant Impacts is a possibility for atmospheres of few % and less if:

- 1) $L_{\text{acc}}=0$, 2) have massive inner disks, typically few tens MMSN and 3) $\Sigma_{\text{gas}}/\Sigma_{\text{dust}} < 10$ to prevent radial drift.

Formation models of close in planets need to account for radial drift of solids and/or migration.