

# Exoplanet Mass Measurements from Solar System Exploration Spacecraft

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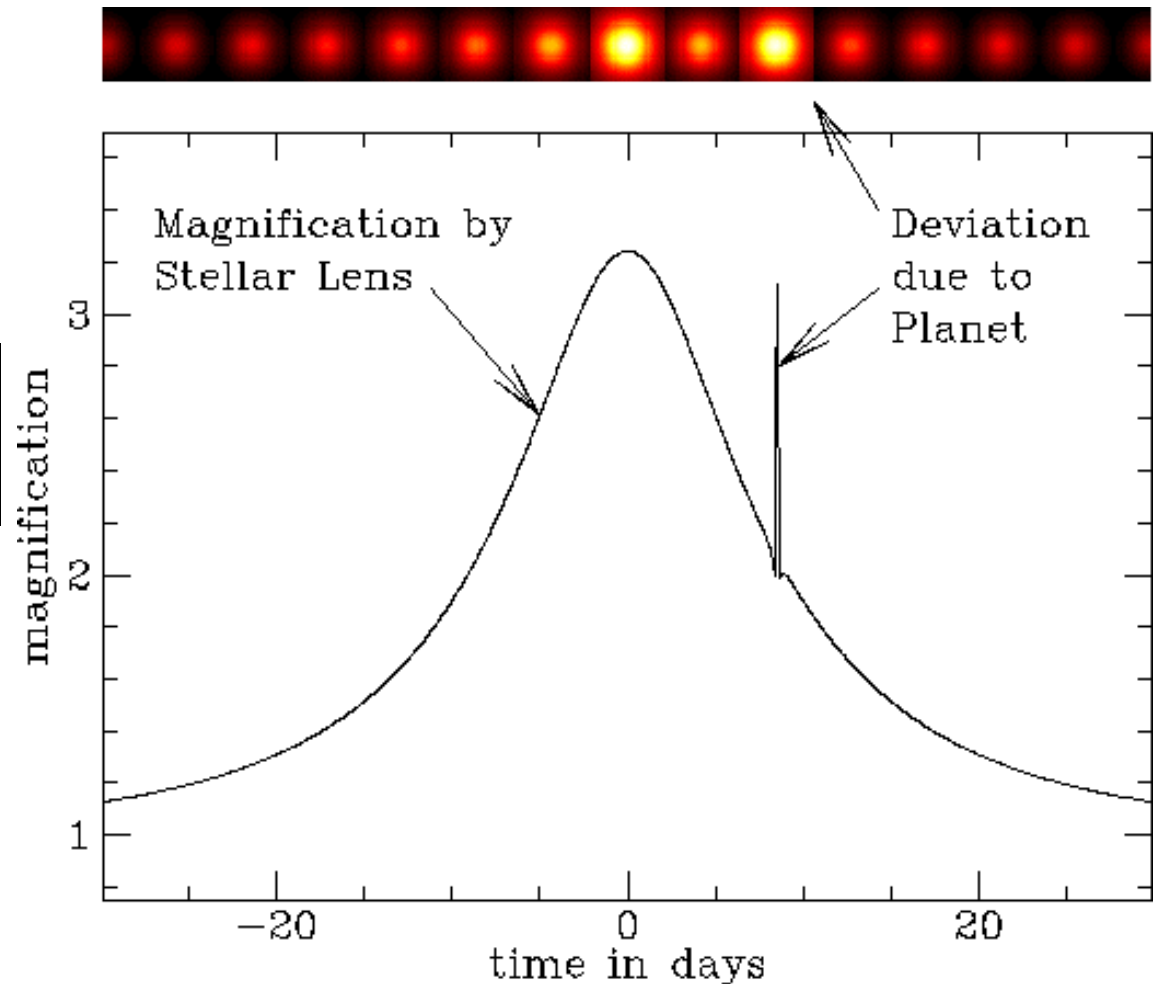


Many results  
in collaboration with

*MicroFUN*

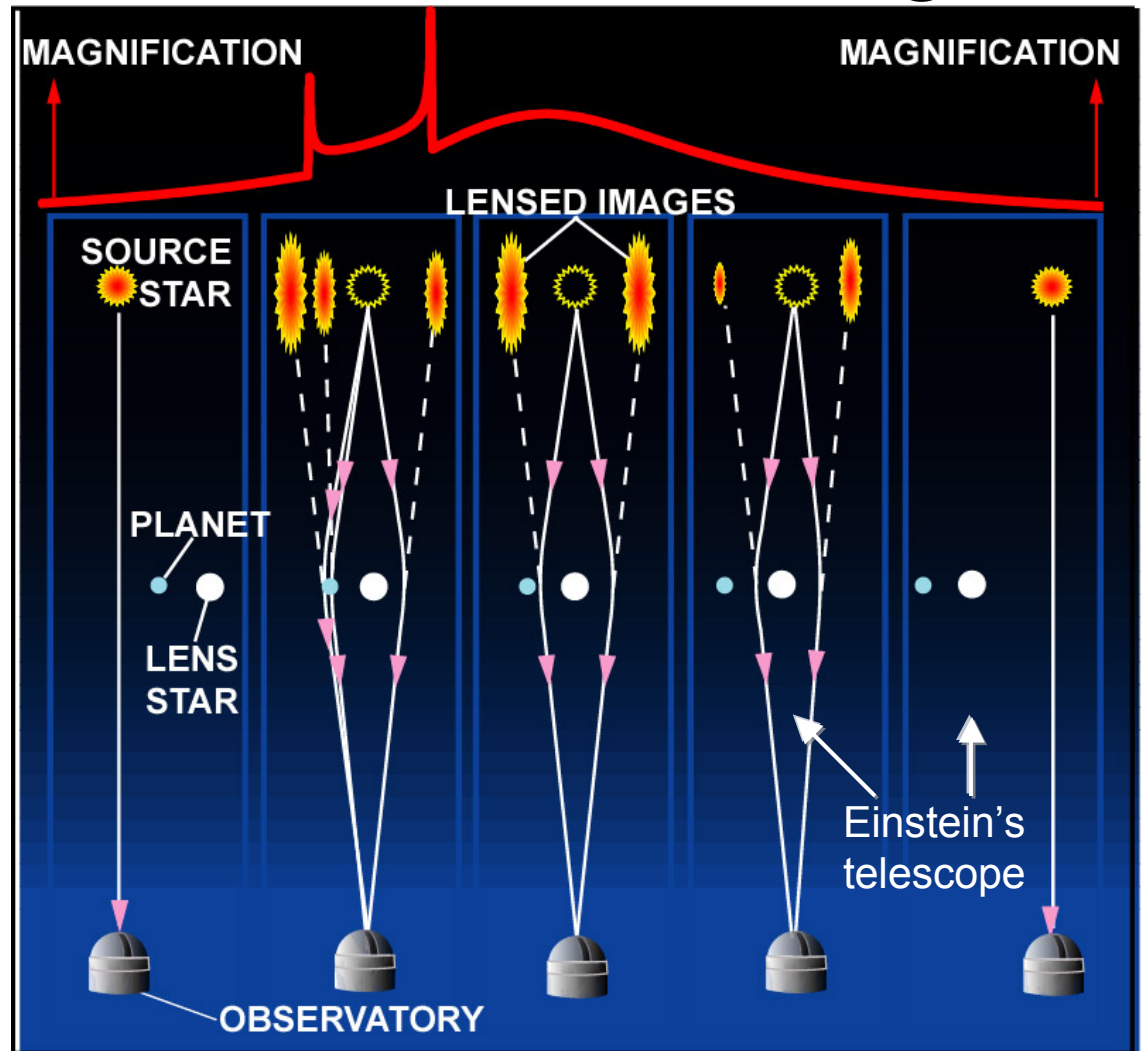
*Microlensing Follow-Up Network*

**OGLE**



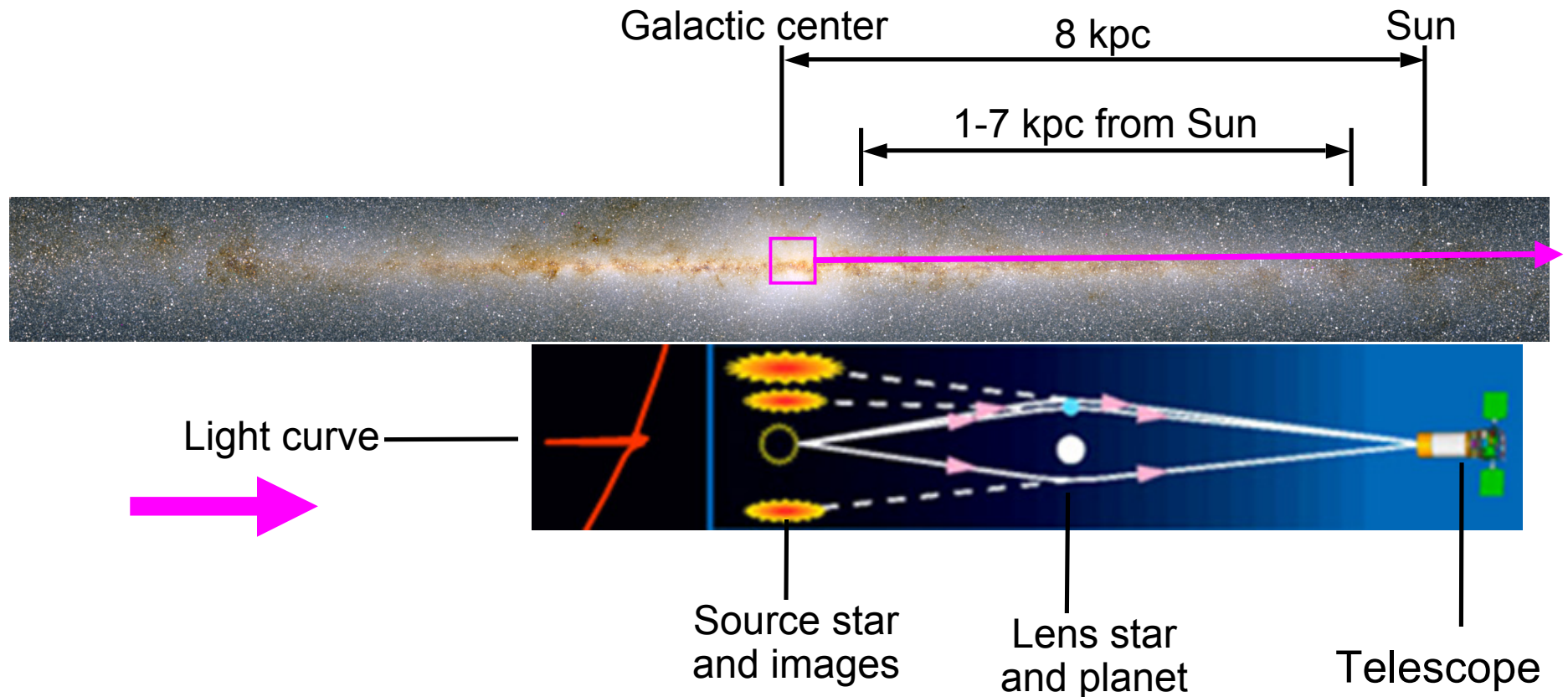
# The Physics of Microlensing

- Foreground “lens” star + planet bend light of “source” star
- Multiple distorted images
  - Only total brightness change is observable
- Sensitive to planetary mass
- Low mass planet signals are rare – not weak
- Stellar lensing probability  $\sim a \text{ few } \times 10^{-6}$ 
  - Planetary lensing probability  $\sim 0.001\text{-}1$  depending on event details
- Peak sensitivity is at 2-3 AU: the Einstein ring radius,  $R_E$



$$\text{Key Fact: } 1 \text{ AU} \approx \sqrt{R_{Sch} R_{GC}} = \sqrt{\frac{2GM}{c^2} R_{GC}}$$

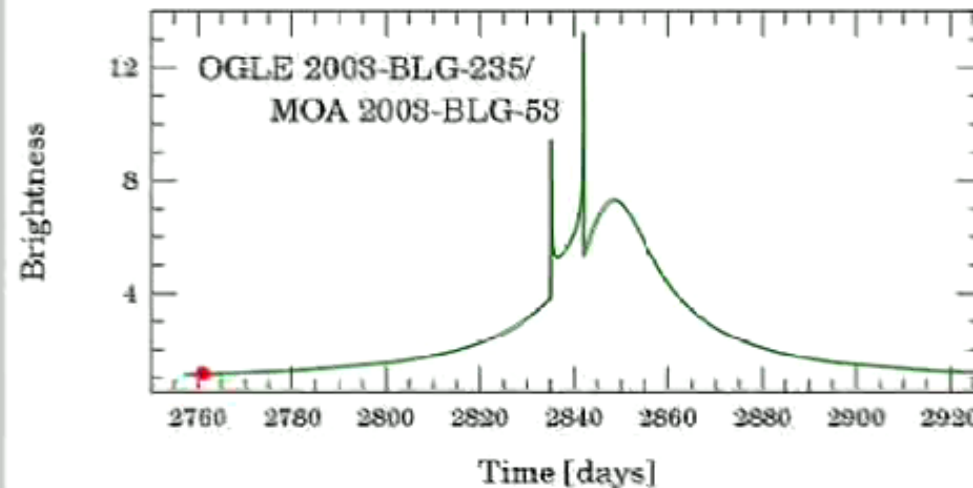
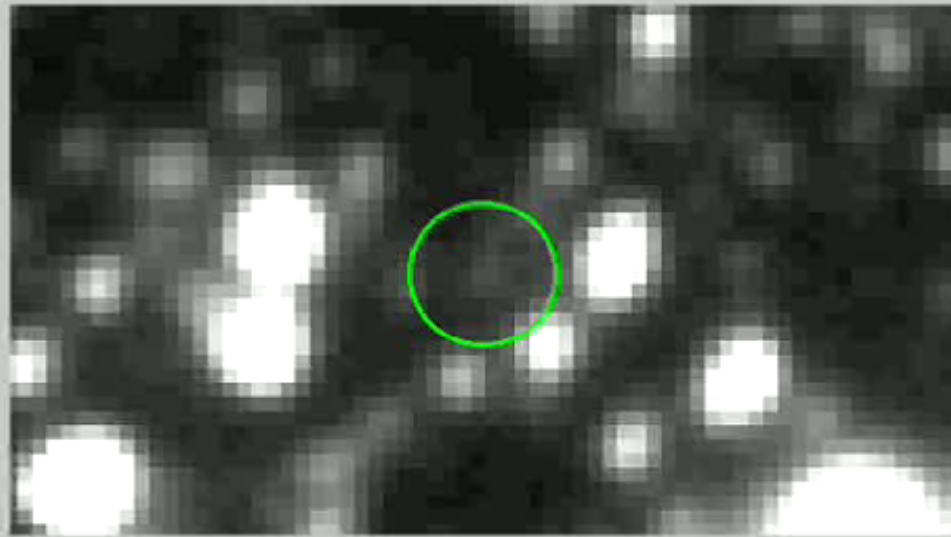
# Microlensing Target Fields are in the Galactic Bulge



**10s of millions of stars in the Galactic bulge in order to detect planetary companions to stars in the Galactic disk and bulge.**

# Simulated Lightcurve of 1st Planetary Event

Simulated version  
of actual data



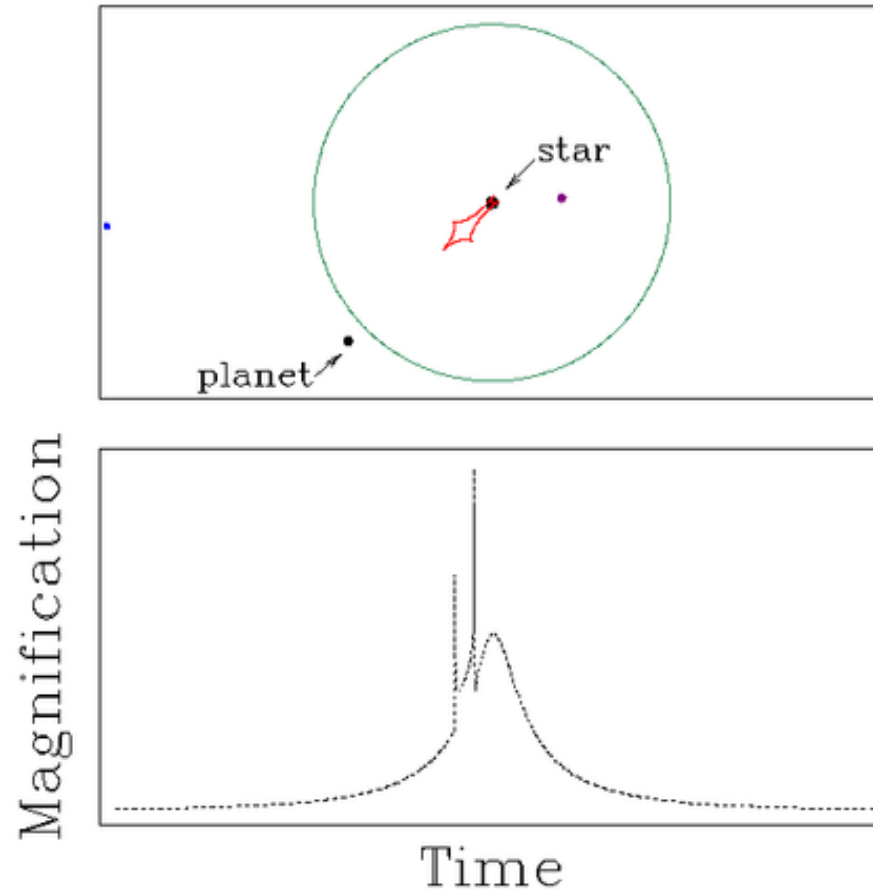
Best fit light curve simulated on an OGLE image



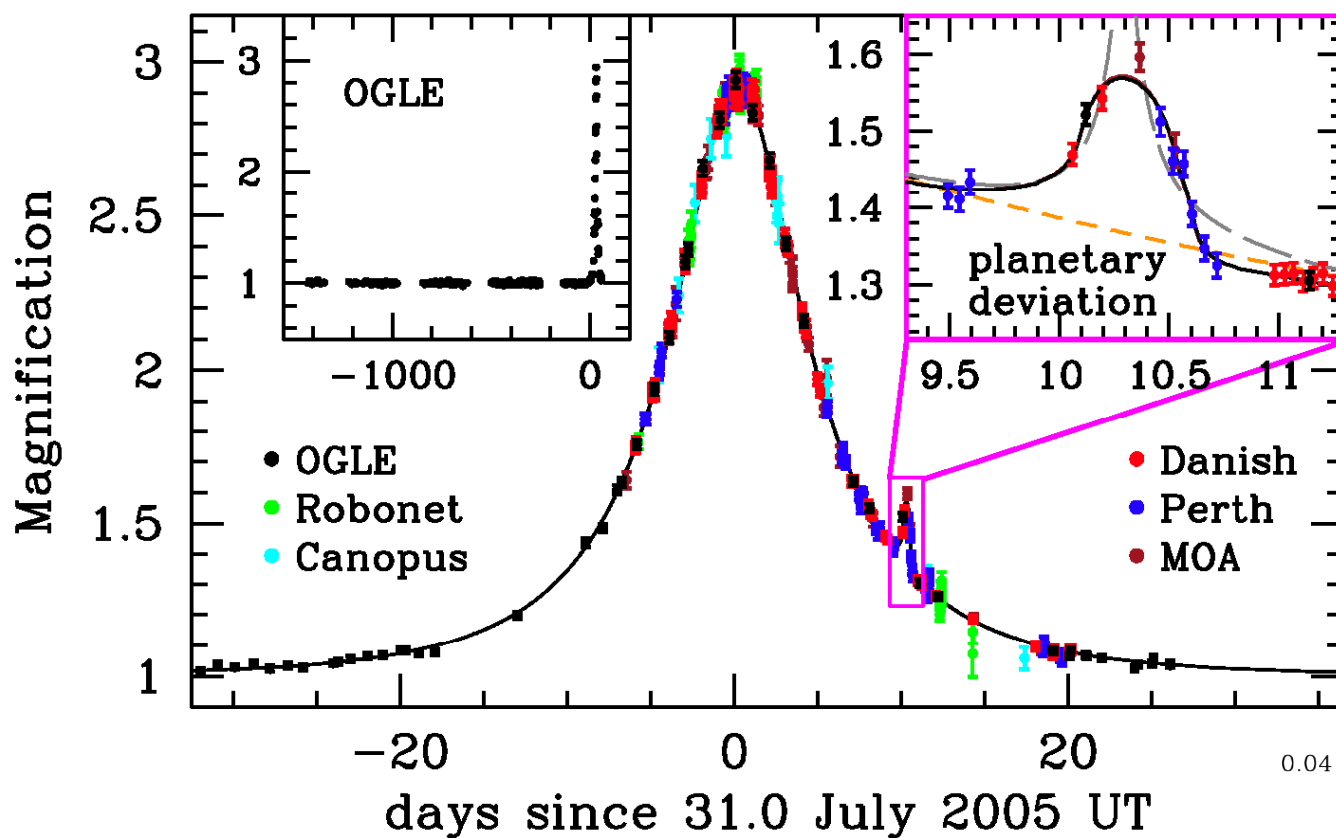
# Lensed images at $\mu\text{arcsec}$ resolution

View from telescope

A planet can be discovered when one of the lensed images approaches its projected position.



# OGLE-2005-BLG-390Lb - “lowest” mass exoplanet

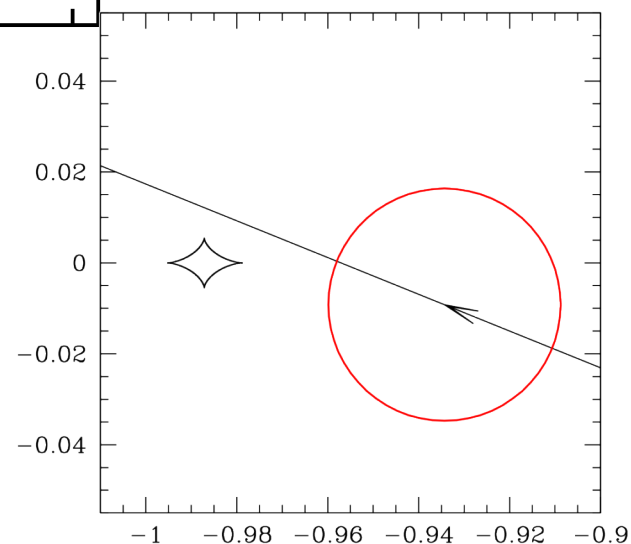


A  $5.5 M_{\oplus}$  planet discovered by microlensing: OGLE-2005-BLG-390Lb. The lowest mass planet discovered when announced in 2006.

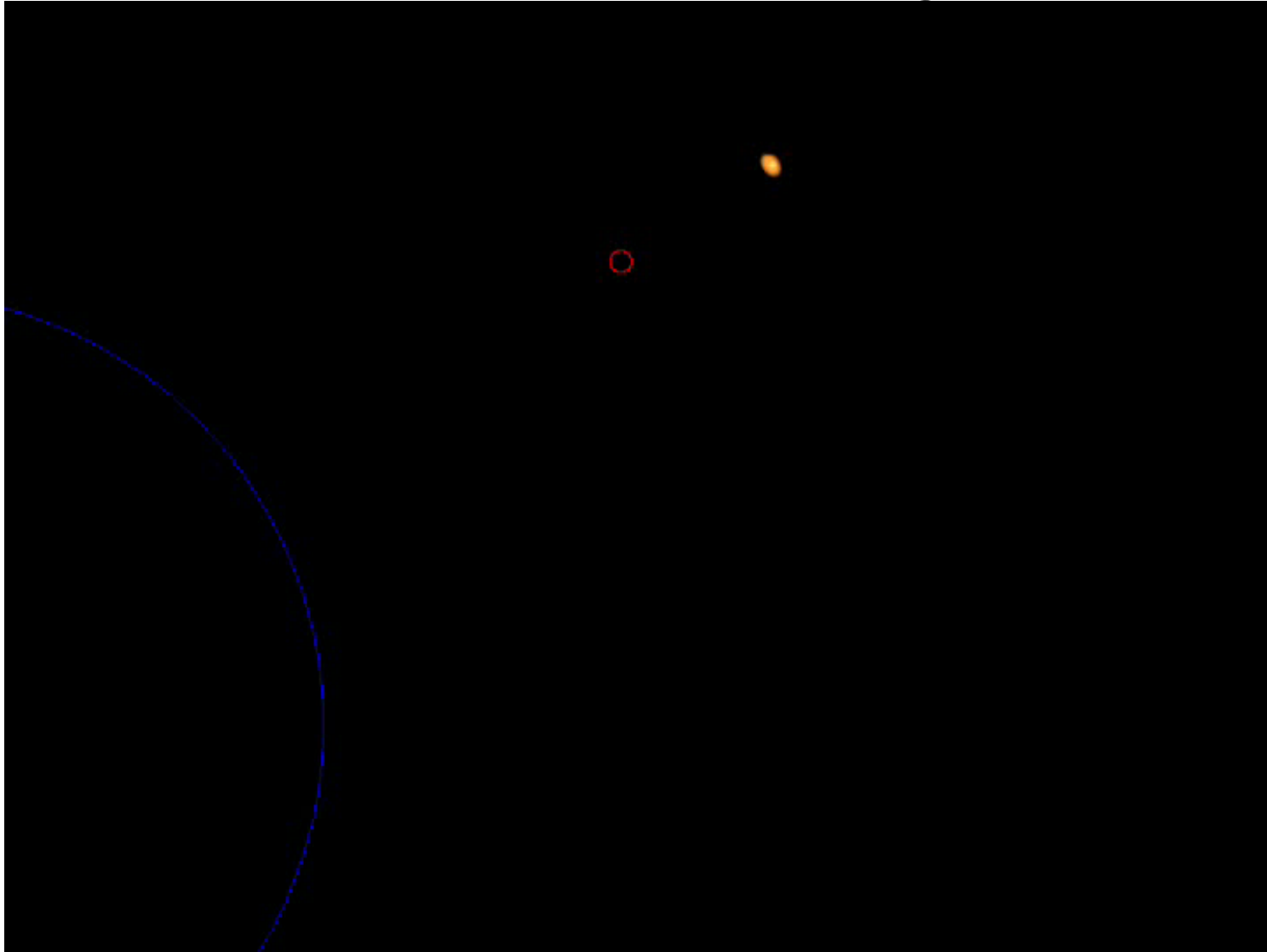
Source passes over caustic => significant finite source effect and clear measurement of  $t_*$

Giant source star means lens star detection will be difficult

PLANET, OGLE & MOA Collaborations

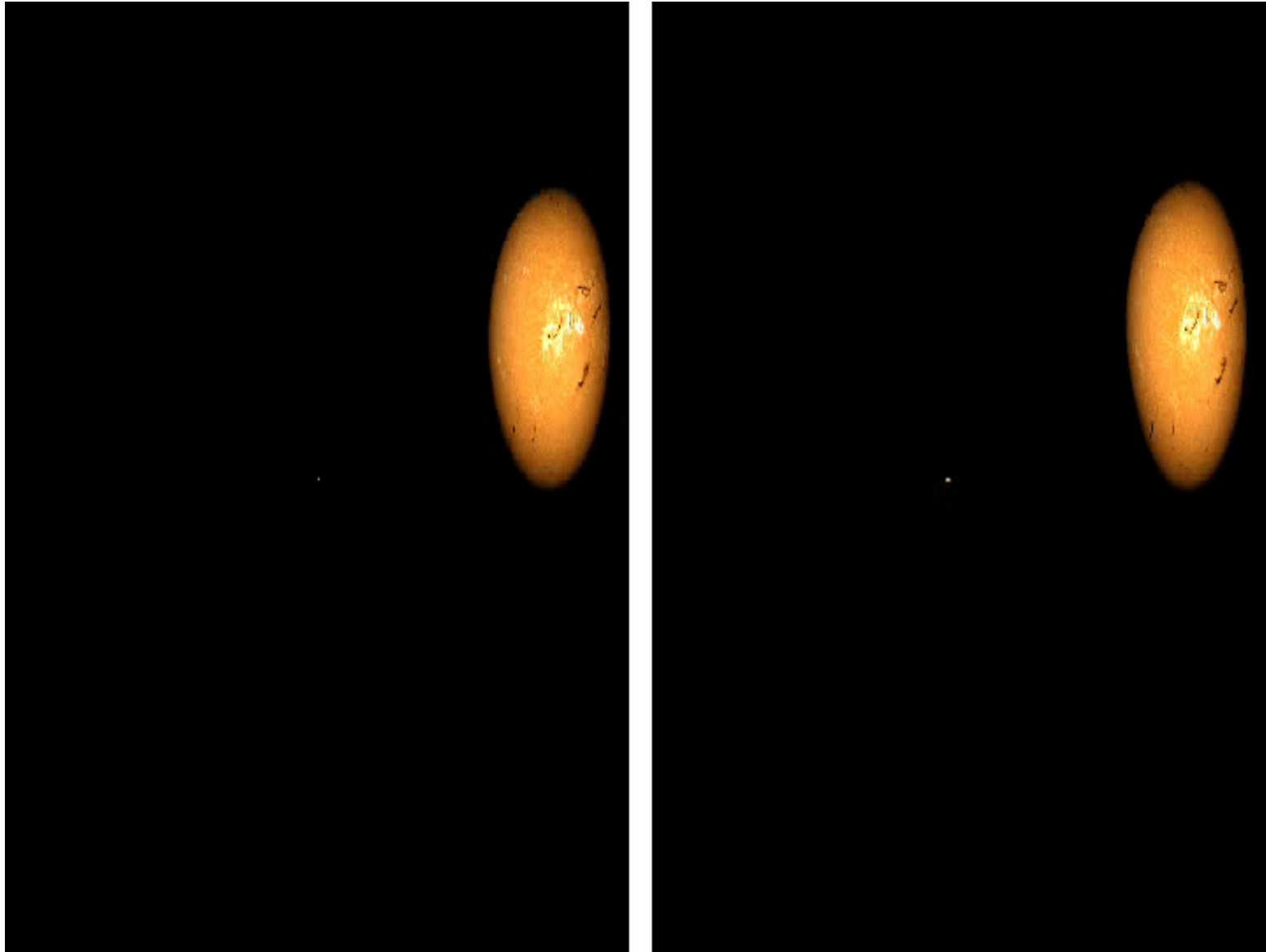


# OGLE-2005-BLG-390Lb at high resolution



- Simulated view from 10,000 km aperture space telescope
- H- $\alpha$  filter Solar images generate cool videos!

# OGLE-2005-BLG-390Lb at high resolution

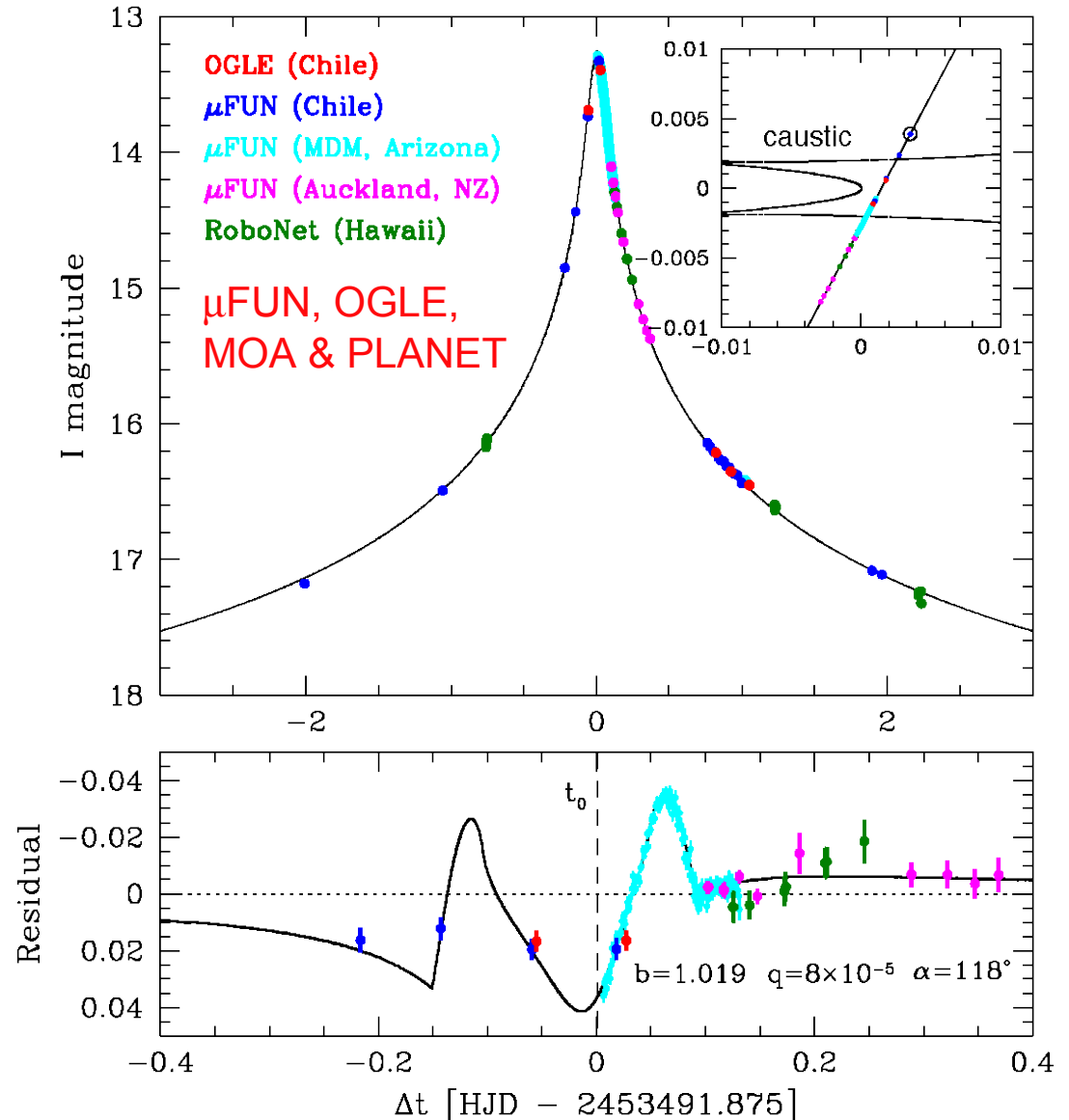


5.5 Earth-mass planet vs. 16.5 Earth-mass planet.

Only the total image area is observable. 5.5 Earth-mass is near limit for giant source.

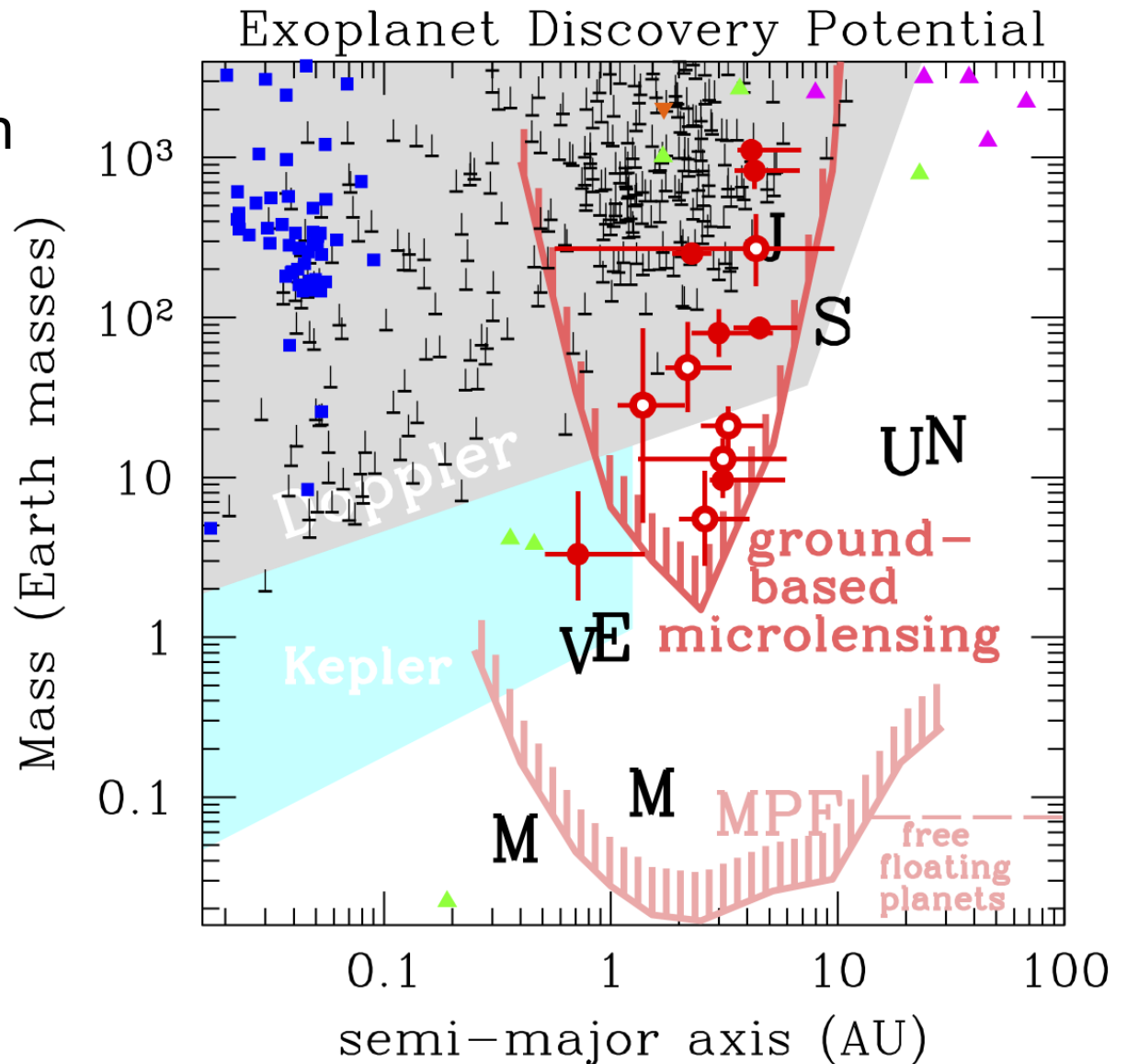
# OGLE-2005-BLG-169Lb

- Detection of a  $\sim 13 M_{\oplus}$  planet in a high magnification microlensing event
- Caustic crossing signal is obvious when light curve is divided by a single lens curve.
- Detection efficiency for  $\sim 10 M_{\oplus}$  planets is  $\ll$  than for Jupiter-mass planets
  - 2/4 microlensing planets are super-Earths ( $\sim 10 M_{\oplus}$ )
  - Super-Earths are much more common than Jupiters at 1-5 AU
  - $\sim 37\%$  of stars have super-Earths at 1.5-4.5 AU ( $> 16\%$  at 90% confidence)



# Microlensing Discoveries vs. Other Techniques

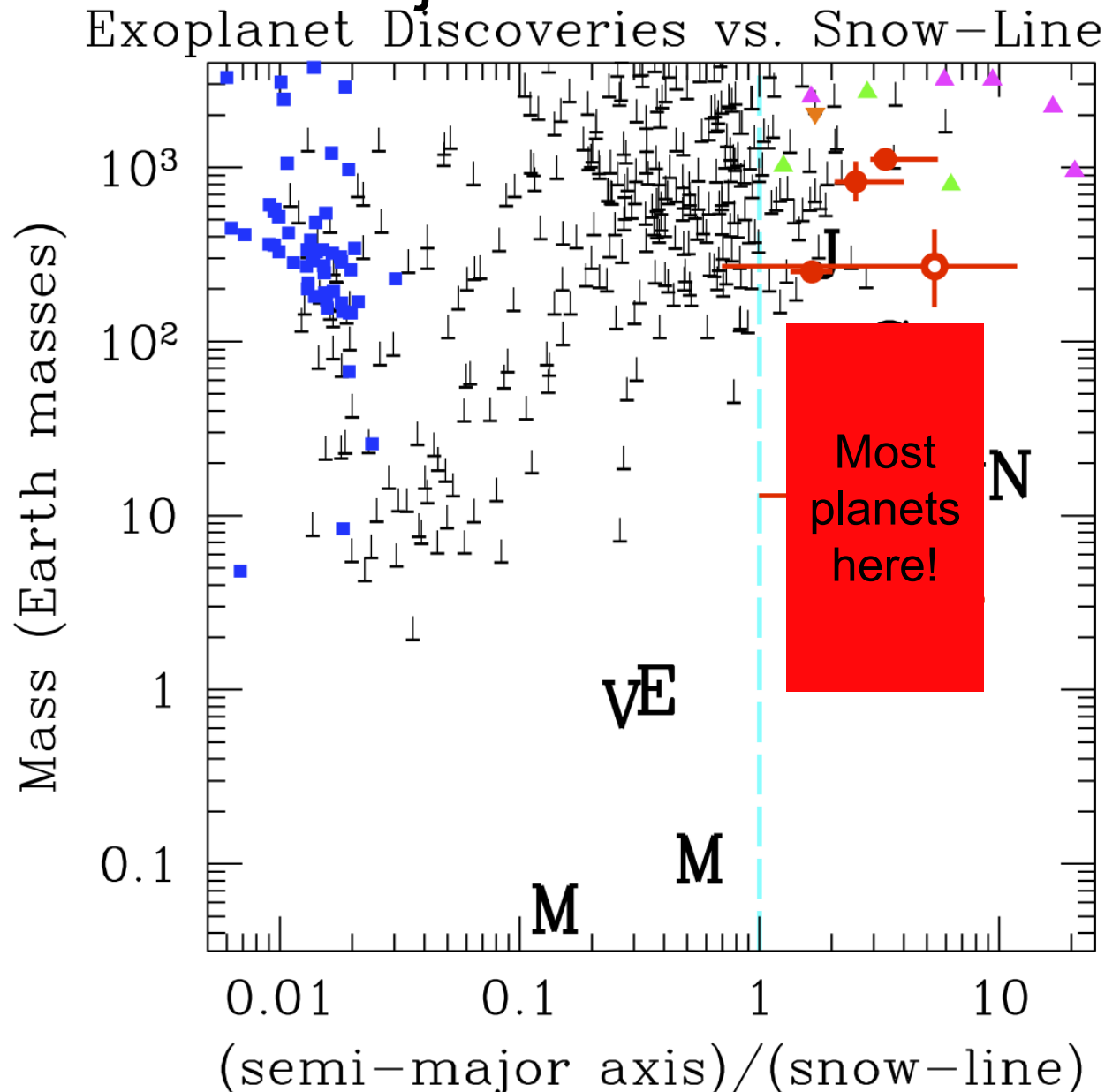
- Microlensing discoveries in **red**
- Doppler discoveries in **black**
- Transit discoveries shown as **blue squares**
- Direct detection, and timing are **magenta** and **green** triangles
- Microlensing opens a new window on exoplanets at 1-5 AU
  - Sensitivity approaching 1 Earth-mass



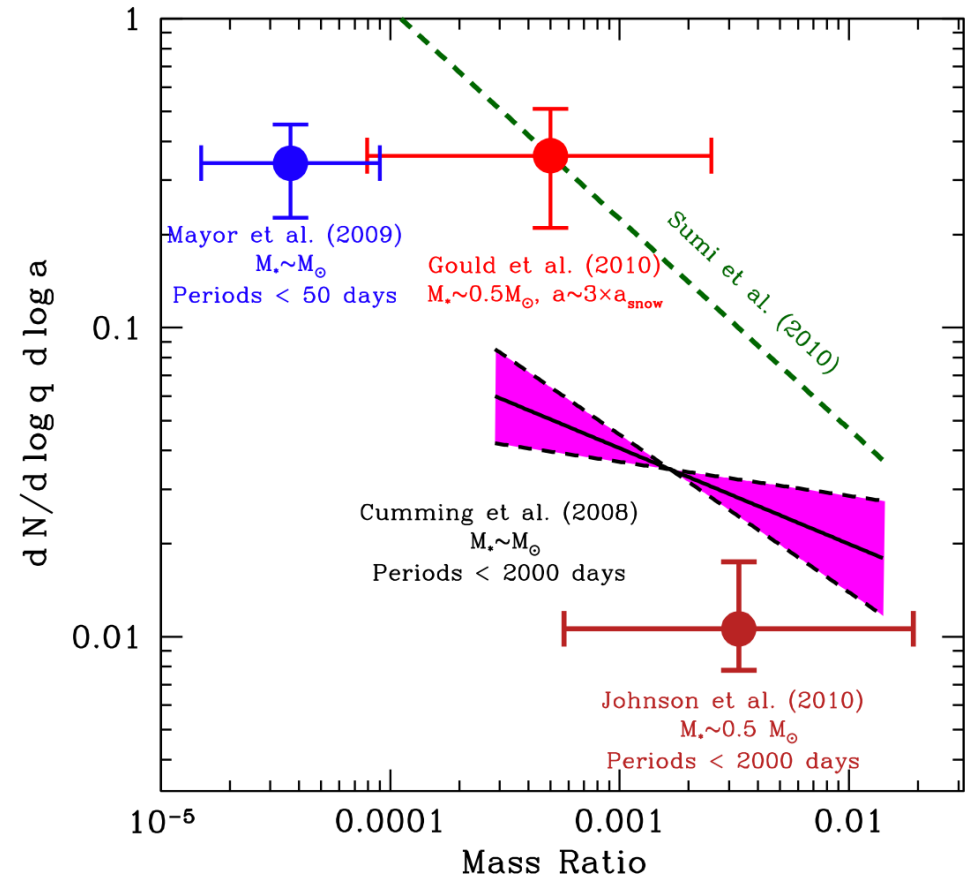
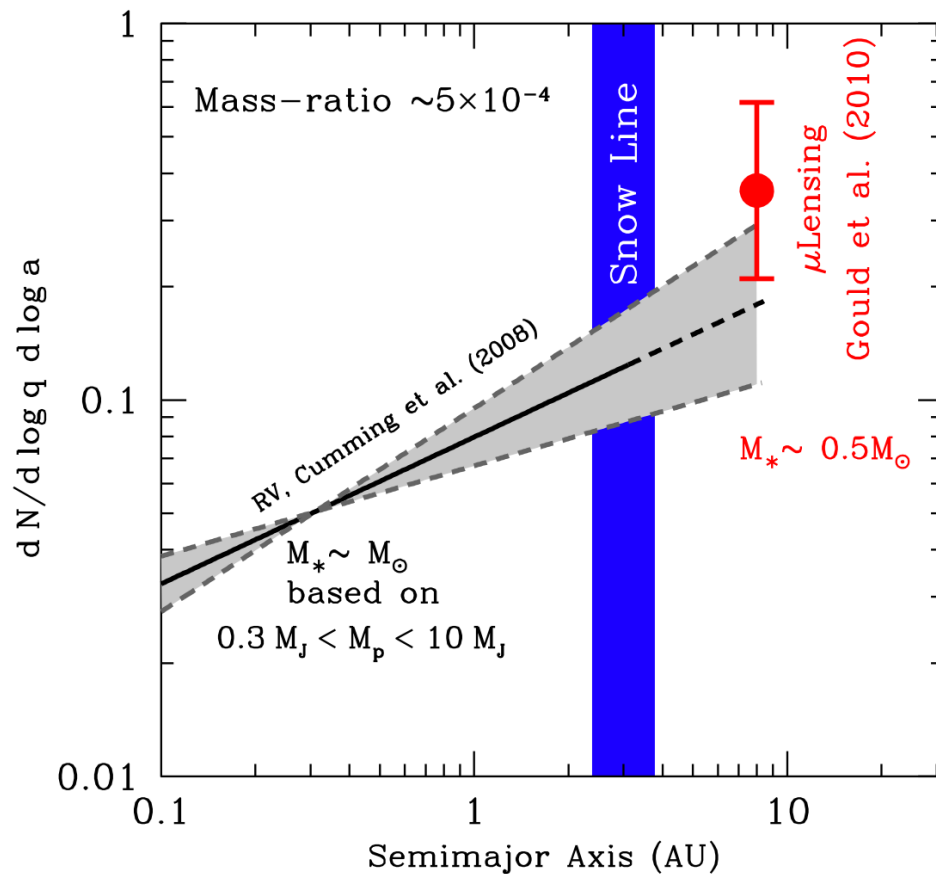


# Planet mass vs. semi-major axis/snow-line

- “snow-line” defined to be 2.7 AU ( $M/M_{\odot}$ )
  - since  $L \propto M^2$  during planet formation
- Microlensing discoveries in **red**.
- Doppler discoveries in black
- Transit discoveries shown as **blue circles**
- Super-Earth planets beyond the snow-line appear to be the most common type yet discovered



# Comparison of Statistical Results



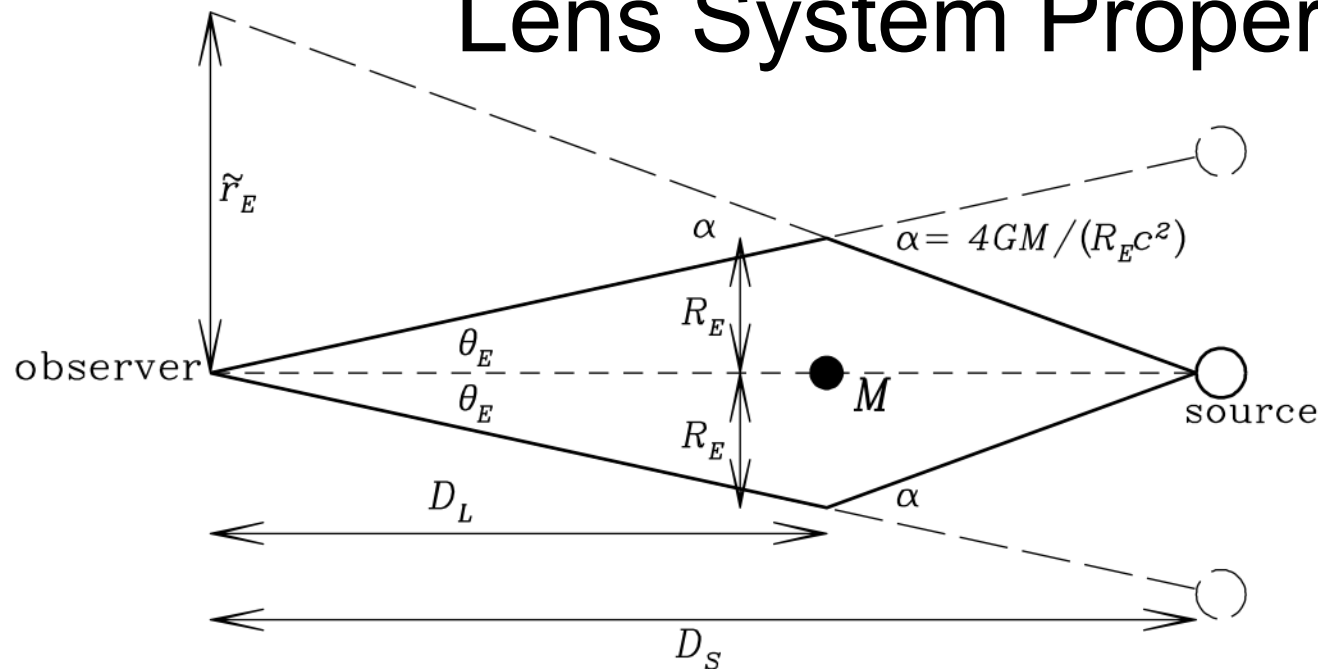
Sumi et al. (2010) :  $dN_p/d(\log q) \sim q^{-0.7}$

Gould et al. (2010) :  $d^2N/d(\log q) d(\log a) = 0.36 \pm 0.15$   
for  $M \approx 0.5 M_\odot$  and  $q \approx 5 \times 10^{-4}$

# Lens System Properties

- For a single lens event, 3 parameters (lens mass, distance, and velocity) are constrained by the Einstein radius crossing time,  $t_E$
- There are two ways to improve upon this with light curve data:
  - Determine the angular Einstein radius :  $\theta_E = \theta_* t_E / t_* = t_E \mu_{\text{rel}}$  where  $\theta_*$  is the angular radius of the star and  $\mu_{\text{rel}}$  is the relative lens-source proper motion
  - Measure the projected Einstein radius,  $\tilde{r}_E$  , with the microlensing parallax effect (due to Earth's orbital motion).

# Lens System Properties



- Einstein radius :  $P_E = \theta_* t_E / t_*$  and projected Einstein radius,  $\tilde{r}_E$ 
  - $t_*$  = the angular radius of the star
  - $\tilde{r}_E$  from the microlensing parallax effect (due to Earth's orbital motion).

$$R_E = \theta_E D_L, \text{ so } \alpha = \frac{\tilde{r}_E}{D_L} = \frac{4GM}{c^2 \theta_E D_L}. \text{ Hence } M = \frac{c^2}{4G} \theta_E \tilde{r}_E$$

# Finite Source Effects & Microlensing Parallax Yield Lens System Mass

- If only  $\theta_E$  or  $\tilde{r}_E$  is measured, then we have a mass-distance relation.
- Such a relation can be solved if we detect the lens star and use a mass-luminosity relation
  - This requires HST or ground-based adaptive optics
- With  $\theta_E$ ,  $\tilde{r}_E$ , and lens star brightness, we have more constraints than parameters

mass-distance relations:

$$M_L = \frac{c^2}{4G} \theta_E^2 \frac{D_S D_L}{D_S - D_L}$$

$$M_L = \frac{c^2}{4G} \tilde{r}_E^2 \frac{D_S - D_L}{D_S D_L}$$

$$M_L = \frac{c^2}{4G} \tilde{r}_E \theta_E$$

# 3 Ways to Measure Microlensing Parallax

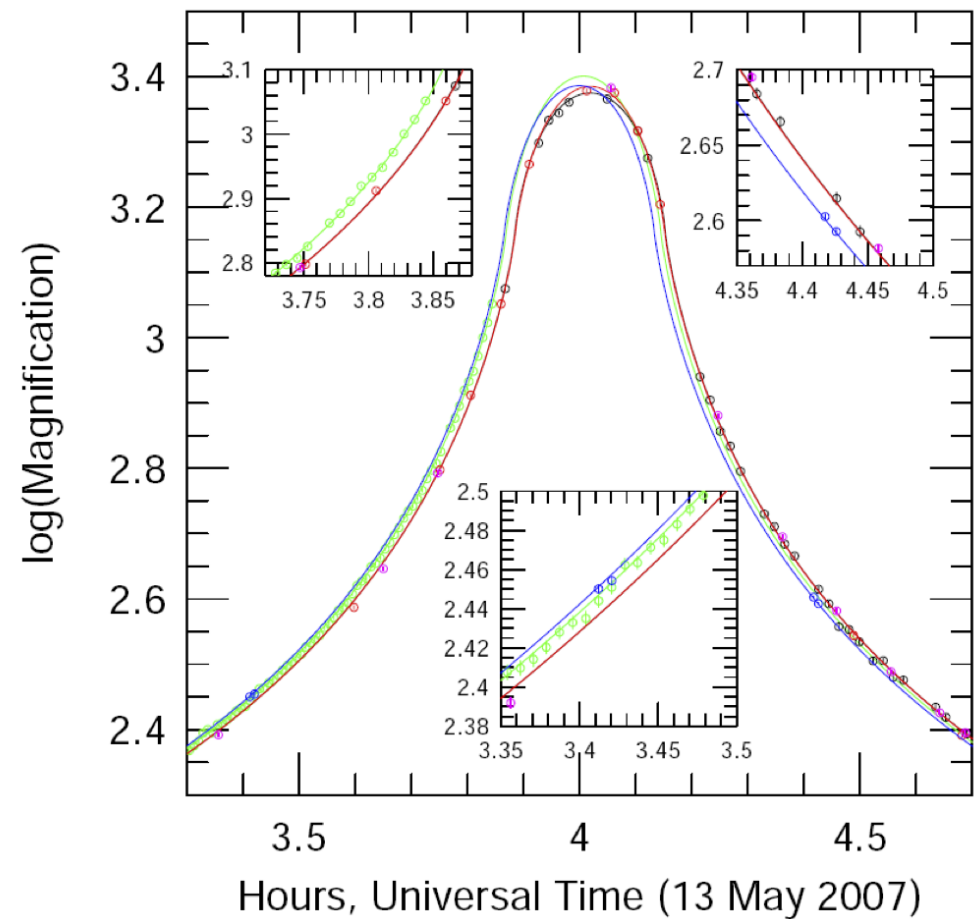
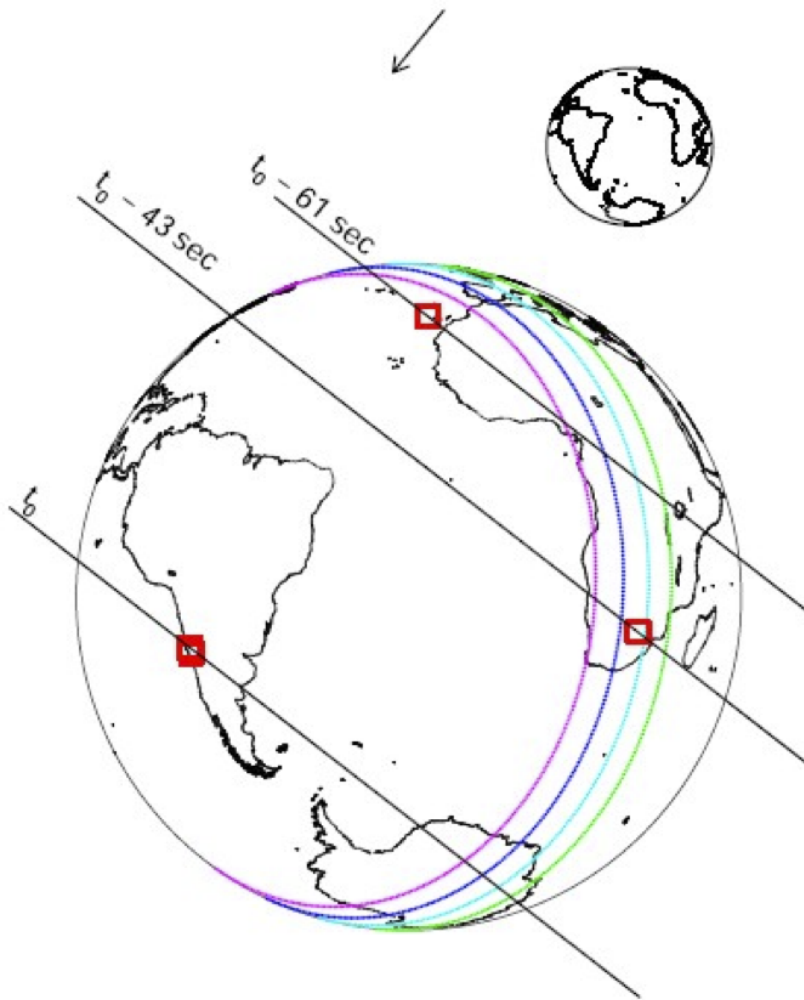
- Terrestrial - from different locations on the Earth
  - Requires very high magnification - rapid change in brightness
  - Measured for OGLE-2007-BLG-224 - disk brown dwarf
- Orbital motion of the Earth
  - Requires a long Einstein radius crossing time,  $t_E \geq 100$  days
  - Measurable for some lenses in the Galactic disk, but not in the Galactic bulge
- From a Satellite far from Earth
  - Solar System missions provide “opportunities”
    - Cassini (late 1990’s)
    - Deep Impact 2004 (proposal)
  - OGLE-2005-SMC-1 measured by Spitzer
  - MOA-2009-BLG-266 - first planetary microlensing event with extra-terrestrial observations - by EPOXI (formerly Deep Impact) in Oct., 2009.



# Terrestrial Microlensing Parallax

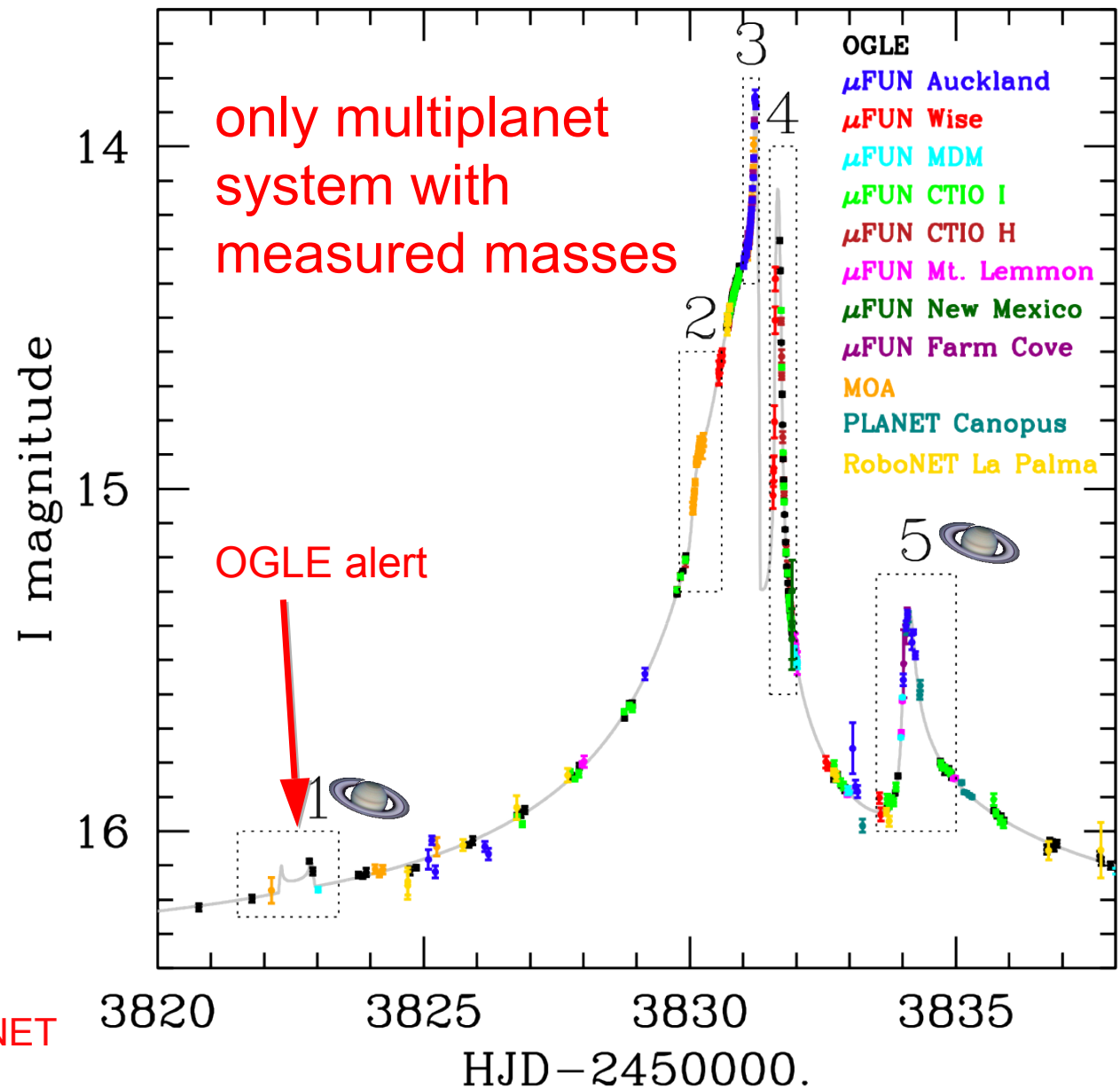
OGLE-2007-BLG-224

Canaries South Africa Chile



# Double-Planet Event: OGLE-2006-BLG-109

- 5 distinct planetary light curve features
- OGLE alerted 1<sup>st</sup> feature as potential planetary signal
- High magnification
- Feature #4 requires an additional planet
- Planetary signals visible for 11 days
- Features #1 & #5 require the orbital motion of the Saturn-mass planet

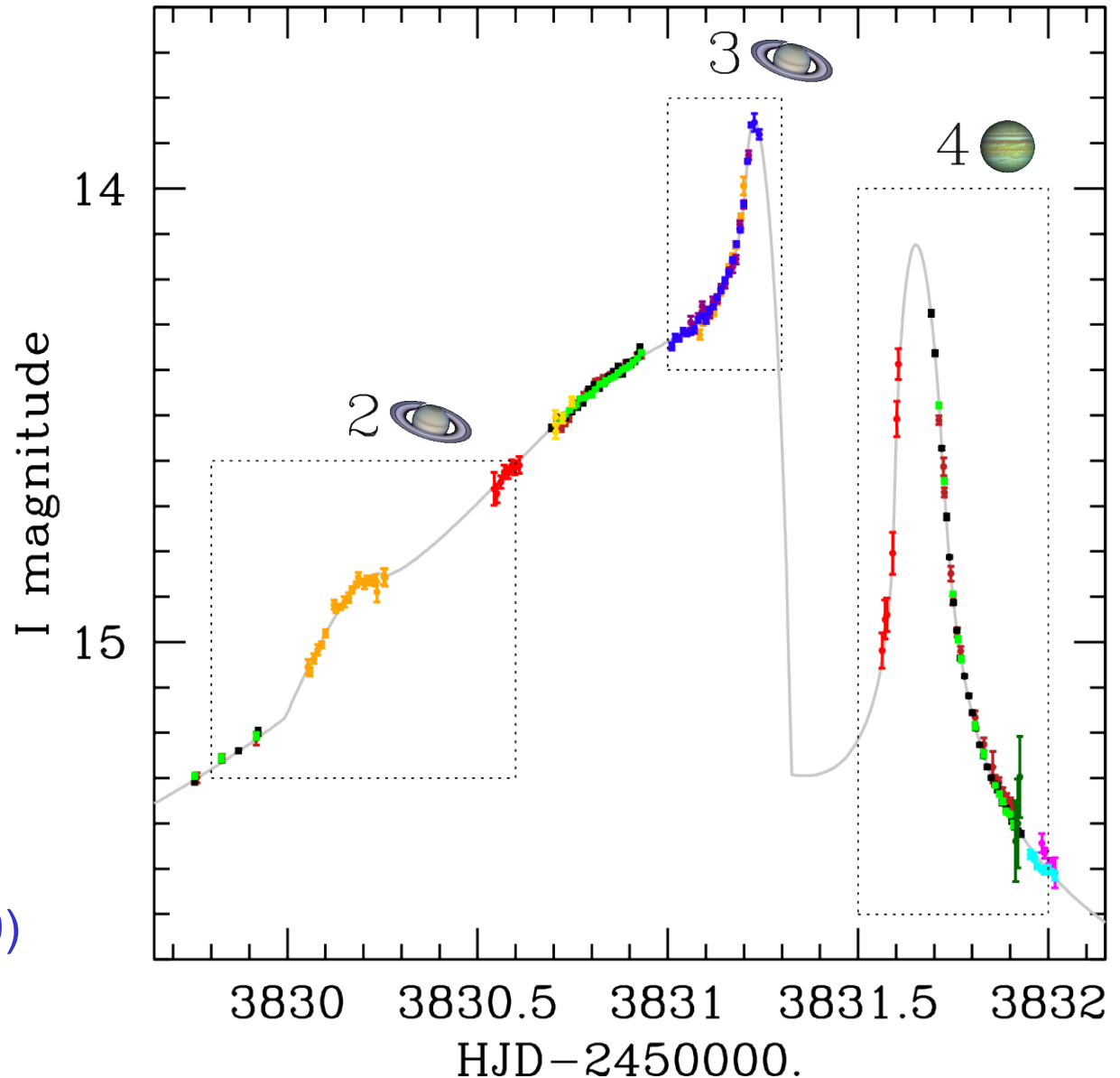


μFUN, OGLE, MOA & PLANET

# OGLE-2006-BLG-109 Light Curve Detail

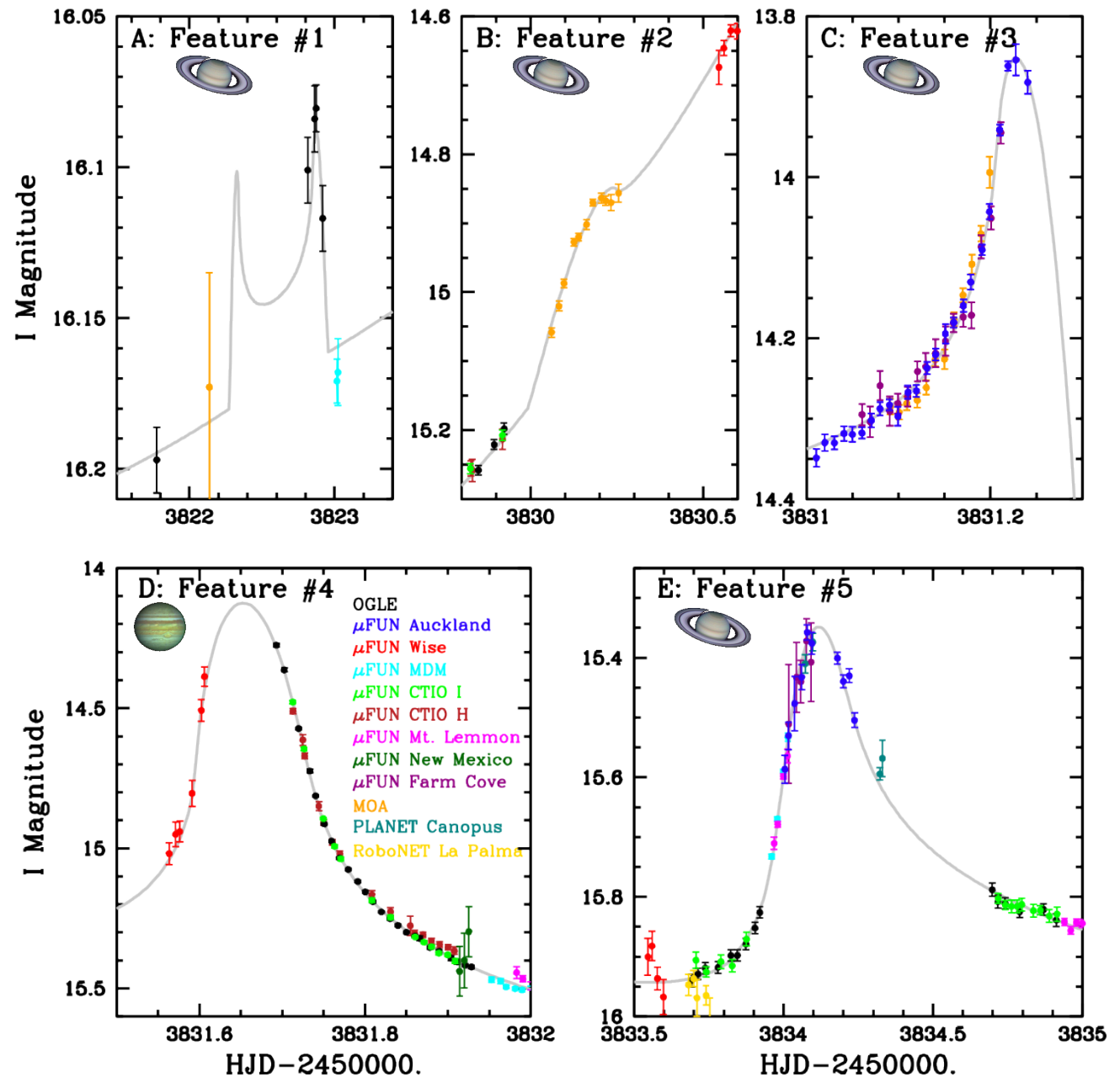
- OGLE alert on feature #1 as a potential planetary feature
- $\mu$ FUN (Gaudi) obtained a model approximately predicting features #3 & #5 prior to the peak
- But feature #4 was not predicted - because it is due to the Jupiter - not the Saturn

Gaudi et al (2008)  
Bennett et al (2010)

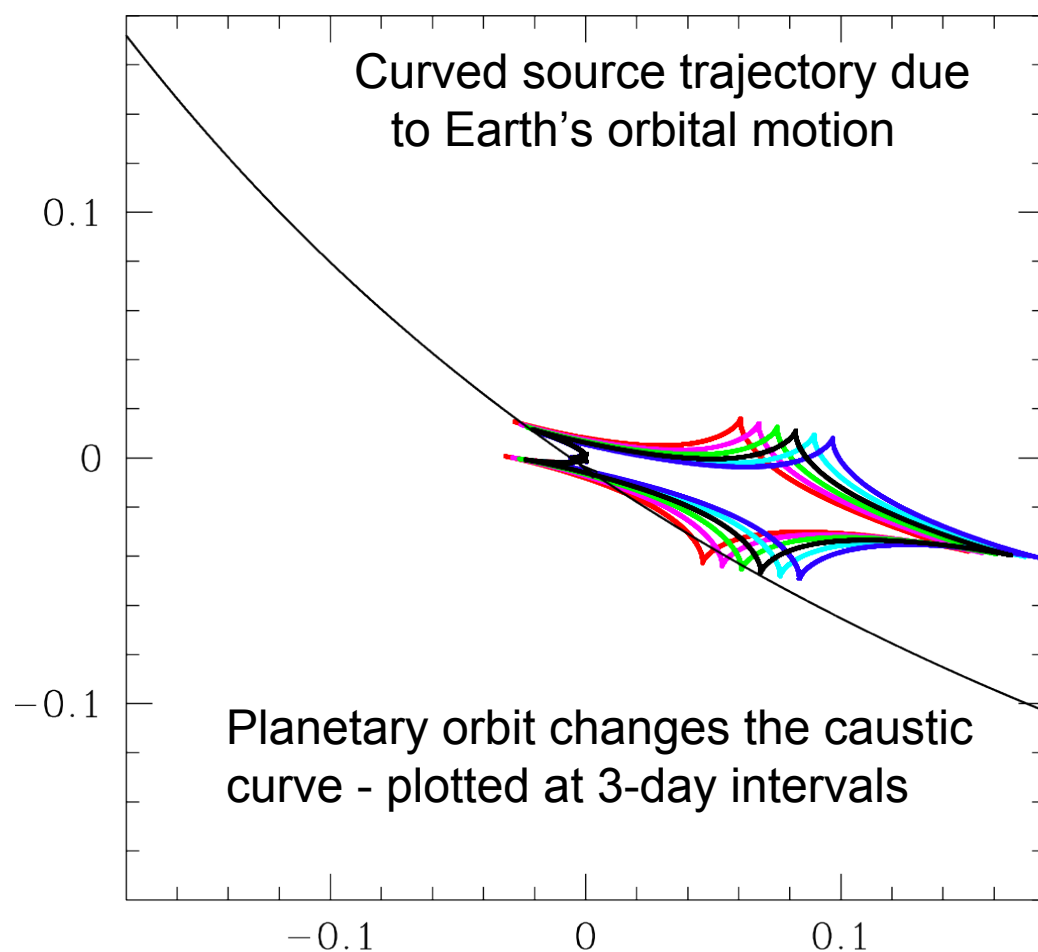


# OGLE-2006-BLG-109 Light Curve Features

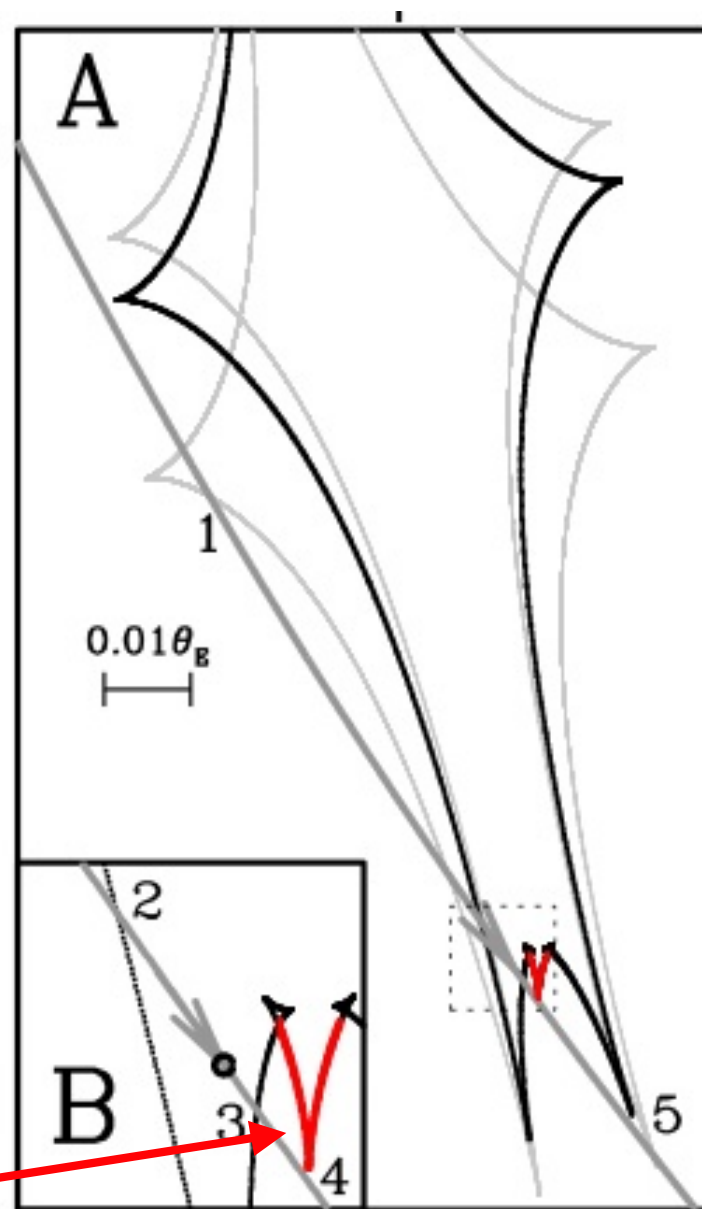
- The basic 2-planet nature of the event was identified during the event,
- But the final model required inclusion of orbital motion, microlensing parallax and computational improvements (by Bennett).



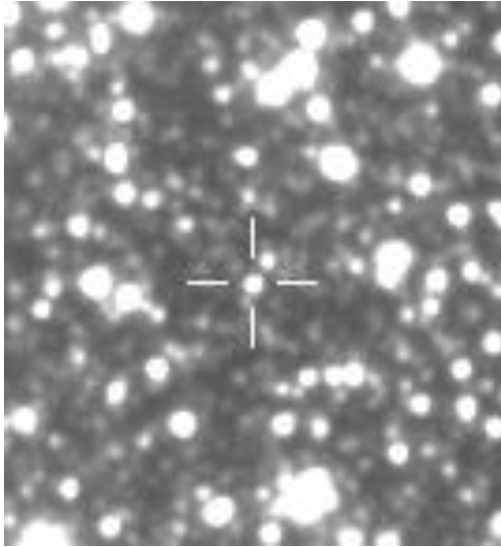
# OGLE-2006-BLG-109Lb,c Caustics



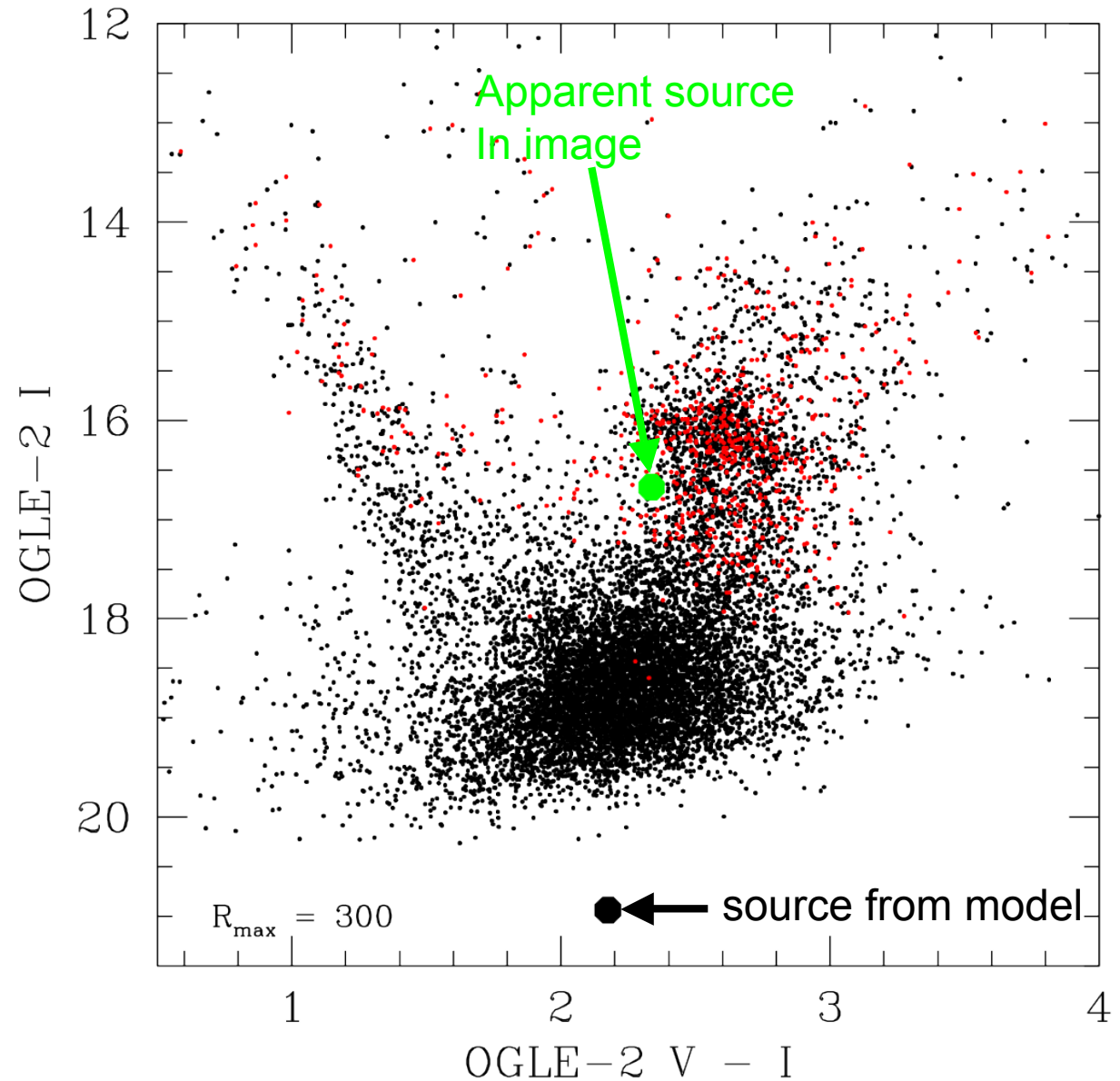
more analysis details later



# OGLE-2006-BLG-109 Source Star

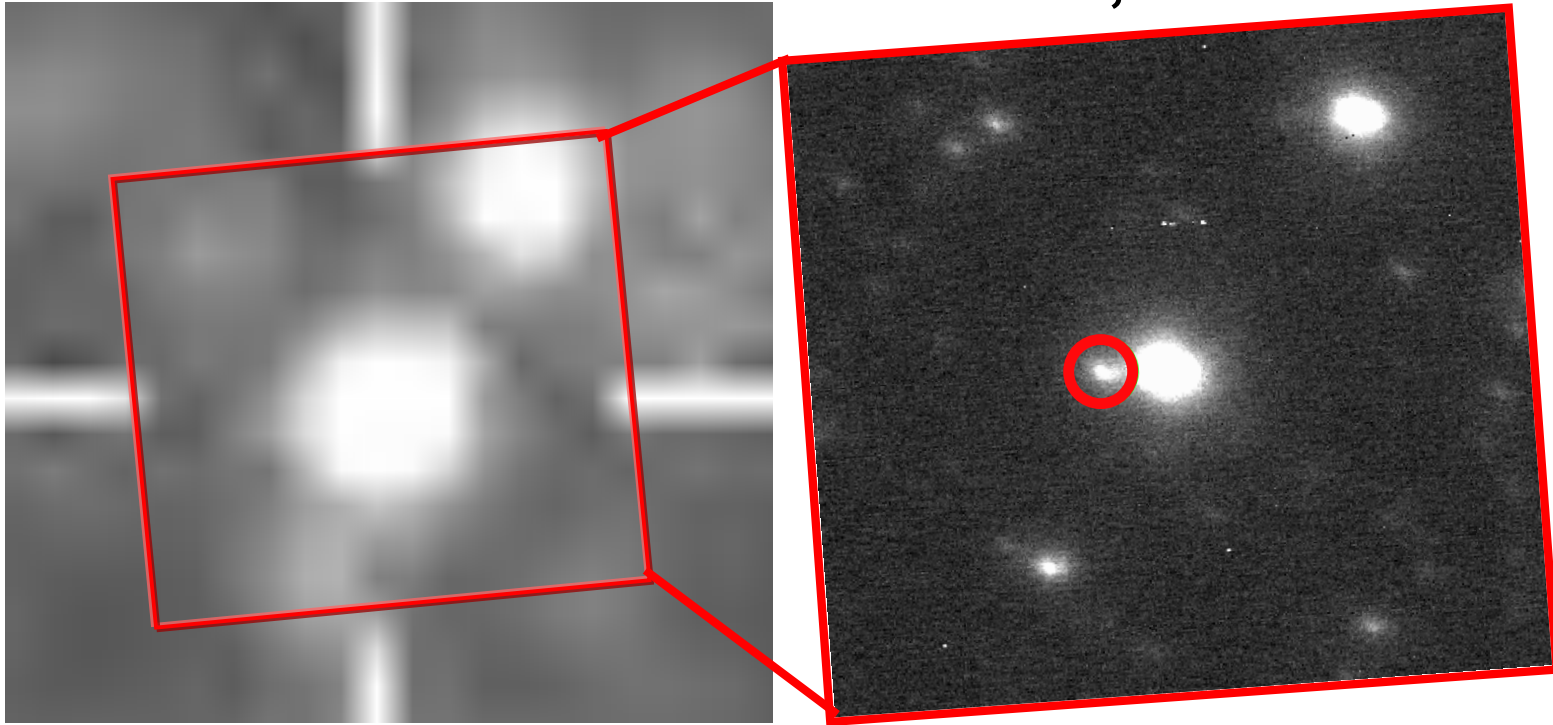


The model indicates that the source is much fainter than the apparent star at the position of the source. Could the brighter star be the lens star?





# OGLE-2006-BLG-109Lb,c Host Star



- OGLE images show that the source is offset from the bright star by 350 mas
- B. Macintosh: Keck AO images resolve lens+source stars from the brighter star.
- But, source+lens blend is  $6\times$  brighter than the source (from CTIO H-band light curve), so the lens star is  $5\times$  brighter than source.
  - H-band observations of the light curve are critical because the lens and source are not resolved
- Planet host (lens) star magnitude  $H \approx 17.17$ 
  - JHK observations will help to constrain the extinction toward the lens star

# Only Multiplanet System with Measured Masses

Host star mass:  $M_L = 0.52^{+0.18}_{-0.07} M_\odot$  from light curve model.

- Apply lens brightness constraint:  $H_L \approx 17.17$ .
- Correcting for extinction:  $H_{L0} = 16.93 \pm 0.25$ 
  - Extinction correction is based on  $H_L - K_L$  color
  - Error bar includes both extinction and photometric uncertainties
- Lens system distance:  $D_L = 1.54 \pm 0.13$  kpc

Host star mass:  $M_L = 0.51 \pm 0.05 M_\odot$  from light curve and lens H-magnitude.

Other parameter values:

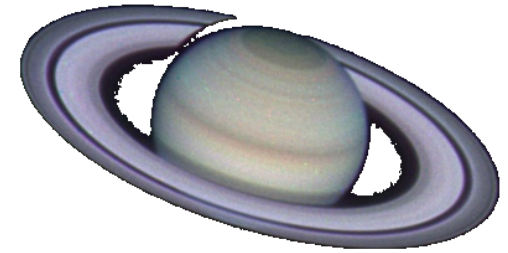
- “Jupiter” mass:  $m_b = 0.73 \pm 0.06 M_{\text{Jup}}$   
 semi-major axis:  $a_b = 2.3 \pm 0.5 \text{ AU}$
- “Saturn” mass:  $m_c = 0.27 \pm 0.03 M_{\text{Jup}} = 0.90 M_{\text{Sat}}$   
 semi-major axis:  $a_c = 4.5^{+2.2}_{-1.0} \text{ AU}$
- “Saturn” orbital velocity  $v_t = 9.5 \pm 0.5 \text{ km/sec}$   
 eccentricity  $\varepsilon = 0.15^{+0.17}_{-0.10}$   
 inclination  $i = 63 \pm 6^\circ$

# Orbital Motion Modeling

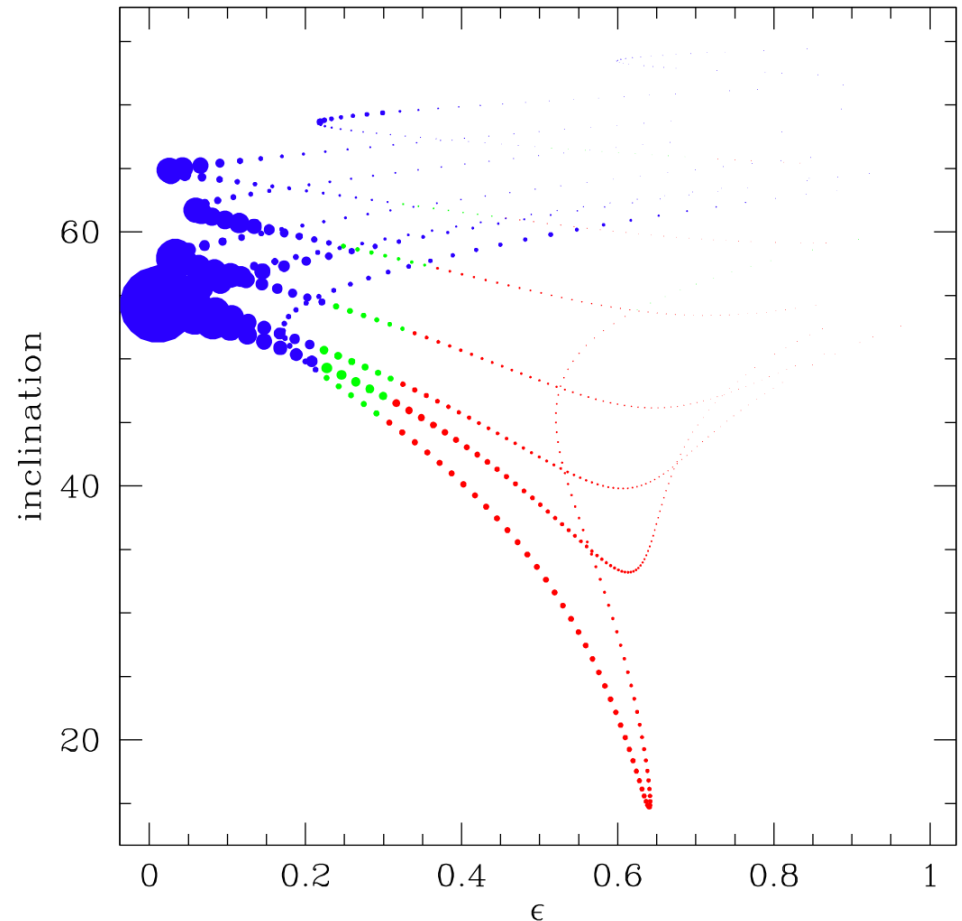


- 4 orbital parameters are well determined from the light curve
  - 2-d positions and velocities
  - Slight dependence on distance to the source star when converting to physical from Einstein Radii units
- Masses of the host star and planets are determined directly from the light curve
  - So a full orbit is described by 6 parameters (3 relative positions & 3 relative velocities)
  - A circular orbit is described by 5 parameters
- Models assume planetary circular motion
  - 2-d positions and velocities are well determined
  - Orbital period is constrained, but not fixed by the light curve
  - The orbital period parameter can be interpreted as acceleration or 3-d Star-Saturn distance (via  $a = GM/r^2$ )
- Details in Bennett et al (2010)

# Full Orbit Determination for OGLE-2006-BLG-109Lc



- Series of fits with fixed orbital acceleration (weight with fit  $\chi^2$ )
- Each fit corresponds to a 1-parameter family of orbits parameterized by  $v_z$ 
  - unless  $\frac{1}{2}(v_x^2 + v_y^2) - \frac{GM}{r} > 0$
- Assume the Jupiter orbits in the same plane and reject solutions **crossing** the Jupiter orbit or that are **Hill-unstable**
- Weight by prior probability of orbital parameters
  - planet is unlikely to be near periastron if  $\epsilon \gg 0$



Families of solutions corresponding to best models at various values of  $a$ .

# Full Orbit Determination for OGLE-2006-BLG-109Lc



- Full calculation using Markov chains run at fixed acceleration.
- Include only Hill-stable orbits
- results:

$$M_{LA} = 0.51 \pm 0.05 M_{\odot}$$

$$M_{Lc} = 0.27 \pm 0.03 M_J$$

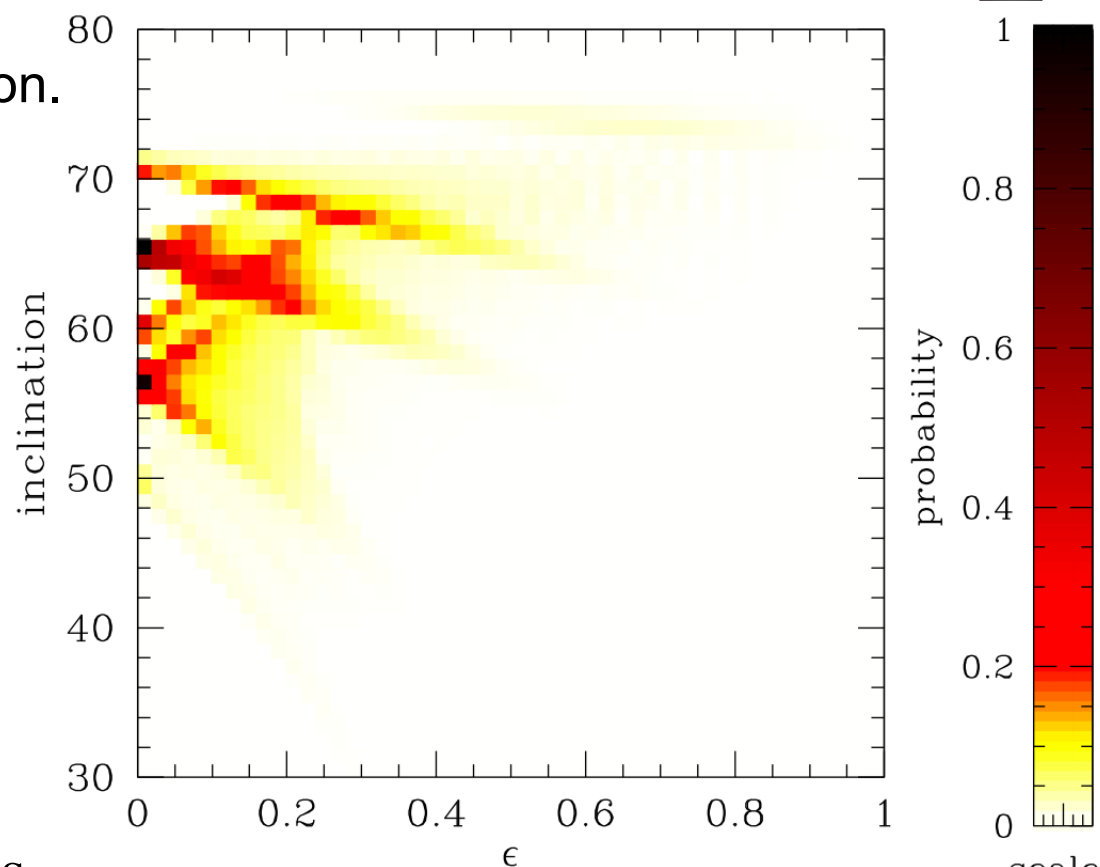
$$M_{Lb} = 0.73 \pm 0.07 M_J$$

$$a_{Lc} = 4.5^{+2.2}_{-1.0} \text{ AU}$$

$$a_{Lb} = 2.3 \pm 0.5 \text{ AU}$$

$$\text{inclination} = 64^{+4}_{-7} \text{ degrees}$$

$$\varepsilon = 0.15^{+0.17}_{-0.10}$$



- RV follow-up w/ 40m telescope  
-K = 19 m/sec (H = 17.2)

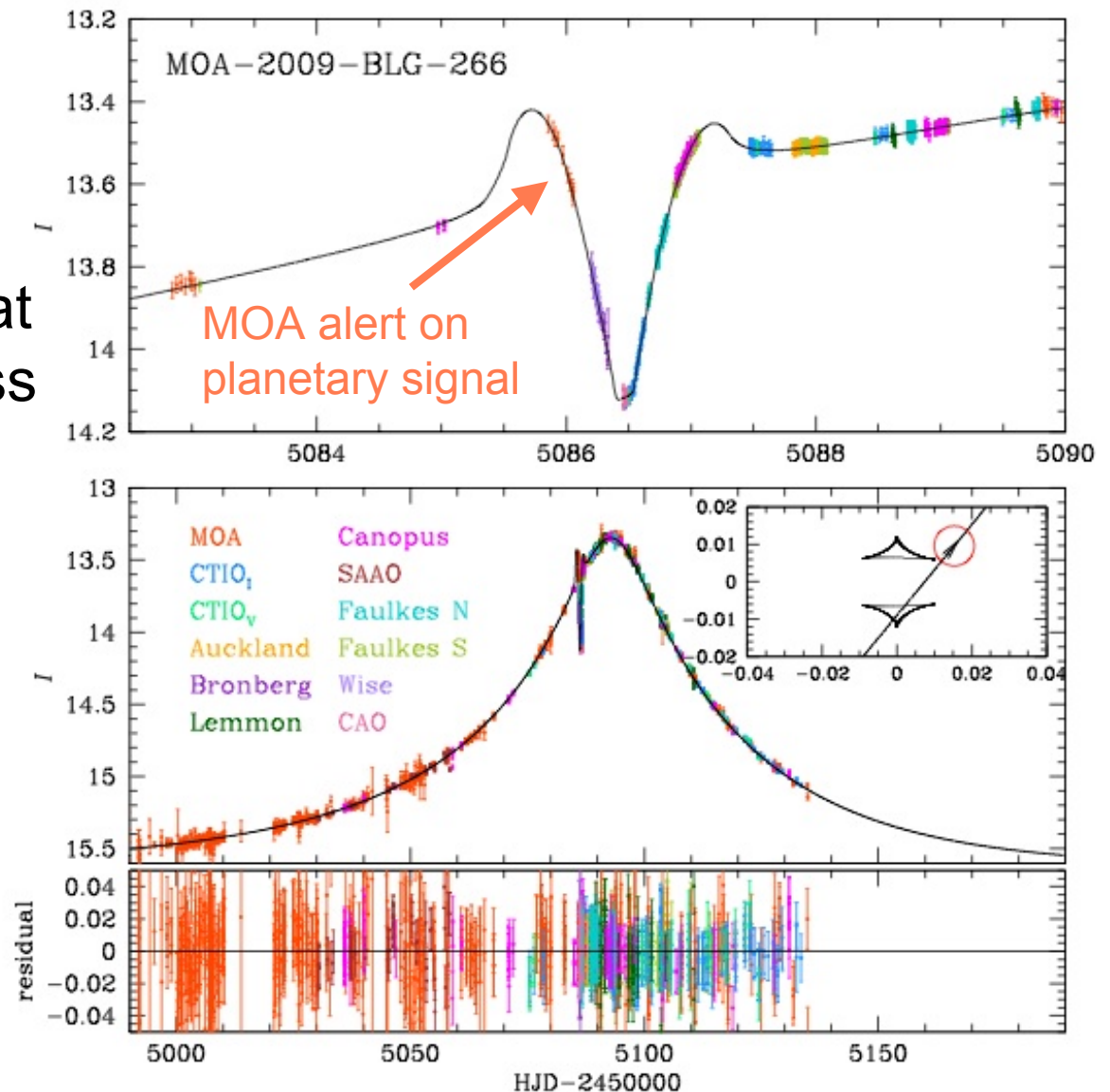
# OGLE-2006-BLG-Lb,c Discovery Implications

- OGLE-2006-BLG-109L is the first lens system with a Jovian Planet which has very high sensitivity to additional Saturn-mass planets
  - OGLE-2003-BLG-235 and OGLE-2005-BLG-71 had much lower magnification
  - OGLE-2005-BLG-169 had only a Neptune (or Super-earth)
- Jupiter + Saturn systems may be common among systems with gas-giant planets
  - Radial velocity planets 47 UMa & 14 Her are similar systems with more massive planets.



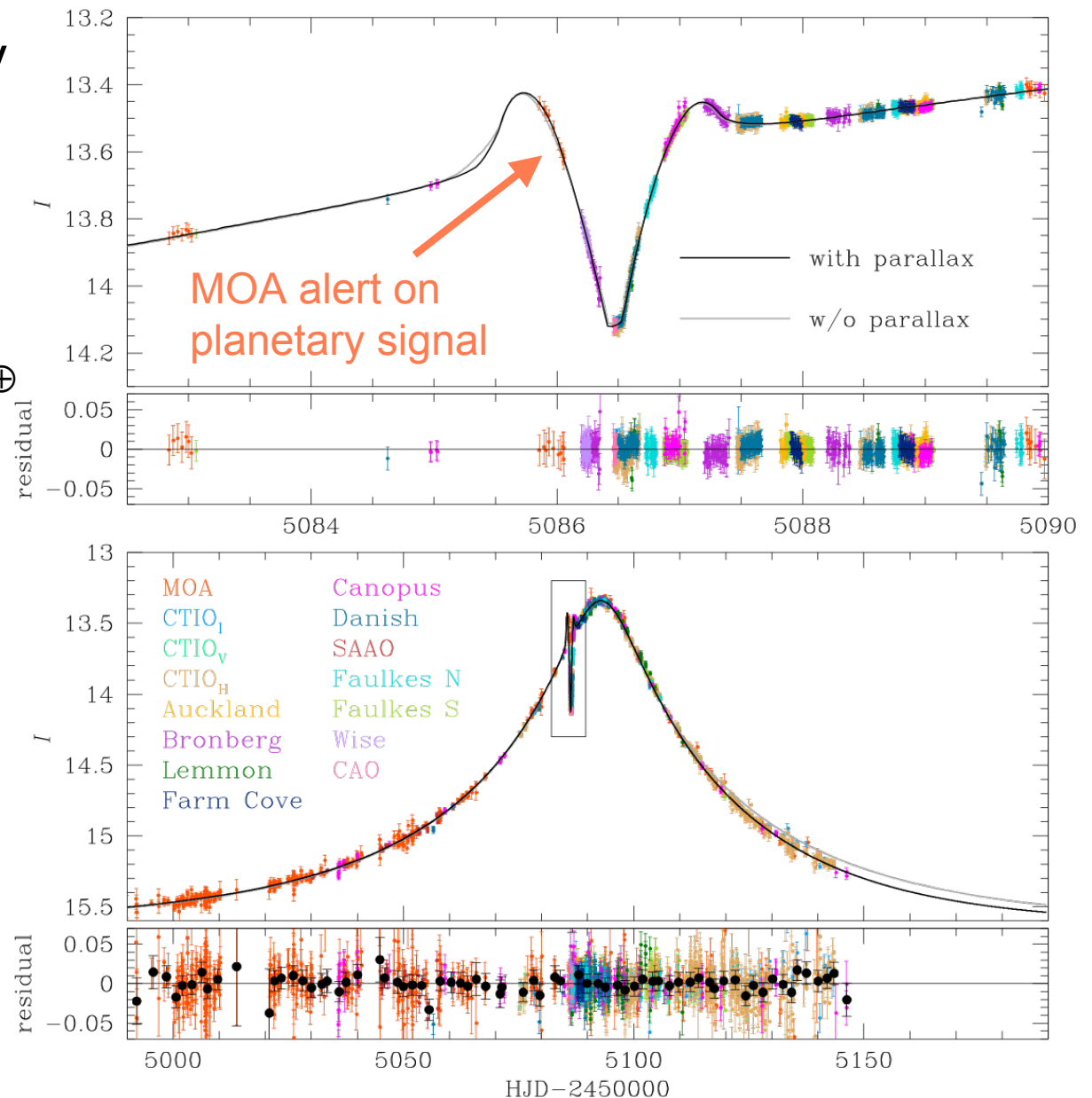
# Survey Discovery: MOA-2009-BLG-266

- Planet discovered by MOA on Sept. 11, 2009
- Lowest mass planet at  $> 0.05$  AU with a mass measurement  
 $\sim 10 M_{\oplus}$  at  $\sim 3$  AU
- Mass measurement from Deep Impact (now EPOXI) Spacecraft



# Survey Discovery: MOA-2009-BLG-266

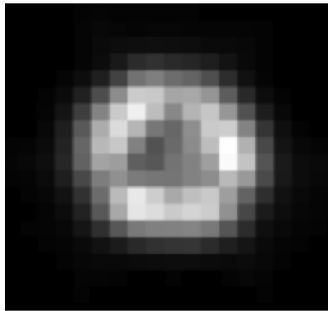
- Planet discovered by MOA on Sept. 11, 2009
- Low-mass planet
  - Probably  $\sim 10M_{\oplus}$
- Mass measurement from Deep Impact (now EPOXI) Spacecraft



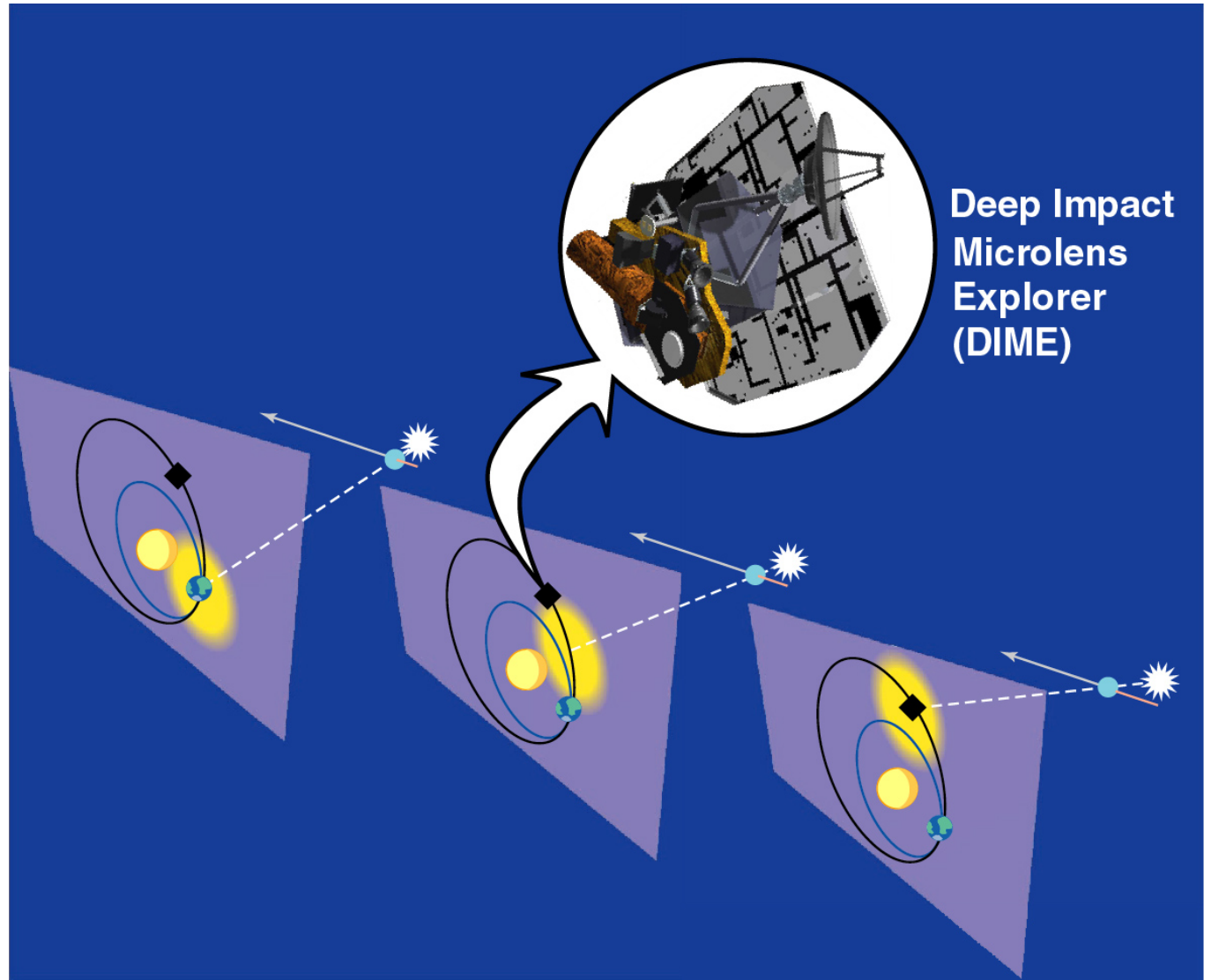
# Space-Based Microlensing Parallax

2004: study LMC  
microlensing w/ DI  
imaging (proposed)

2009: Geometric  
exoplanet and host  
star mass  
measurements  
with DI



EPOXI PSF!



Deep Impact  
Microlens  
Explorer  
(DIME)

observations in Oct. - see Andy Becker's talk

# Satellite Observations of Exoplanet Microlensing events

- Observe during host star lensing event
  - Targets are known only weeks to months before event is over
  - But most targets are within 5-10 degrees of the central Galactic bulge
  - Plan observations of a central bulge field, and update the coordinates just before the observations?
- Optimum Earth-satellite separation ~a few times smaller than Einstein Radius,  $R_E$ 
  - But depends on detailed characteristics of the event
- Different event classes
  - Long events - months
  - Short events - 1-2 weeks
- Targets are usually “faint”  $I \sim 13-20$ 
  - Long exposures, good pointing stability
  - Low precision photometry compared to transits

# Long Exoplanet Microlensing events

- Long events - months
  - Planetary host stars in the Galactic disk and/or have high mass
    - High mass means  $M > 0.3$  solar masses
  - Many have partial or full microlensing parallax measurements
  - Projected Einstein radius  $\sim 4$  AU
  - Satellite observations to remove degeneracies in modeling
  - MOA-2009-BLG-266 is an example
    - 3 kpc away
    - Host mass = 0.5 or 0.7 solar masses
  - Best observed by a satellite 0.5-2 AU from the Earth in projected separation
    - e.g. Cassini in 2016 or 2017
    - Mars missions

# Short Exoplanet Microlensing events

- Short events - 1-2 weeks
  - Host stars in the bulge and/or low mass ( $< 0.3$  solar masses)
  - No microlensing parallax data from the ground
  - Projected Einstein radius 10-30 AU
  - Best observed by a satellite at 2-15 AU in projected separation
    - e.g. Cassini in 2011-2015
  - Usually no signal from the ground
  - A few observations from a 2nd satellite are sometimes helpful

