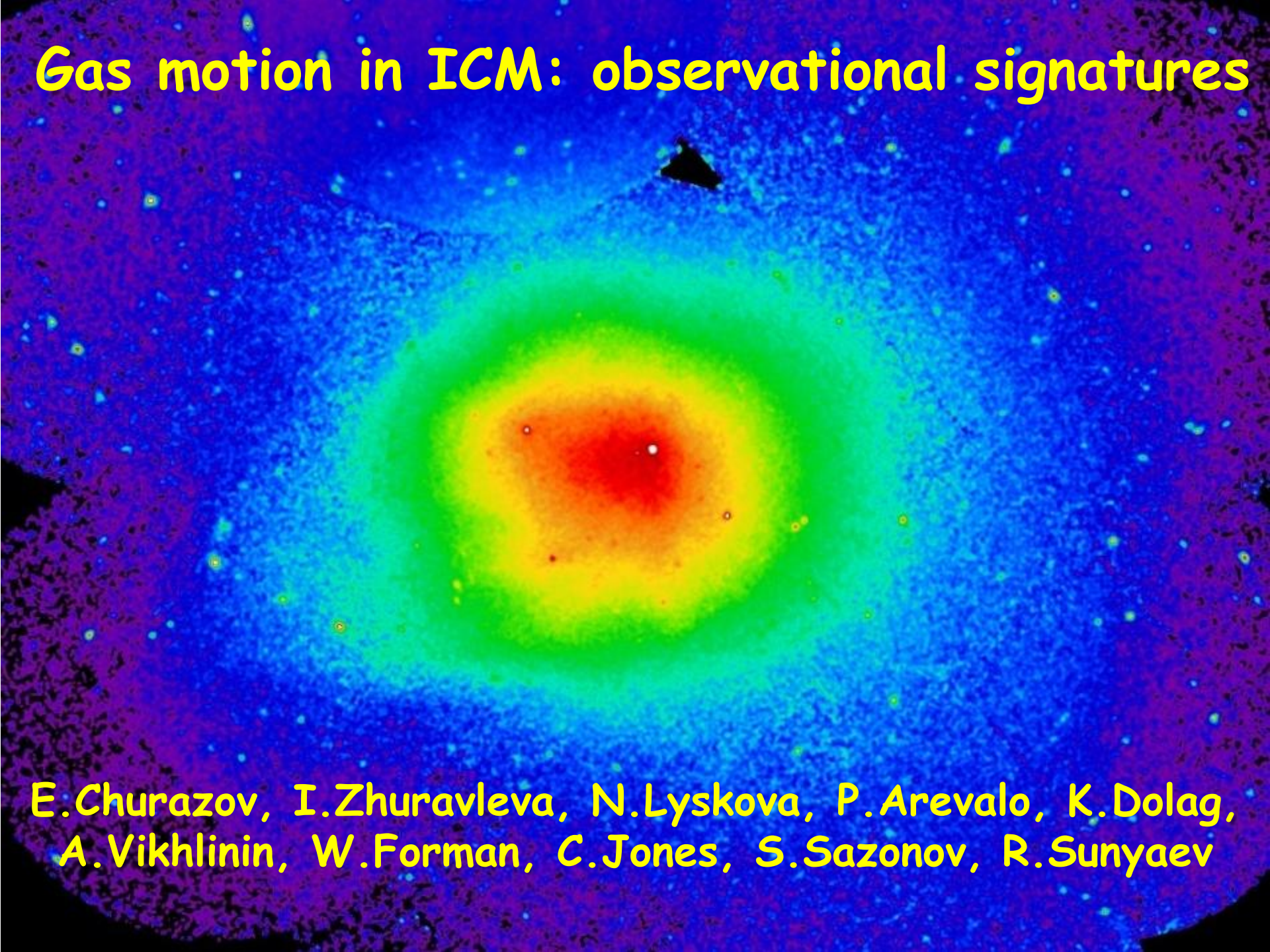


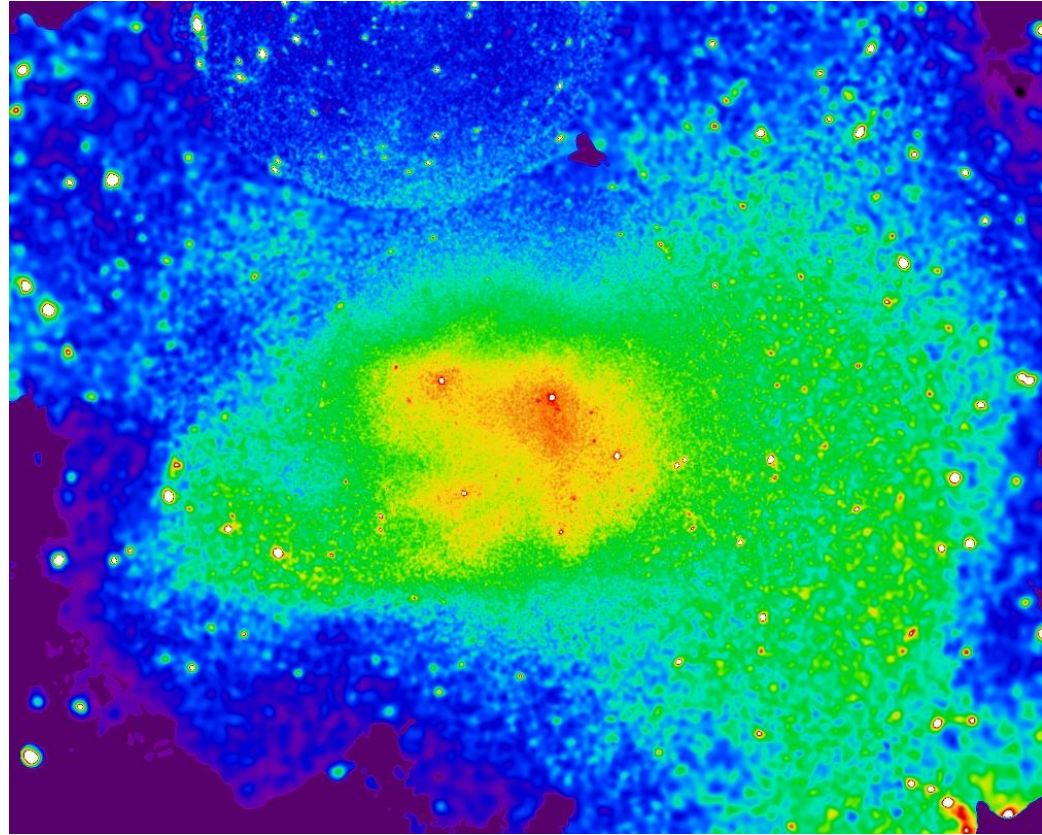
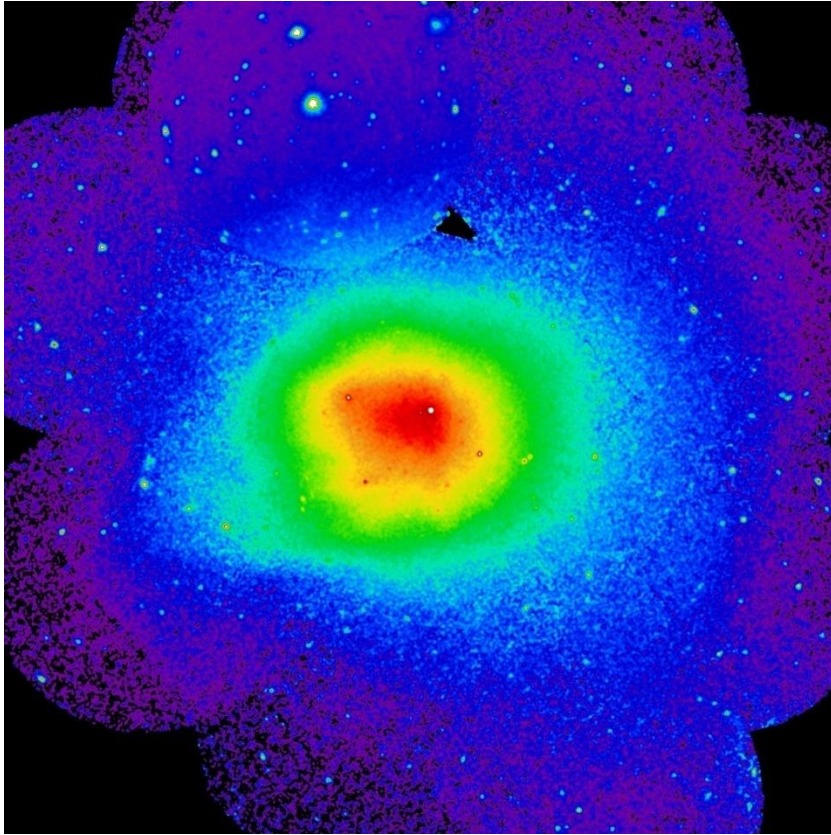
Gas motion in ICM: observational signatures



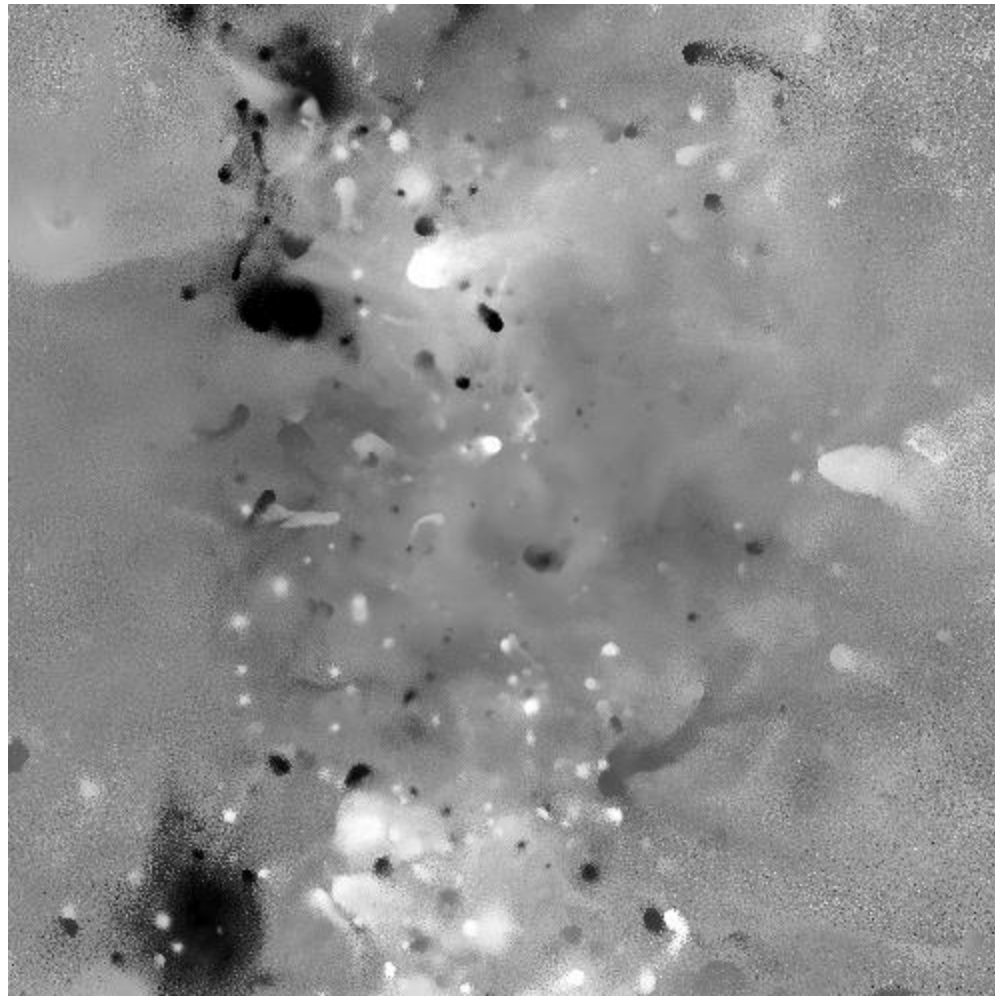
E.Churazov, I.Zhuravleva, N.Lyskova, P.Arevalo, K.Dolag,
A.Vikhlinin, W.Forman, C.Jones, S.Sazonov, R.Sunyaev

Coma

X-ray image and residuals from symmetric model



Gas is not at rest!



We want to “measure” hot ICM velocity field

How to measure?

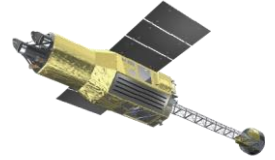
How we characterize the velocity field and observables?

Using simulations to calibrate observables

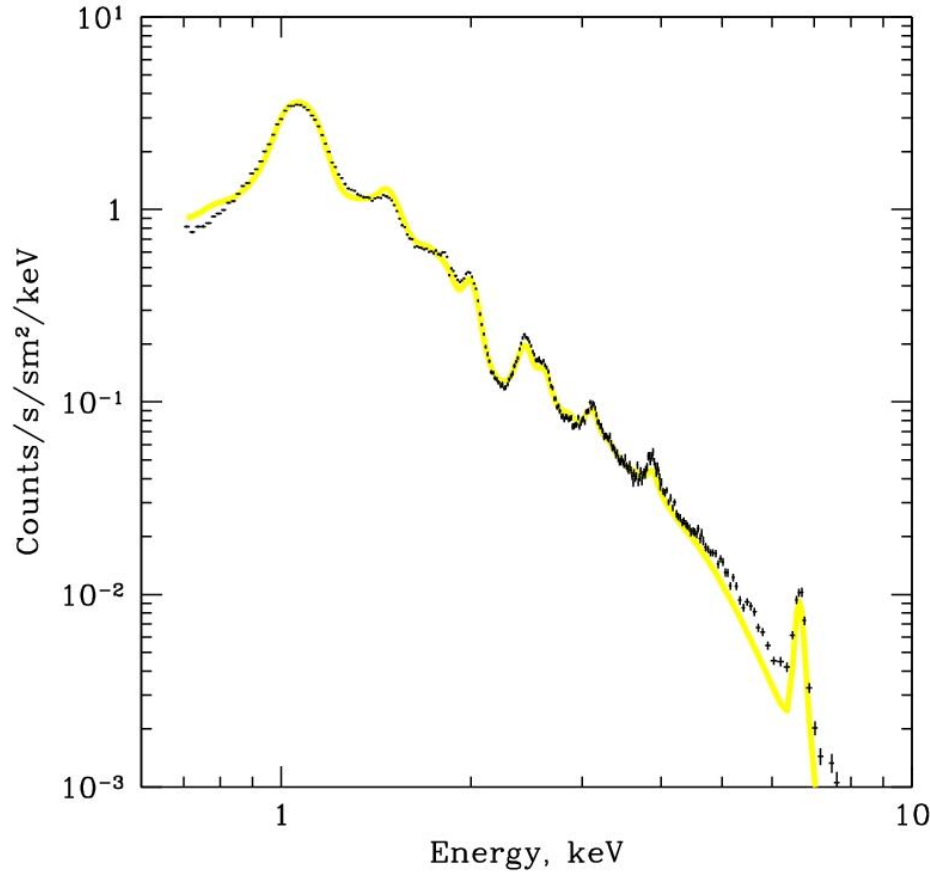
Any differential gas motions

Gaussian isotropic random field

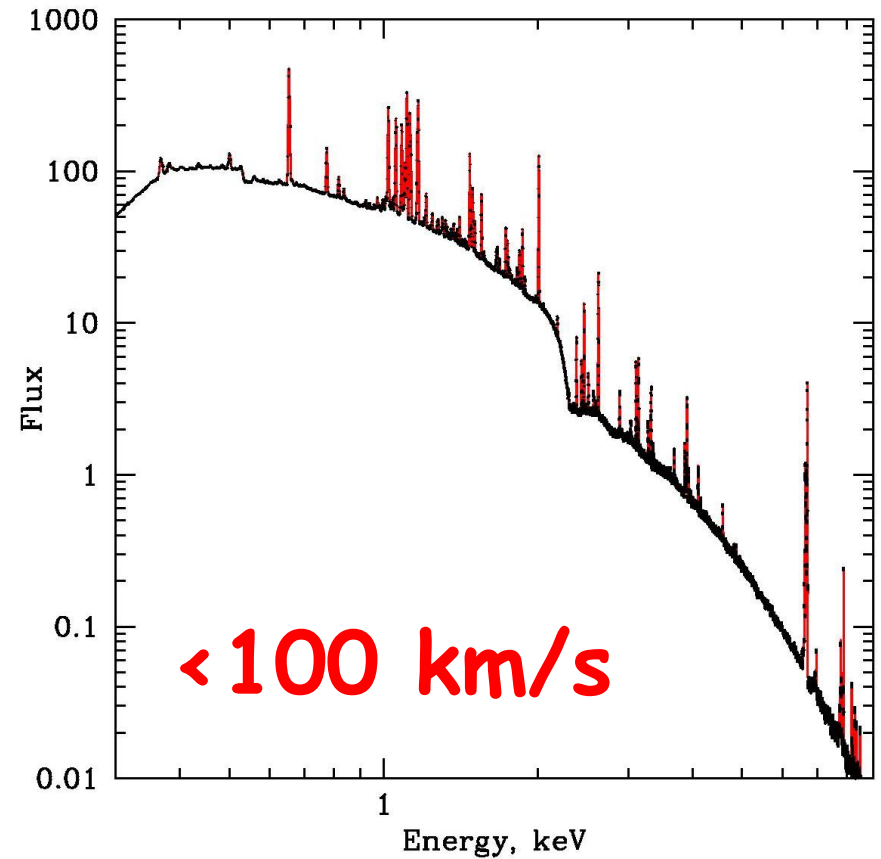
Direct velocity measurements



Chandra



Astro-H, 2013

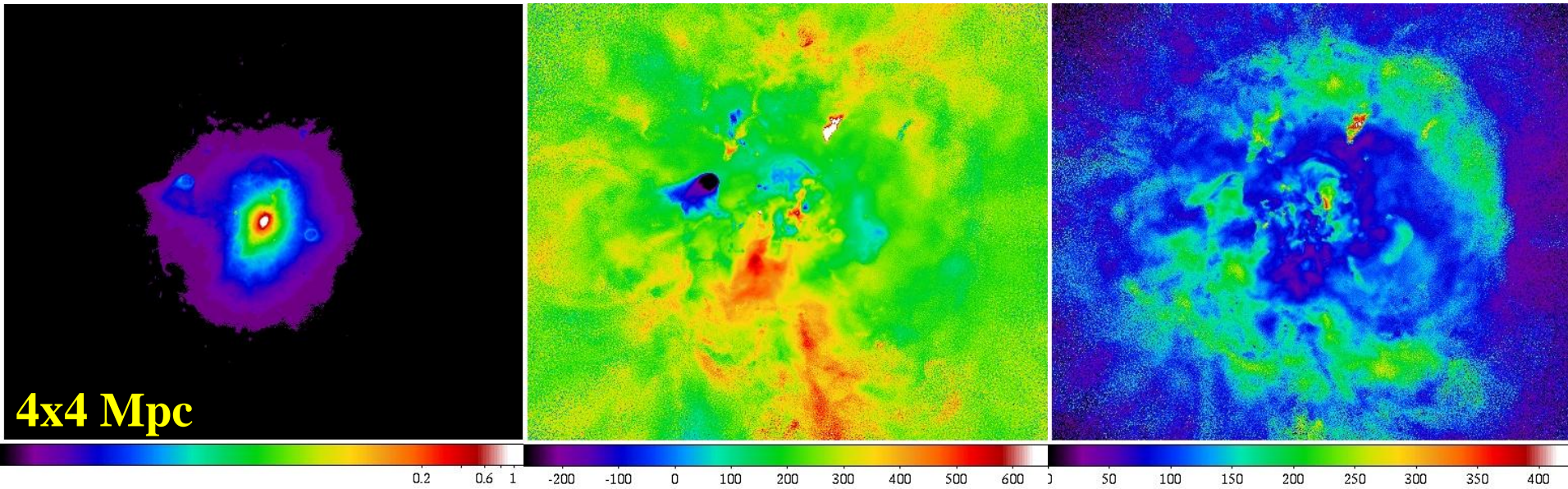


XMM/RGS, broadening < 200 km/s [1D] (Sanders+10,11)

$$\int n_e^2 dl$$

$$\langle v_z \rangle_l$$

$$\sqrt{\langle v_z^2 \rangle_l - \langle v_z \rangle_l^2}$$



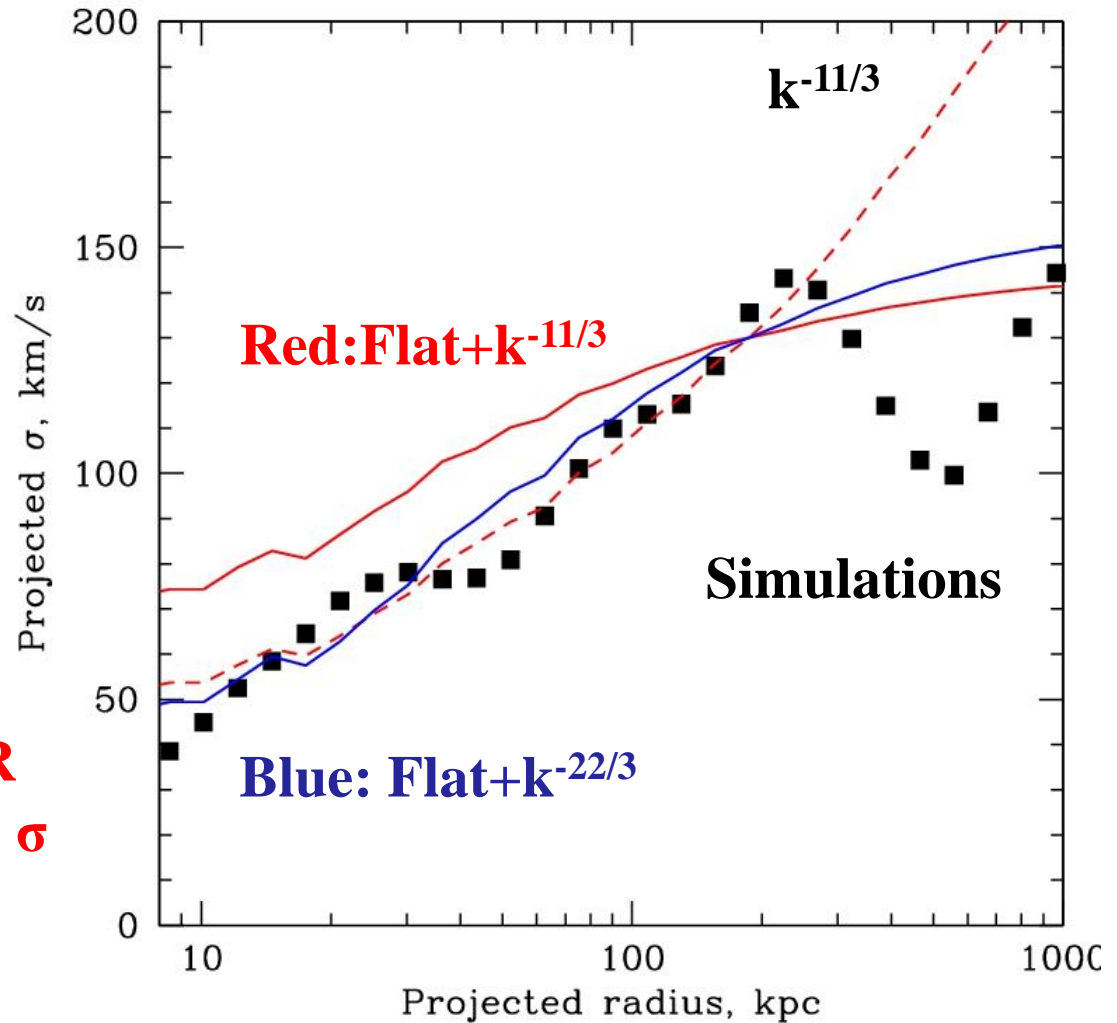
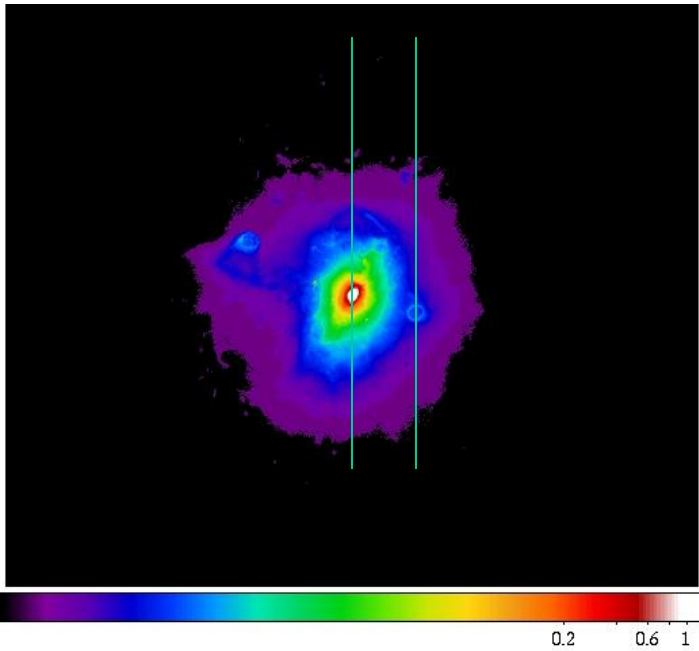
Observables: n_e , emission measure weighted v_z , σ

$$V_{2D} = \int V_{3D} n_e^2(z) dz$$

$$P_{2D}(k) = \int P_{3D} \left(\sqrt{k^2 + k_z^2} \right) W^2(k_z) dk_z$$

Projected velocity dispersion \approx Structure Function

$$S(\Delta x) = \left\langle \left| \mathbf{v}(x + \Delta x) - \mathbf{v}(x) \right|^2 \right\rangle$$



At a given projected radius R
 an interval $\sim R$ contributes to σ
 $\sigma^2 \approx$ structure function

$$\sigma^2 = \int P_{3D} \left[-W^2(k_z) \right] dk_z dk_x dk_y$$

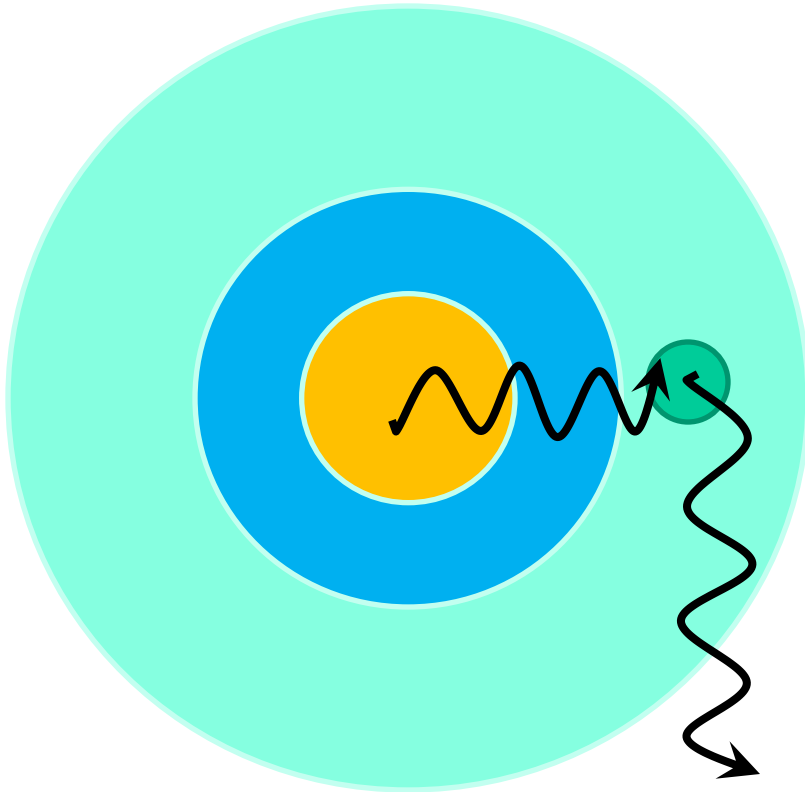
Zhuravleva, 2011

Less direct ways of measuring ICM velocities.

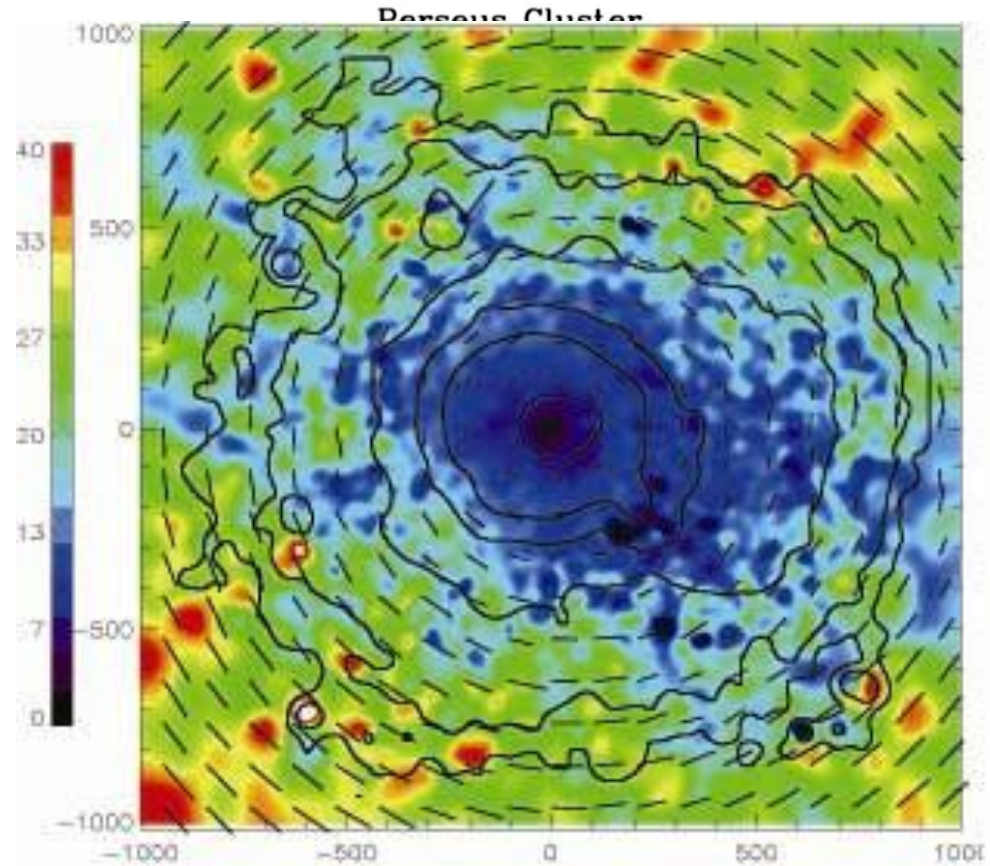
Kinetic SZ effect	$\langle V \rangle, \Delta V$	Benson+03 Osborne+11
Resonant scattering	$\Delta V, PS(V)$	Werner+09, Hayshi+09, Zhuravleva+11
Polarization due to resonant scattering	$V, \Delta V$	Zhuravleva+10
Faraday Rotation	$PS(B) \rightarrow V$	Vogt+03, Bonafede+10
H $_{\alpha}$ filaments	V	Fabian+03
Pressure fluctuations	$PS(P) \rightarrow V$	Schuecker+04
SB fluctuations	$PS(n_e)$	

Polarization of 6.7 keV Iron line

Rayleigh phase function + Quadrupole = Polarization



100% polarized



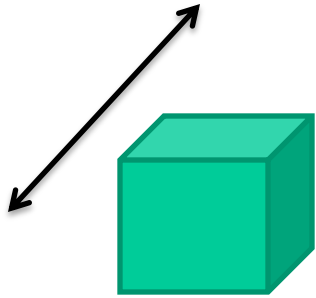
Center: 0%

Outskirts: 10%

Transverse ICM velocities and polarization

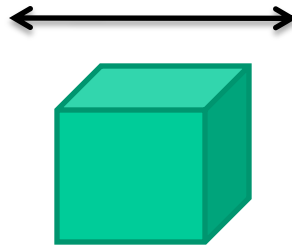
Quadrupole component can be induced by gas motions!

Motion along l.o.s.

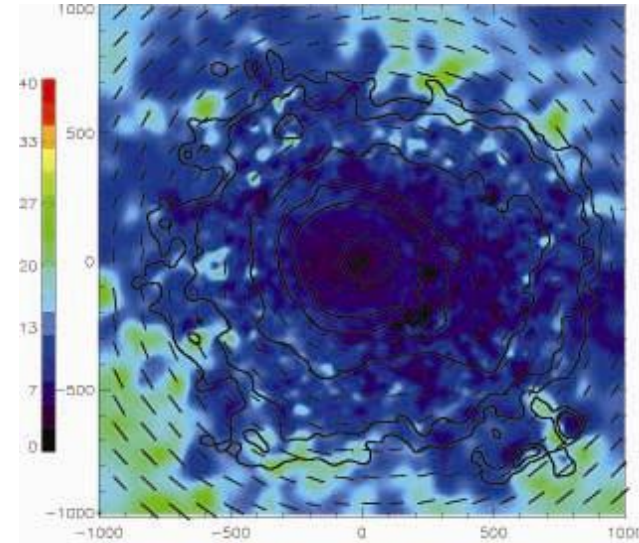


Doppler shift
No polarization

Motion transverse l.o.s.



No Doppler shift
Polarization



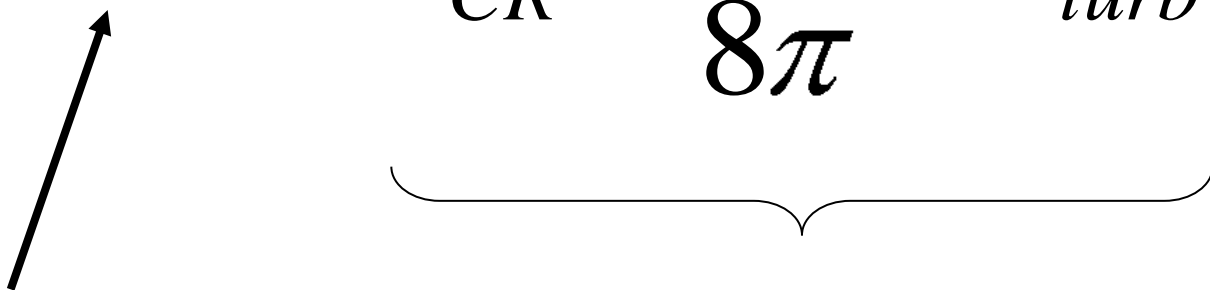
- 1) On average gas motions reduce optical depth
- 2) But can cause polarization in the cluster core

Very indirect ways of measuring ICM velocities.

Turbulent Diffusion of metals	$D \sim VL$	Rebusco+05
Cool Cores: Heating=Cooling	Heating $\sim V^3/L$	
Correction to mass from hydrostatic equilibrium	v^2	EC+08, 10
Many more...		

Combinations provide both V , L

$$\frac{1}{\rho} \frac{dP}{dr} = - \frac{GM}{r^2}$$

$$P = nkT + P_{CR} + \frac{B^2}{8\pi} + P_{turb}$$


Thermal pressure
(easy to measure)

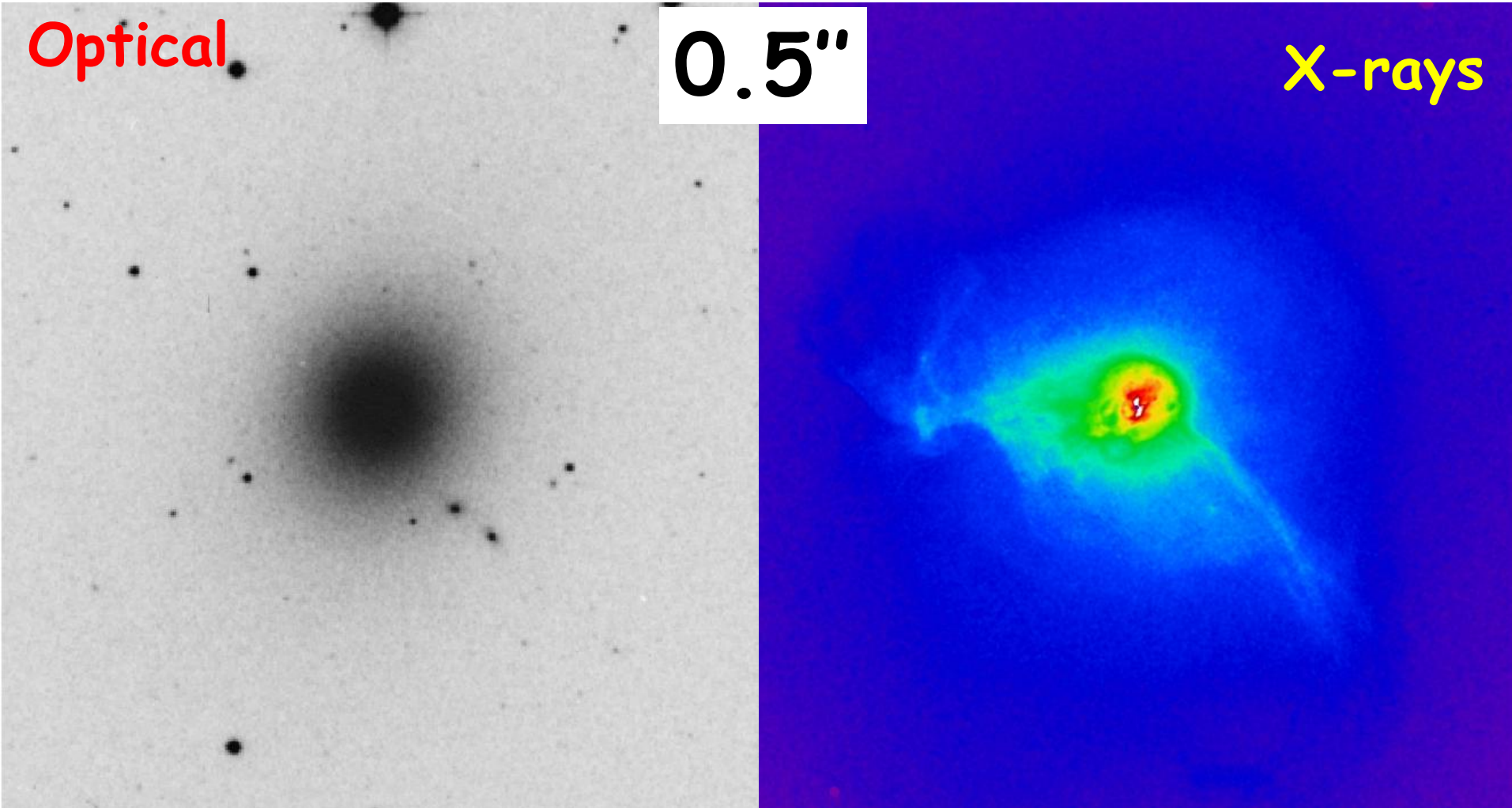
Non-thermal pressure (invisible)

M87

Optical

0.5''

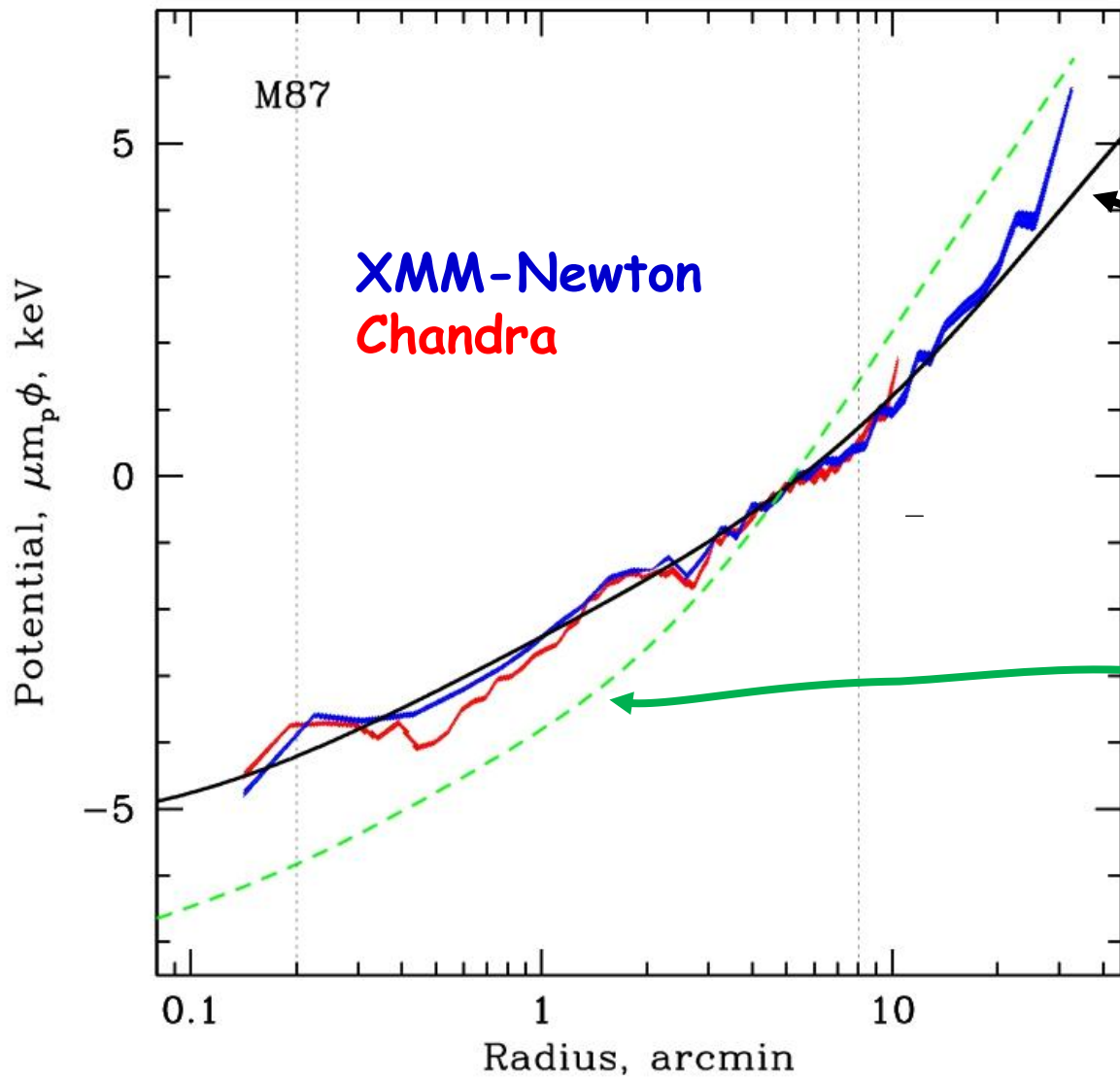
X-rays



Stars: gravity only
(anisotropy)

Gas: gravity, magnetic fields, cosmic rays, turbulent motions, non-stationarity

M87: X-rays + stellar kinematics



Romanowsky & Kochanek, 2001

$$\frac{P_{nt}}{P_{gas}} \leq 0.1$$

Gebhardt & Thomas, 2010

$$\frac{P_{nt}}{P_{gas}} \approx 0.35$$

$V \sim \text{few } 100 \text{ km/s} \rightarrow \text{Power Spectra}$

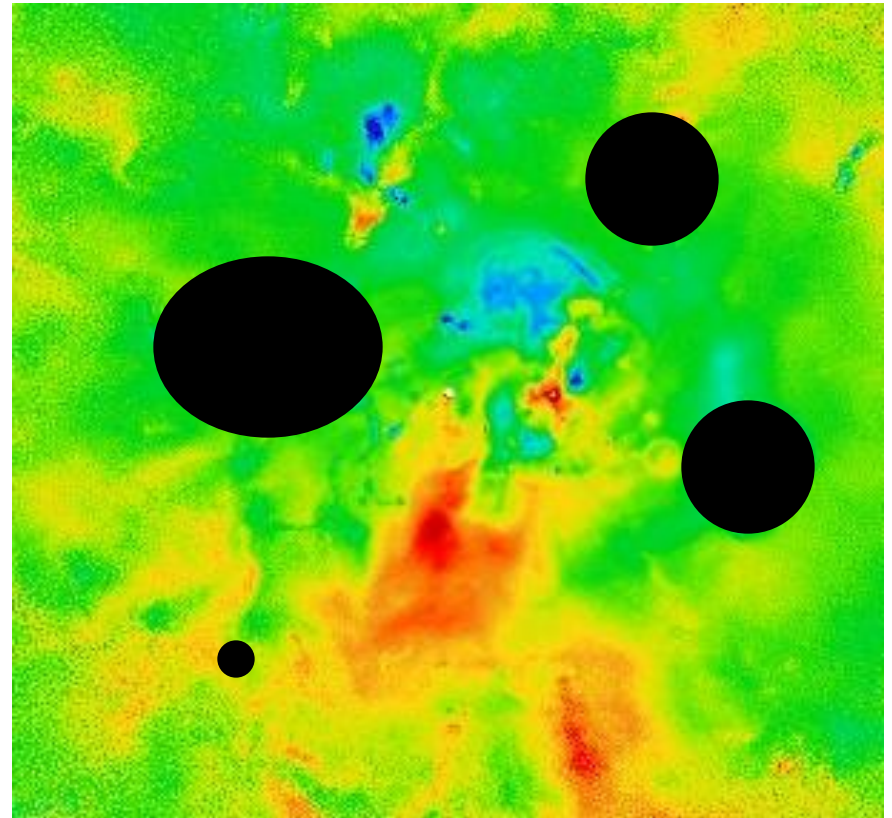
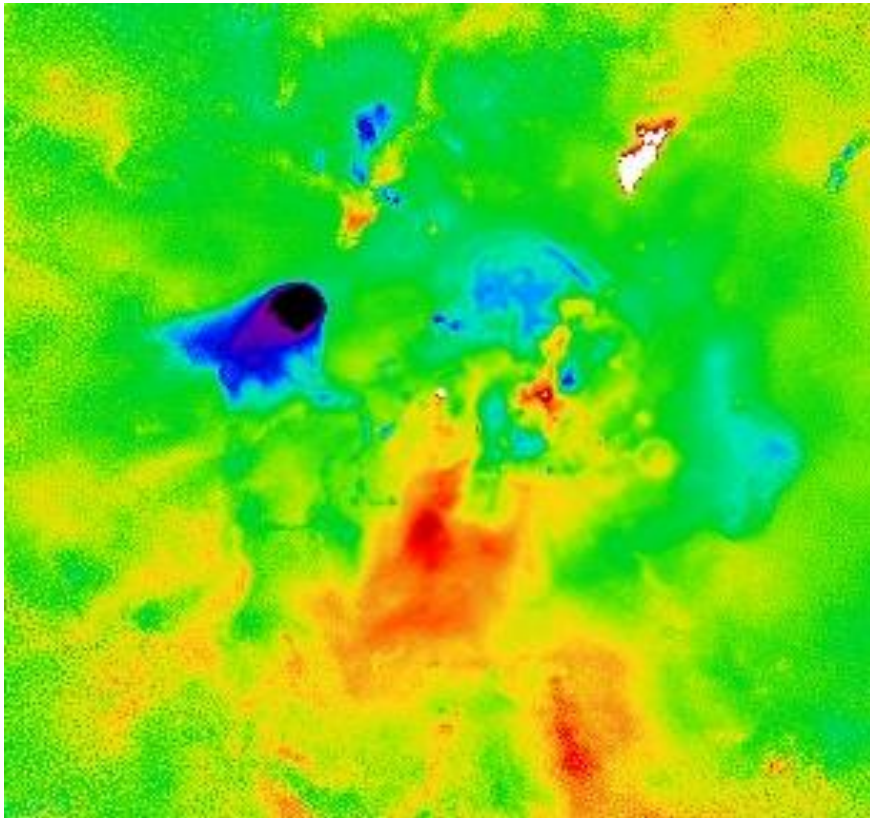
**Characterizing ICM velocity field
(3D simulations, RM maps, etc)**

**Calculating Power Density Spectra
for featureless continuum**

**Calculating characteristic amplitude
associated with a given spatial scale**

Calculating Power Density Spectrum for the data with holes (making Fourier transform of the velocity map)

1. Non-periodic
2. Missing data (points sources, gaps between CCDs,...)



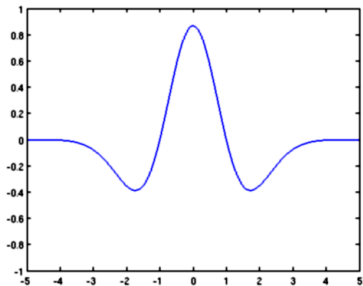
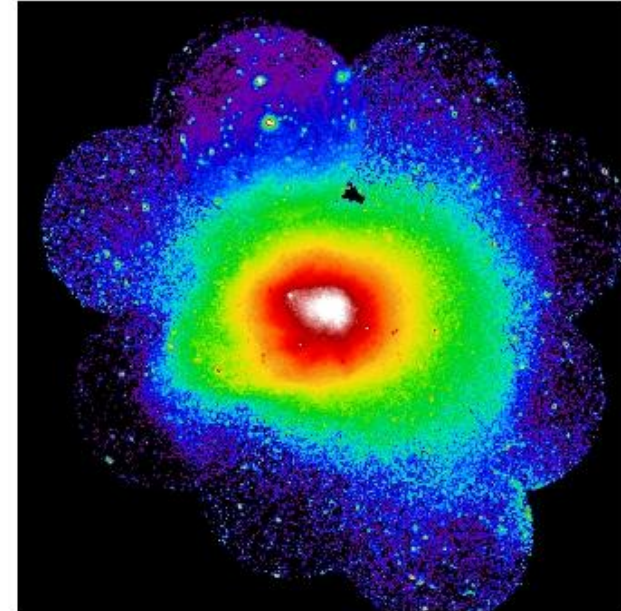
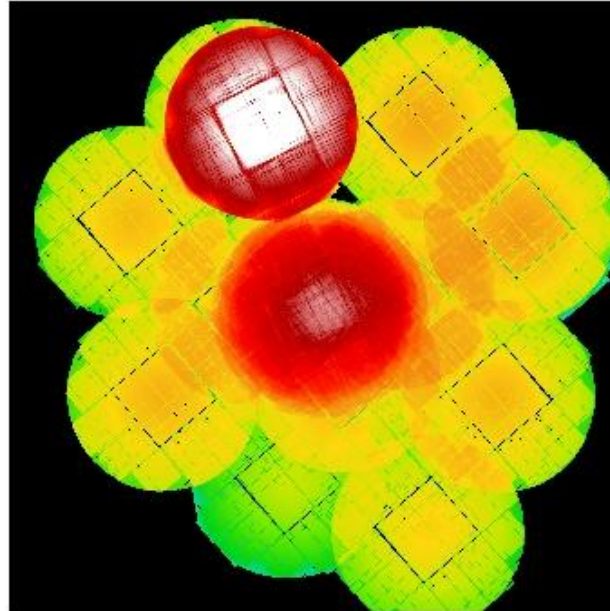
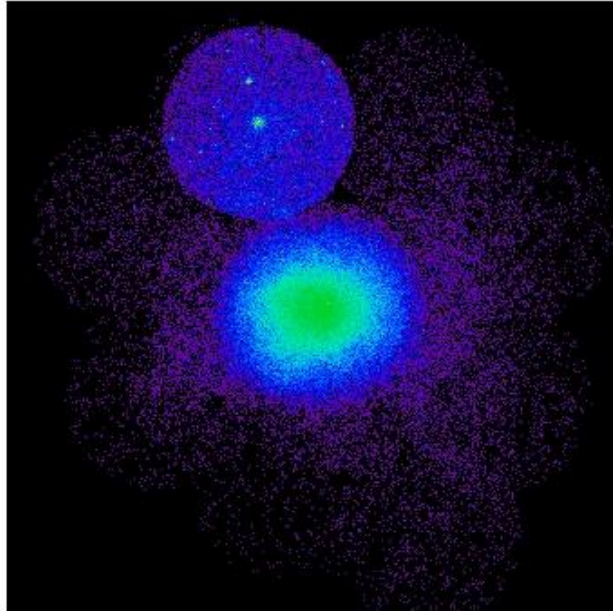
Fourier is tuned for periodic arrays without gaps

Smoothing of X-ray images

Raw image

Exposure map

$S(\text{Images})/S(\text{E_map})$



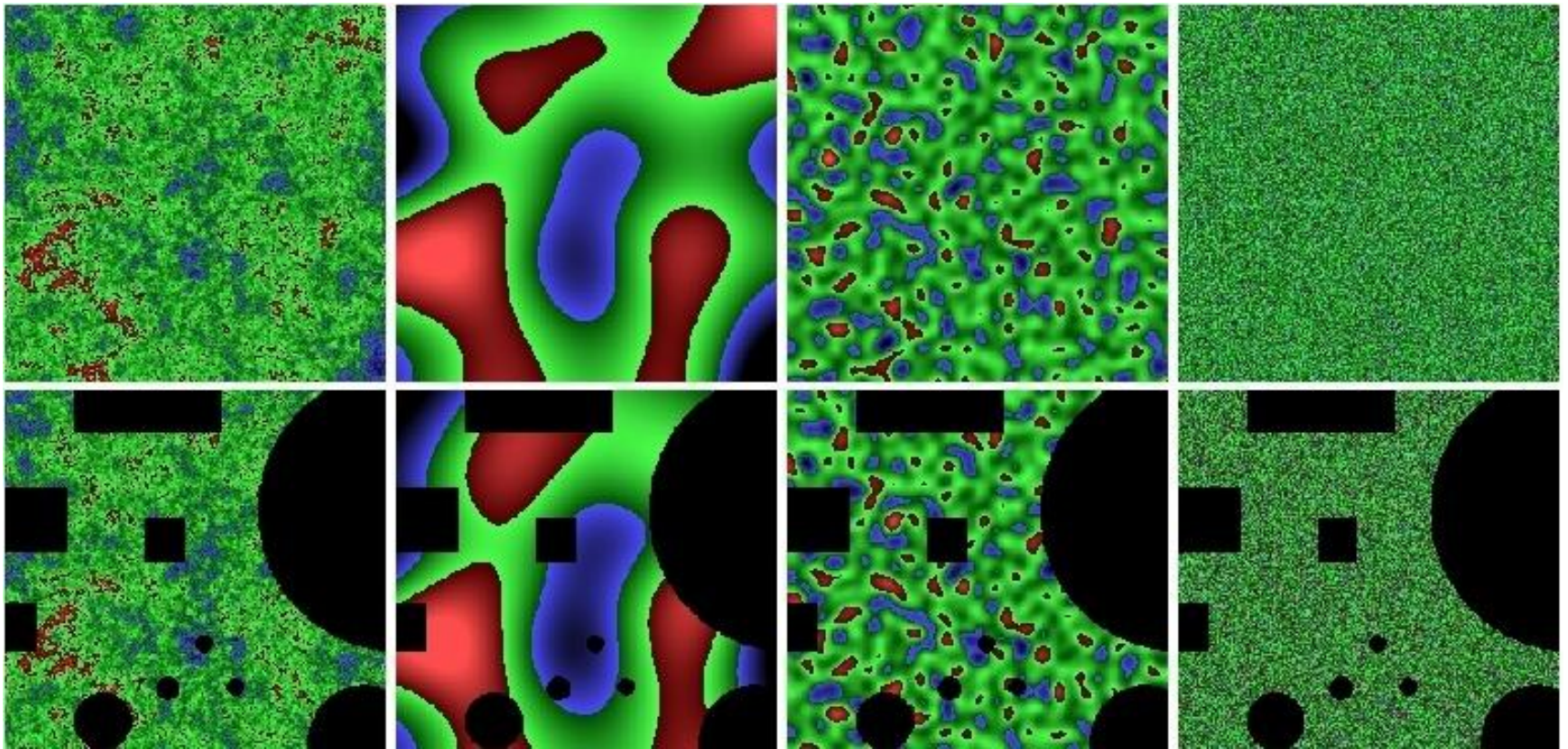
$$G_{\sigma_1} \circ I = \frac{G_{\sigma_1} \circ I}{G_{\sigma_1} \circ M}$$

$$G_{\sigma_1} \circ I - G_{\sigma_2} \circ I = \text{Mexican Hat Filter}$$

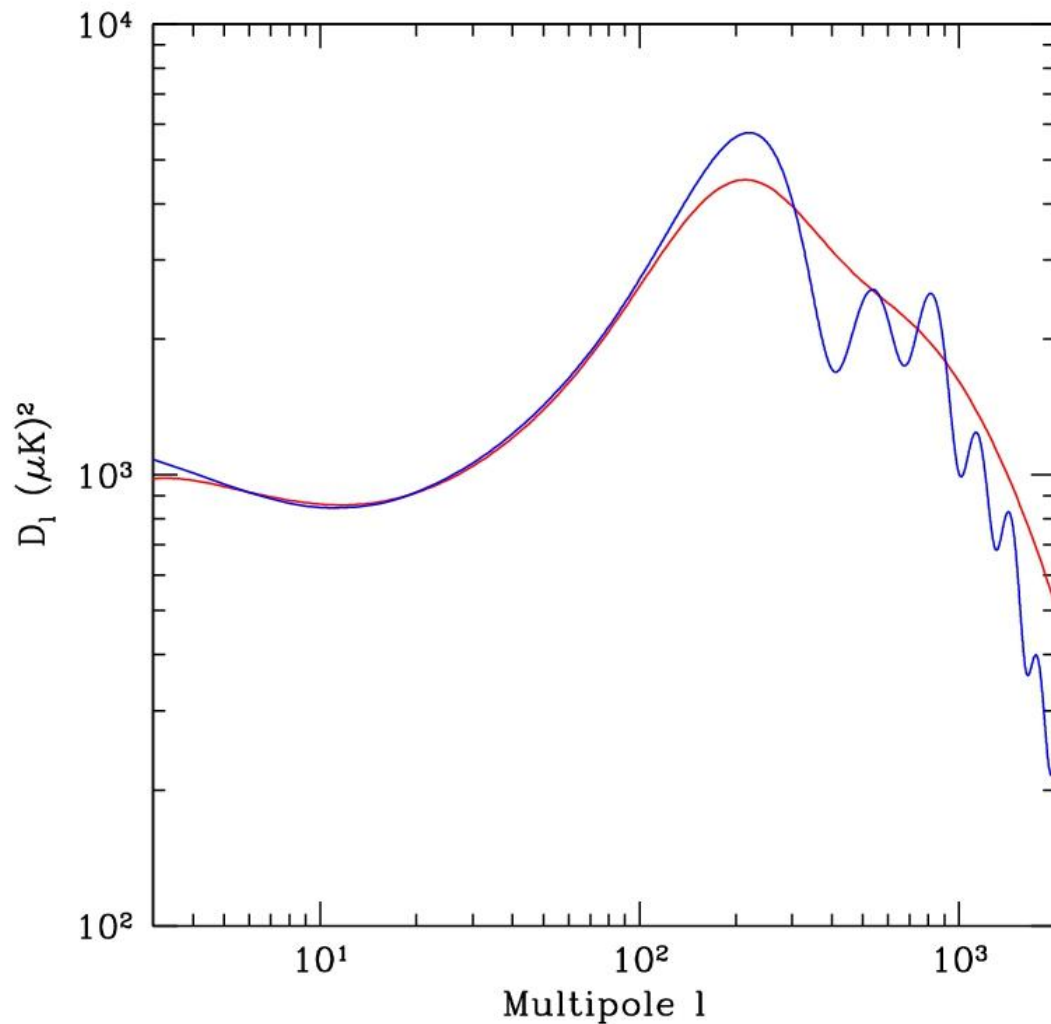
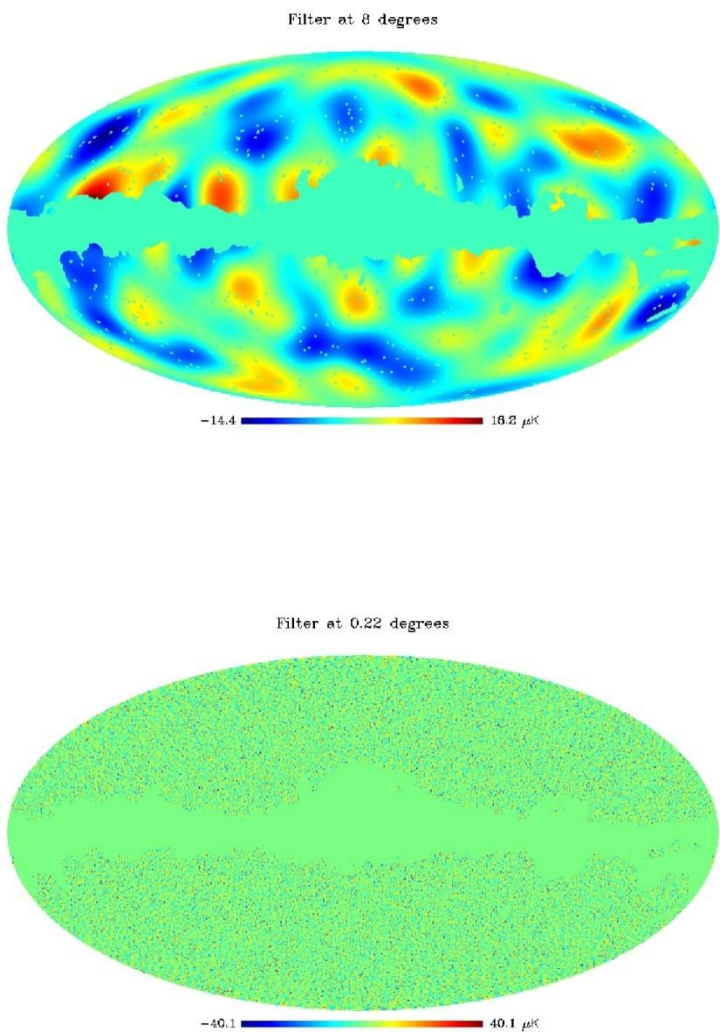
Modified Mexican Hat Filter for data with gaps

$$\tilde{F} \circ I = \frac{G_{\sigma_1} \circ I}{G_{\sigma_1} \circ M} - \frac{G_{\sigma_2} \circ I}{G_{\sigma_2} \circ M}$$

(Arevalo et al, submitted, see also Ossenkopf+08)



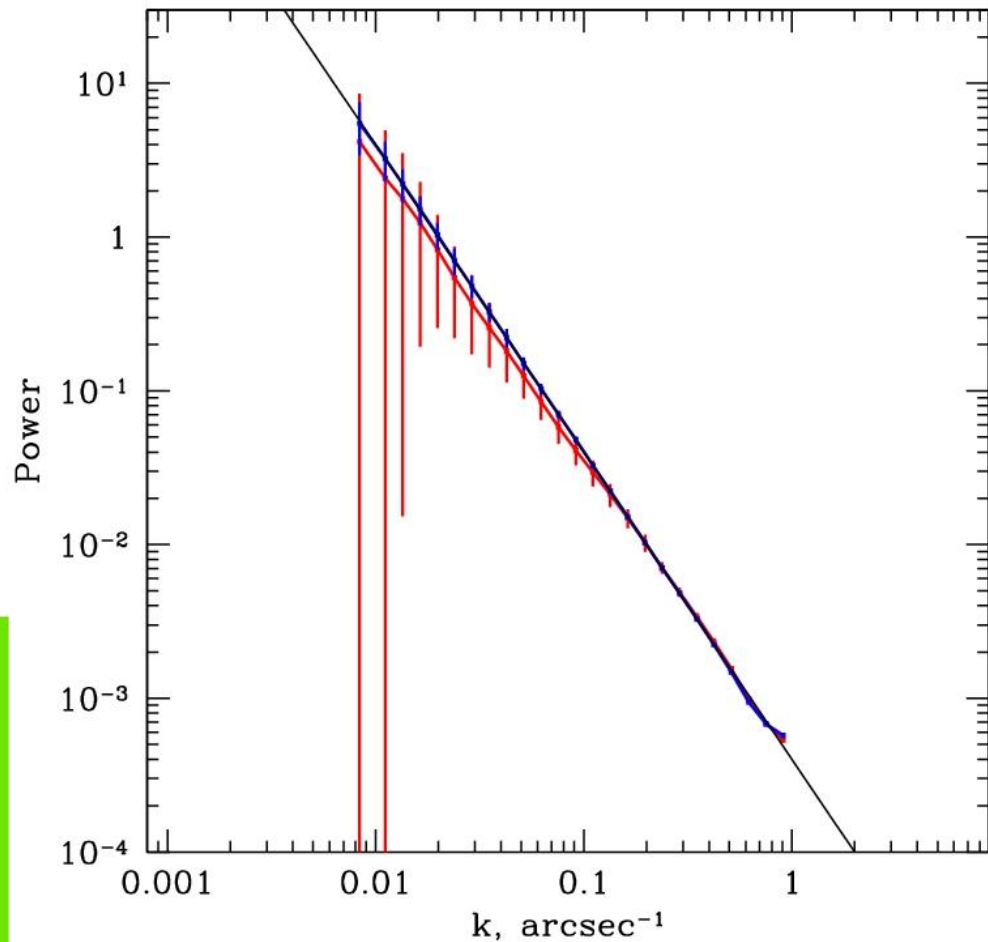
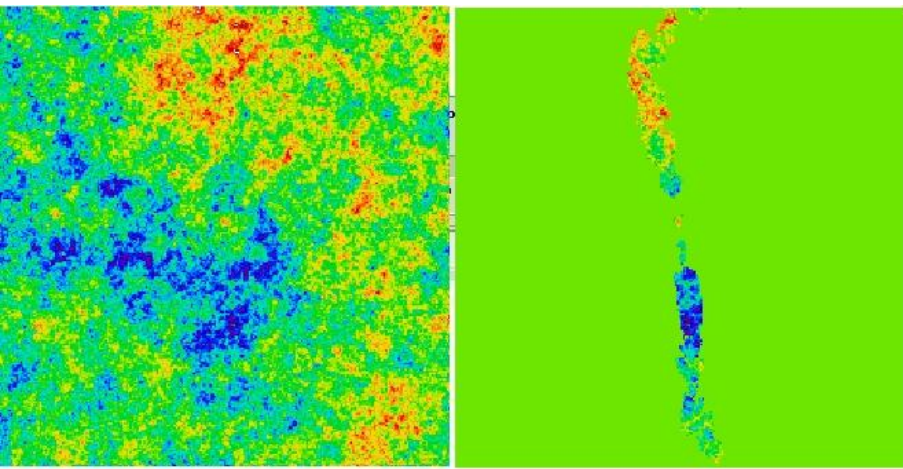
CMB: Works fine for low resolution PS



Arevalo+, submitted

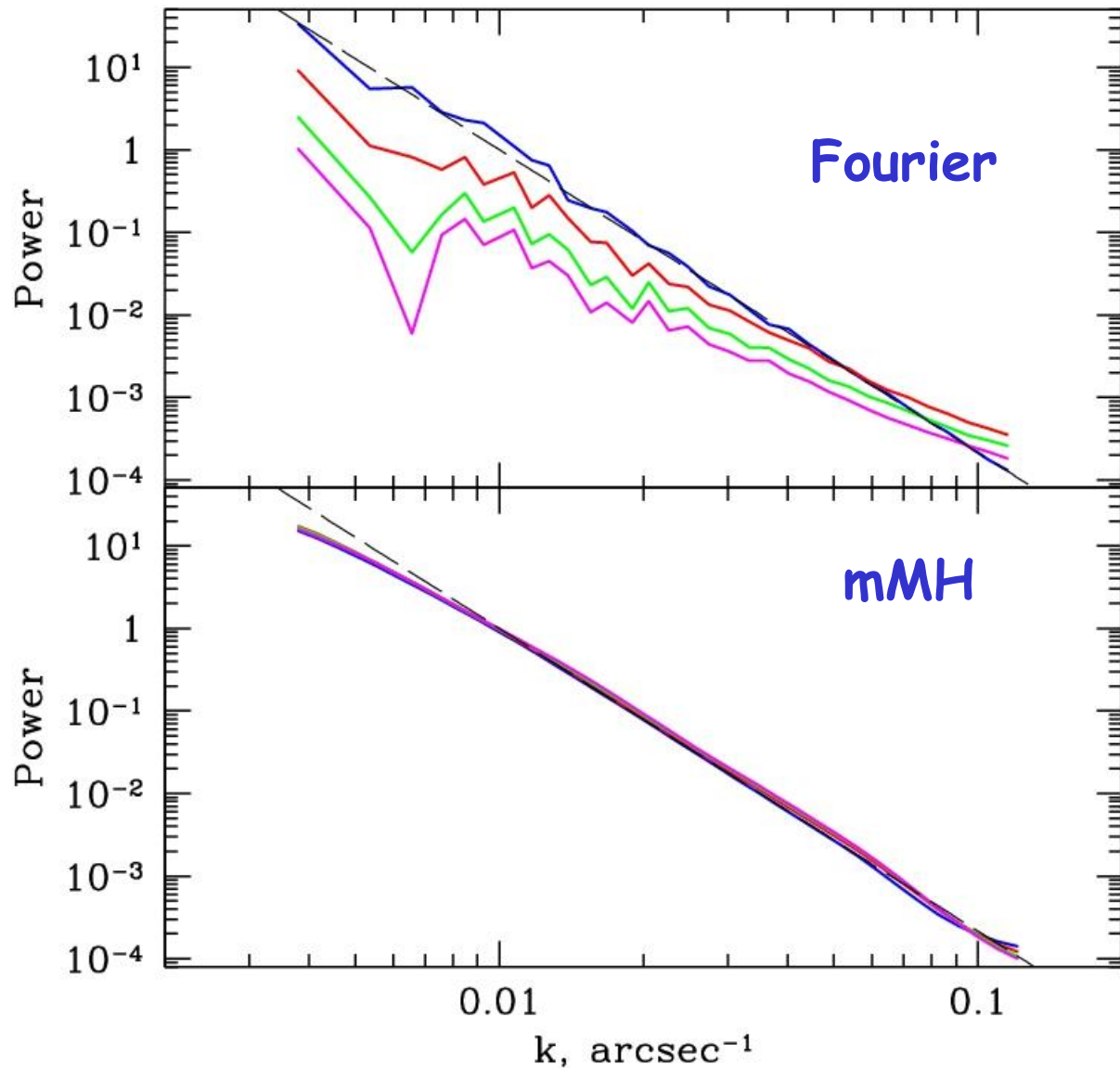
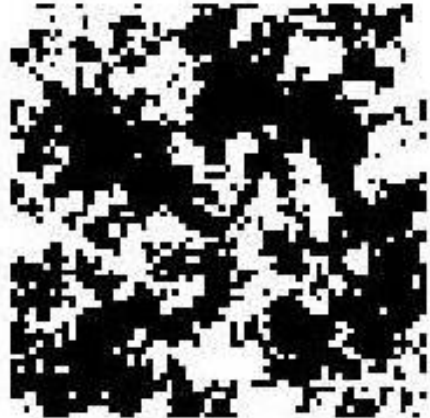
Faraday Rotation Measure

$$\int n_e B_{\parallel} dl$$



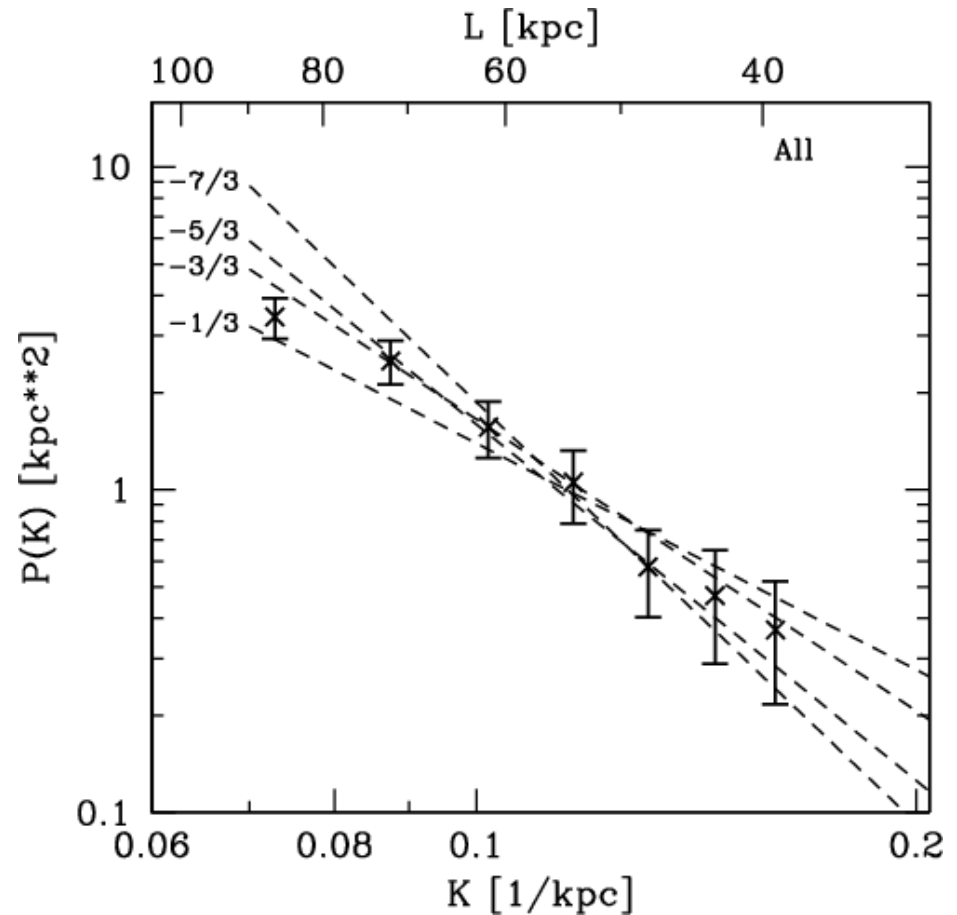
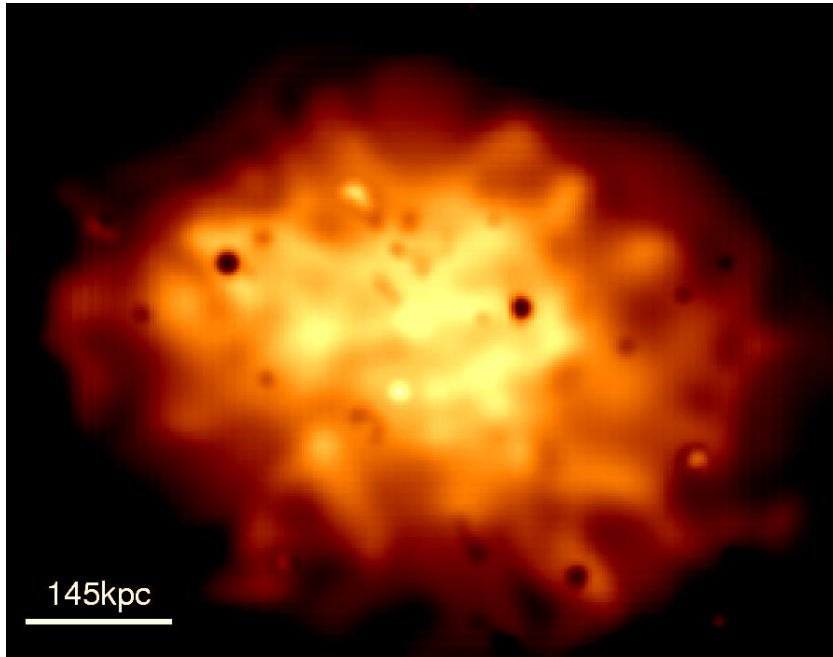
Lyskova+

Simulated 3D velocity cube



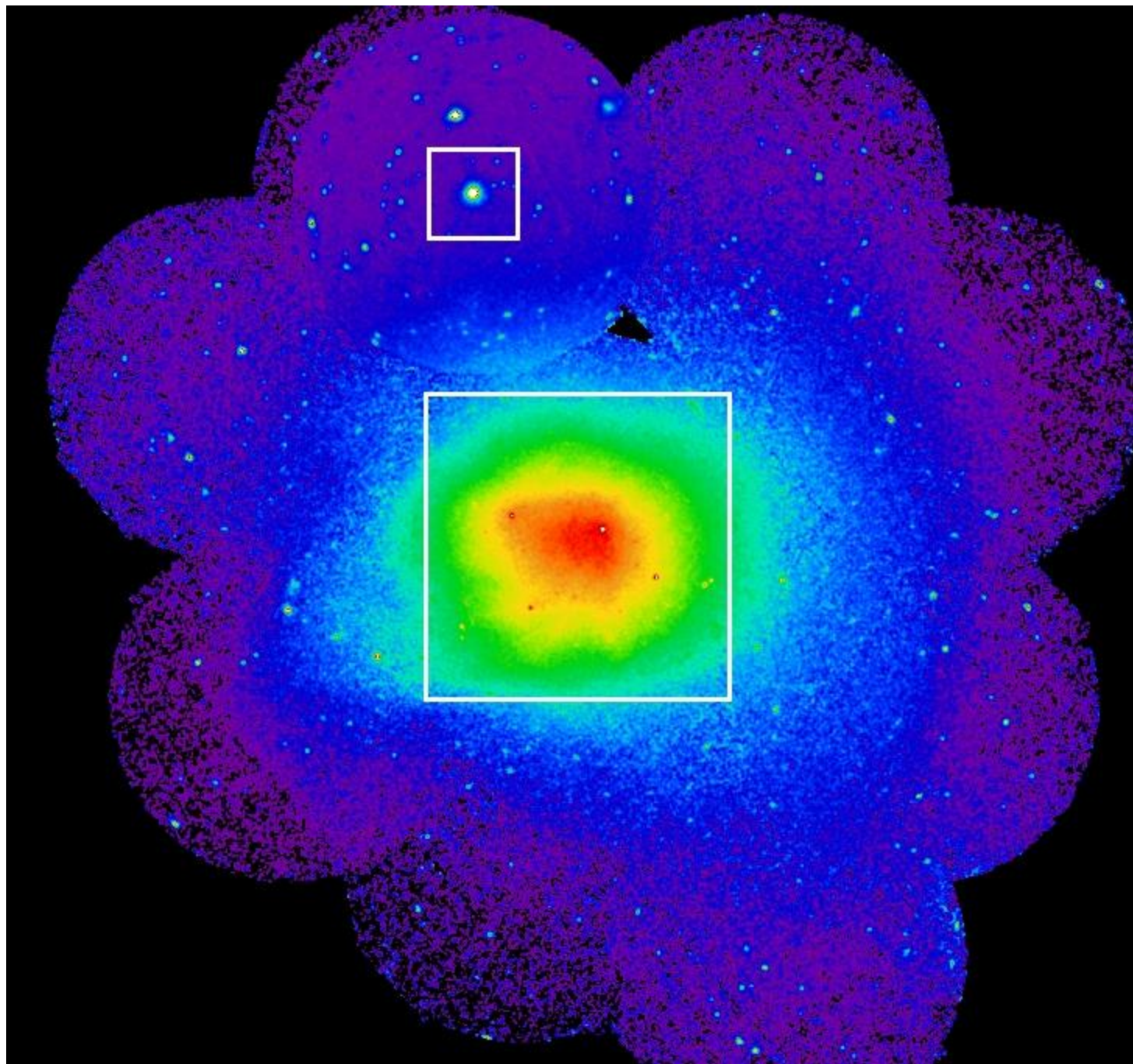
Zhuravleva+

Pressure fluctuations in Coma

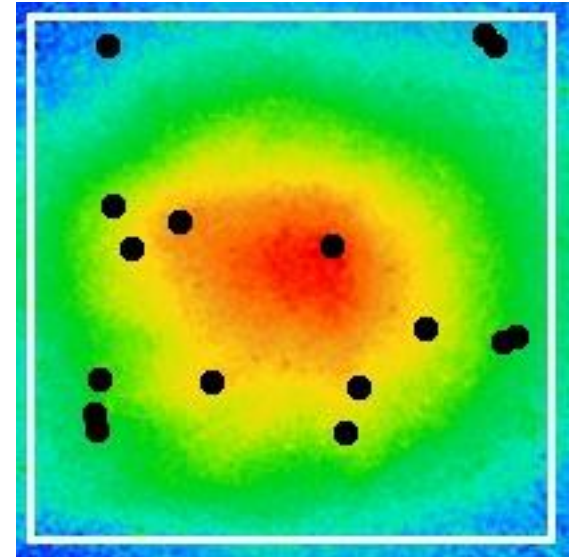
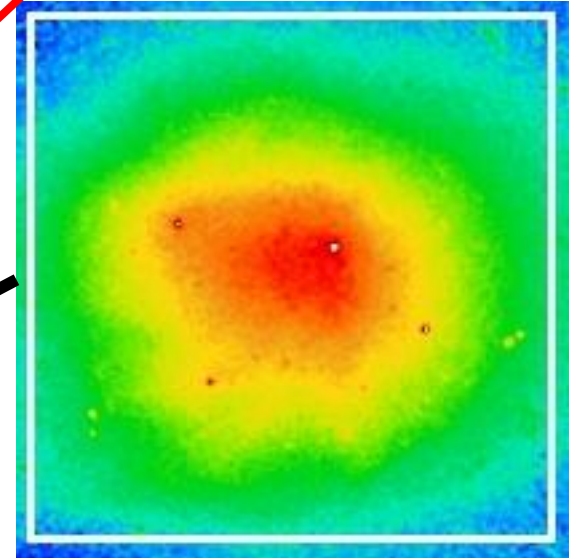
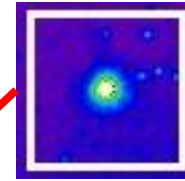
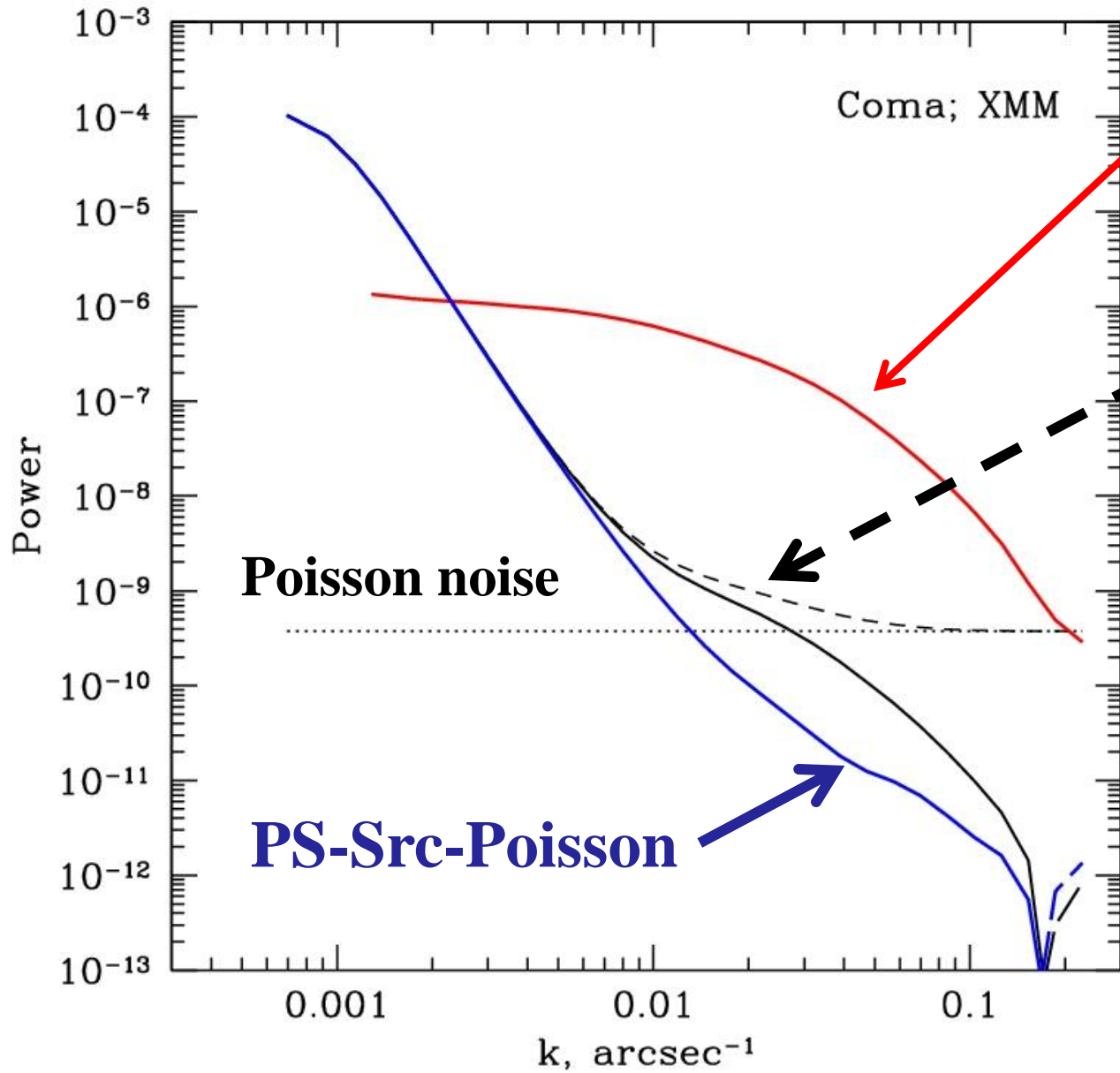


Schuecker et al. (2004)

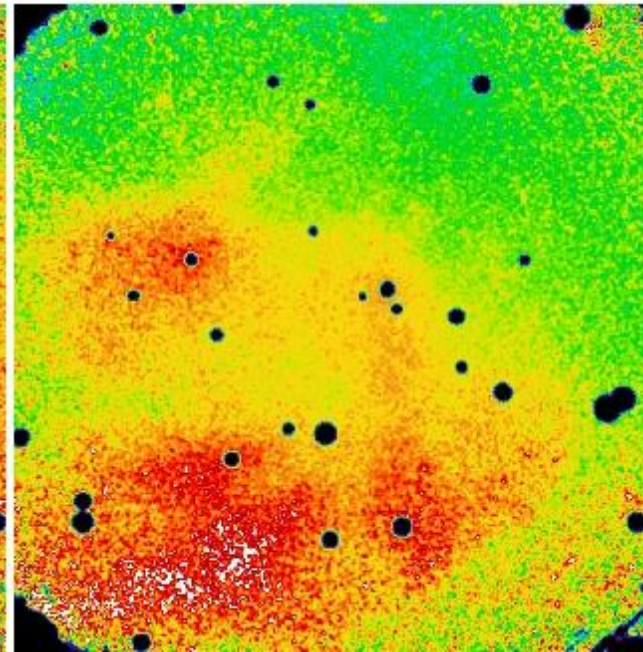
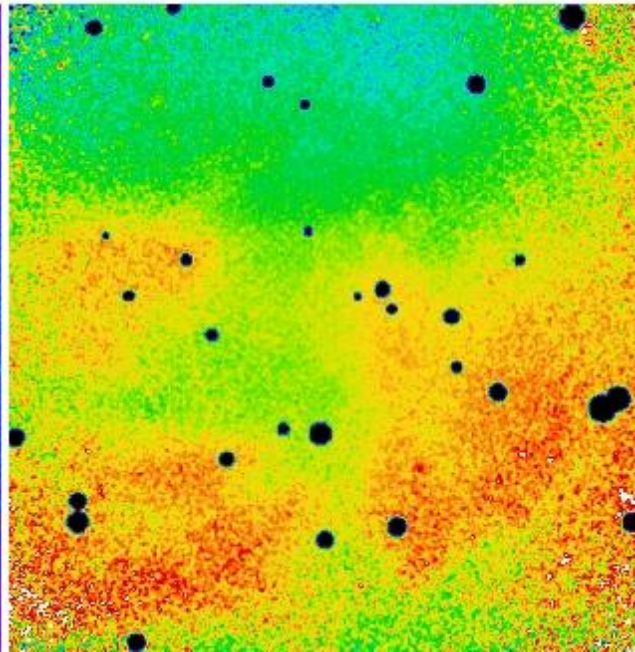
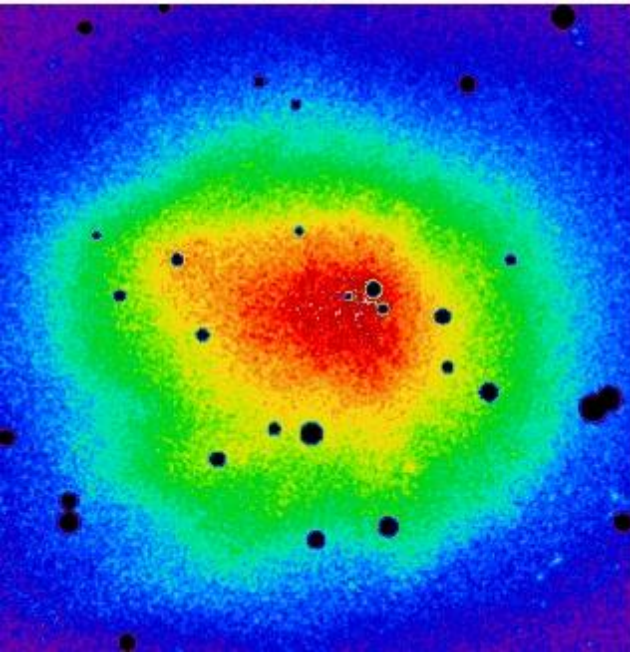
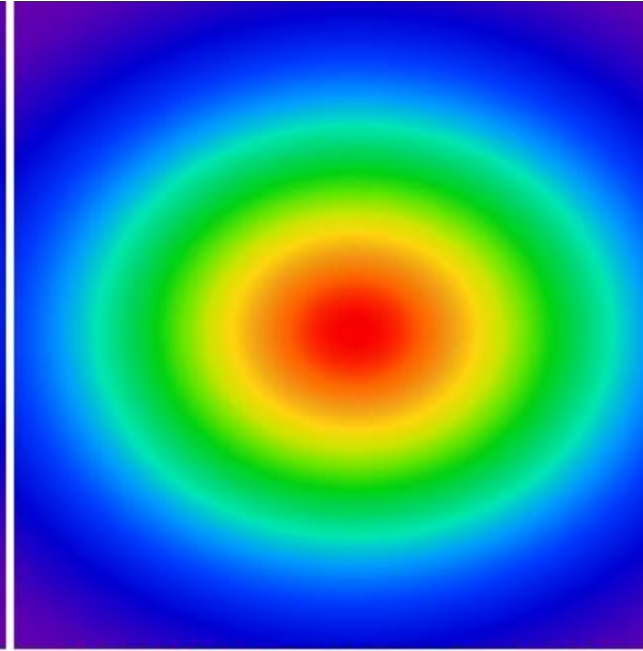
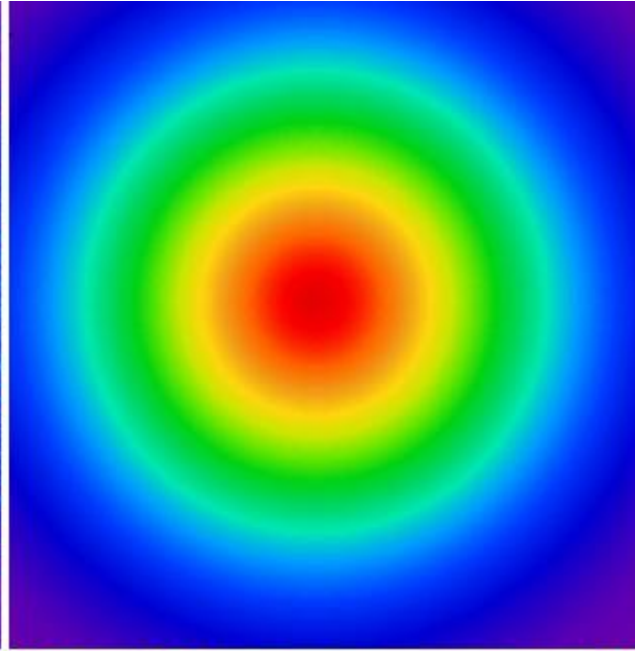
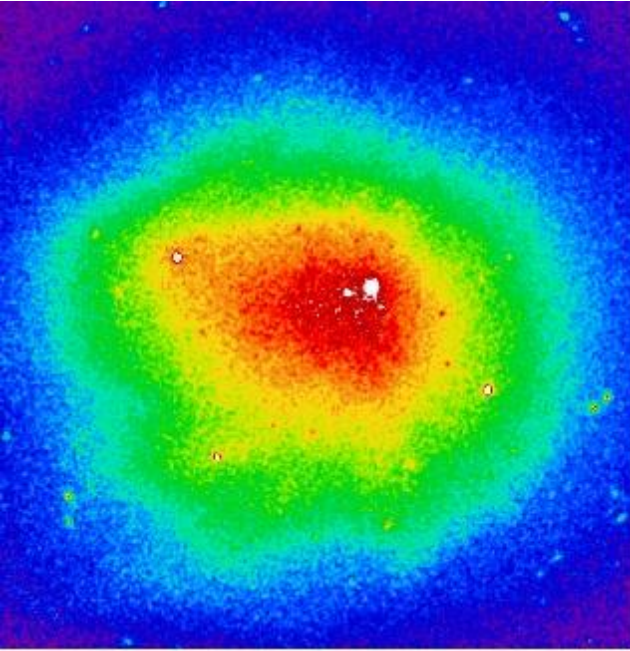
Let us do SB fluctuations



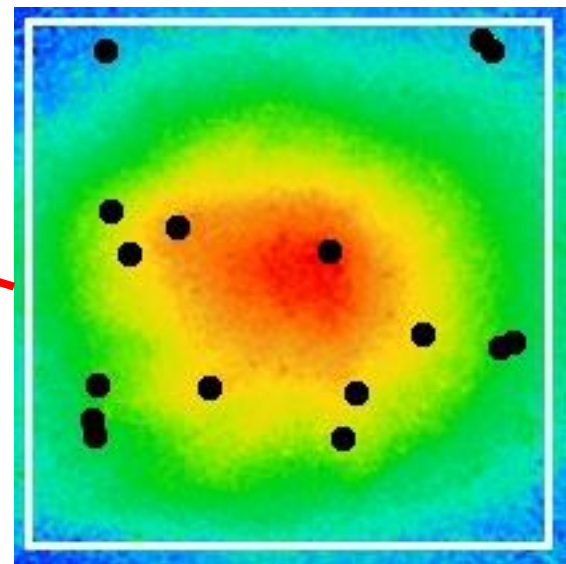
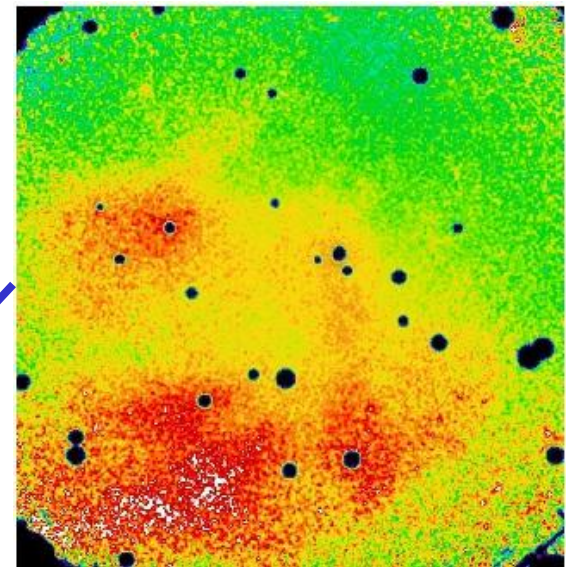
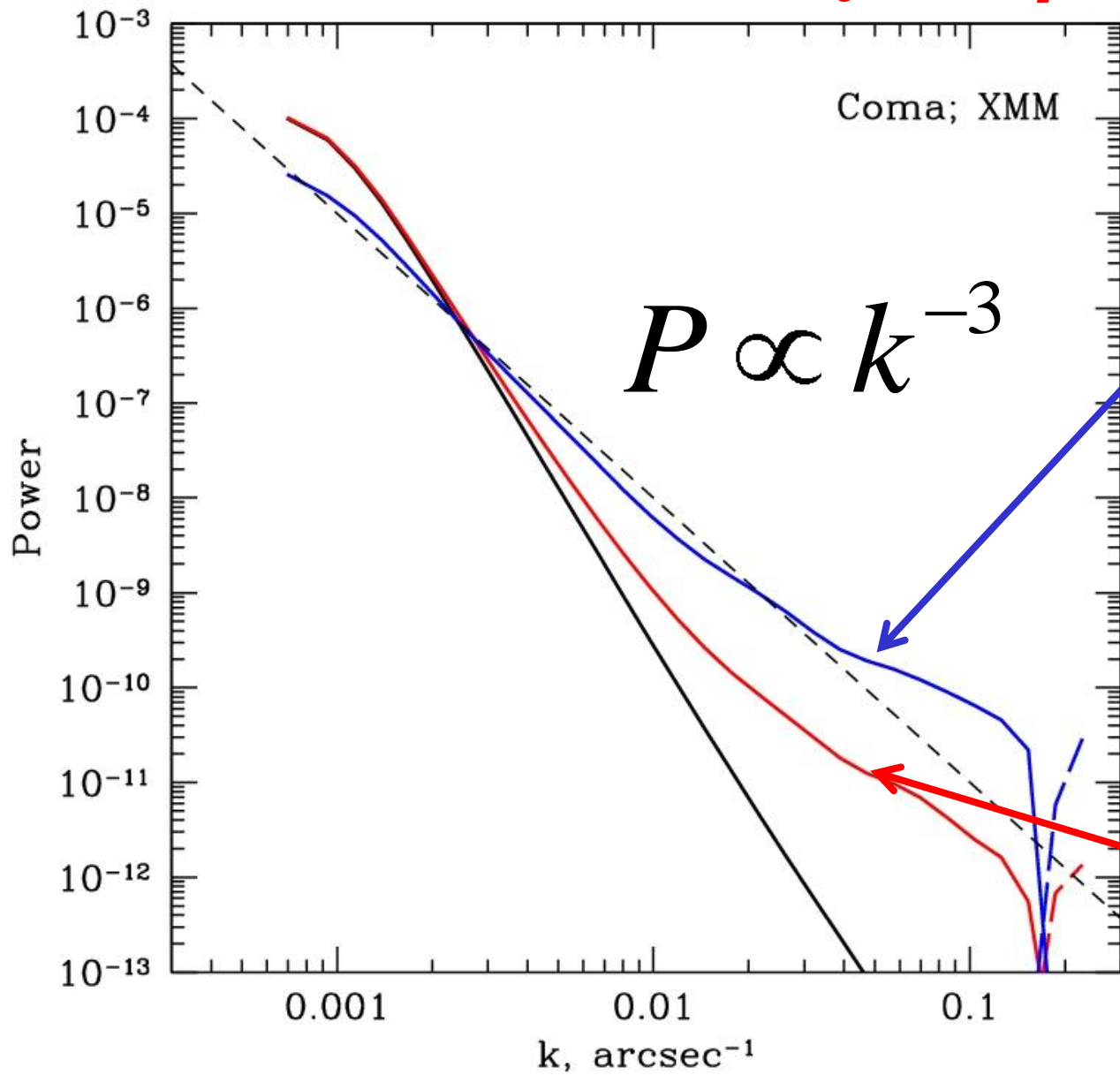
Power Spectrum of X-ray Surface Brightness



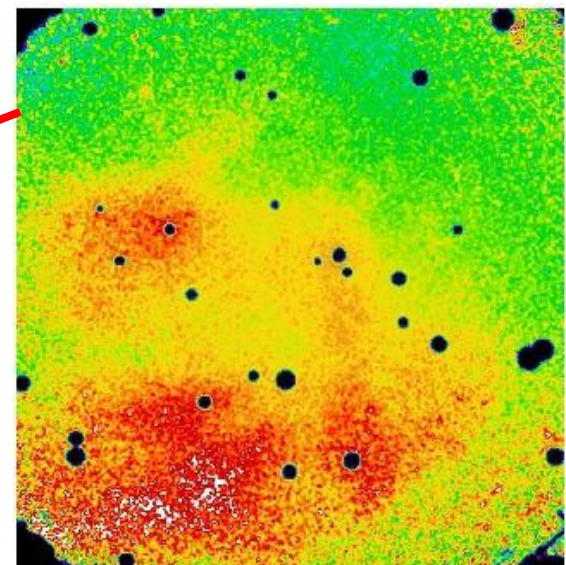
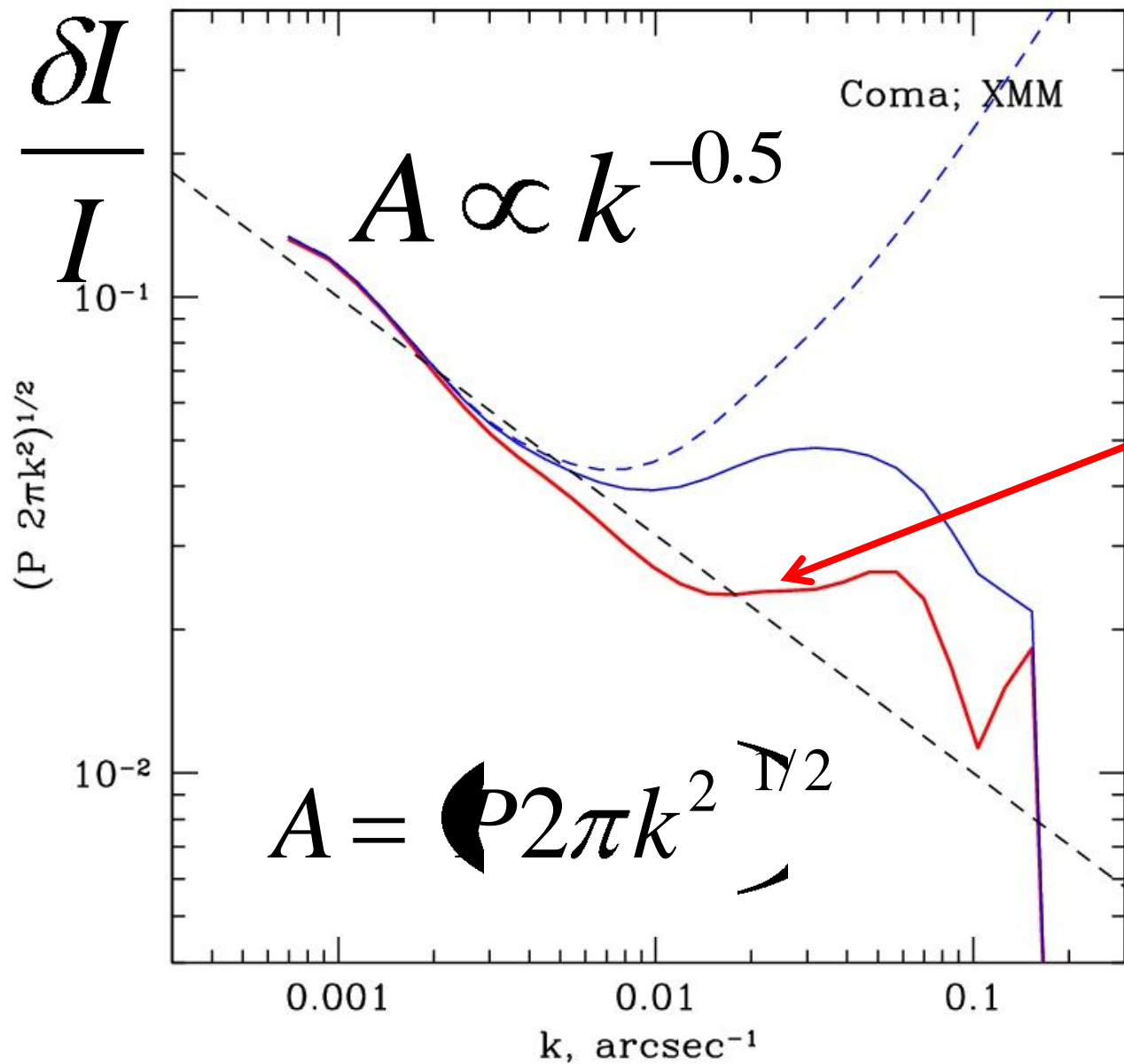
Removing global Coma profile



Coma divided by the β model



Converting to Amplitudes



Relating 3D and 2D power spectra

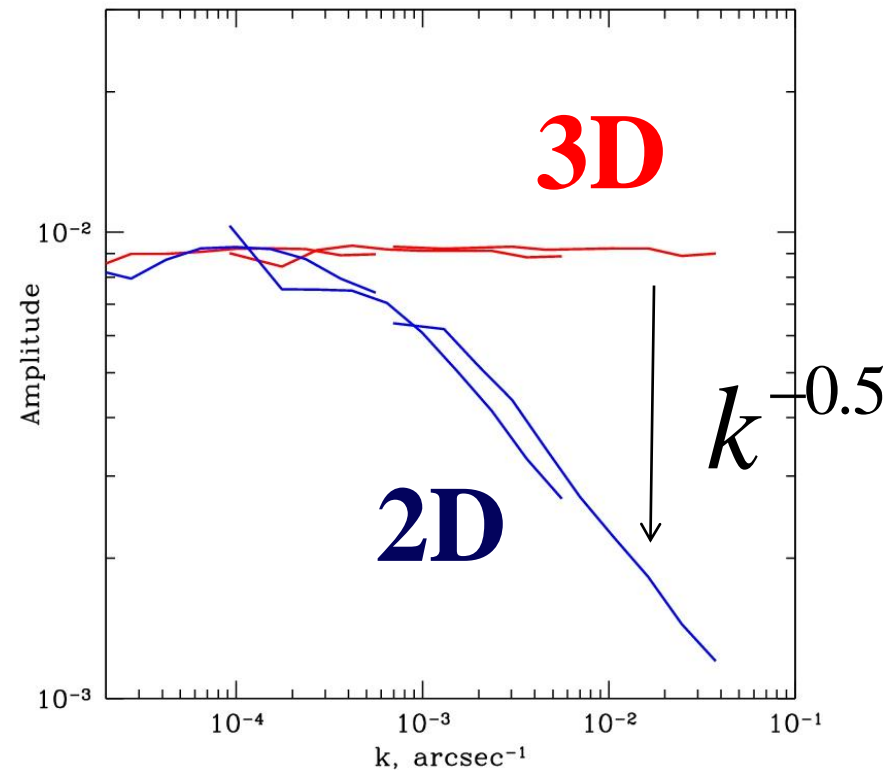
$$I(x, y) = \int \delta(x, y, z) n_e^2(x, y, z) dz$$

$$P_{2D}(k) = \int P_{3D}(\sqrt{k^2 + k_z^2}) W(k_z) dk_z$$

$$W = P_1[n_e^2(z)]$$

$$k \gg \frac{1}{l_z} \Rightarrow P_{2D} = aP_{3D}$$

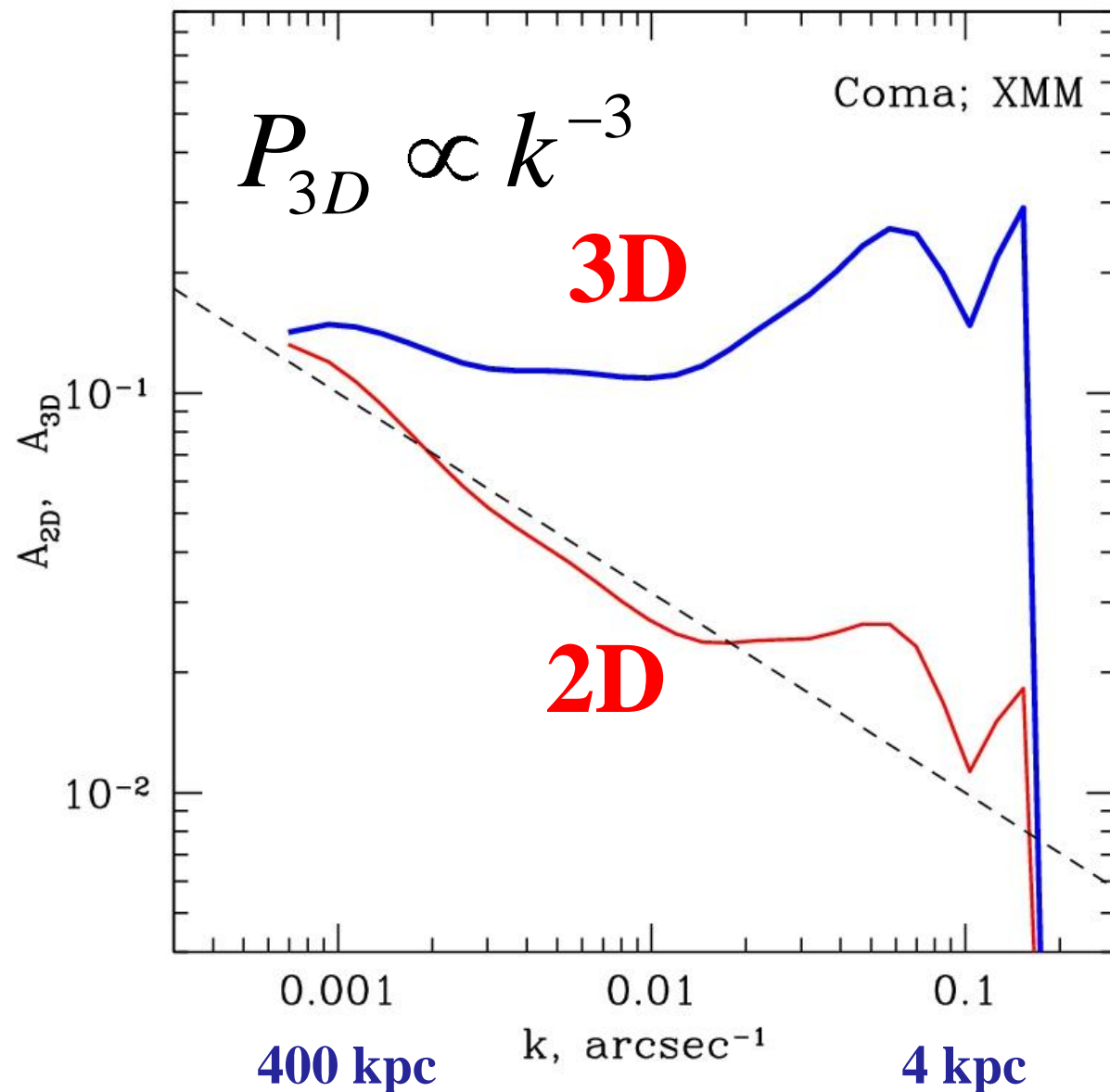
$$k \ll \frac{1}{l_z} \Rightarrow P_{2D} = aP_{3D} \times k$$



3D Density fluctuations in Coma

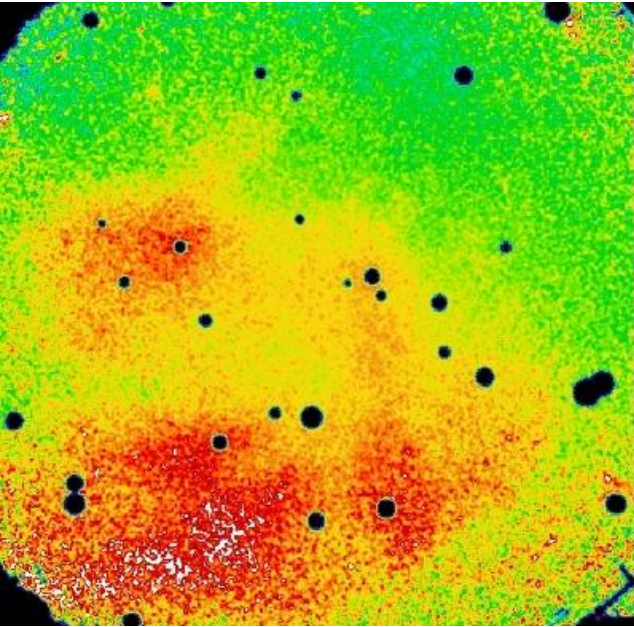
$$2 \frac{\delta n_e}{n_e}$$

$$\frac{\delta I}{I}$$

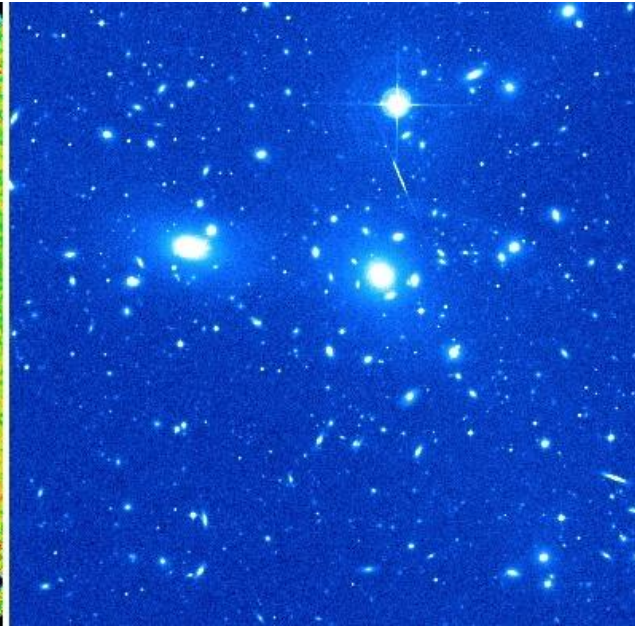


Density fluctuations ~5-10% on scales 4-400 kpc

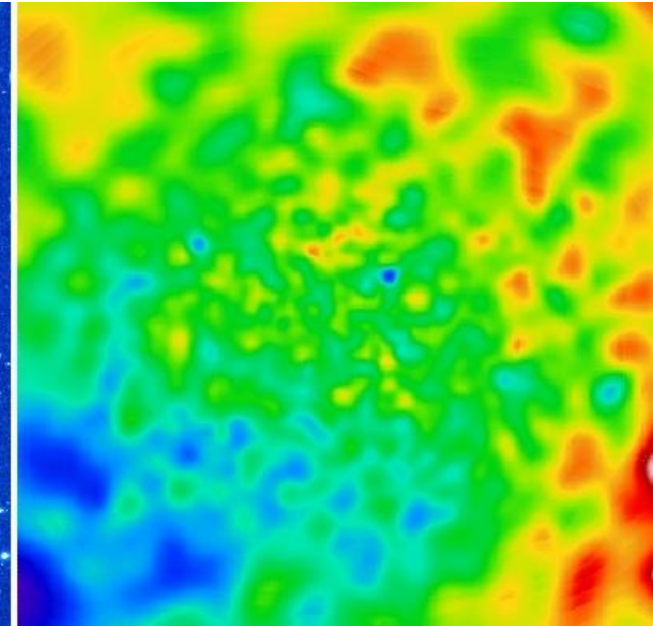
X-Image/ β



Optical



Gas T-map



**~5-10% density fluctuations include (4-400 kpc):
potential perturbation (big galaxies)
entropy fluctuations (infalling groups)**

$$P_{3D} \propto k^{-3}$$

Conclusions

ICM velocities ~ few 100 km/s
[except for mergers]

Direct V measurements ->
structure function

Modified MH method provides robust
measure of $V(k)$

We are approaching "precision ICMology"