

# Constraining axion inflation with gravitational waves across 29 decades in frequency

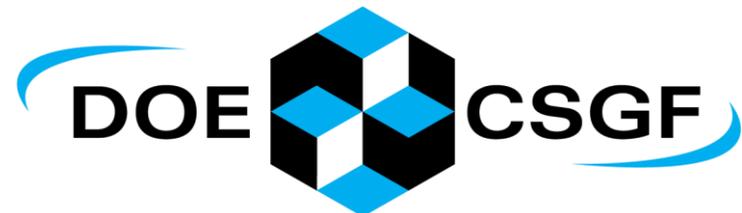
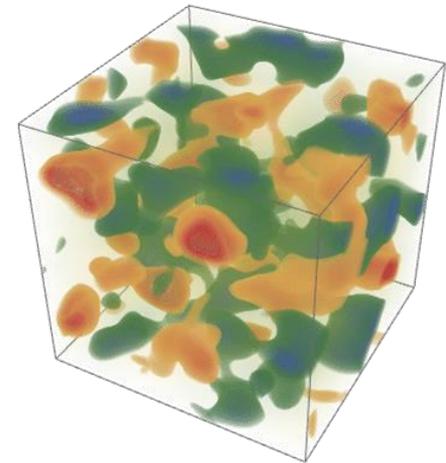
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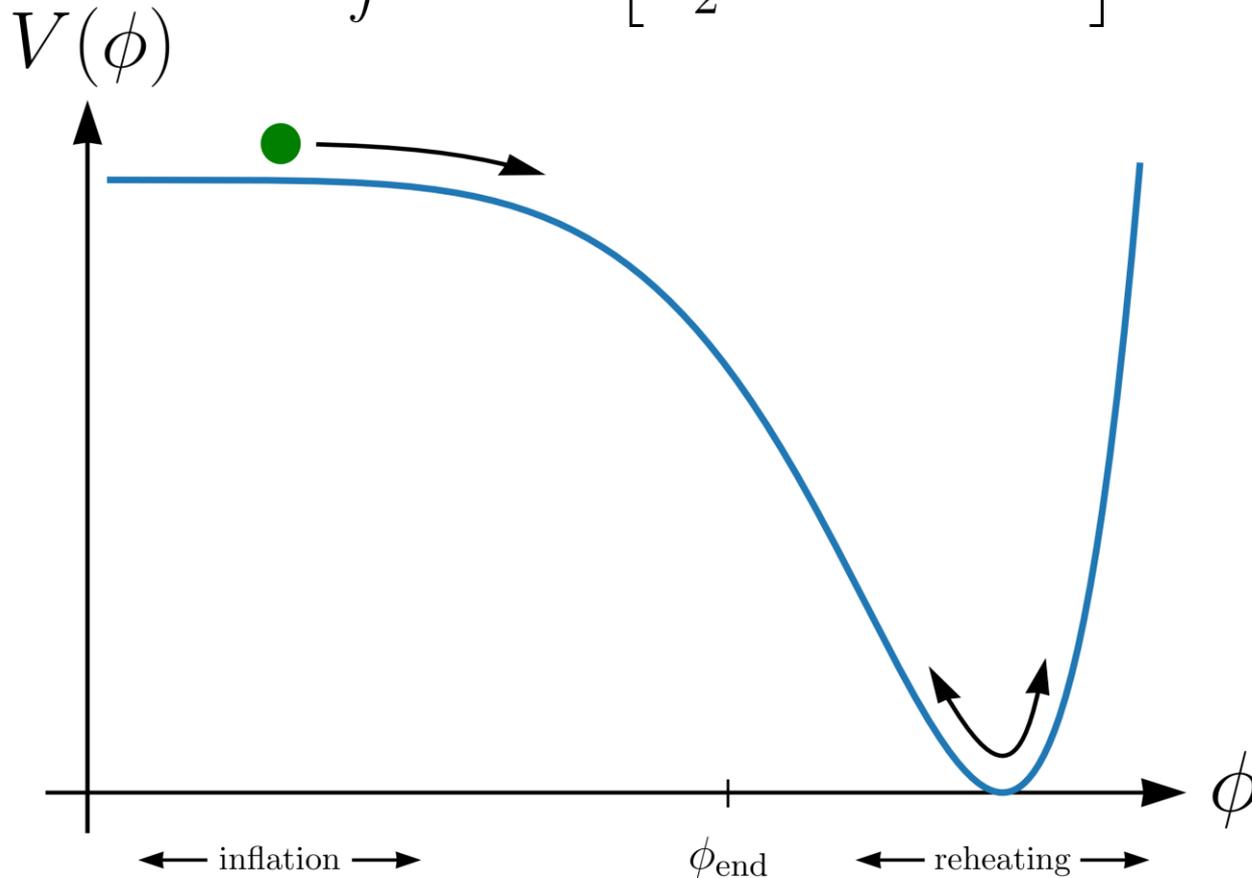
February 3, 2020

arXiv: 1909.12842 and 1909.12843  
with Peter Adshead, Tom Giblin, and Mauro Pieroni



# Why (p)reheating?

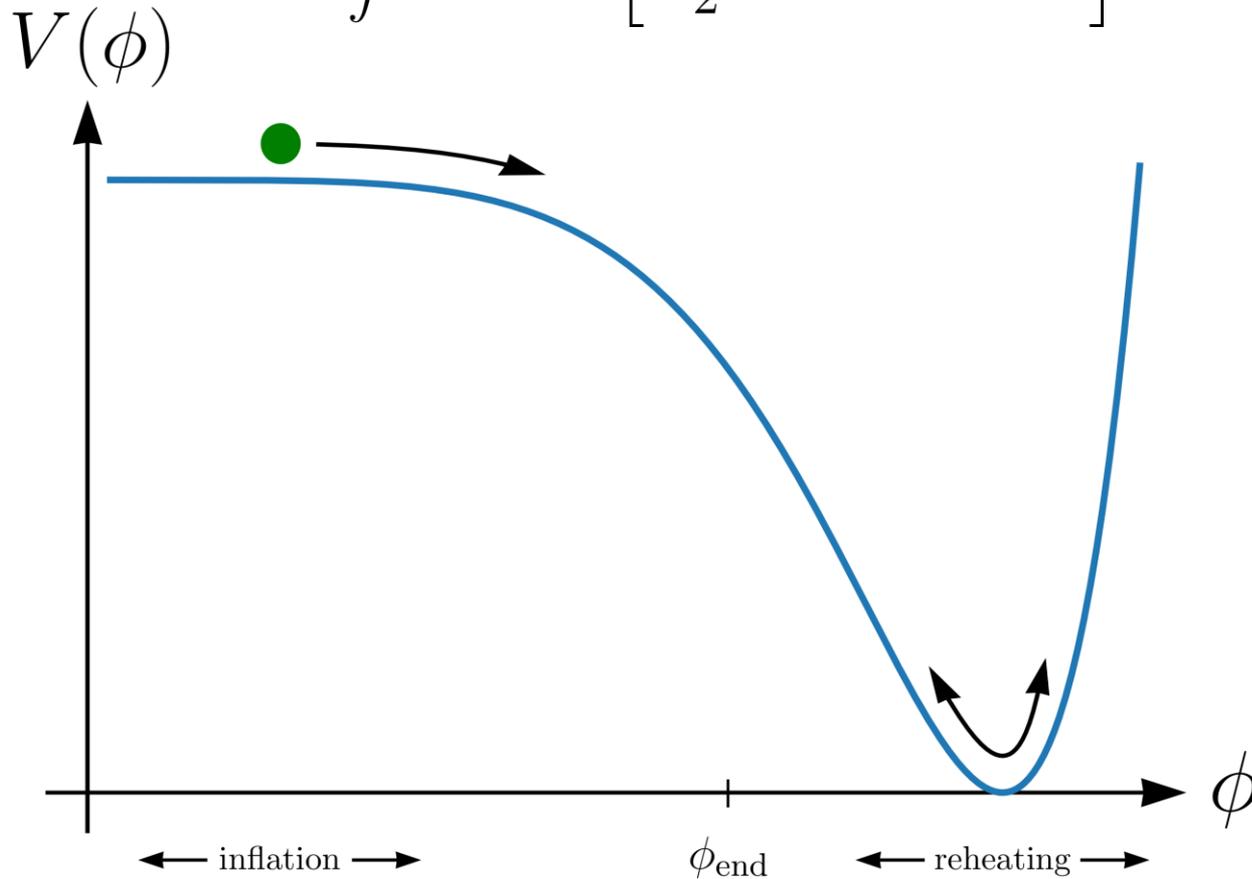
$$S = \int d^4x \sqrt{-g} \left[ -\frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) \right]$$



# Why (p)reheating?

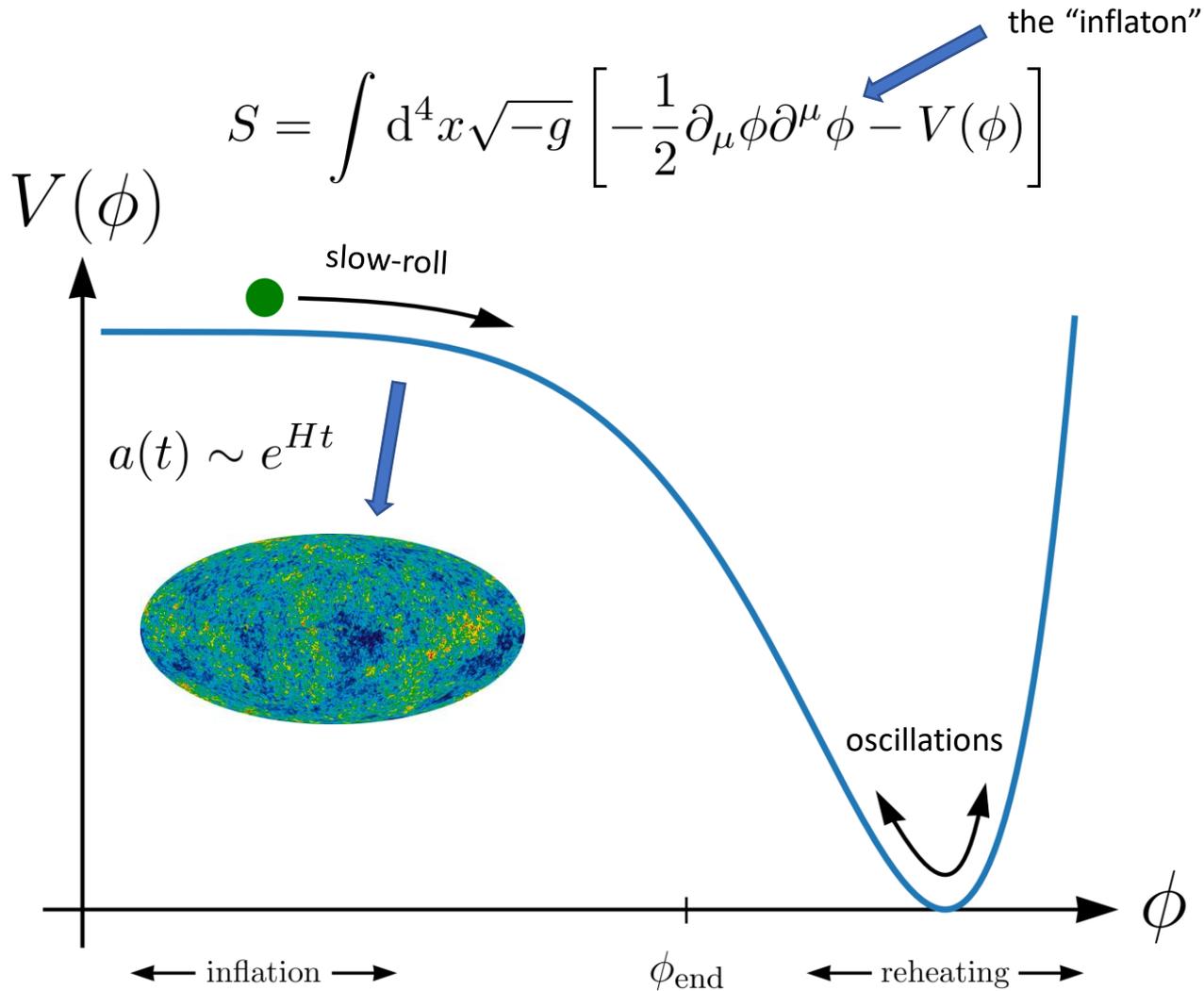
$$S = \int d^4x \sqrt{-g} \left[ -\frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) \right]$$

the "inflaton"

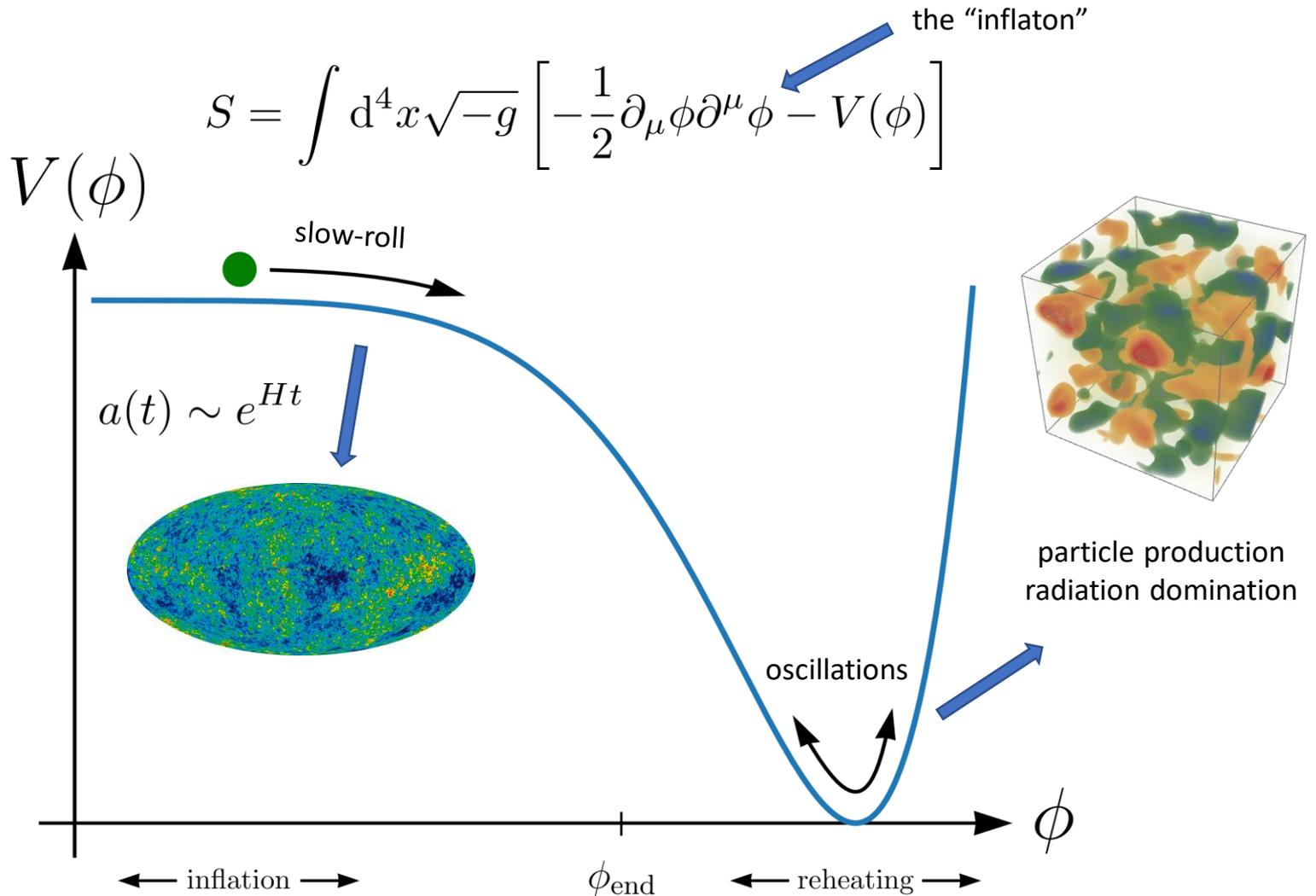




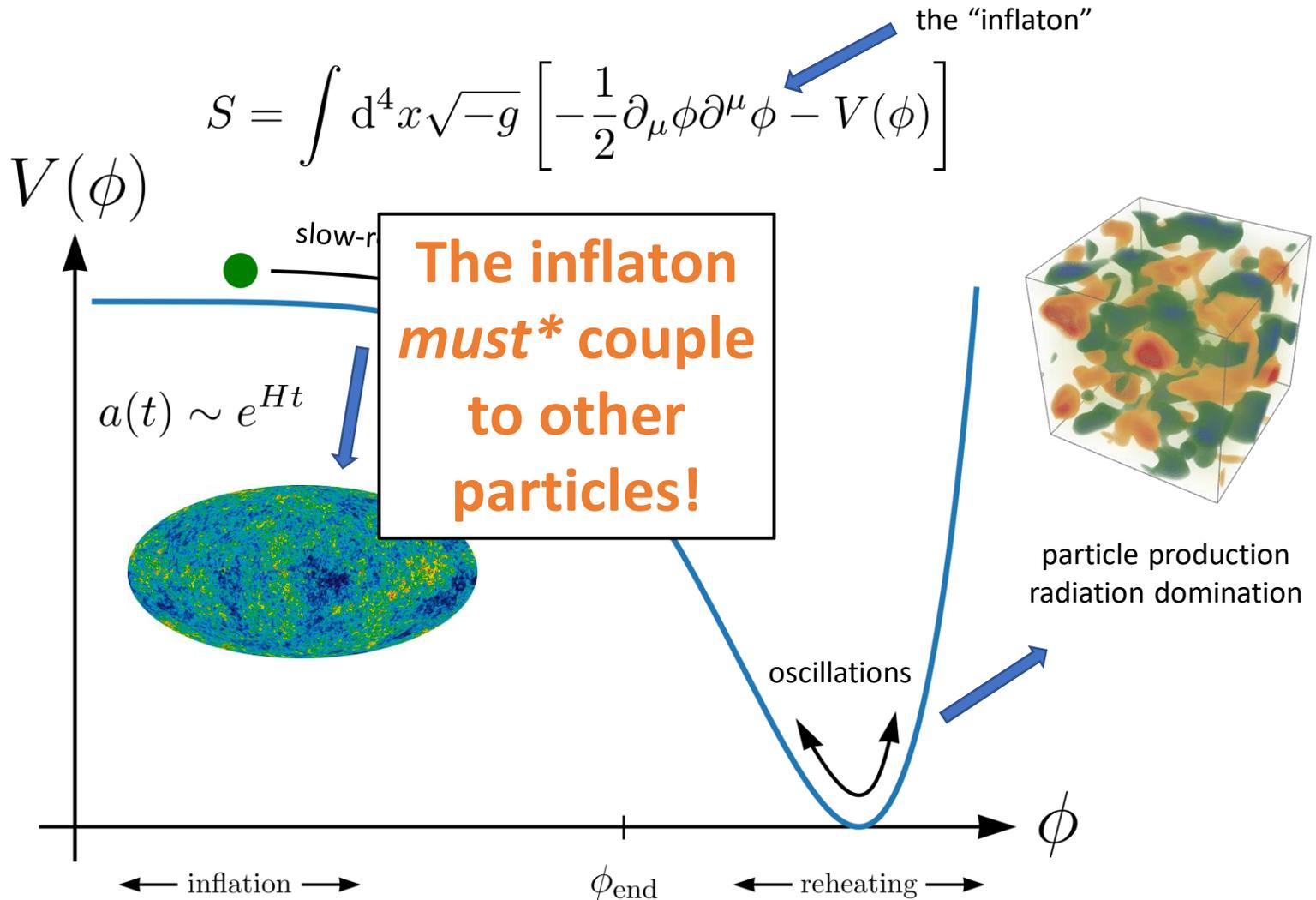
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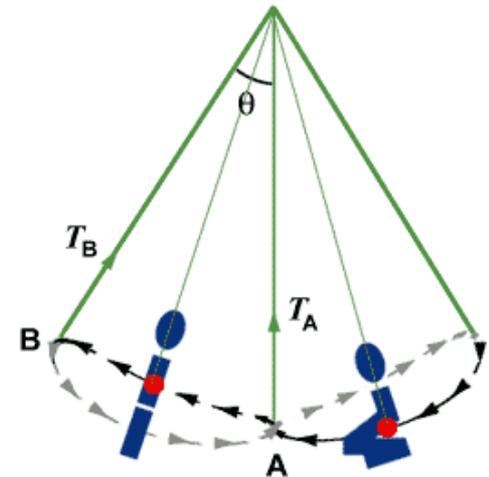


# Reheating via perturbative decay

- Couple the inflaton to some other field, compute its decay rate
- The Universe is **reheated** once decay becomes efficient
  - I.e., the lifetime is shorter than the Hubble time
- Limitations:
  - Ignores **coherent nature of inflaton**
  - Misses possible **nonperturbative** and **nonlinear** effects

# Preheating after inflation

- Perturbative reheating may be preceded by a phase of nonperturbative **preheating**
  - Exponential particle production, i.e., exponential growth of Fourier modes
  - Are induced by various types of **resonances** from the homogeneous oscillation of the inflaton
- Analogous to a child on a swing: pumping legs amplifies the amplitude of swinging



[http://www.hk-phy.org/articles/swing/swing\\_e.html](http://www.hk-phy.org/articles/swing/swing_e.html)

# Tachyonic resonance

- Schematically: interaction of the form

$$V_{\text{int}} = \frac{1}{2} \lambda \phi \chi^2$$

leads to the mode equation

$$\chi_k'' + (k^2 + \lambda \phi) \chi_k = 0$$

- Modes exhibit **exponential growth** whenever their squared effective frequency is negative:

$$k^2 + \lambda \phi_0 \sin(m_\phi t) < 0$$

# Reality check

- The Universe expands
  - Homogeneous inflaton is a **damped** harmonic oscillator
  - Momenta redshift in and out of instability bands
- The inflaton itself will **fragment**
  - $\chi$  particles can backreact onto the inflaton
- Need to eventually populate Standard Model (or SM-like) degrees of freedom

# Axial coupling to gauge fields

- Pseudoscalar axion  $\phi$  coupled to gauge fields:

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \underbrace{\frac{\alpha}{4f}\phi F_{\mu\nu}\tilde{F}^{\mu\nu}}_{\frac{\alpha}{f}\phi\mathbf{E}\cdot\mathbf{B}}$$

- System of equations:

$$\phi'' - \partial_i\partial_i\phi + 2\mathcal{H}\phi' + a^2\frac{dV}{d\phi} = -a^2\frac{\alpha}{4f}F_{\mu\nu}\tilde{F}^{\mu\nu}$$

$$A_i'' - \partial_j\partial_j A_i - \frac{\alpha}{f}\epsilon^{ikl}\phi'\partial_k A_l + \frac{\alpha}{f}\epsilon^{ikl}\partial_k\phi(A_l' - \partial_l A_0) = 0$$

# Tachyonic production of gauge bosons

- Linearized EOM of gauge-field polarizations:

$$A''_{\pm} + \underbrace{\left( k^2 \mp \frac{\alpha}{f} k \phi' \right)} A_{\pm} = 0$$

one polarization: negative effective frequency  $\rightarrow$  exponential growth for  $k < \frac{\alpha}{f} |\phi'|$

- Controlled by instability parameter,  $\xi \equiv \frac{\alpha}{f} \frac{\phi'}{2aH}$ :

$$A_{-}(k) \sim e^{|\xi|}$$

even during inflation!

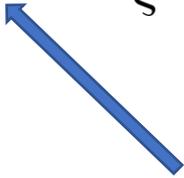
# Inflationary dynamics

- Gauge fields backreact onto inflaton background:

$$\bar{\phi}'' + 2\mathcal{H}\bar{\phi}' + a^2 \frac{dV}{d\bar{\phi}} = \frac{\alpha}{f} a^2 \langle \mathbf{E} \cdot \mathbf{B} \rangle$$

- In de Sitter limit,

$$\langle \mathbf{E} \cdot \mathbf{B} \rangle \simeq -2.4 \times 10^{-4} \text{sign}(\phi') \frac{H^4}{\xi^4} e^{2\pi|\xi|}$$



opposes inflaton's  
velocity  $\rightarrow$  friction!

# Phenomenology during inflation

- **Exponential enhancement** of gauge fields during axion inflation leads to
  - Polarized electromagnetic fields
  - Non-Gaussianity
  - Chiral gravitational waves
  - Primordial black holes
- Also (in principle) can realize **warm inflation**

# Preheating after axion inflation

- Important nonperturbative dynamics during inflation set the stage for preheating
- Nonlinear effects quickly become important

$$\phi'' - \partial_i \partial_i \phi + 2\mathcal{H}\phi' + a^2 \frac{dV}{d\phi} = -a^2 \frac{\alpha}{4f} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

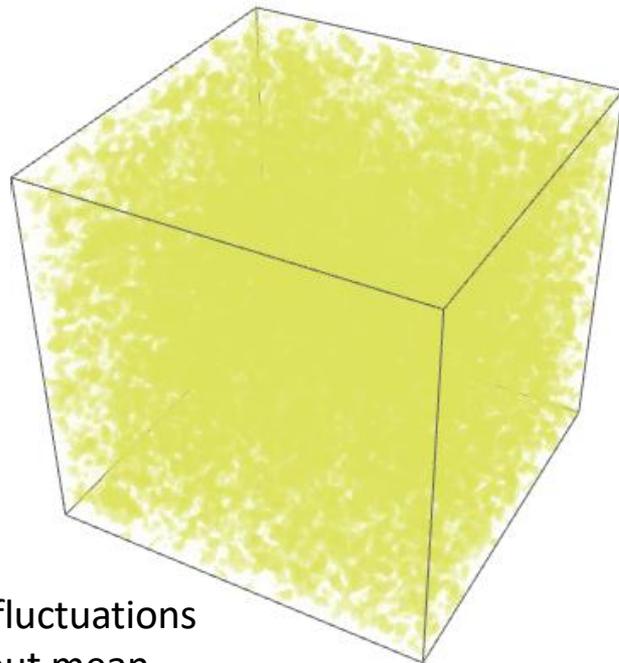
$$A_i'' - \partial_j \partial_j A_i - \frac{\alpha}{f} \epsilon^{ikl} \phi' \partial_k A_l + \frac{\alpha}{f} \epsilon^{ikl} \partial_k \phi (A_l' - \partial_l A_0) = 0$$

# Lattice simulations of preheating

classical fields: PDE initial-value problem

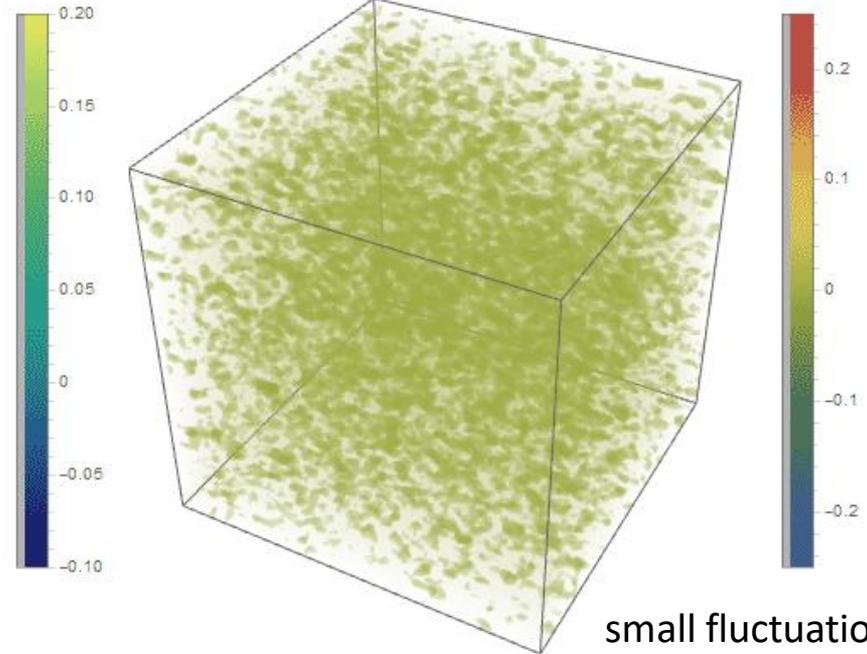
discretize onto a 3D grid

inflaton



small fluctuations  
about mean

coupled field



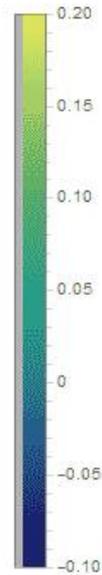
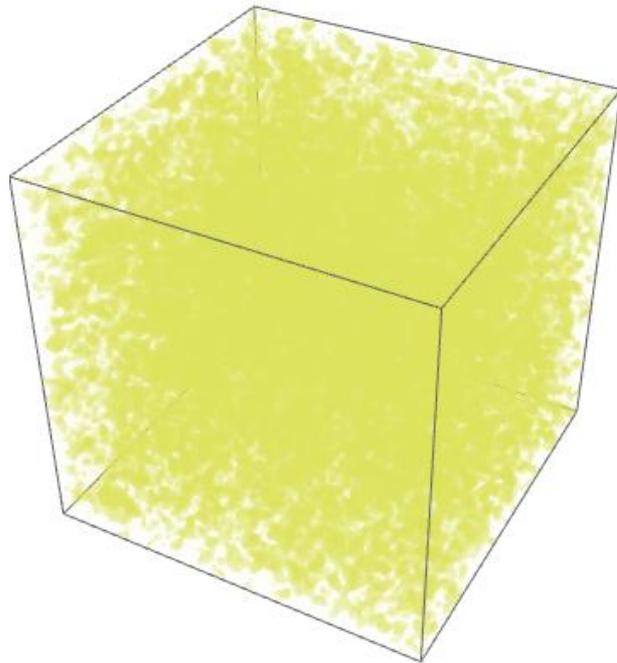
small fluctuations  
about zero

# Lattice simulations of preheating

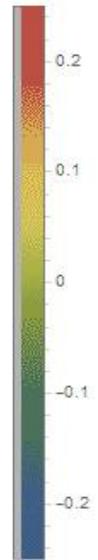
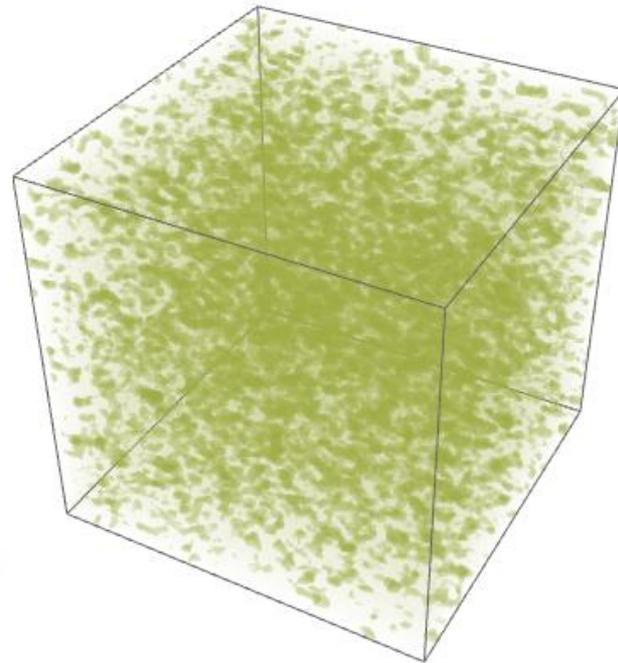
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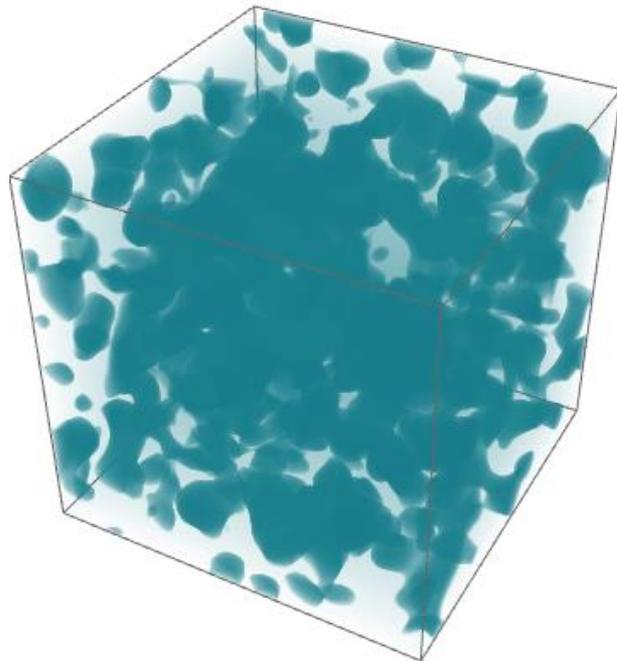


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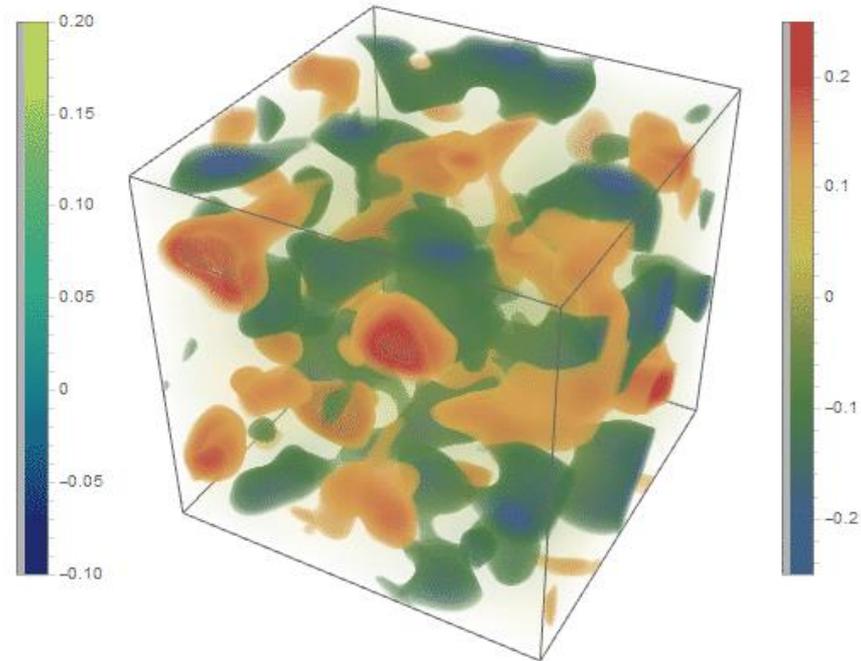
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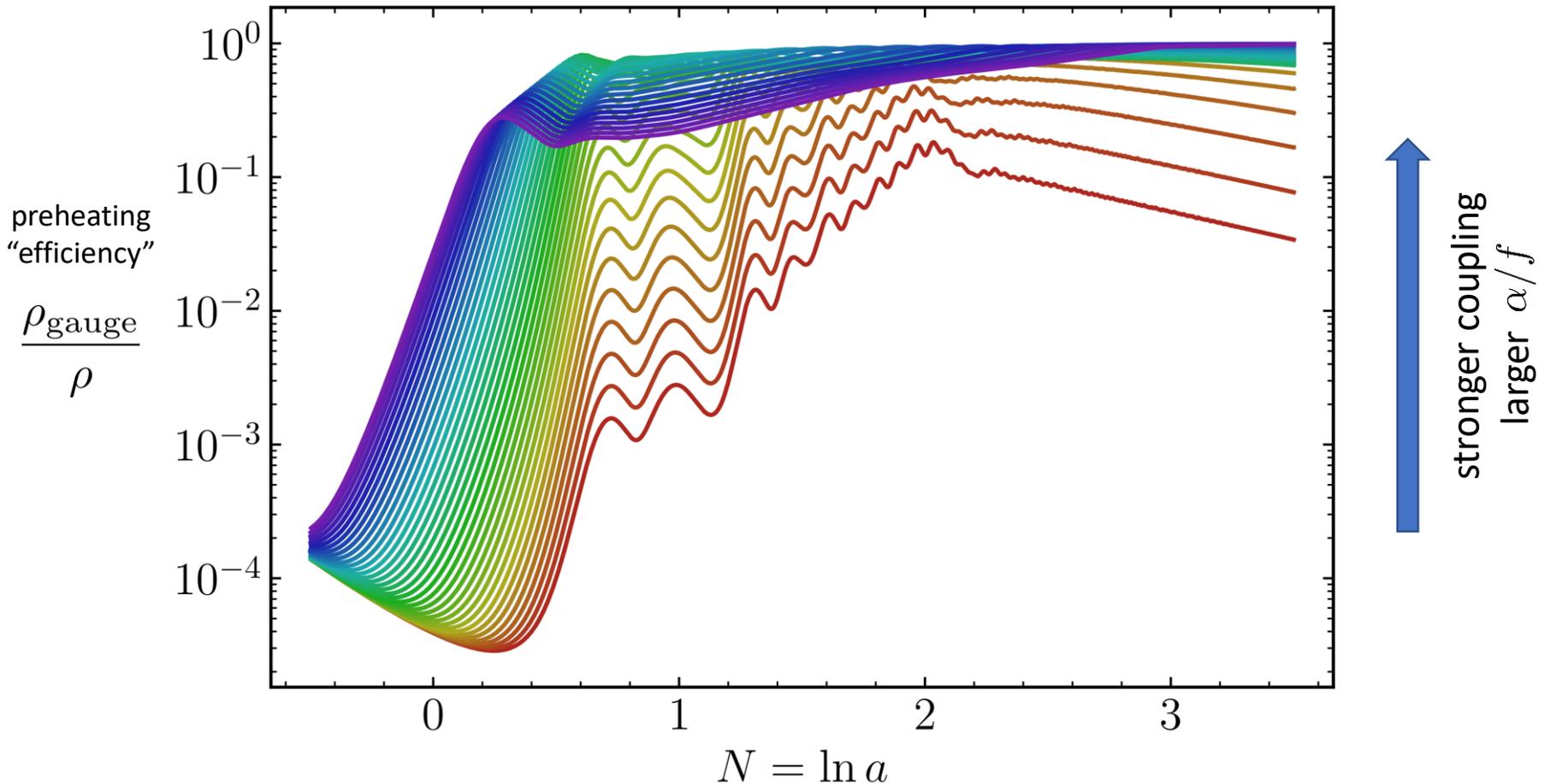
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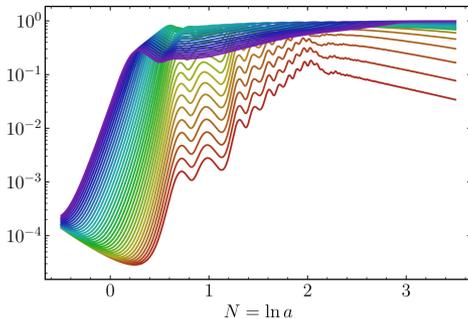
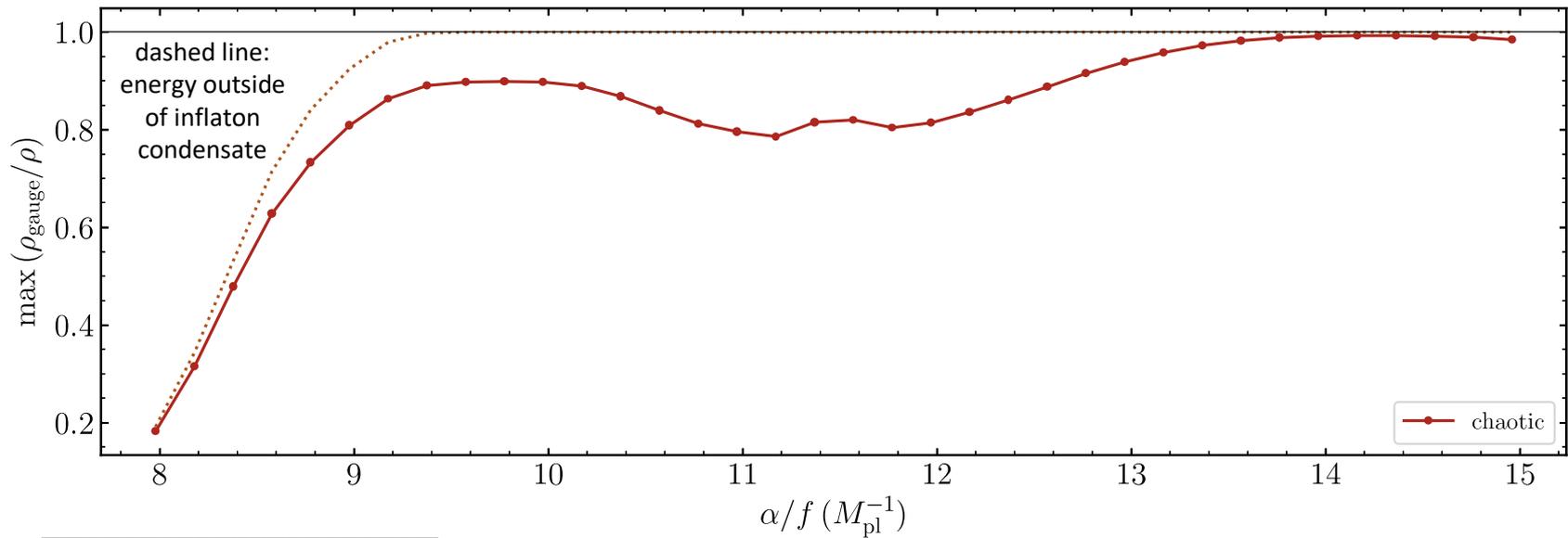


# Gauge preheating after inflation



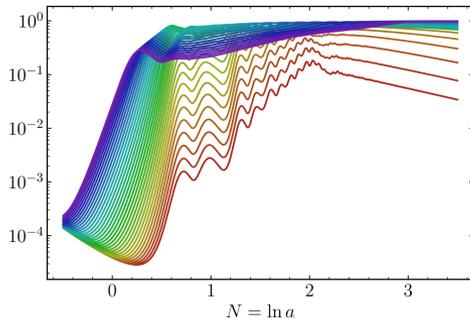
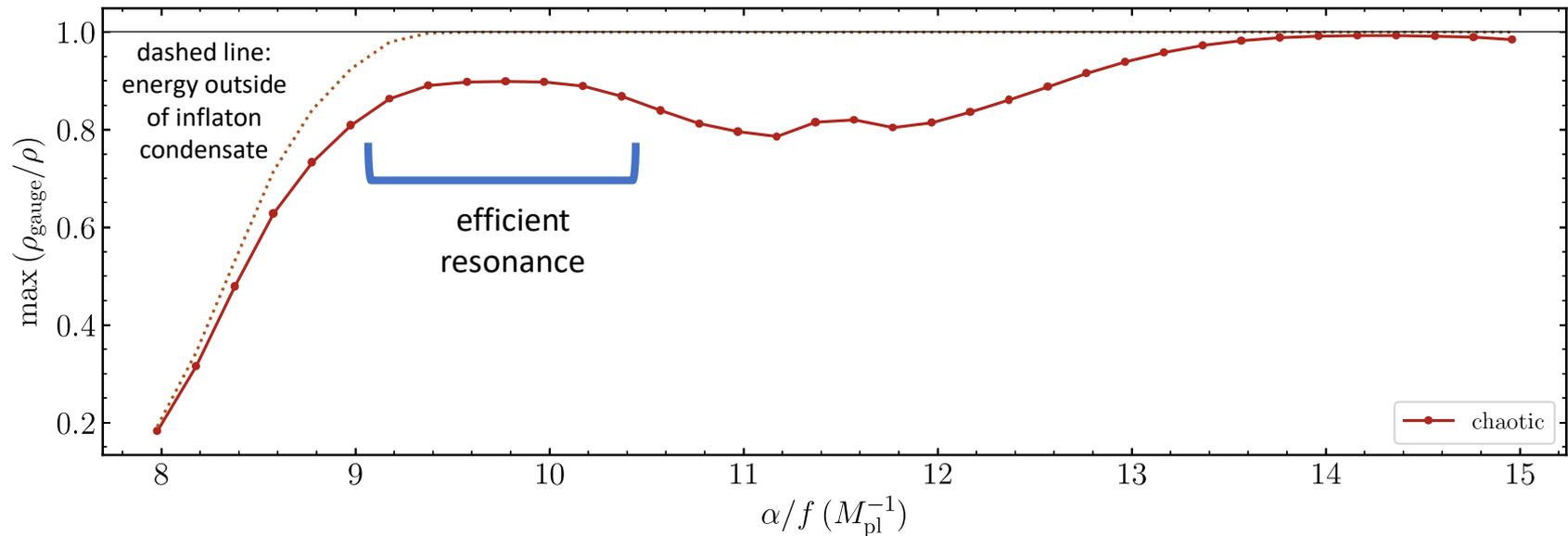
# Efficiency of preheating

$$A_i'' - \partial_j \partial_j A_i - \frac{\alpha}{f} \epsilon^{ijkl} \phi' \partial_k A_l + \frac{\alpha}{f} \epsilon^{ijkl} \partial_k \phi (A_l' - \partial_l A_0) = 0$$



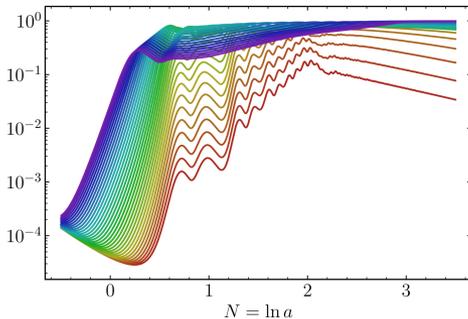
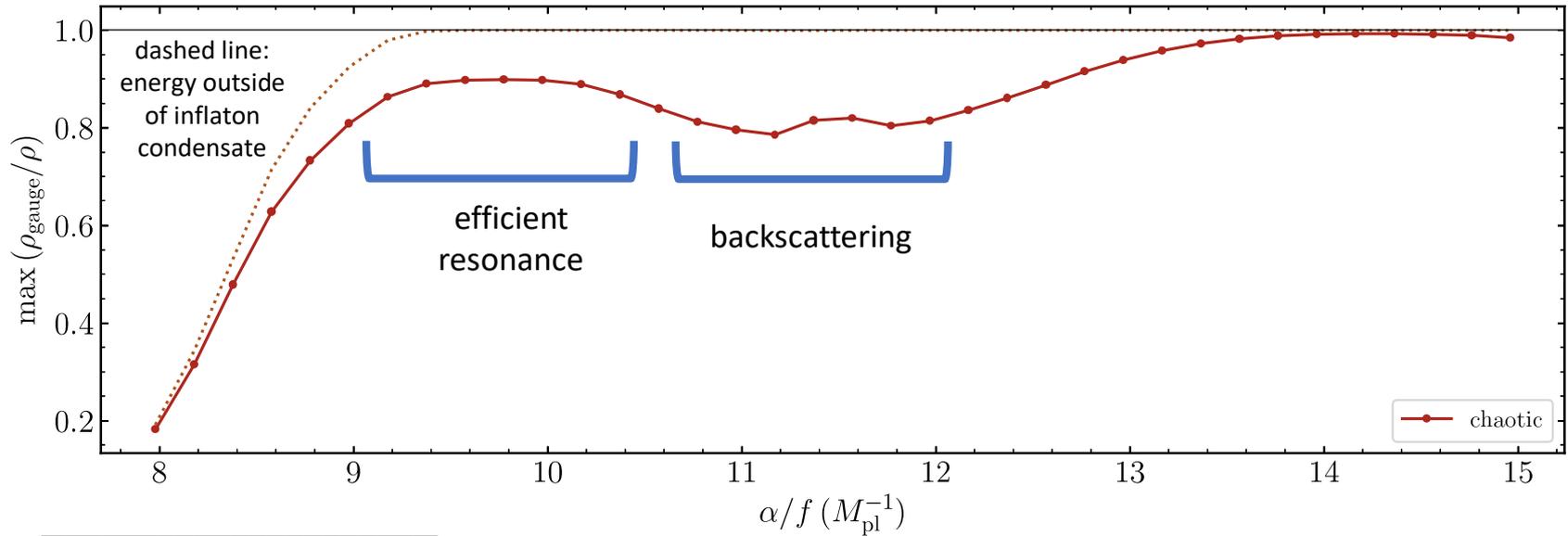
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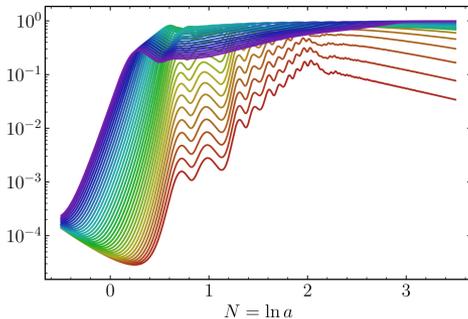
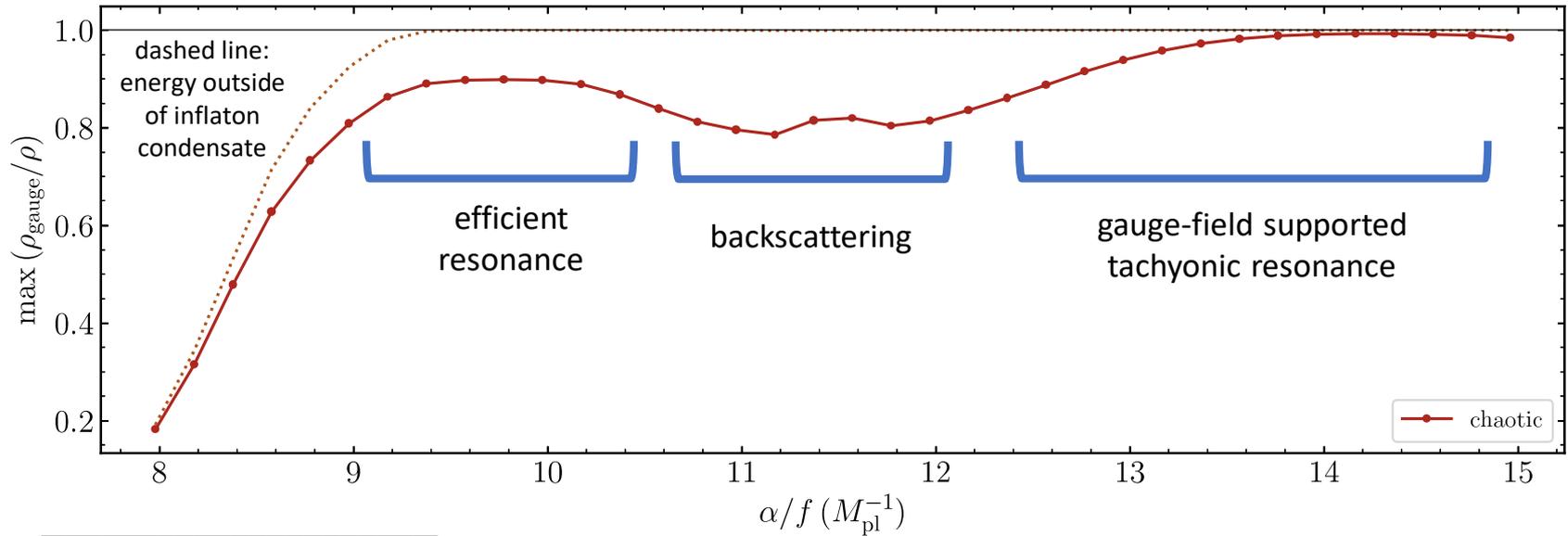
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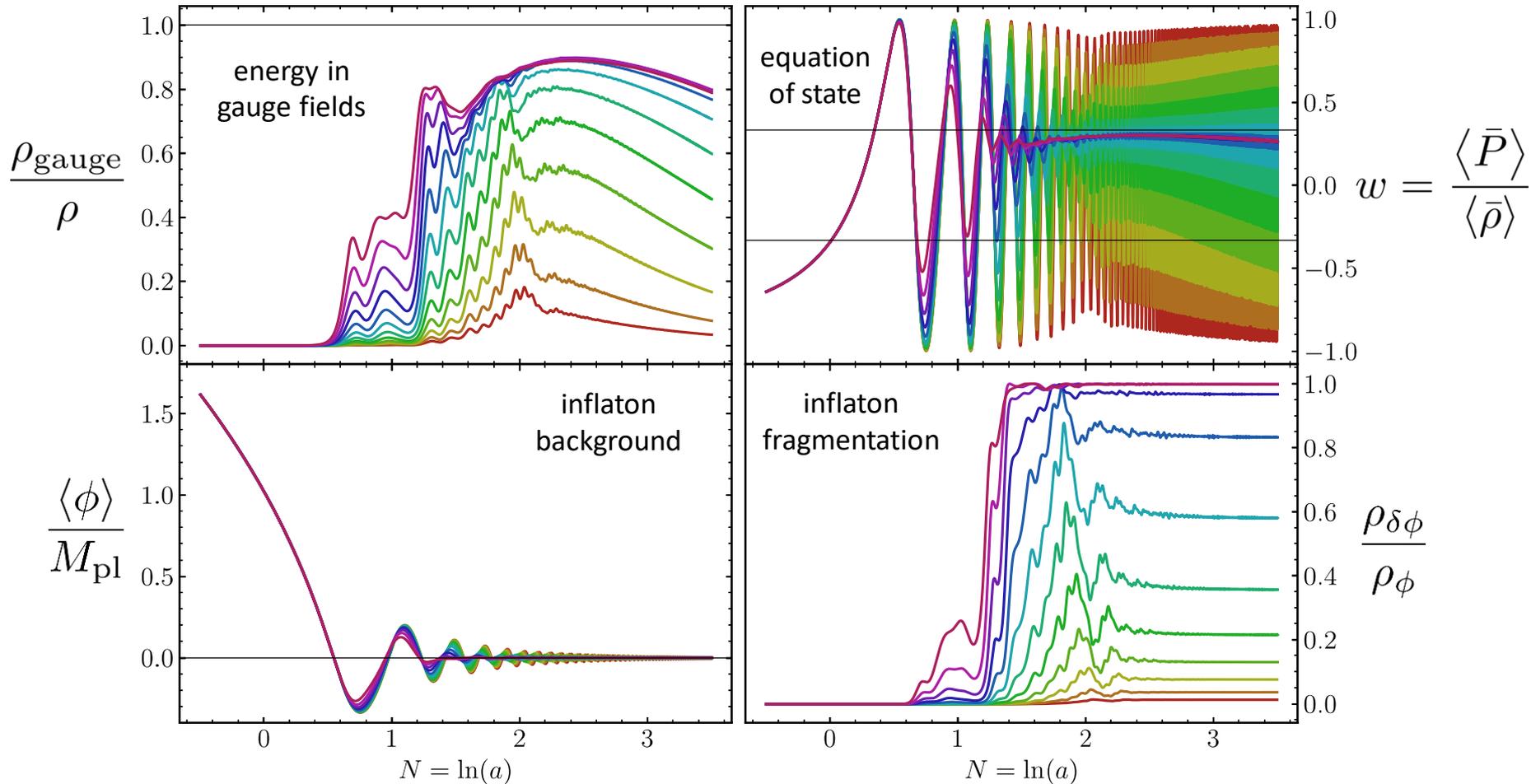


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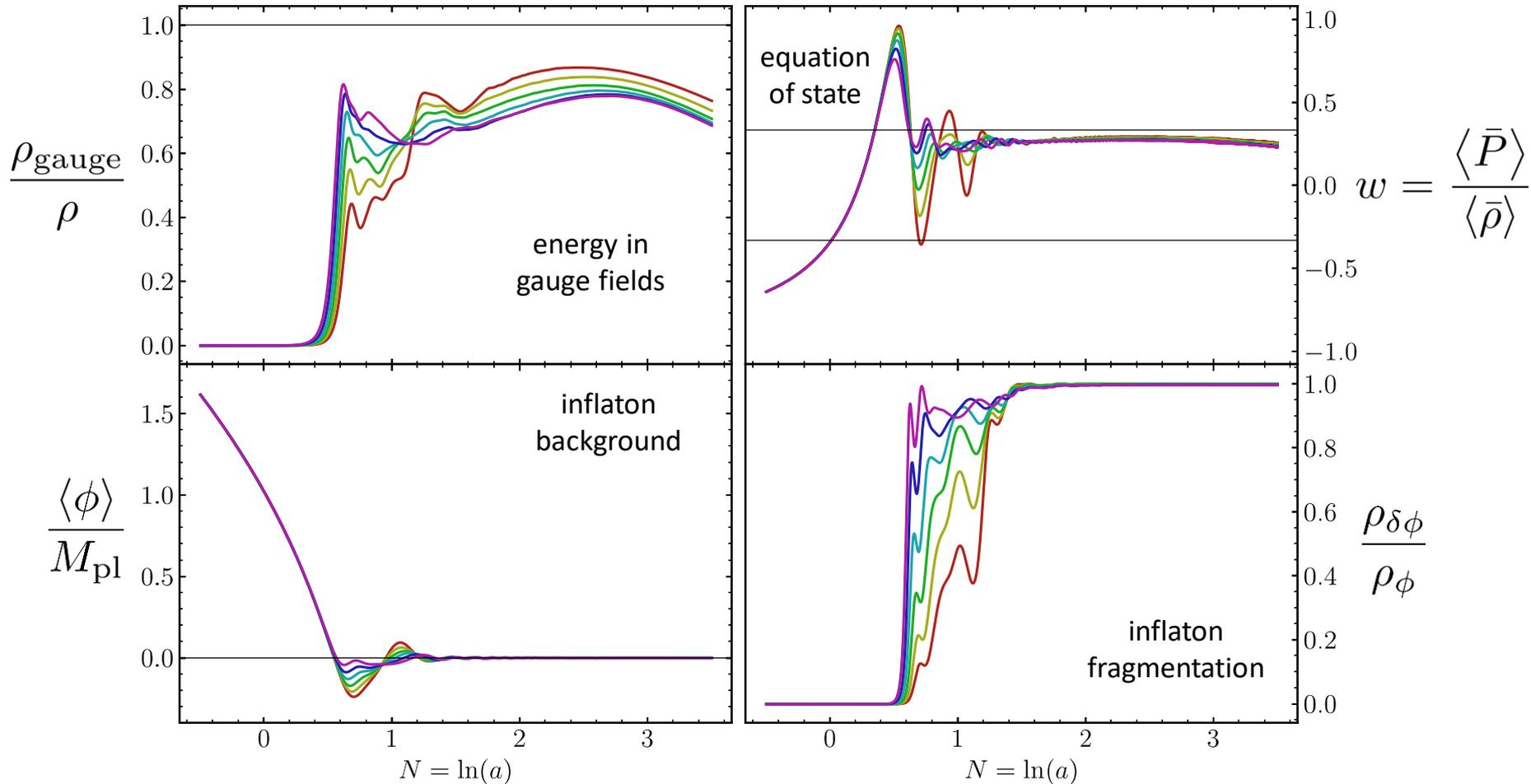
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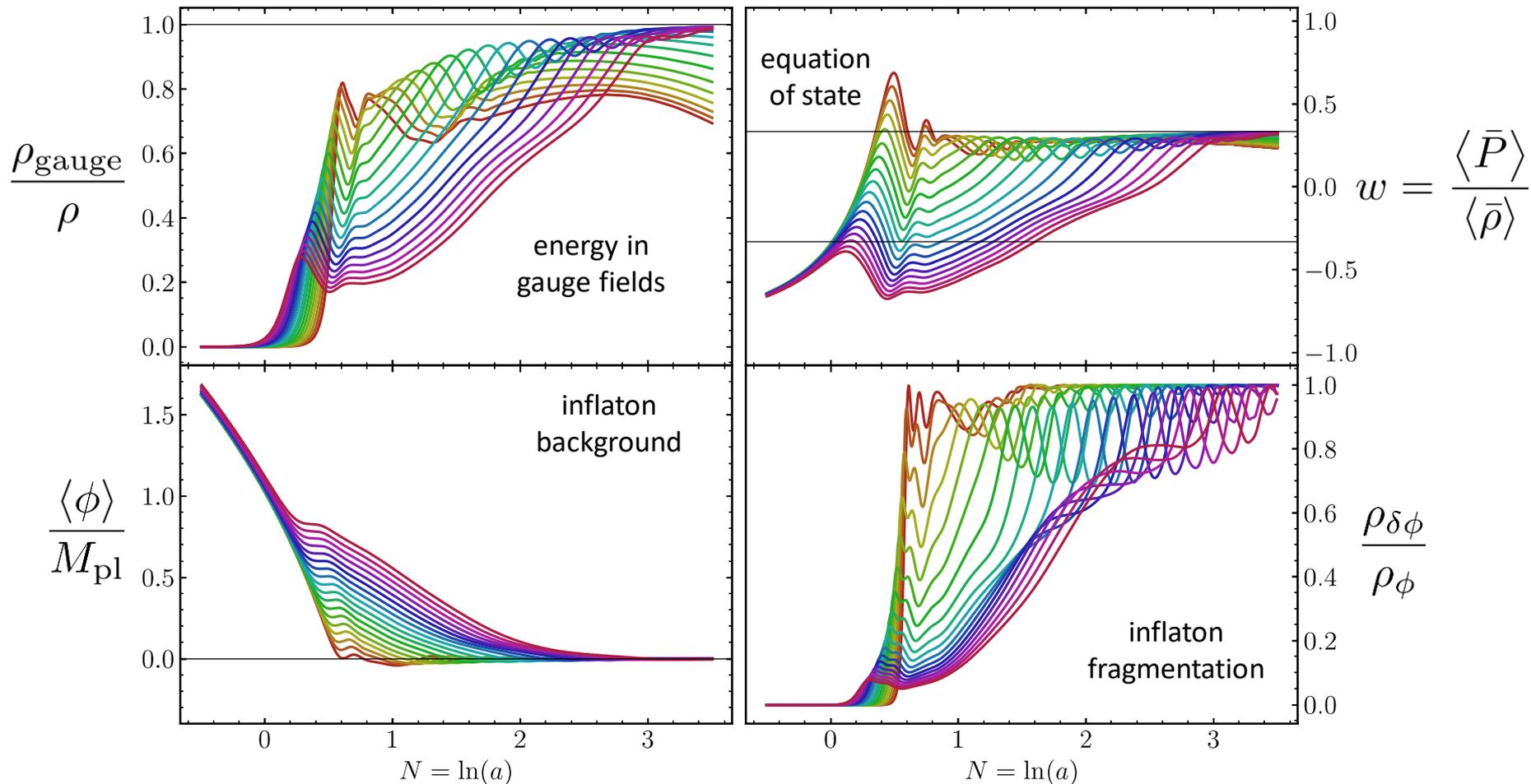
# Low coupling: efficient resonance



# Moderate coupling: backreaction



# High coupling: gauge-field supported tachyonic resonance



# Generation of gravitational waves

- Preheating generates **anisotropic stress**

$$T_{ij}^A = -\frac{1}{a^2} \left[ E_i E_j + B_i B_j + \frac{\delta_{ij}}{2} (\mathbf{E}^2 + \mathbf{B}^2) \right]$$
$$T_{ij}^\phi = \partial_i \phi \partial_j \phi - a^2 \delta_{ij} \left( \frac{1}{2} \partial_\mu \partial^\mu \phi + V(\phi) \right)$$

which sources **gravitational waves**

$$h''_{ij} - \nabla^2 h_{ij} + 2\mathcal{H}h'_{ij} = \frac{2}{M_{\text{pl}}^2} T_{ij}^{\text{TT}}$$



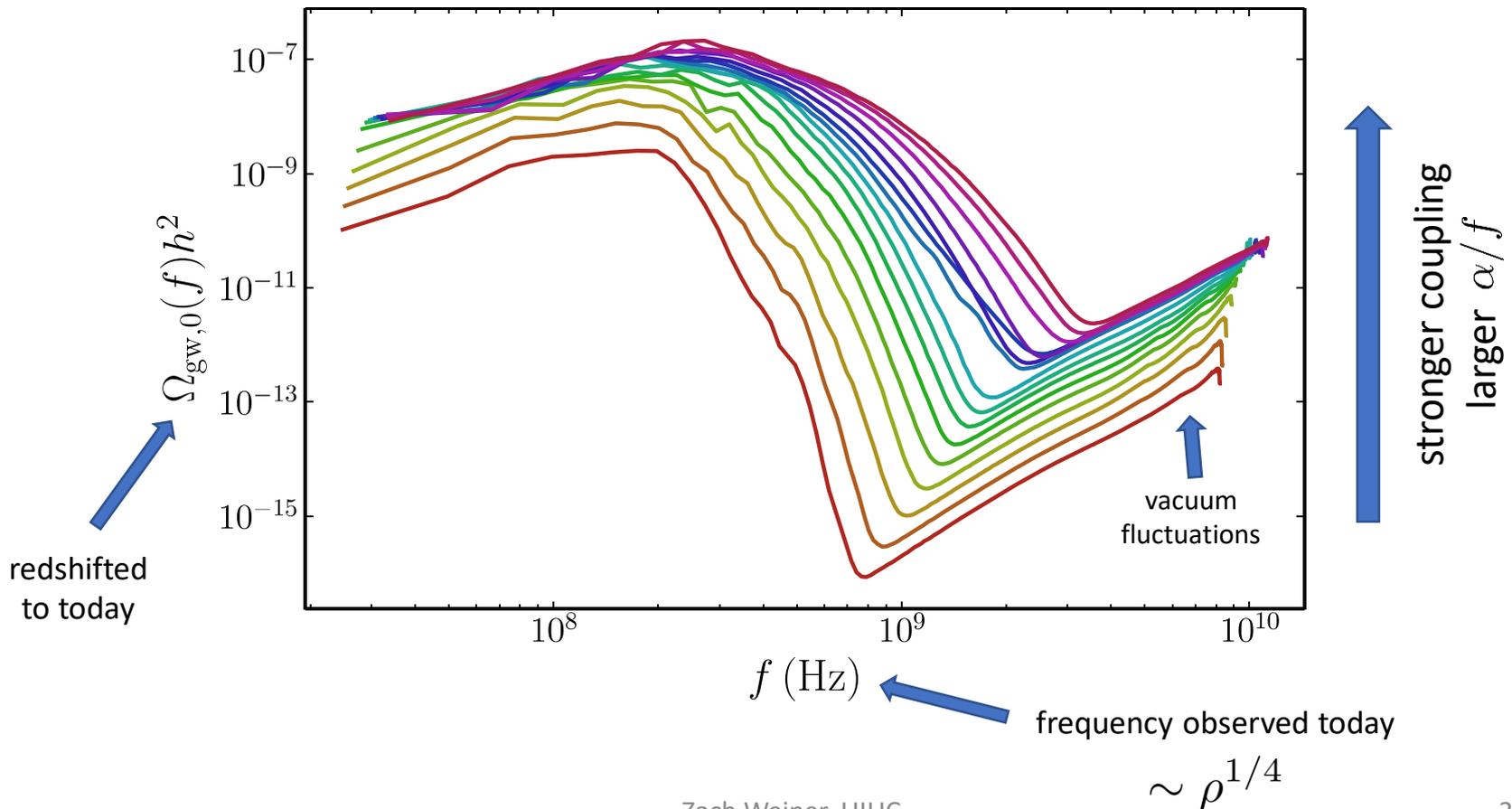
linear, inhomogeneous PDE



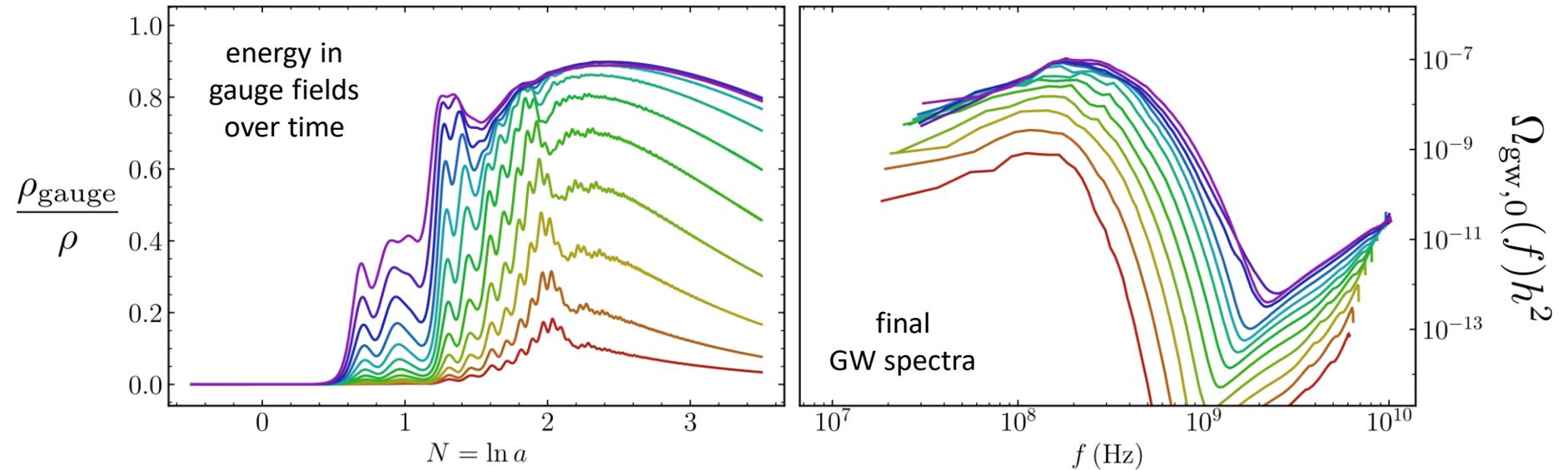
transverse-traceless  
projection of the  
stress tensor

# Generation of gravitational waves

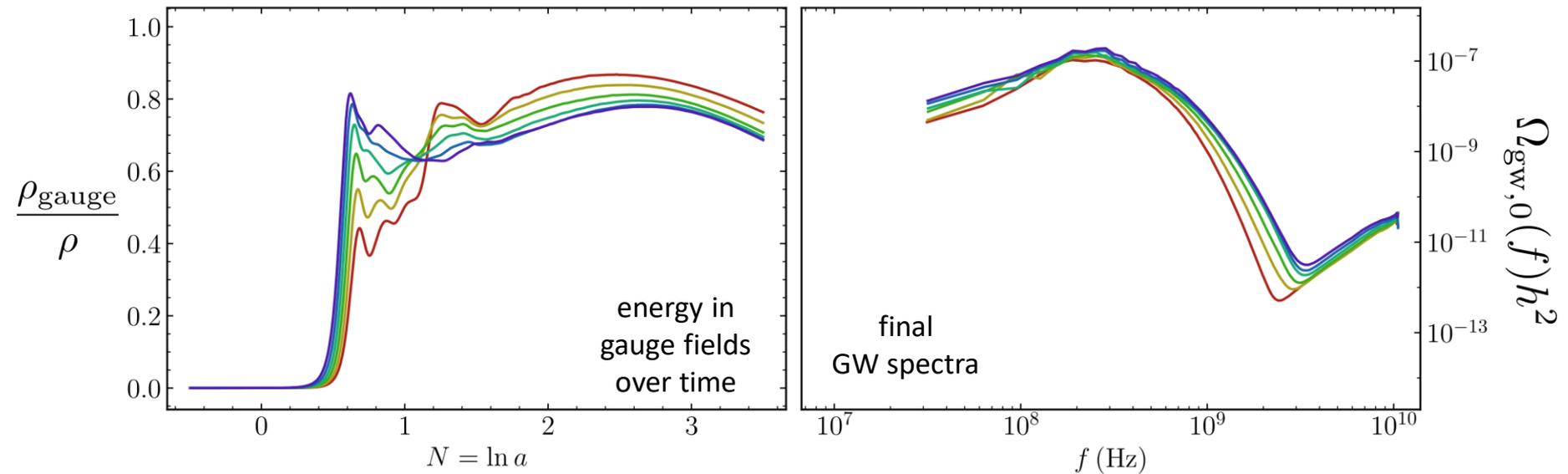
$$\Omega_{\text{gw}}(k) \equiv \frac{1}{\rho} \frac{d\rho_{\text{gw}}}{d \ln k} = \frac{1}{24\pi^2 L^3 \mathcal{H}^2} \sum_{\lambda} |h_k^{\lambda'}(\tau)|^2$$



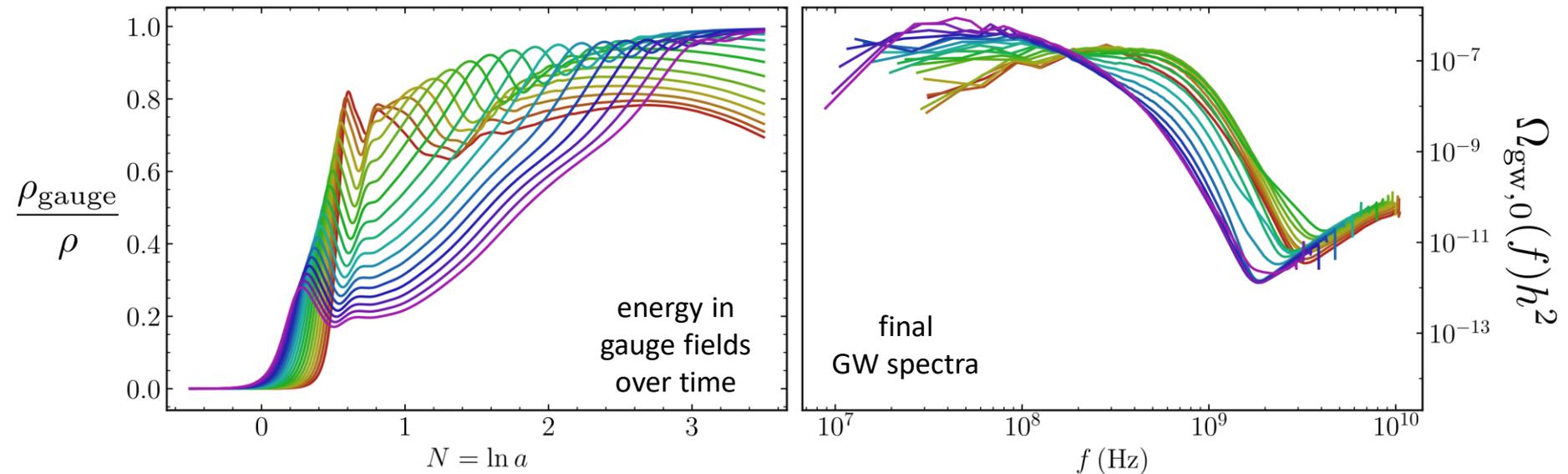
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# Constraints from $N_{\text{eff}}$

- As radiation, GWs contribute to the effective number of relativistic degrees of freedom:

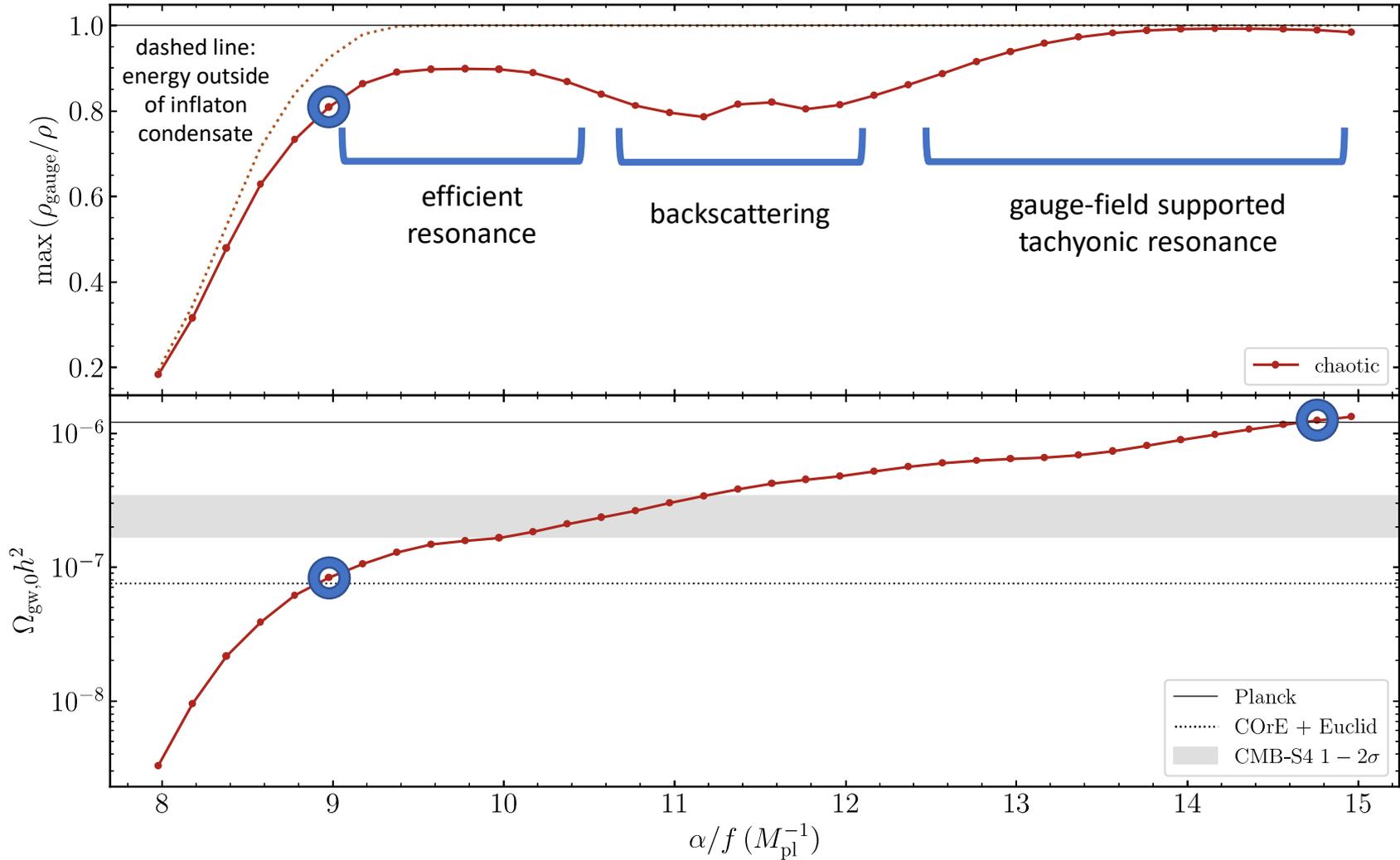
$$\frac{\Omega_{\text{gw},0} h^2}{\Omega_{\gamma,0} h^2} = \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \Delta N_{\text{eff}}$$

- CMB-S4 will probe  $\Delta N_{\text{eff}}$  to a level that would constrain\*

$$\Omega_{\text{gw},0} h^2 \lesssim 7.6 \times 10^{-8}$$

$$(\Omega_{\text{radiation},0} h^2 \sim 10^{-5})$$

# Efficiency of GW production



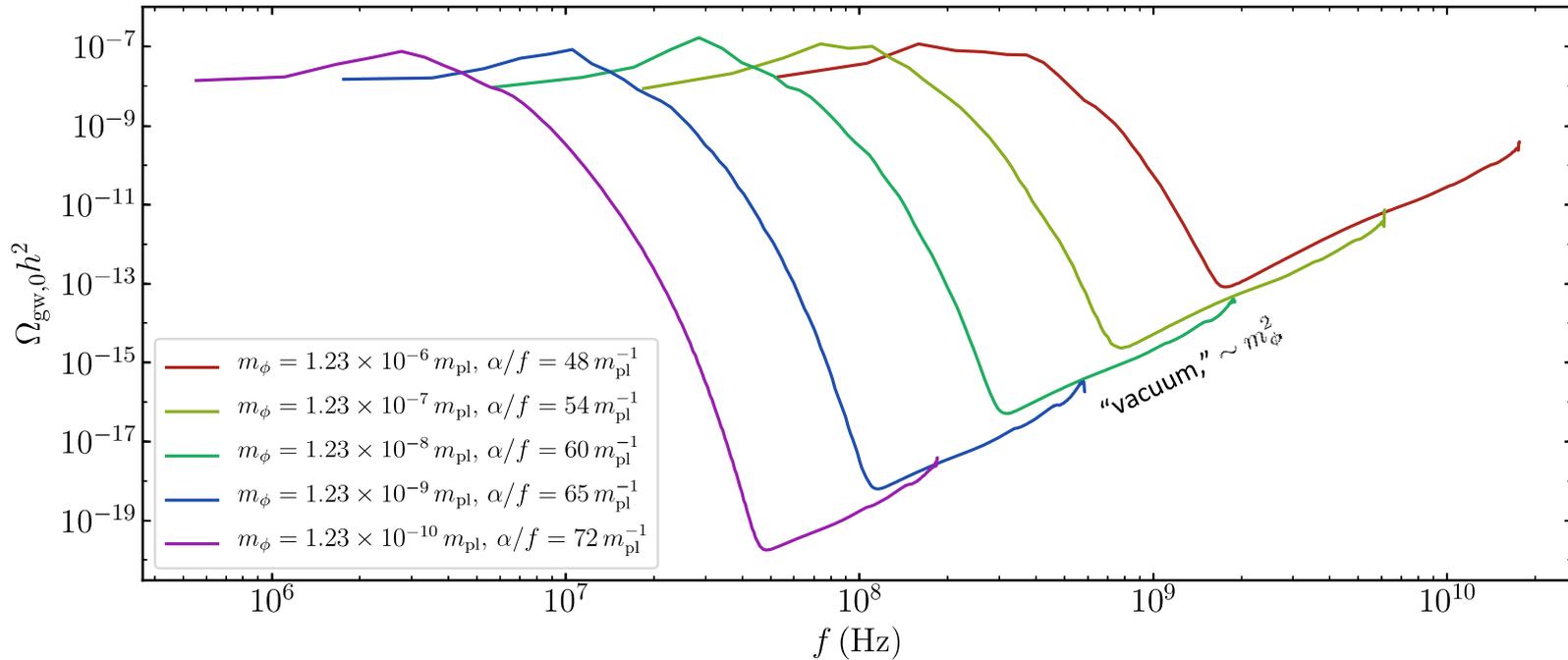
# Dependence on the potential?

- Planck 2018, 68% CL:

$$n_s \simeq 0.9649 \pm 0.0042$$
$$r < 0.1$$

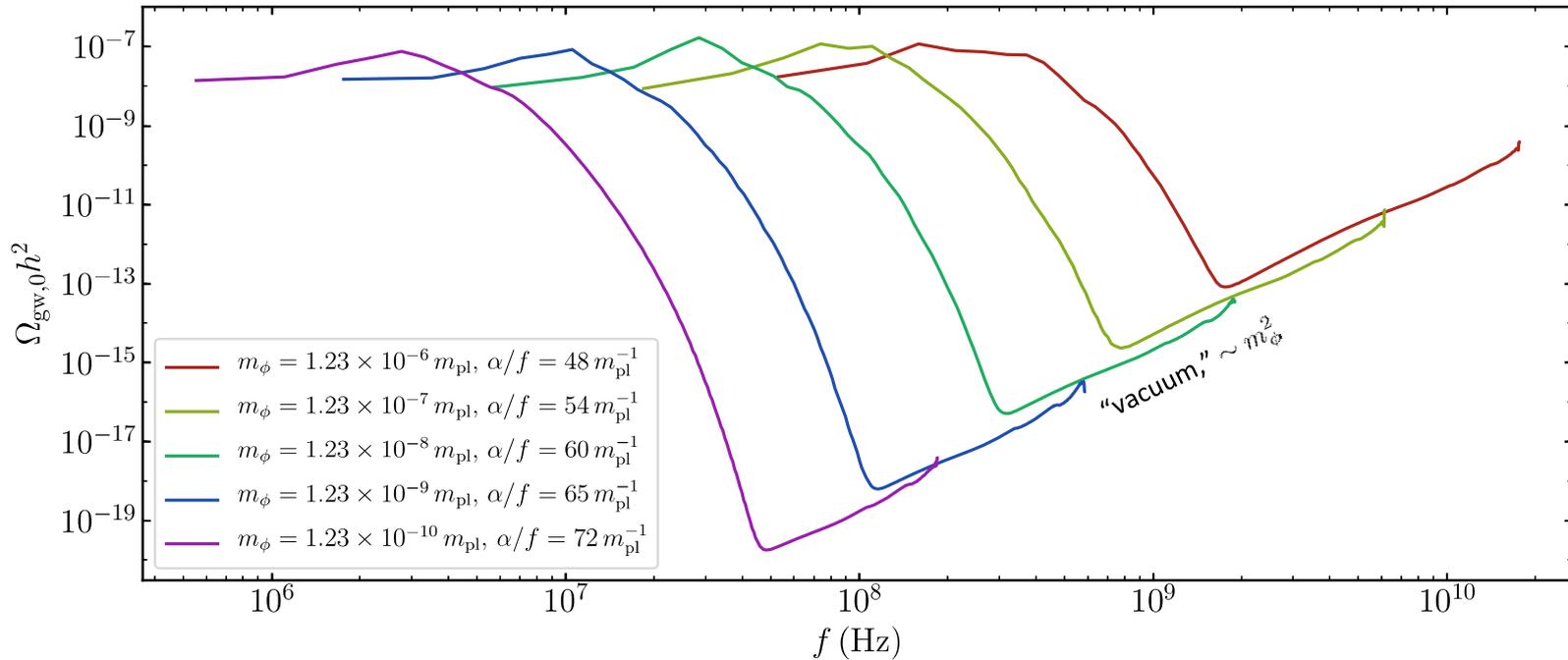
- Chaotic inflation is in fact **disfavored** at the 95% CL
- Quadratic potential models oscillations about a generic potential's minimum to leading order
  - Does the true **shape** of the potential matter?
- Does the inflationary **energy scale** have an effect?

# Scaling of the GW spectrum



$$\sim \sqrt{m_\phi m_{\text{pl}}}$$

# Scaling of the GW spectrum



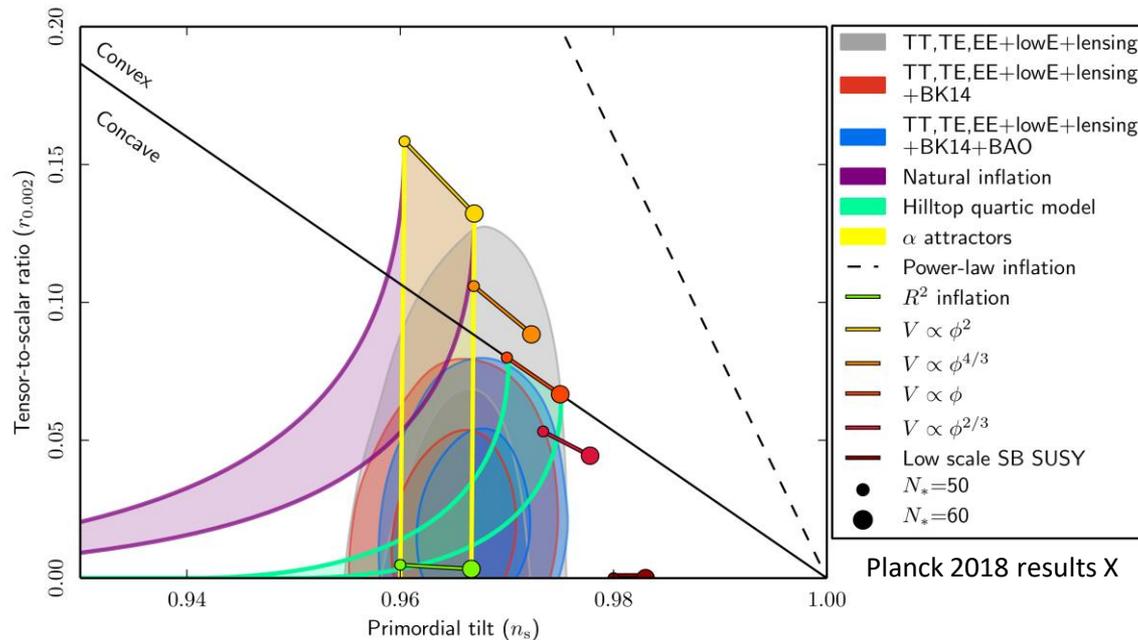
$$\sim \sqrt{m_\phi m_{\text{pl}}}$$

direct detection?

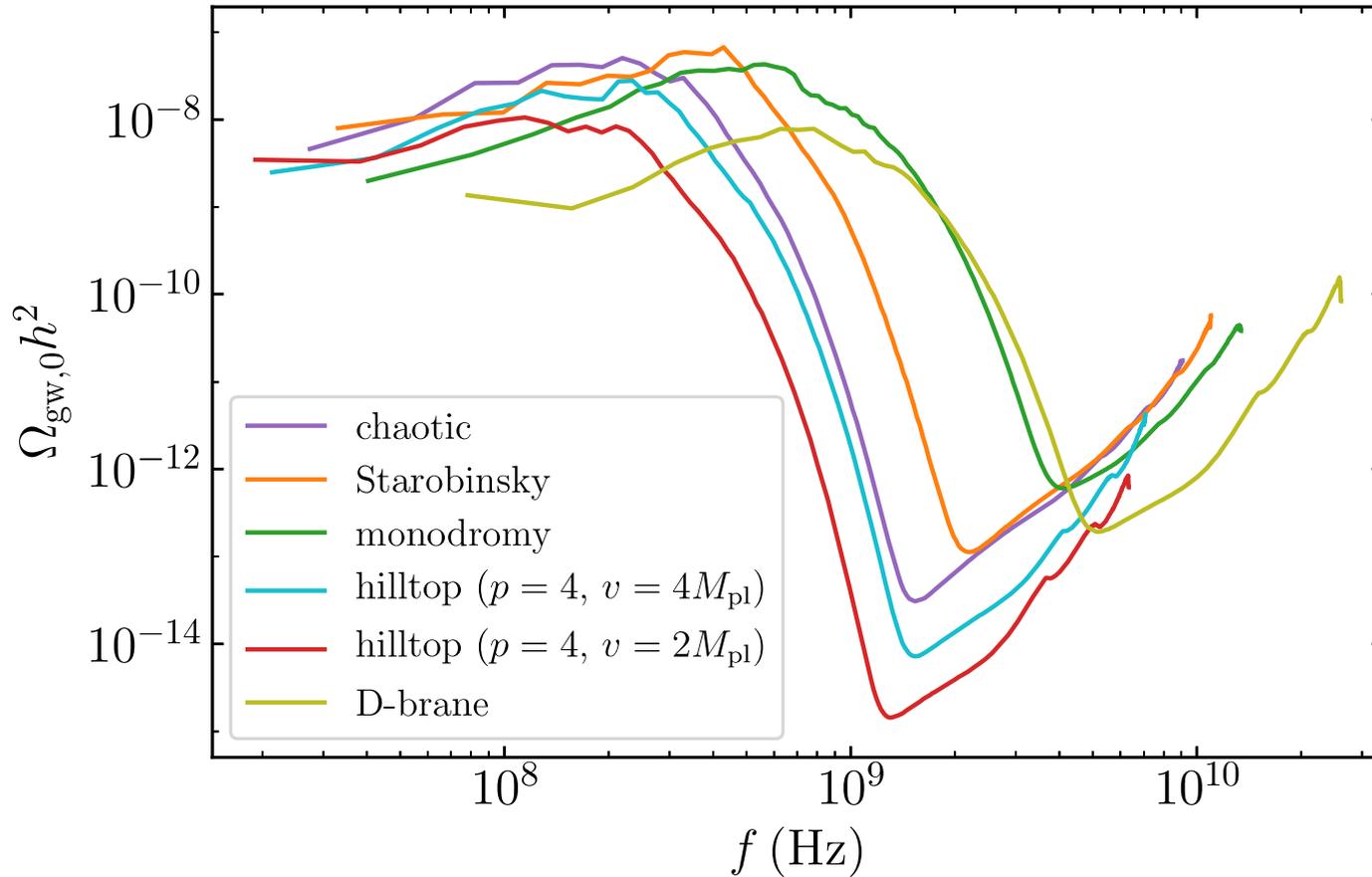
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# What about the shape of the potential?

- Models are characterized by predicted scalar tilts and tensor-to-scalar ratios
- Is there a connection to preheating/GW production?

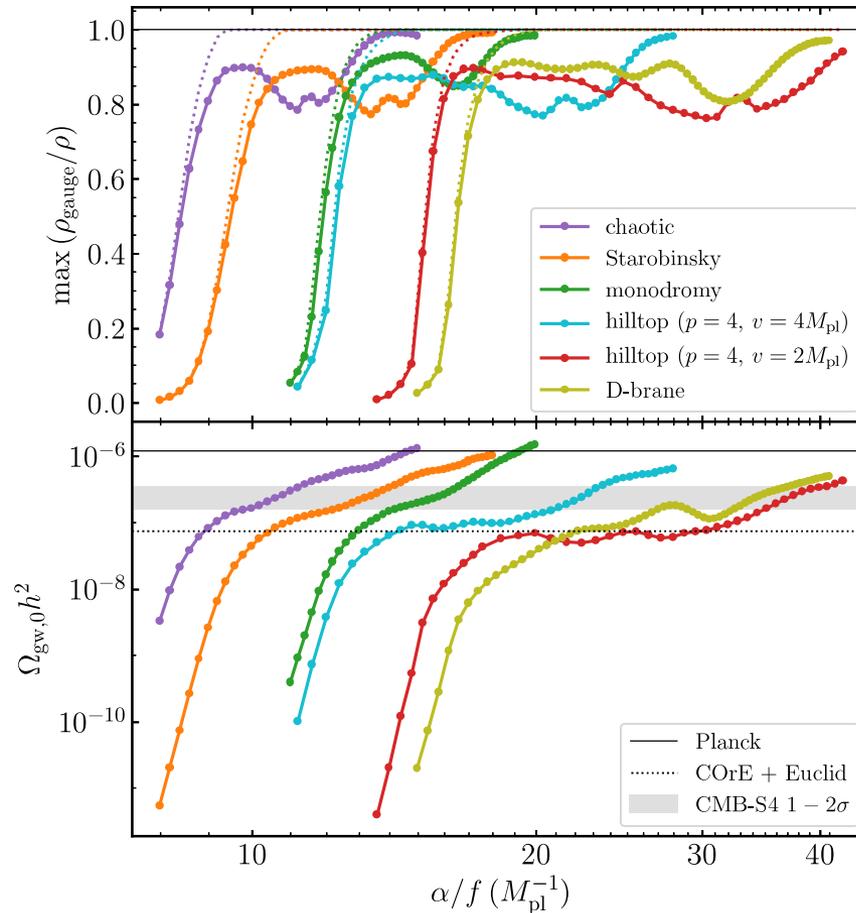


# Gravitational wave signals

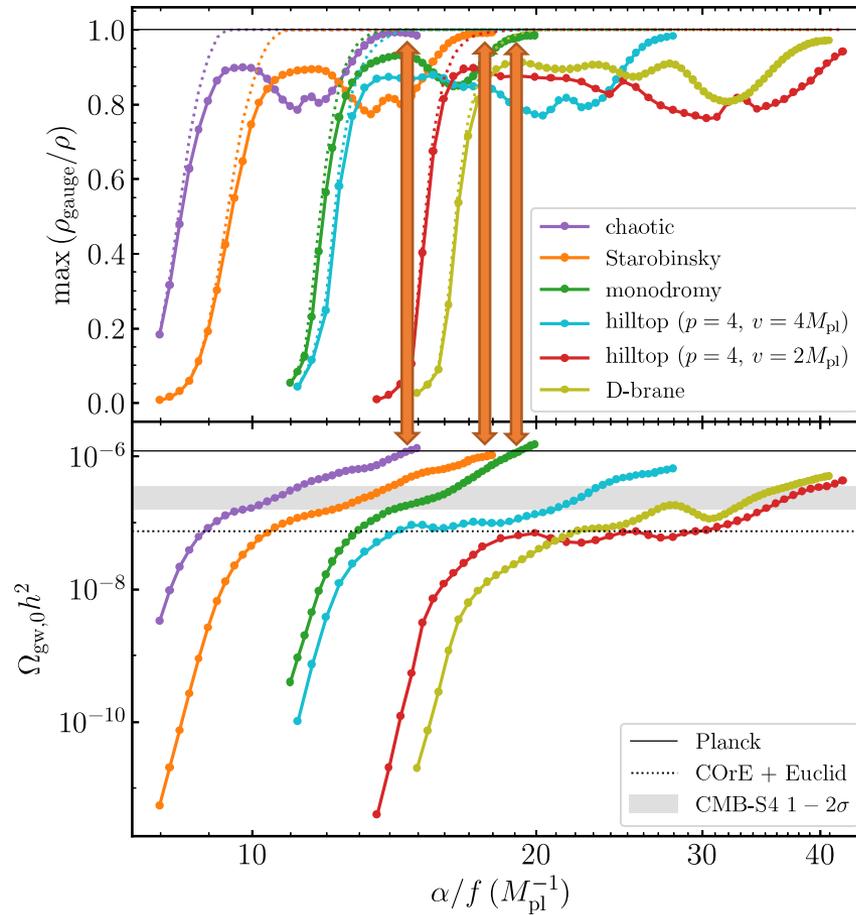


In all cases:  
preheating is  
85% efficient

# Dependence on potential shape

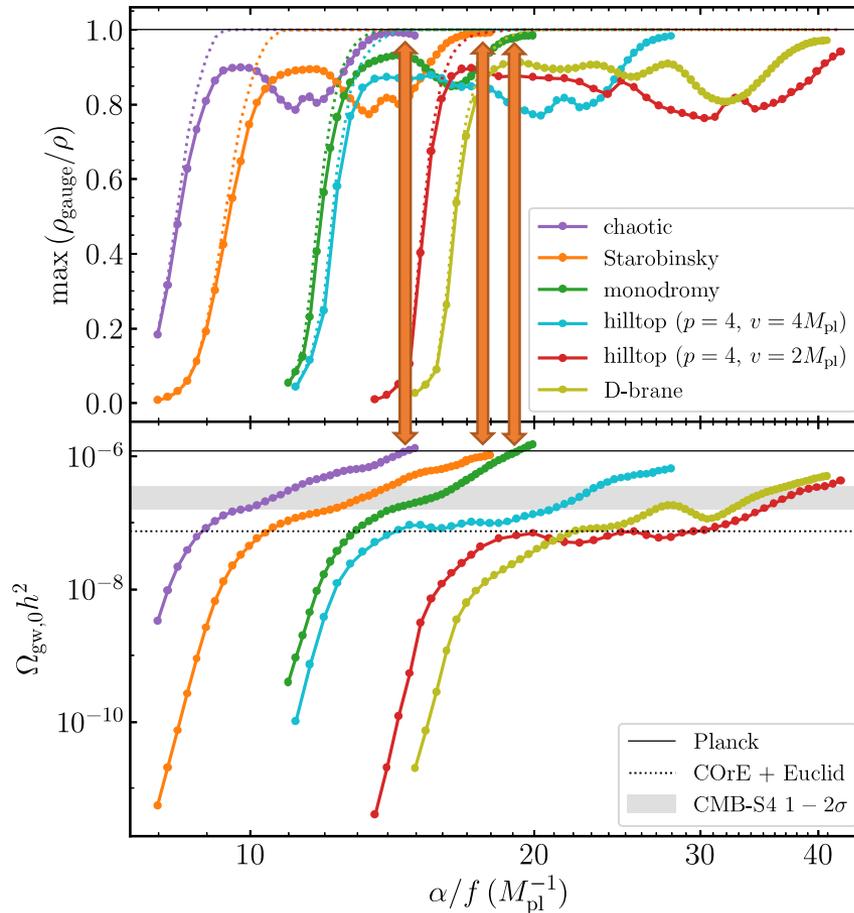


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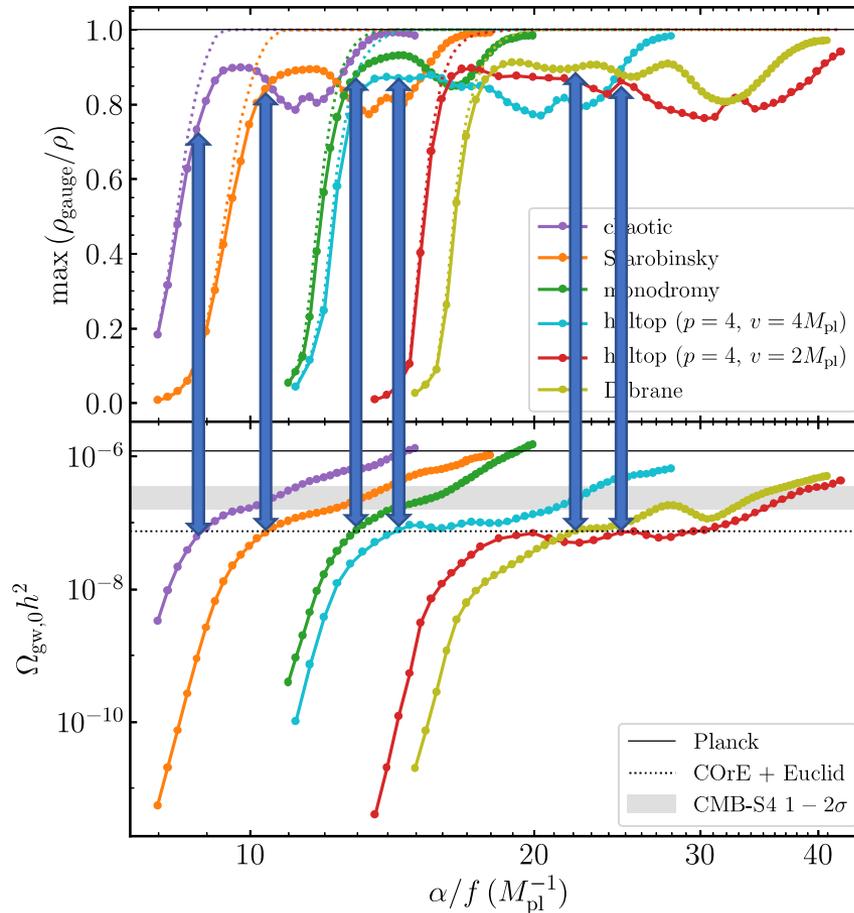
# Dependence on potential shape

Now: constrain coupling for high-scale inflation models



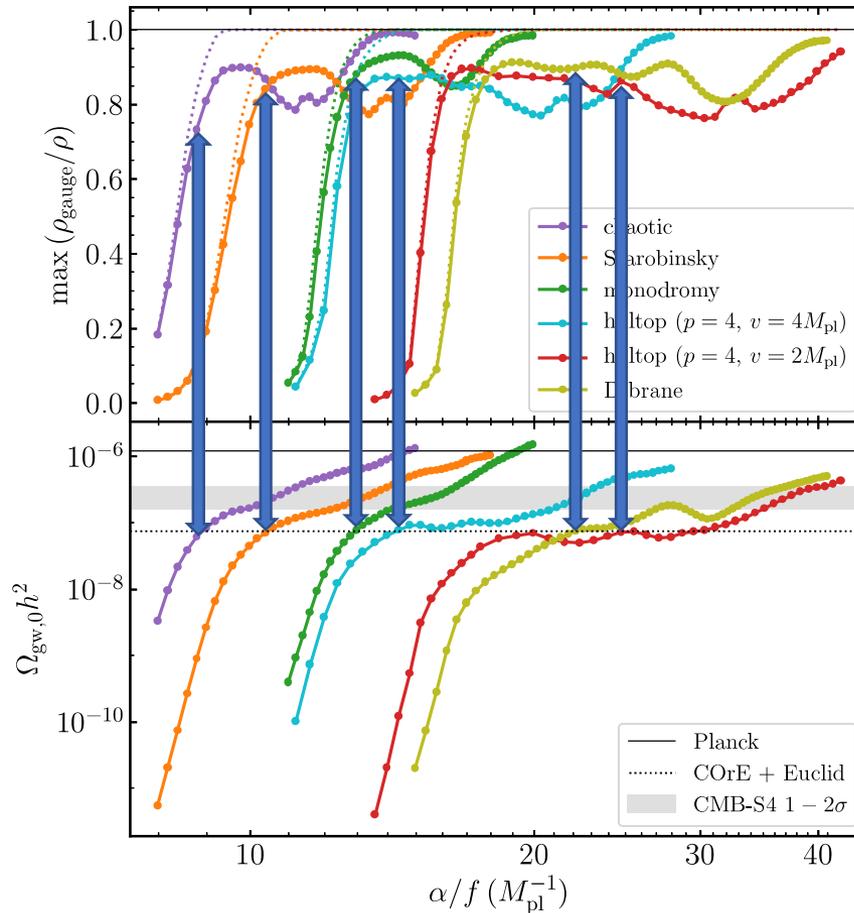
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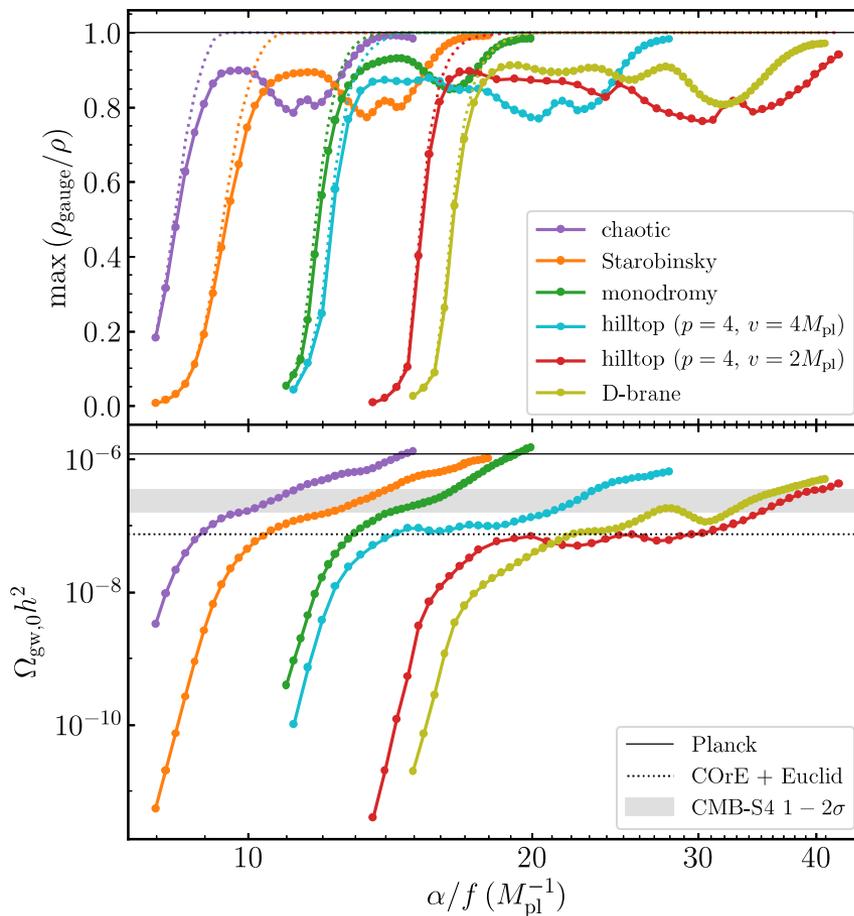
Now: constrain  
coupling for high-scale  
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In the future:  
probe/rule out regime  
of complete preheating

# Dependence on potential shape

constraints are strongest for high-scale inflation ( $\rightarrow$  large tensor-to-scalar ratio)



observe  $r \gtrsim 10^{-3}$   
and nonzero  $\Delta N_{\text{eff}}$   
 $\rightarrow$  consistent with large scale inflaton coupled to gauge fields

# Conclusions

- Inflaton couplings to gauge fields: compelling models, observable phenomenology
- Complete preheating in these models results in a (possibly) **detectable relic gravitational wave background** via CMB measurements of  $\Delta N_{\text{eff}}$ 
  - Places strongest current bounds on coupling strength
  - Could probe or rule out entire regime of gauge preheating after high scale inflation
- Future considerations
  - Primordial black hole (over)production?
  - Metric backreaction?
  - Plasma effects?