

# Particle-hole symmetry in the metallic phase of disordered 2D superconductors



Nicholas P. Breznay



3 August 2017

*(Intertwined) Order, Fluctuations, and Strong Correlations*  
KITP / UCSB

# Acknowledgments

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**Aharon Kapitulnik**  
*Stanford University*



**Myles Steiner**  
*NREL*



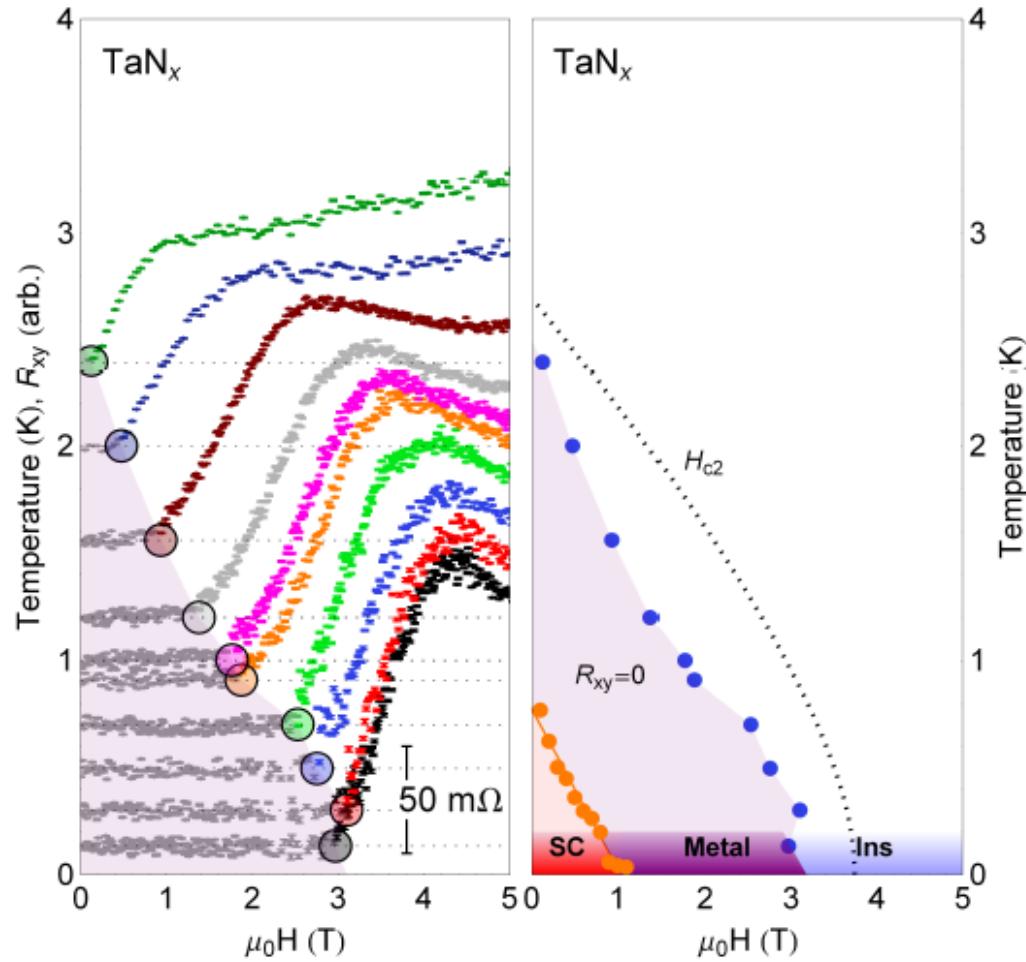
**Mihir Tendulkar**  
*Stanford University*



**Steven Kivelson**  
*Stanford University*



# Punchline: $\rho_{xy}$ evidence for a robust “failed SC” metal near the SIT



# Particle-hole symmetry in the metallic phase near the SIT

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## (1) Motivation & Background

- dogma: no metals in 2D
- rich phase diagram of disordered 2D superconductors
- trivial “quantum metal” at the SIT
- weak insulators ( $\rho \sim 1$  kOhm) show metallic behavior across all systems

## (2) Key question

- What does the metallic state near the SIT in weakly insulating films have to do with superconductivity?

## (3) Data on $\text{InO}_x$ , $\text{TaN}_x$ films

- Characteristic fields from MR, Hall
- Common behavior

## (4) Phase diagram of weakly insulating 2D SC

- PHS from “failed superconductivity” in the metallic phase
- Other recent work

# Quantum diffusion and the hunt for a 2D metal

VOLUME 42, NUMBER 10

PHYSICAL REVIEW LETTERS

5 MARCH 1979

## Scaling Theory of Localization: Absence of Quantum Diffusion in Two Dimensions

E. Abrahams

Serin Physics Laboratory, Rutgers University, Piscataway, New Jersey 08854

and

P. W. Anderson,<sup>(a)</sup> D. C. Licciardello, and T. V. Ramakrishnan<sup>(b)</sup>  
Joseph Henry Laboratories of Physics, Princeton University, Princeton, New Jersey 08544  
(Received 7 December 1978)

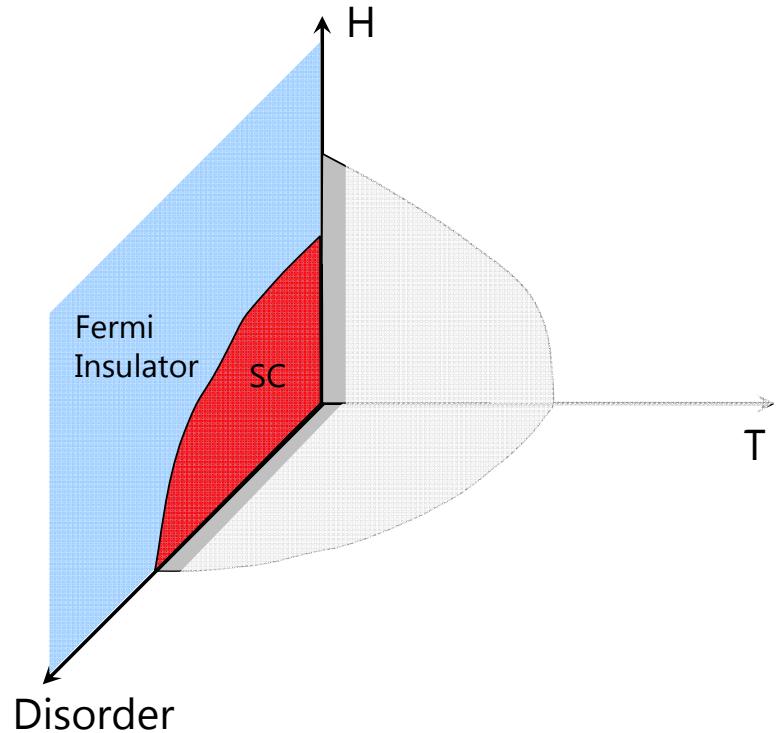
Arguments are presented that the  $T = 0$  conductance  $G$  of a disordered electronic system depends on its length scale  $L$  in a universal manner. Asymptotic forms are obtained for the scaling function  $\beta(G) = d \ln G / d \ln L$ , valid for both  $G \ll G_c \approx e^2/\hbar$  and  $G \gg G_c$ . In three dimensions  $G_c$  is an unstable fixed point. In two dimensions, there is no true metallic behavior; conductance crosses over smoothly from logarithmic or slower to exponential decrease.

Scaling theories of localization have been discussed by Thouless and co-authors<sup>1-3</sup> and by Wegner.<sup>4</sup> Recently Schuster,<sup>5</sup> using methods related to those of Aharony and Imry,<sup>6</sup> has proposed a close relationship of the localization problem to

scribed by Thouless and co-w

$$\frac{\langle V \rangle}{W} = \frac{\Delta E}{dE/dN} = \frac{2\hbar}{e^2} C = \frac{2\hbar}{e^2} \sigma L^4$$

Here  $G$  is the conductance (not



- Strict distinction between metals and insulators only valid at  $T = 0$
- Interactions stabilize SC

# Metallic "state" in presence of SC interactions

VOLUME 42, NUMBER 10

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5 MARCH 1979

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VOLUME 64, NUMBER 5

PHYSICAL REVIEW LETTERS

29 JANUARY 1990

## Presence of Quantum Diffusion in Two Dimensions: Universal Resistance at the Superconductor-Insulator Transition

Matthew P. A. Fisher and G. Grinstein

IBM Research Division, T.J. Watson Research Center, Yorktown Heights, New York 10598

S. M. Girvin

Physics Department, Swain Hall West 117, Indiana University, Bloomington, Indiana 47405

(Received 17 November 1989)

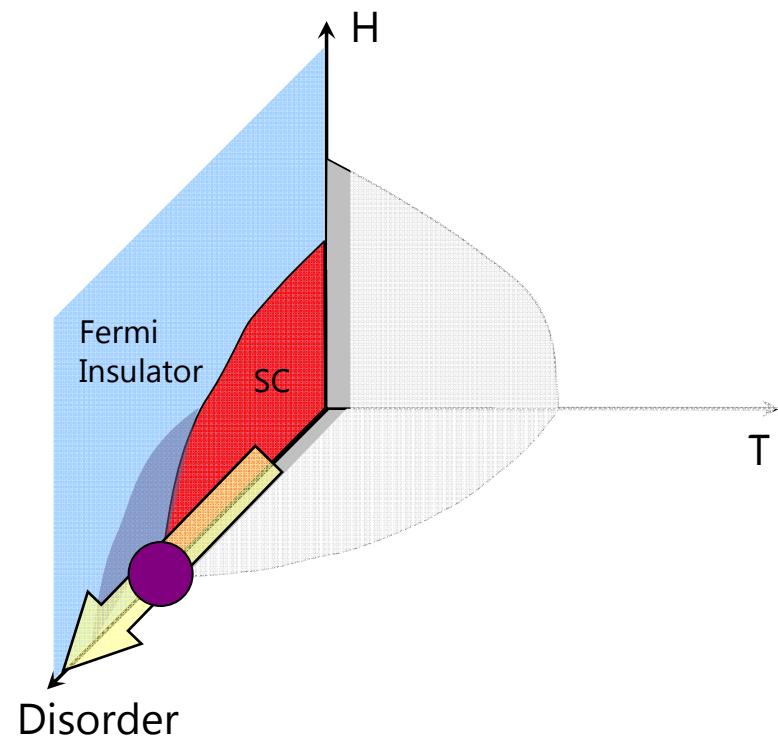
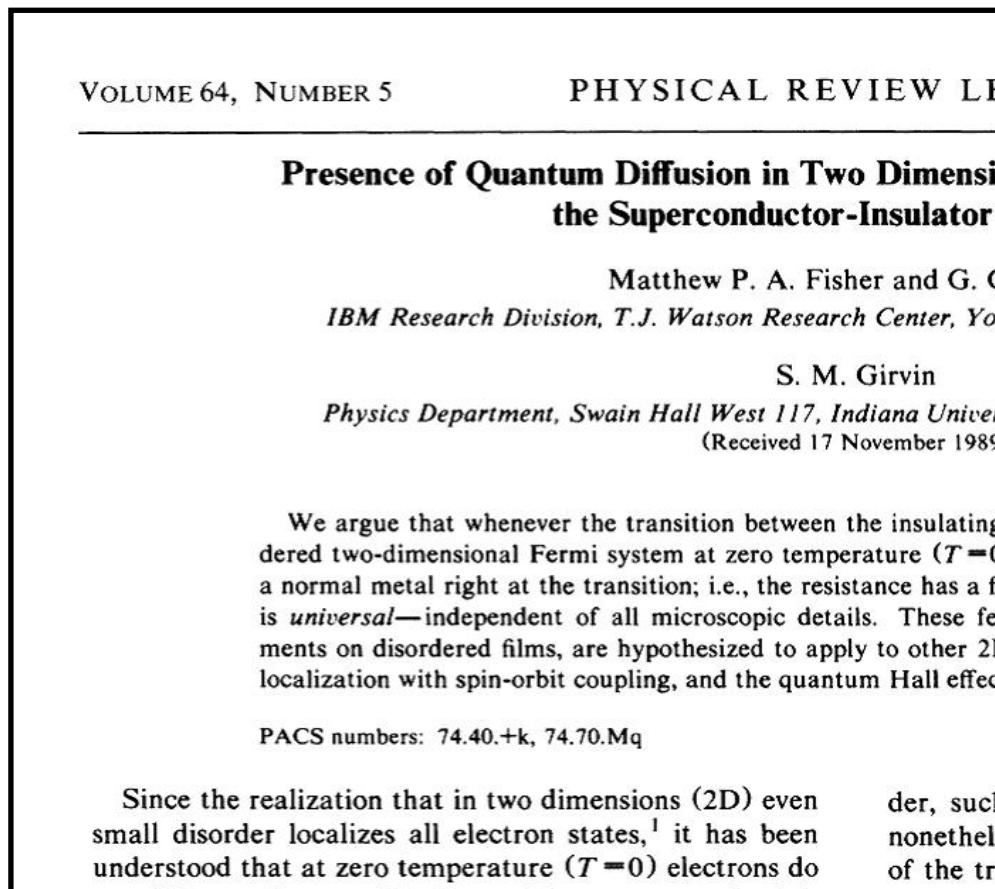
We argue that whenever the transition between the insulating and superconducting phases of a disordered two-dimensional Fermi system at zero temperature ( $T=0$ ) is continuous, the system behaves like a normal metal right at the transition; i.e., the resistance has a finite, nonzero value at  $T=0$ . This value is *universal*—independent of all microscopic details. These features, consistent with recent measurements on disordered films, are hypothesized to apply to other 2D transitions at  $T=0$ , such as Anderson localization with spin-orbit coupling, and the quantum Hall effect.

PACS numbers: 74.40.+k, 74.70.Mq

Since the realization that in two dimensions (2D) even small disorder localizes all electron states,<sup>1</sup> it has been understood that at zero temperature ( $T=0$ ) electrons do

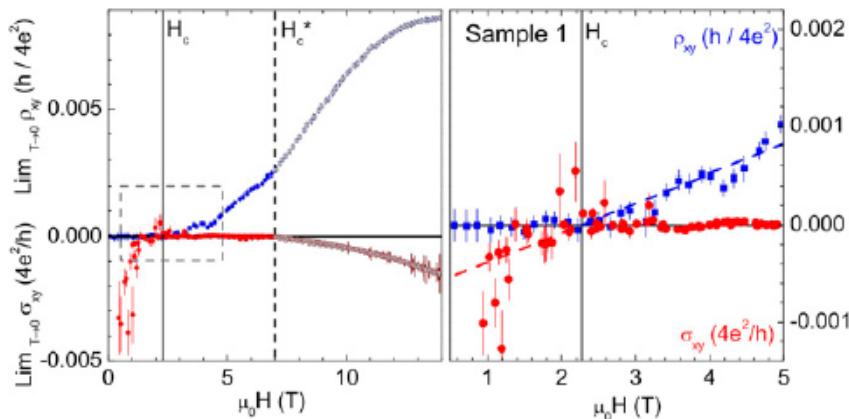
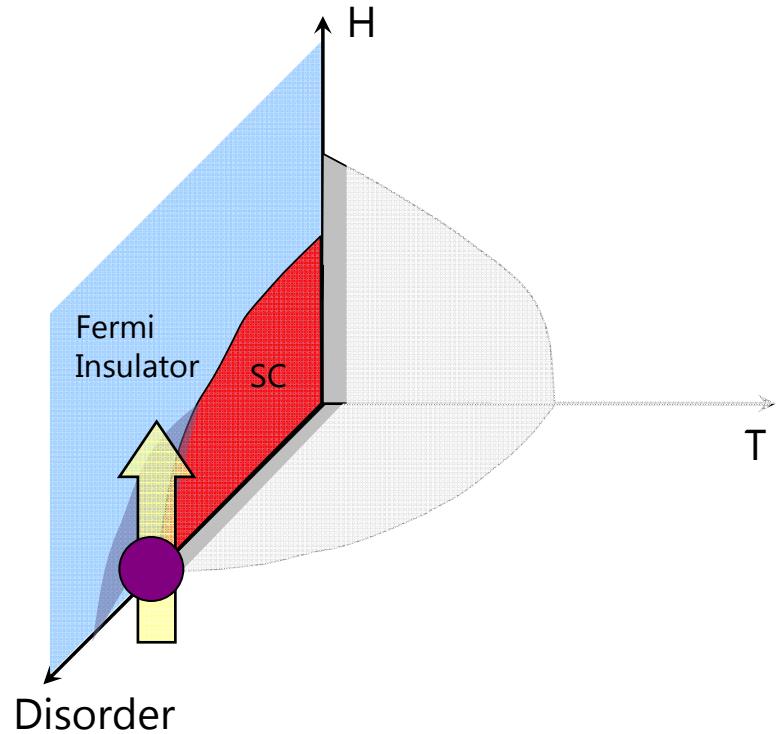
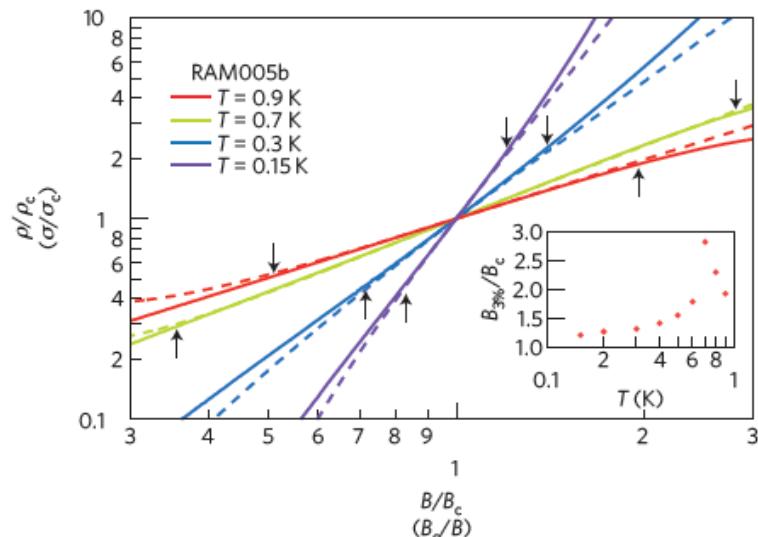
der, such a description is clearly inadequate. It seems nonetheless likely that the asymptotic critical properties of the transition are insensitive to the obvious difference

# A Bose metal at the SIT critical point



- Fisher proposes a metallic point separating SC, (Bose) insulator

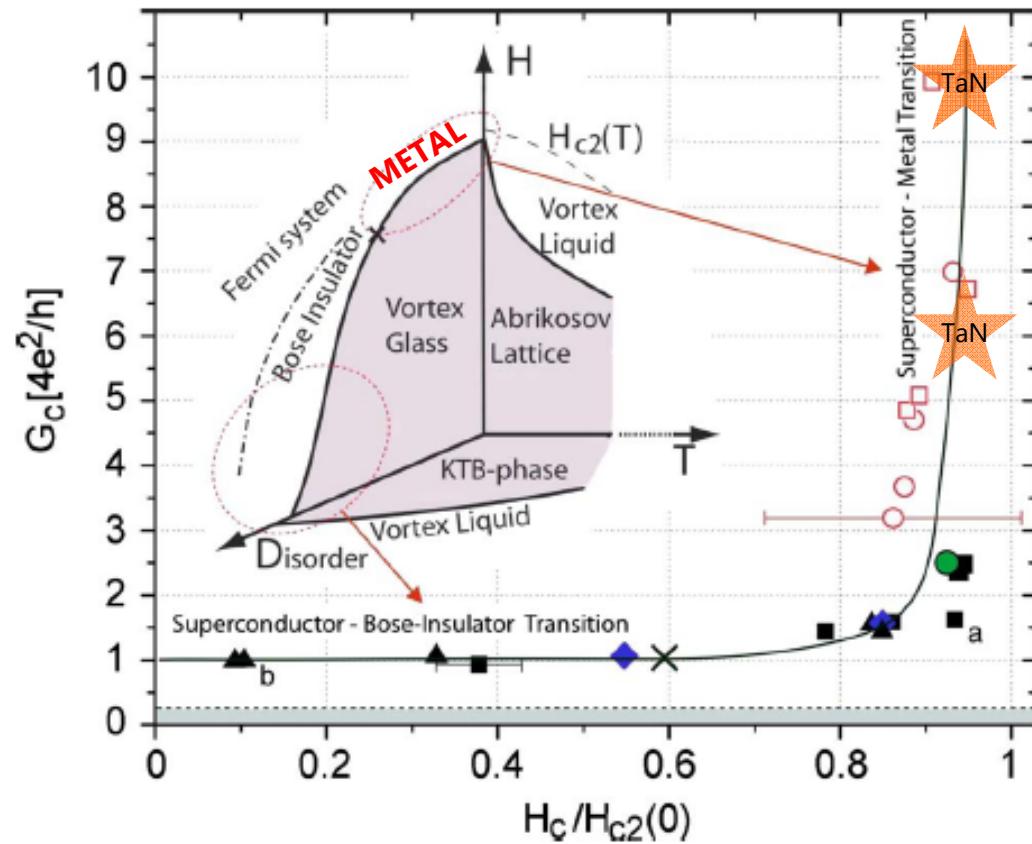
# A Bose metal at the (dual) SIT critical point



- Fisher proposes a metallic ‘point’ separating SC, insulator
- Dirty bosons description (self-dual  $\rightarrow \rho_c \sim h/4e^2$ , scaling)

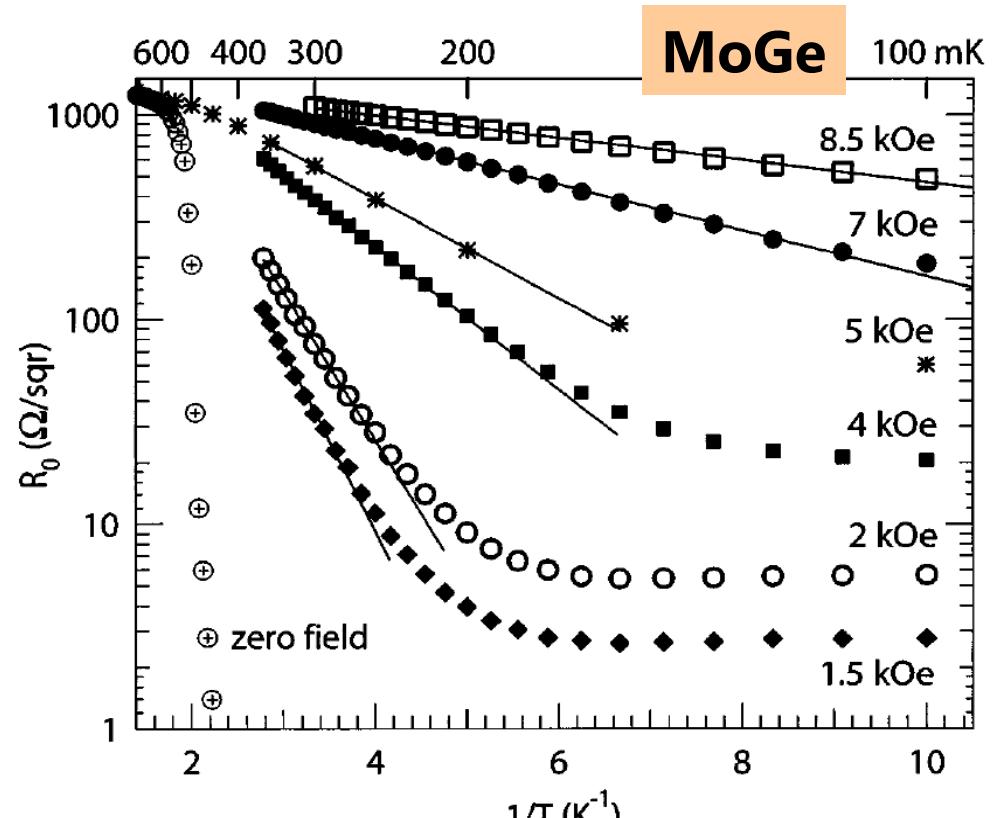
# Unified phenomenology in the strong, weak disorder limits

- Regimes of behavior for TiN, InOx, Ta, MoGe, TaN<sub>x</sub>, ...
- Characterized by behavior near the breakdown of SC: G<sub>c</sub>, H<sub>c</sub>, scaling, **metal**



# Metallic state - Ephron et al. (1996)

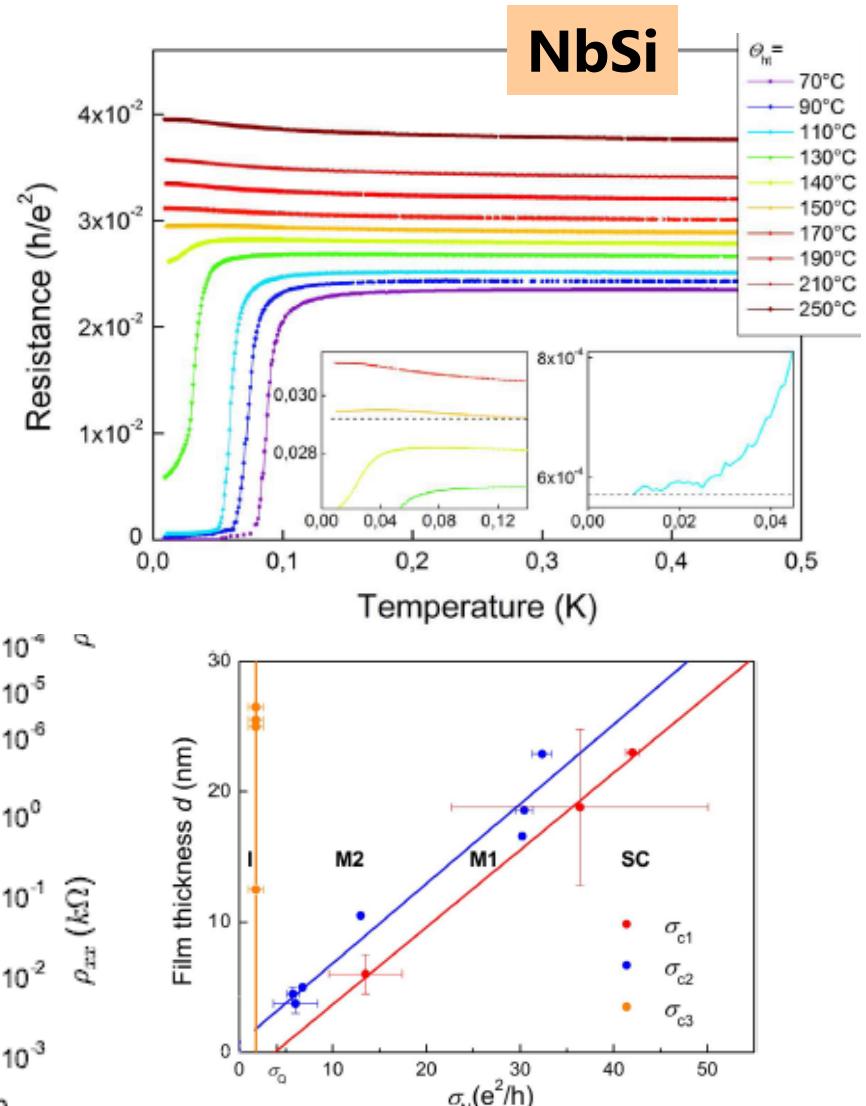
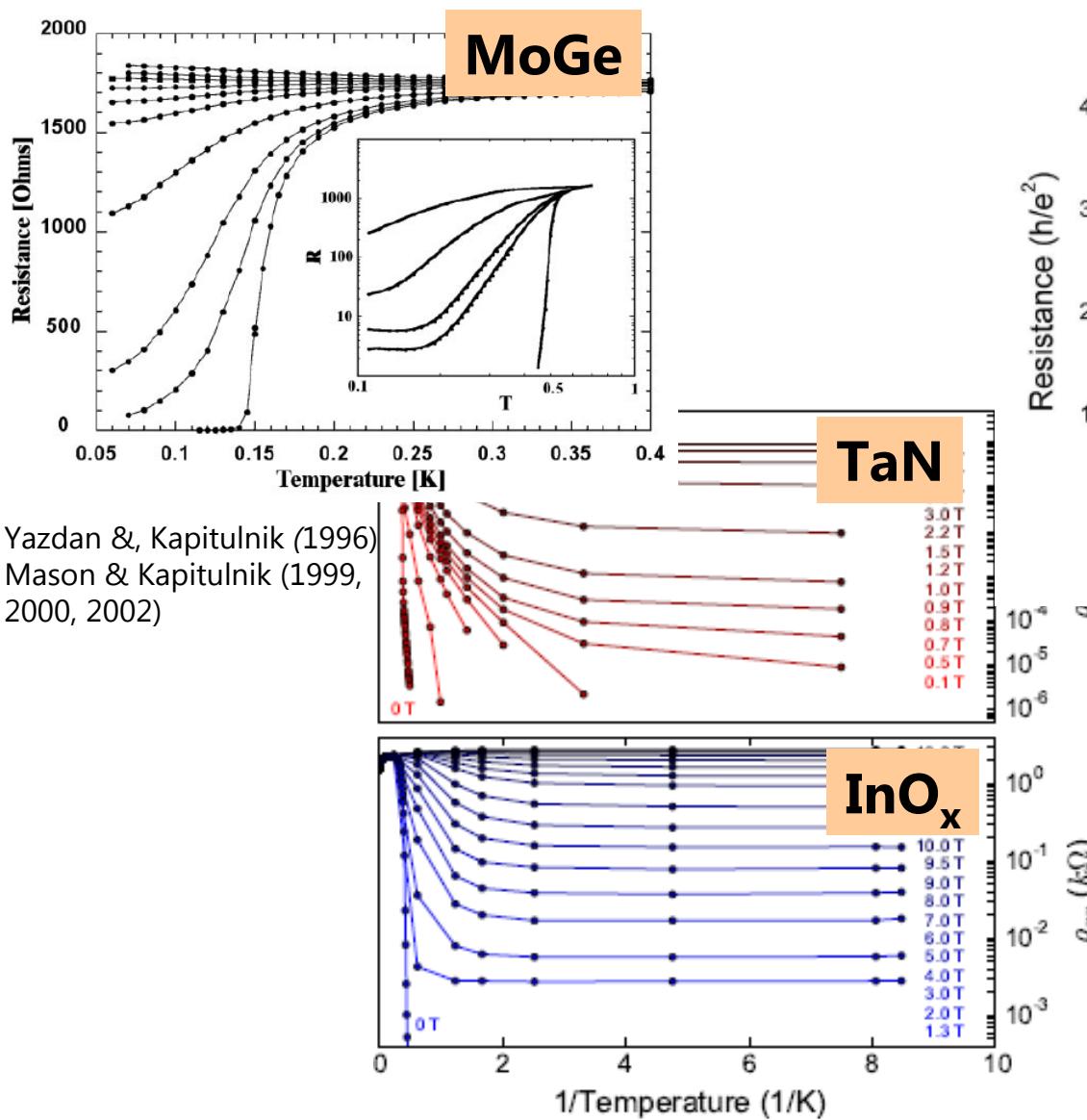
- $\rho_{xx} \sim 1.35 \text{ k}\Omega$ ,  $T_C \sim 0.5 \text{ K}$
- Activated behavior at high T:  
$$R(T) = R_0 \exp(T_0 / T)$$
... disappears at low T!



"... we do not exclude the possibility of a novel quantum mechanical process or phase lurking behind our lowest temperature data."

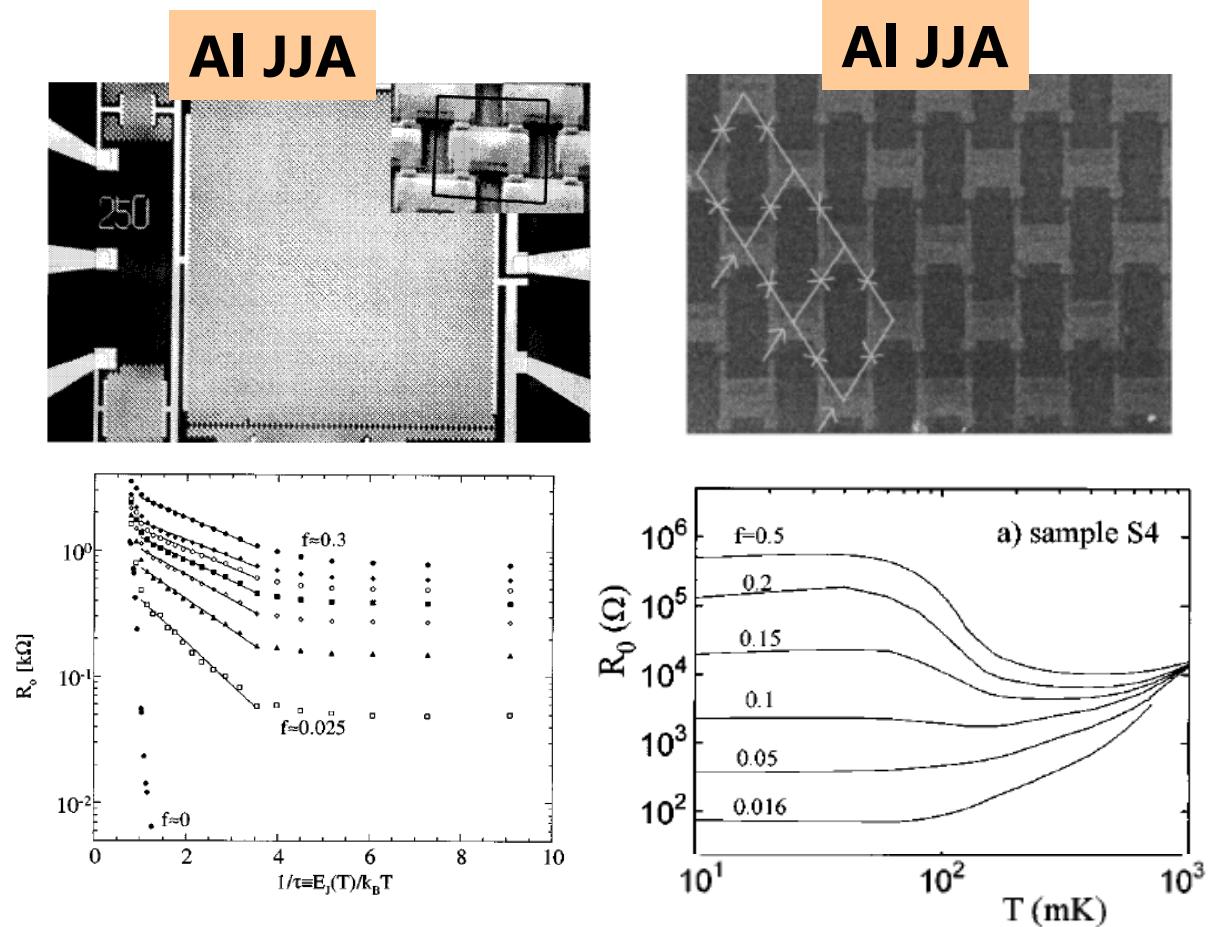
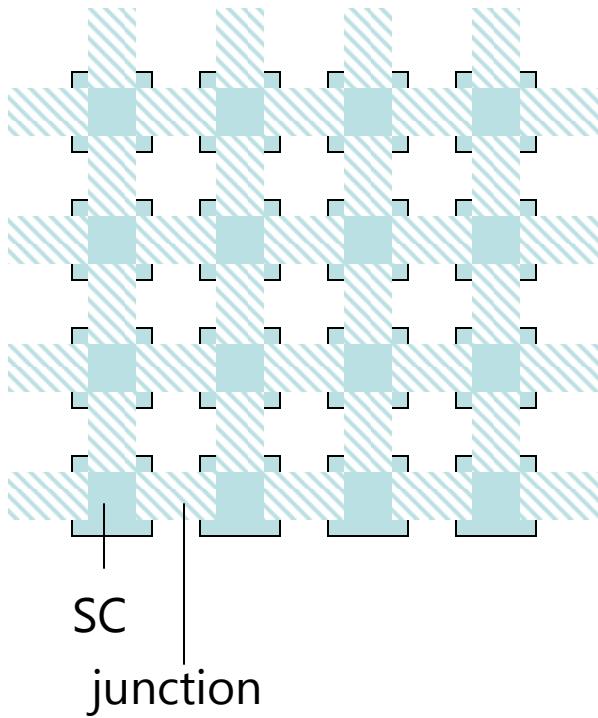
Ephron Yazdani Kapitulnik Beasley *PRL* **79** 1529 (1996)

# Metallic state – Amorphous metal alloy films



# Metallic state – Josephson Junction Arrays

- Same universality class as thin-film SIT

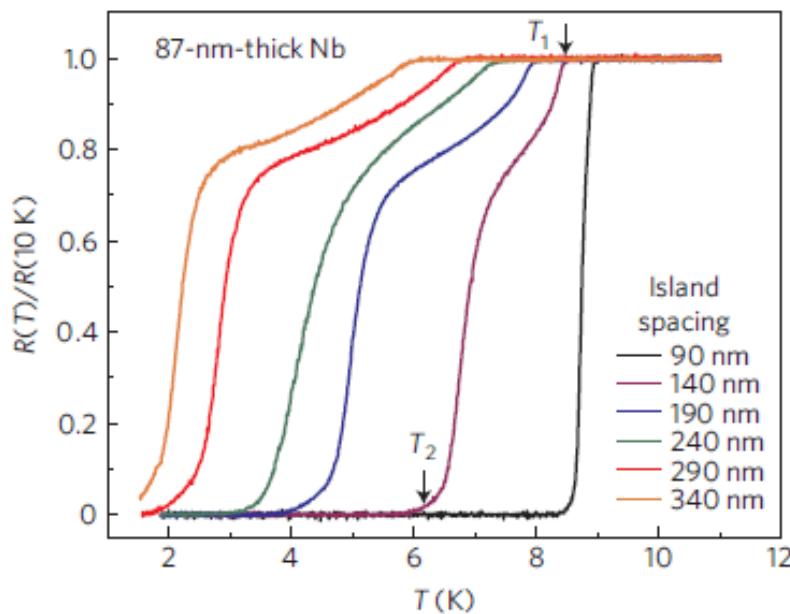
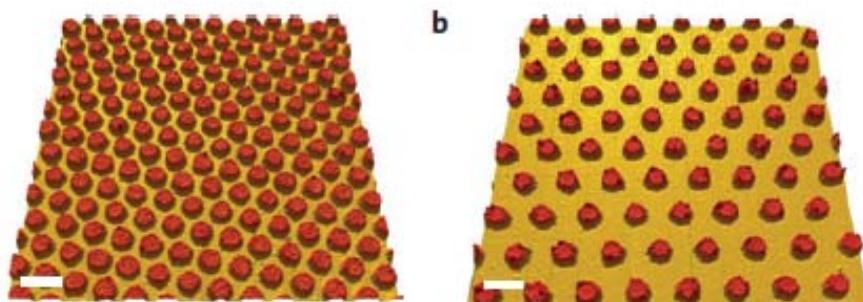


C. D. Chen et al. *PRB* 54 9449 (1996)

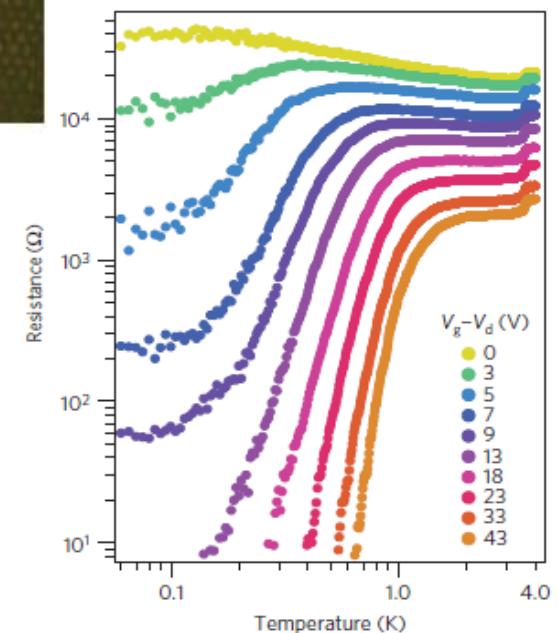
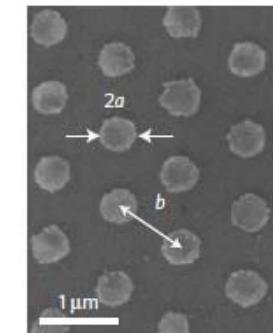
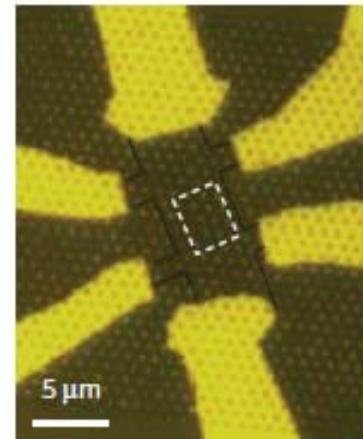
van der Zant et al. *PRB* 54 10081 (1996)

# Metallic state - Nanostructured SC arrays

## Nb on Au



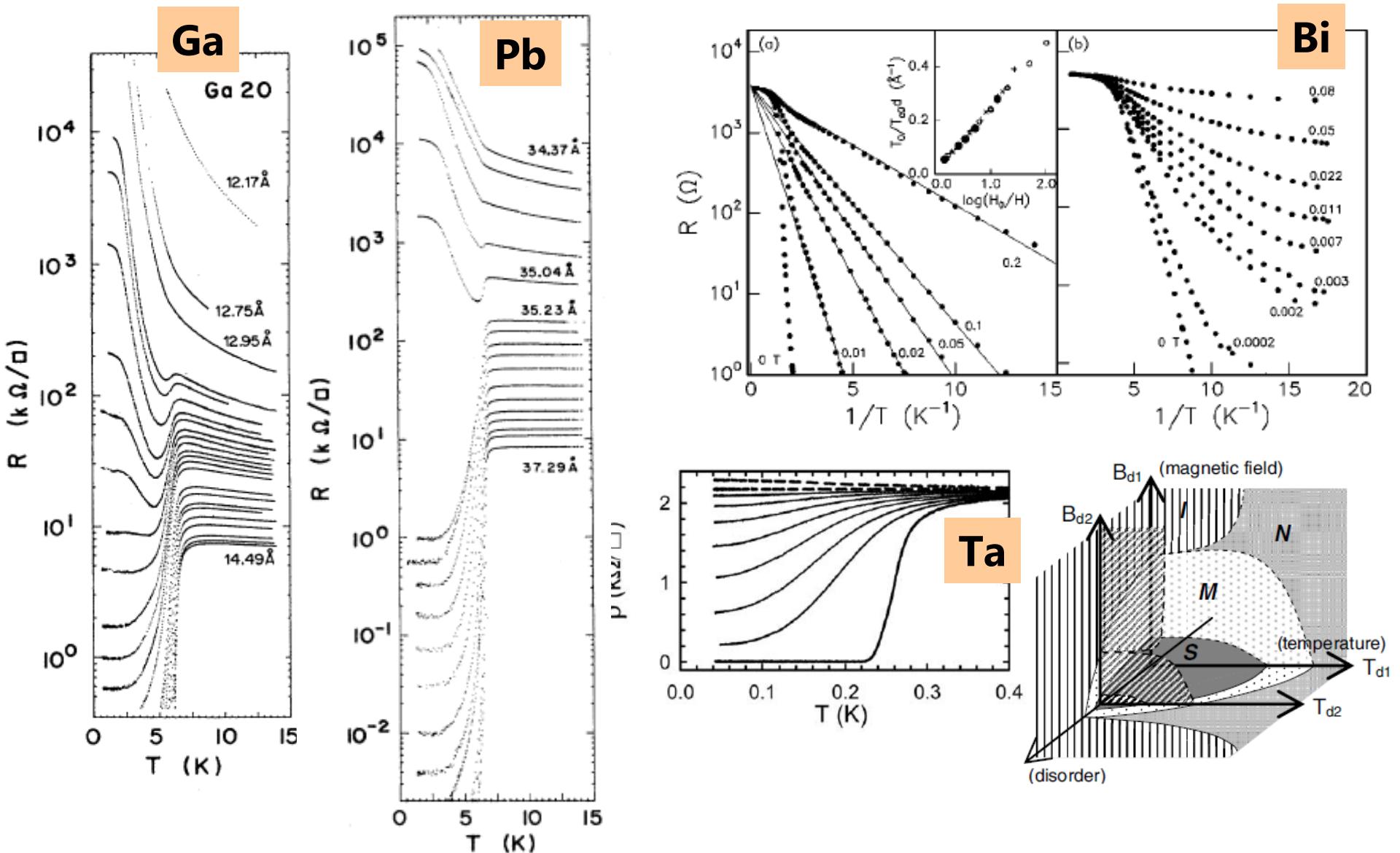
## Sn on graphene



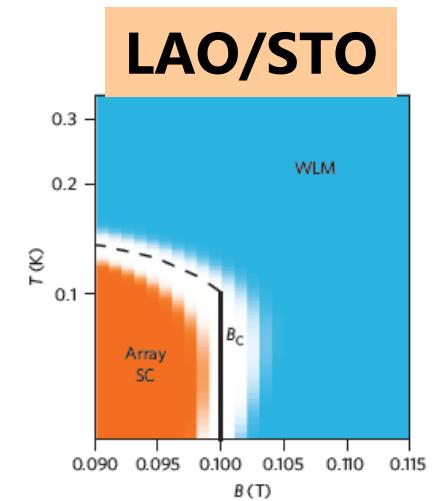
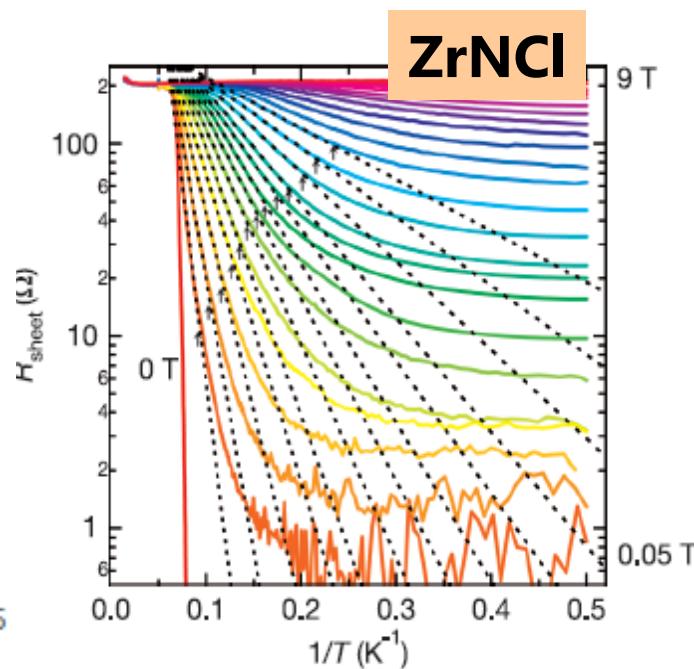
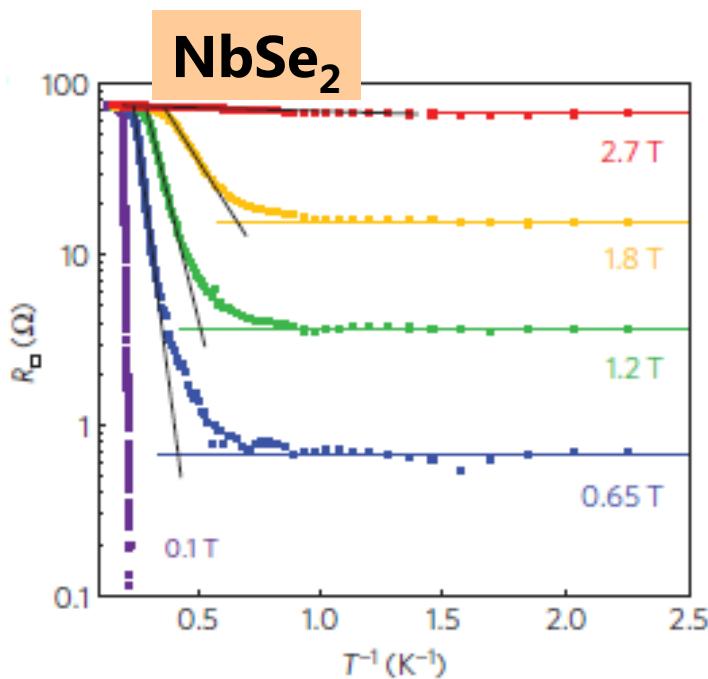
S. Eley, N. Mason et al. *Nature Physics* (2011)

Z. Han et al. *Nature Physics* (2014)

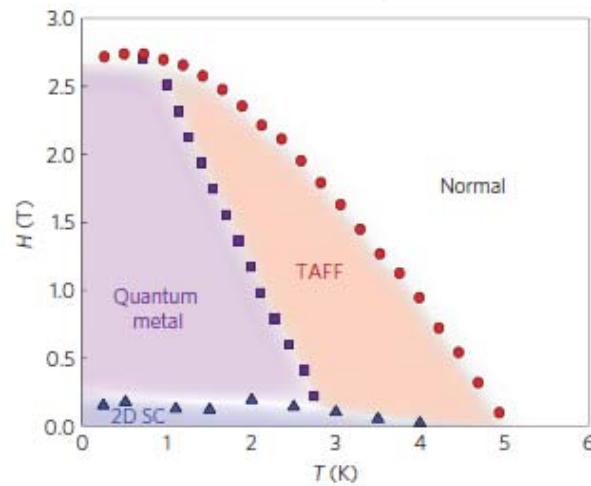
# Metallic State – Elemental / granular metals



# Metallic State – Crystalline materials ( $\sim 100 \Omega$ )

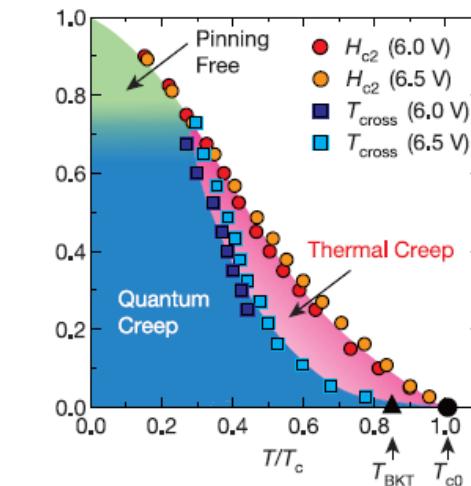


J. Biscaras et al. *Nat. Mat.* 12 (2013)



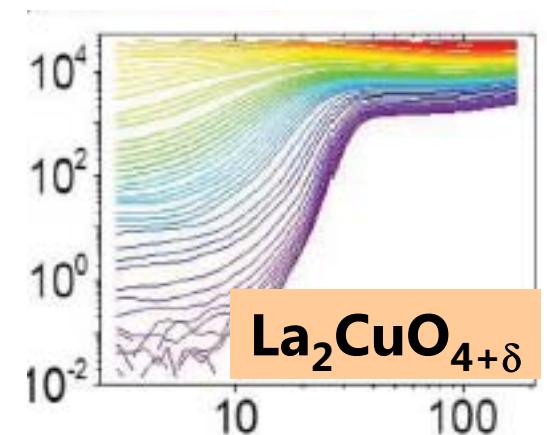
A. W. Tsen, A. Pasupathy et al. *Nature Physics* (2016)

Nicholas P. Breznay



Y. Saito, Y. Iwasa et al. *Science* (2015)

Particle-hole symmetry in the metallic phase of disordered 2D superconductors



J. Garcia-Barriocanal, A. M. Goldman et al. *Phys. Rev. B* 87, 024509 (2013)

# Particle-hole symmetry in the metallic phase near the SIT

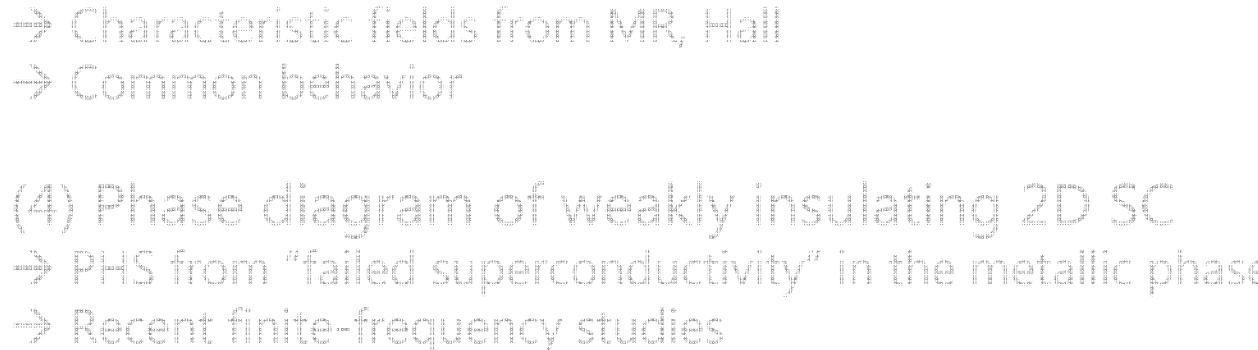
## (1) Motivation & Background

- dogma: no metals in 2D
- rich phase diagram of disordered 2D superconductors
- metal “quantum meta” at the SIT
- $\Delta \approx 2\text{ K}$ ,  $T_{\text{c}} \approx 1\text{ K}$ ,  $\rho \approx 1\text{ k}\Omega\text{m}$ , show metallic behavior at  $T > 2\text{ K}$  for  $\Delta \gg \Delta_{\text{SIT}}$

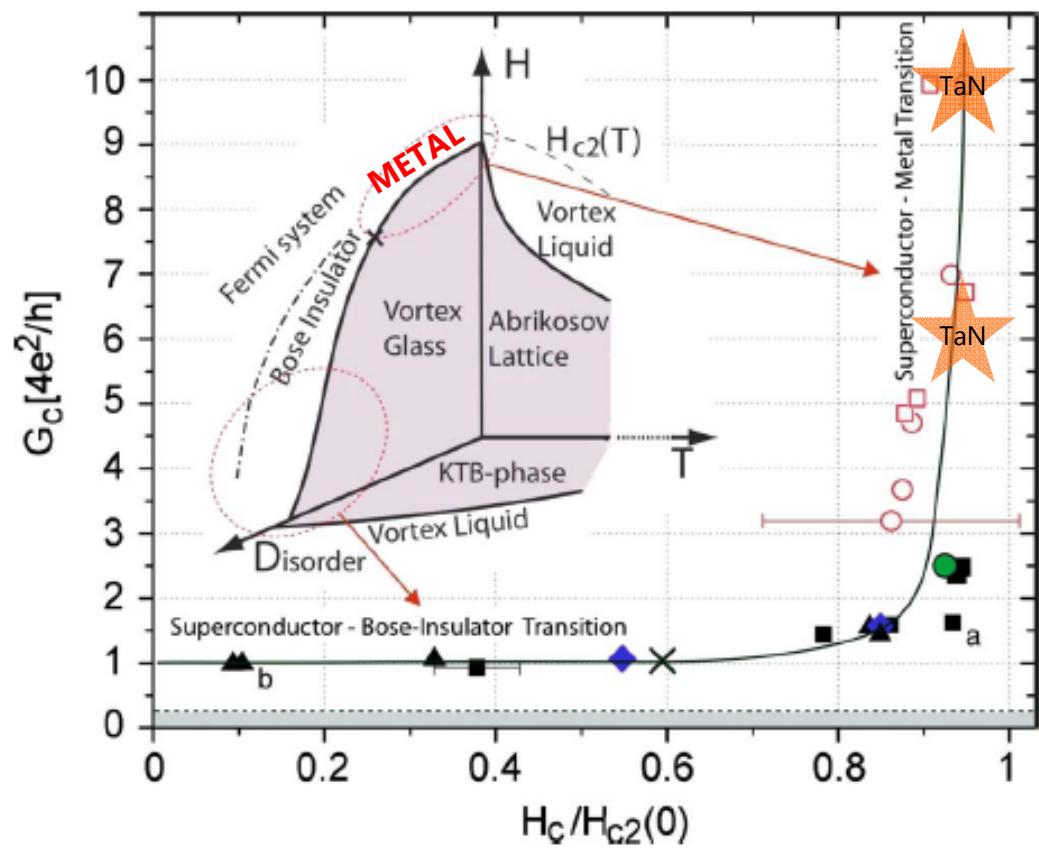
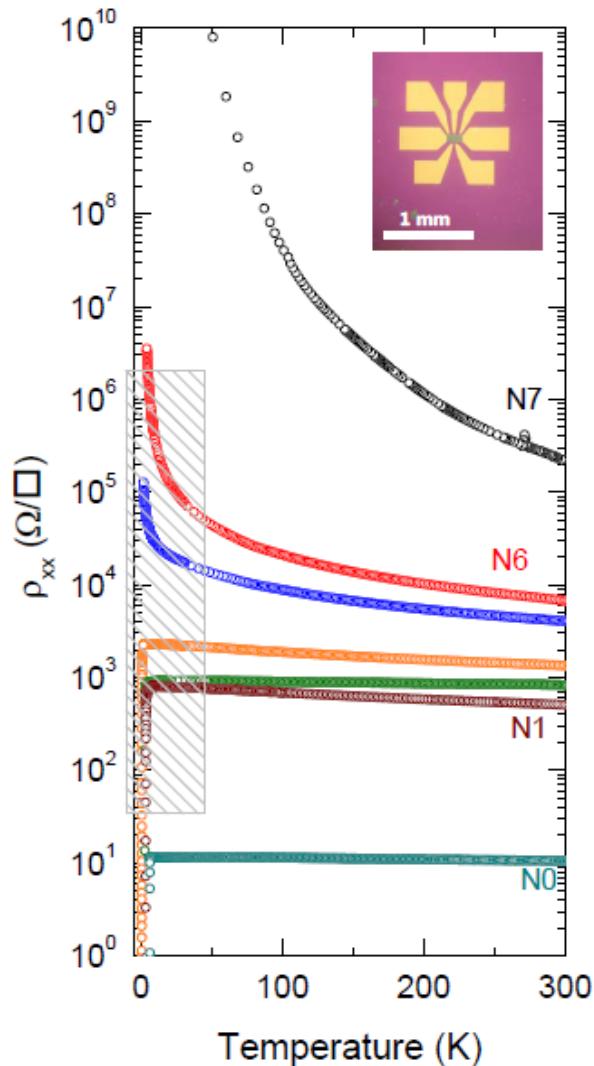
## (2) Key question

- What does the metallic state near the SIT in weakly insulating films have to do with superconductivity?

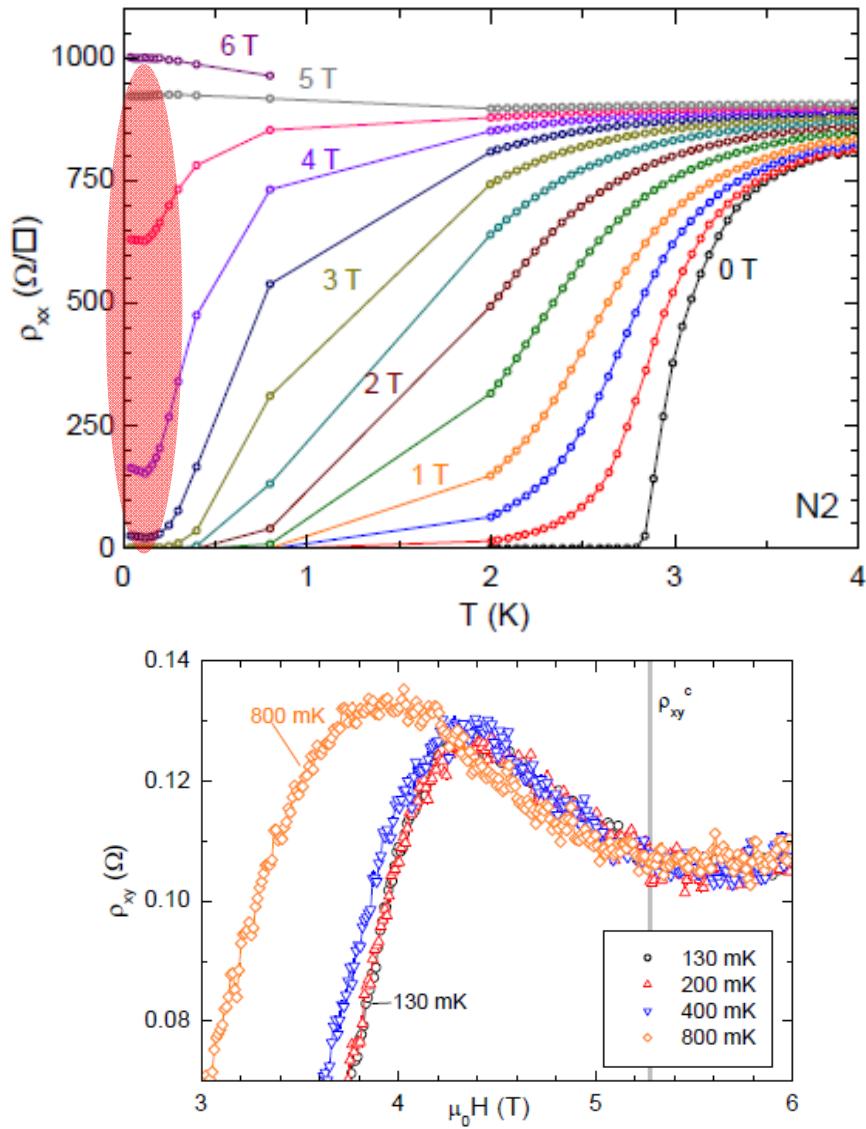
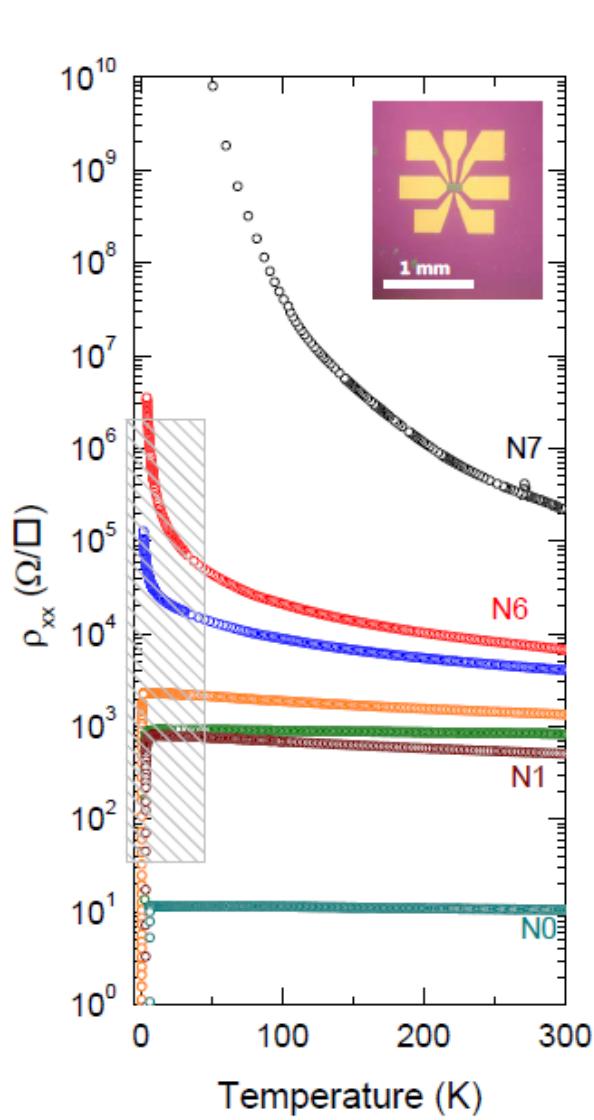
## (3) Data on $\text{InO}_x$ , $\text{TaN}_x$ films



# Disorder and field-tuned SIT in Tantalum Nitride

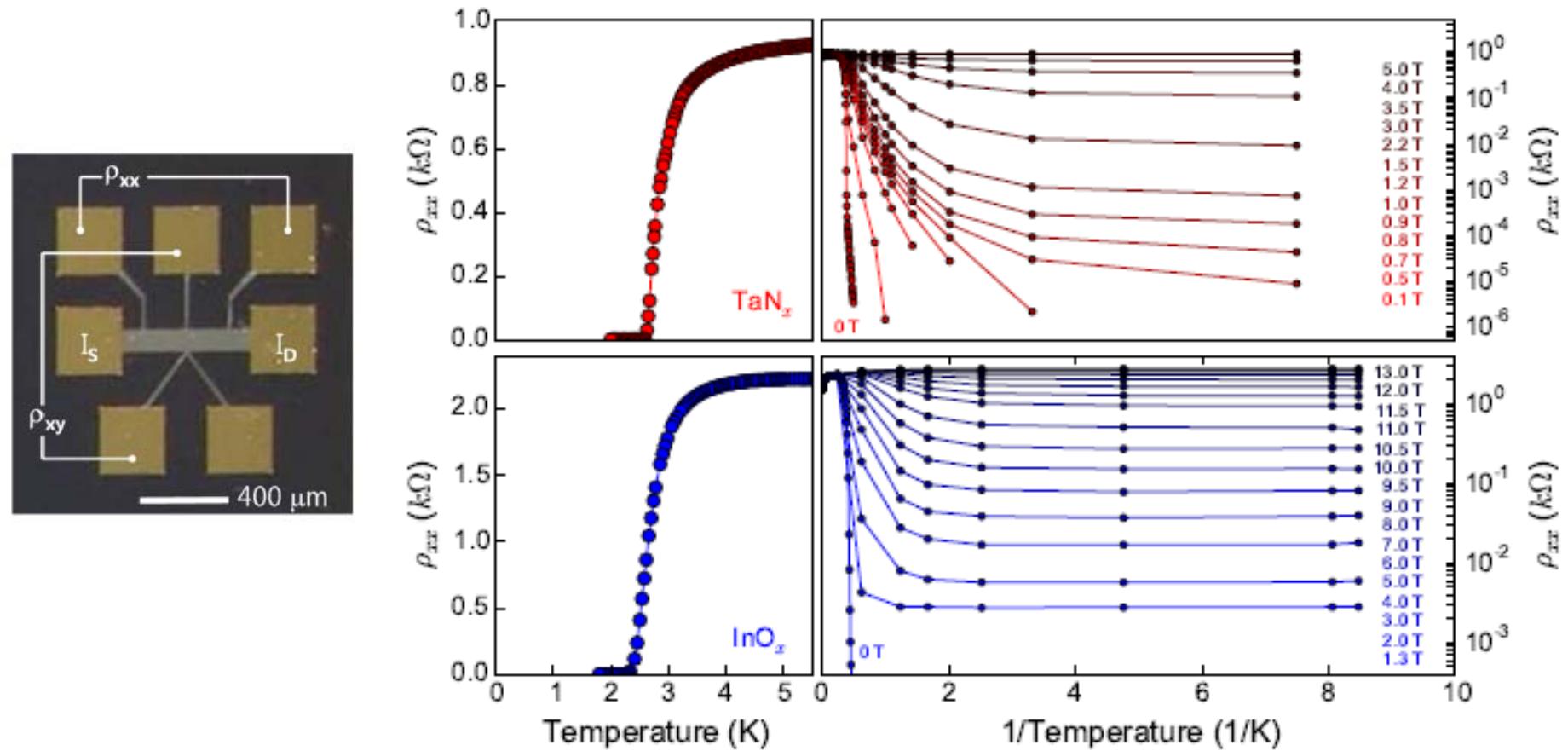


# Disorder and field-tuned SIT in Tantalum Nitride



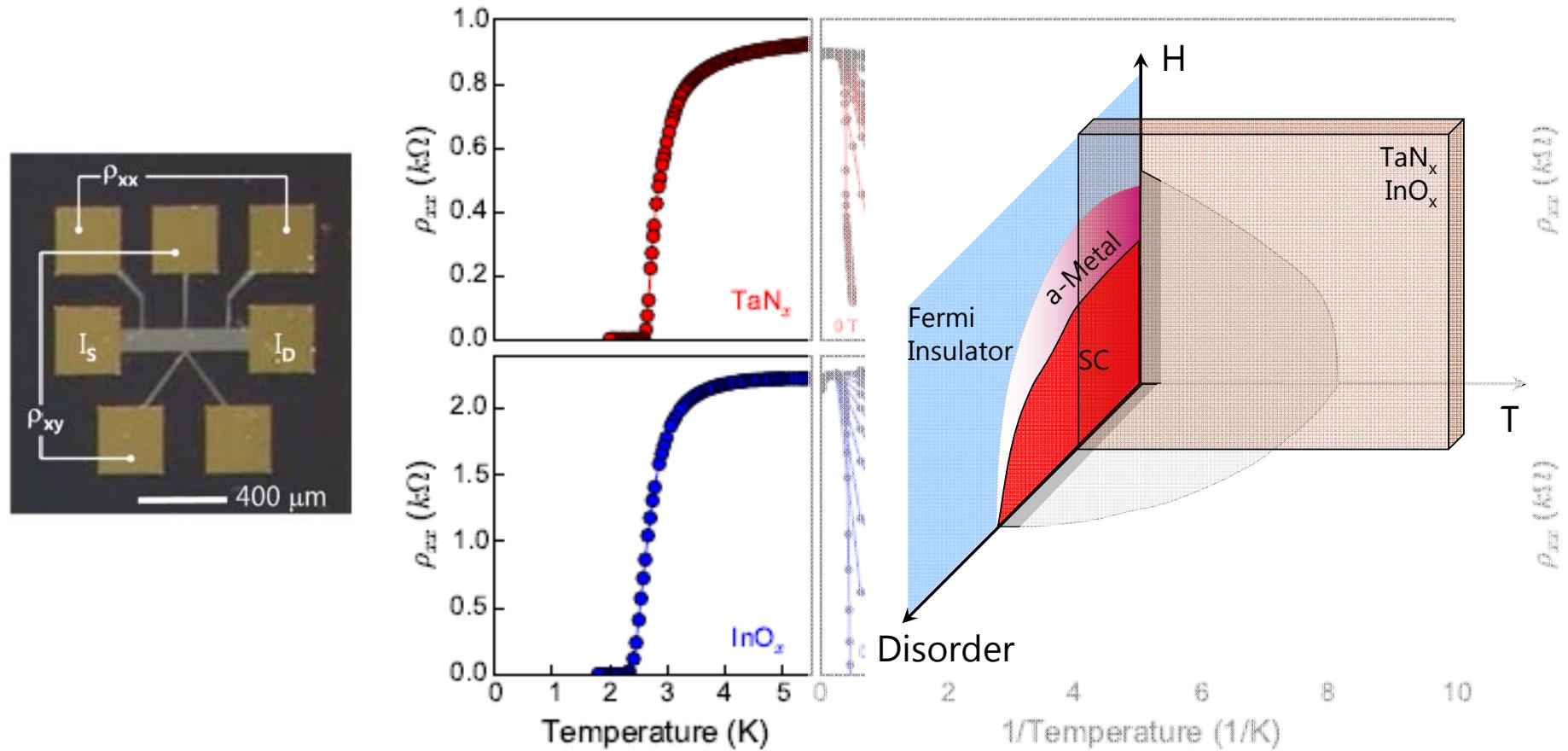
# Results – evidence for metallic saturation in two materials

- Two amorphous materials proximal to the SIT:  $\text{TaN}_{x'}$ ,  $\text{InO}_x$



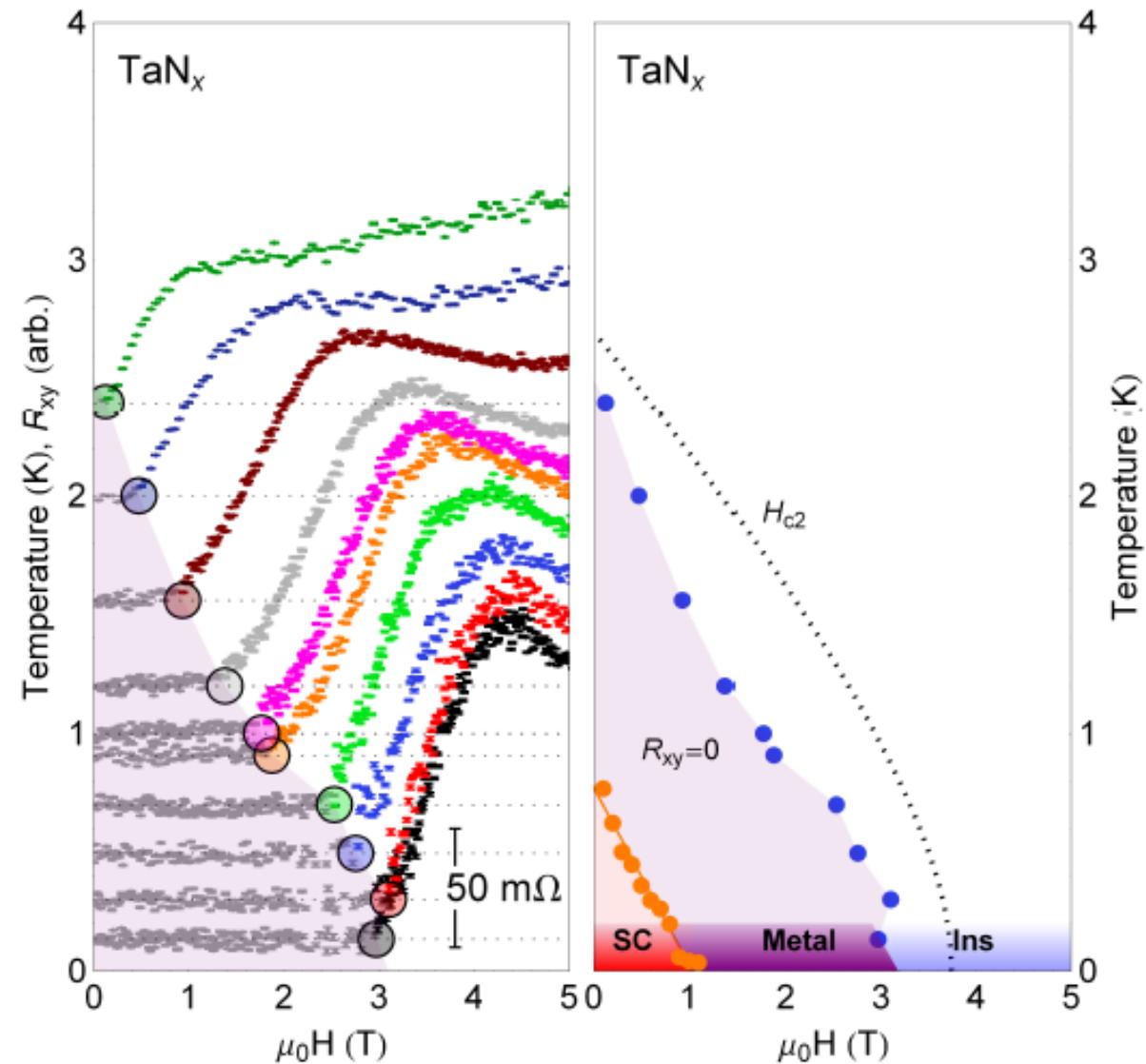
# Results – evidence for metallic saturation in two materials

- Two amorphous materials proximal to the SIT:  $\text{TaN}_x$ ,  $\text{InO}_x$



# Zero Hall effect in $\text{TaN}_x$

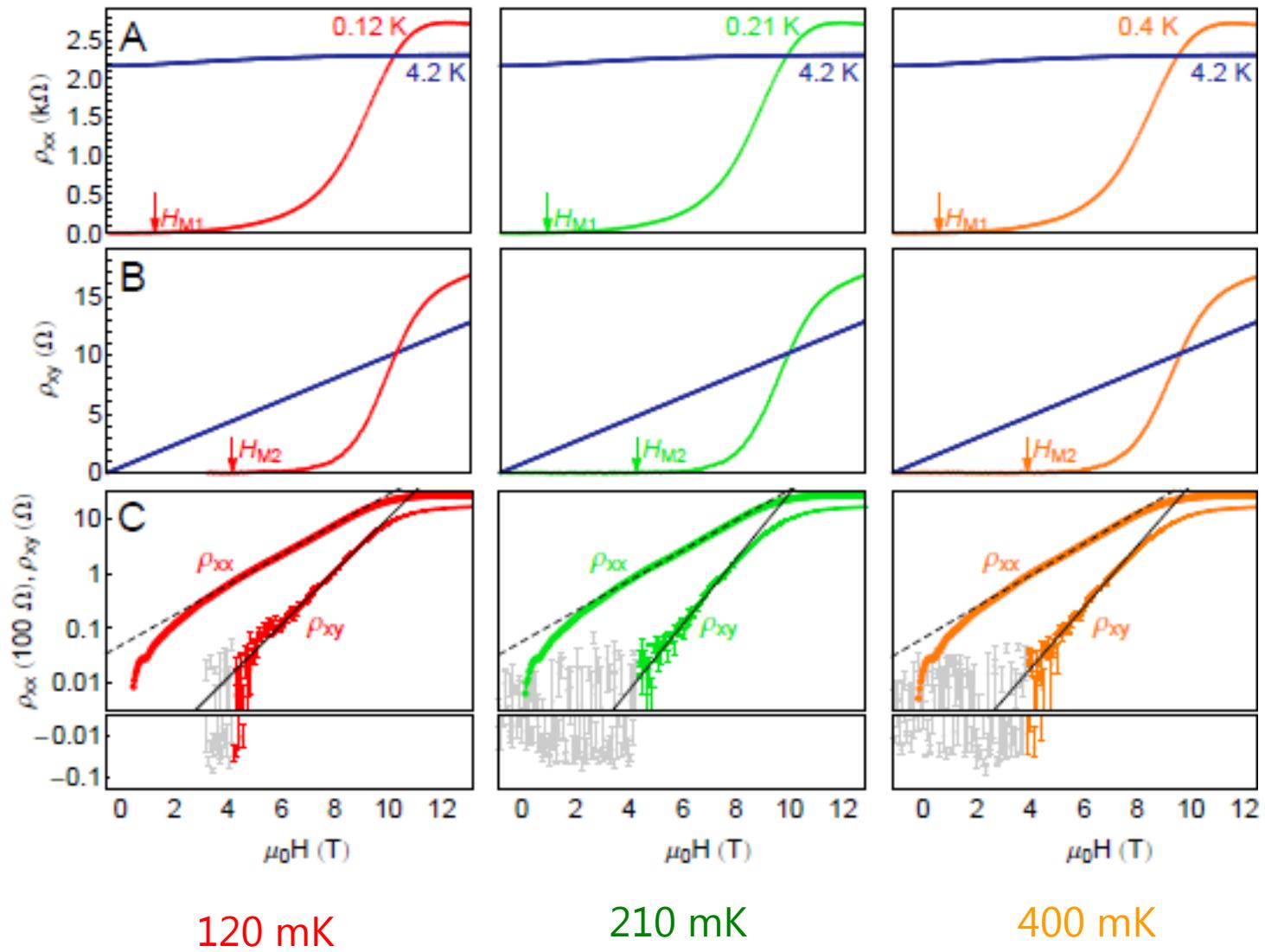
- Measure  $\rho_{xy}$  in the  $T \rightarrow 0$  limit



# InO<sub>x</sub>: Regimes of behavior in $\rho_{xx}$ , $\rho_{xy}$

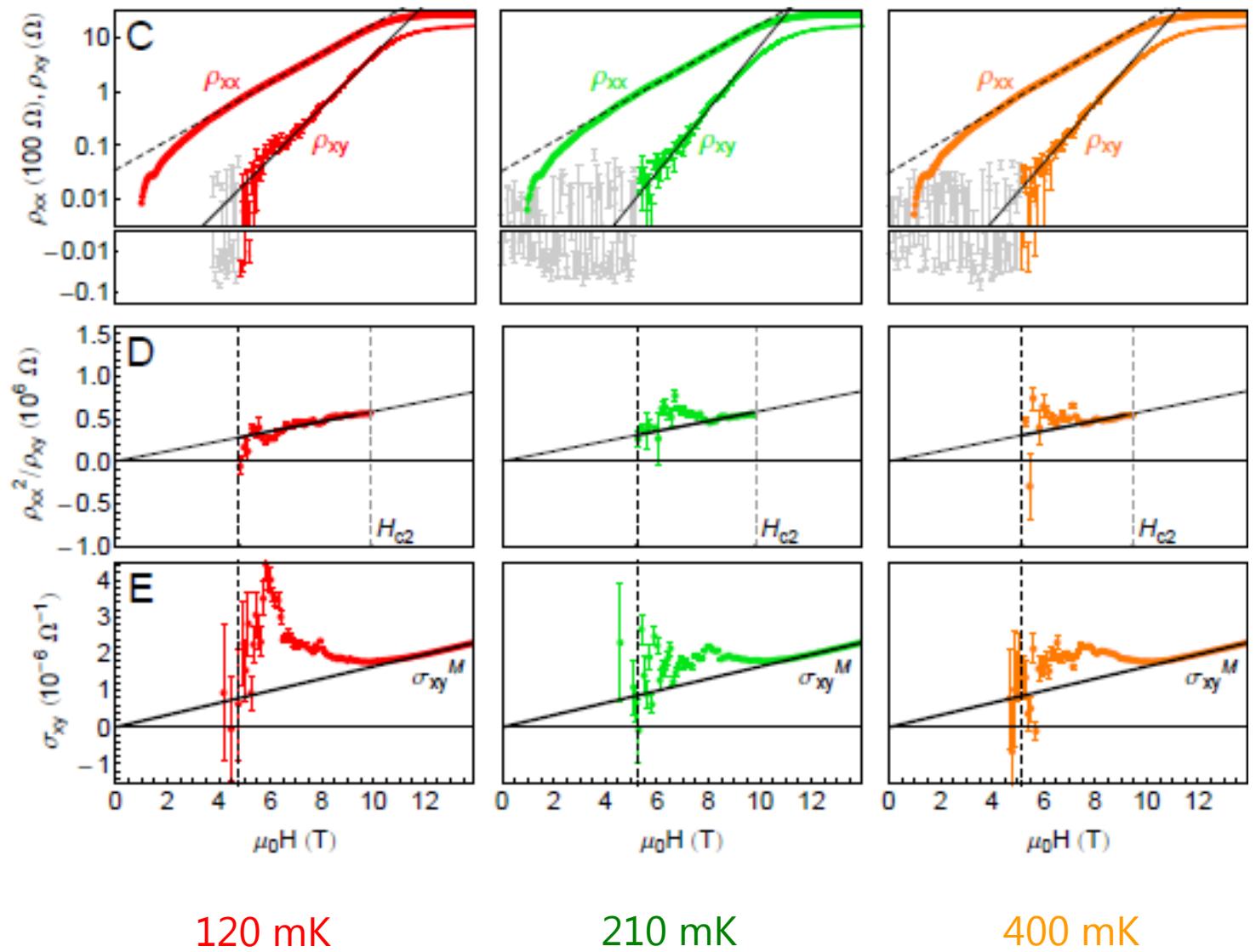
- $\rho_{xx} \rightarrow 0$  at  $H_{M1}$
- $\rho_{xy} \rightarrow 0$  at  $H_{M2}$

→ track with T

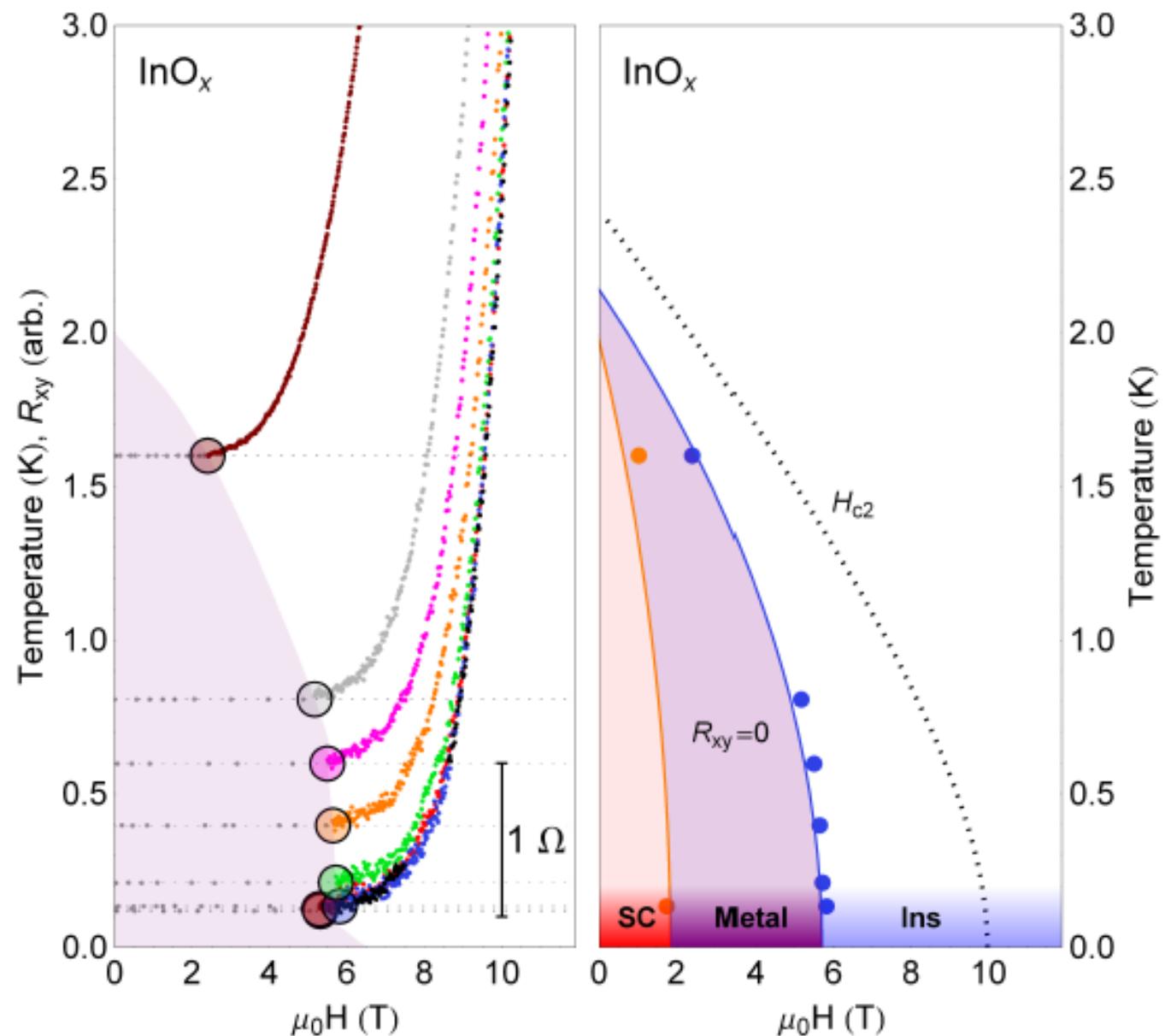


# InO<sub>x</sub>: Scaling behavior at higher field

- $\rho_{xx} \rightarrow 0$  at  $H_{M1}$
- $\rho_{xy} \rightarrow 0$  at  $H_{M2}$
- $\rho_{xx}^2/\rho_{xy} \sim H$   
(vortex state)
- $\sigma_{xy} \rightarrow \sigma^M$   
(above  $H_{c2}$ )



# InO<sub>x</sub> Hall effect



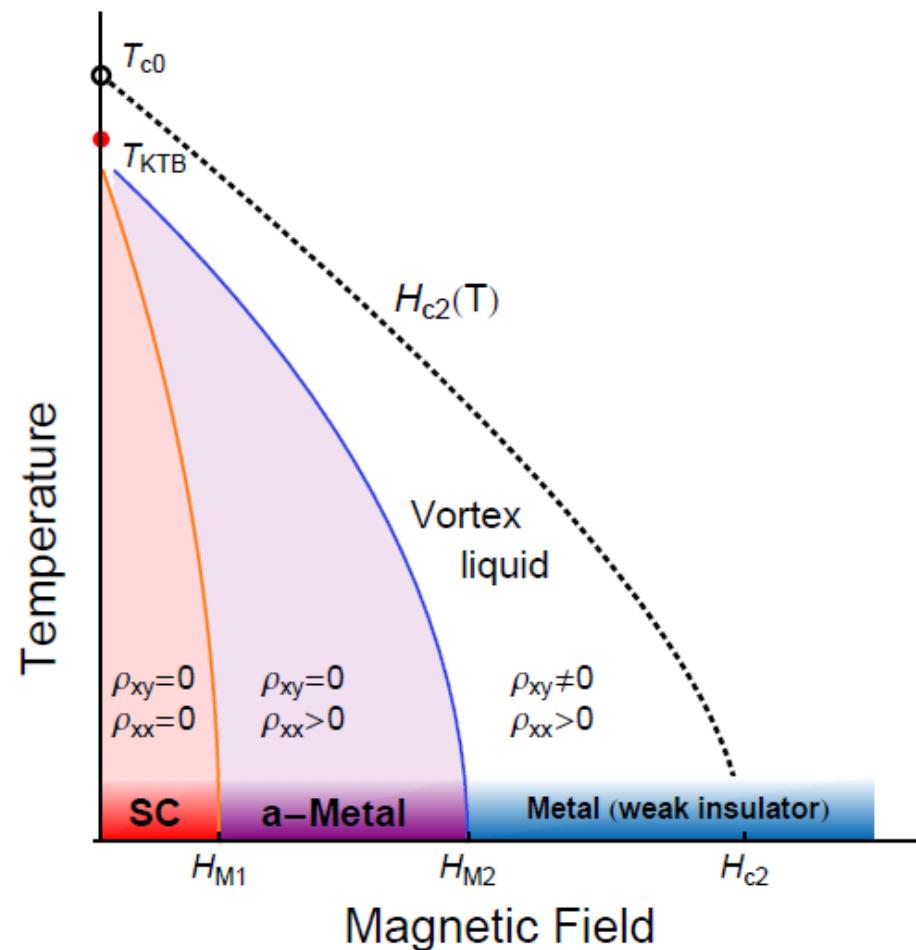
# Phase diagram for a weakly disordered 2D superconductor

- In the anomalous metallic state:

- $\rho_{xx}$  saturates  $> 0$
- Zero Hall effect

→ Particle-hole symmetry retained in the “quantum metal” phase

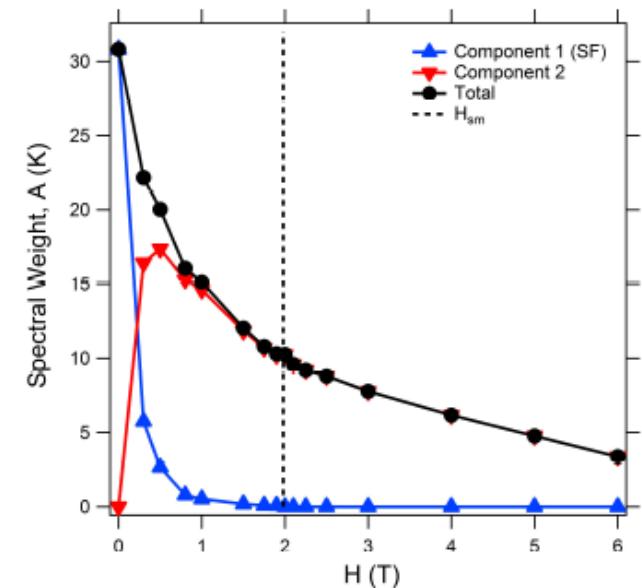
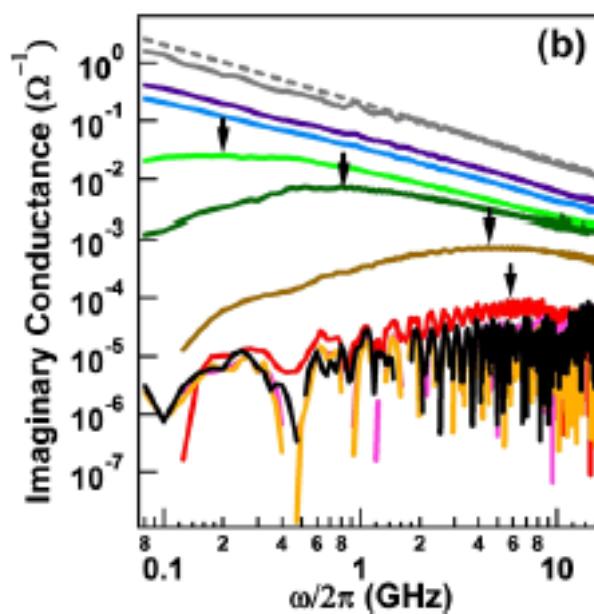
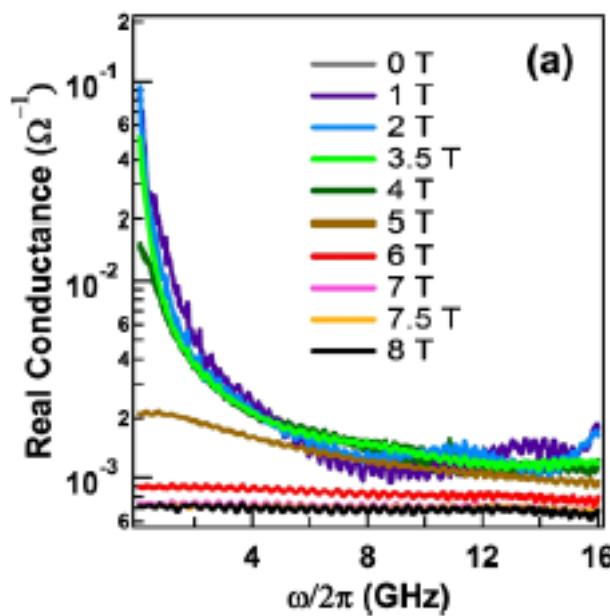
→ metal appears to remember PHS from the disrupted superconducting state



# No cyclotron resonance in the anomalous metallic state

- Microwave spectroscopy of amorphous  $\text{InO}_x$  films (N. P. Armitage/JHU)

→ No FL fermionic excitations



W. Liu, N. P. Armitage et al. *PRL* **111** 067003 (2013)

Y. Wang, N. P. Armitage et al. (arXiv, 2017)

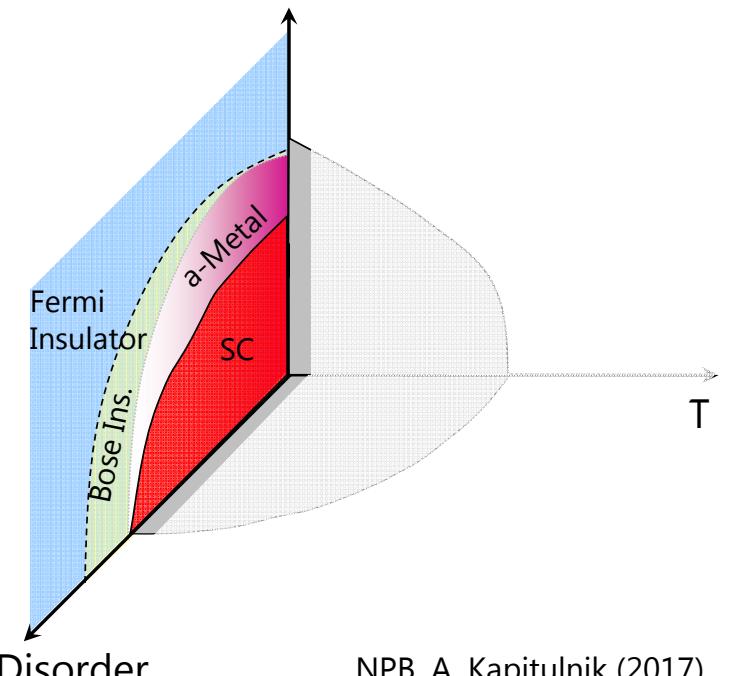
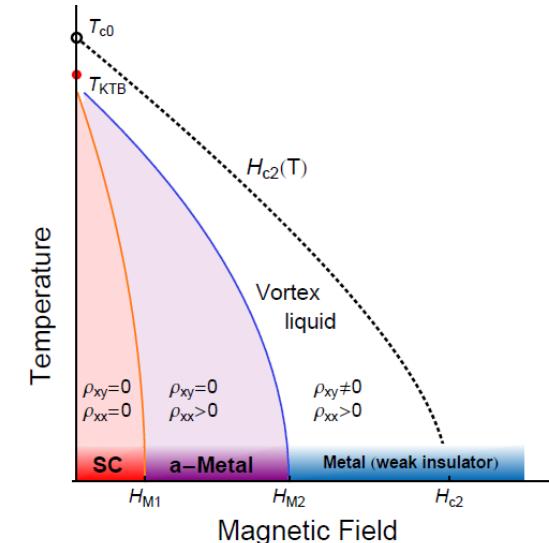
# Summary & Outlook

- Unavoidable, robust, exciting evidence for an anomalous metallic phase in 2D superconductors  
→ amorphous films, JAs, nanostructures, crystalline materials
- Zero Hall effect within the broad metallic phase region
- Indicates particle-hole symmetry from disrupted SC state

Q: How is the anomalous metal connected to the direct (self-dual) SIT?

Q: Bose metal / Inhomogeneity / composite Fermions

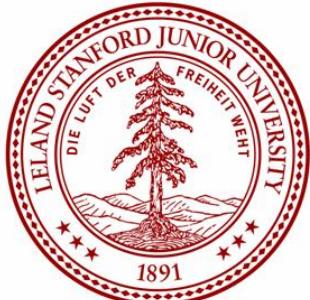
→ Next talk (S. Raghu, Stanford)



NPB, A. Kapitulnik (2017)

# Thanks to many project collaborators

---



**Steve Kivelson, Myles Steiner, Mihir Tendulkar, Li Zhang, Sang-Chul Lee, Mac Beasley, Ted Geballe, Aharon Kapitulnik**  
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*Texas A&M, Weizmann Institute*



**Alexey Suslov, Tim Murphy**  
*NHMFL Tallahassee*



**Ian Hayes, Alejandro Ruiz, Alex Frano, Mitchell Maciorski, Xue Fan, Gilbert Lopez, Jeffrey Wirjo, Maiya Vranas, James Analytis**  
*University of California, Berkeley  
Lawrence Berkeley National Lab*