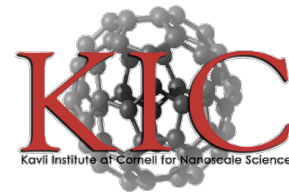


# Strong correlations in 2D semiconductor moiré superlattices



Jie Shan

KITP Reunion Conference

"Return of the Intertwined: New Developments in Correlated Materials  
(July 30, 2020)



Yanhao Tang



Lihong Li



Tingxin Li



Yang Xu



Chenhao Jin



Zui Tao



Kin Fai Mak

**Theory:** Allan MacDonald (UT Austin), Veit Elser (Cornell), Liang Fu (MIT)

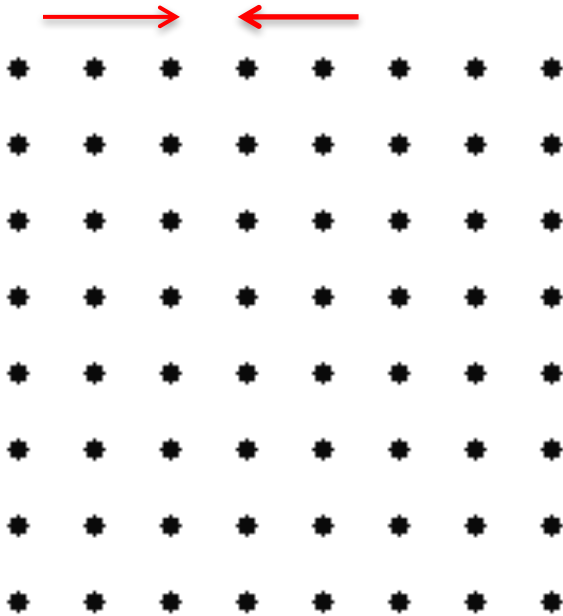
**WSe<sub>2</sub>, WS<sub>2</sub> bulk crystals:** Columbia team (Song Liu, Katayun Barmak, Jim Hone)

**Boron nitride crystals:** Kenji Watanabe, Takashi Taniguchi (NIMS)

**Moiré superlattices, new length & energy scale:  
Correlation engineering**

# Interacting quantum particles on a lattice

moiré length scale  $a$



Effect of moiré potential  
Flat band

Electron-electron interaction energy

$$U \sim \frac{e^2}{\epsilon a}$$

Bandwidth of lowest electronic miniband

$$W \sim \frac{\hbar^2 k^2}{2m^*} \sim \frac{\hbar^2 \pi^2}{2m^* a^2}$$

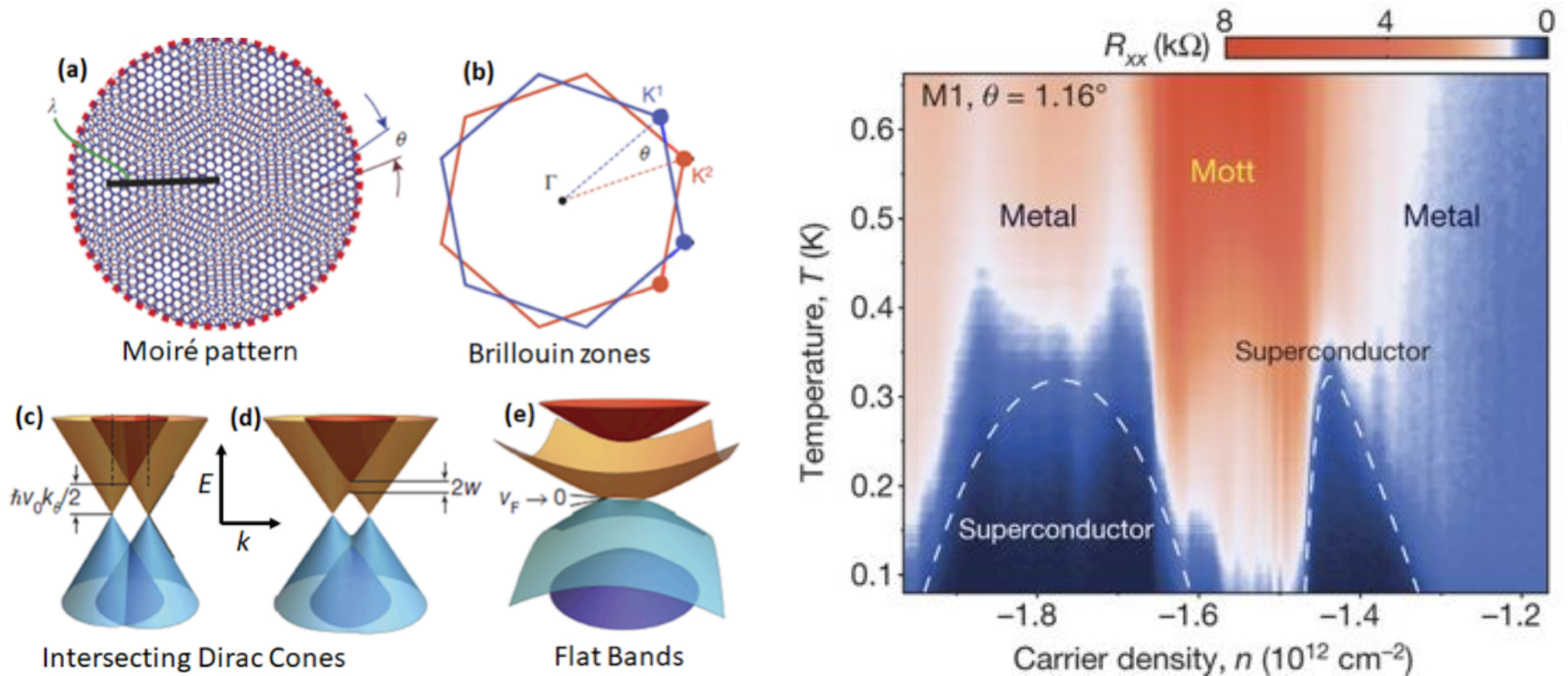
Strong correlation

$$\frac{U}{W} \sim m^* a > 1$$

For TMD monolayers,  $m^* \sim 0.5 m_0$ ,  $\epsilon \sim 4$ ,  $a \sim 10$  nm

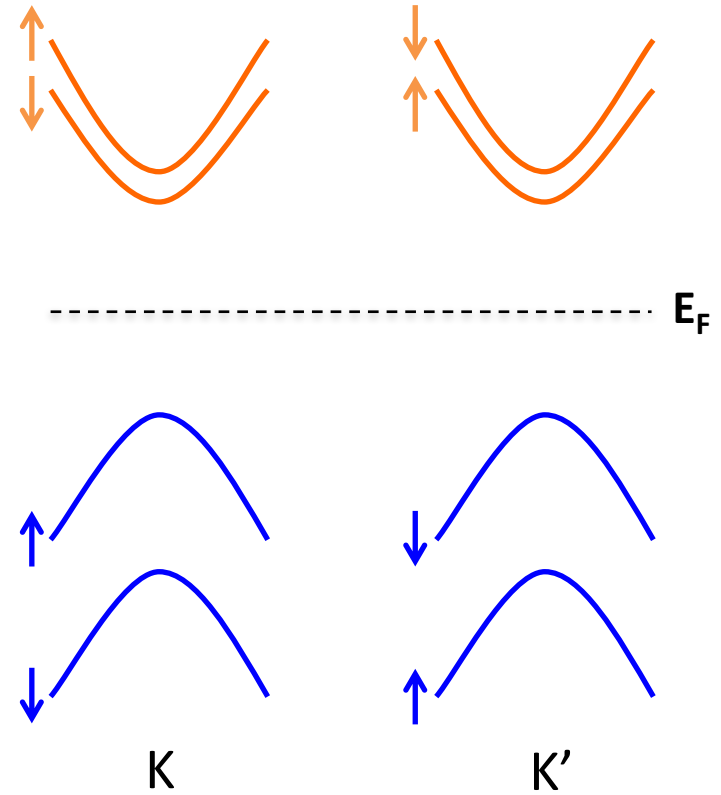
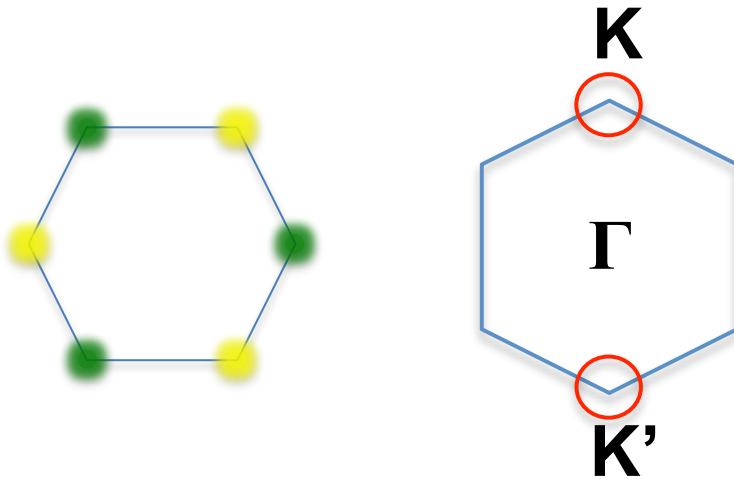
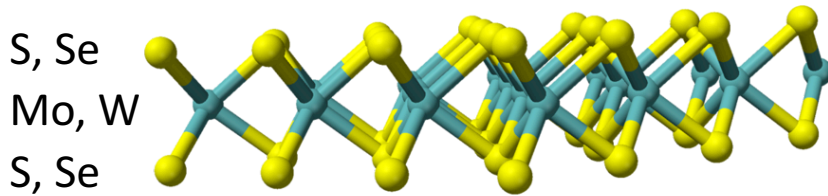
$$\frac{U}{W} \sim 5$$

# MATBG: superconductivity & insulating states



Prediction: Bistritzer & MacDonald, PNAS (2011)  
Experiment: Chen, Jarillo-Herrero, Nature (2018)

# Monolayer transition metal dichalcogenides (TMD)

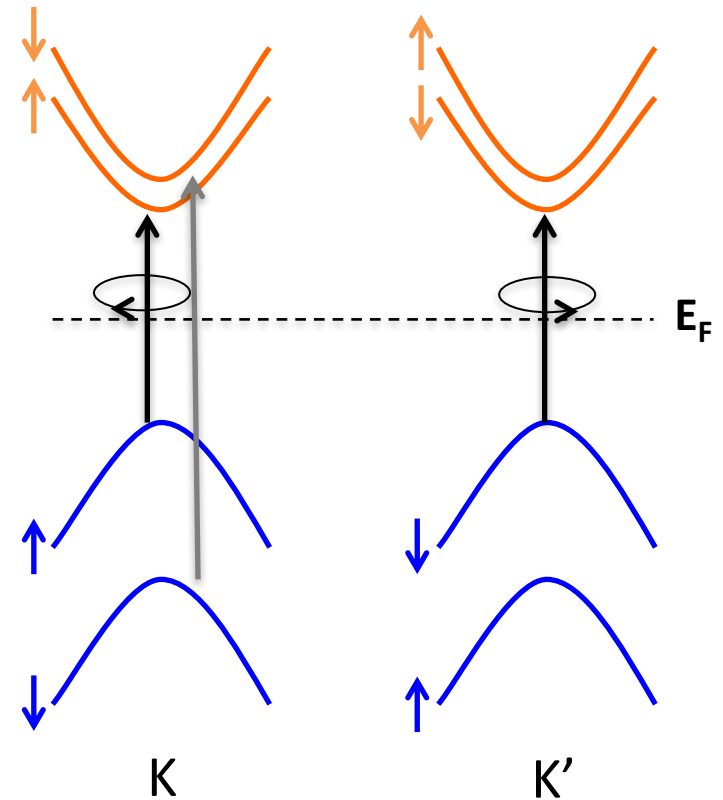
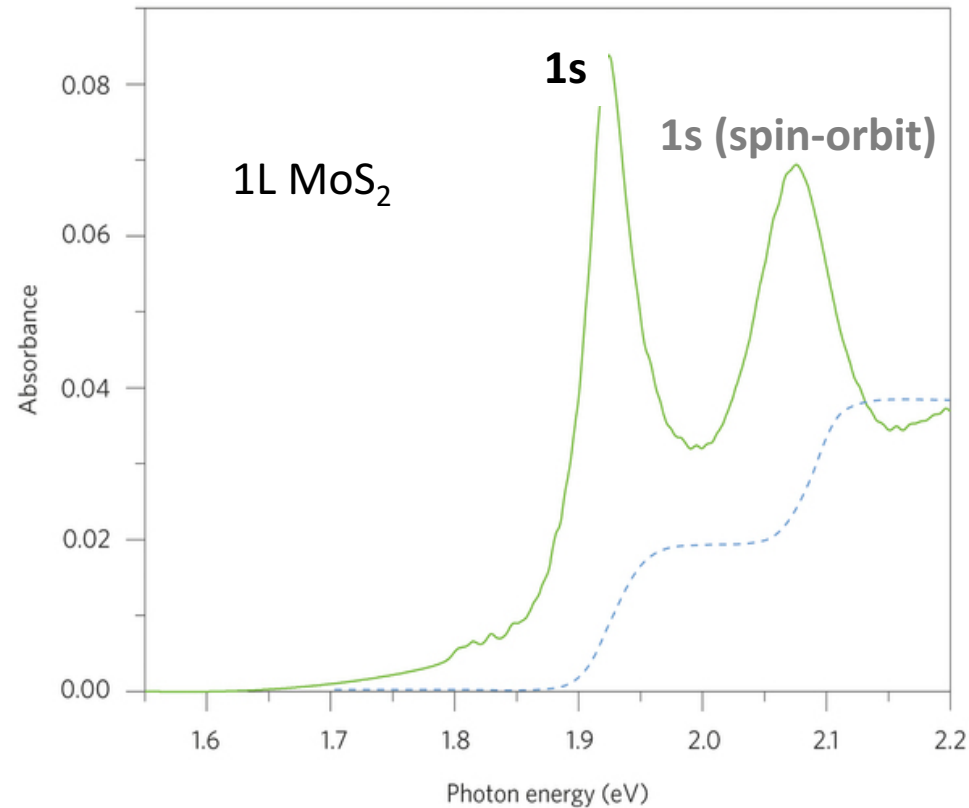


*Broken sublattice symmetry:*

- *Energy gap at K and K'*
- *Mass  $\sim 0.5 m_0$*
- *Spin splitting at K and K' from SOC*
- *Spin-valley locking*

Mak, Lee, Hone, Shan, Heinz, PRL (2010)  
Splendiani, Wang et al. Nano Lett. (2010)

# Strong light-matter interaction in TMDs

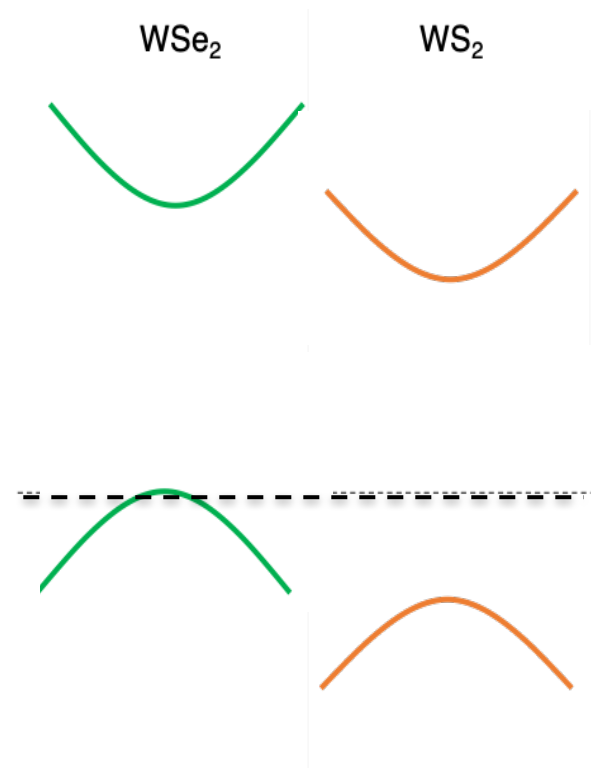


- *Strong exciton effects*
- *Optical selection rules*

# TMD hetero-bilayers

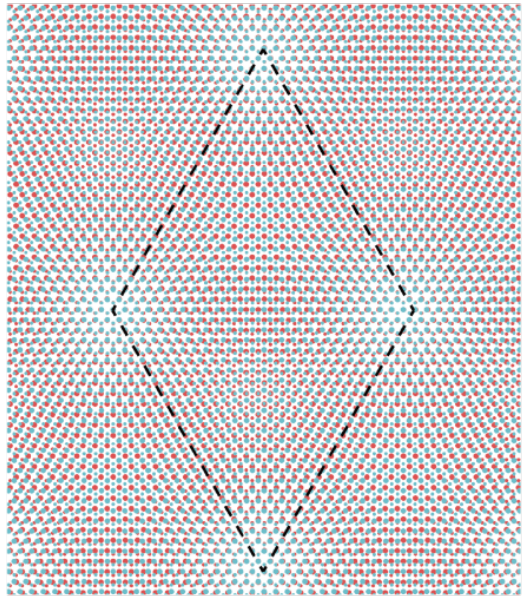
E.g.  $\text{WSe}_2$ - $\text{WS}_2$  bilayer

Type-II band alignment



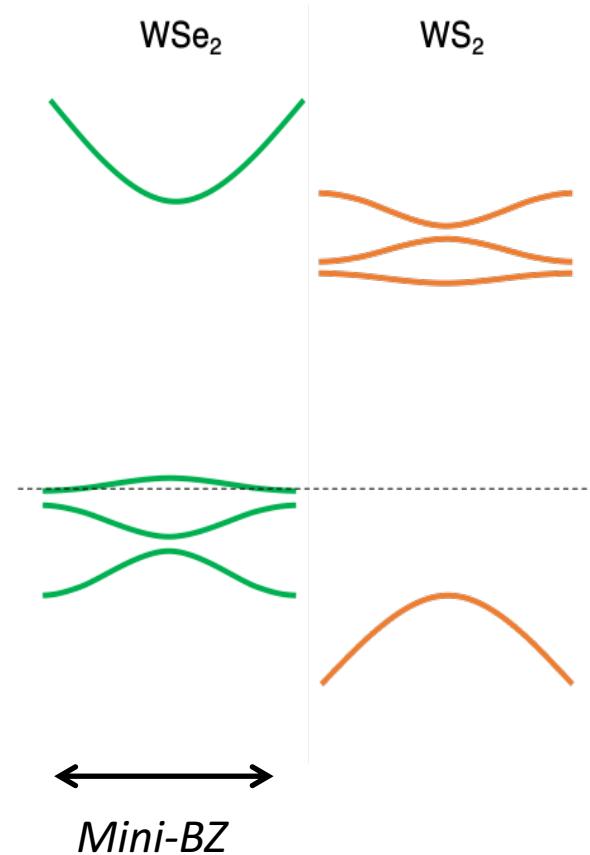
# TMD hetero-bilayers

E.g. WSe<sub>2</sub>-WS<sub>2</sub> bilayer (0-degree, 4% mismatch, 8 nm)



*Bragg reflection*

Type-II band alignment  
K valley K valley



*Lattice mismatch -> moiré superlattice*

$$\lambda \approx \frac{a}{\sqrt{\delta^2 + \theta^2}}$$



# Triangular lattice Hubbard model

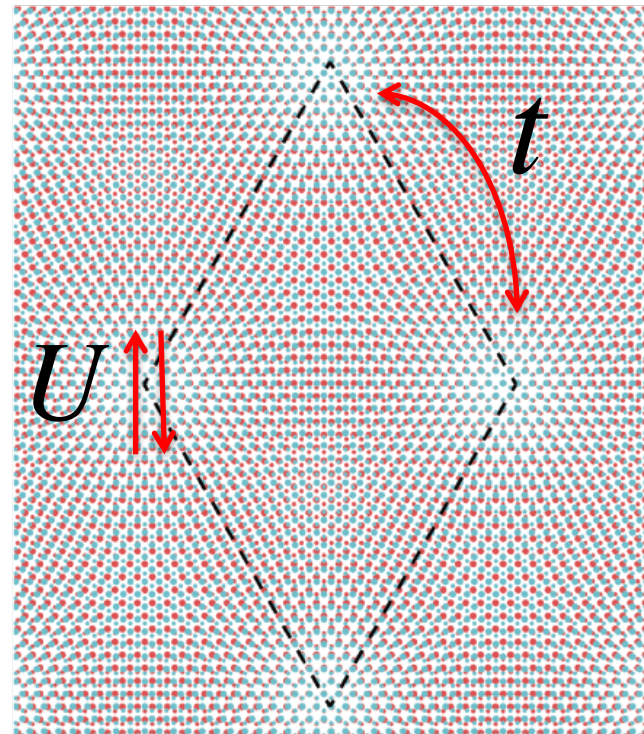
$$\mathcal{H} = -t \sum_{\langle ij \rangle, \sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

Inter-site hopping

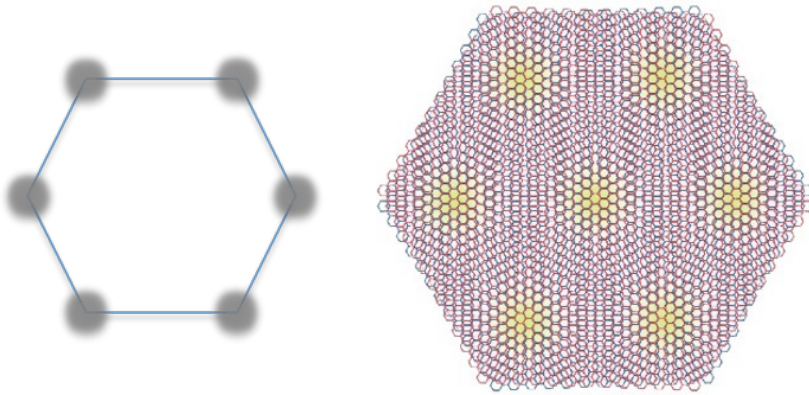
$$t \sim 1-10 \text{ meV}$$

On-site repulsion

$$U \sim \frac{e^2}{\epsilon a} \sim 10\text{'s} - 100 \text{ meV}$$

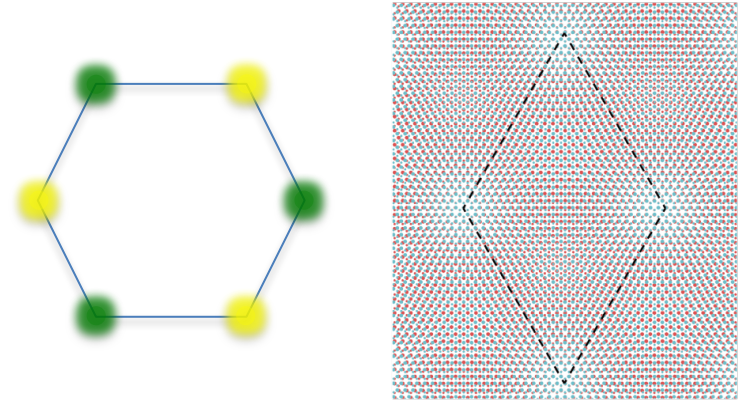


# Twisted bilayer graphene vs TMD hetero-bilayers



## *Twisted bilayer graphene (topology)*

- Wannier obstructions
- Total degeneracy: 8-fold
- Magic angle

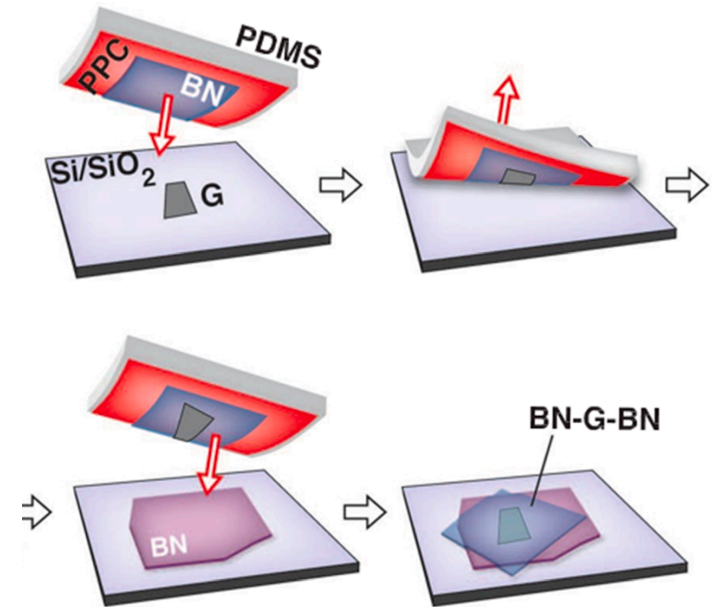
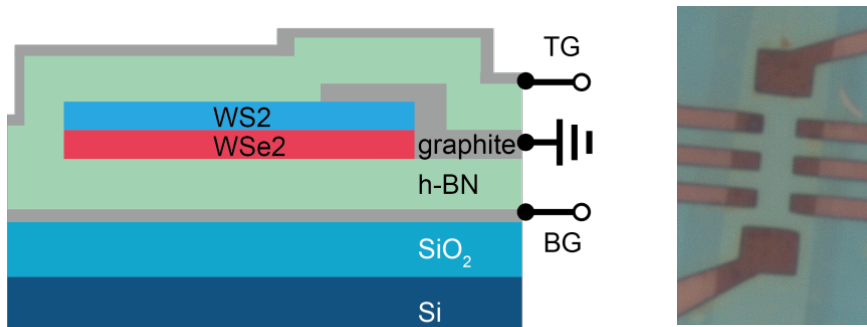


## *TMD hetero-bilayer (correlation)*

- Localized Wannier orbitals
- Stronger moiré potential (correlation)
- Total degeneracy: 2-fold, spin-valley DOF
- Wide range of twist angle

# Sample and device fabrication

Dual-gate device continuous control of fillings  
Angle-aligned WSe<sub>2</sub>/WS<sub>2</sub> (0 and 60 degrees)



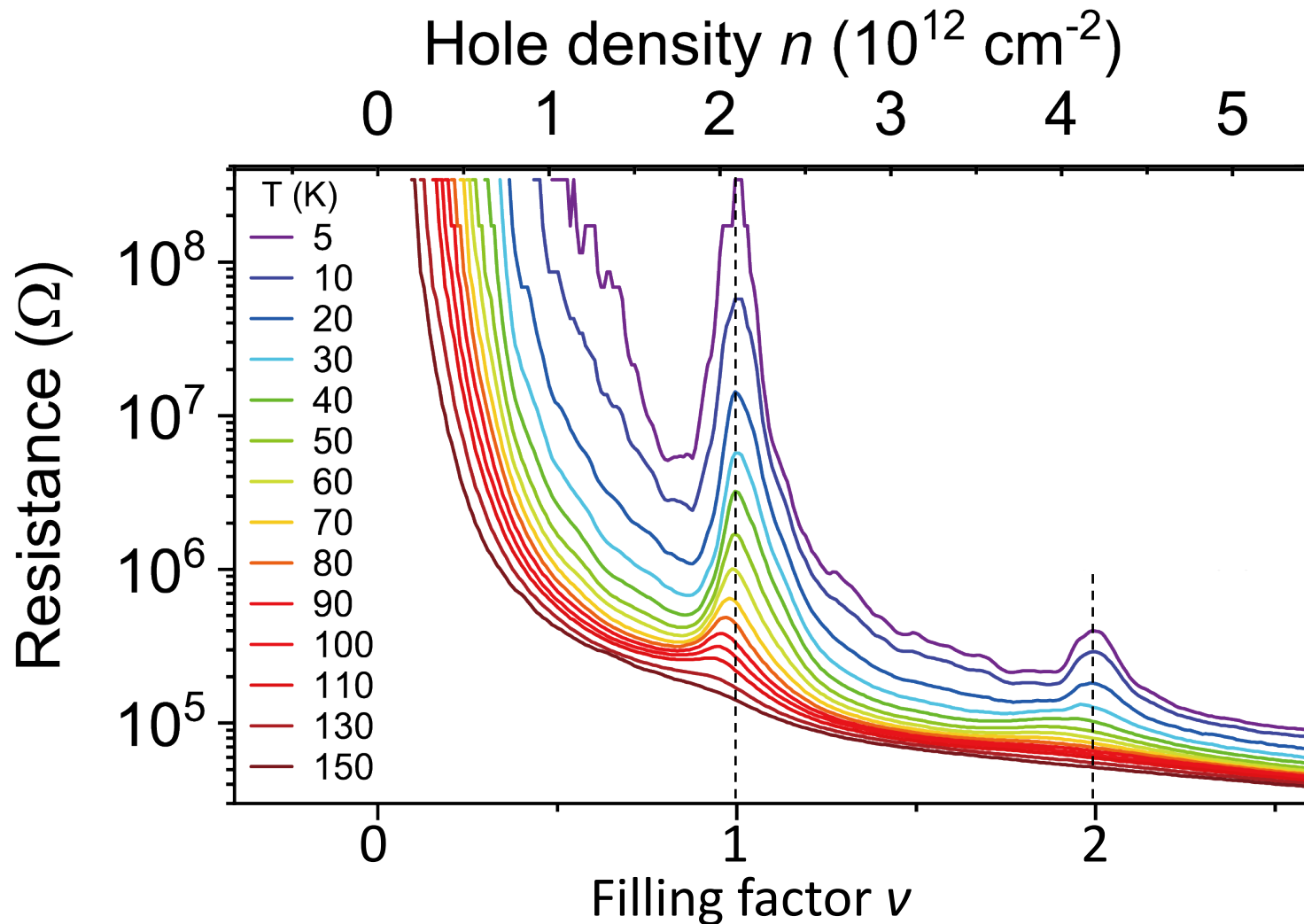
## Measurements

- Optical measurements (1 micron)
- In-plane transport
- Capacitance (compressibility)

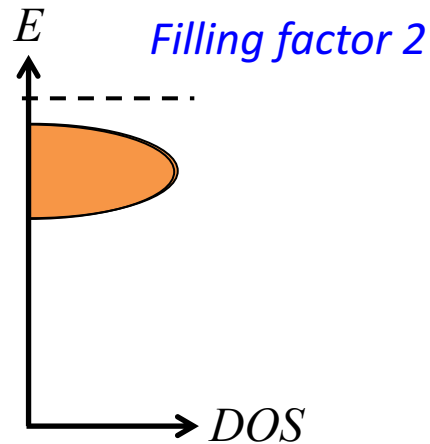
- Crystal axis orientation determined by nonlinear optical techniques
- Alignment of different materials within 0.5 degree

**TMD moiré superlattices ( $\nu = 1$ )**

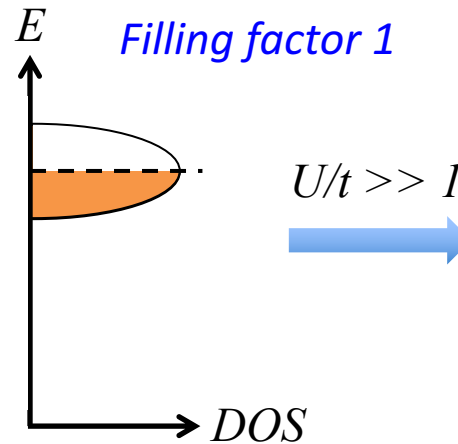
# Insulating state at half filling ( $\nu = 1$ )



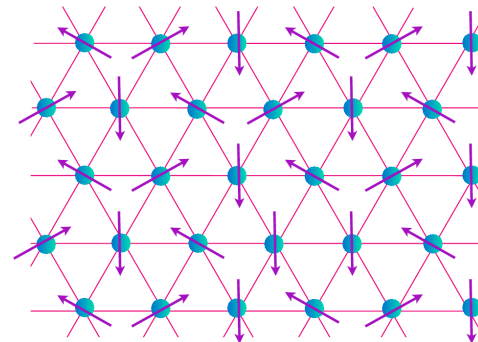
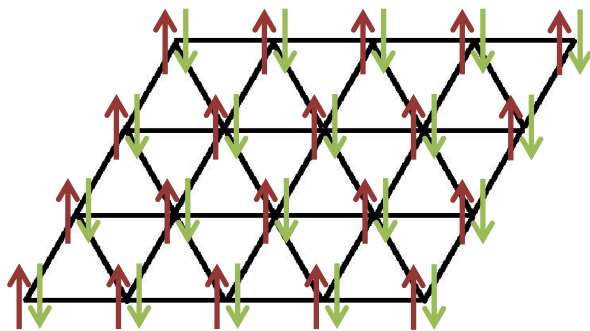
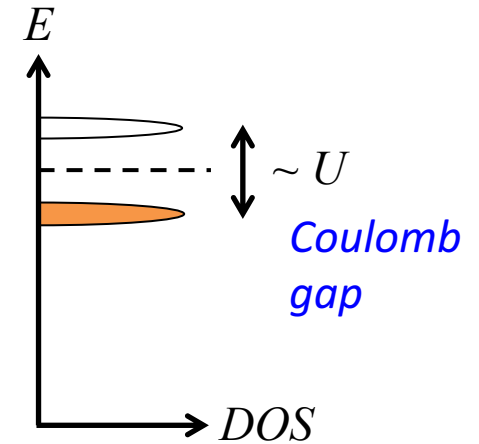
# Mott insulating state at half filling ( $\nu = 1$ )



Band insulator



Mott insulator



$\frac{1}{2}$ -filling R peak vanishes  
at  $\sim 150$ - $200$  K

->  $U \sim 20$  meV

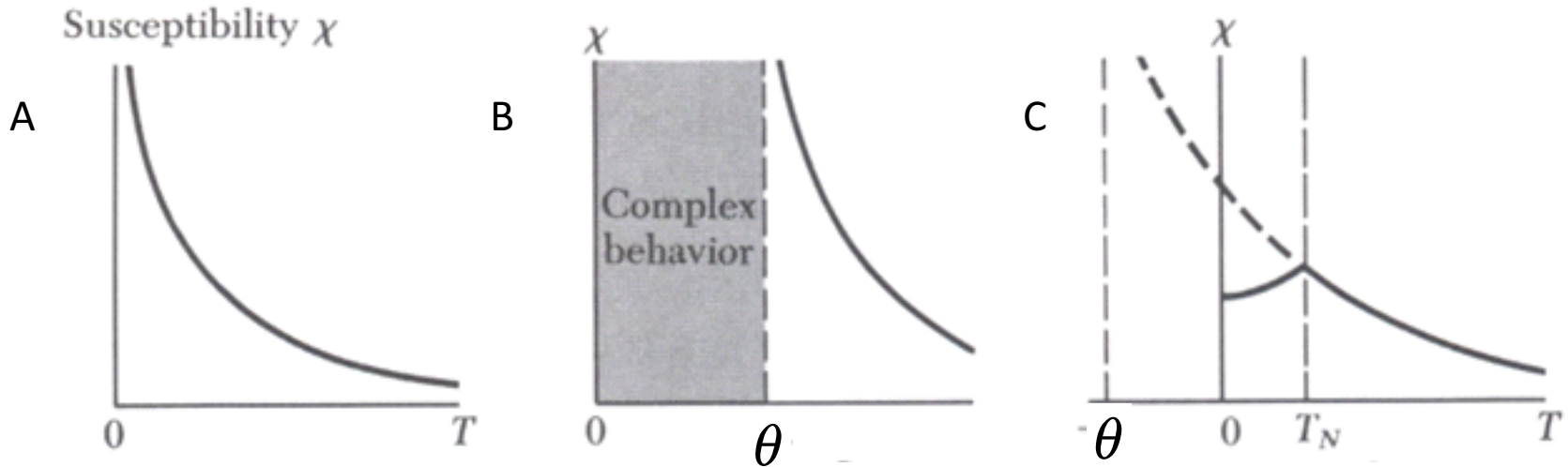
Alternative: Charge-transfer insulator (Liang Fu)  
arXiv:1910.14061

# Magnetic susceptibility

Paramagnetism

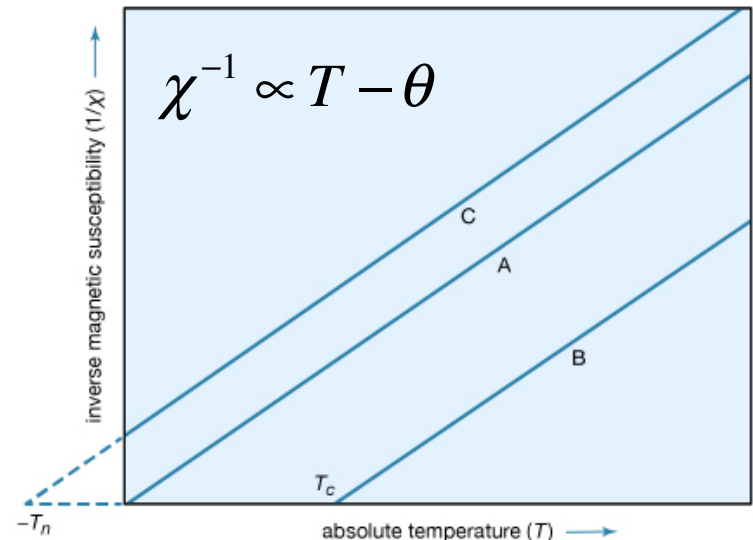
Ferromagnetism

Antiferromagnetism

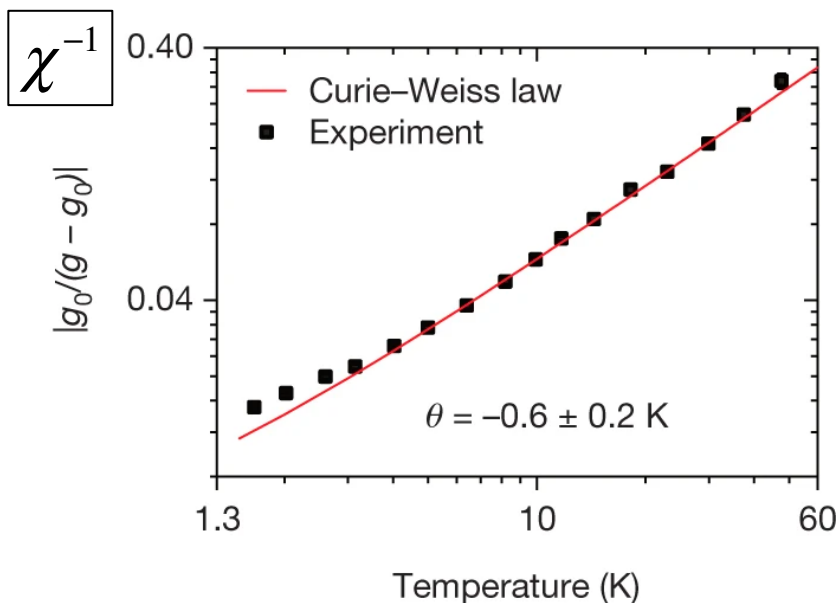
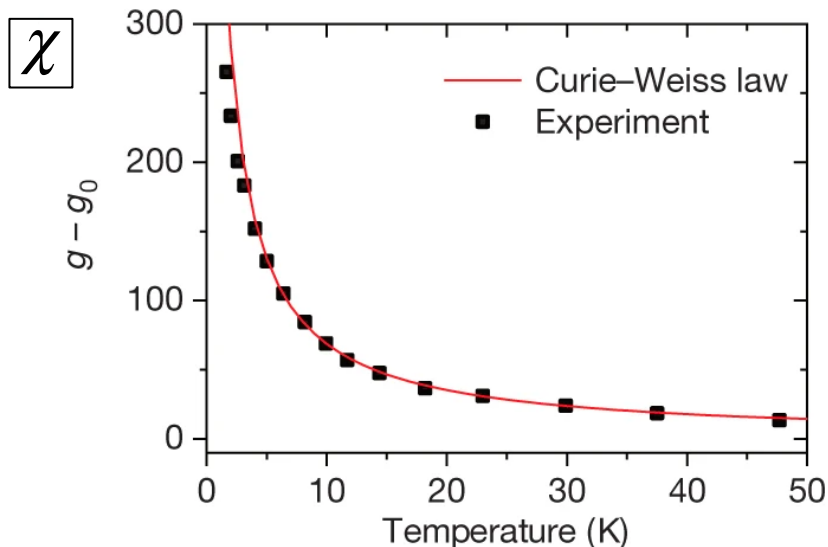


For  $T \gg J$   $\chi = \frac{C}{T - \theta}$   $\theta \sim -J$   
 Weiss temperature

**$\theta > 0$ : ferromagnetic**  
 **$\theta < 0$ : antiferromagnetic**



# Magnetic susceptibility measurement

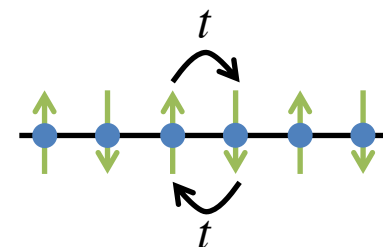


Curie-Weiss law

$$\chi^{-1} \propto T - \theta$$

$$\theta \approx -0.6 \text{ K} \sim -0.05 \text{ meV}$$

$$\theta \sim -J \sim \frac{t^2}{U}$$



Super-exchange

$$U \sim 20 \text{ meV}$$

$$\rightarrow t \sim 1 \text{ meV}$$

$$\rightarrow \frac{U}{t} \sim 20$$

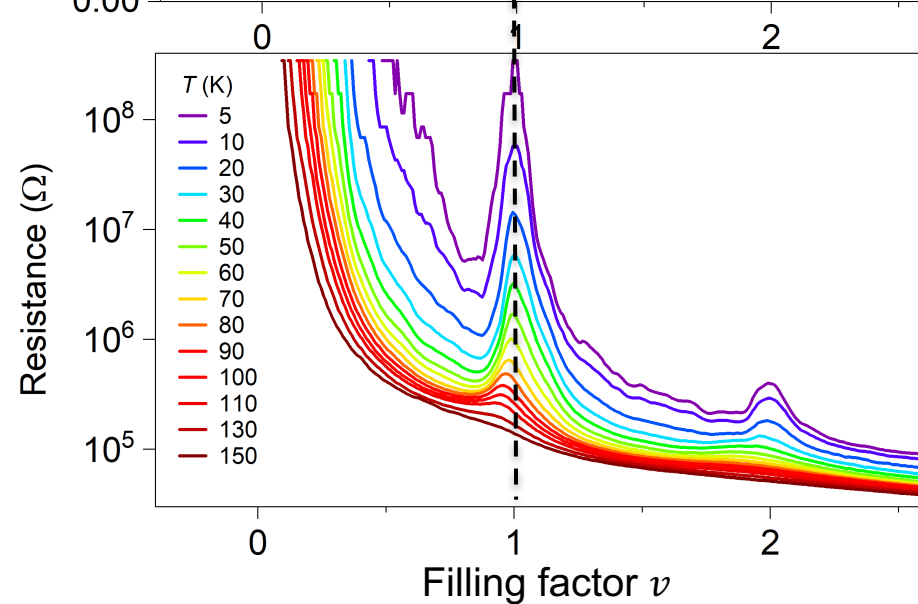
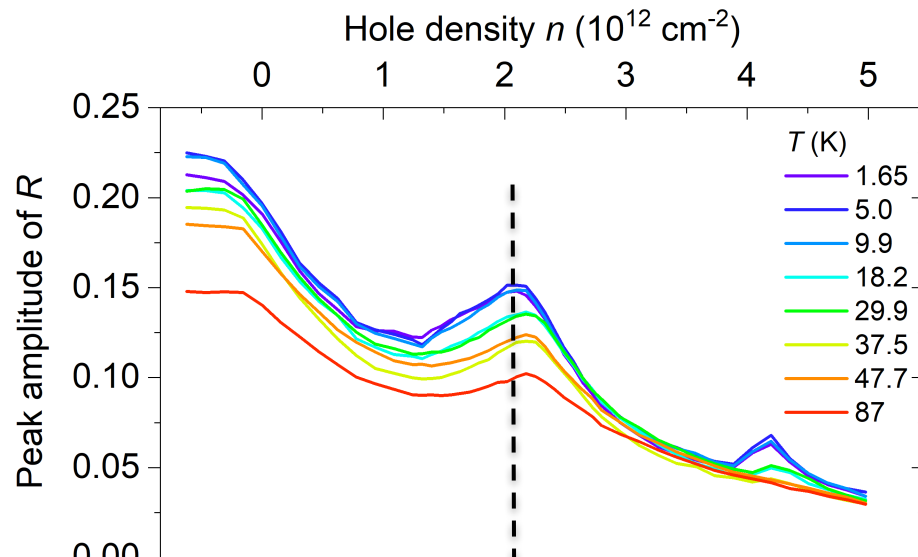
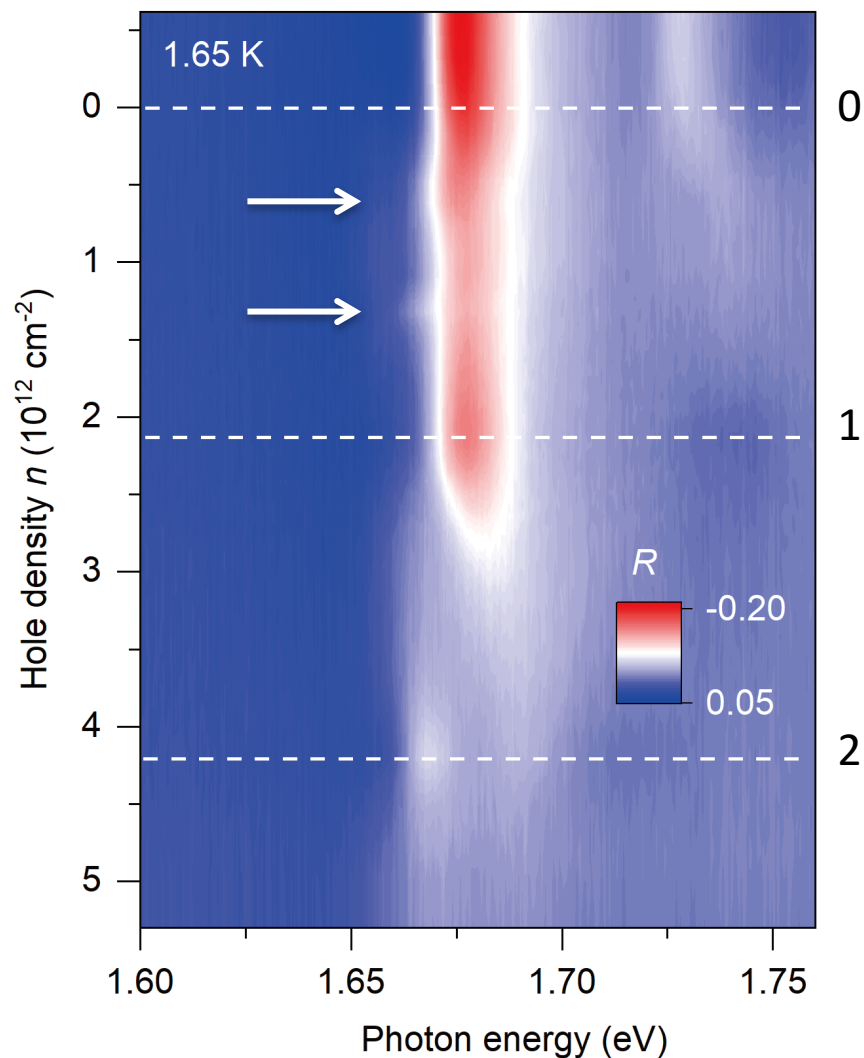
$$H_S = \sum_{R,R'} J(R' - R) \mathbf{S}_R \cdot \mathbf{S}_{R'}$$

Heisenberg model

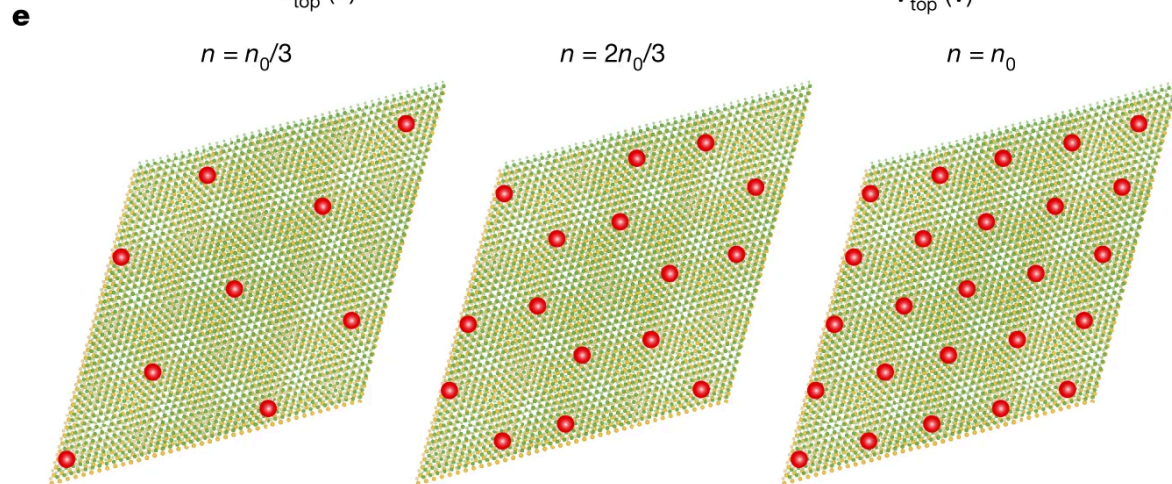
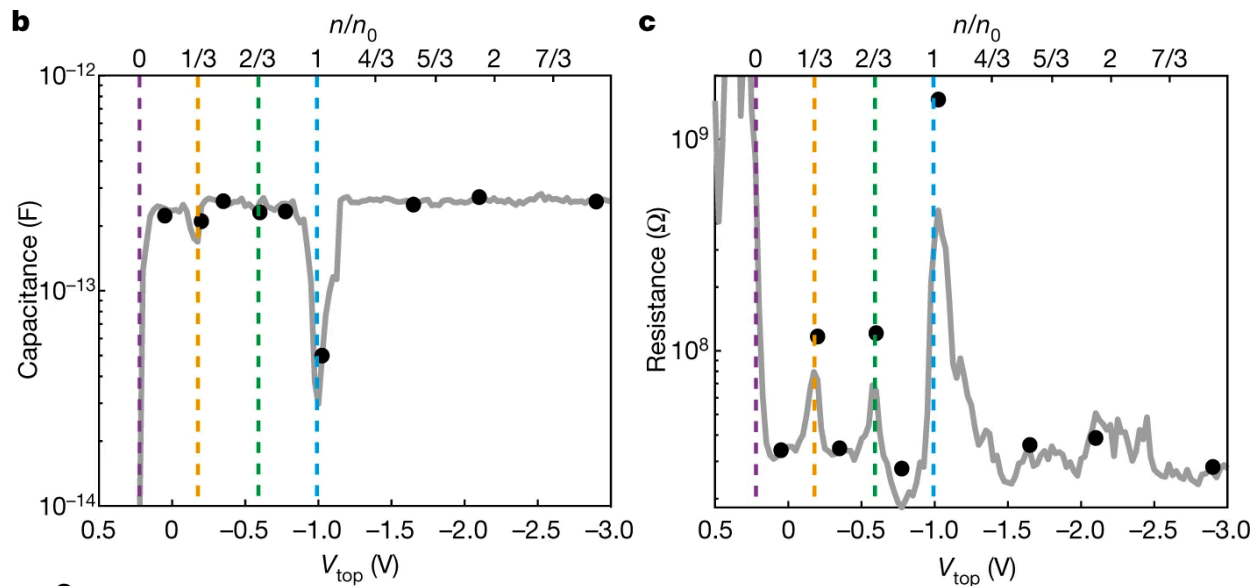


# Optical signature of the Mott insulating state

Fundamental exciton in WSe<sub>2</sub>



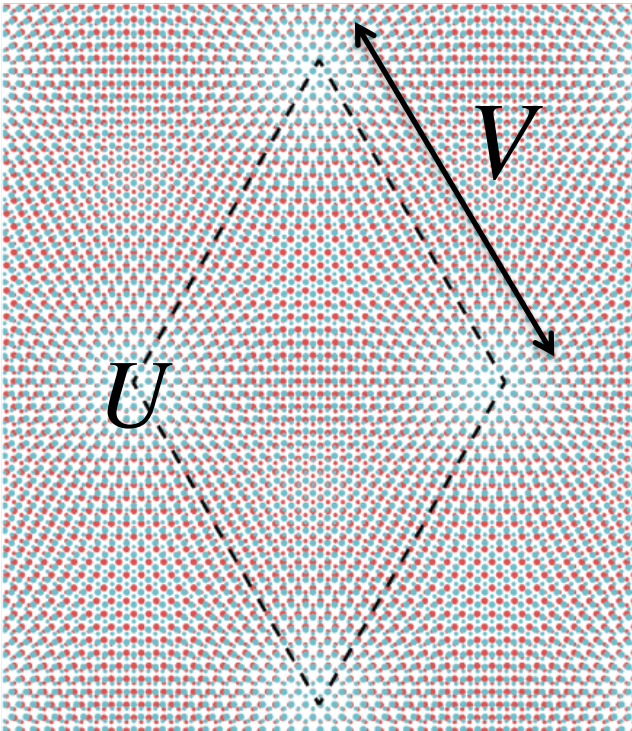
# Charge-ordered states ( $\nu = 1/3, 2/3$ )



Charge-ordered states  
(minimize long-range V)

Regan, Wang, Jin et al. Nature (2020)

# Extended Hubbard model



Gate separation much bigger than moiré period

$$V(r) \approx \frac{e^2}{4\pi\epsilon\epsilon_0 r}$$

Long-range Coulomb  $> t$

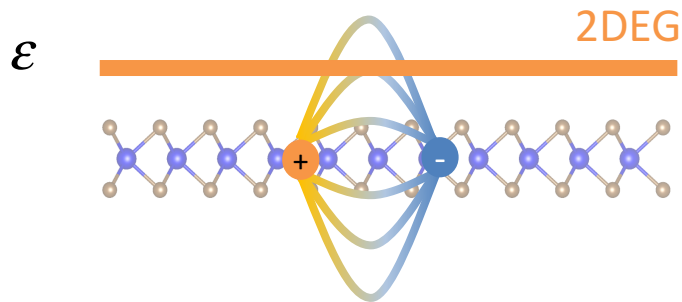
Extended Hubbard model

$$H = H_0 + \frac{1}{2} \sum_i \sum_{j \neq i} V(r_{ij}) n_i n_j$$

$H_0$  Hubbard model Hamiltonian

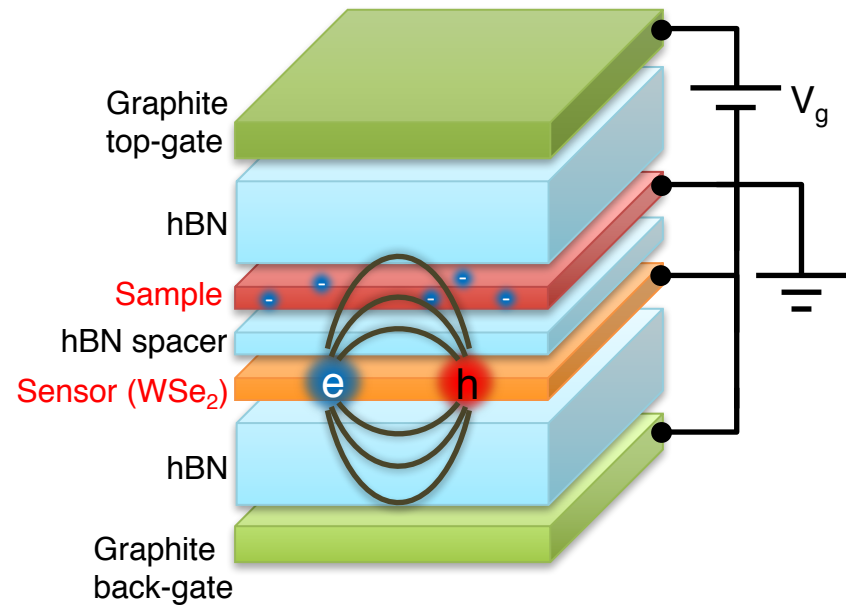
**Charge-ordered states ( $\nu < 1$ )**

# A new exciton sensing technique



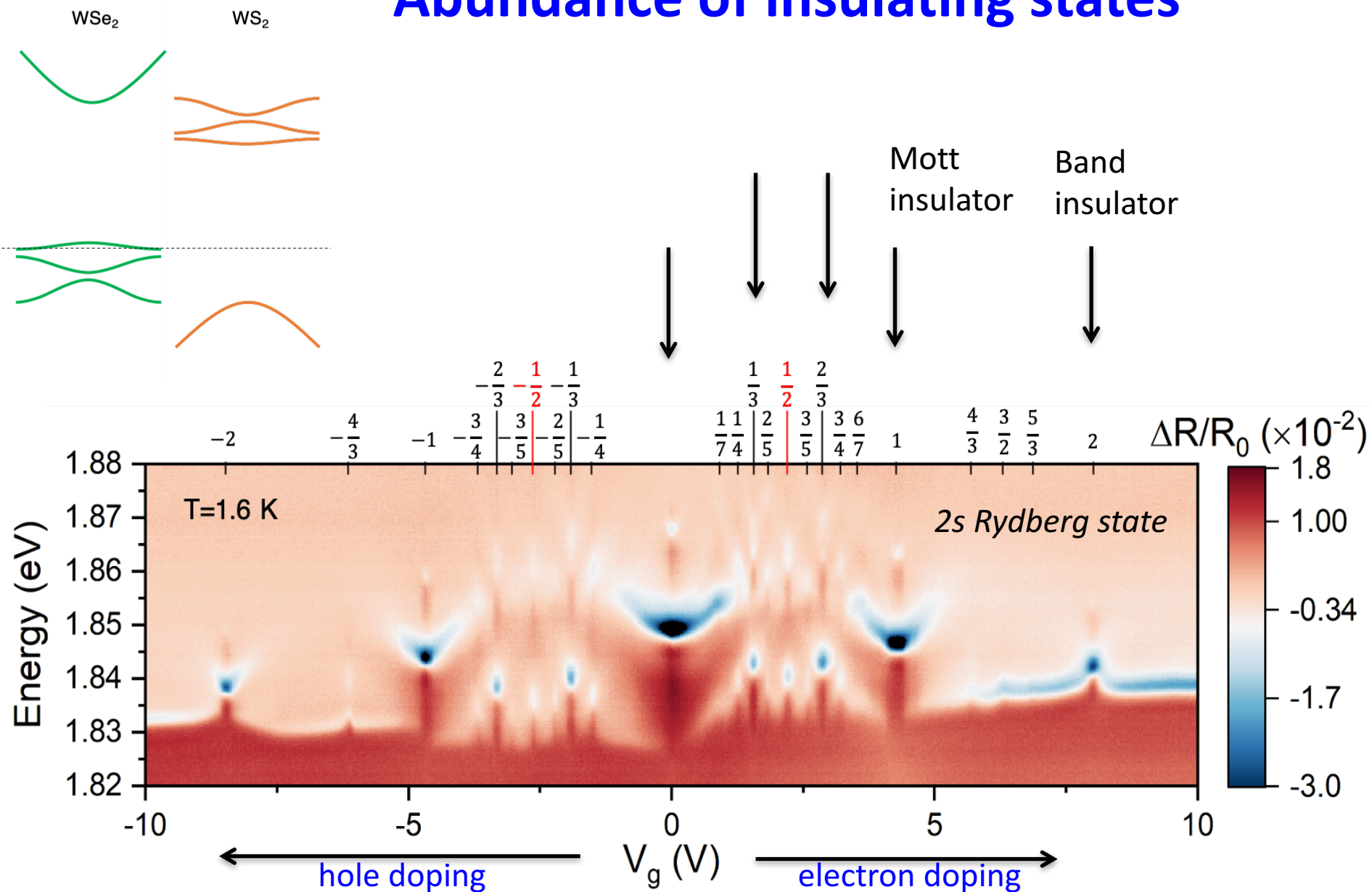
2D H-atom with  $1/r$  potential  
 1s state  $\sim 1$  nm  
 2s state  $\sim 5$  nm

$$E_b^{(n)} = \frac{m_r e^4}{2\hbar^2 (4\pi\epsilon\epsilon_0)^2 (n-1/2)^2} \propto \frac{1}{(\epsilon)^2}$$

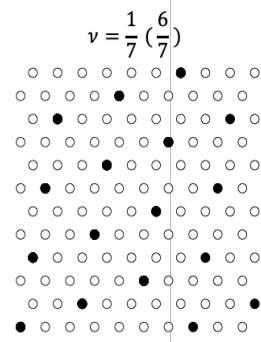
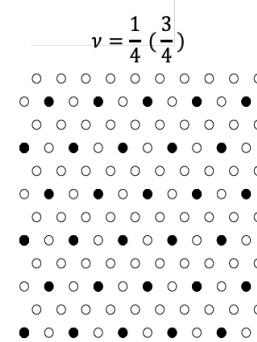
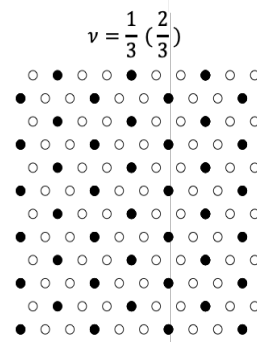
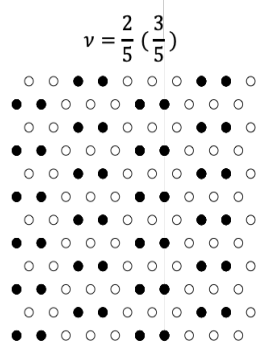
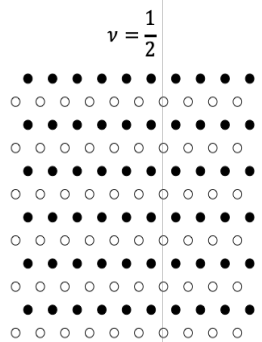
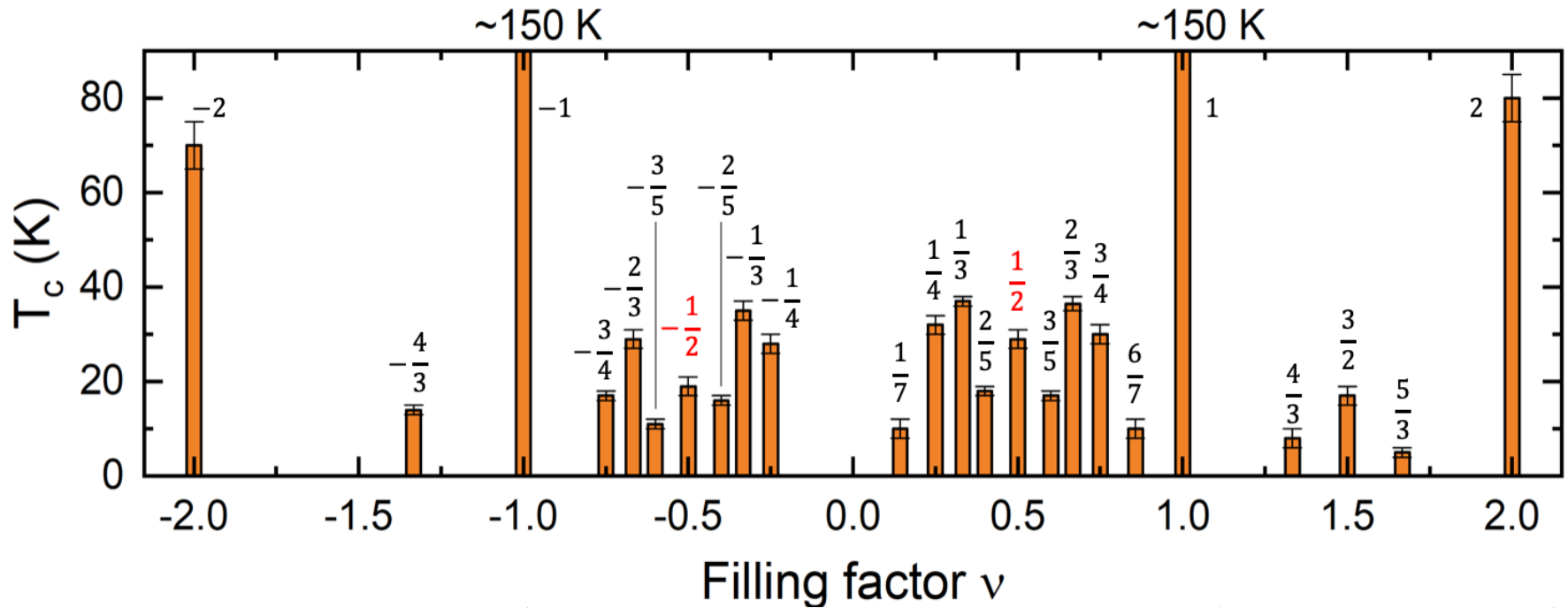


- ***Metallic (compressible): smaller binding energy, lower intensity***
- ***Insulating (incompressible): larger binding energy, higher intensity***

# Abundance of insulating states



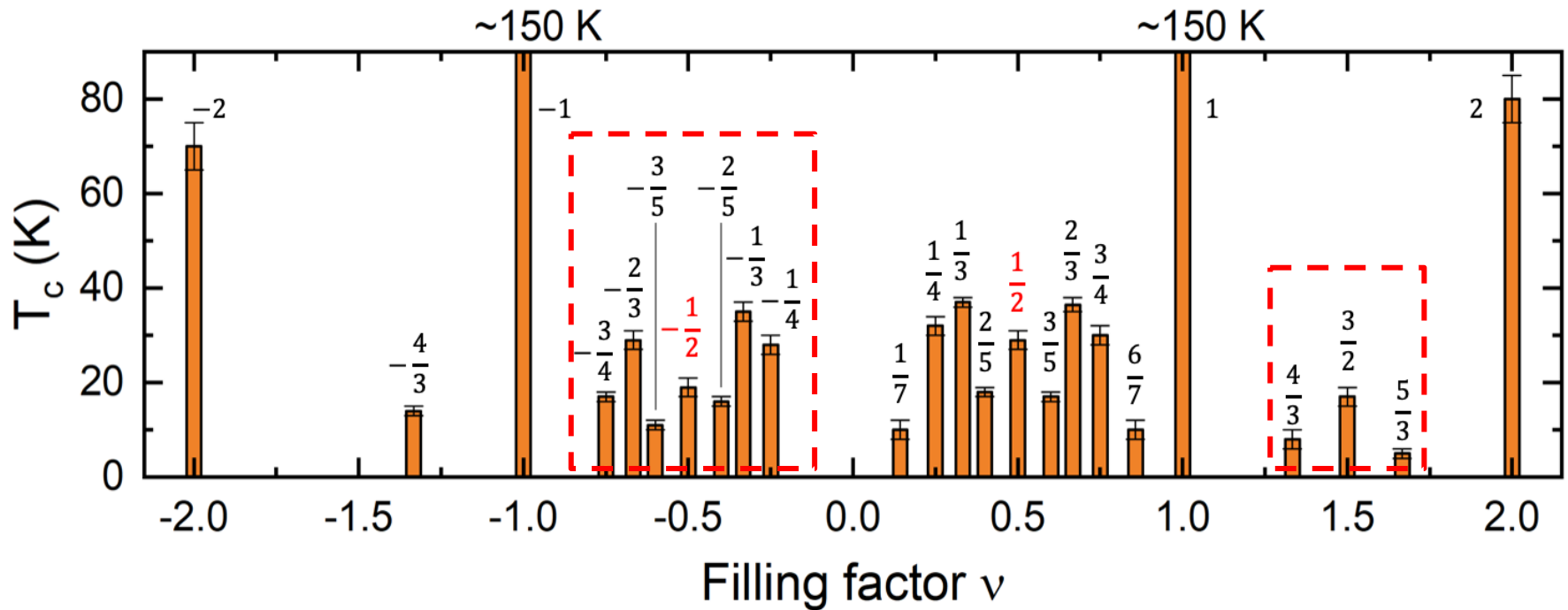
# Ordering temperature



$$H = \frac{1}{2} \sum_i \sum_{j \neq i} V(r_{ij}) n_i n_j \quad (\text{Monte Carlo, Veit Elser})$$

Xu et al. (arXiv:2007.11128)

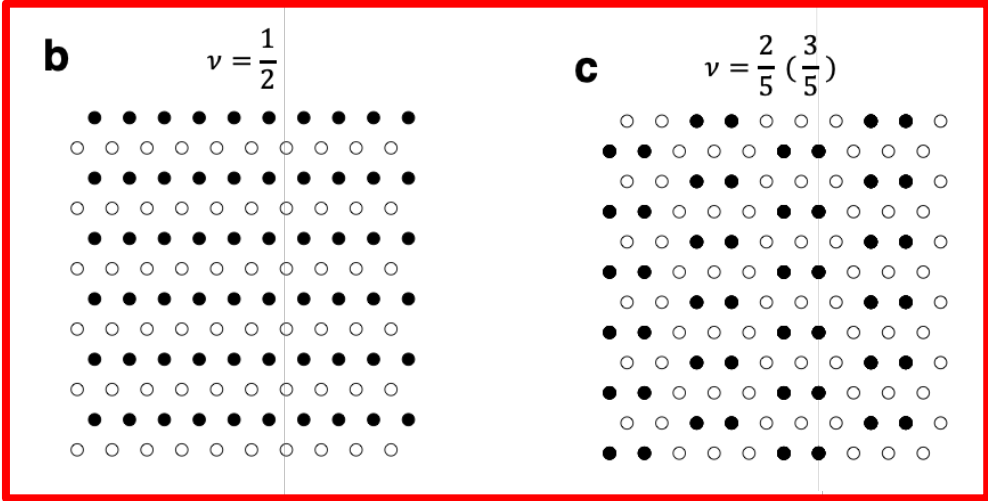
# Quantum effects



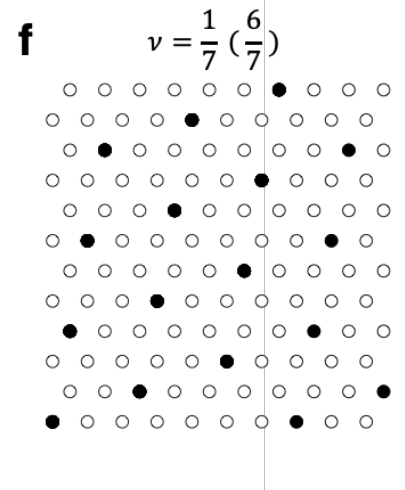
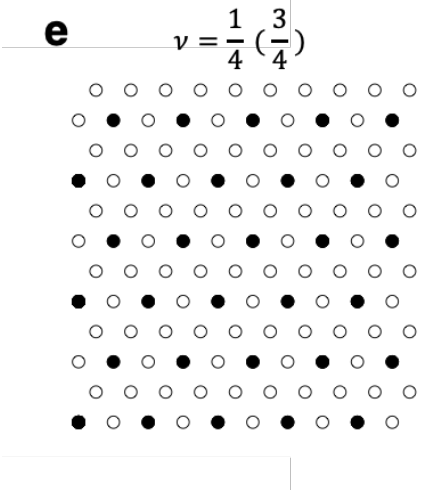
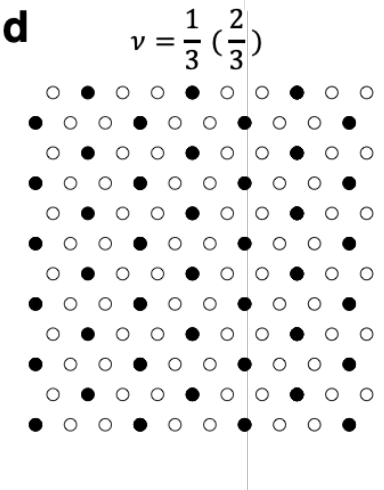
- Asymmetry about  $\frac{1}{2}$  indicates effects of quantum fluctuations
- Much weaker states for  $\nu > 1$   $\rightarrow$  higher kinetic energy for  $\nu > 1$
- Stronger insulating states on the electron side



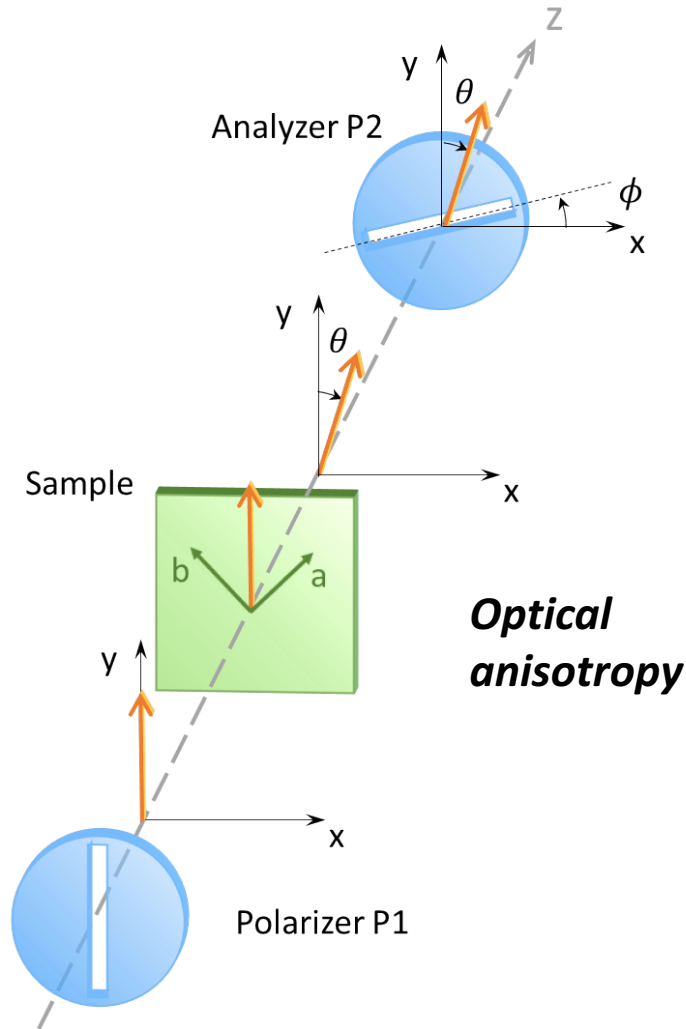
# Stripe phases



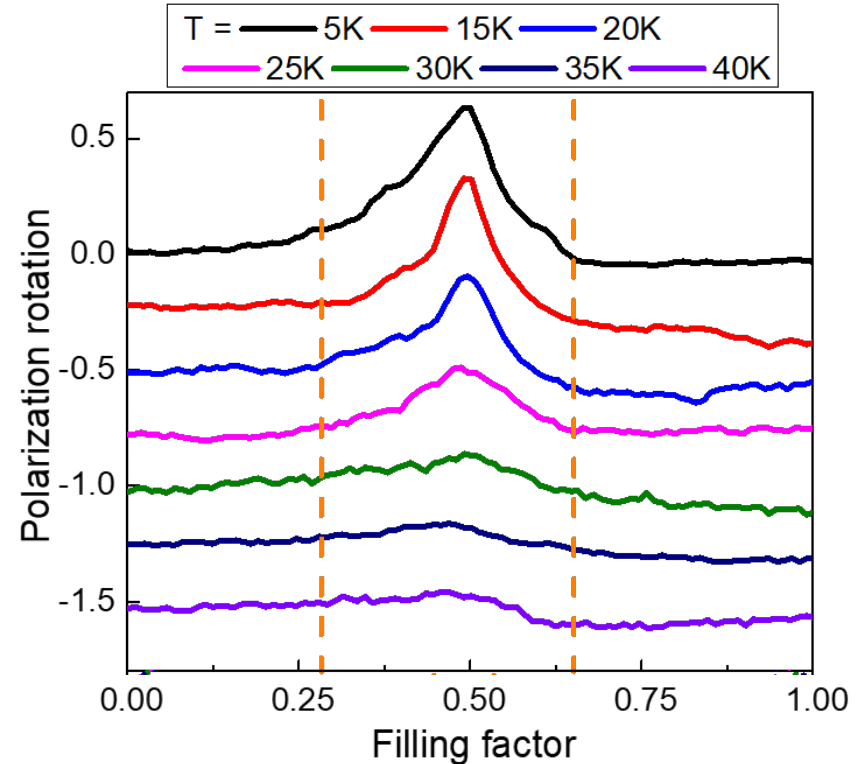
*Break rotational symmetry!*



# Optical detection of stripe phases

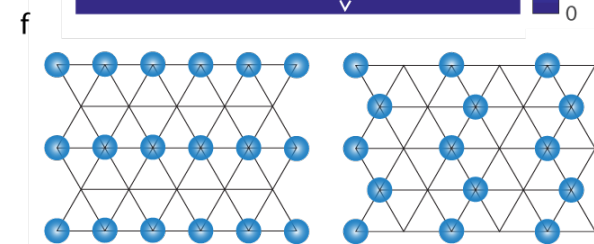
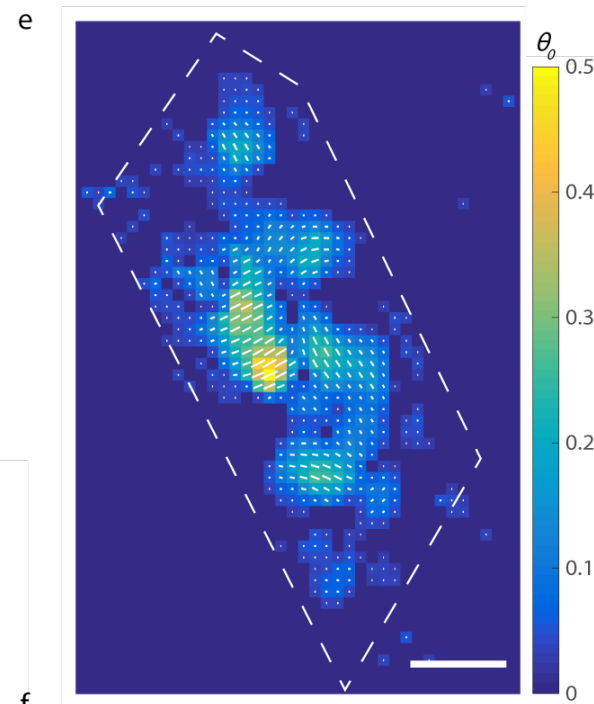
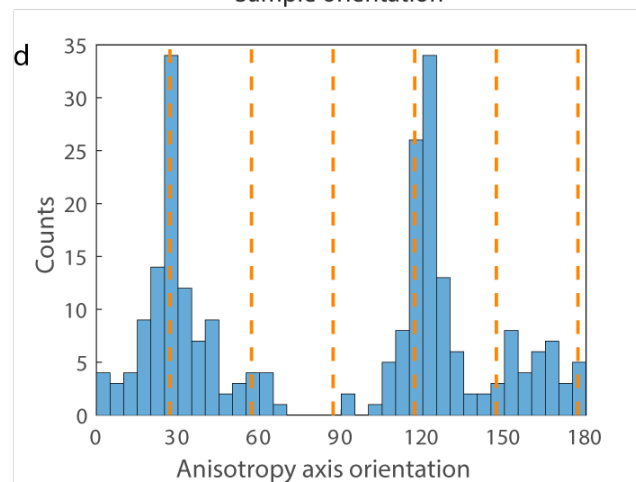
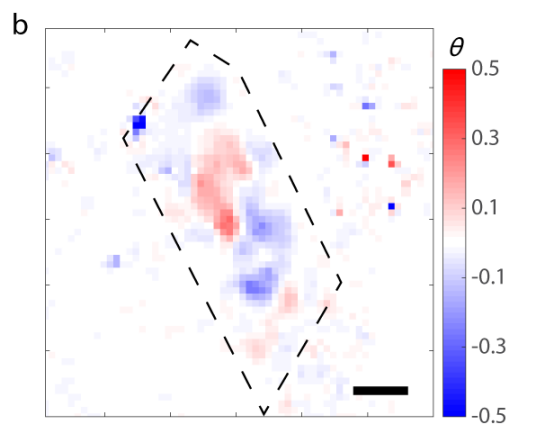
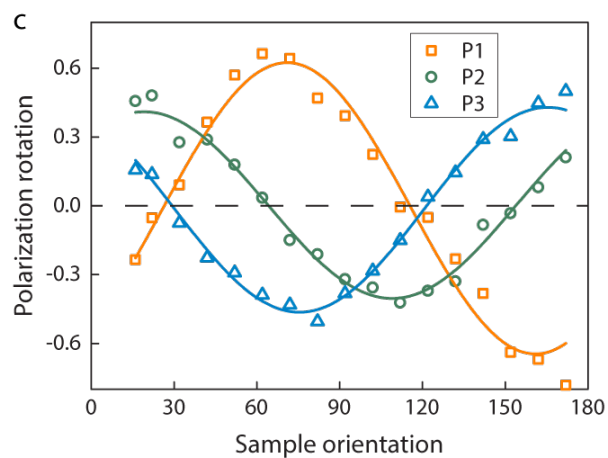
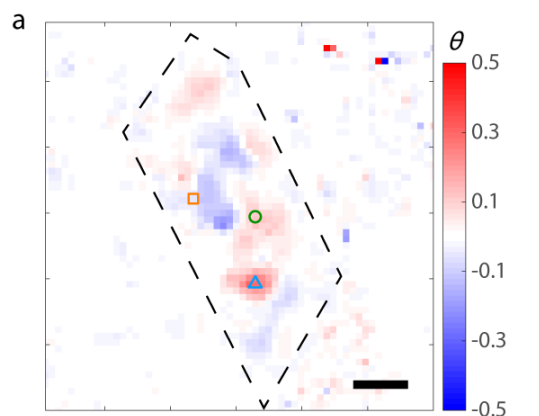


In collaboration with Liang Fu  
Jin, Tao, Li et al. (arXiv:2007.12068)



- Pronounced electronic anisotropy  $v@1/2$
- Disappear linearly with  $T$  around 35 K
- Anisotropy @ compressible regions  
-> nematic/smectic phases

# Stripe domain patterns



# Summary and outlook

- TMD moiré system provides a unique platform to study strong correlations with highly tunable parameters
- Extended Hubbard model on triangular lattices
- Experimental observation
  - AF Mott insulator at half filling ( $\nu = 1$ )
  - Abundance of charge-ordered states at fractional fillings
  - Some are stripe crystals, electronic liquid crystals also possible
- The system is very rich. Research is at an early stage.
- Unconventional superconductivity?
- Interplay of topology and correlation?
- Bose-Hubbard model physics (with iexcitons)?
- Ohmic contact?
- new experimental probes that can access the intertwined charge, spin, valley and collective excitations?