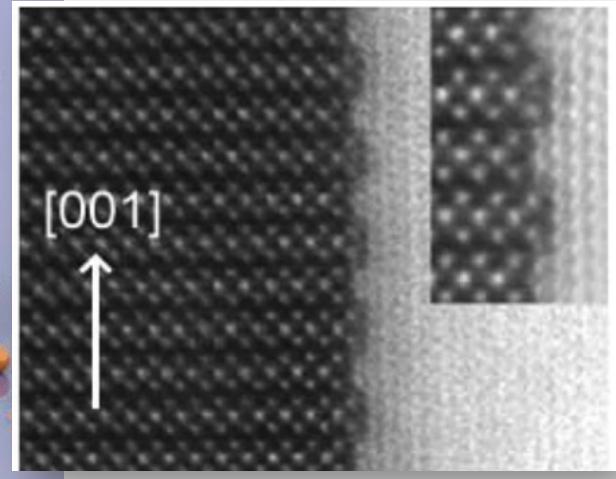
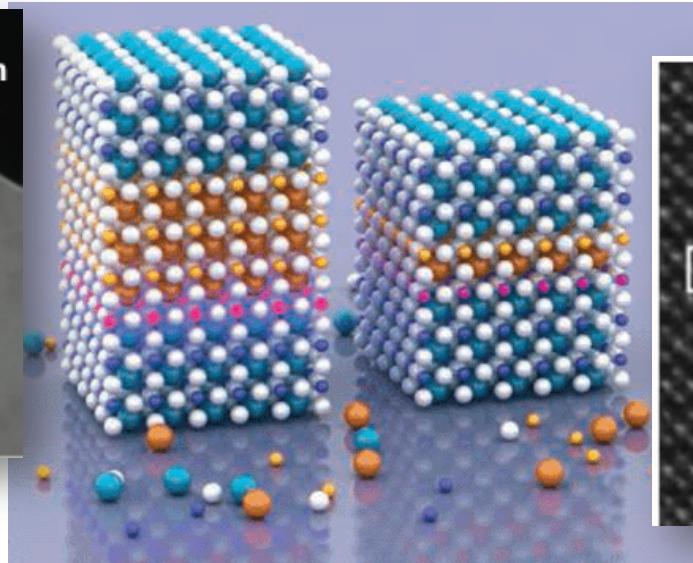
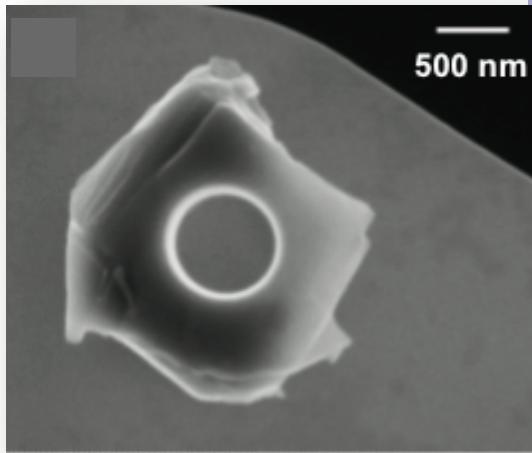


Artificially Structured Superconductors

Loops, Boundaries and Interfaces

Manfred Sigrist

ETH Zürich



Artificially Structured Superconductors

Loops, Boundaries and Interfaces

Manfred Sigrist

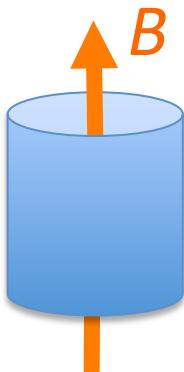


- artificial structures:
new properties and robustness of superconducting phases
- unconventional superconductivity in confined spaces
- spin-triplet superconductivity: d-vector manipulation

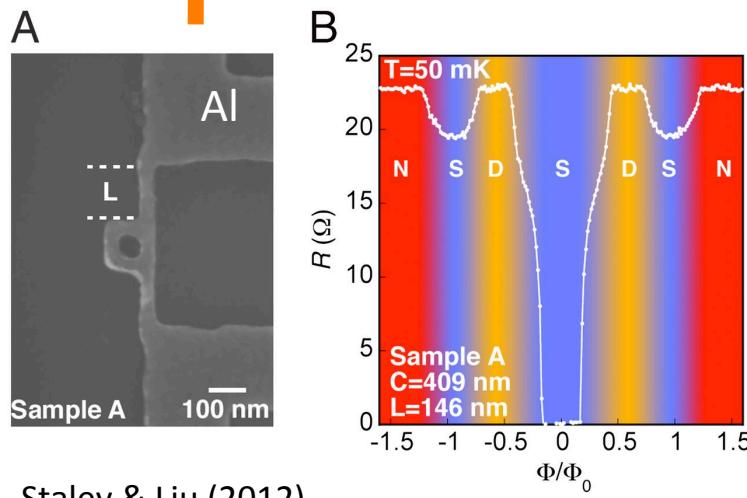
Artificially structured superconductors

Small devices give insights into the structure
of the superconducting condensate

Little-Parks effect

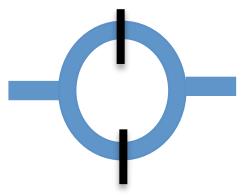


$$\Phi_0 = \frac{hc}{2e}$$

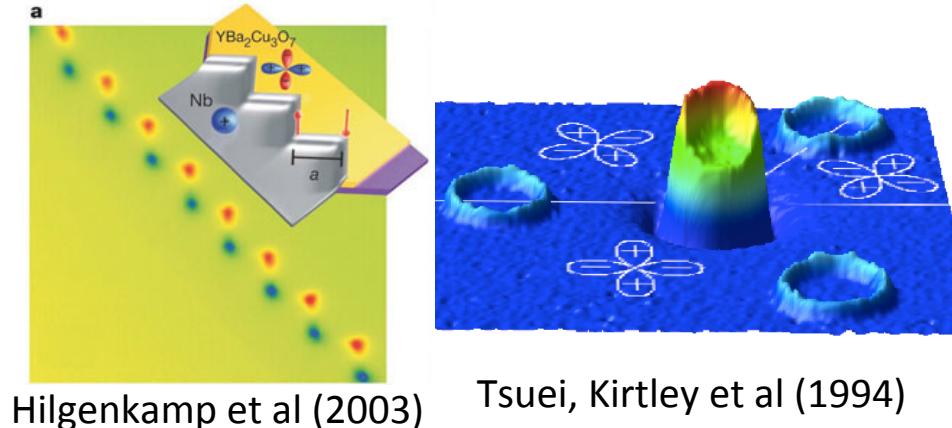
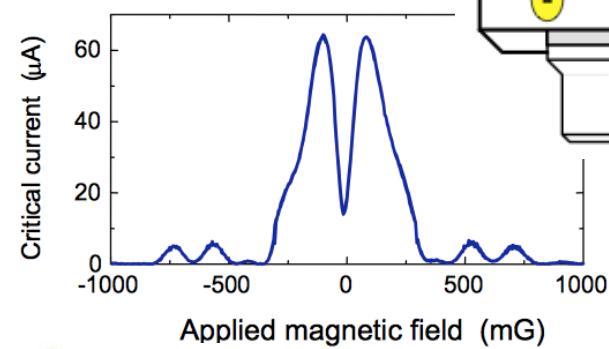


Staley & Liu (2012)

Josephson effect - SQUID



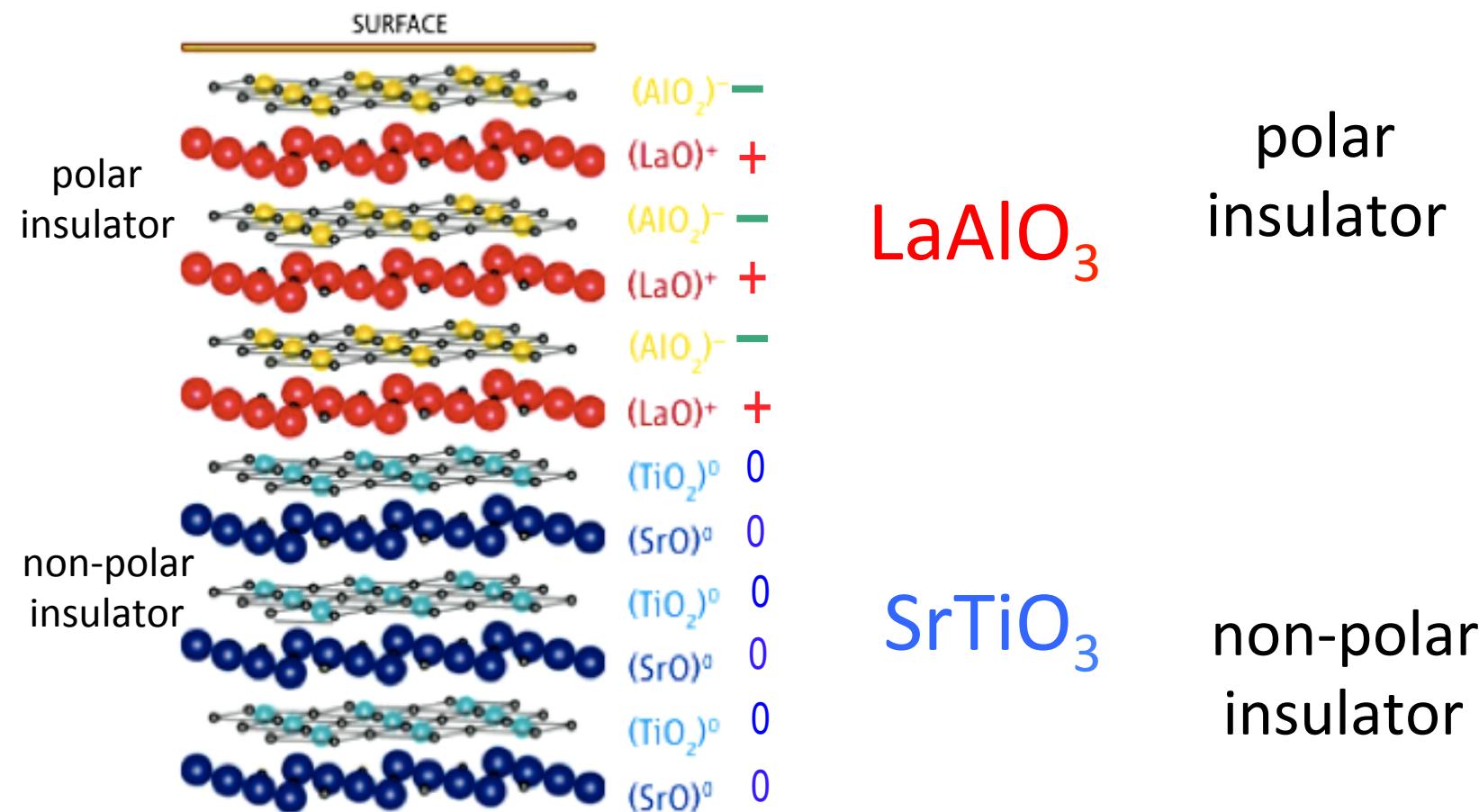
van Harlingen et al (1993)



Superconducting
heterostructures
&
superlattices

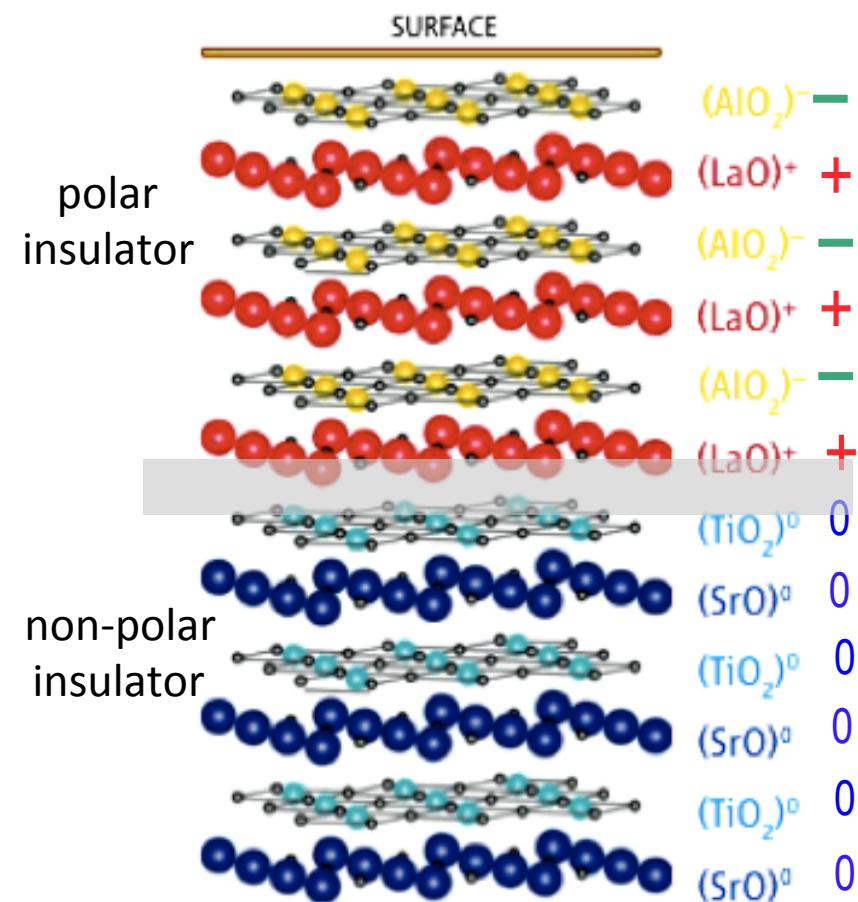
Heterostructures / superlattices

LaAlO_3 / SrTiO_3



Heterostructures / superlattices

LaAlO_3 / SrTiO_3



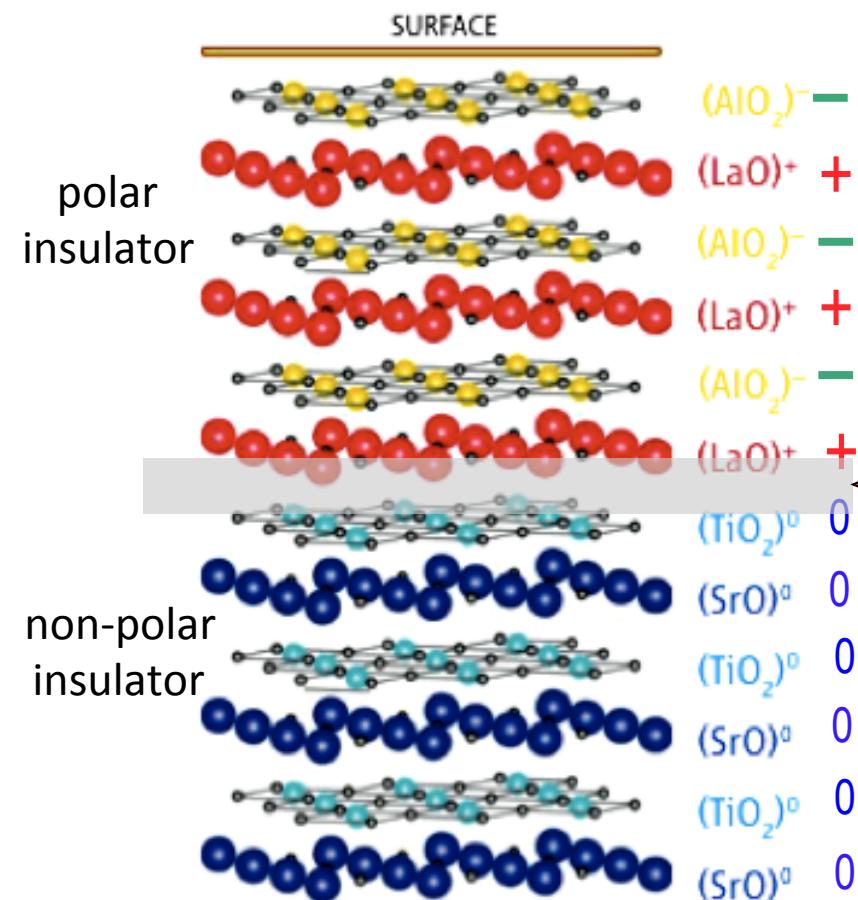
LaAlO_3 polar insulator

polar breakdown ?
2D metallic interface

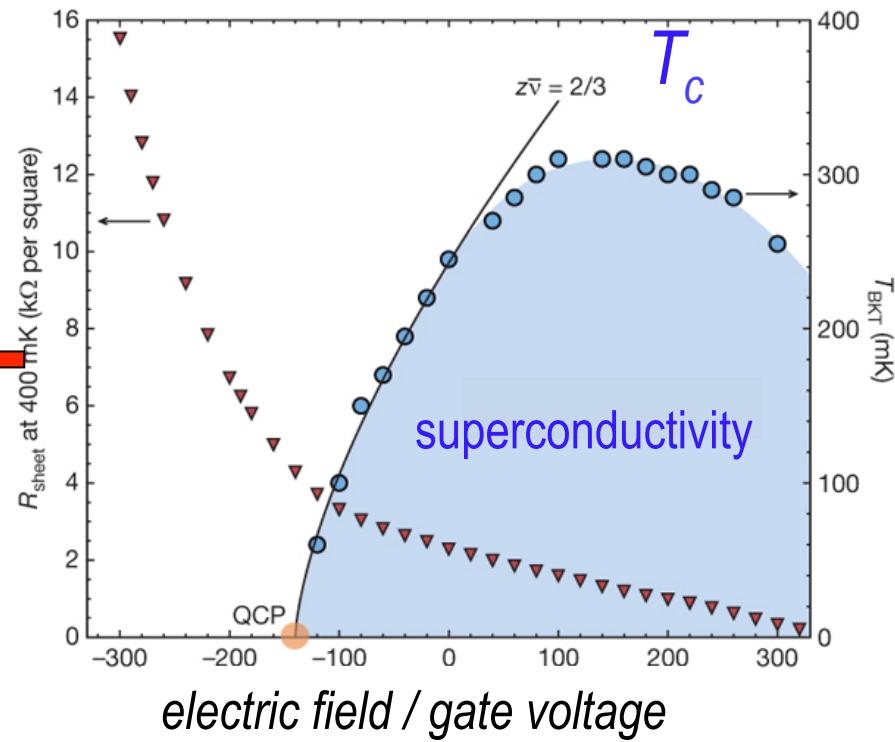
SrTiO_3 non-polar insulator

Heterostructures / superlattices

LaAlO₃ / SrTiO₃



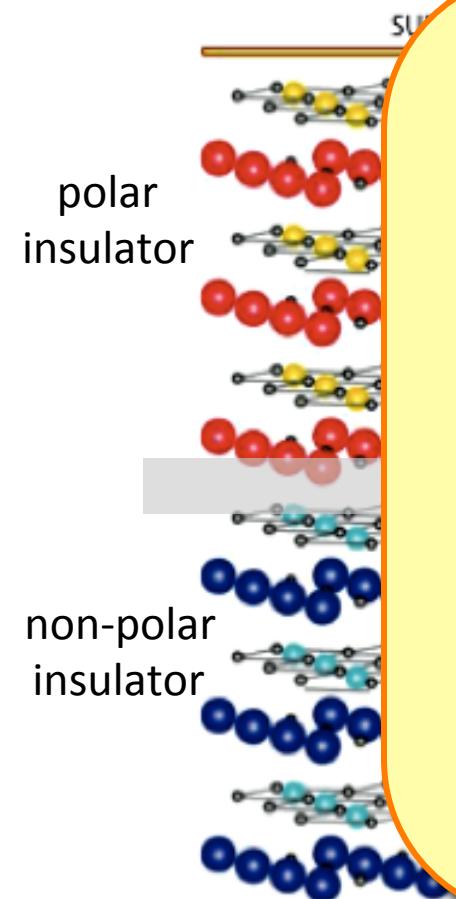
interface superconductivity



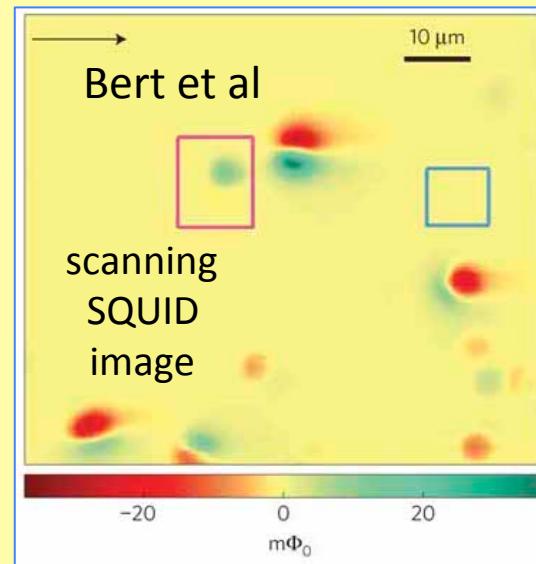
Reyren, Triscone, Mannhart et al.

Heterostructures / superlattices

LaAlO₃ / SrTiO₃



Spontaneous inplane ferromagnetism
and inhomogeneity



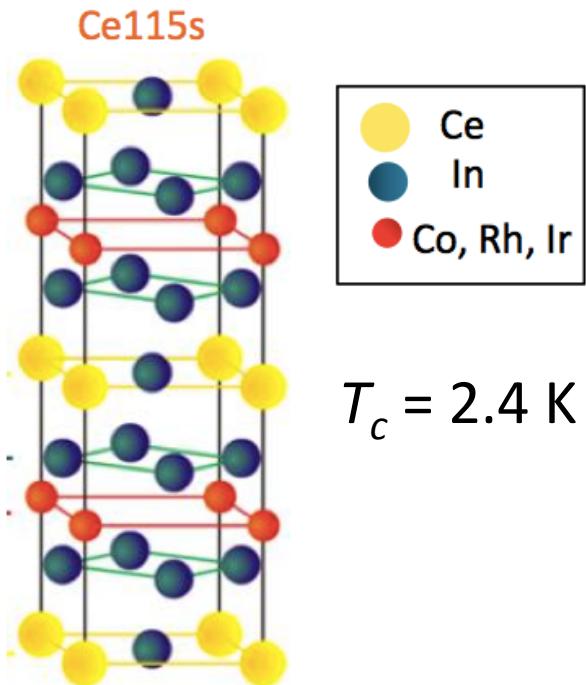
H. Hwang, K.A. Moler et al., R. Ashori et al.

Reyren, Triscone, Mannhart et al.

H.Y. Hwang group

Heavy Fermion superconductors

CeColn₅



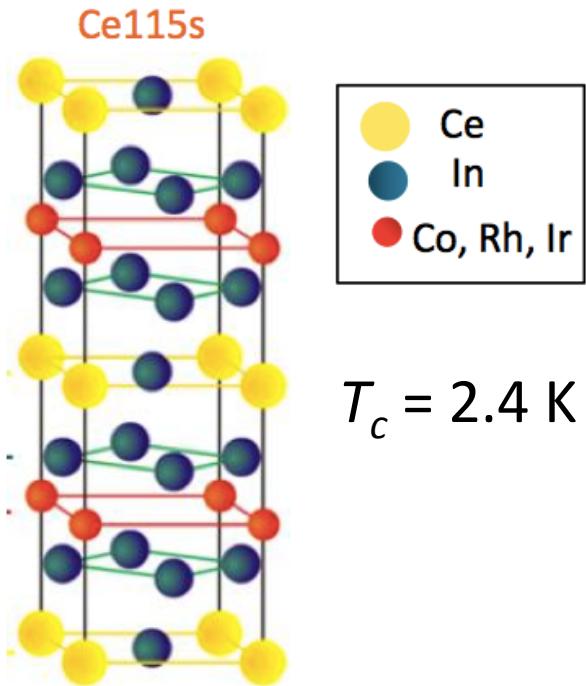
d-wave
spin-singlet
pairing

$$T_c = 2.4 \text{ K}$$

Sarrao, Thompson et al

Heavy Fermion superconductors

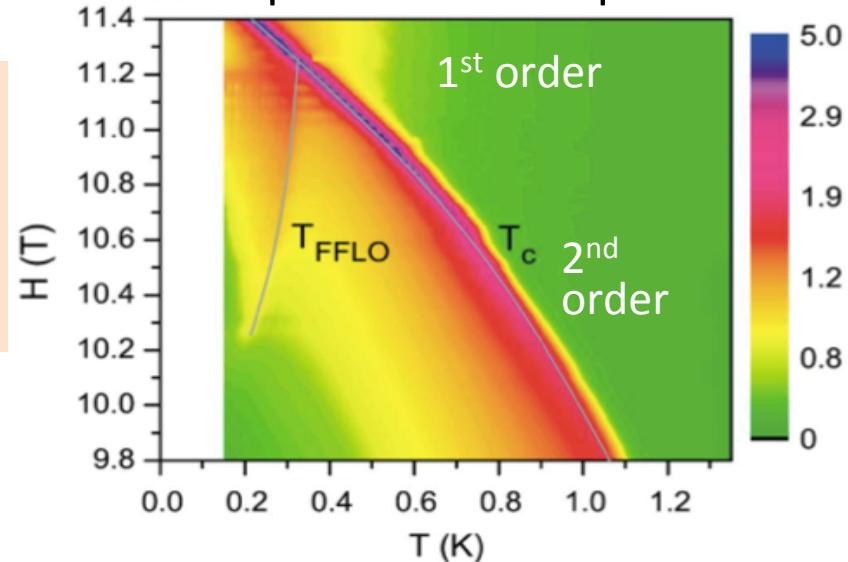
CeCoIn₅



d-wave
spin-singlet
pairing

paramagnetic limiting & “FFLO”

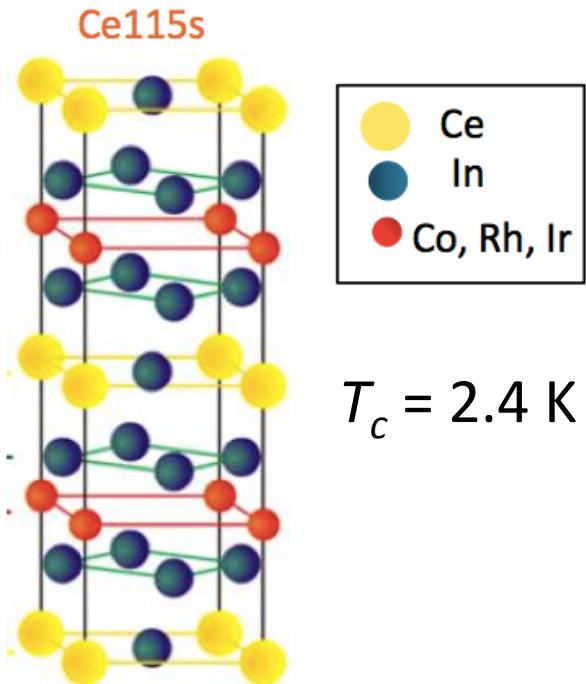
specific heat map



Sarrao, Thompson et al

Heavy Fermion superconductors

CeColn₅

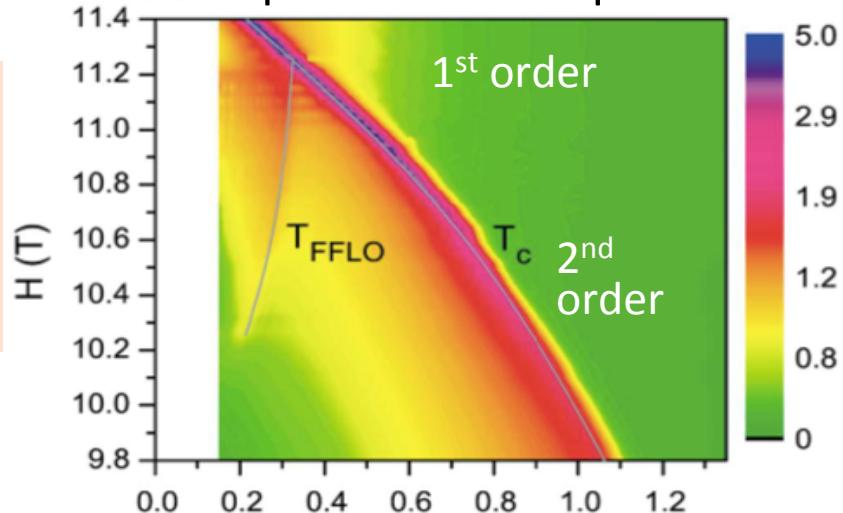


Sarrao, Thompson et al

d-wave
spin-singlet
pairing

paramagnetic limiting & “FFLO”

specific heat map



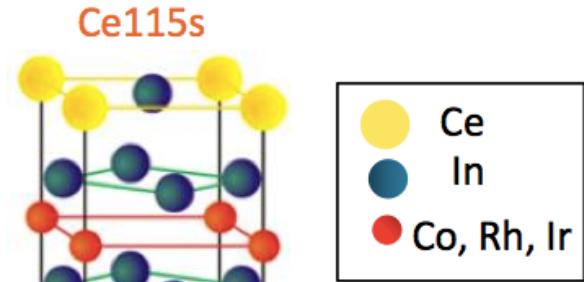
Maki parameter $\alpha = \sqrt{2} \frac{H_{c2}^0}{H_P}$

$$H_{c2}^0 = 0.7T_c \left. \frac{dH_{c2}}{dT} \right|_{T_c}$$

bulk CeColn₅
 $\alpha \approx 6$

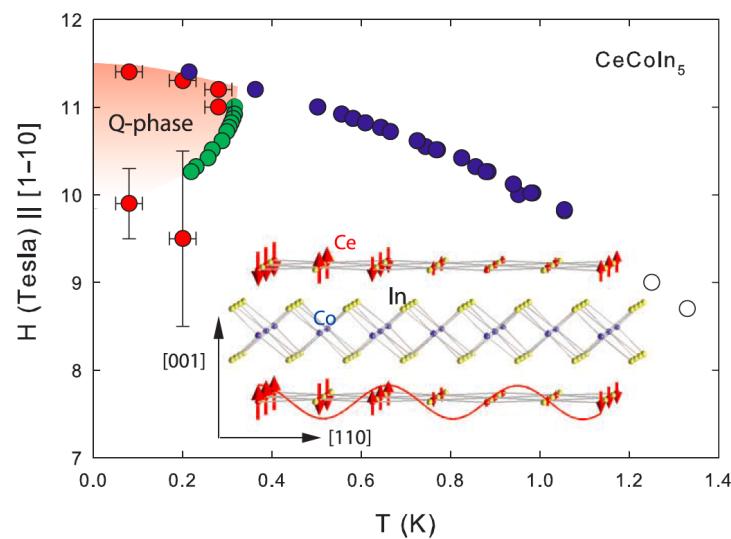
Heavy Fermion superconductors

CeCoIn₅



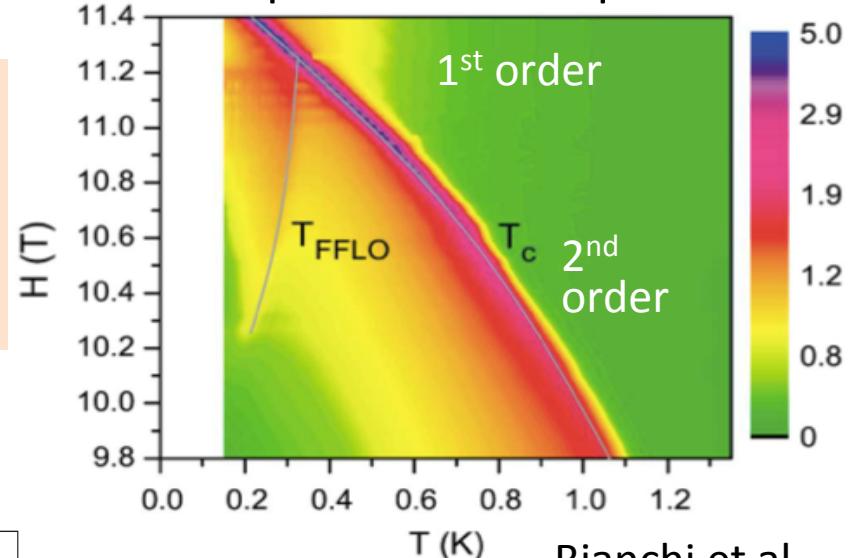
$T_c = 2.4 \text{ K}$

d-wave
spin-singlet
pairing



paramagnetic limiting & “FFLO”

specific heat map



Bianchi et al

coexistence with
incommensurate SDW

“Q-phase”

Curro et al
Kumagai et al



NMR

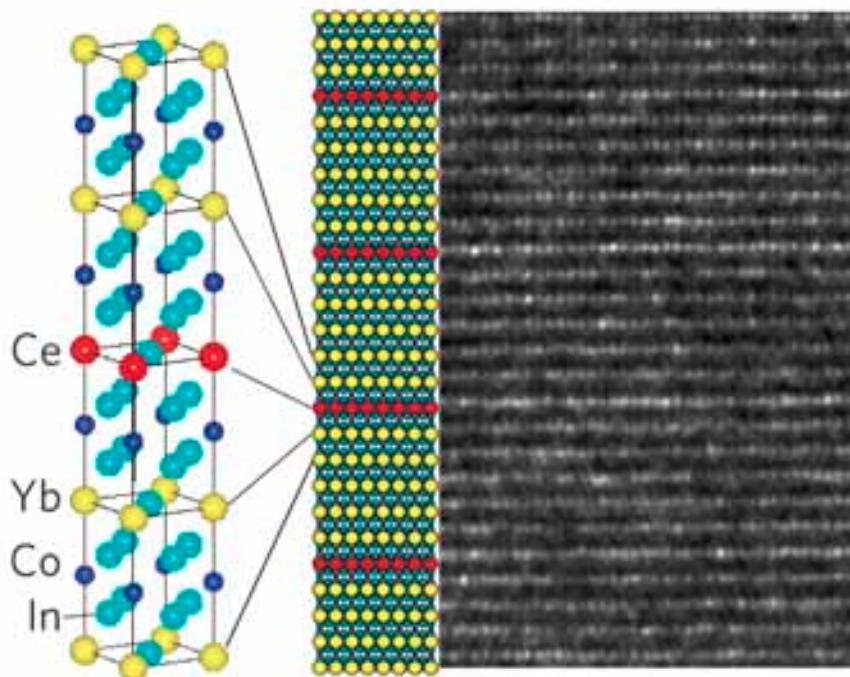
Kenzelmann et al

neutron scattering

Heterostructures / superlattices

“towards a more 2D system”

CeCoIn_5 / YbCoIn_5



Matsuda & Shibauchi group
(2011)

$$(\text{Ce}, \text{Yb}) = (n, 5)$$

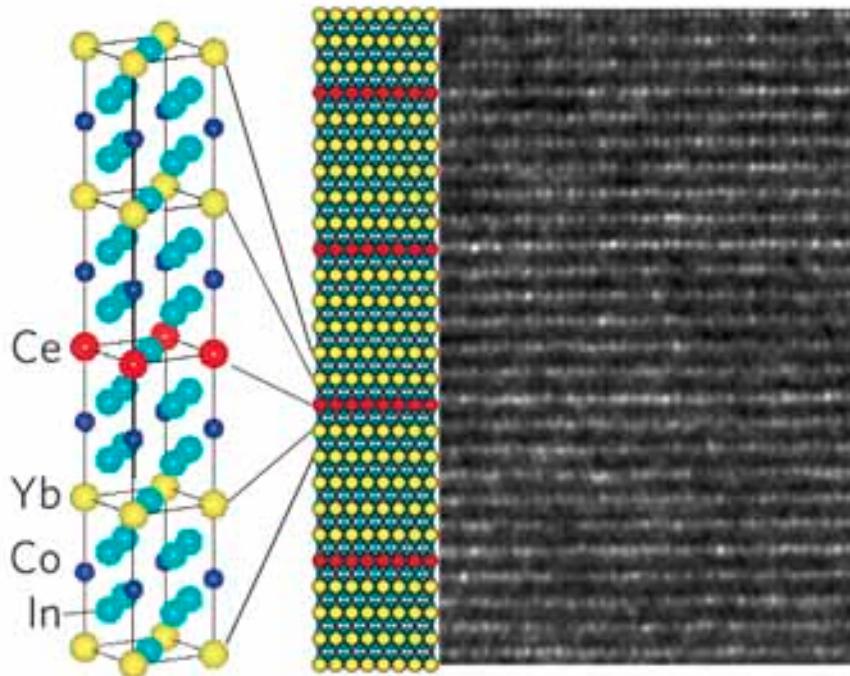
CeCoIn_5 heavy Fermion

YbCoIn_5 ordinary metal

Heterostructures / superlattices

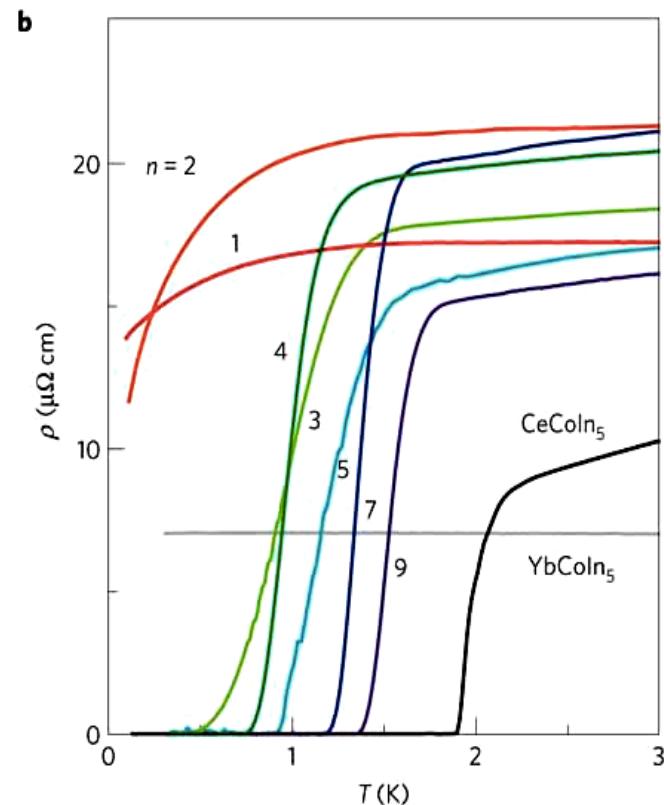
“towards a more 2D system”

CeColn₅ / YbColn₅



Matsuda & Shibauchi group
(2011)

$$(Ce, Yb) = (n, 5)$$

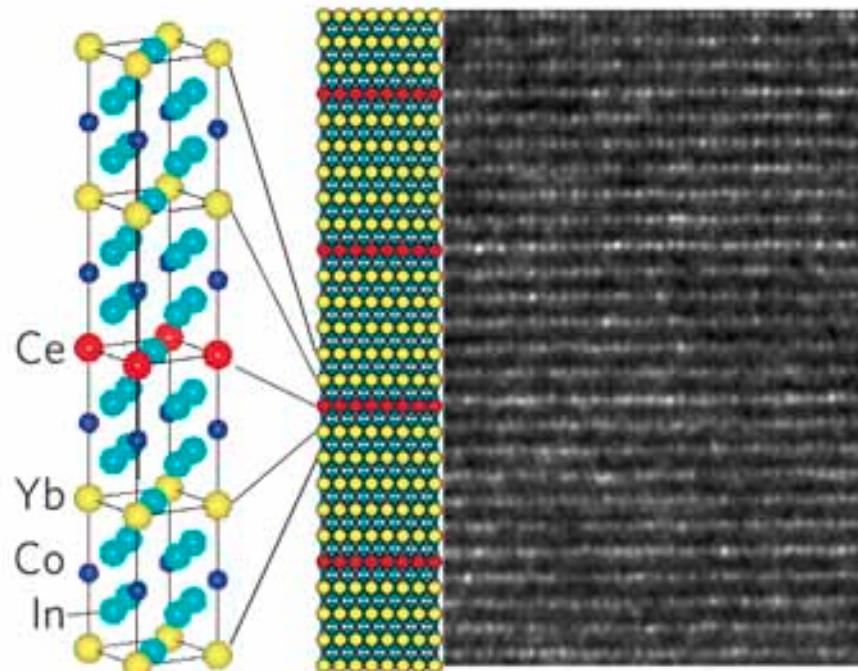


superconducting for
 $n \geq 3$

Heterostructures / superlattices

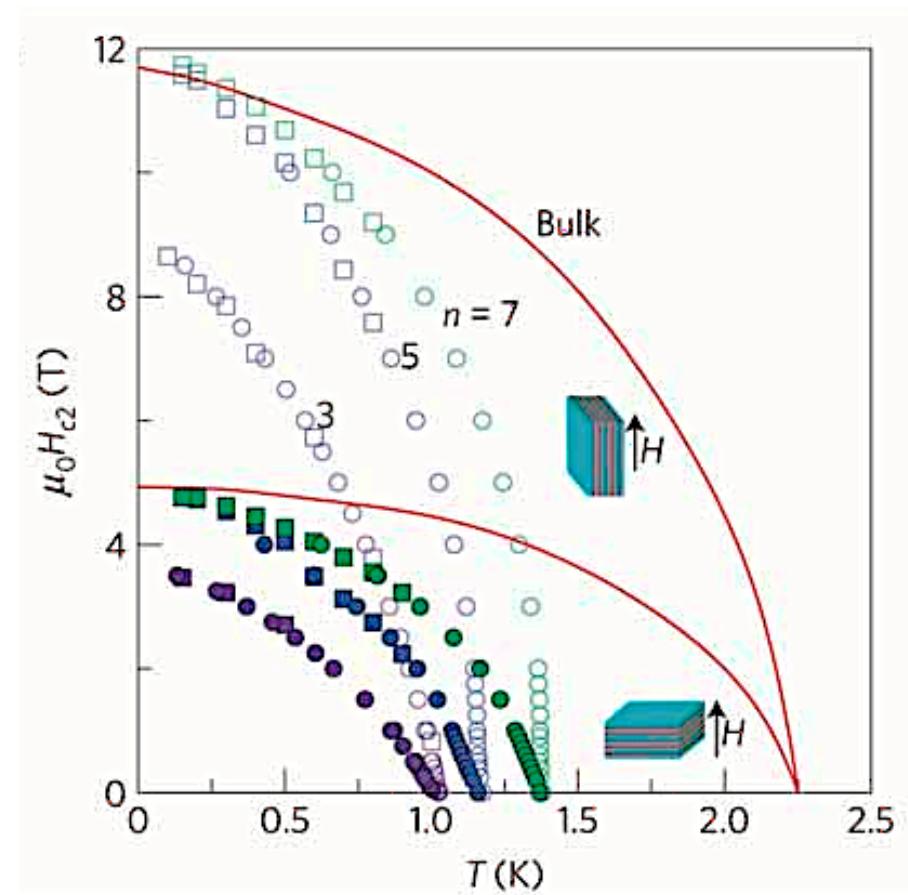
“towards a more 2D system”

CeColn₅ / YbColn₅



Matsuda & Shibauchi group
(2011)

(Ce,Yb) = (n,5)



Non-centrosymmetry

heterostructure



superlattice



non-
centrosymmetric

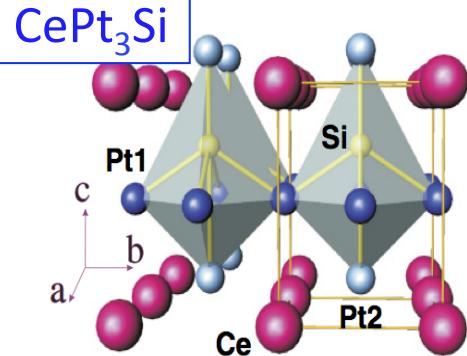
lack of
mirror symmetry

Rashba spin-orbit coupling

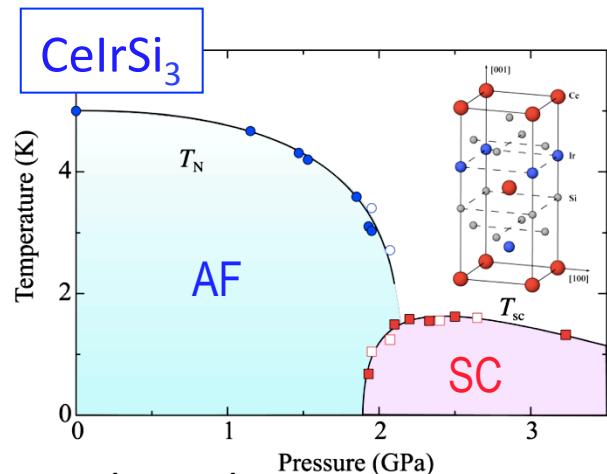
$$\mathcal{H} = \sum_{\mathbf{k}, s} \epsilon_{\mathbf{k}} c_{\mathbf{k}s}^\dagger c_{\mathbf{k}s} + \alpha \sum_{\mathbf{k}} \sum_{ss'} g_{\mathbf{k}} \cdot \boldsymbol{\sigma}_{ss'} c_{\mathbf{k}s}^\dagger c_{\mathbf{k}s'}$$

Non-centrosymmetric superconductors

Heavy Fermion superconductors



Bauer et al

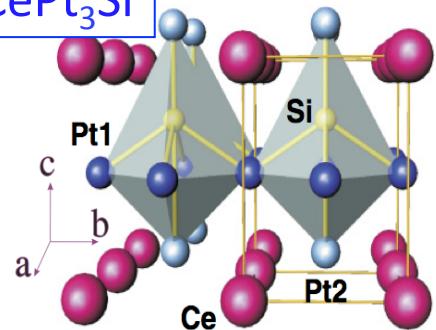


Onuki et al

Non-centrosymmetric superconductors

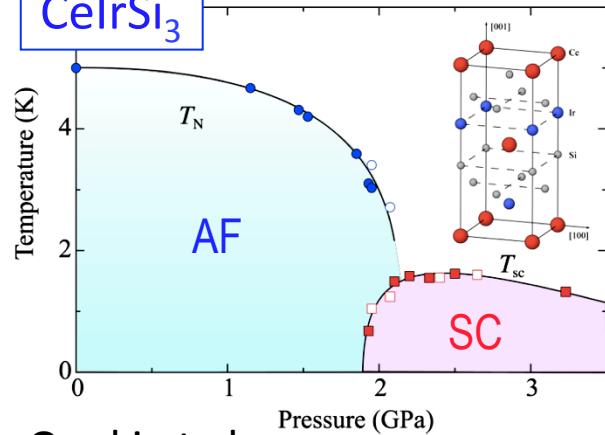
Heavy Fermion superconductors

CePt₃Si



Bauer et al

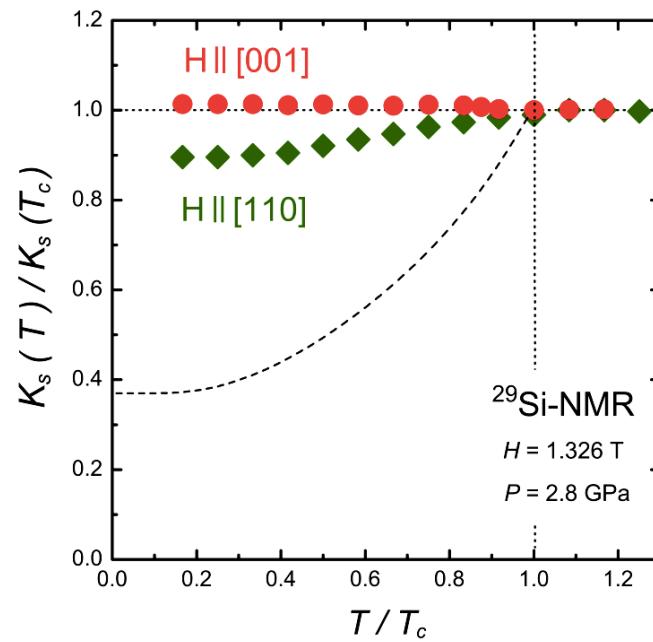
CeIrSi₃



Onuki et al

spin susceptibility

²⁹Si-Knight shift

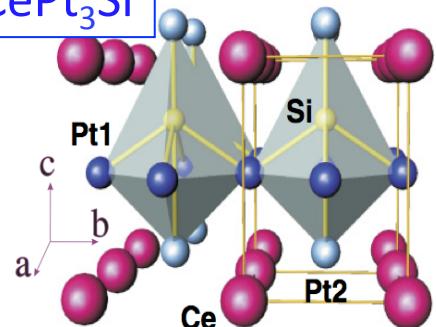


Mukuda et al

Non-centrosymmetric superconductors

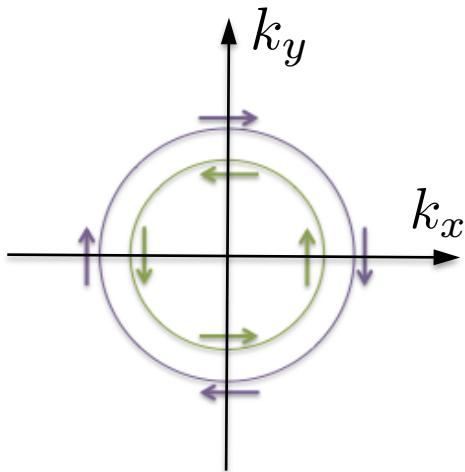
Heavy Fermion superconductors

CePt₃Si



Bauer et al.

Rashba spin-orbit coupling



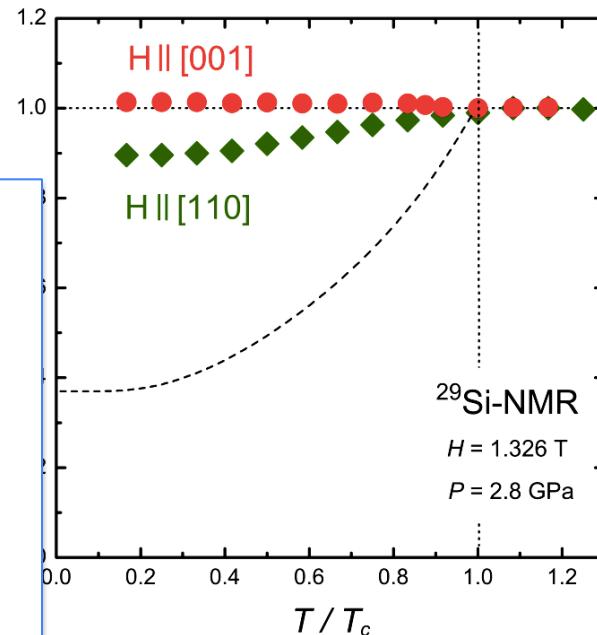
spin polarization
through
van Vleck effect



no pair breaking!

spin susceptibility

²⁹Si-Knight shift

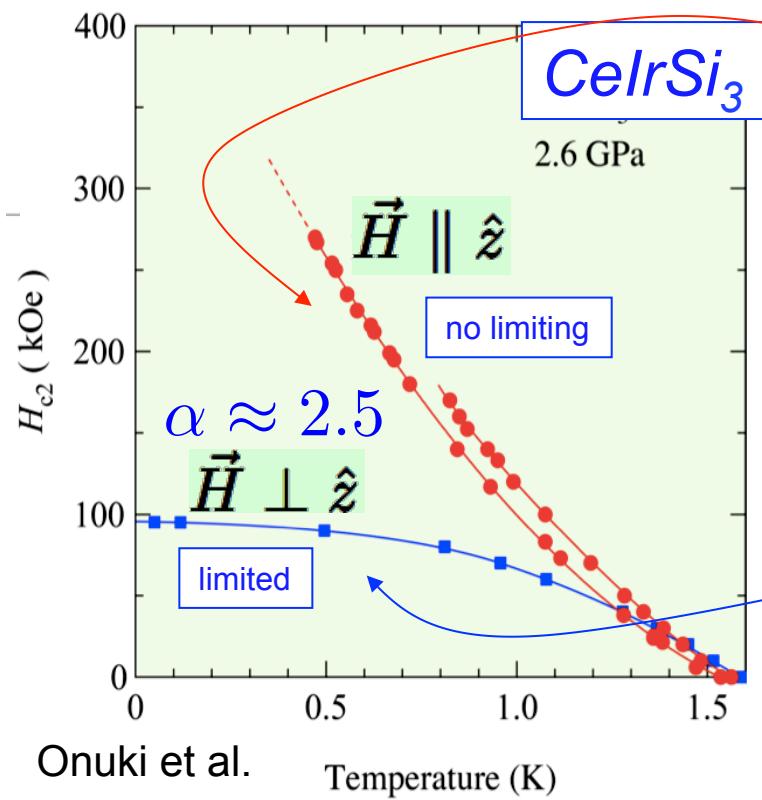


uda et al

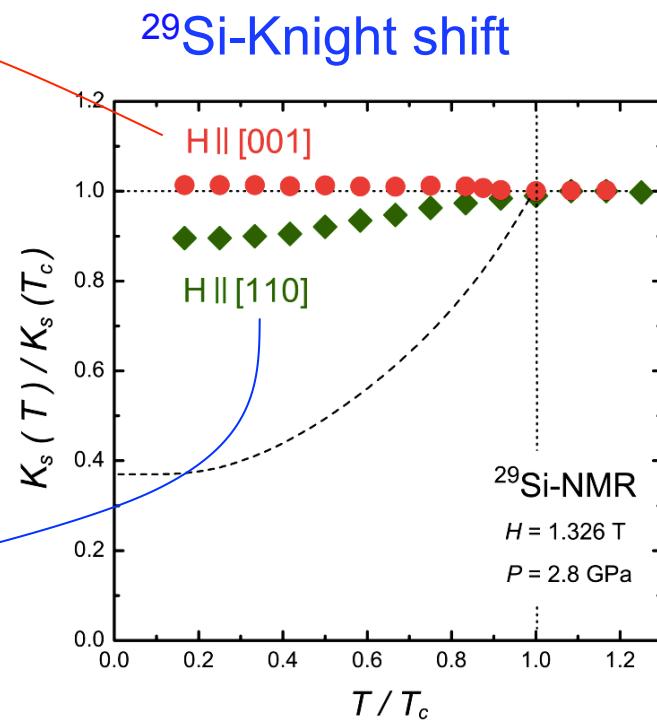
Non-centrosymmetric superconductors

Heavy Fermion superconductors

upper critical field



spin susceptibility



Onuki et al.

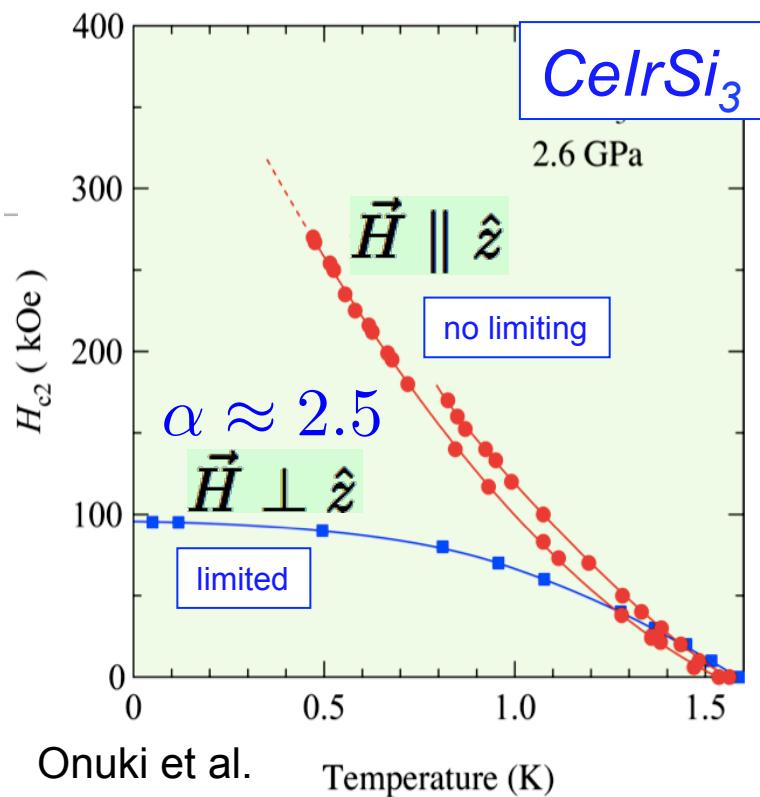
Temperature (K)

Mukuda et al

Non-centrosymmetric superconductors

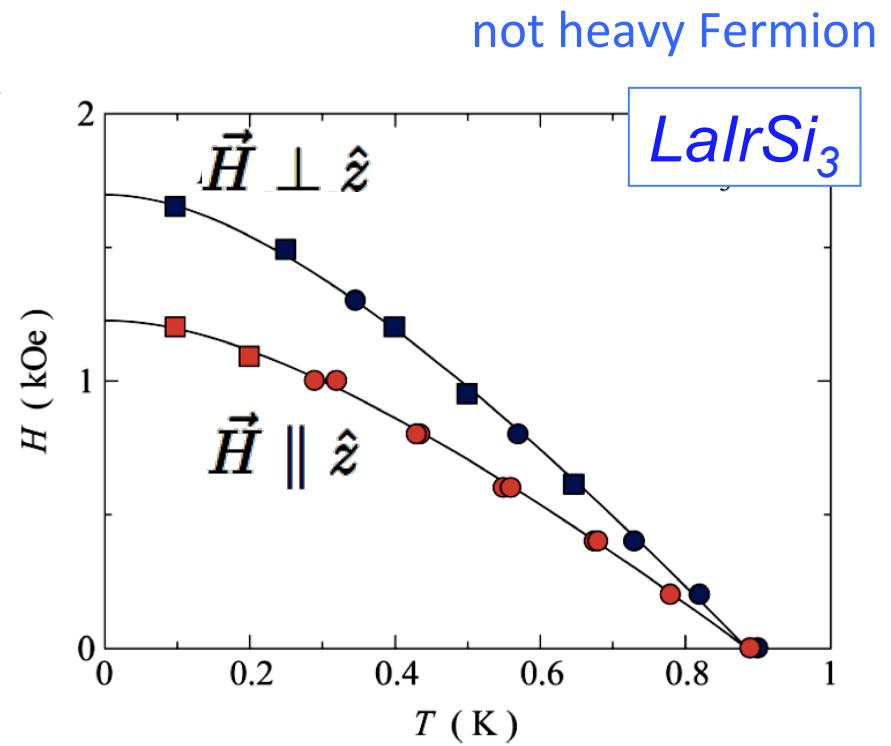
Heavy Fermion superconductors

upper critical field



Onuki et al.

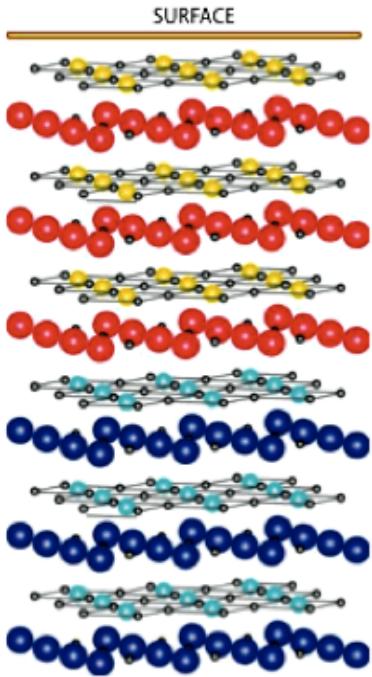
Temperature (K)



- 100 x smaller H_{c2}
- orbital depairing relevant light electrons → large ξ

Heterostructure – LAO/STO

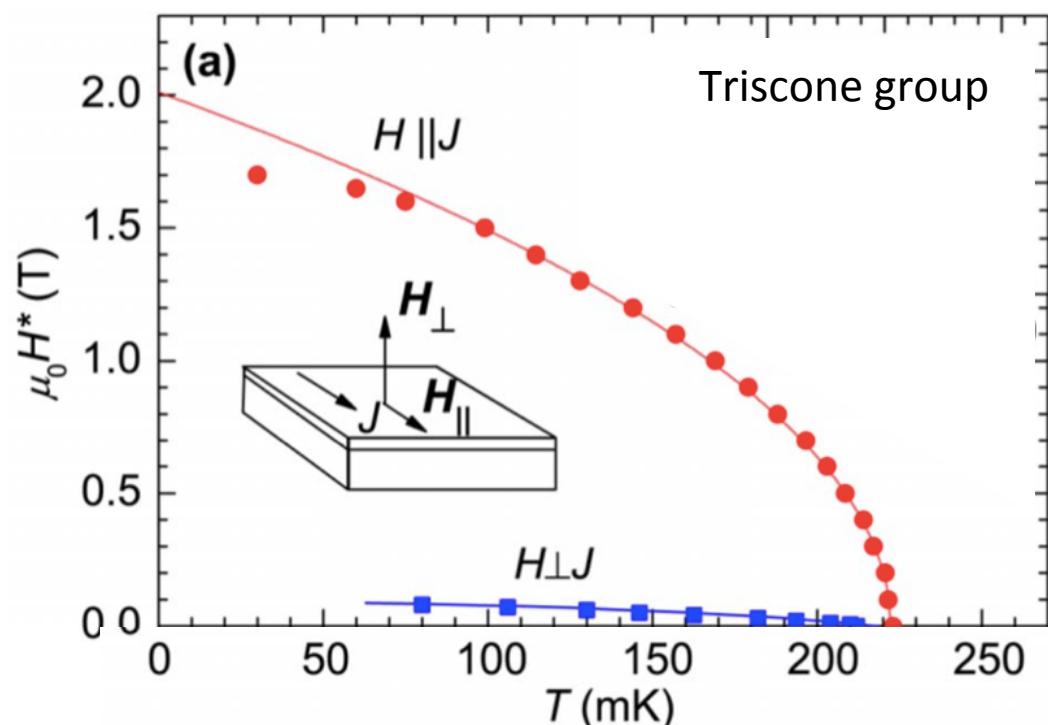
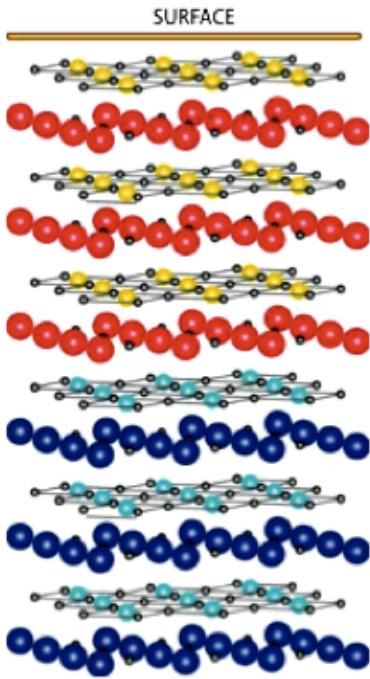
$\text{LaAlO}_3 / \text{SrTiO}_3$



*Does non-centrosymmetry
play a role
for upper critical field?*

Heterostructure – LAO/STO

$\text{LaAlO}_3 / \text{SrTiO}_3$



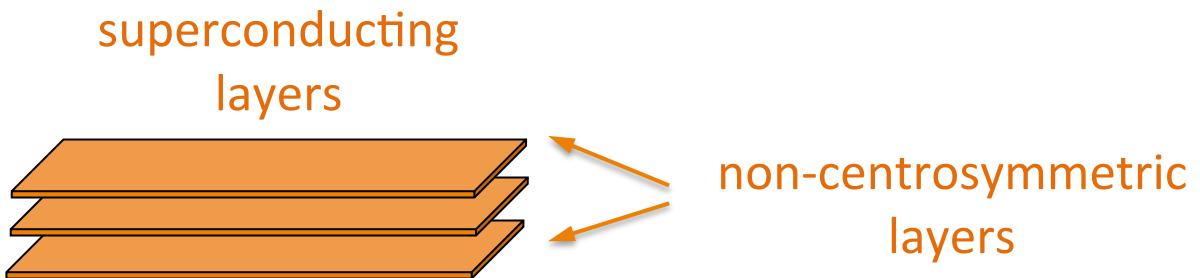
paramagnetic limiting field

Does non-centrosymmetry play a role for upper critical field?

$$H_p \sim \frac{\Delta_0}{\sqrt{2}\mu_B} \sim \frac{k_B T_c}{\mu_B} \sim 1 - 2T$$

Superlattice – Ce₁₁₅ / Yb₁₁₅

CeColn₅ / YbColn₅

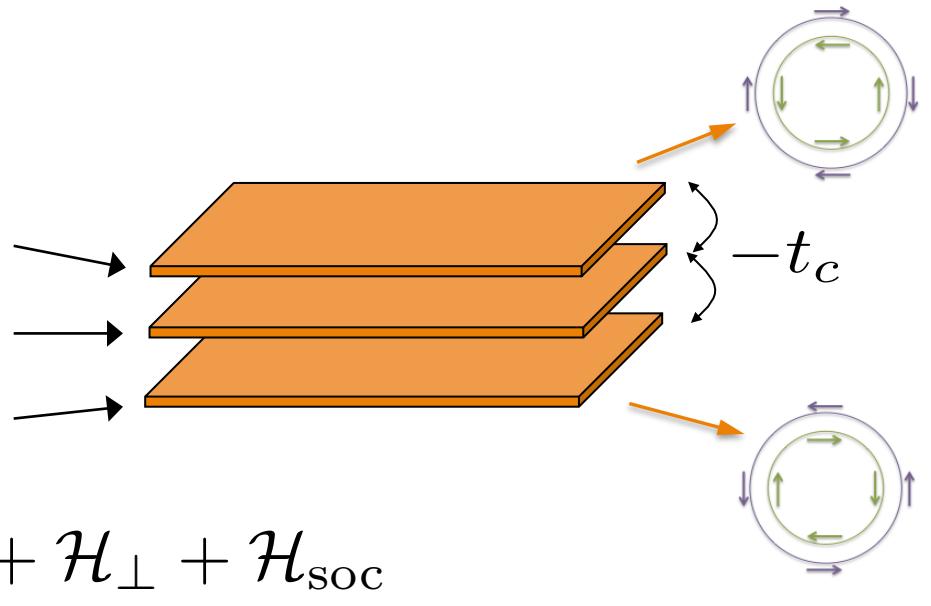


Superlattice – Ce115 / Yb115

CeColn₅ / YbColn₅



$$\begin{aligned}\alpha_1 &= +\alpha \\ \alpha_2 &= 0 \\ \alpha_3 &= -\alpha\end{aligned}$$



$$\mathcal{H} = \mathcal{H}_{\parallel} + \mathcal{H}_{\perp} + \mathcal{H}_{\text{SOC}}$$

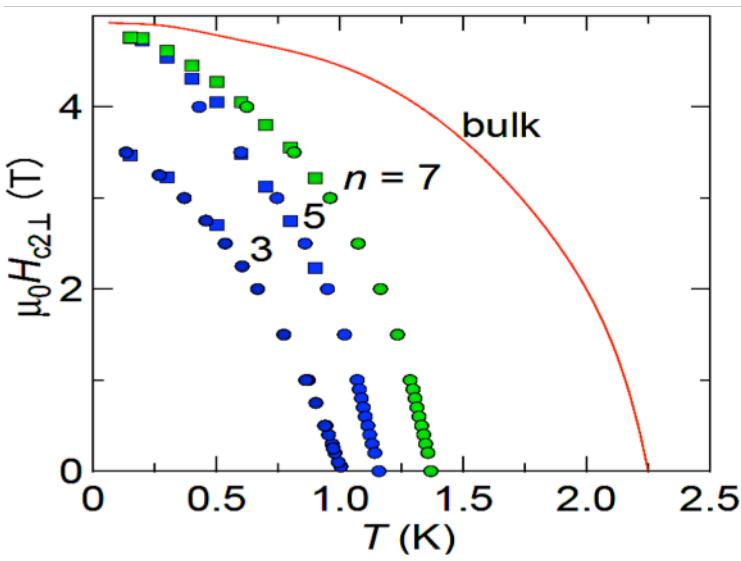
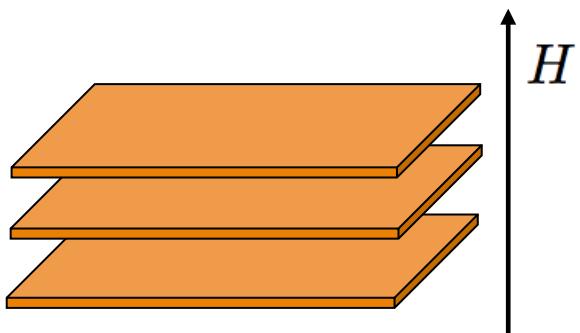
$$\mathcal{H}_{\parallel} = \sum_{l=1,2,3} \sum_{\mathbf{k},s} \epsilon_{\mathbf{k}} c_{\mathbf{k}ls}^{\dagger} c_{\mathbf{k}ls} \quad \text{intra-layer}$$

$$\mathcal{H}_{\perp} = -t_c \sum_{\mathbf{k},s} \left\{ c_{\mathbf{k}1s}^{\dagger} c_{\mathbf{k}2s} + c_{\mathbf{k}2s}^{\dagger} c_{\mathbf{k}1s} \right\} \quad \text{inter-layer}$$

$$\mathcal{H}_{soc} = \sum_{l=1,2,3} \alpha_l \sum_{\mathbf{k},s,s'} \mathbf{g}_{\mathbf{k}} \cdot \boldsymbol{\sigma}_{ss'} c_{\mathbf{k}s}^{\dagger} c_{\mathbf{k}s'} \quad \text{Rashba-SOC}$$

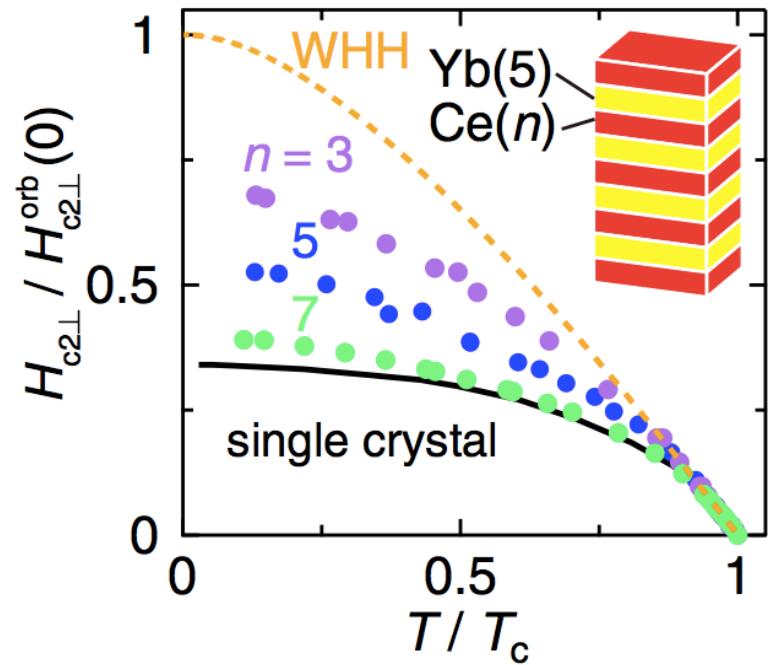
Superlattice – Ce115 / Yb115

paramagnetic limiting



Matsuda group

Comparison with orbital depairing

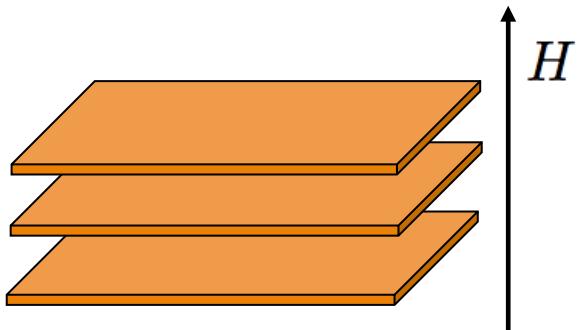


Rashba spin-orbit coupling
reduces the paramagnetic limit
due van Vleck spin polarization

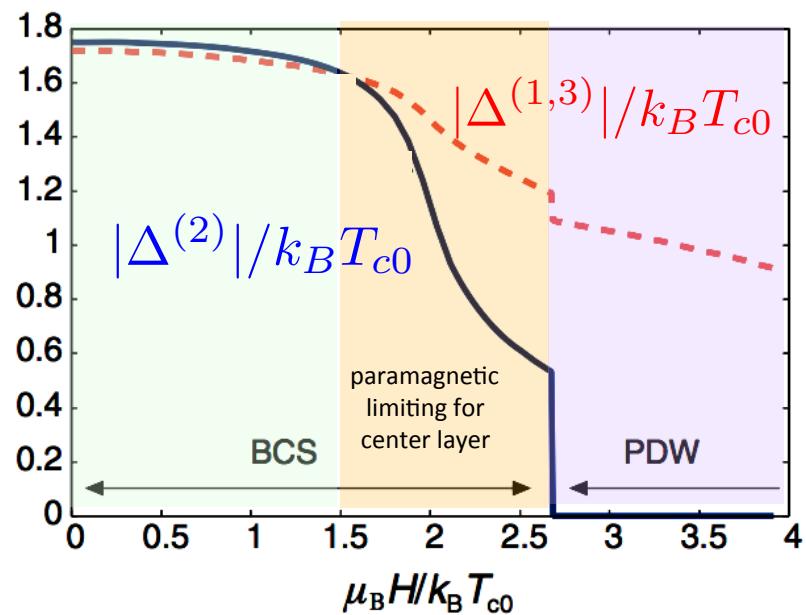
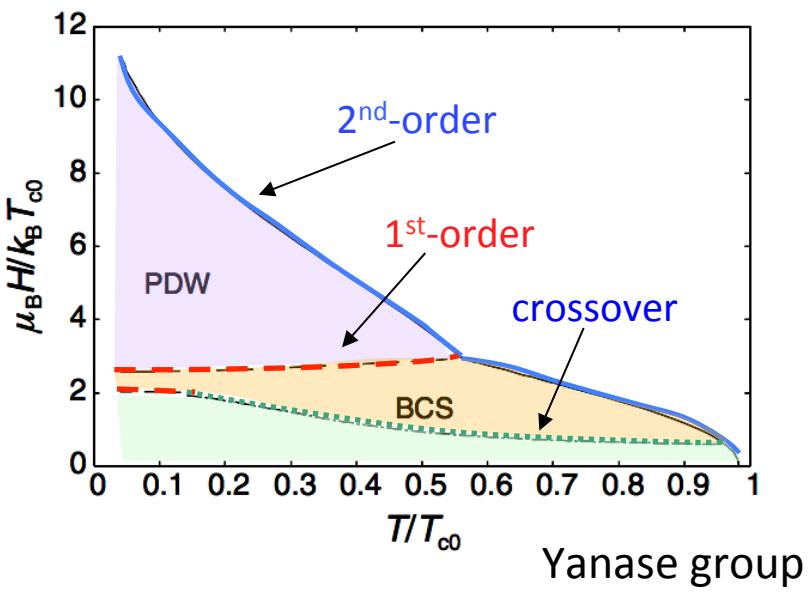
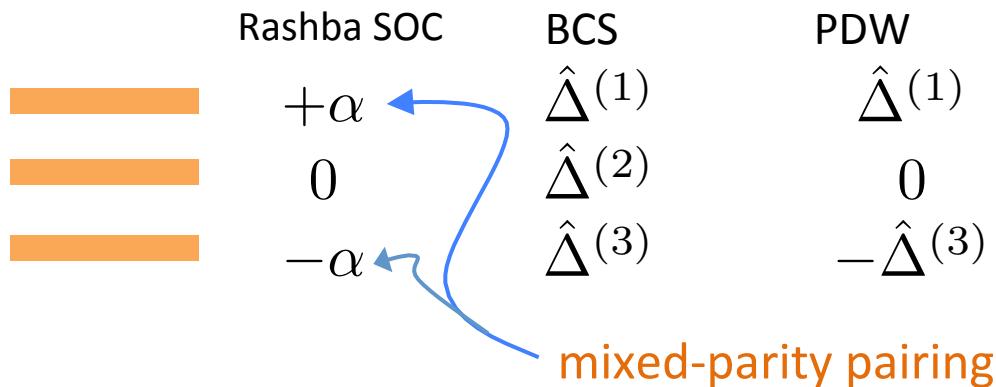
smaller $n \rightarrow$ more boundary layers
 \rightarrow more robust

Superlattice – Ce115 / Yb115

pair density wave

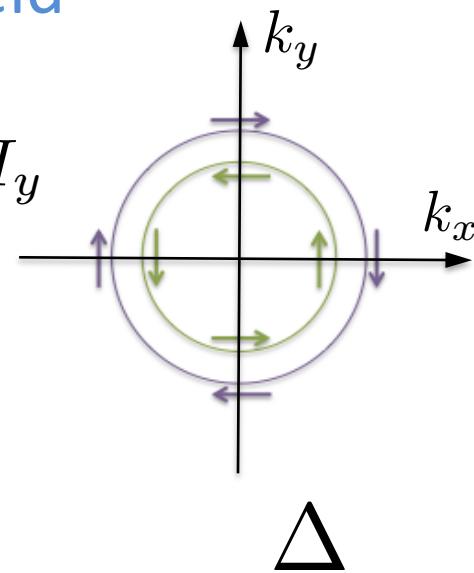
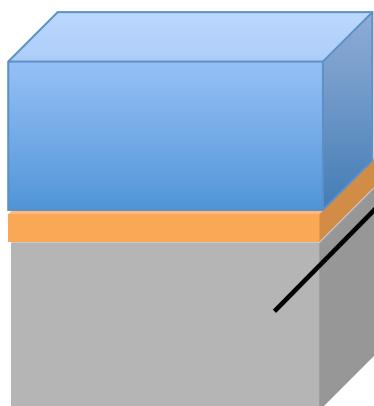


model system : without orbital depairing

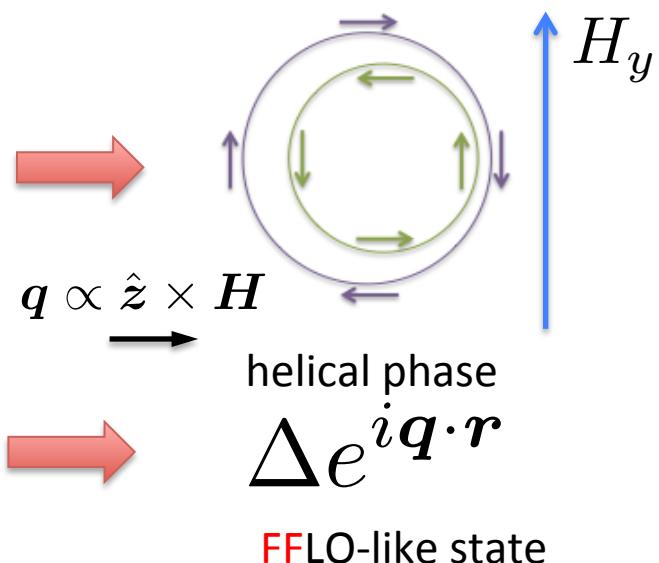


Helical phase - heterostructure

in-plane magnetic field

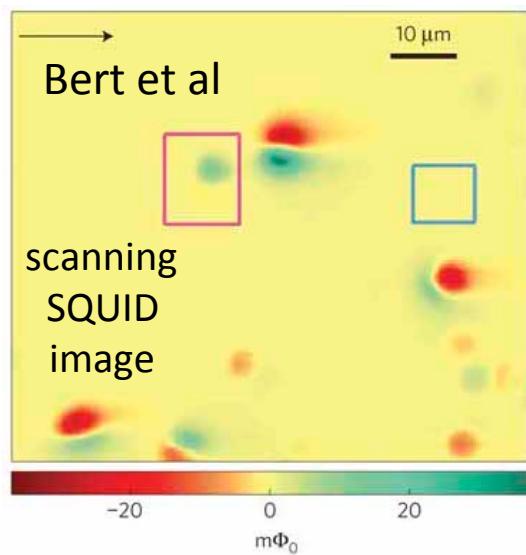
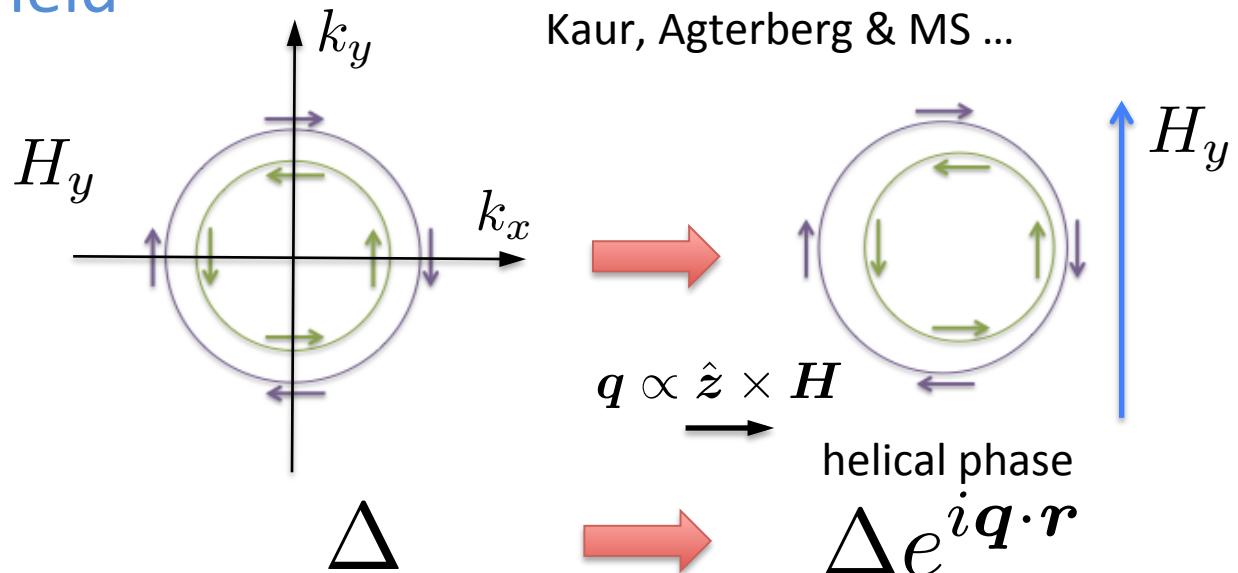
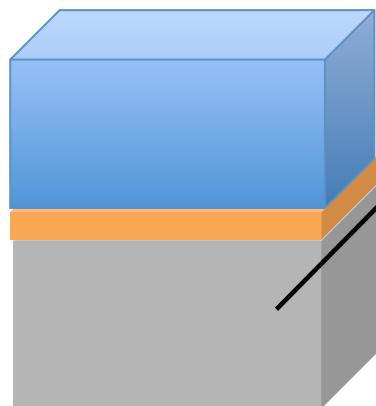


Edelstein; Dimitrova & Feigelman
Kaur, Agterberg & MS ...



Helical phase - heterostructure

in-plane magnetic field



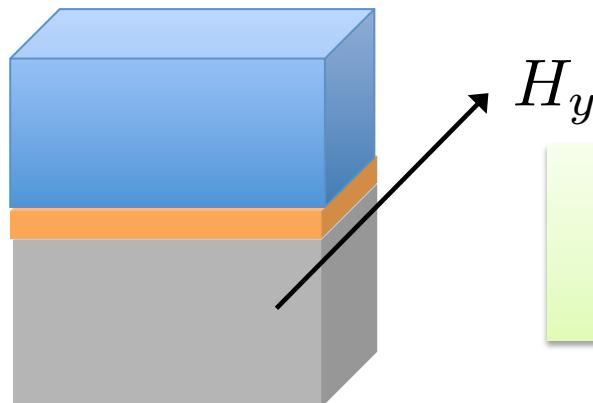
coexistence of SC and inplane ferromagnetism

Lu et al (Mannhart-Ashoori groups)
Bert et al (Hwang-Moler groups)

Michaeli, Potter & Lee: { coexistence of SC & FM
in a helical phase (robustness)

Helical phase - heterostructure

in-plane magnetic field



$$\Delta e^{i\mathbf{q} \cdot \mathbf{r}}$$

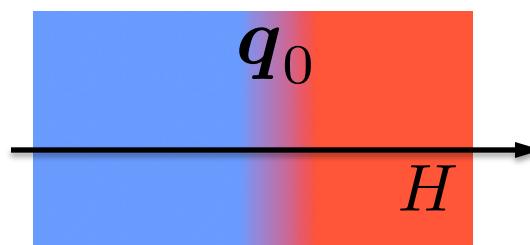
gauge freedom

$$\mathbf{q} = K(\hat{\mathbf{z}} \times \mathbf{H}) - \frac{2e}{\hbar c} \mathbf{A} = \mathbf{q}_0 - \frac{2e}{\hbar c} \mathbf{A}$$

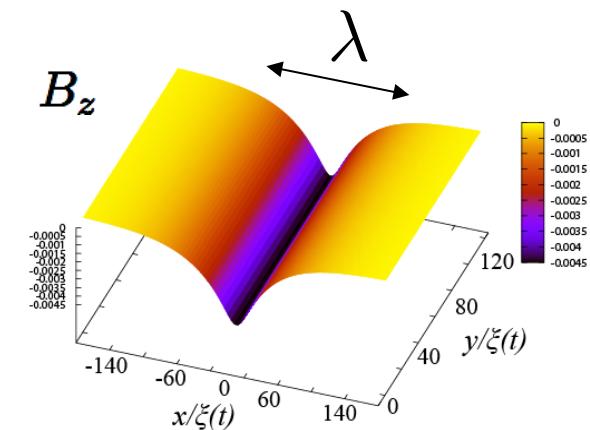
Inhomogeneous phase

order parameter rigid
 $\mathbf{q} = const$

$$\mathbf{B} = \frac{\hbar c}{2e} \nabla \times \mathbf{q}_0 \perp \hat{\mathbf{z}}$$



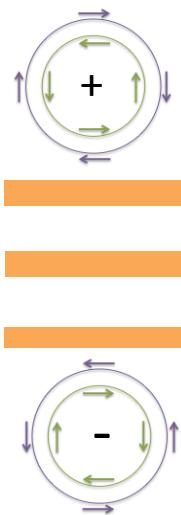
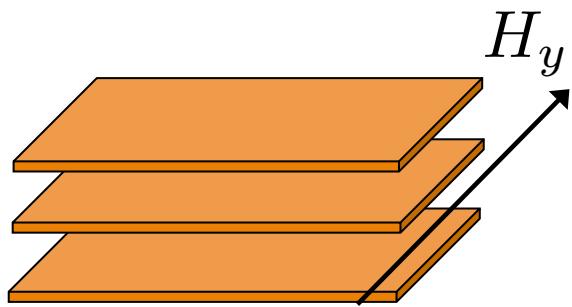
spatial variation in \mathbf{q}_0



Aoyama & MS

Helical phase - superlattice – Ce115 / Yb115

in-plane magnetic field



SOC
+ α
0
- α

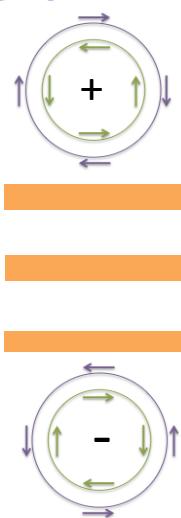
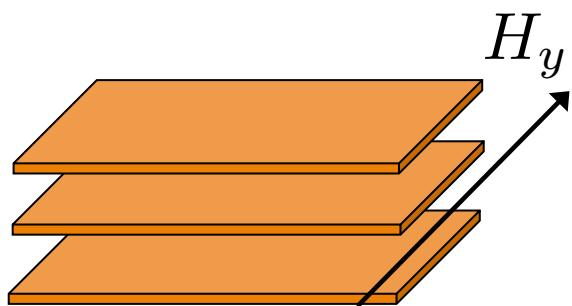
model - helical phase

pure helical
phases
 $\hat{\Delta}_0^{(1)} e^{+iqx}$
 $\hat{\Delta}_0^{(2)}$
 $\hat{\Delta}_0^{(3)} e^{-iqx}$

$$t_c = 0$$

Helical phase - superlattice – Ce115 / Yb115

in-plane magnetic field



SOC
+ α
0
- α

model - helical phase

pure helical
phases

$$\hat{\Delta}_0^{(1)} e^{+iqx}$$

$$\hat{\Delta}_0^{(2)}$$

$$\hat{\Delta}_0^{(3)} e^{-iqx}$$

$$t_c = 0$$

interlayer
transfer

$$\hat{\Delta}_0^{(1)} (e^{iqx} + \epsilon e^{-iqx})$$

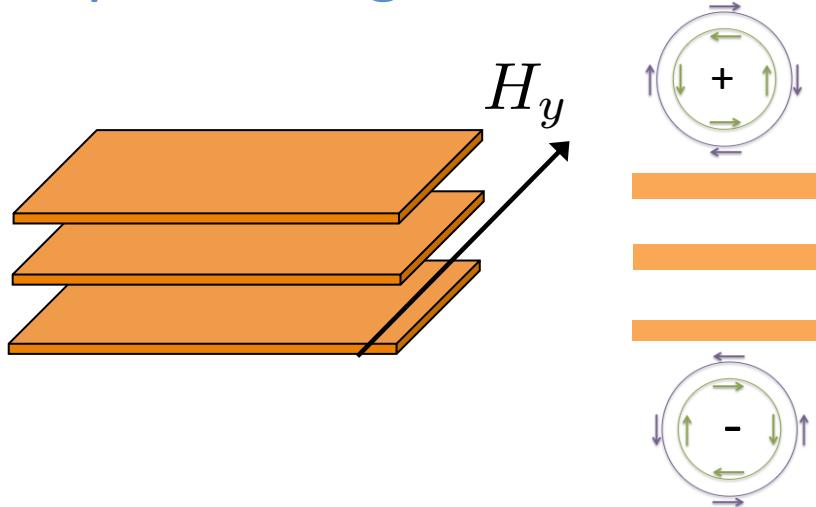
$$\hat{\Delta}_0^{(2)} (e^{iqx} + e^{-iqx})$$

$$\hat{\Delta}_0^{(3)} (\epsilon e^{iqx} + e^{-iqx})$$

$$t_c \neq 0$$

Helical phase - superlattice – Ce115 / Yb115

in-plane magnetic field

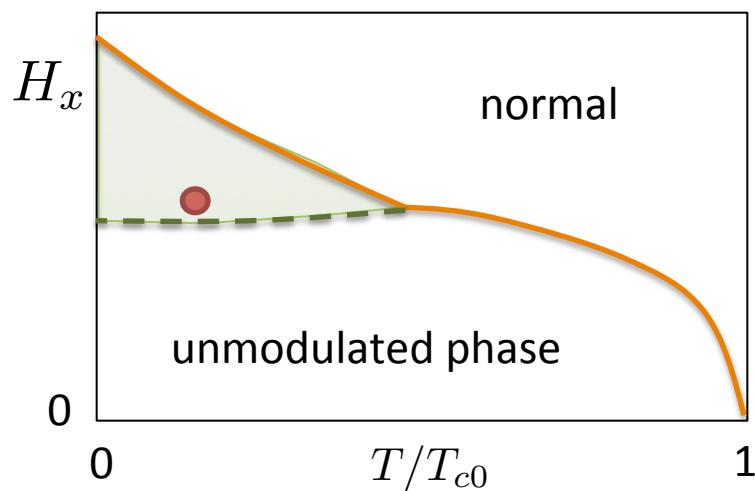


model - helical phase

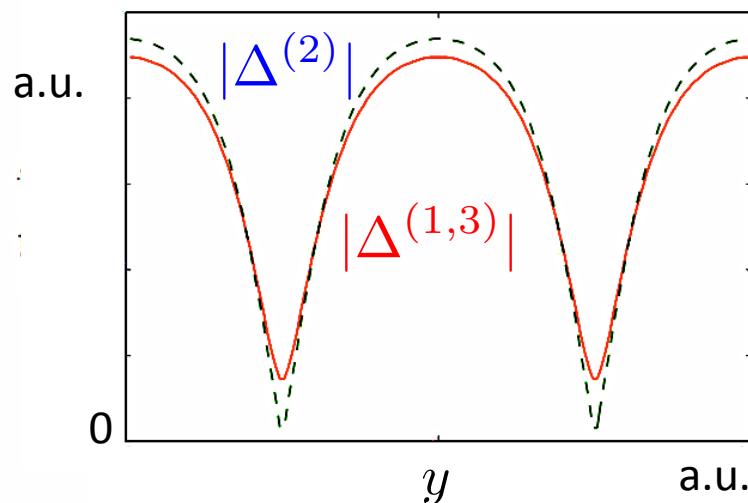
SOC	pure helical phases
$+ \alpha$	$\hat{\Delta}_0^{(1)} e^{+iqx}$
0	$\hat{\Delta}_0^{(2)}$
$- \alpha$	$\hat{\Delta}_0^{(3)} e^{-iqx}$

interlayer transfer

$$\begin{aligned} & \hat{\Delta}_0^{(1)} (e^{iqx} + \epsilon e^{-iqx}) \\ & \hat{\Delta}_0^{(2)} (e^{iqx} + e^{-iqx}) \\ & \hat{\Delta}_0^{(3)} (\epsilon e^{iqx} + e^{-iqx}) \end{aligned}$$

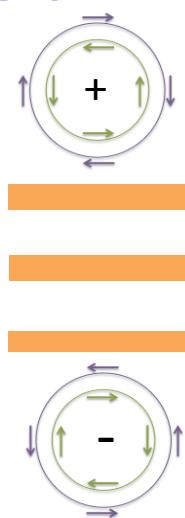
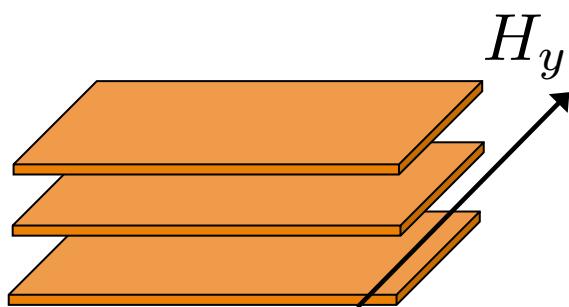


Larkin-Ovchinnikov-like modulation



Helical phase - superlattice – Ce115 / Yb115

in-plane magnetic field



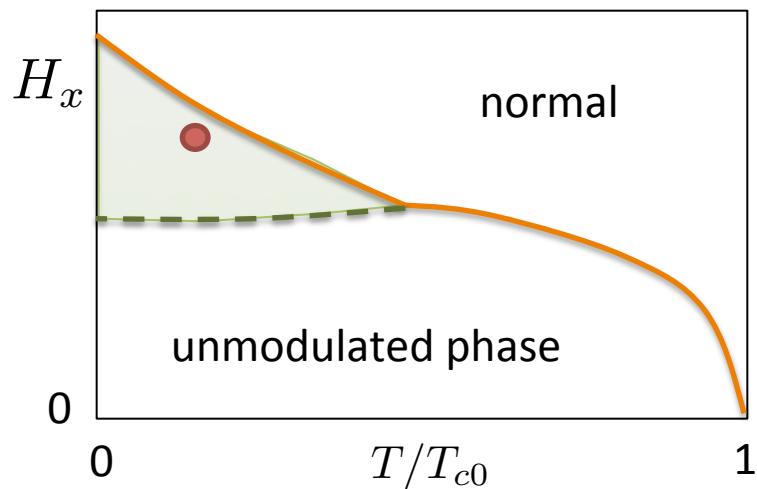
SOC
+ α
0
− α

model - helical phase

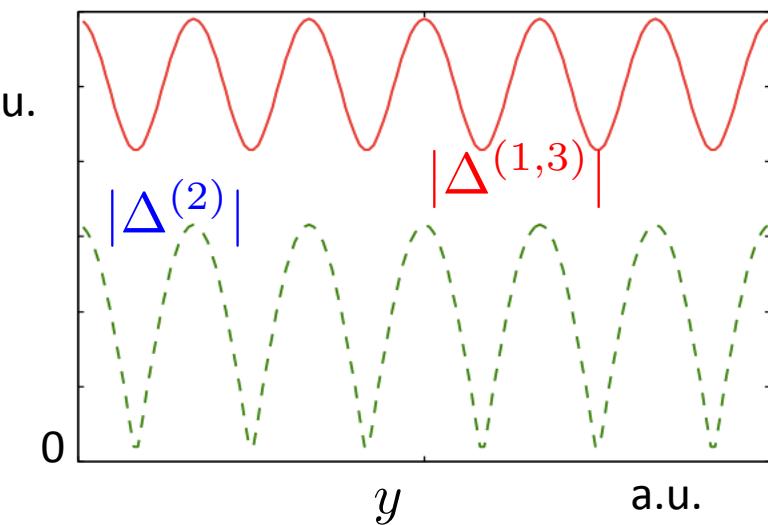
pure helical phases
 $\hat{\Delta}_0^{(1)} e^{+iqx}$
 $\hat{\Delta}_0^{(2)}$
 $\hat{\Delta}_0^{(3)} e^{-iqx}$

interlayer transfer

$$\begin{aligned} \hat{\Delta}_0^{(1)} (e^{iqx} + \epsilon e^{-iqx}) \\ \hat{\Delta}_0^{(2)} (e^{iqx} + e^{-iqx}) \\ \hat{\Delta}_0^{(3)} (\epsilon e^{iqx} + e^{-iqx}) \end{aligned}$$



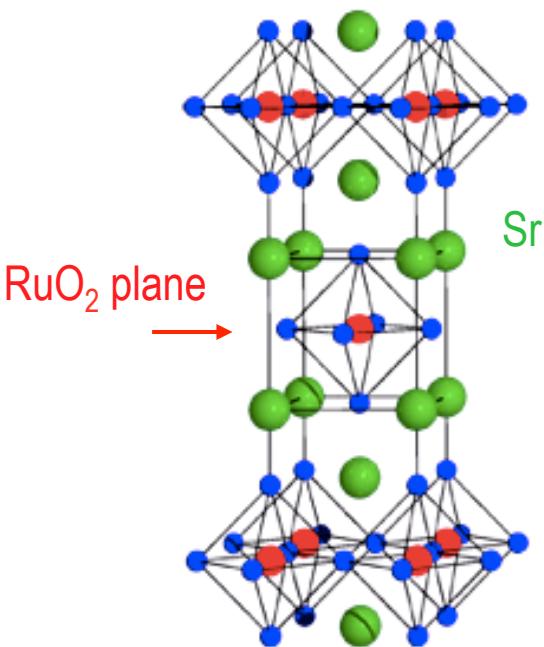
Fulde-Ferrel-like modulation



3-Kelvin phase
In
Ru-Sr₂RuO₄ eutectics

Sr_2RuO_4 - unconventional superconductor

Sr_2RuO_4



Maeno et al (1994)

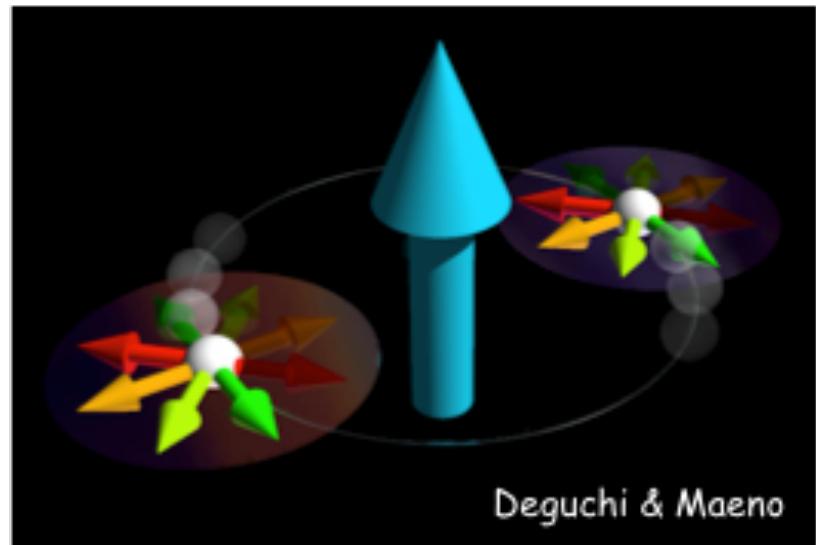
$$T_c \approx 1.5\text{K}$$

pairing symmetry

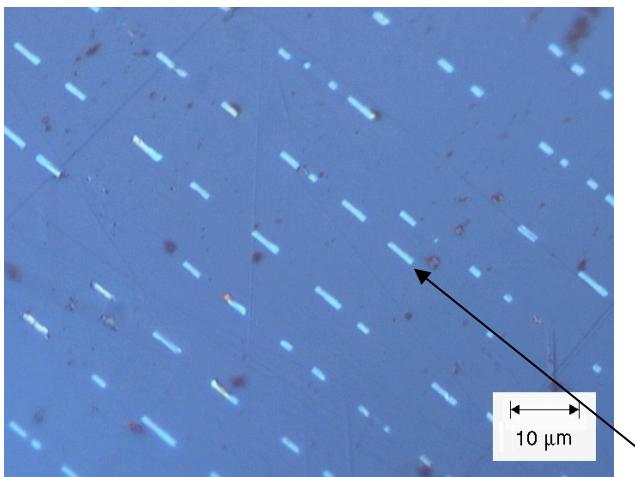
spin-triplet odd-parity

$$\vec{d}(\vec{k}) = \hat{z} (k_x \pm i k_y)$$

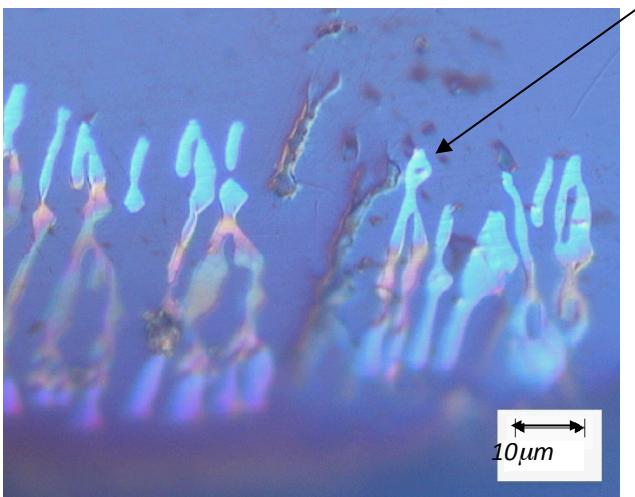
chiral p-wave



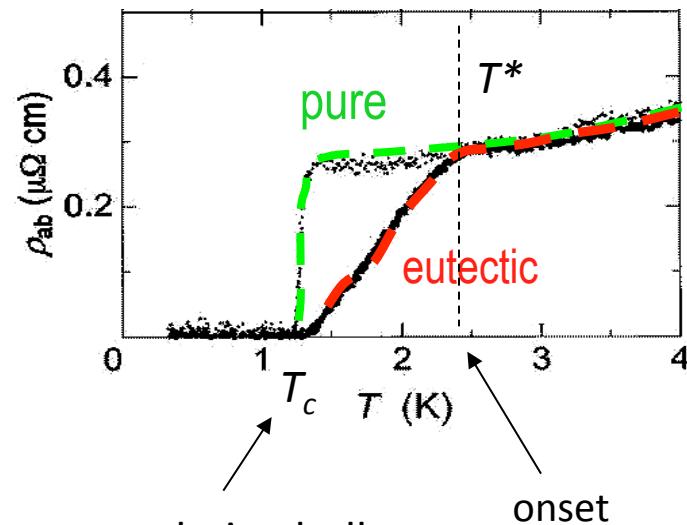
Eutectic Sr_2RuO_4 -Ru



μm -sized
Ru-metal
inclusions



nucleation of inhomogeneous
superconductivity

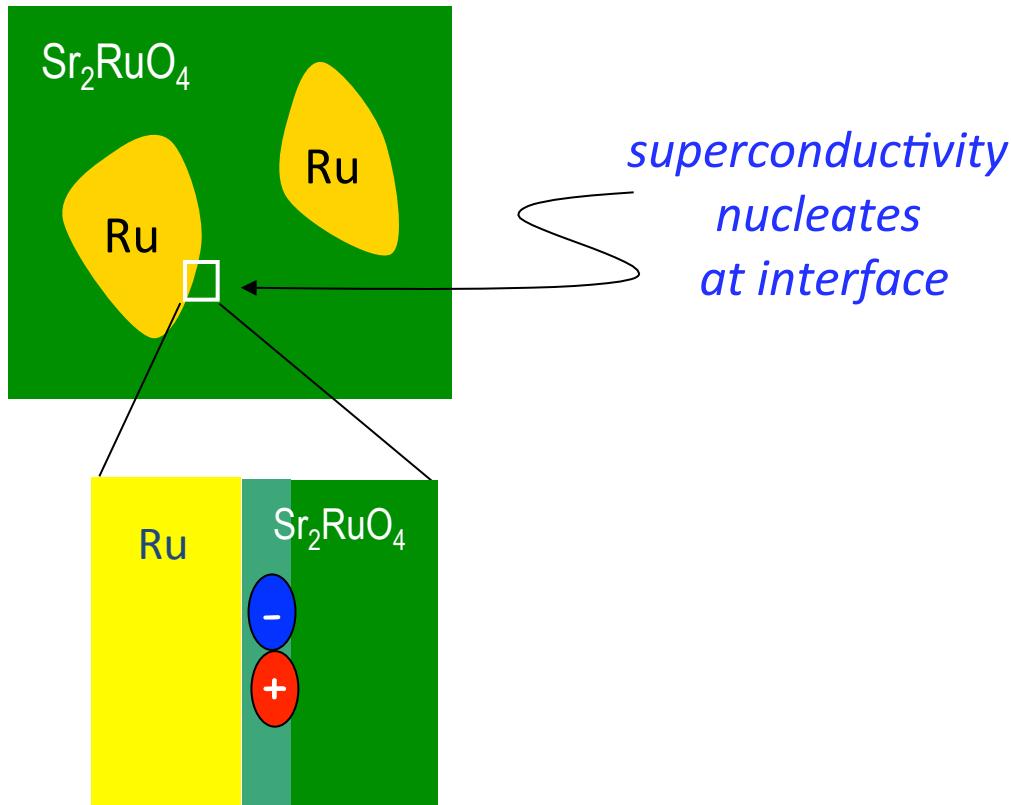


percolating bulk
superconductivity

$$T^* \sim 2xT_c \sim 3 \text{ K}$$

"3 - Kelvin phase"

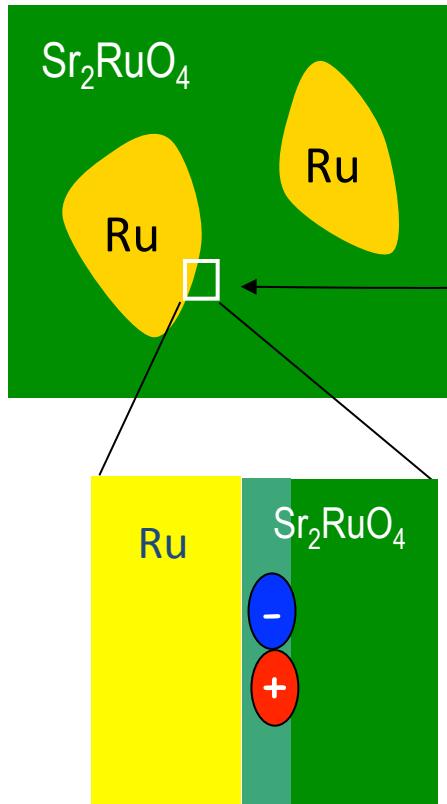
Eutectic Sr_2RuO_4 -Ru - nucleation



MS & Monien

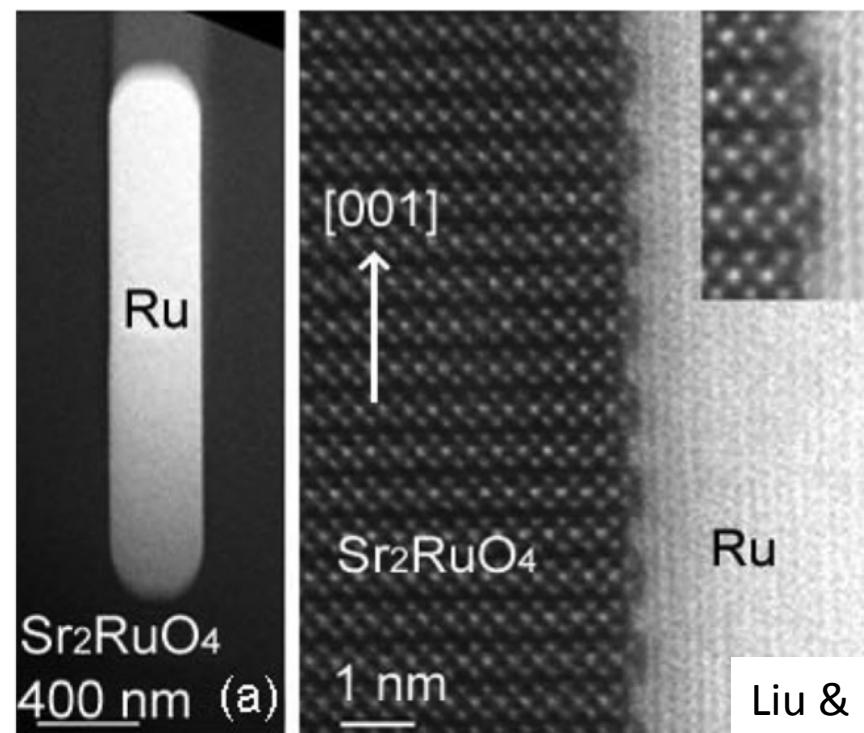
energetically favored
time reversal symmetry
conserving

Eutectic Sr_2RuO_4 -Ru - nucleation



*superconductivity
nucleates
at interface*

very clean interfaces

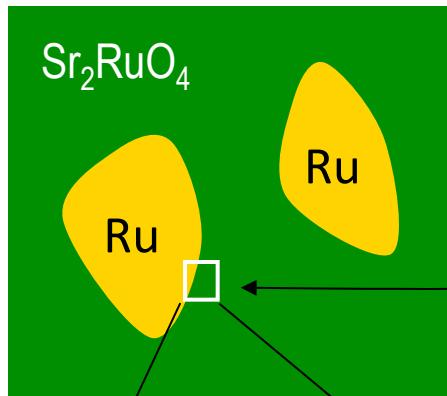


MS & Monien

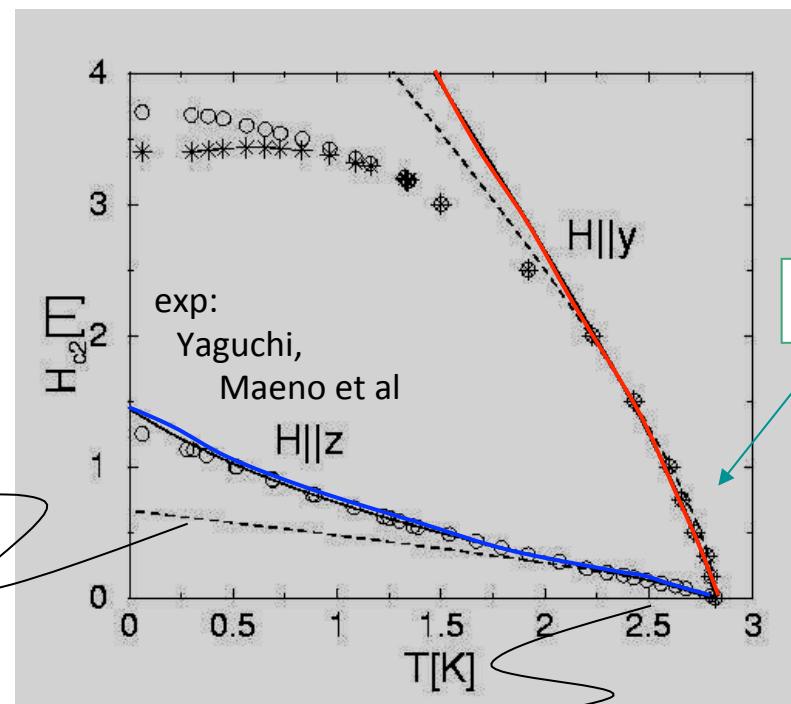
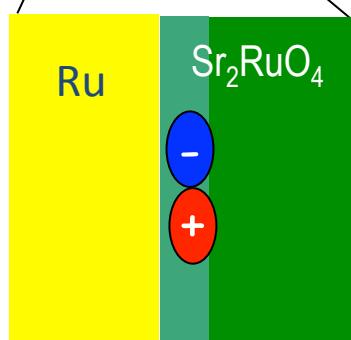
energetically favored
time reversal symmetry
conserving

Liu & Mao groups

Eutectic Sr_2RuO_4 -Ru - nucleation



*superconductivity
nucleates
at interface*

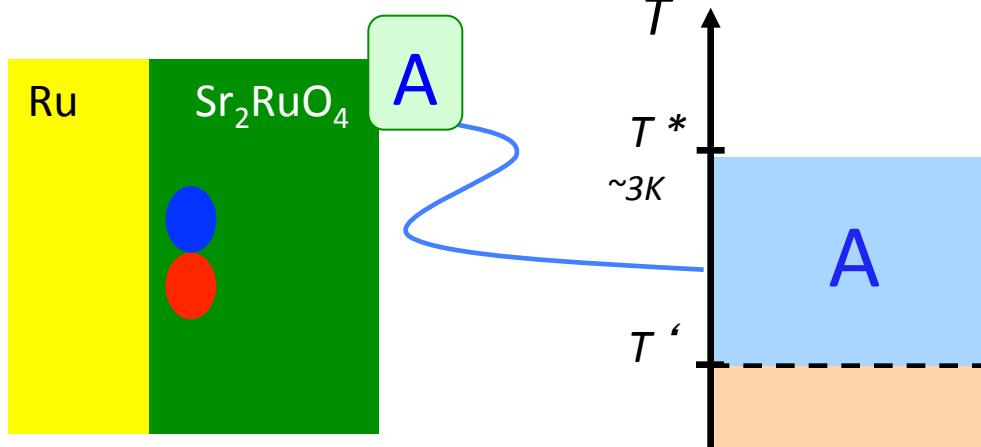


sublinear
**filamentary
superconductivity**

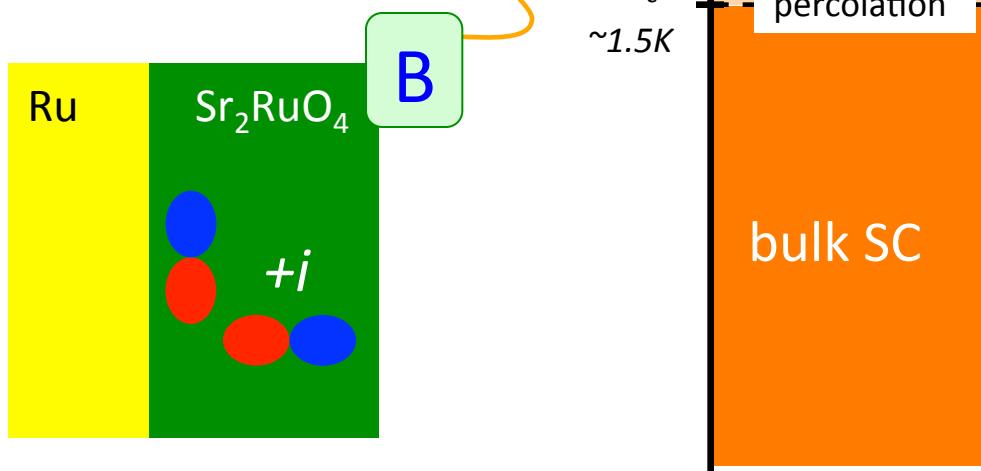
theo: Belardinelli, Matsumoto & MS

Sequence of phases

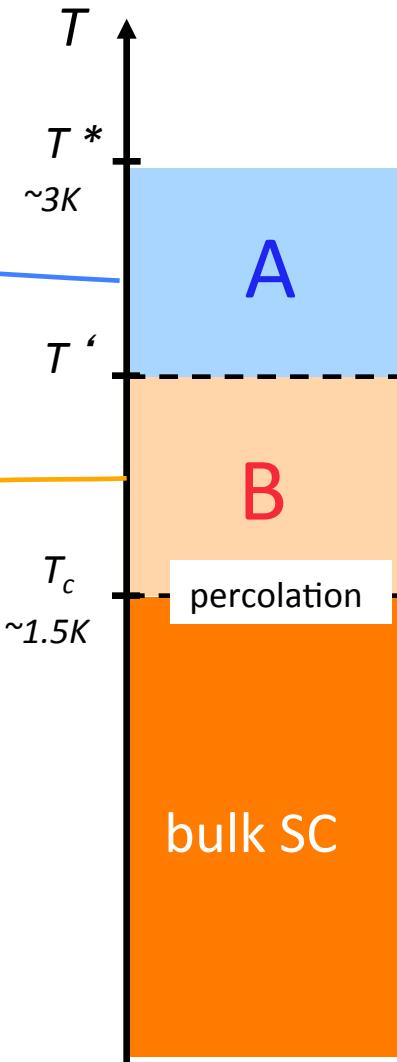
first nucleation



T-violating transition

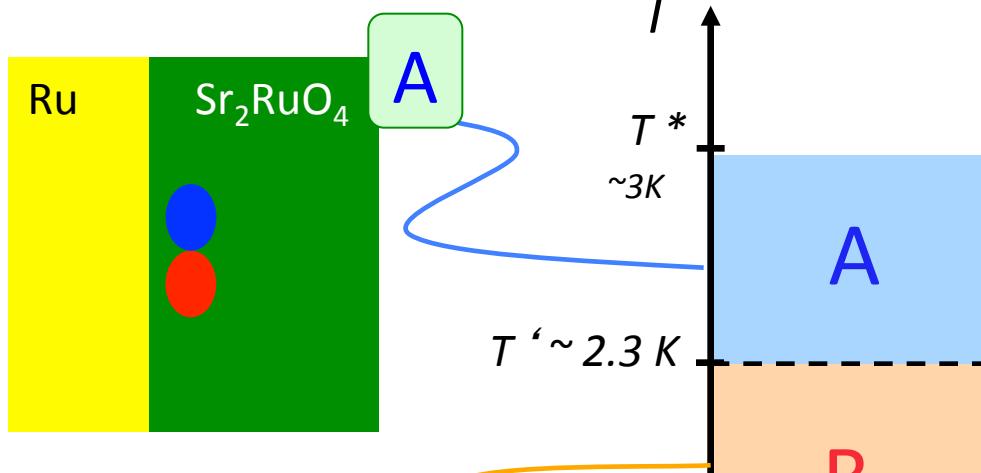


Kaneyasu et al (2010)

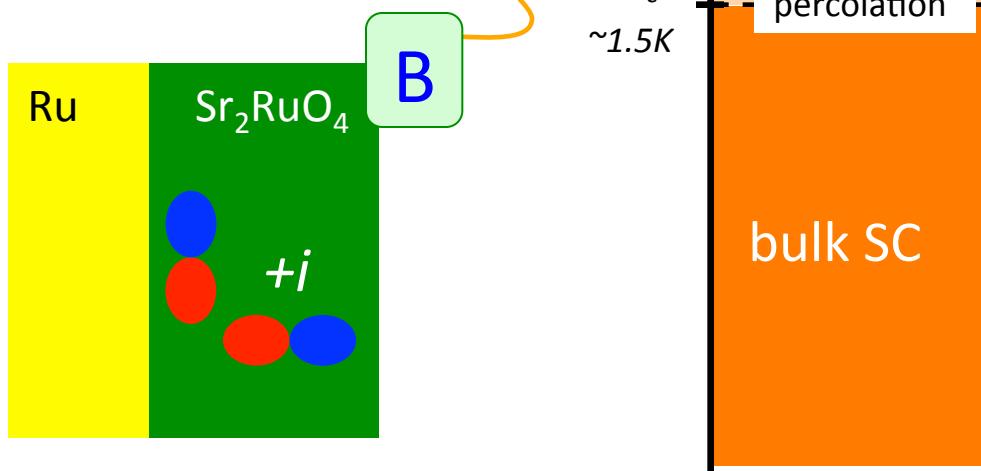


Sequence of phases

first nucleation

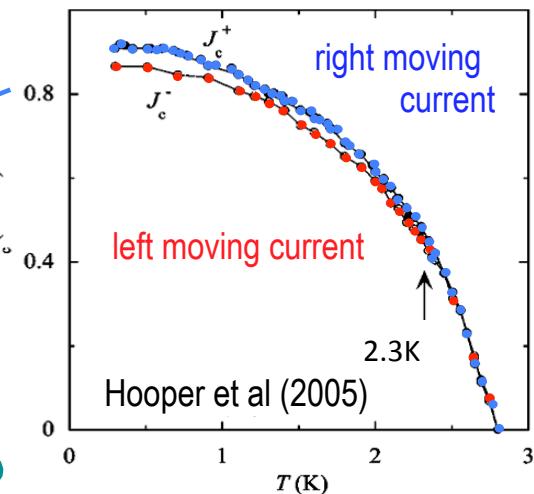


T -violating transition

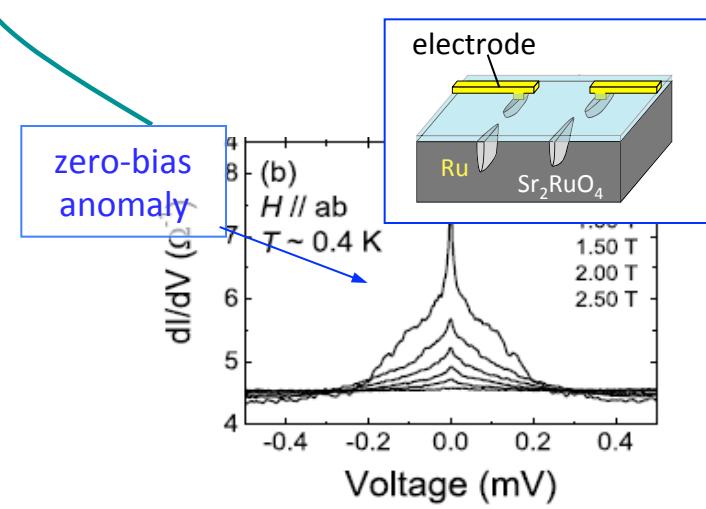


Kaneyasu et al (2010)

critical current of 3K-phase



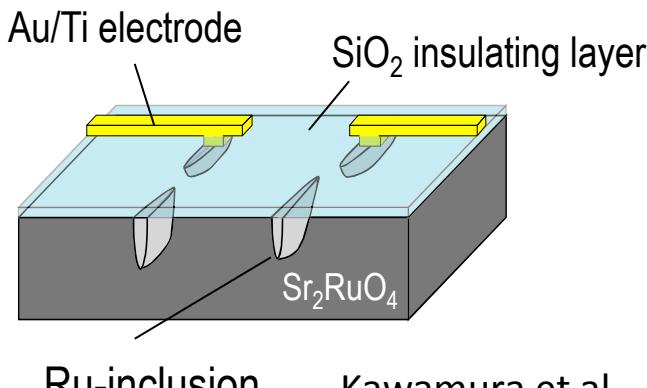
tunneling $\text{Ru}-\text{Sr}_2\text{RuO}_4$



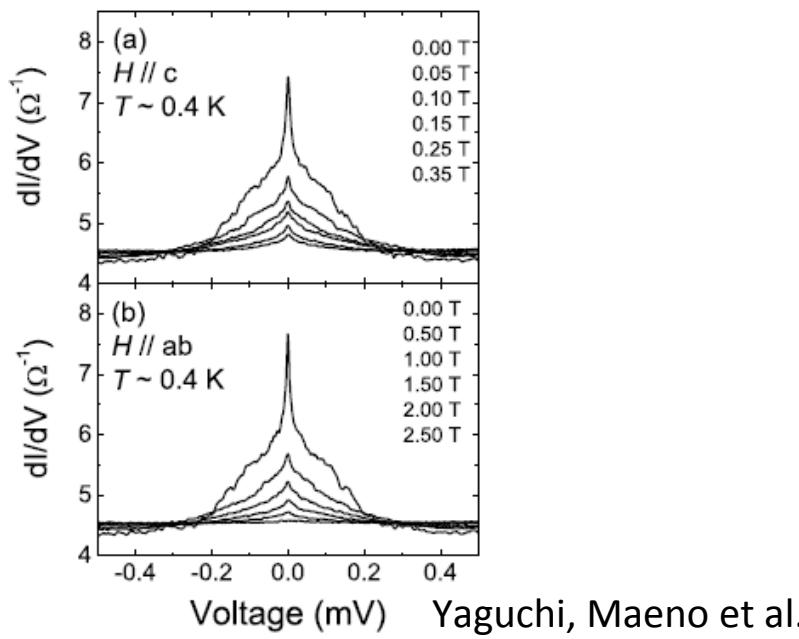
Yaguchi et al (2006)

A-to-B transition - zero-bias anomaly

Tunneling through Ru-inclusions

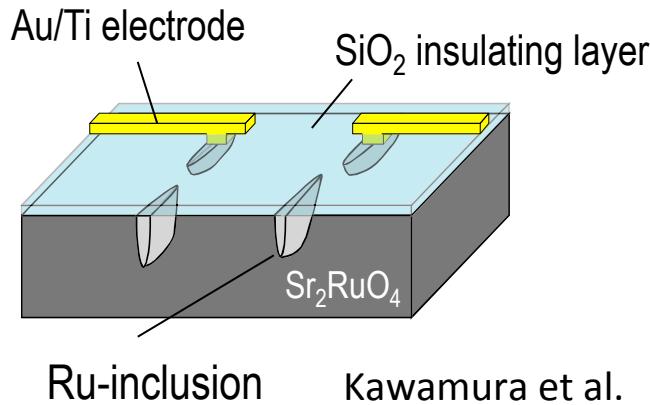


Kawamura et al.



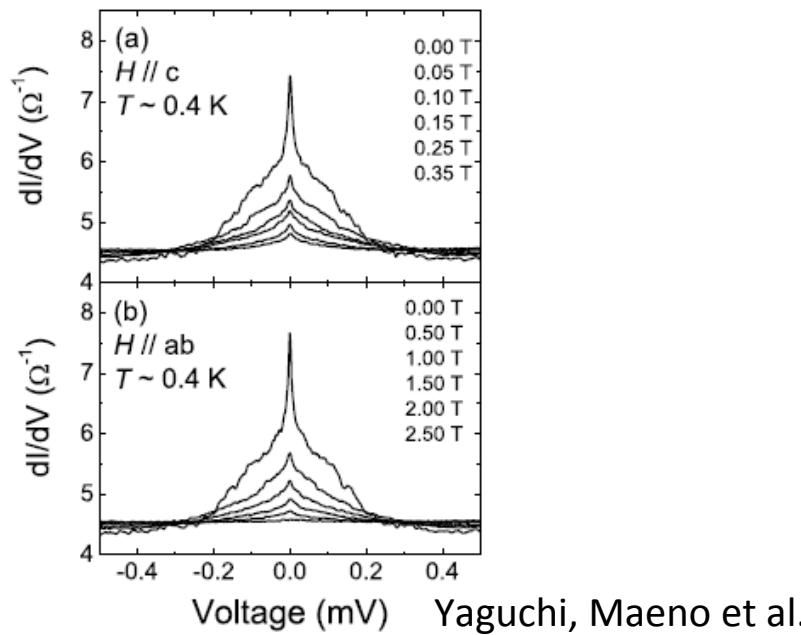
A-to-B transition - zero-bias anomaly

Tunneling through Ru-inclusions



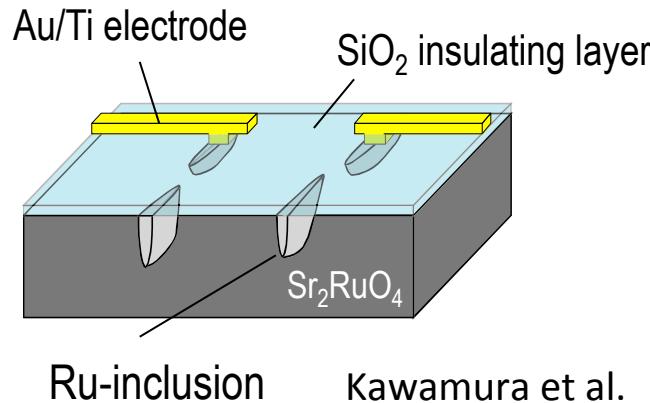
onset of
zero-bias anomaly at

$$T' \approx 2.3\text{K}$$



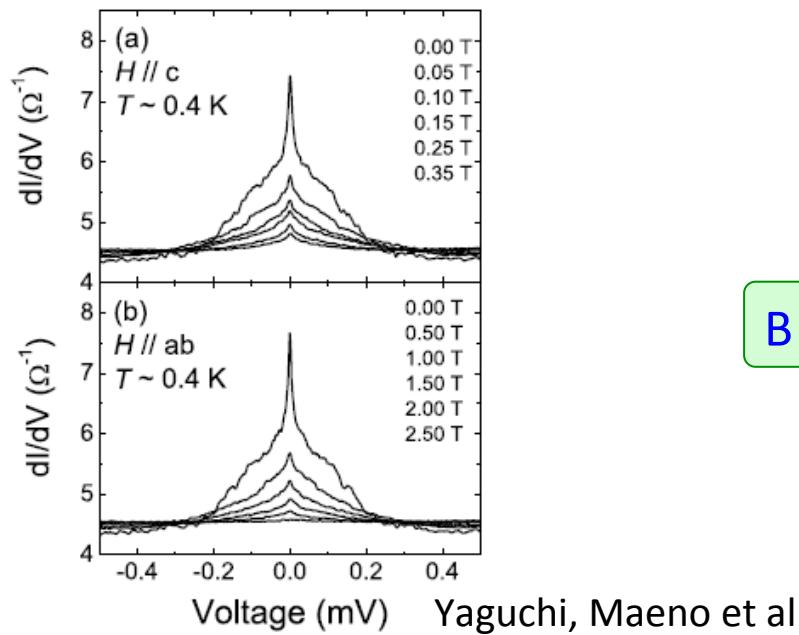
A-to-B transition - zero-bias anomaly

Tunneling spectroscopy



Ru-inclusion

Kawamura et al.

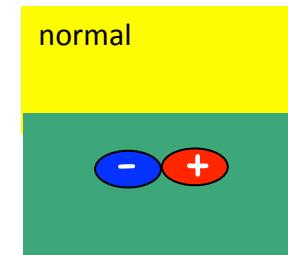


Voltage (mV) Yaguchi, Maeno et al.

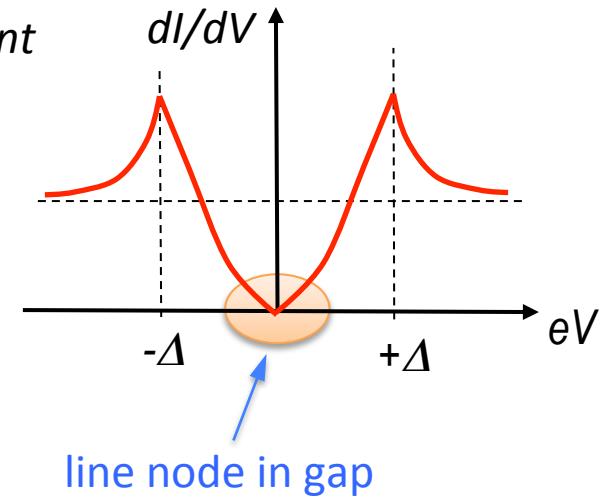
Andreev bound states

parallel component

A

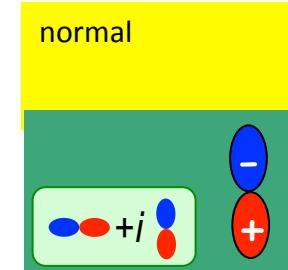


no bound states

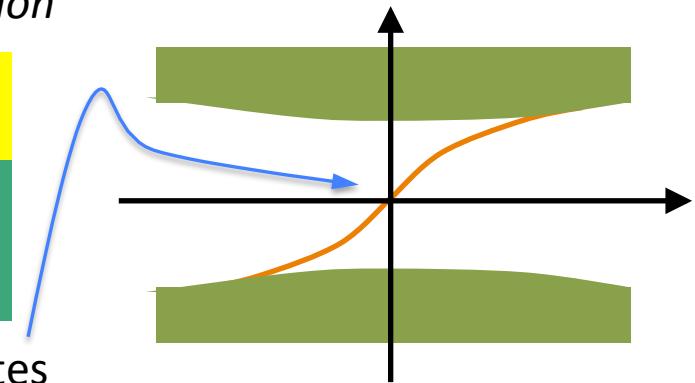


chiral combination

B

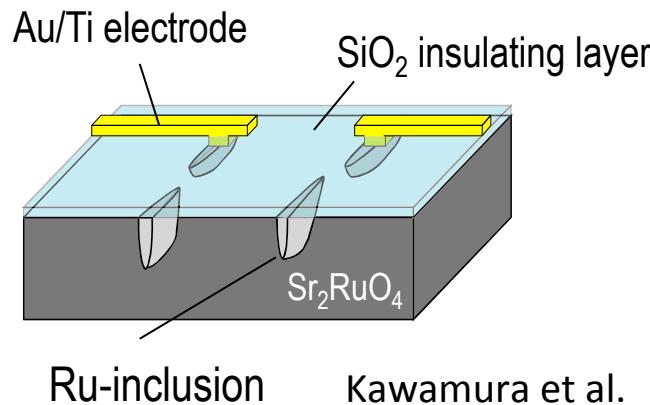


chiral edge states

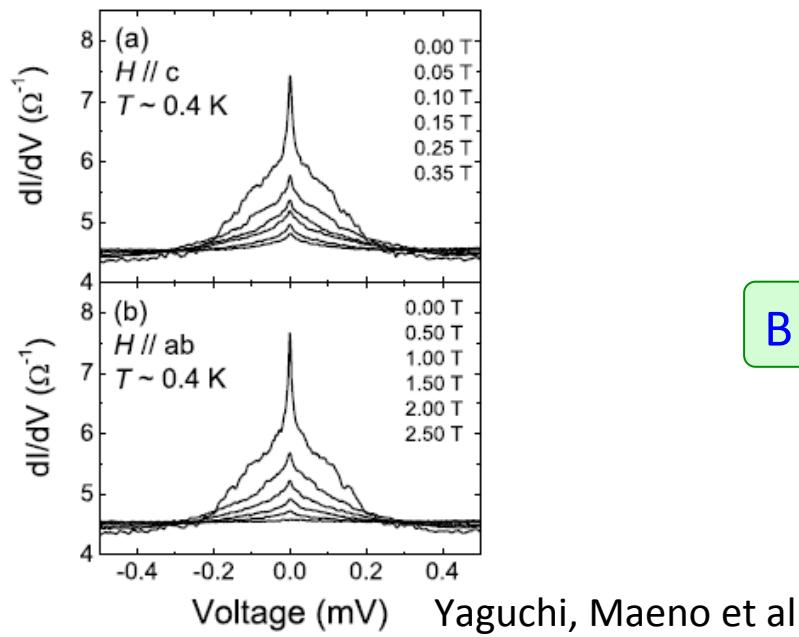


A-to-B transition - zero-bias anomaly

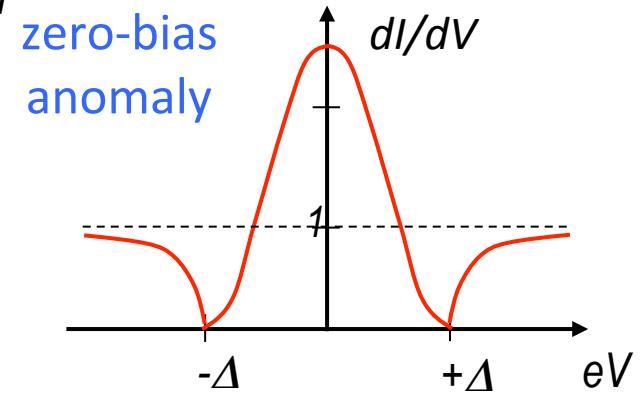
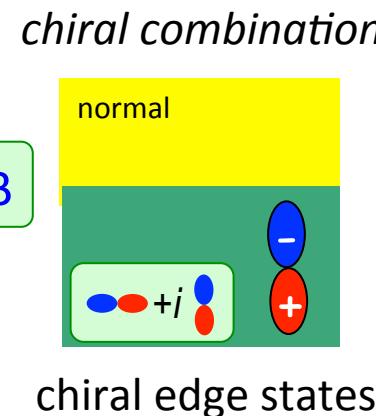
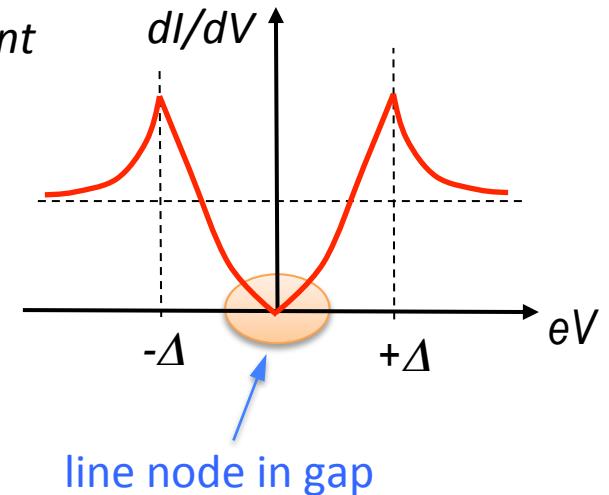
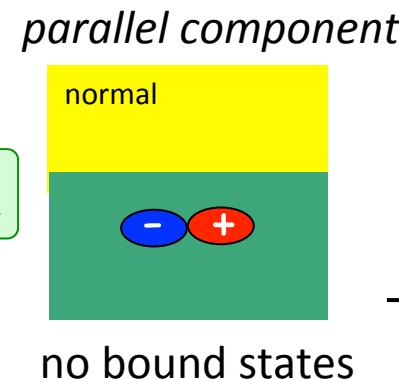
Tunneling spectroscopy



Kawamura et al.

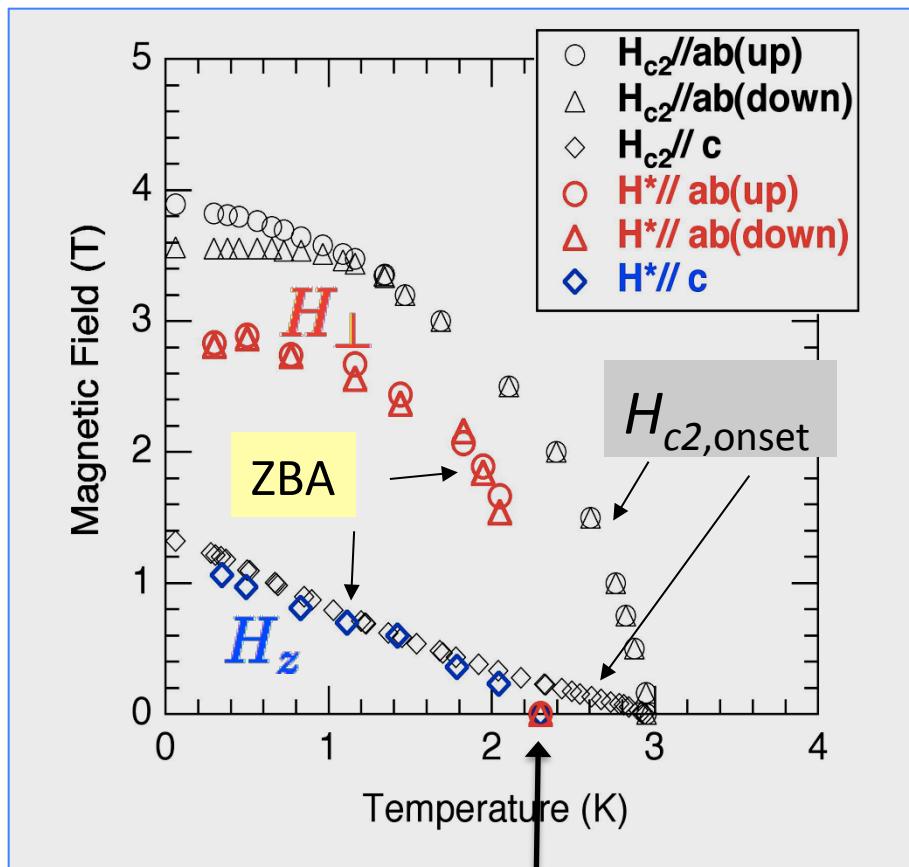


Andreev bound states

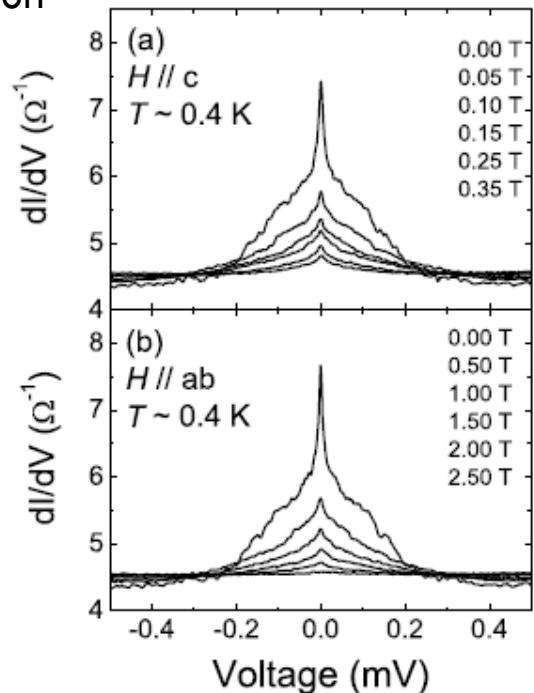
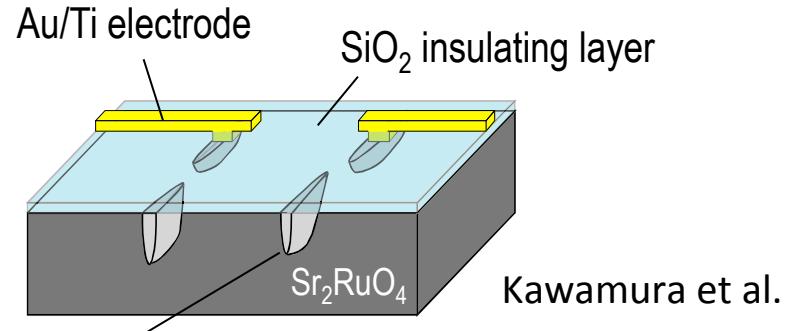


A-to-B transition - zero-bias anomaly

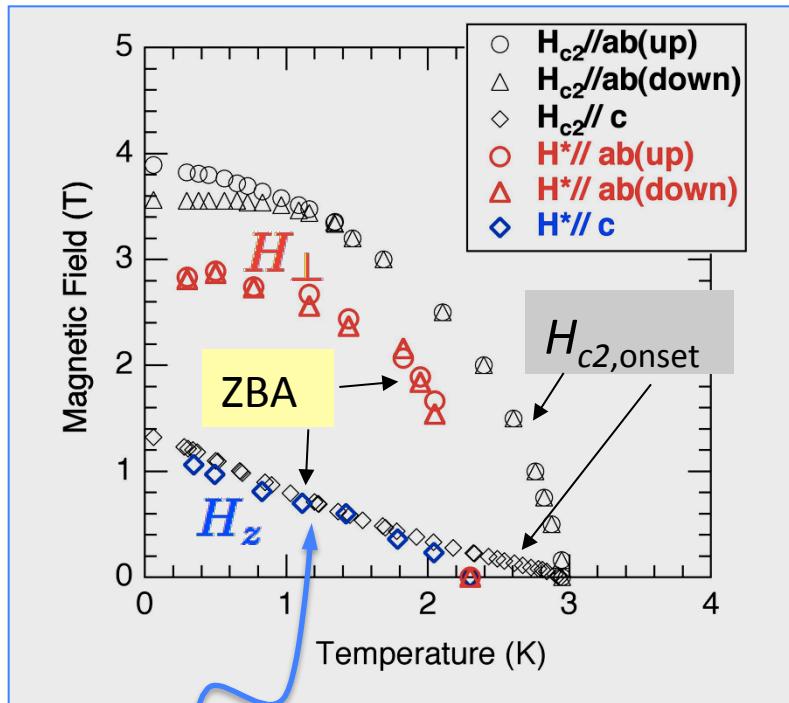
magnetic field



direct contacts to Ru-inclusions

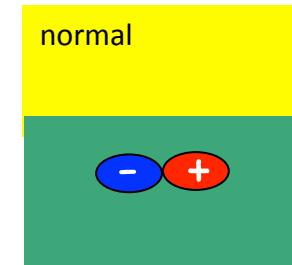


A-to-B transition - zero-bias anomaly

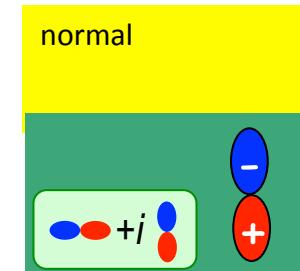


magnetic field induces perpendicular component once parallel component is present

parallel component



perpendicular component



magnetic field parallel z-axis

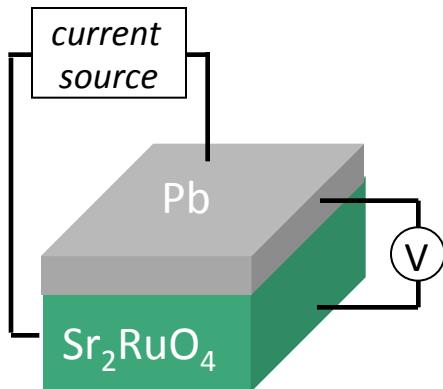
Zeeman coupling to
Cooper pair angular momentum

$$L_z \propto i(\eta_x^* \eta_y - \eta_x \eta_y^*)$$

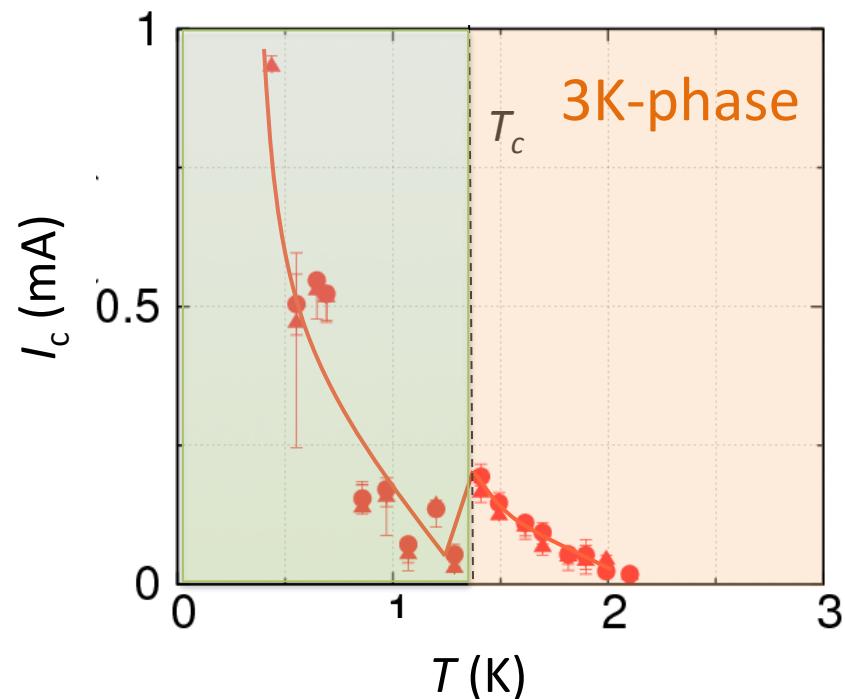
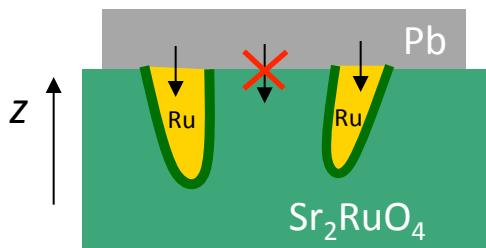
$$F_Z = i\gamma H_z (\eta_x^* \eta_y - \eta_x \eta_y^*)$$

Anomalous Josephson coupling

device – Josephson coupling

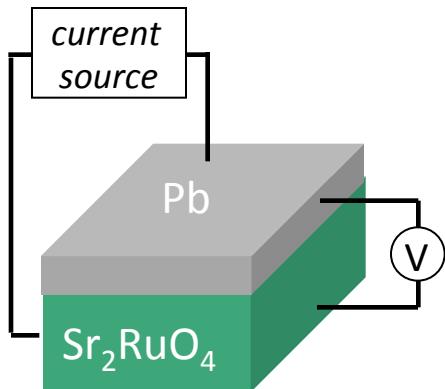


Nakamura, Maeno et al (2010)

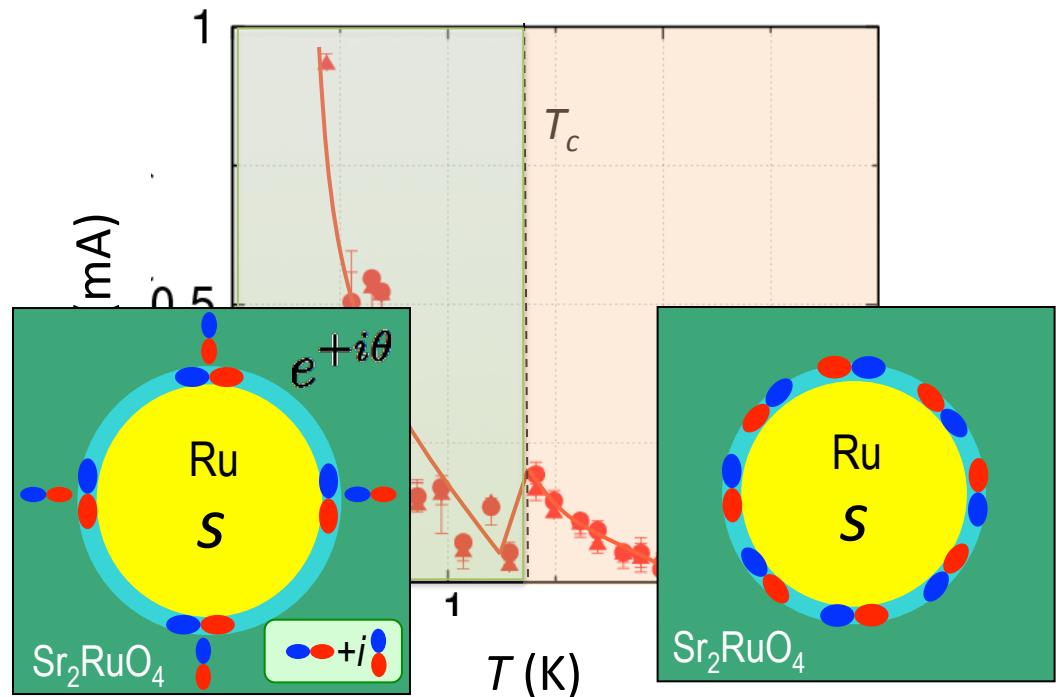
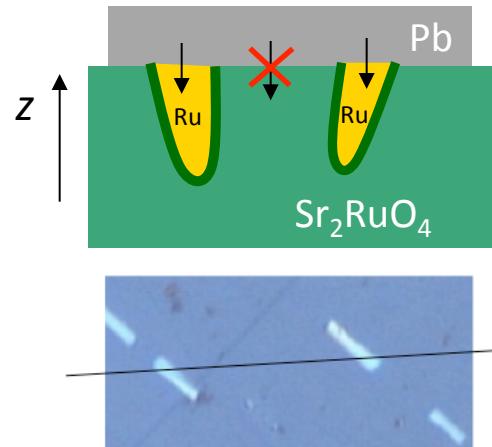


Anomalous Josephson coupling

device – Josephson coupling



Nakamura, Maeno et al (2010)



frustrated
coupling into
chiral p-wave

Etter et al

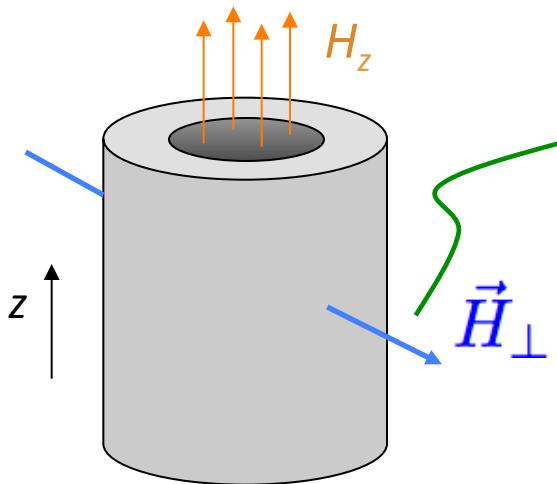
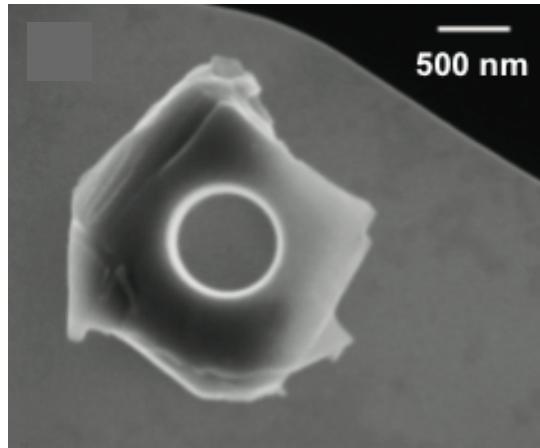
coupling
through Ru
to 3K-phase

Owen-Scalapino

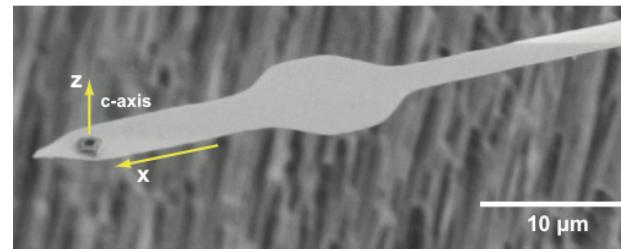
Loops & half-flux quanta In Sr_2RuO_4

Half-flux quantization

Sr_2RuO_4 micro-loops



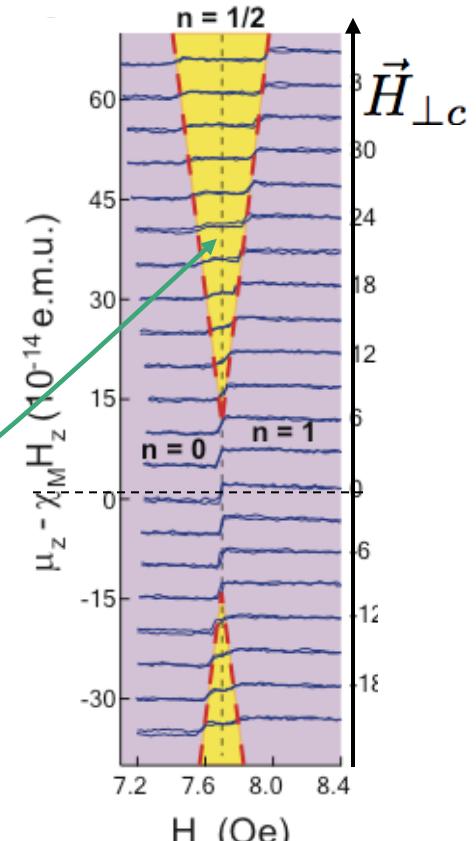
cantilever magnetometer



Budakian et al

inplane field supports
half-flux quantum steps

intermediate half-flux quantum

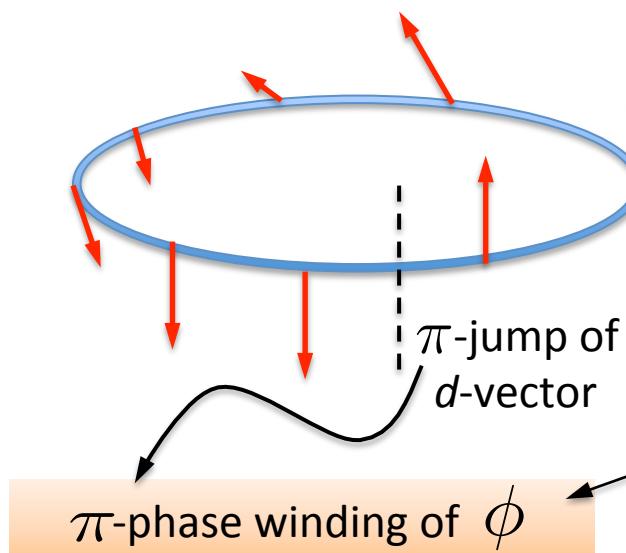


Jang et al (2010)

$$\Phi = \Phi_0/2$$

d -vector „manipulation“

d -texture / d -soliton



$$d(\mathbf{k}) = \Delta \hat{d} g(\mathbf{k})$$



$$d(\mathbf{k}, \mathbf{r}) = |\Delta(\mathbf{r})| e^{i\phi(\mathbf{r})} \hat{d}(\mathbf{r}) g(\mathbf{k})$$

$$\Phi = \frac{\Phi_0}{2\pi} \int d\vec{l} \cdot \vec{\nabla} \phi = \frac{\Phi_0}{2}$$

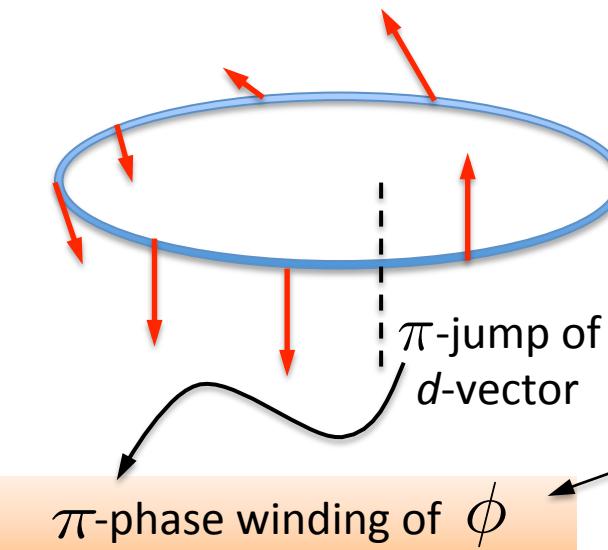
half-flux quantum

Volovik & Salomaa ; Ivanov
Chung, Blum & Kim;

Vakaryuk & Leggett
Roberts, Budakian & Stone
Kee & MS

d -vector „manipulation“

d -texture / d -soliton



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half-flux quantum

Volovik & Salomaa ; Ivano Chung, Blum & Kim;
Vakaryuk & Leggett
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Kee & MS

weak
spin-orbit coupling

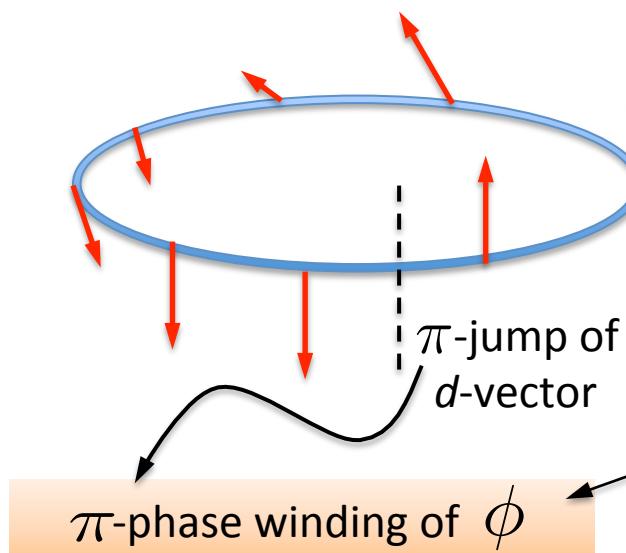
d -texture

strong
spin-orbit coupling

d -soliton

d -vector „manipulation“

d -texture / d -soliton



$$\mathbf{d}(\mathbf{k}) = \Delta \hat{\mathbf{d}} g(\mathbf{k})$$

$$\mathbf{d}(\mathbf{k}, \mathbf{r}) = |\Delta(\mathbf{r})| e^{i\phi(\mathbf{r})} \hat{\mathbf{d}}(\mathbf{r}) g(\mathbf{k})$$

supercurrent:

$$J_\alpha \propto |\Delta|^2 \left(\nabla \phi - \frac{2\pi}{\Phi_0} \mathbf{A} \right)_\alpha$$

spin current:

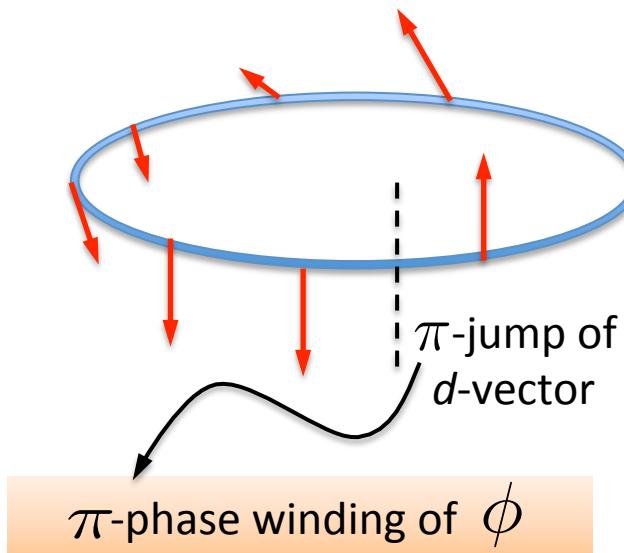
$$J_{\alpha m} \propto |\Delta|^2 \left(\hat{\mathbf{d}}^* \times \nabla_\alpha \hat{\mathbf{d}} \right)_m$$

spin polarization

$$S_m \propto \sum_\alpha J_\alpha J_{\alpha m}$$

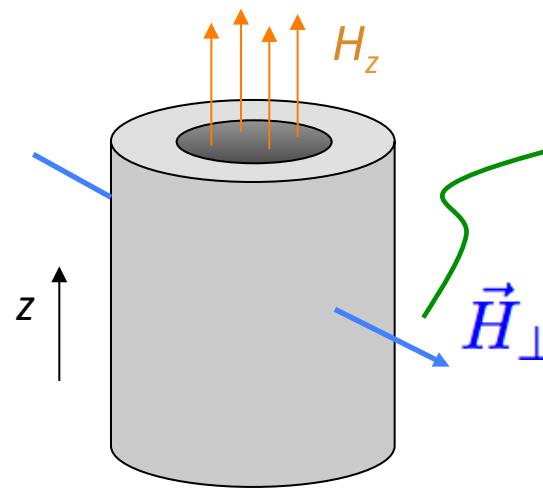
d -vector „manipulation“

d -texture / d -soliton

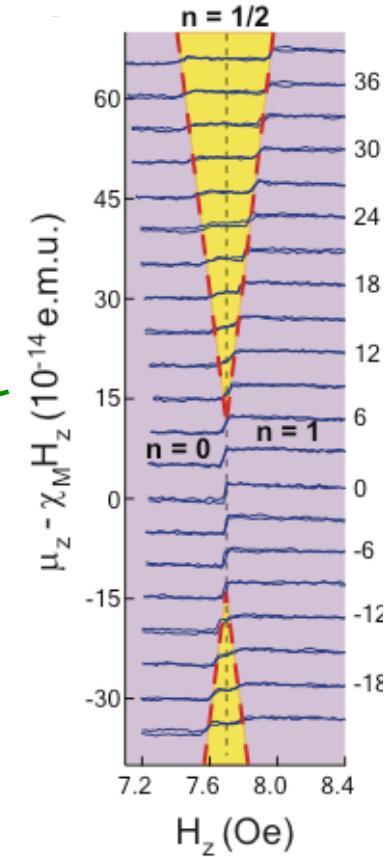


spin polarization

$$S_m \propto \sum_{\alpha} J_{\alpha} J_{\alpha m}$$



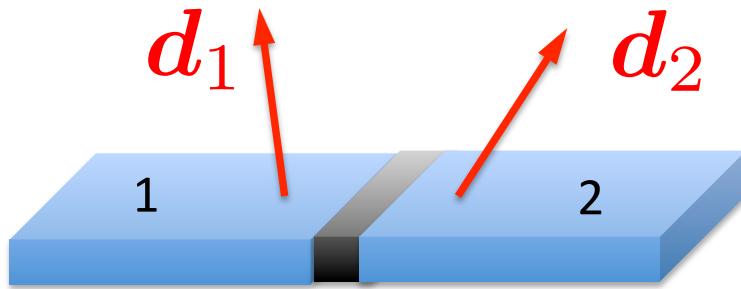
Budakian et al



magnetic field perpendicular to d -twist
facilitates d -texture / d -soliton

d -vector „manipulation“

d -twist in Josephson junctions



Asano; Brydon, Manske et al,

Josephson current:

$$J = J_0 \cos \alpha \sin \phi$$

$$\phi = \phi_2 - \phi_1 \quad \text{Josephson phase}$$

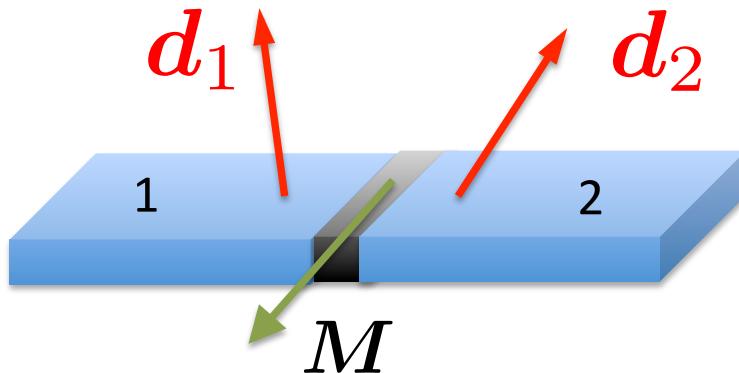
$$\hat{d}_1 \cdot \hat{d}_2 = \cos \alpha$$

Josephson spin current:

$$J_s = J_{s0} \sin \alpha \cos \phi$$

d -vector „manipulation“

d -twist in Josephson junctions



Josephson current:

$$J = J_0 \cos \alpha \sin \phi$$

$$\phi = \phi_2 - \phi_1 \quad \text{Josephson phase}$$

$$\hat{d}_1 \cdot \hat{d}_2 = \cos \alpha$$

Josephson spin current:

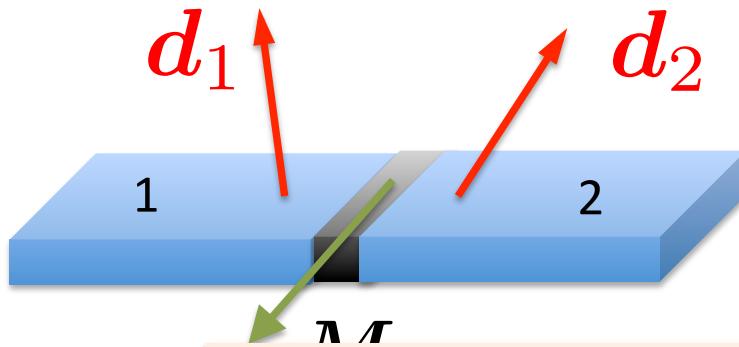
$$J_s = J_{s0} \sin \alpha \cos \phi$$

junction magnetization modifies current-phase coupling

$$F_J = t \hat{d}_1 \cdot \hat{d}_2 \cos \phi + t' M \cdot (\hat{d}_1 \times \hat{d}_2) \sin \phi$$

d -vector „manipulation“

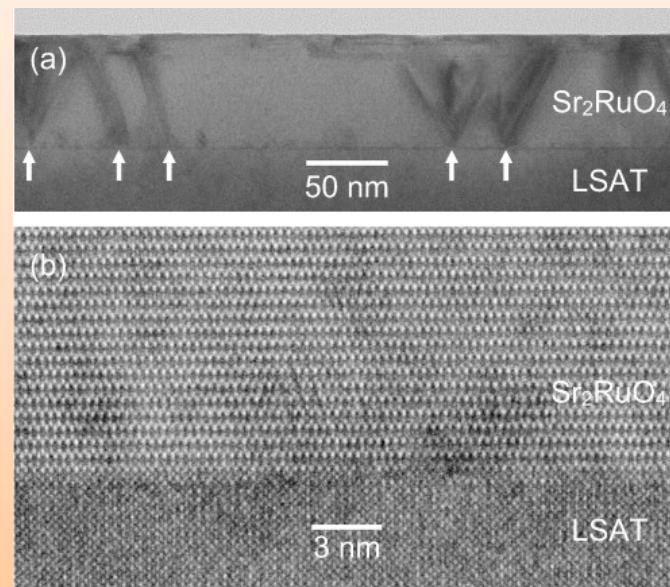
d -twist in Josephson junctions



Joseph

$$J =$$

junction



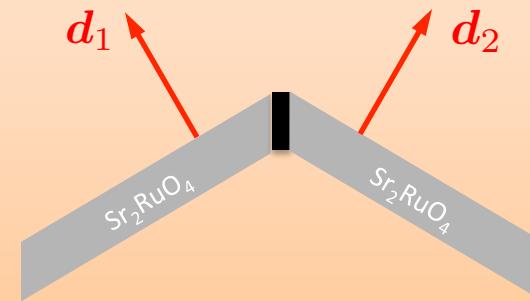
$$\phi = \phi_2 - \phi_1 \quad \text{Josephson phase}$$

$$\hat{d}_1 \cdot \hat{d}_2 = \cos \alpha$$

thin films of Sr_2RuO_4

Krockenberger et al (NTT)

$$T_c \lesssim 1\text{K}$$



Opportunities – this is just the beginning

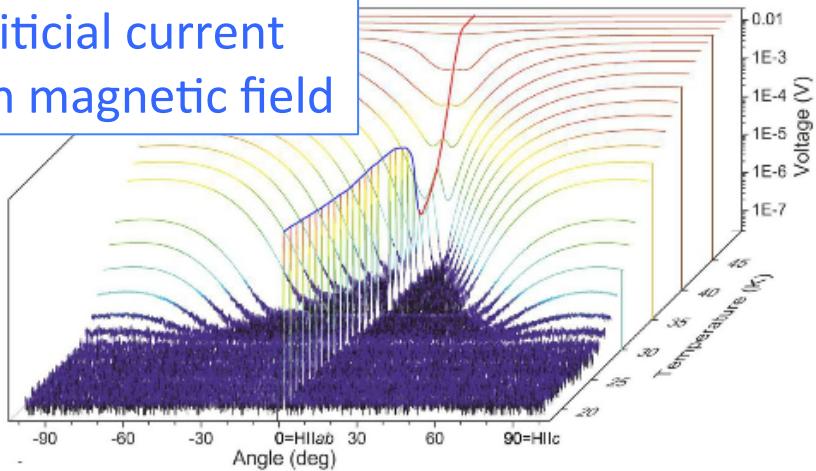
Structured samples

SmFeAs(O,F)



Focussed Ion Beam

Critical current
in magnetic field



Moll, Batlogg et al

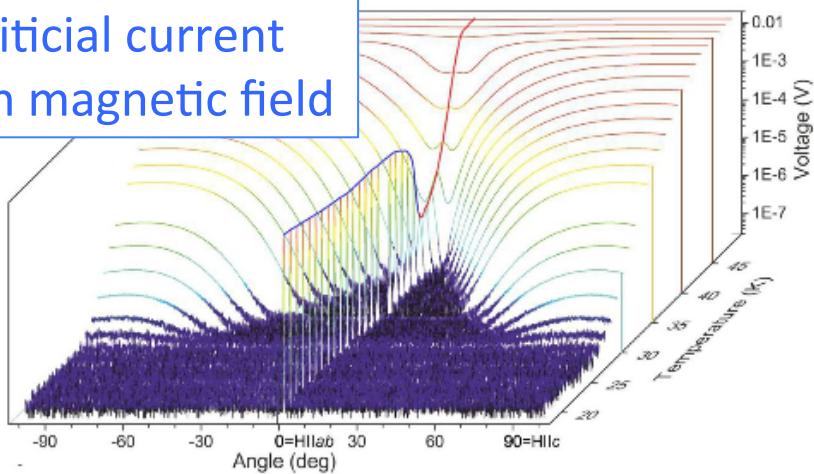
Opportunities – this is just the beginning

Structured samples

SmFeAs(O,F)

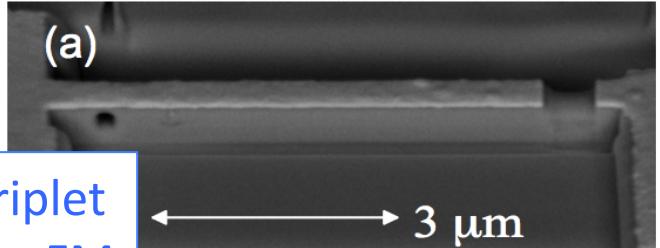


Critical current
in magnetic field



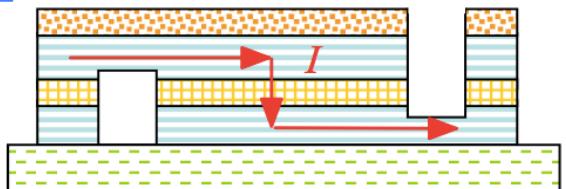
Moll, Batlogg et al

YBCO-LMO heterostructures



singlet-triplet
proximity FM

Au
YBCO
LMO
YBCO
LSAT



Krasnov & Bernhard groups

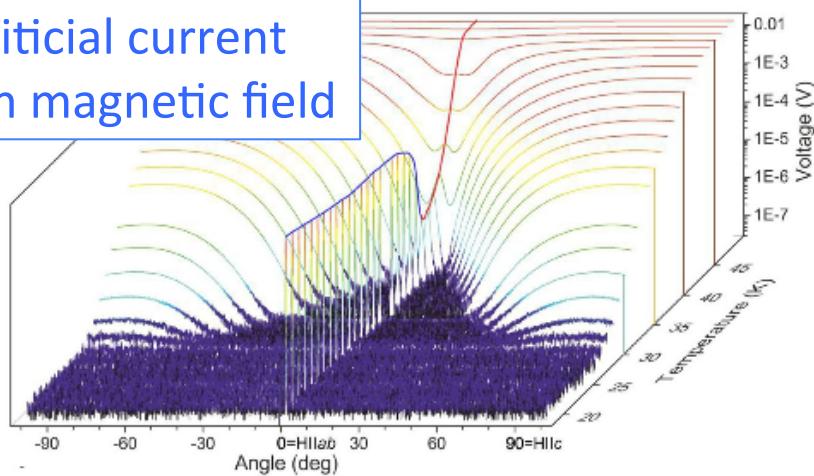
Opportunities – this is just the beginning

Structured samples

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Critical current
in magnetic field

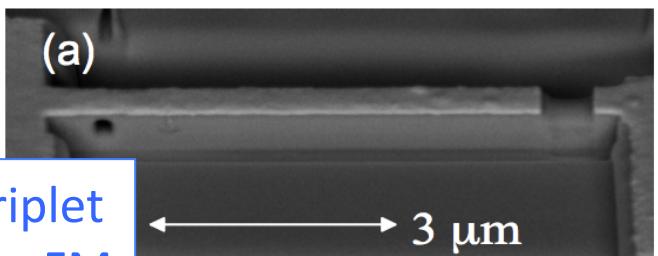


Moll, Batlogg et al

Focussed Ion Beam

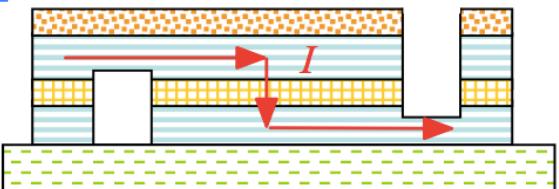
YBCO-LMO heterostructures

(a)



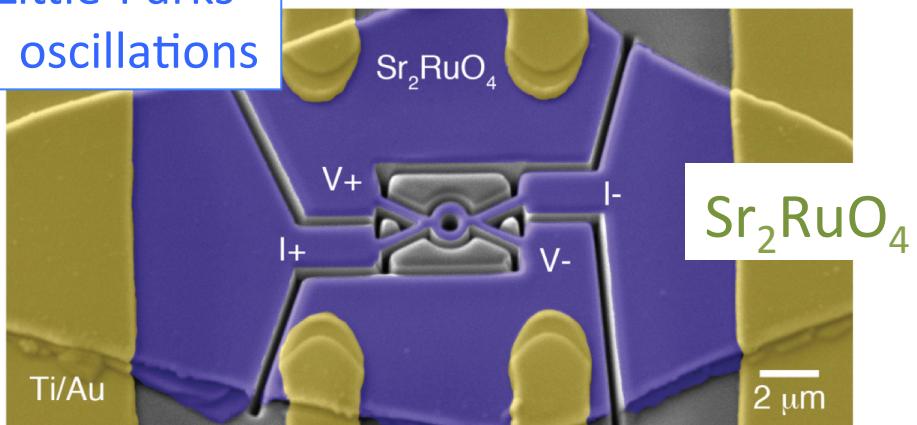
singlet-triplet
proximity FM

Au
YBCO
LMO
YBCO
LSAT



Krasnov & Bernhard groups

Little-Parks
oscillations



Sr_2RuO_4

Liu & Mao groups

$\Phi_0/2 \rightarrow d$ -textures ?

