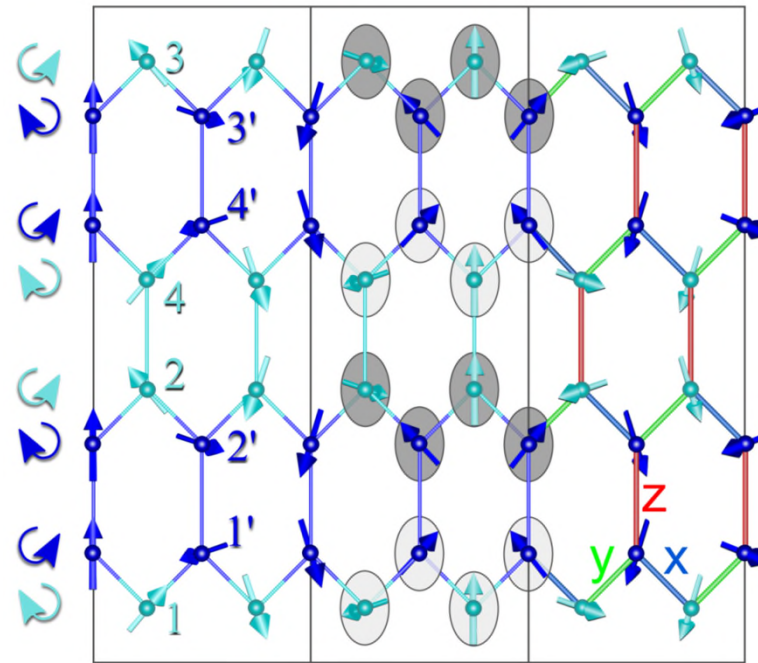
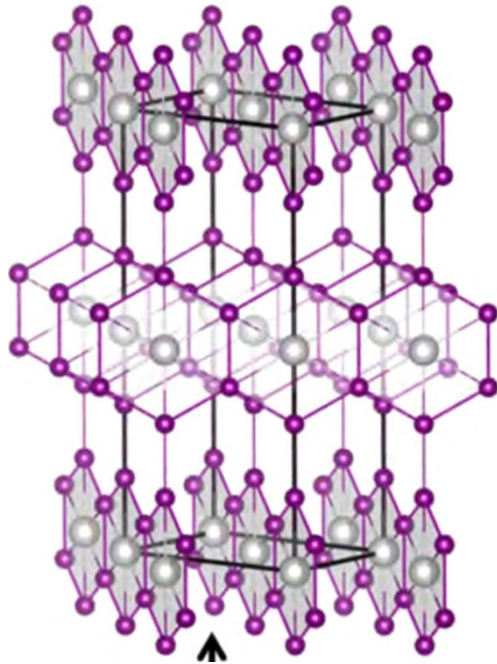


Unconventional magnetic order in 3D Kitaev materials revealed by resonant x-ray diffraction

Radu Coldea

Oxford



Collaborators



Alun Biffin (Oxford->PSI)



Roger D. Johnson



S. Choi



P. Manuel



A. Bombardi



Sample synthesis

F. Freund, S. Manni (β - Li_2IrO_3) P. Gegenwart (Augsburg)



J. Analytis (γ - Li_2IrO_3) (Berkeley)

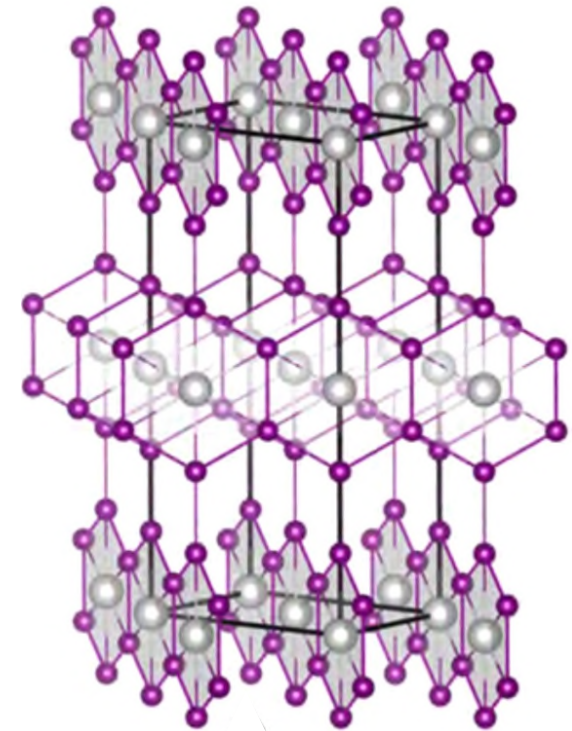
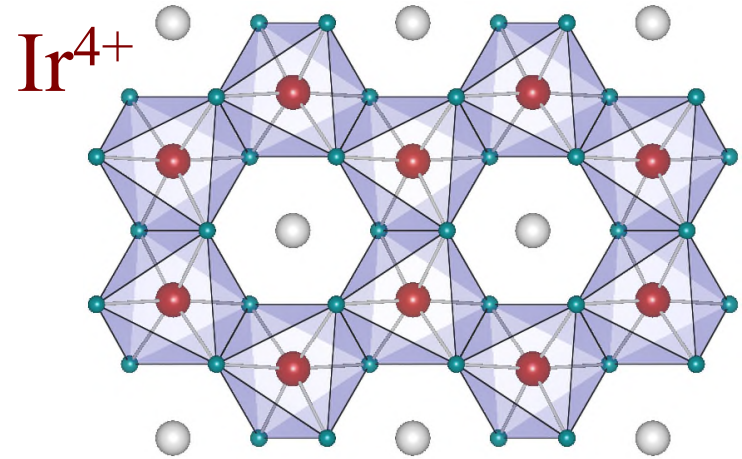


Theory

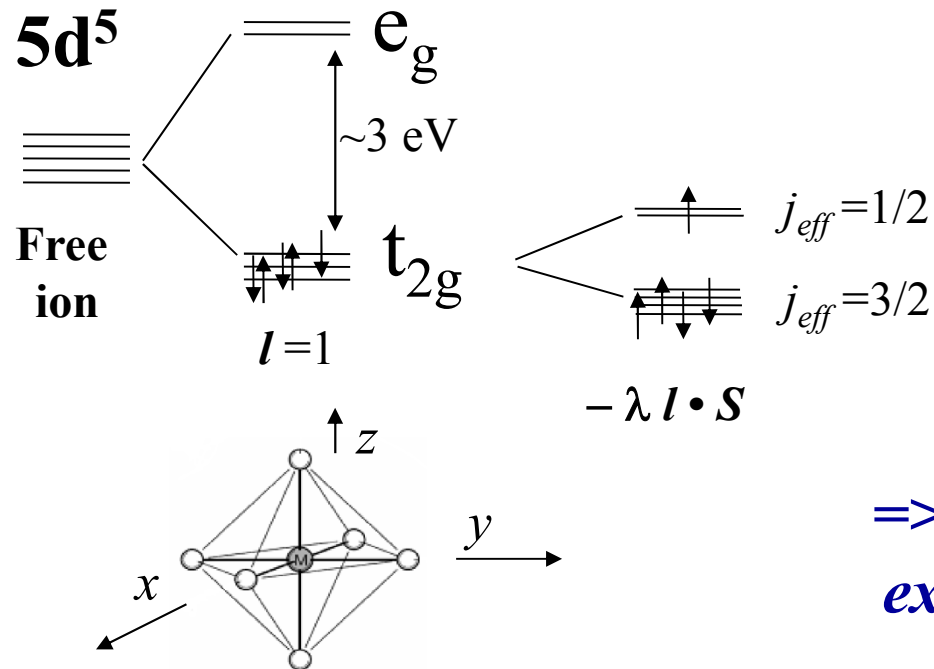
Itamar Kimchi + Ashvin Vishwanath (Berkeley)

Outline

- Kitaev model on honeycomb lattice
- 3D structural polytypes of Li_2IrO_3
- resonant x-ray experiments to solve the magnetic order in 3D γ - and β - Li_2IrO_3



Spin-orbit coupling in Ir^{4+} ($\lambda \sim 0.4 \text{ eV}$)

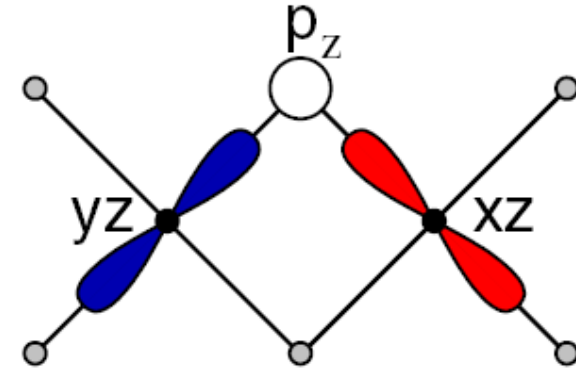
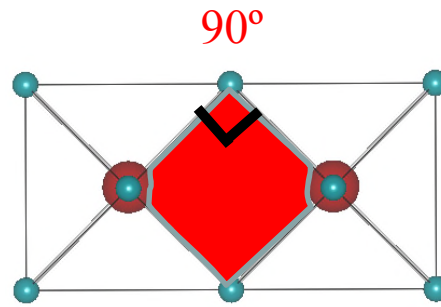
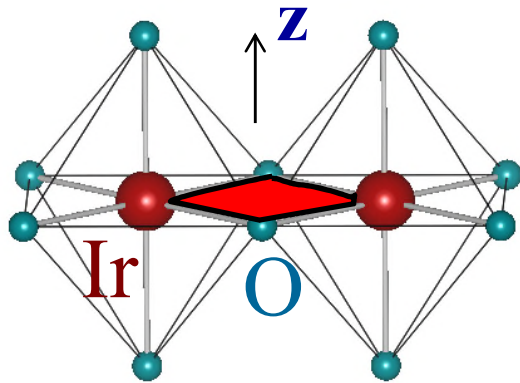


- composite spin-orbital moment

=> potentially non-Heisenberg exchanges & novel cooperative magnetism stabilized by SO coupling

Bond-directional exchange in edge-sharing IrO_6 octahedra

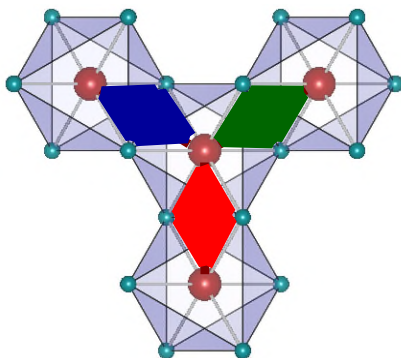
Jackeli, Khaliulin (2009)



$$|j_{\text{eff}}^z = +\frac{1}{2}\rangle = \frac{1}{\sqrt{3}} (d_{xy} \uparrow + (i d_{xz} + d_{yz}) \downarrow)$$

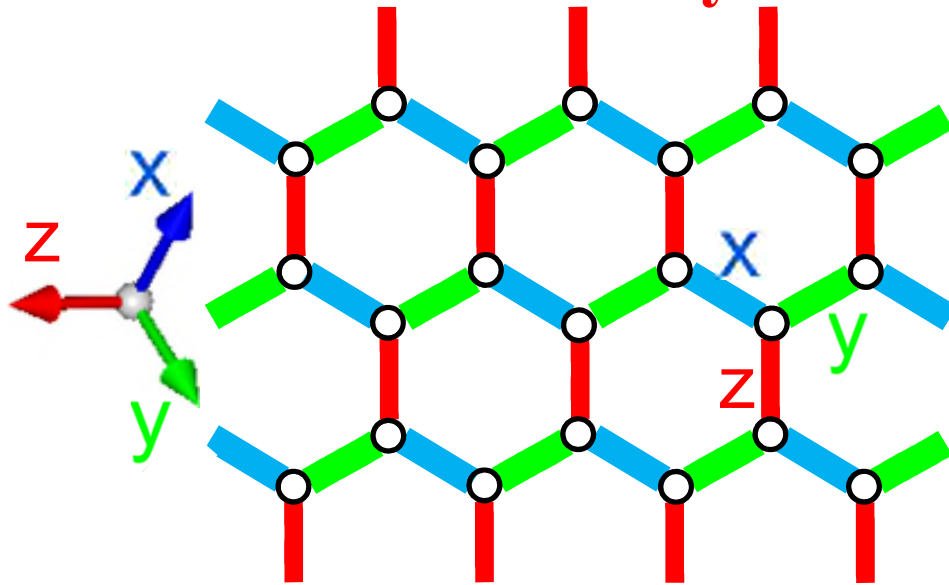
$$|j_{\text{eff}}^z = -\frac{1}{2}\rangle = \frac{1}{\sqrt{3}} (d_{xy} \downarrow + (-i d_{xz} + d_{yz}) \downarrow)$$

- 90° Ir-O₂-Ir superexchange \Rightarrow Ising form $-K S_1^z S_2^z$
 $j_{\text{eff}} = 1/2$



- 3-fold coordination \Rightarrow orthogonal Ising axes for the 3 bonds
- frustration from bond-dependent anisotropic interactions

Kitaev model on honeycomb lattice



Kitaev (2006)

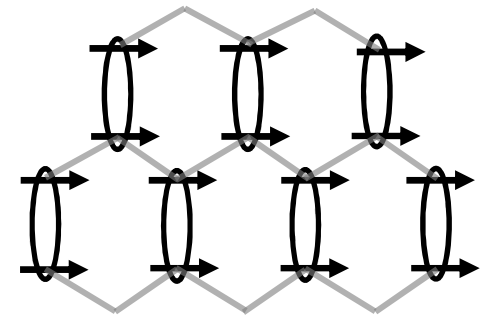
x -bond $-K S_i^x S_j^x$

y -bond $-K S_i^y S_j^y$

z -bond $-K S_i^z S_j^z$

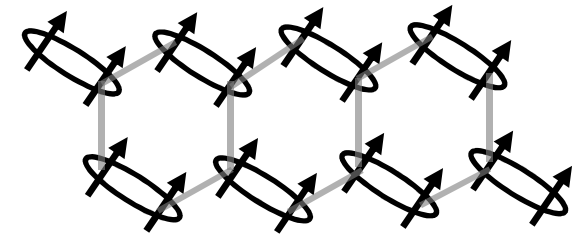
- quantum spin liquid (exactly solvable)
- spinon + flux excitations

if only z -bonds

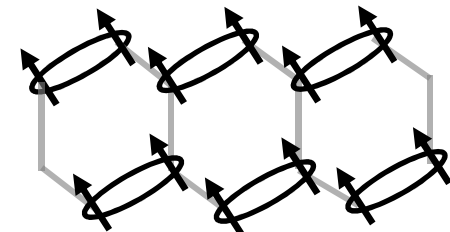


ferromagnetic dimers

if only x -bonds

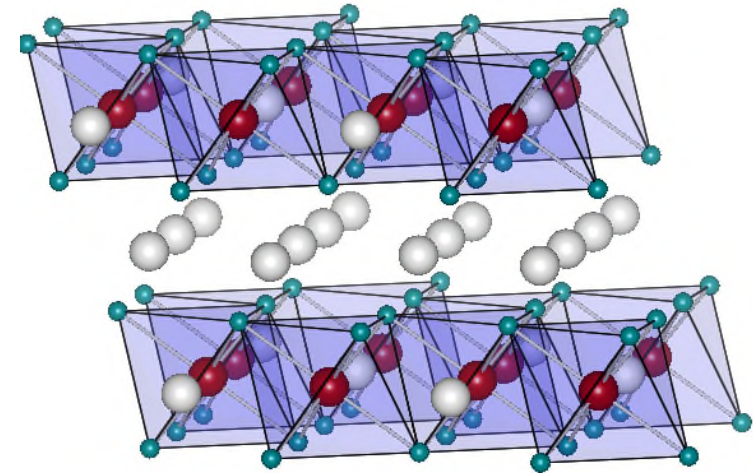
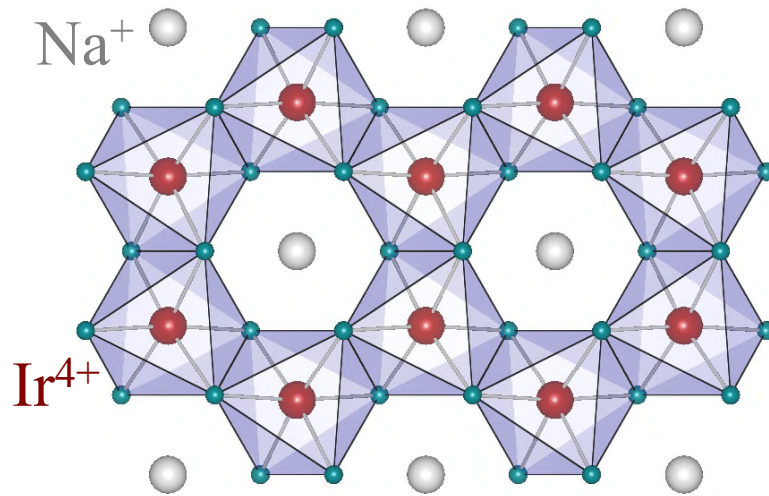


if only y -bonds

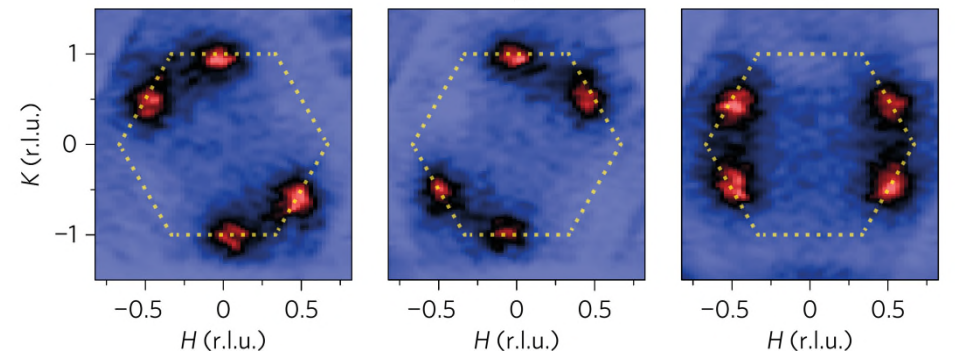
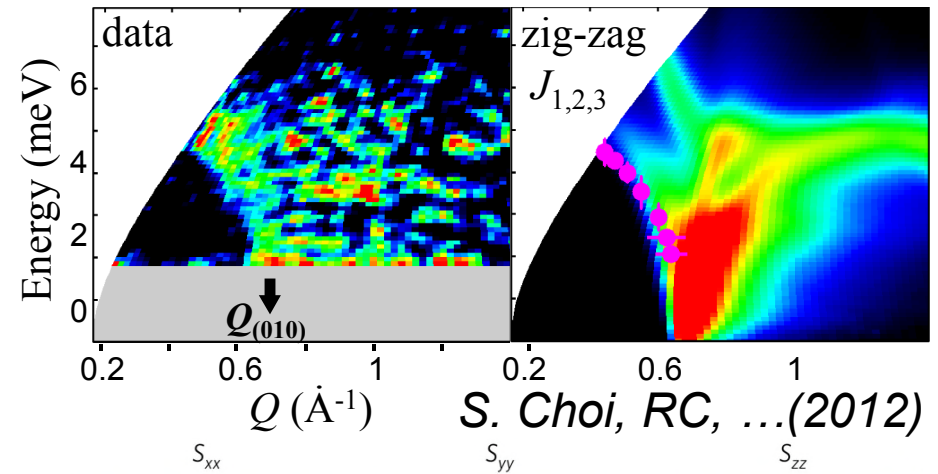
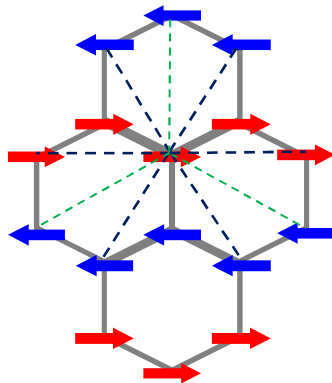


Honeycomb magnet $\alpha\text{-Na}_2\text{IrO}_3$

- edge-shared MO_6 octahedra
- alternating layers of hexagonal Na and honeycomb Na:Ir=1:2 layers

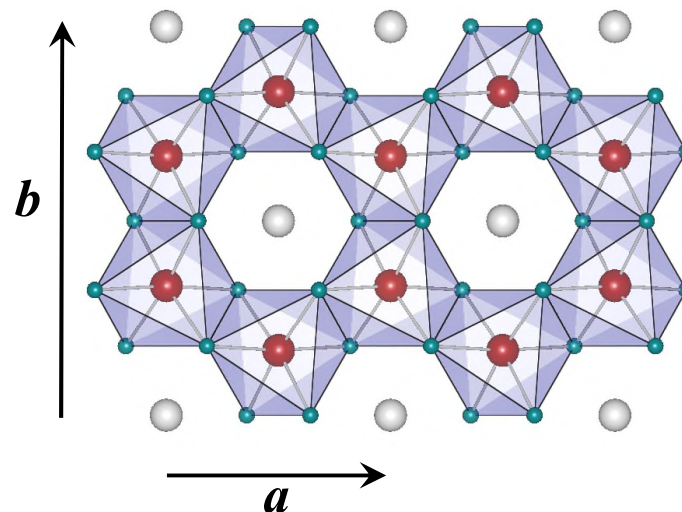
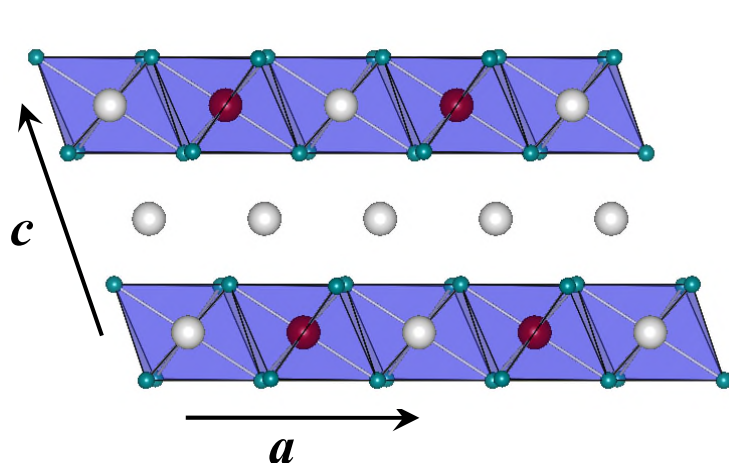


- zig-zag magnetic order



BJ Kim (2015)

$\alpha\text{-Na}_2\text{IrO}_3$ and $\alpha\text{-Li}_2\text{IrO}_3$



$$r(\text{Li}^+) = 0.76 \text{ \AA}$$

$$r(\text{Na}^+) = 1.02 \text{ \AA}$$

$$r(\text{Ir}^{4+}) = 0.625 \text{ \AA}$$

layered honeycomb structure, IrO_6 in planes

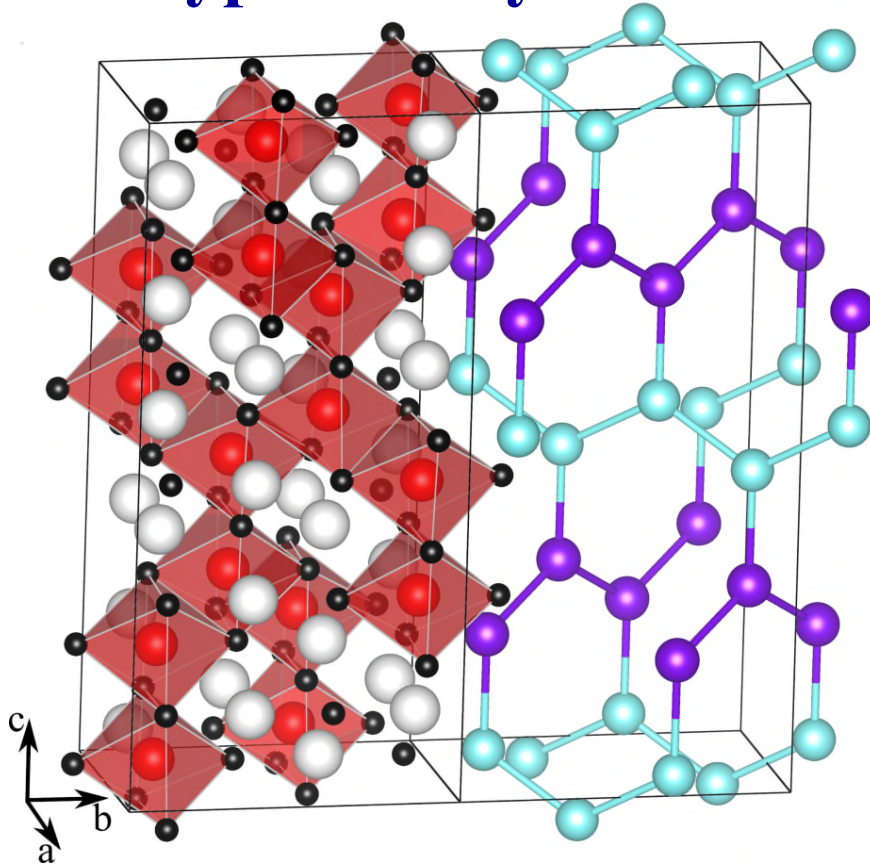
honeycomb Na_2IrO_3 $a=5.427(1) \text{ \AA}$, $b=9.395(1) \text{ \AA}$, $c=5.614(1) \text{ \AA}$

honeycomb Li_2IrO_3 $a=5.1633(2) \text{ \AA}$, $b=8.9294(3) \text{ \AA}$, $c=5.1219(2) \text{ \AA}$

Li^+ small, close to Ir^{4+} , IrO_6 and LiO_6 can more easily interchange

3D polytypes of β - and γ - Li_2IrO_3

hyper-honeycomb



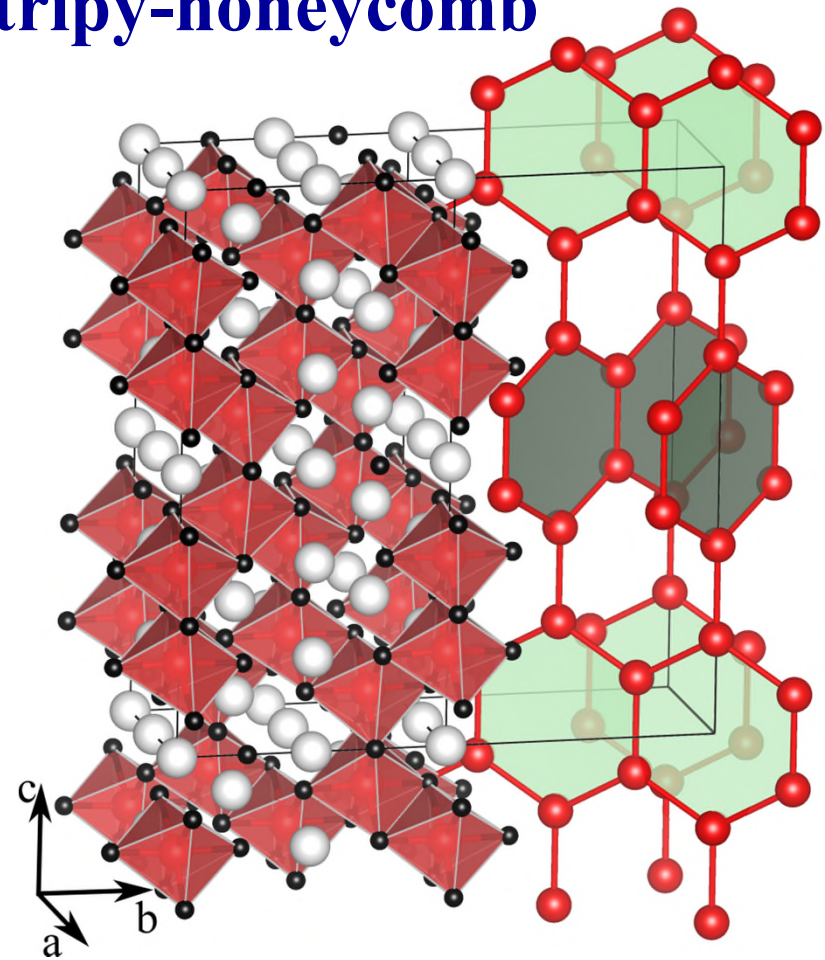
Takayama, ... Takagi,

arXiv:1403.3296

(Na_2PtO_3 structure type)

- edge-shared IrO_6 octahedra
- 3-fold coordination

stripy-honeycomb



Modic, ..., RC... ,Analytis,

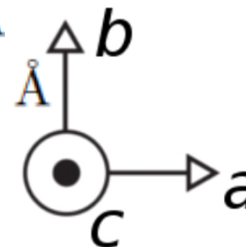
Nature Comm. (2014)

X-ray diffraction from single crystals of γ -Li₂IrO₃

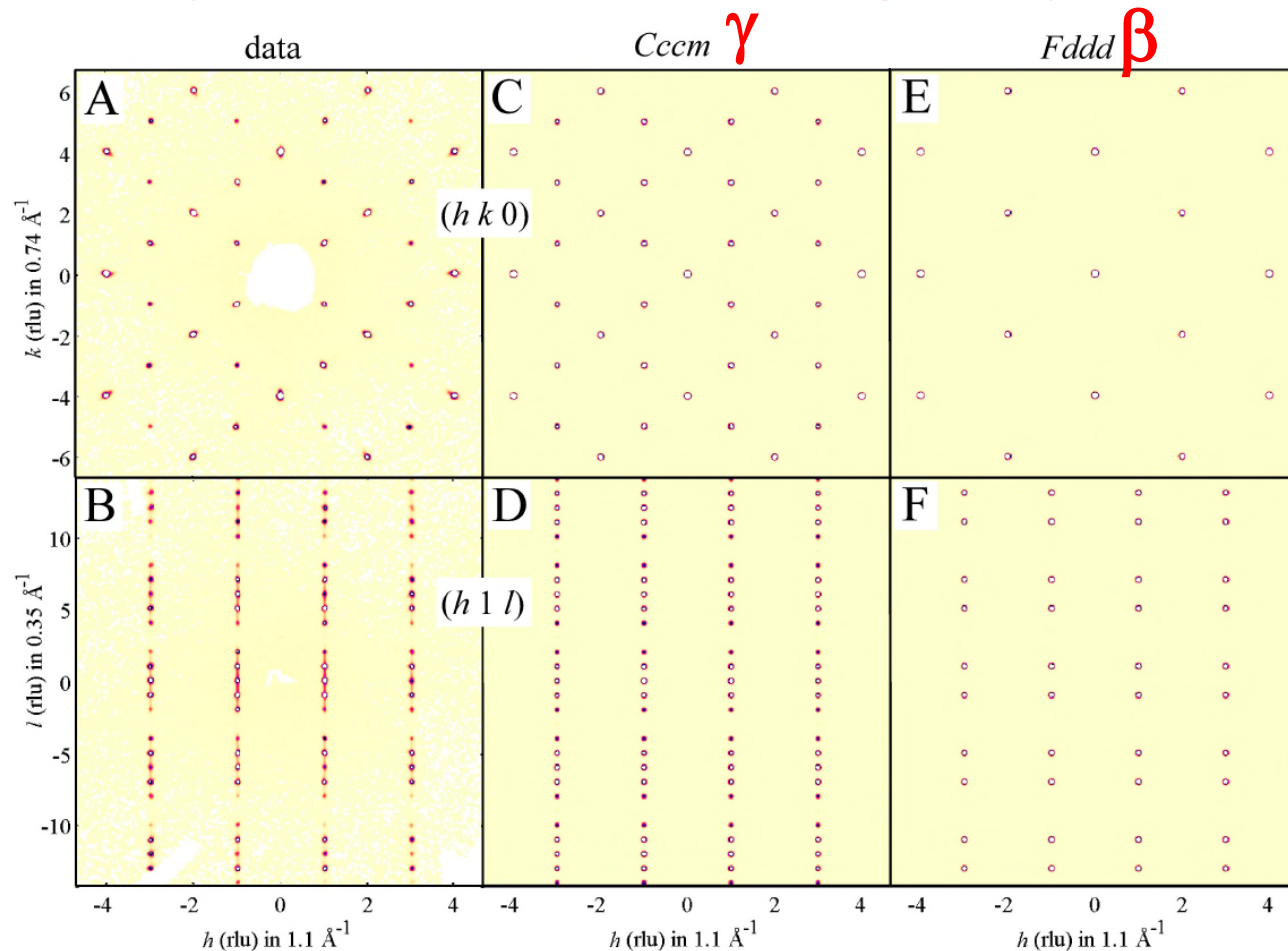
~60 μ m



orthorhombic
 $a = 5.9119(3) \text{ \AA}$,
 $b = 8.4461(5) \text{ \AA}$
 $c = 17.8363(10) \text{ \AA}$

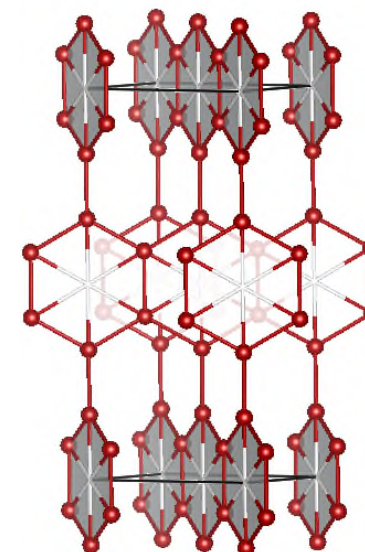


- unit cell volume = 4
 x u.c. volume ($C2/m$)
 $c = 2 b_m$



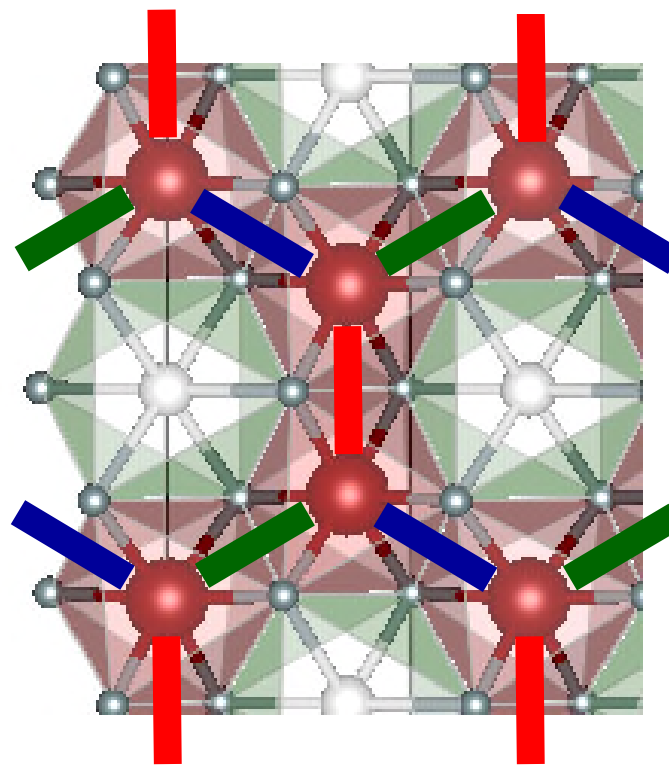
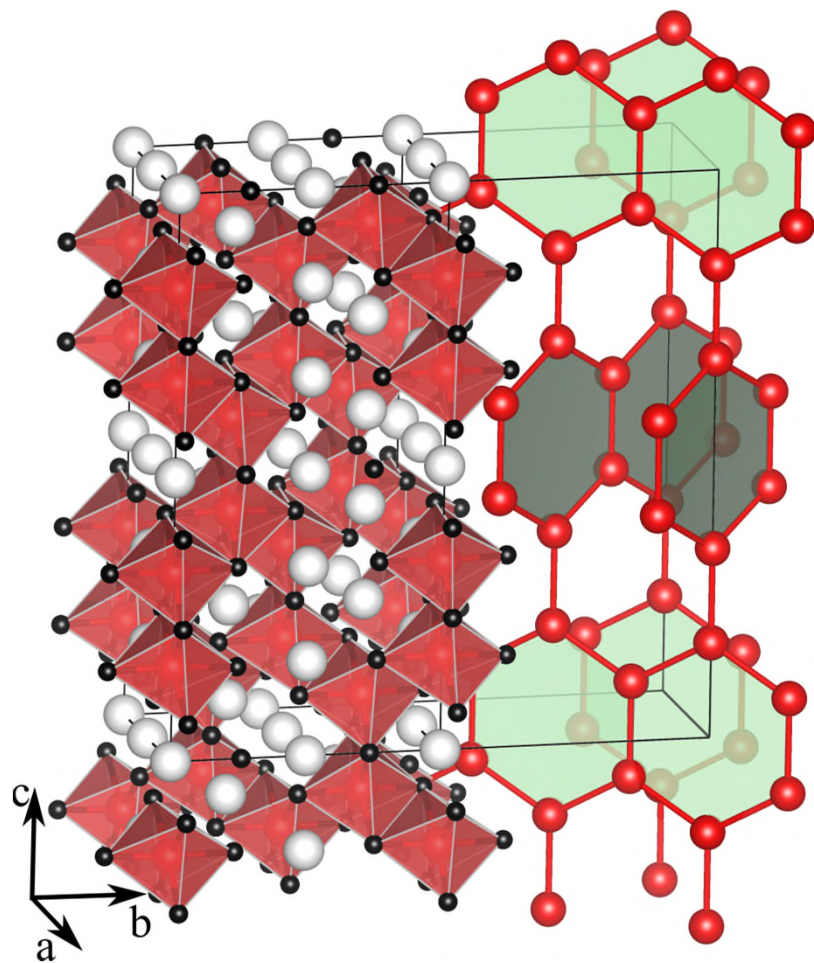
*K.A. Modic et al,
 Nature Comm. (2014)*

- highest-symmetry orth.
 space group that explains
 all diffraction peaks is
 $Cccm$ (#66)



Stripyhoneycomb Kitaev lattice in $\gamma\text{-Li}_2\text{IrO}_3$

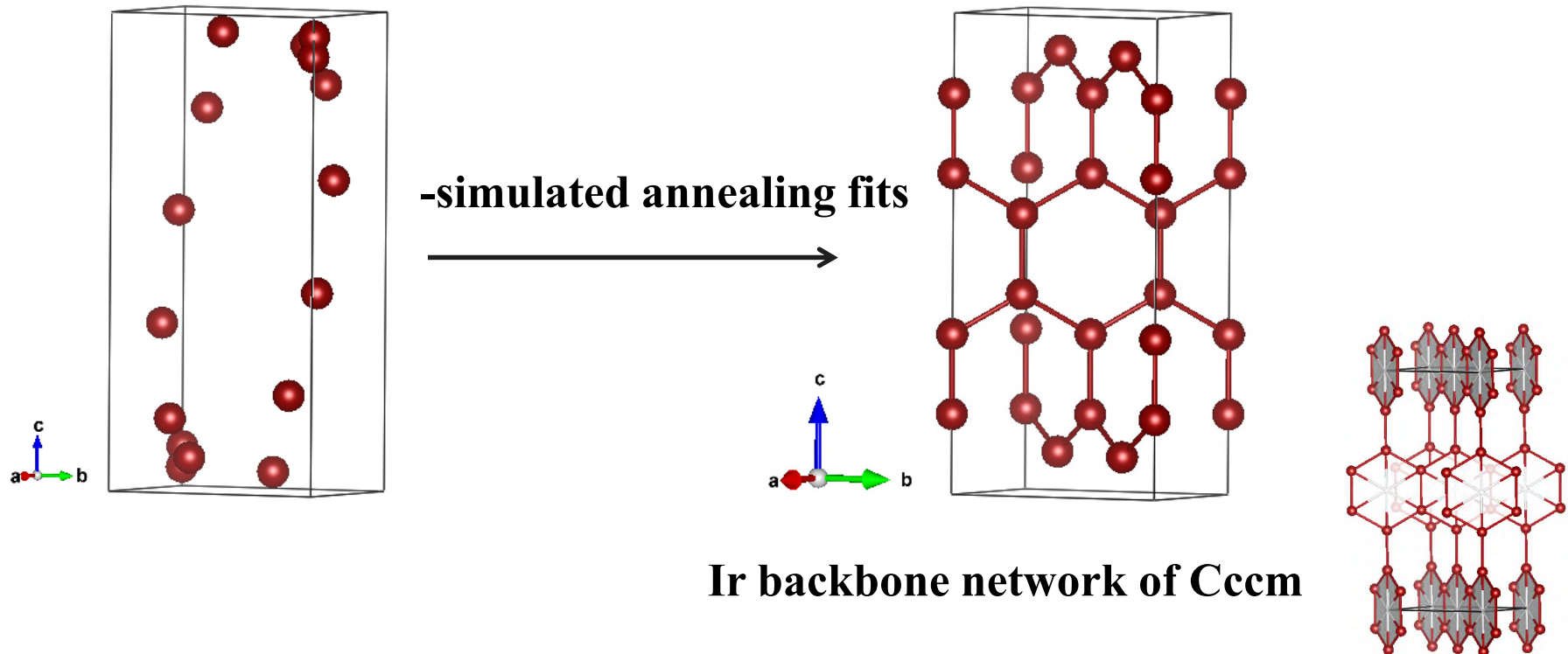
- edge-sharing IrO_6 octahedra
- 3-fold coordination



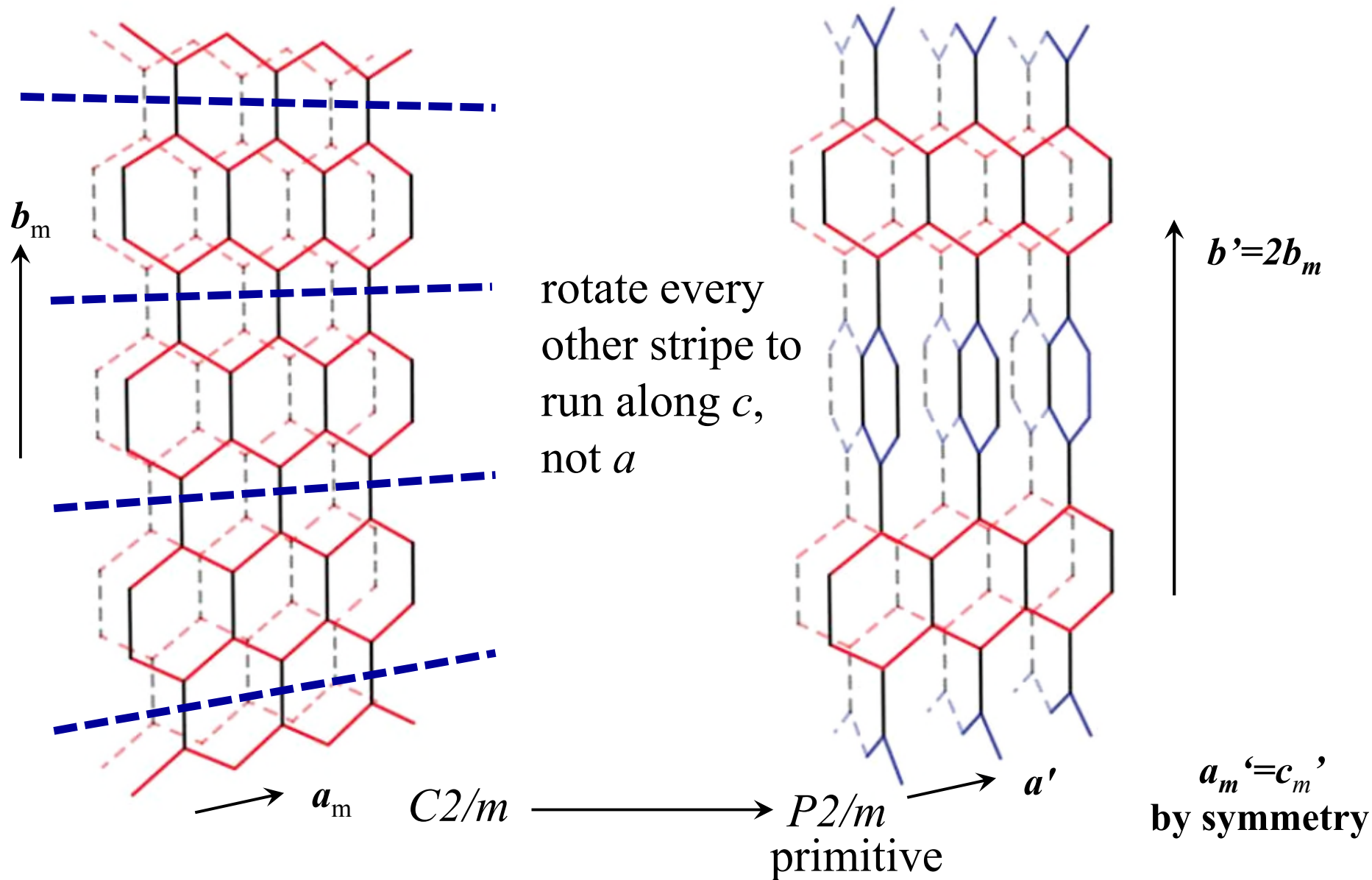
Further tests : simulated annealing fits in $P\bar{1}$

$$a = 5.9119(3) \text{ \AA}, b = 8.4461(5) \text{ \AA}, c = 17.8363(10) \text{ \AA}$$

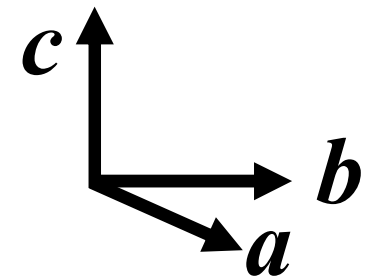
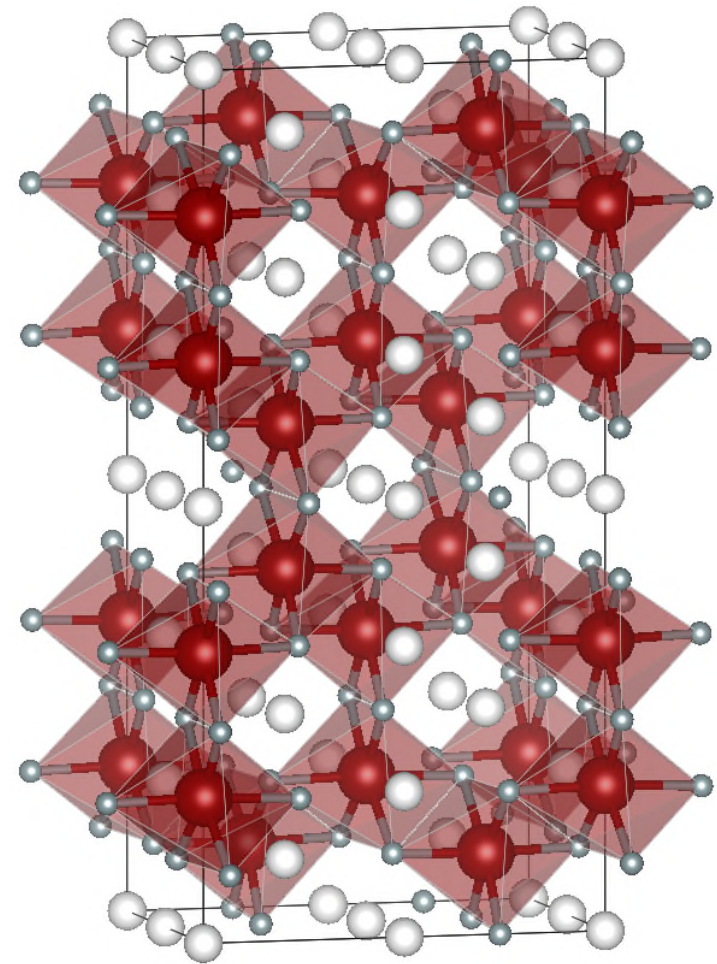
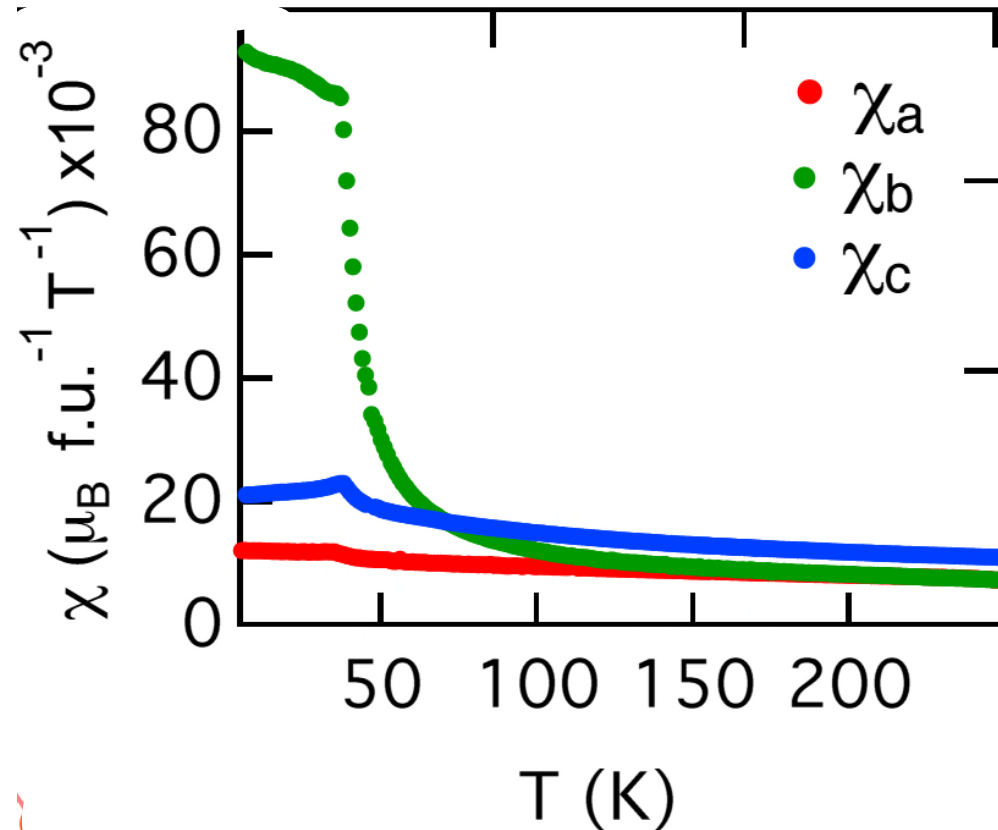
- use orthorhombic $a \times b \times c$ unit cell and assume only inversion symmetry, so $P\bar{1}$
- allow 8 Ir (+ inversion images) to move anywhere in unit cell (simulated annealing fits)
- fit all diffraction peaks (without assuming any symmetry apart from Friedel pair equivalence)



from α to γ - Li_2IrO_3



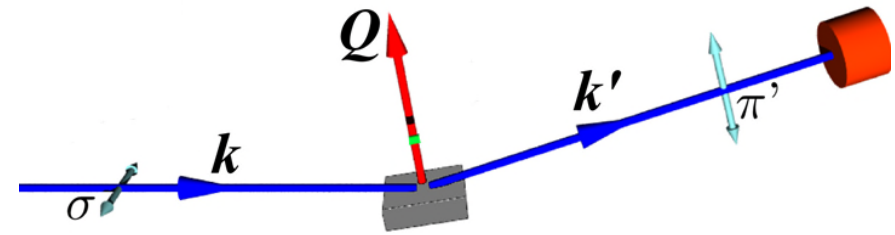
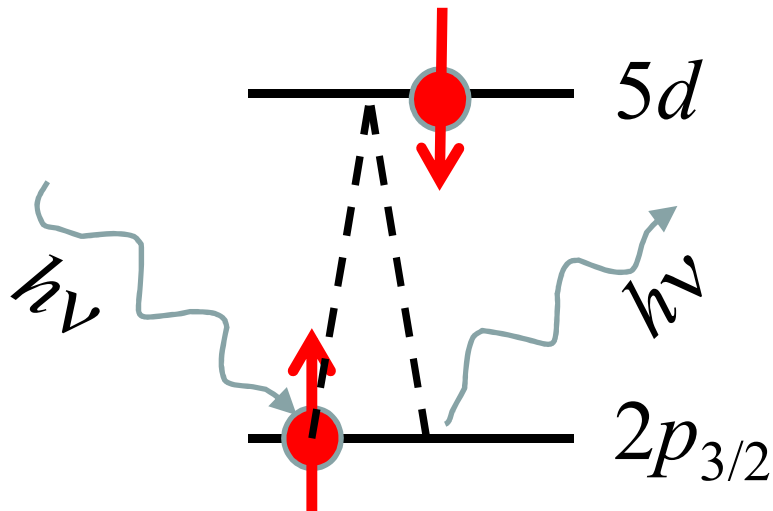
γ -Li₂IrO₃ - anisotropic susceptibility



- strongly anisotropic along a, b, c axes, anisotropy is T-dependent, attributed to anisotropic exchanges

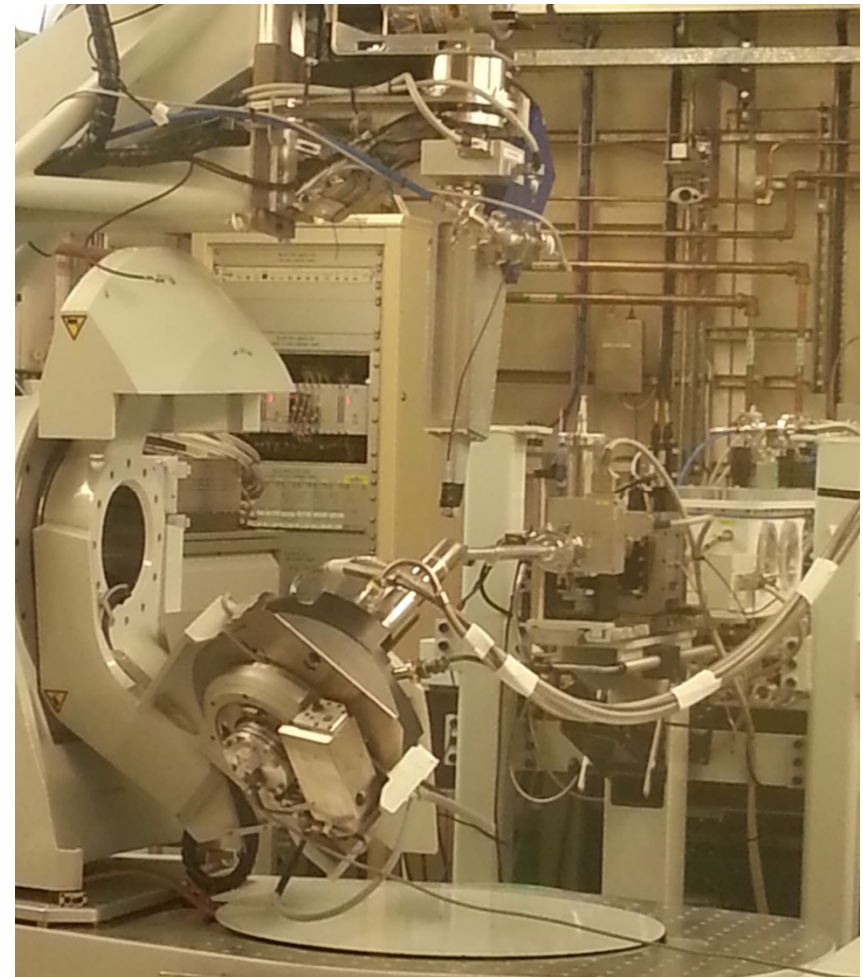
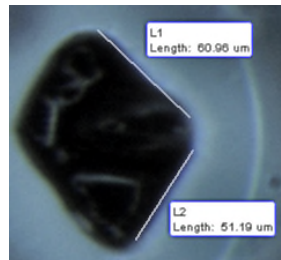
K.A. Modic et al, Nature Comm. (2014)

Magnetic Resonant x-ray diffraction at Ir L₃ edge



- x-ray scattering at resonance
sensitive to magnetism of final
state

$\phi < 60 \mu\text{m}$
 $\gamma\text{-Li}_2\text{IrO}_3$

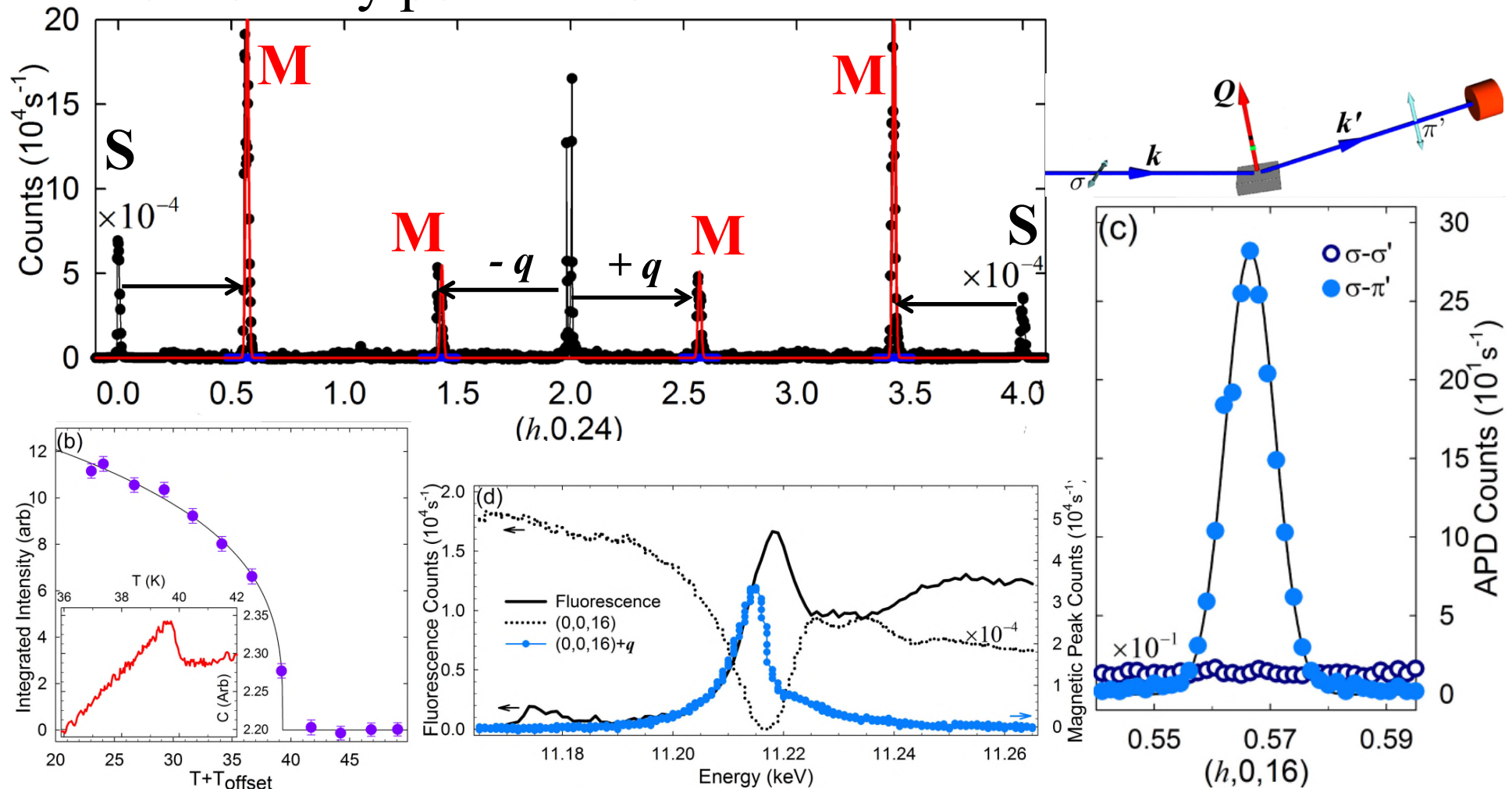


Magnetic Resonant x-ray diffraction on γ -Li₂IrO₃

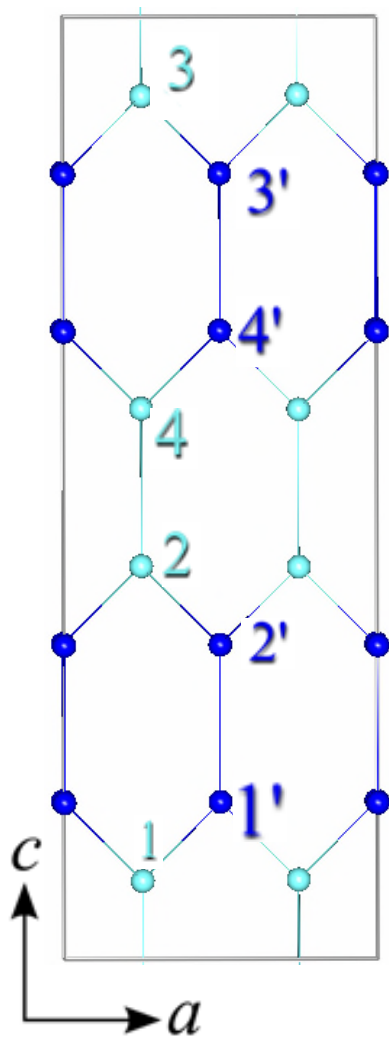
- incommensurate magnetic propagation vector

$$q = (0.57(1), 0, 0)$$

- peaks go away upon heating, appear only at resonance, rotate x-ray polarization



Solving the magnetic structure of γ -Li₂IrO₃



16 Ir sites/unit cell, 2 (independent) Ir sublattices
each 4 sites/primitive cell **1-4** , **1'-4'**

4 types of magnetic basis vectors

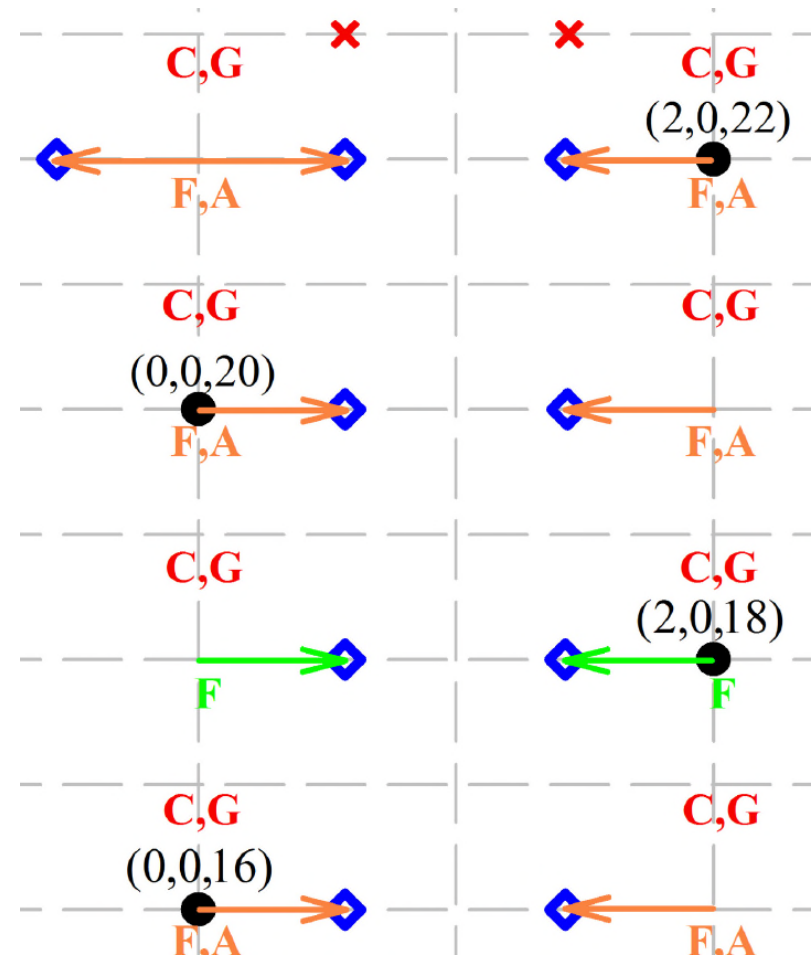
F + + + +

C + + - -

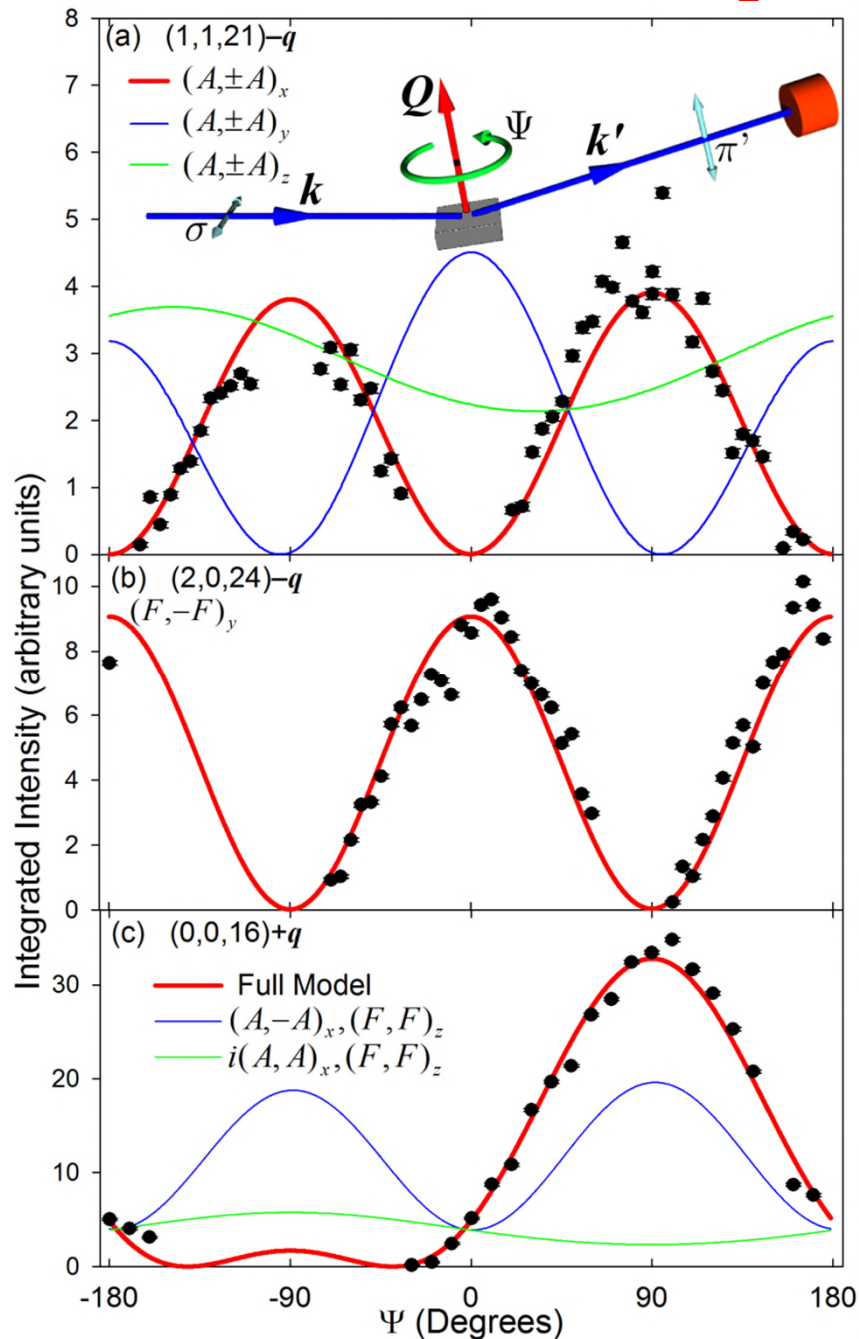
A + - - +

G + - + -

- selection rules identify
F and **A** present



Azimuth scans on γ -Li₂IrO₃



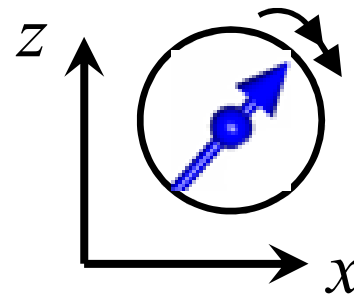
$$I \sim \left| (\hat{\epsilon}' \times \hat{\epsilon}) \cdot \mathcal{F}(Q) \right|^2$$

$$= |\hat{k}' \cdot \mathcal{F}(Q)|^2 = |\mathcal{F}_{\parallel}|^2$$

- projection of structure factor onto scattered beam

$$M_x : M_y : M_z = 0.65(4) : 0.58(1) : 1$$

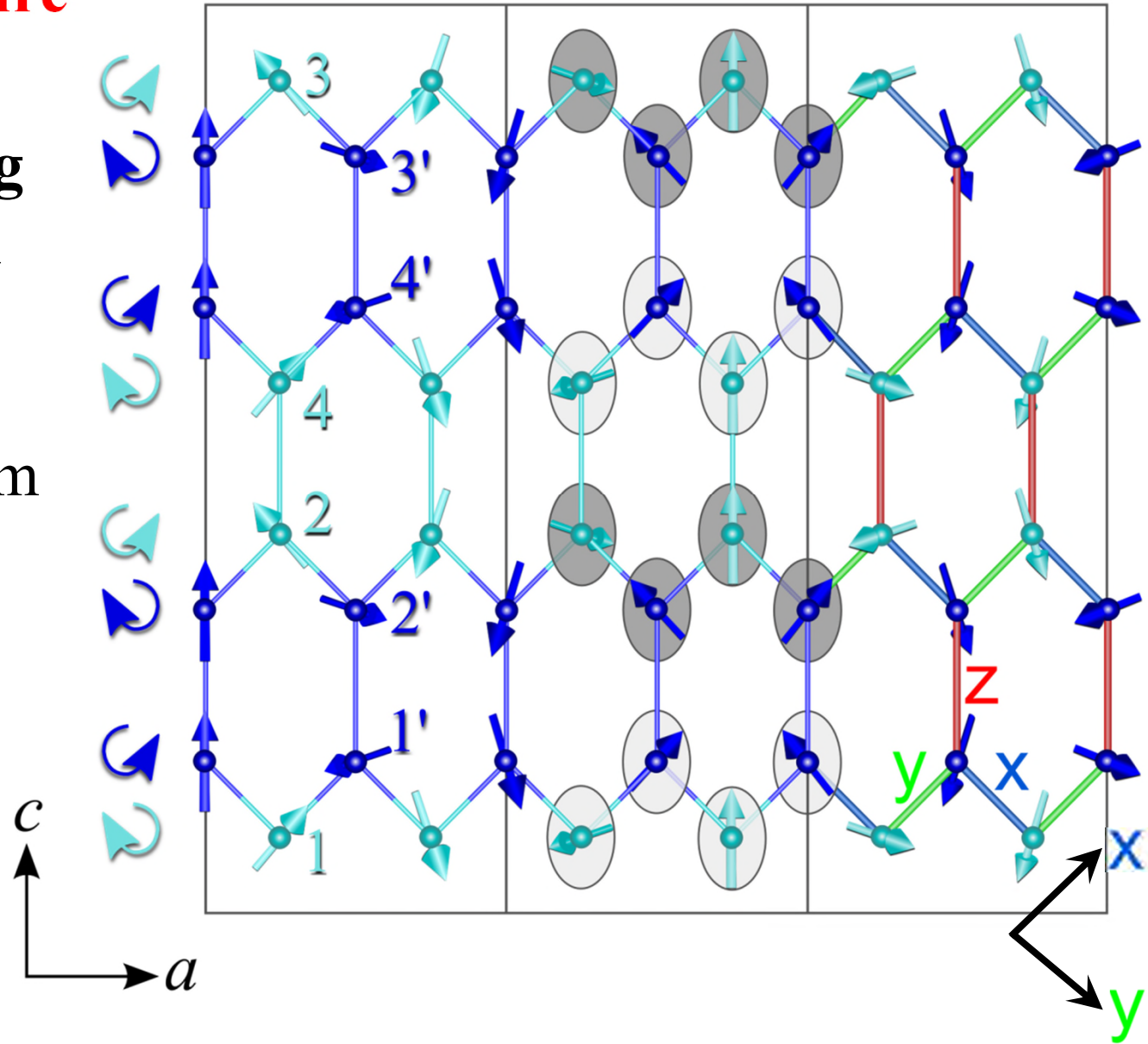
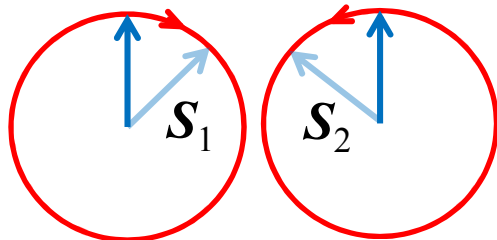
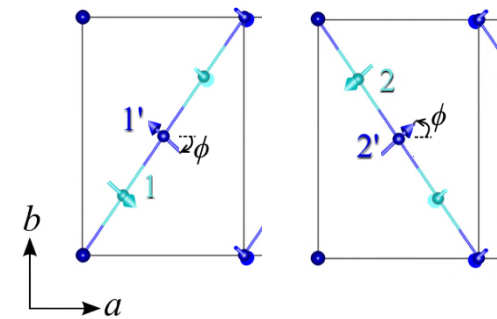
$$i(A, -A)_x, -i(F, -F)_y, (F, F)_z$$



- moments rotate in a plane tilted away from the ac face

Magnetic structure of γ -Li₂IrO₃

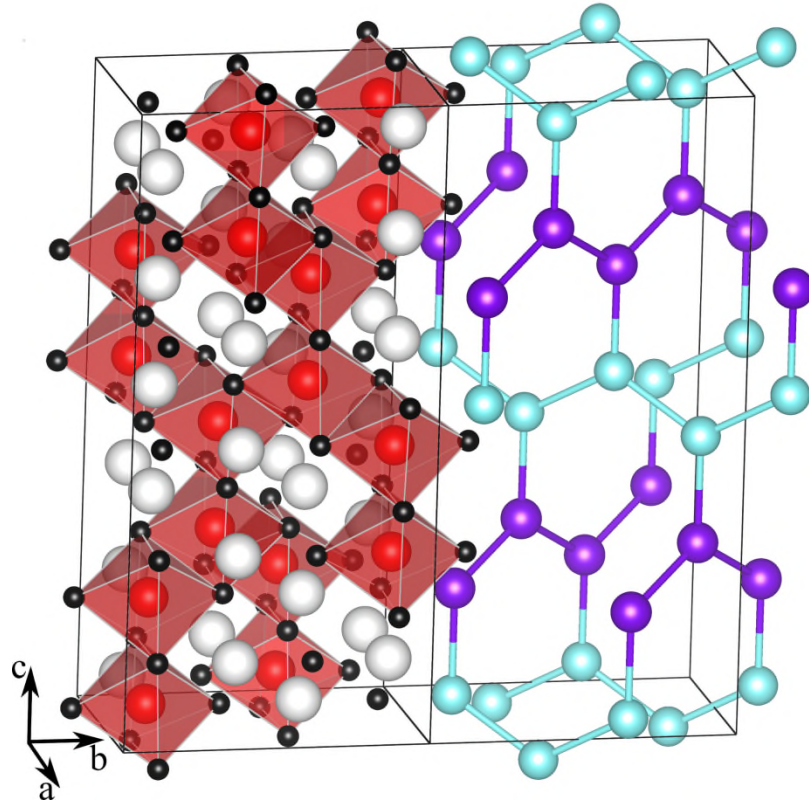
- counter-rotating moments between every nn sites
- non coplanar - alternating tilt from *ac* face



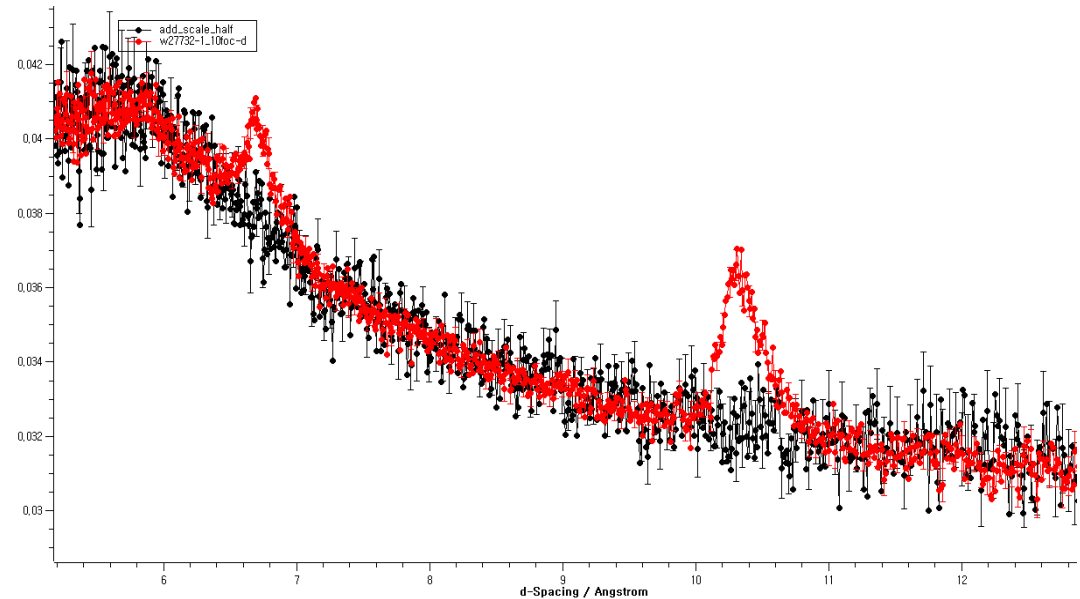
- counter-rotation \rightarrow zero energy gain for nn Heisenberg exchange $J \langle \mathbf{S}_1 \cdot \mathbf{S}_2 \rangle = 0$

Magnetic order in hyper-honeycomb β -Li₂IrO₃

Takayama, ... Takagi,
arXiv:1403.3296



- see magnetic Bragg peaks in powder neutron diffraction

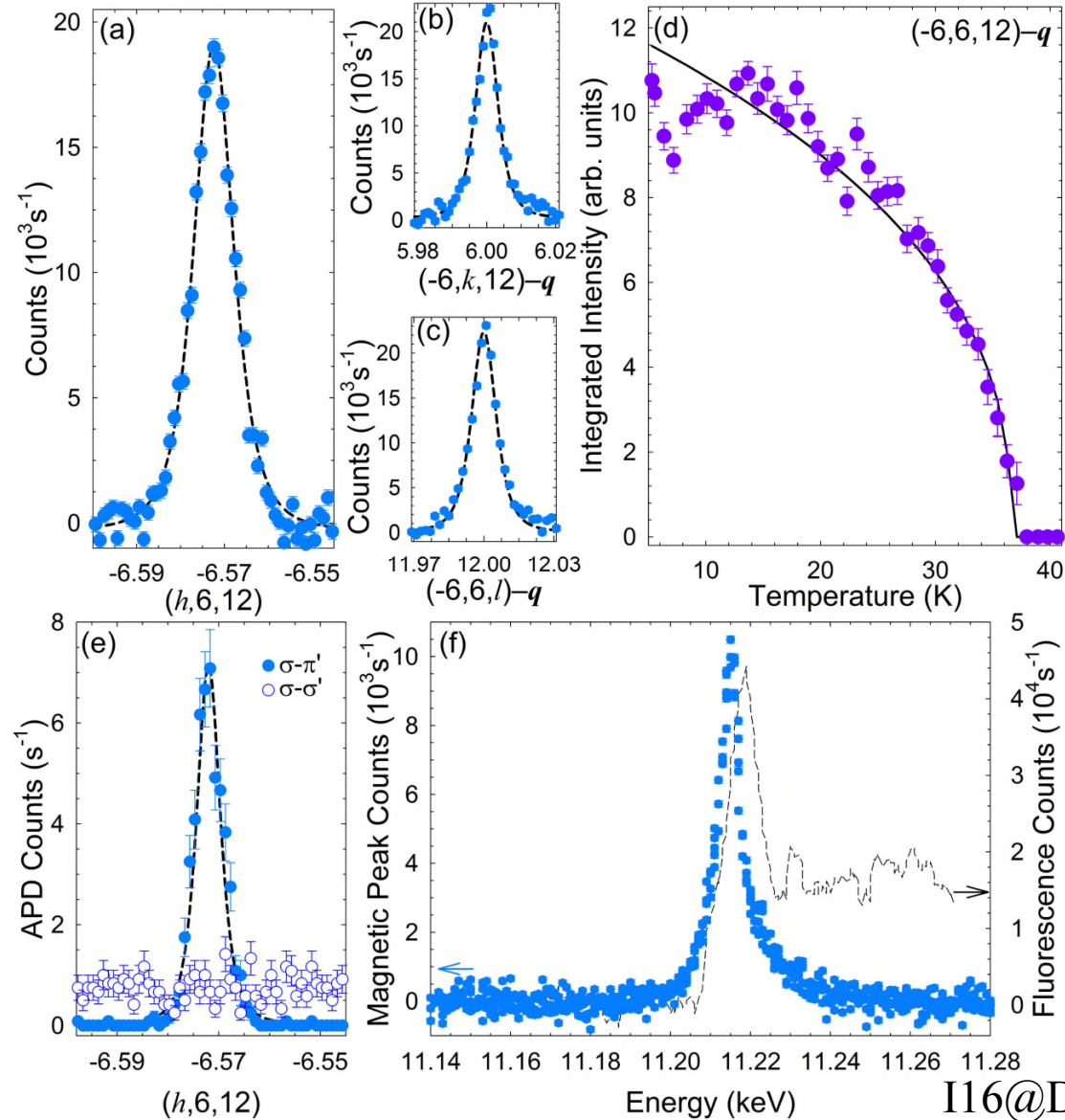
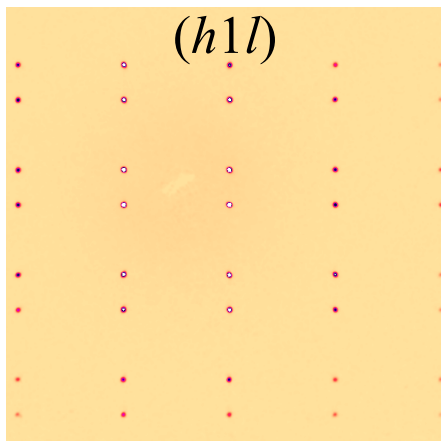
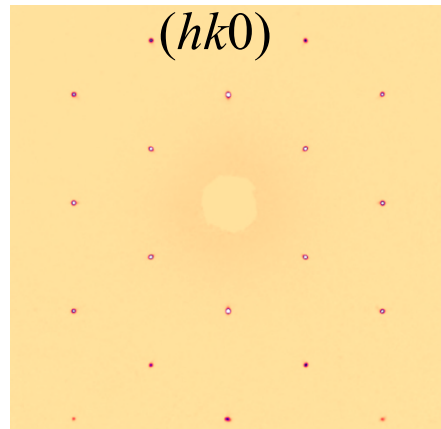


WISH@ISIS

- orthorhombic space group $Fddd$
- susceptibility indicates magnetic order below ~ 38 K

Resonant magnetic x-ray diffraction on a single-crystal of $\beta\text{-Li}_2\text{IrO}_3$

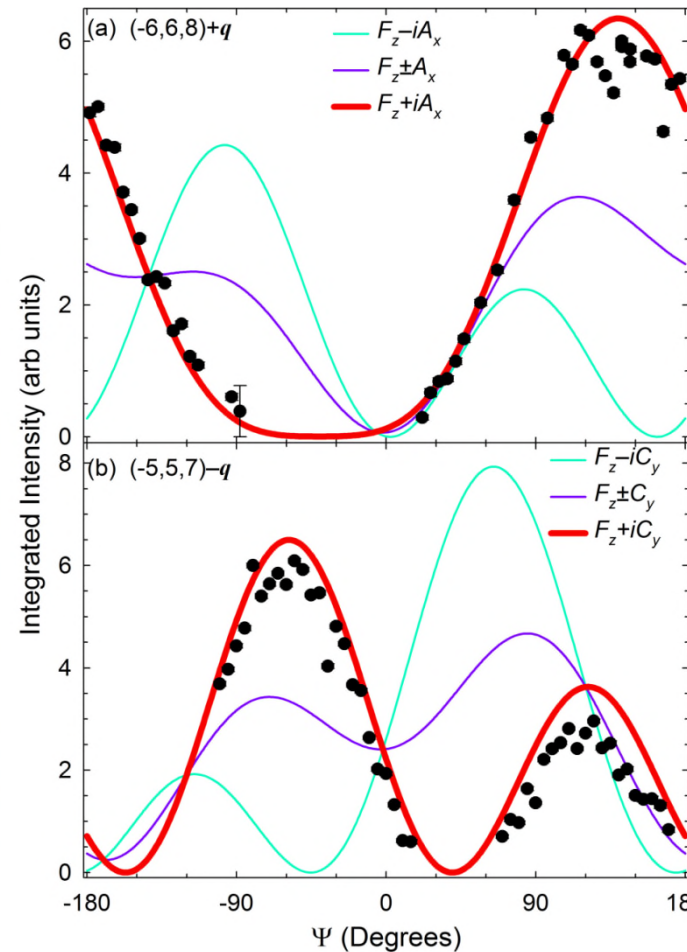
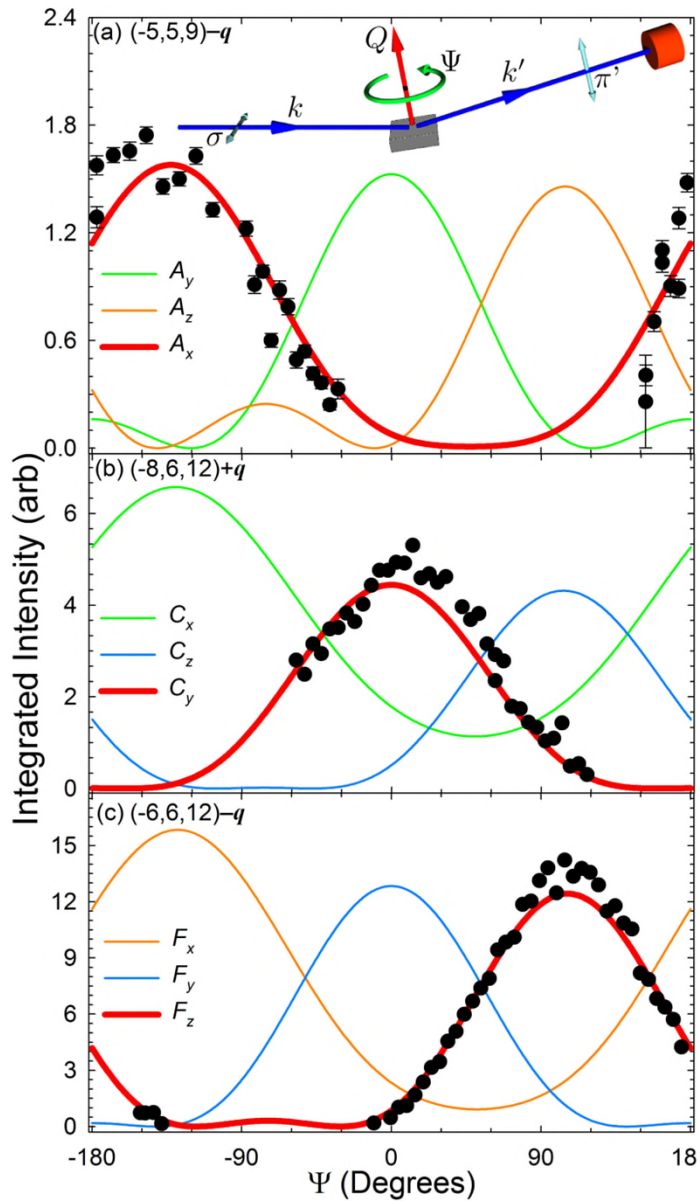
diameter $< 17 \mu\text{m}$



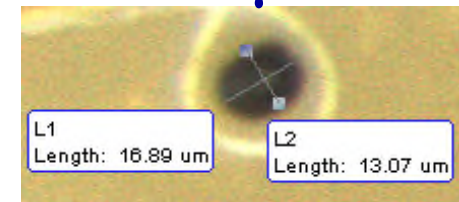
I16@Diamond
 - “same” magnetic propagation vector as in $\gamma\text{-Li}_2\text{IrO}_3$ (within experimental accuracy)

β -Li₂IrO₃ azimuth scans: complete magnetic structure

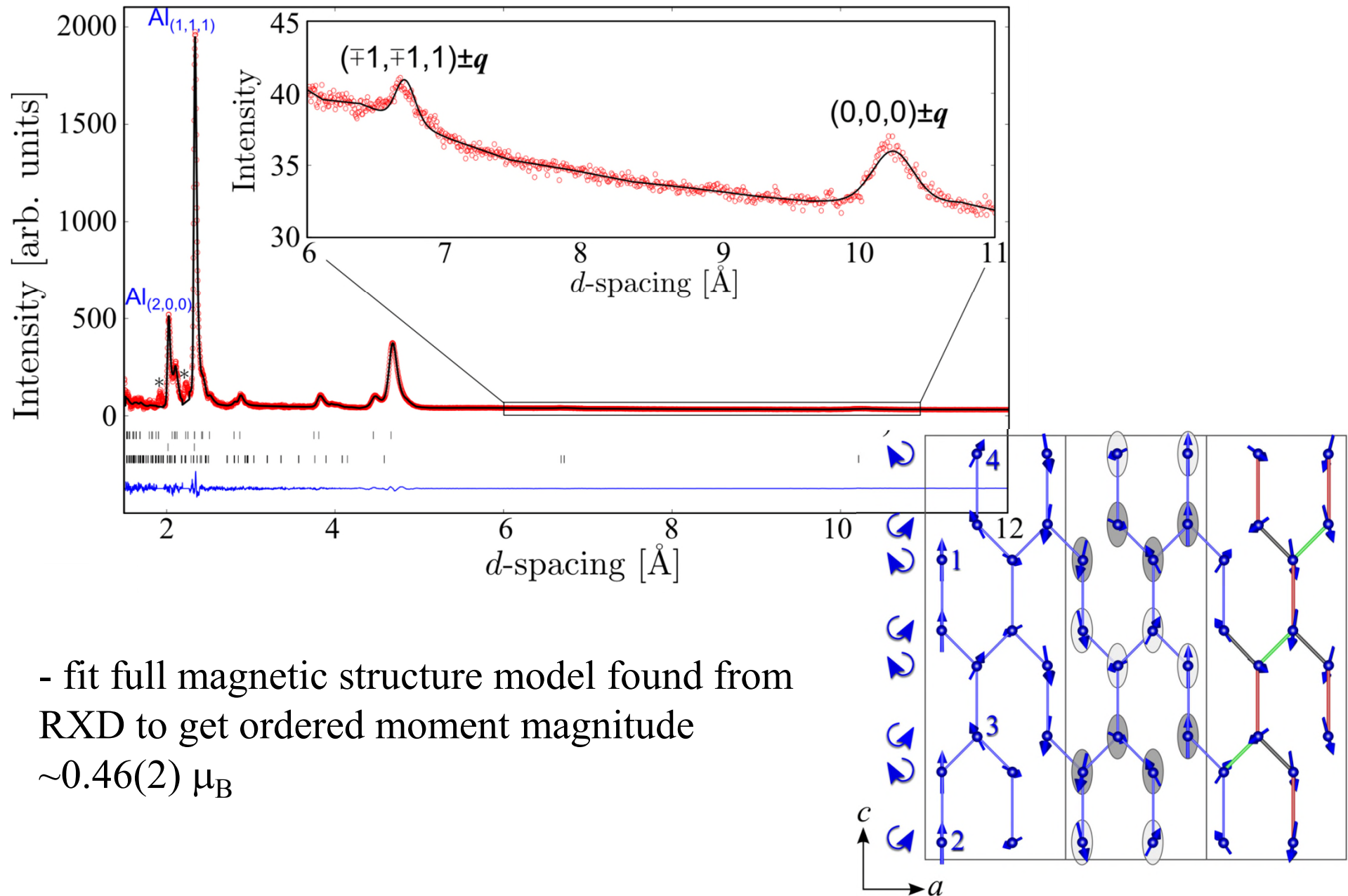
one Ir sublattice, 4 sites/primitive
 (iA_x, iC_y, F_z) single irrep
 $M_x : M_y : M_z = 0.45(1) : 0.65(1) : 1$



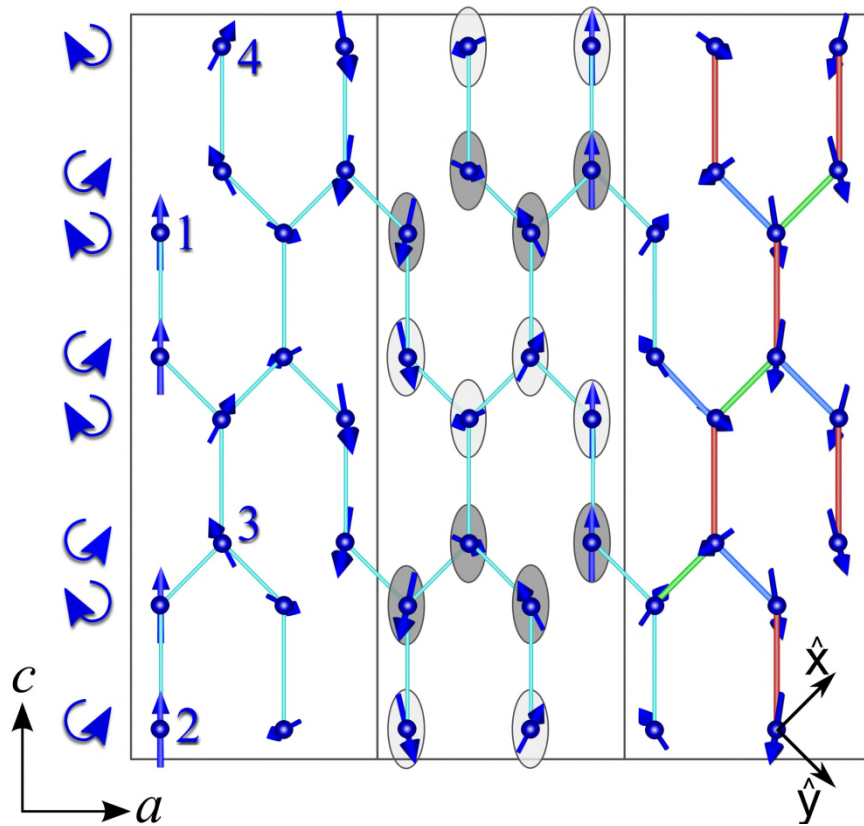
$< 17 \mu\text{m}$



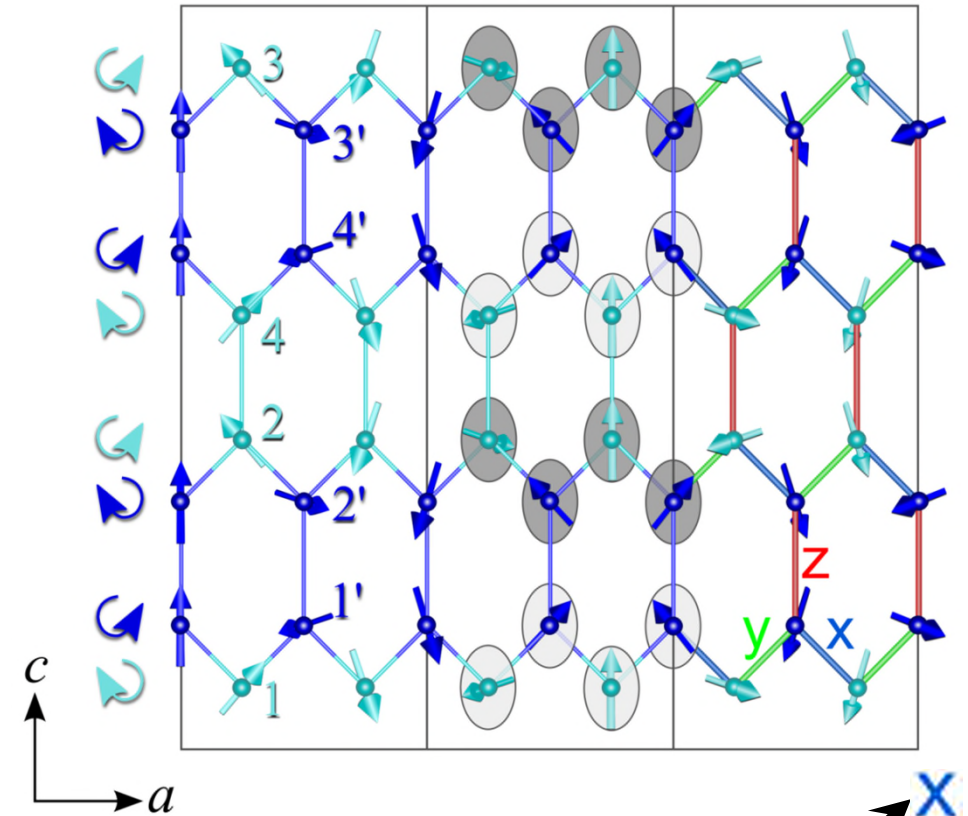
Powder neutron diffraction in $\beta\text{-Li}_2\text{IrO}_3$



β -Li₂IrO₃ magnetic structure



γ -Li₂IrO₃



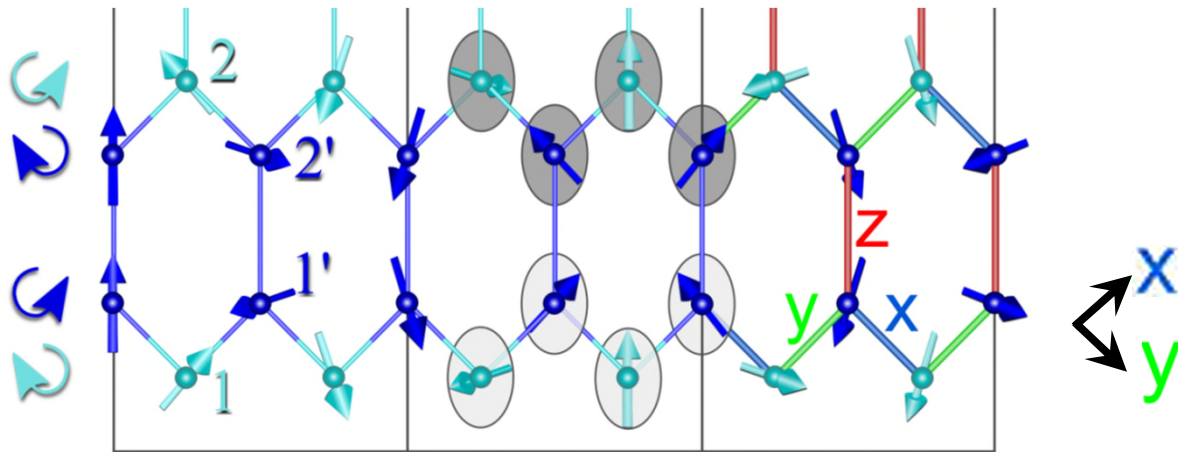
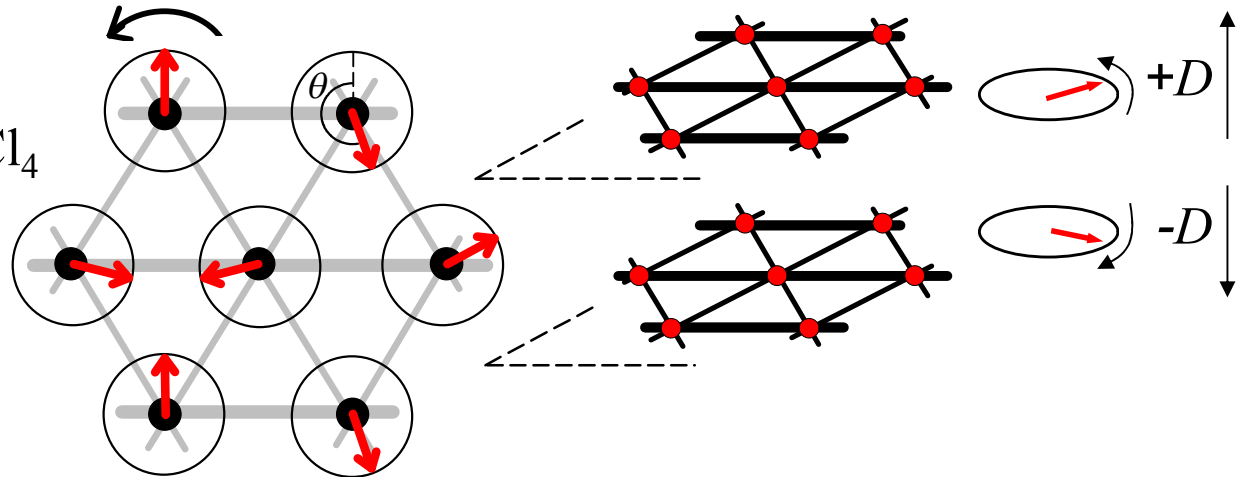
- same \mathbf{q} -vector, counter-rotating moments, alternating planes of rotation along vertical bonds
- only difference is b -axis position of sites
- **counter-rotation + non-coplanarity** difficult to explained by Heisenberg couplings

Counter-rotation of moments

- for dominant Heisenberg exchanges multi-sublattice spiral orders can counter-rotate, but on the weakest bonds, and co-rotate on the strongest bonds

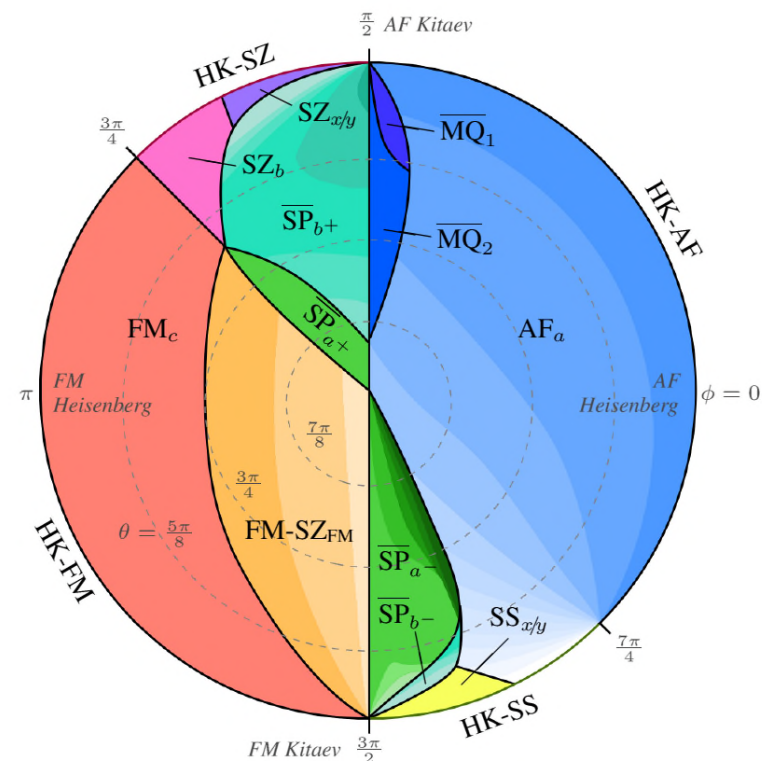
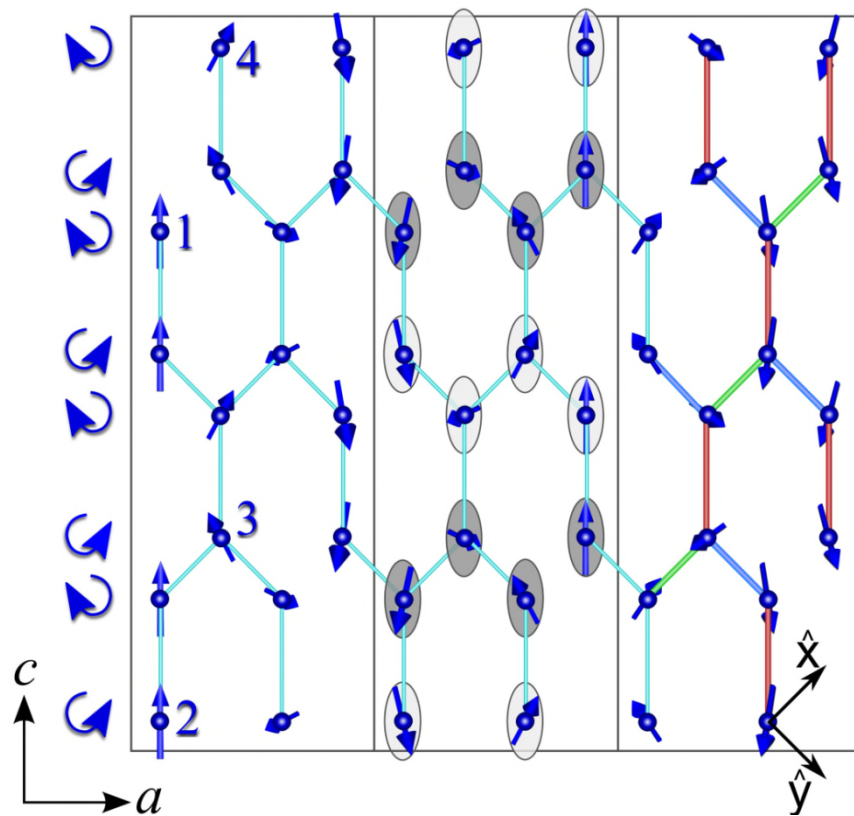
quasi-2D Heisenberg Cs_2CuCl_4

$J_{\text{interlayer}}, D \sim 0.05 J$
R.C. et al (1997,2001)



- counter-rotation on every nn bond
- along x-bonds when spins along x then \sim FM, when along y then \sim AFM
 \Rightarrow favoured by a FM Kitaev and AFM HB J

Perturbations around FM Kitaev limit: JKG model

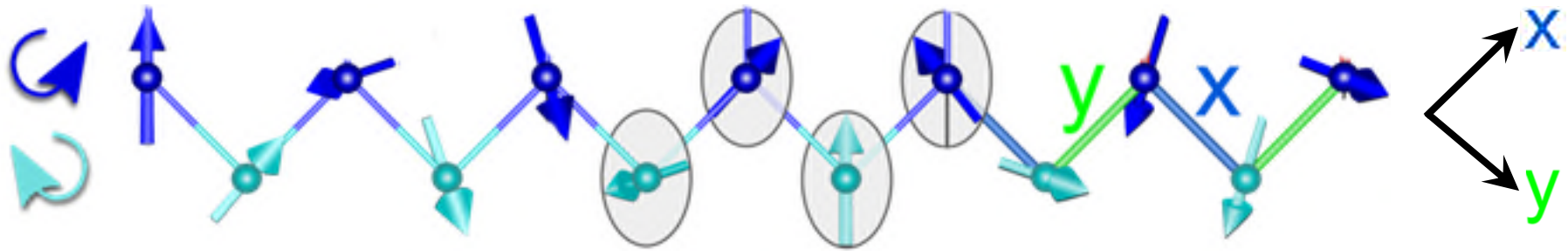


J K Γ model : FM Kitaev K
 small AFM Heisenberg $J \mathbf{S}_i \cdot \mathbf{S}_j$
 small $\Gamma (S^x S^y + S^y S^x)$ for *all* bonds

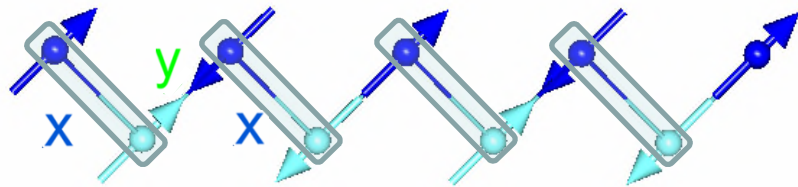
β -phase (yes) and γ (almost, not coplanarity pattern)

E.K-H. Lee ... Y.B. Kim PRB (2015), arXiv (2015).

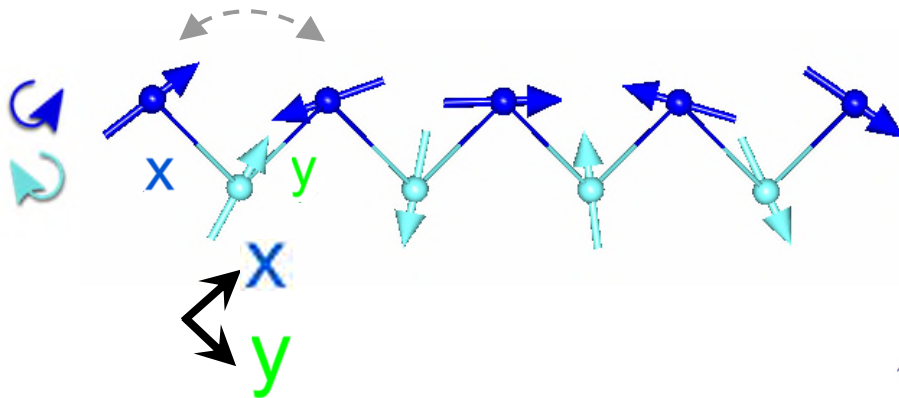
Minimal model: Kitaev zig-zag chain



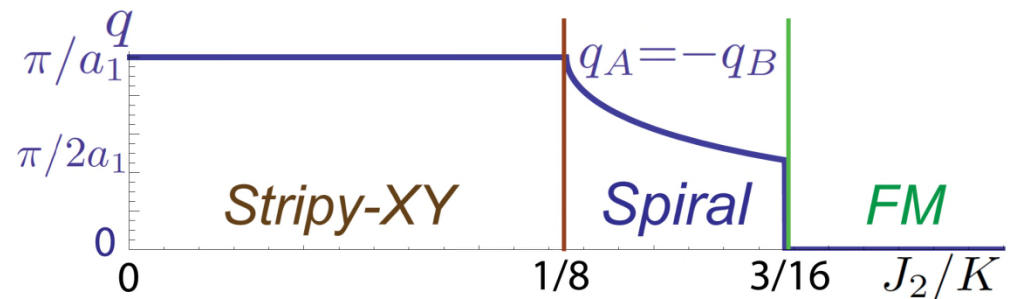
rotating version of “stripy” order



FM Kitaev K
+ small AF Heisenberg J

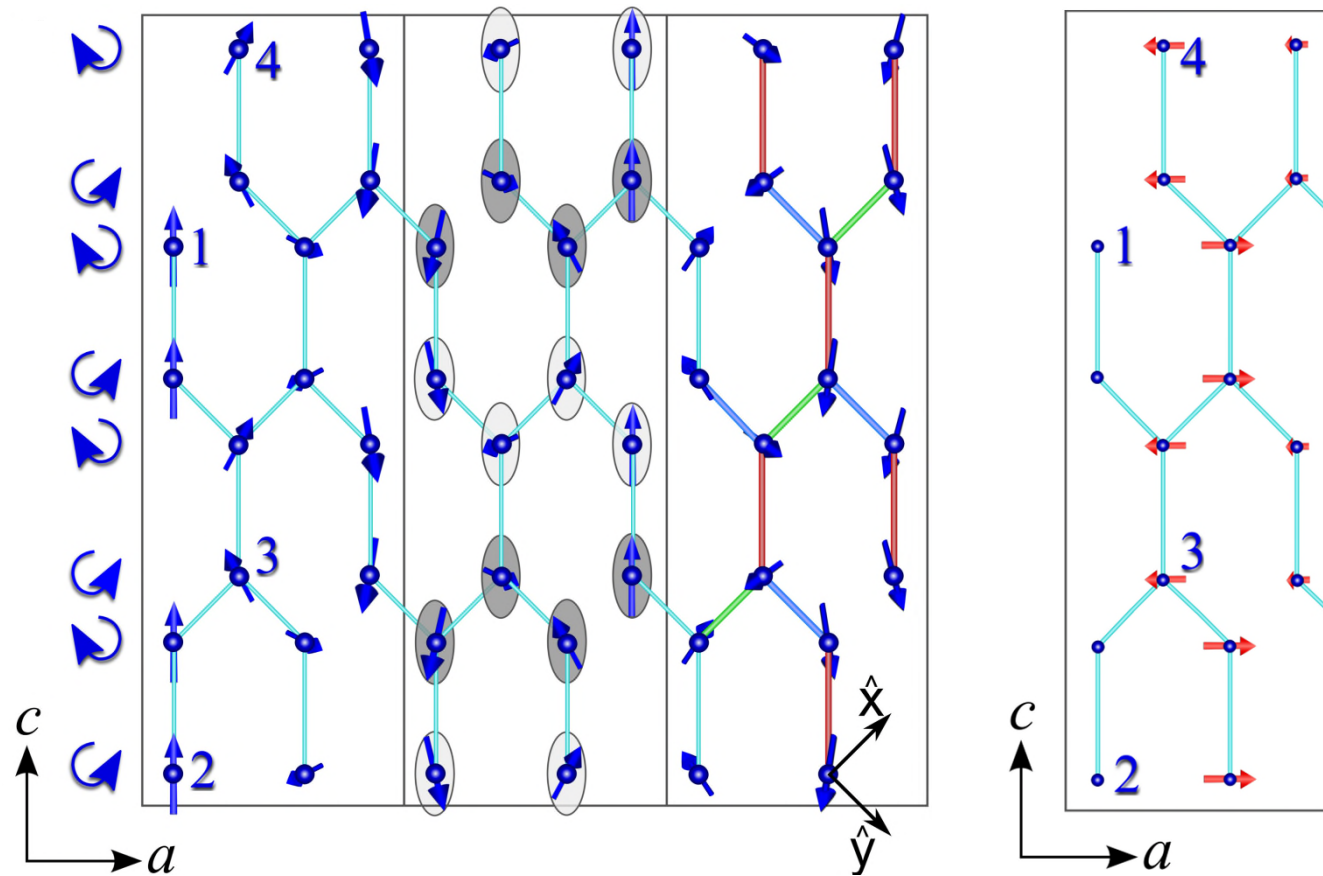


frustrate with small FM J_2



Itamar Kimchi, R.C, A.Vishwanath,
arXiv (2014) PRB(2015)

Non-coplanarity due to Kitaev couplings along c-bonds

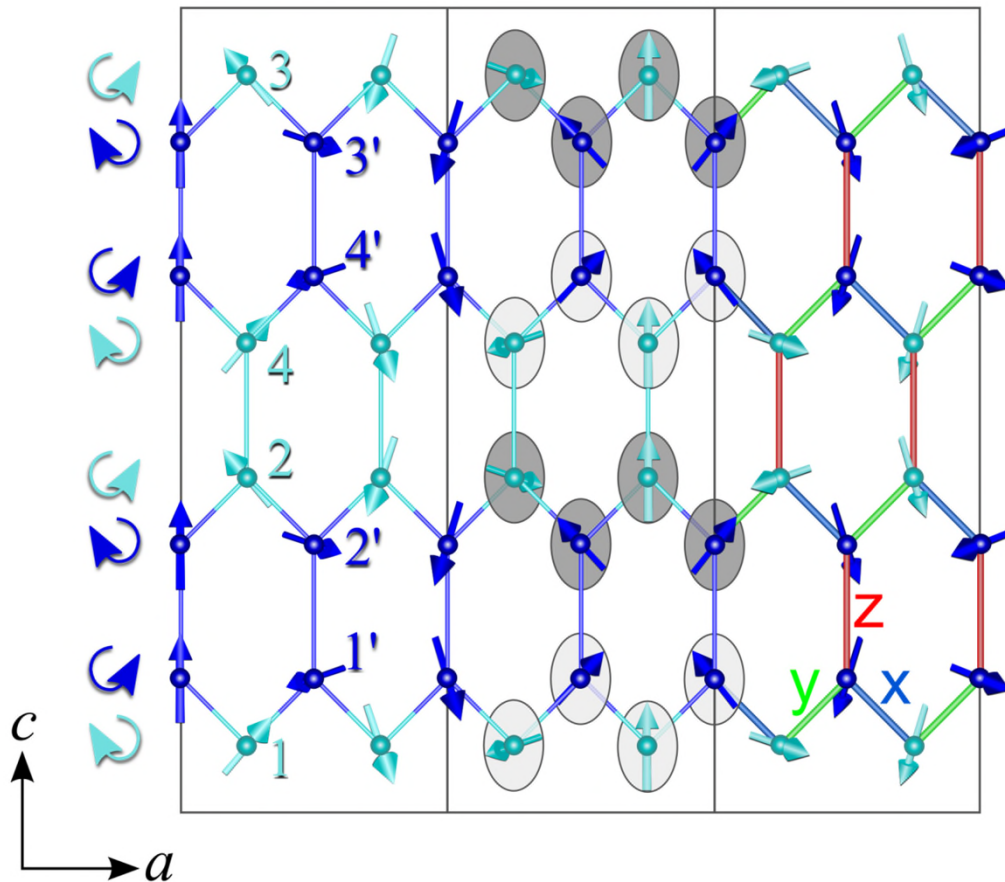
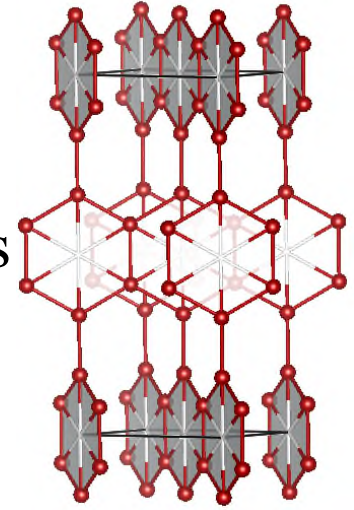


- non-coplanar along each vertical bond, FM aligned $S^b = S^z$ for all c -bonds
- full structure captured (soft spin approach) by FM Kitaev K + small AFM J + small Ising I_c in *both* β and γ polytypes

Itamar Kimchi, R.C, A.Vishwanath, arXiv (2014) PRB(2015)

Summary

- solved crystal structure of new polytype γ - Li_2IrO_3
- β - and γ - Li_2IrO_3 have non-coplanar counter-rotating spirals



- structure stabilized by dominant Kitaev terms + small interactions

A. Biffin, R.D. Johnson, ...R.C. PRL, PRB (2014)