

Discontinuous Shear Thickening fluids: Shear-induced system spanning structures

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Discontinuous Shear Thickening (DST) fluids

suspension of cornstarch in water



- Problem: why does shear lead to solid-like properties in DST fluids?
- ➔ a transiently jammed region develops in response to shear and supports a load when it spans between solid boundaries

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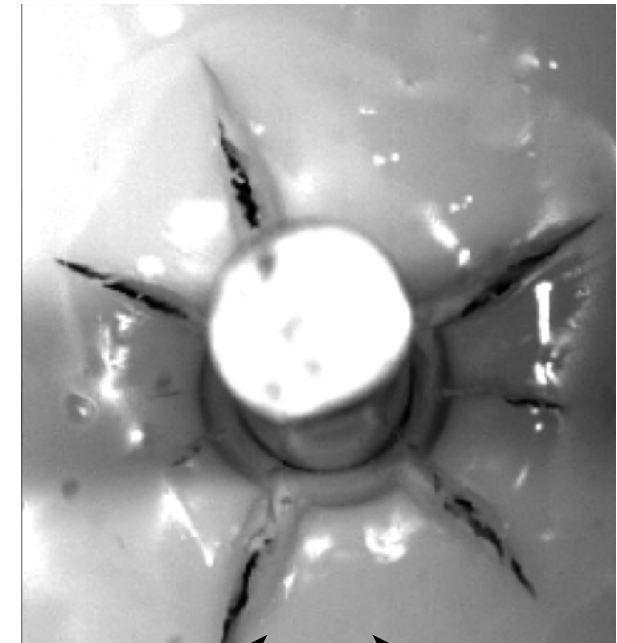
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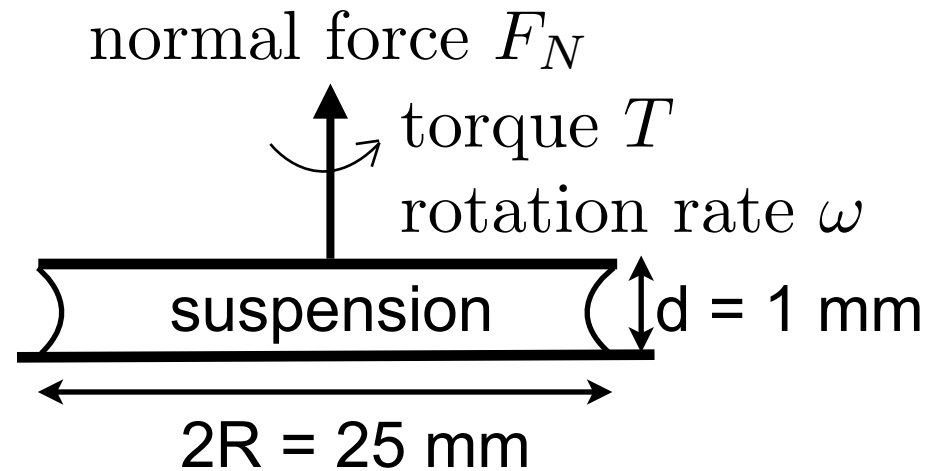
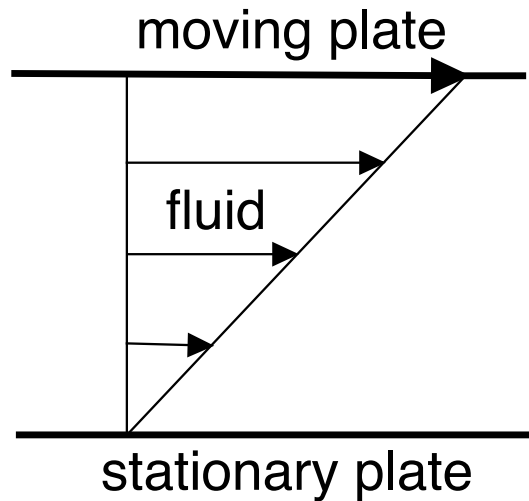


1 cm

• Roche et al. PRL 2013

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steady state rheology measurements:



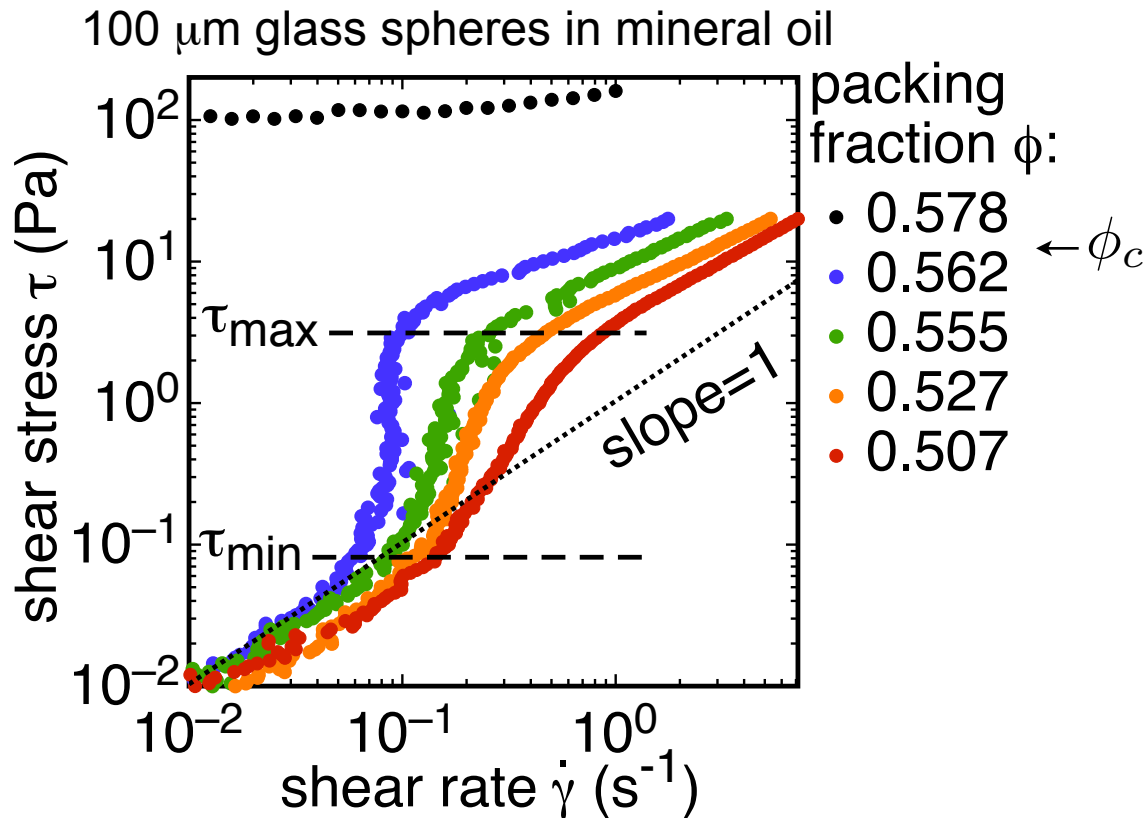
shear rate $\dot{\gamma} = \omega R/d$ (average velocity gradient)

shear stress $\tau = 2T/\pi R^3$ (average shear force/area)

viscosity $\eta = \tau/\dot{\gamma}$

viscosity is a measure of globally averaged energy
dissipation rate in steady state flow

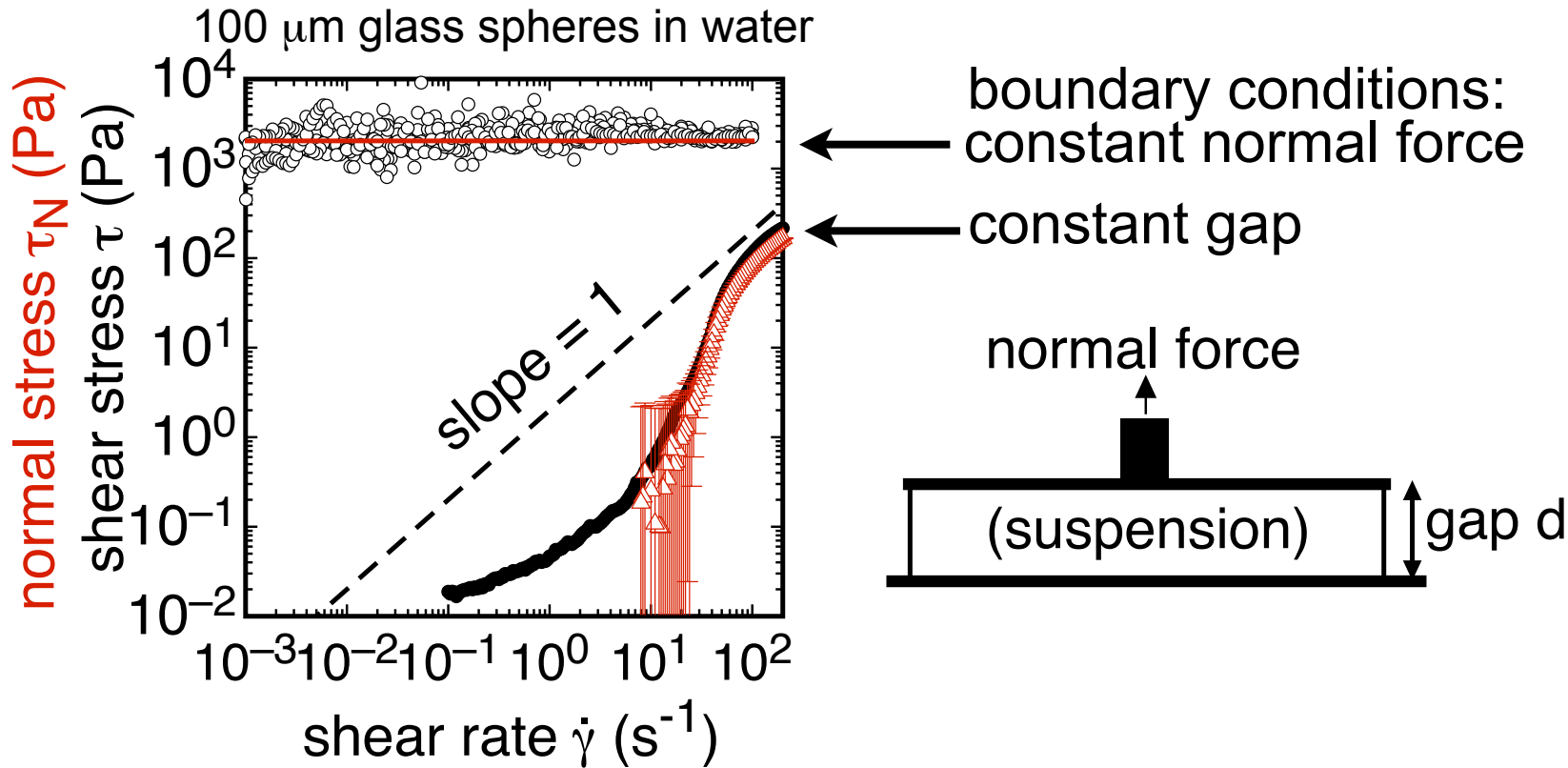
Discontinuous Shear Thickening



- slope diverges as second order phase transition
 - critical point ϕ_c is the jamming transition [Brown & Jaeger, PRL 2009]
- occurs generally in sufficiently concentrated suspensions of hard, frictional, non-attractive particles

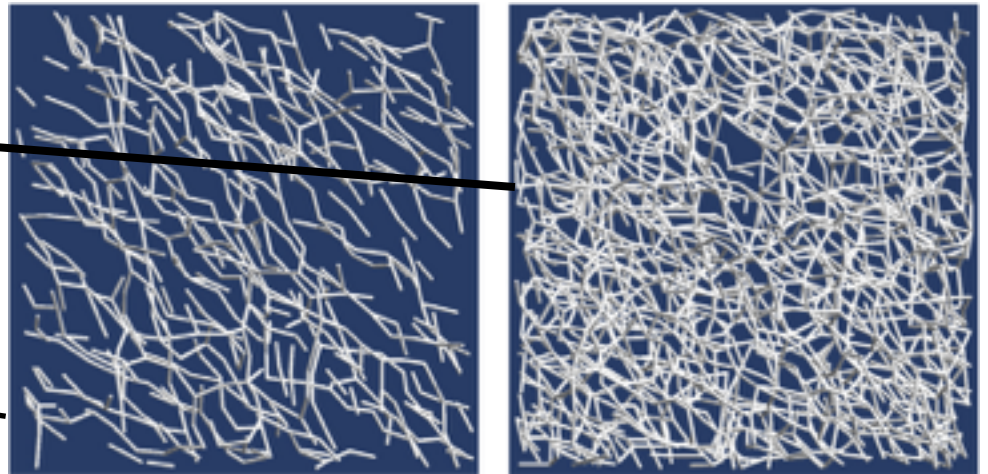
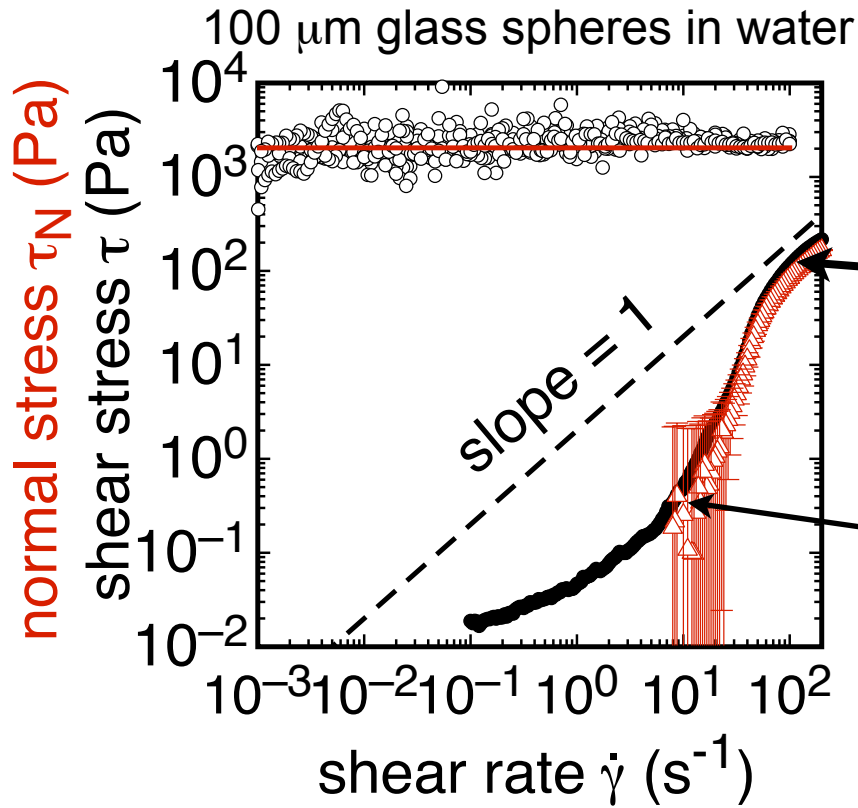
What causes the stress increase in the DST regime?

Frictional relation between shear and normal stress

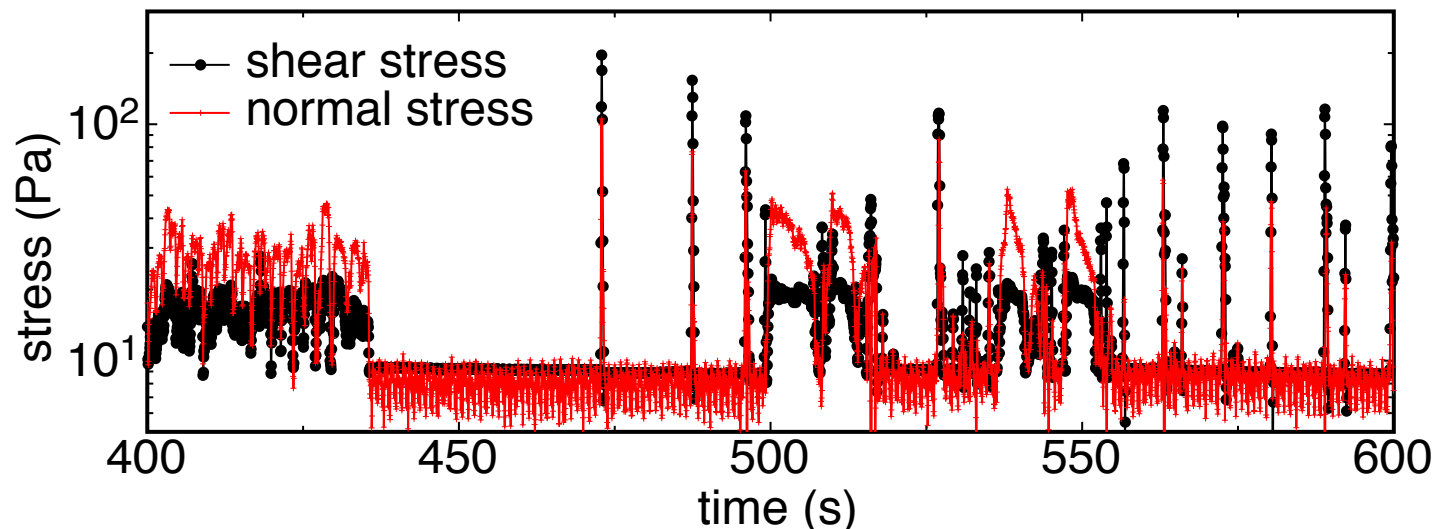


- shear stress (black) proportional to normal stress (red)
 - ➔ friction (Lootens et al. PRL 2003, 2005, Brown & Jaeger J. Rheol. 2012)
- existence of DST depends on boundary conditions
 - ➔ not a bulk constitutive relation dependent on local shear rate (Fall et al. PRL 2008, Brown & Jaeger J. Rheol. 2012)

Dynamic force chain formation



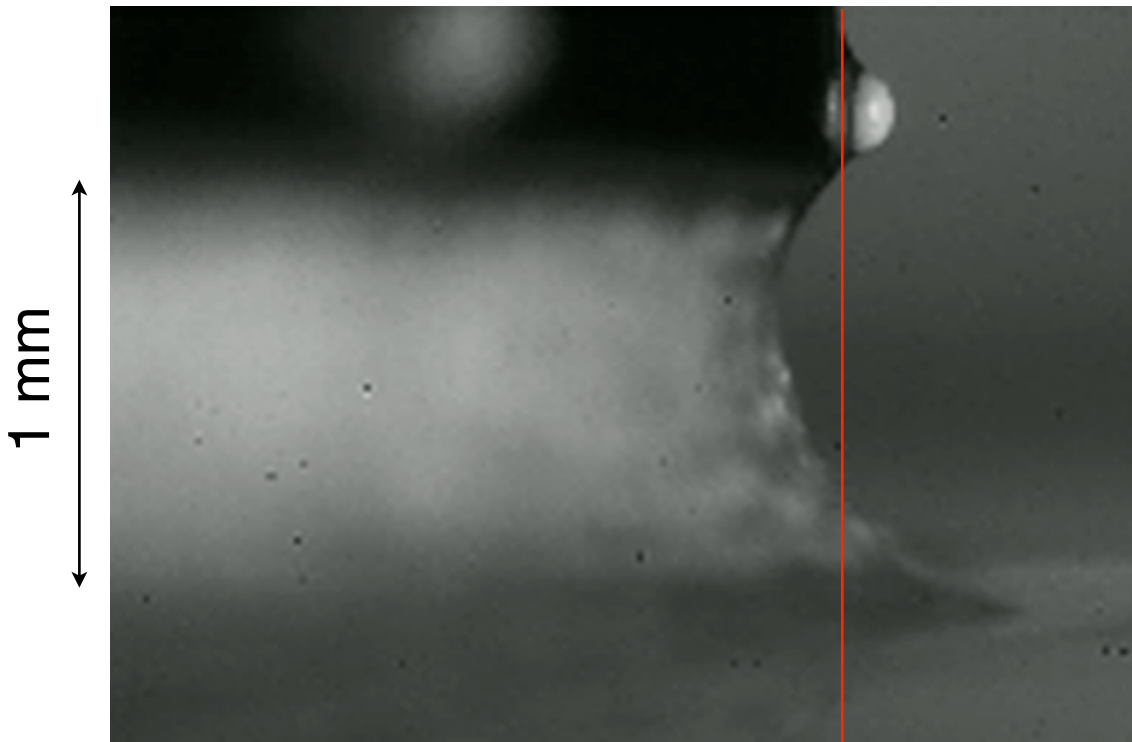
- force chains in DST regime (Seto et al. 2013)



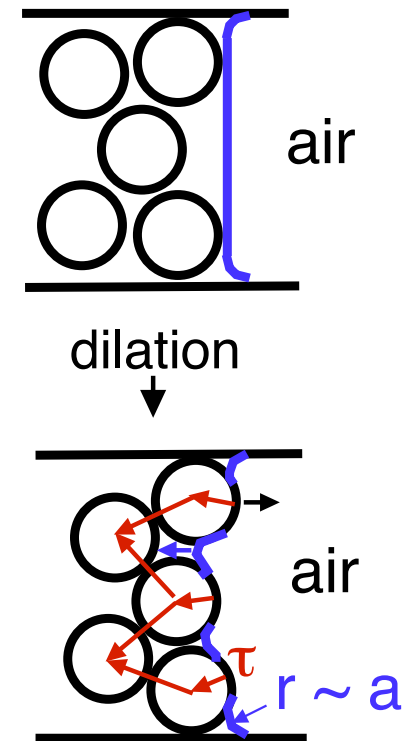
- giant fluctuations (Lootens et al. PRL 2003, 2005)

What supports the stress?
 Dilation against liquid-air interface
 -> confining stress from surface tension

150 μm ZrO_2 in mineral oil
 side view (tangent to surface), shear rate = 3 s^{-1} , 0.33x



Brown & Jaeger J. Rheol. 2012



maximum confining stress:

$$\tau_{max} \approx \frac{\gamma}{r} \sim \frac{\gamma}{a}$$

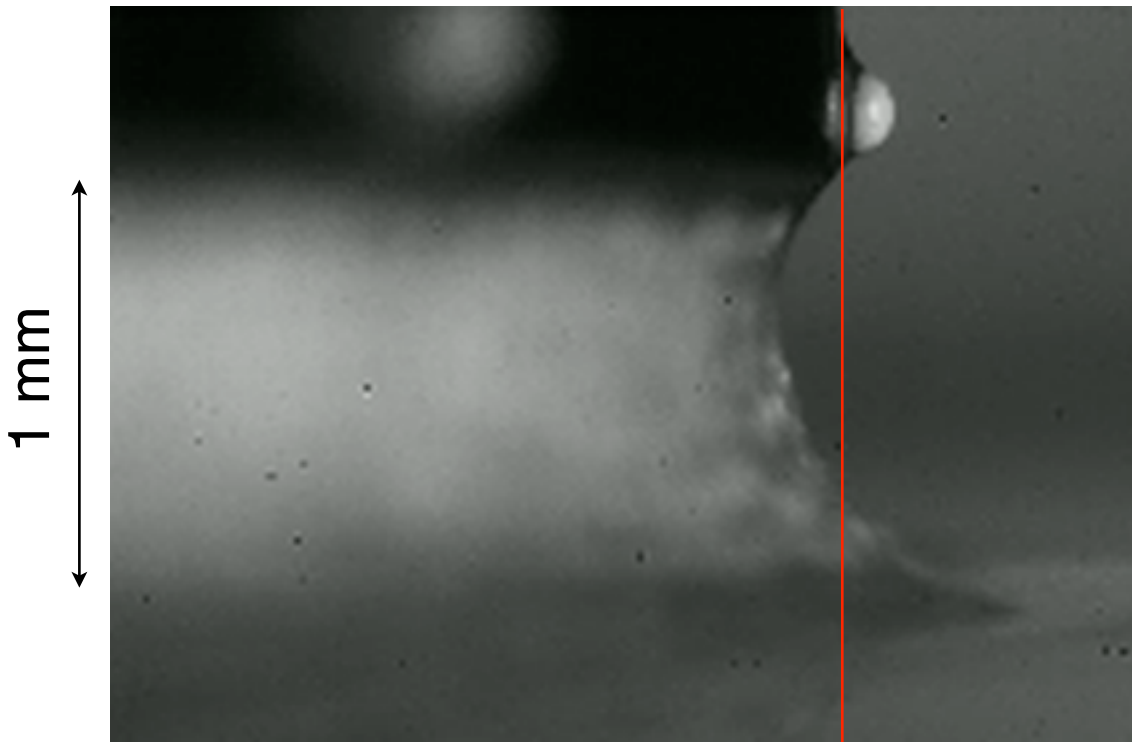
γ = surface tension

a = particle diameter

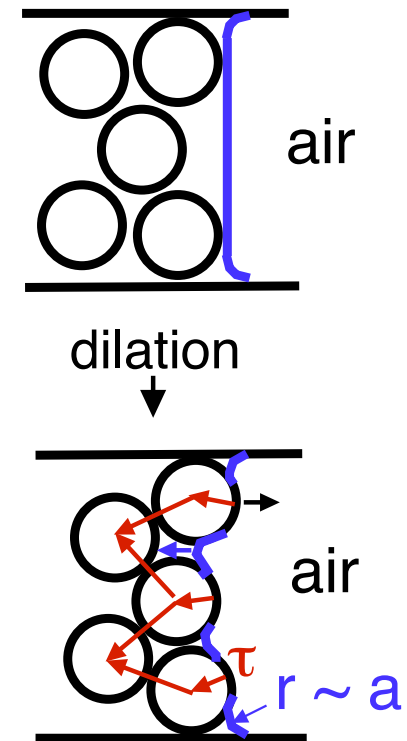
Cates et al. 2005

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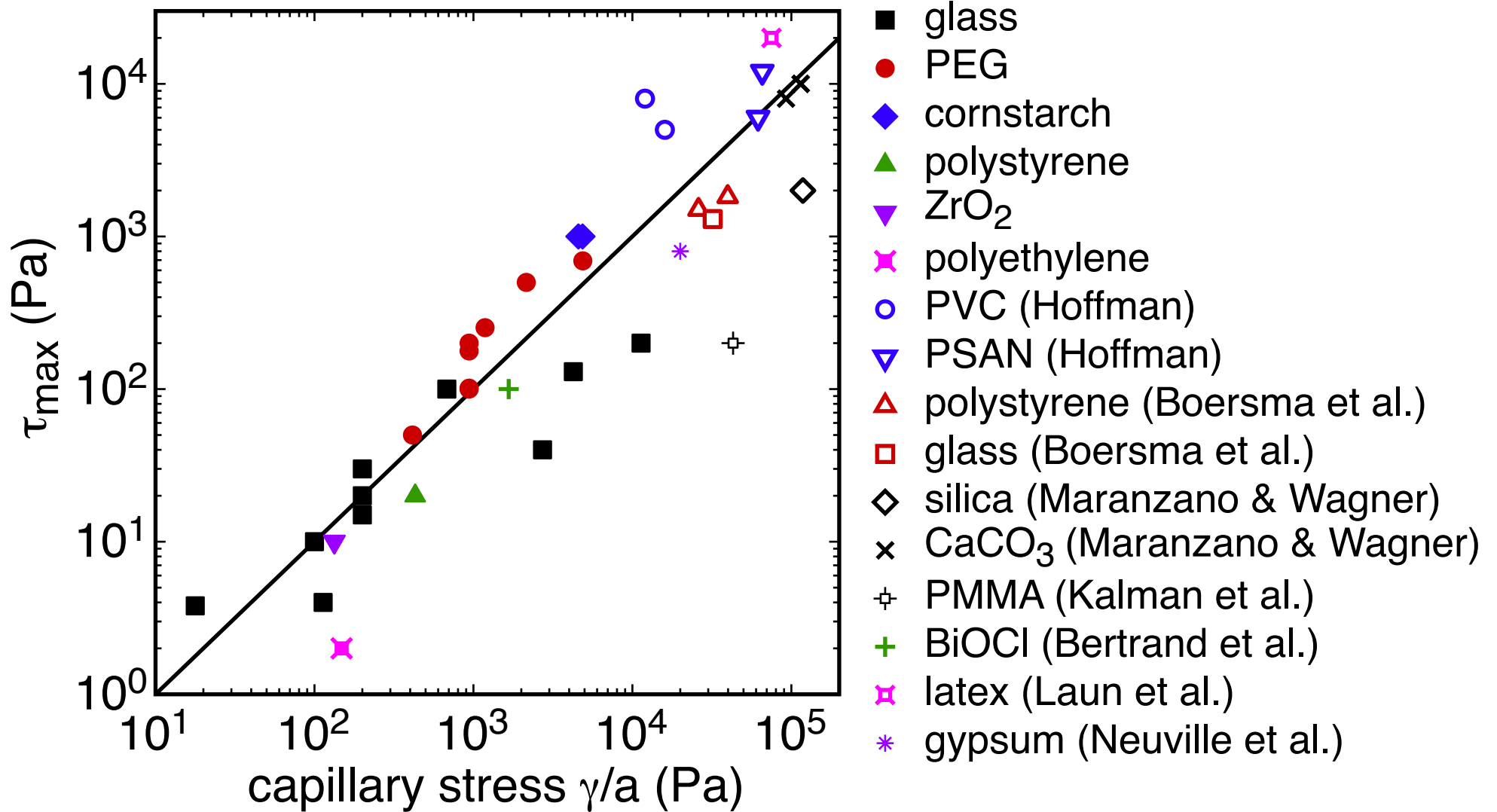
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Cates et al. 2005

maximum stress (τ_{\max}) in DST limited by surface tension



Summary of steady state DST:

DST occurs in dense suspensions of hard, frictional, non-attractive particles

-dilation leads to a dynamically jammed state with contact between particles

- shear stress must exceed all stresses that prevent dilation

- gravity for settling particles (Brown & Jaeger J. Rheol. 2012)

- electrostatic forces (Hoffman 1982, Maranzano & Wagner 2001)

- osmotic pressure (colloids) (Bergenholtz et al. 2002, Maranzano & Wagner 2002)

-stress is transmitted along force chains of frictional solid-solid contacts

-DST is not a local relationship between stress and shear rate -> it depends on boundary conditions

- stress is limited by smaller stiffness of:

- boundary (usually surface tension) (Brown & Jaeger J. Rheol. 2012)

- particle (Otsuki & Hayakawa 2010, Seto et al PRL 2013)

- DST does not occur under certain boundary conditions if confining stress does not increase in response to dilation

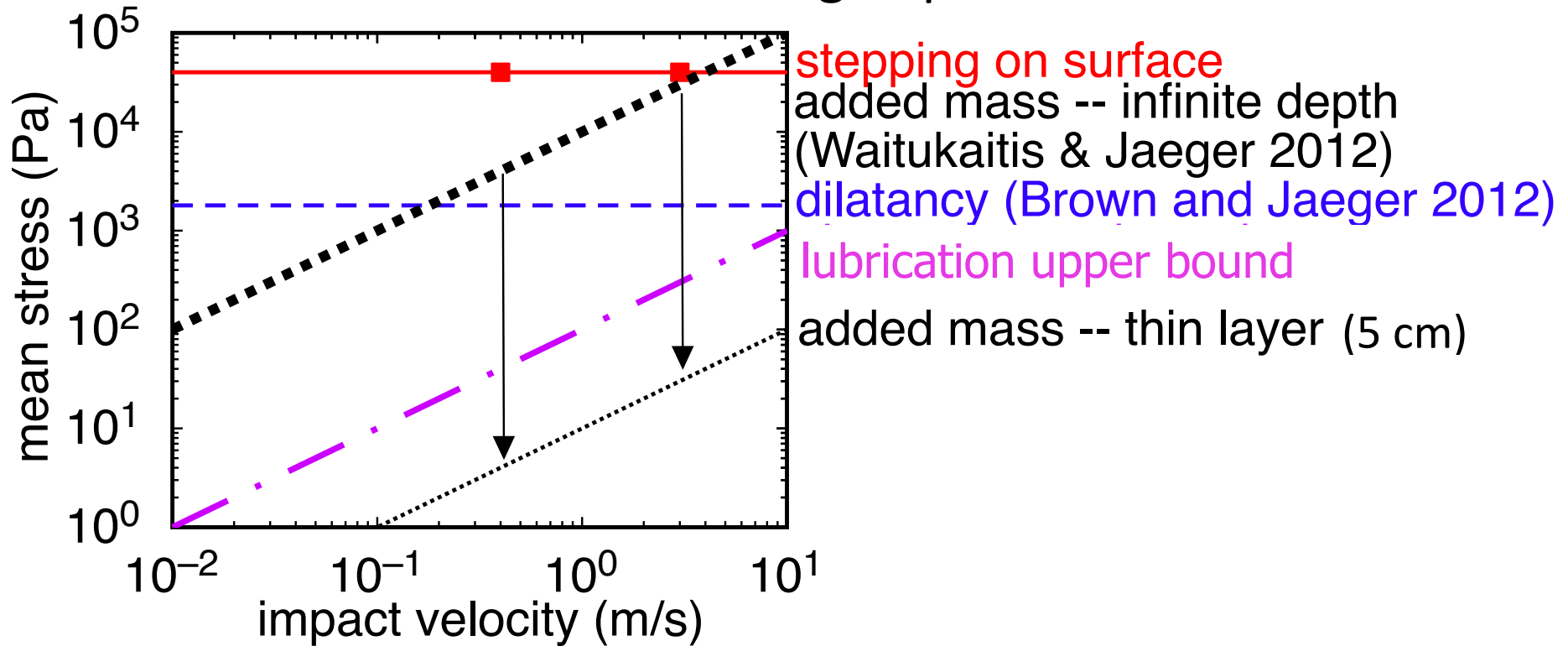
for a review, see Brown & Jaeger, Reports on Progress in Physics, 2014

Open Problem:

- Most of the dynamic phenomena of DST fluids remain unexplained
 - i.e. How can a suspension support a person's weight under impact?



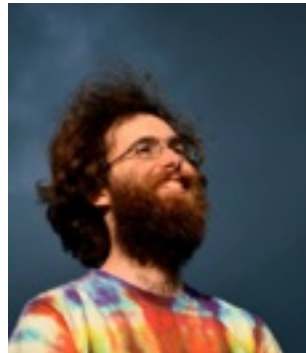
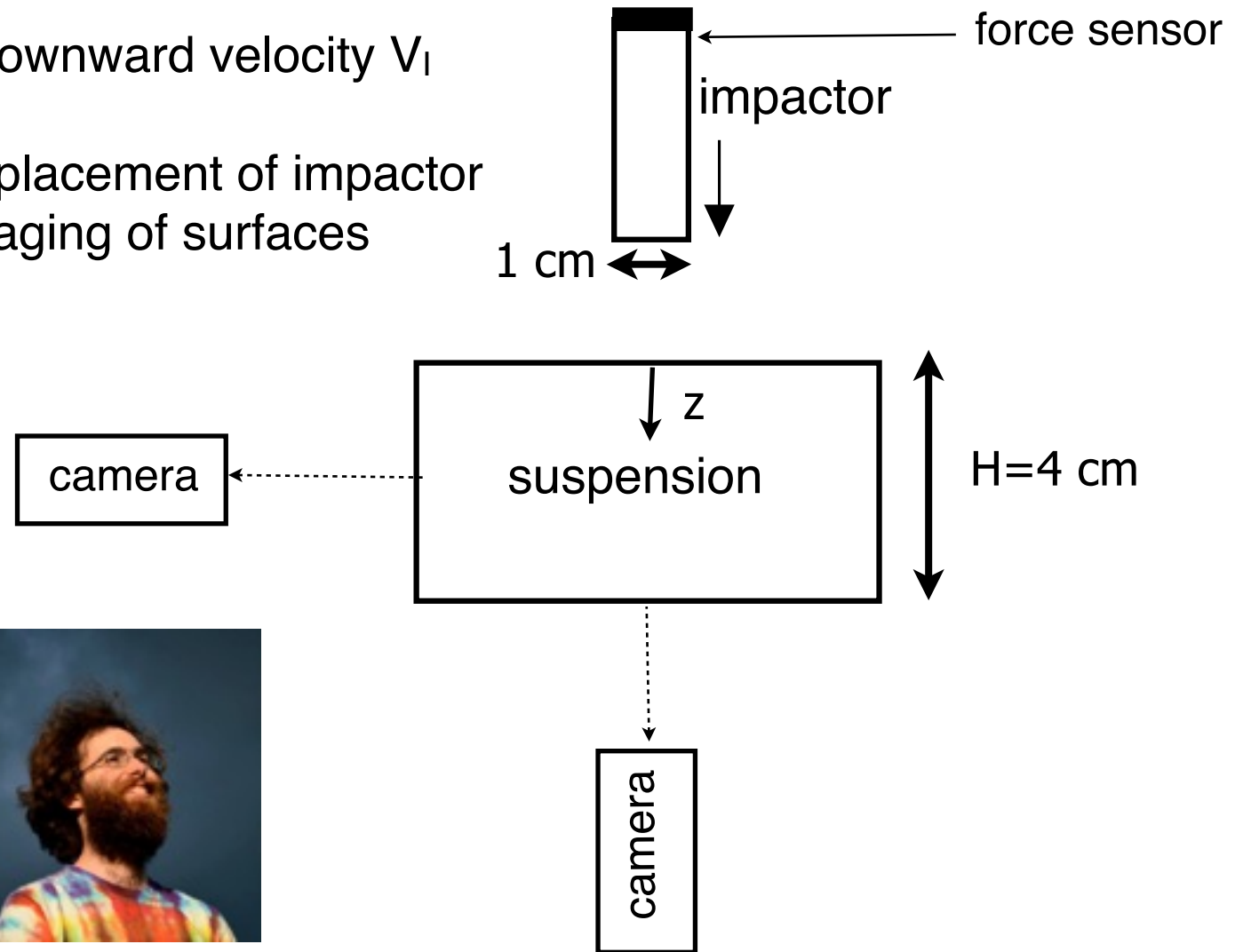
Steady state models can't explain large scale of transient stress during impact



➡ New mechanism needed to explain impact response, especially in regime of thin layers important for impact protection applications

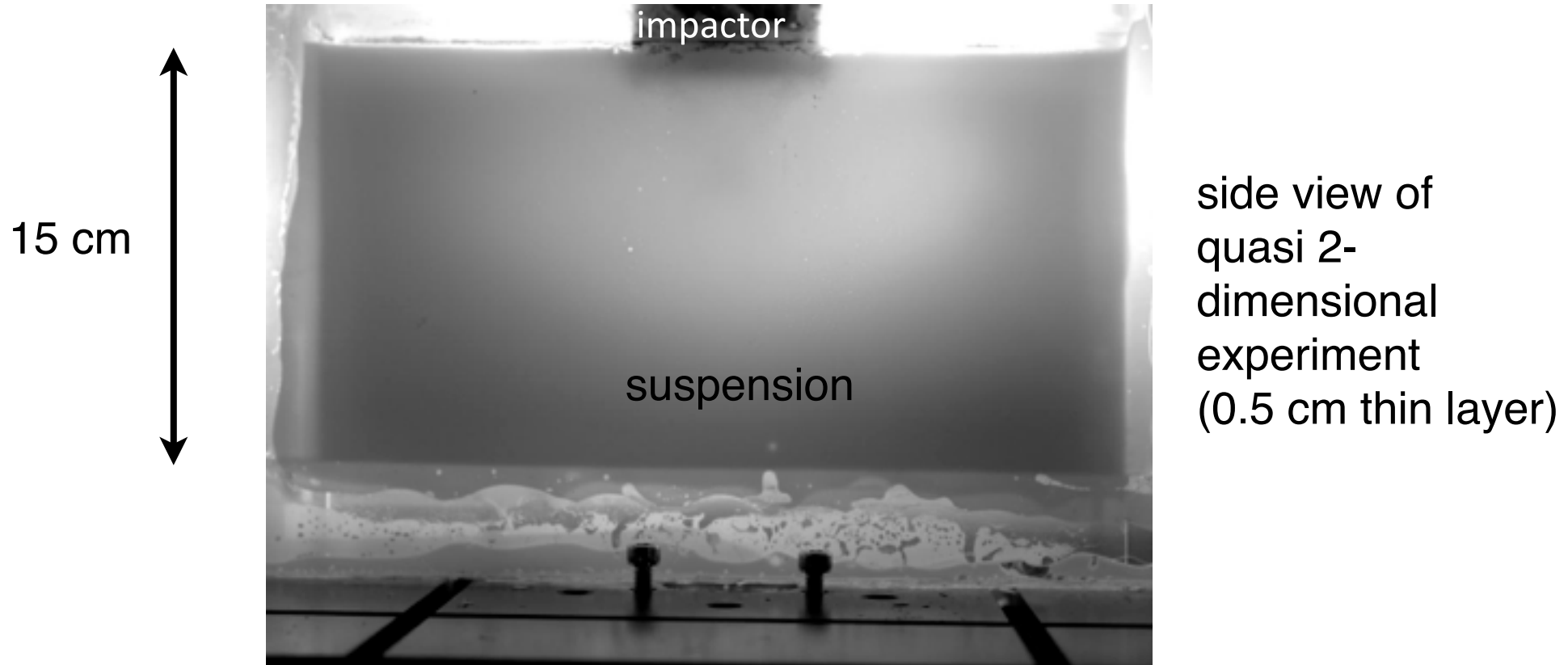
A model experimental system for impacts

- impact at constant downward velocity V_I into suspension
- measure force & displacement of impactor with simultaneous imaging of surfaces



Shomeek Mukhopadhyay & Ben Allen
arXiv:1407.0719

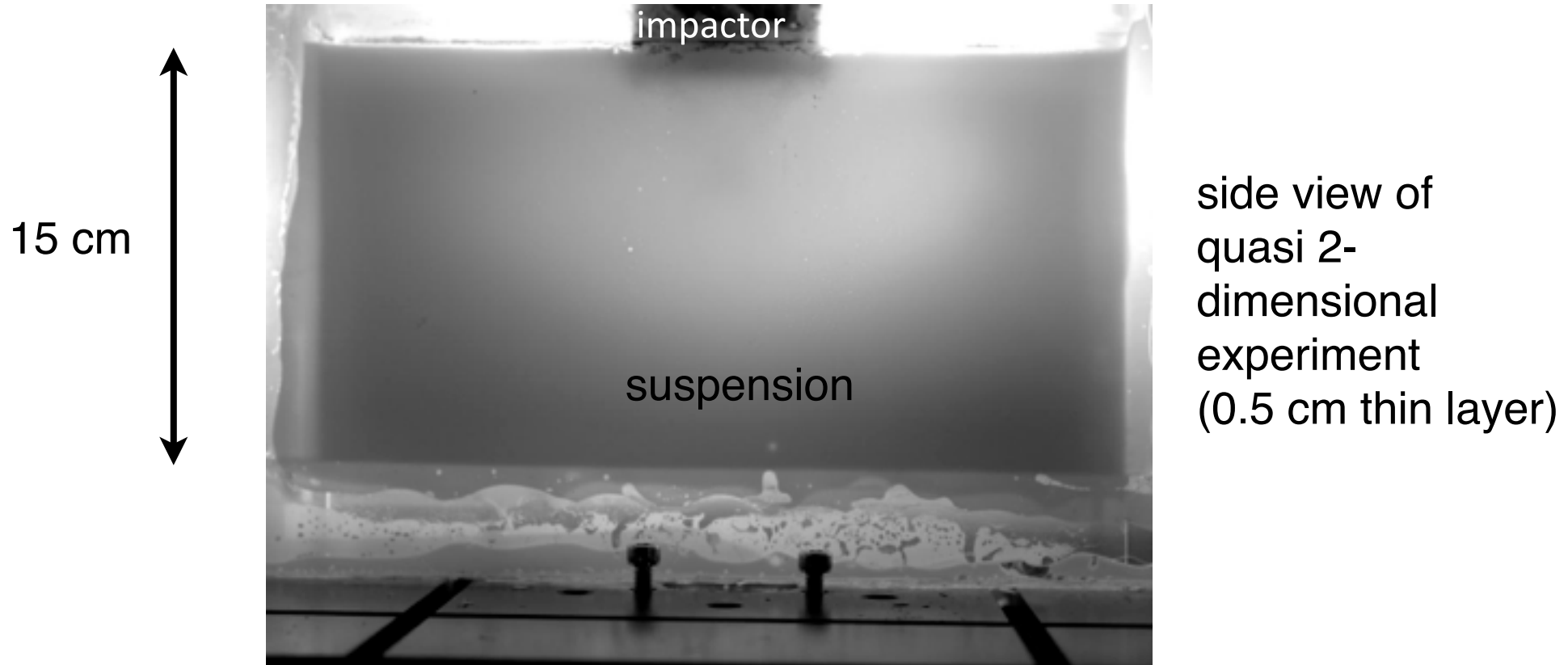
Dynamically jammed region propagates in front of impact proposed by
Waitukaitus and Jaeger, Nature 2012



- cracks suggest the region in front of the impactor can transmit stress like a solid/jammed system

Hypothesis: If the dynamically jammed region spans to a boundary, then it can support stress like a solid

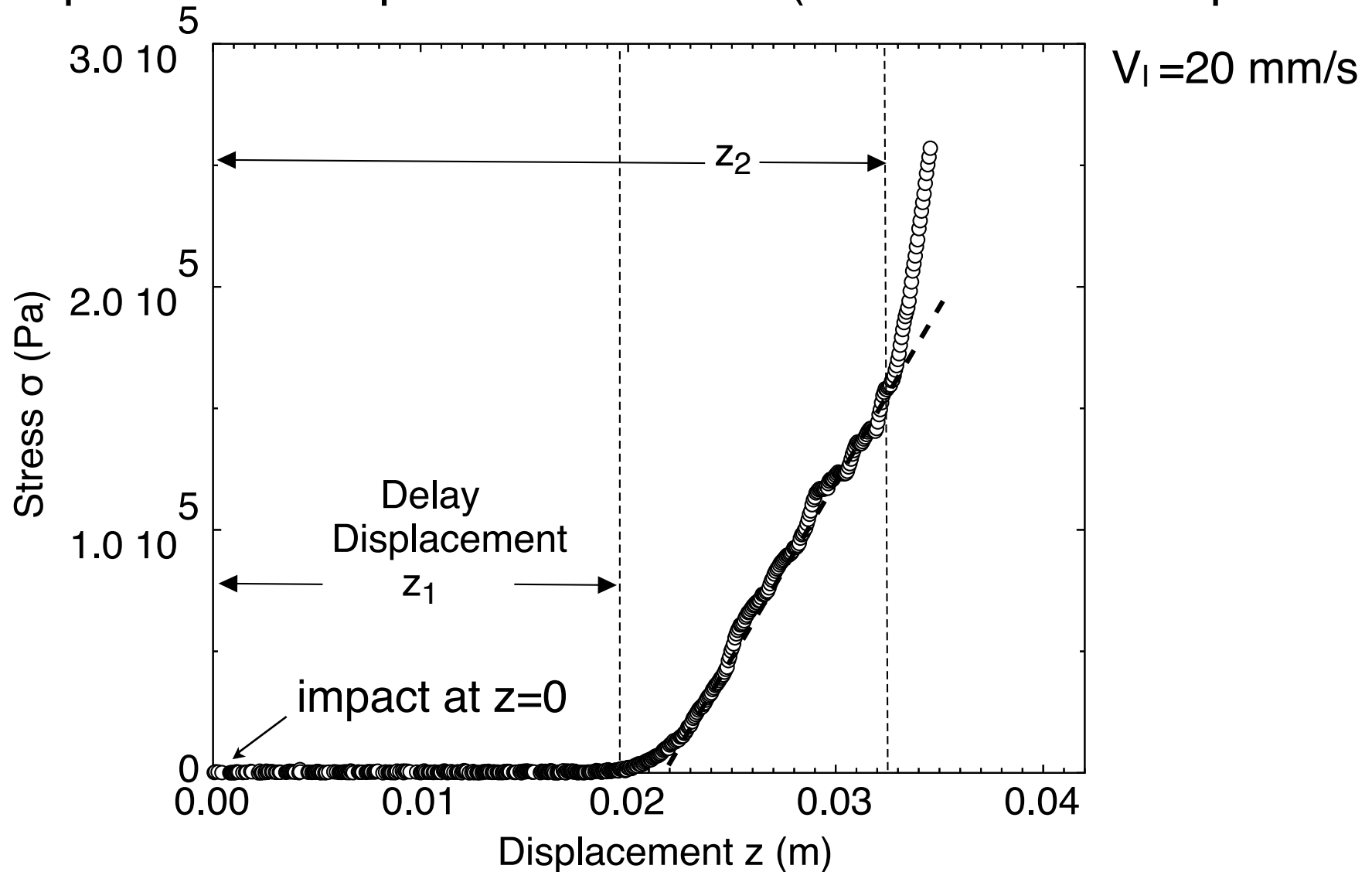
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Example stress-displacement curve (3-dimensional experiment)



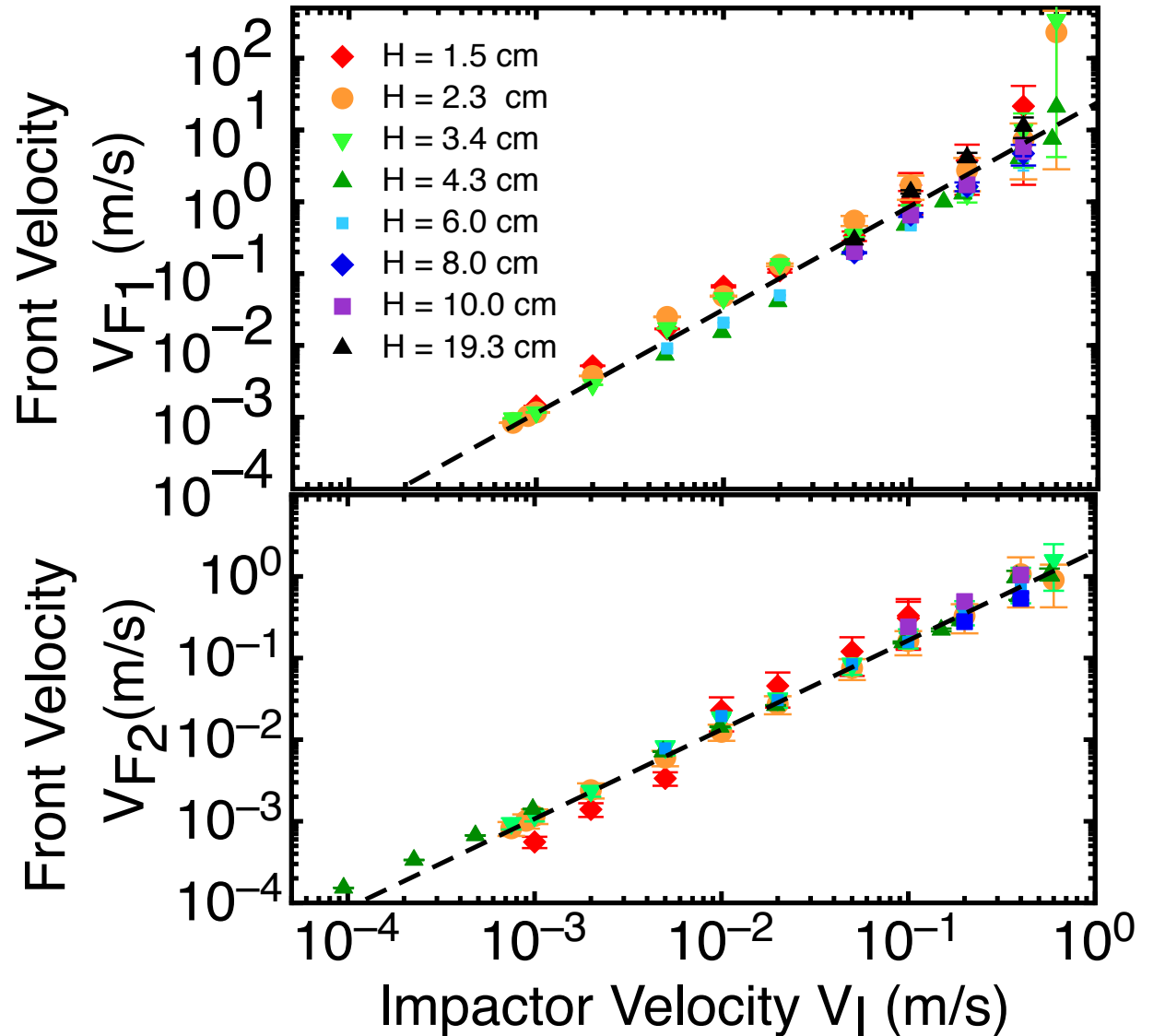
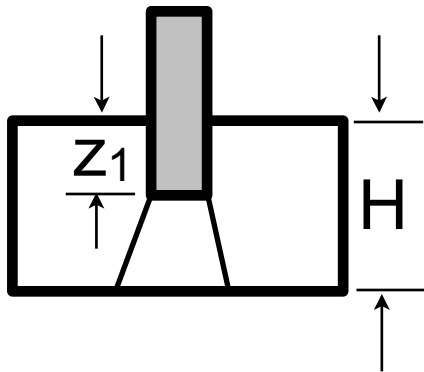
- delay z_1 between impact and increasing force response
 - bulk models predict stress $\sigma < 10^3$ Pa (buoyancy, inertia, lubrication)
 - stress enough to hold up a person's weight (4×10^4 Pa)

Is delay before force increase due to time required for front to reach boundary?

delay time $T_1 = z_1/v_1$

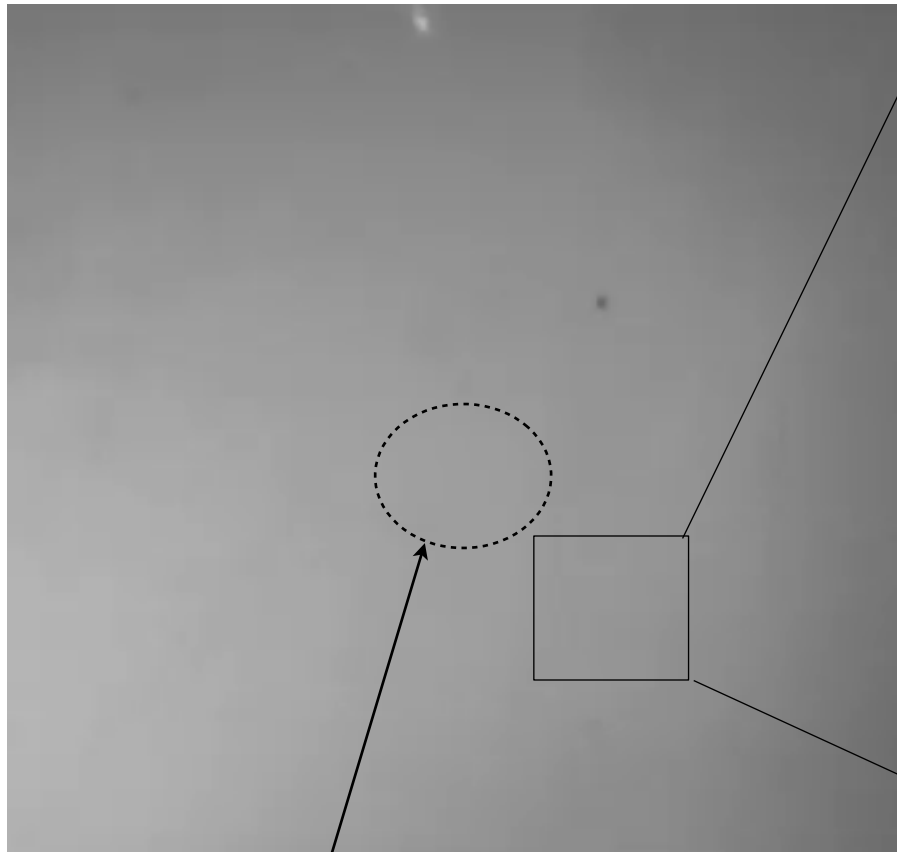
front velocity

$$V_{F1} = H/T_1$$

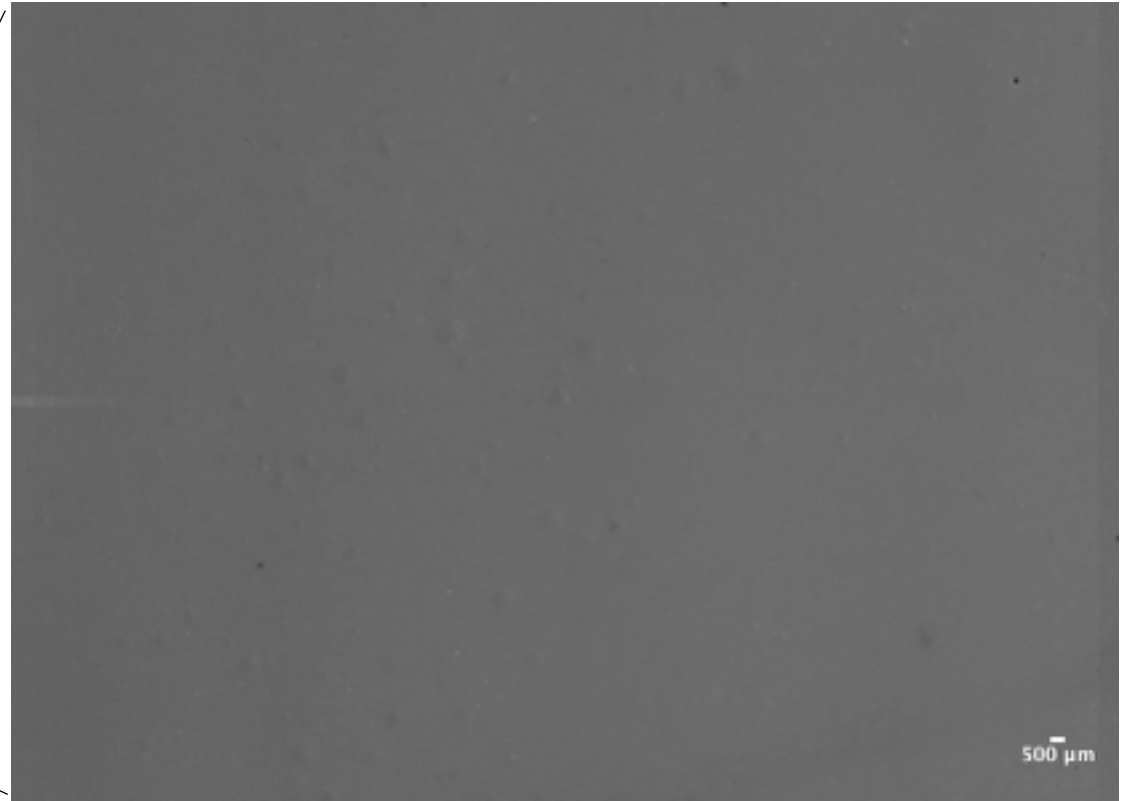


- Delay time T_1 before force increase scales with fluid depth H
- ➡ stress increase due to propagating fronts reaching the boundary

Voids in pores appear at bottom surface after a delay

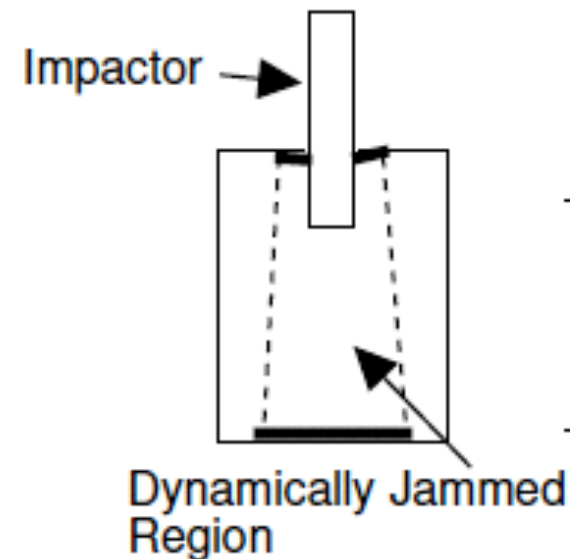


impactor diameter $d=12.7$ mm
20x real time

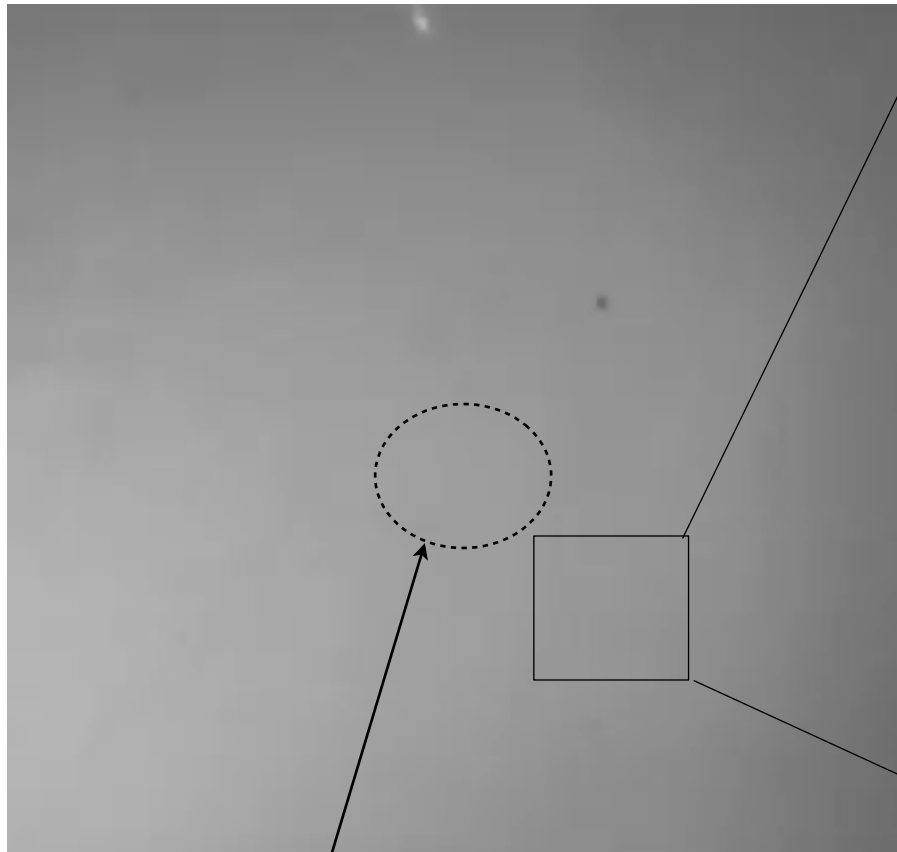


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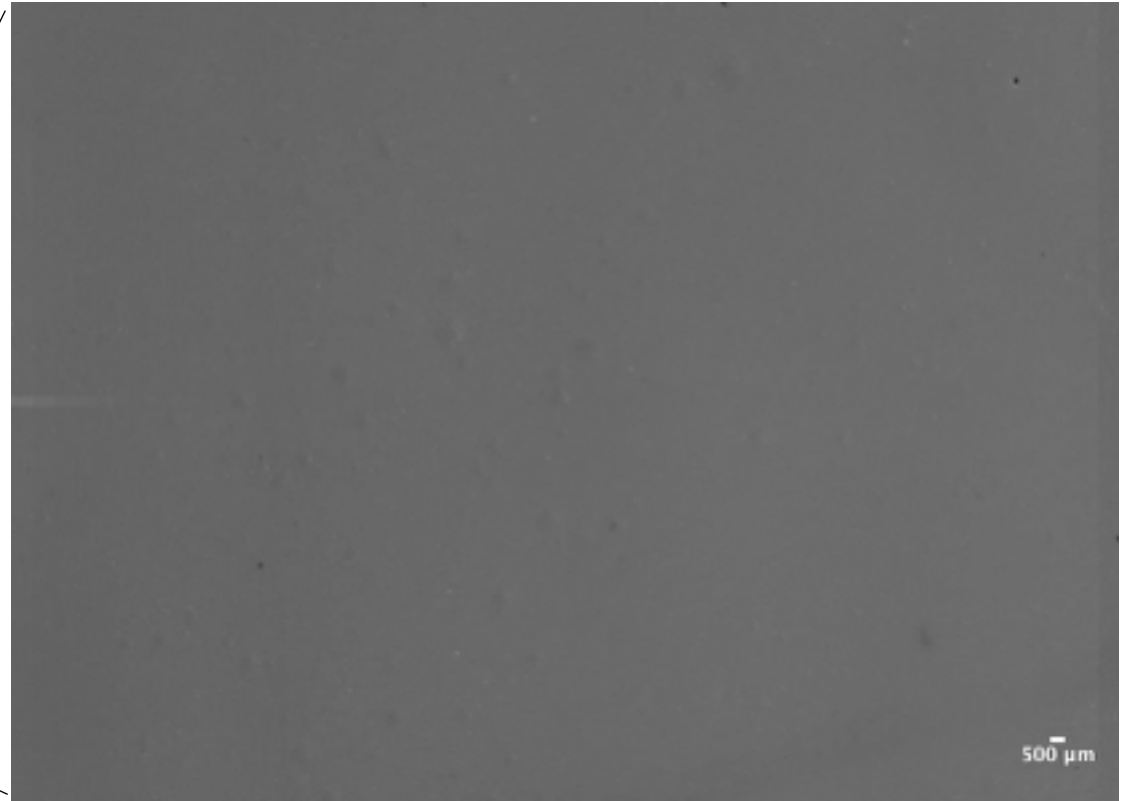
- rough surface (result of dilation) also observed at top
- ➡ dynamically jammed region spans from top to bottom
- ➡ stress isn't limited by surface tension in transient if it can be supported by solid boundaries



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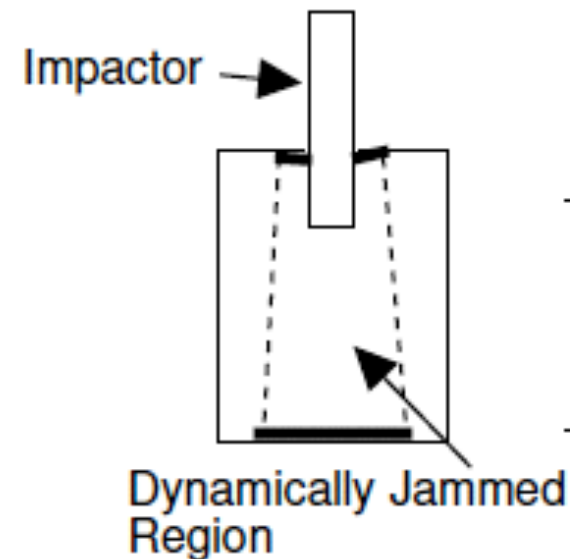


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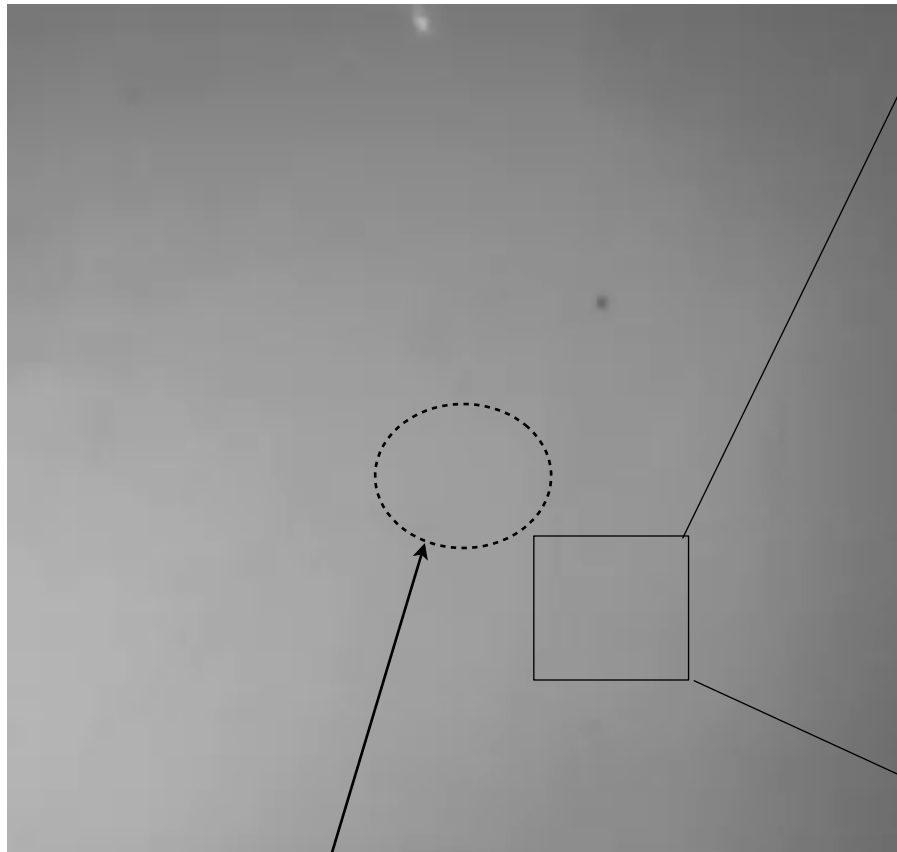


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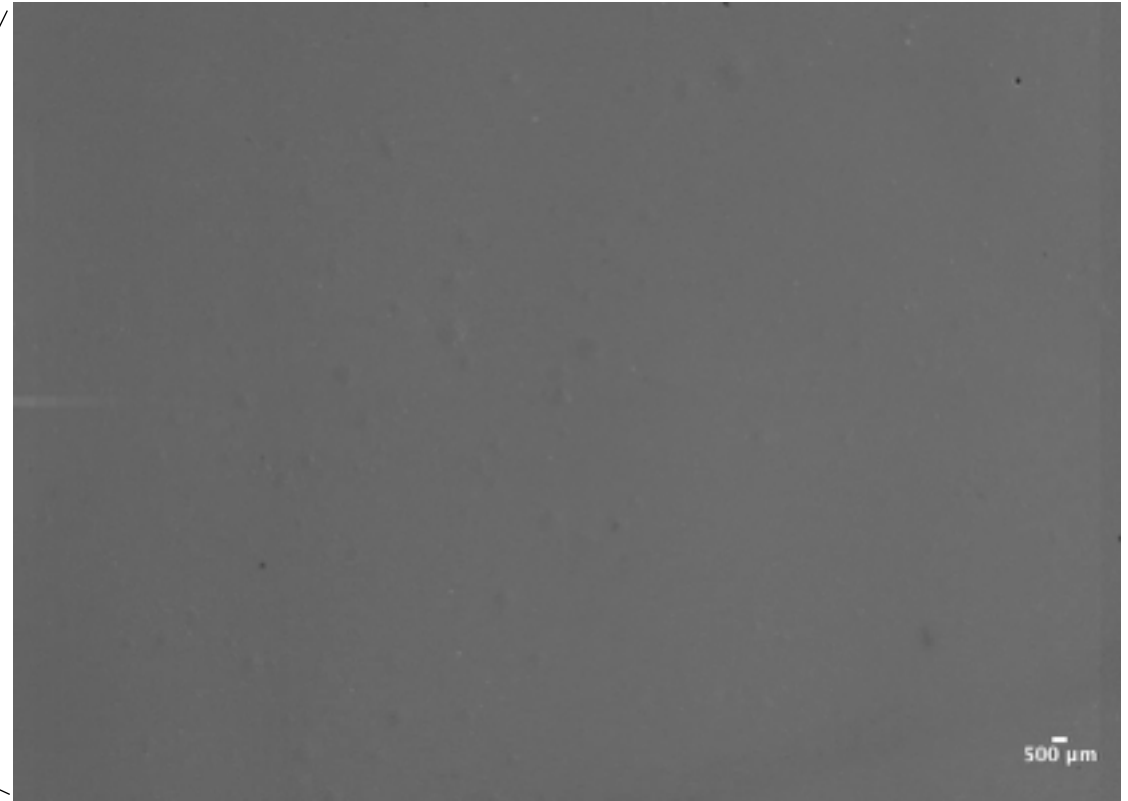
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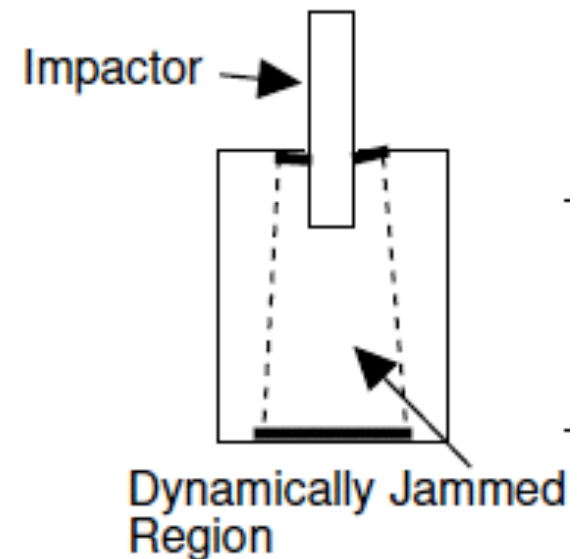


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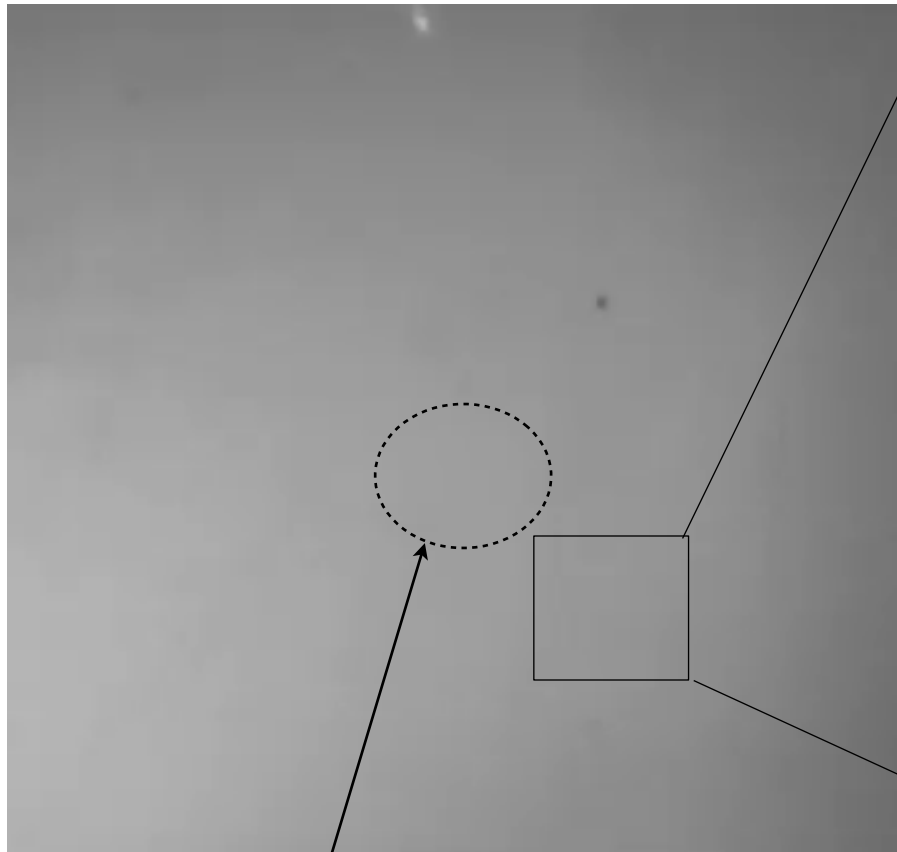


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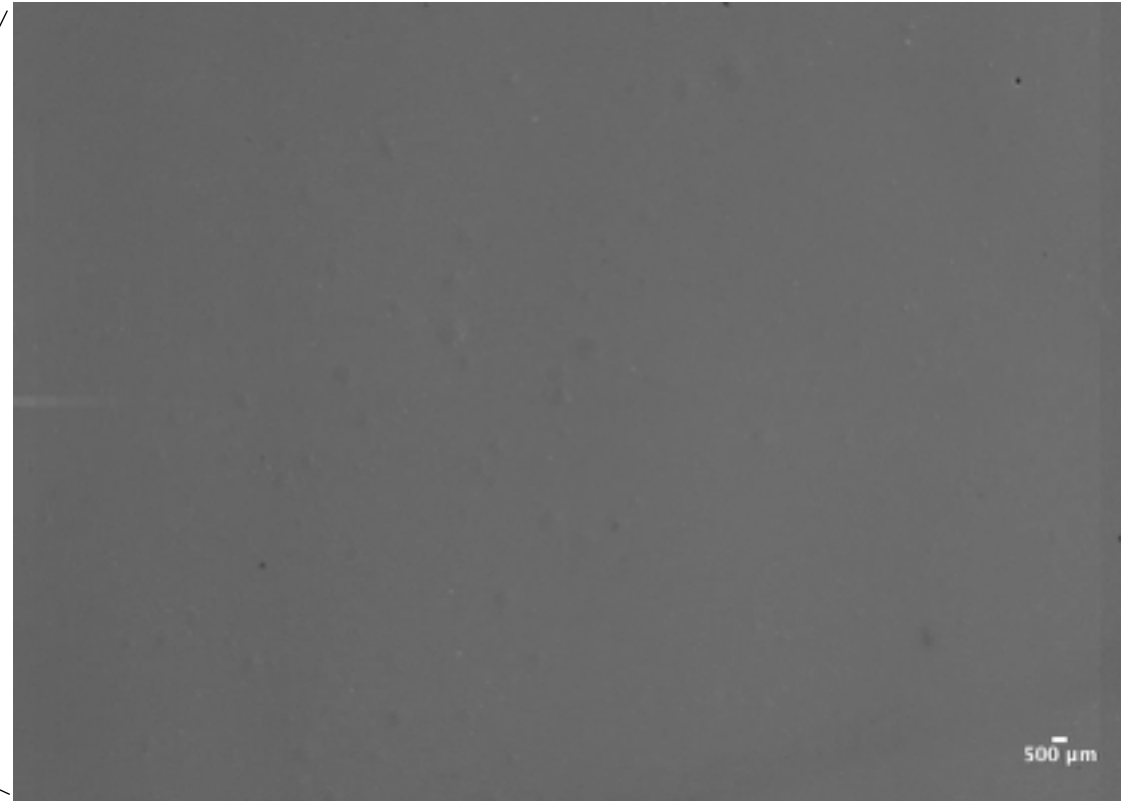
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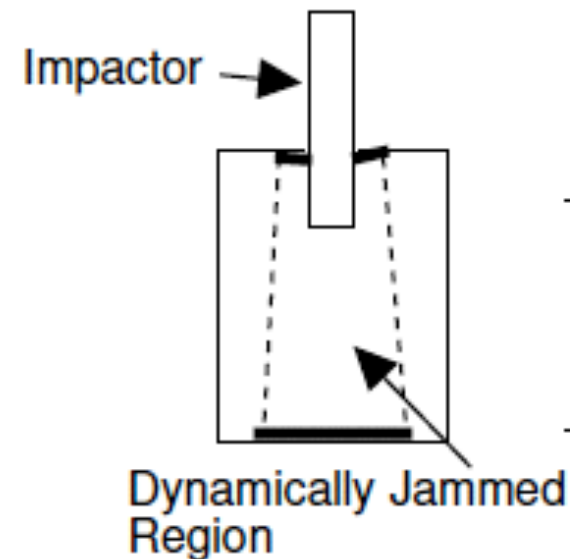


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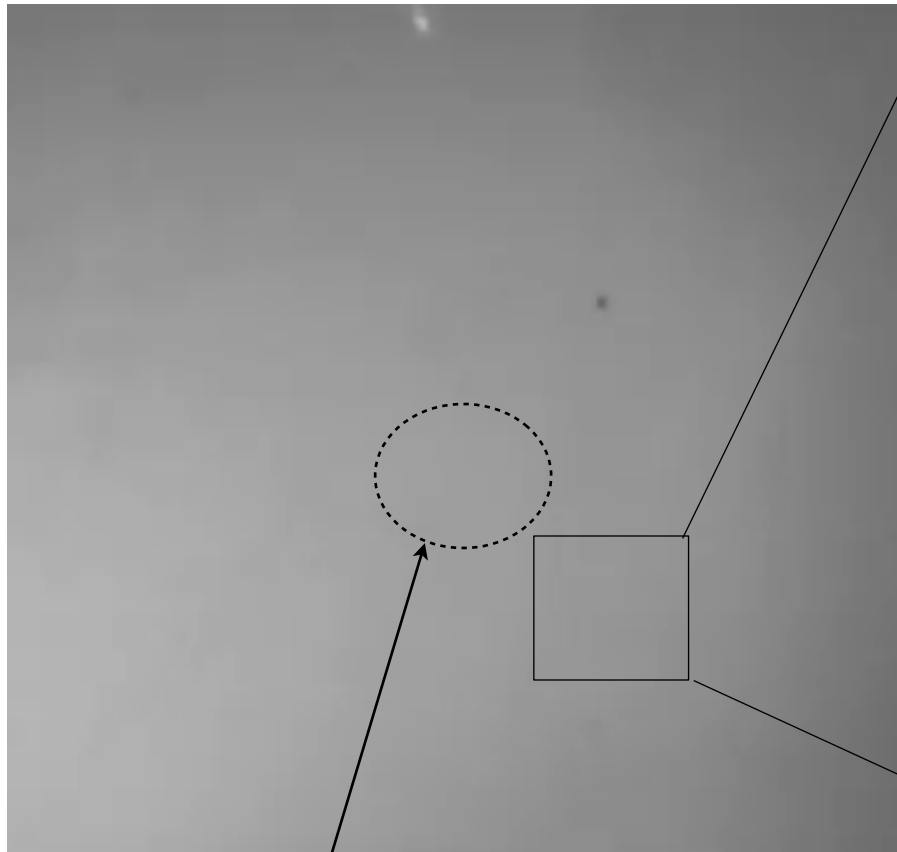


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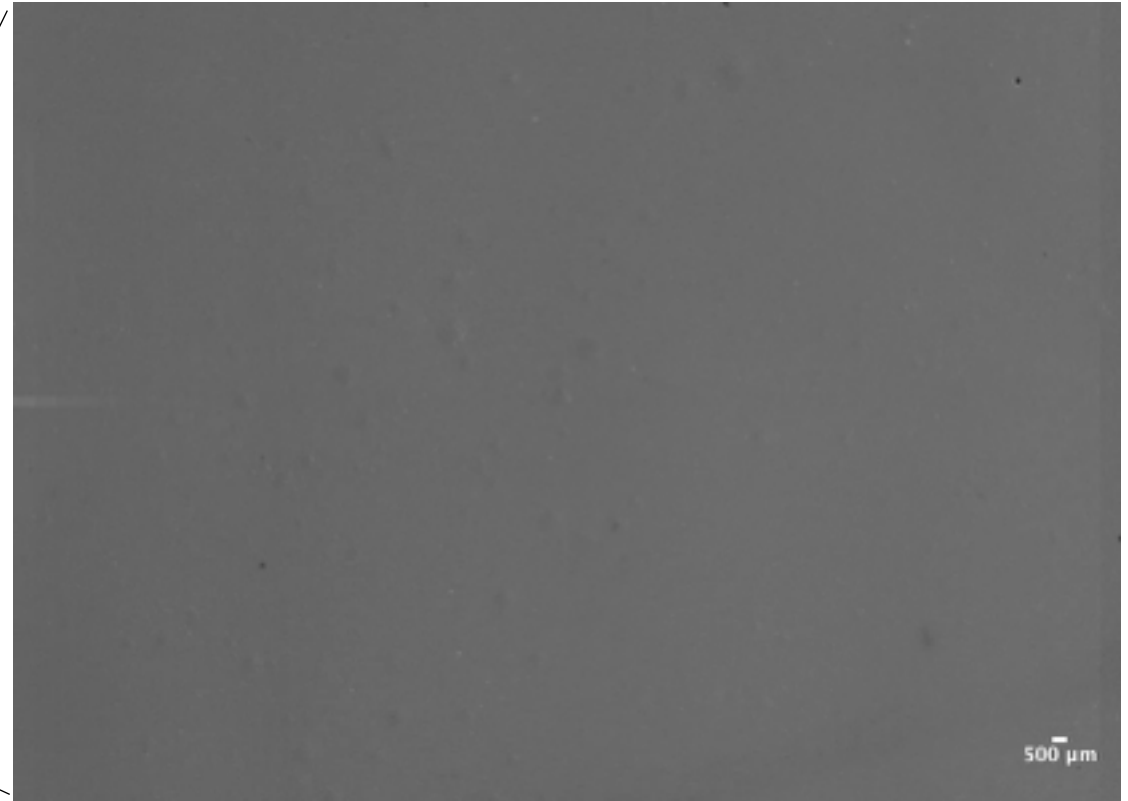
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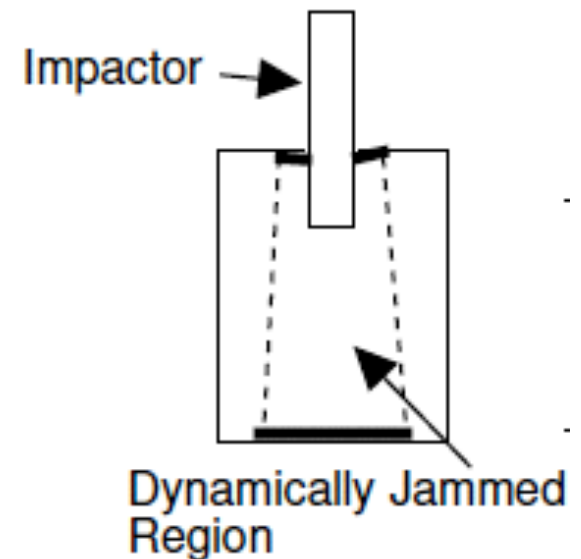


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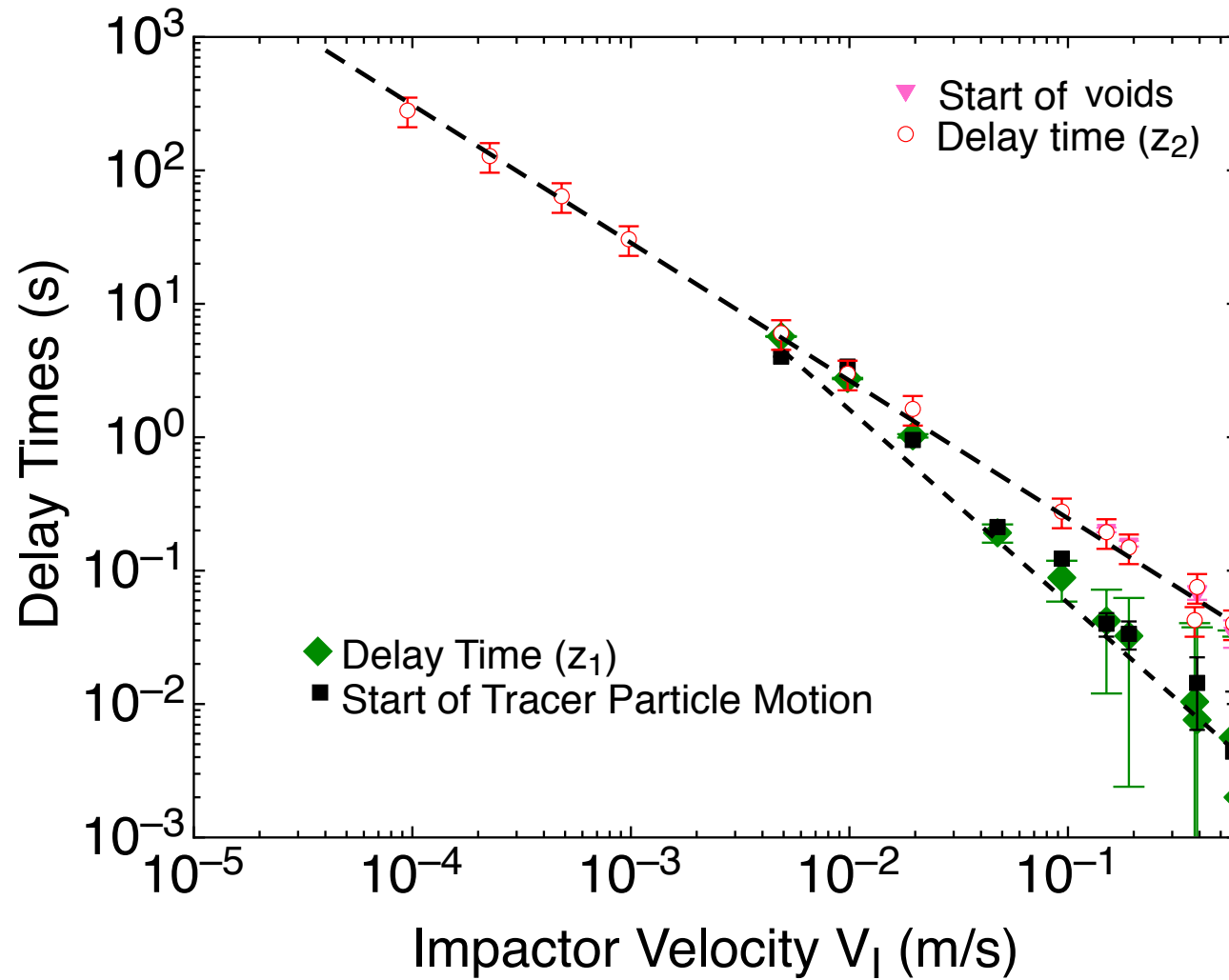


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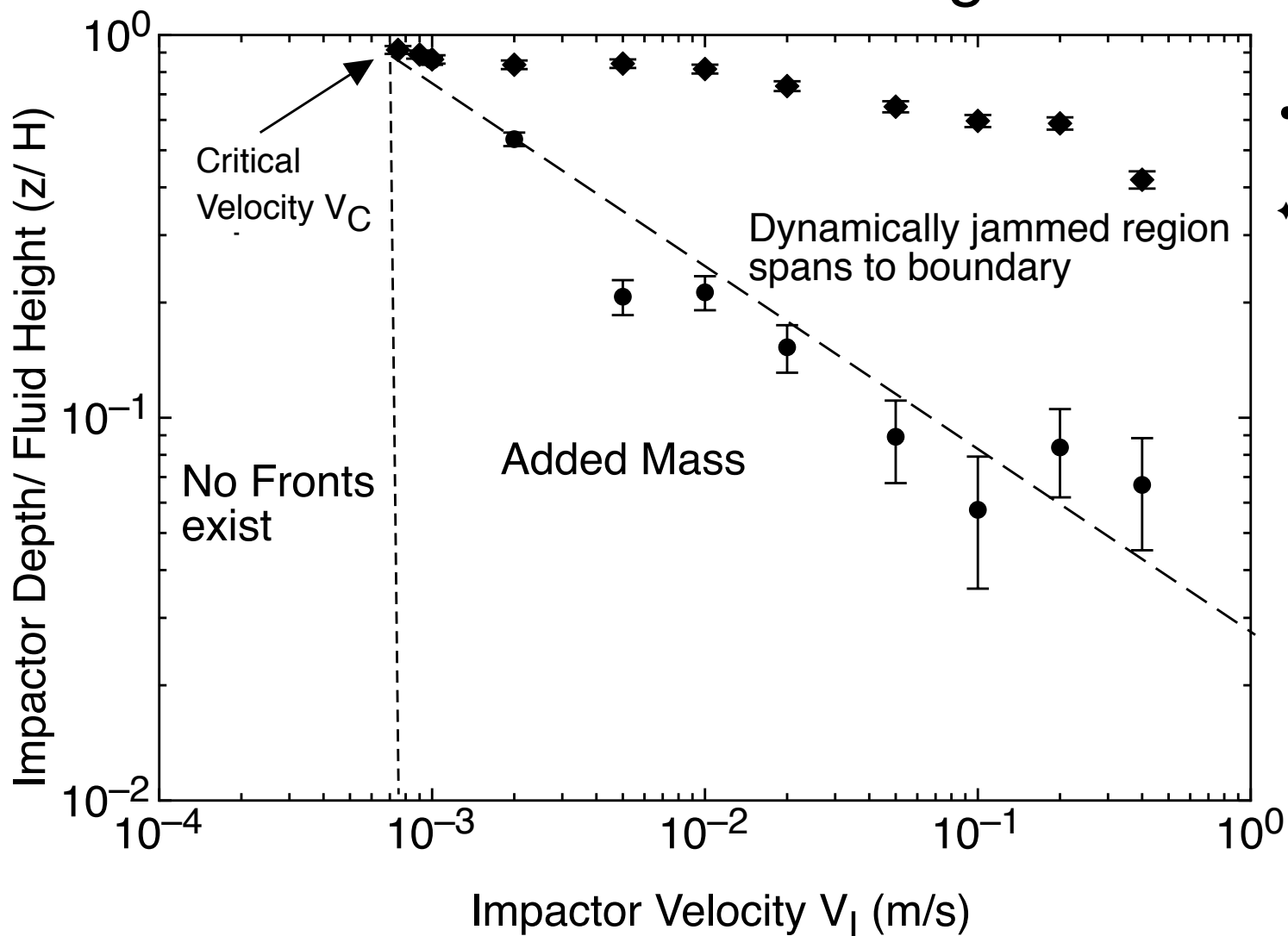


Stress increases at same time as structural changes at boundary



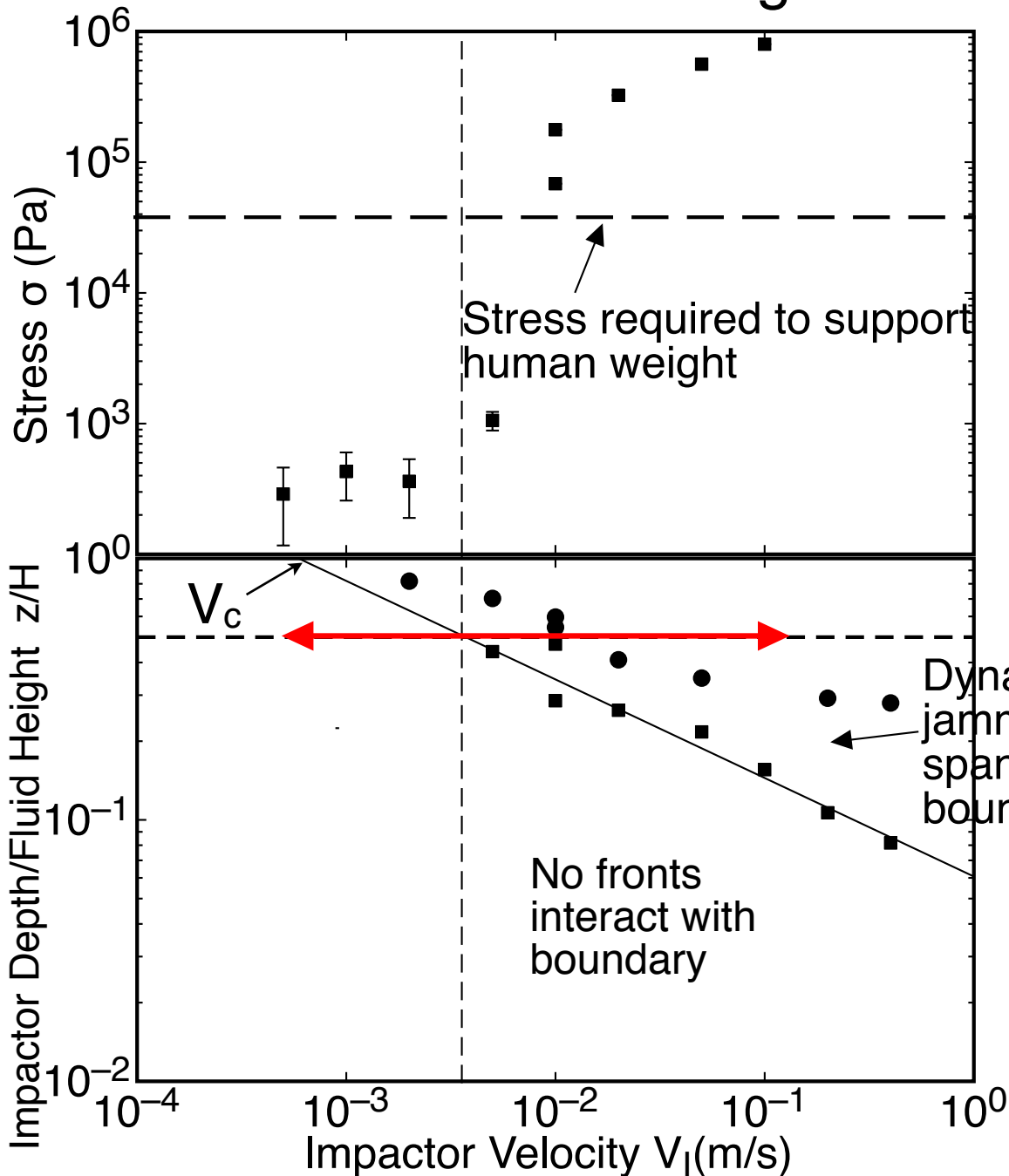
- front 1 is same as Waitukaitis & Jaeger, Nature 2012

Phase diagram



- critical velocity V_c required for front propagation

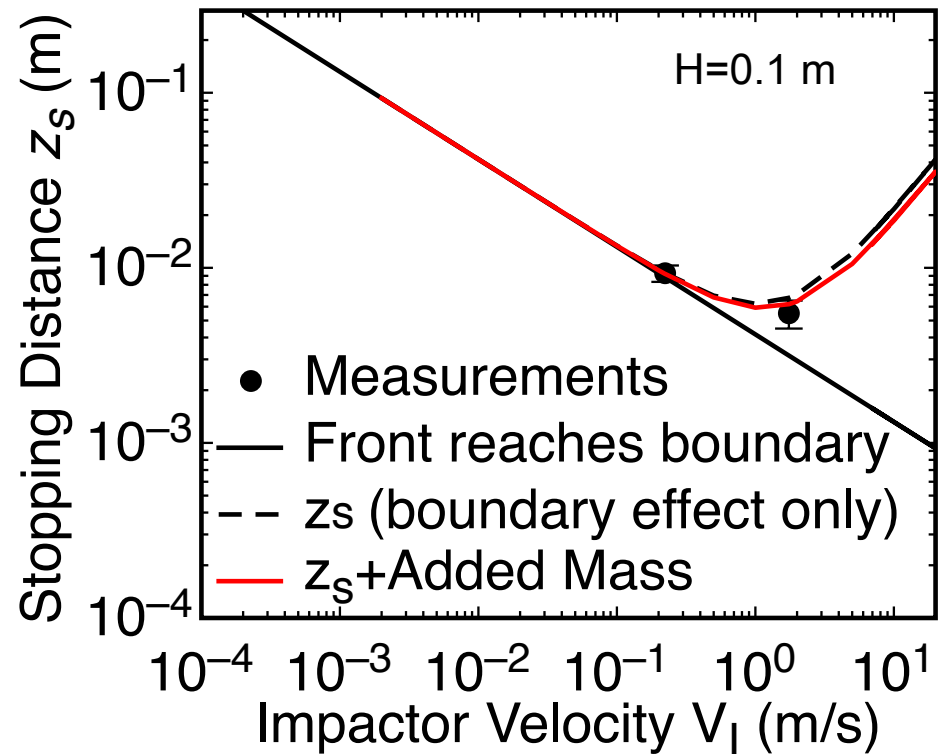
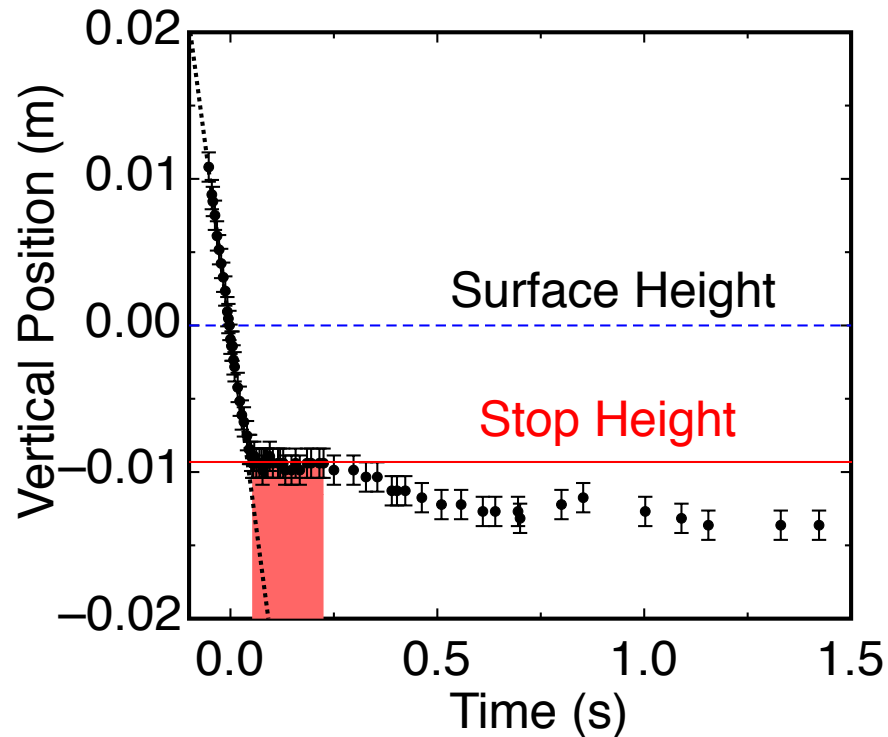
discontinuous shear thickening transition due to front reaching solid boundary



- shear thickening transition if phase boundary crossed at fixed z/H (no transition if $V_F \sim V_I$ [Waitukaitis & Jaeger 2012, Gomez et al. 2012])
- stress is $\sim 10^2$ times larger than steady state DST

- V_c similar to a 1st order critical point (discontinuity vanishes as $V_I \rightarrow V_c$)

Walking on cornstarch and water



- foot stops abruptly with delay after hitting surface due to time for front to reach boundary
- foot continues to sink after relaxation time
- stopping distance determined by balance of work done by fluid and kinetic energy

Conclusions about impact response of DST suspensions

- a critical (minimum) velocity is required to observe front propagation and the dynamically jammed region
- a discontinuous shear thickening transition results from a front colliding with a solid boundary above the critical velocity
 - the solid-like regime can support enough stress to hold up a person's weight