

# ~~Spatial~~ Avalanches in magnetization dynamics

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<sup>5</sup>CBPF, Rio de Janeiro

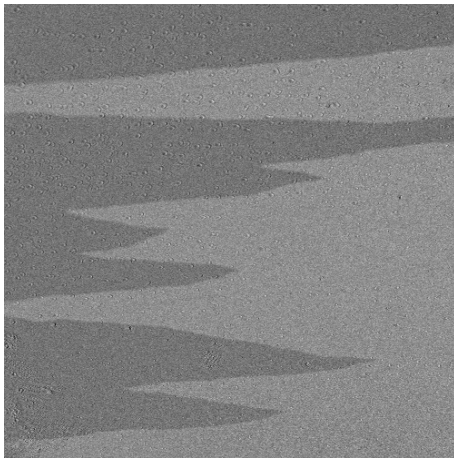
<sup>6</sup>Ghent Univ., Belgium

<sup>7</sup>Aalto Univ., Finland

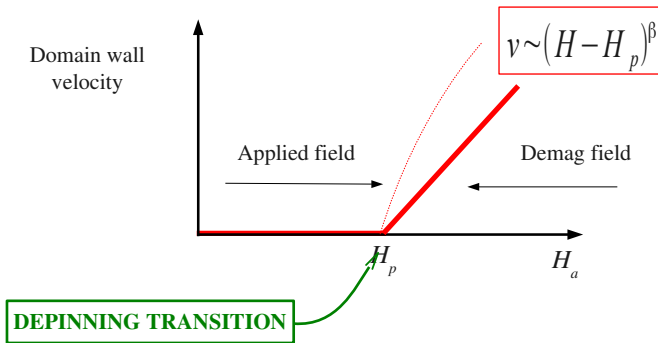
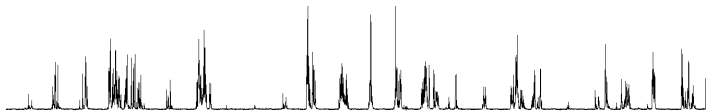
<sup>8</sup>INRIM, Torino, Italy

@Complexity in mechanics - KITP (CA) - Oct. 21, 2014

# Magnetization dynamics: motion of domain walls



# Pinning and depinning of domain walls



# Outline

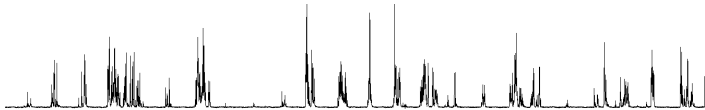
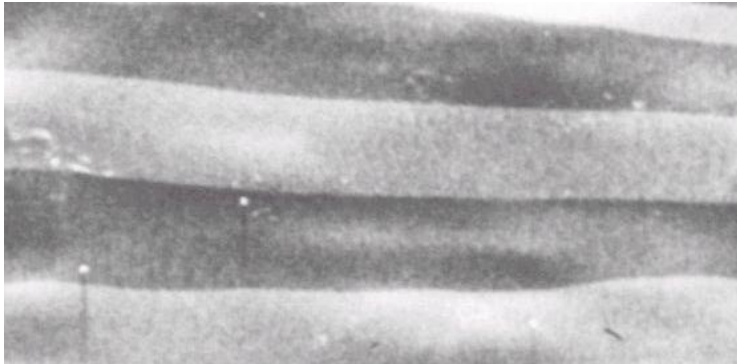
- 1 Magnetization dynamics: temporal structure
  - Universality and depinning transition
  - Asymmetry in the avalanche average shape
  - Simmetric avalanches in thin films
- 2 Magnetization dynamics: spatial structure
  - Spatial avalanches in a window
  - Searching for the universality classes
  - Experimental avalanches from MOKE
- 3 Domain walls for spintronics devices
  - Future DW devices
  - Role of disorder in DW dynamics
  - Creep and DW structure



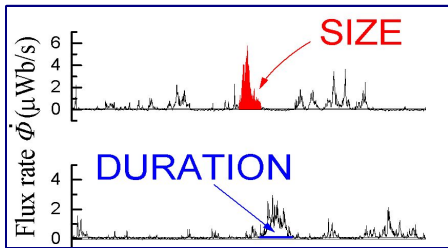
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# Bulk systems: extended domain walls

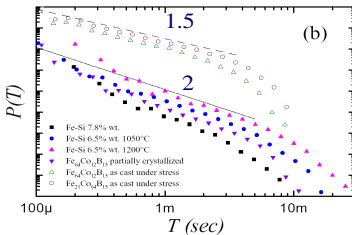
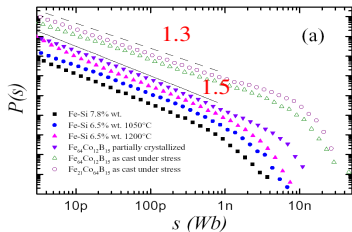


# Avalanches, power laws, and universality classes



Power law distributions

$$P(S) \sim S^{-\tau} \quad P(T) \sim T^{-\alpha}$$



UNIVERSALITY CLASSES

# The origin of the universality classes in 3D systems

$$\frac{\partial h(\mathbf{r}, t)}{\partial t} = H(t) - k M_s^2 \bar{h} + \gamma \nabla^2 h(\mathbf{r}, t) + \int d^2 r' K(\mathbf{r}' - \mathbf{r})(h(\mathbf{r}', t) - h(\mathbf{r}, t)) + \eta(\mathbf{r}, h)$$

Range of interactions:  $J(\mathbf{q}) = |\mathbf{q}|^\mu$

Stray fields  
 LONG RANGE ( $\mu = 1$ )

Surface tension  
 SHORT RANGE ( $\mu = 2$ )

3

Upper critical  
 dimension

5

1.5

$P(S) \sim S^{-\tau}$

1.3

2

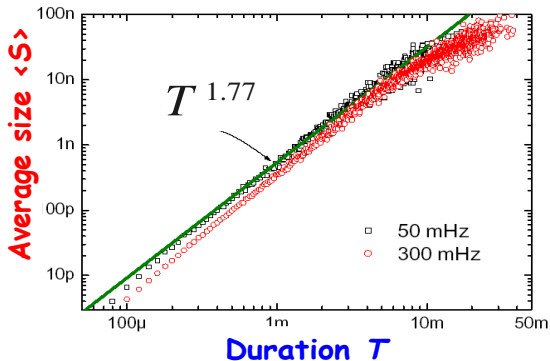
$P(T) \sim T^{-\alpha}$

1.5

# The $\gamma = 1/\sigma v z$ exponent

**Average size**  
& **duration**

$$\langle S(T) \rangle \sim T^{1/\sigma v z}$$



## Universal scaling function: the average shape

$$\langle S(T) \rangle \sim T^{1/\sigma \nu z} \quad \rightarrow \quad V \sim \frac{\langle S \rangle}{T}$$

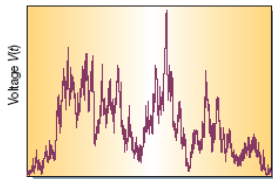
### Average avalanche shape

$$V(t, T) = T^{1/\sigma \nu z - 1} g_{shape}(t/T)$$

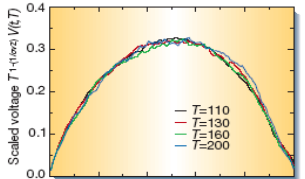
$$V \sim \langle S \rangle / T$$

Universal scaling  
functions

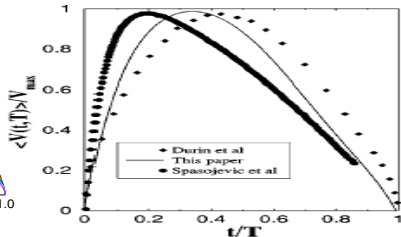
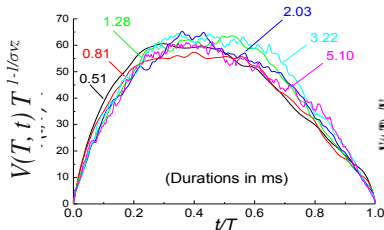
# Asymmetry in the avalanche average shape



Time  $t$



Scaled time  $t/T$

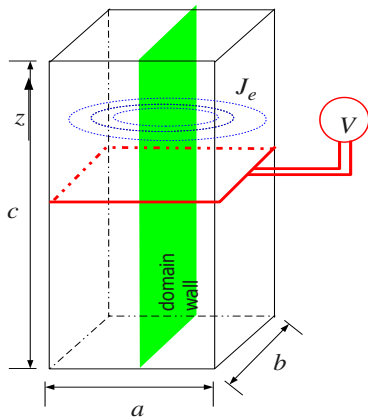


Theory

Experiments

Marked time asymmetry

## The delay of the eddy currents



$$\uparrow \mathbf{H}_e = H_e(x, y, t) \hat{z}$$

$$\nabla^2 H_e = \sigma \mu \frac{\partial H_e}{\partial t}$$

Usual approximation:

**No time delay between  
the magnetization change  
and the eddy current field**

We need to calculate the mean pressure  
integrating  $H_e$  over the thickness



## A negative mass for domain walls!

$$\Gamma v = H_a(t) - H_{dem} + H_p(x)$$

$$\Gamma v + \Gamma_0 \int^t e^{-(t-t')/\tau_0} v(t') dt' / \tau_0$$

Non - local  
damping

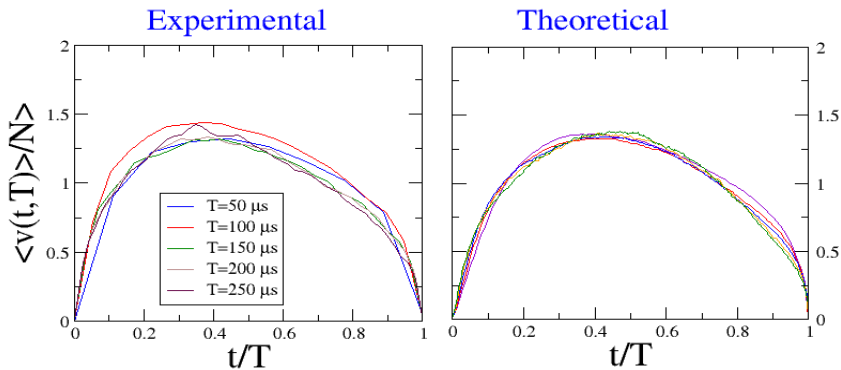
In Fourier space:

$$\tilde{P}_e = [(\Gamma + \Gamma_0) + i\omega \bar{M}] \tilde{v}$$

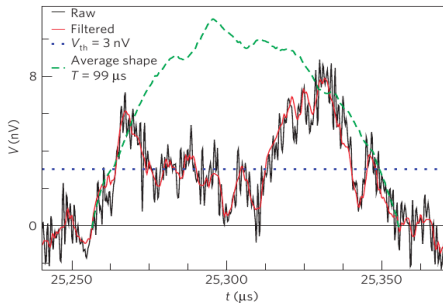
Negative mass!

$$\bar{M} \sim -I_s \Gamma \tau_0$$

## Shapes in experiments and in the model



## Detection of avalanches in thin films



in thin films (Py, 1  $\mu\text{m}$ ),  
the signal to noise is too low  
→ a threshold splits avalanches



we need a good  
filtering technique

Wiegner filter

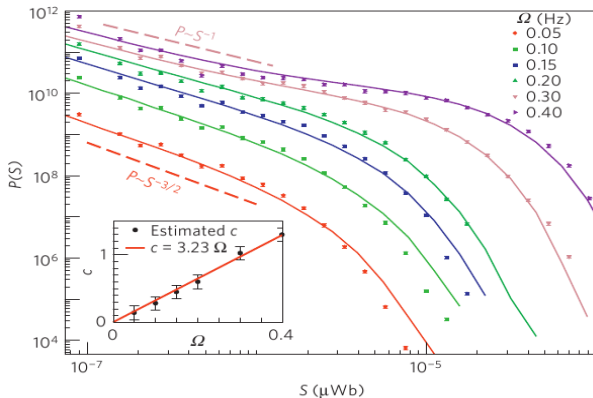
$$\tilde{V}(f) = \frac{\tilde{V}_{out}(f)}{\tilde{h}(f)} \frac{|\tilde{v}(f)|^2}{|\tilde{n}(f)|^2 + |\tilde{v}(f)|^2}$$

← guess of signal spectrum

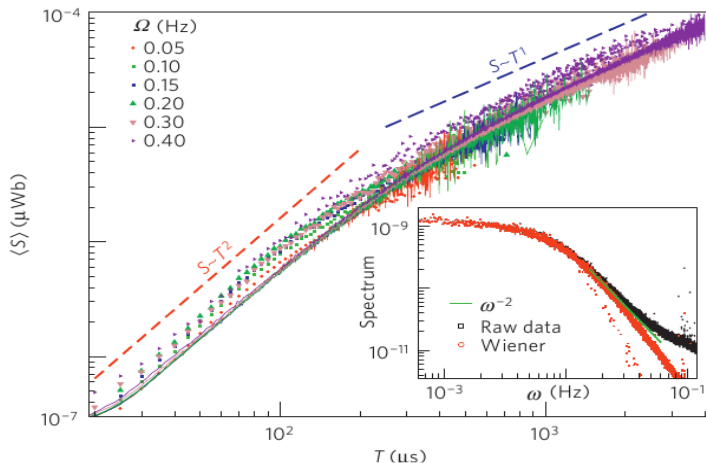
← background noise spectrum

← impulse response

# Size distributions in a 'long range' film (3D)



## The $1/\sigma v z$ again



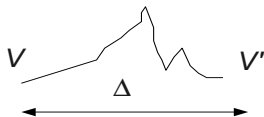
it perfectly follows the model (and no eddy currents)!

## Universal scaling function revisited

$$G_{c,k}(V, t; V', t + \Delta)$$

c: field rate

k: demagnetizing factor



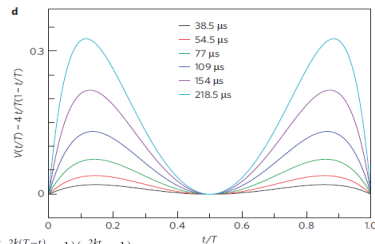
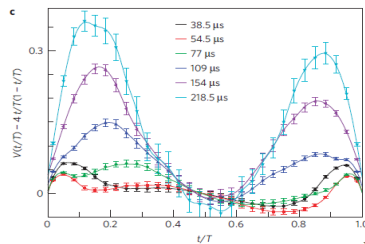
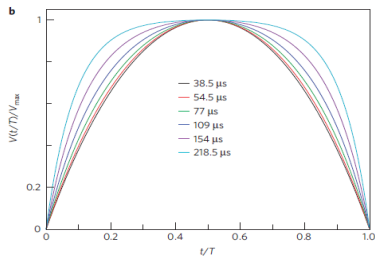
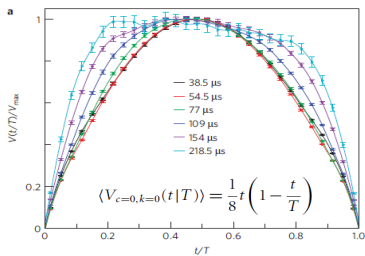
$$\langle V_{c,k}(\Delta|T) \rangle = \frac{\int dV' V' G_{c,k}(0^+, 0; V', \Delta) G_{c,k}(V', \Delta; 0, T)}{\int dV' G_{c,k}(0^+, 0; V', \Delta) G_{c,k}(V', \Delta; 0, T)}$$

$$= T^x \mathcal{V}(\Delta/T, (k/k_0)T^w, c/c_0 T^y)$$

relevant

marginal

# Universal scaling function: results



$$\langle V_{c=0, k}(t|T) \rangle = \frac{1}{2k} \frac{(e^{2k(T-t)} - 1)(e^{2kt} - 1)}{e^{2kT} - 1}$$

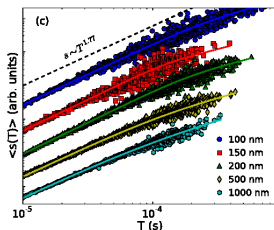
# Just published on PRE: short range films

## General scaling forms

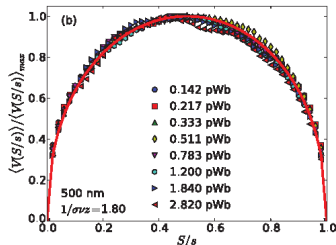
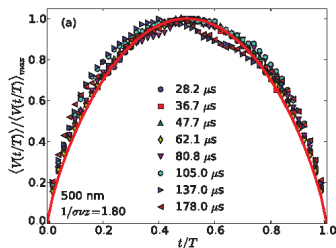
$$\langle V(t|T) \rangle \propto \left[ \frac{t}{T} \left( 1 - \frac{t}{T} \right) \right]^{1/\sigma\nu z - 1}$$

$$\langle V(S|s) \rangle \propto \left[ \frac{S}{s} \left( 1 - \frac{S}{s} \right) \right]^{1 - \sigma\nu z}$$

see Laurson et al, Nat. Com. 4, 2927 (2013)



with  $1/\sigma\nu z = 1.80$ . See Bohn et al, 90, 032821 (2014)





## Something more... from Pierre and Kay

Using normalized units:

- $S/S_m$ , with  $S_m = \frac{\langle S^2 \rangle}{2\langle S \rangle}$
- $T/\tau_m$ , with  $\tau_m$  to be determined

the average shape for avalanches of given size  $S$  follows:

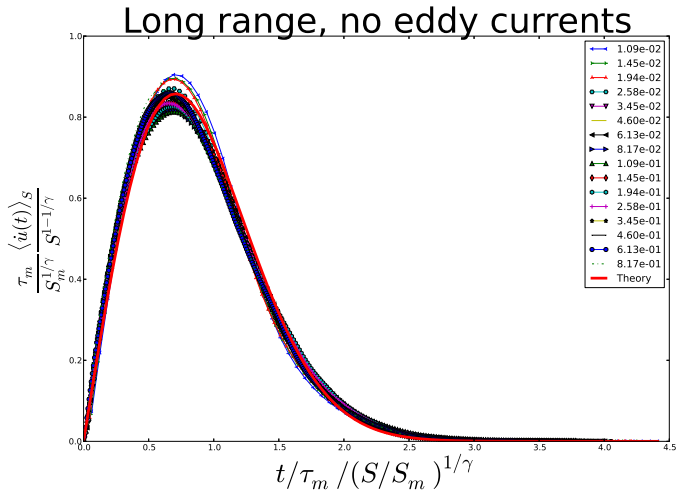
$$\langle v(t) \rangle_S = \frac{S}{\tau_m} \left( \frac{S}{S_m} \right)^{-1/\gamma} F(\tilde{t})$$

with:  $\tilde{t} = \frac{t}{\tau_m} / \left( \frac{S}{S_m} \right)^{1/\gamma}$ ,  $\int dt \langle v(t) \rangle_S = S$ ,  $\int d\tilde{t} F(\tilde{t}) = 1$ .

In the ABBM mean field model, one has:

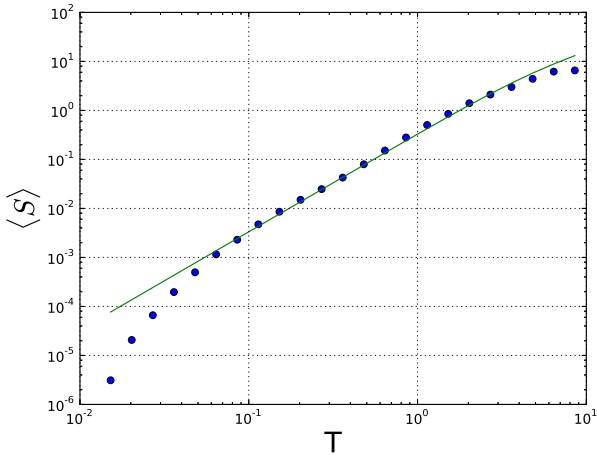
$$F(\tilde{t}) = 2\tilde{t}e^{-\tilde{t}^2}, \gamma = 2$$

# Comparison with experiments (1)



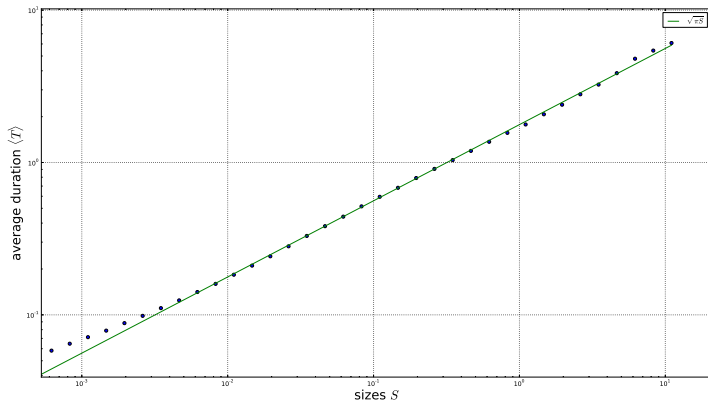
## Comparison with experiments (2)

$$\langle S \rangle = 2T \coth(T/2) - 4$$



## Comparison with experiments (3)

$$\langle T \rangle = \sqrt{\pi S}$$



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# Visualization of DW dynamics in thin films

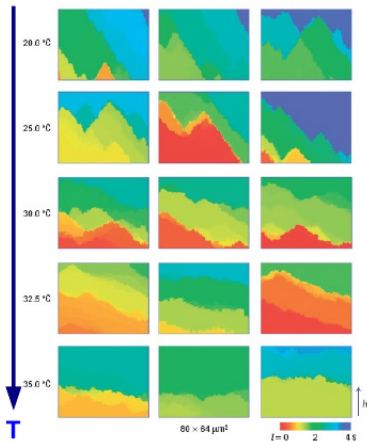
Tunable scaling behaviour observed in  
Barkhausen criticality of a ferromagnetic film

KWANG-SU RYU<sup>1</sup>, HIRO AKINAGA<sup>2</sup> AND SUNG-CHUL SHIN<sup>1\*</sup>

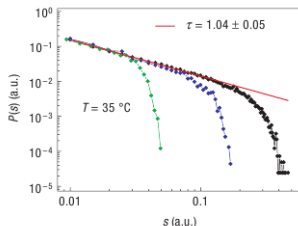
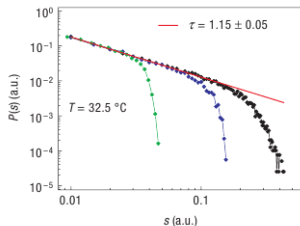
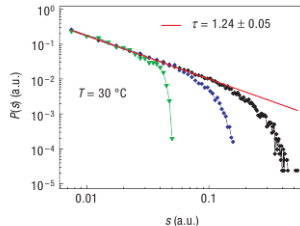
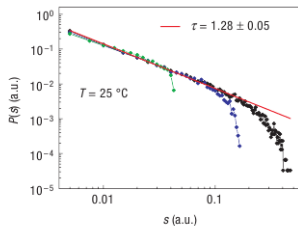
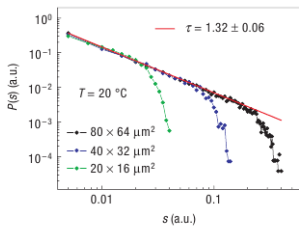
<sup>1</sup>Department of Physics and Center for Nanospinics of Spintronic Materials, Korea Advanced Institute of Science and Technology, Daejeon 305-701, Korea

<sup>2</sup>Nanotechnology Research Institute, National Institute of Advanced Industrial Science and Technology, 1-1-1 Higashi, Tsukuba, Ibaraki 305-8562, Japan

- FM MnAs 50 nm film on GaAs(001)
- Fixed field at 99%  $H_c$
- Different spot sizes
- Local magnetization changes
- $T_c \sim 40$  °C
- Distribution of avalanche sizes  $P(S)$



# Barkhausen avalanche distributions

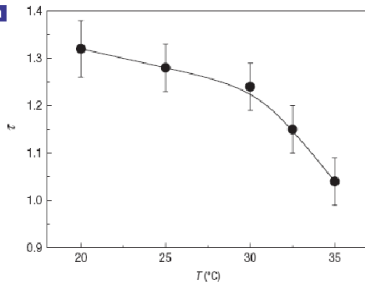


# Cross-over between two universality classes(?)

Zigzag walls **a**



Low temperature /  
high dipolar forces



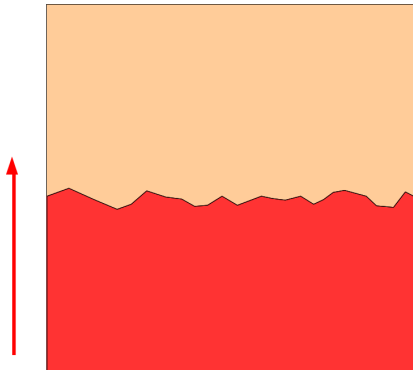
High temperature /  
low dipolar forces



Rough walls



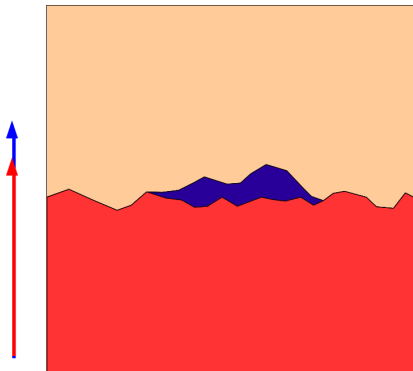
# Avalanches in a window frame



## The effect of the frame

- Front in the full system
- Avalanche in the full system
- Avalanche in the window
- Avalanche cut by smaller windows

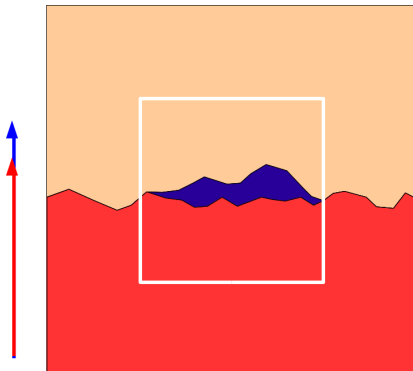
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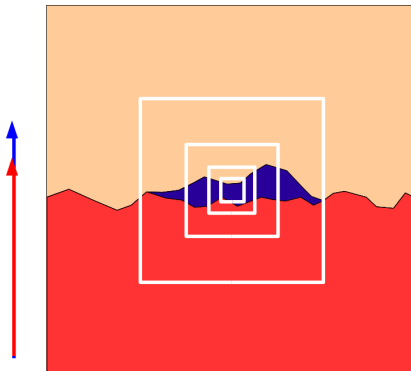
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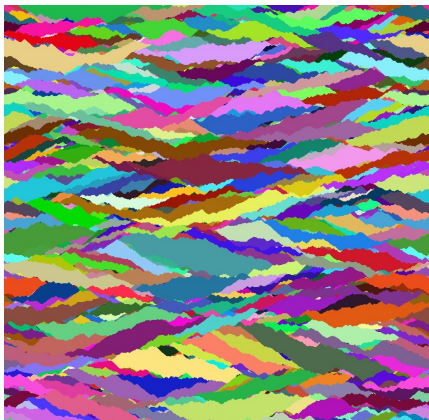
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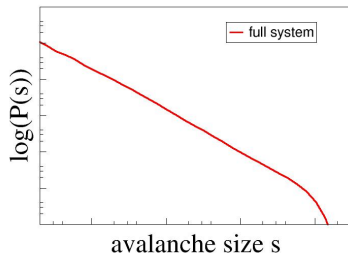
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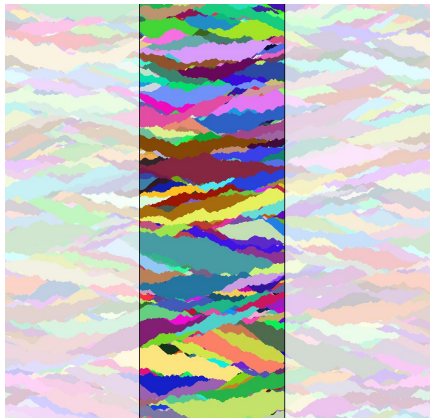
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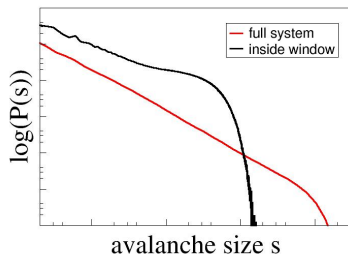
## Distribution of avalanches In the Full System



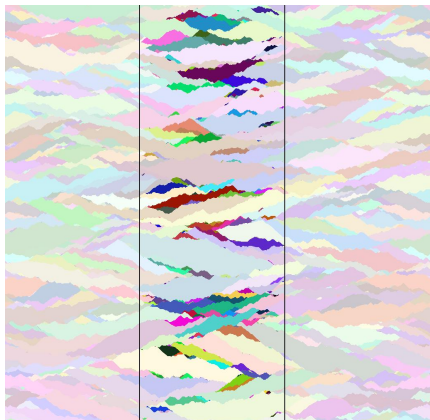
# Avalanches in a window frame



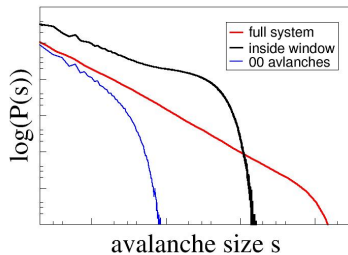
## Distribution of avalanches Within the Window frame



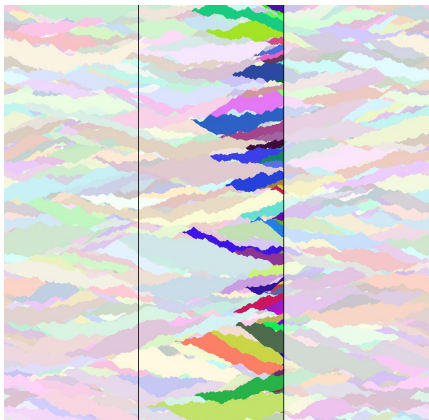
# Avalanches in a window frame



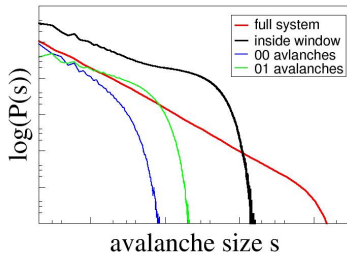
Distribution of avalanches  
No touching any edge (00)



# Avalanches in a window frame

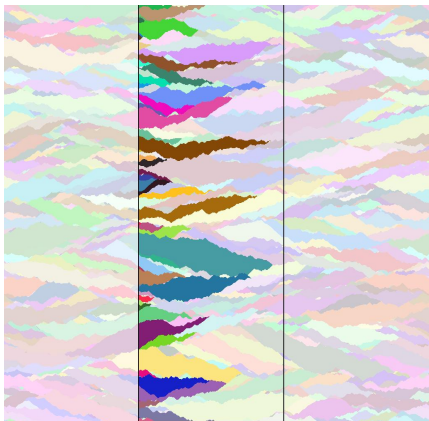


## Distribution of avalanches Touching the right edge(01)

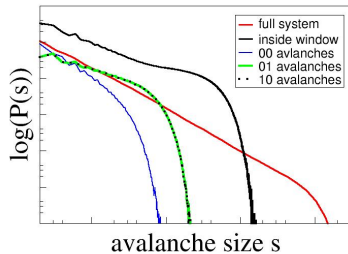




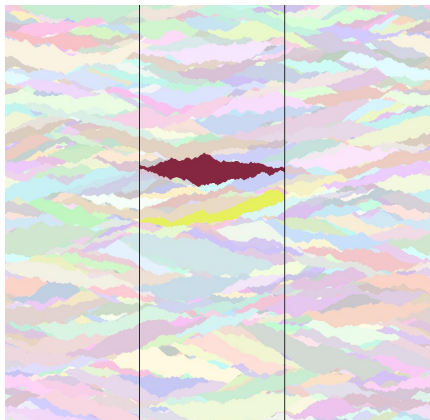
# Avalanches in a window frame



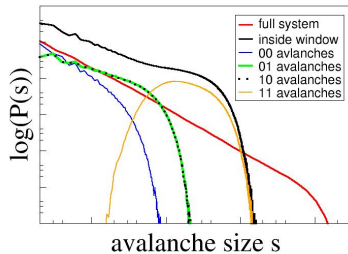
## Distribution of avalanches Touching the left edge (10)



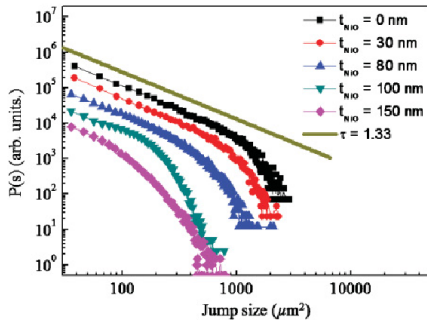
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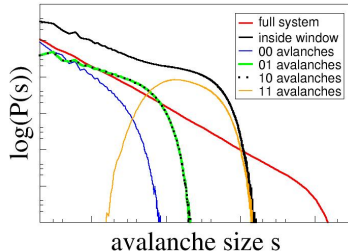
## Distribution of avalanches Touching both edges (11)



# Avalanches in a window frame



## Distribution of avalanches Sound familiar?



# Spatial structure of avalanches in DPD

## Directed Percolation Depinning: the quenched KPZ model

$$\frac{\partial h(x, t)}{\partial t} = F - k \langle h \rangle + \gamma \nabla^2 h + \lambda (\nabla h)^2 + \eta(x, h)$$

- $h(x, t)$ : height of the front
- $F$ : the driving force
- $k$ : the “demagnetization field”
- $\gamma, \lambda$ : linear and non-linear terms
- $\eta$ : gaussian random noise.

## Critical exponents are well known

- size exponent:  $\tau = 1.24$
- roughness exponent:  $\zeta = 0.63$

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# Area-weighted size distributions in the full system

## Traditional size distributions

$$P(S|L_k) = S^{-\tau} \mathcal{P}(S/L_k^{1+\zeta}), \text{ where } L_k \sim k^{-\nu_k}$$

## Problem: normalization depends on lattice space!

$$N^{-1} = \int_{a^2}^{\infty} P(S|k) dS \sim \int_{a^2}^{L_k^{1+\zeta}} S^{-\tau} dS \sim a^{2(1-\tau)} - L_k^{(1-\tau)(1+\zeta)}$$

## The area-weighted size distribution

$$A(S) = S \cdot P(S)$$

$$A(S|L_k) = L_k^{(\tau-2)(1+\zeta)} S^{1-\tau} \mathcal{A}_{Sk}(S/L_k^{1+\zeta})$$

$$= (S/L_k^{1+\zeta})^{2-\tau} \mathcal{A}_{Sk}(S/L_k^{1+\zeta}) / S = S_k^{2-\tau} \mathcal{A}_{Sk}(S_k) / S$$

This is the fraction of the full system area covered by avalanches with sizes between  $S$  and  $S + dS$ .

# Theoretical avalanche distributions in the window

## Internal (00) avalanches

$$A_{00}(s|W, L_k) = L_k^{(\tau-2)(1+\zeta)} s^{1-\tau} \mathcal{A}_{00} \left( \frac{s}{L_k^{1+\zeta}}, \frac{W}{L_k} \right)$$

## Split (01-10) avalanches

$$A_{10}(s|W, L_k) = \frac{1}{W} L_k^{(\tau-2)(1+\zeta)} s^{1-\tau+1/(1+\zeta)} \mathcal{A}_{10} \left( \frac{s}{L_k^{1+\zeta}}, \frac{W}{L_k} \right)$$

## Spanning (11) avalanches

$$A_{11}(s|W, L_k) = \frac{1}{s} \left( \frac{s}{WL_k^\zeta} \right)^{(2-\tau)(1+\zeta)/\zeta} \mathcal{A}_{11} \left( \frac{s}{WL_k^\zeta}, \frac{W}{L_k} \right)$$



# SloppyScaling environment

## The goal

Fitting  $A_{00}, A_{10}, A_{11}$  together, with a functional form of the  $\mathcal{A}_{00}, \mathcal{A}_{10}, \mathcal{A}_{11}$  universal functions *plus* corrections to scaling.

## Functional forms of $\mathcal{A}_{xy}$ universal functions

$$\mathcal{A}_{00} = \exp\left(-\left(U_{00}s_k^{1/2} + Z_{00}s_k^{\delta_{00}} + C_{00}\left(\frac{s_k}{W_k^{n_{00}}}\right)^{m_{00}}\right)\right)$$

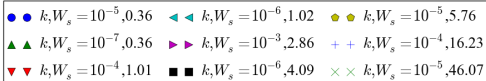
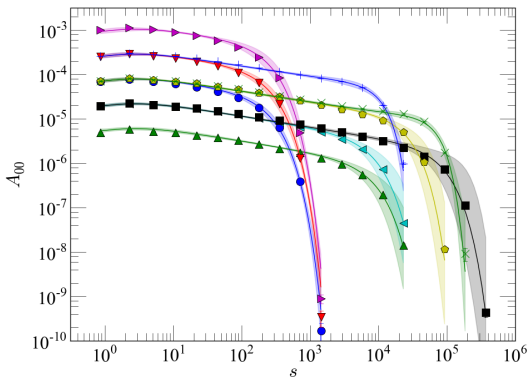
$$\mathcal{A}_{10} = \exp\left(-\left(U_{10}s_k^{1/2} + Z_{10}s_k^{\delta_{10}} + C_{10}\left(\frac{s_k}{W_k^{n_{10}}}\right)^{m_{10}}\right)\right)$$

$$\mathcal{A}_{11} = \exp\left(-\left(U_{11}s_k^{1/2} + Z_{11}s_k^{\delta_{11}} + D_{11}\left(\frac{s_k}{W_k}\right)^{m_1} + C_{11}\left(\frac{s_k}{W_k^{n_{11}}}\right)^{-m_2}\right)\right)$$

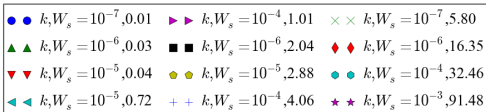
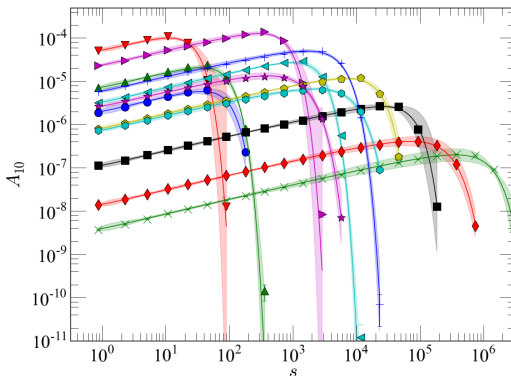
## In sum

3 functions, 27 fitting parameters, 24 data sets (for different  $L_k$  and  $W$ ),  $133 + 167 + 60 = 360$  points

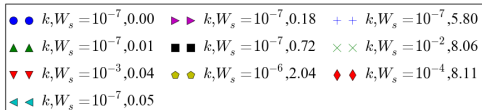
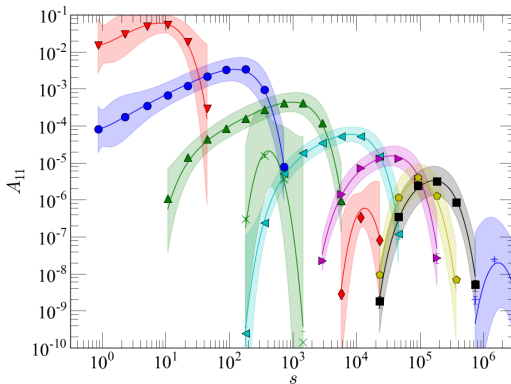
# Multiple data fits



# Multiple data fits



# Multiple data fits

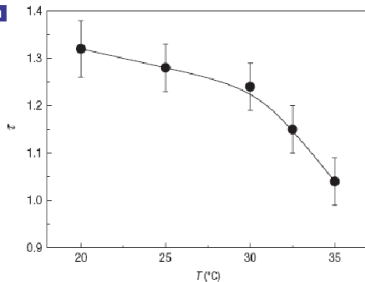


# Cross-over between two universality classes(?)

Zigzag walls **a**



Low temperature /  
high dipolar forces



High temperature /  
low dipolar forces



Rough walls

# A simple front propagation model

Eq. of motion of DW segment along the vertical direction

$$\Gamma \frac{\partial h_i}{\partial t} = \frac{1}{\cos \theta_i} \left[ \gamma_w \frac{\partial^2 h_i}{\partial x^2} + \right. \quad \text{elastic}$$
$$2M_s \mu_0 H_a + \quad \text{field}$$
$$\eta(i, h_i) + \quad \text{noise}$$
$$\left. 4 \mu_0 M_s^2 \Delta_z^2 \sum_{j \neq i} \frac{h_i - h_j}{[\Delta_z^2 (i - j)^2 + (h_i - h_j)^2]^{3/2}} \right] \quad \text{dipolar}$$

Laurson, L.; Durin, G. Zapperi, S. PRB 89, 104402 (2014)

## A simple front propagation model

Eq. of motion of DW segment along the vertical direction

$$\Gamma \frac{\partial h_i}{\partial t} = \frac{1}{\cos \theta_i} \left[ \gamma_w \frac{\partial^2 h_i}{\partial x^2} + 2M_s \mu_0 H_a + \eta(i, h_i) + 4 \mu_0 M_s^2 \Delta_z^2 \sum_{j \neq i} \frac{h_i - h_j}{[\Delta_z^2 (i - j)^2 + (h_i - h_j)^2]^{3/2}} \right]$$

Eq. of motion in dimensionless units

$$\frac{\partial h_i}{\partial t} = \frac{1}{\cos \theta_i} \left[ \lambda \frac{\partial^2 h_i}{\partial x^2} + F_{ext} + \eta(i, h_i) + 4 \sum_{j \neq i} \frac{h_i - h_j}{[(i - j)^2 + (h_i - h_j)^2]^{3/2}} \right]$$

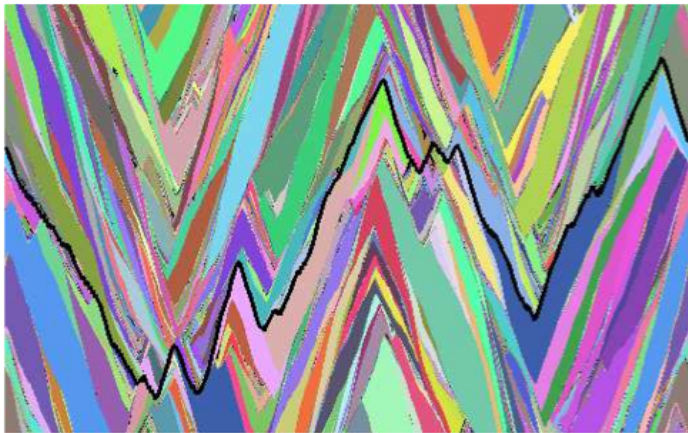
where  $\lambda = l_D / \Delta_z$ , with  $l_D = \gamma_w / (\mu_0 M_s^2)$  the “domain formation”

# A simple front propagation model



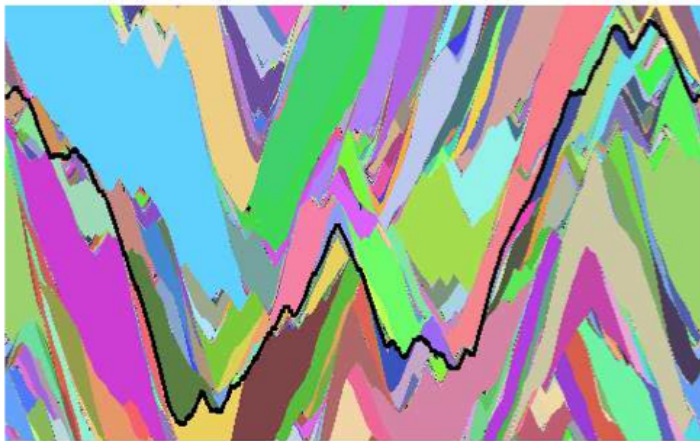


# The effect of length $\lambda$



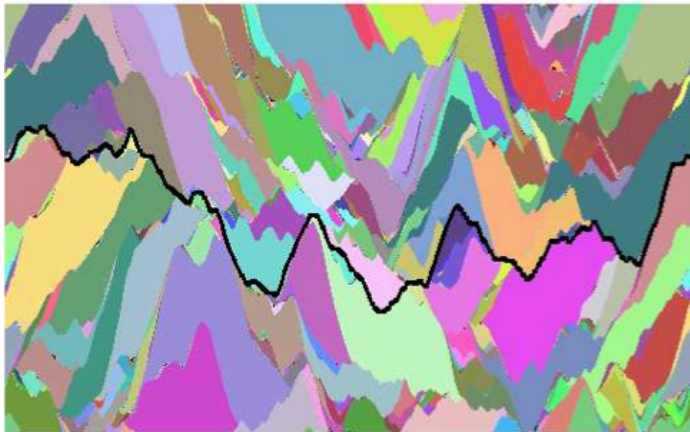
$\lambda = 1$

# The effect of length $\lambda$



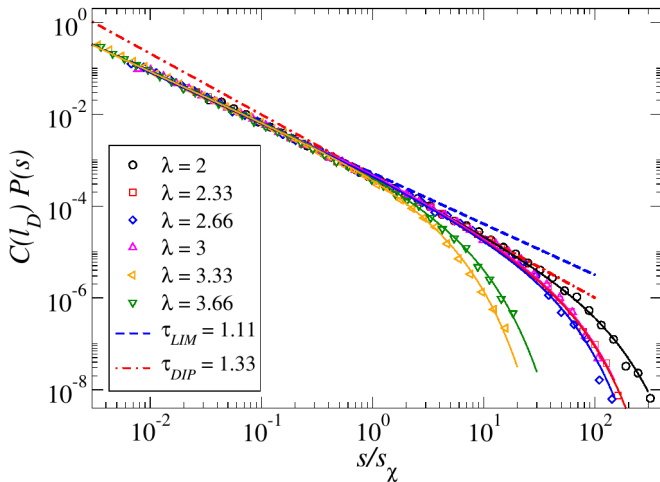
$\lambda = 2$

# The effect of length $\lambda$

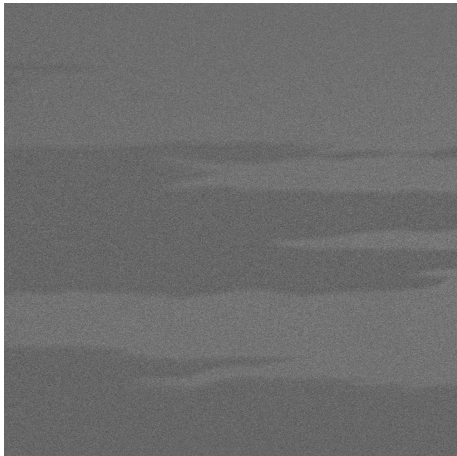


$\lambda = 4$

# The real crossover: elastic vs. dipolar

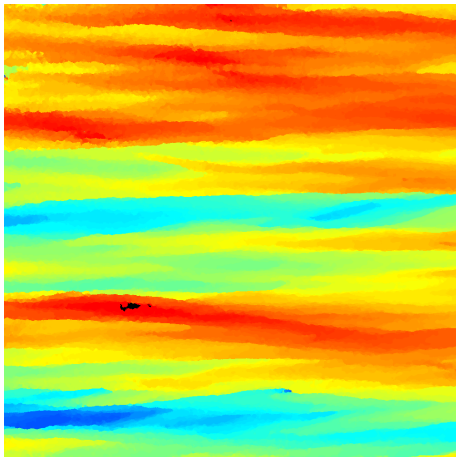


## Getting avalanches from MOKE experiments



- Domain wall dynamics in a  $NiO(t_{NiO})/Fe(30nm)$  with  $t_{NiO} = 80nm$
- Fixed field applied in the horizontal direction
- Magnification: 10x (values: 5, 10, 20, 50)
- Area:  $900 \times 900 \mu m^2$
- Camera Speed: 2.5 frames/s

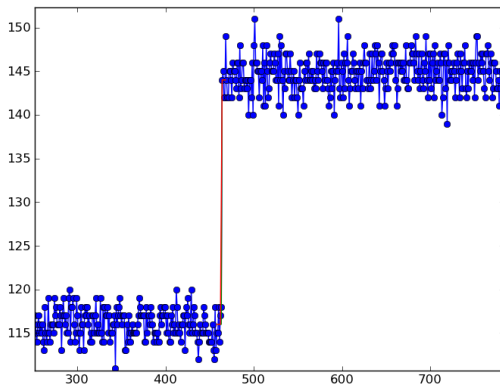
# Getting avalanches from MOKE experiments



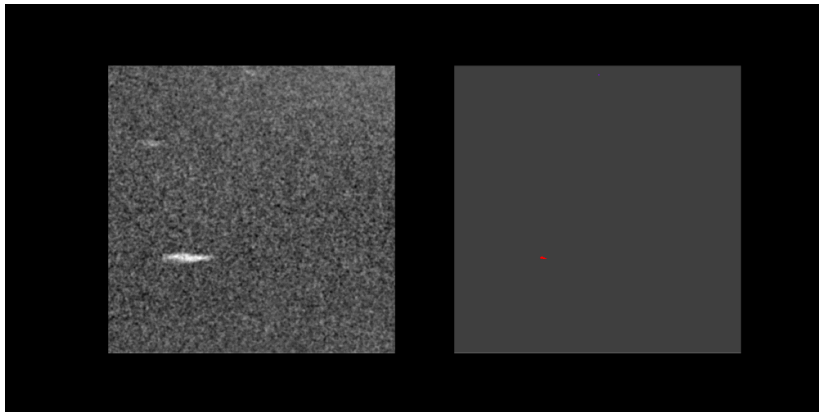
- Domain wall dynamics in a  $NiO(t_{NiO})/Fe(30nm)$  with  $t_{NiO} = 80nm$
- Fixed field applied in the horizontal direction
- Magnification: 10x (values: 5, 10, 20, 50)
- Area:  $900 \times 900 \mu m^2$
- Camera Speed: 2.5 frames/s

# Pixel analysis

Detect grey level change for each pixel

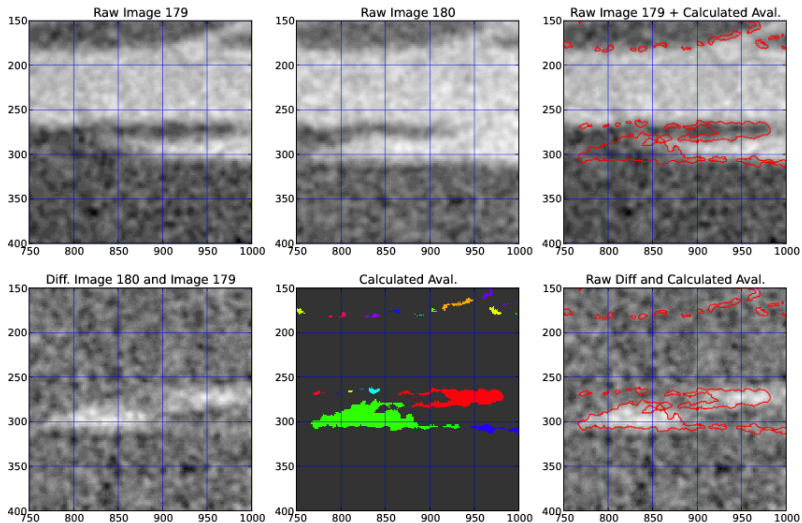


# Pixel analysis

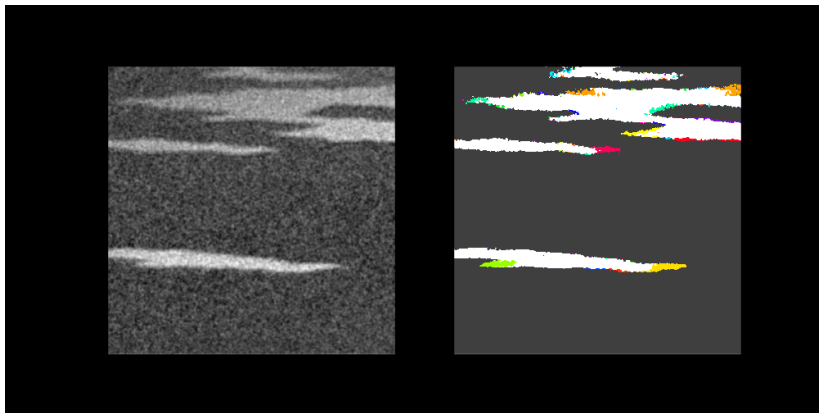




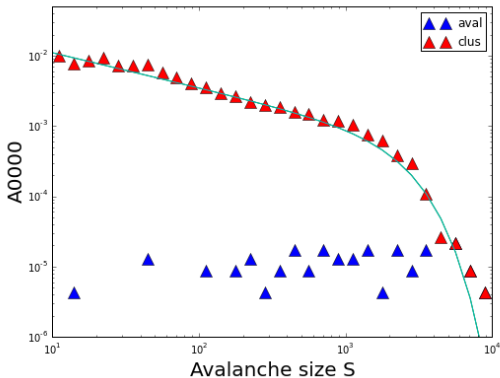
# Pixel analysis



# Avalanches or clusters?

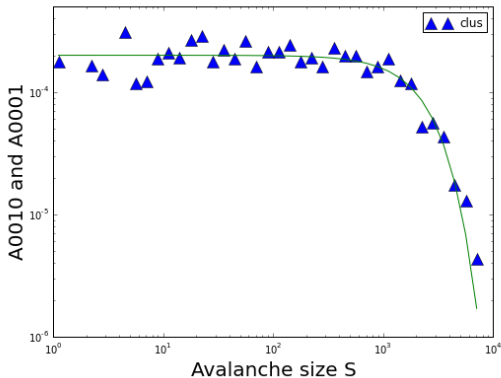


# Not yet exhaustive



For clusters:  $A_{00}(S) \sim S^{1-\tau} \mathcal{A}_{00}(S/S_0)$  with  $\tau \sim 1.5$

# Not yet exhaustive



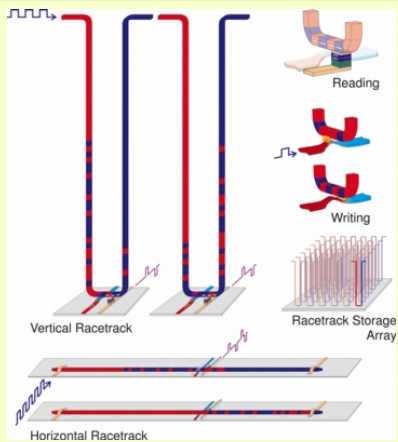
For clusters:  $A_{01}(S) \sim S^{1-\tau+1/(1+\zeta)} \mathcal{A}_{01}(S/S_o)$

# Outline

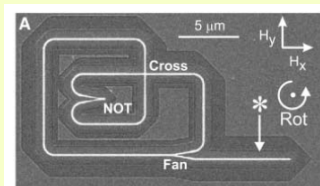
- 1 Magnetization dynamics: temporal structure
  - Universality and depinning transition
  - Asymmetry in the avalanche average shape
  - Simmetric avalanches in thin films
- 2 Magnetization dynamics: spatial structure
  - Spatial avalanches in a window
  - Searching for the universality classes
  - Experimental avalanches from MOKE
- 3 Domain walls for spintronics devices
  - Future DW devices
  - Role of disorder in DW dynamics
  - Creep and DW structure

# DW for spintronics devices

## Racetrack memory (2008)



## Magnetologic memory (2005)



## DW oscillator (2008)

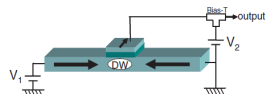


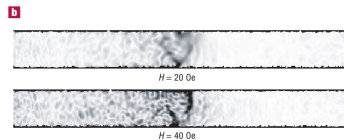
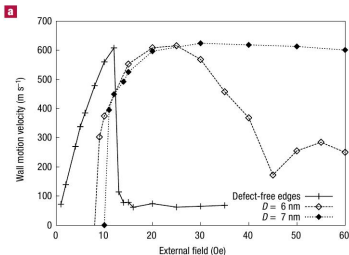
Fig. 3. Schematic illustration of a three-terminal device that produces microwaves by utilizing the current-induced DW rotation.

# Role of disorder in DW dynamics: rough edges

LETTERS

## Faster magnetic walls in rough wires

YOSHINOBU NAKATANI<sup>1,2</sup>, ANDRÉ THIAVILLE\*<sup>1</sup> AND JACQUES MILTAT<sup>1</sup>

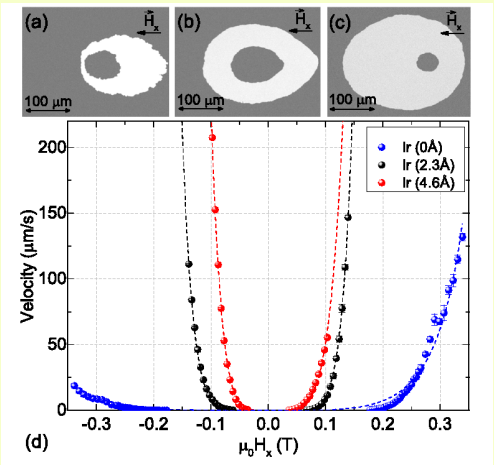


Turbulent DW motion:  
no Walker breakdown

Main conclusion...

*Roughness should rather be engineered than avoided*

## Creep and DW structure





Thank you very much for your attention