

# Numerical Simulations of Neutron Star-Neutron Star and Black Hole–Neutron Star Binaries:

Introduction and status report  
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# Observational Motivations

- Binary pulsars observed
- Predict  $\sim 10^1$  NS-NS detections per year for advanced LIGO
- (Unfortunately, merger waves are  $\sim$  kHz)
- Electromagnetic counterpart – short GRBs?
- Neutrino counterpart?

# NS-NS evolution overview

- Inspiral → ISCO → plunge →  $\sim 3M_{\odot}$  remnant
- 2 possibilities
  - Prompt collapse
  - Quasi-stationary **hypermassive** star
- Remnant may form an **ellipsoid**
  - GW signal → spin down → collapse + no disk
- Remnant core may be spun down by **MRI**
  - Collapse + big disk → GRB?

# BH-NS evolution overview

2 possibilities:

1)  $M_{BH} > 4 M_{NS} \rightarrow$  NS swallowed whole

2)  $M_{BH} < 4 M_{NS}$ ,  $\frac{M_{BH} R_{NS}}{r^3} > \frac{M_{NS}}{R_{NS}^2}$

$\rightarrow$  Roche lobe overflow

mass transfer may be

- unstable: tidal destruction of NS
- stable: multiple mass transfers

# Parameter Space

- Inspiring NS are (to 1<sup>st</sup> approximation)
  - cold ( $P_{\text{th}} \blacksquare P_{\text{cold}}$ ), irrotational ( $\Omega_{\text{sp}} \blacksquare \Omega_{\text{orb}}$ ), with low B field ( $B^2 \blacksquare P$ )
- 1) Real parameters which vary significantly
  - NS mass(es), BH mass and spin (for BH-NS)
- 2) Parameterized ignorance
  - Equation of State (EoS):  $P = P(\rho, T, Y_e)$
- EoS-dependent tidal effects affect inspiral
- EoS affects ISCO or disruption radius
- Signs of stiff EoS:
  - Ellipsoidal remnant (for NS-NS)
  - Multiple mass transfers (for BH-NS)

# Potentially Relevant physics

- GR ( $Rc^2/GM \sim 5$ )
- Cold EoS
- Hot EoS
  - Study by [Oechslin, Janka, and Marek 2007](#)
  - Esp. important for disks around final BH
- Magnetic fields
  - Rapid growth in NS-NS remnant
  - c.f. [Price and Rosswog \(2006\)](#), [Duez et al \(2006\)](#)
- Neutrino cooling/emission/radiation pressure
  - Crucial for understanding post-merger disk, GRB generation

# Two paths to dynamical simulations

1. Complicated microphysics,  
simplified (e.g. Newtonian) gravity
2. Exact general relativity,  
simplified (e.g. polytropic) description  
of matter

# NS-NS binaries: the state of the art

## An incomplete survey

- Newtonian
  - Price & Rosswog (2006): 1<sup>st</sup> NS-NS merger simulation with *magnetic fields*,  $T, Y_e$ -dependent EoS of Shen (1998), neutrino effects,  $Y_e$  evolution, SPH
  - Ruffert & Janka (2001):  $T, Y_e$ -dependent EoS of Lattimer-Swesty (1991), PPM FD FMR
- Conformal
  - Oechslin, Janka, & Marek (2007): Shen & LS EoS,  $Y_e$  advected
- Full GR
  - Shibata & Taniguchi (2006):  $T=0$  APR & SLy EoS, PPM FD uniform grid,  $\Delta x \sim 0.15 M_0$ ,  $L \sim 0.45 \lambda_{\text{GW}0}$



# BH-NS binaries: the state of the art

- Newtonian
  - Janka (1999): LS EoS, neutrino effects
- Newtonian + Paczynski-Wiita potential
  - Rosswog (2005): Shen EoS, neutrino effects
- Conformal
  - Faber et al (2006): limited to  $M_{\text{NS}} \ll M_{\text{BH}}$
- Full GR
  - Shibata & Taniguchi (2007), Etienne *et al* (2007), use  $\Gamma=2$  polytropes
- Note: BH spin effects have not been studied in these simulations, but they are very important (c.f. Rantisiou *et al* 2007)

# Short gamma ray burst properties

- cosmological distances
- $L \sim 10^{50}$  erg, duration  $< 2$  sec, hard spectrum
- Compact source
- Nonthermal spectrum  $\rightarrow$   $\gamma$ -rays emitted from ultrarelativistic ( $\Gamma \sim$  hundred) outflow
- Found in non-star forming regions
- No evidence of associated SNe
- Sometimes, reactivation of source (X-ray flares)

# Recipe for a GRB central engine

- Need to dump a lot of energy into a region with not much matter
- Need to do it in 10-100ms

## Massive hyperaccreting disk around a BH

- Baryon poor region above disk
- Energy extracted by thermal neutrino radiation or magnetic fields
- Do NS-NS or BH-NS mergers create the right setup?

# Things to consider

- How to survey the parameter space (esp. EoS)?
- How much physics do we need for just the gravitational waves?
- How far back must numerical simulations start?
- How to combine gravitational and EM signals?
  
- Other sources
- Collaboration with a third community: computational astrophysicists

# BH-NS binaries with a mixed pseudospectral / finite difference code

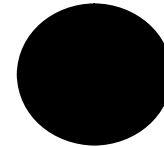
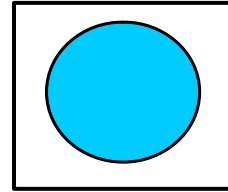
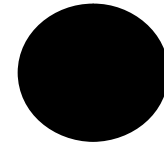
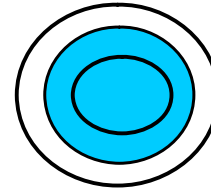
Matt Duez, Larry Kidder, Saul Teukolsky

- FD/FV codes
  - Good at capturing discontinuities
  - Require large grids
- PS codes
  - Rapid convergence for smooth solutions
  - Problems with discontinuities
- FD for hydro, PS for  $g_{\mu\nu}$ ? [Dimmelmeier et al (2005)]

- Why?

- Loss of accuracy in PS code limited to few domains

- FD code only needs to cover matter



Test: equal mass BH-NS binary

