



Hurricanes and Tornados in Planet Formation

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KITP, Feb 12th 2004



Vortex Formation via the Global Baroclinic Instability
in Protoplanetary Accretion Disks **Klahr & Bodenheimer,**
ApJ, 2003, 582, 869

The Global Baroclinic Instability in Accretion Disks. II:
Local Linear Analysis **Klahr, ApJ, 2004, in press**

Formation of Giant Planets by Concurrent Accretion of
Solids and Gas inside an Anti-Cyclonic Vortex
Klahr & Bodenheimer, ApJ, submitted

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Things I will and things I will not talk about today, as this is an informal talk :

- Where do vortices come from?
- What is the lifetime of vortices?
- The 1m->1km Problem in Planet Formation!
- Vortices and the Core Accretion Model.

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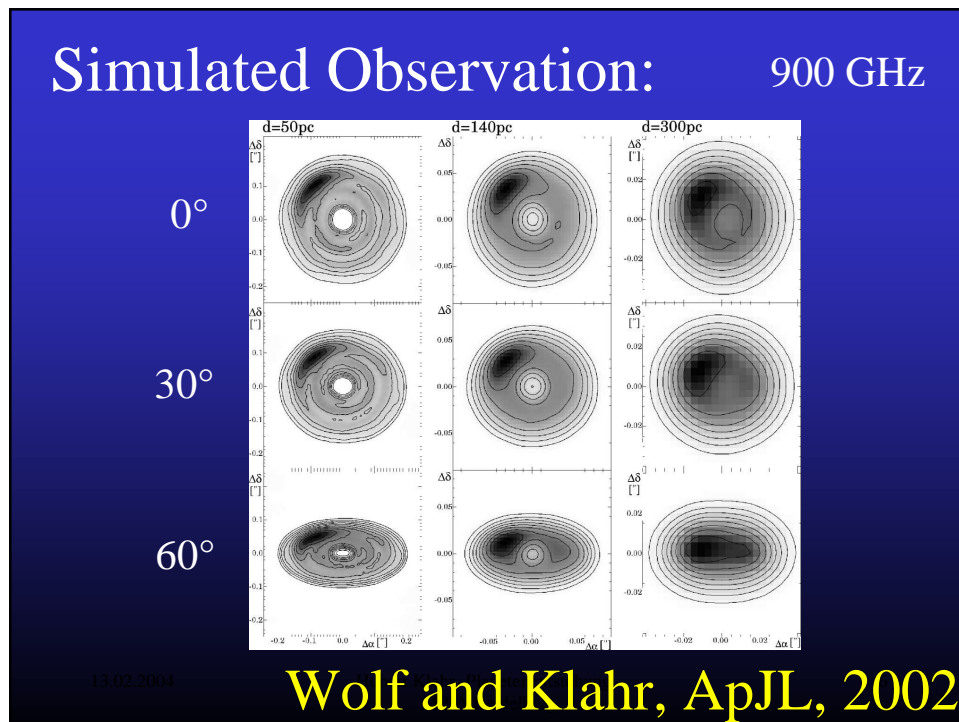
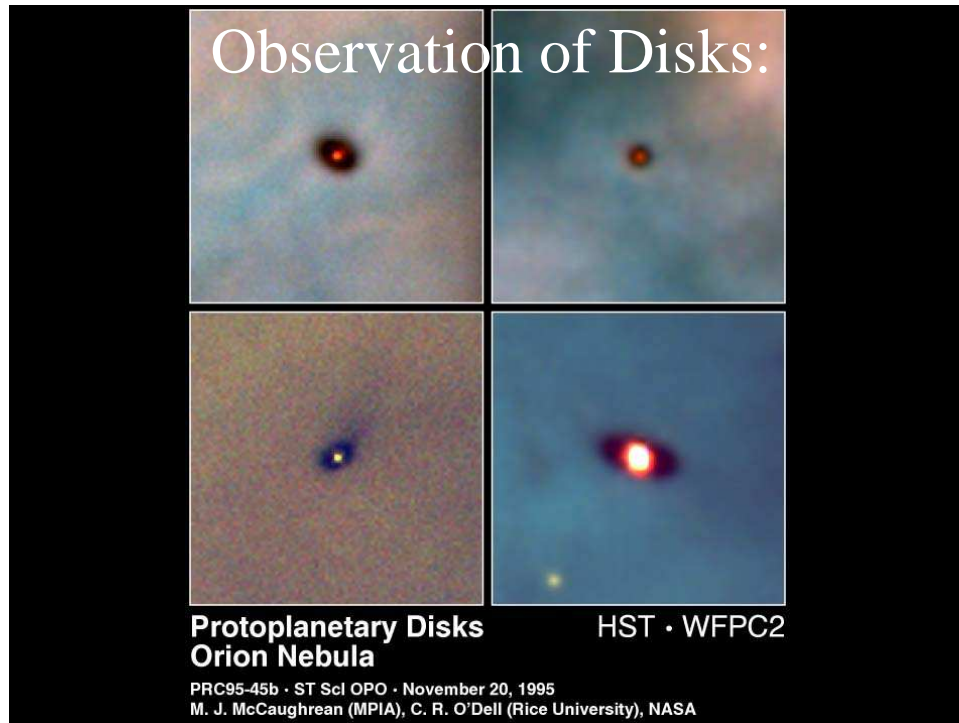
Where do vortices come from?

- Primordial: [Barranco & Marcus 2000](#)
- (MHD -) Turbulence in general:
- Rossby Wave Instability: [Li et al. 2001](#)
- Global Baroclinic Instability: [Klahr & Bodenheimer 2003](#)

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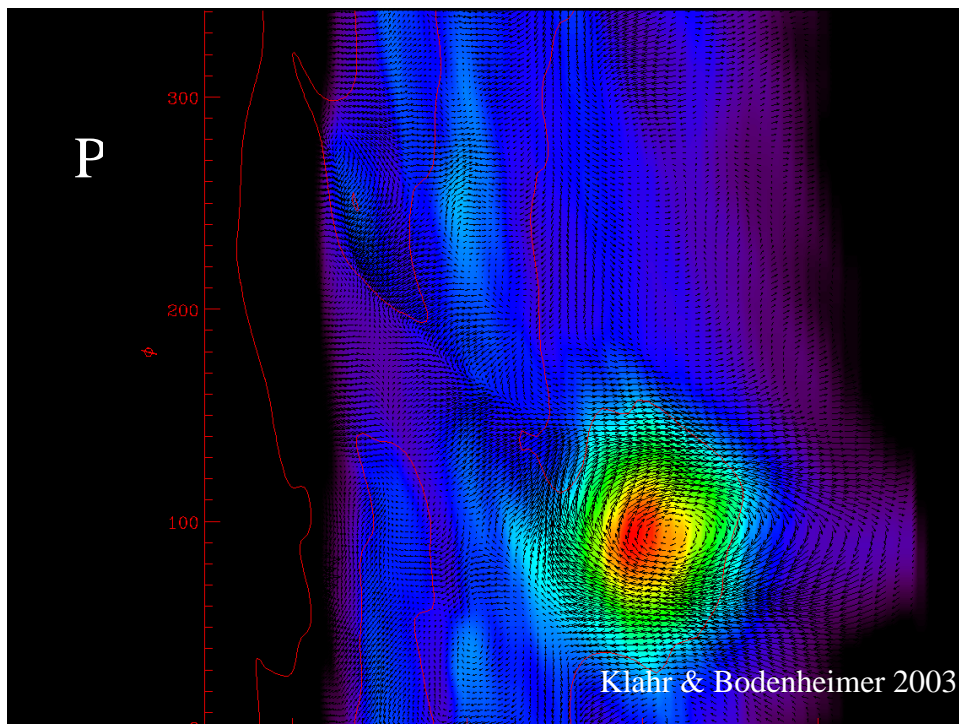
Part of the disk is not ionized enough
for magnetic instabilities to work!



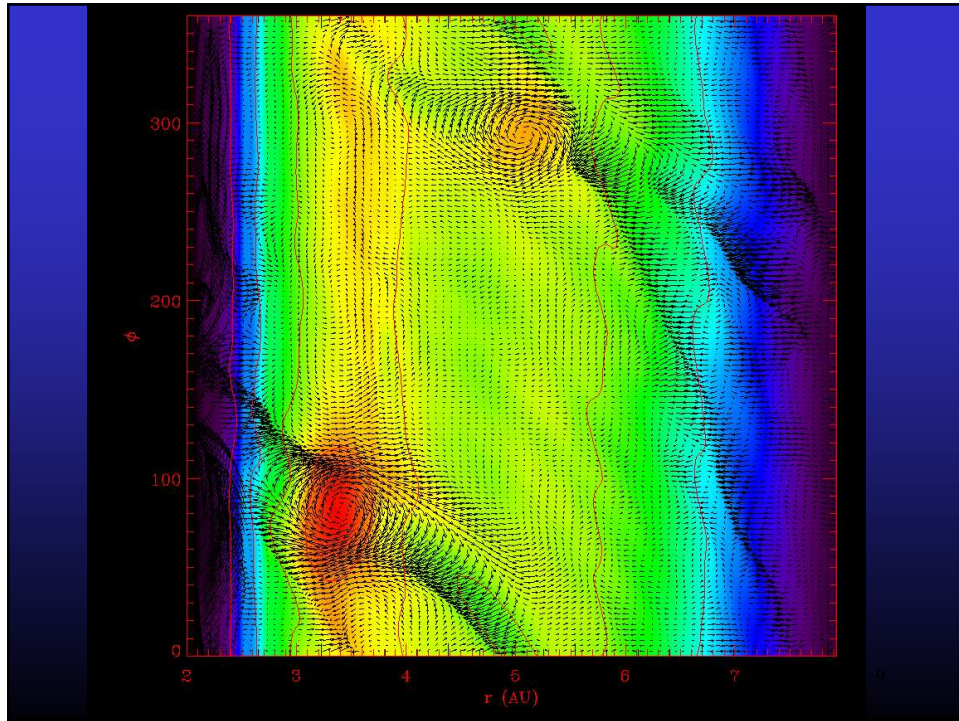
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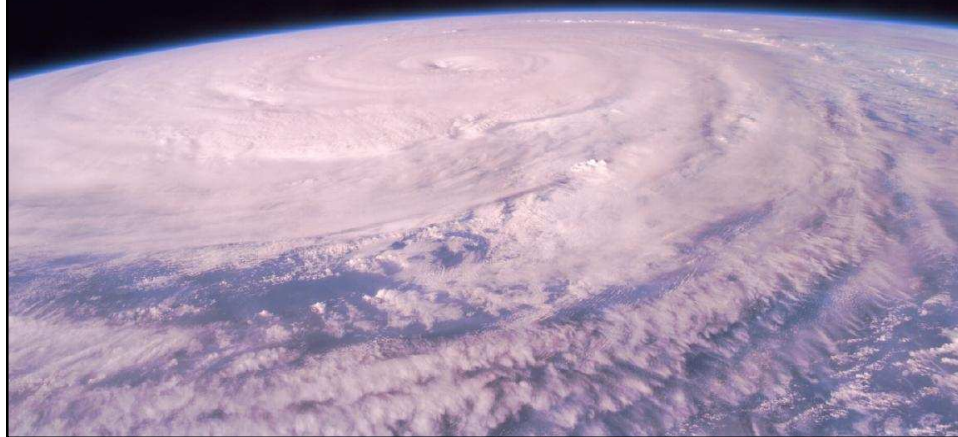
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Vortices in Planet Formation



Baroclinic Effects on Earth: Formation of Hurricanes



Buoyancy in the radial direction of a rotating system can lead to Rossby waves, which can break into vortices.

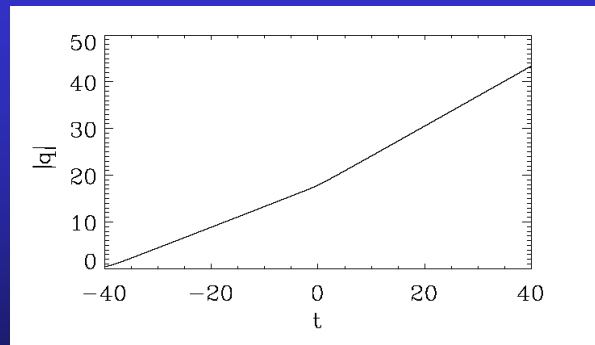
Klahr 2004 ApJ, in press

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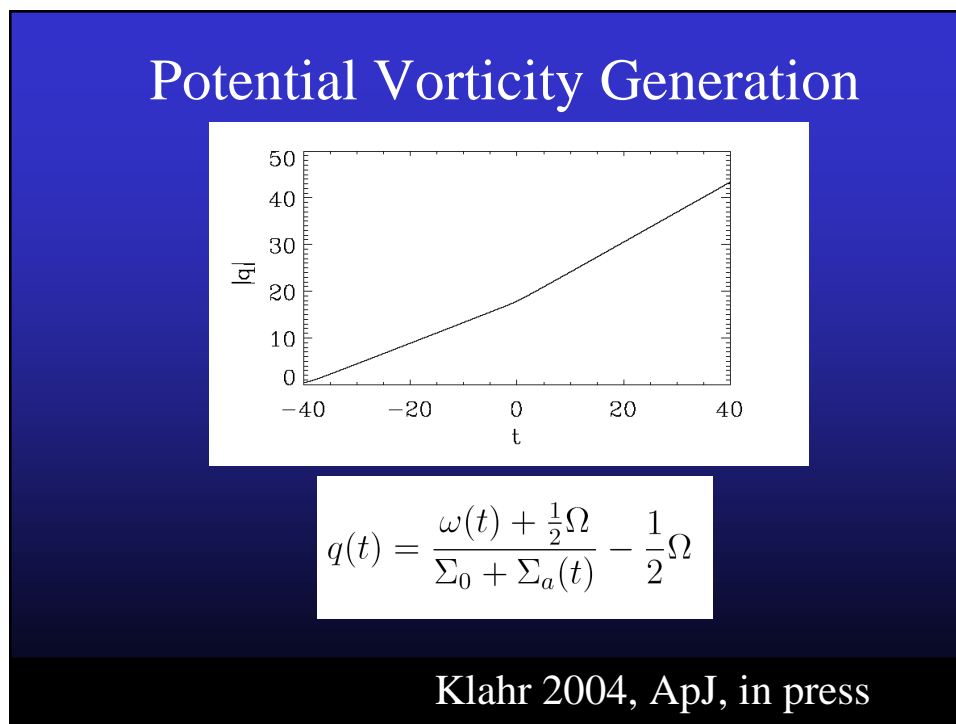
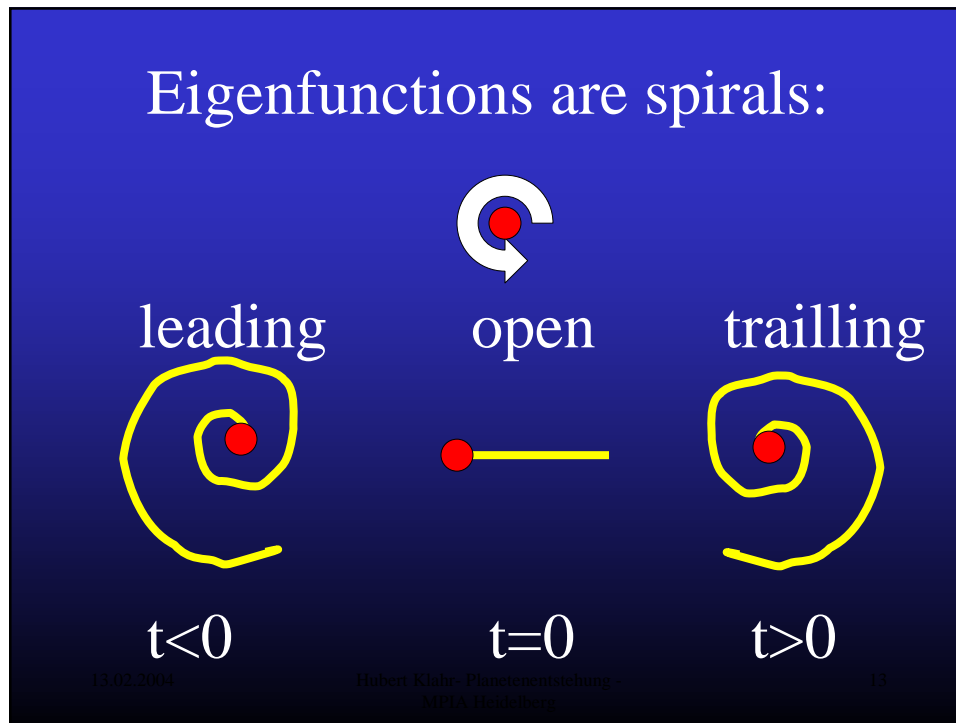
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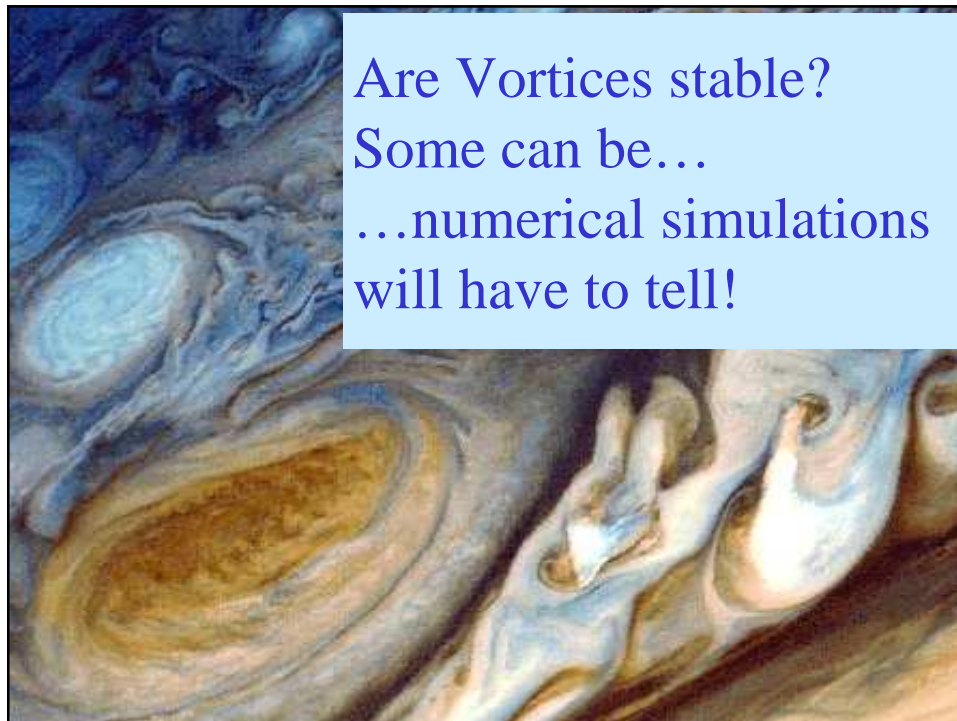
Potential Vorticity Generation



$$q(t) = \frac{\omega(t) + \frac{1}{2}\Omega}{\Sigma_0 + \Sigma_a(t)} - \frac{1}{2}\Omega$$

Klahr 2004, ApJ, in press





The biggest Problem
in Planet Formation:

Experiments by
Blum & Wurm show:
No sticking if $dV > 10\text{m/s}$
(~1m boulders)

sedimentation & radial drift:

Growth by sweep up of tiny dust grains.

=> 1m boulders get lost to the star.

The biggest Problem
in Planet Formation:

How to grow boulders
from 1m to 100m?

dust \Rightarrow 1m ... 100m \Rightarrow Planet Core

surface tension \rightarrow $dV > 10\text{m/s}$? \rightarrow gravity

Vorticity can help!

The diagram illustrates the growth of boulders from dust to planet core. It shows a yellow dot representing dust on the left, which grows into a vertical yellow line representing a 1m boulder. A red arrow labeled 'surface tension' points from the dust towards the 1m boulder. To the right of the 1m boulder is a red question mark, and above it is the text 'dV > 10m/s'. A second red arrow labeled 'gravity' points from the 1m boulder towards a larger red semi-circle on the right representing the planet core. Below the diagram, the text 'Vorticity can help!' is written.

A possible Solution:

Capture of boulders in
vortices.

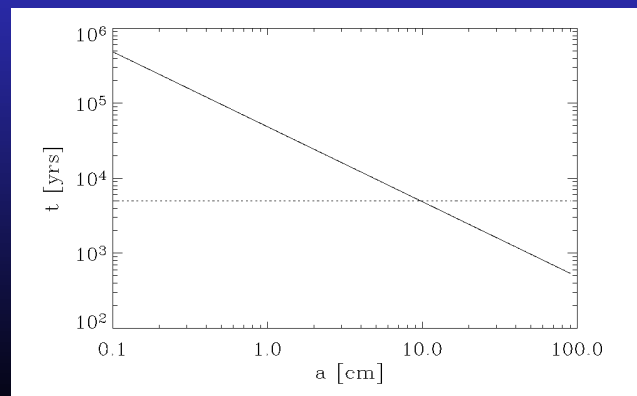
\Rightarrow 0.1m boulders get trapped in vortices.

The diagram shows a yellow star on the left emitting a light blue cone representing a protoplanetary disk. Inside the disk, a blue oval represents a vortex with red curved arrows indicating its rotation. A red line with a dot at the end shows a boulder's path starting from the outer edge of the disk and spiraling inward to be captured by the vortex. Below the diagram, a blue box contains the text '=> 0.1m boulders get trapped in vortices.'

Core Accretion in Vortices

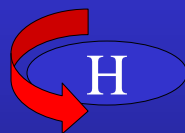
(Bodenheimer & Klahr submitted.)

Comparison between timescales for drift versus growth
@ 7AU in minimum mass nebula:



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What makes a vortex so special?
In contrast to the disk...



Pressure Maximum = Eye

... a vortex (Eye) moves at Keplerian rate!

... a vortex has no vertical shear.

... a vortex has a non turbulent Eye!

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Anti Cyclonic Vortices are Dust Traps!

Balance between Centrifugal Forces, Gravity and Friction.

Inner side : Gas faster than Kepler!

Surplus of Centrifugal Acceleration:

⇒ Drift of dust outward towards the vortex center

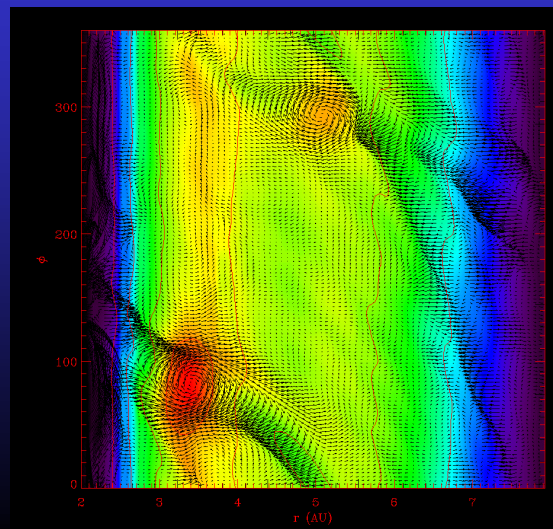
Analog: Outer side Drift inwards

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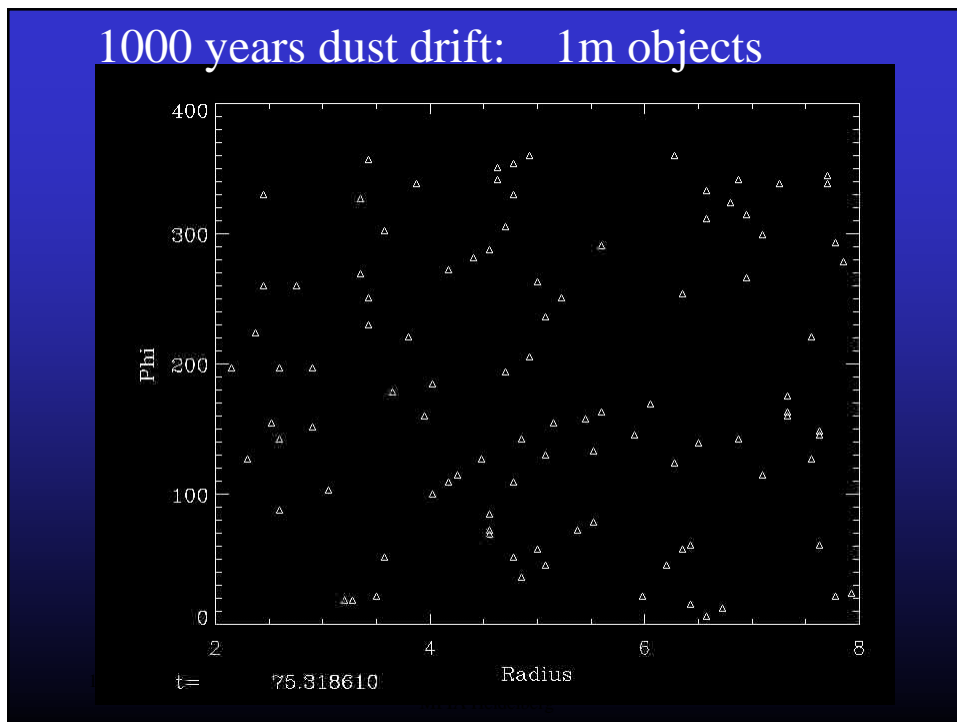
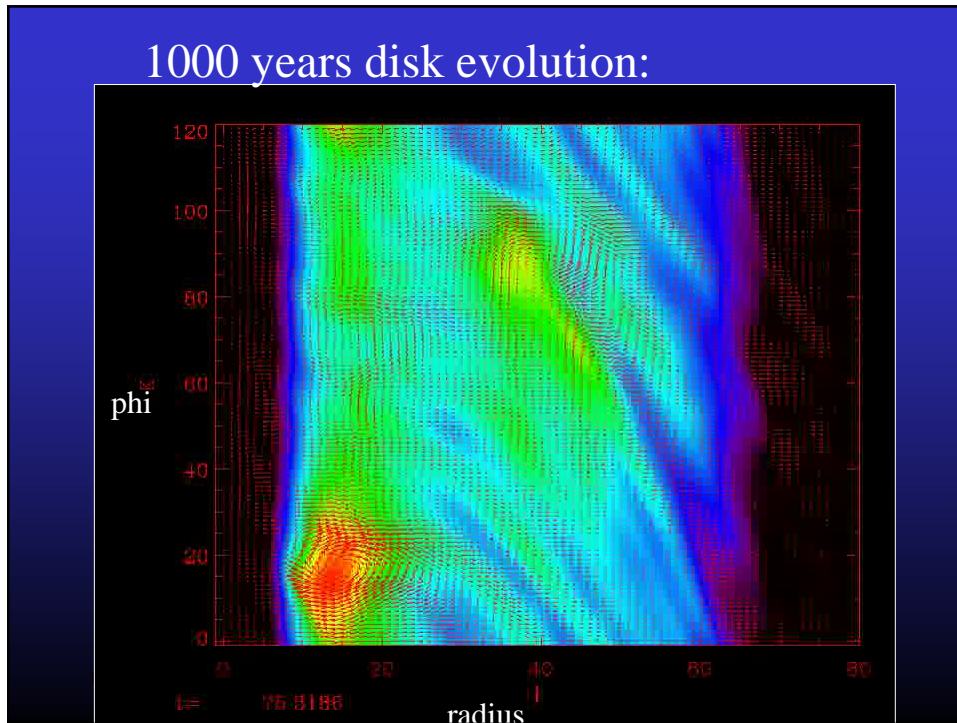
Will boulders be concentrated in these vortices?



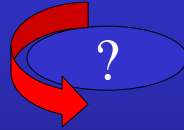
c.f. Barge &
Sommeria 1995

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What happens to the boulders inside the Vortex?



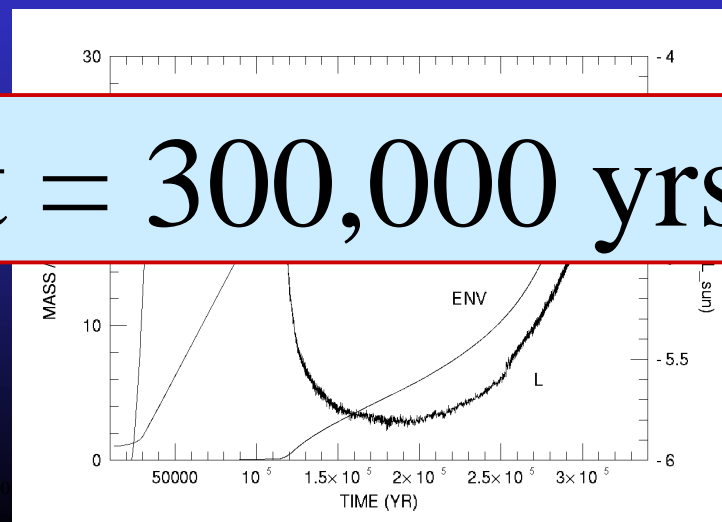
1. they accumulate to one large core.
2. they enrich the gas until they undergo Gravitational Collaps. (Gurevich & Lebedinskii 1950, Safronov 1969, Goldreich & Ward 1973, etc.)
3. they accumulate to planetesimals and scatter (in part / at all) out of the vortex.

Core Accretion in Vortices

(Bodenheimer & Klahr submitted)

$2.2E-4 M_{\text{earth}}/\text{yr}$; $3\text{g}/\text{cm}^2$; minimum Nebula!

$t = 300,000 \text{ yrs}$



Core Accretion plus Vortices:

- Collision velocities for boulders
 $dV < 10 \text{ m/s} \Rightarrow$ no fragmentation
- No loss of 1m boulders into central object
- Fast buildup of cores from 0.1-1m boulders
- Minimum mass nebula and solar metallicity
- Accretion time for 12 Earth mass core $< 10^5$ yrs
- Formation time for Jupiter $< 10^6$ yrs

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Summary:

An entropy gradient makes a disk hydro-dynamically unstable.

Entropy gradients generate vorticity in disks.

Vortices accelerate the core accretion for giant planets.

Three Phases of Planet Formation:

- Vortex Formation
- Dust Concentration
- Gas Accretion

