

# **A Minority Report on the Time-scale for Planetary Accretion and Differentiation:**

**Isotopic Constraints and Dynamic Requirements**

**Kavli Institute for Theoretical Physics at UCSB: Planet Formation Program**

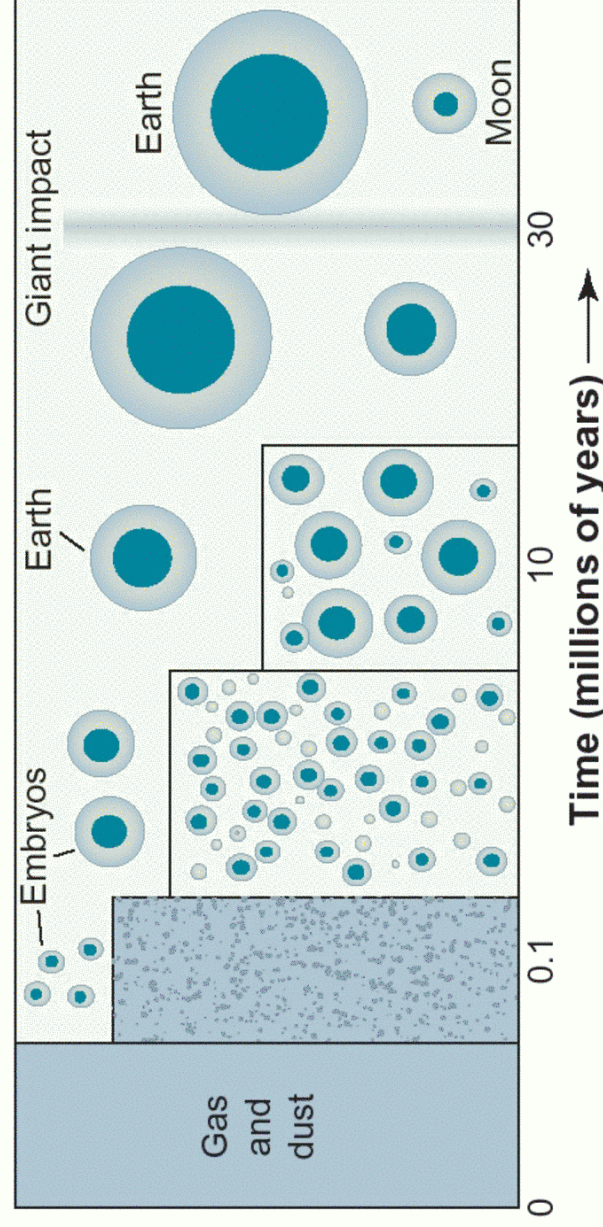
**March 4, 2004**

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**Accretion, mixing, & metal-silicate segregation according to**

**Standard Planet Formation Theory**



*Jacobsen (2003)*

**Core formation is rate limited by accretion!**

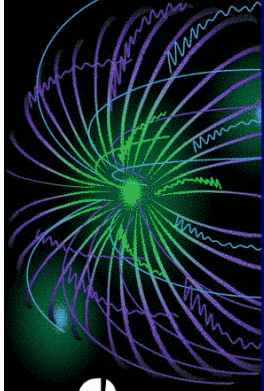
$$N = N_0 e^{-\lambda t}$$

Some major event that will leave behind permanent isotopic trace



**T<sub>0</sub>**  
**CAI (4567.2±0.6Ma)**  
**Amelin et al. (2002)**

## Radioactivities in the Early Solar System

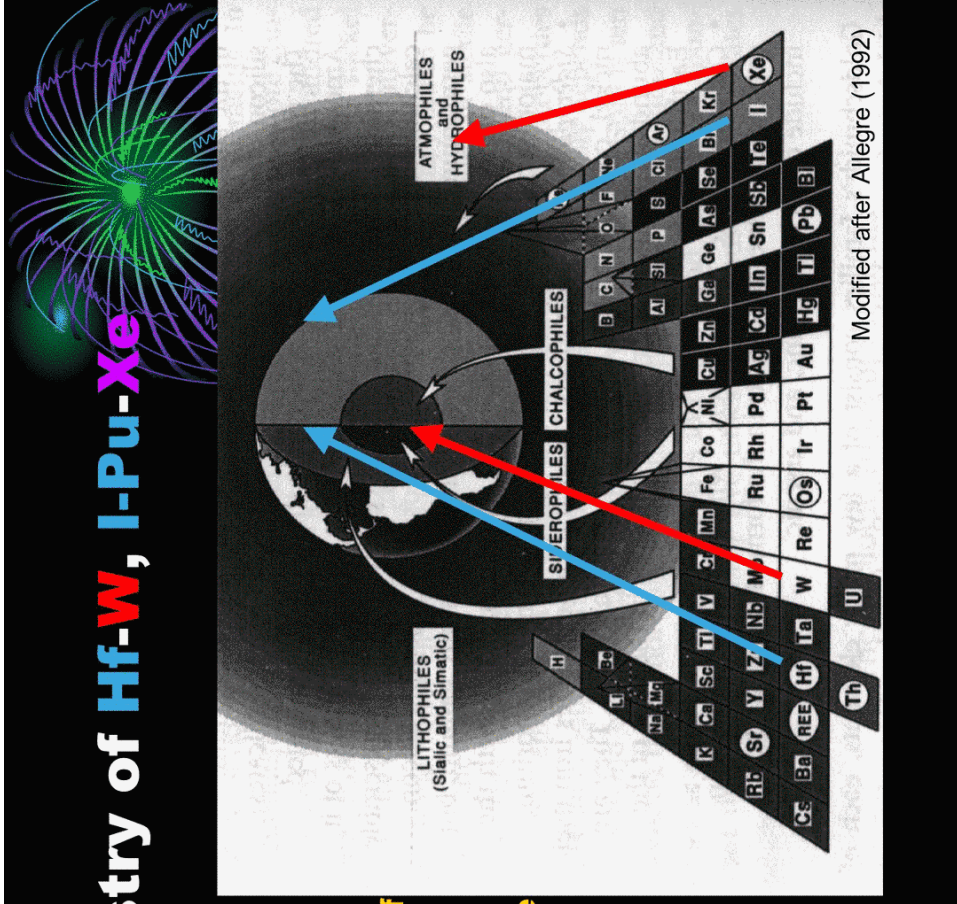


Score	Parent	Daughter	Half-life (in Ma)	Score	Parent	Daughter	Half-life (in Ma)
?/+	<sup>7</sup> Be	<sup>7</sup> Li	53.28 days	+	<sup>107</sup> Pd	<sup>107</sup> Ag	6.5
+	<sup>10</sup> Be	<sup>10</sup> B	1.6	Active research	<sup>126</sup> Sn	<sup>126</sup> Te	0.2
+	<sup>26</sup> Al	<sup>26</sup> Mg	0.73	+	<b><sup>129</sup>I</b>	<b><sup>129</sup>Xe</b>	<b>15.7</b>
+	<sup>36</sup> Cl	<sup>36</sup> Ar	0.301	+	<sup>135</sup> Cs	<sup>135</sup> Ba	2.3
+	<sup>41</sup> Ca	<sup>41</sup> K	0.103	+	<sup>137</sup> La	<sup>137</sup> Ba	0.06
+	<sup>53</sup> Mn	<sup>53</sup> Cr	3.7	+	<sup>146</sup> Sm	<sup>142</sup> Nd	103
+	<sup>60</sup> Fe	<sup>60</sup> Ni	1.5	+	<sup>150</sup> Gd	( <sup>146</sup> Sm)	1.8
	<sup>59</sup> Ni	<sup>59</sup> Co	0.076	+	<b><sup>182</sup>Hf</b>	<b><sup>182</sup>W</b>	<b>9</b>
	<sup>76</sup> Se	<sup>76</sup> Br	0.065	Active research	<sup>202</sup> Pb	<sup>202</sup> Hg	0.053
	<sup>81</sup> Kr	<sup>81</sup> Br	0.21	Active research	<sup>205</sup> Pb	<sup>205</sup> Tl	15
?	<sup>93</sup> Zr	<sup>93</sup> Nb	1.5	+	<sup>239</sup> Pu	a, SF	0.0241
+	<sup>92</sup> Nb	<sup>92</sup> Zr	36	+	<sup>242</sup> Pu	a, SF	0.375
Active research	<sup>97</sup> Tc	<sup>97</sup> Mo	2.6	+	<b><sup>244</sup>Pu</b>	<b>a, SF</b>	<b>80</b>
Active research	<sup>98</sup> Tc	<sup>98</sup> Ru	4.2	Renewed search	<sup>247</sup> Cm	( <sup>235</sup> U)	15.6
Active research	<sup>99</sup> Tc	<sup>99</sup> Ru	0.213		<sup>248</sup> Cm	( <sup>244</sup> Pu)	0.348

Select appropriate "ruler or clock" for different purposes!

## Geochemistry of Hf-W, I-Pu-Xe

- **Hf-I-Pu** is highly *lithophile*, retain in the silicate portion of the Earth.
- **W** is *moderately siderophile*, some enters core, some remains in the silicate mantle.
- **Xe** is *atmophile* (gas)



## Chronometers for Planet Formation

- Both Hf-W and I-Pu-Xe clocks are uniquely affected by large-scale processes; core-mantle segregation in a Hf-W clock and atmosphere-solid Earth segregation in I-Pu-Xe system.
- “Ruler” sizes are just right:  $^{182}\text{Hf}$  (9Ma);  $^{129}\text{I}$  (15.6 Ma);  $^{244}\text{Pu}$  (80 Ma)

# $^{182}\text{W}$ \* Evolution due to $^{182}\text{Hf}$ Decay

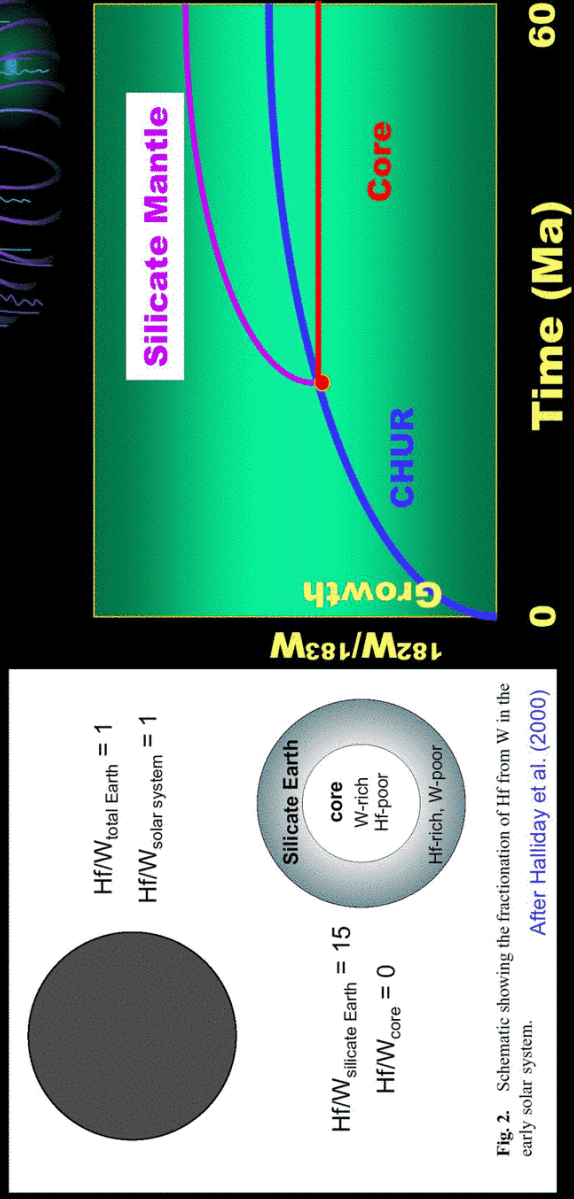
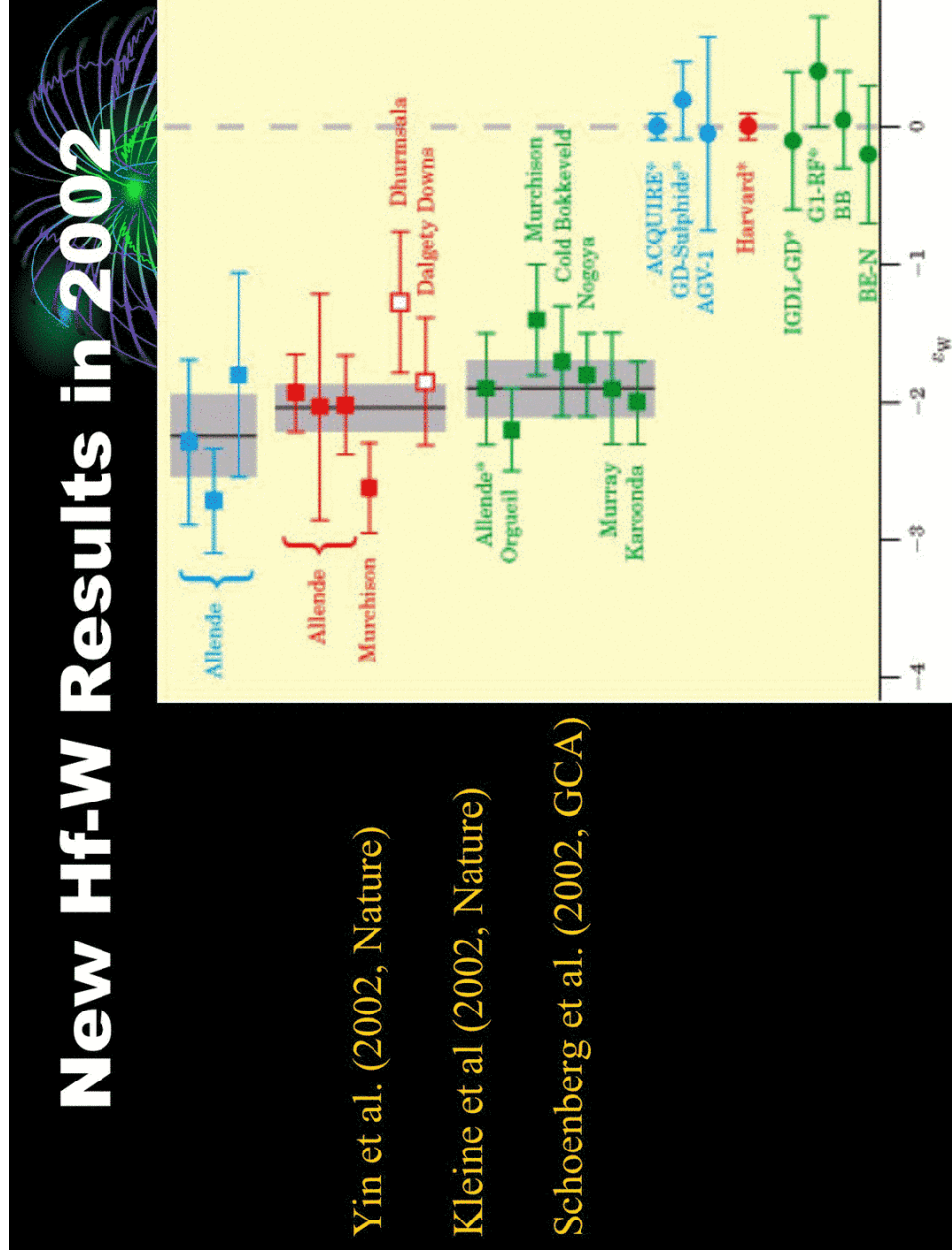
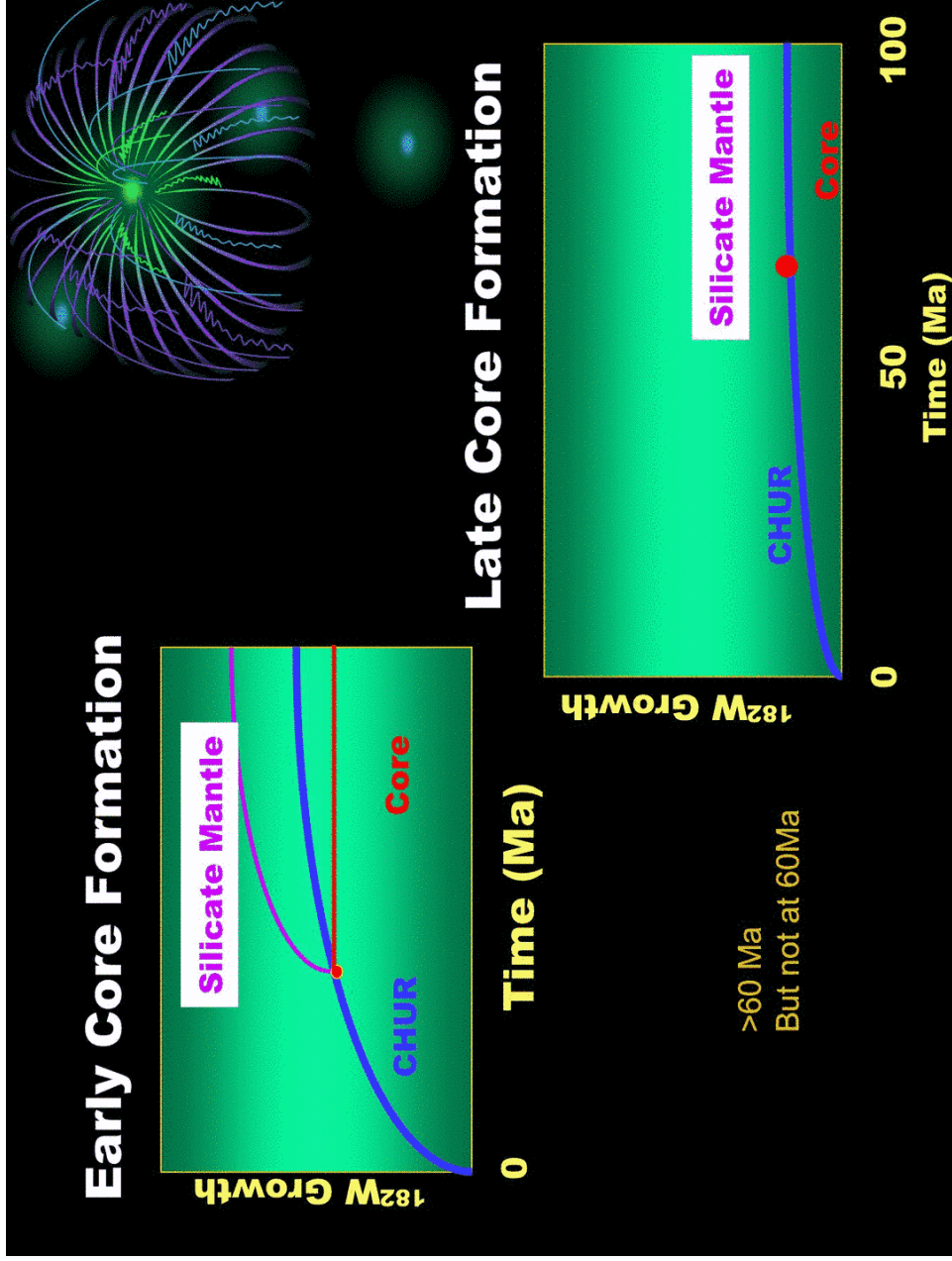


Fig. 2. Schematic showing the fractionation of Hf from W in the early solar system. After Halliday et al. (2000)

**W isotope data that have been widely cited and dominated our thinking between 1995-2002**

- **Lee and Halliday (1995, 1996 and many later papers)**
- **Sample**  $\epsilon^{182}\text{W}$  (part per  $10^4$ )
- **Allende-1**  $-0.10 \pm 0.56\epsilon$
- **Allende-2**  $-0.50 \pm 0.50\epsilon$
- **Murchison**  $-0.05 \pm 0.50\epsilon$
- **Mean**  $-0.17 \pm 0.29\epsilon$

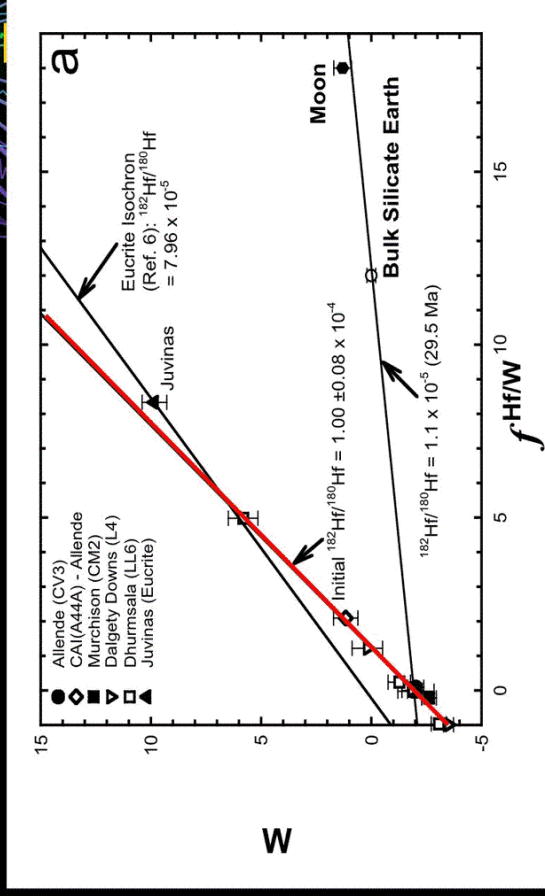


Yin et al. (2002, Nature)

Kleine et al (2002, Nature)

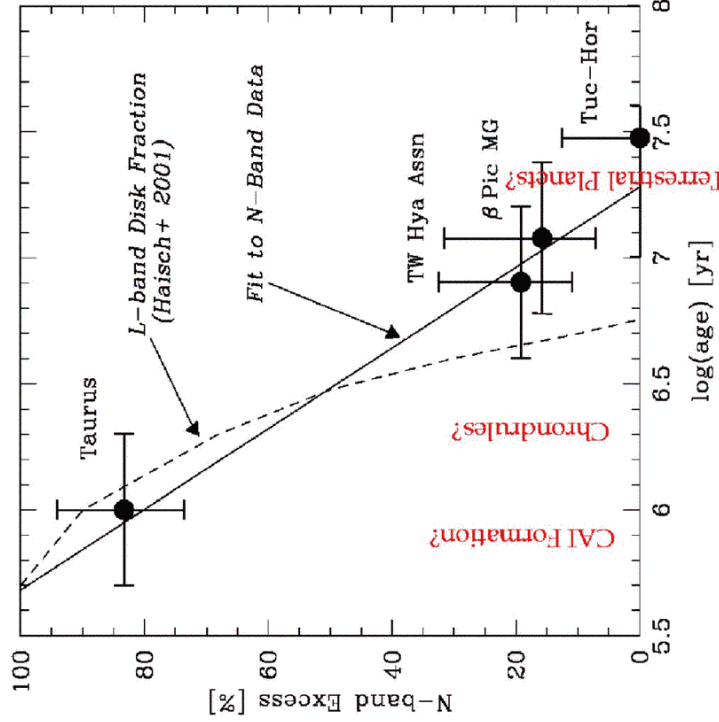
Schoenberg et al. (2002, GCA)

# Hf-W Systematics for the Early Solar System



**Bulk of metal-silicate separation in the entire Solar System was completed within <30 Ma (Earth: 50% mass of inner solar system)**

## MIR Excess Fraction (0.3-1.0 AU) vs. Cluster Age



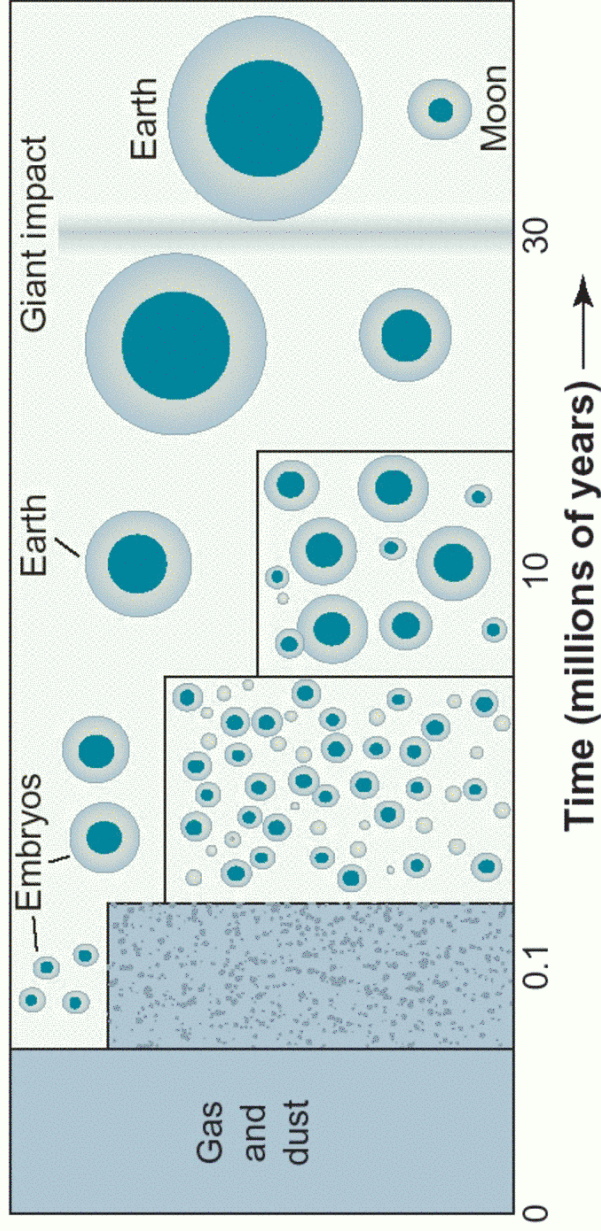
**Dust in terrestrial planet zone dissipates when accretion stops!**

Mamajek et al in preparation.

Metchev, Hillenbrand, and Meyer, ApJ, January, 2004.

Courtesy of M. Meyer

Accretion, mixing, & metal-silicate segregation  
according to  
**Standard Planet Formation Theory**



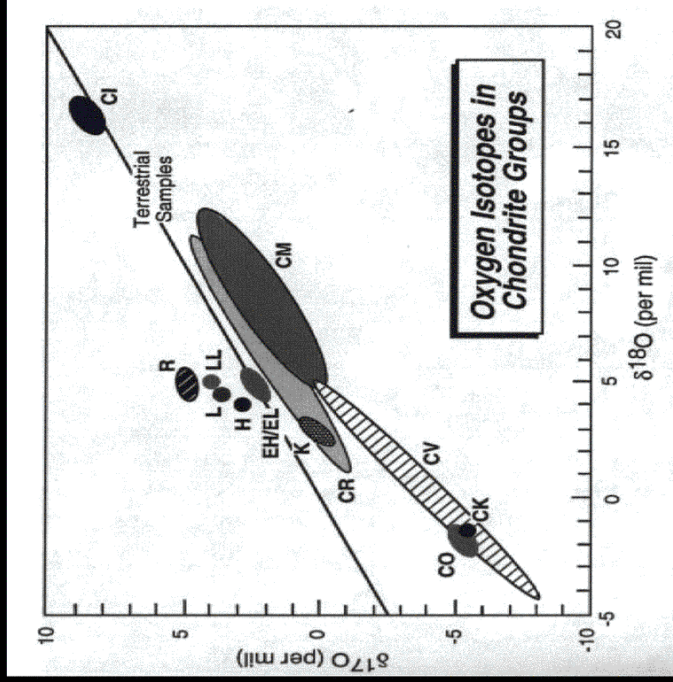
Jacobsen (2003)

**Core formation is rate limited by accretion!**

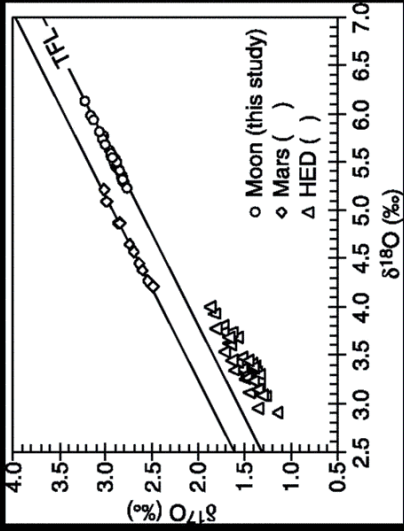
Evidences for Chemical Equilibrium  
during Planet Building Processes

- (1). Vesta (0.6 to 3 Ma), Mars (3-12 Ma), Earth (10-30 Ma) (Yin et al., 2002; Kleine et al., 2002; Schoenberg et al., 2002).
- (2) **Testable Predictions: If there was NO chemical equilibrium during the planet formation, W isotope anomalies (with large + and - epsilons) should be found on Earth.**

### (3) Identical Oxygen Isotopes between Earth and Moon.

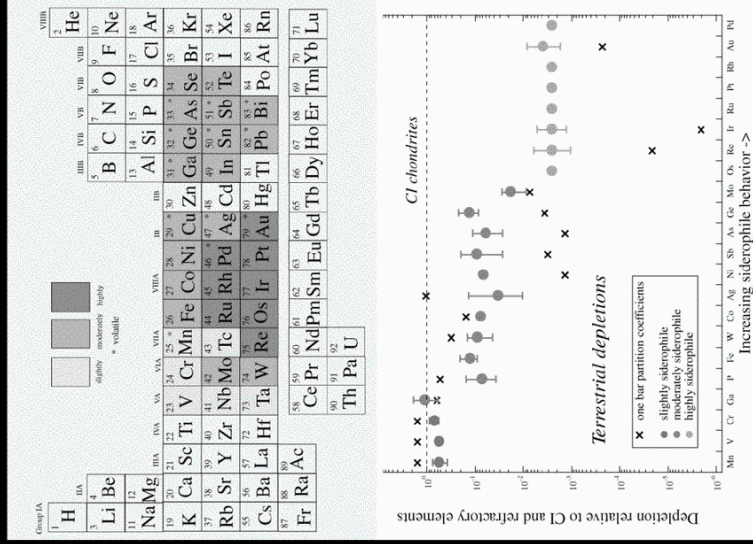


Hap McSween (1999)



Wiechert et al. (2001)

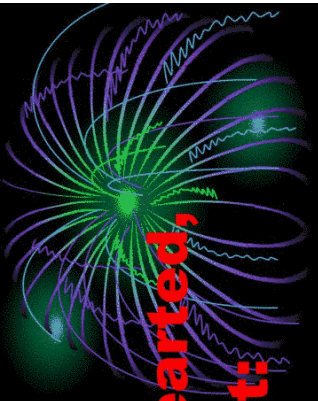
### (4) Flat PGE patterns in Upper Mantle and the “Late Veneer”



• After Kevin Righter (2003)



# Accretion Energy



- **Simple physics for faint-hearted, point-and-click geochemist:**

$$\frac{GM^2}{r_p} = MC_p \Delta T$$

$$\Delta T = \frac{1}{C_p} \frac{GM}{r_p} \propto r_p^2$$

$G$ : gravity constant

$M$ : mass of the planet

$r_p$ : planetary radius

$C_p$ : specific heat

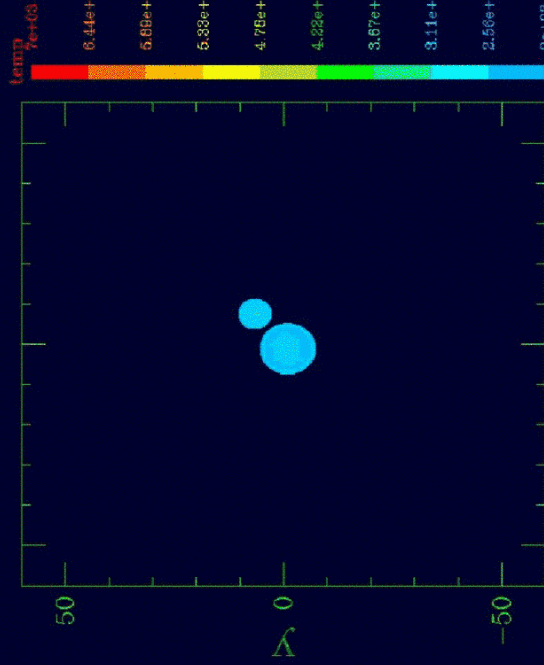
$\Delta T$ : temperature increase

$\Delta T \sim 5E3$  to  $1E4$  K for terrestrial planets

- **Enough energy to warrant chemical equilibrium!**
- **If you think this is too simple and naïve?**

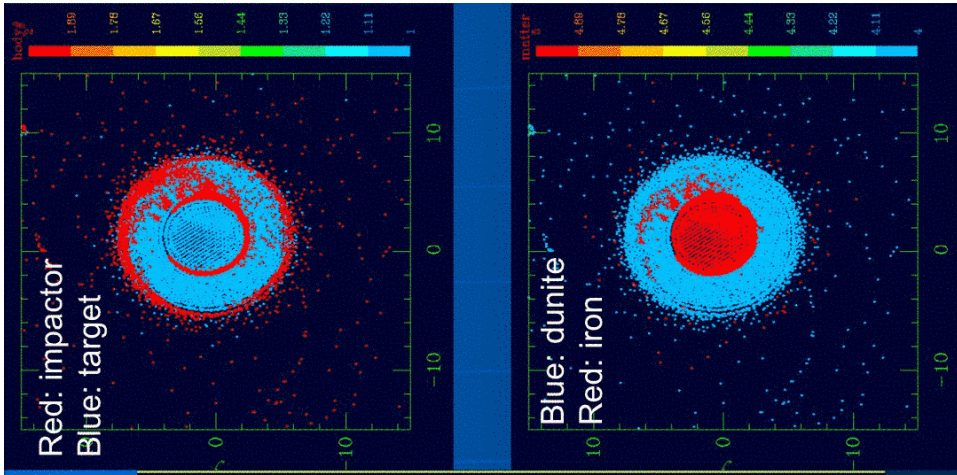
## R. Canup (2004)

Run 119



SPH

SwRI



## Chandrasekhar (1961); Rubie et al. (2003) Stevenson (1990)

Think about pouring down a bucket of water from a balcony of a high rise building :  
by the time it reach the ground.....

- When dense liquid (metal) falls through a less dense liquid (silicates).
- Rayleigh-Taylor instabilities (density contrast) cause “pancake flattening” of infalling denser materials.
- This instabilities will initiate a cascade of disruption into smaller droplet size.
- Initial core (size < magma ocean depth) break up to the rain of cm-size droplets by the time it reaches magma ocean depth.
- Rubie et al. (2003) showed full chemical equilibration is achieved in 400 second, as soon as it reach cm-sized droplets.
- Stevenson (1990) the largest iron droplets are ~1cm following the rapid (~hours) emulsification event of a large impact”

## Sasaki and Abe (2003)

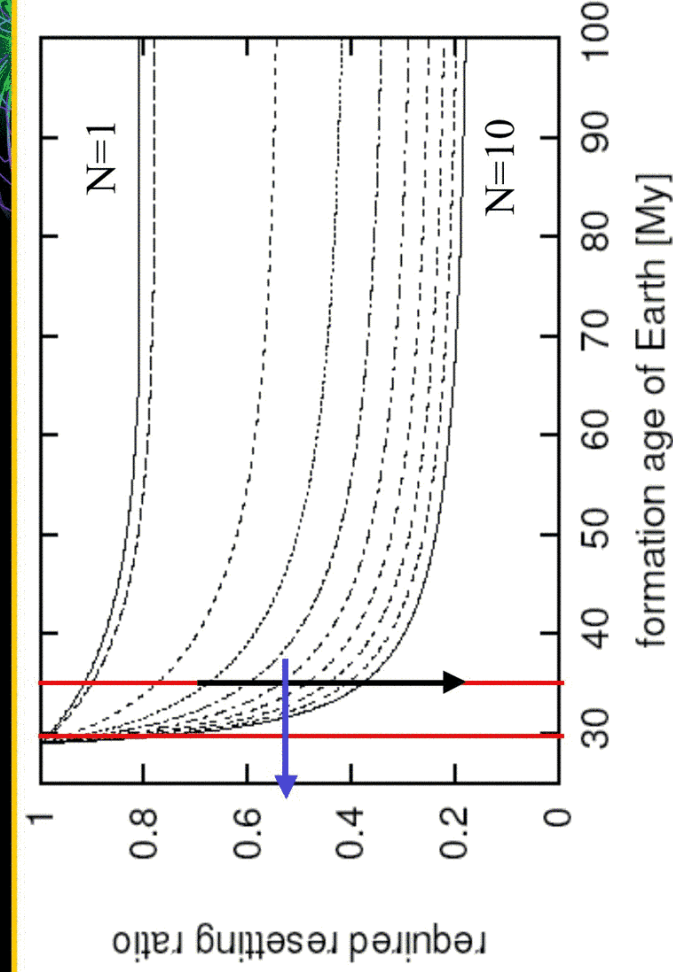


Fig. 4.— Required resetting ratio for observed value of Earth’s samples as a function of Earth formation age. The number of giant impacts is 1 to 10 from top to bottom. Initial state is  $\epsilon = 8$  and  $t = 10$ . Total time for perfect resetting (resetting ratio = 1) is about 30 Myr, corresponds to previous study (Yin et al. 2002).

## Summary

- Give or take, fully grown Earth is (4567-30)= 4537 ±1Ma old. Equivalent to a 45 year old man with a memory from his infancy (first 100 days) to within 3.5 days
- Hf-W age (accretion and core formation age) and I-Pu-Xe closure age (accretion and atmospheric formation age) are consistent at 30 Ma.

## Summary (cont.)

- **30 Ma timescale is consistent with disk observation in young stellar objects.**
- **There are many evidences to support that equilibrium is achieved. The 30 Ma timescale could be accommodated in dis-equilibrium case. Halliday's 50Ma is not unique solution.**
- **Debates 100 years ago:**