

A heatmap background with a color scale from black to yellow, showing a grid of data points. The colors transition from black on the left to yellow on the right, with some red and orange spots scattered throughout.

Encoding and Decoding 3D Genome Organization

Noam Kaplan

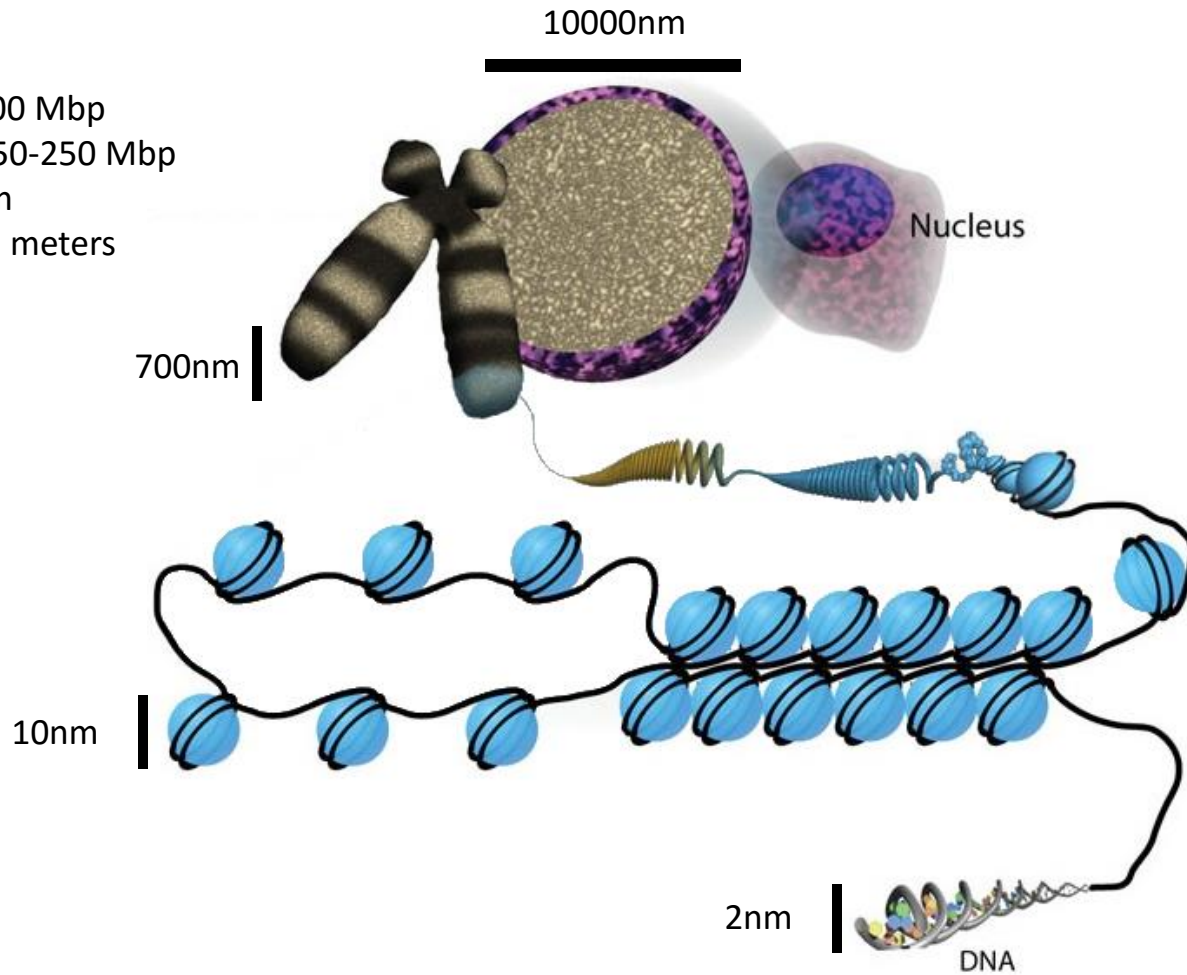
Dekker Lab

Program in Systems Biology

University of Massachusetts Medical School

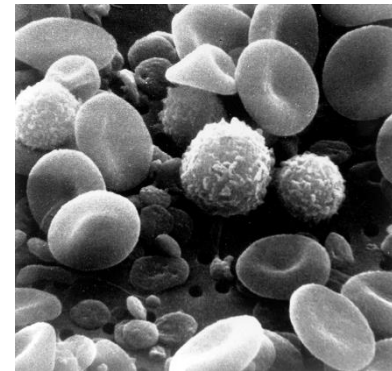
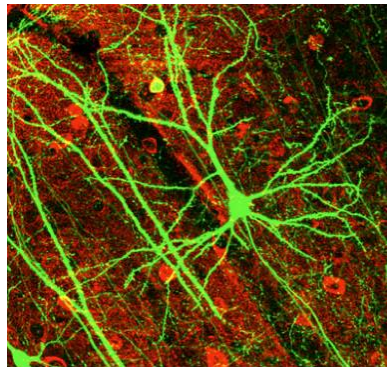
Chromatin organization

Human genome: 2x3000 Mbp
Human chromosome: 50-250 Mbp
Avg. bp length: 0.33 nm
Total genome length: 2 meters

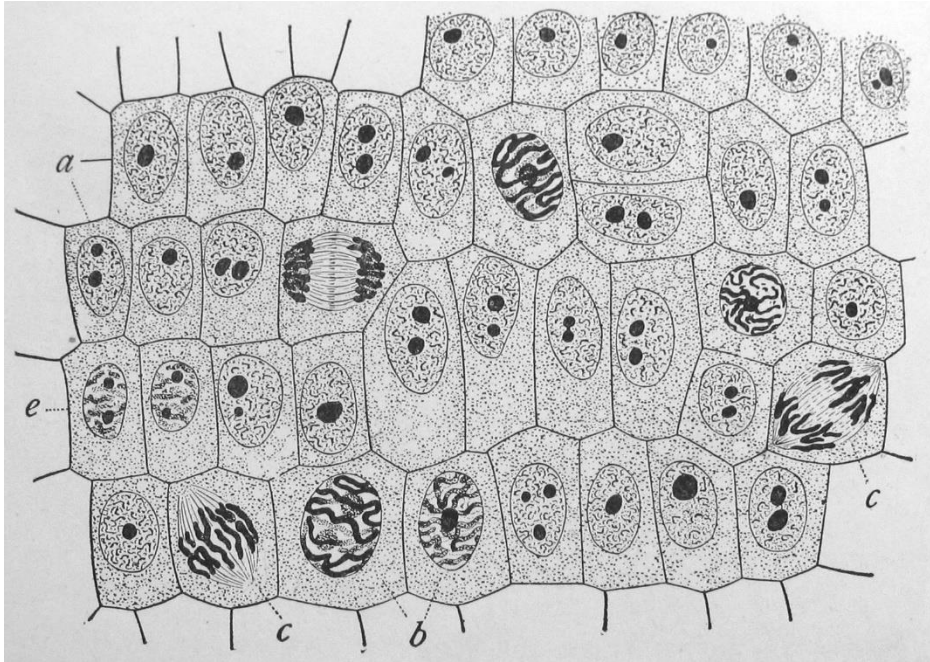


Chromatin structure and function

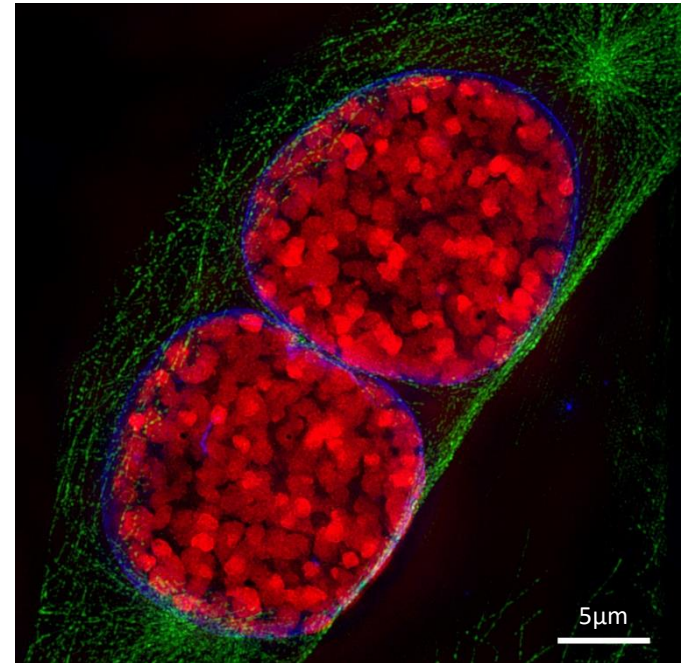
Gene regulation



Studying chromatin: From microscopy to genomics



Wilson, *The Cell* 1900



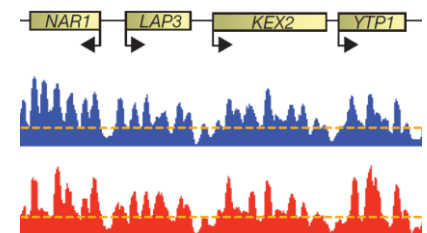
Schermelleh et al., *Science* 2008



The human genome (2001)

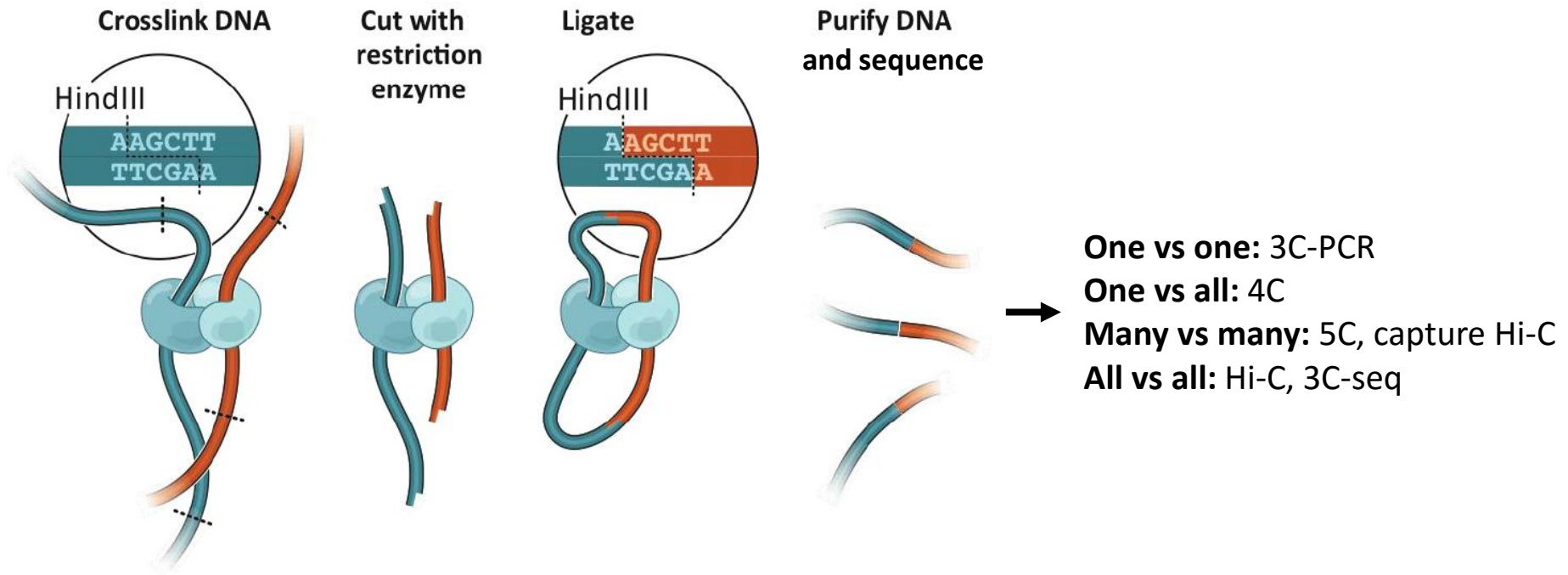


Next Generation Sequencing



Genomic tracks

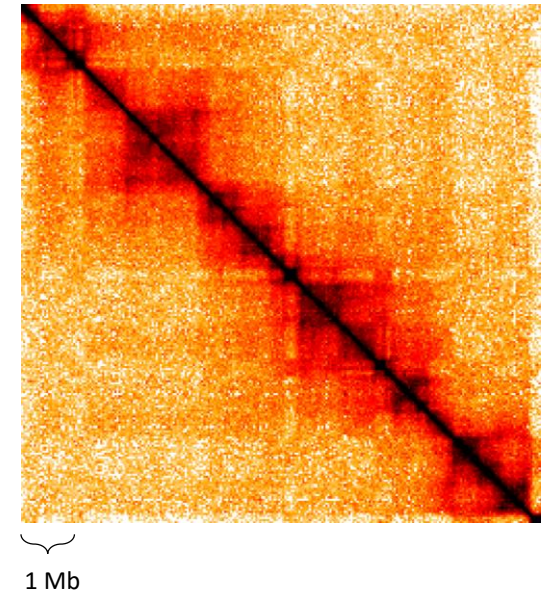
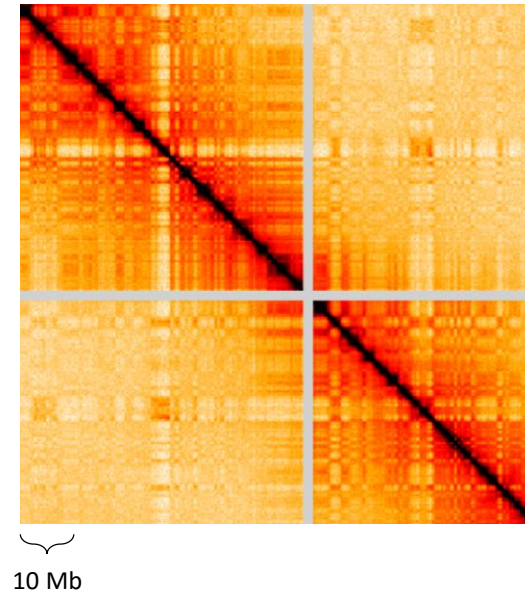
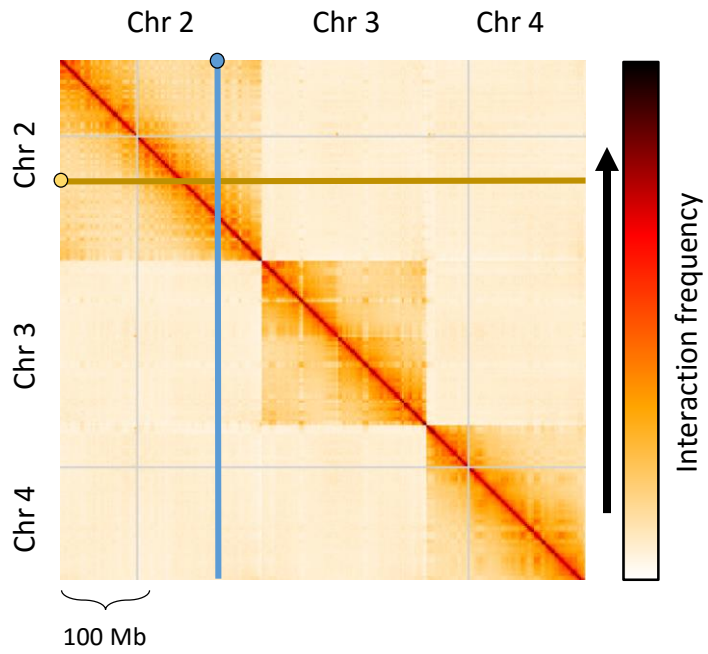
Chromosome Conformation Capture (3C)



3C: Dekker et al., *Science* 2002

Hi-C: Lieberman-Aiden et al., *Science* 2009

Interaction maps



Hi-C resolution: Some numbers

- **Human genome size:** 3×10^9 bp
- **Restriction enzyme site:** 6 bp (4 bp in some cases)
- **Restriction fragment length:** ~ 4 kbp “optimal resolution”
- **Number of restriction fragments:** $\sim 7.5 \times 10^5$ bp
- **Size of interaction space:** 5.6×10^{11} possible interactions

- **Next Generation Sequencing lane:** 10^8 usable reads, 2.5K USD
- **Number of cells per experiment:** 10^6 - 10^8
- **Number of interactions measured per cell:** 10^4 - 10^5 (?)

Interaction space is under-sampled

BUT interaction map is highly non-uniform

Solutions:

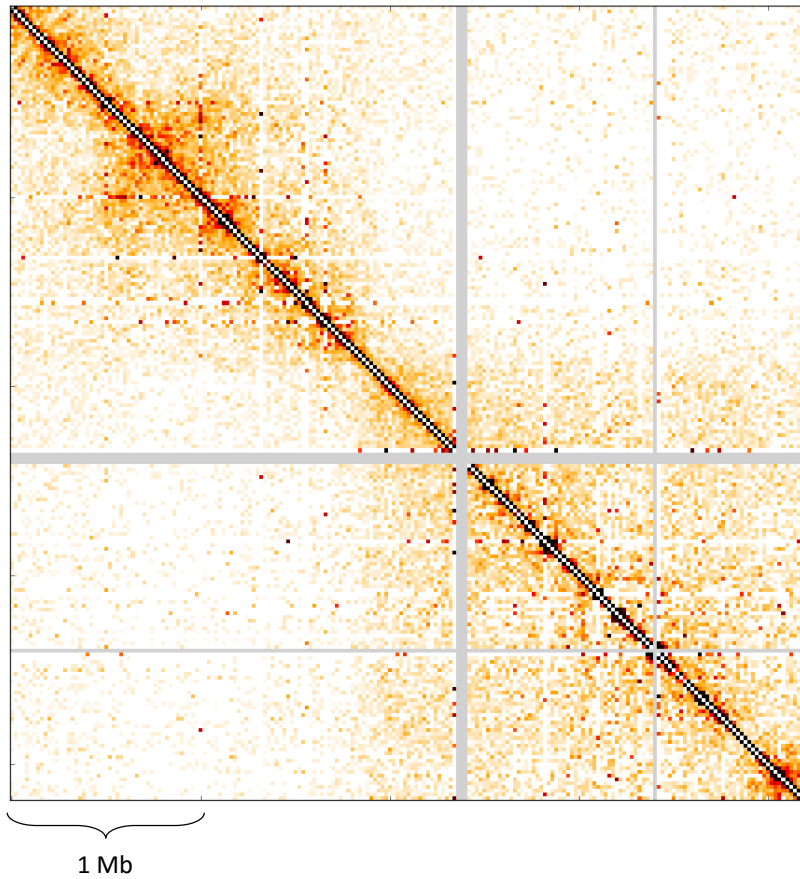
1. Reduce interaction space (binning; focused experiment)
2. Sequence more (\$\$\$)
3. Acknowledge limitations in measurement of infrequent interactions

Practically:

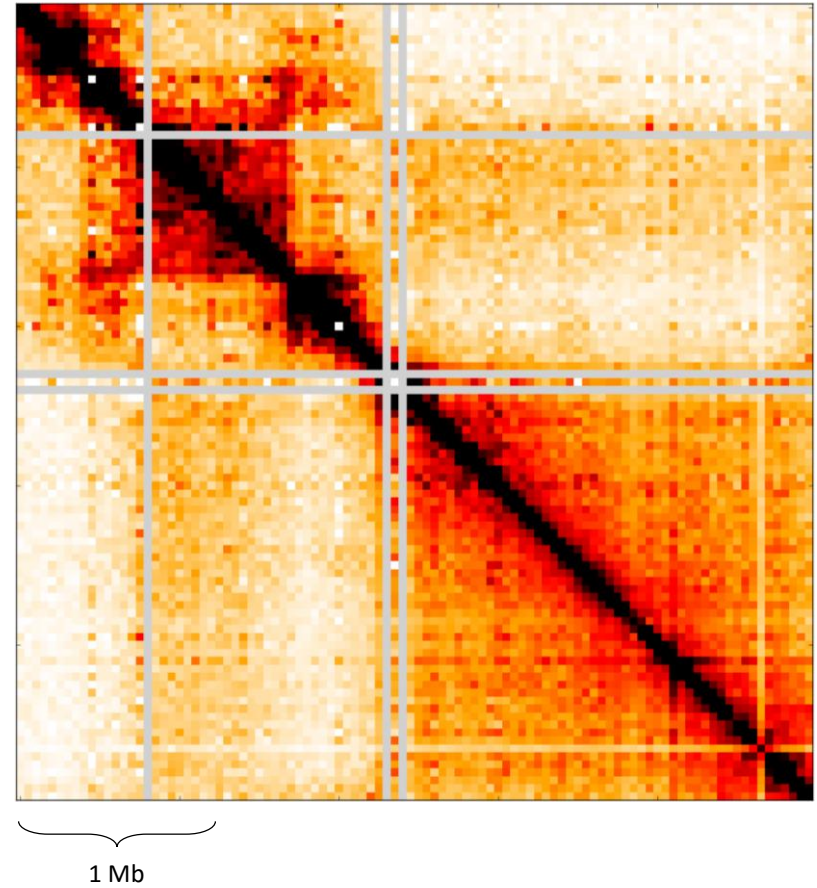
1. ~ 5 -50kb resolution in human genome
2. Library complexity is not a major issue yet

Hi-C resolution

Fragment (~4kb) resolution



40 kb resolution



Bias normalization

- **Problem:** Locus-specific biases (e.g. sequencing, mapping)
- **Assumption:** Sum of reads from every row/col should be approx. equal

Imakaev et al., *Nature Methods* 2012

- Sinkhorn (1964): Given symmetric matrix A with positive elements, find a unique doubly stochastic matrix B , and diagonal matrix D with strictly positive elements, such that $A = DBD$.

Bias factors
(locus-specific)

↓ ↓

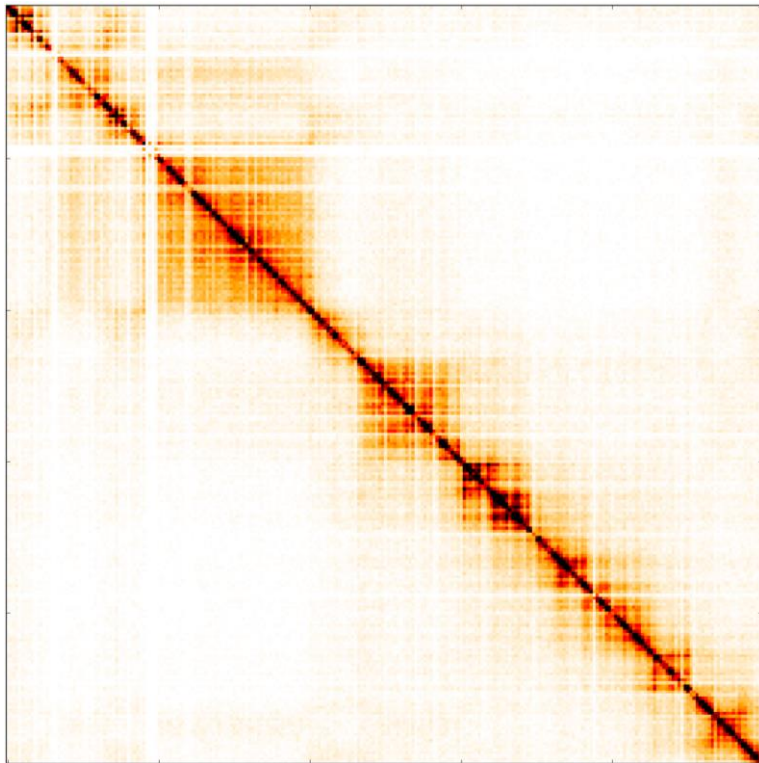
• So: $A_{i,j} = d_i d_j B_{i,j}$

↑ ↑

Read count Normalized
Read count

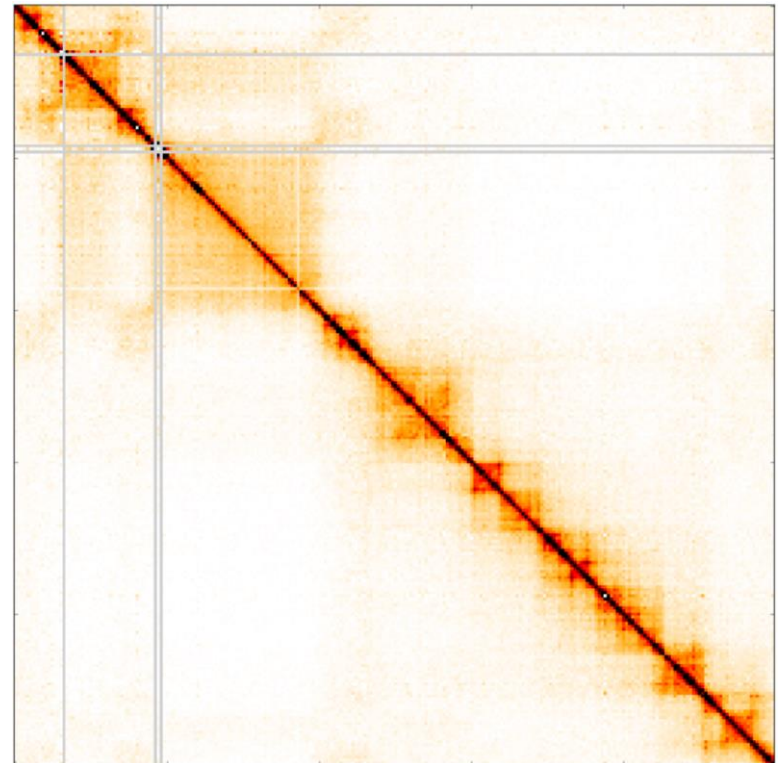
Normalization

Before



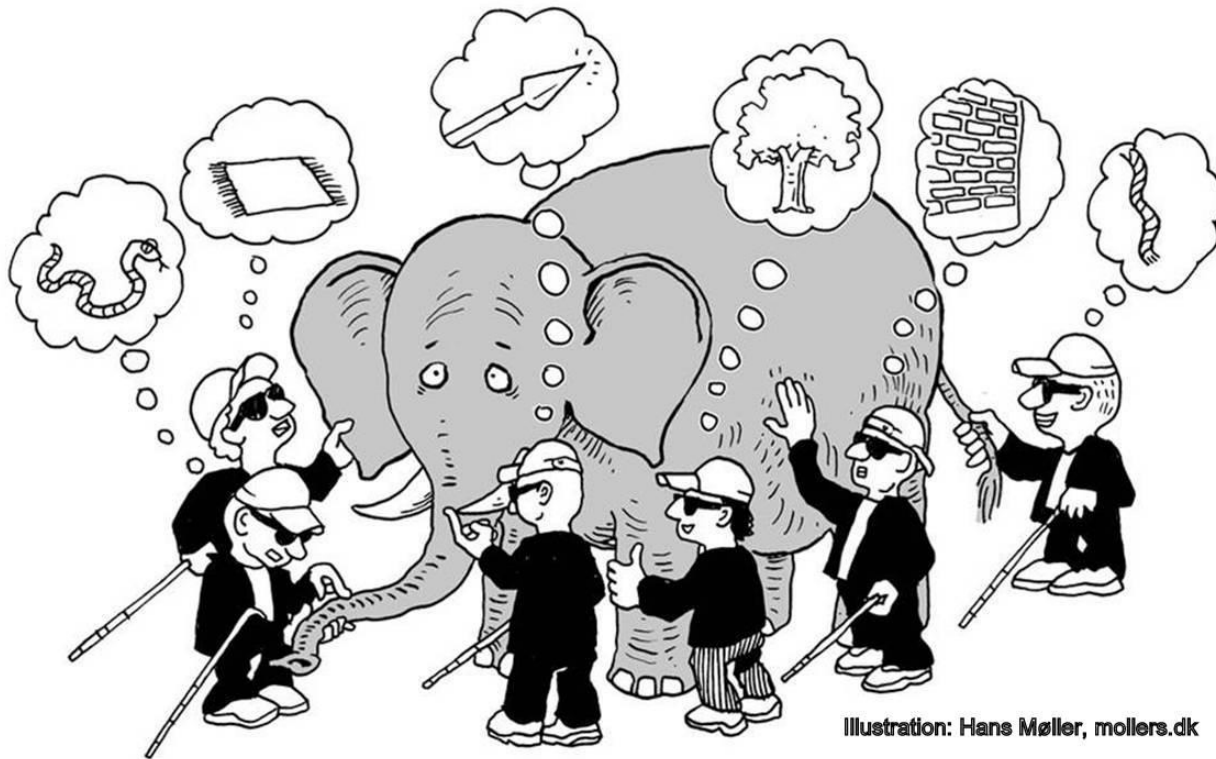
1 Mb

After



1 Mb

Hi-C interpretation



Approaches to Hi-C analysis

Physical



Informatic

Structure-based

Pattern-based

Specifies mechanism

Doesn't specify mechanism

Physical assumptions required

No assumptions

Can be predictive

Typically not predictive

Rigorous

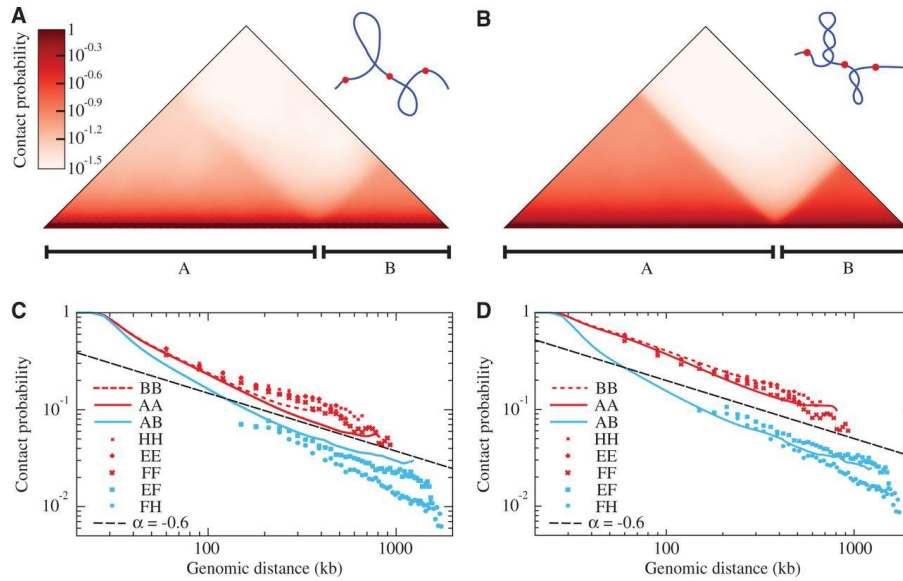
Not rigorous

Less useful for genomic analyses

Useful for genomic analyses

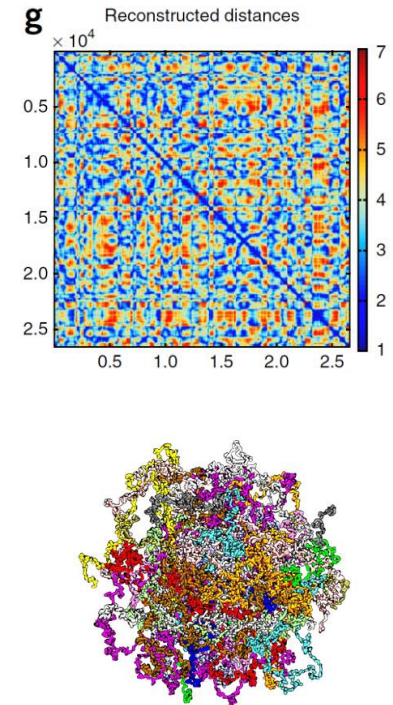
Structural approaches: 2 examples

“Model driven”



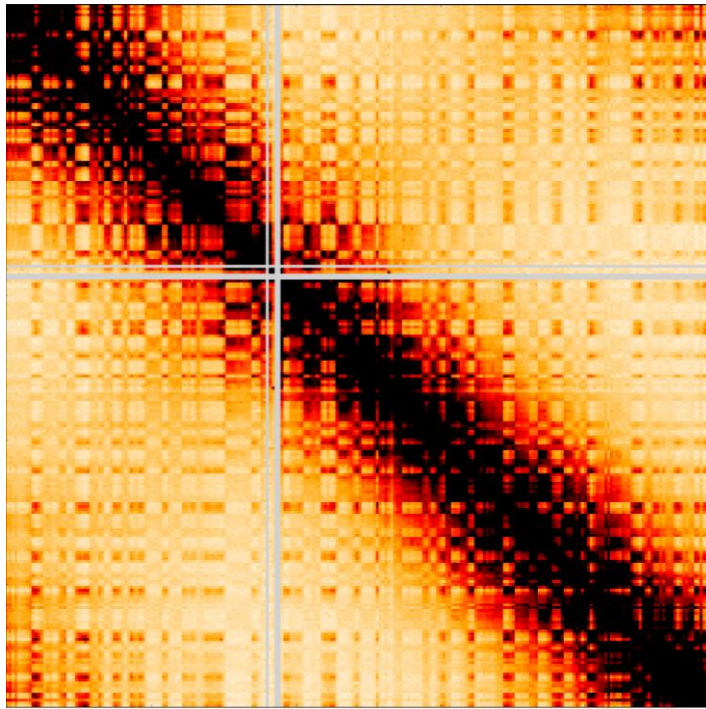
Benedetti et al., *Nucleic Acids Research* 2013

“Data driven”

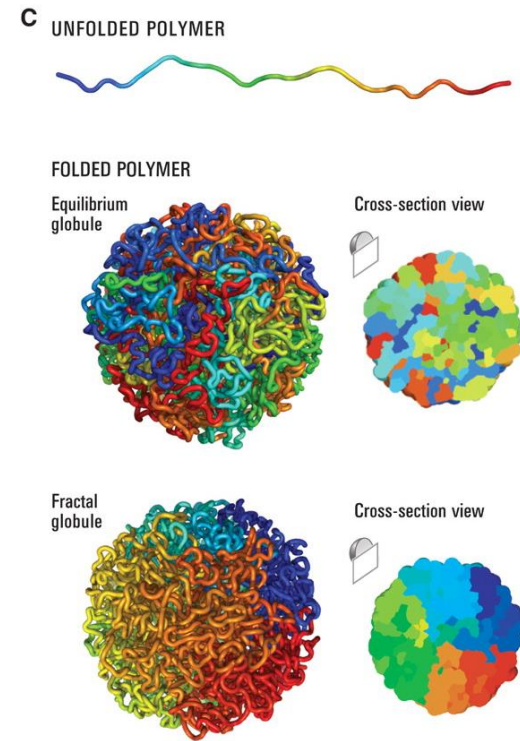
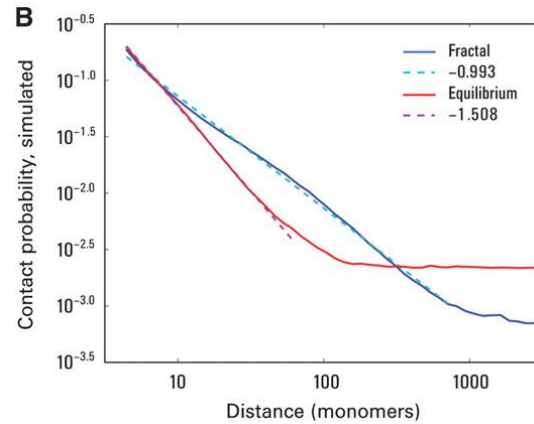
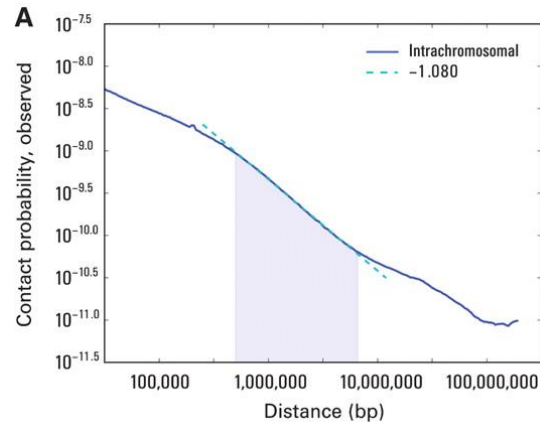


Lesne et al., *Nature Methods* 2013

Distance-dependent interaction

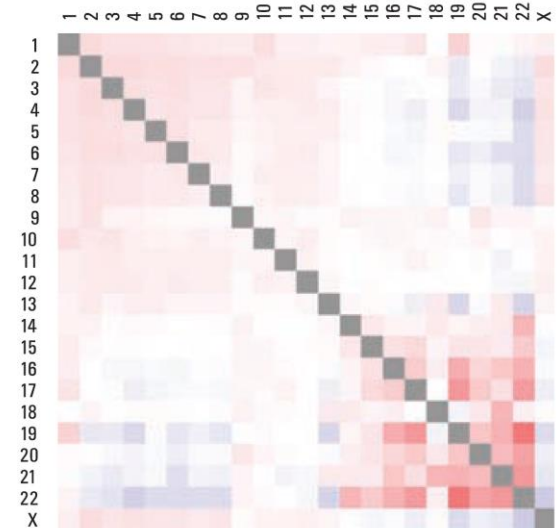
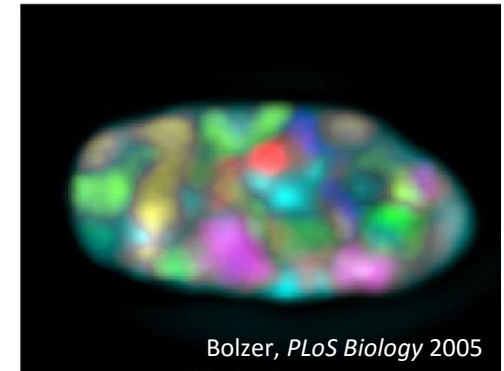
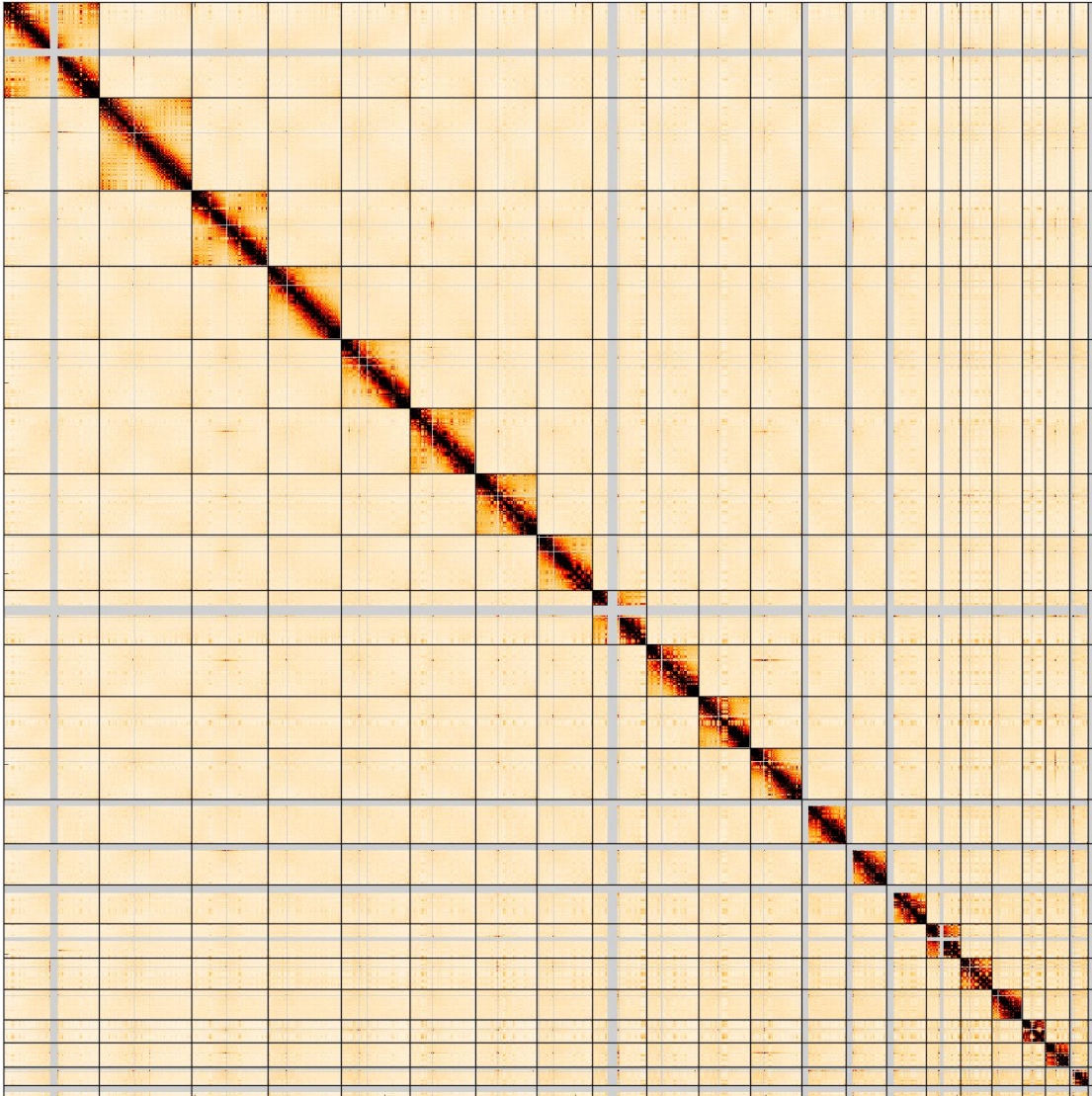


50 Mb



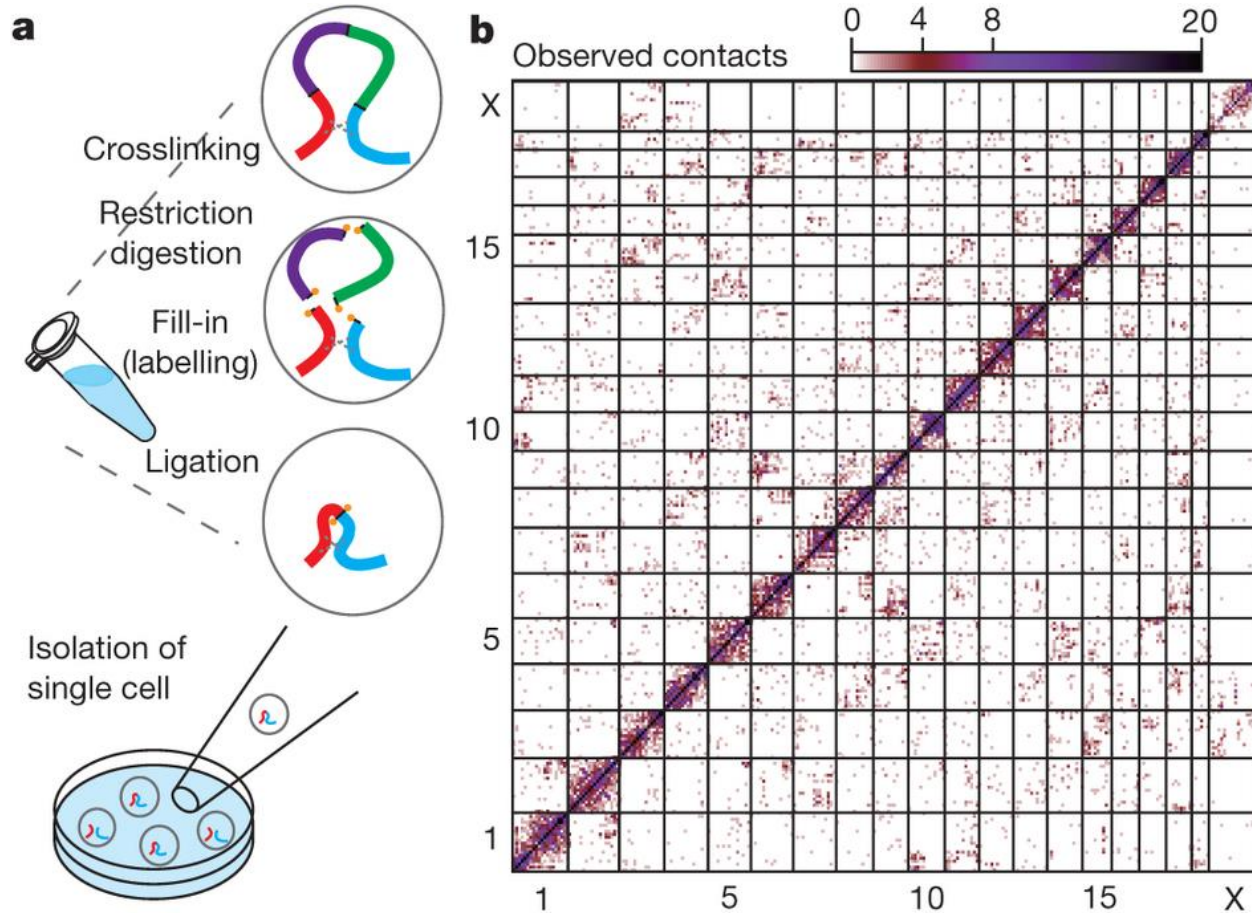
Lieberman-Aiden et al., *Science* 2009

Chromosome territories



Lieberman-Aiden et al., *Science* 2009

Single cell Hi-C

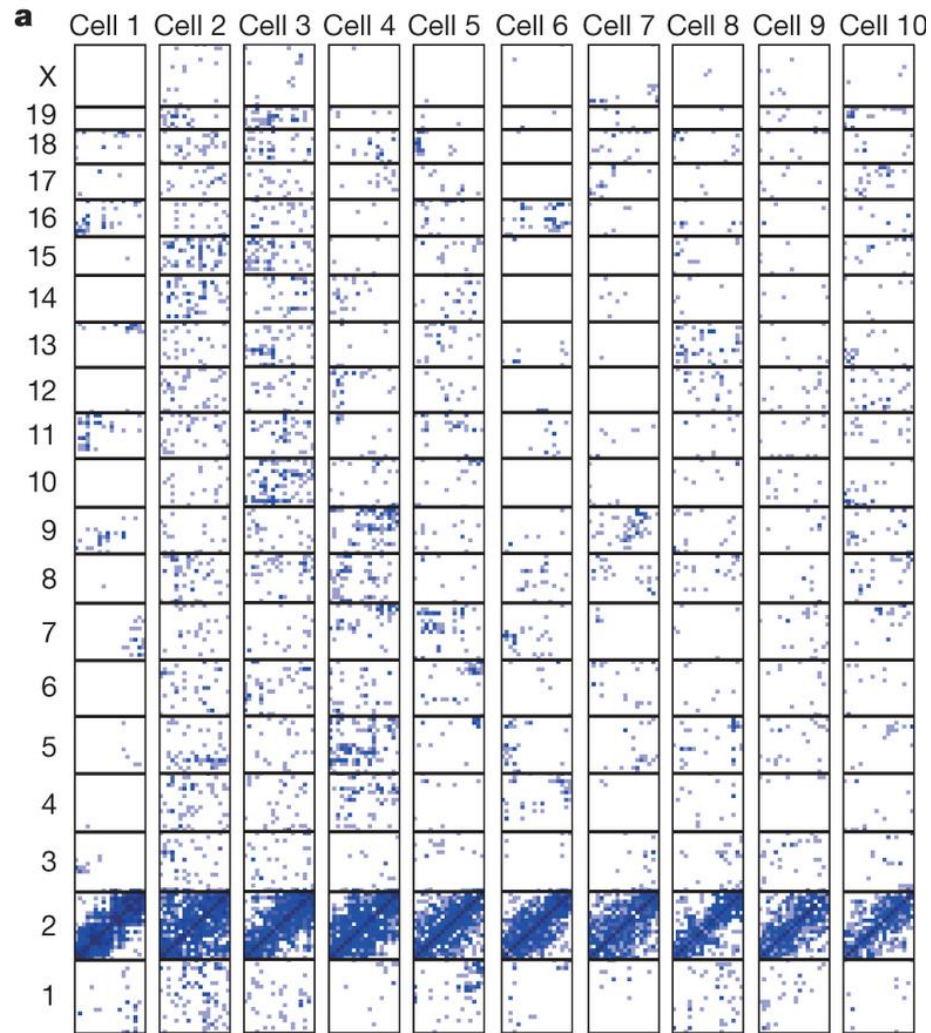


Nagano et al., *Nature* 2013

Caveats:

- Diploid
- ~10K-30K int. per cell

Single cell Hi-C

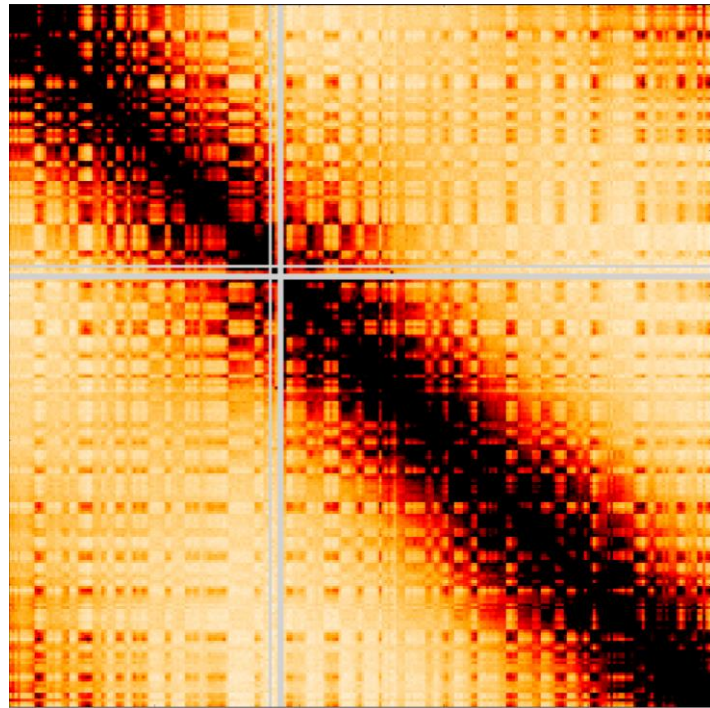


Nagano et al., *Nature* 2013

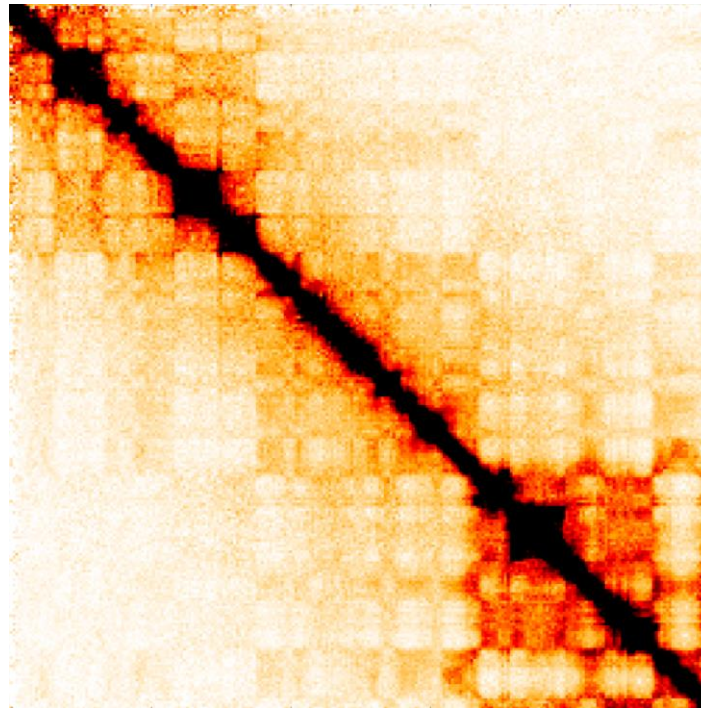
Coming soon (?):

- Haploid cell line
- ~100K-300K int. per cell

Genomic compartments



50 Mb

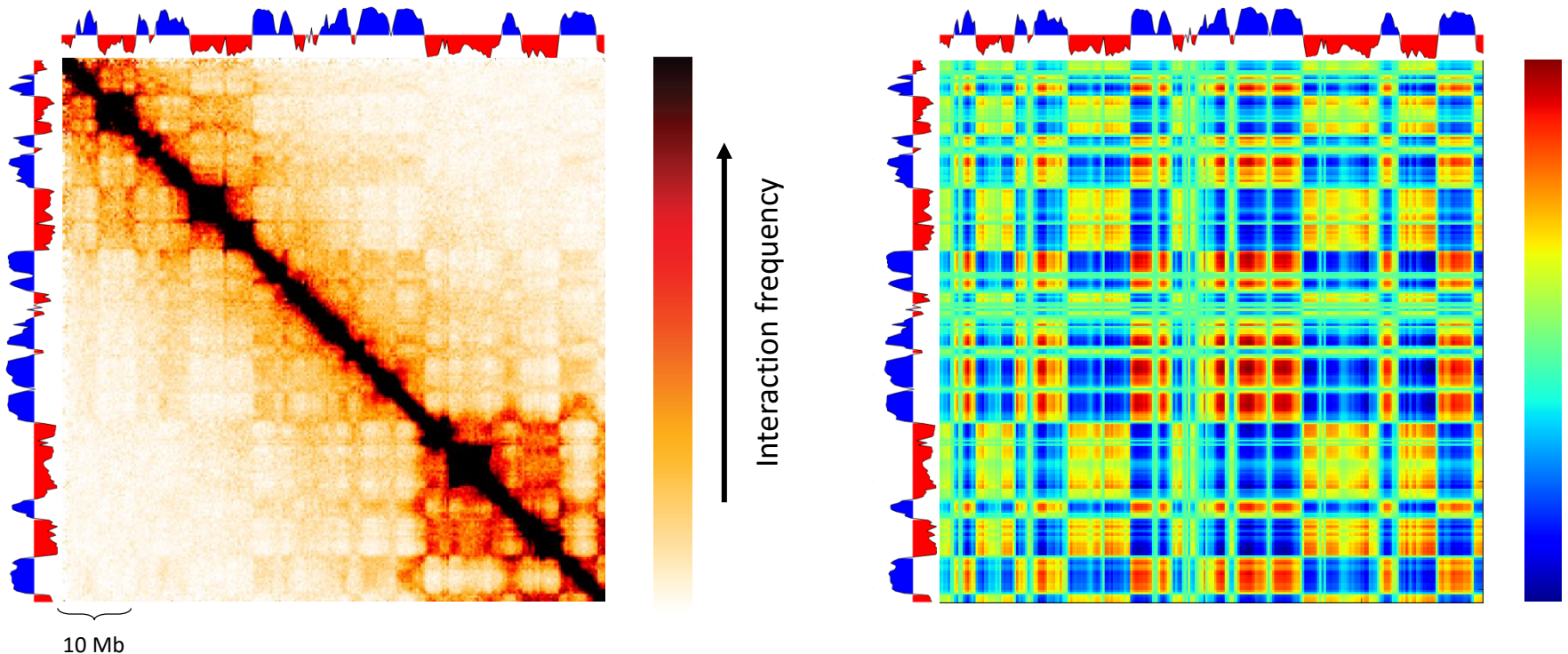


10 Mb

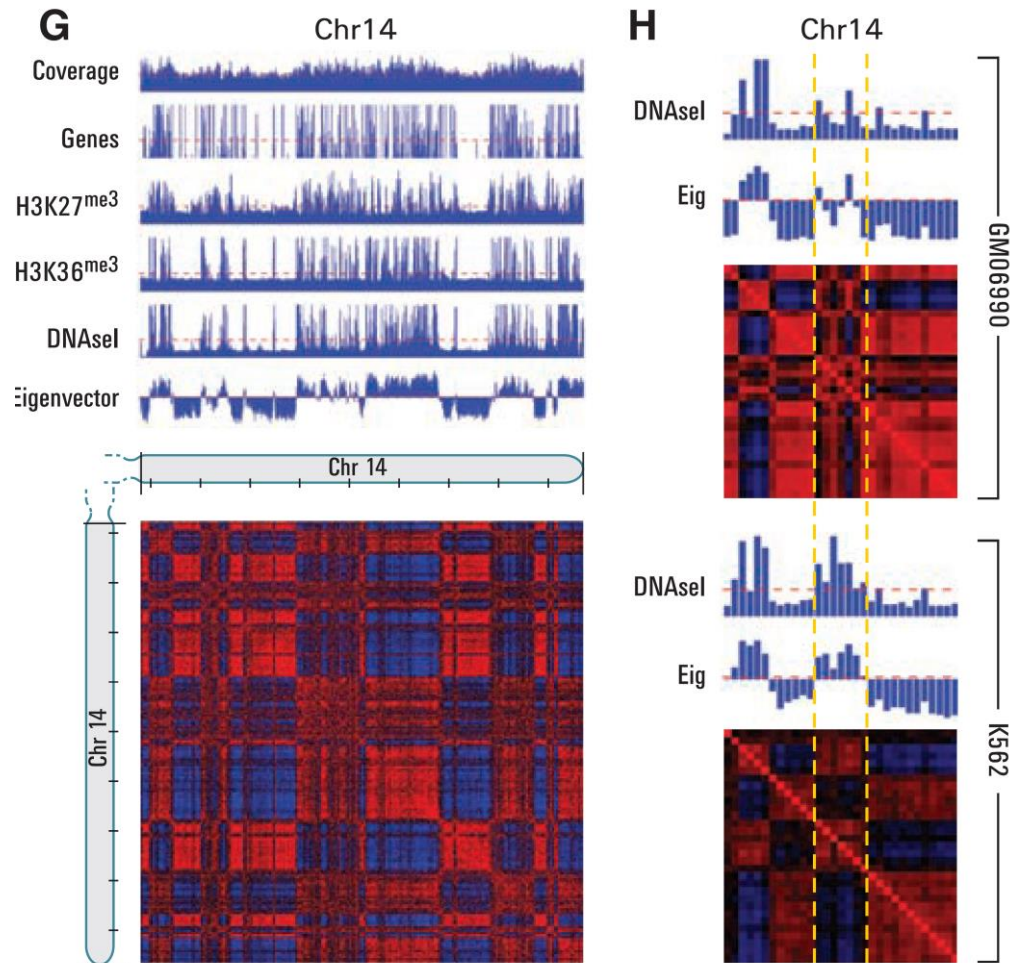
	A	B	A	B
A	Red	White	Red	White
B	White	Red	White	Red
A	Red	White	Red	White
B	White	Red	White	Red

Finding genomic compartments

- Use the first eigenvector v of the PCA/SVD. Why?
- v is the vector that minimizes $\|svv^T - A\|_F$ (Eckart-Young 1936), or in other words $A_{i,j}$ will be “near” $sv_i v_j$.
- So:
 - if v_i and v_j have the same sign, their product will be positive (high interaction bins i,j)
 - if v_i and v_j have the opposite sign, their product will be negative (low interaction bins i,j)



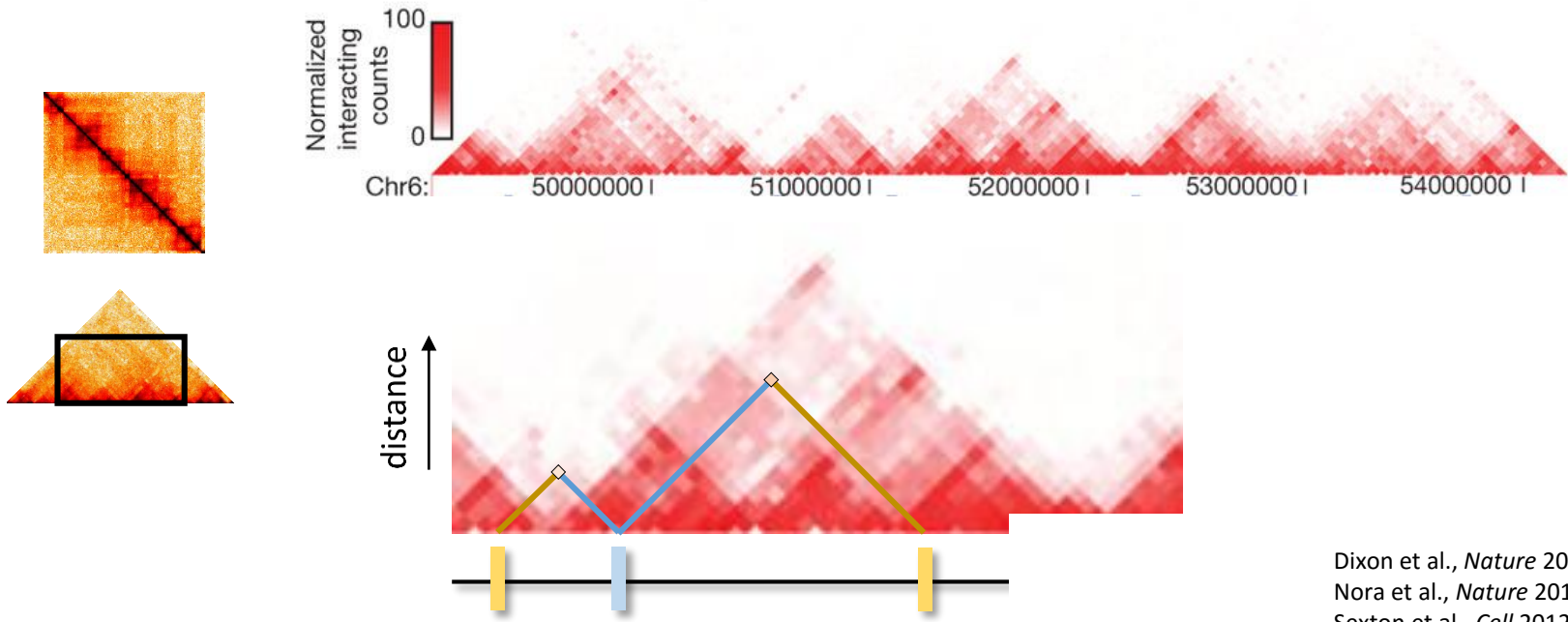
What are genomic compartments?



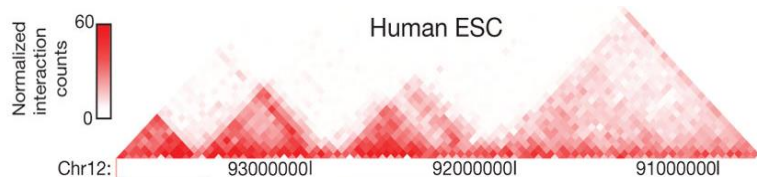
Lieberman-Aiden et al., *Science* 2009

- Correlated with chromatin state
- Cell type-specific
- Structure unclear
- Probably variable on single-cell level

Topologically Associating Domains (TADs)



Dixon et al., *Nature* 2012
Nora et al., *Nature* 2012
Sexton et al., *Cell* 2012

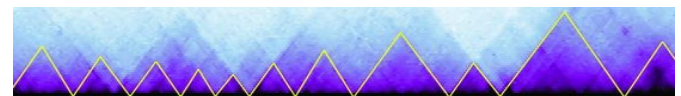


Dixon et al., *Nature* 2012

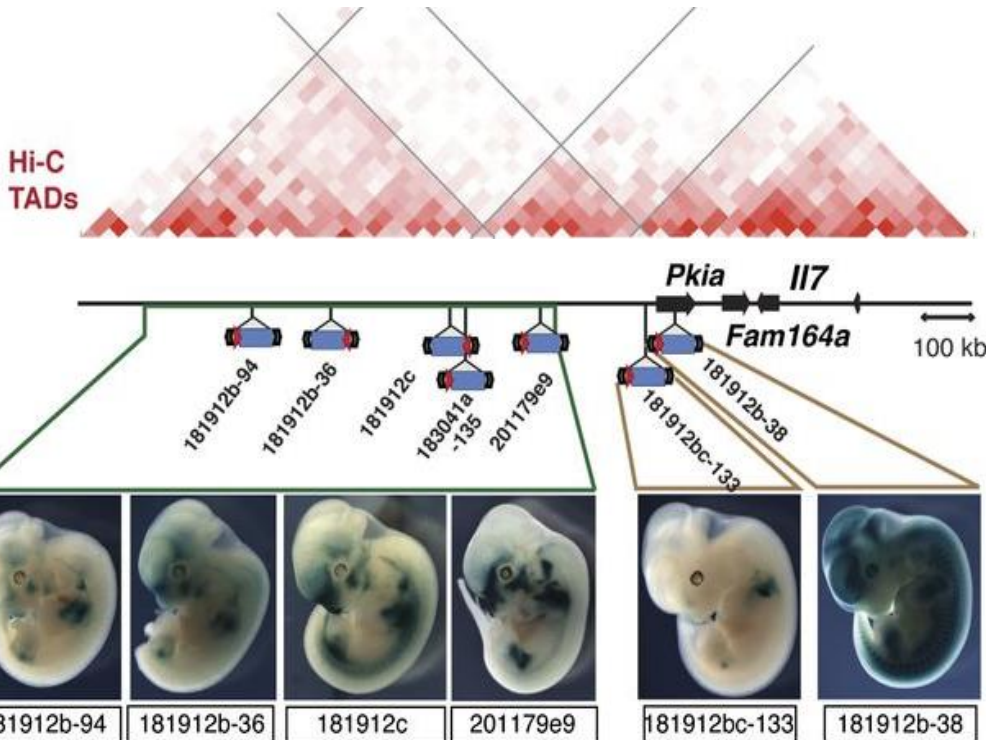
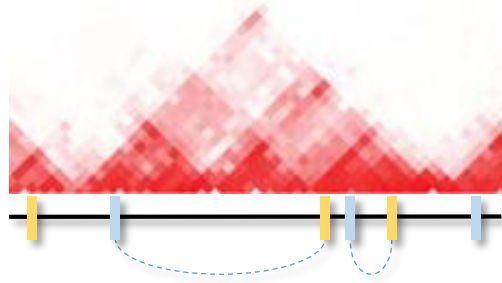
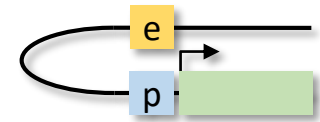
Schizosaccharomyces pombe (Mizuguchi et al., *Nature* 2014)



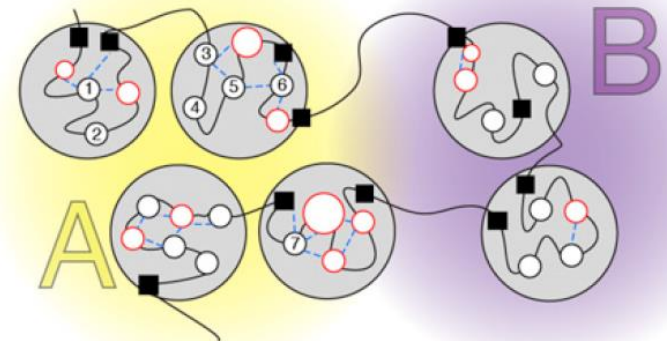
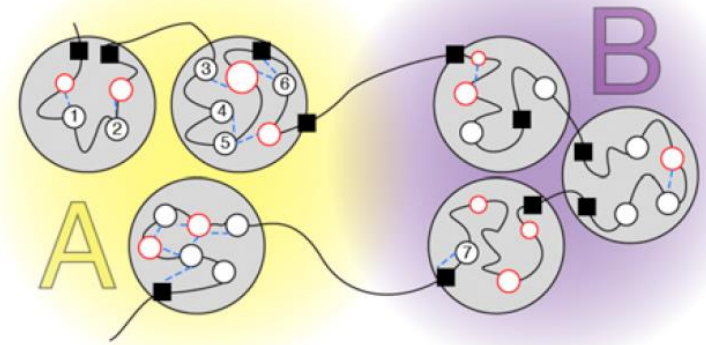
Caulobacter crescentus (Le et al., *Science* 2013)



TADs in gene regulation

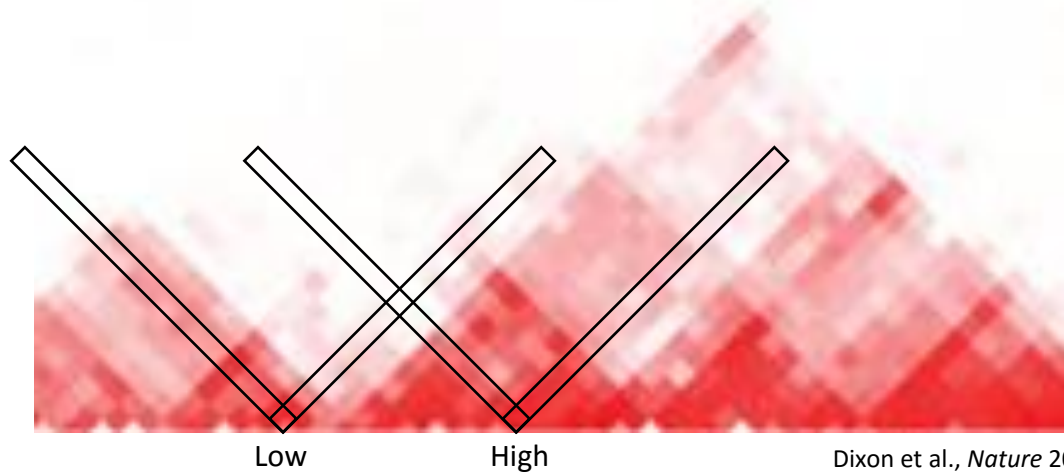


Symmons, *Genome Research* 2014

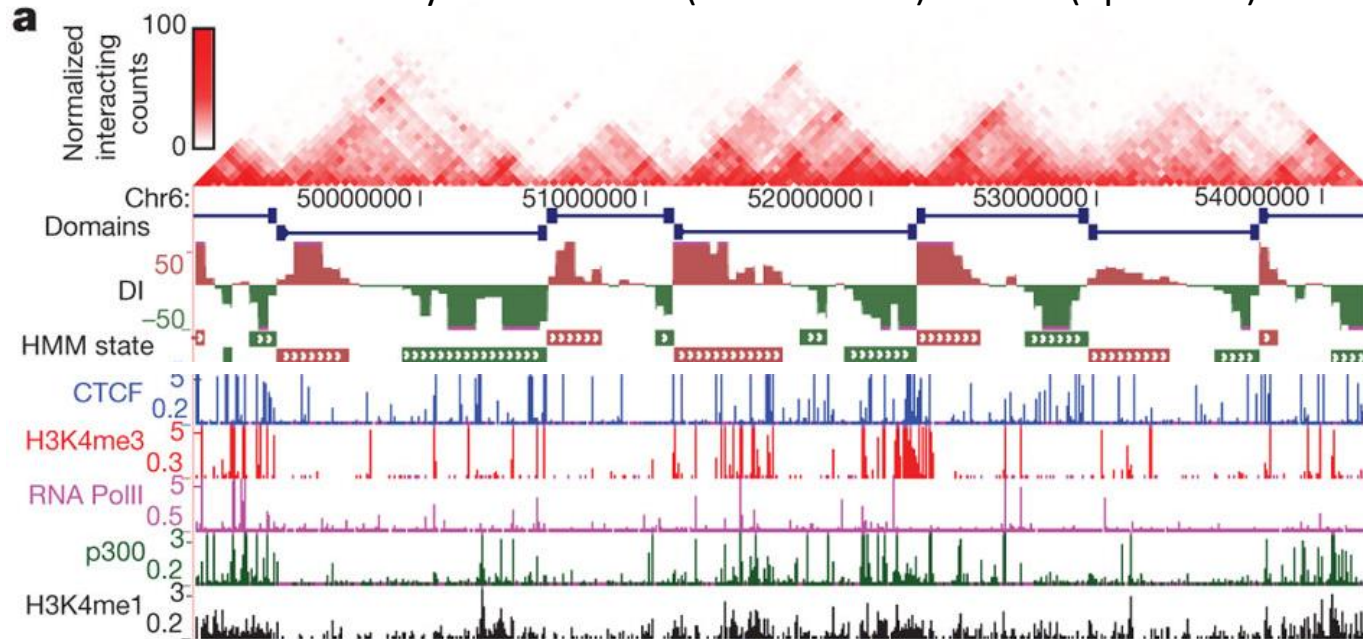


Gibcus et al., *Molecular Cell* 2015

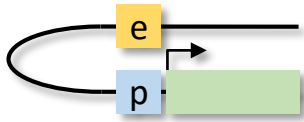
Finding TADs



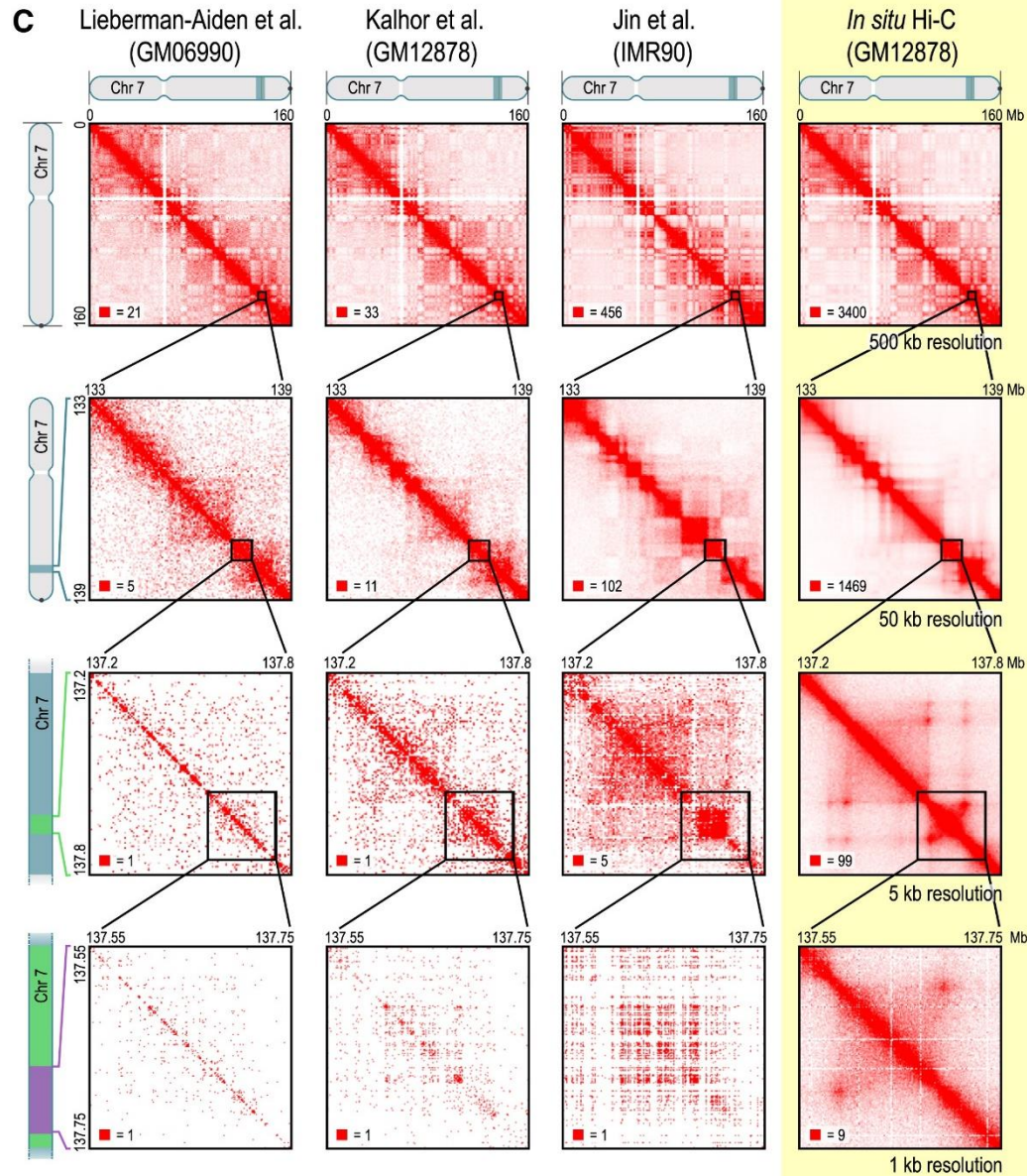
Directionality Index = $\text{mean}(\text{downstream}) - \text{mean}(\text{upstream})$



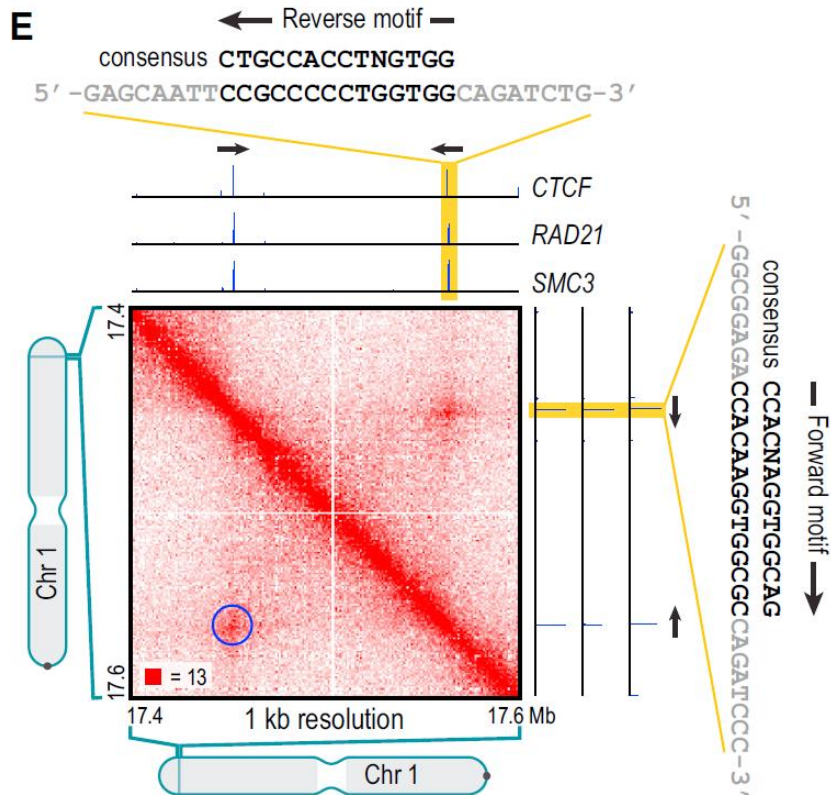
Point interactions



- Resolution problem
- Solutions:
 - Reduced interaction space (e.g. 5C)
 - More sequencing (& 4-cutter)

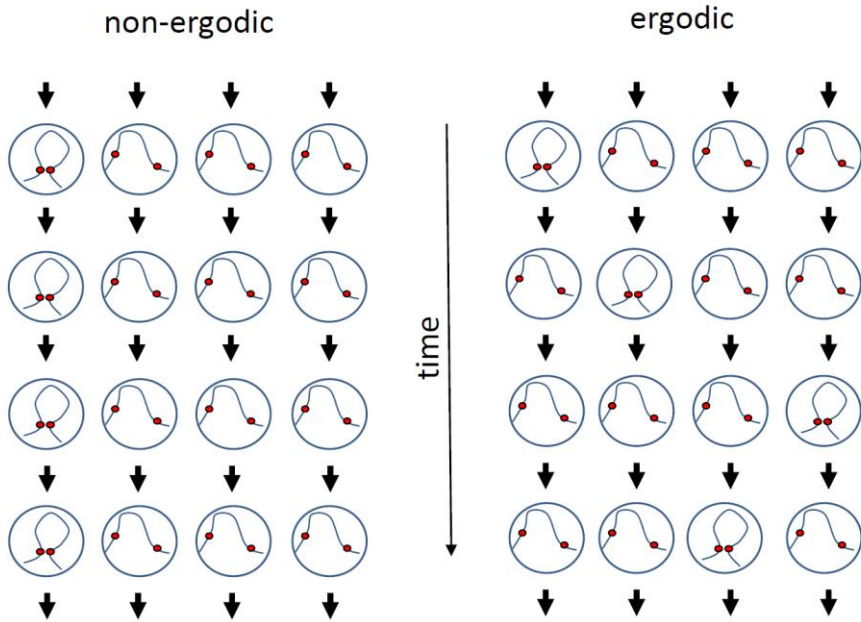


What drives point interactions?

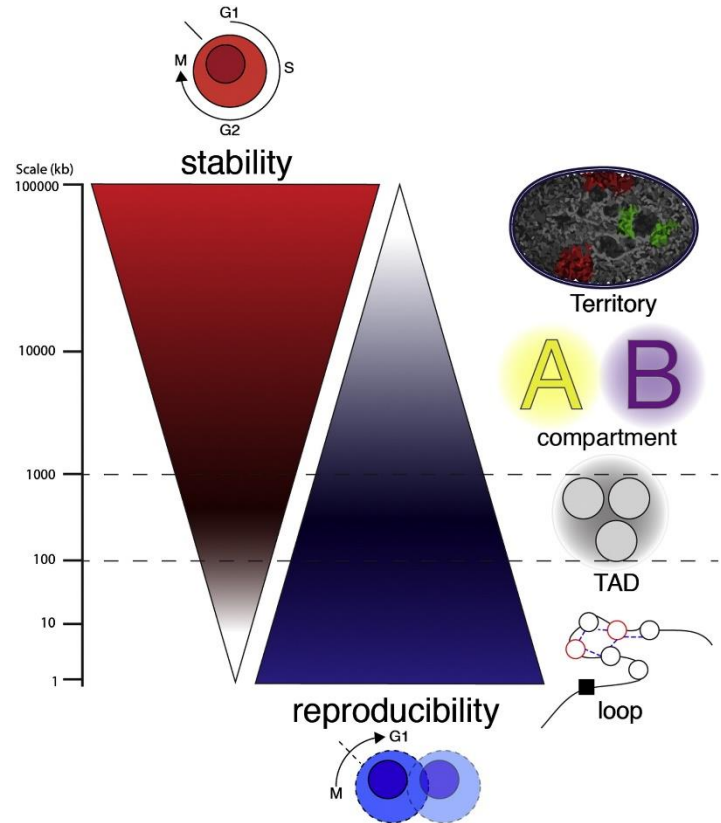


- How to identify point interactions?
- Are these all the point interactions?
(Rao et al.: 3K-8K; 30% P-E)
- Stability between cell types
- Relation to gene expression unclear

Chromatin dynamics



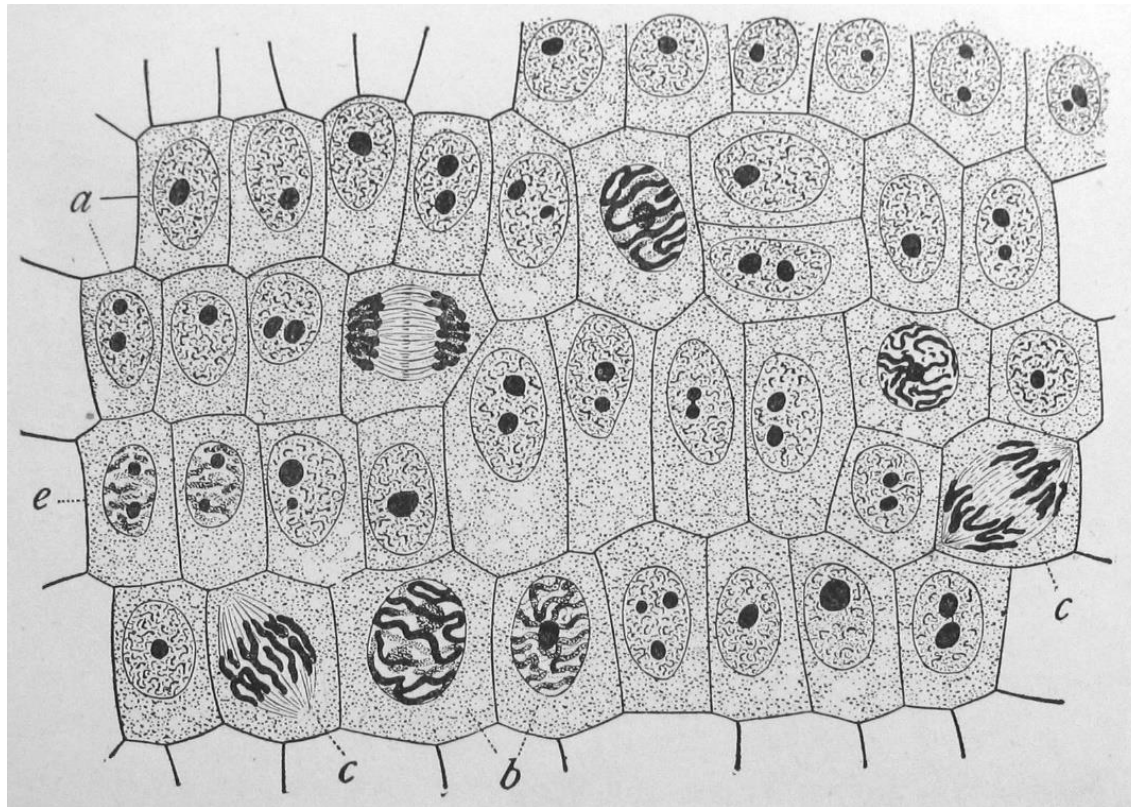
Lajoie et al., *Methods* 2015



Gibcus et al., *Molecular Cell* 2015

Generally Hi-C does not provide dynamics

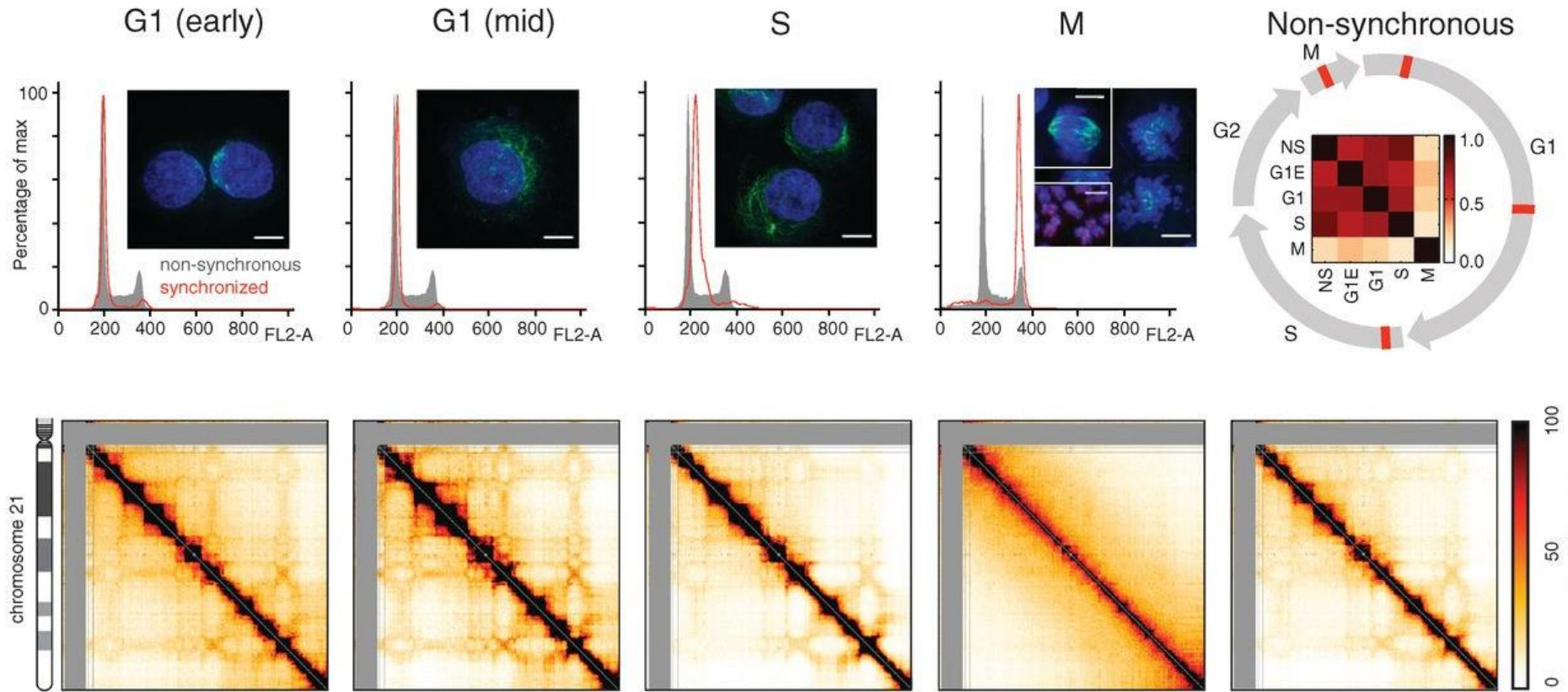
Back to the cell cycle



Wilson, *The Cell* 1900

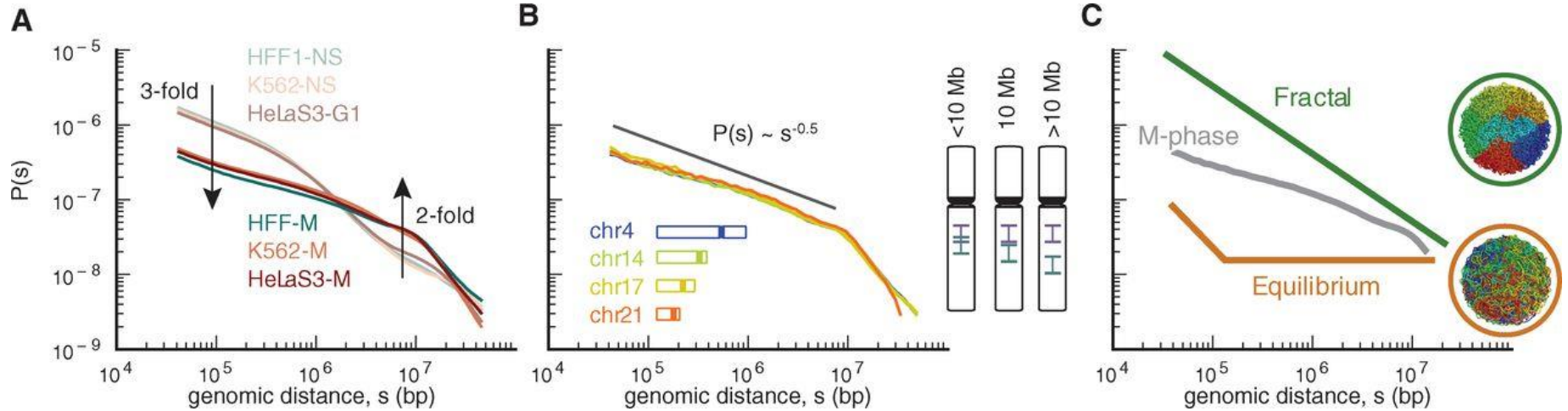
Cell cycle Hi-C

Naumova et al., *Science* 2013

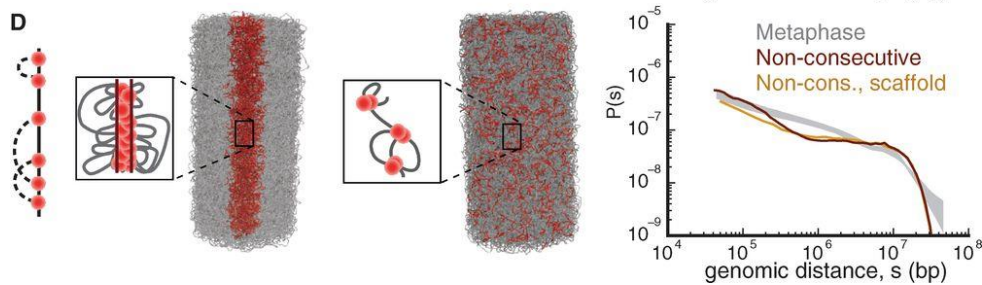
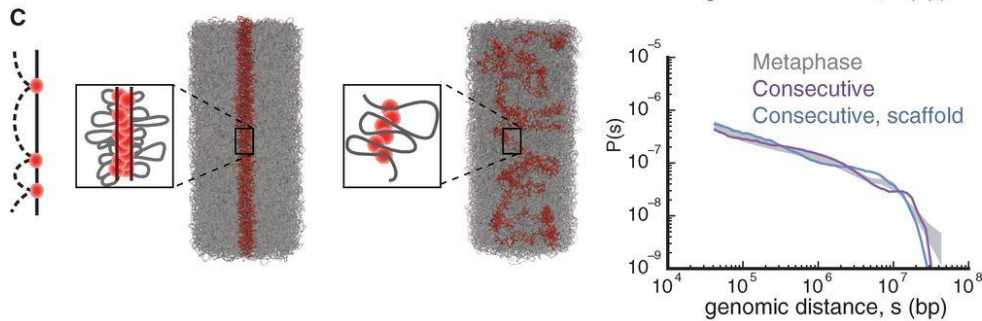
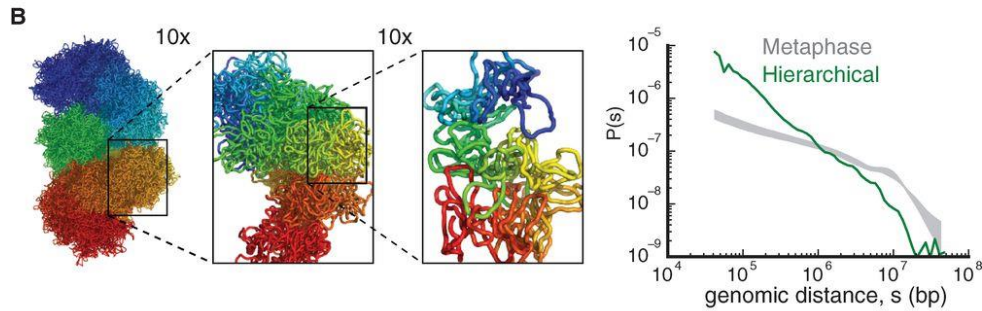
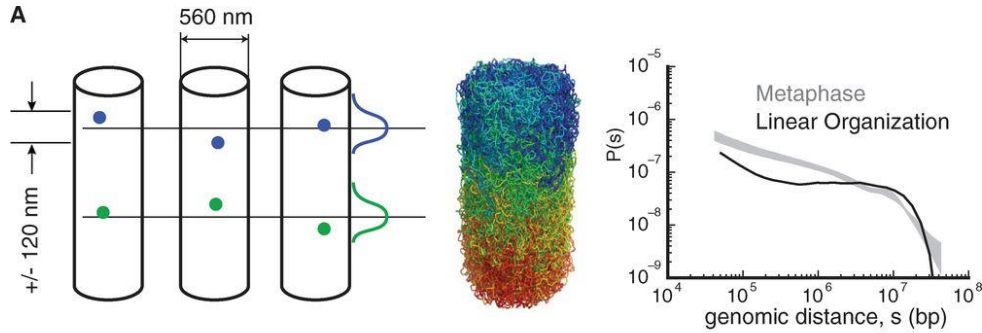


Modelling metaphase chromosomes

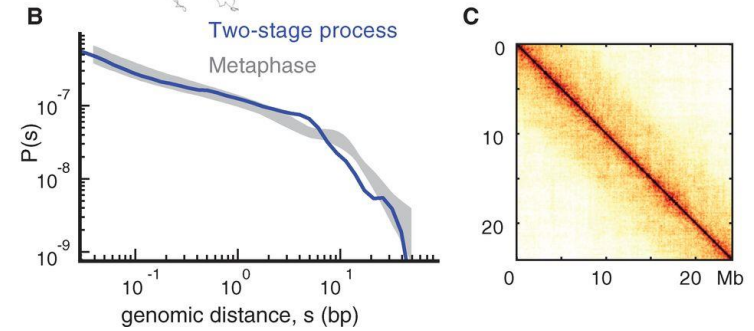
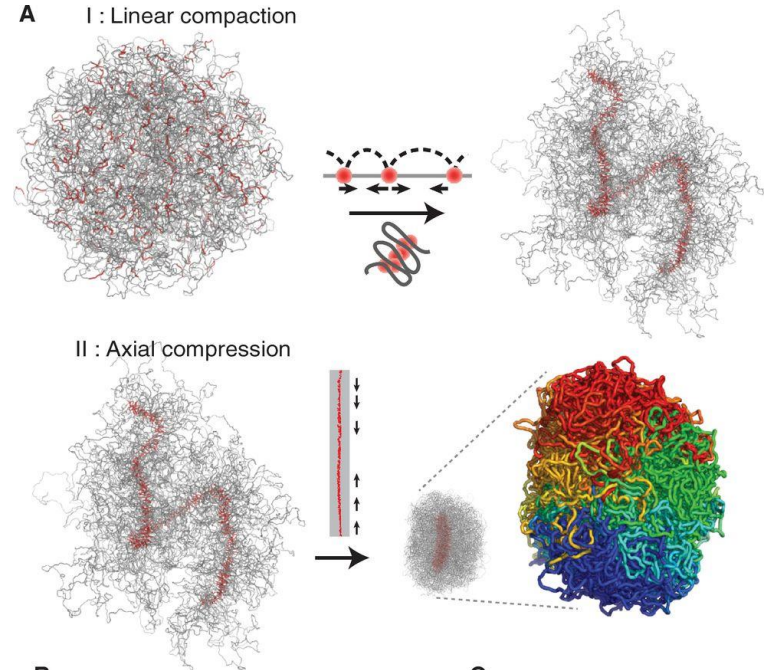
Naumova et al., *Science* 2013



Modelling metaphase chromosomes



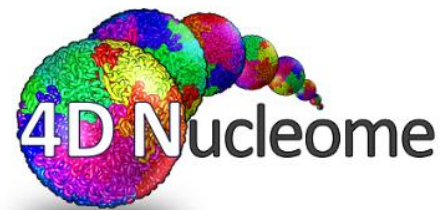
Naumova et al., *Science* 2013



How is structure re-established?

Questions and challenges

- What are the patterns/structures we observe?
- How and when are structures established?
- How do the structures relate to each other?
- How are structures related to function? Causality?
- How is functional robustness achieved for highly variable interactions?
- What are the dynamics? How are functional movements achieved?



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Liyan Yang

Ye Zhan



Some references

Original 3C paper:

Dekker, J., Rippe, K., Dekker, M., & Kleckner, N. (2002). Capturing chromosome conformation. *Science (New York, N.Y.)*, 295(5558), 1306–11.

<http://doi.org/10.1126/science.1067799>

Original Hi-C paper (also relevant for chromosomes territories, genomic compartments and fractal globule):

Lieberman-Aiden, E., van Berkum, N. L., Williams, L., Imakaev, M., Ragooczy, T., Telling, A., ... Dekker, J. (2009). Comprehensive Mapping of Long-Range Interactions Reveals Folding Principles of the Human Genome. *Science*, 326(5950), 289–293.

<http://doi.org/10.1126/science.1181369>

Single-cell Hi-C:

Nagano, T., Lubling, Y., Stevens, T. J., Schoenfelder, S., Yaffe, E., Dean, W., ... Fraser, P. (2013). Single-cell Hi-C reveals cell-to-cell variability in chromosome structure. *Nature*, 502(7469), 59–64.

<http://doi.org/10.1038/nature12593>

First genome-wide measurement of TAD structures (“topologically associating domains”):

Dixon, J. R., Selvaraj, S., Yue, F., Kim, A., Li, Y., Shen, Y., ... Ren, B. (2012). Topological domains in mammalian genomes identified by analysis of chromatin interactions. *Nature*, 485(7398), 376–380.

<http://doi.org/10.1038/nature11082>

High resolution Hi-C (where point interactions are observed):

Rao, S. S. P., Huntley, M. H., Durand, N. C., Stamenova, E. K., Bochkov, I. D., Robinson, J. T., ... Aiden, E. L. (2014). A 3D map of the human genome at kilobase resolution reveals principles of chromatin looping. *Cell*, 159(7), 1665–80.

<http://doi.org/10.1016/j.cell.2014.11.021>

Cell cycle Hi-C (genomic structures disappear when chromosomes are condensed):

Naumova, N., Imakaev, M., Fudenberg, G., Zhan, Y., Lajoie, B. R., Mirny, L. A., & Dekker, J. (2013). Organization of the Mitotic Chromosome. *Science (New York, N.Y.)*, 342, 948–53.

<http://doi.org/10.1126/science.1236083>

Some references

Biological review of Hi-C/genome structure:

Gibcus, J. H., & Dekker, J. (2013). The Hierarchy of the 3D Genome. *Molecular Cell*.

<http://doi.org/10.1016/j.molcel.2013.02.011>

Review on structural modeling of Hi-C:

Imakaev, M. V., Fudenberg, G., & Mirny, L. A. (2015). Modeling chromosomes: Beyond pretty pictures. *FEBS Letters*, 589(20), 3031–3036.

<http://doi.org/10.1016/j.febslet.2015.09.004>

Overview of Hi-C data processing and analysis (descriptive):

Lajoie, B. R., Dekker, J., & Kaplan, N. (2014). The Hitchhiker's Guide to Hi-C Analysis: Practical guidelines. *Methods*, 72, 65–75

<http://doi.org/10.1016/j.ymeth.2014.10.031>

Solving problems in 1D genome assembly by using Hi-C data:

Kaplan, N., & Dekker, J. (2013). High-throughput genome scaffolding from in vivo DNA interaction frequency. *Nature Biotechnology*, 31, 1143–1147.

<http://doi.org/10.1038/nbt.2768>

Effect of DNA sequence on genomic nucleosome organization:

Kaplan, N., Moore, I. K., Fondufe-Mittendorf, Y., Gossett, A. J., Tillo, D., Field, Y., ... Segal, E. (2009). The DNA-encoded nucleosome organization of a eukaryotic genome. *Nature*, 458(7236), 362–6.

<http://doi.org/10.1038/nature07667>