Spin interferometry and entanglement generation with Rashba spin splitting

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and

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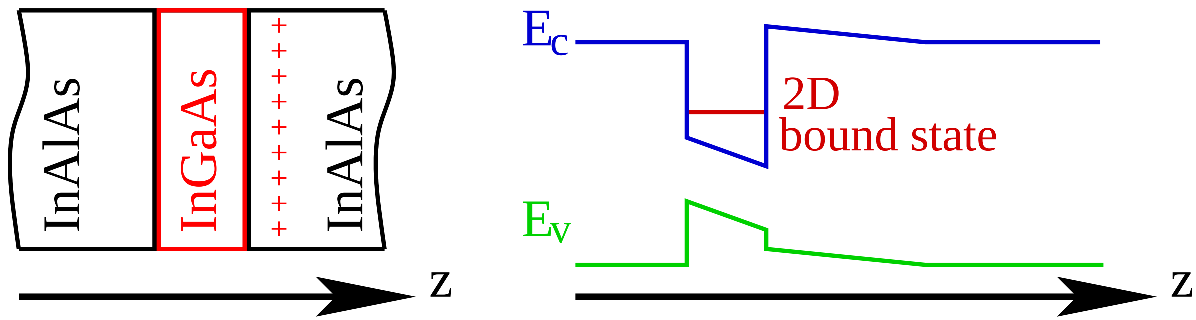
Outline

- Introduction
  - Rashba spin splitting: basics
  - electron–wave interference
- Single–electron interference at a Mach–Zehnder interferometer with Rashba spin splitting
  - theory: spin–resolved scattering matrix
  - results & applications
- Two–particle interference and entanglement generation
  - spin–dependent two–particle scattering matrix
  - entanglement from projective charge measurement
- Conclusions

Rashba spin splitting: Basics

- band bending in heterostructures: 2D electron system



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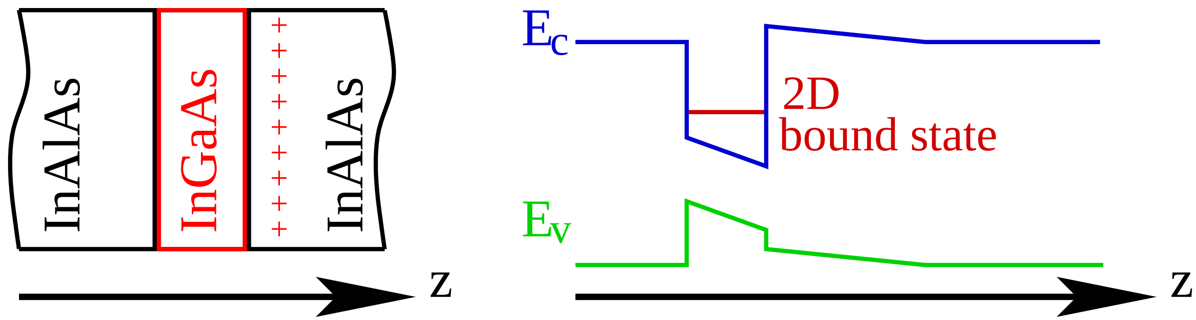

- structural inversion asymmetry ⇒ spin–orbit coupling

$$H_{\mathrm{so}} = \frac{1}{2m_*}\left[\vec{p}\times\hbar\vec{\nabla}\left(\frac{V_{\mathrm{ext}}}{2E_{\mathrm{g}}}\right)\right]\cdot\vec{\sigma}$$

(for small band gap E_{g})

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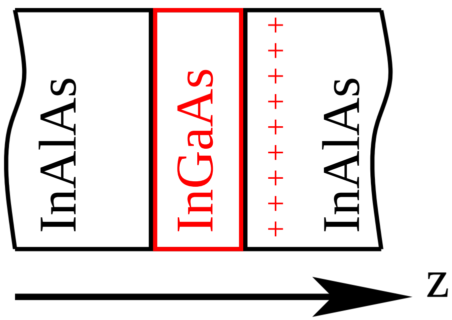
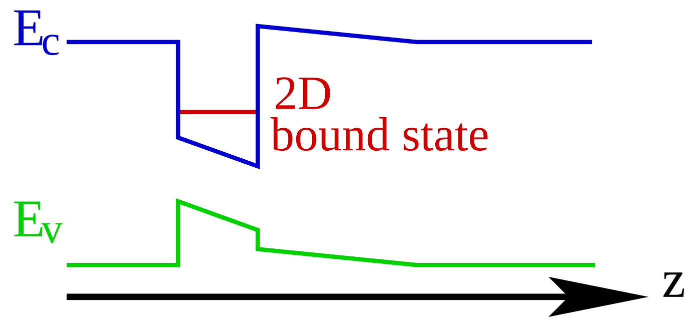
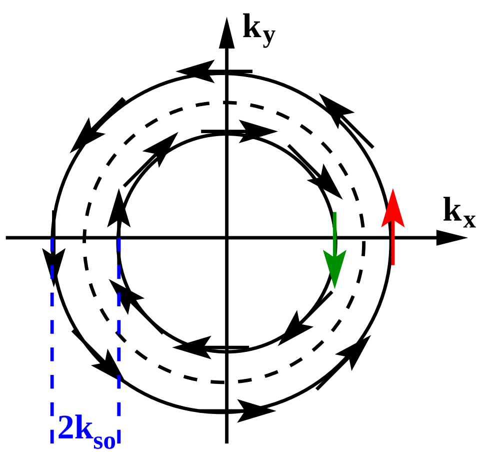




- structural inversion asymmetry $\Rightarrow$ spin–orbit coupling

$H_{\mathrm{R}} = \frac{\hbar}{m} k_{\mathrm{so}}\, \hat{z} \cdot [\vec{\sigma} \times \vec{p}]$, w/ $k_{\mathrm{so}} = \frac{\pi}{L_{\mathrm{so}}}$ tunable by gate voltage



Fermi surface splits into two; electron spin $\perp$ momentum $\hbar\vec{k}$; spin precesses

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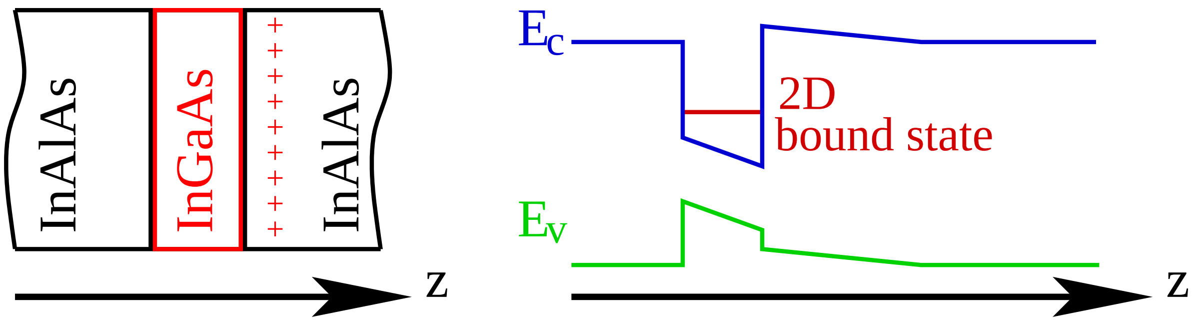

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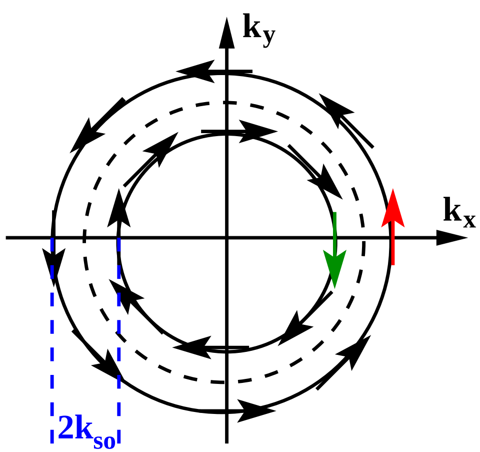

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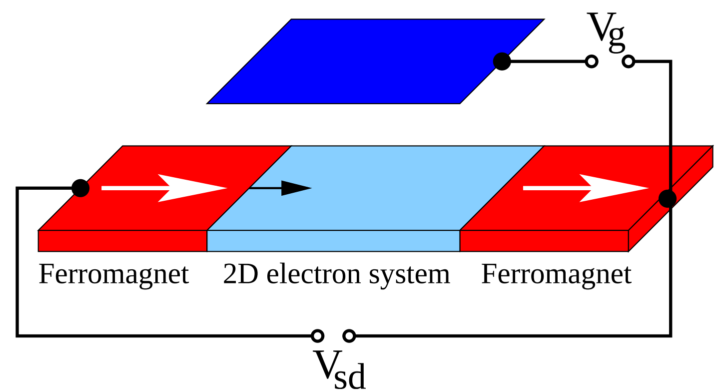

(Datta & Das, Appl. Phys. Lett. 1990)

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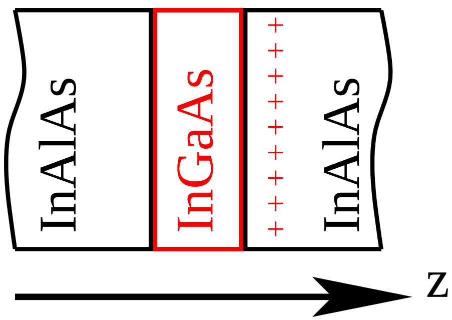

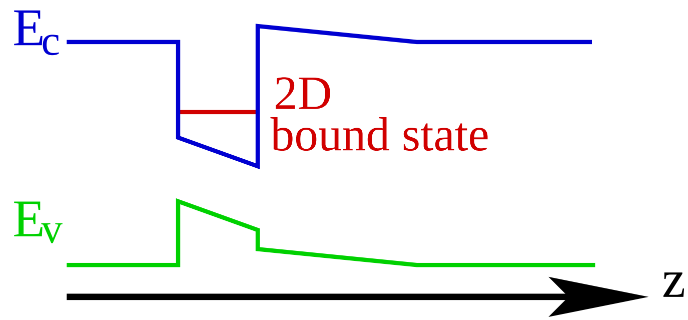

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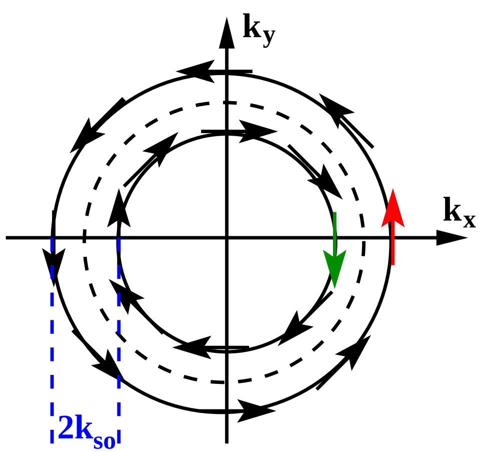

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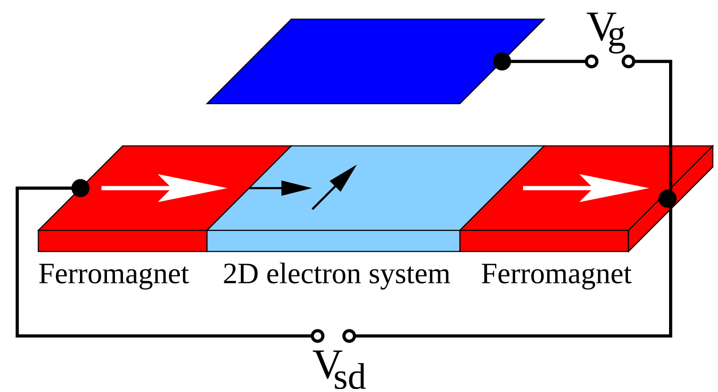

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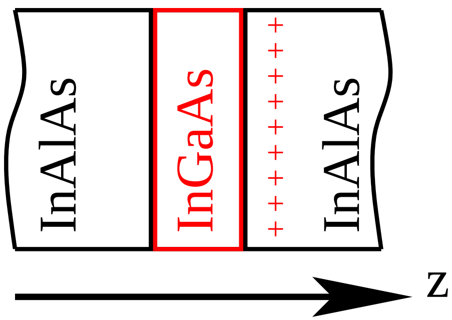

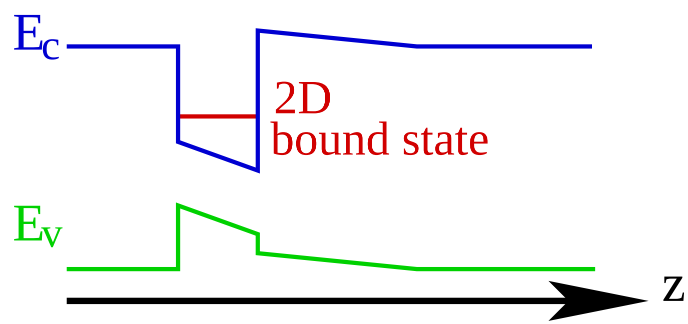

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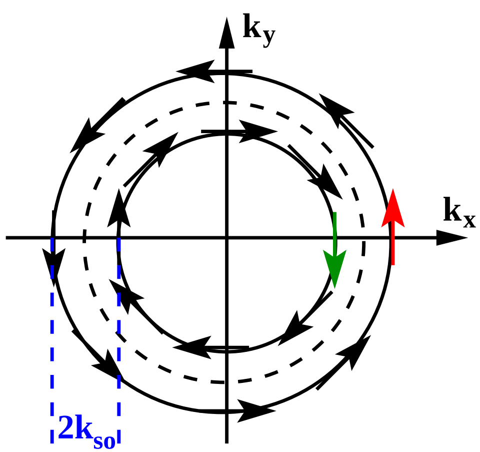

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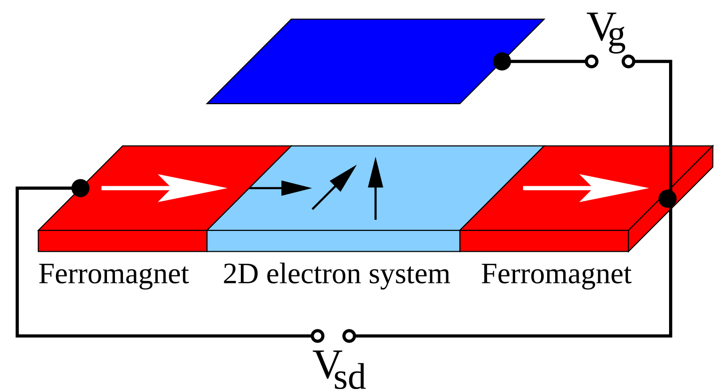

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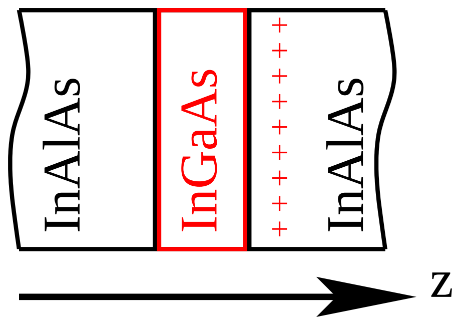

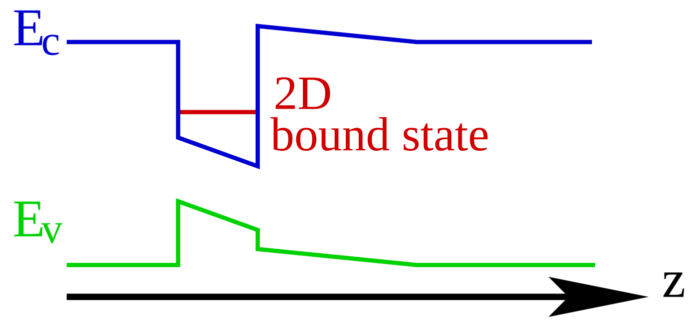

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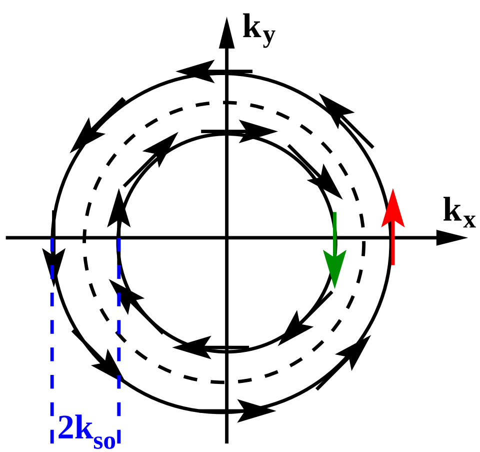

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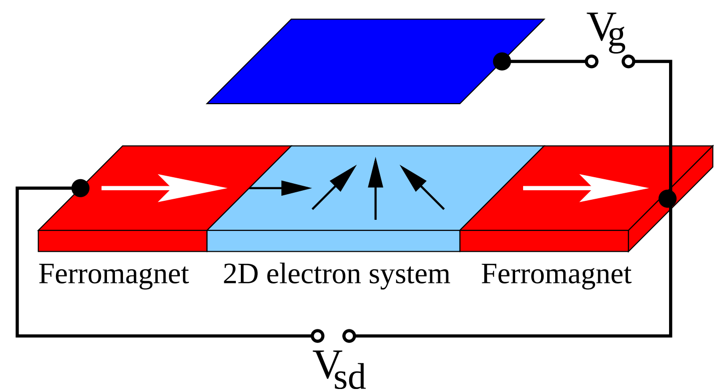

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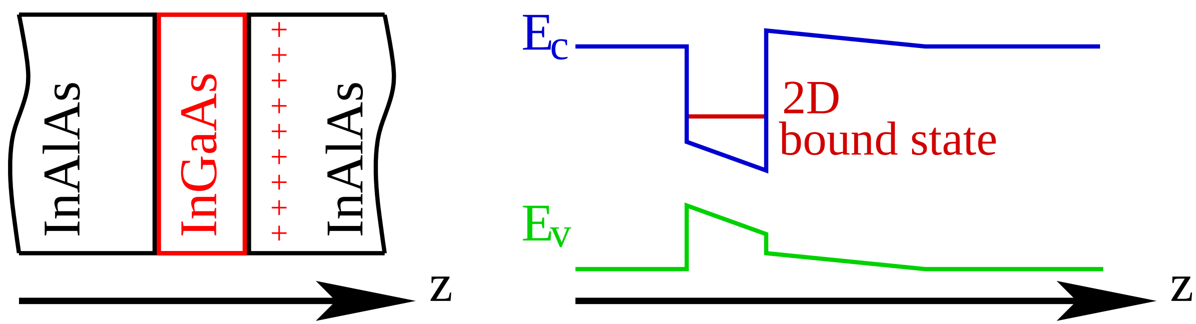

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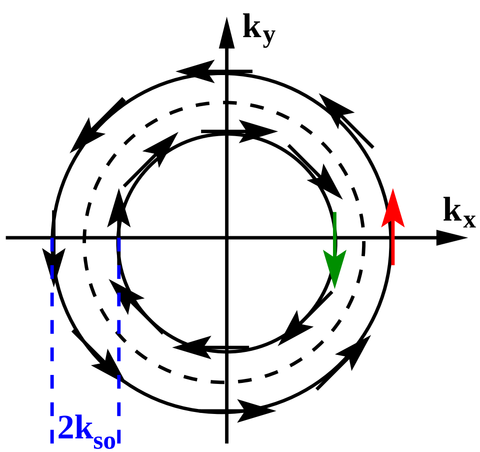

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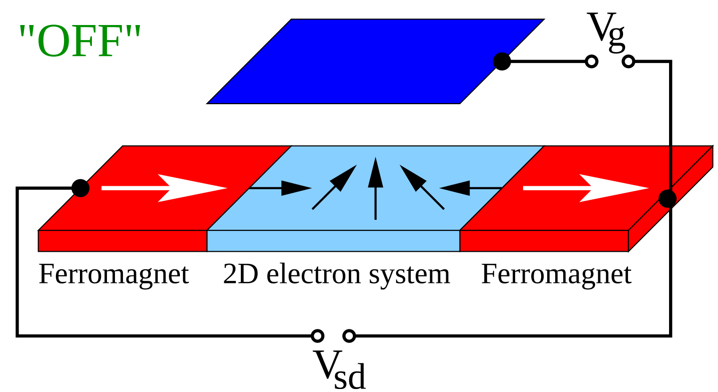

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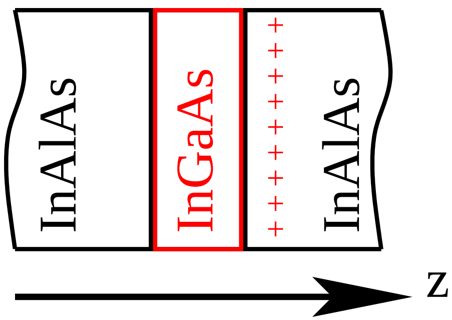

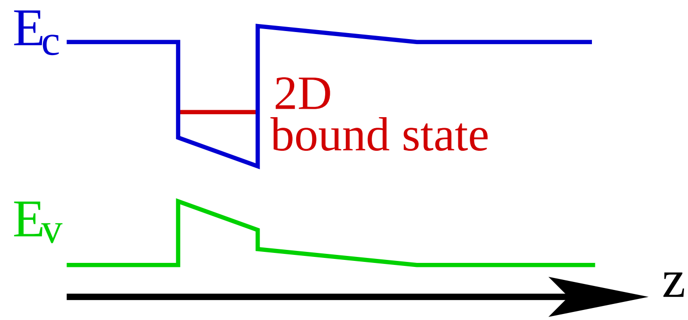

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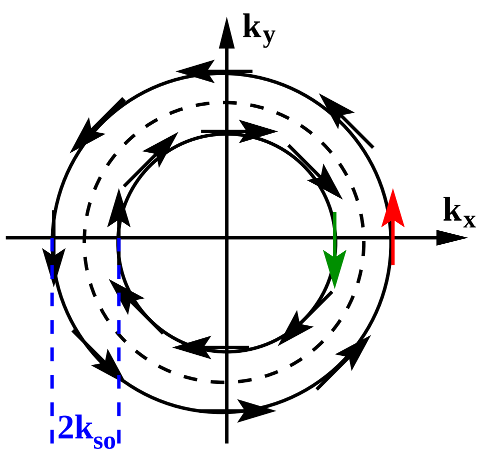

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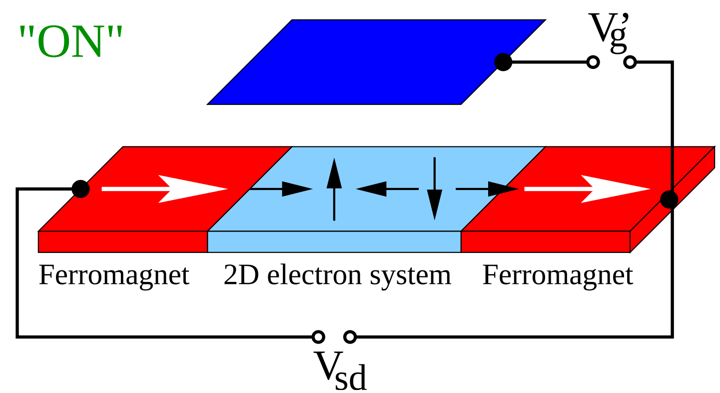

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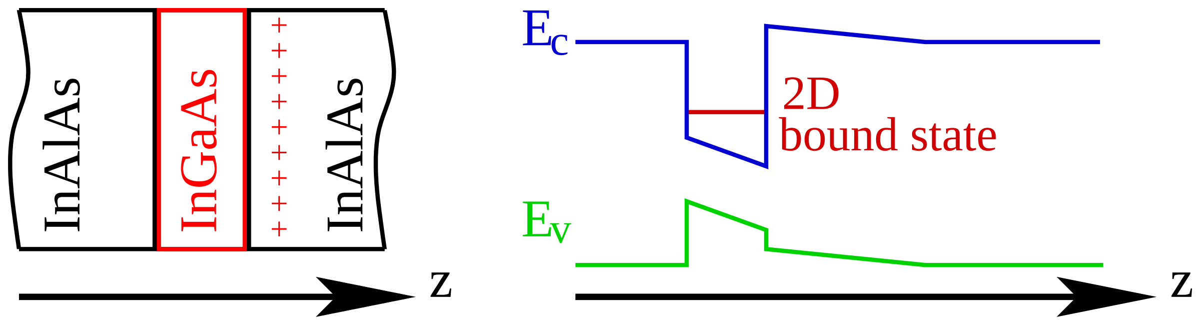

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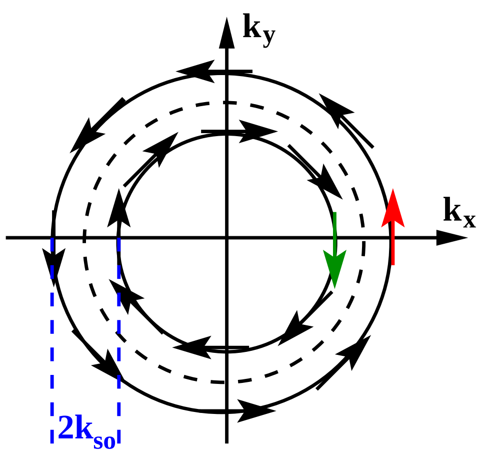

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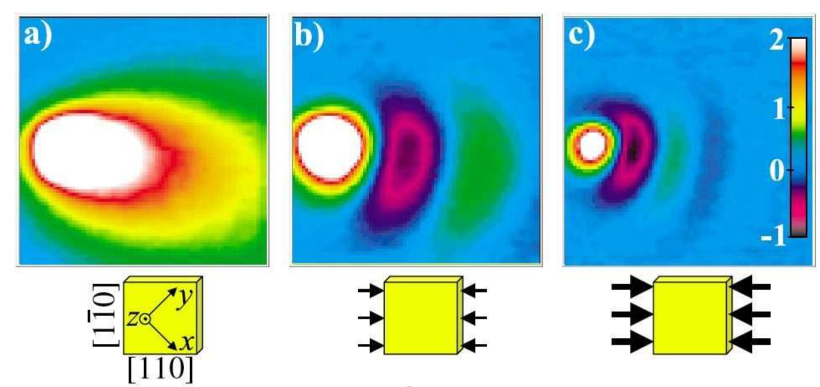

(Crooker & Smith, Phys. Rev. Lett. 2005)

Interference of electron waves

- quantum optics: see interference fringes in intensity

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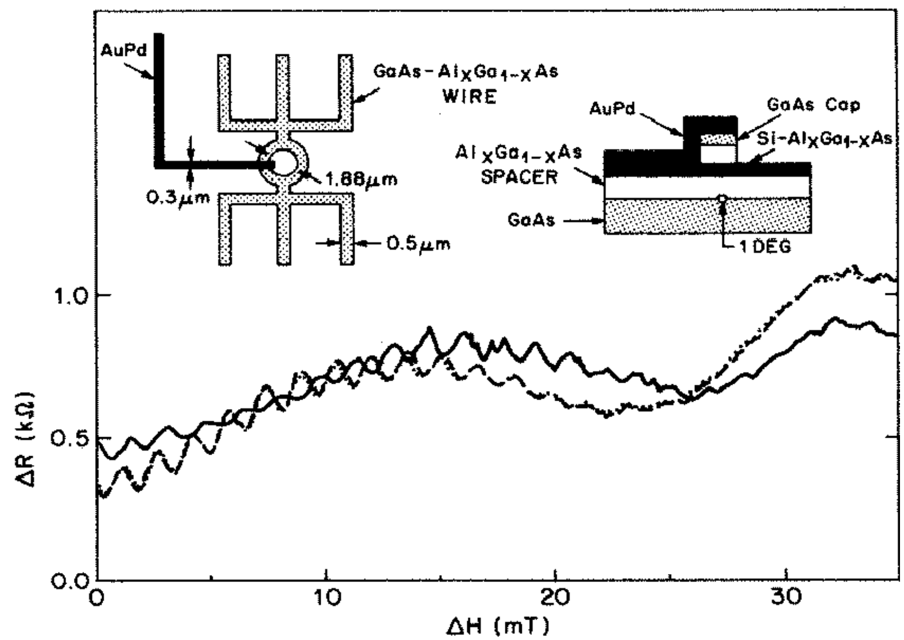
- celebrated examples: Aharonov–Bohm oscillations



(de Vegvar et al., PRB 1989)

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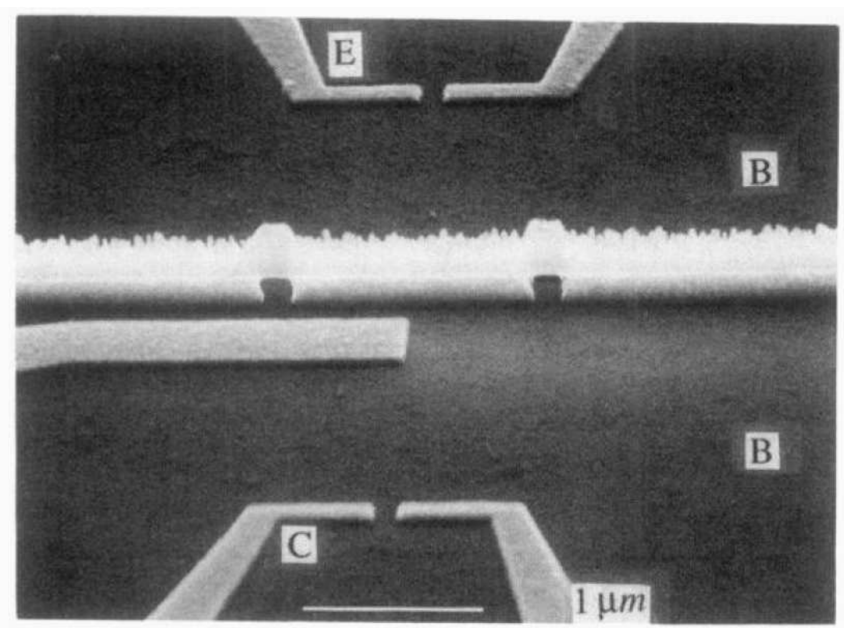
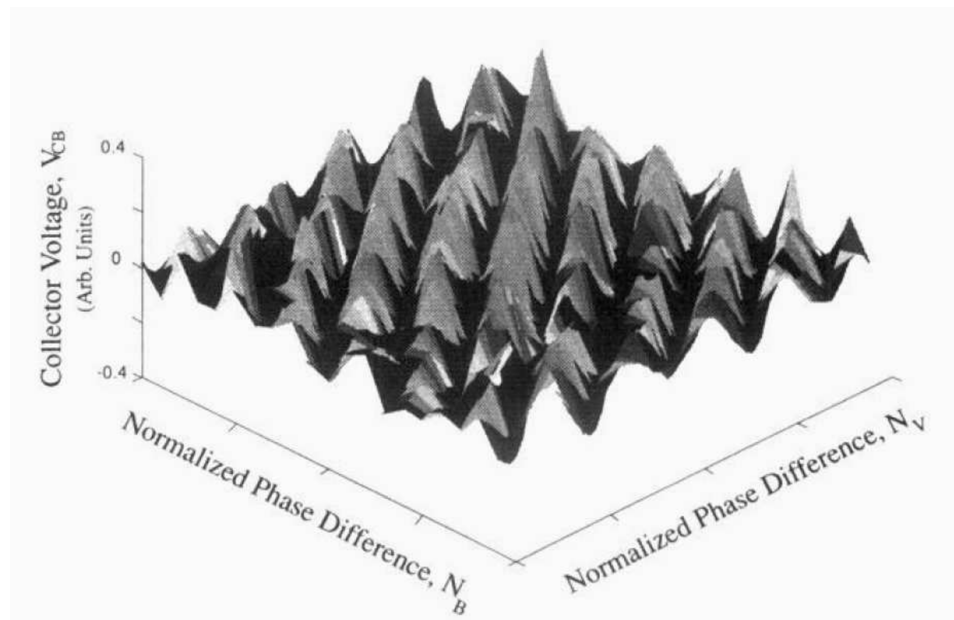
- celebrated examples: Young's Double–Slit experiment





(Yacoby et al., PRL 1994)

Interference of electron waves

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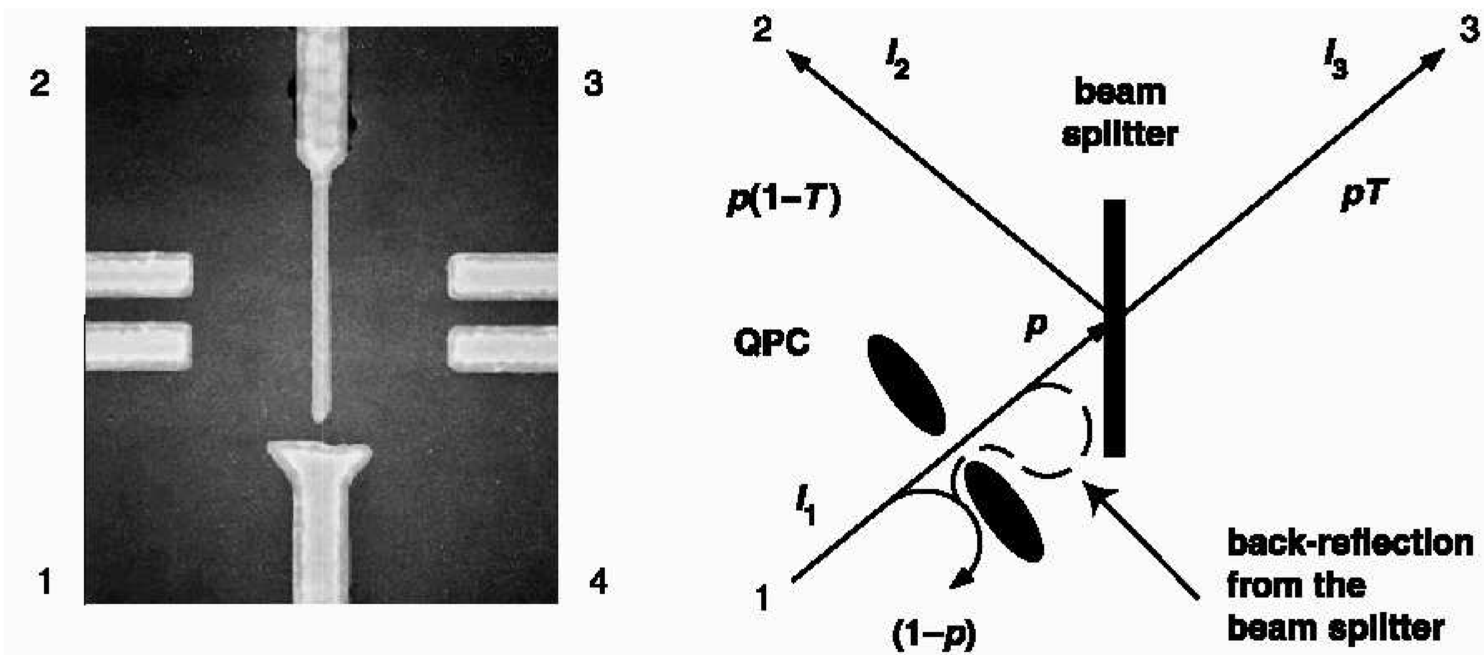
- phase–coherent electronics: conductance modulation (e.g., as function of gate voltage or magnetic field)
- celebrated examples: Hanbury-Brown and Twiss expt.



(Oliver et al., Science 1999)

Mach–Zehnder interferometer

- invented in optics for measuring 1^{st}–order coherence

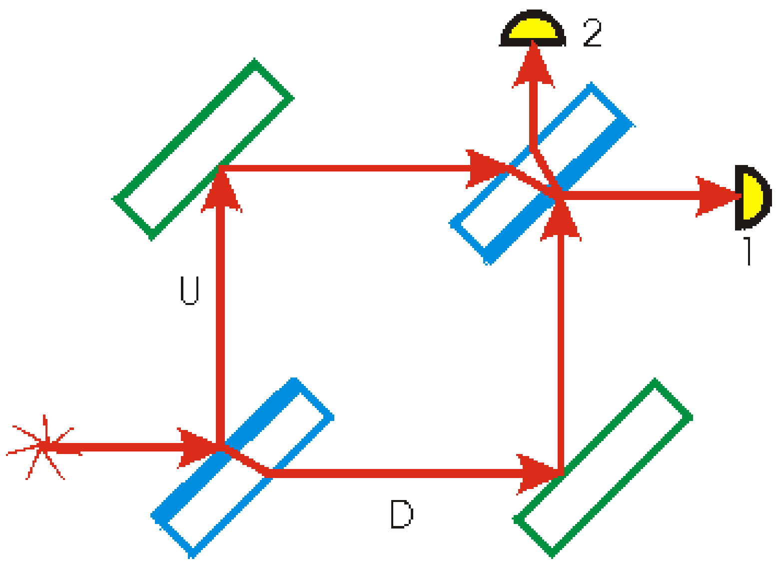


Illustration: D. M. Harrison, U Toronto

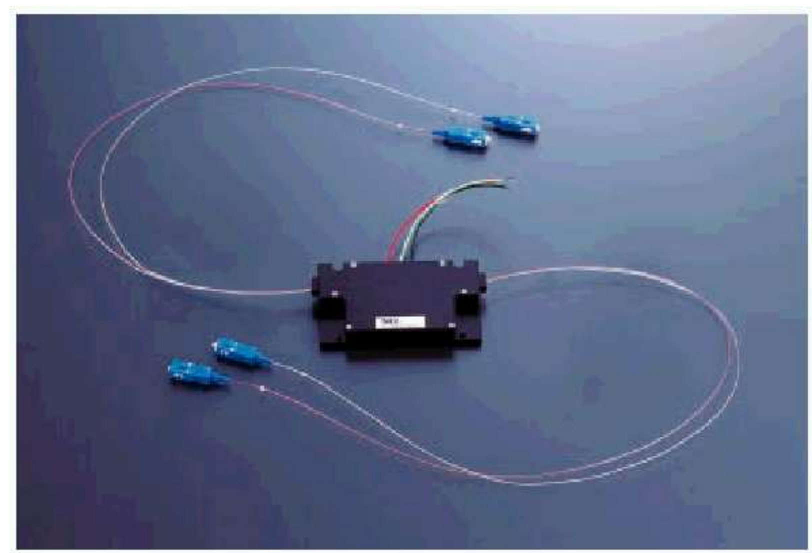
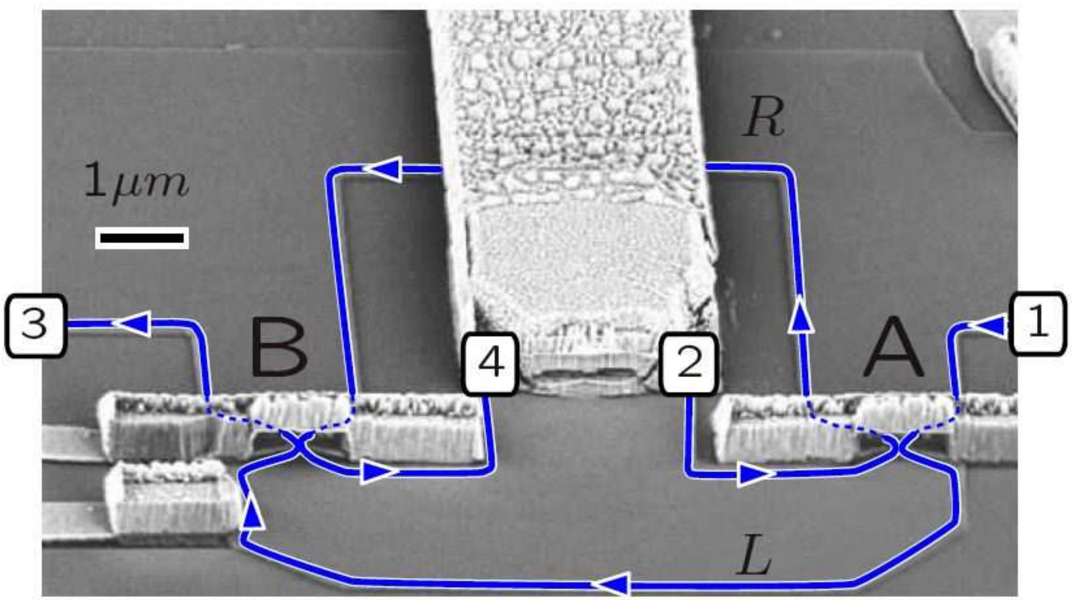


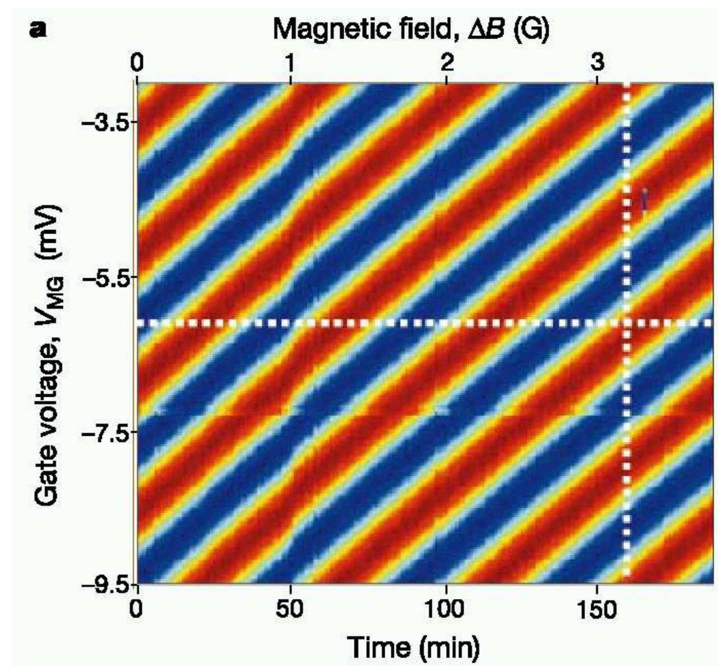
Photo: Website of NTT Electronics Corp.

Mach–Zehnder interferometer

- invented in optics for measuring 1^{st}–order coherence
- an electronic version was only recently realized using quantum–Hall edge states

(Ji et al., Nature 2003, Neder et al., Phys. Rev. Lett. 2006)





(Image: F. Marquardt, cond-mat/0604626)

Electron interference with spin

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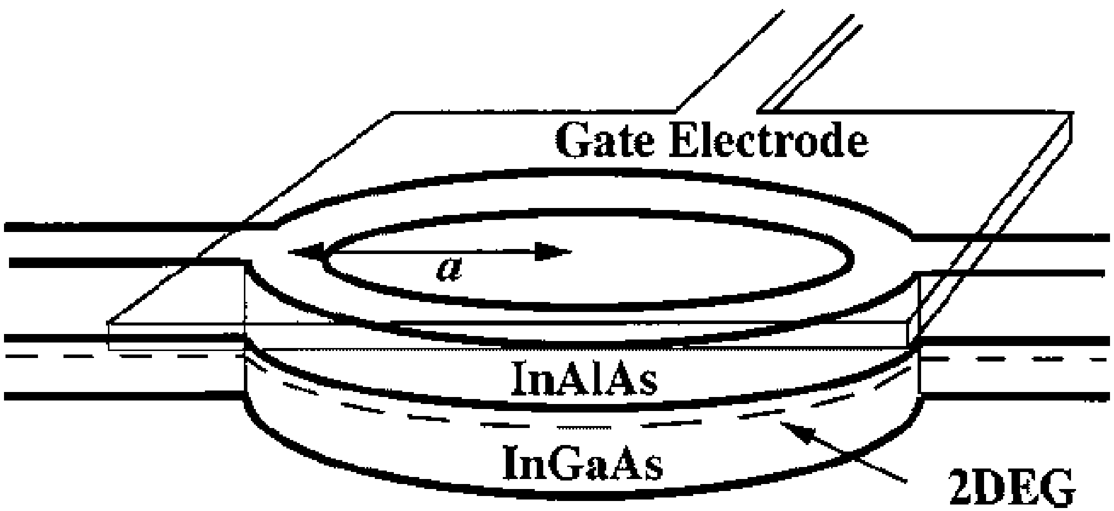
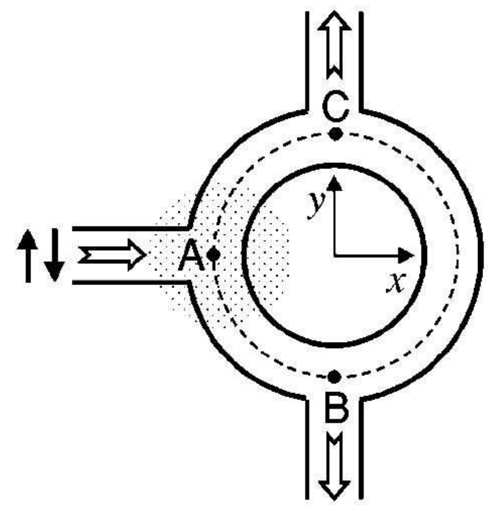


(Nitta et al., Appl. Phys. Lett. 1999)



(Kiselev & Kim, J. Appl. Phys. 2003)

Electron interference with spin

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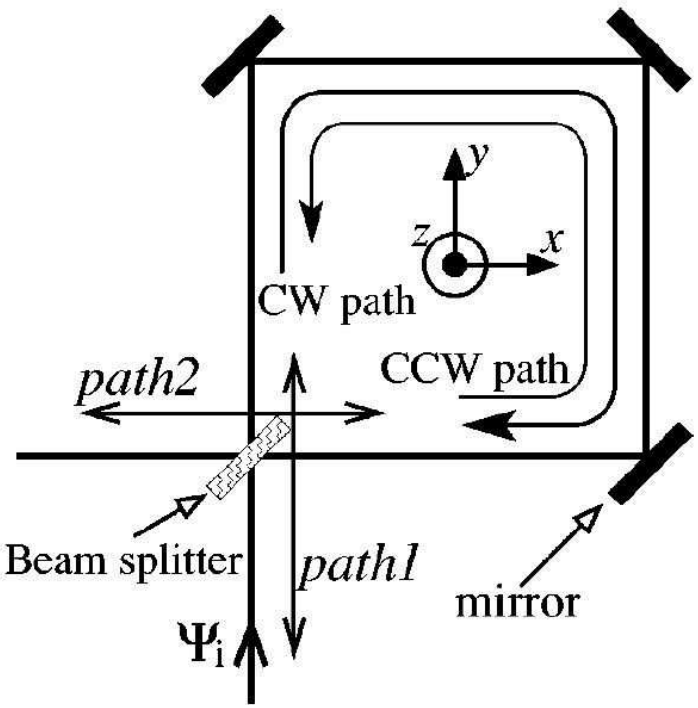
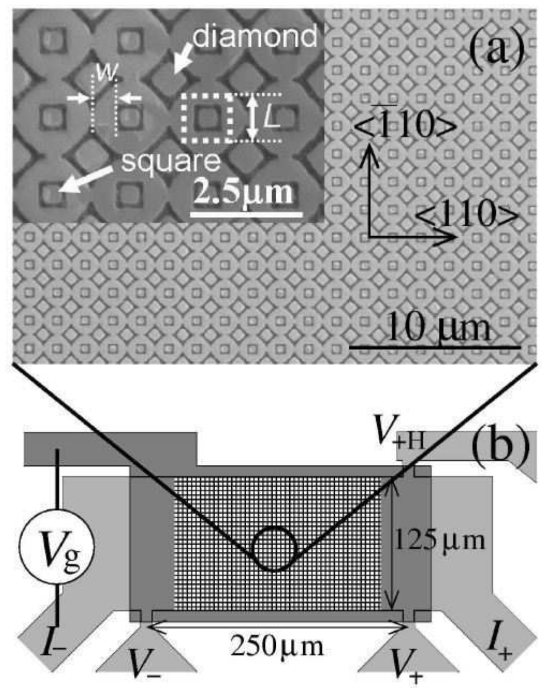
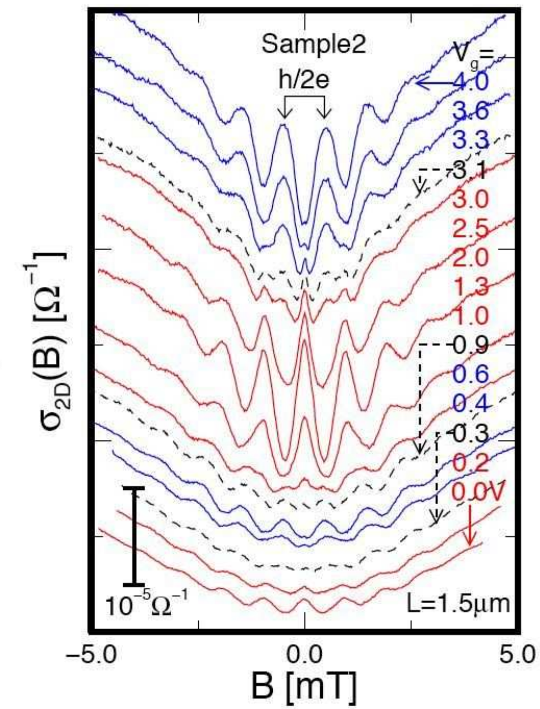
- recent experiments: Altshuler-Aronov-Spivak oscillations







(Koga et al., Phys. Rev. B 2004, see also cond-mat/0504743)

Spin–dependent electron interferometry based on Rashba spin–orbit coupling

Interferometer + spin splitting

- basic building blocks (wave guides, beam splitter, mirror) are realized in semiconductor heterostructures

Interferometer + spin splitting

- basic building blocks (wave guides, beam splitter, mirror) are realized in semiconductor heterostructures
- spin-dependent feature: tuneable Rashba spin splitting

  (Nitta et al., Phys. Rev. Lett. 1997; Engels et al., Phys. Rev. B 1997)

Interferometer + spin splitting

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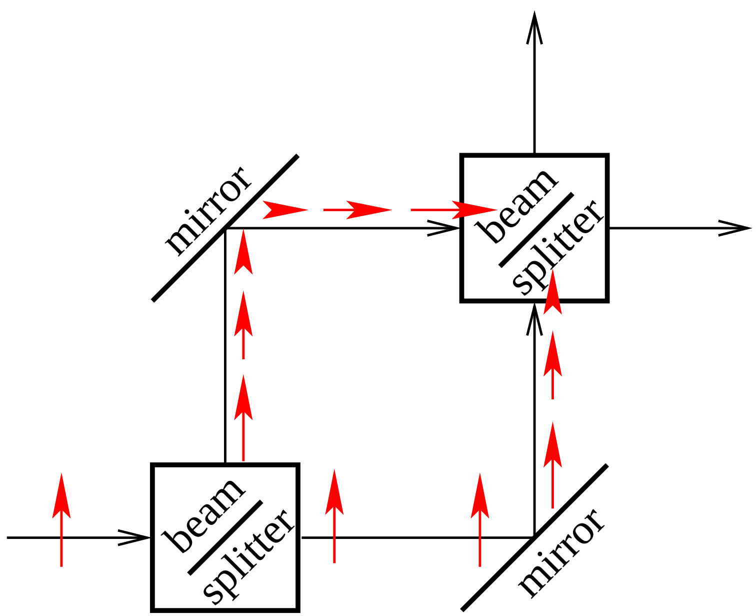
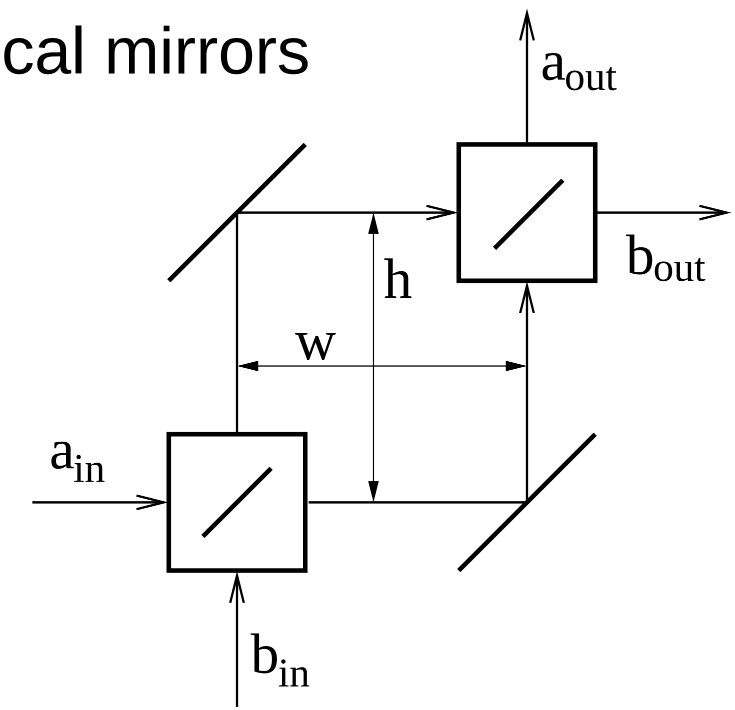
- spin-dependent feature: tuneable Rashba spin splitting
  (Nitta et al., Phys. Rev. Lett. 1997; Engels et al., Phys. Rev. B 1997)
- our model: single 1D subband, symmetric and identical beam splitters, perfect and identical mirrors





Theoretical description

- elements characterized by their 4×4 spin–resolved scattering matrix, use basis of spin–split eigenstates

$$\begin{pmatrix} a_{\text{out}+} \\ a_{\text{out}-} \\ b_{\text{out}+} \\ b_{\text{out}-} \end{pmatrix} = \underbrace{\begin{pmatrix} r_{1++} & r_{1+-} & t_{2++} & t_{2+-} \\ r_{1-+} & r_{1--} & t_{2-+} & t_{2--} \\ t_{1++} & t_{1+-} & r_{2++} & r_{2+-} \\ t_{1-+} & t_{1--} & r_{2-+} & r_{2--} \end{pmatrix}}_{\mathcal{S}} \begin{pmatrix} a_{\text{in}+} \\ a_{\text{in}-} \\ b_{\text{in}+} \\ b_{\text{in}-} \end{pmatrix}$$

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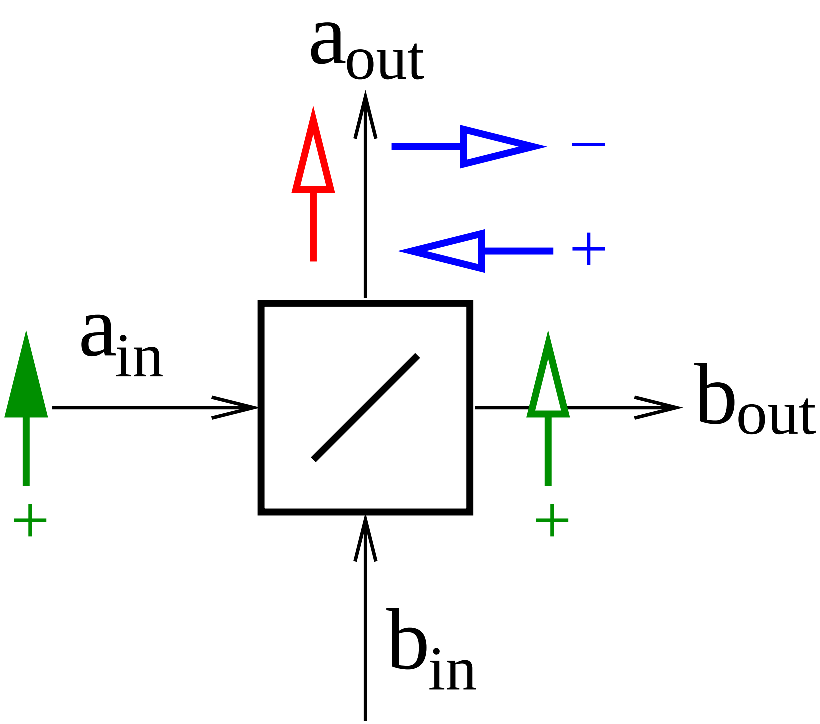
- spin conservation at beam splitter / mirror: incident basis state reflected into mixture of basis states in outgoing arm



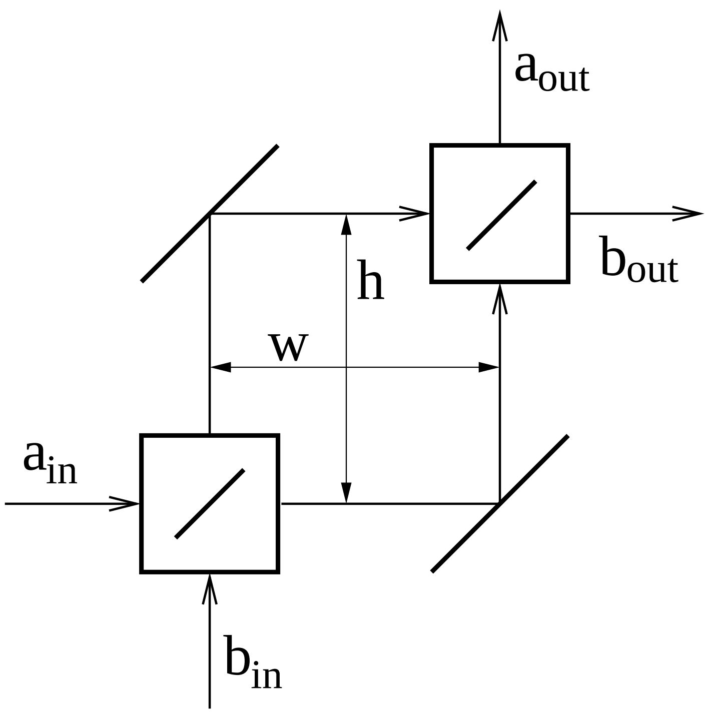
$$\mathcal{S}_{bs} = \begin{pmatrix} \frac{i}{2} & -\frac{1}{2} & \frac{1}{\sqrt{2}} & 0 \\ -\frac{1}{2} & \frac{i}{2} & 0 & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & 0 & \frac{i}{2} & \frac{1}{2} \\ 0 & \frac{1}{\sqrt{2}} & \frac{1}{2} & \frac{i}{2} \end{pmatrix}$$

(Feve et al., Phys. Rev. B 2002)

MZ spin interferometer: Results

UZ, Appl. Phys. Lett. **85**, 2616 (2004)

- spin mixture for reflection + spin–dependent dynamical phase: all included in total scattering matrix



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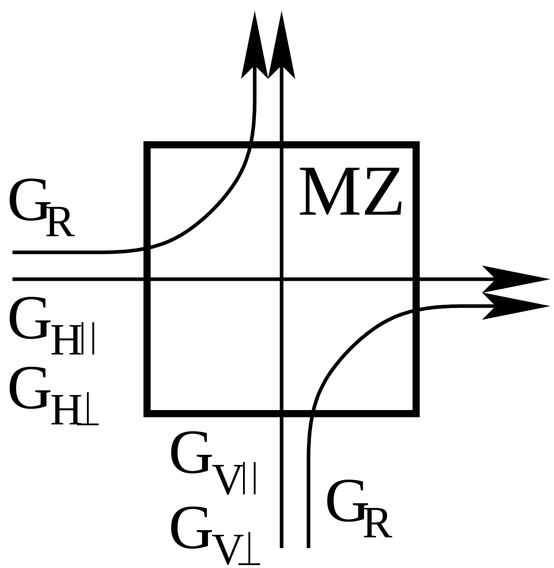

$$\mathcal{G} = \begin{pmatrix} G_R & G_R & G_{V||} & G_{V\perp} \\ G_R & G_R & G_{V\perp} & G_{V||} \\ G_{H||} & G_{H\perp} & G_R & G_R \\ G_{H\perp} & G_{H||} & G_R & G_R \end{pmatrix}$$

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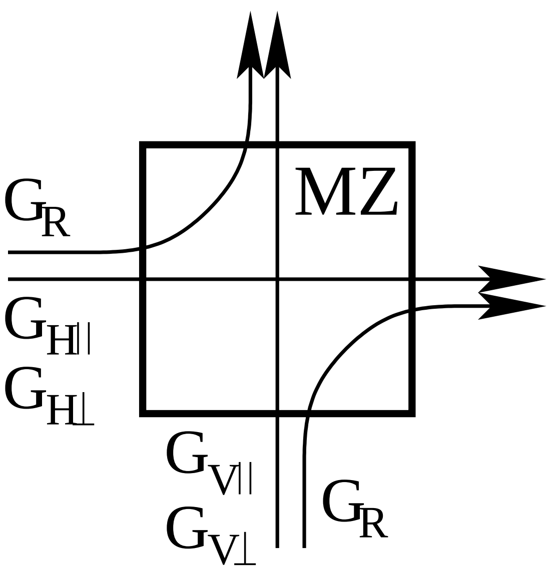
- oscillating conductance coefficients: $L_{so} = \pi / k_{so}$



$$
\begin{aligned}
G_{\mathrm{R}} &= \frac{1}{8}\left[1-\cos\left(\frac{2\pi w}{L_{so}}\right)\right]\left[1-\cos\left(\frac{2\pi h}{L_{so}}\right)\right], \\
G_{\mathrm{V}\|} &= \frac{1}{2}\left[1+\cos\left(\frac{2\pi w}{L_{so}}\right)\right], \\
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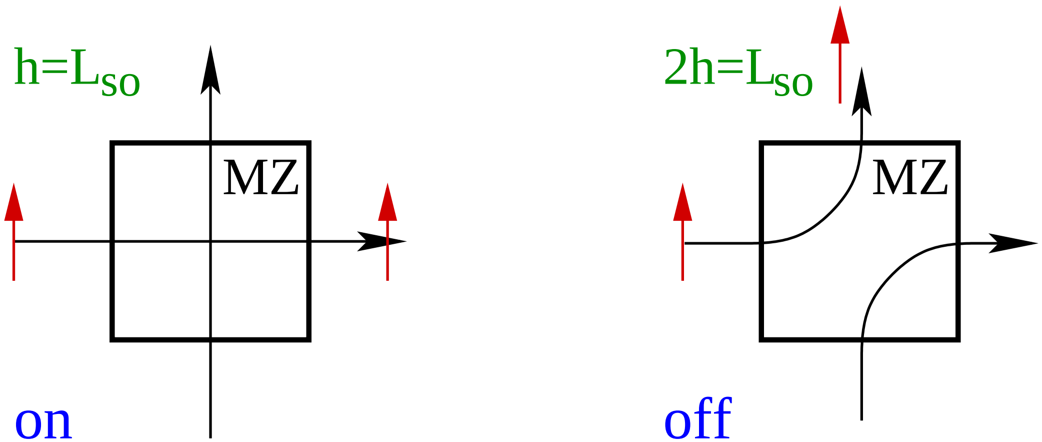
\end{aligned}
$$

Applications: Single–input manipulation

UZ, Appl. Phys. Lett. **85**, 2616 (2004)

- spin transistor (switch) without magnets: when $w = h$



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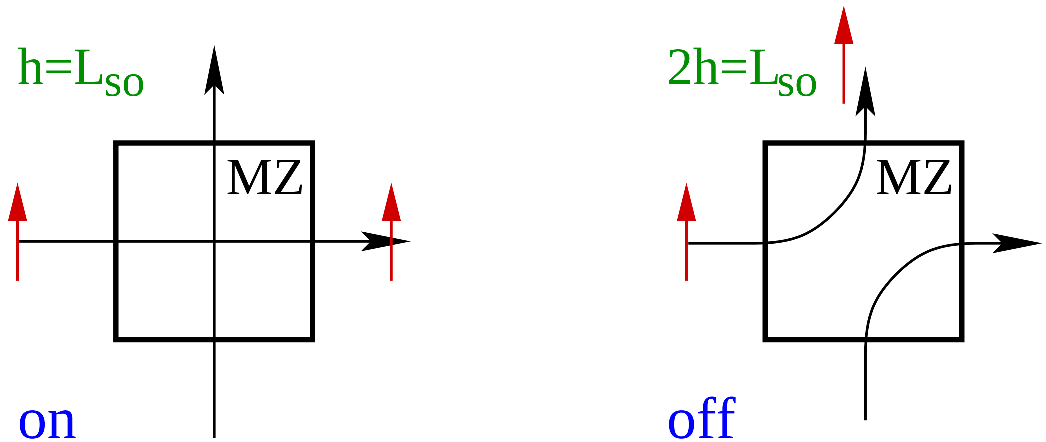
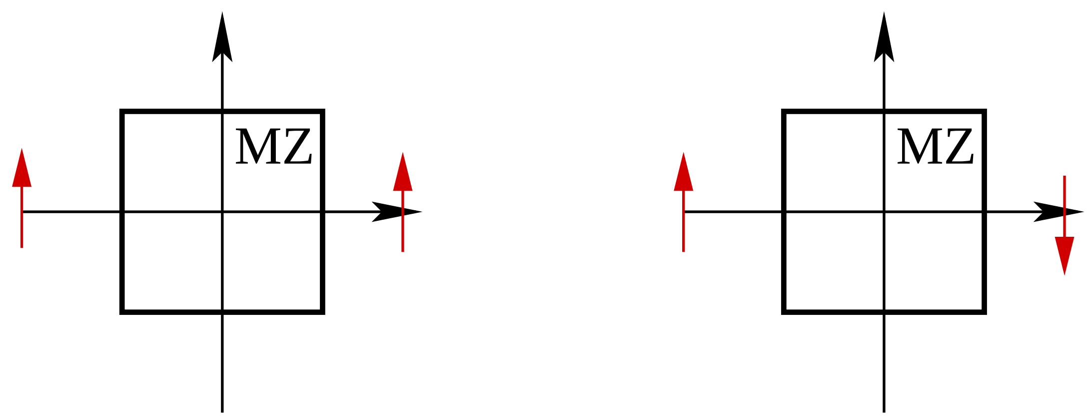


- single–qubit rotations (quantum negator when $h = w/2$)



Spin–dependent linear electron optics and quantum information processing

Linear optics & QIP

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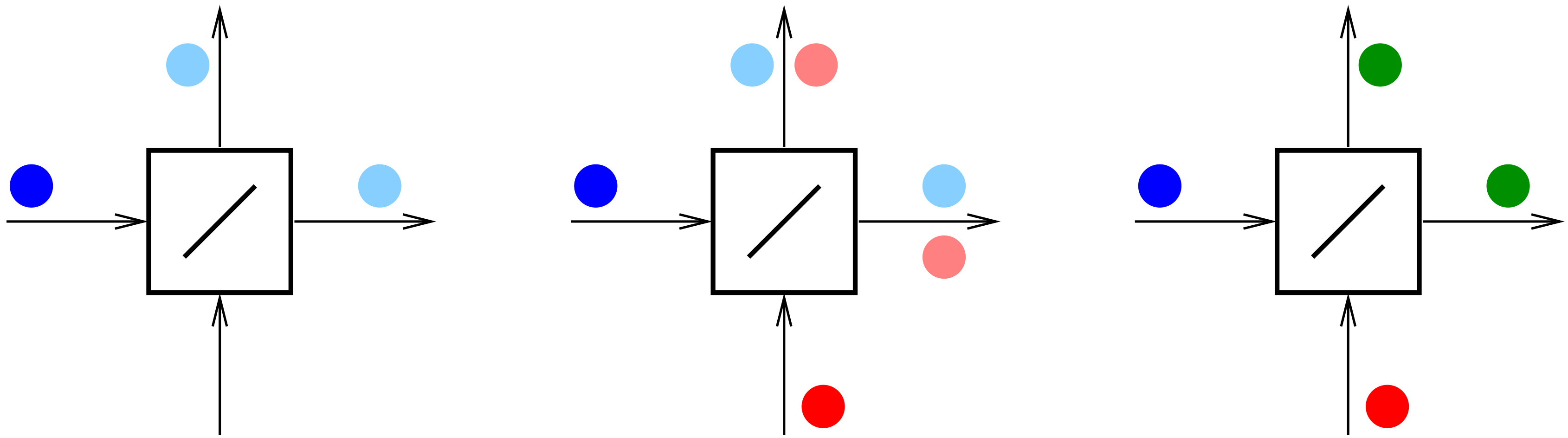
  - charge detection enables quantum computation with linear fermion optics (Beenakker et al., Phys. Rev. Lett. 2004)

Single vs. two–electron input

- Fermi statistics affects scattering, e.g., at beam splitters

(Loudon, Phys. Rev. A 1998)



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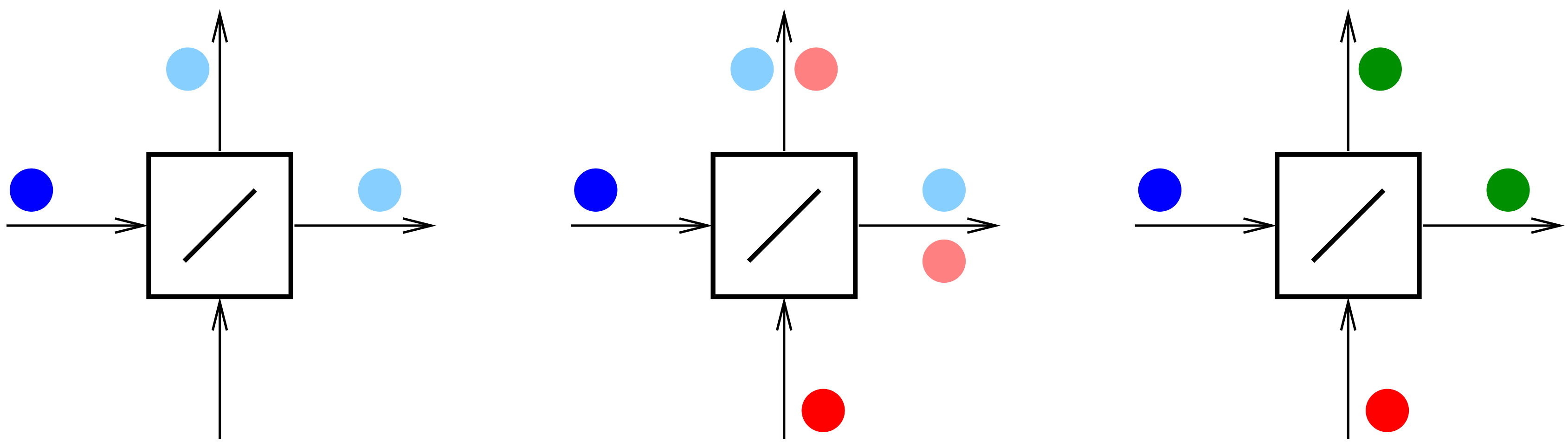
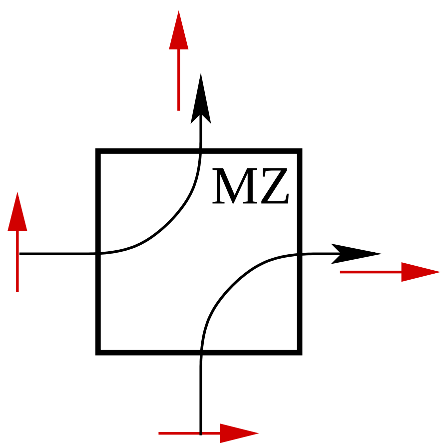


- at Mach–Zehnder interferometer: several scenarios



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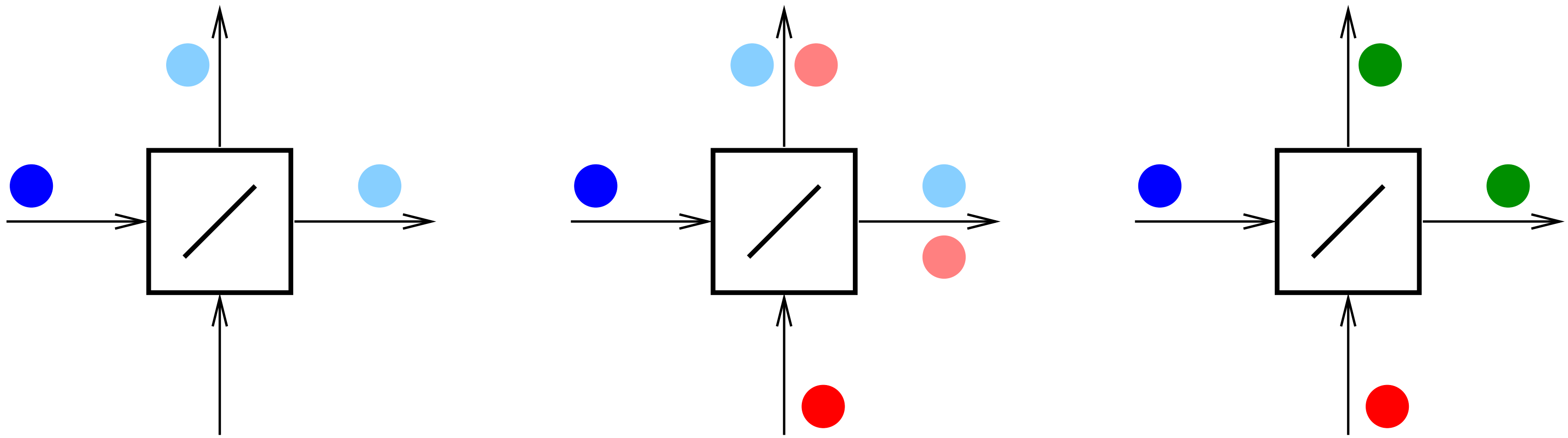

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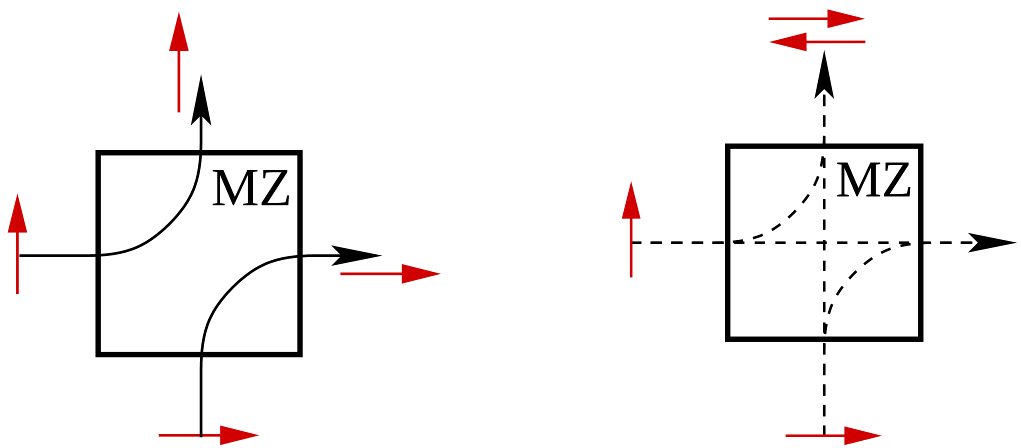

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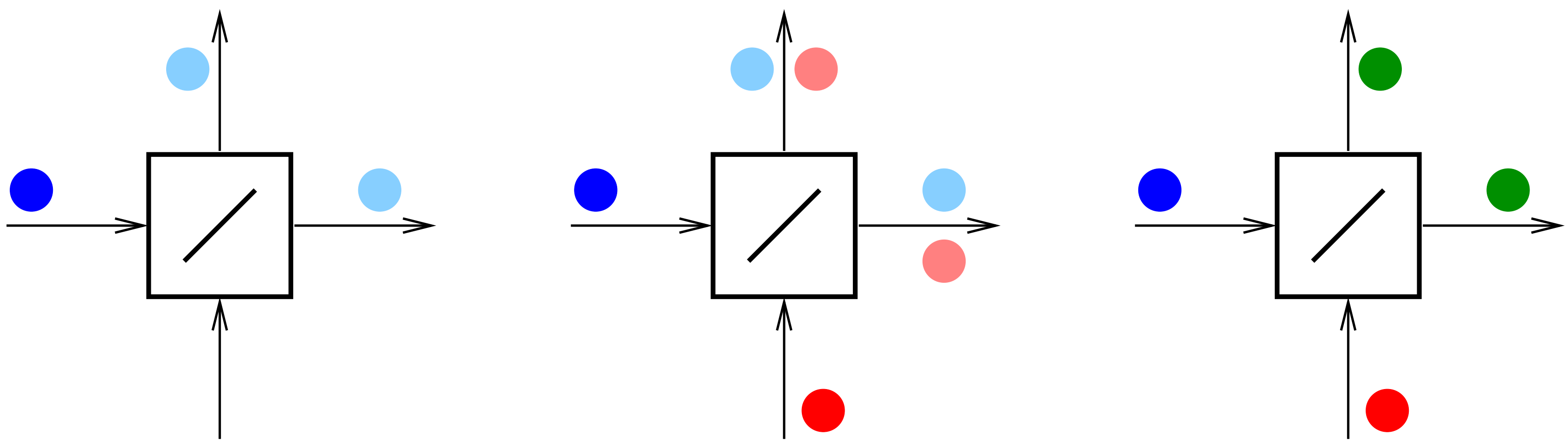

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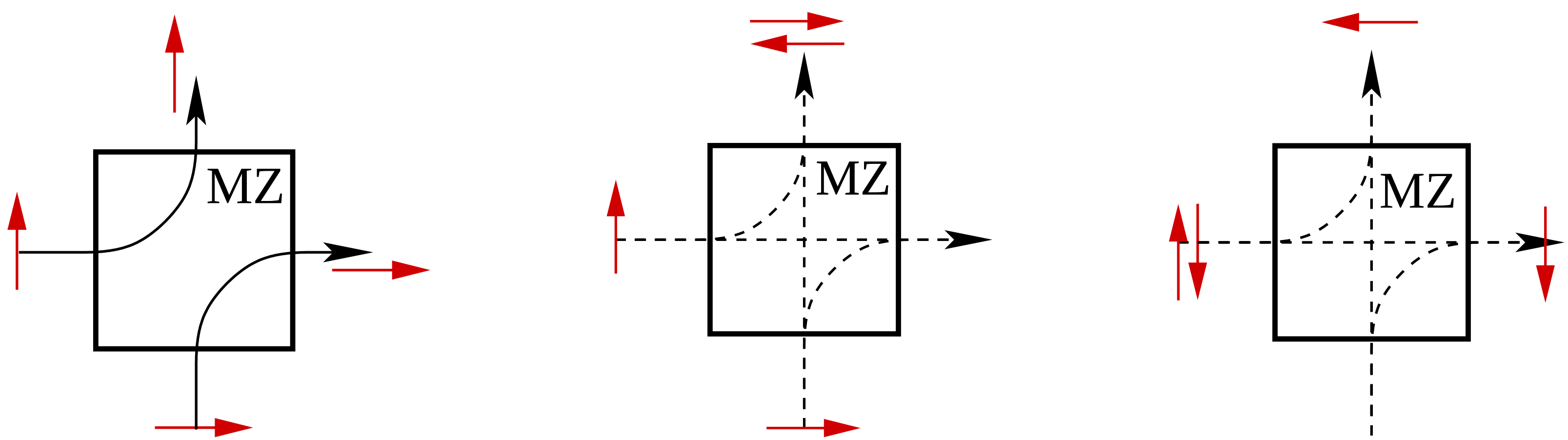

Theoretical description

- 4D single–electron space with basis $|\sigma = +, -; \alpha = \mathrm{a}, \mathrm{b}\rangle$
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- use magic basis of Bell states (Eckert et al., Ann. Phys. 2002)

$$\chi_1 = \frac{1}{\sqrt{2}}\left(c^\dagger_{\mathrm{a}+}c^\dagger_{\mathrm{a}-} + c^\dagger_{\mathrm{b}+}c^\dagger_{\mathrm{b}-}\right) \qquad \chi_2 = \frac{1}{\sqrt{2}}\left(c^\dagger_{\mathrm{a}+}c^\dagger_{\mathrm{b}+} - c^\dagger_{\mathrm{a}-}c^\dagger_{\mathrm{b}-}\right)$$

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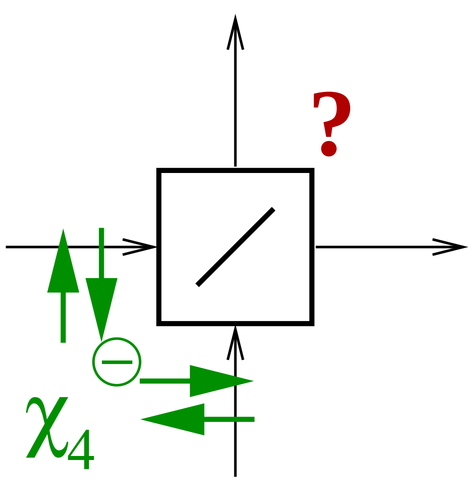
Theoretical description cont'd

- need the two–electron–state scattering matrix for each linear electron–optics element (e.g., beam splitter)



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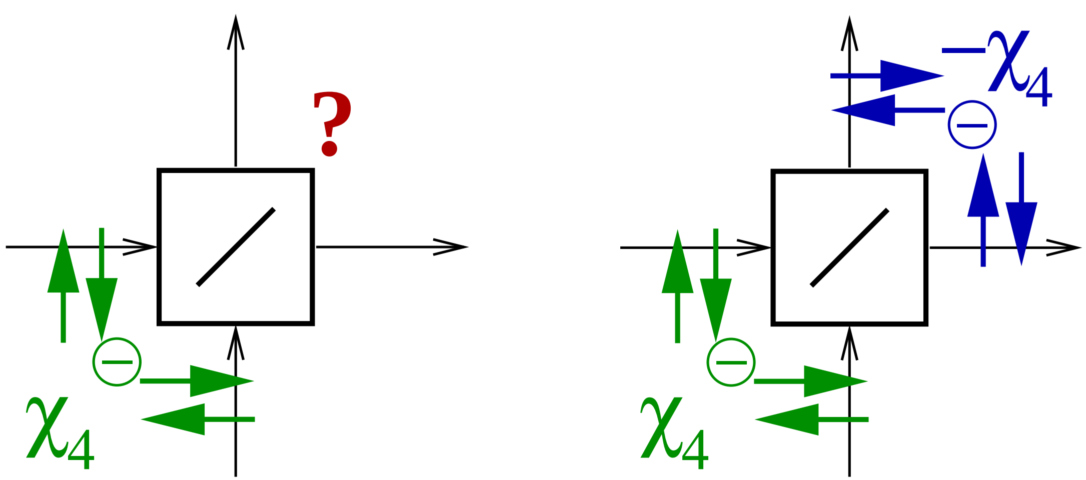

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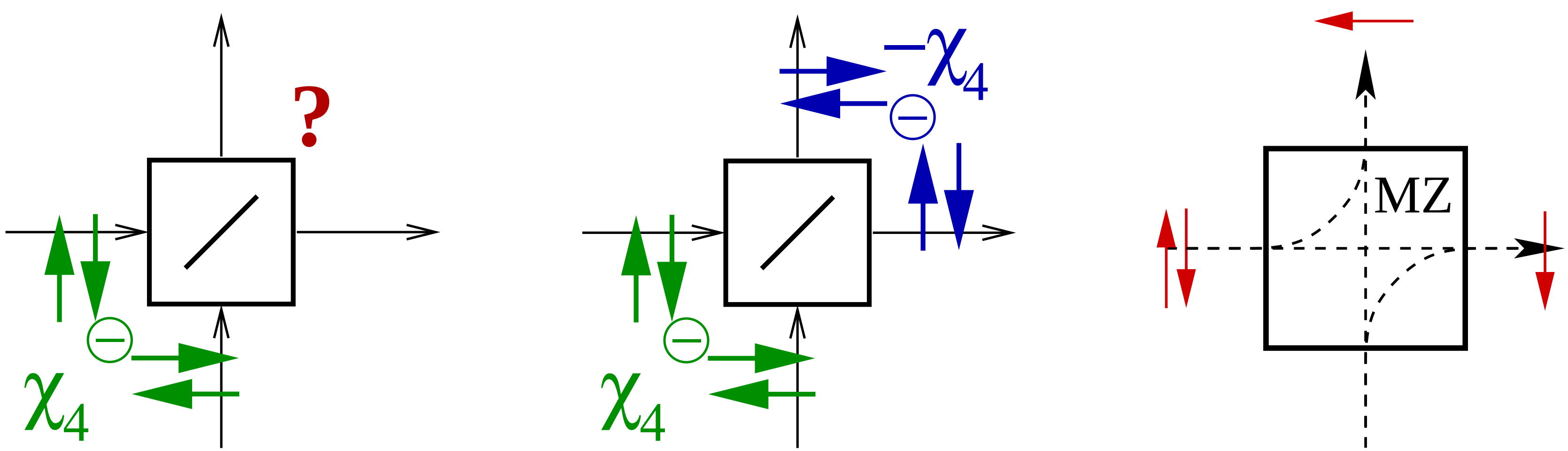
- find two–particle scattering matrix analytically for entire interferometer: oscillatory in size / spin–precession length



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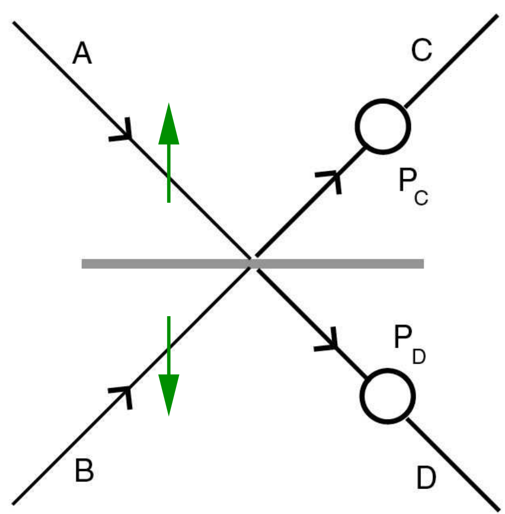

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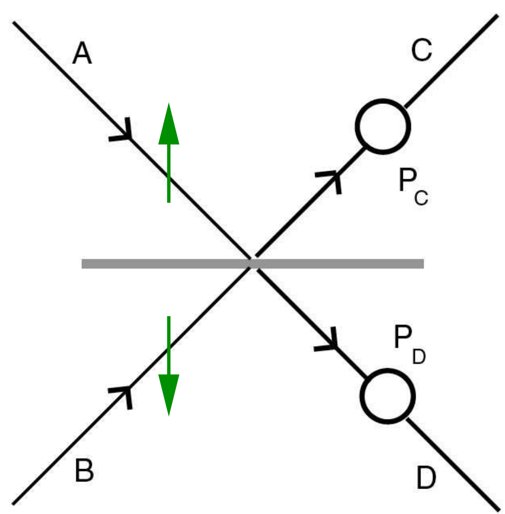

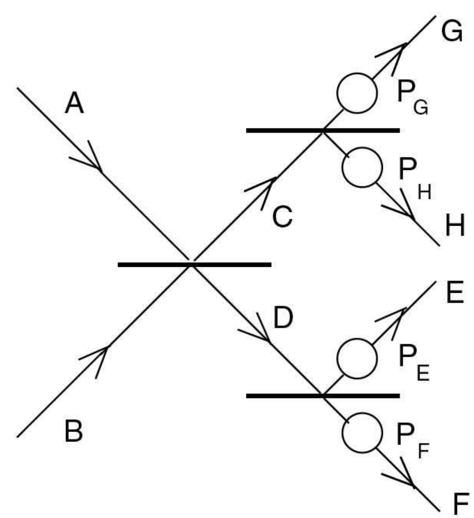

Entanglement generation at a spin MZI

Signal & UZ, Appl. Phys. Lett. **87**, 102102 (2005)

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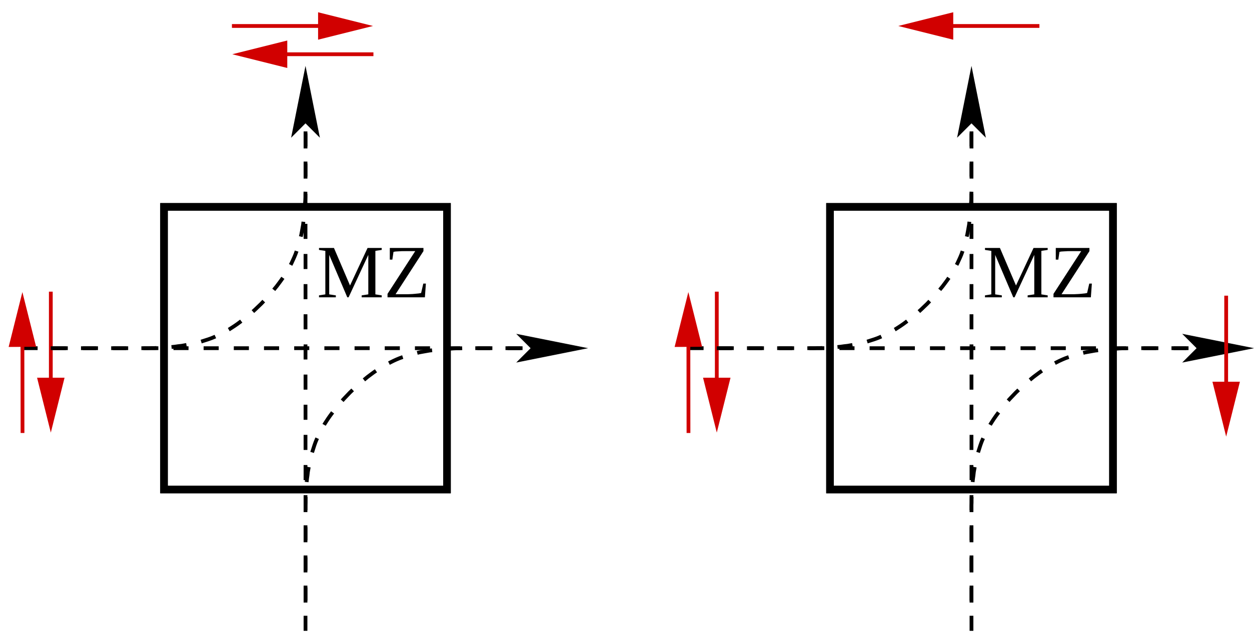

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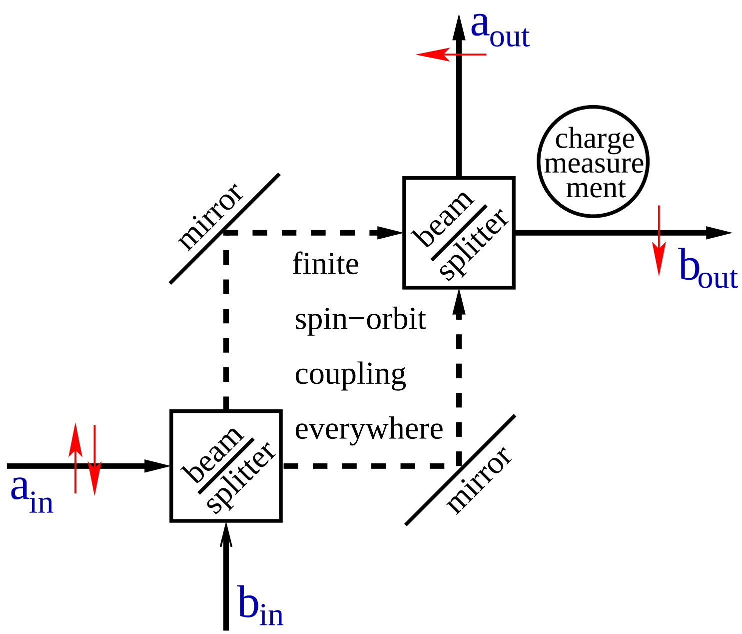

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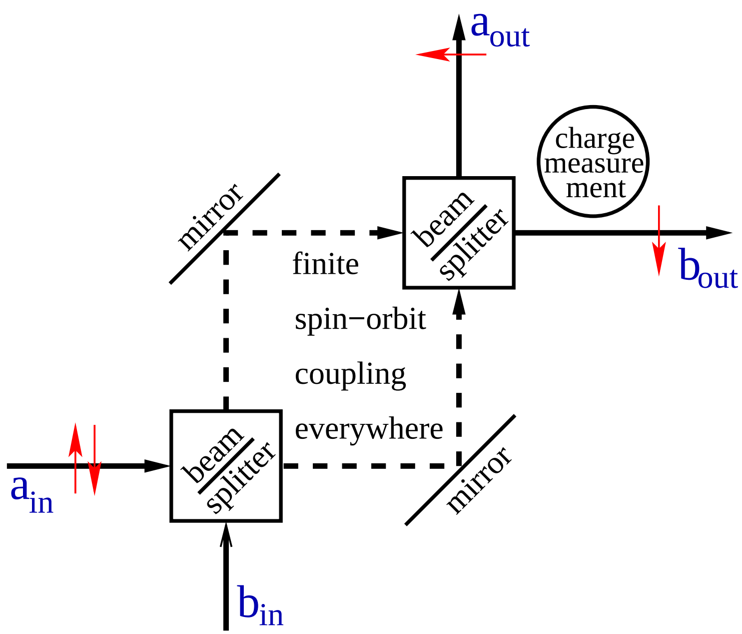

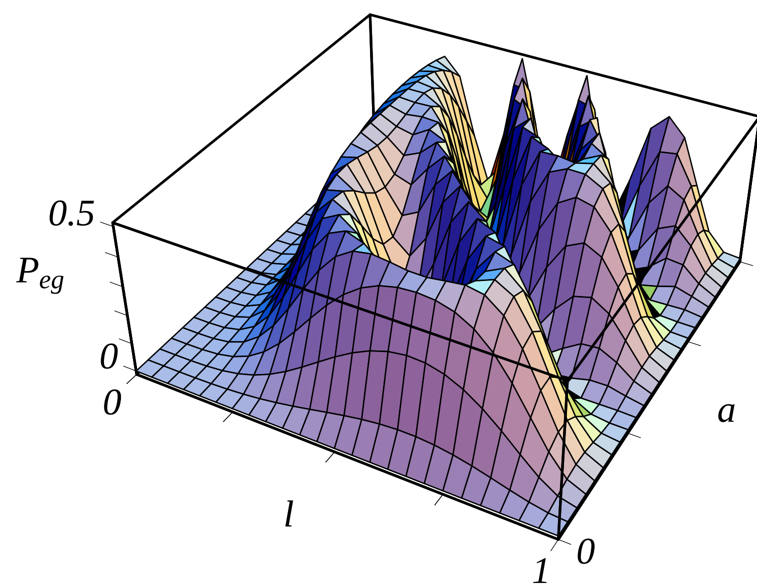

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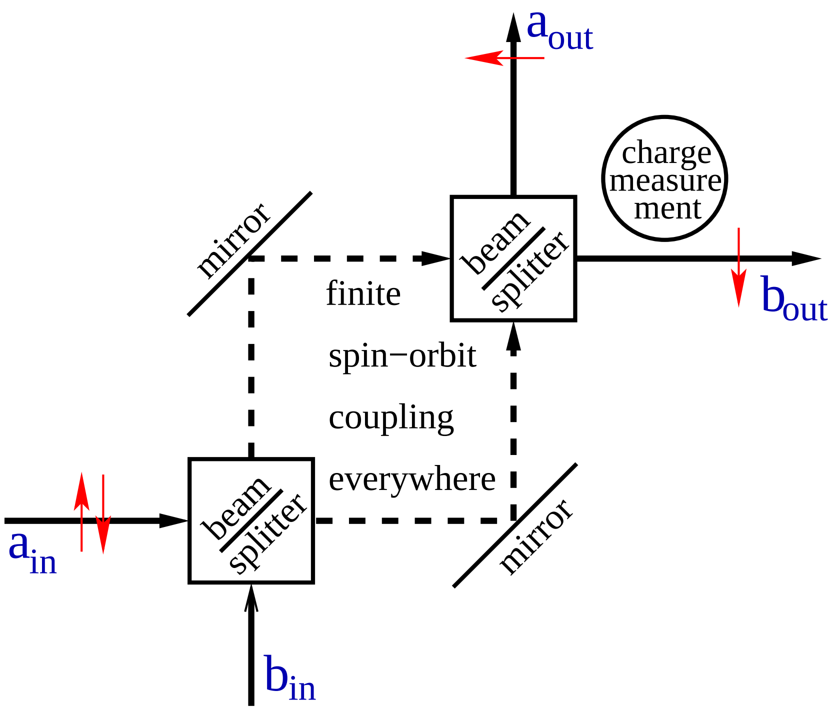

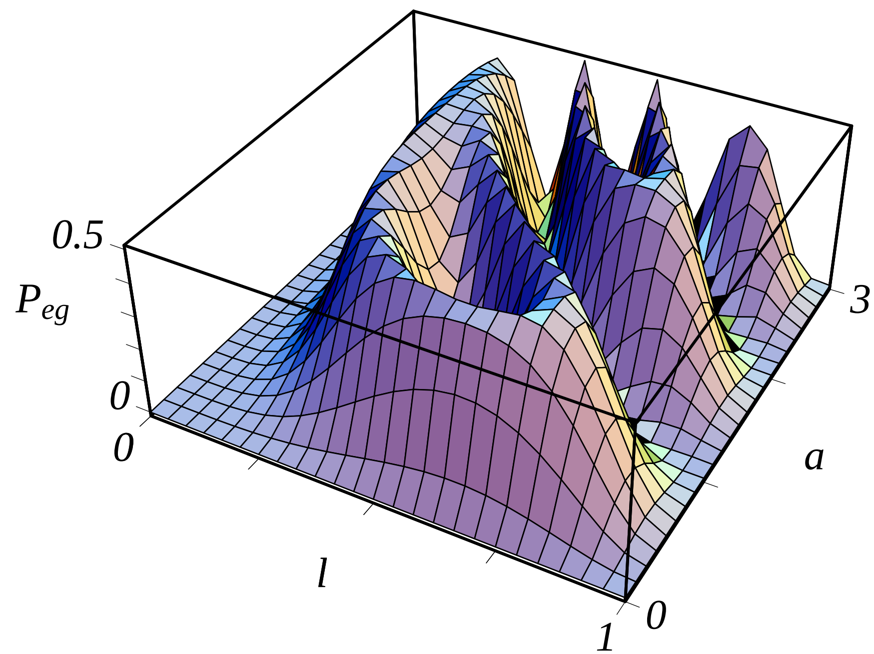

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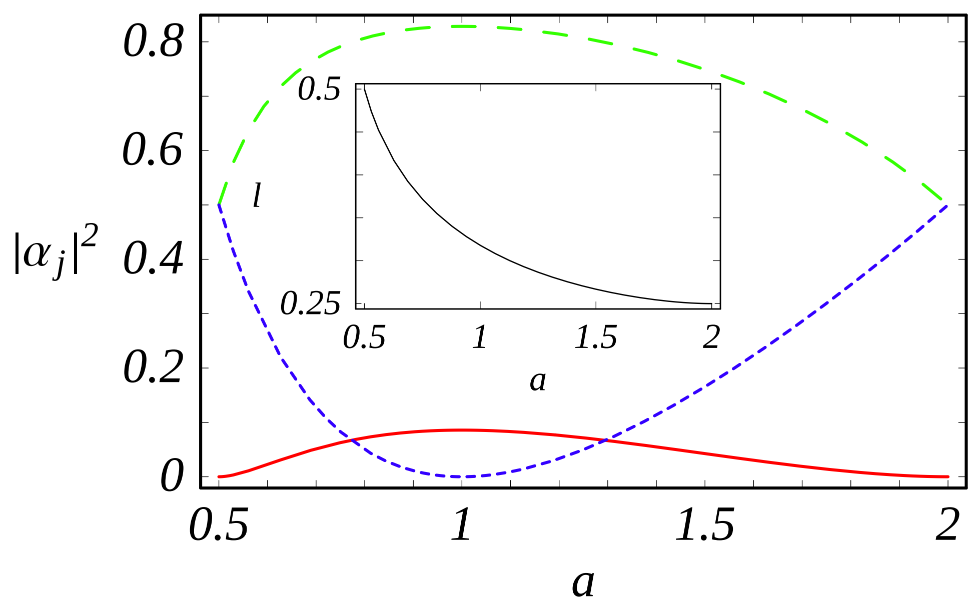

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Conclusions, Outlook & Acknowledgment

- calculated single and two–electron interference at a spin–dependent Mach–Zehnder interferometer
- single–electron–input applications: magnet–less spin switch and quantum gates for mobile–electron spin qubit
- interferometer can act as entangler: 50% max. efficiency + electric-field control of entanglement generation!!
- in progress: classify possible two-qubit gates realised by spin–MZI (Bremner et al., Phys. Rev. Lett. ’02; Makhlin, Quant. Inf. Proc. ’03)

Collaboration with:	A. I. Signal	(Massey U)
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	J. König	(Ruhr–U Bochum)
	Y. Tokura	(NTT Labs)
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