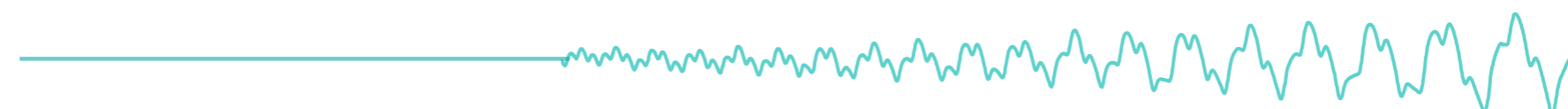


# Fermi surface topology and chirality in Weyl semimetals

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resistivity



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Yan Sun

Band structure

Magnetization

Michael Baenitz

Marcus Schmidt

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Dmitry Sokolov

Michael Nicklas

Claudia Felser

Max-Planck Institute for  
Chemical Physics

Samples +  
orientation

# Outline

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- Fermi surface of TaP
- Negative longitudinal magnetoresistance
- Fermi surface of TaAs, chirality and Berry phase

# Weyl fermions - relativistic particles

fundamental particles

Massless (= gapless) solution of Dirac equation

$$H = \pm v \vec{\sigma} \cdot \vec{k}$$

Chirality

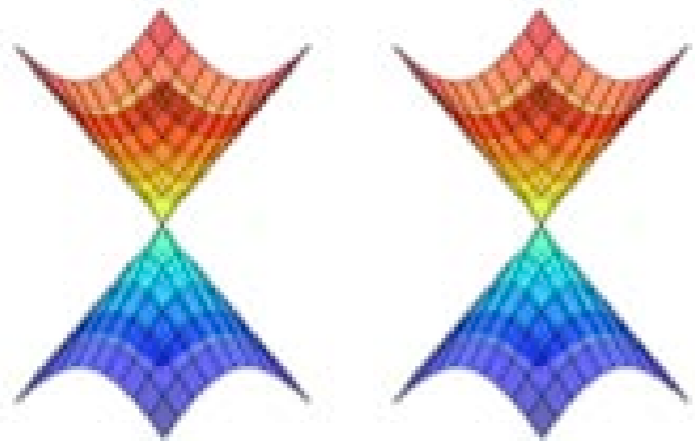
Linear dispersion



Hermann Weyl  
1929

# Dirac versus Weyl semimetals

Linear dispersion  
from band crossing



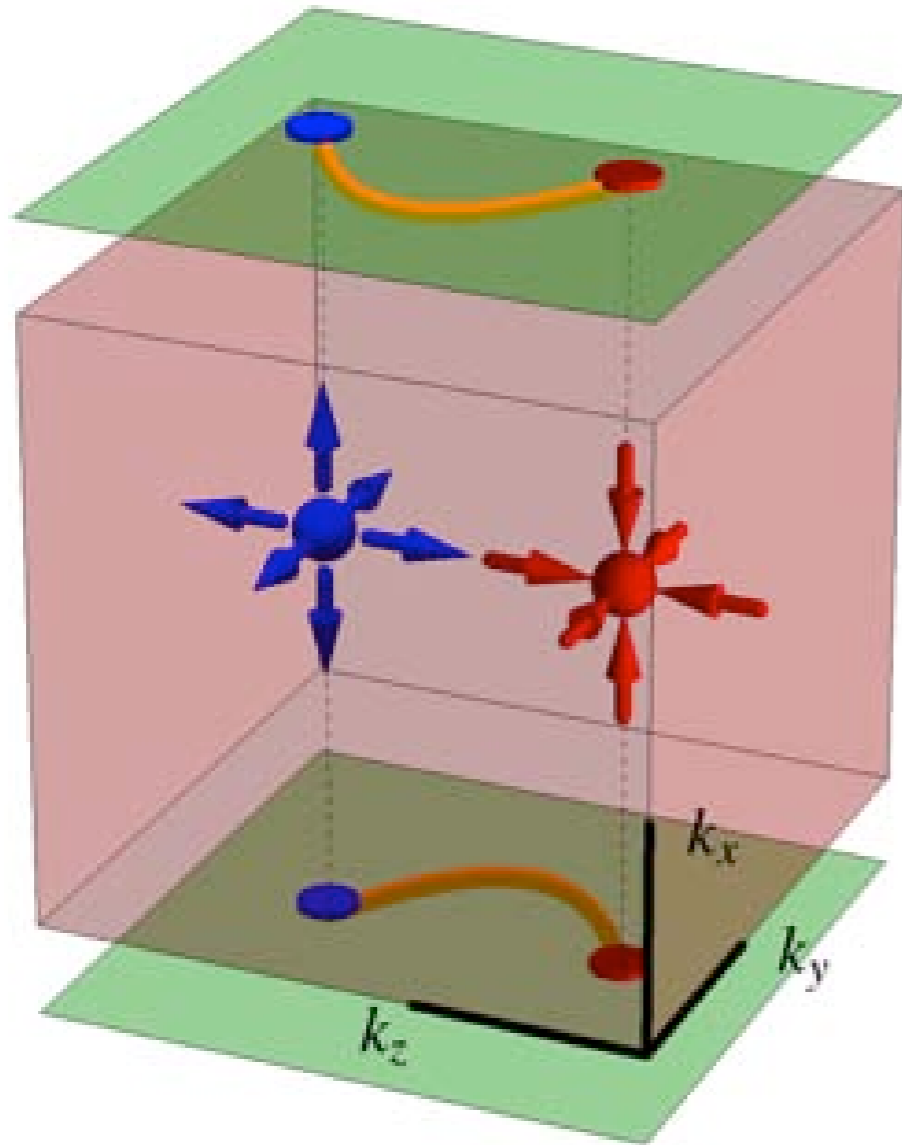
Dirac cone  
in 3D

Dirac semimetals:  
Degenerate 3D Dirac  
cones

Weyl semimetals:  
Non-degenerate 3D Dirac  
cone

$$H = \pm v \vec{\sigma} \cdot \vec{k}$$

# Weyl semimetals – spin structure



Chirality from spin structure

Magnetic monopoles in k-space

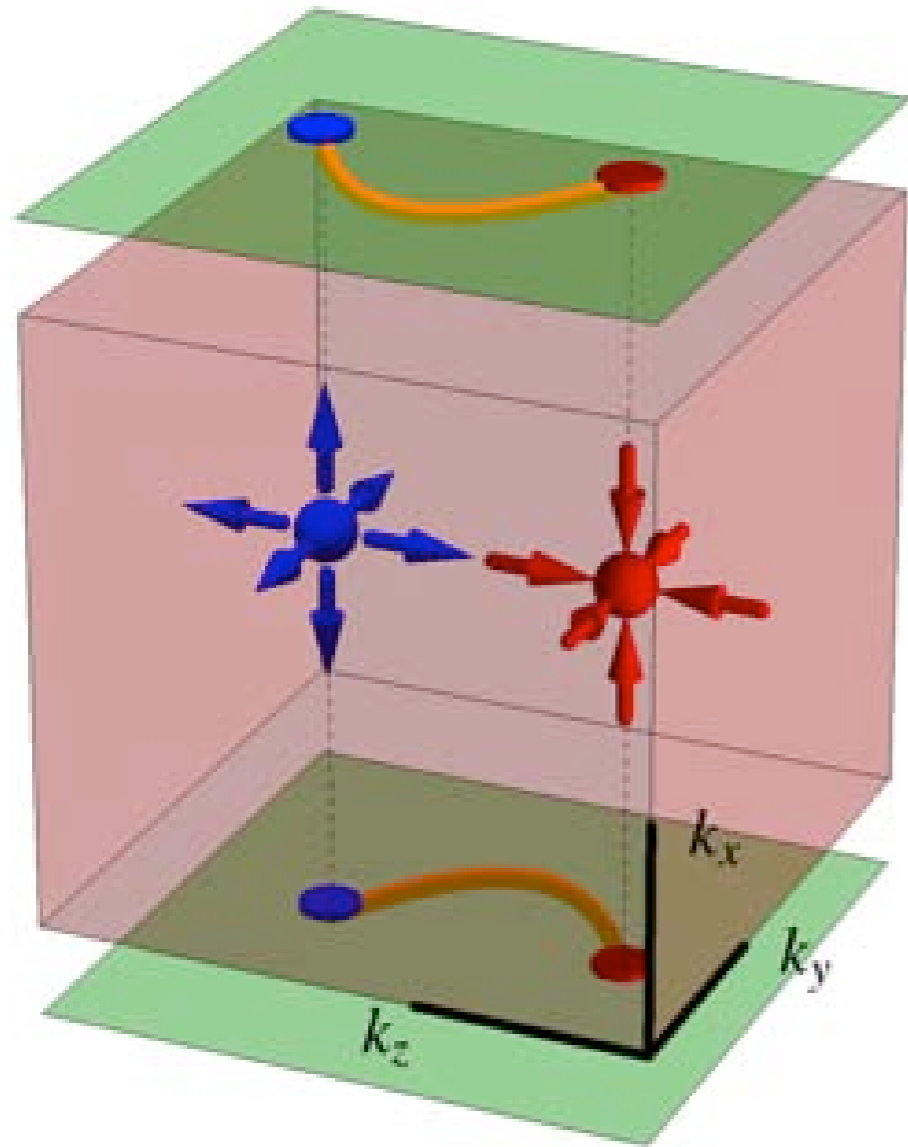
(Source or drain of Berry curvature)

Always come in pairs

Strong spin-orbit coupling required

$$H = \pm v \vec{\sigma} \cdot \vec{k}$$

# Weyl semimetals – experimental signature



Fermi arc surface states

Detected in ARPES

Reference	material
B. Q. Lv et al., PRX (2015)	TaAs
S. Y. Xu et al., Science (2015)	TaAs
L. X. Yang et al., Nat. Phys. (2015)	TaAs
S. Y. Xu et al., Sci. Adv. (2015)	TaP
S. Y. Xu et al., Nat. Phys. (2015)	NbAs
B. Q. Lv et al., Nat. Phys. (2015)	TaAs
D. F. Xu et al., Chin. Phys. Lett. (2015)	NbP
N. Xu et al., Nat Comm. (2016)	TaP
Z. K. Liu et al., Nat. Mat. (2016)	all 4

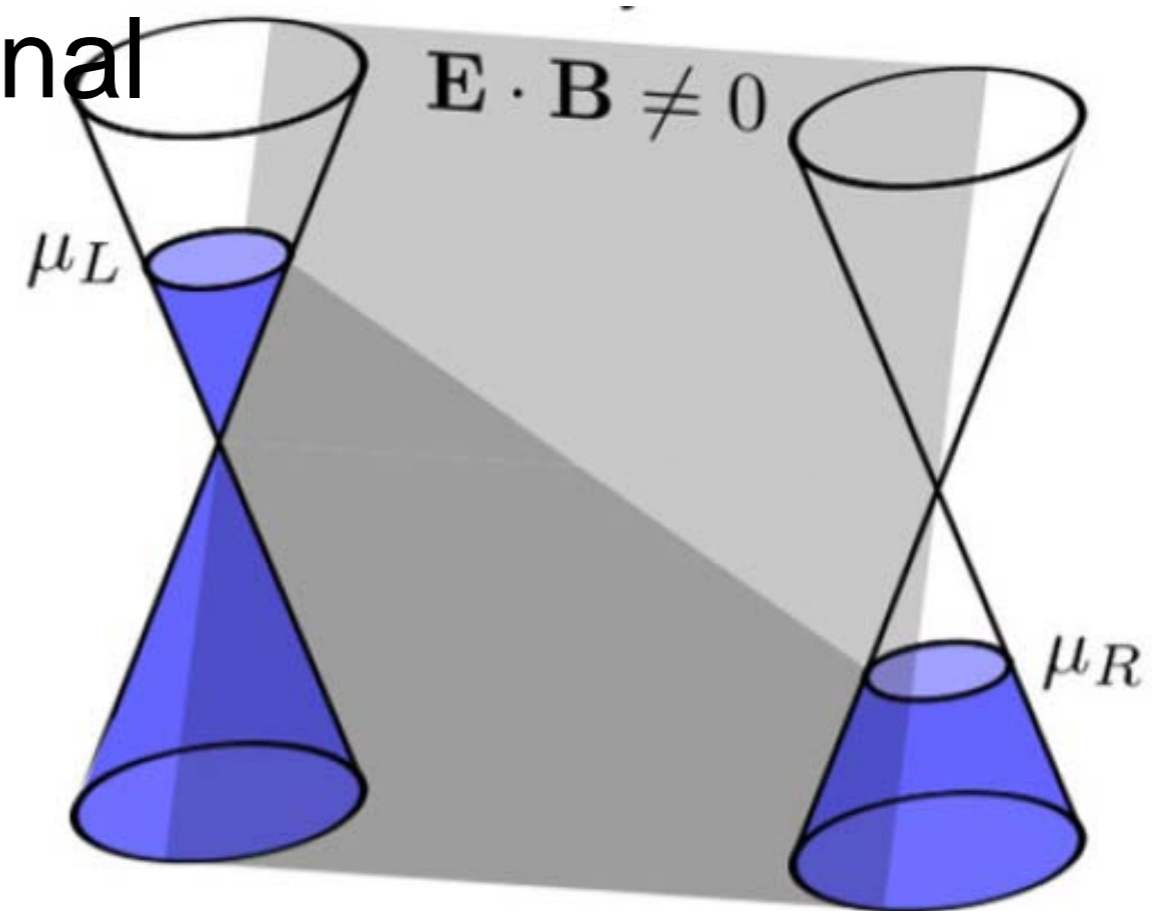
# Weyl semimetals – experimental signature

chiral anomaly

Adler-Bell-Jackiw anomaly

Axial anomaly

Leads to negative longitudinal magnetoresistance



S. Adler, Phys. Rev. 177, 2426 (1969).

J. S. Bell and R. A. Jackiw, Nuovo Cimento A 60, 47 (1969).

H. B. Nielsen and M. Ninomiya, Phys. Lett. B 130, 389 (1983). [negative MR in crystal]

Wan, Turner, Vishwanath, PRB 2011

Burkov, Hook Balents, PRB 2011

Son, Spivak, PRB 2013

Parameswaran et al. PRX 2014

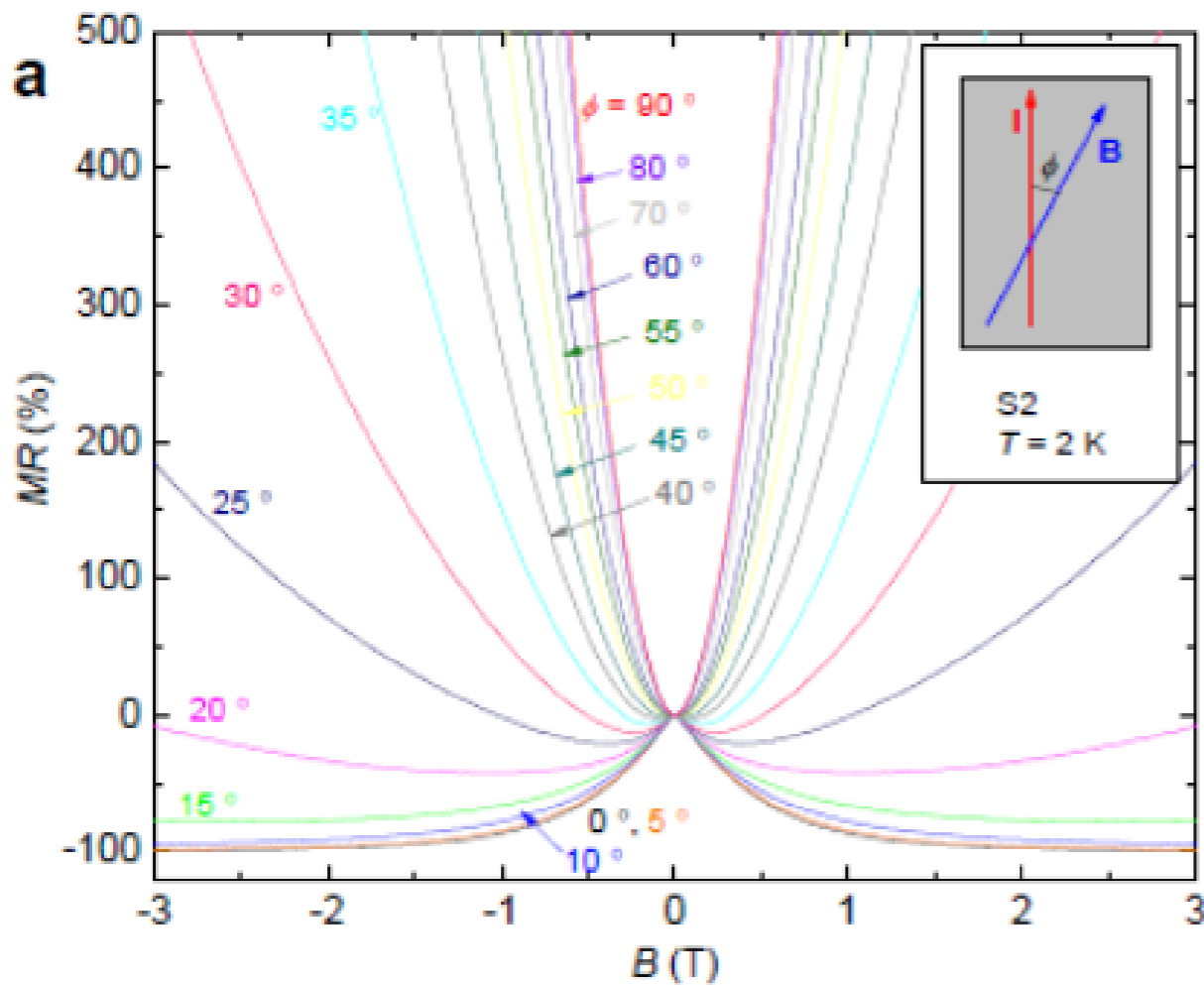
Hosur and Qi, Comp. Rend. Phys. 2013



# Negative longitudinal magnetoresistance

TaAs<sub>2</sub> (not a Weyl semimetal)

$$\sigma_a = \frac{e^3 v_f^3}{4\pi^2 \hbar \mu^2 c} B^2$$



$$MR = (\rho - \rho_0) / \rho_0$$

Luo et al., Scientific Reports (2016)

Reference

X. C. Huang et al., PRX (2015) TaAs

C. L. Zhang et al., Nat. Comm (2015) TaAs

X. J. Yang et al., arxiv (2015)

NbAs

J. H. Du et al., Sci. China-Phys.

(2015) TaP

Z. Wang et al., PRB (2015)

NbP

J. Xiong et al., Science (2015)

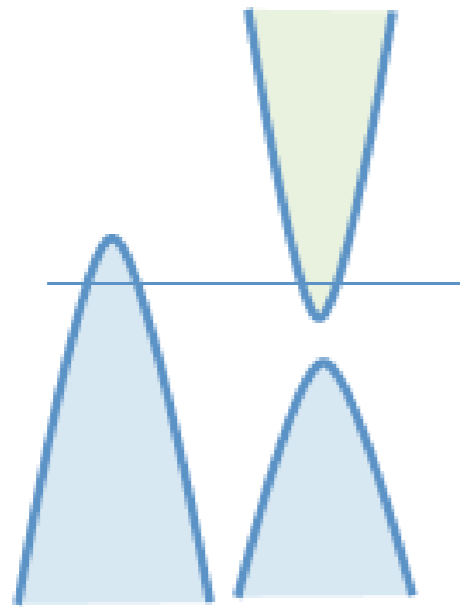
Na<sub>3</sub>Bi

G. L. Zheng et al., PRB (2015)

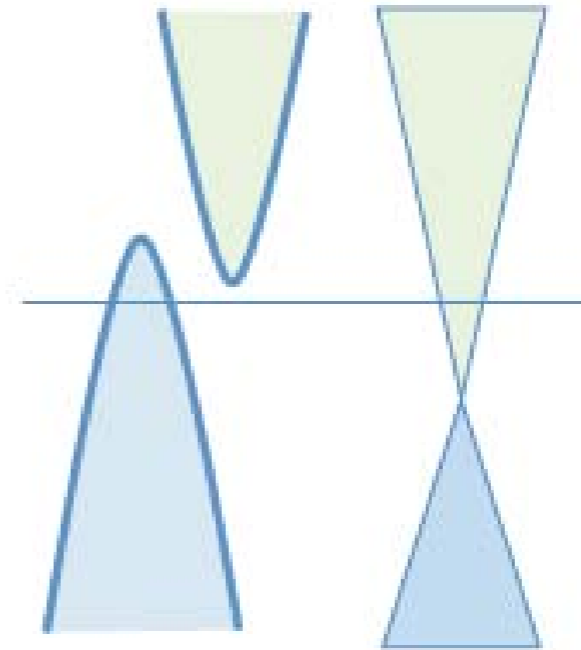
ZrTe<sub>5</sub>

W. Li et al., Nat. Comm (2015) TaAs

# Normal versus Weyl semimetals



Bi, WTe<sub>2</sub>



NbP

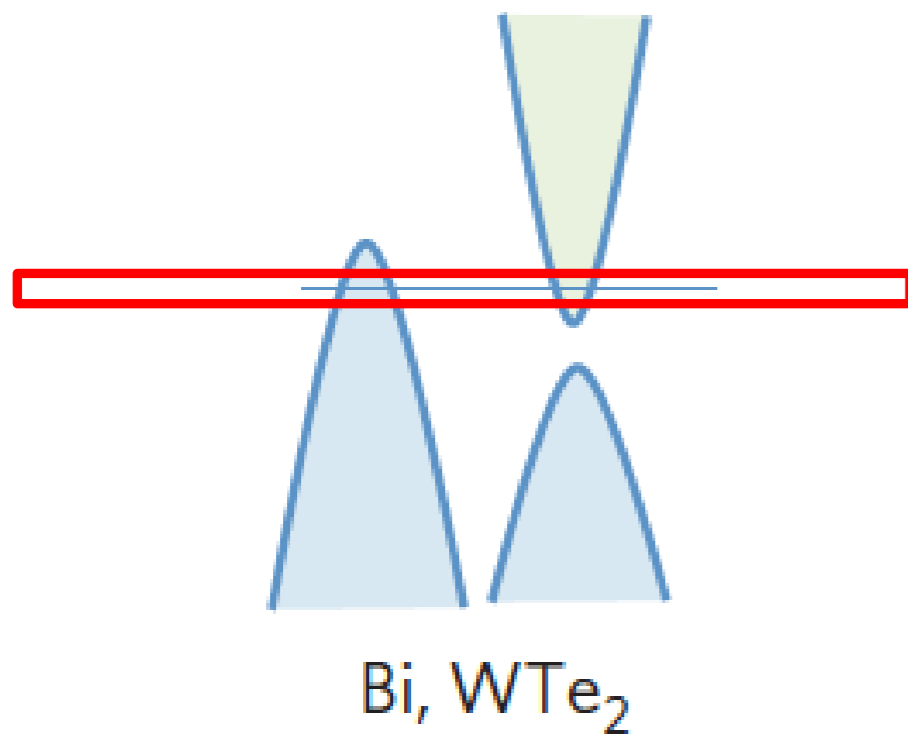
## Normal semimetal

- Low carrier density
- Small effective masses ( $0.01m_0$ )
- High mobility
- Compensated systems

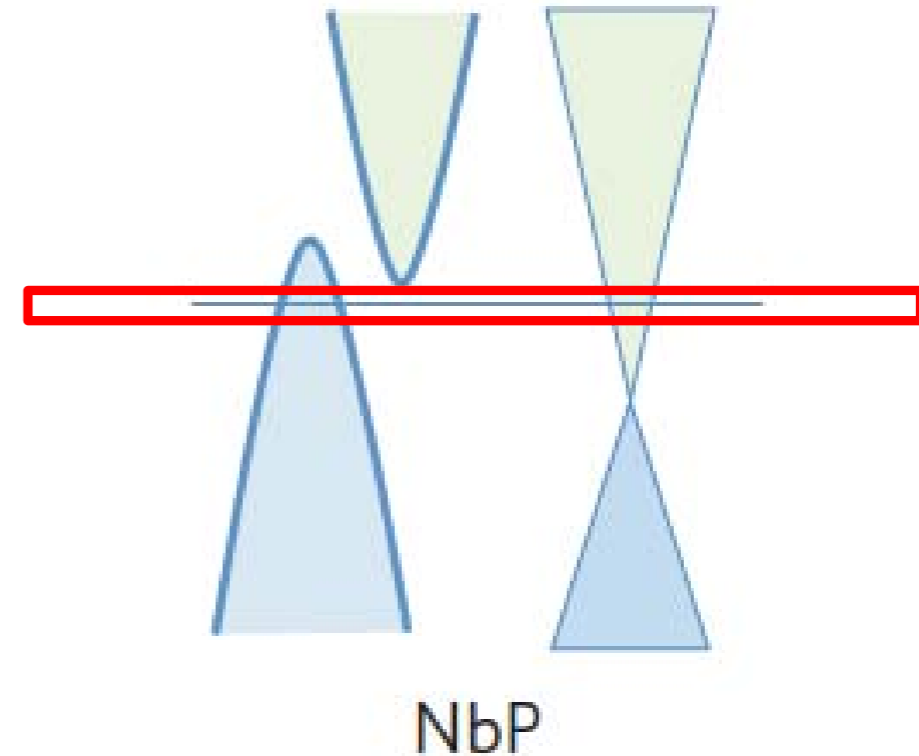
## Weyl semimetal

- Weyl nodes near Fermi energy

# Normal versus Weyl semimetals



Normal semimetal



Weyl semimetal

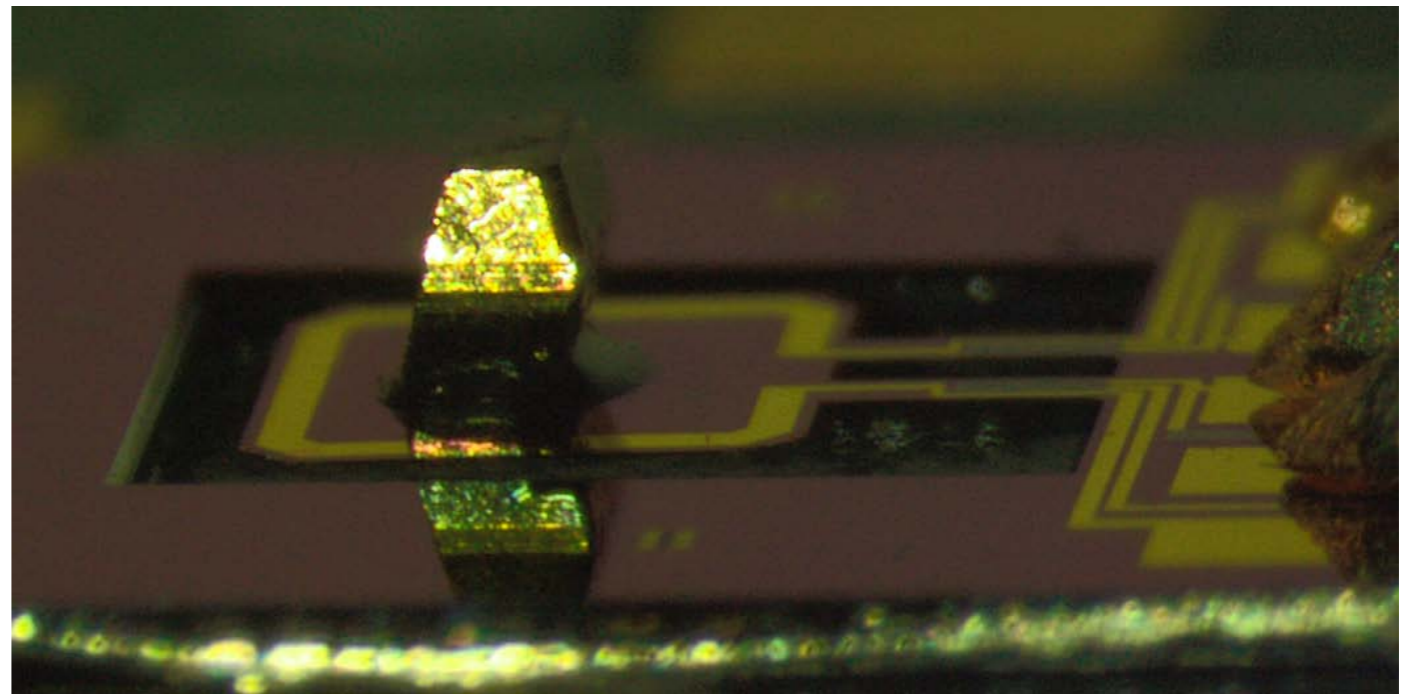
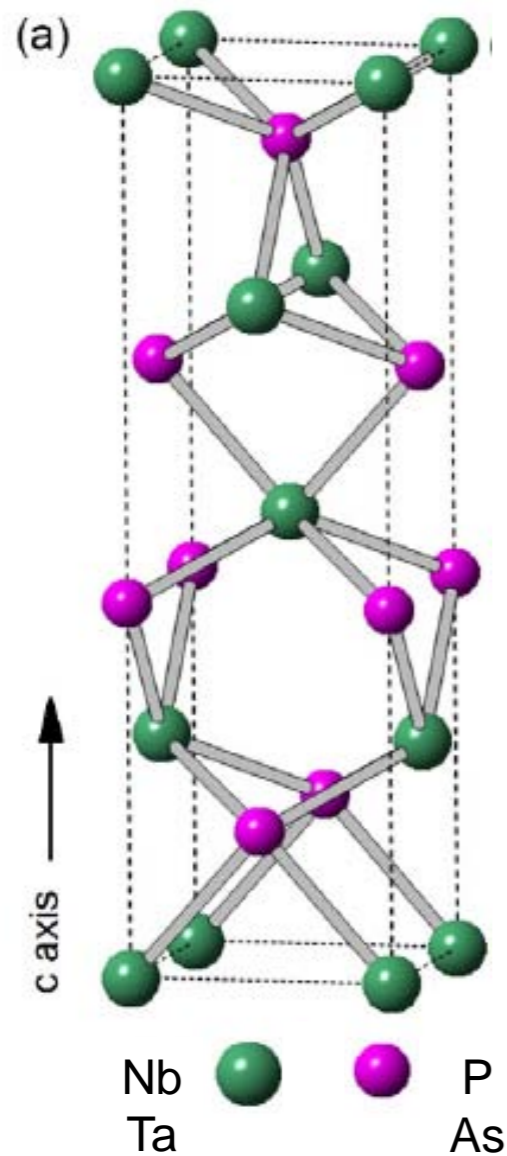
How far are Weyl nodes from  $E_F$ ?

Do we expect to see experimental bulk signatures of them?

# NbP, NbAs, TaP, TaAs

## Predicted topological Weyl semimetals

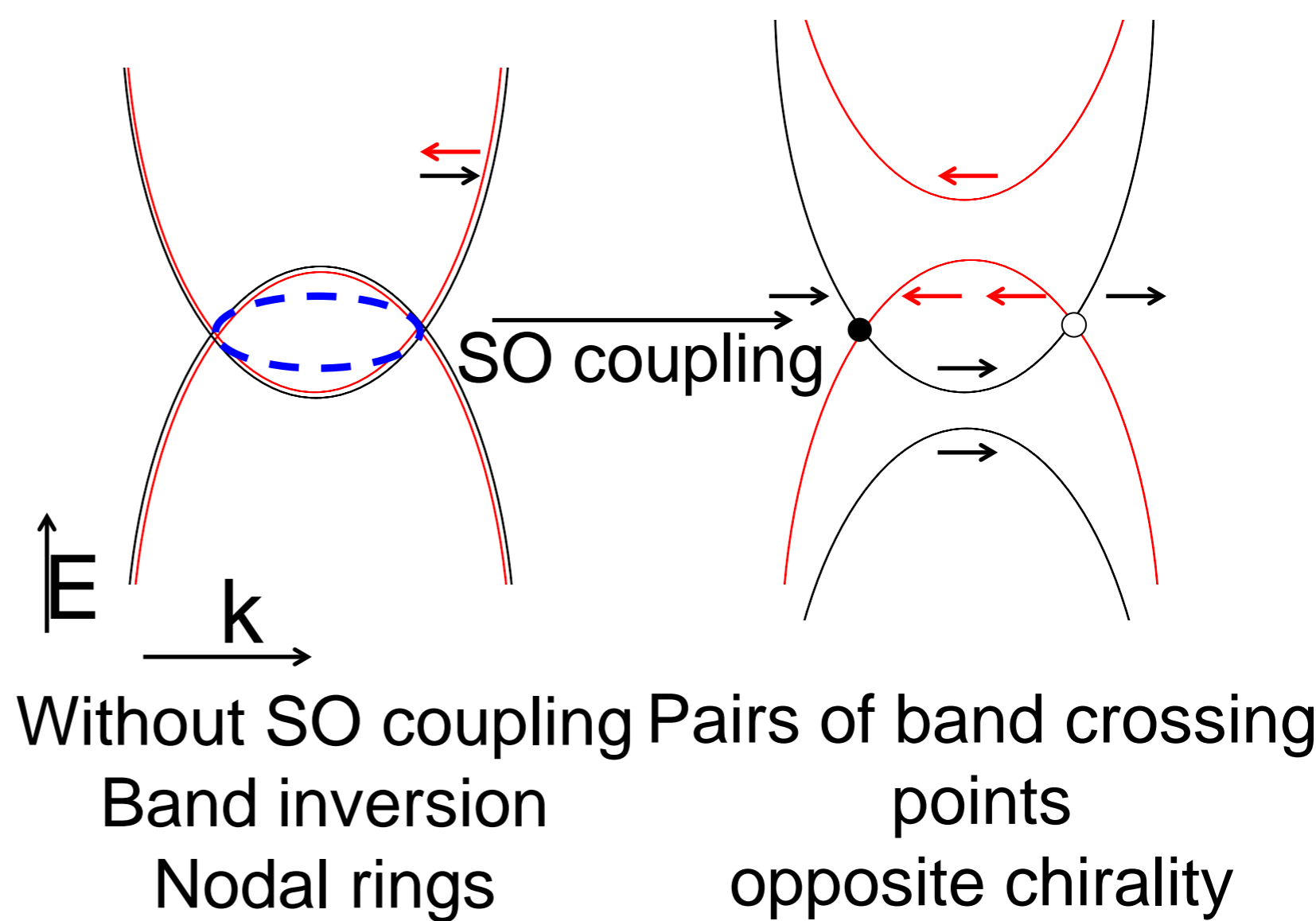
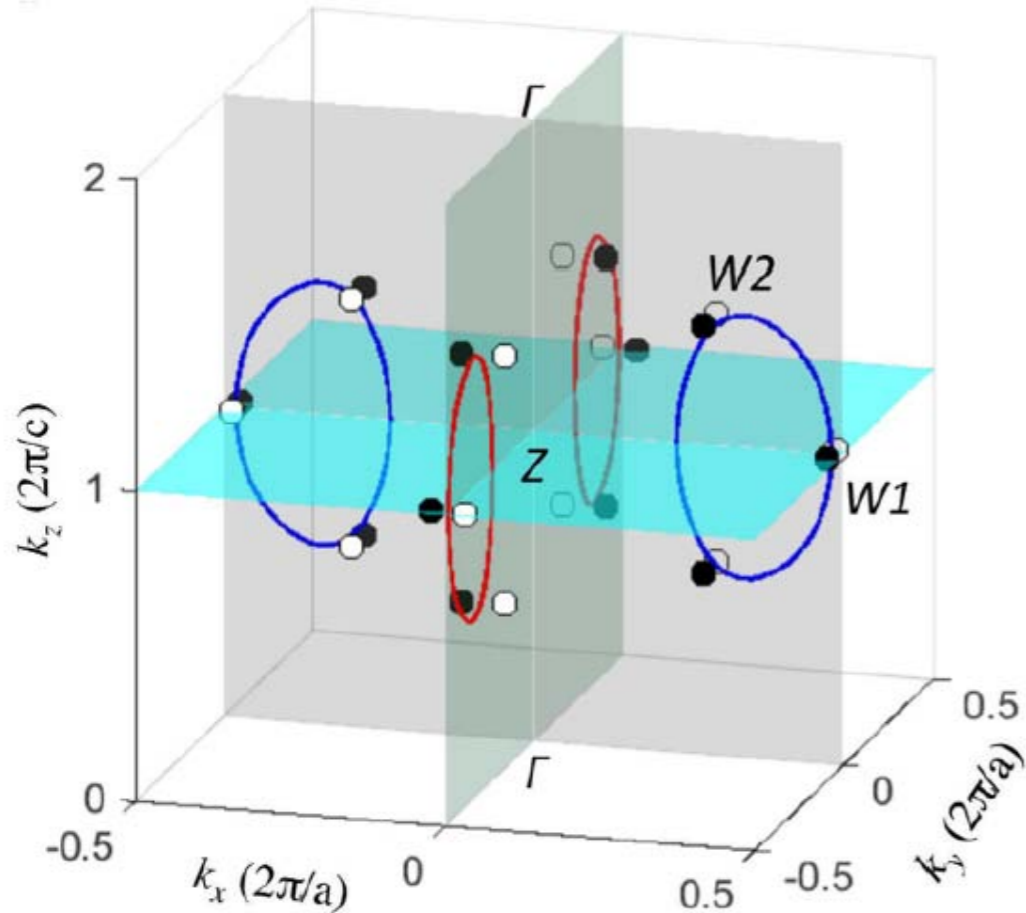
Tetragonal without inversion symmetry



$I4_1md$

# Chiral massless fermions in TaAs semime

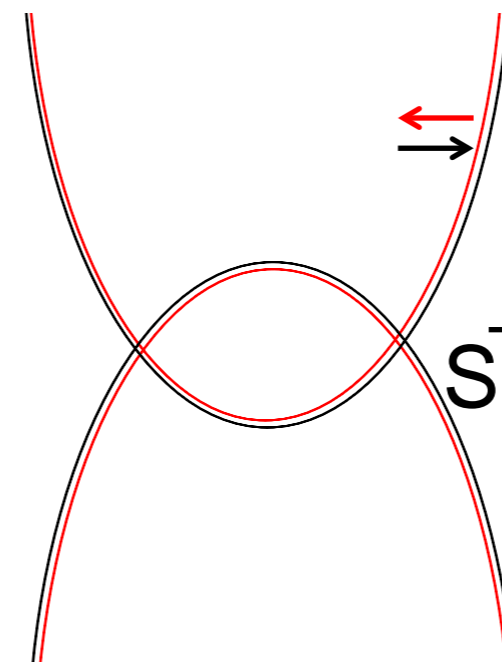
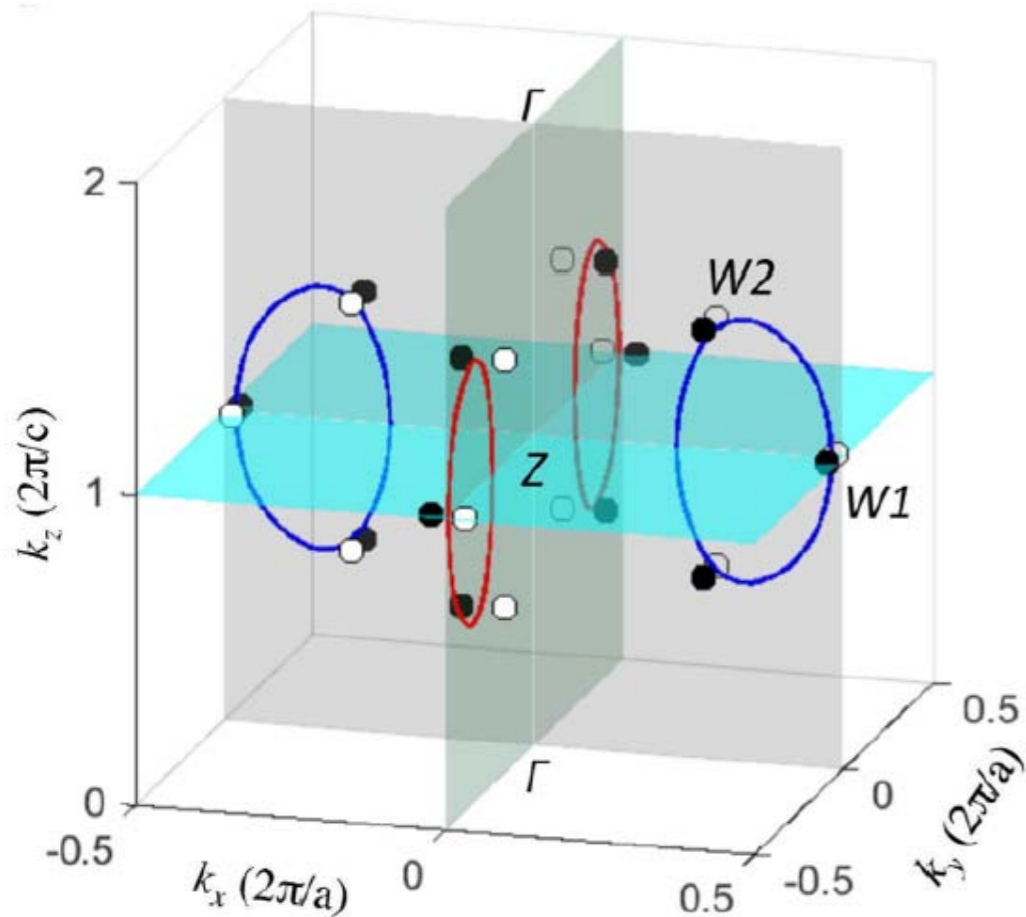
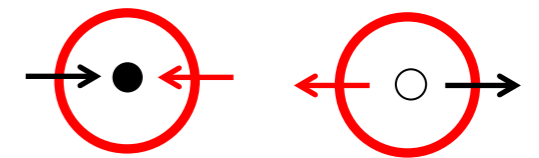
Strong spin-orbit coupling,  
broken inversion symmetry



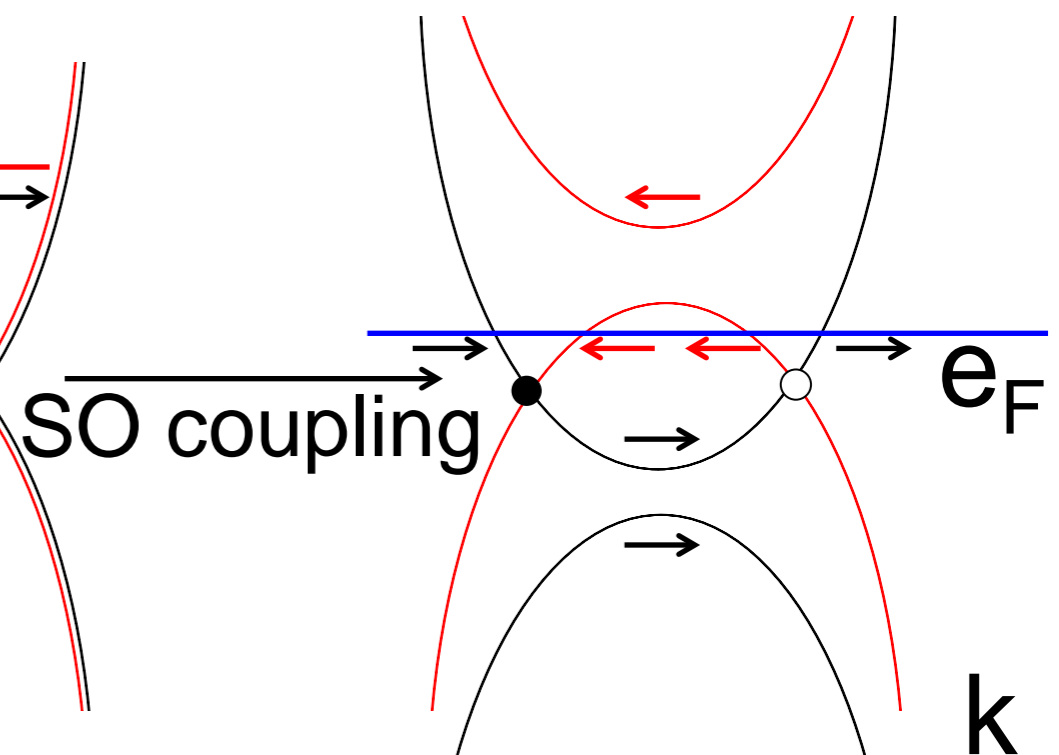
# Chiral massless fermions in TaAs semime

Strong spin-orbit coupling,  
broken inversion symmetry

Fermi surface



Without SO coupling  
Band inversion  
Nodal rings



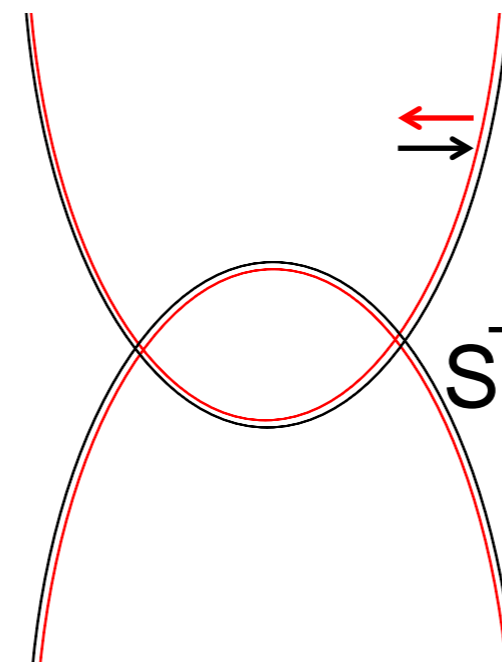
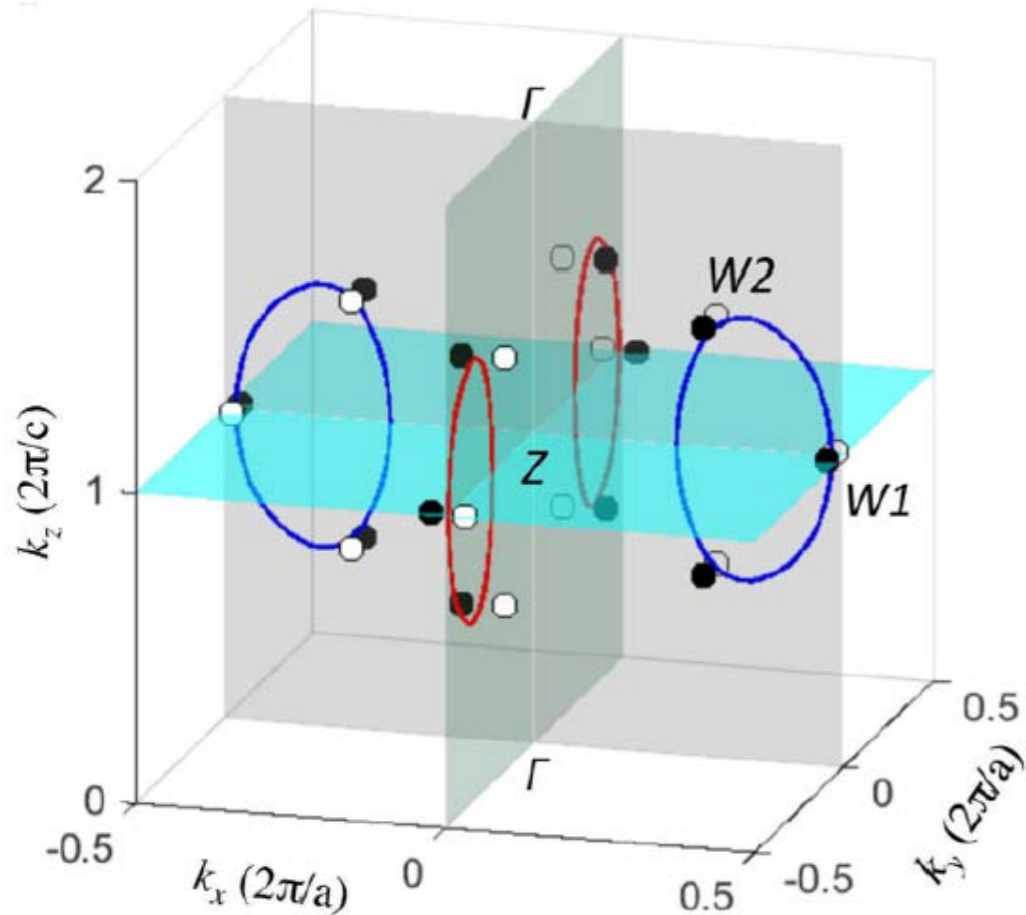
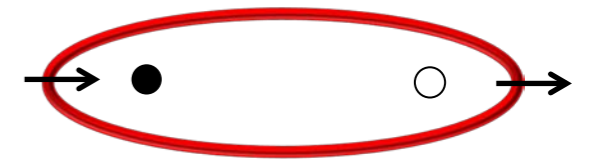
Well-defined  
chirality



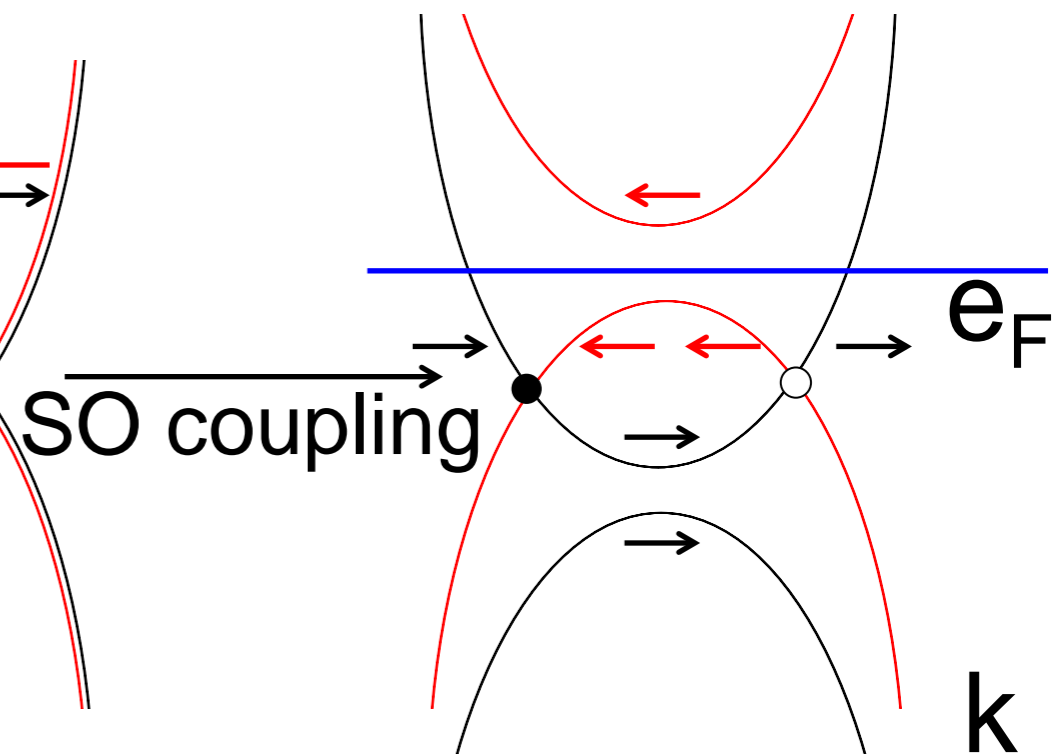
# Chiral massless fermions in TaAs semime

Strong spin-orbit coupling,  
broken inversion symmetry

Fermi surface



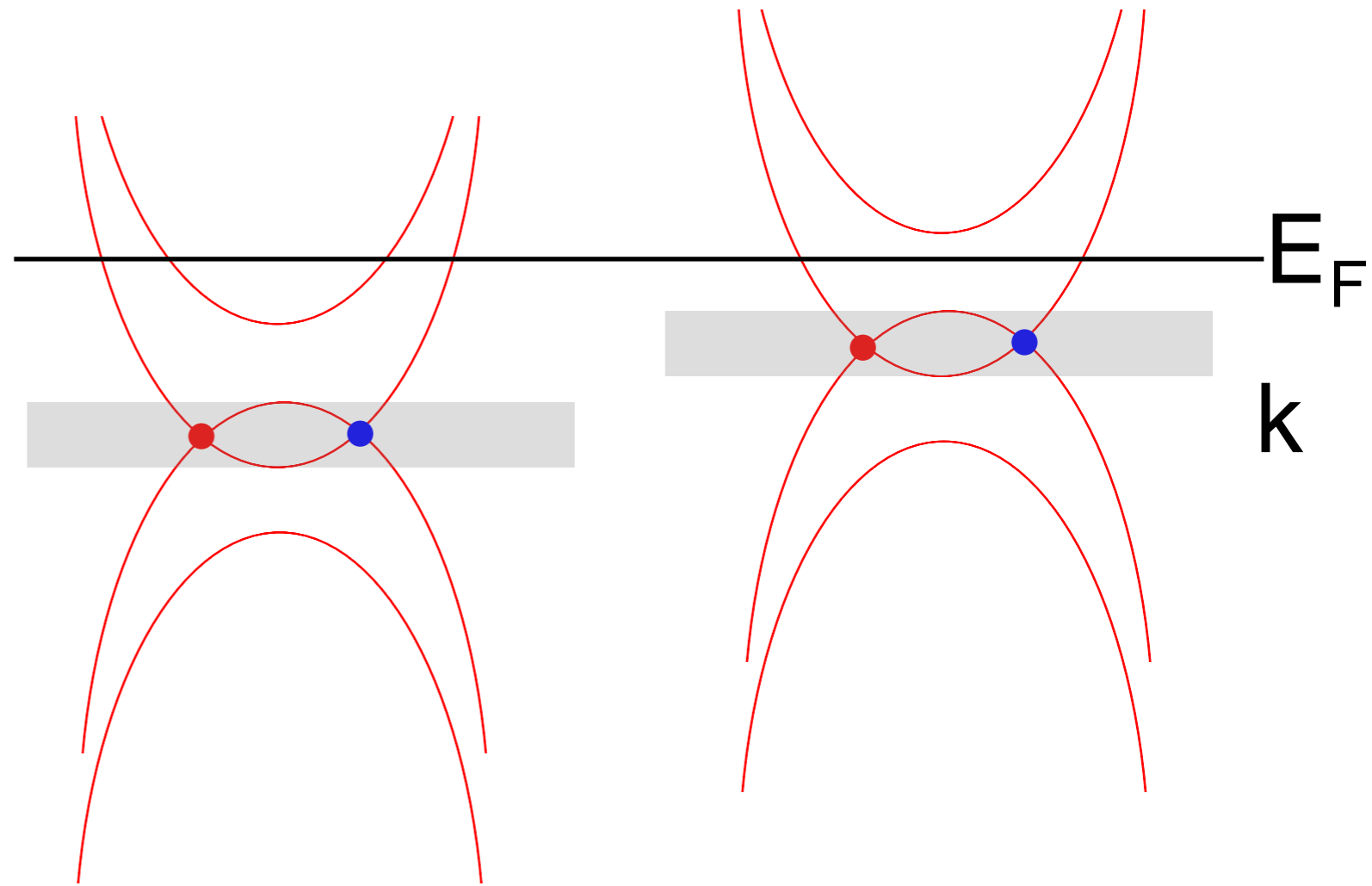
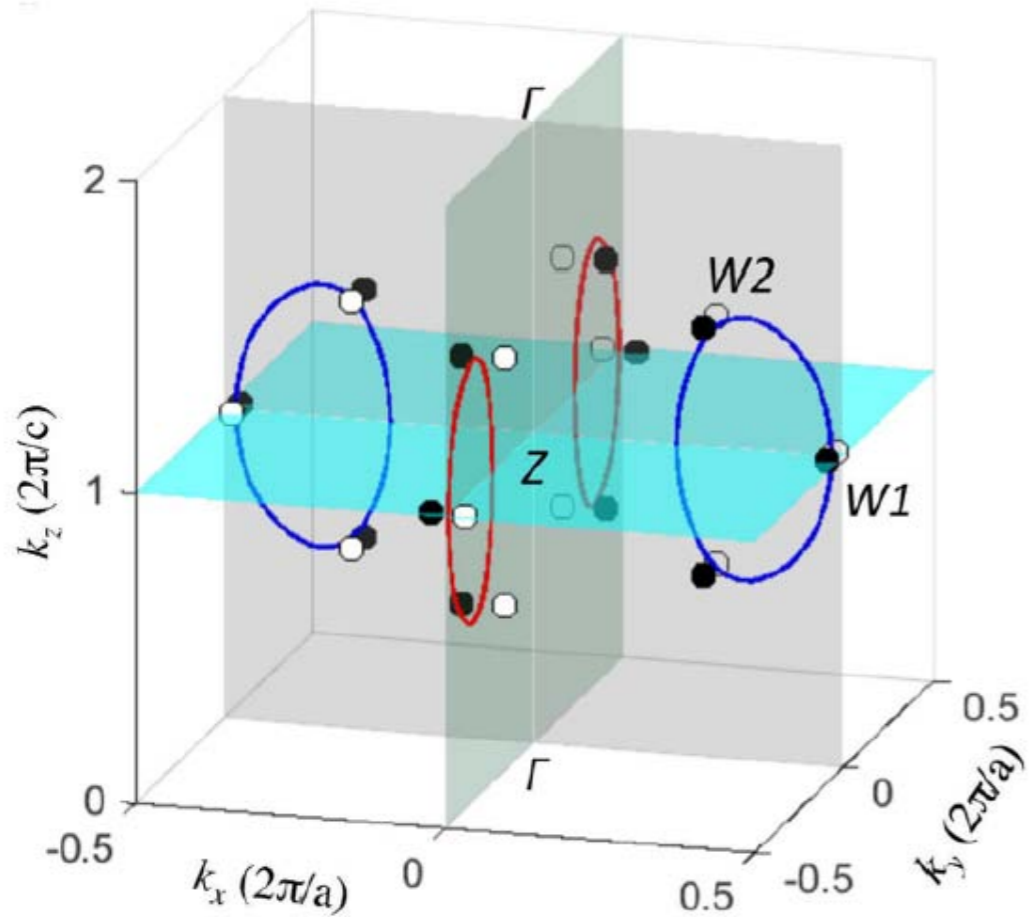
Without SO coupling  
Band inversion  
Nodal rings



ill-defined chirality

# Is the Fermi energy close to the Weyl points

## Two types of Weyl points

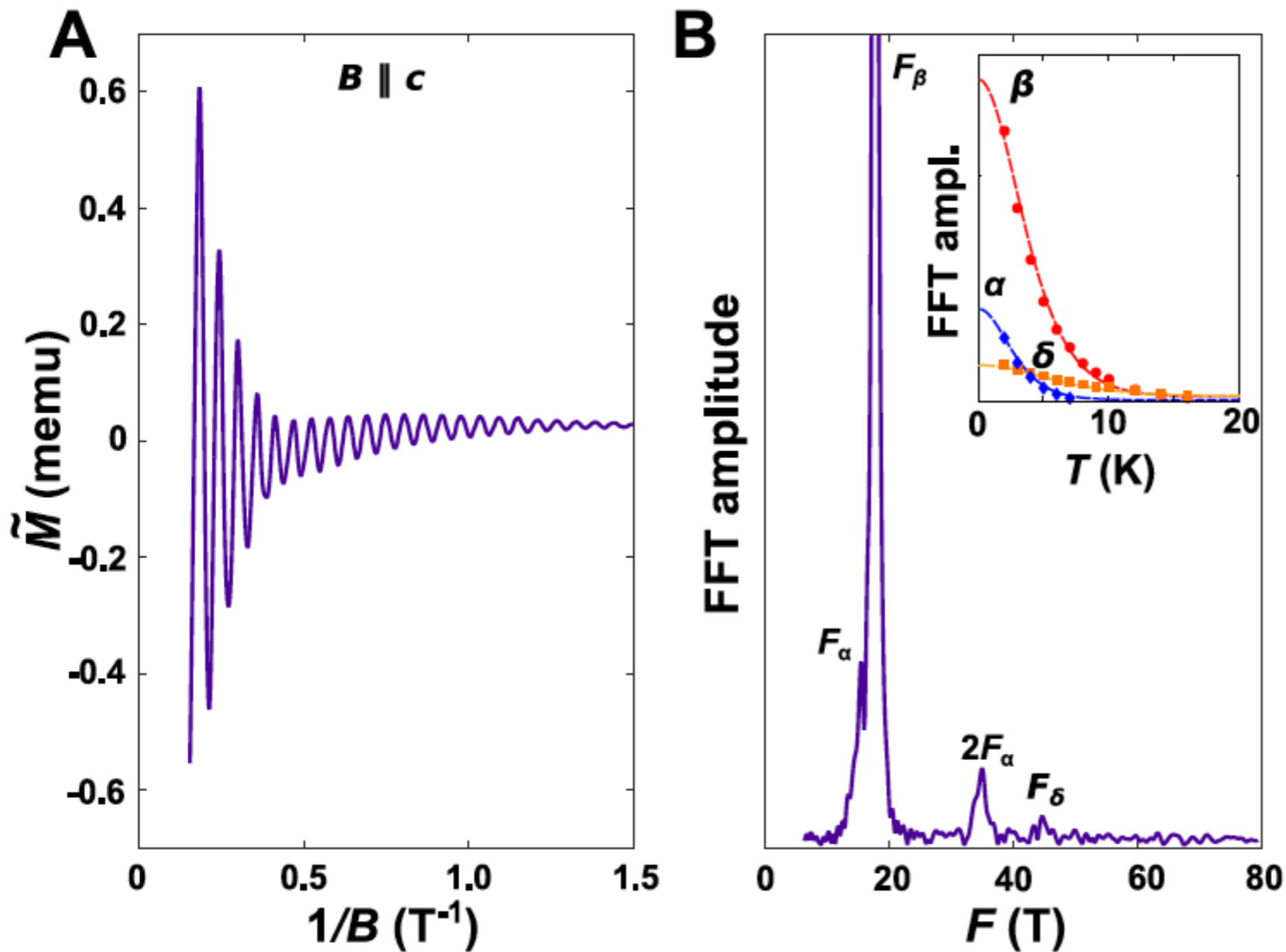


W1

W2



# TaP: Magnetization oscillations



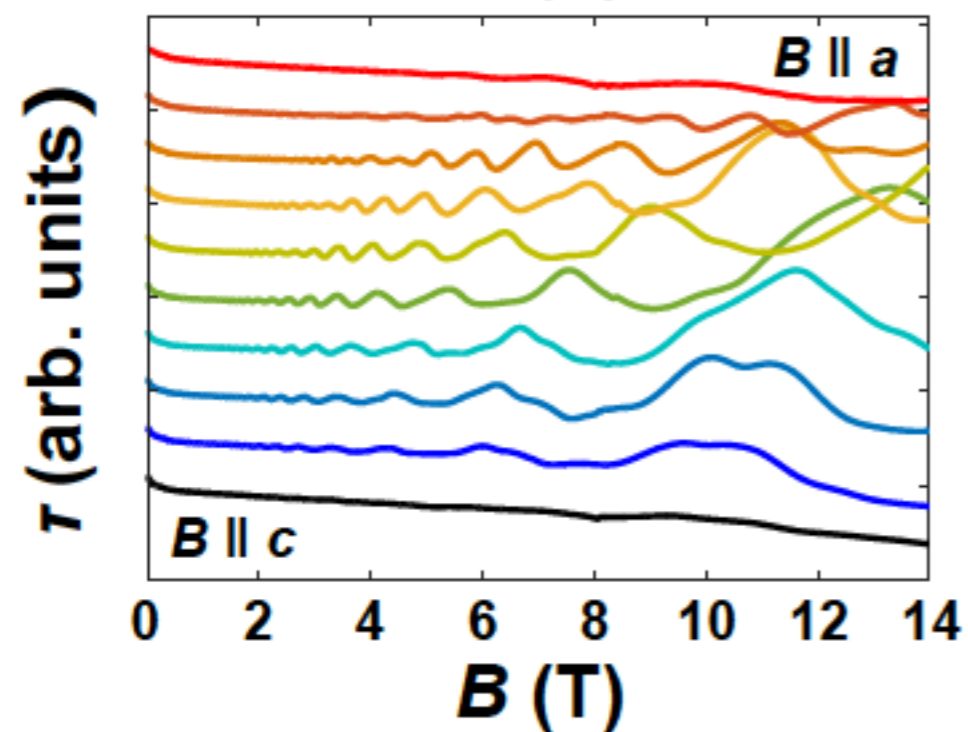
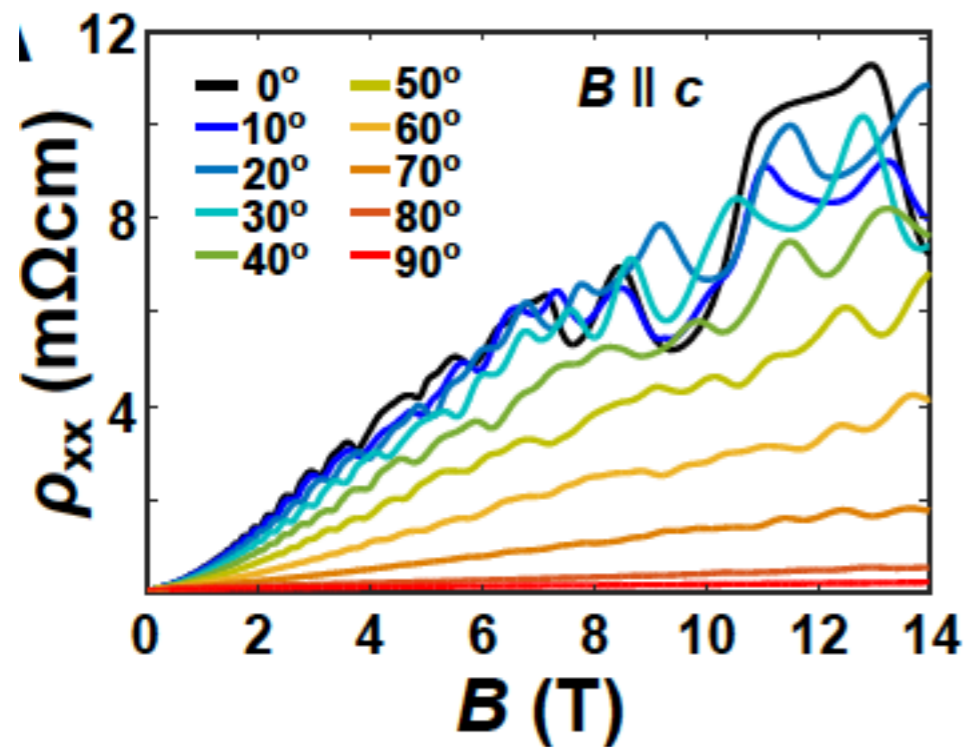
High quality  
single crystals  
Small  
frequencies  
**17 T** and **45 T**

Electron  
 $m^* = 0.1$

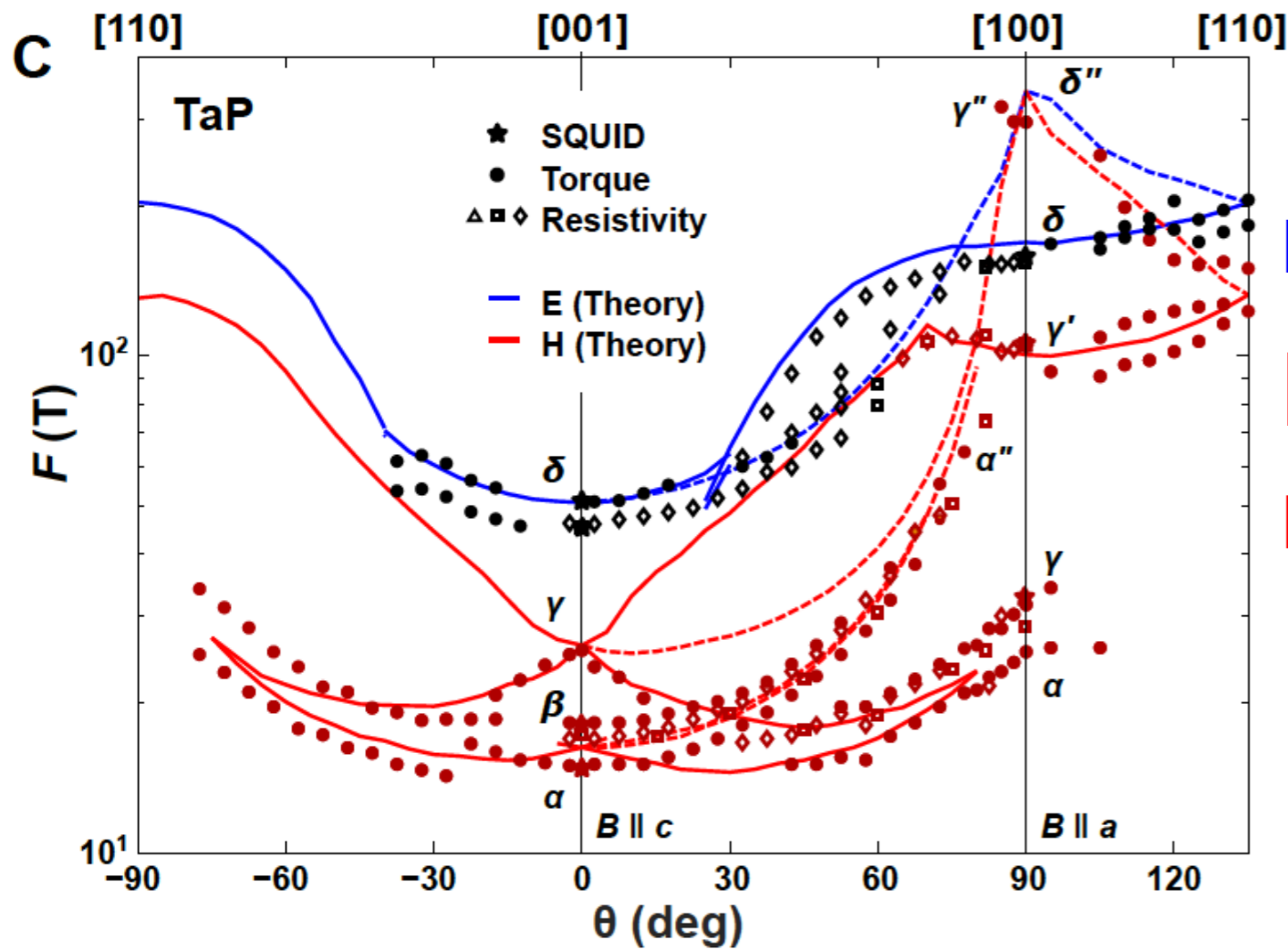
Hole  
 $m^* = 0.02$

Mobility  $3 \times 10^4 \text{ cm}^2/\text{Vs} = 3 \text{ T}^{-1}$   
Mean free path  $l = 0.4 \text{ }\mu\text{m}$

# Quantum oscillations – angular dependence

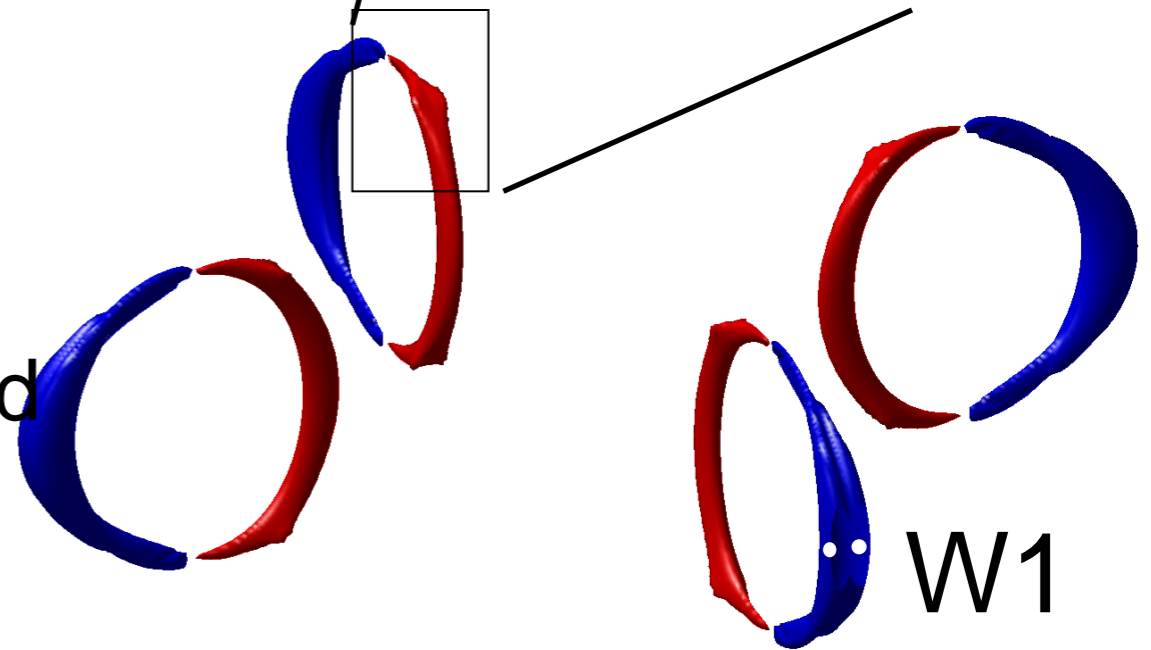
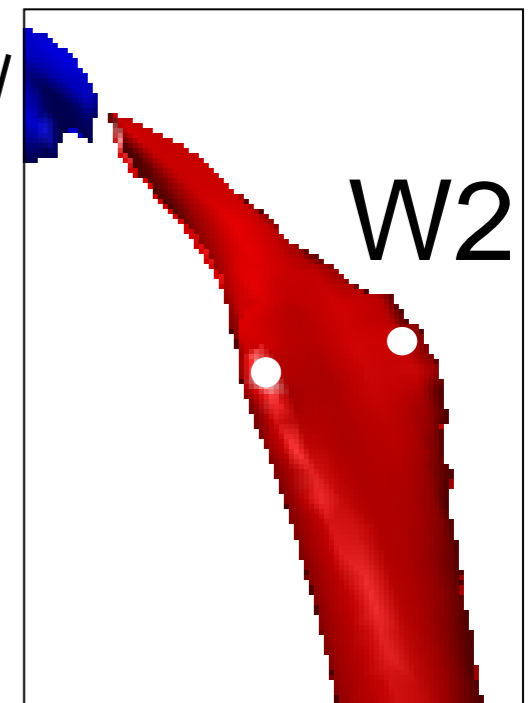


# TaP - Bulk Fermi surface



Electron  
 $m^* = 0.1$

Hole  
 $m^* = 0.02$

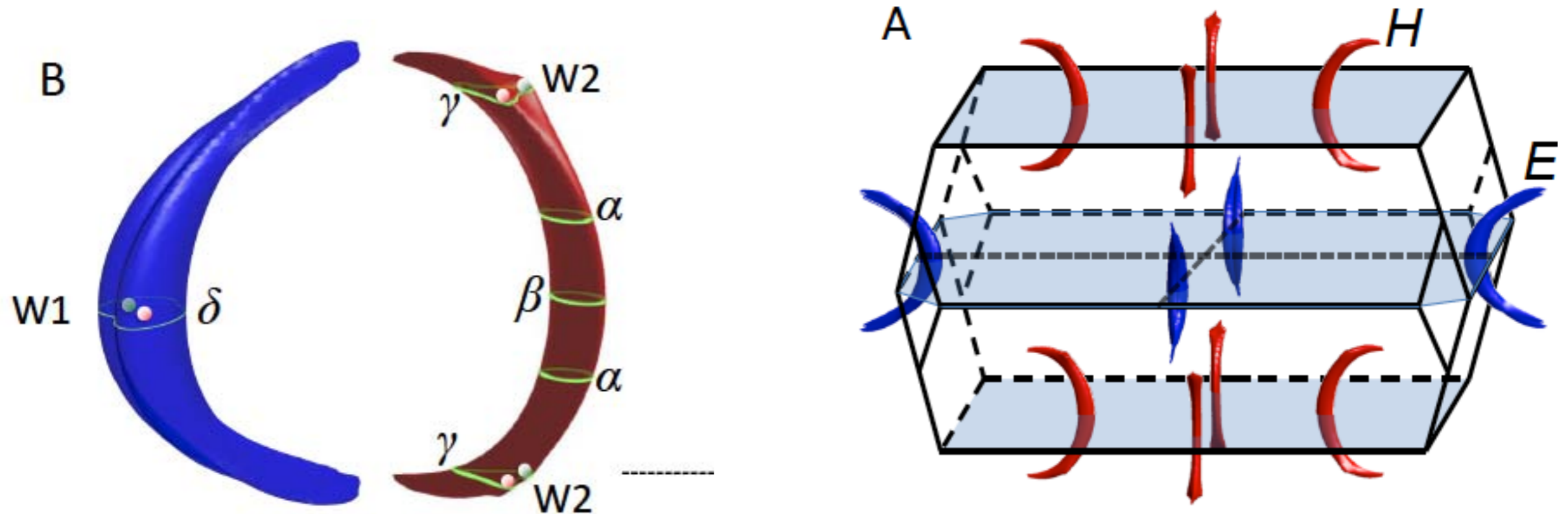


Points from torque, magnetization and resistivity

5 samples from 2 batches

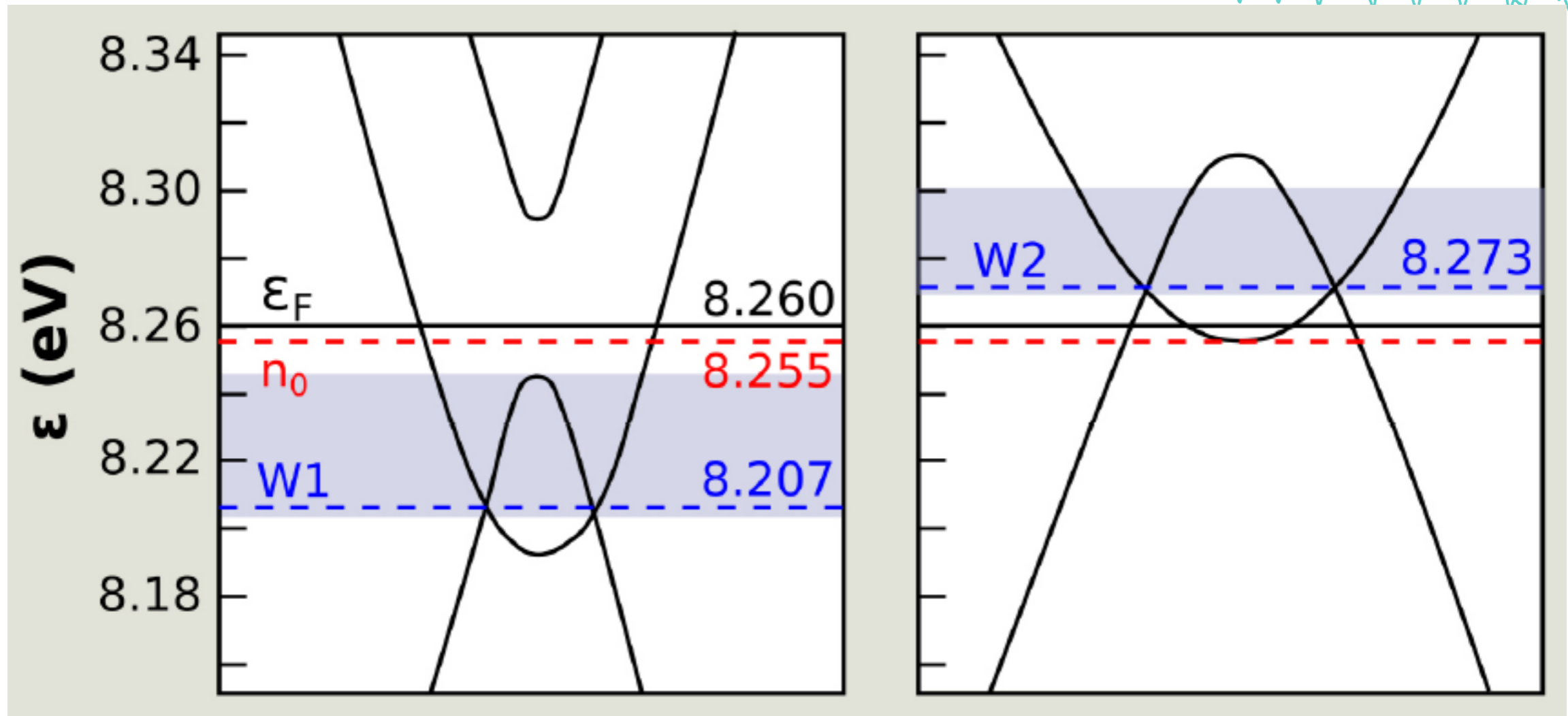
Lines from DFT

# Fermi surface topology



Along nodal rings  
FS pockets contain pairs of Weyl points

# Position of Fermi level with respect to Weyl points



Determined Fermi level with meV resolution  
 $E_F$  is 5 meV above charge neutral Fermi level  
In agreement with Hall measurements  
Carrier density:  $n \approx 10^{19}$

# TaP



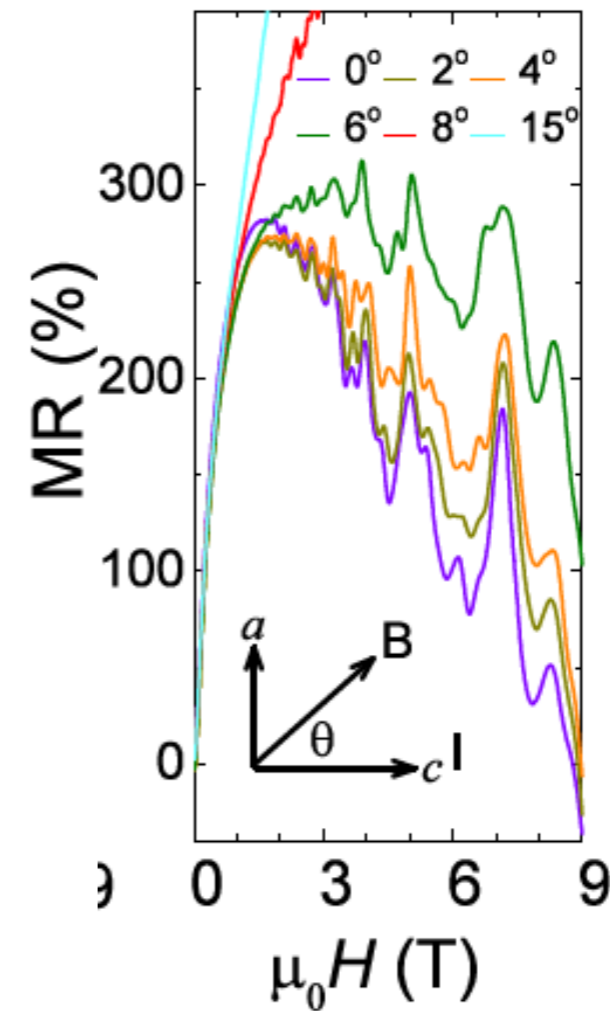
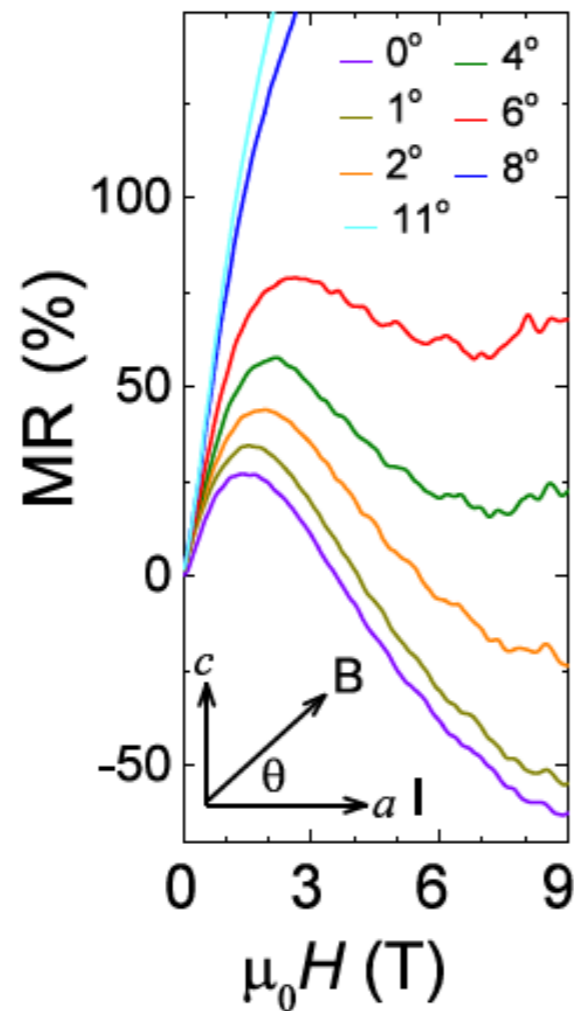
- No independent Fermi surface pockets around Weyl points
- No well-defined chirality
- Physical properties based on chirality such as chiral anomaly not expected

# Negative longitudinal magnetoresistance

TaP

$I \parallel a$   $B \parallel a$

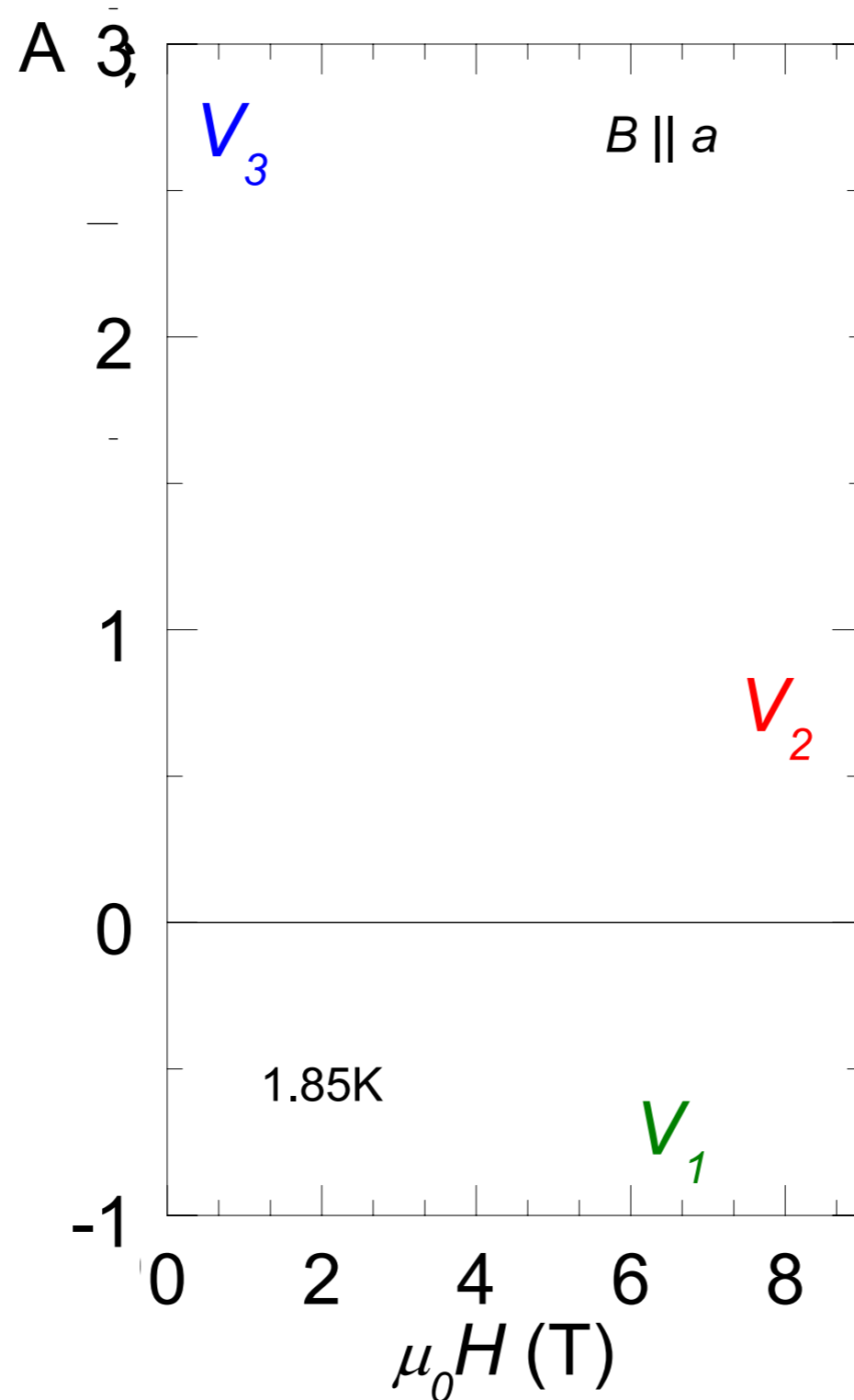
$I \parallel c$   $B \parallel c$



Appears in very small angular window  
 $I$  and  $B$  have to be parallel within  $2^\circ$



# Inhomogeneous current distribution

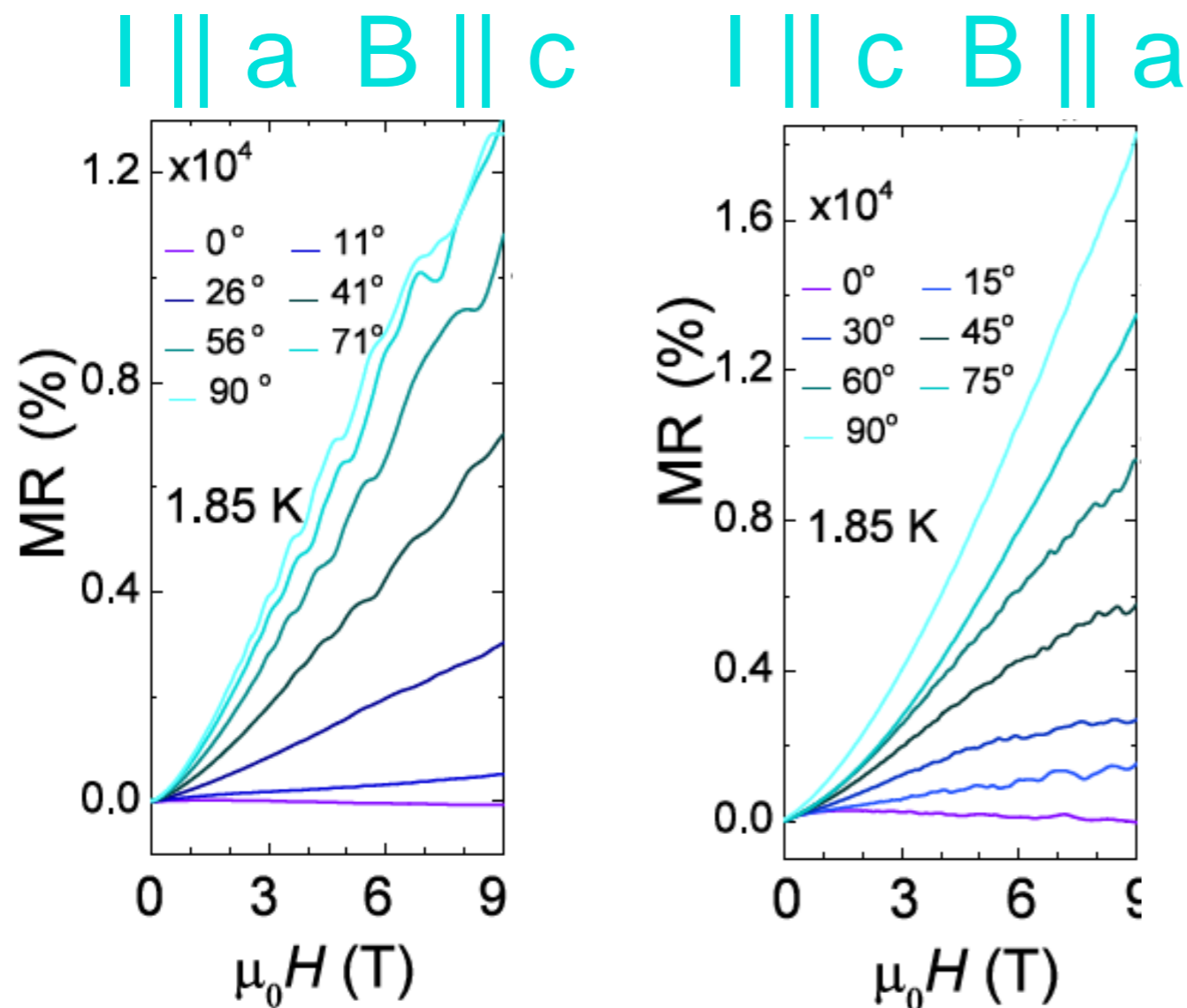


Point-like contacts

Reed 1971  
Yoshida JPSJ 1975  
Pippard, Magnetoresistance in Metals



# Large transverse magnetoresistance



- Large transverse MR due to strong orbital effect
- Orbital effect absent in longitudinal magnetic fields

High mobility:  $\mu B = \omega_c \tau$

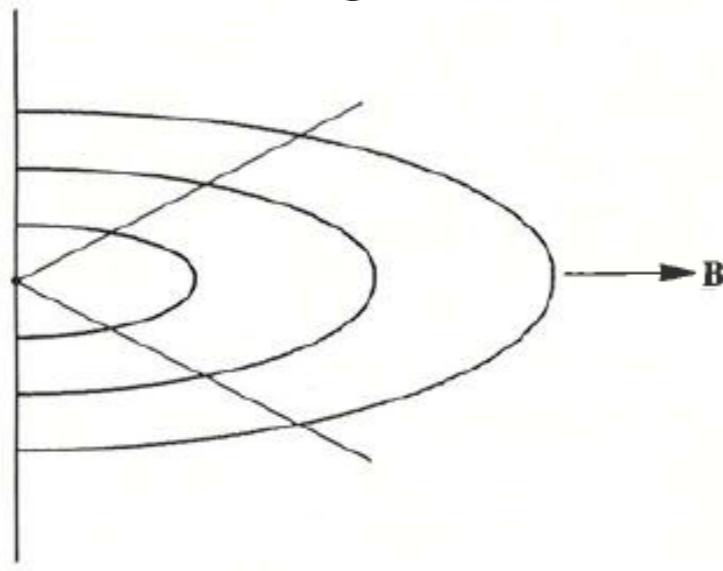
Anisotropy over  $R_t / R_l > 100$

# Potential distribution in systems with anisotropic resistivity tensor

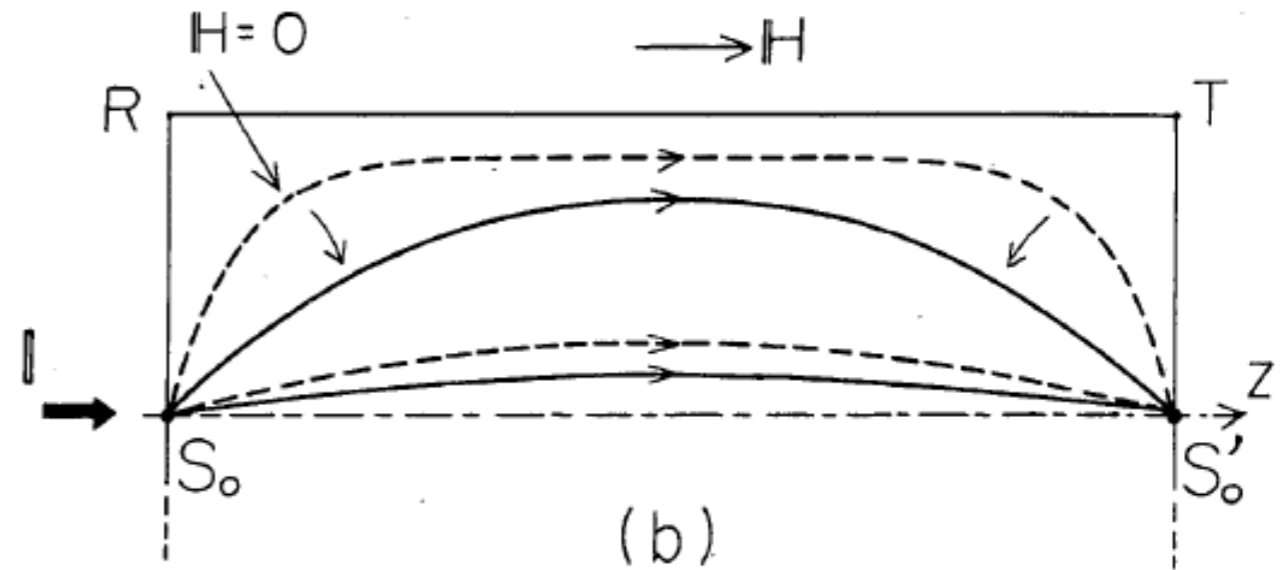
$H = 0$



$H > 0$



## Current trajectory



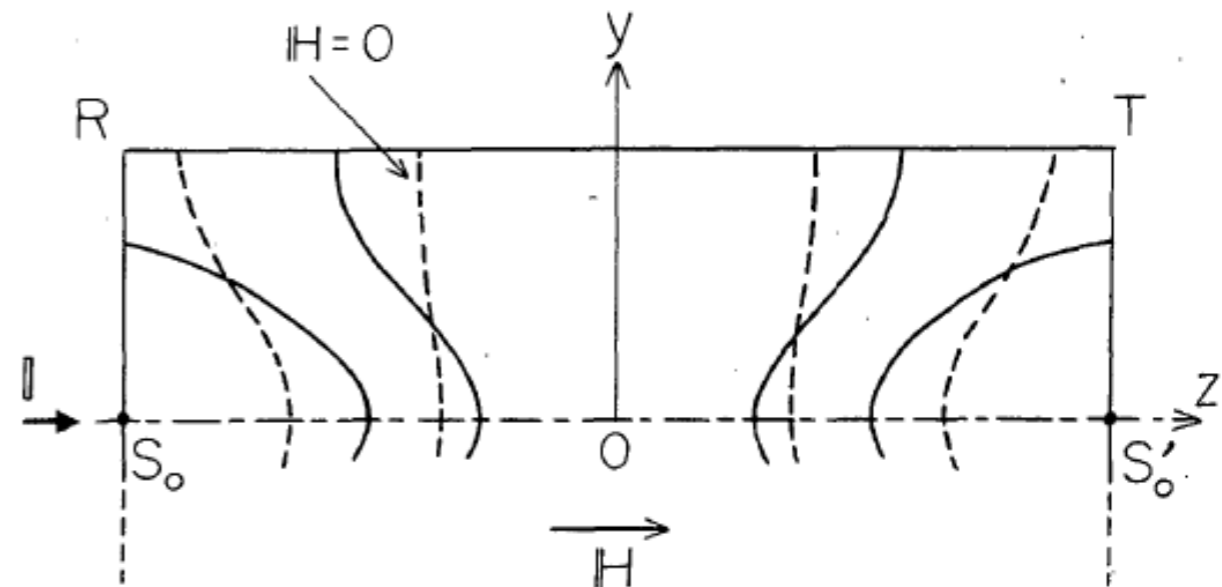
$B$

$\rho_{zz}$

$\rho_{xx}$

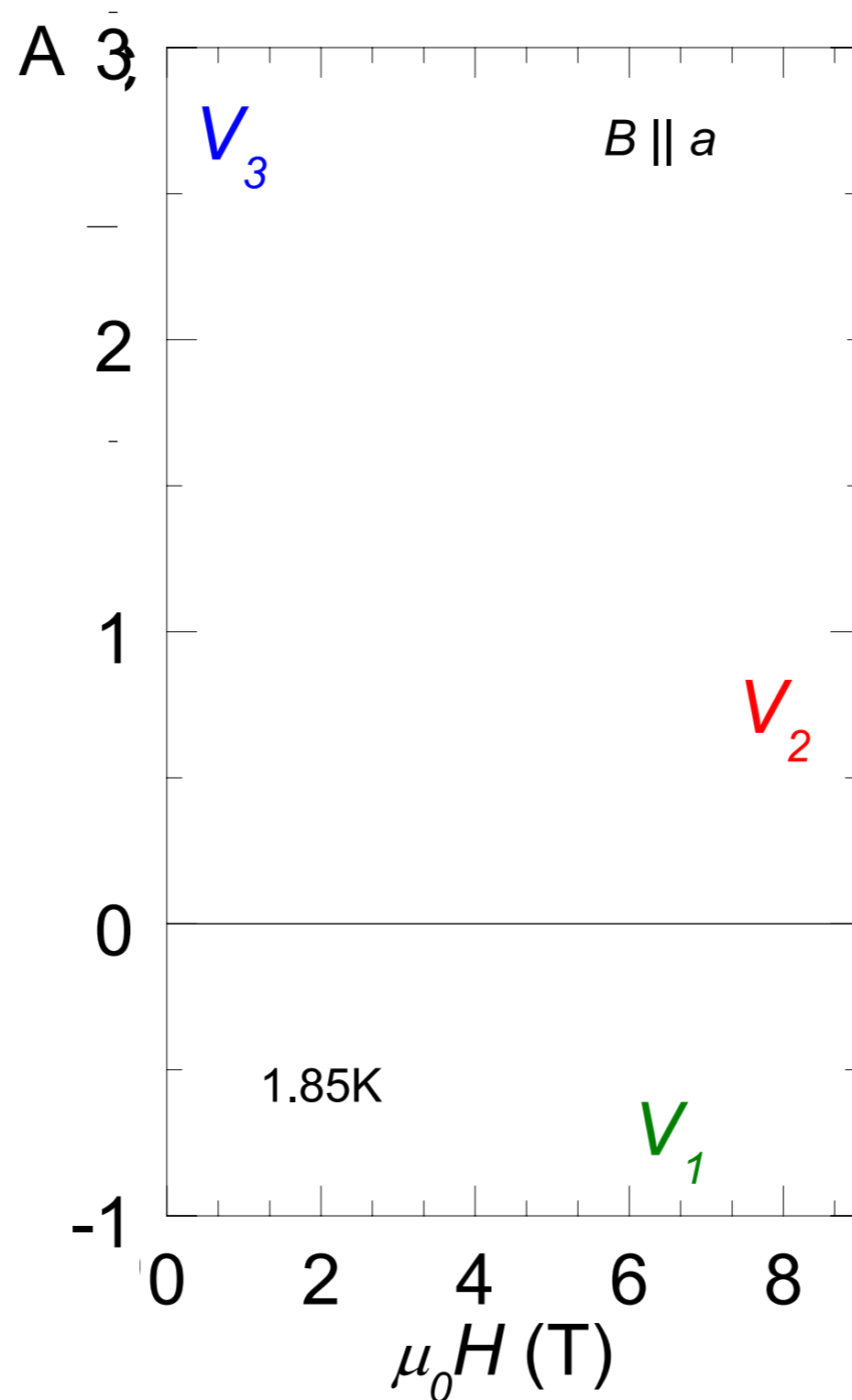
$$A = \frac{\rho_{xx}}{\rho_{zz}}$$

## Potential distribution

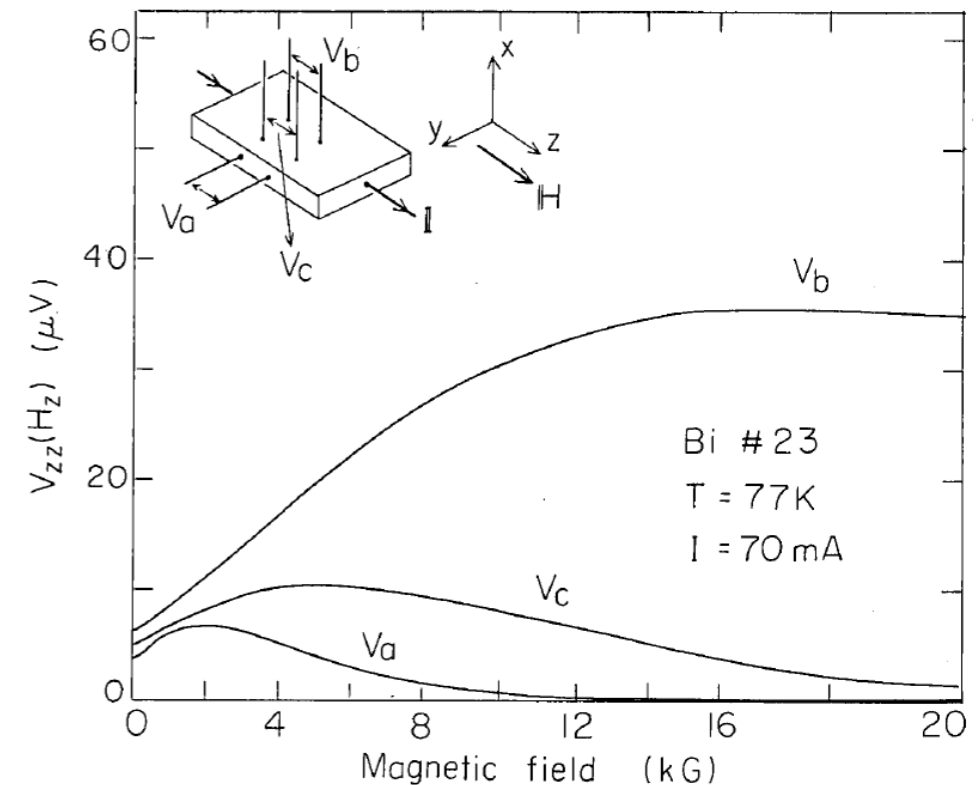


# Inhomogeneous current distribution

Point-like contacts



## Bismuth 1976



Reed 1971

Yoshida JPSJ 1975

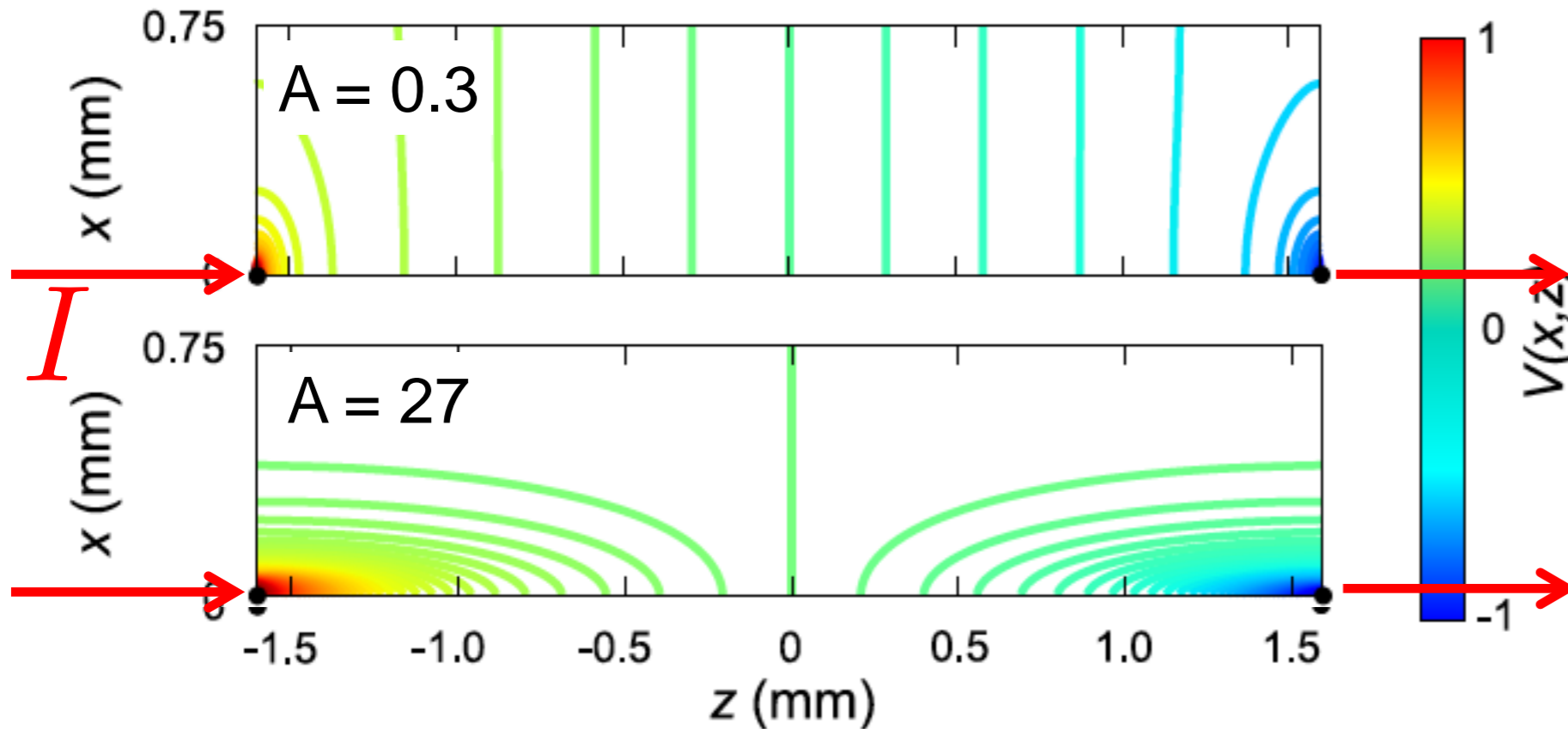
Pippard, Magnetoresistance in Metals

# Current jetting



Equipotential lines

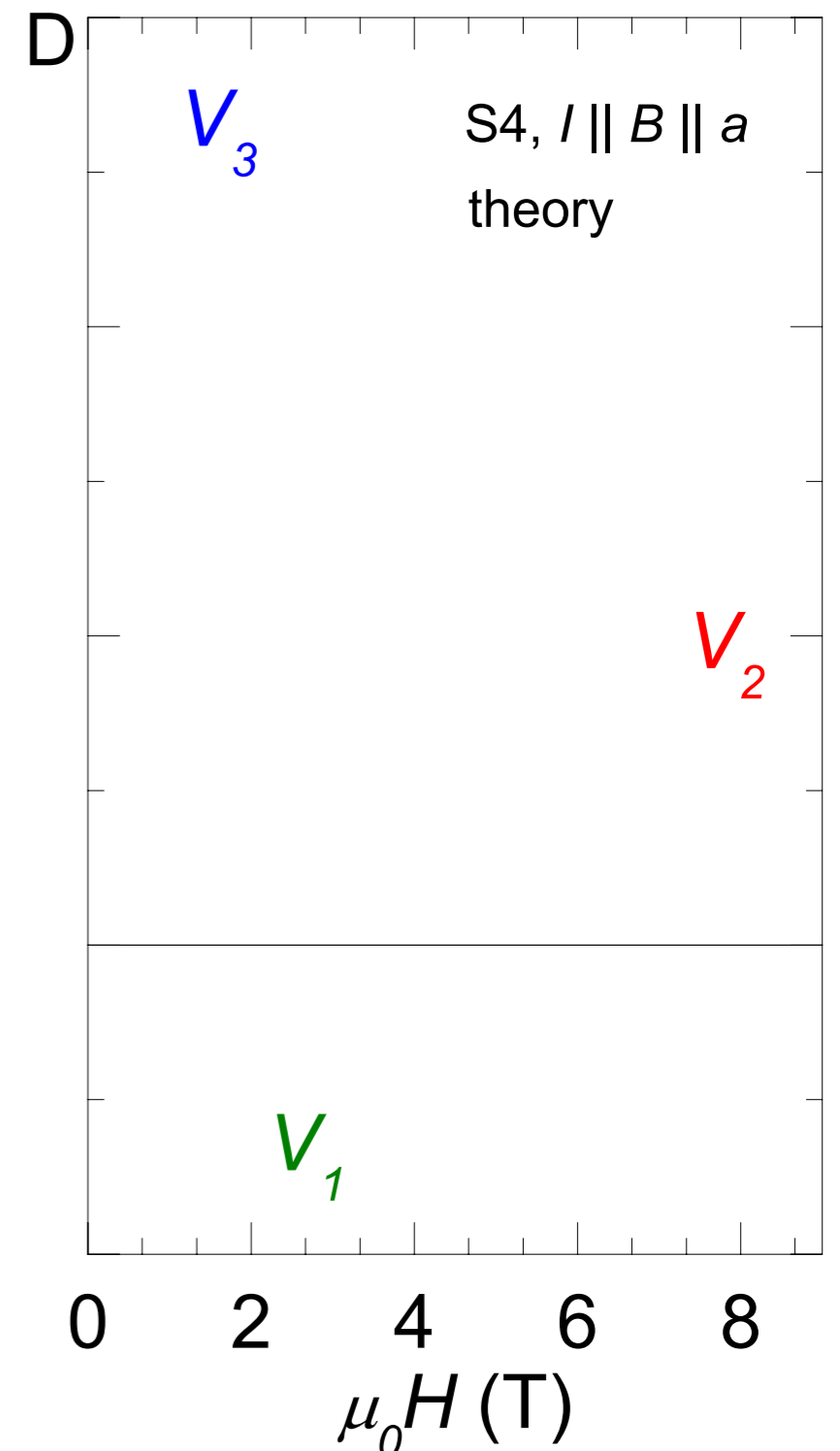
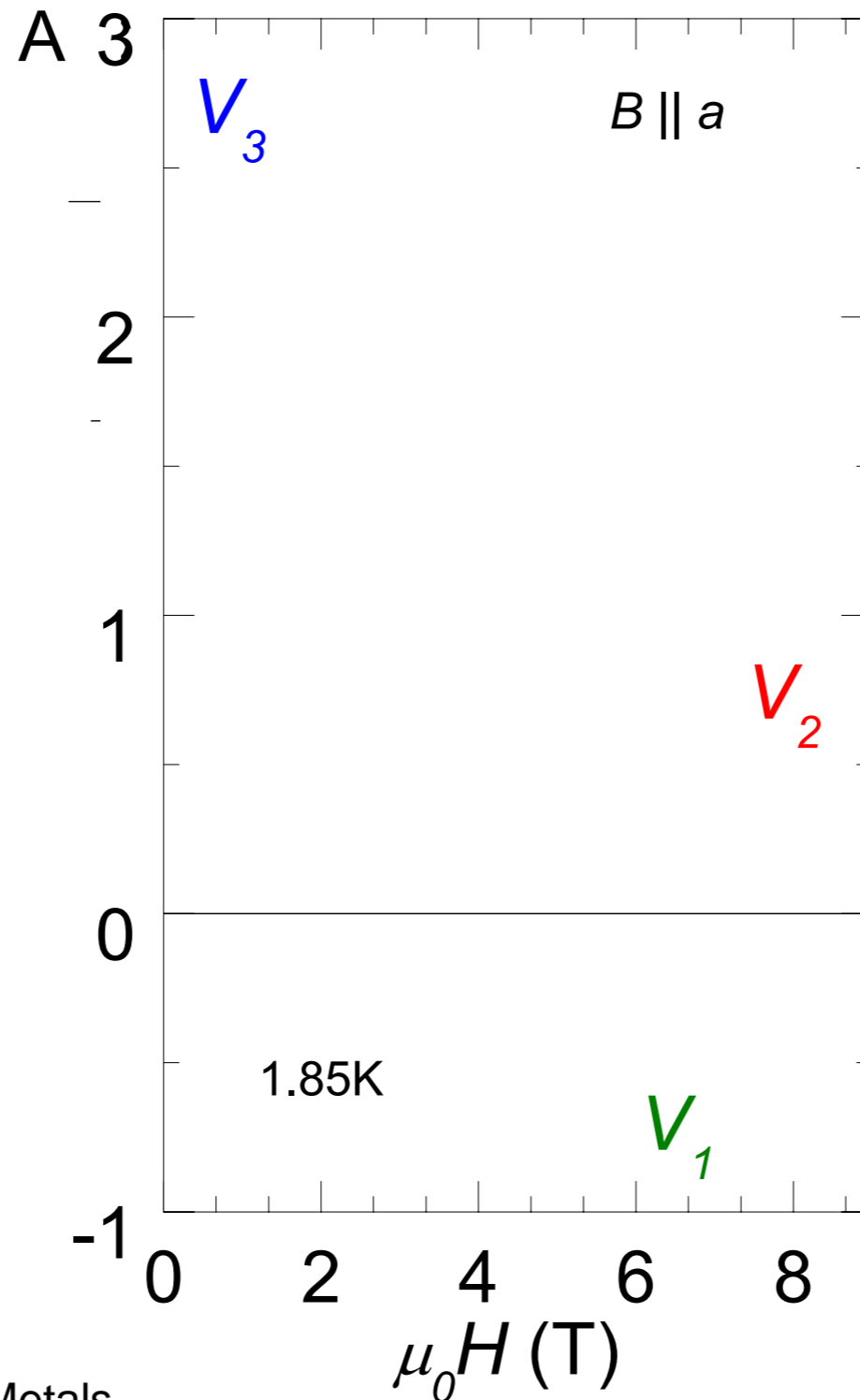
$B \longrightarrow$



Resistance anisotropy  $A = R_t / R_l = 27$

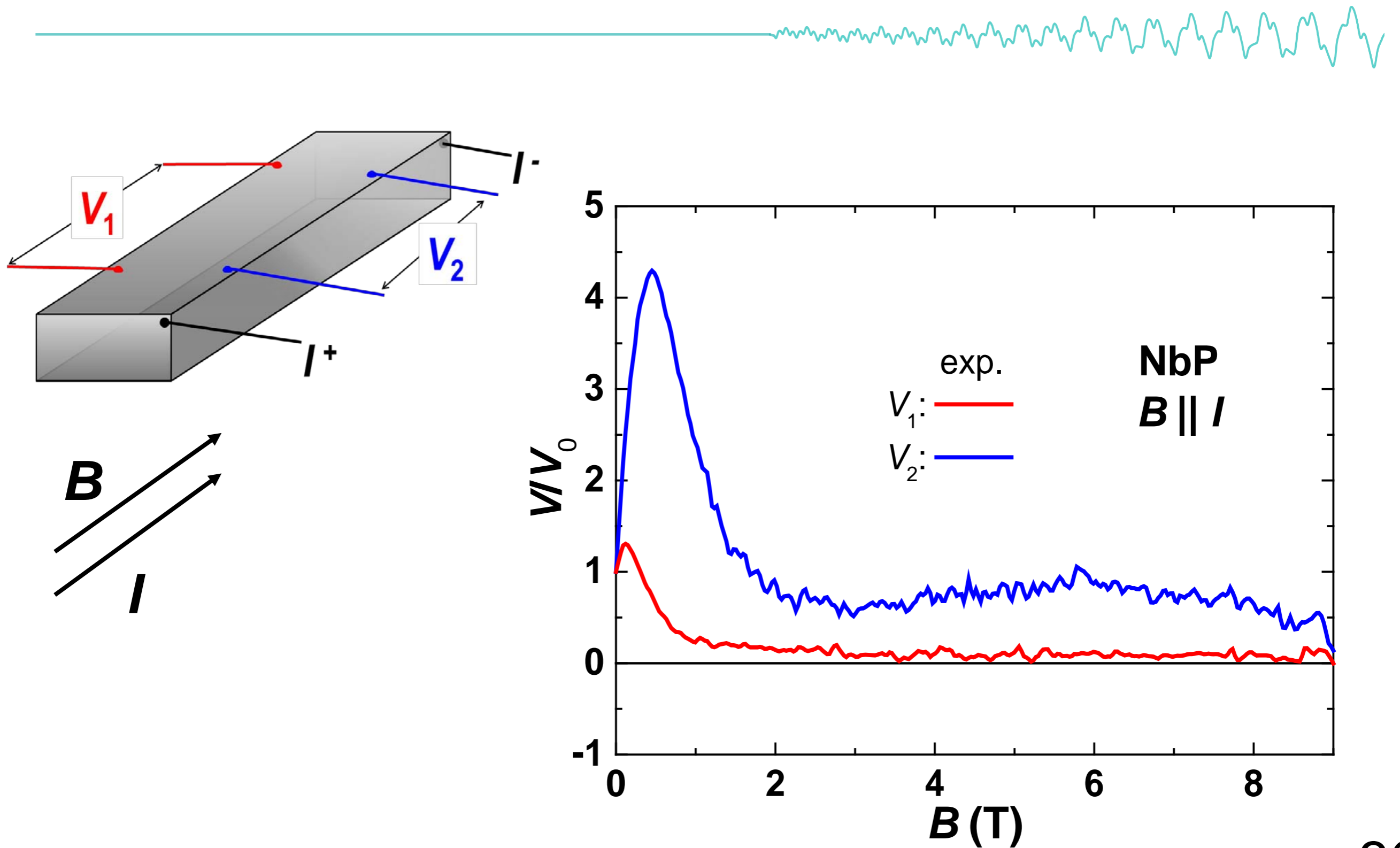
# Inhomogeneous current

Point-like  
contacts  
 $R_l = R_l(0 \text{ T})$



Reed 1971  
Yoshida JPSJ 1975  
Pippard, Magnetoresistance in Metals

# The case of NbP



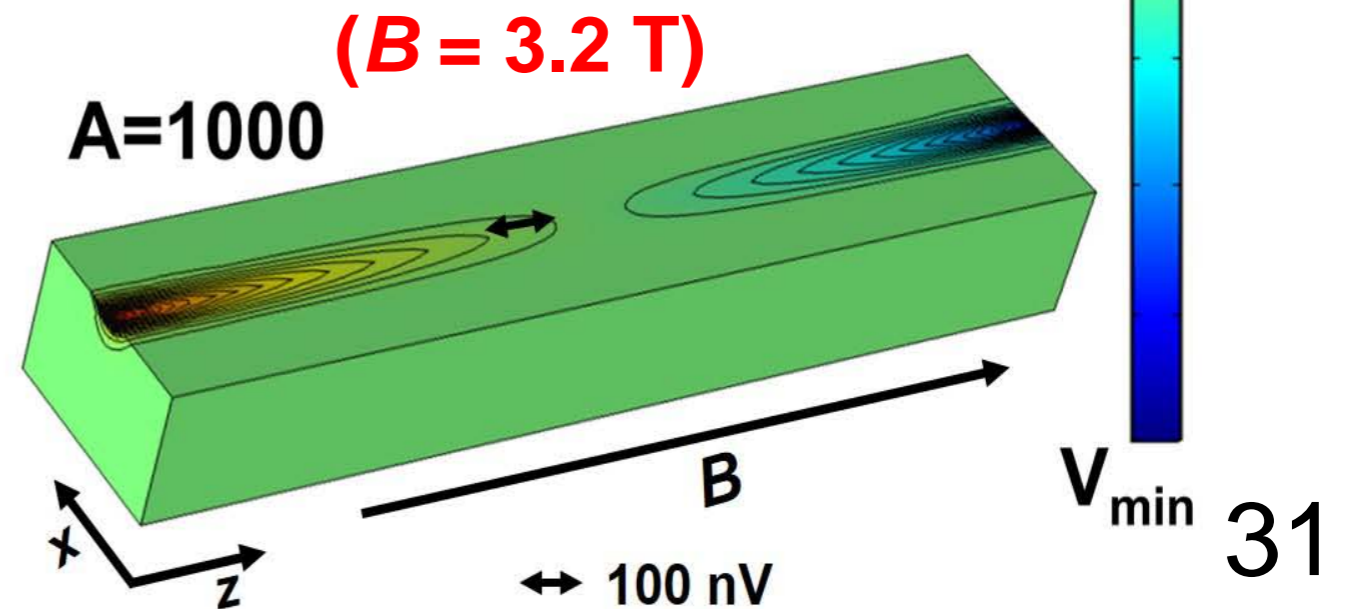
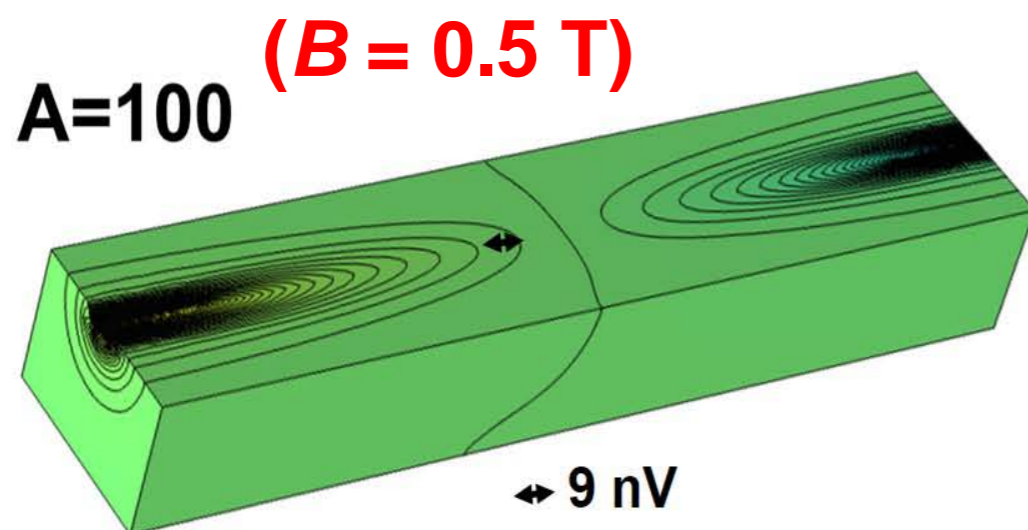
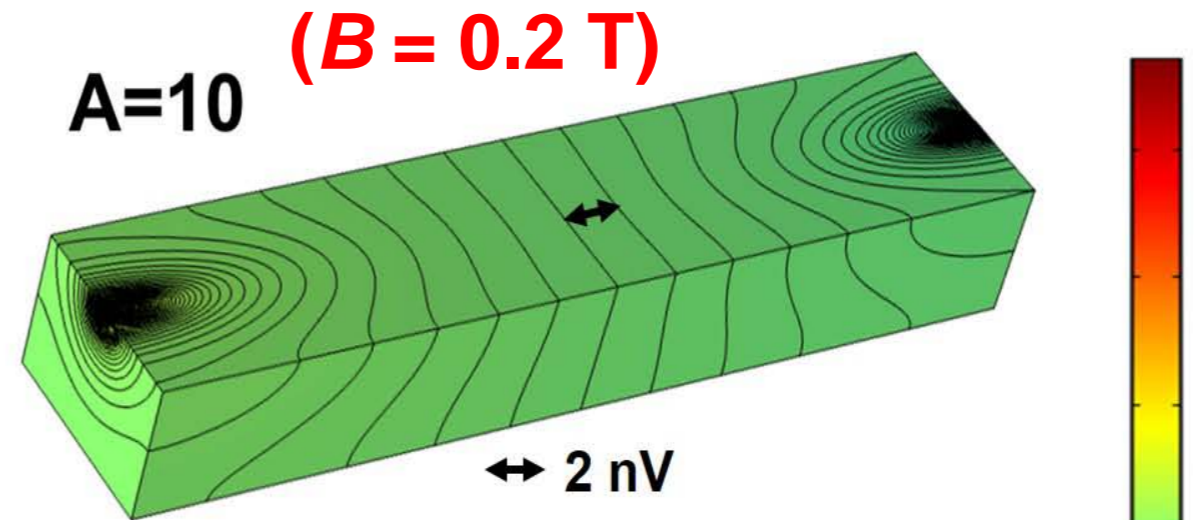
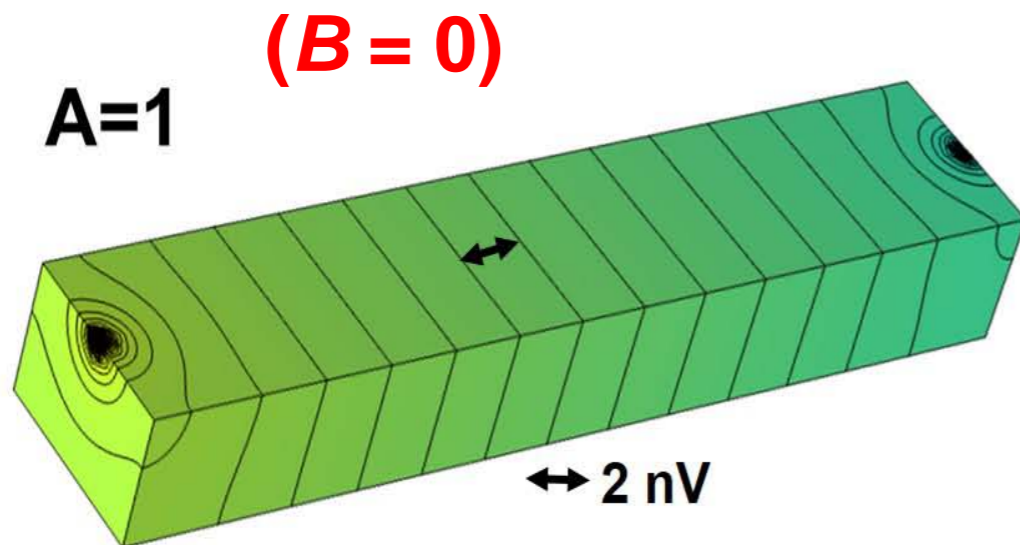
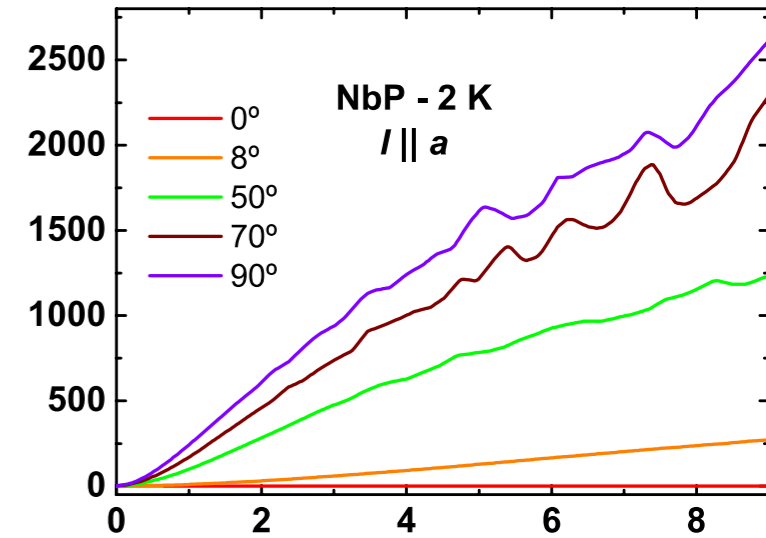


# Finite element simulations

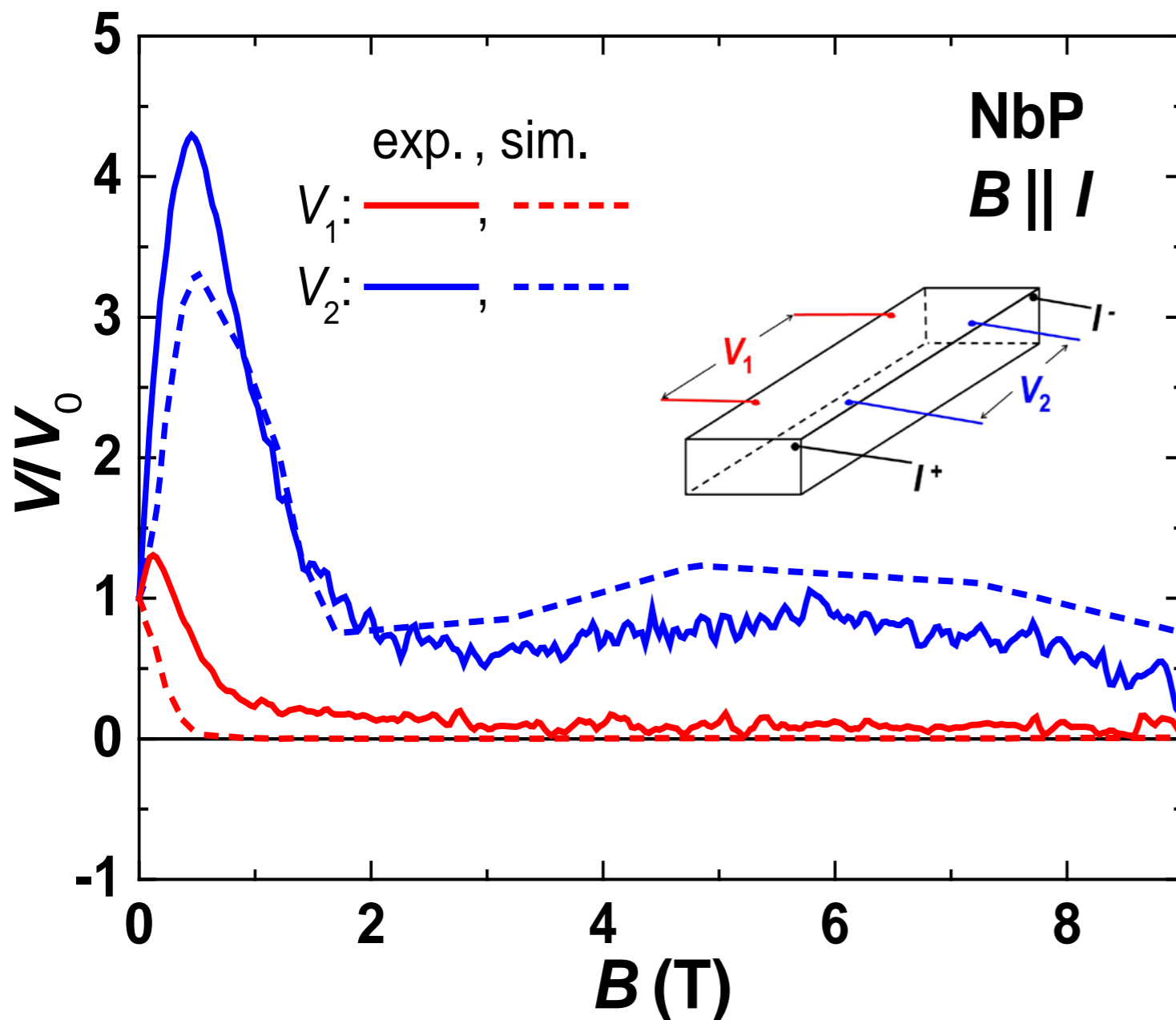
$\rho_{xx}$  is obtained from the transversal MR ( $B \perp I$ )

$\rho_{zz}$  is assumed field independent-  $\rho_{zz}(B) = \rho_{zz}(B=0)$

$$A = \rho_{xx}(B) / \rho_{zz}(B) = \rho_{xx}(B) / \rho(0)$$



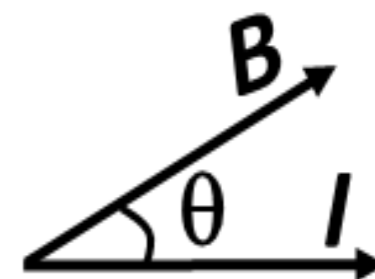
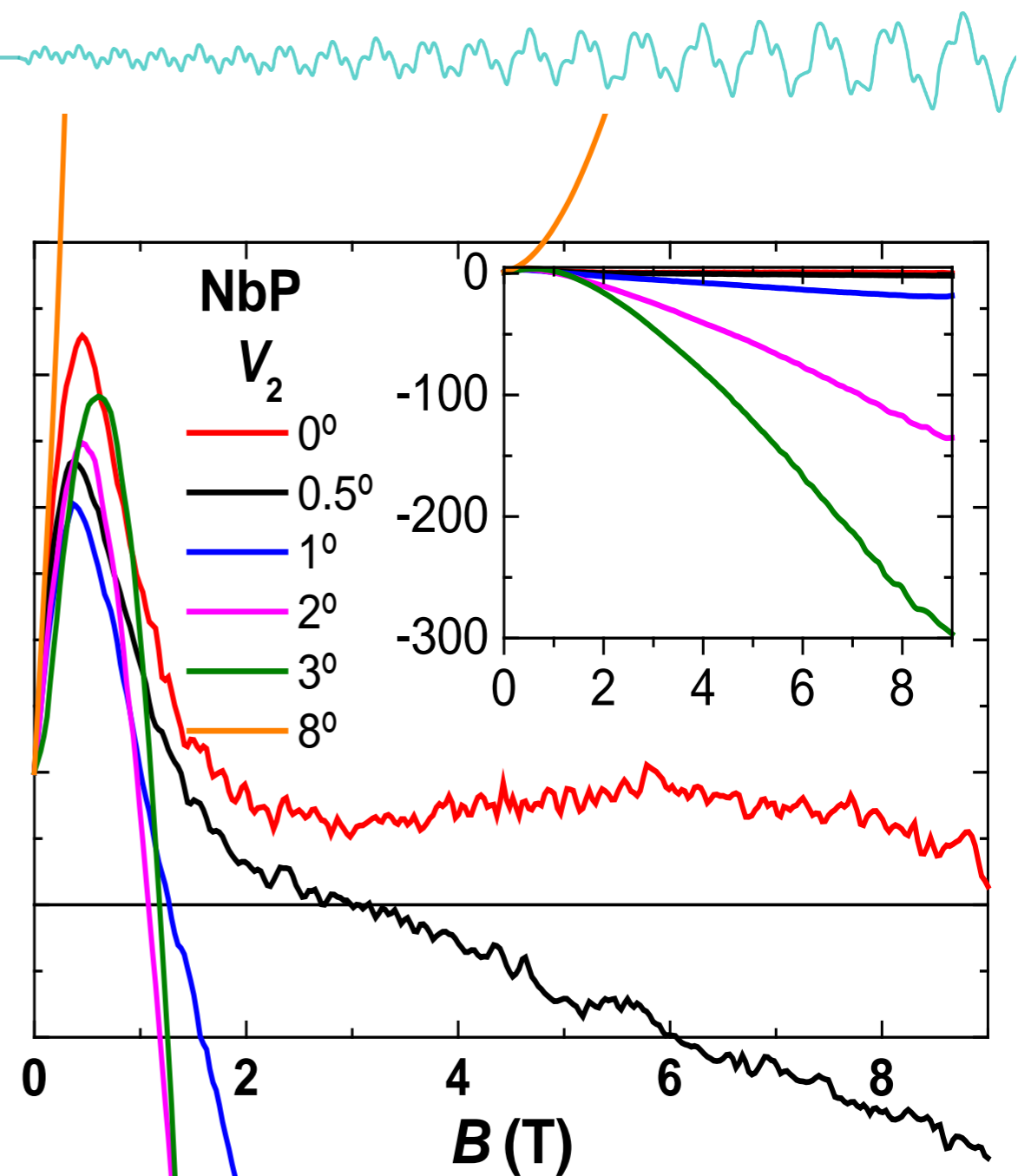
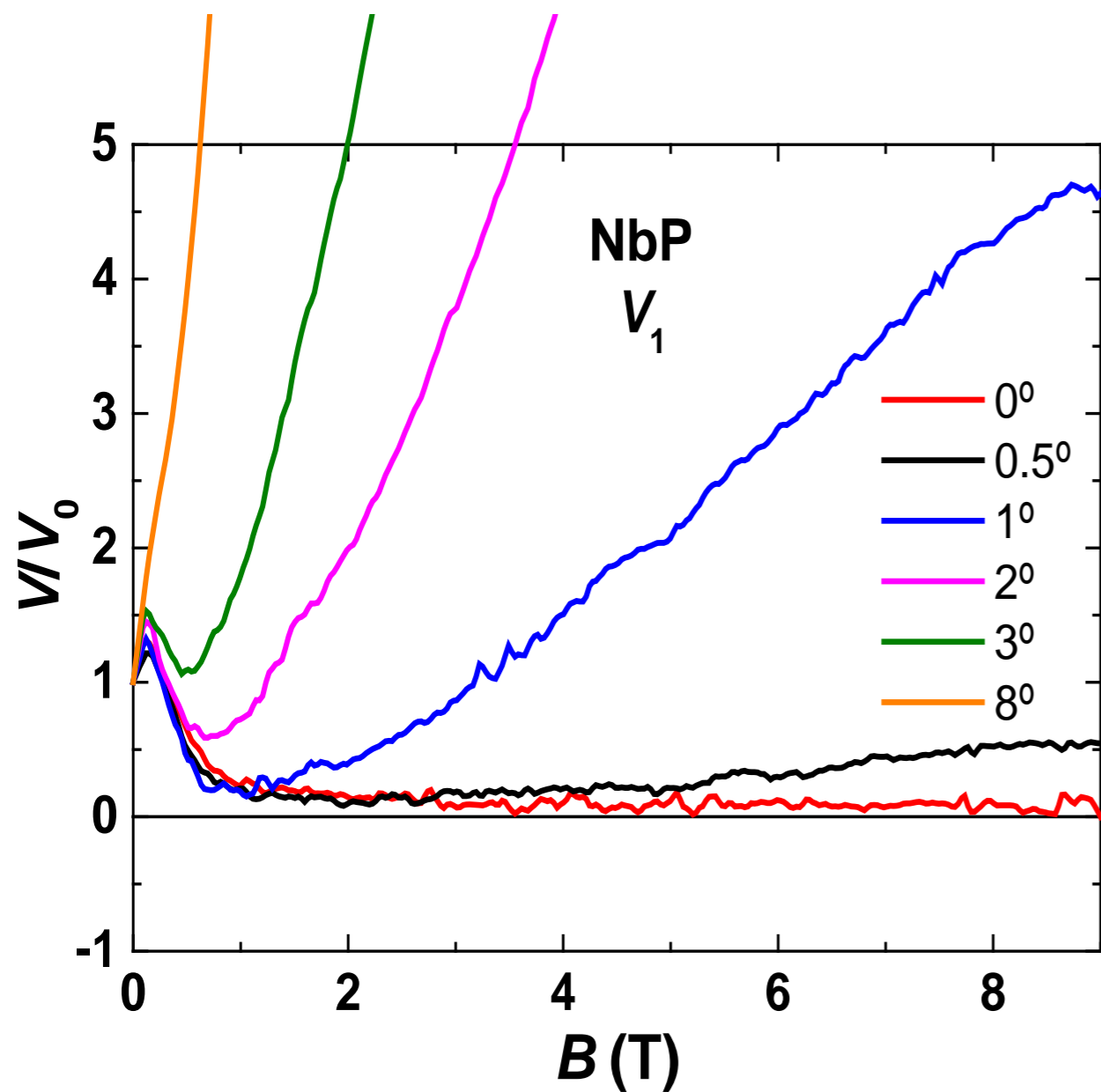
# Comparison with experiment



- The voltage drop is caused by increase of the transverse MR (anisotropy  $A$ )  
→ the current concentrates along a straight line connecting the current electrodes.
- The increase of  $V_2$  below 1 T occurs because the effective cross section of the sample is reduced → higher currents and voltages close to the current jet.



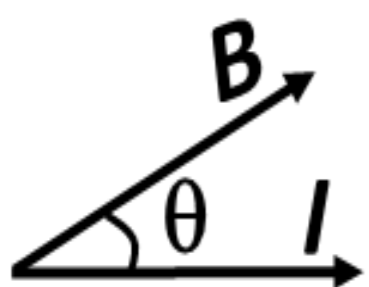
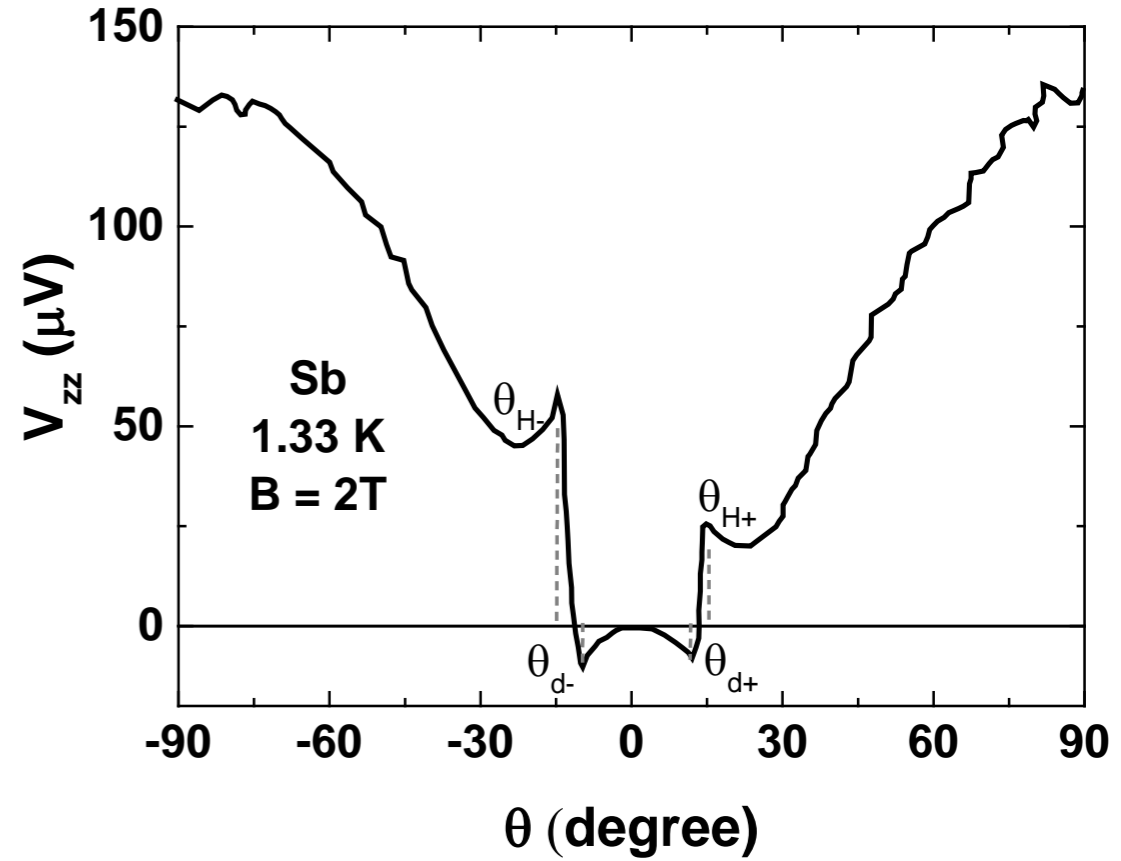
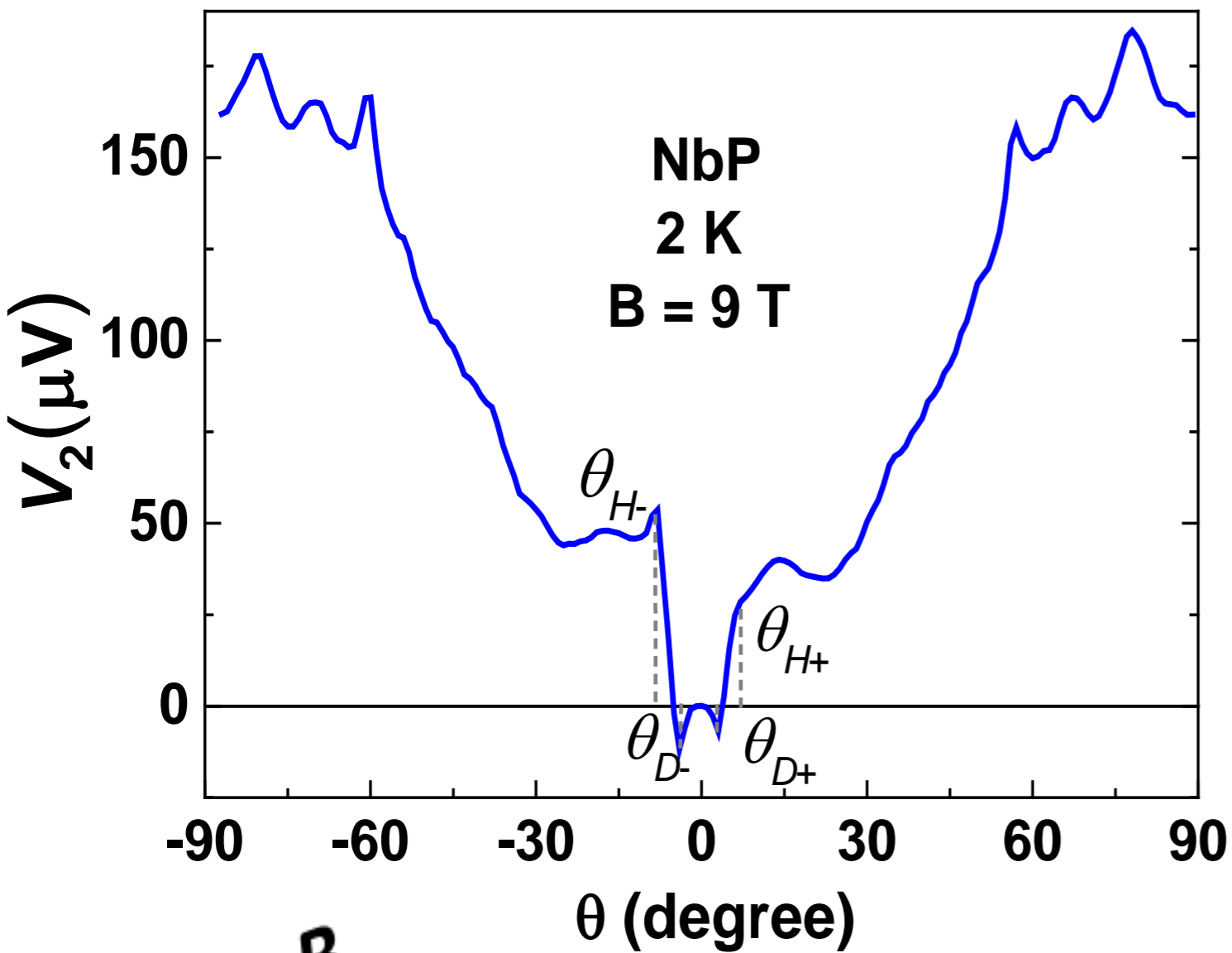
# Angular dependence



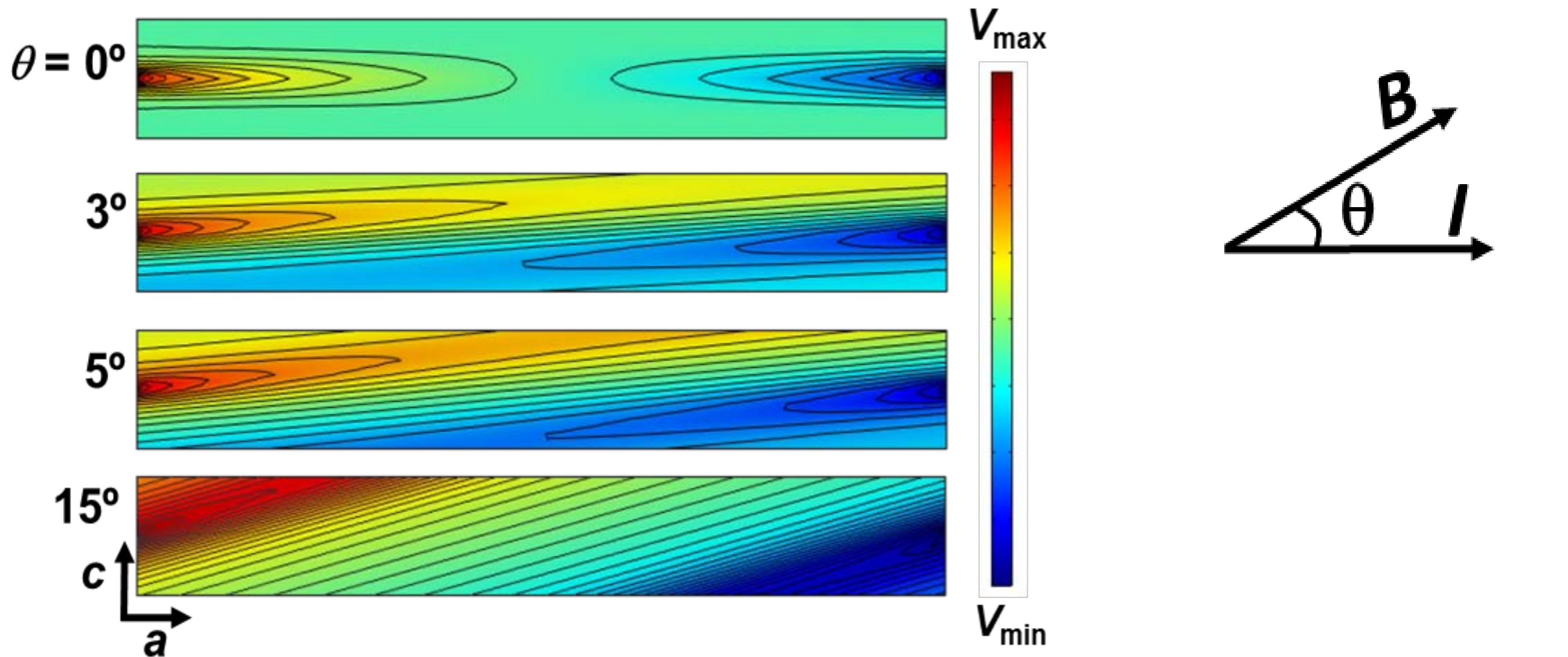
# Inhomogeneous current



A similar angular dependence has been reported for Sb about 40 years ago.

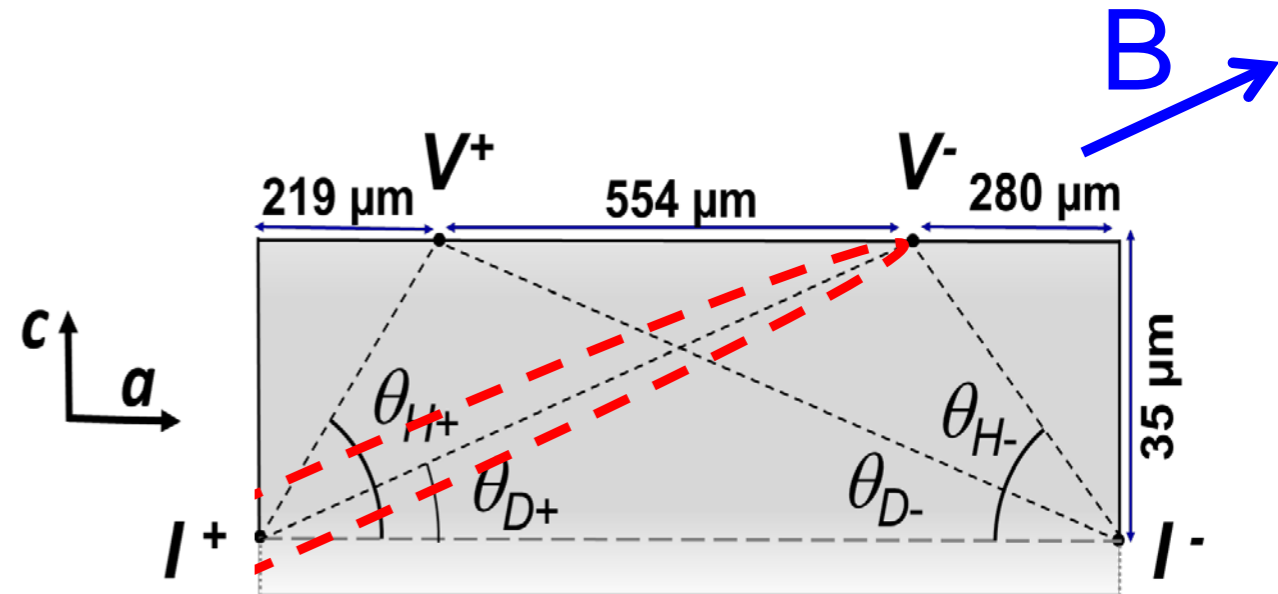
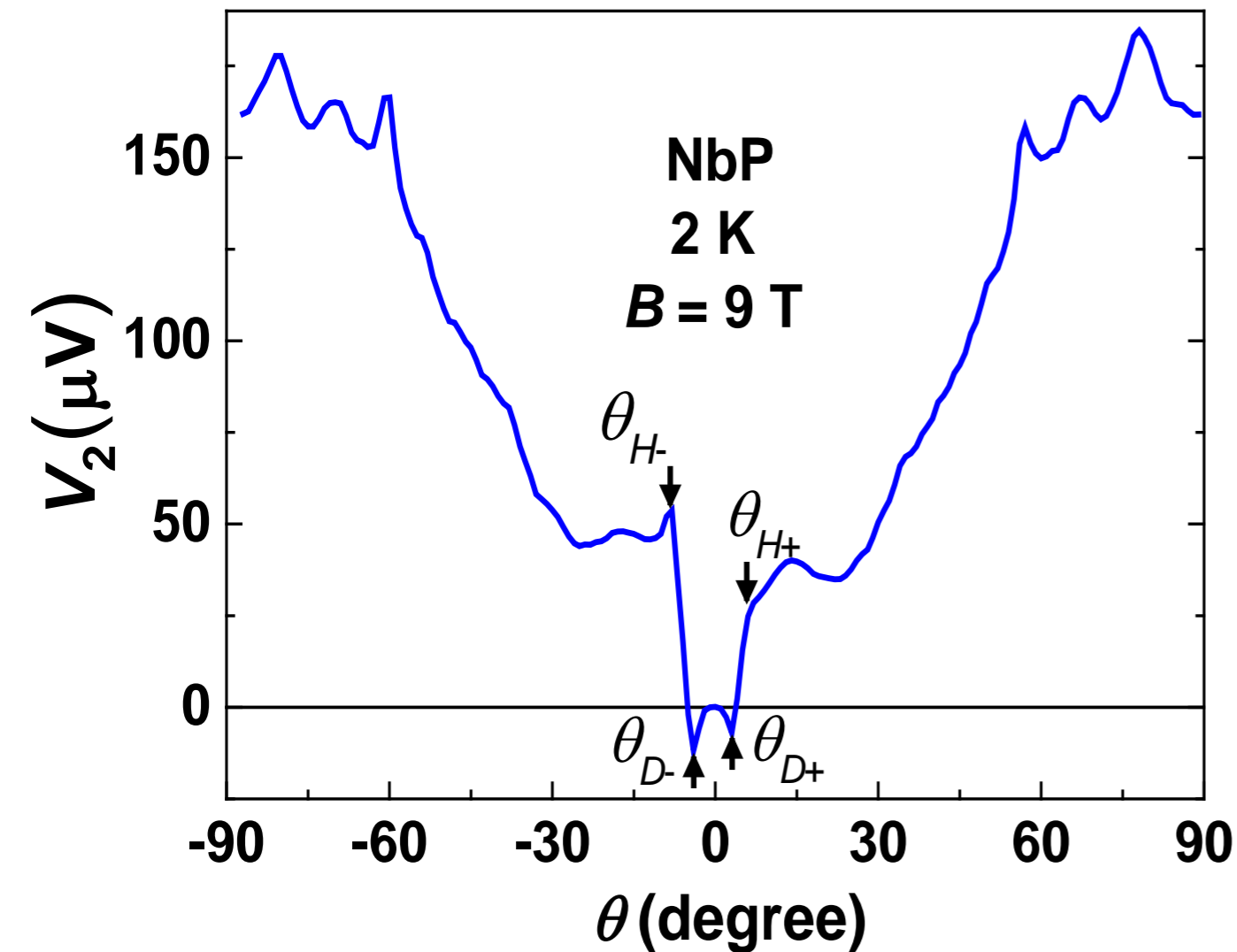


# Potential distribution for tilted magnetic field



Current rotates with the magnetic field

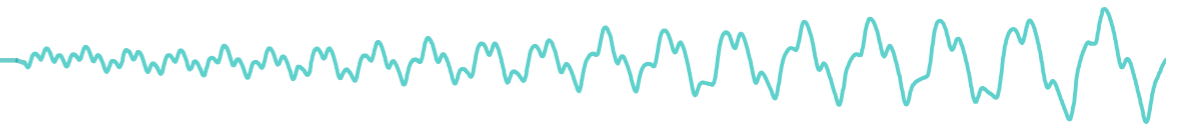
# Geometric determination of dip and hump angles



Good agreement between the angles observed in the experiment and the angles expected from the geometry.

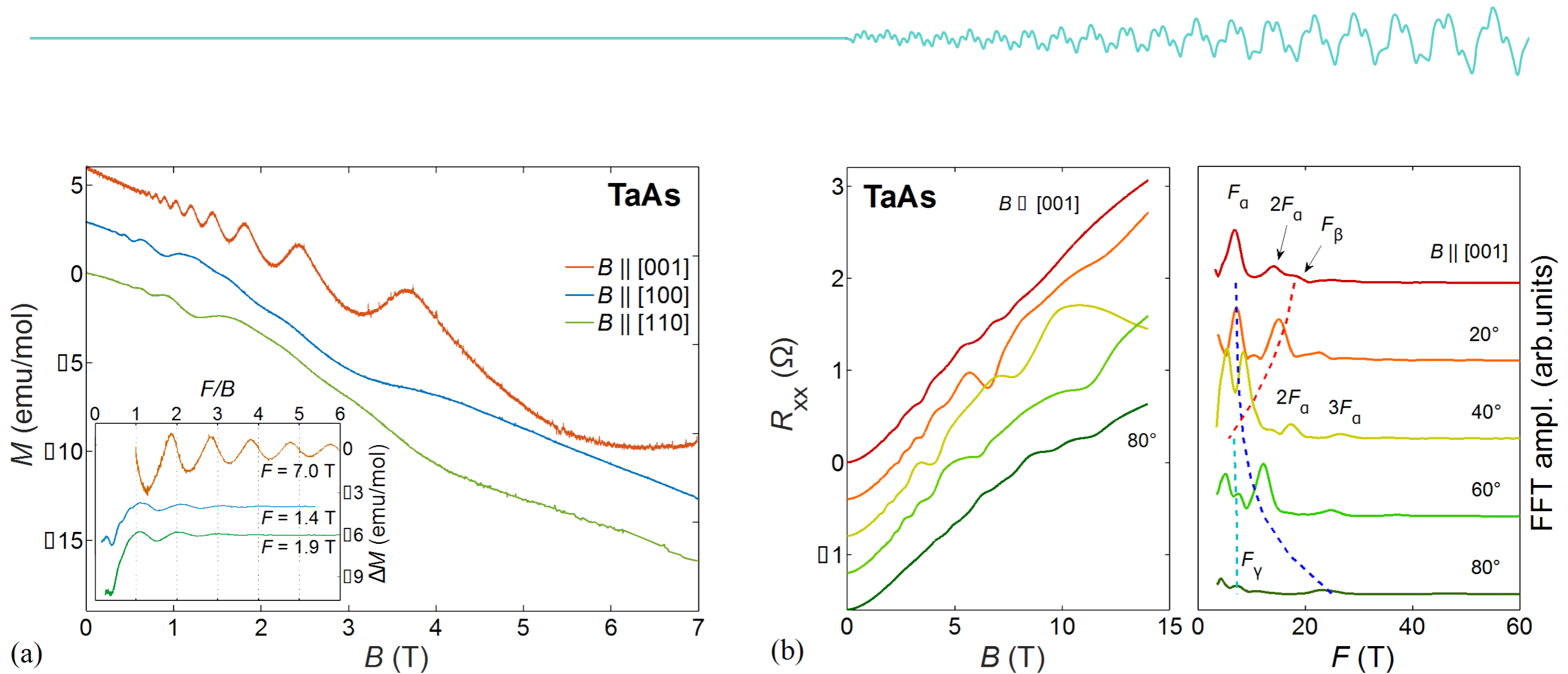
# Chiral anomaly?

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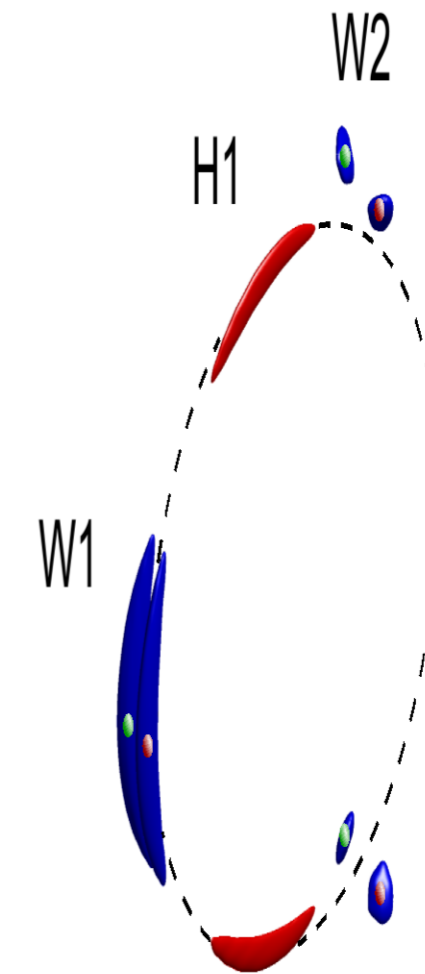
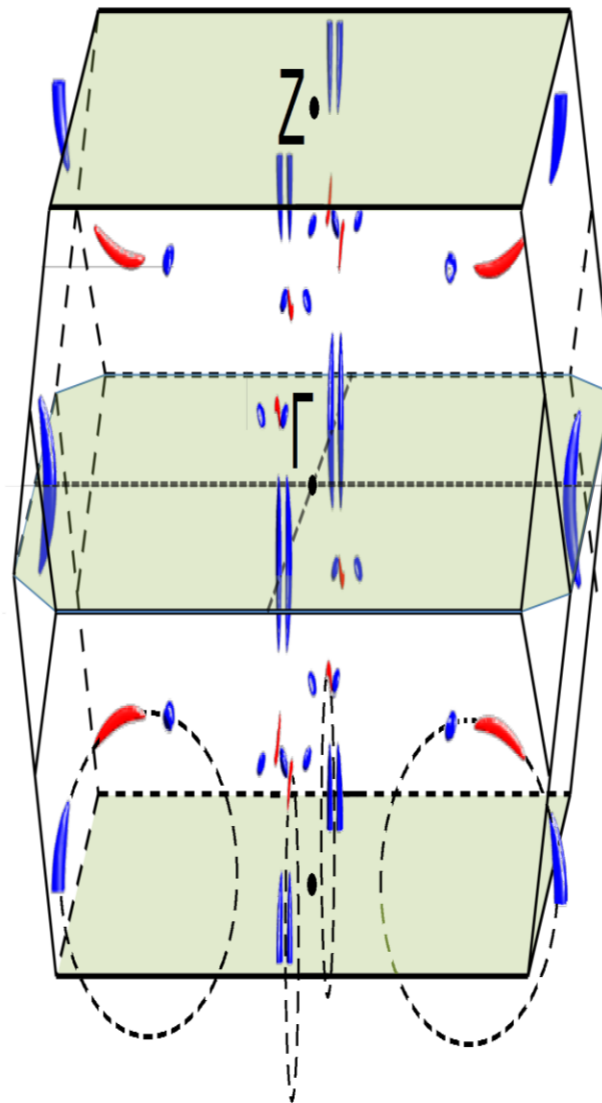
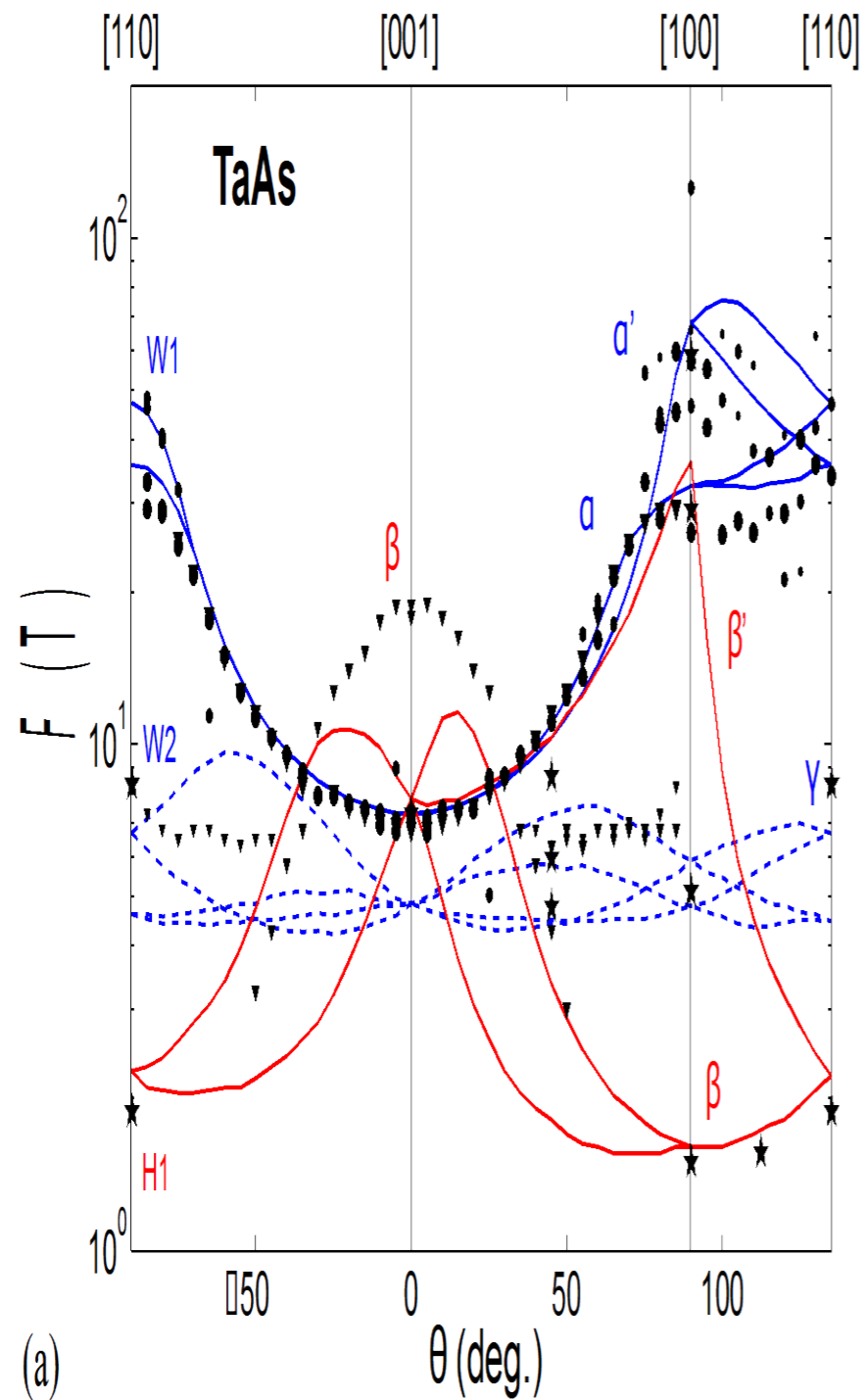
- Current jetting is a general phenomenon appearing in longitudinal MR measurements when the resistance anisotropy changes in field, even for low anisotropies (low fields or high temperature)
- Explains naturally the field dependence of the measured signal (small hump for low fields, reduction of voltage)
- Explains naturally the angle dependence ( $\neq \mathbf{E} \cdot \mathbf{B}$ )
- Measurements of longitudinal MR have to be carefully checked in order to exclude the current jetting
- Effect of chiral anomaly might exist but we need better measurements

# TaAs – Quantum oscillations



- Diamagnetic, strong QO in all directions
- Two new oscillation frequencies compared to other studies

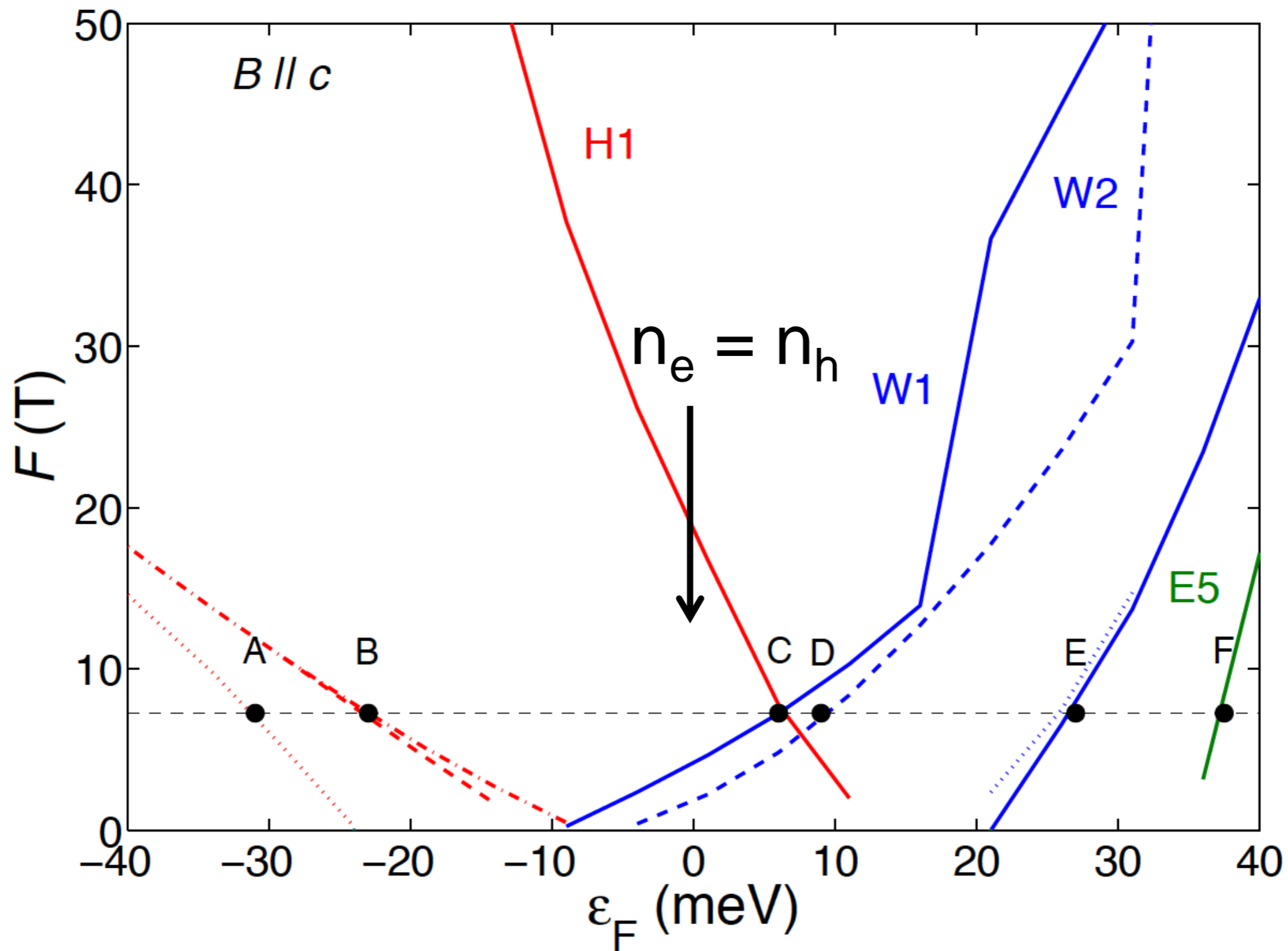
# Angular dependence



How do we determine the Fermi energy?

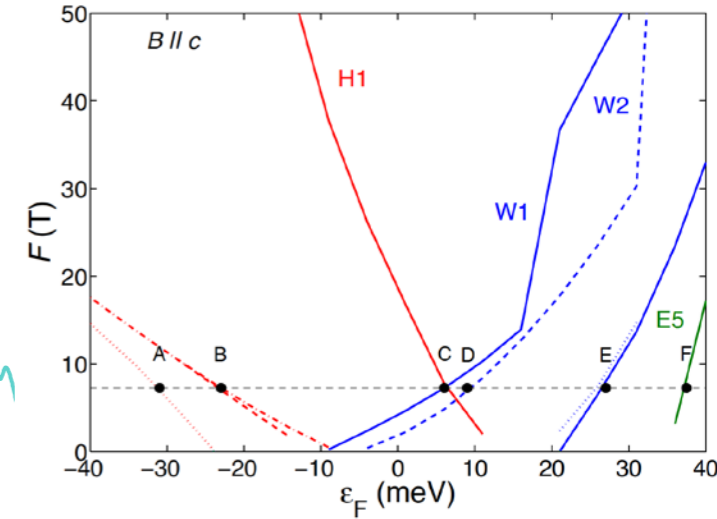


# TaAs – oscillation frequency as a function of the Fermi energy

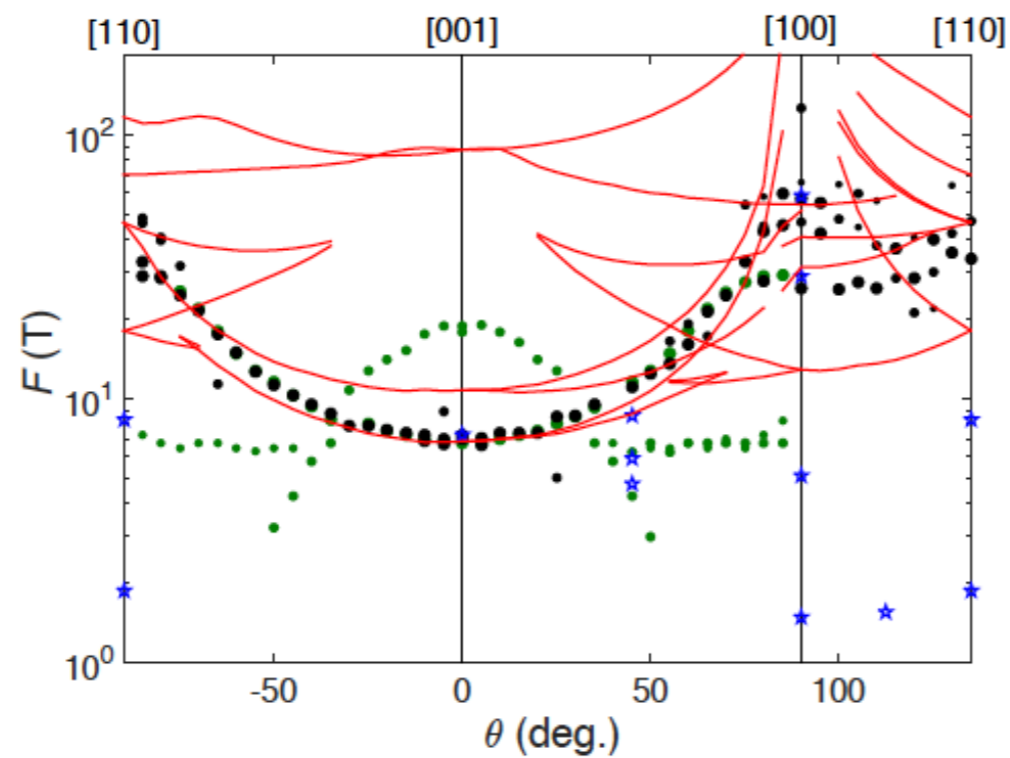




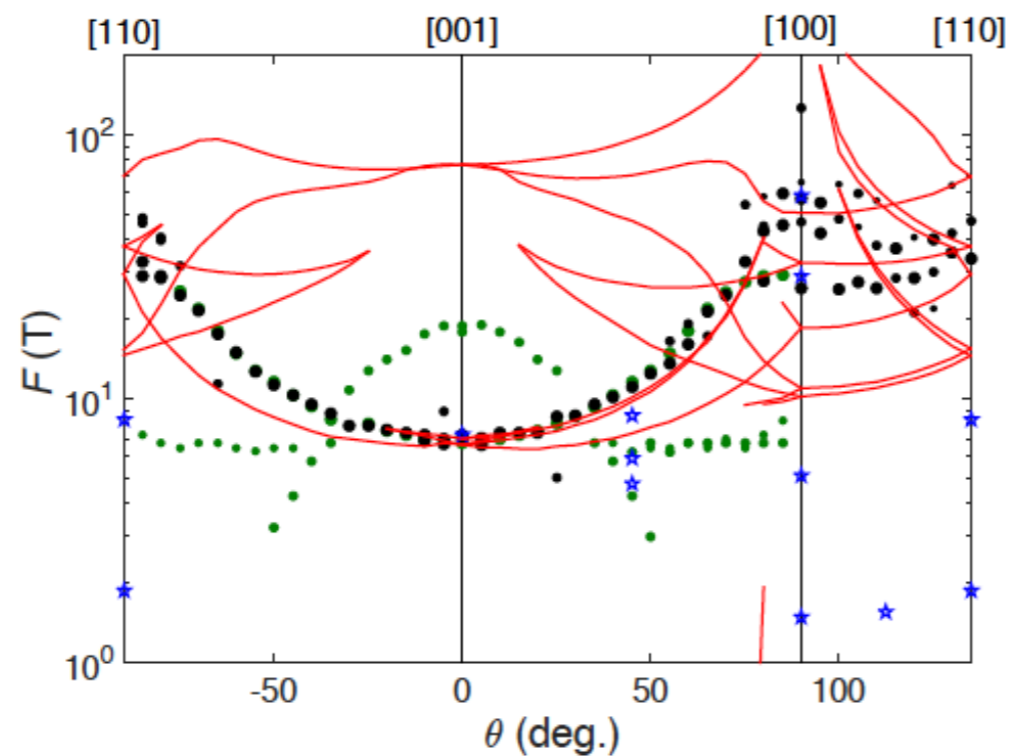
# TaAs



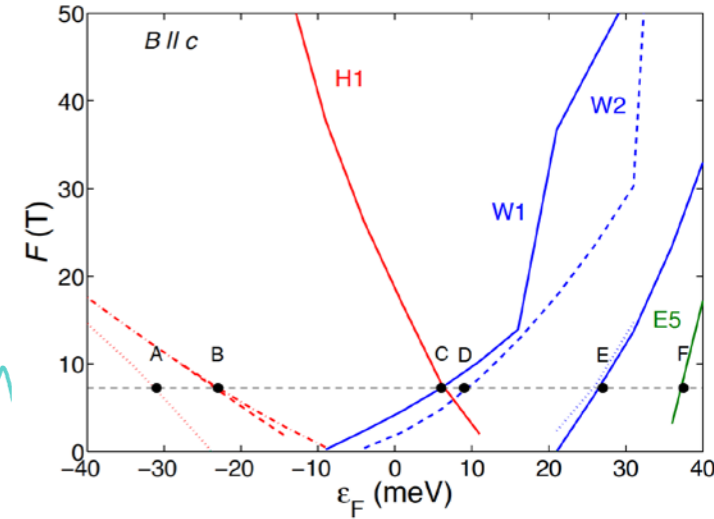
**A**  
-32 meV



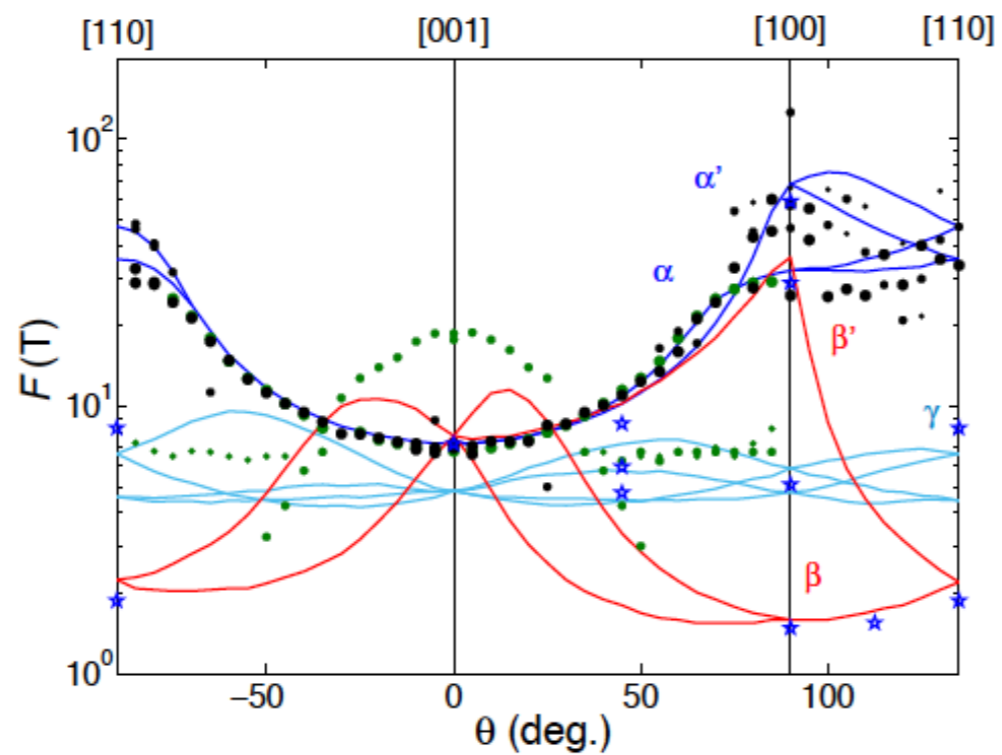
**B**  
-23 meV



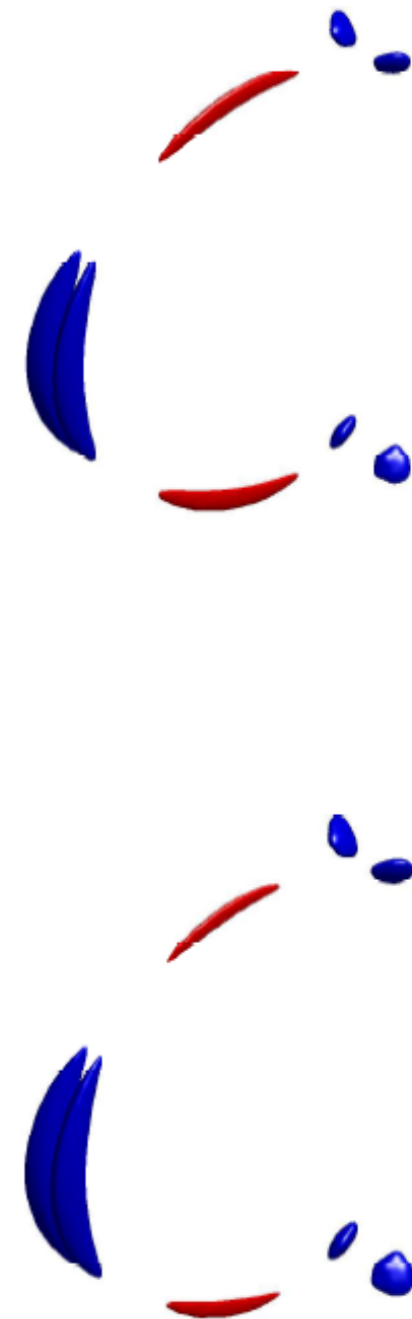
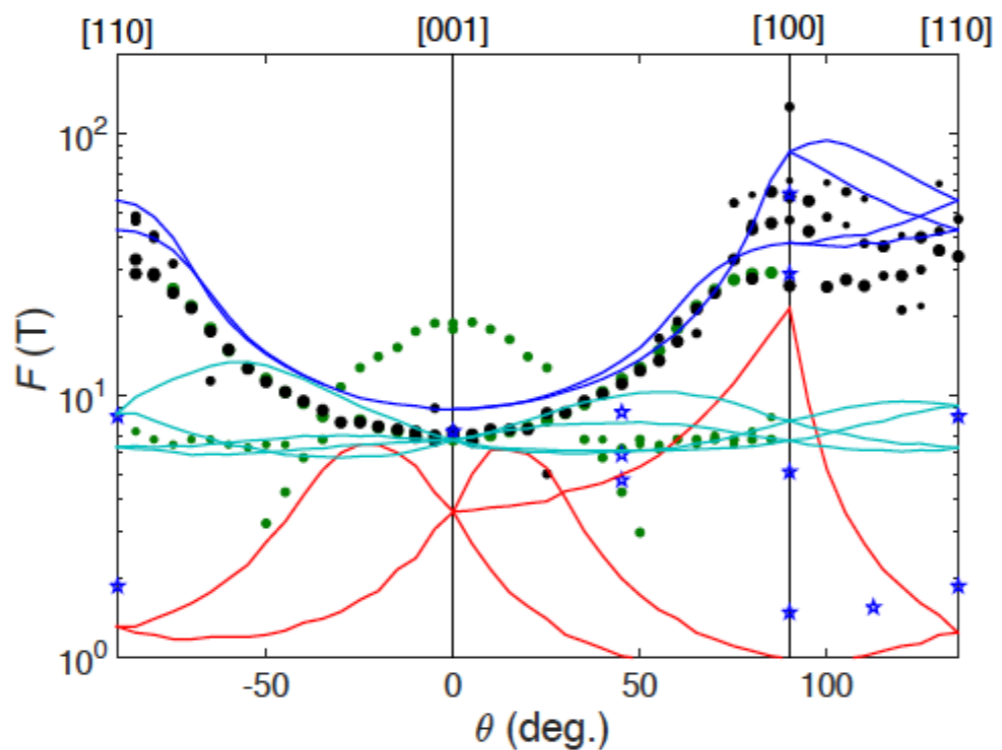
# TaAs



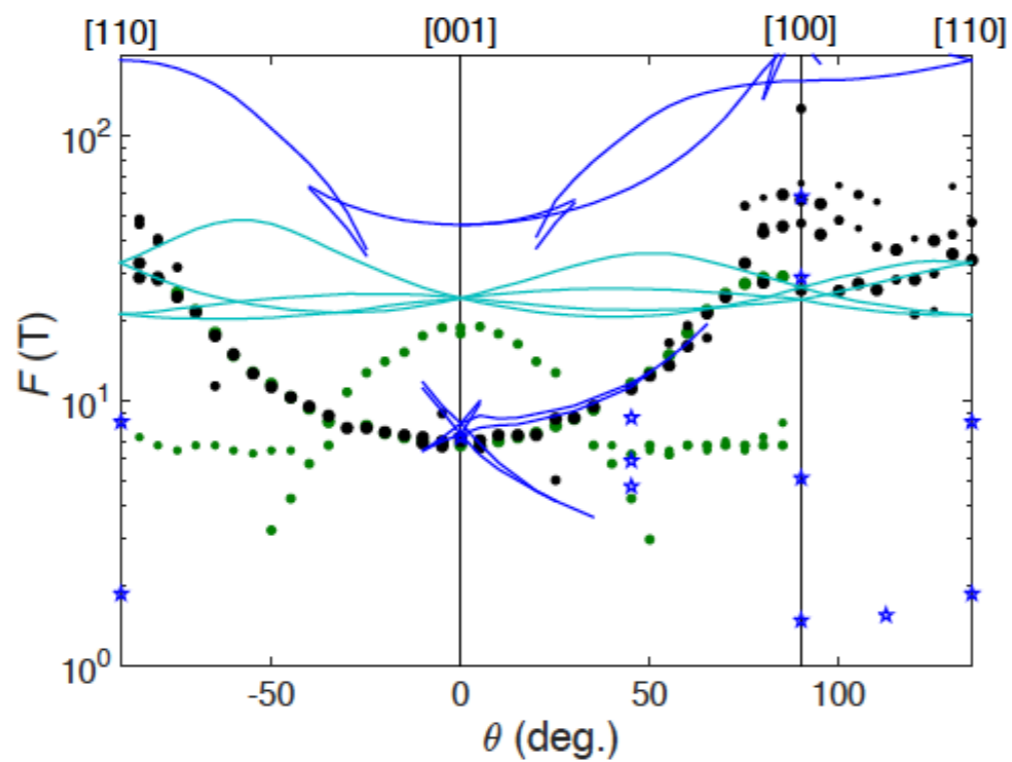
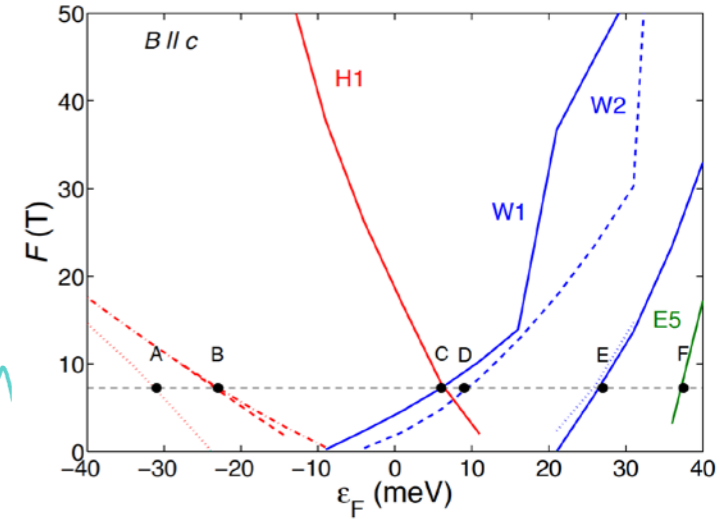
**C**  
+6 meV



**D**  
+9 meV



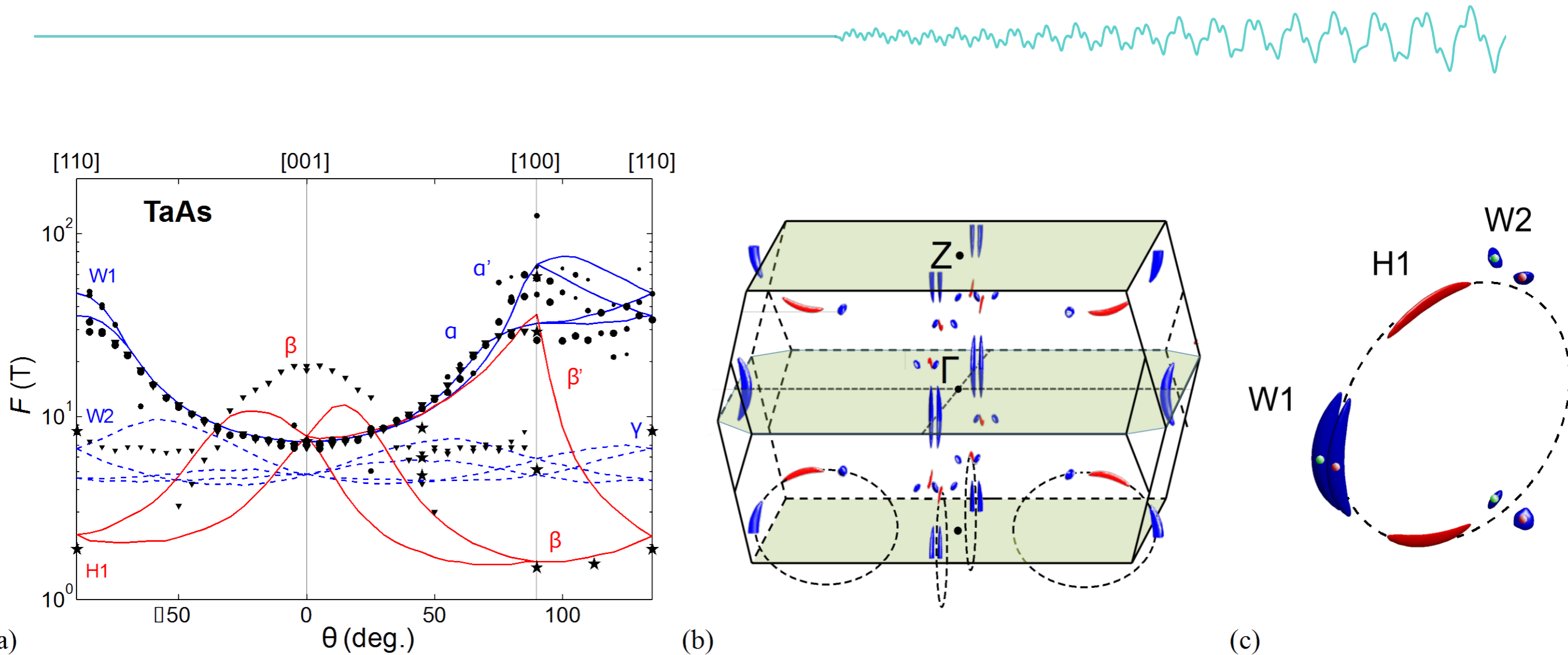
# TaAs



**E**  
+27 meV



# TaAs - Fermi surface



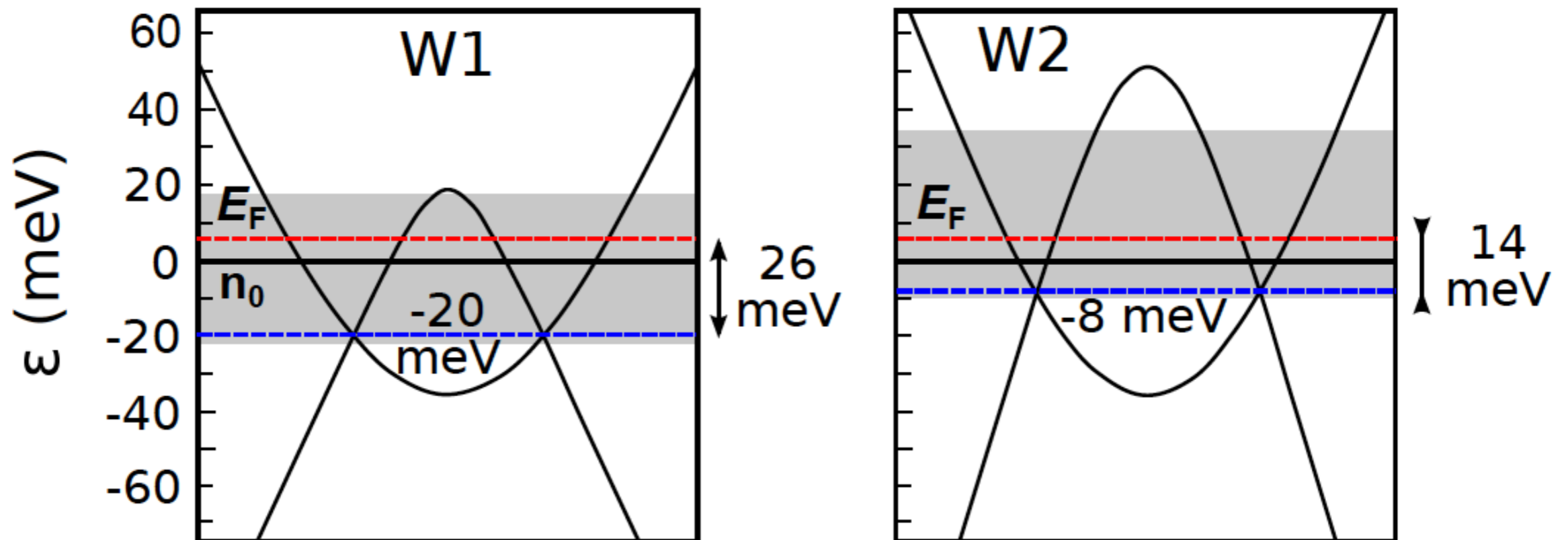
3 Fermi surfaces detected

First experimental evidence for separate

Fermi surface pockets around  $W1$  and  $W2$

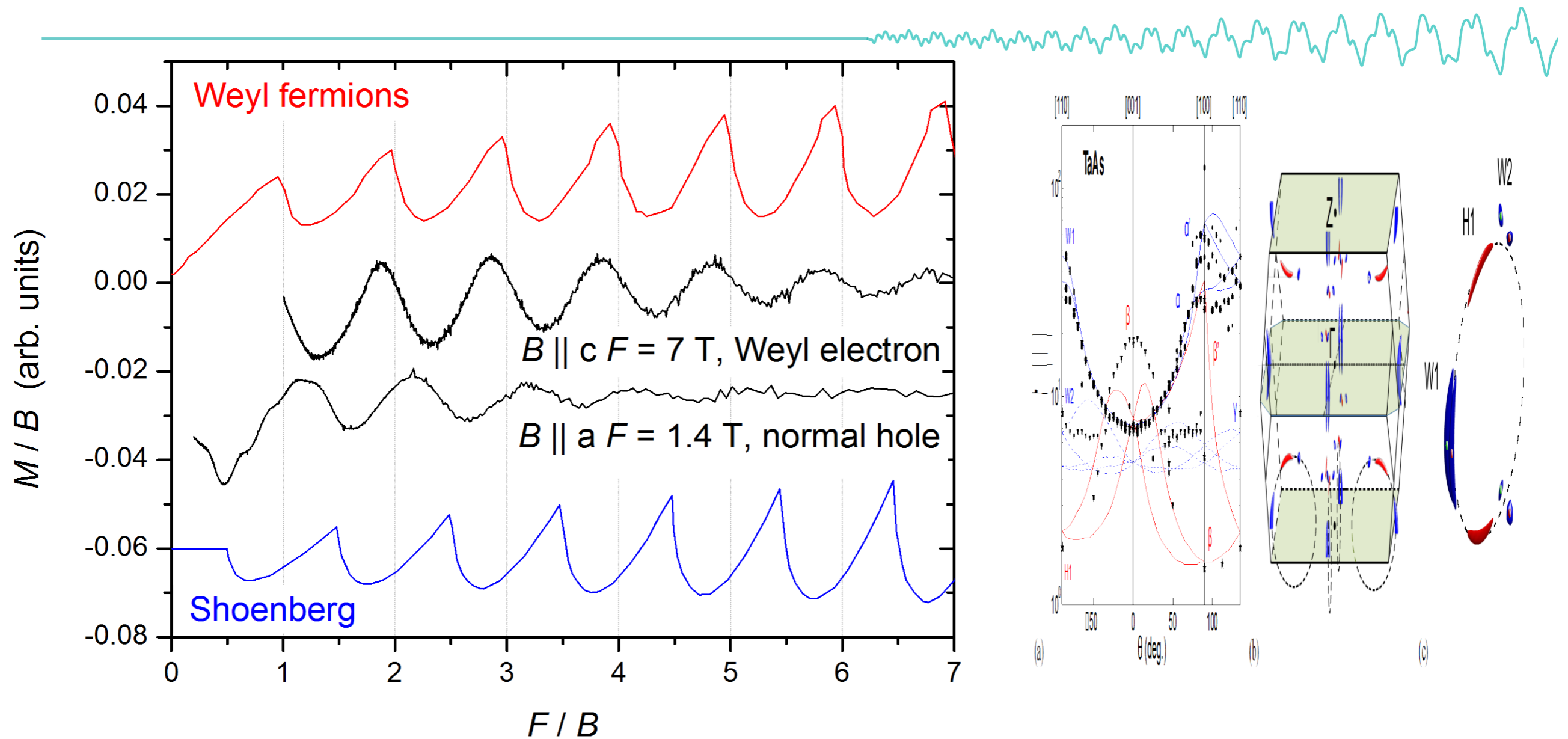
Weyl points

# TaAs - band structure



Overlap of energy range for independent FS pockets for W1 and W2  
Chirality well defined

# Band-resolved Berry phase

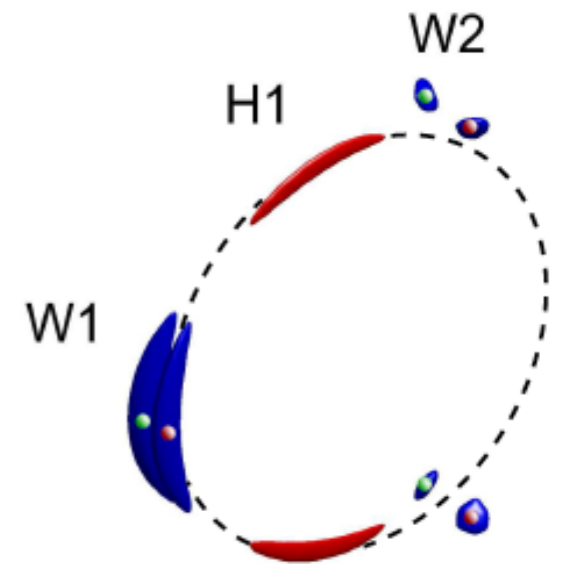


Phase shift between chiral and non-chiral oscillations

First thermodynamic evidence for Berry phase

# TaAs

- Independent Weyl pockets
- Well-defined chirality
- Weyl nodes close to the Fermi energy





# Summary

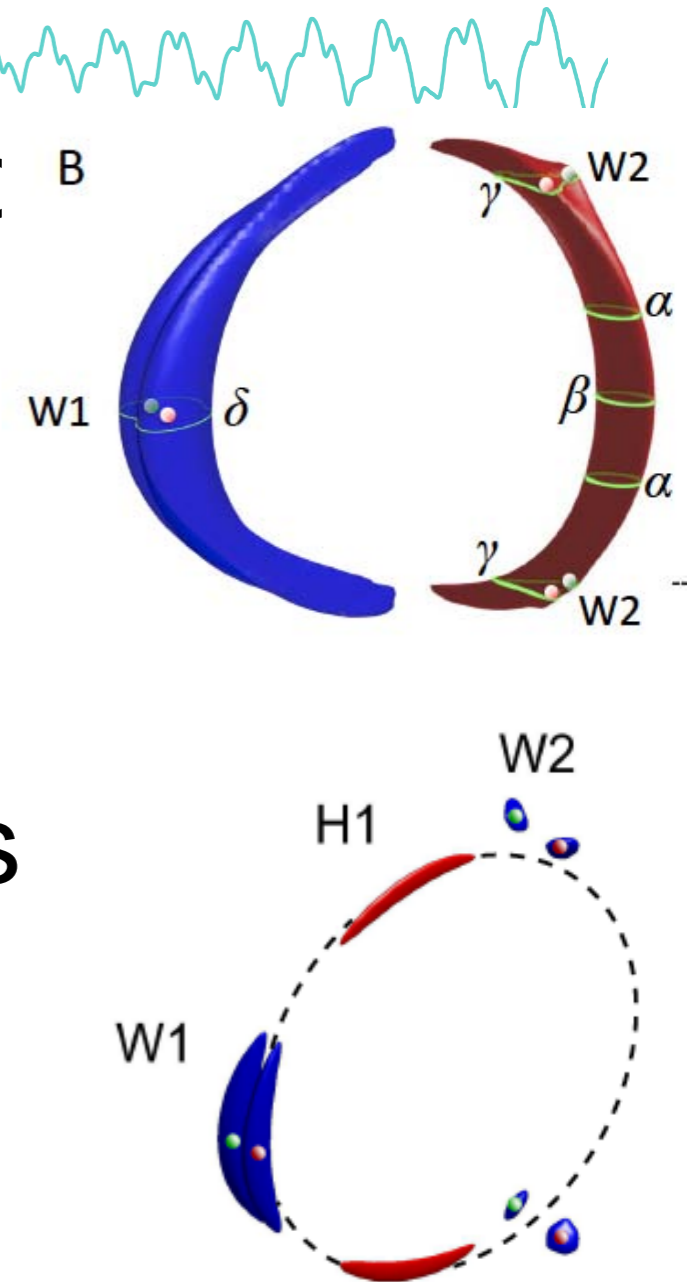
- TaP: Pairs of Weyl nodes embedded in big Fermi surfaces
- TaAs: Separate Weyl pockets, well-defined chirality
- Berry phase in chiral pockets in TaAs

Arnold *et al.* Nat. Comm. 2016

Arnold *et al.* PRL 2016

- Watch out for current jetting!

Dos Reis *et al.* New J. Phys. 2016





**Thank you for your attention!**