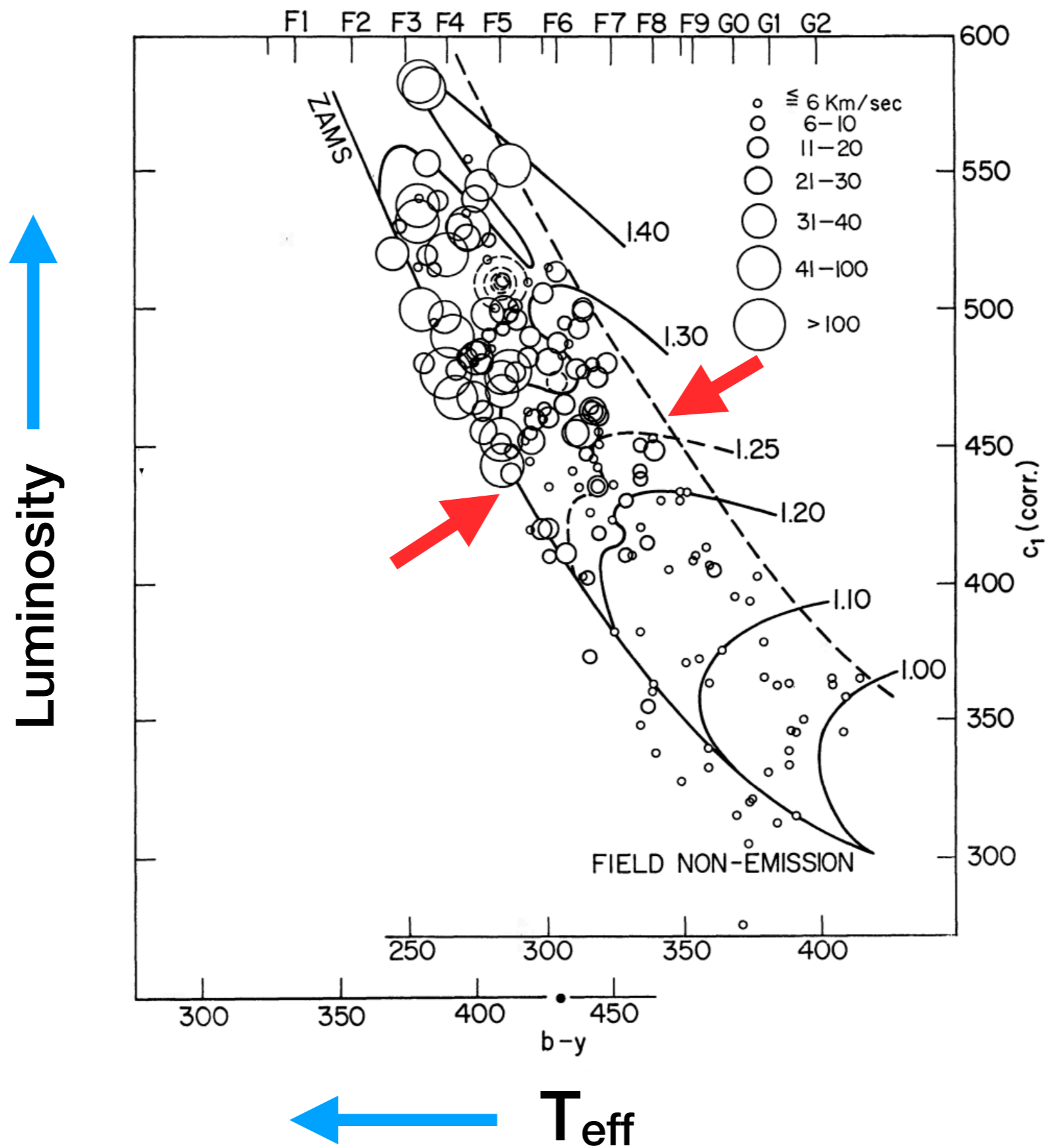


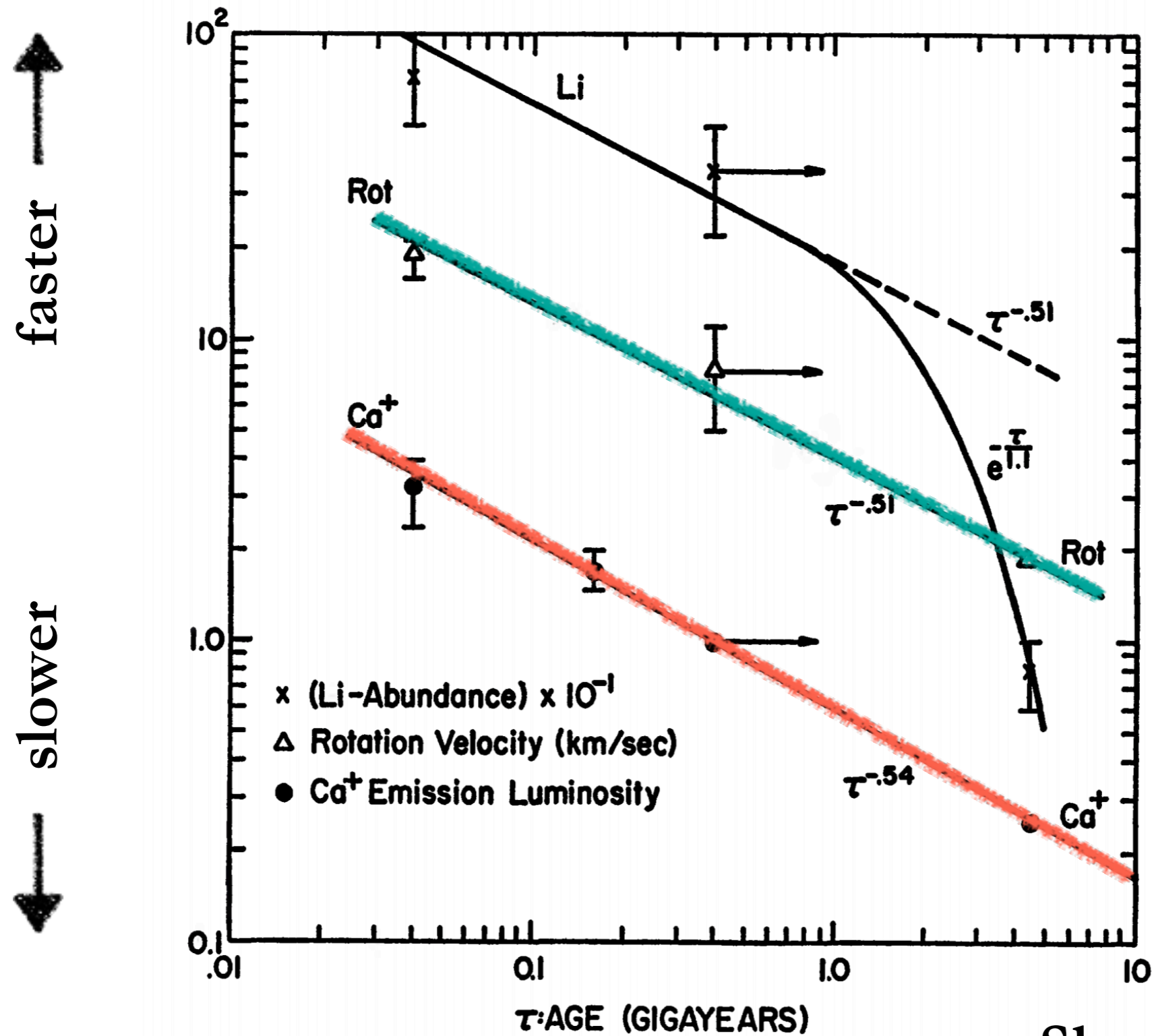


Rotation in Low-mass stars: Physics, Patterns, and Puzzles

Jennifer van Saders
Assistant Astronomer
Institute for Astronomy
University of Hawai'i at Mānoa



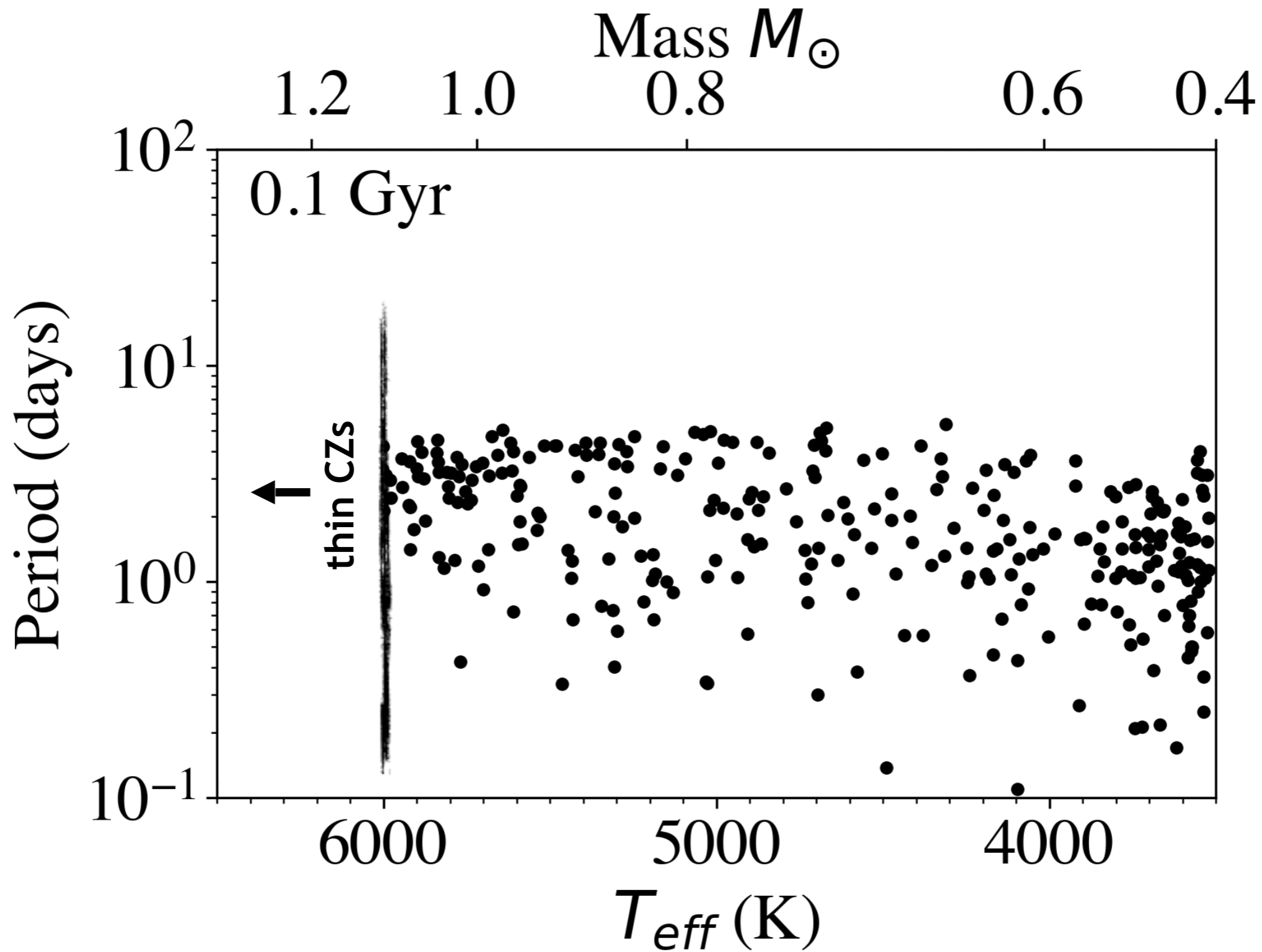
Skumanich laws

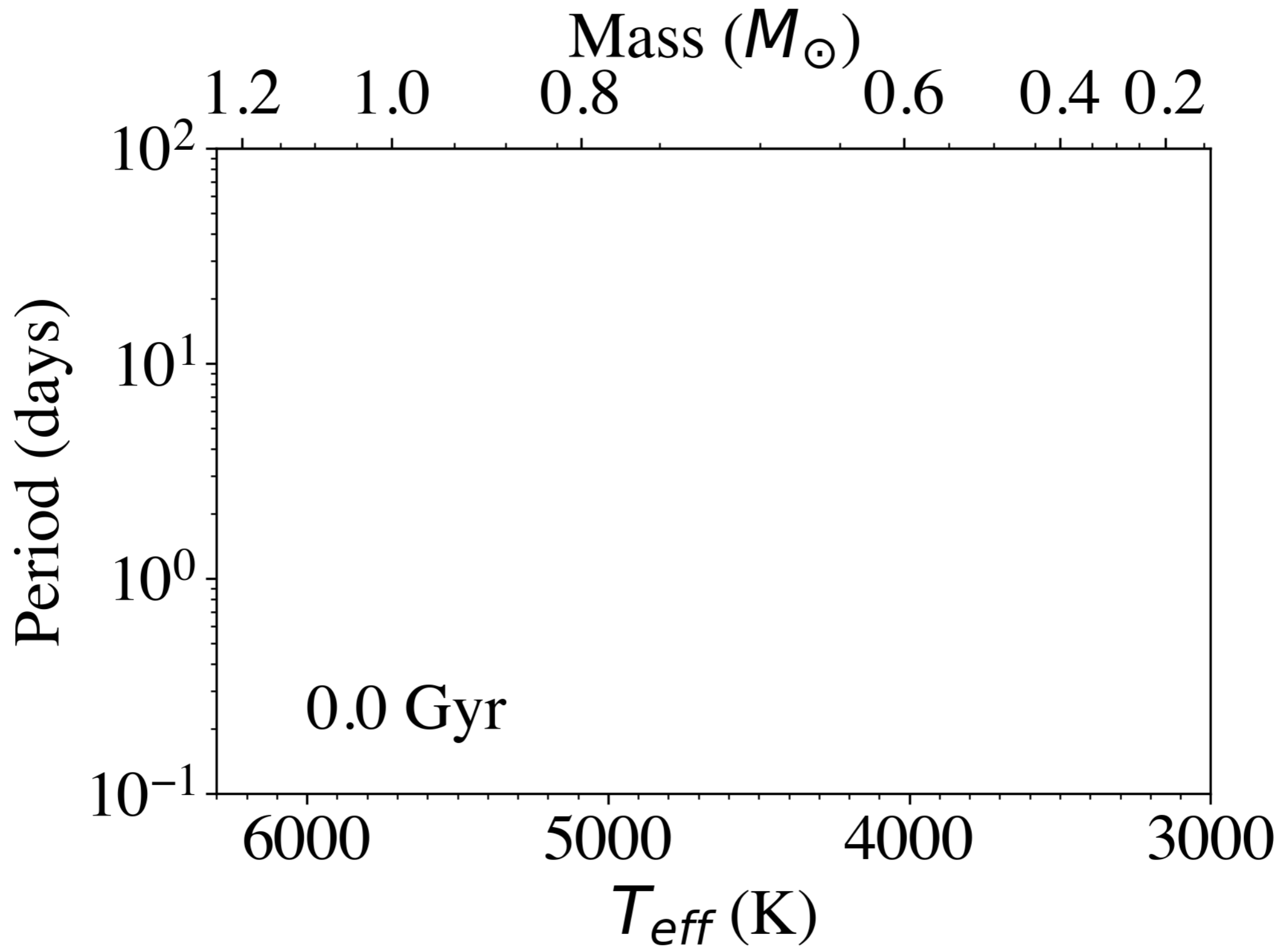


$$\Rightarrow \frac{dJ}{dt} \propto \Omega^3$$

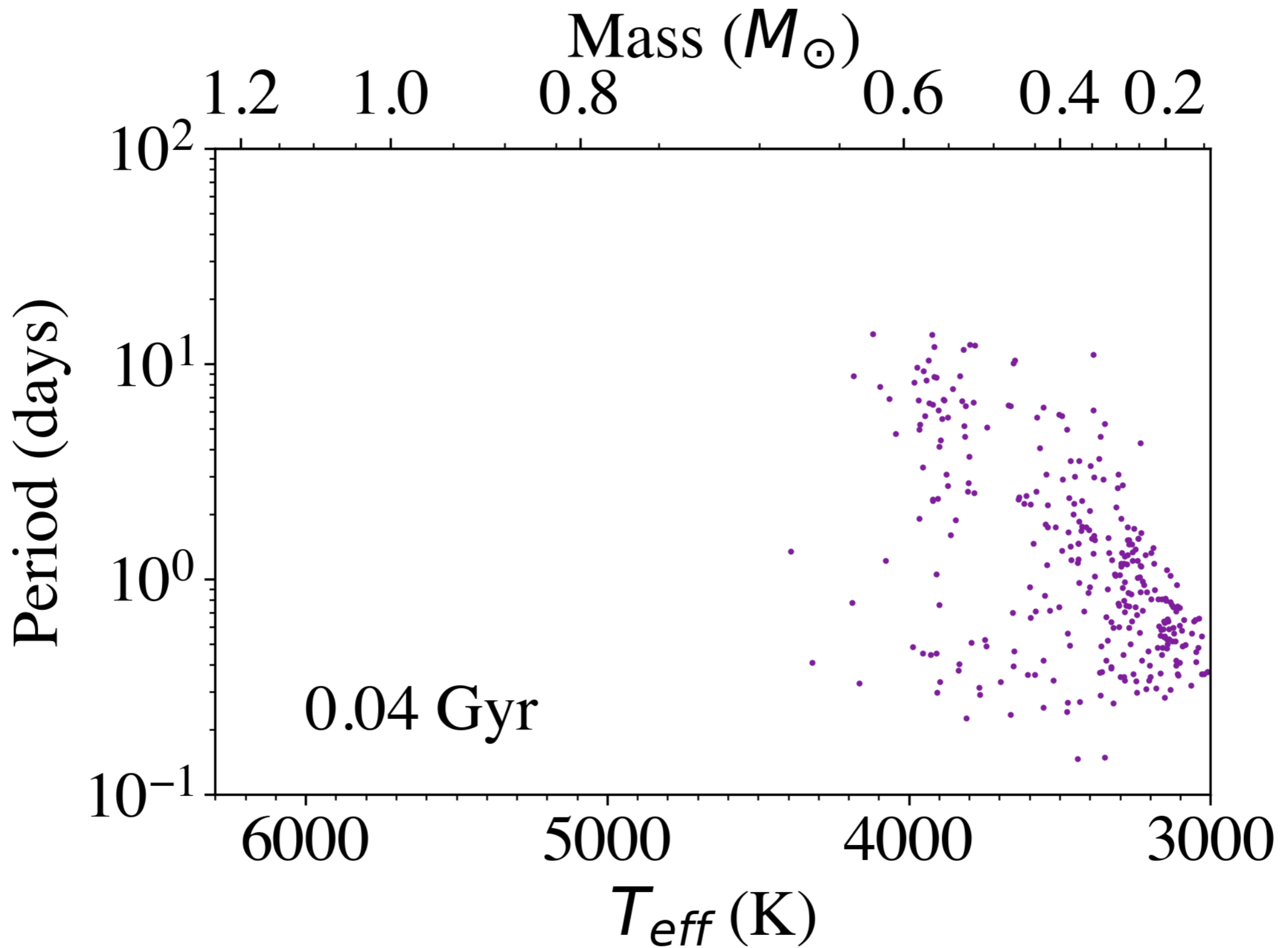
Skumanich 1972

A model of stellar spin down

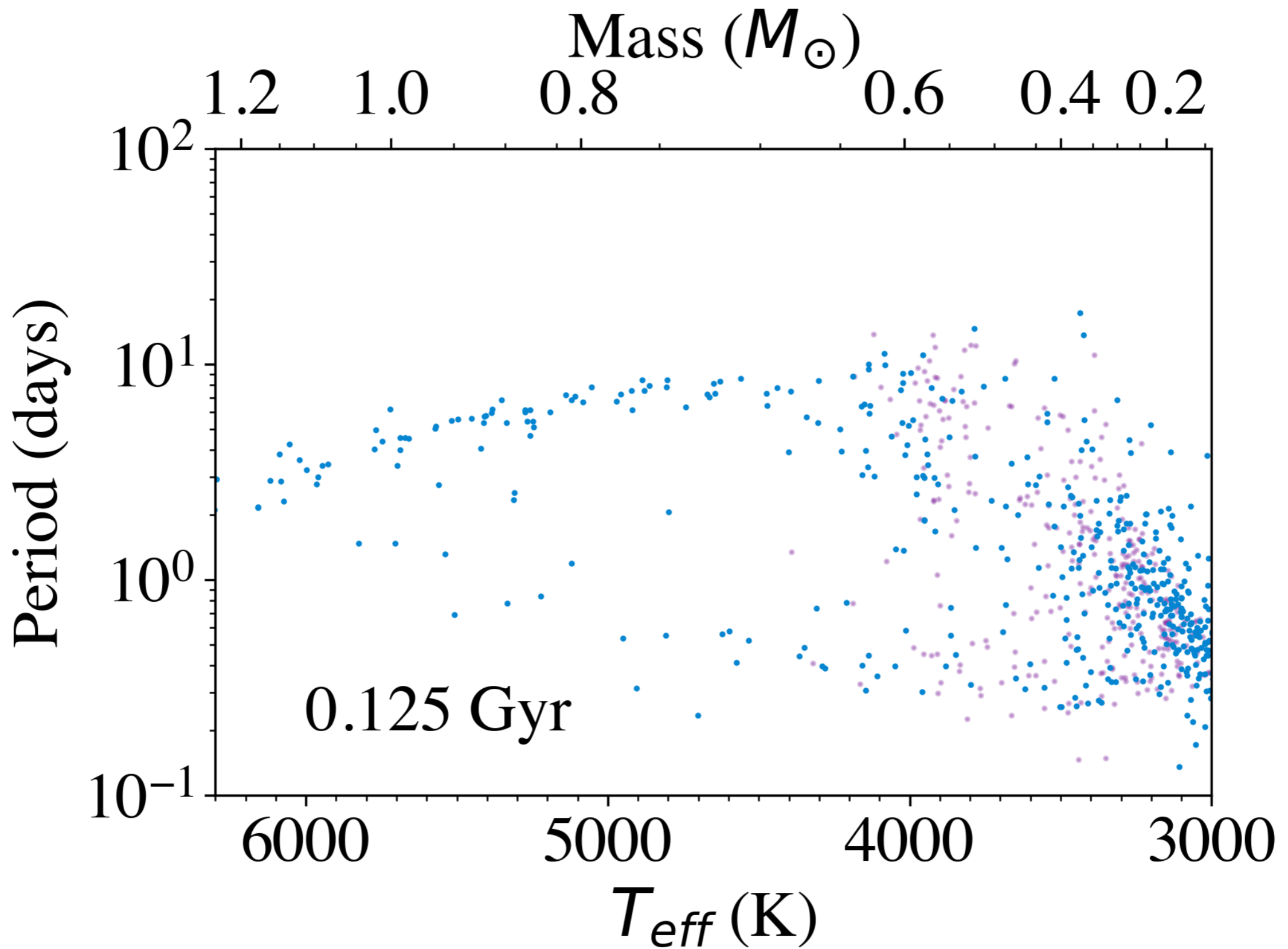




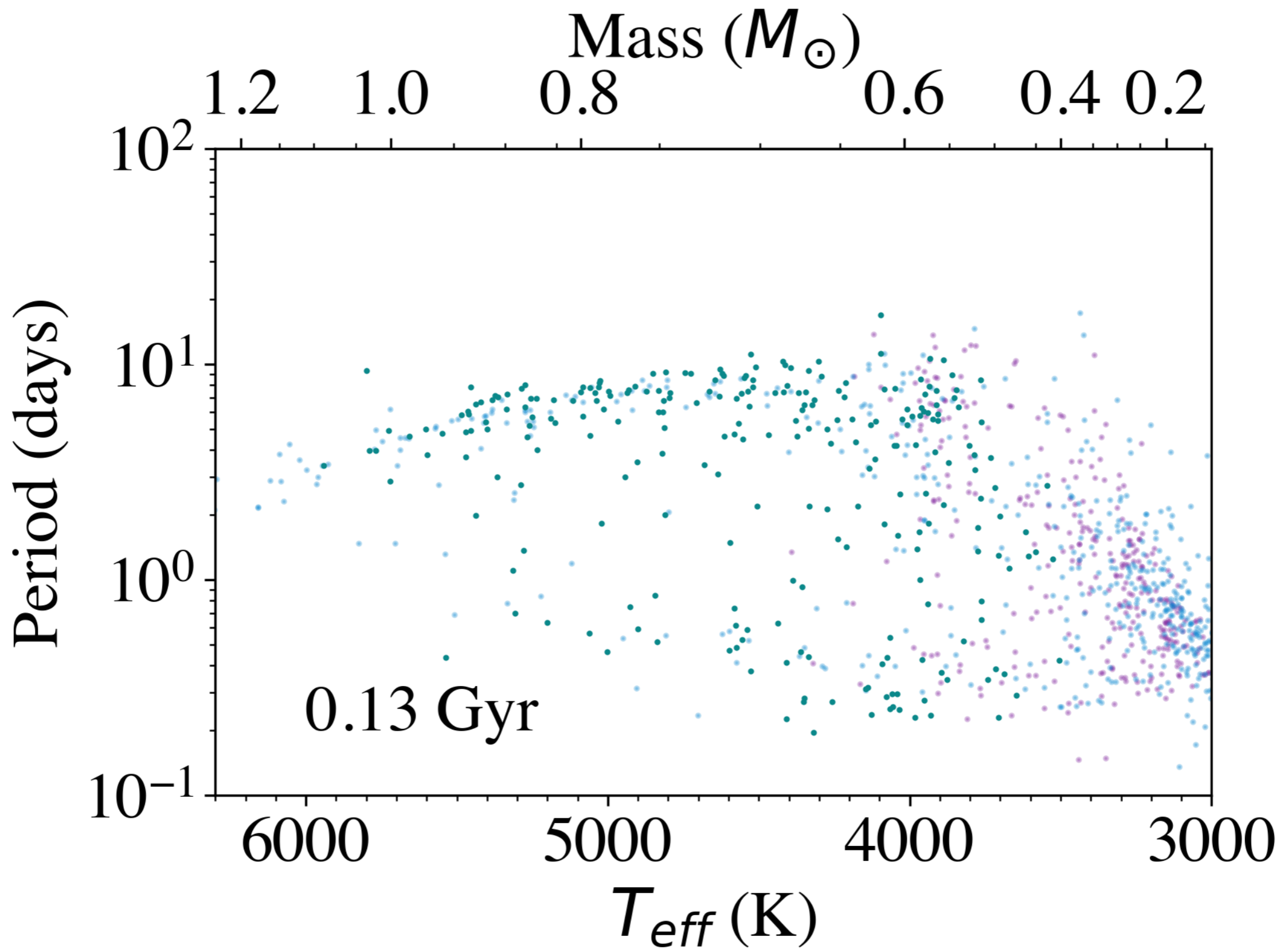
NGC2547 (Irwin et al. 2008), Pleiades (Rebull et al. 2016), M50 (Irwin et al. 2009), M37 (Hartman et al. 2009, Praesepe (Rebull et al. 2017), NGC 6811 (Curtis et al. 2019, Meibom et al. 2011), NGC 6819 (Meibom et al. 2015), Rup147 (Curtis et al. 2020), M67 (Barnes et al. 2016, Esselstein 2016)



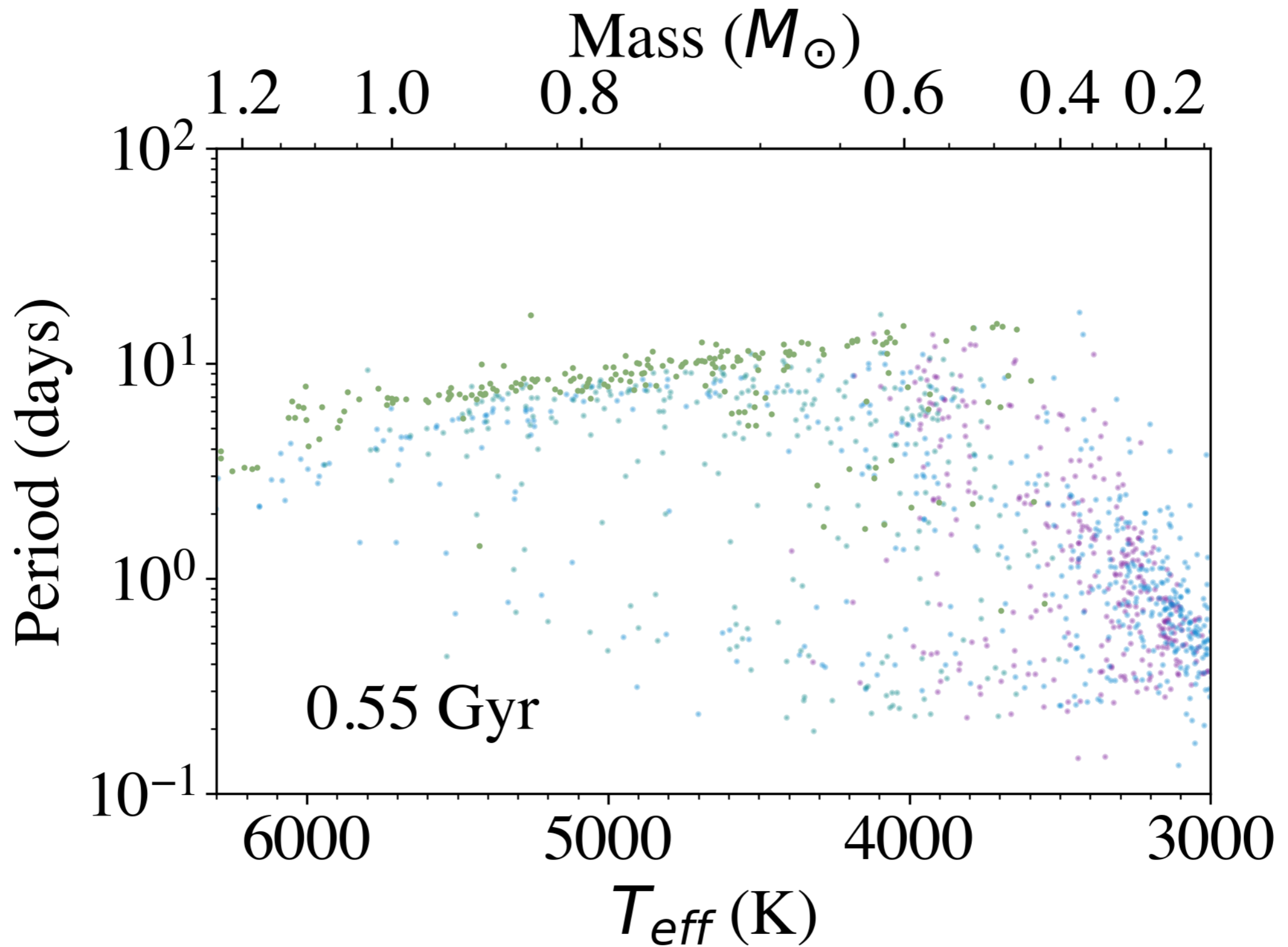
NGC2547 (Irwin et al. 2008), Pleiades (Rebull et al. 2016), M50 (Irwin et al. 2009), M37 (Hartman et al. 2009, Praesepe (Rebull et al. 2017), NGC 6811 (Curtis et al. 2019, Meibom et al. 2011), NGC 6819 (Meibom et al. 2015), Rup147 (Curtis et al. 2020), M67 (Barnes et al. 2016, Esselstein 2016)



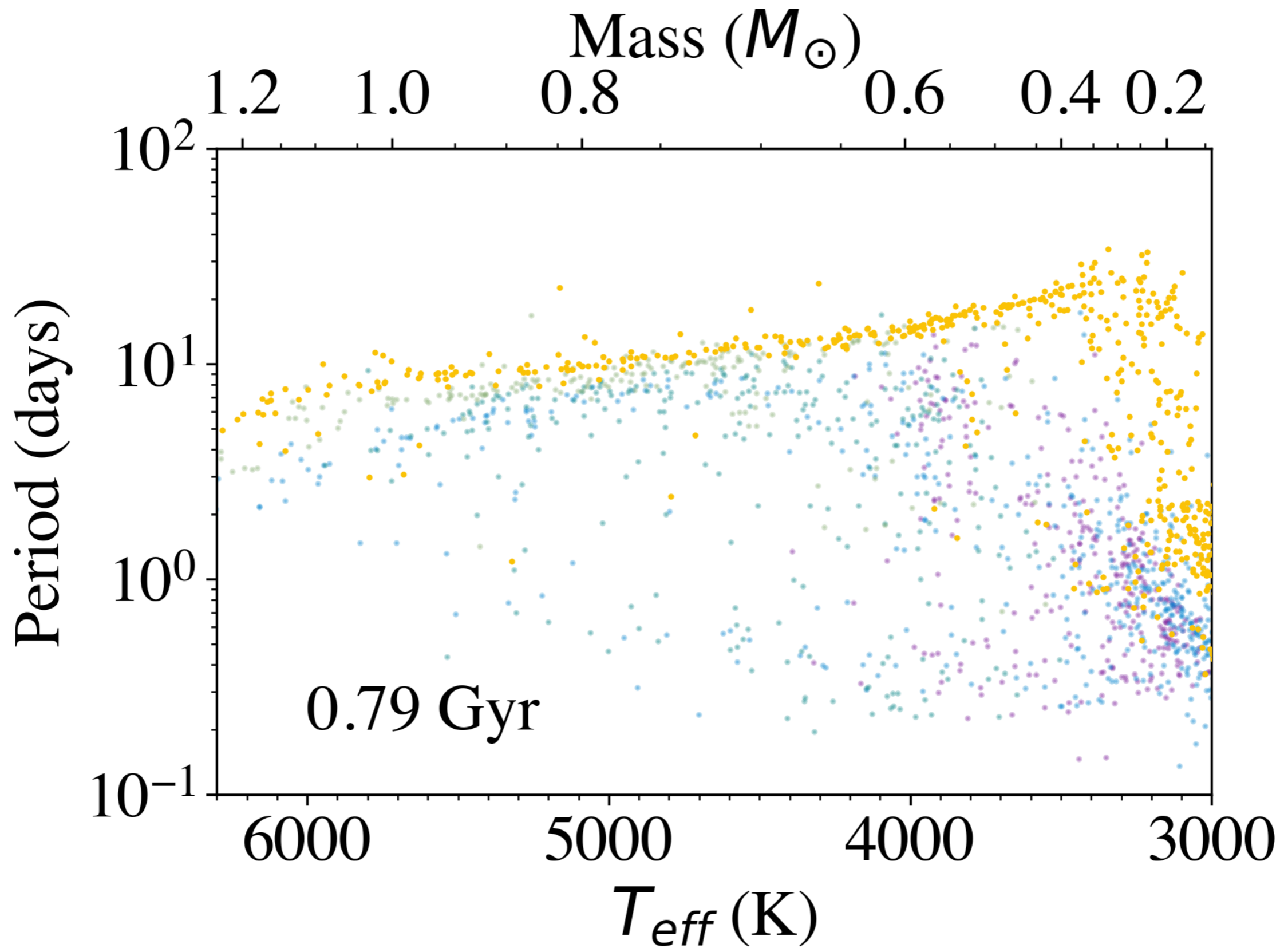
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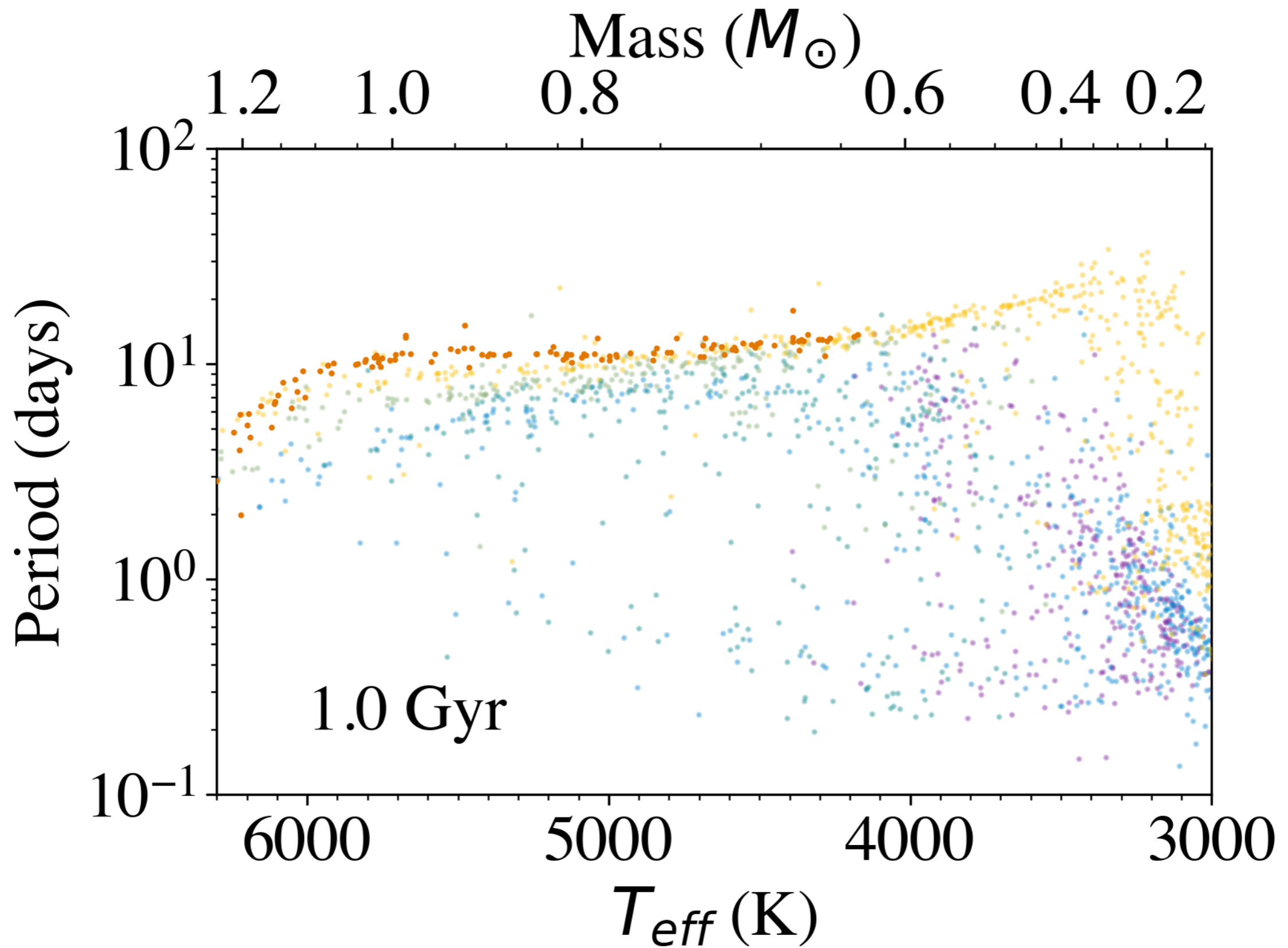
NGC2547 (Irwin et al. 2008), Pleiades (Rebull et al. 2016), M50 (Irwin et al. 2009), M37 (Hartman et al. 2009, Praesepe (Rebull et al. 2017), NGC 6811 (Curtis et al. 2019, Meibom et al. 2011), NGC 6819 (Meibom et al. 2015), Rup147 (Curtis et al. 2020), M67 (Barnes et al. 2016, Esselstein 2016)



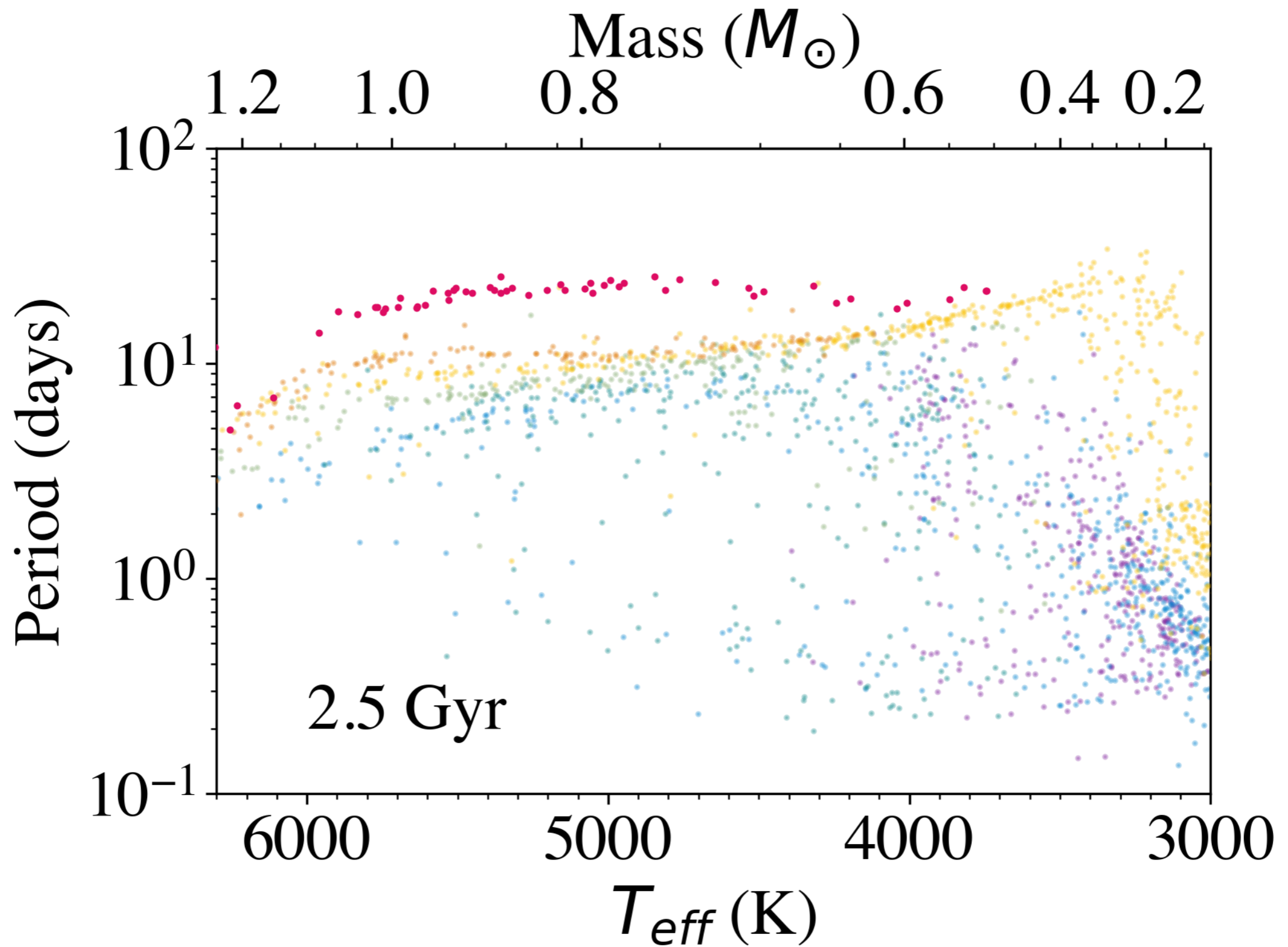
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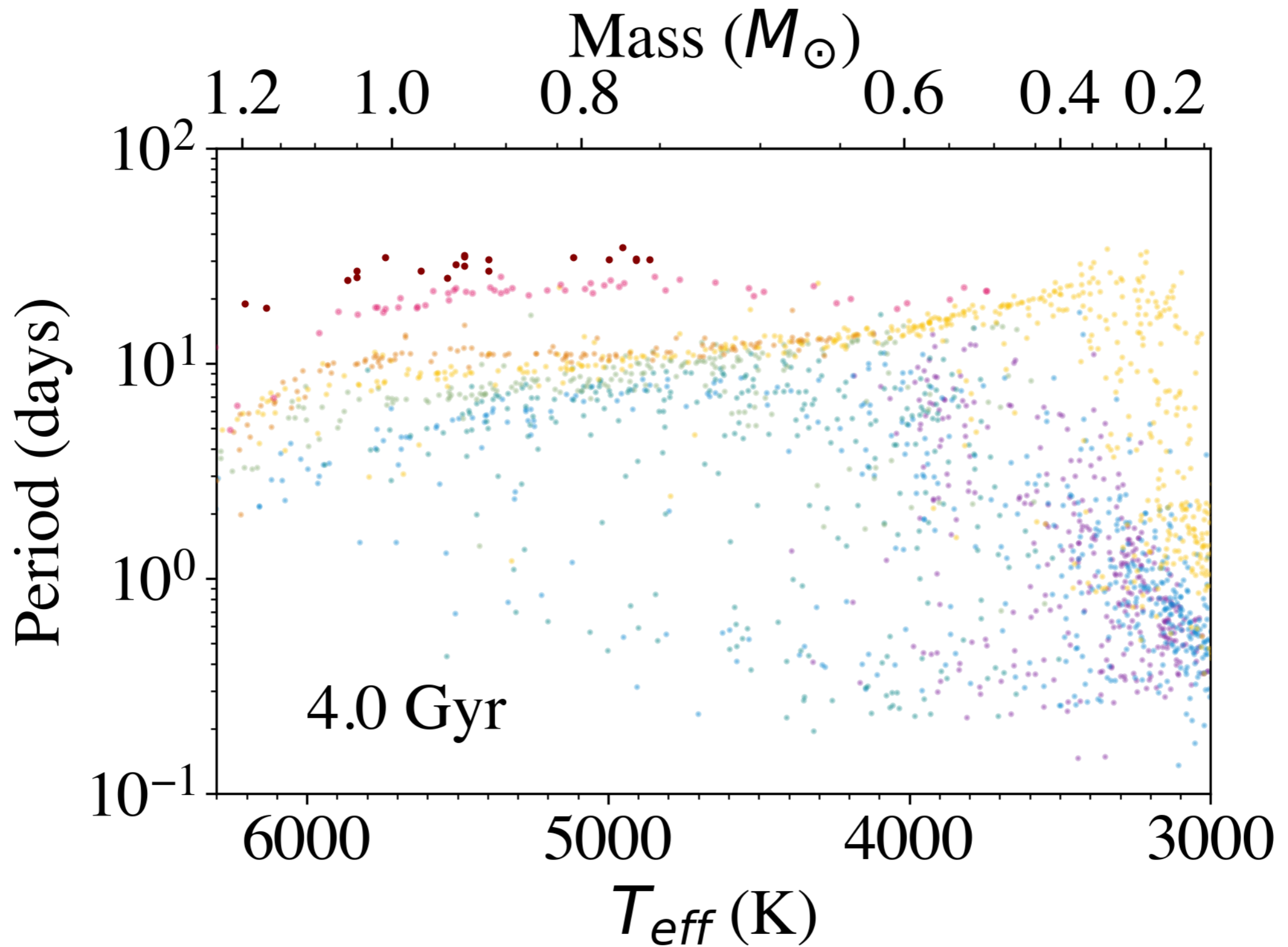
NGC2547 (Irwin et al. 2008), Pleiades (Rebull et al. 2016), M50 (Irwin et al. 2009), M37 (Hartman et al. 2009, Praesepe (Rebull et al. 2017), NGC 6811 (Curtis et al. 2019, Meibom et al. 2011), NGC 6819 (Meibom et al. 2015), Rup147 (Curtis et al. 2020), M67 (Barnes et al. 2016, Esselstein 2016)



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Model Ingredients

- 1.) A description of initial conditions
- 2.) A description of magnetic braking at the stellar surface
- 3.) A description interior angular momentum transport

Model Ingredients

1.) A description of initial conditions

2.) A description of magnetic braking at the stellar surface

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Very young stars display a wide range of initial rotation periods

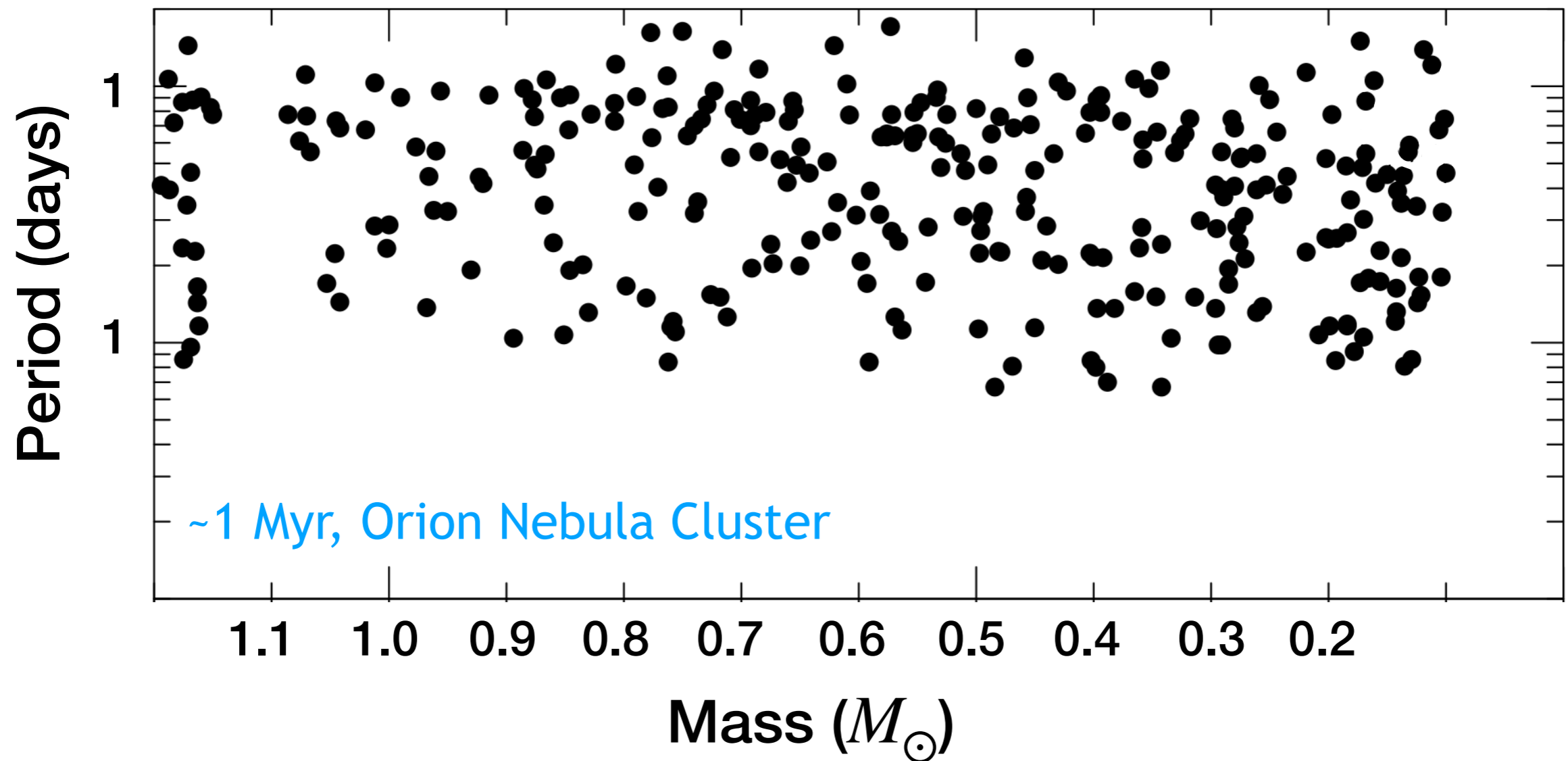


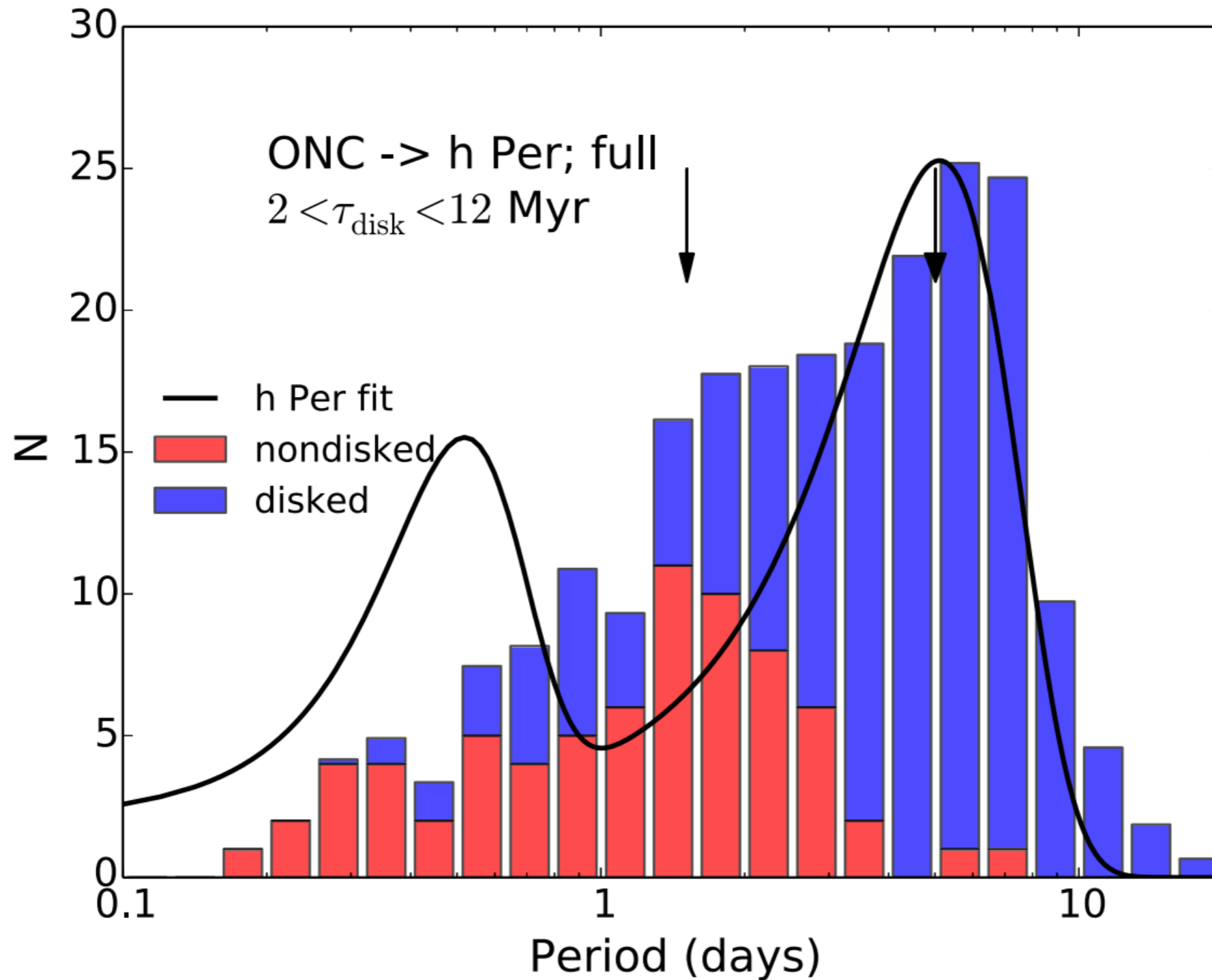
Fig from Bouvier et al. 2013
Data from Herbst et al. 2000

Problem #1

There may be real variance in the starting distributions of rotation periods that depends on environment

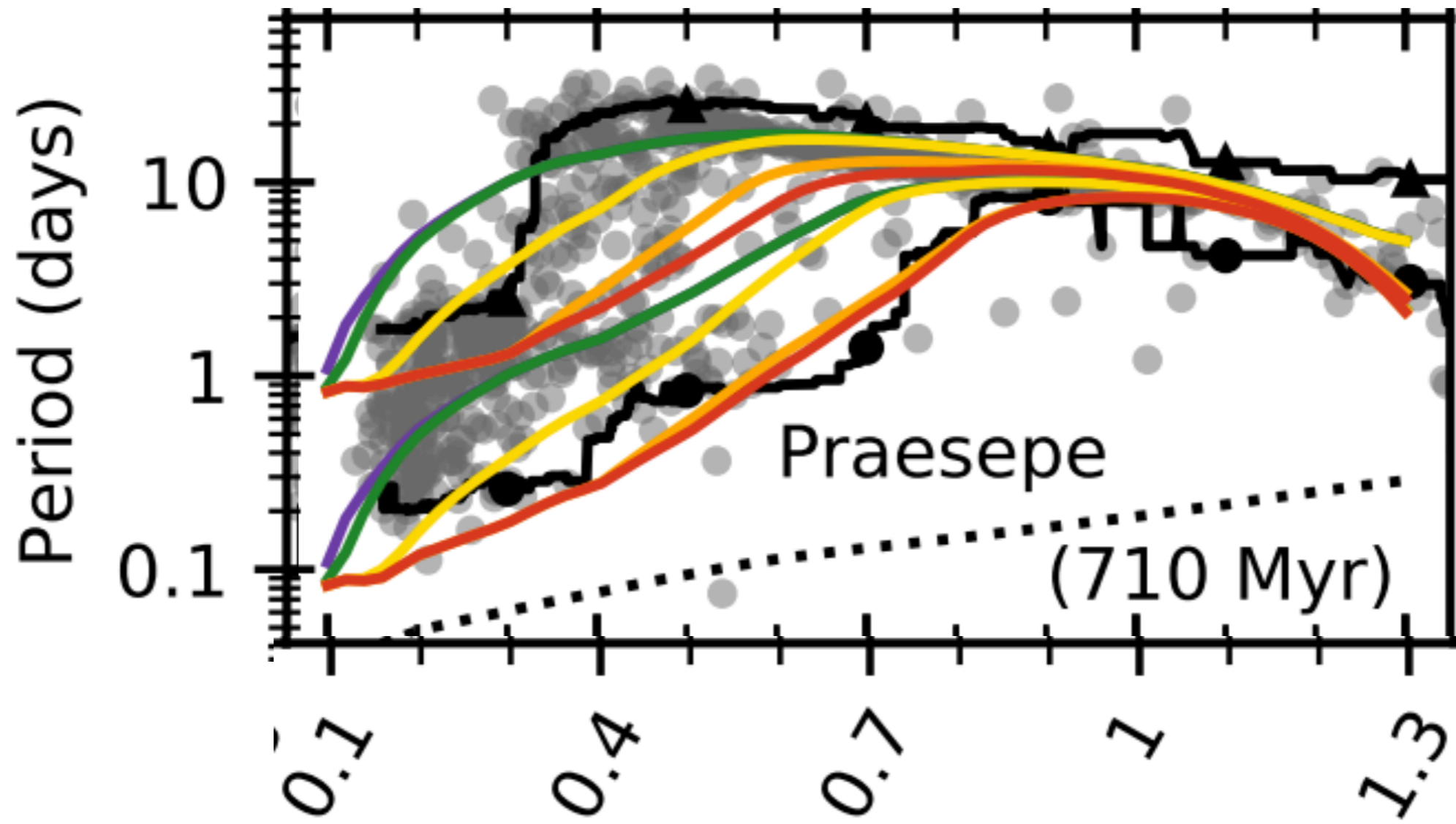
Assuming clusters at different ages represent an evolutionary sequence may not be safe

Example: the problem of h Per



Stronger FUV exposure

Weaker FUV exposure



Model Ingredients

1.) A description of initial conditions

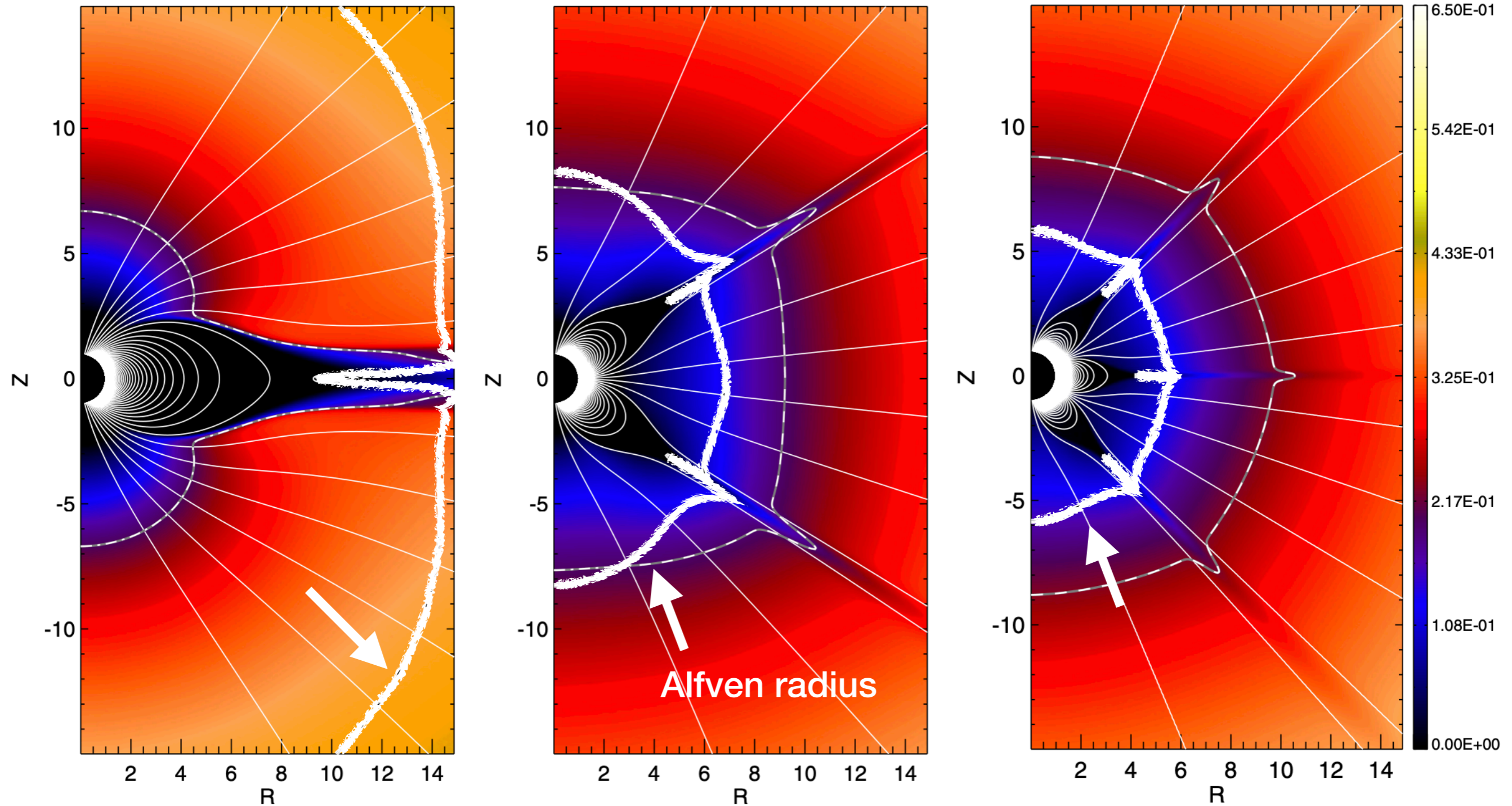
2.) A description of magnetic braking at the stellar surface

3.) A description interior angular momentum transport

Magnetic braking prescriptions

$$\frac{dJ}{dt} \propto \dot{M} \Omega R_{\star}^2 \left(\frac{r_A}{R_{\star}} \right)^2$$

Magnetic field strength and morphology matter



$r_A \uparrow$ as $B \uparrow$, $r_A \downarrow$ with increasing field order

Reville et al. 2015, see also Garraffo et al. 2015, 2016, Finley & Matt 2018, See et al. 2019

Magnetic braking prescriptions

$$\frac{dJ}{dt} = -K \left(\frac{M_{\star}}{M_{\odot}} \right)^{-m} \left(\frac{R_{\star}}{R_{\odot}} \right)^{5m+2} \left(\frac{B_{\star}}{B_{\odot}} \right)^{4m} \left(\frac{\dot{M}_{\star}}{\dot{M}_{\odot}} \right)^{1-2m} \left(\frac{\Omega_{\star}}{\Omega_{\odot}} \right)$$

Matt et al. 2012

Matt et al. 2015

van Saders & Pinsonneault 2013

Magnetic braking prescriptions

Set by field morphology, wind acceleration

$$\frac{dJ}{dt} = -K \left(\frac{M_{\star}}{M_{\odot}} \right)^{-m} \left(\frac{R_{\star}}{R_{\odot}} \right)^{5m+2} \left(\frac{B_{\star}}{B_{\odot}} \right)^{4m} \left(\frac{\dot{M}_{\star}}{\dot{M}_{\odot}} \right)^{1-2m} \left(\frac{\Omega_{\star}}{\Omega_{\odot}} \right)$$


Normalization constant

Matt et al. 2012

Matt et al. 2015

van Saders & Pinsonneault 2013

Magnetic braking prescriptions

$$\frac{dJ}{dt} = -K \left(\frac{M_{\star}}{M_{\odot}} \right)^{-m} \left(\frac{R_{\star}}{R_{\odot}} \right)^{5m+2} \left(\frac{B_{\star}}{B_{\odot}} \right)^{4m} \left(\frac{\dot{M}_{\star}}{\dot{M}_{\odot}} \right)^{1-2m} \left(\frac{\Omega_{\star}}{\Omega_{\odot}} \right)$$


Matt et al. 2012

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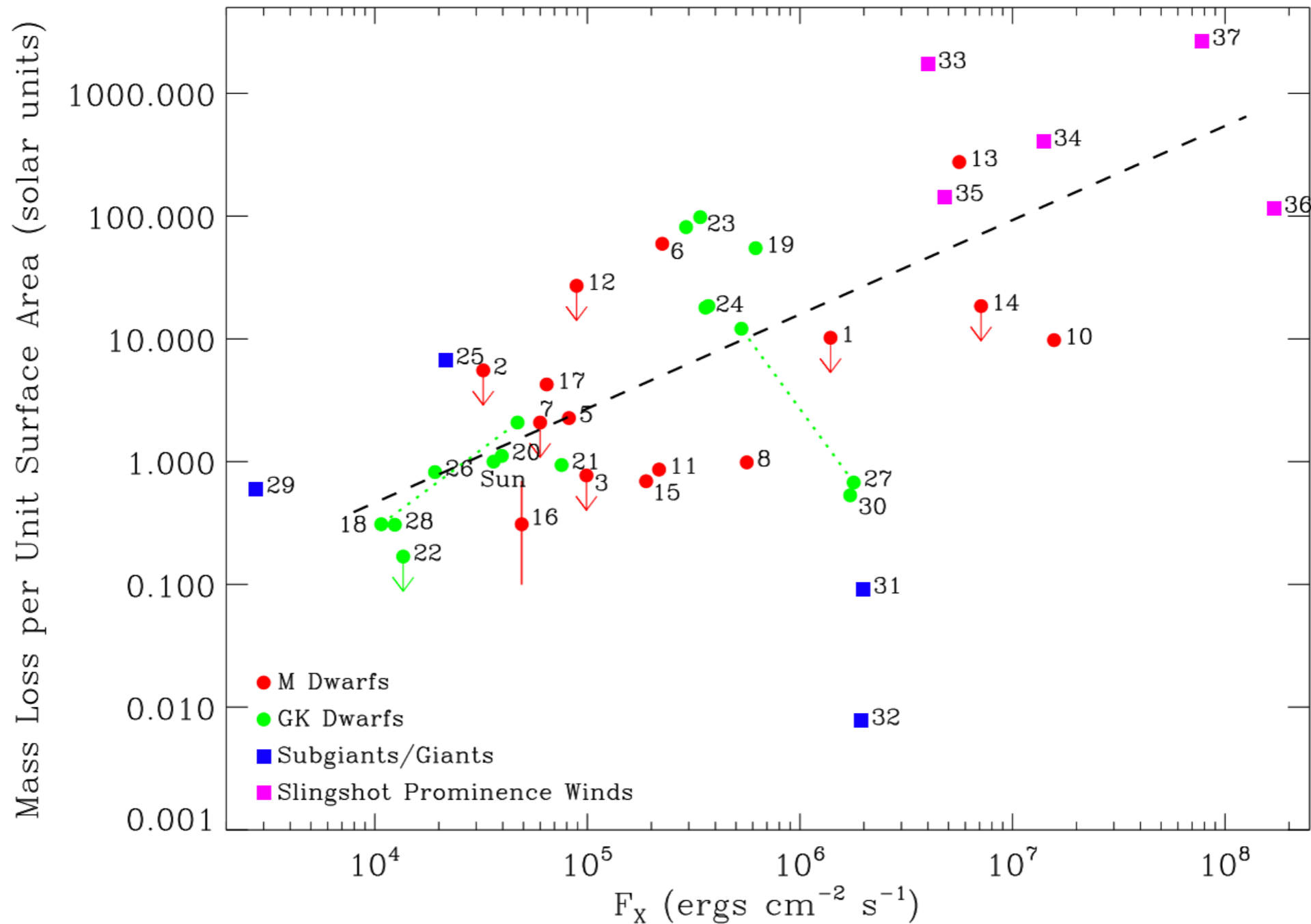
van Saders & Pinsonneault 2013

Magnetic braking prescriptions

$$\frac{dJ}{dt} = -K \left(\frac{M_{\star}}{M_{\odot}} \right)^{-m} \left(\frac{R_{\star}}{R_{\odot}} \right)^{5m+2} \left(\frac{B_{\star}}{B_{\odot}} \right)^{4m} \left(\frac{\dot{M}_{\star}}{\dot{M}_{\odot}} \right)^{1-2m} \left(\frac{\Omega_{\star}}{\Omega_{\odot}} \right)$$



Measurements of mass loss rates for dwarfs exist, but they are few.



Magnetic braking prescriptions

$$\frac{dJ}{dt} = -K \left(\frac{M_{\star}}{M_{\odot}} \right)^{-m} \left(\frac{R_{\star}}{R_{\odot}} \right)^{5m+2} \left(\frac{B_{\star}}{B_{\odot}} \right)^{4m} \left(\frac{\dot{M}_{\star}}{\dot{M}_{\odot}} \right)^{1-2m} \left(\frac{\Omega_{\star}}{\Omega_{\odot}} \right)$$



Magnetic braking prescriptions

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First, assume a dipole*

Magnetic braking prescriptions

$$\frac{dJ}{dt} = -K \left(\frac{M_{\star}}{M_{\odot}} \right)^{-m} \left(\frac{R_{\star}}{R_{\odot}} \right)^{5m+2} \left(\frac{B_{\star}}{B_{\odot}} \right)^{4m} \left(\frac{\dot{M}_{\star}}{\dot{M}_{\odot}} \right)^{1-2m} \left(\frac{\Omega_{\star}}{\Omega_{\odot}} \right)$$



First, assume a dipole*

Second, assume a Rossby scaling*


Magnetic phenomena (appear to) depend on the Rossby number

$$Ro = \frac{P_{rot}}{\tau_{cz}}$$

increases as the star spins down with time

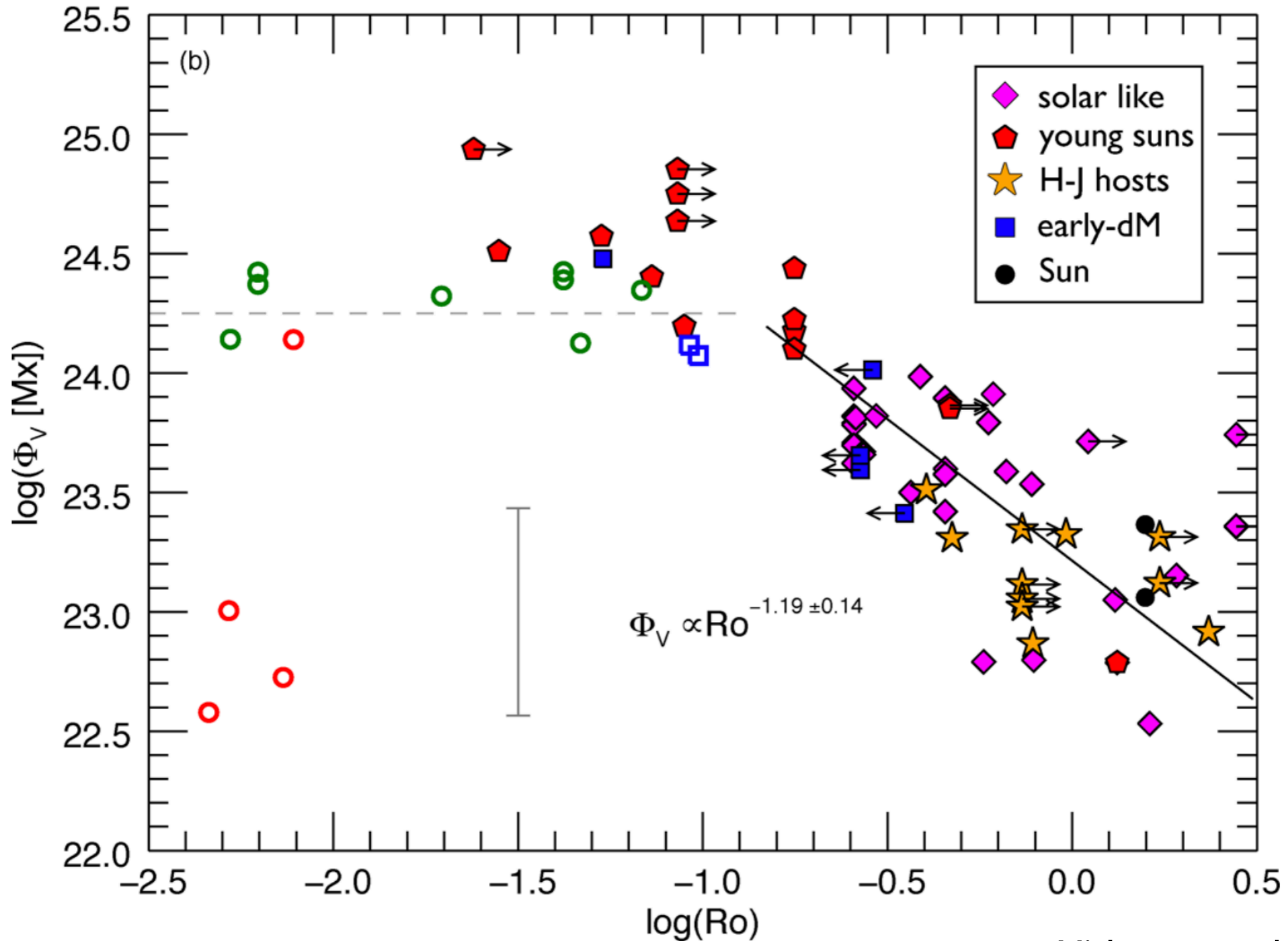


Roughly constant during the main sequence, but a strong function of mass



Objects with lower Rossby numbers are more active, with stronger fields

(ZDI magnetic flux)



Magnetic braking prescriptions

$$\frac{dJ}{dt} = -K \left(\frac{M_{\star}}{M_{\odot}} \right)^{-m} \left(\frac{R_{\star}}{R_{\odot}} \right)^{5m+2} \left(\frac{B_{\star}}{B_{\odot}} \right)^{4m} \left(\frac{\dot{M}_{\star}}{\dot{M}_{\odot}} \right)^{1-2m} \left(\frac{\Omega_{\star}}{\Omega_{\odot}} \right)$$

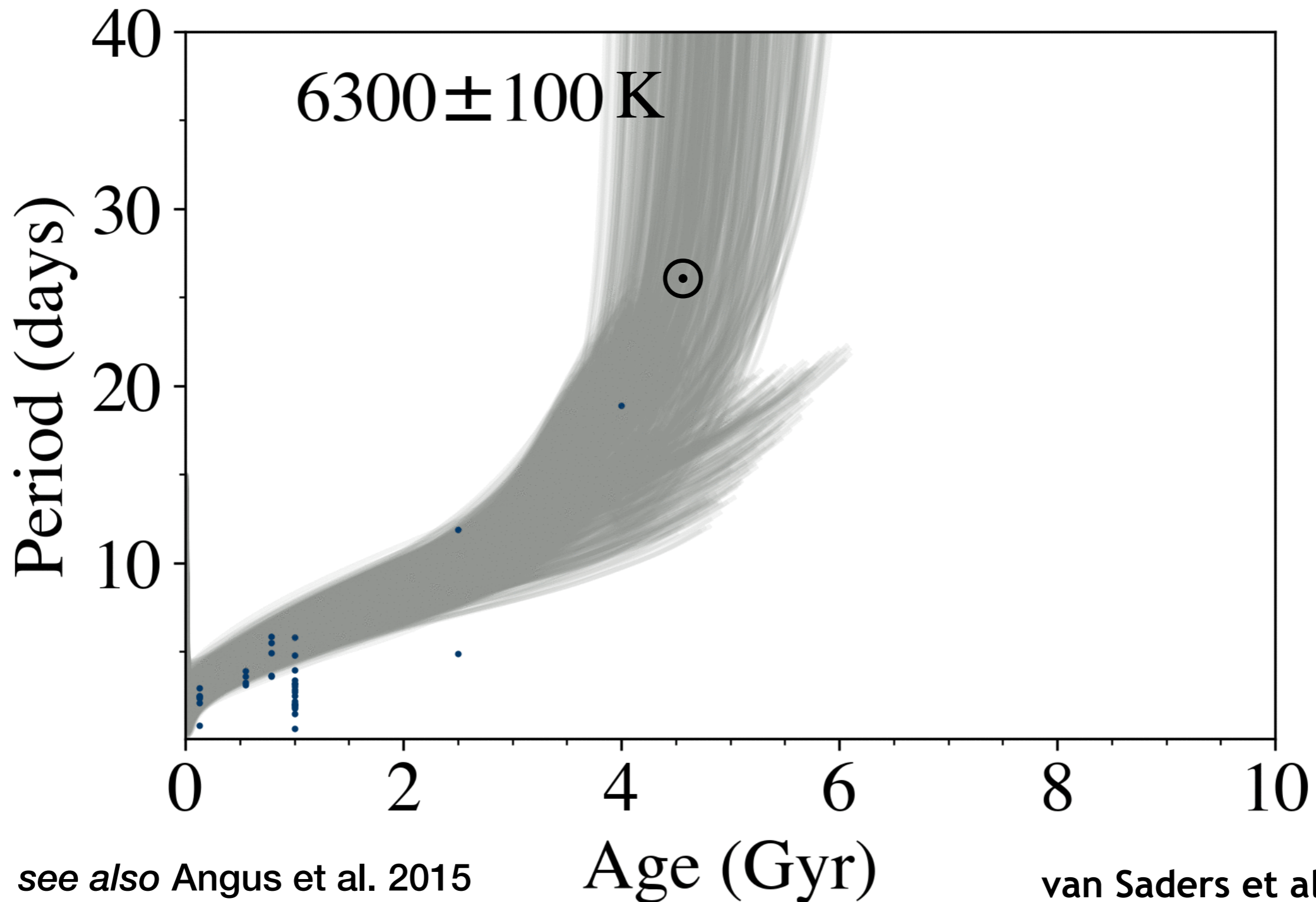
Generally:

$$\frac{dJ}{dt} \propto \Omega^3$$

To reproduce the observed
time dependence of spin
down

dJ/dt is a strong
function of mass
(or T_{eff} , or color)
of the star

A standard spin-down model

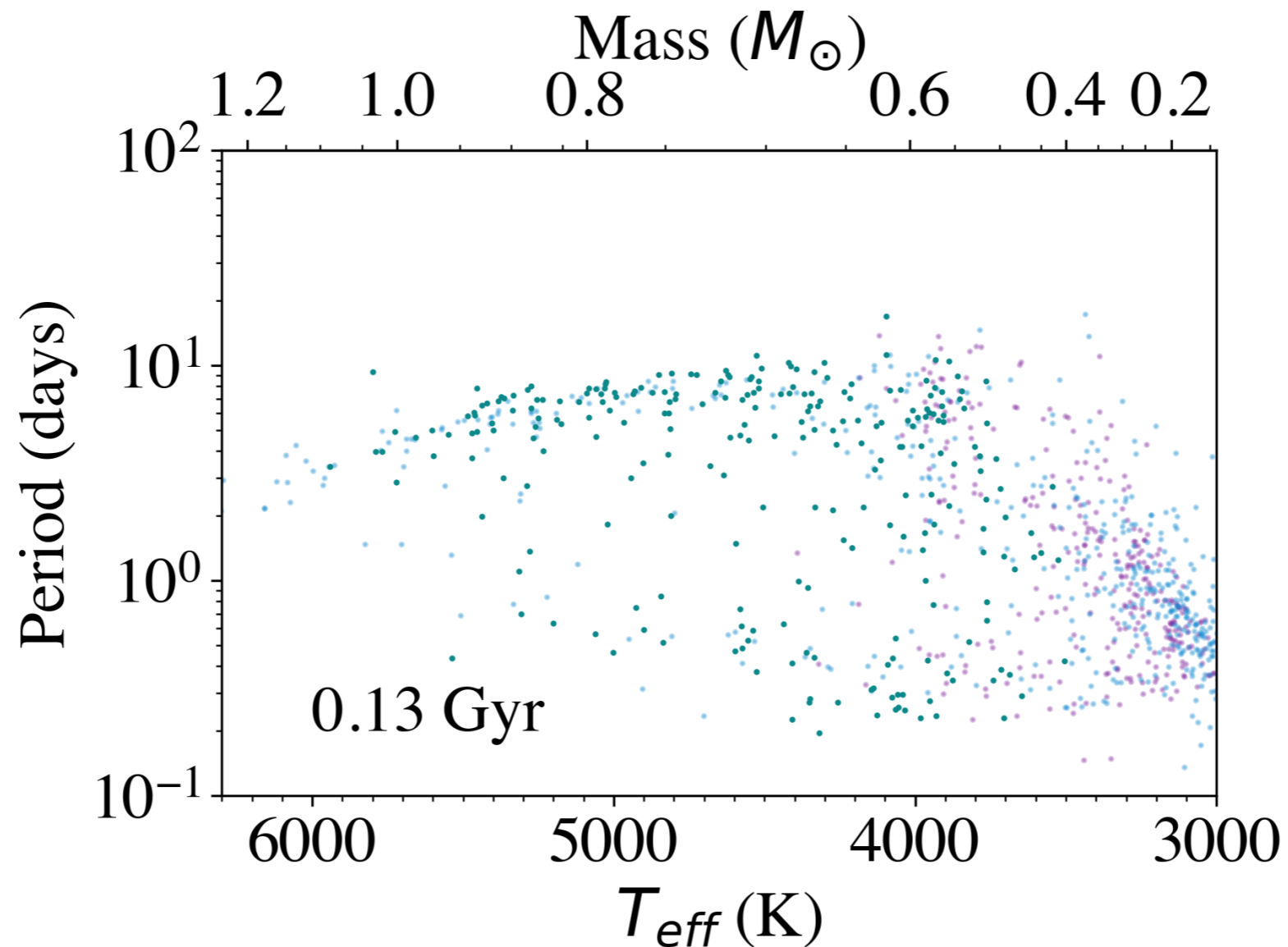


see also Angus et al. 2015

van Saders et al. 2016
Hall et al. 2021

Problem #2

Rapid rotators cannot survive to their observed ages with Ω^3 spin down



Problem #2

Rapid rotators cannot survive to their observed ages with Ω^3 spin down

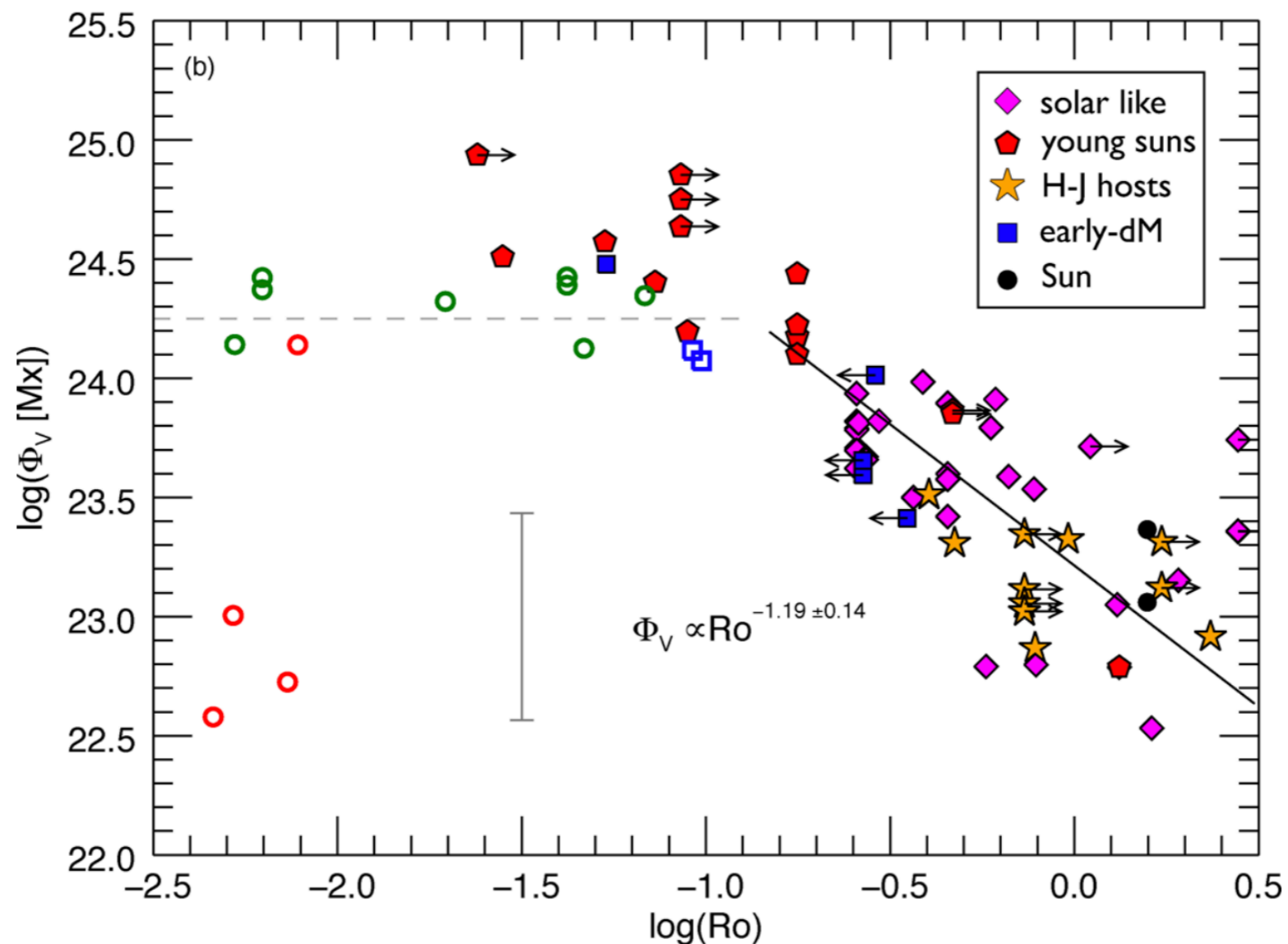
$$\frac{dJ}{dt} \propto \Omega^3, \Omega < \Omega_{crit}$$

$$\frac{dJ}{dt} \propto \Omega, \Omega > \Omega_{crit}$$

“Saturation”: At some Ω_{crit} , spinning the star faster does not yield a stronger field, thus you do not have stronger braking

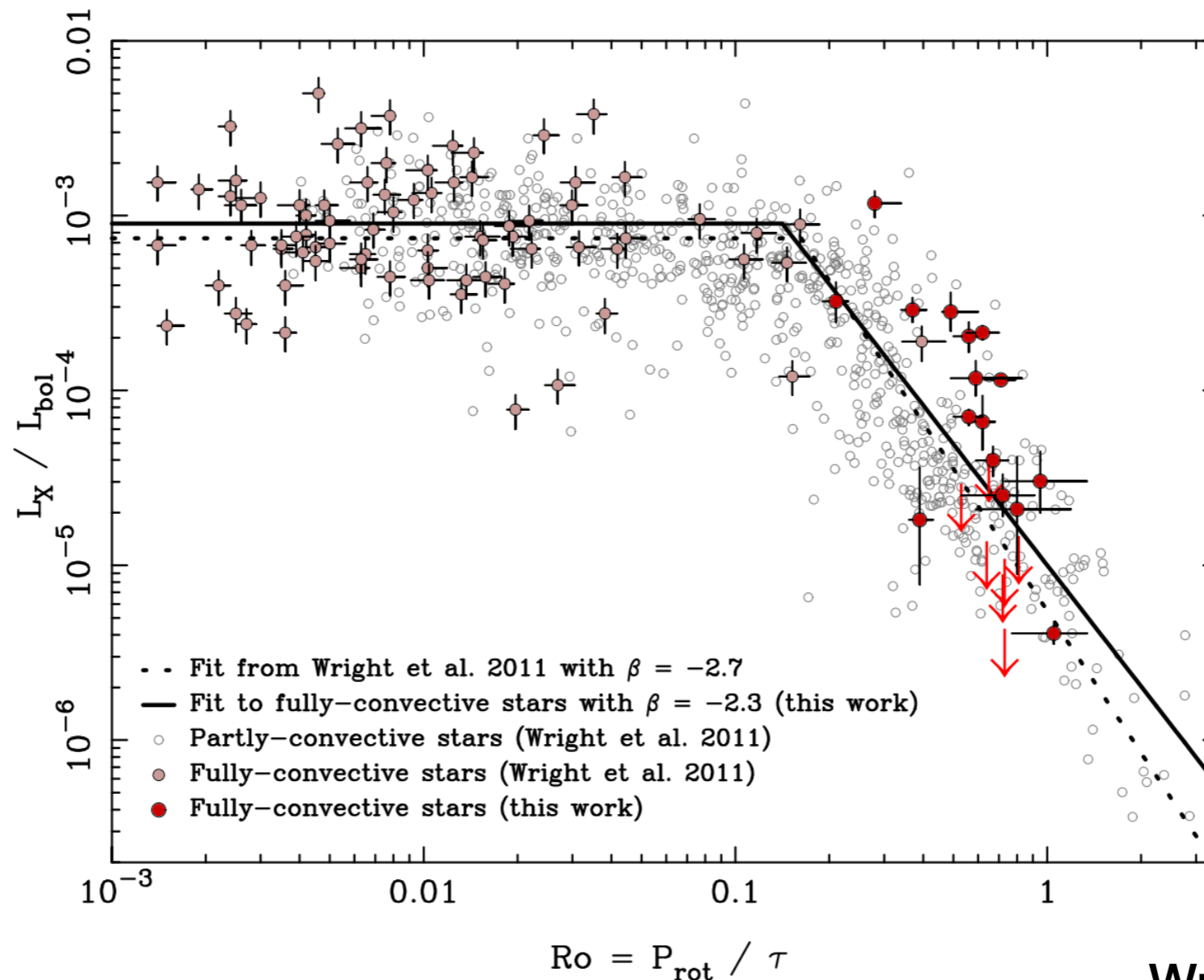
Problem #2

Rapid rotators cannot survive to their observed ages with Ω^3 spin down

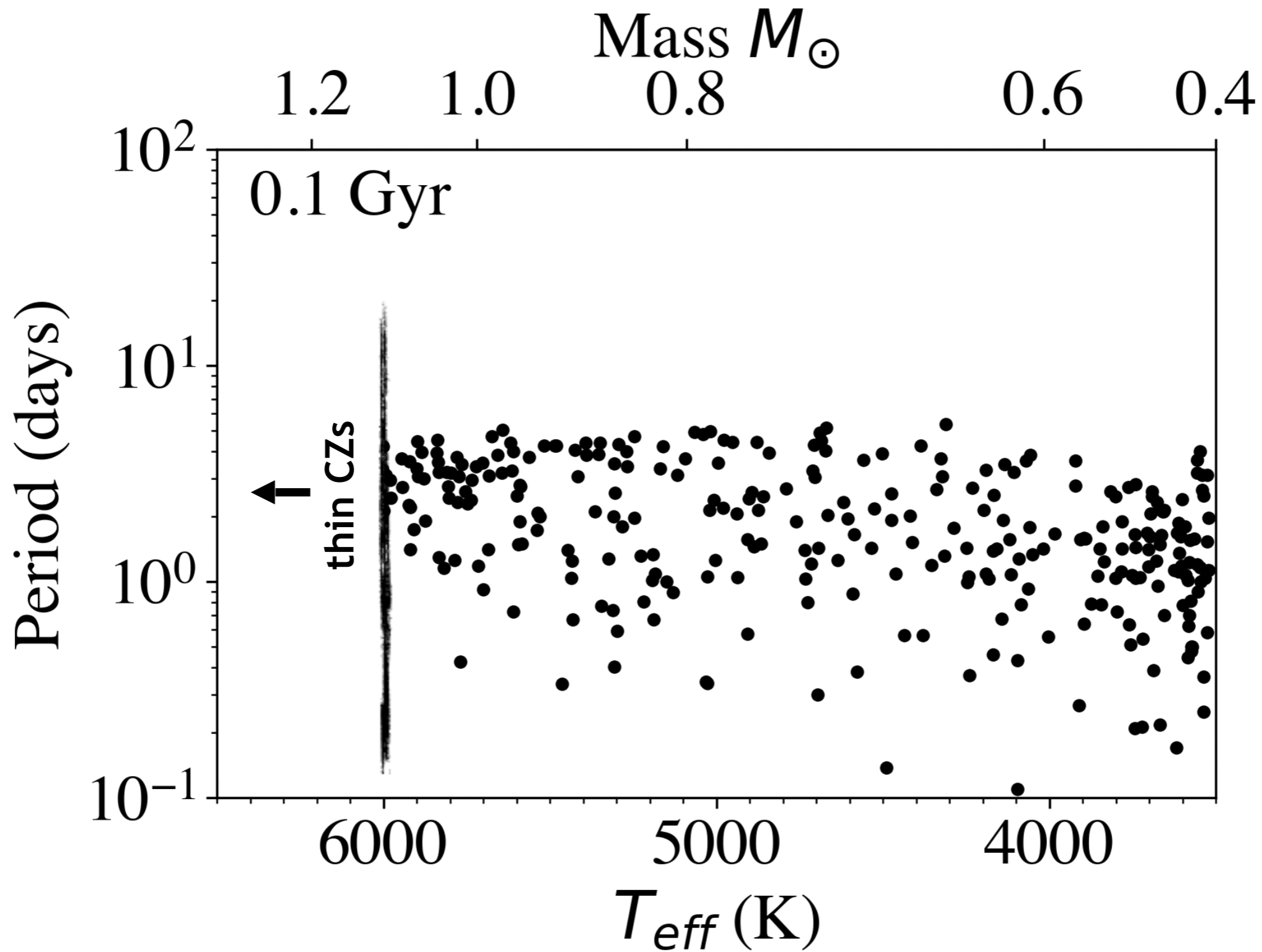


Problem #2

Rapid rotators cannot survive to their observed ages with Ω^3 spin down



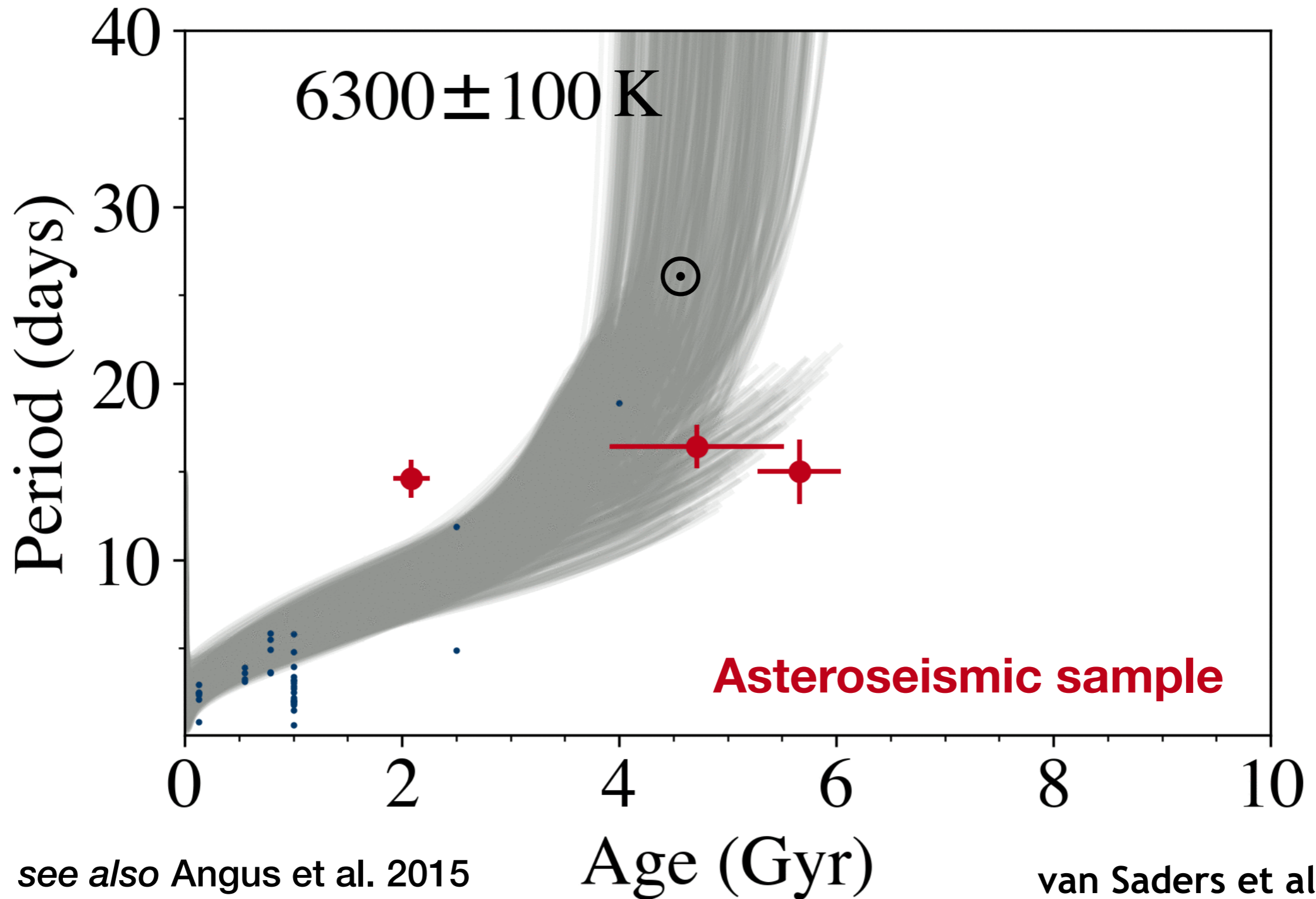
A model of stellar spin down



Problem #3

Old stars appear to stop losing angular momentum at Rossby numbers larger than solar

A standard spin-down model

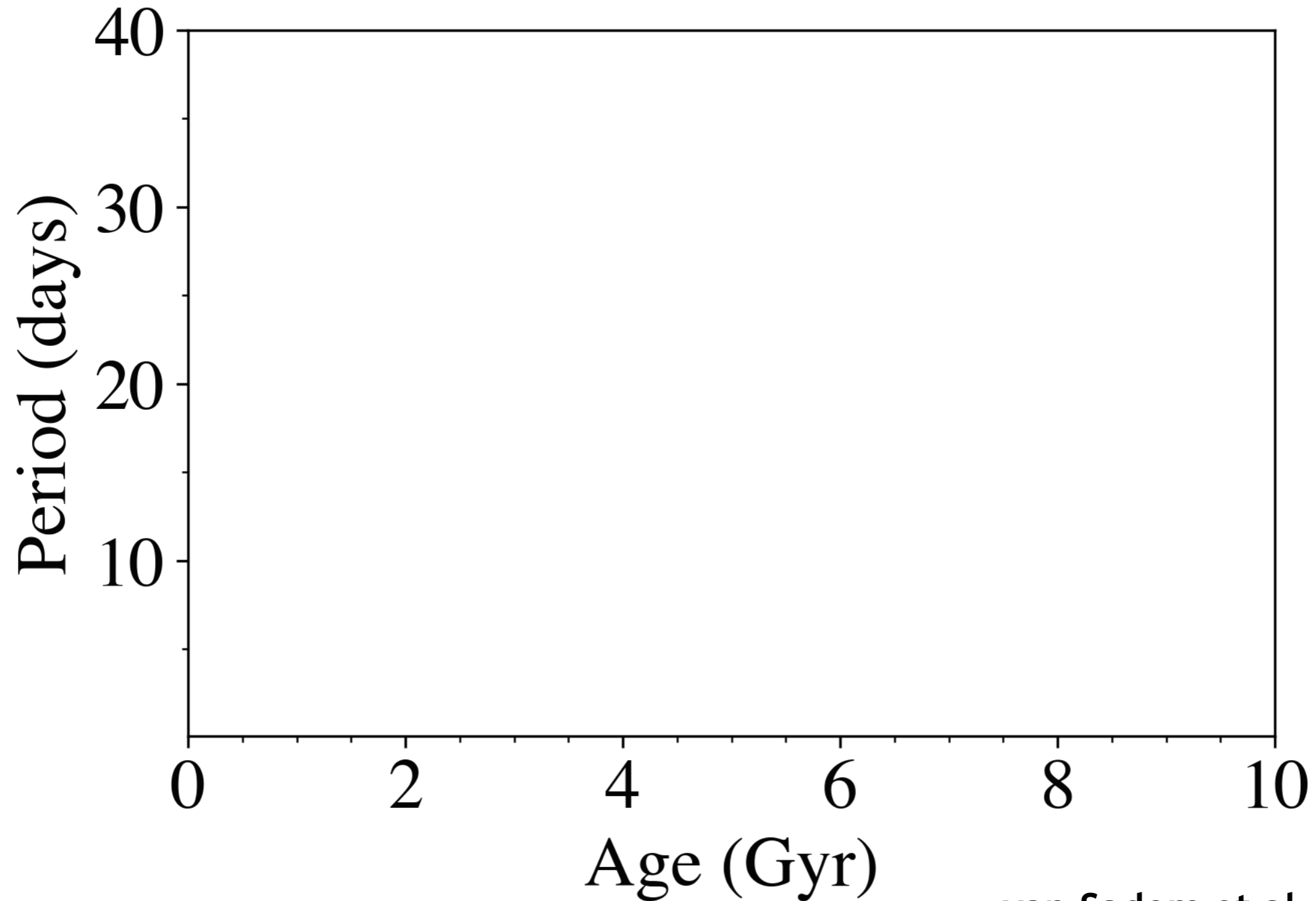


see also Angus et al. 2015

van Saders et al. 2016
Hall et al. 2021

Weakened magnetic braking

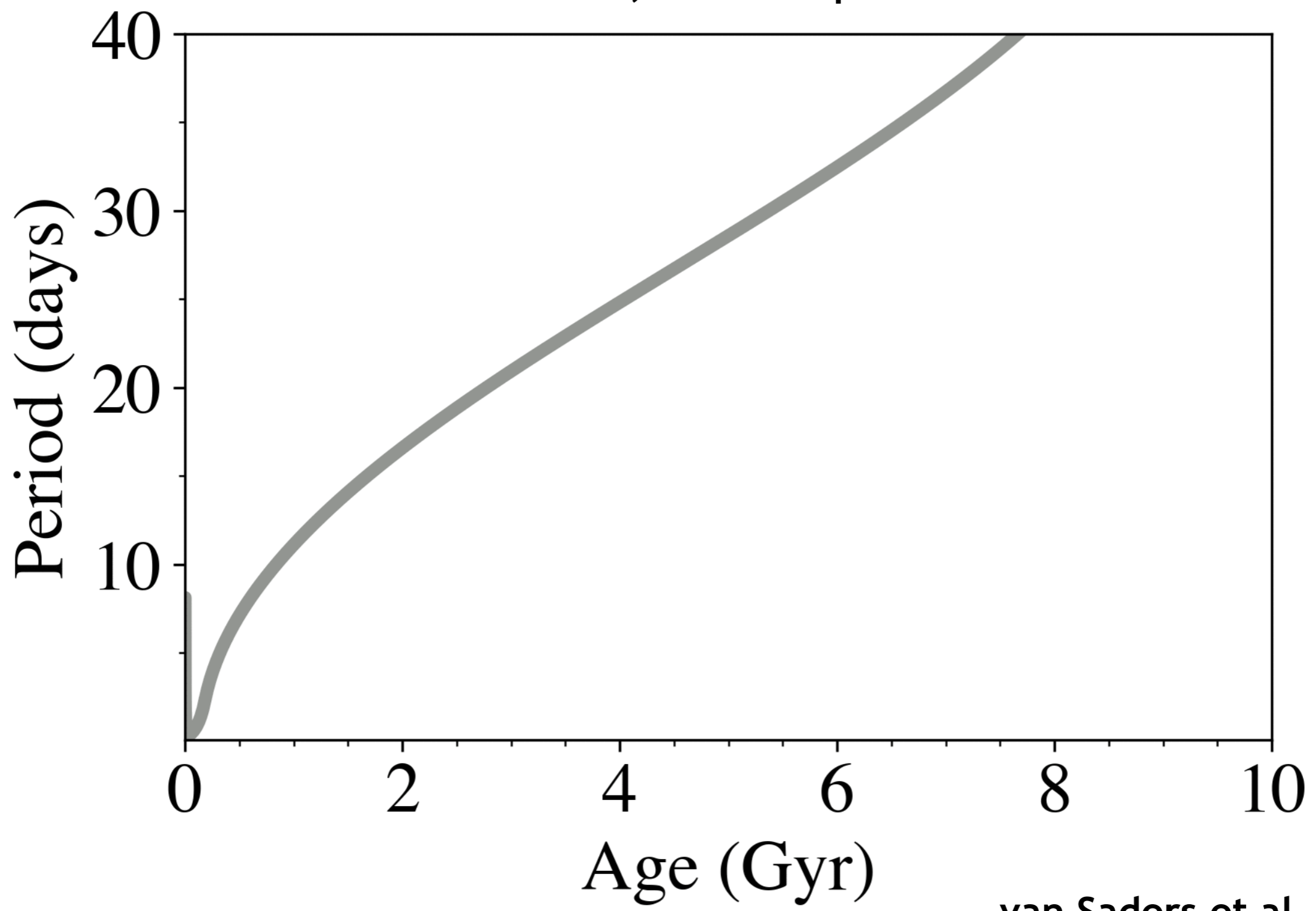
Solar mass, solar composition



van Saders et al. 2016

Weakened magnetic braking

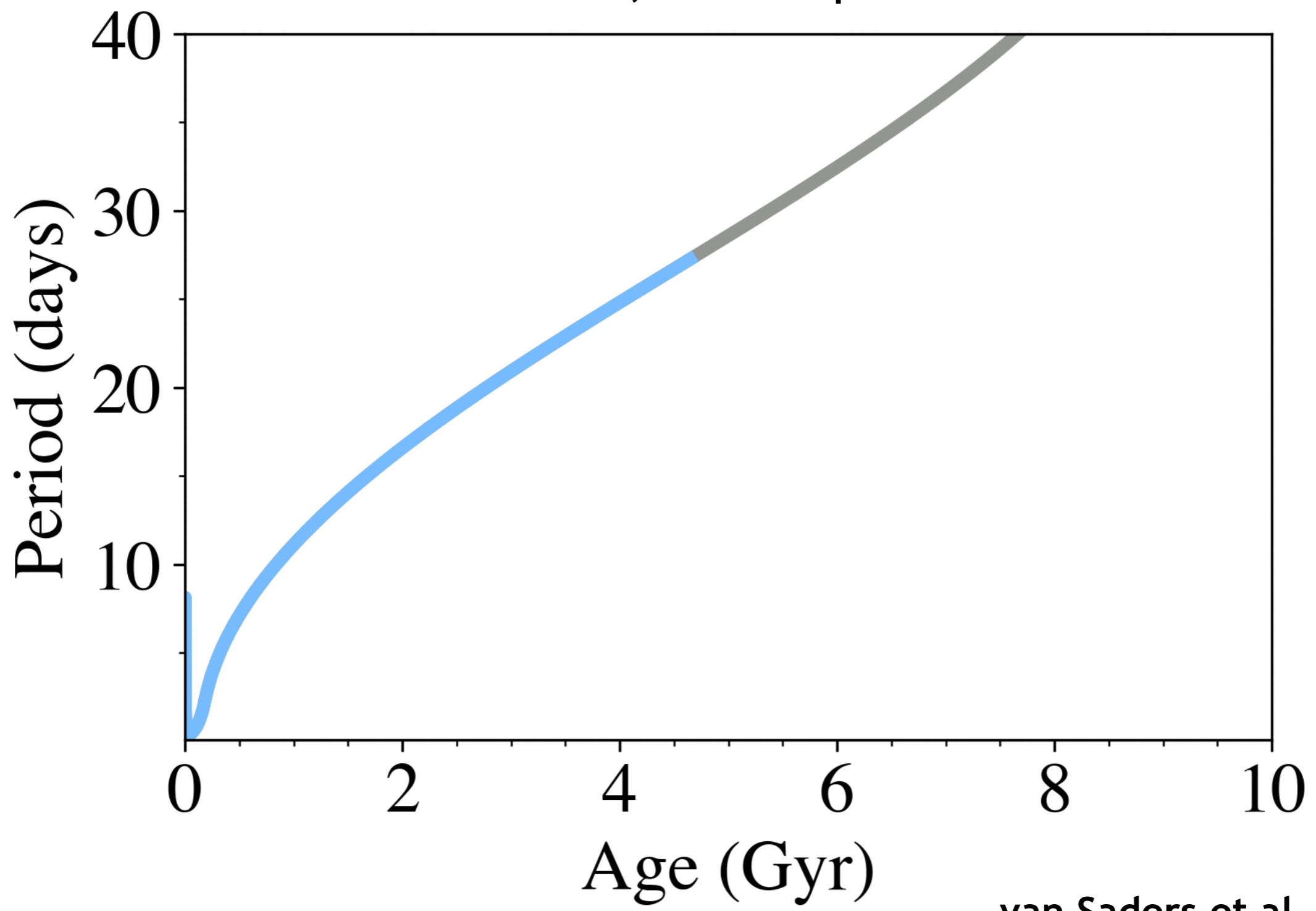
Solar mass, solar composition



van Saders et al. 2016

Weakened magnetic braking

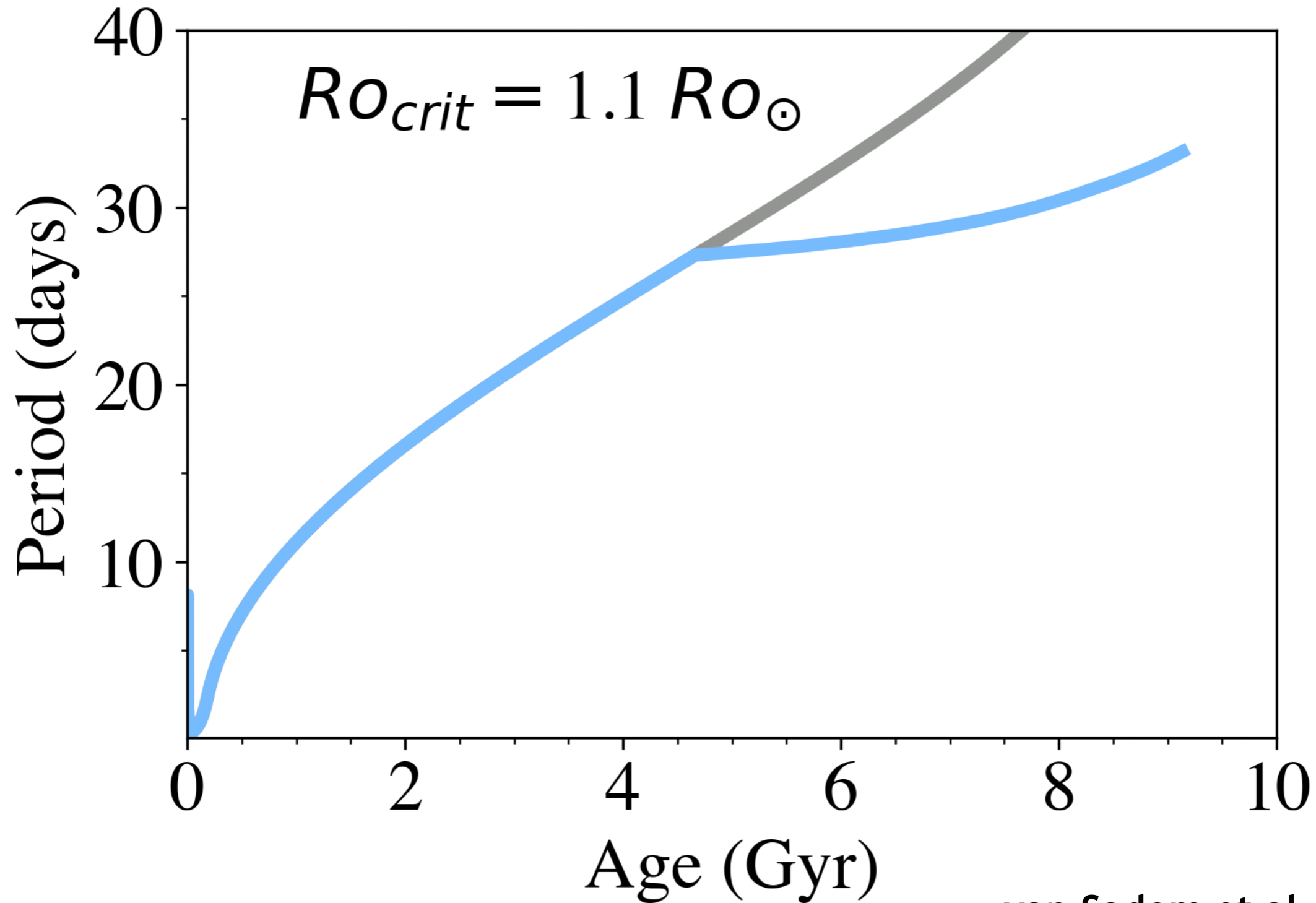
Solar mass, solar composition



van Saders et al. 2016

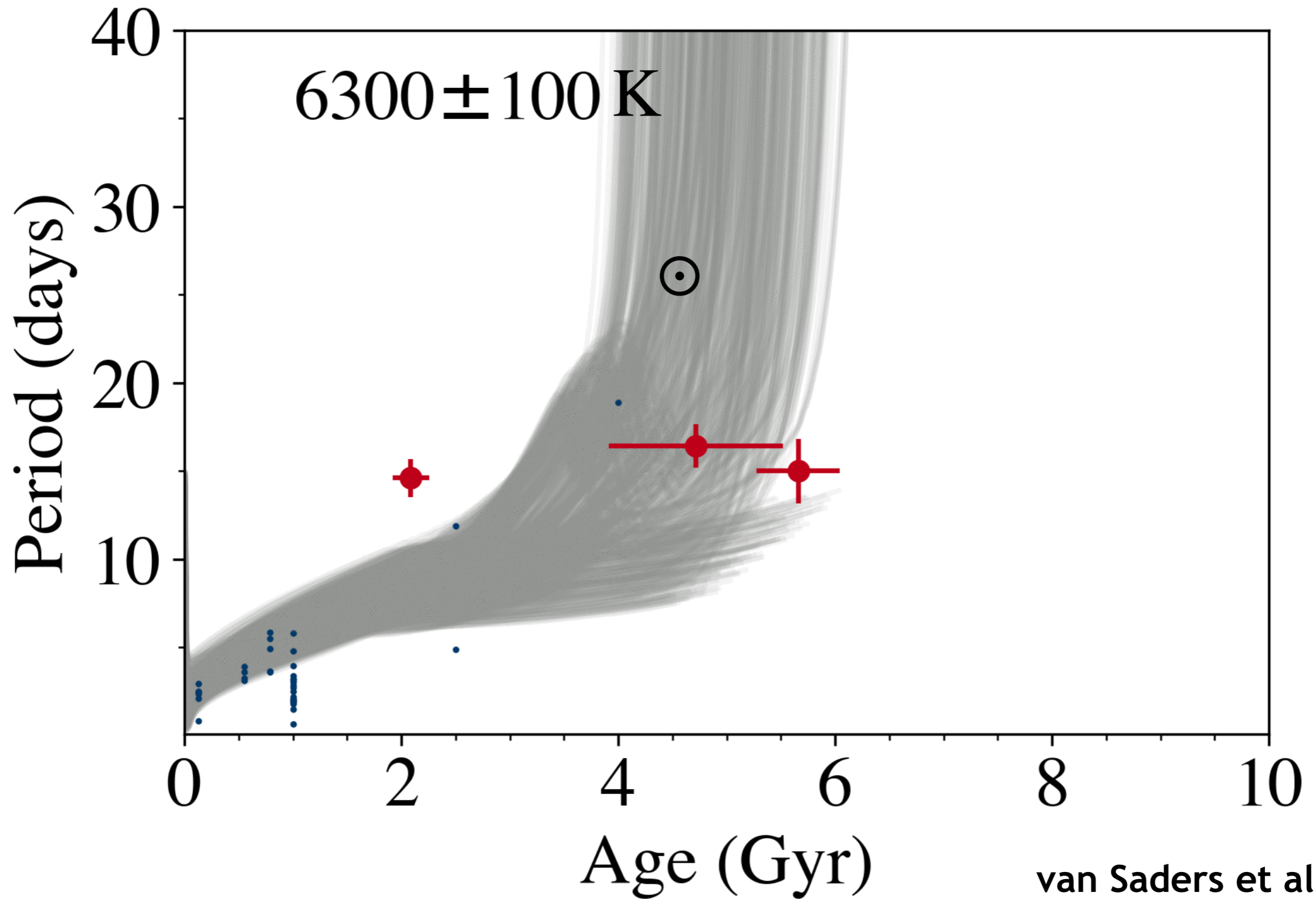
Weakened magnetic braking

Solar mass, solar composition



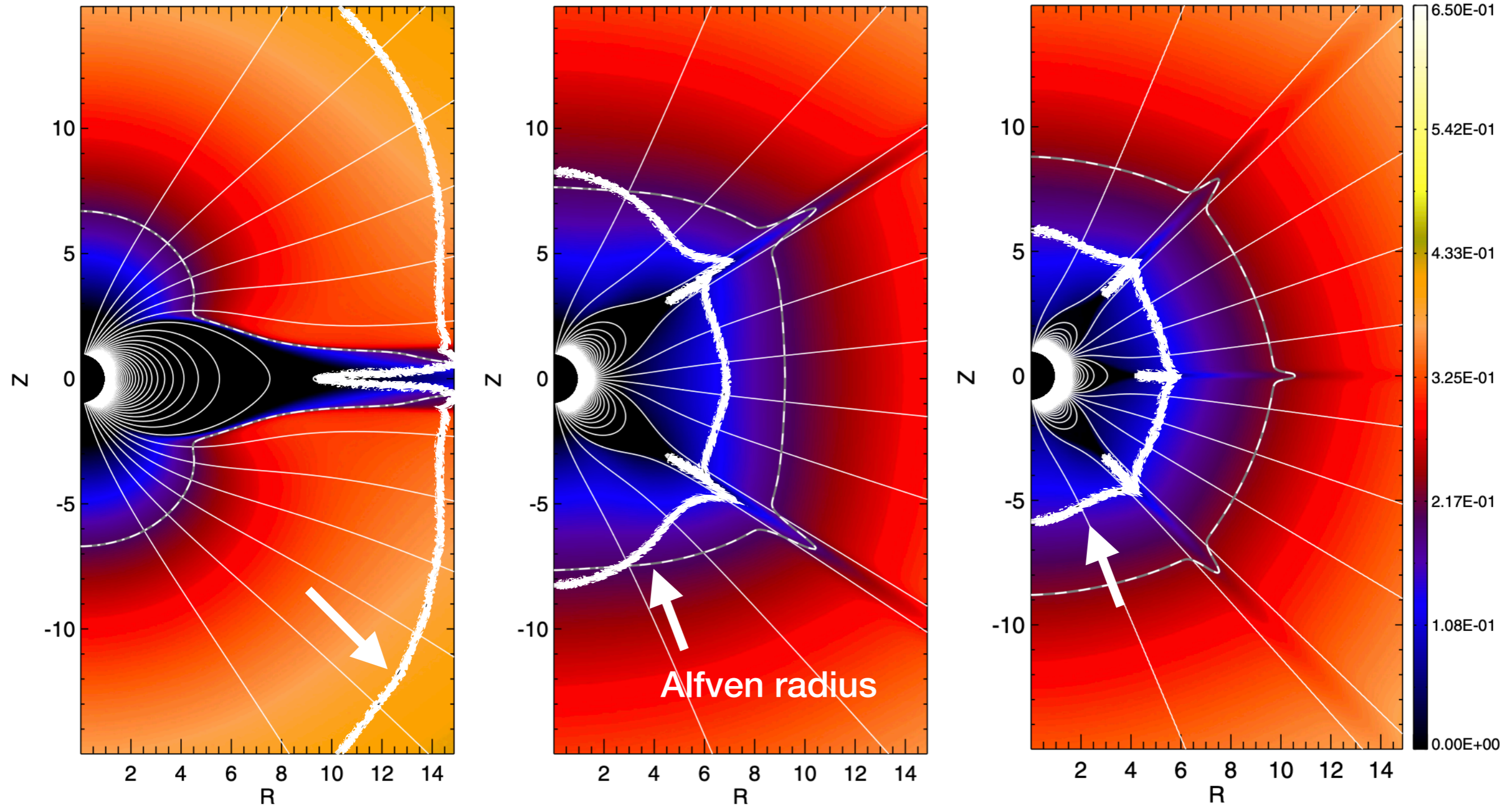
van Saders et al. 2016

Halt spin-down past a critical Rossby number



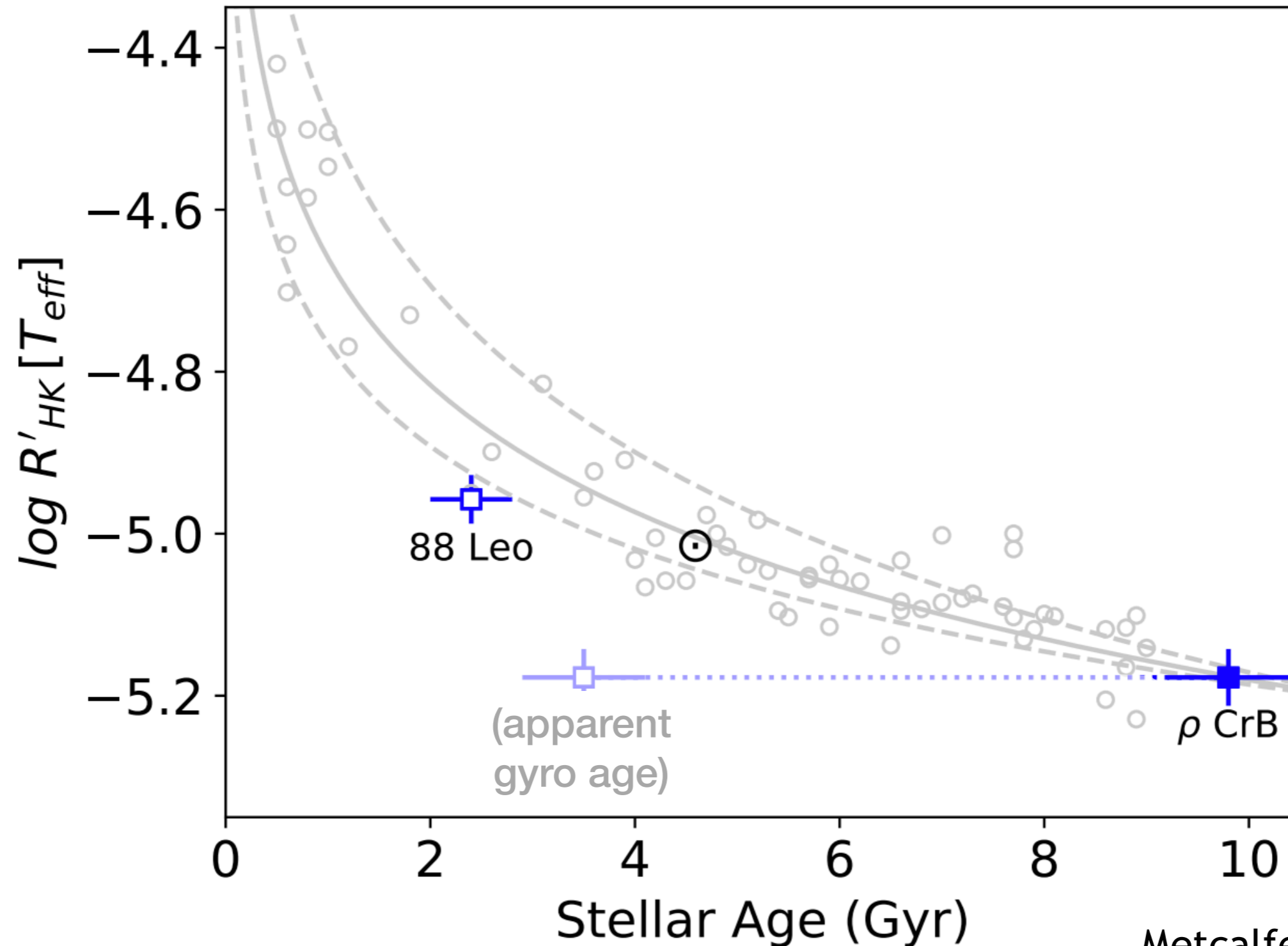
van Saders et al. 2016
Hall et al. 2021

Magnetic field strength and morphology matter

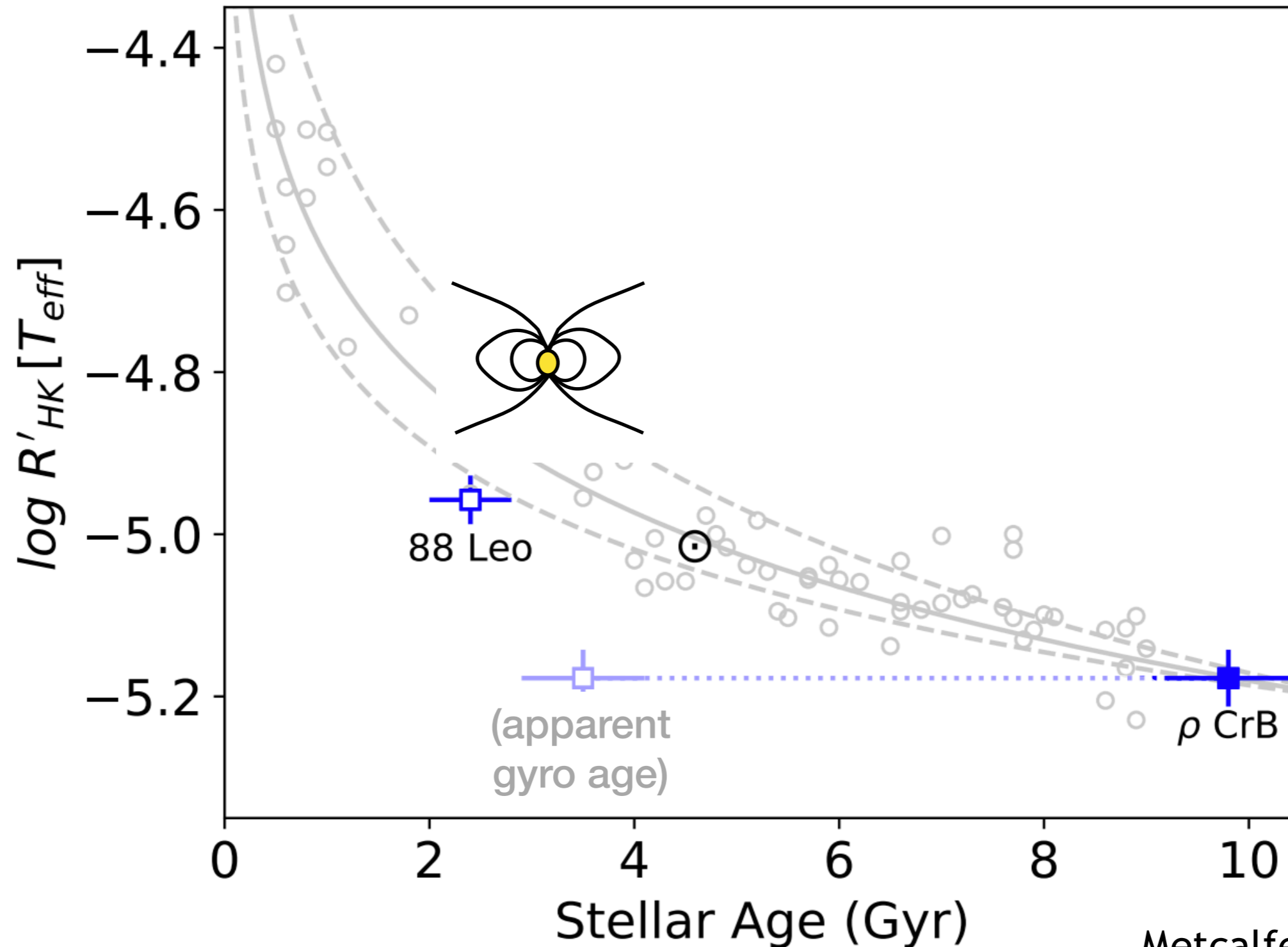


Reville et al. 2015, see also Garraffo et al. 2015, 2016, Finley & Matt 2018, See et al. 2019

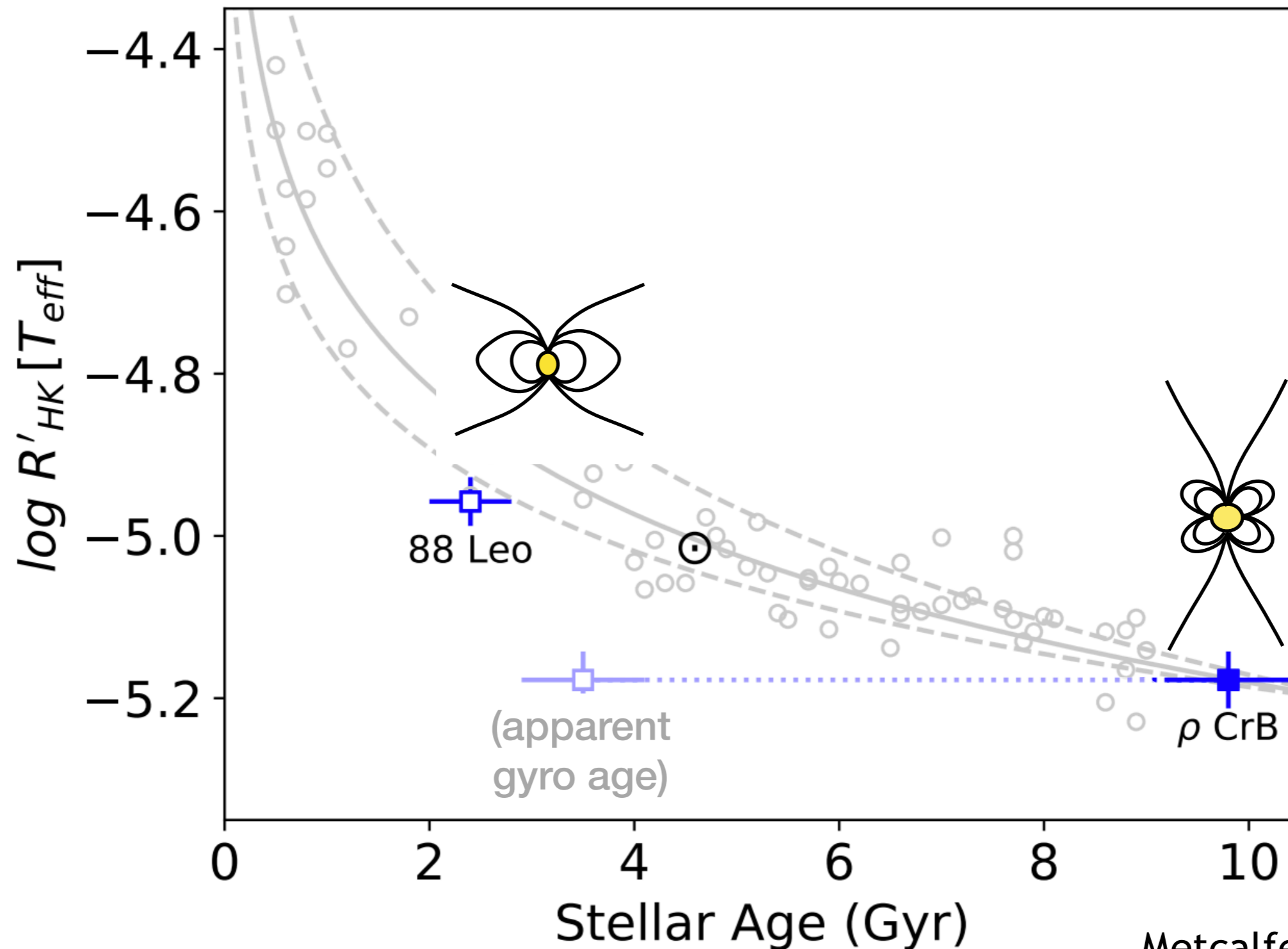
A shift in magnetic field morphology?



A shift in magnetic field morphology?



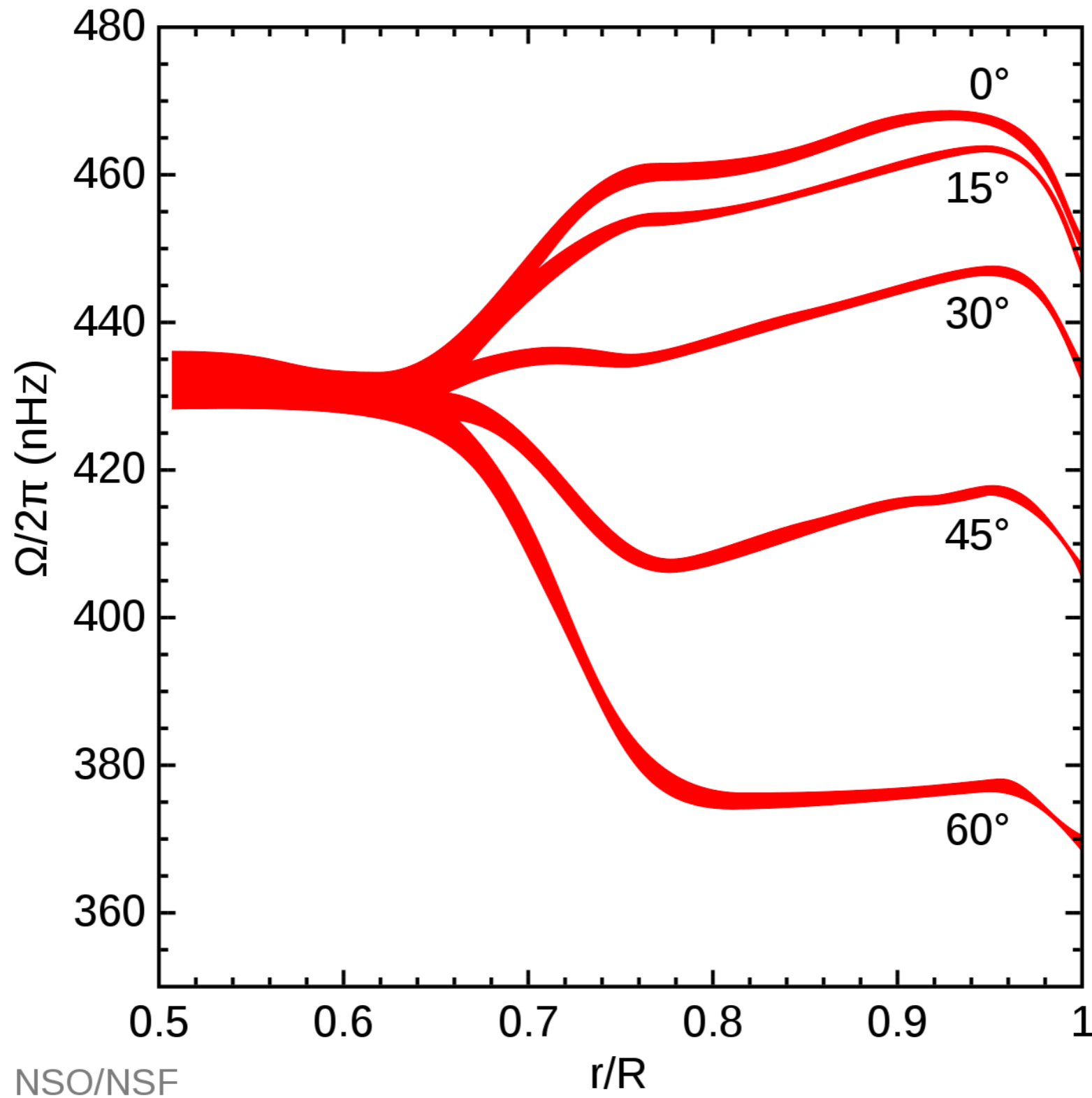
A shift in magnetic field morphology?



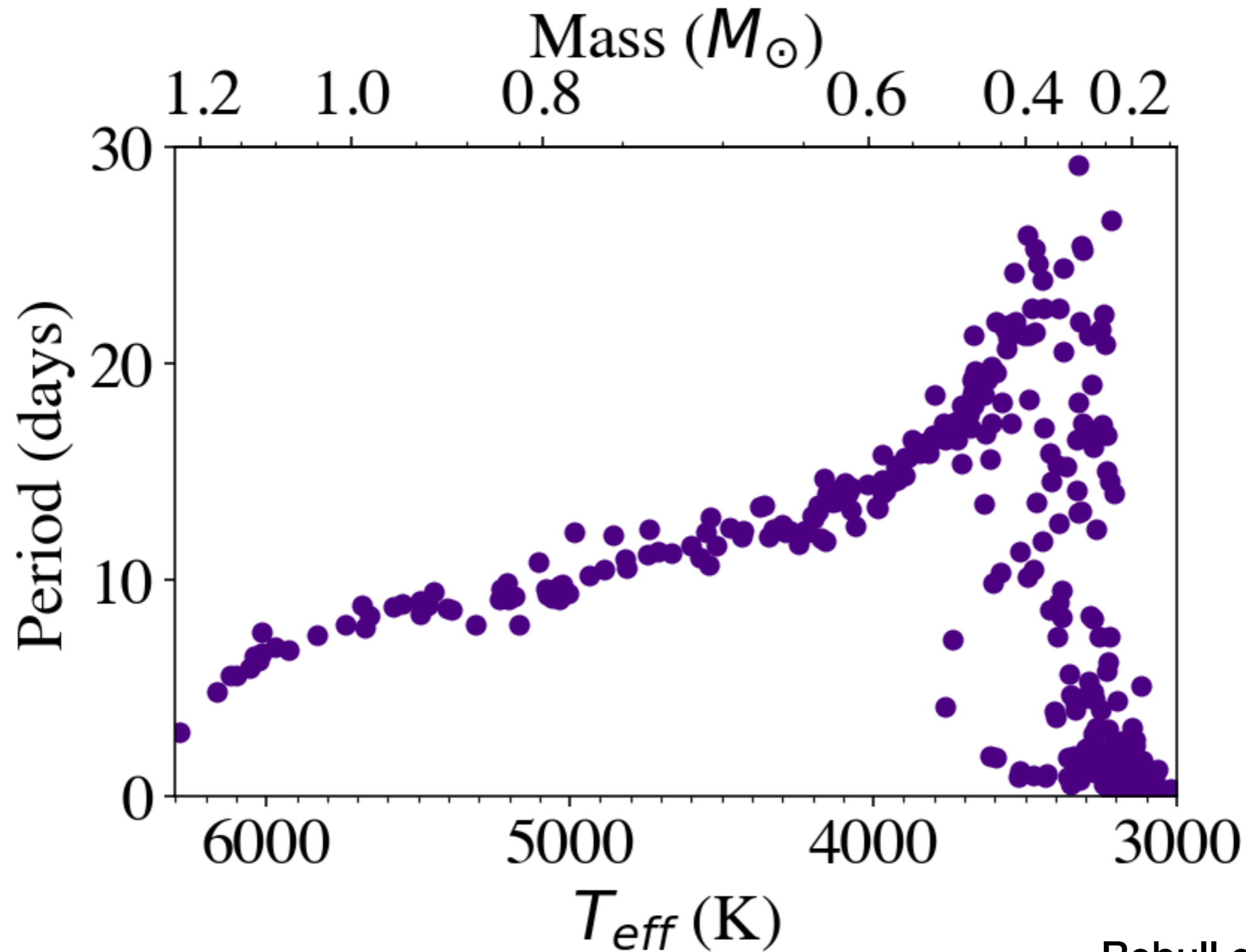
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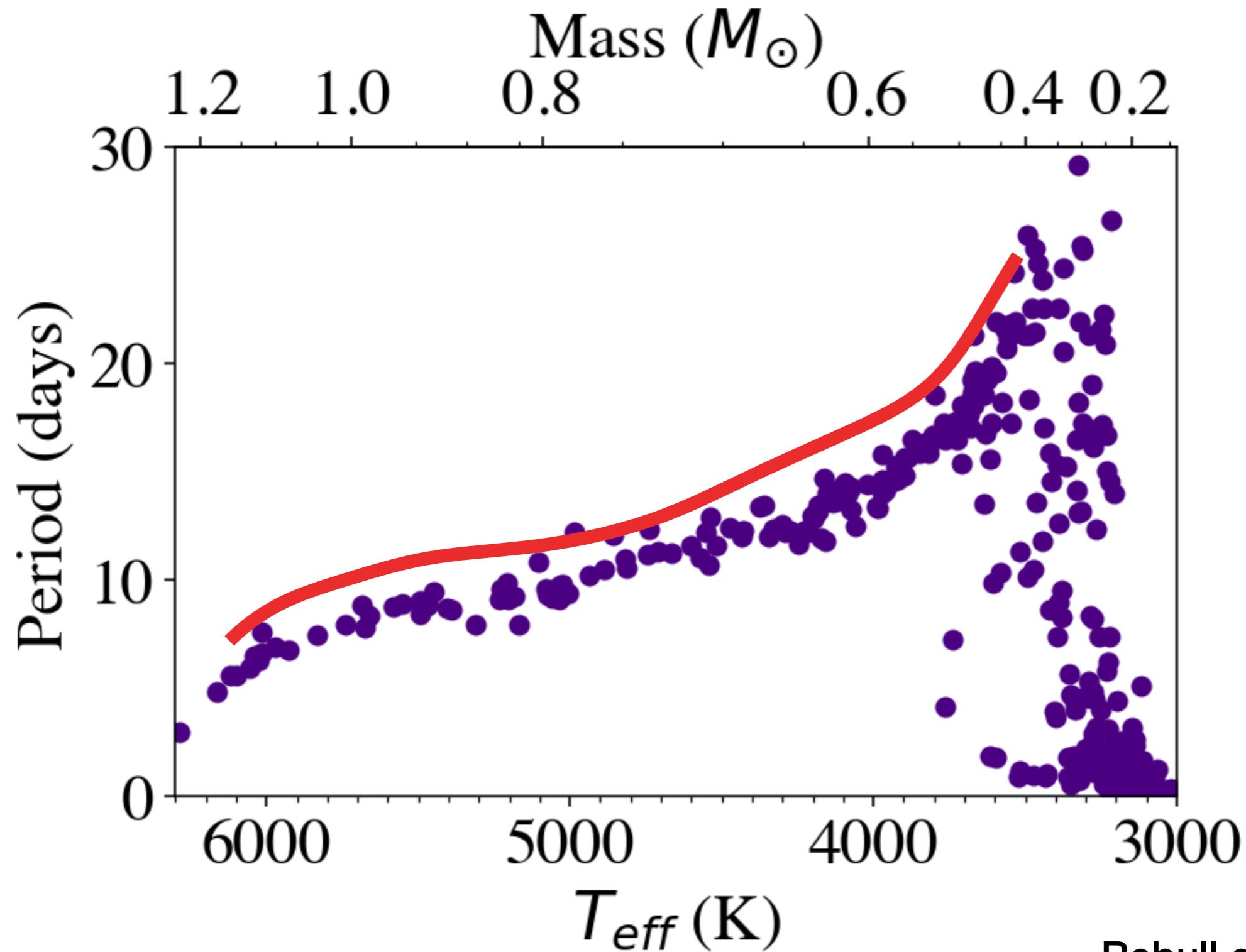
The Sun is not far from a solid body



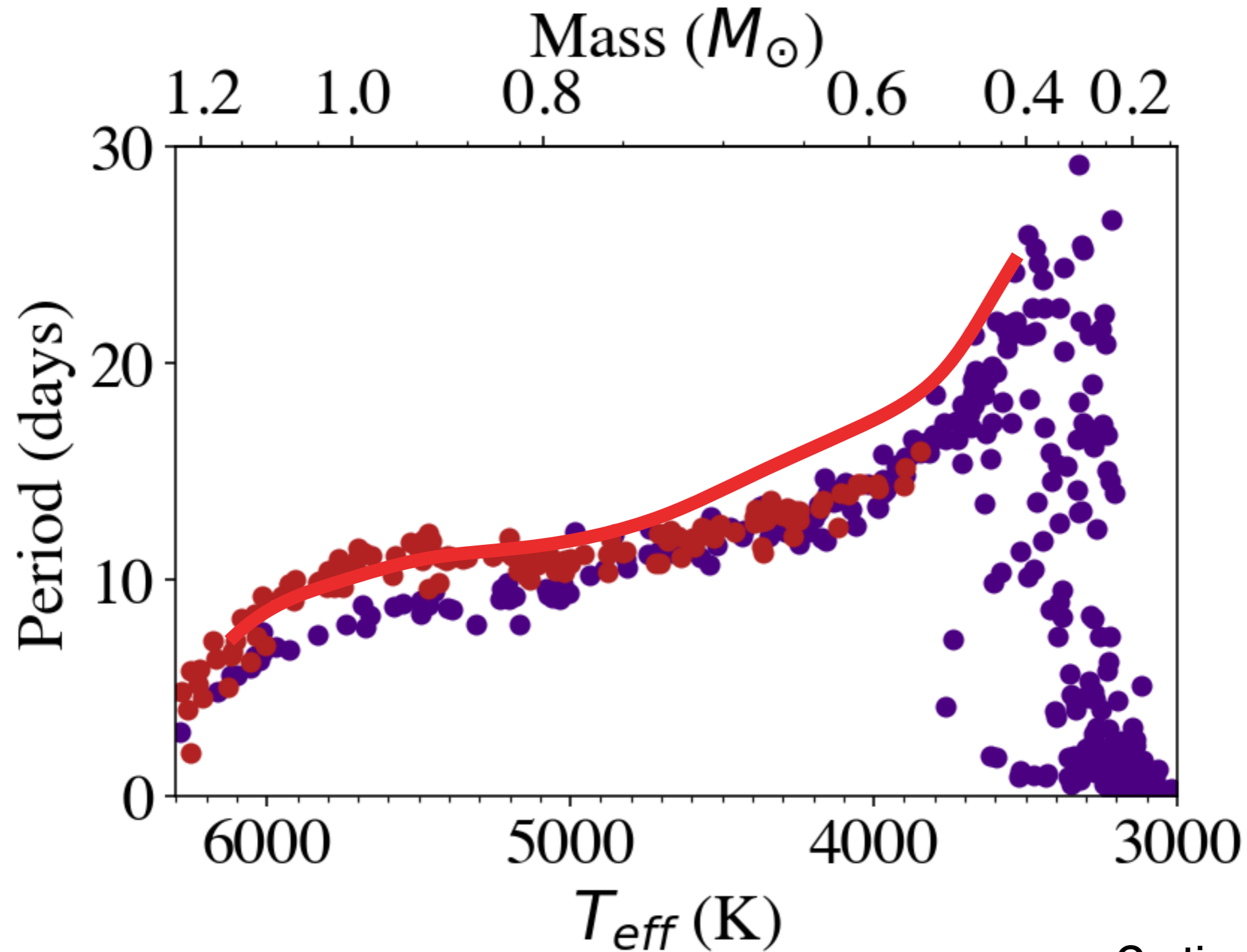
Problem #4



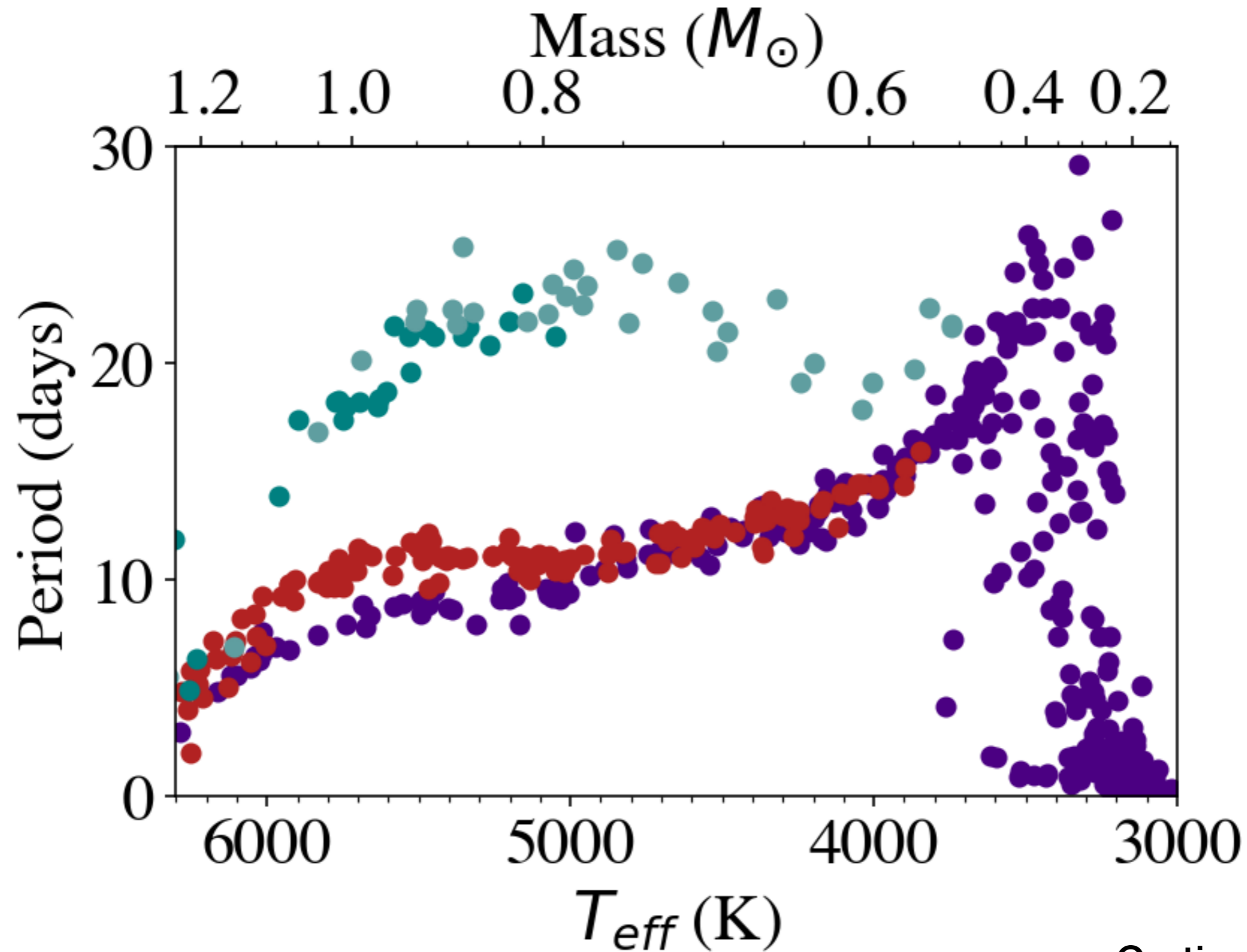
Problem #4



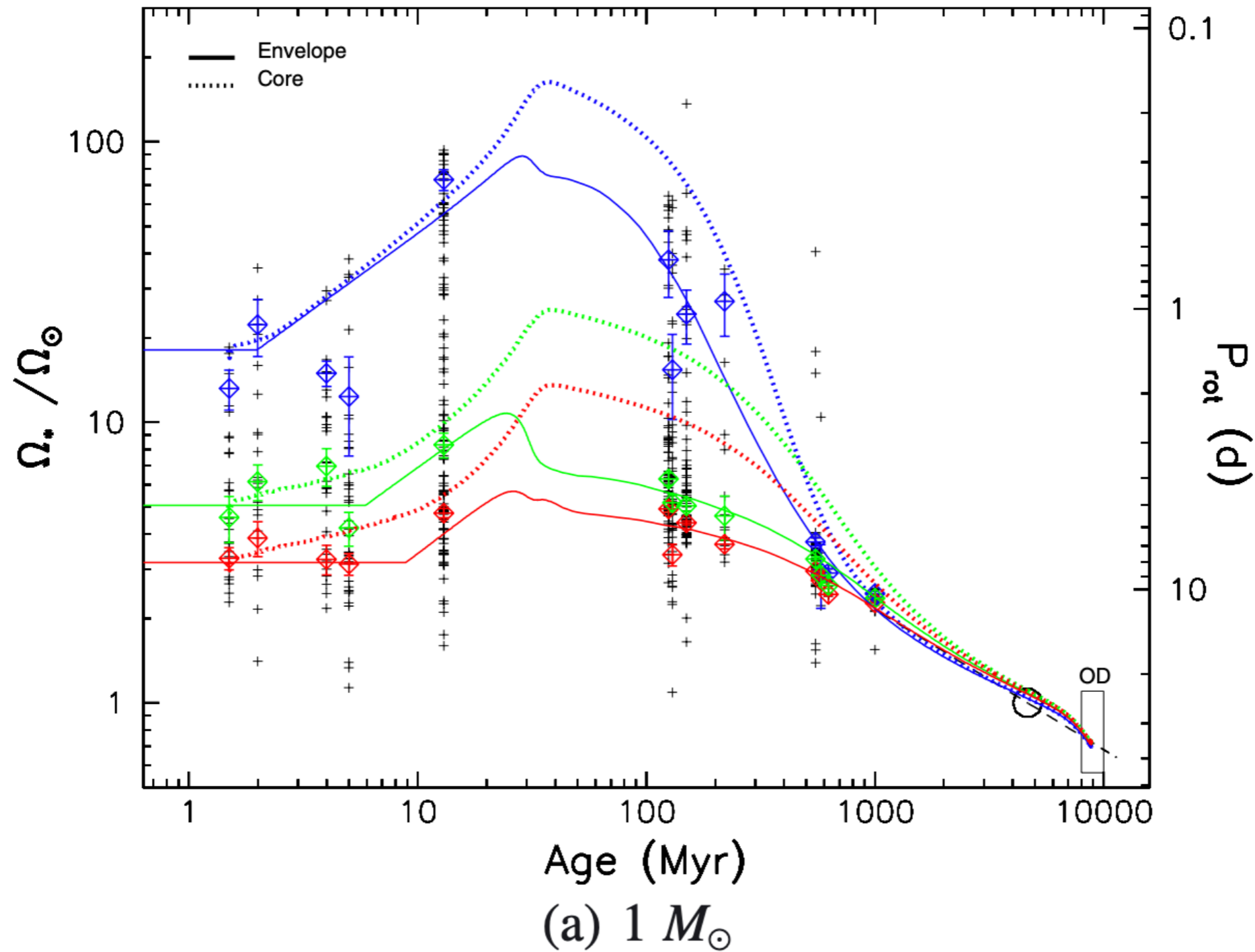
Problem #4



Problem #4

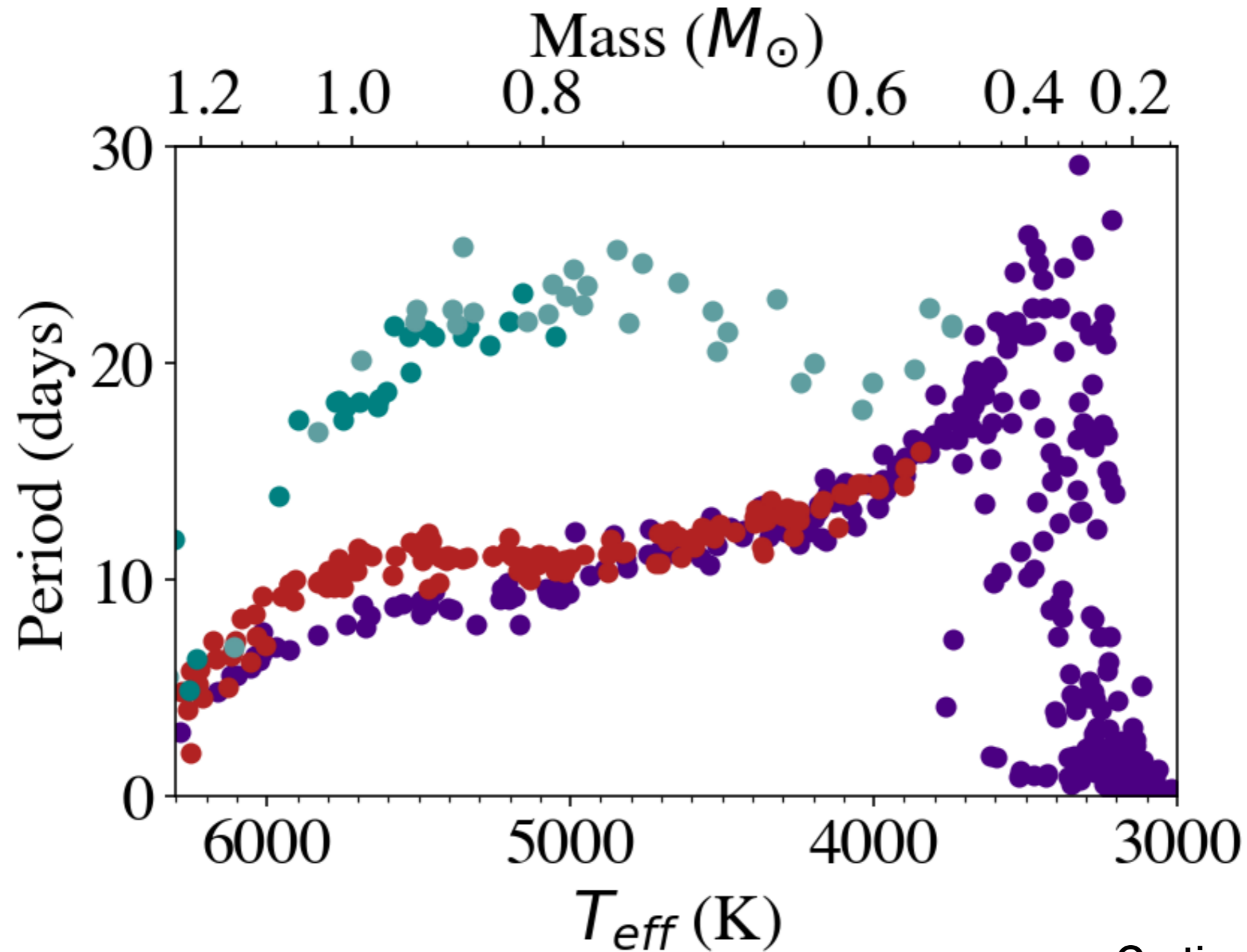


Allow envelopes and cores to “decouple”

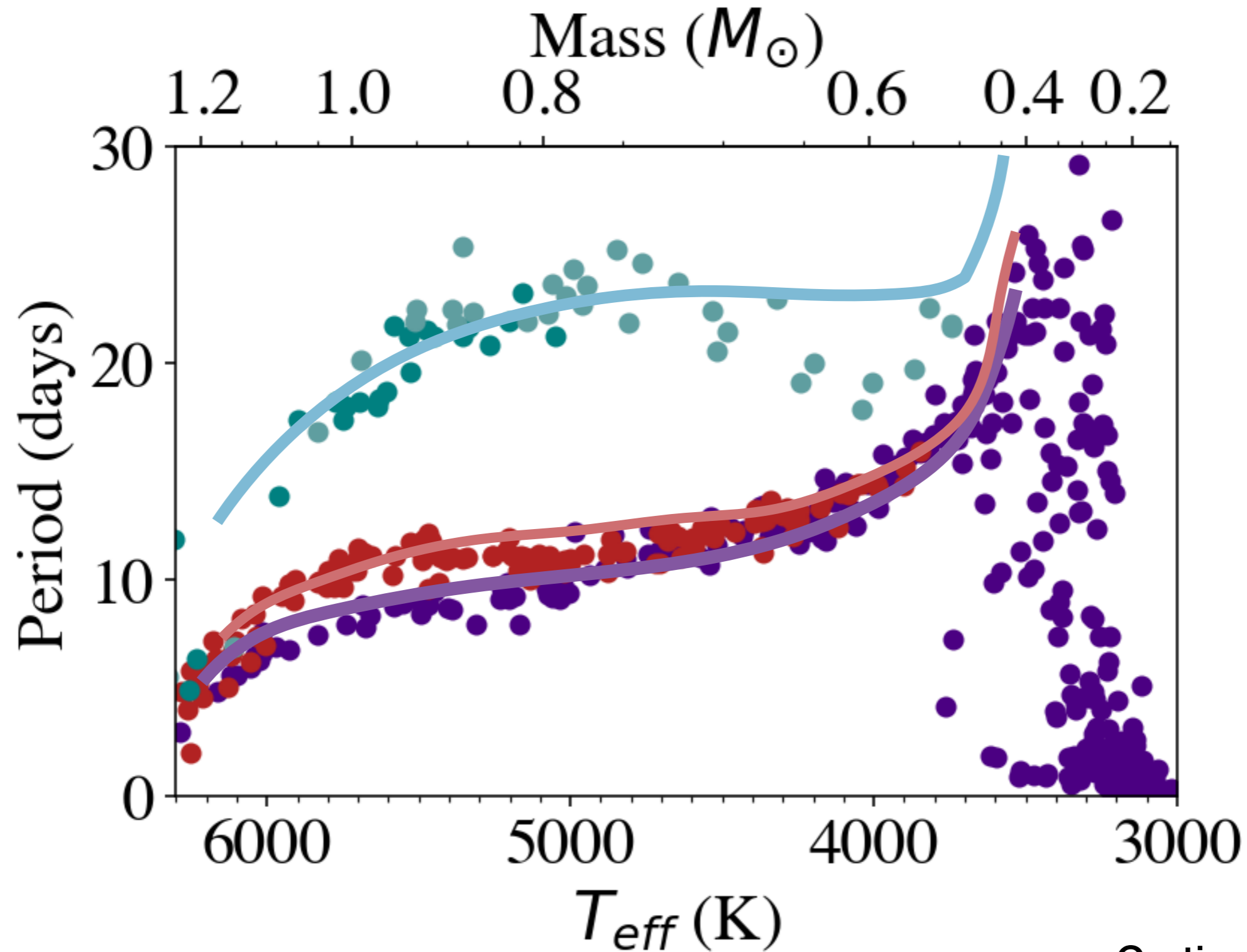


MacGregor & Brenner 1991, Krishnamurthi et al. 1997, Gallet & Bouvier 2015,
Denissenkov & Pinsonneault 2010, Spada & Lanzafame 2020

Problem #4



Problem #4



Rotation cares about the things you care about: internal transport, magnetic field generation, convection zone properties, stellar structure