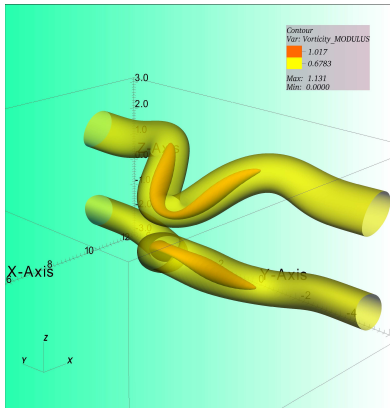


# Vortex Stretching as a Mechanism for Quantum Kinetic Energy Decay

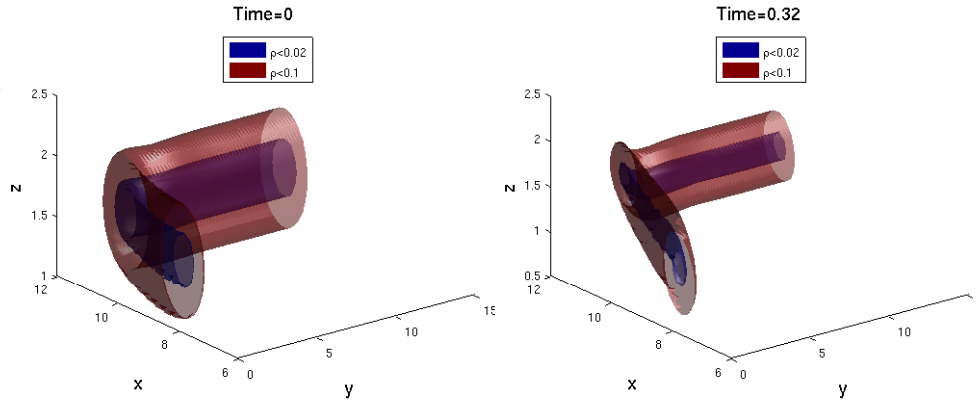
Robert M. Kerr, Warwick University



At reconnection, Kelvin wave moves out. Time=1

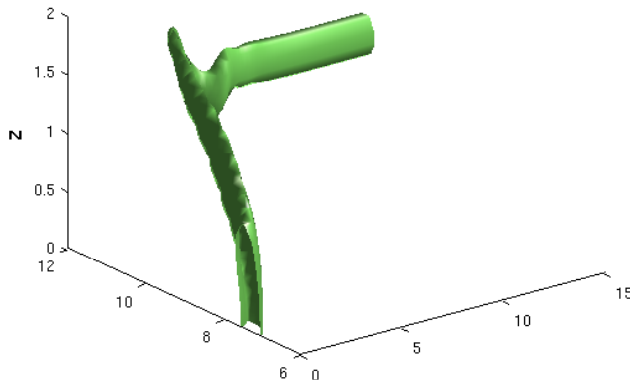
**Left: Classical Euler, isosurfaces of high vorticity magnitude.**

**Right/below: Quantum, isosurfaces of low density.  $T = .64, 1, 2-3.2$**

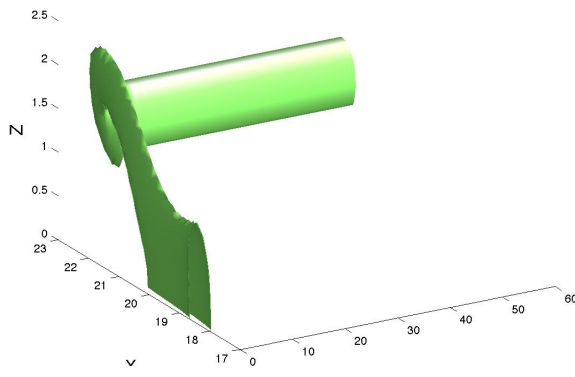


Time=1.5  $\zeta=0.05$

Time=3  $\zeta=0.05$

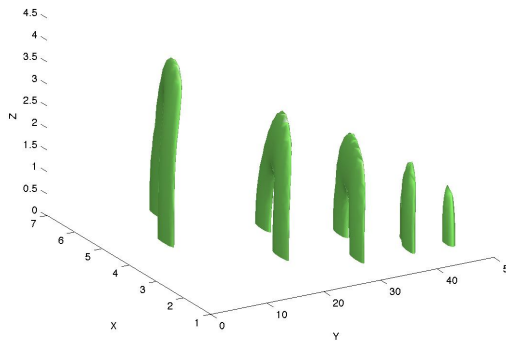
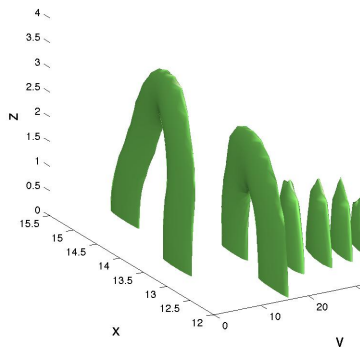
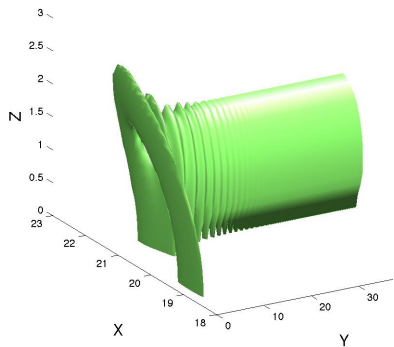
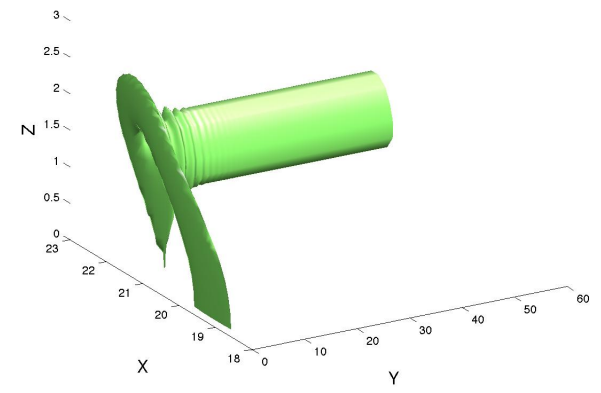


Time=4.5  $\zeta=0.05$



Time=24

$\zeta=0.05, l=4.8, \text{case: vcooh3}$



Quantum fluids are **compressible**. In any compressible fluid, vortex cores have low density. Example: **Tornados**

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- Differences are many and similarities are proving more difficult to show.
- If this could be shown: Then these events could be the building blocks for all of classical turbulence, **with minimal viscosity**, including: **finite energy dissipation and a  $-5/3$  energy spectrum.**

## Classical ENCORE?

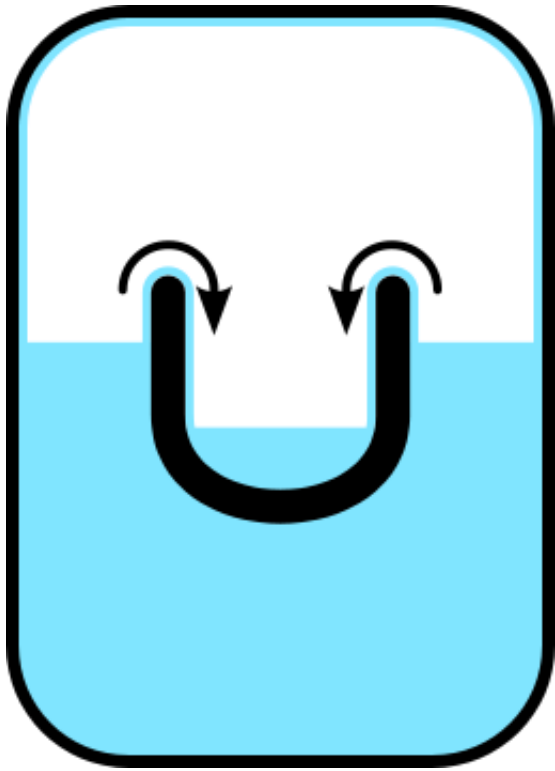
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## Classical ENCORE?

- **With only minimal viscous reconnection singularities one could get:**
- **An energy cascade** including:  
Finite energy dissipation and a  $-5/3$  energy spectrum.
- **In the compressible case**, a mechanism for the efficient generation of acoustic radiation during reconnection.

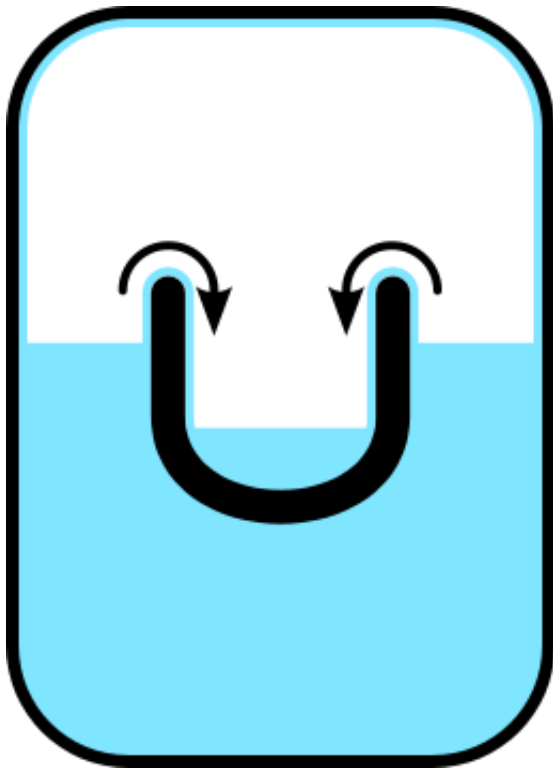
If this was understood, then we might have a better handle on controlling noise from jet engines, a high priority for the UK aeronautics industry.



**Early super-**

**fluid  
experiments  
1937-38**

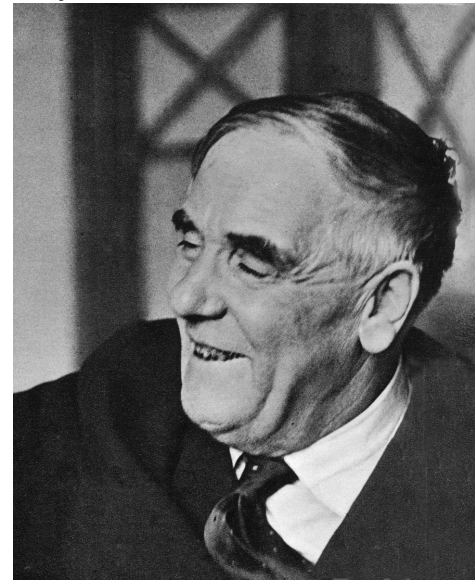
Superfluid Helium II will "creep" along surfaces in order to find its own level - after a short while, the levels in the two containers will equalize. The Rollin film also covers the interior of the larger container; if it were not sealed, the helium II would creep out and escape.



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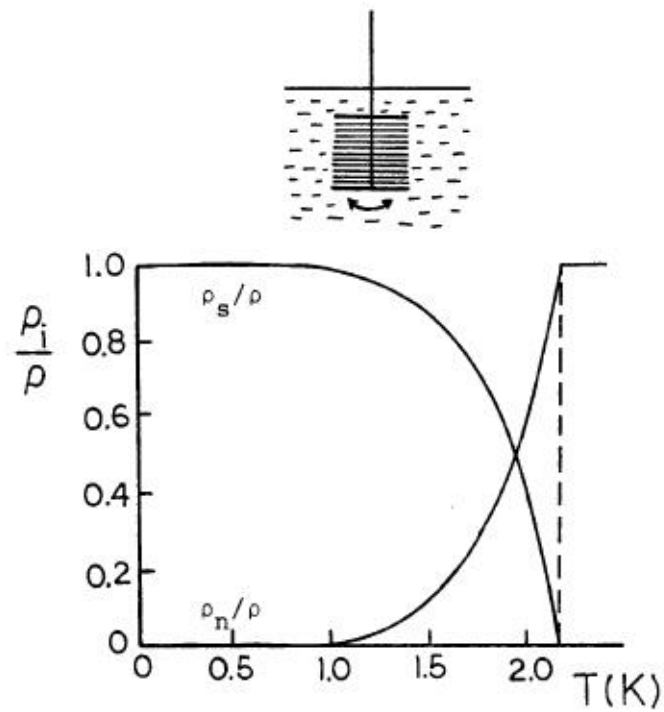
Cambridge

Pyotr Leonidovich Kapitsa

In 1934 he developed new and original apparatus (based on the adiabatic principle) for making significant quantities of liquid helium.

Then, on a visit to the USSR, his passport was confiscated. He stayed in Moscow and Rutherford allowed his Cambridge equipment to be bought.

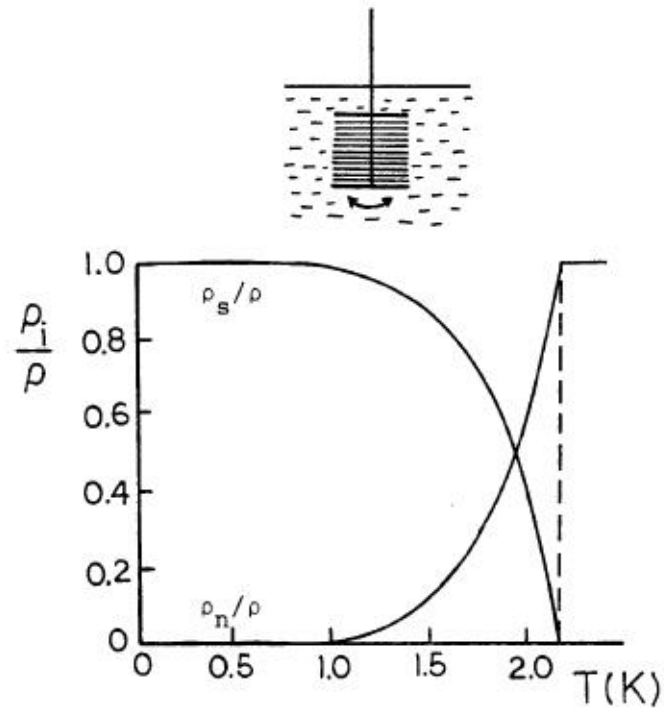
This led to a new series of experiments, eventually in 1937 discovering **superfluidity**.



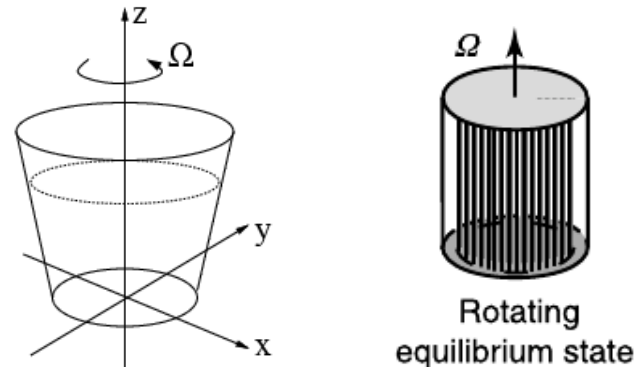
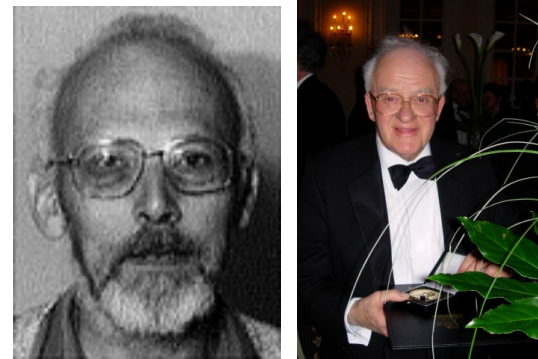
The original experiment by Andronikashvili for the densities of normal and superfluid based on Landau's two-fluid model. Andronikashvili was the first to notice that above certain flow rates (through openings) that the superfluid resisted motion in a manner analogous to a classical, viscous fluid.

## Heat currents and Rotating buckets

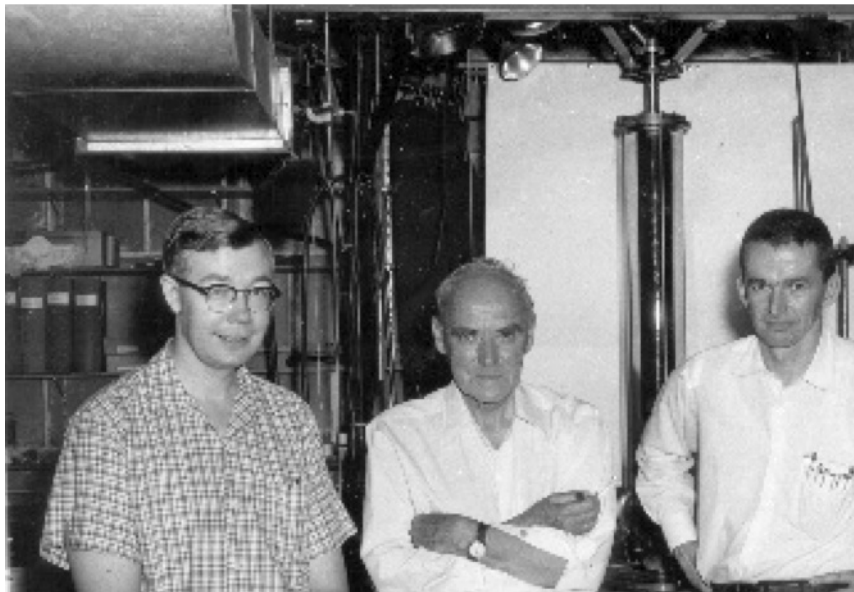
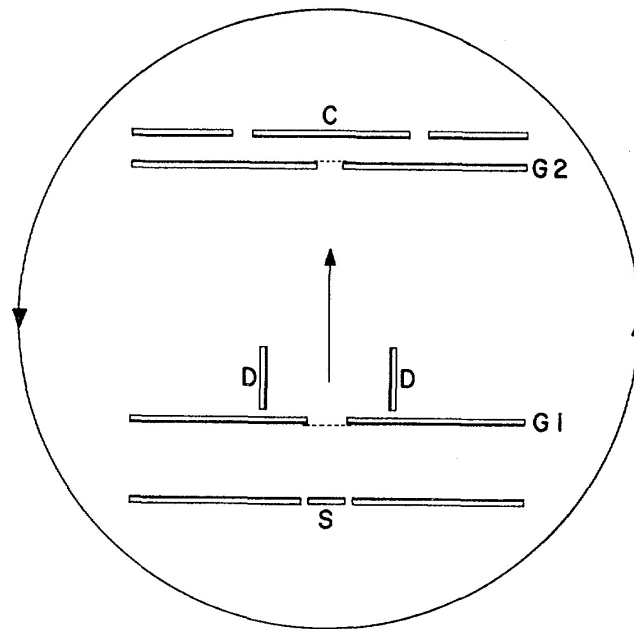
- Heat currents and mutual friction: 1950s
- Through a series of experiments measuring heat currents, Henry Hall (left) and Joe (W.F.) Vinen (right) established the idea of **mutual friction between the quantum and normal fluids along vortex cores**.
- First use of second-sound: waves carrying oscillations between the normal and quantum parts of a superfluid.



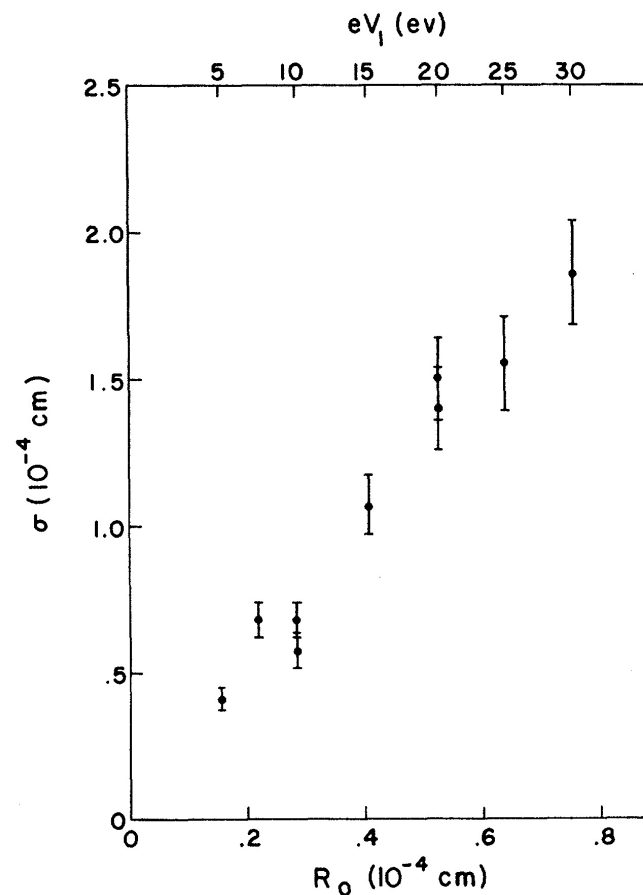
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- **Rotating buckets and ions: 1960s/70s**
- Donnelly/Schwarz at Chicago created one, then fired ions at it.
- The ions have vortex rings attached, so these are really vortex ring scattering experiments.
- Ions from source S were fired through the superfluid vat between the electrodes G1 and G2.



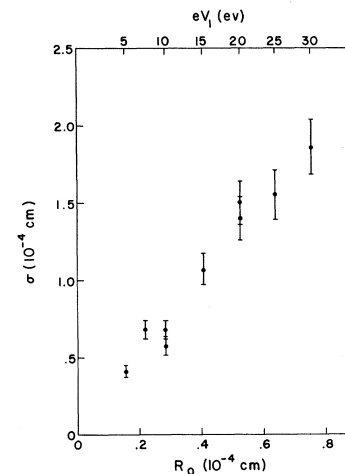
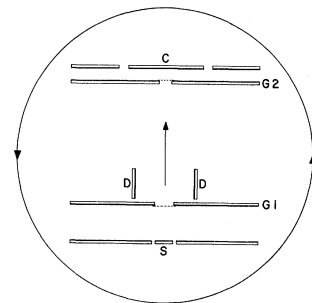
Russ Donnelly (Chicago), GI Taylor (Cambridge), Dave Fultz (Chicago)



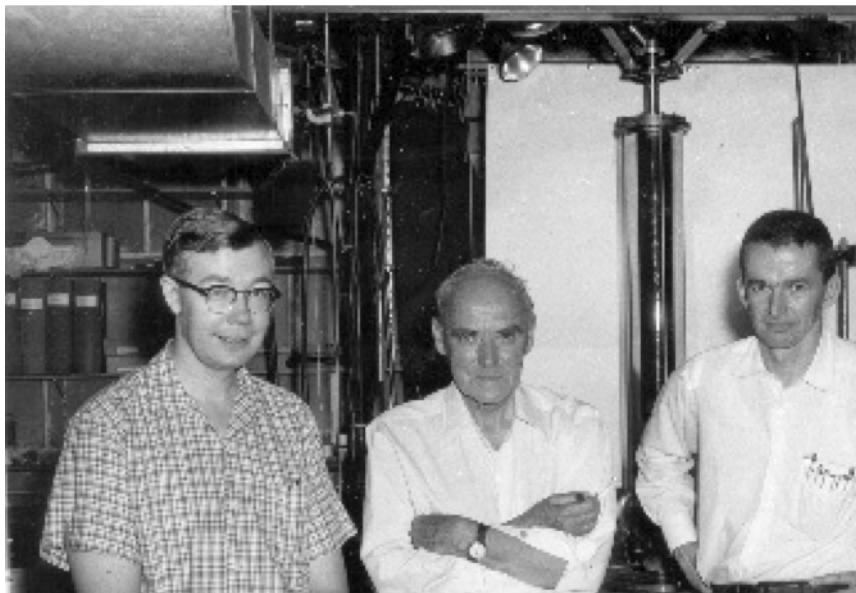


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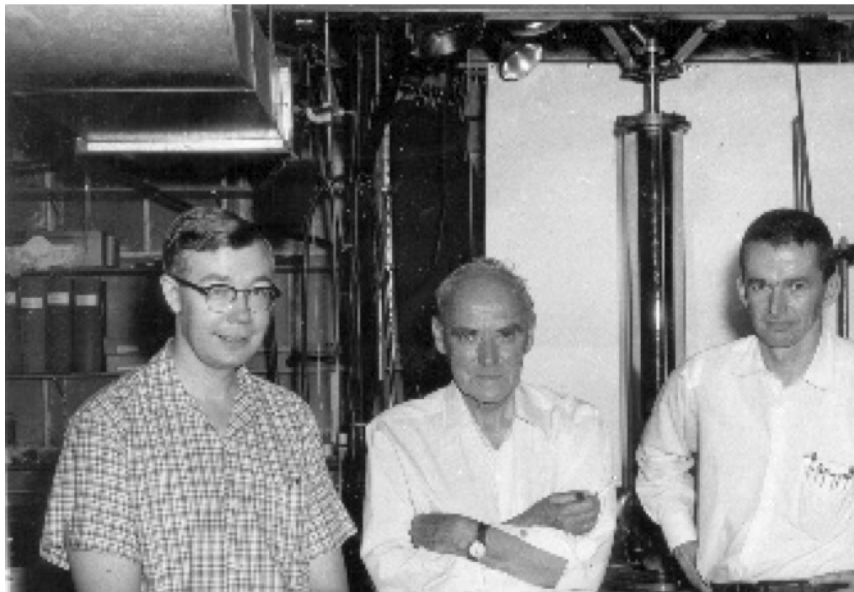
- More voltage meant more energy and bigger, but slower, rings.
- Experiment established the possibility of quantum vortices distinct from those due to rotation and that they were very thin:
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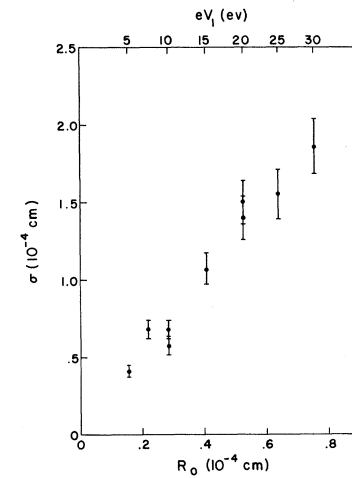
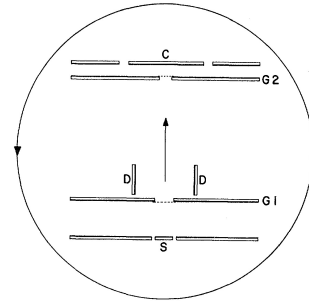
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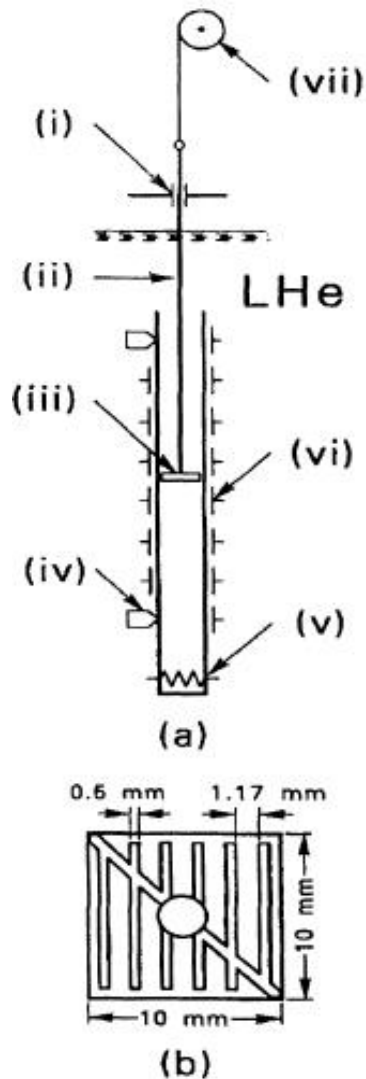
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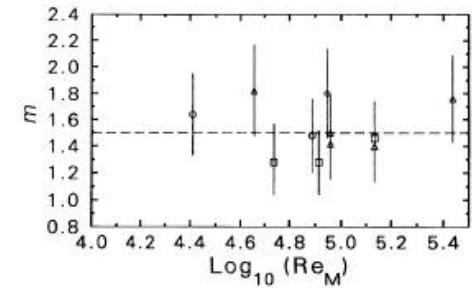
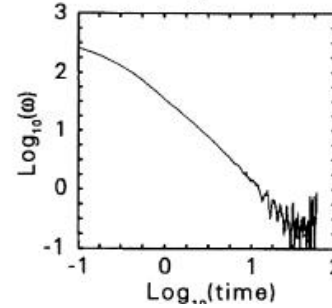
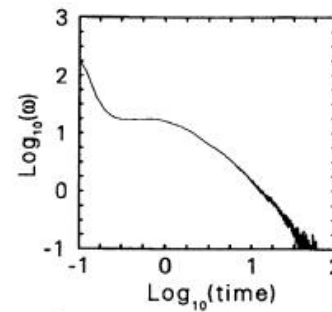


- More voltage meant more energy and bigger, but slower, rings.
- Experiment established the possibility of quantum vortices distinct from those due to rotation and that they were very thin: That is there was no interaction unless the vortex rings hit a central vortex.
- **This is the basis of the LIA myth, but that is the wrong interpretation.**
- This approach to generating vortices in the interior, and detecting them, is the basis of the recent Golov and Walmsley experiments.



Smith, Donnelly, Goldenfeld, Vinen Phys. Rev. Lett. (1993)

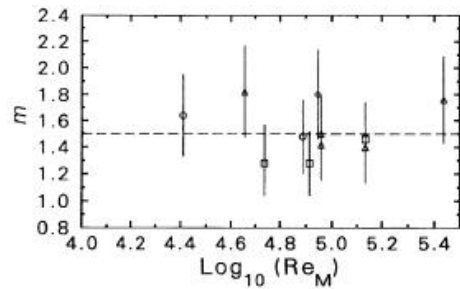
(a) Layout of apparatus used to study grid turbulence. (i) Vacuum seal, (ii) 5/16 rod, (iii) grid, (iv) germanium thermometer, (v) counterflow heater, (vi) second sound transducer pair, and (vii) stepper motor. (b) Detail of grid construction.



- Two experiments (counterflow versus grid) show the same decay at long times. **This obeys  $\ell \sim t^{-m}$  with  $m = 1.5 \pm 0.2$ .**

- This corresponds to a classical decay of enstrophy of  $\Omega \sim t^{-3}$  **which corresponds to a classical kinetic energy decay of  $KE \sim t^{-2}$**

**However, despite serious flaws, the theoretical interpretation was still based on the existence of the normal fluid component.**



- Decay was based on the two-fluid model. In addition to the ideal superfluid component, there was a classical (maybe not Navier-Stokes) normal fluid component, and mutual friction to couple the two.
- Quantum turbulence was not expected to be similar to classical turbulence.
- Note: The  $KE \sim t^{-2}$  law is the classical decay law only when there are periodic boundary conditions. (Reference: Kerr, 1981, PhD thesis, Cornell) This condition and decay rate are never realised in a physical system with real boundaries.

# 1975: Why my Chicago professors said to go to Cornell

DAVID M. LEE, DOUGLAS D. OSHEROFF and BOB RICHARDSON



Richardson at cryostat



Nobel toast of David Lee  
and Bob Richardson

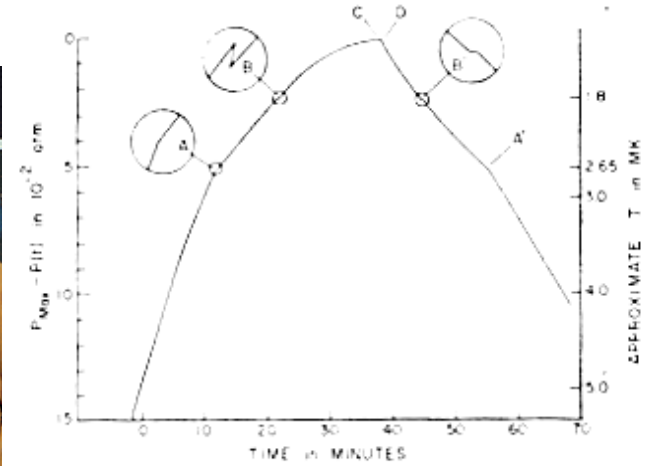


FIG. 2. Time evolution of the pressure in the Pom-eranchuk cell during compression and subsequent decompression.

Phase diagram from 1972  
PRL.



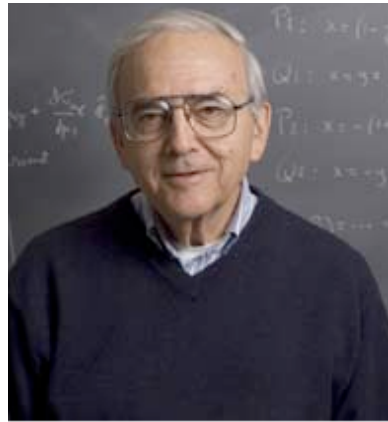
Doug Osheroff

## And also the Renormal-ization Group

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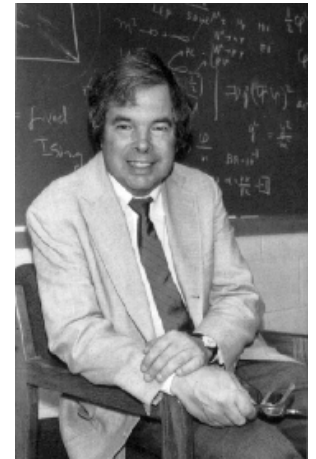
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Ben Widom



Michael Fisher



Ken Wilson

**Euler**

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\nabla p \quad (1)$$

$$\rho = 1 \quad \underbrace{\nabla \cdot \mathbf{u} = 0}_{\text{incompressibility}}$$

What is integrated is vorticity:  $\boldsymbol{\omega} = \nabla \times \mathbf{u}$

$$\frac{\partial \boldsymbol{\omega}}{\partial t} + \underbrace{(\mathbf{u} \cdot \nabla) \boldsymbol{\omega}}_{\text{advection}} = \underbrace{(\boldsymbol{\omega} \cdot \nabla) \mathbf{u}}_{\text{vortex stretching}} \quad (2)$$

**Gross-Pitaevskii**

$$\rho \frac{D\mathbf{v}}{Dt} = -\nabla p + \nabla \Sigma \quad (3)$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

Integrate:  $\psi = \sqrt{\rho} e^{i\phi}$ ,  $\mathbf{v} = \nabla \phi$

$$\frac{1}{i} \frac{\partial}{\partial t} \psi = 0.5 \nabla^2 \psi + 0.5 \psi (1 - |\psi|^2) \quad (4)$$

## Euler

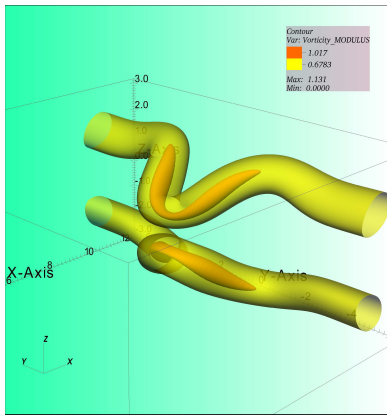
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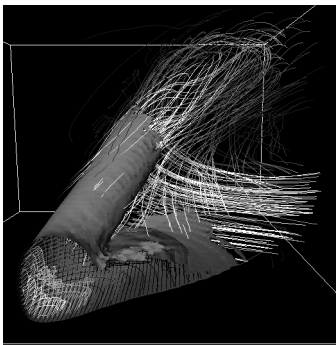
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3D anti-parallel

Full domain, Early times.

Kinks, then reconnect



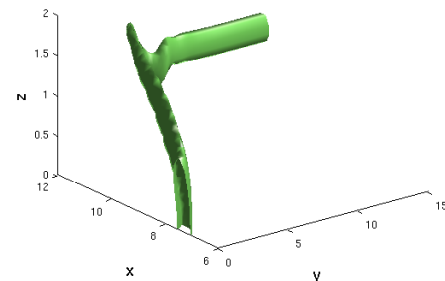
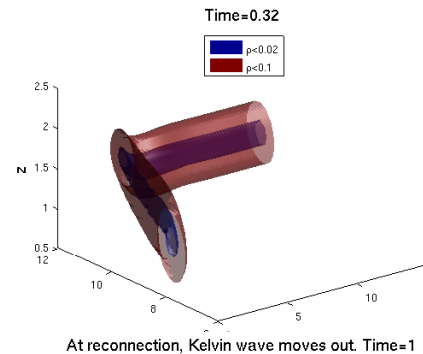
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$$\frac{1}{i} \frac{\partial}{\partial t} \psi = 0.5 \nabla^2 \psi + 0.5 \psi (1 - |\psi|^2) \quad \text{cubic nonlinearity}$$

- Conserves mass  $M = \int dV |\psi|^2$
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- A **semi-classical velocity** can be defined by the gradient of the phase of the wave function.  $\mathbf{v} = \nabla \phi$ . This gives potential flow.

If  $\psi = \sqrt{\rho} e^{i\phi}$ , then by the Madelung transformation:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0, \quad p = \frac{V_0}{2m^2} \rho^2, \quad \Sigma_{jk} = \left( \frac{\hbar}{2m} \right)^2 \rho \frac{\partial^2 \log \rho}{\partial x_j \partial x_k}$$

$$\rho \frac{D\mathbf{v}}{Dt} = -\nabla \mathbf{p} + \nabla \Sigma \quad \text{a strange type of barotropic Euler equation.}$$

(I use  $E_0 = 0.5$ ,  $V_0 = 0.5$ ,  $\hbar = m = 1$ .)

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To these equations, people usually add a **normal fluid** component whose details are still debated, but is certainly some type of barotropic fluid with a classical viscous term, i.e. not Hamiltonian and dissipates energy. **Its role is discussed below.**

## How can there be circulation?

- **A quantum fluid is irrotational except along infinitely thin defects, quantum vortices.**
  - If the wavefunction is  $\psi = \sqrt{\rho}e^{i\phi}$ , consider points around which  $\phi$  changes by  $2\pi$ .
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- In a classical fluid, vorticity is distributed uniformly in space and the circulation about vortex cores depends on the initial condition.
  - For an ideal classical fluid (**Euler equations**), these values of the circulation are constant along Lagrangian trajectories.

With viscosity (**Navier-Stokes**) vortices **reconnect**, the topology of circulation changes and **not** follow Lagrangian trajectories.

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– Around these defects  $\int \mathbf{v} \cdot d\mathbf{s} = 2\pi$  and the **quantum** circulation is defined as  $\Gamma = 2\pi\rho_0$  **for all vortices.**

- In a classical fluid, vorticity is distributed uniformly in space and the circulation about vortex cores depends on the initial condition.

– For an ideal classical fluid (**Euler equations**), these values of the circulation are constant along Lagrangian trajectories.

With viscosity (**Navier-Stokes**) vortices **reconnect**, the topology of circulation changes and **not** follow Lagrangian trajectories.

- **What is the analogy** for a quantum fluid for how in a viscous fluid the circulation changes in time?

There will be **reconnection** associated with how the topology of the zero density lines changes.

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- **A quantum fluid has no dissipation.**
- **Its Hamiltonian includes components described as the kinetic, quantum and interaction energies**

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These observations suggest that despite different physics, classical and quantum turbulence share many properties. **Turbulence in both has notable similarities.**

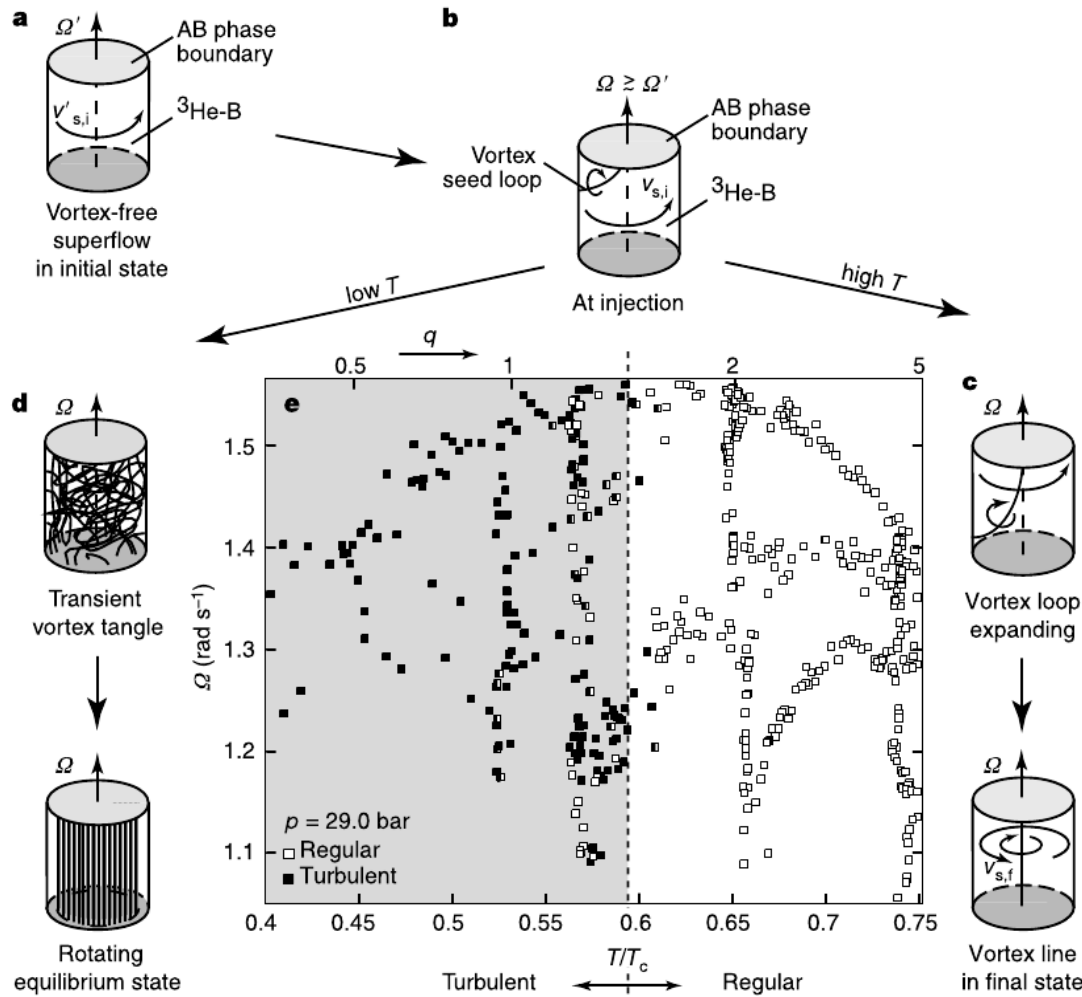
**These include:**

- There is a fluid-like equation (Madelung transformation)
- Circulation
- Energy transfer
- Reconnection

## Ultra-cold $^3\text{He}$

An intrinsic velocity-independent criterion for superfluid turbulence. Finne et al (mostly **Helsinki**) Nature 242, 1022 (**2003**).

Figure 3 Measurement and phase diagram of turbulent superflow in  $^3\text{He-B}$ .

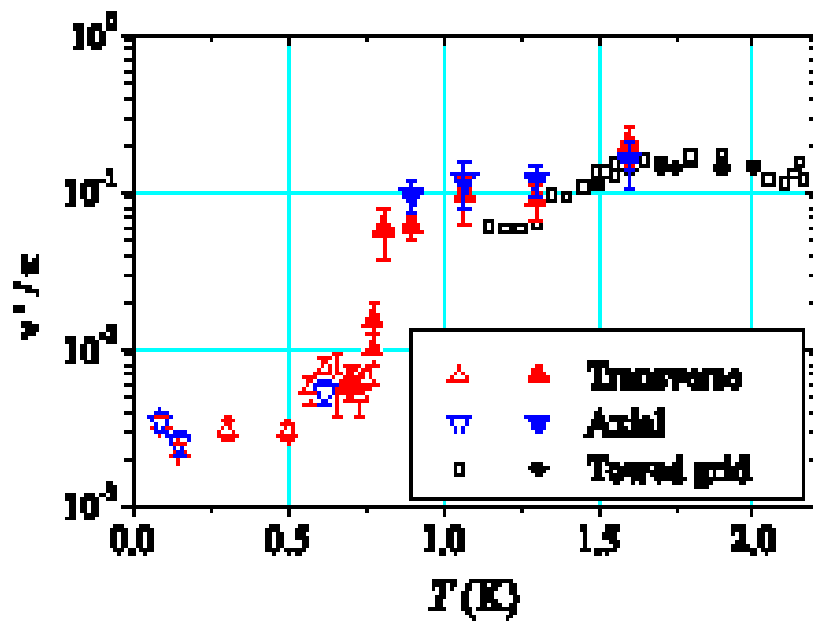


**b**, A few ( $\Delta N$ ) vortex loops are injected and, after a transient period of loop expansion, the number of rectilinear vortex lines  $N_f$  in the final steady state is measured. It is found to fall in one of two categories. **c** and **d**

**d**,  $\Delta N \ll N_f \leq N_{eq}$ , turbulent loop expansion. This process leads to a total removal of the macroscopic vortex-free superflow as the superfluid component is forced into solid- body-like rotation

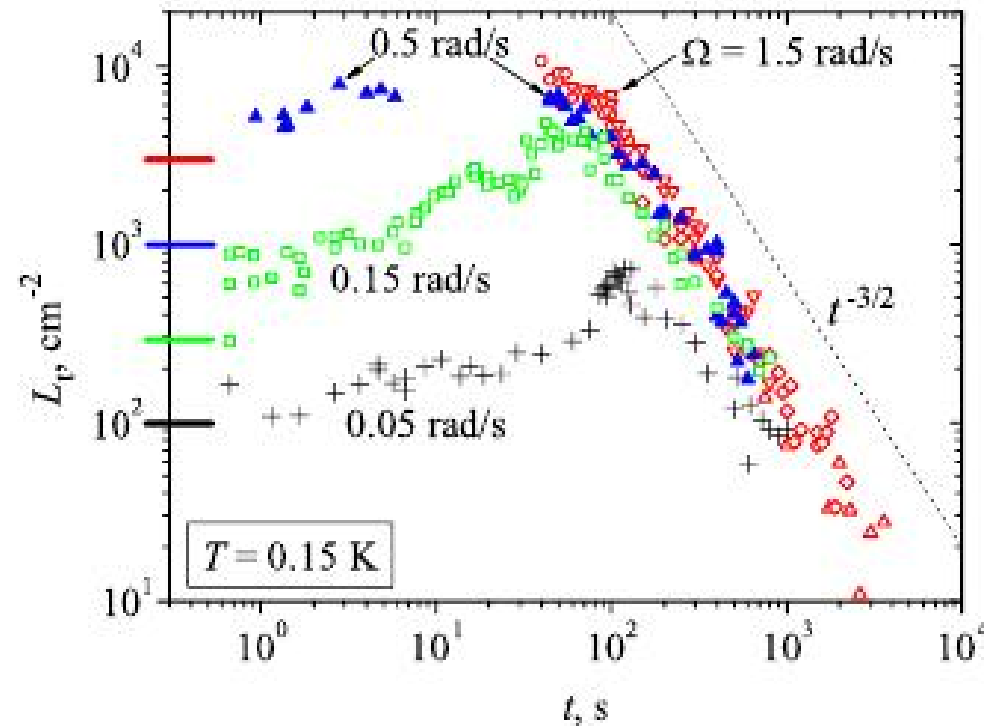
I learned of this result in 2007 from Dieter Vollhardt, Augsburg. I haven't quite figured out how they can claim this is equivalent to the -3/2 decay rate.

Ultra-cold Walmsley, Golov etc (2007).



Left:

FIG. 5 The effective kinematic  $\nu'$  after a spin down from  $\Omega = 1.5$  rad/s measured in the transverse ( $\triangle$ ) and axial ( $\nabla$ ) directions. Closed (open) triangles correspond to measurements with free ions (charged vortex rings). Error bars specify the uncertainty of fitting. Squares and diamonds: second sound measurements of grid turbulence [12,22].

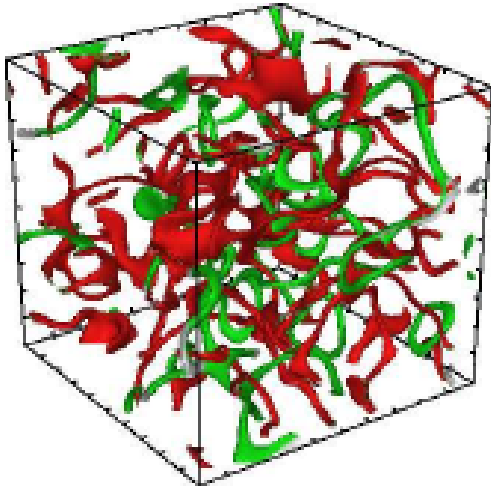


Right: FIG. 2  $L_t(t)$  at  $T = 0.15$  K for four values of  $\Omega$ . Average electric fields used for  $\Omega = 1.5$  rad/s: 5 V/cm ( $\diamond$ ), 10 V/cm ( $\triangle$ ), 20 V/cm ( $\circ$ ), 25 V/cm ( $\nabla$ ). The dashed line shows the dependence  $t^{-3/2}$ . Horizontal bars indicate the equilibrium values of  $L$  at  $\Omega=1.5, 0.5, 0.15, 0.05$  rad/s (from top to bottom).

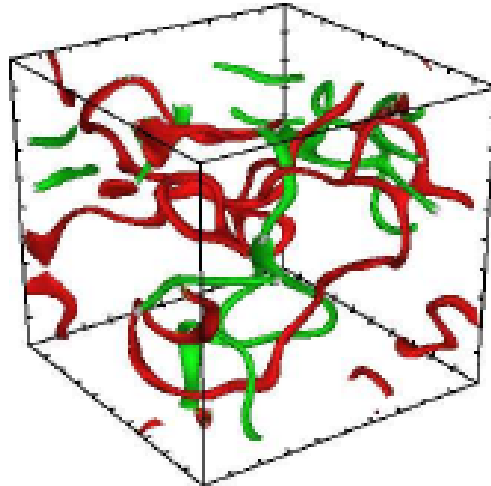
Now the normal fluid explanation cannot be used and the decay still looks classical. Where is the energy going?

What people usually think superfluid turbulence looks like. Berloff review (2007).

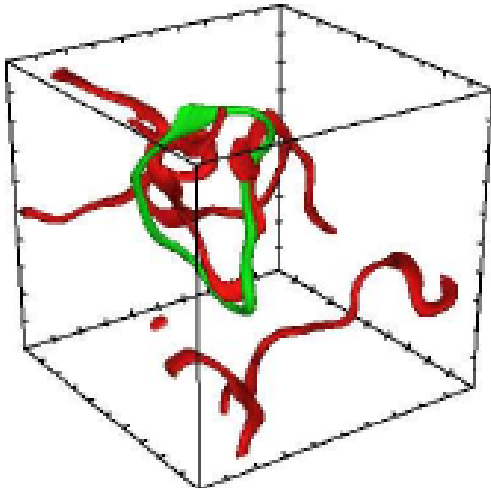
$t = 500$



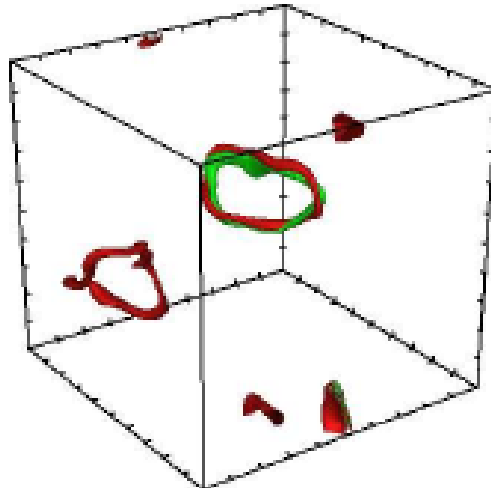
$t = 1000$



$t = 1500$

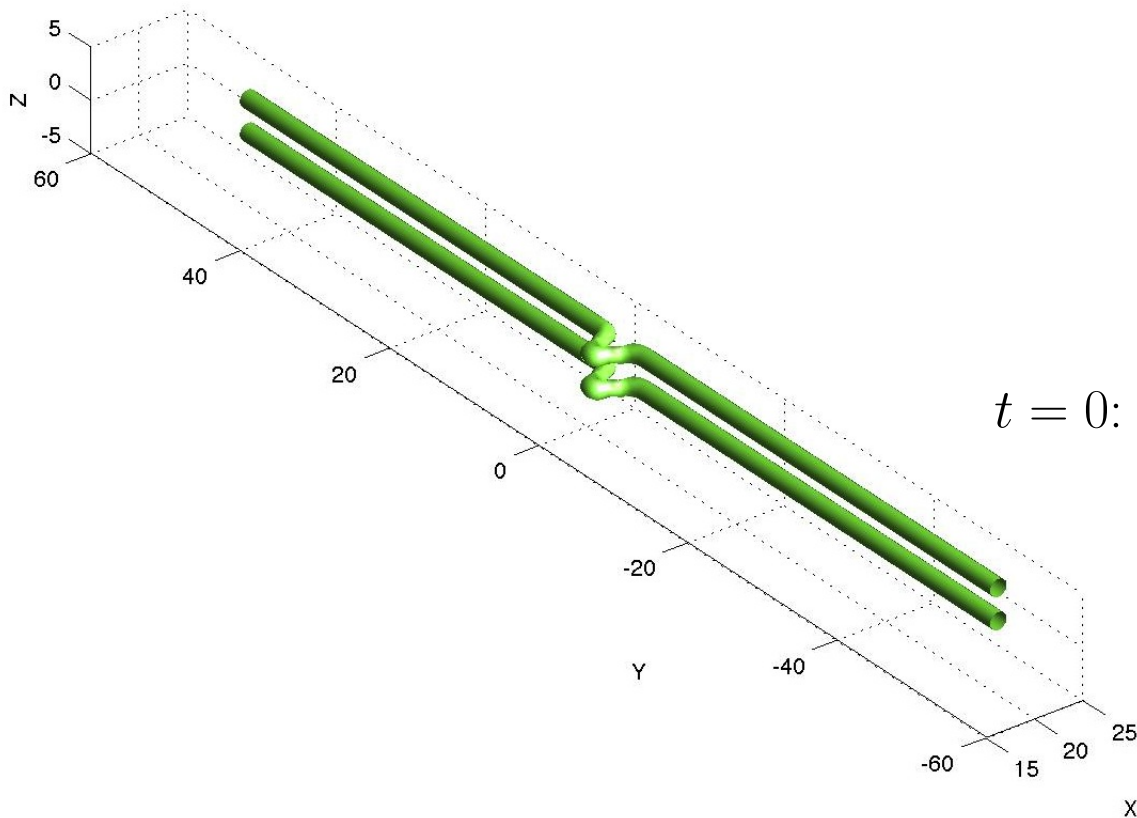


$t = 2000$



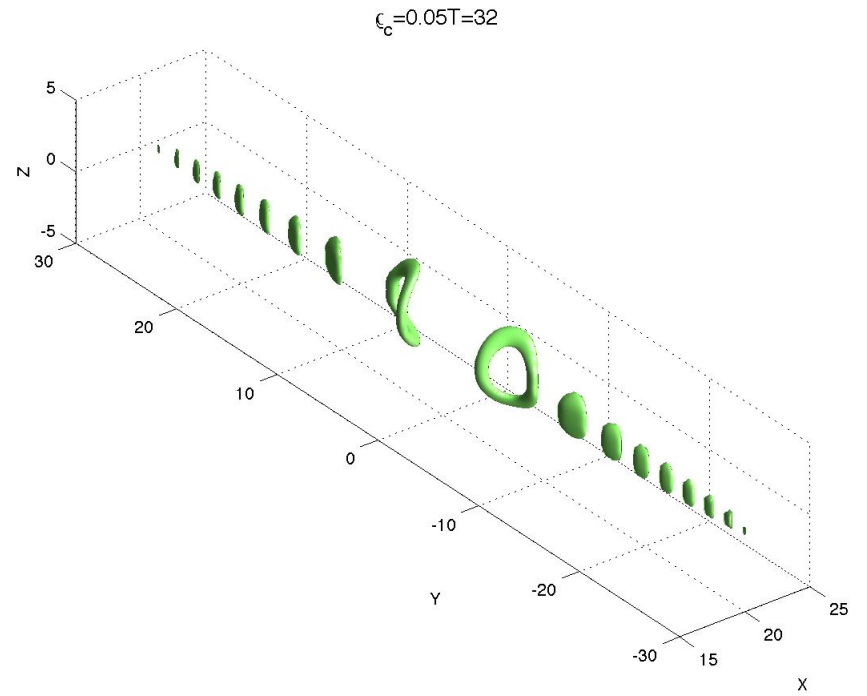
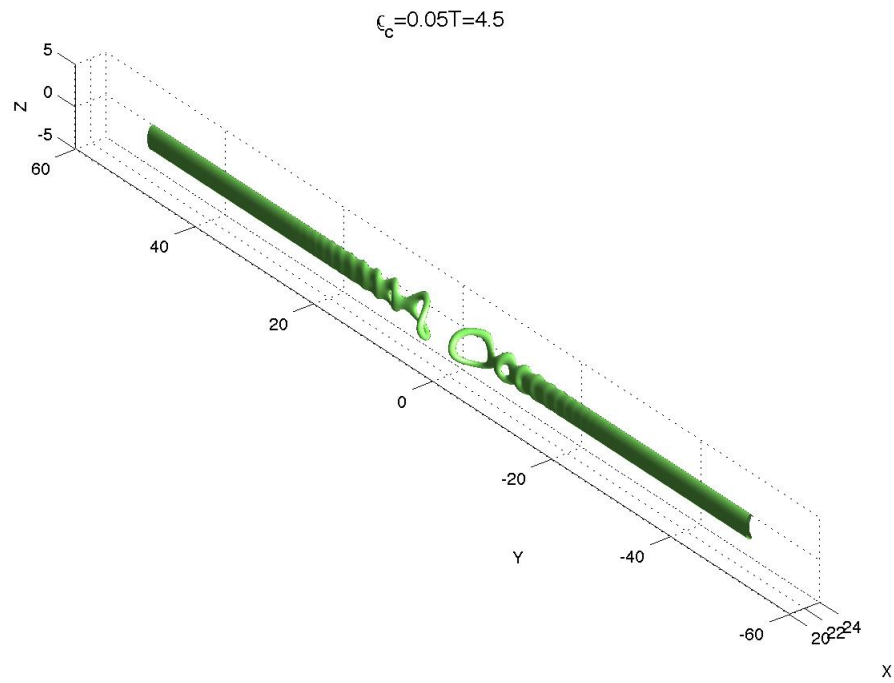
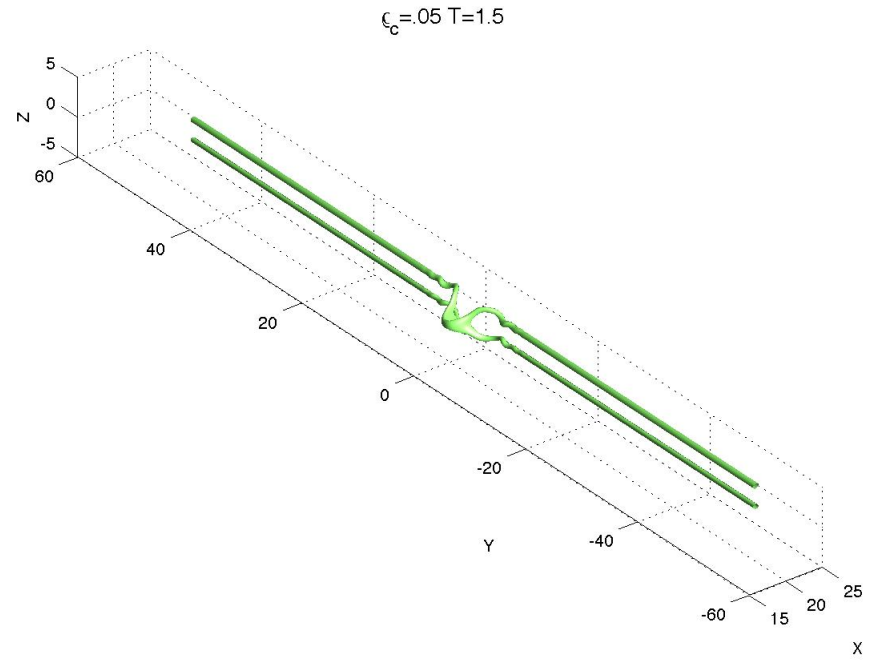
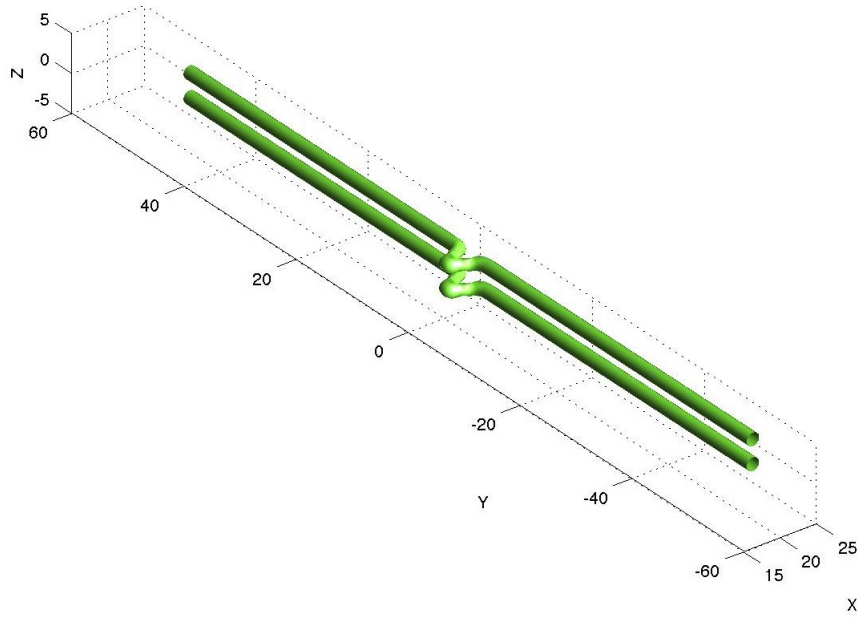
- **My numerics:**  $128 \times 512 \times 64$  for  $8\pi \times 16\pi \times 4\pi$  domain.
  - Spectral, – 3rd-order Runge-Kutta on nonlinear term.
  - Integrating factor on linear term. – Timestep chosen by  $\nabla\psi$ .
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  - Using symmetries, I simulation only 1/2 of 1 of 2 vortices.
- Still, to get smooth functions at the boundaries, I found that the initial condition needs to be a superposition of 24 image vortices.
- This suppresses anomalous waves generated by discontinuities in the I.C.

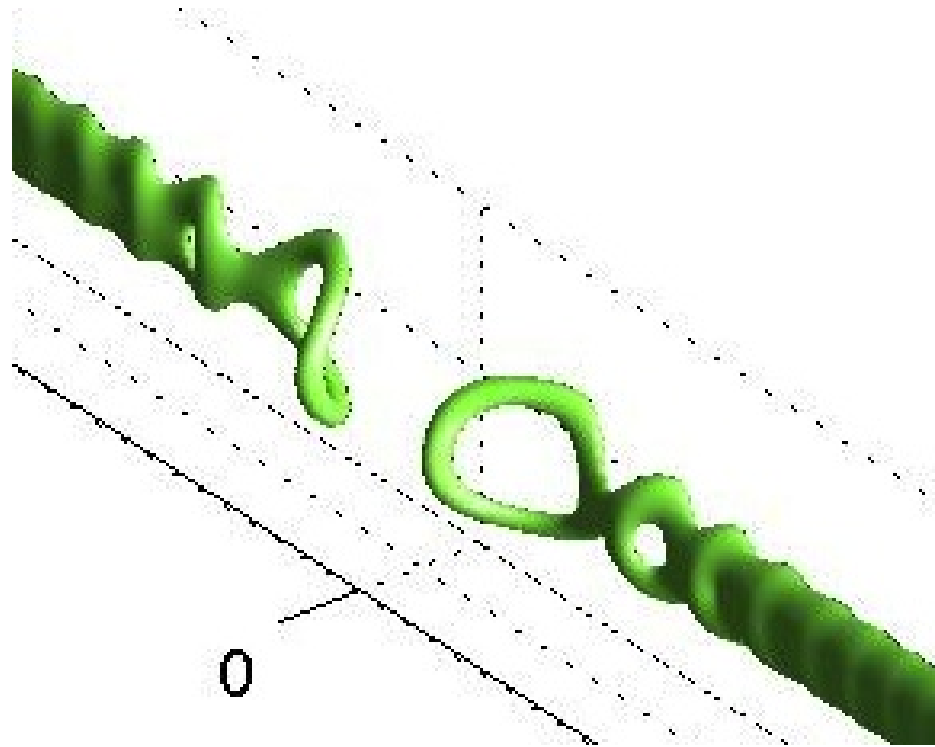
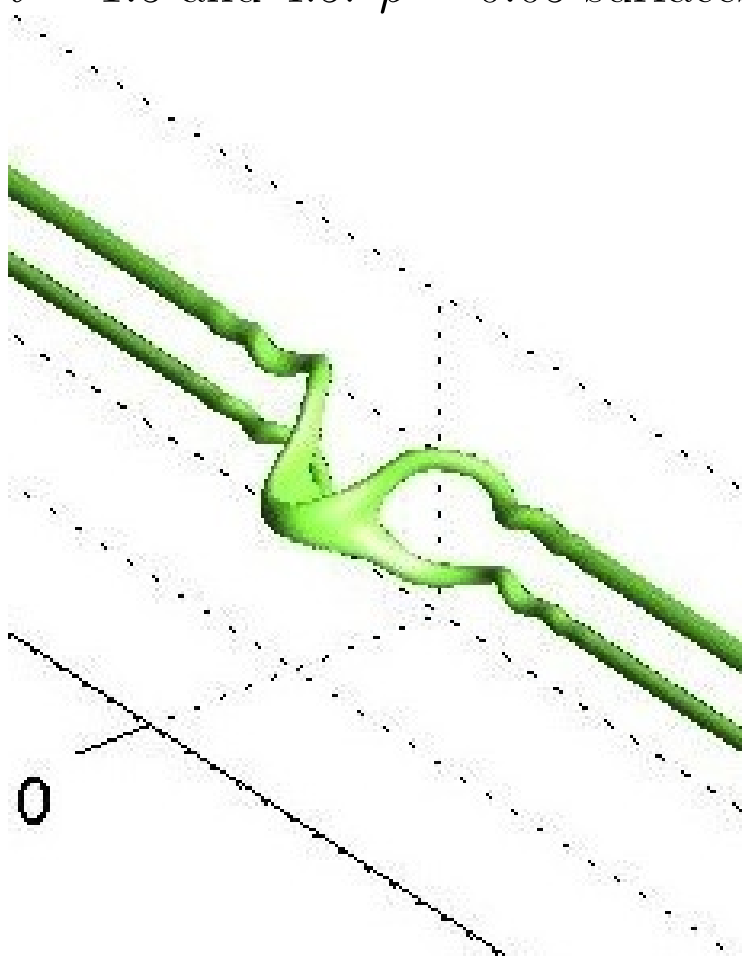


$t = 0$ :  $\rho = 0.05$  surfaces. Full domain

$t = 0, 1.5, 4.5, 32$ :  $\rho = 0.05$  surfaces. Full domain



$t = 1.5$  and  $4.5$ :  $\rho = 0.05$  surfaces.



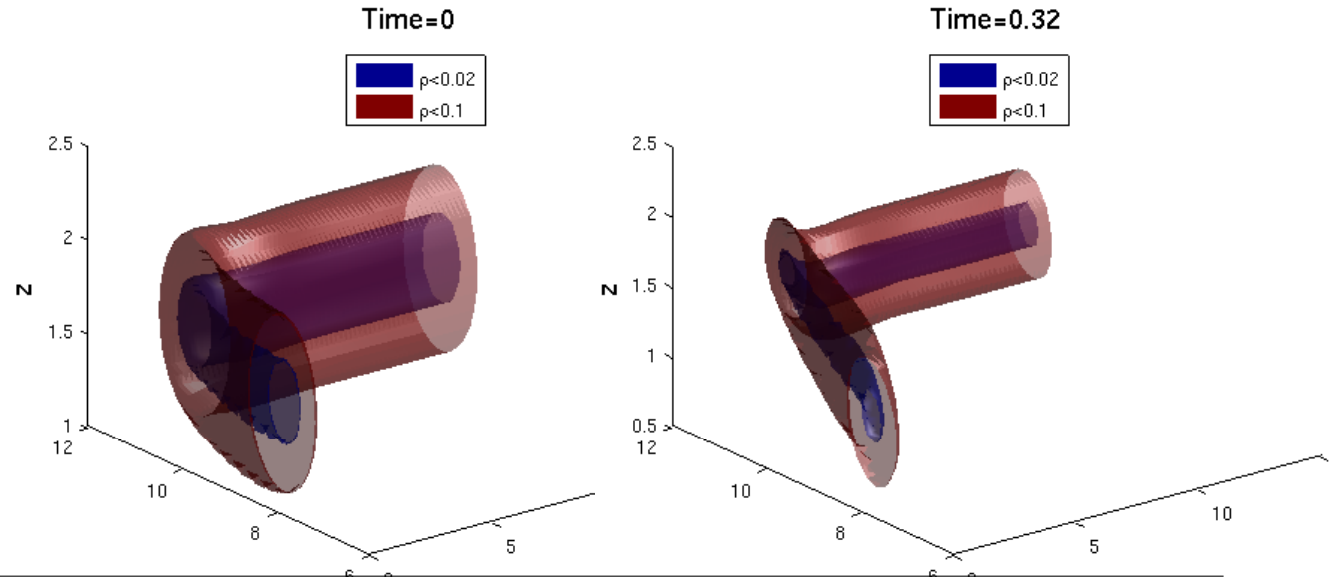


# How do we get to $t=1.5$ ?

## 1.1 Early times: $\rho = \text{constant}$ surfaces.

- Recall background:  $\rho \approx 1$ , at vortex cores  $\rho \equiv 0$ .
- $\rho = 0.02$
- $\rho = 0.1$
- Below:  $\rho = 0.02$

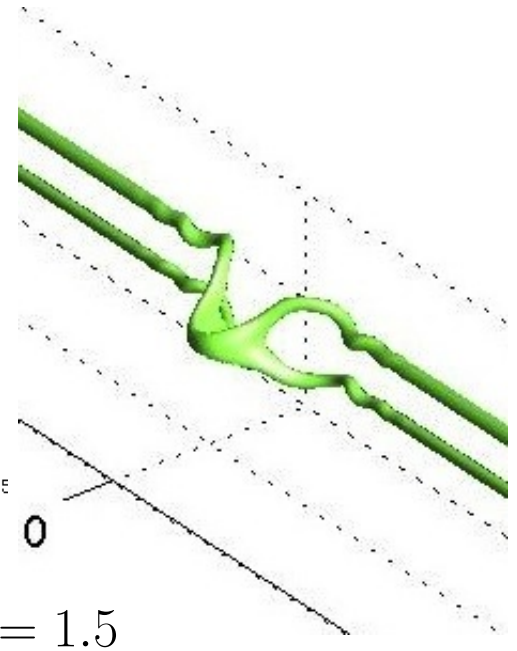
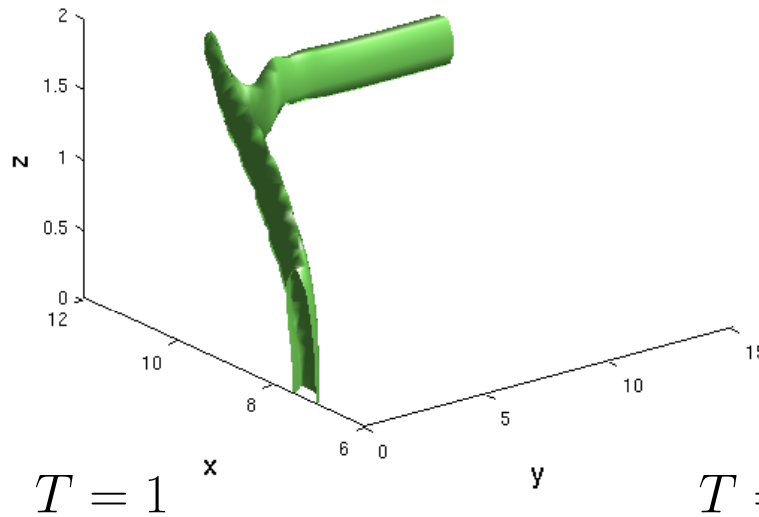
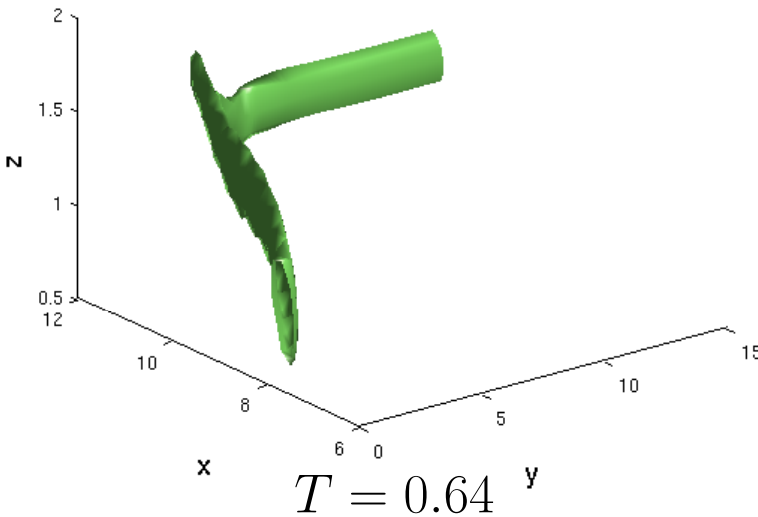
Plots from case v3\_646464.



Note  $\rho = 0$  hole on  $x - z, y = 0$  plane. By  $t = 1$ :  $\rho = 0$  hole on  $y = 0$  plane extends to  $z = 0$ .

Pre-reconnection, beginning of Kelvin wave. Time=0.64

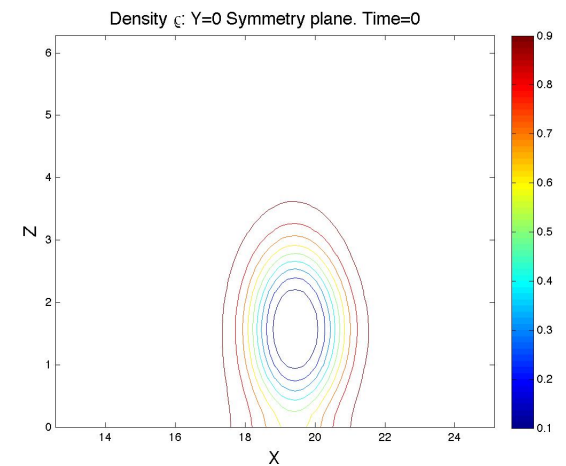
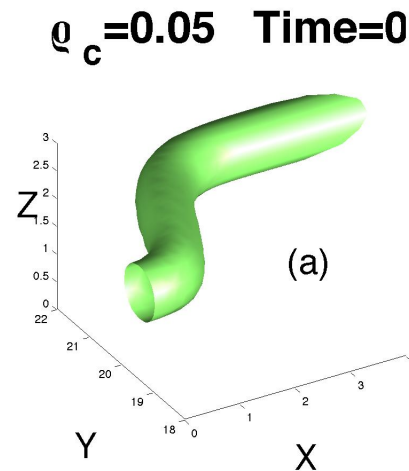
At reconnection, Kelvin wave moves out. Time=1



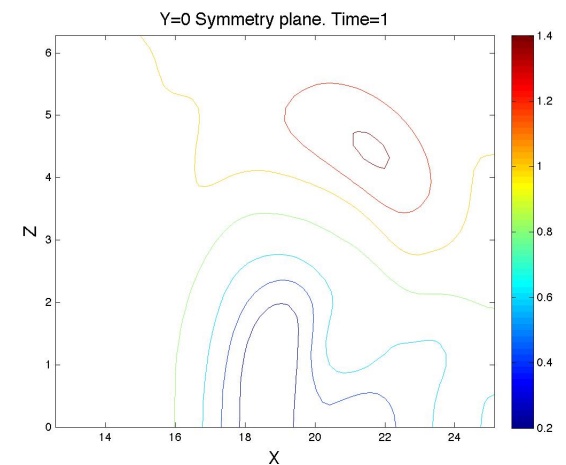
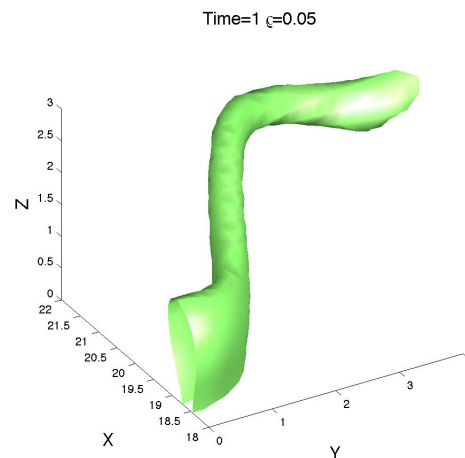
Foreshortened views.

## Zooming in $\rho = 0.05$ isosurfaces. Larger calculation

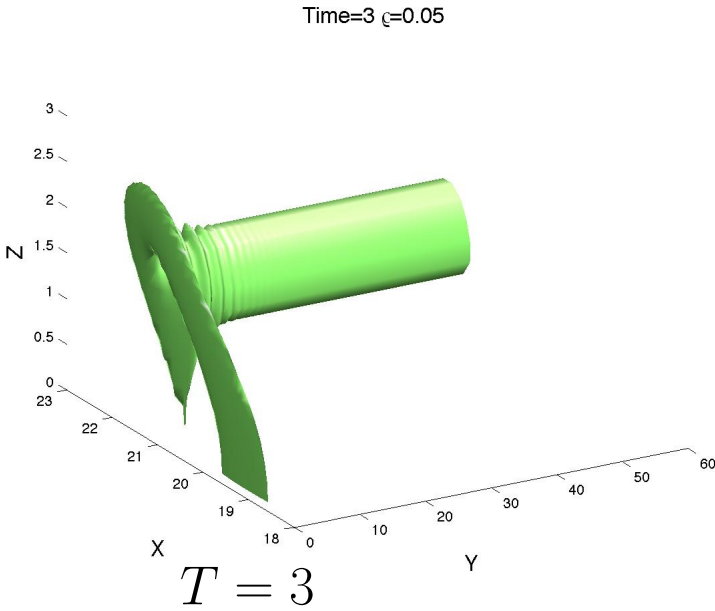
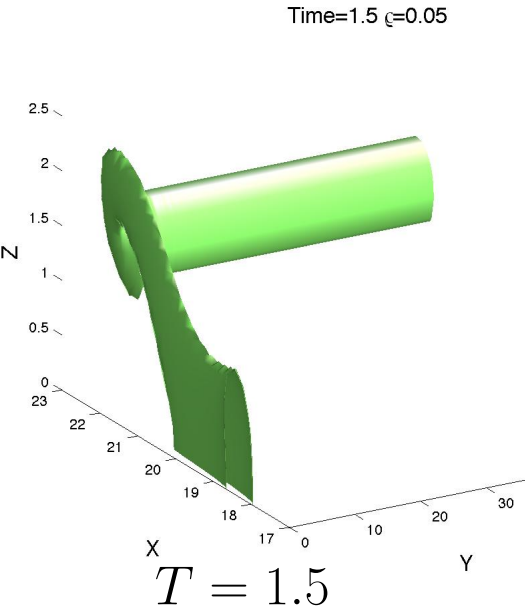
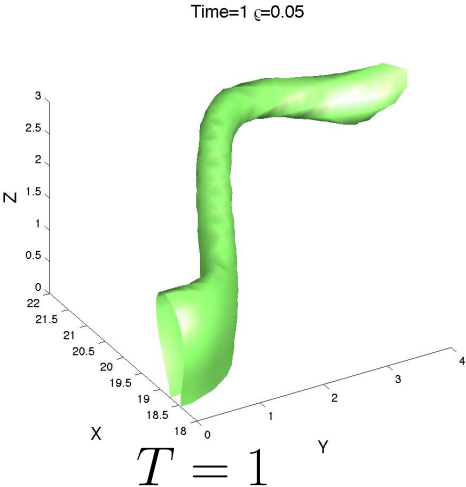
$t = 0$ . Left: 3D. Right: Density contours through the  $y = 0$  symmetry plane of maximum perturbation. Recall that this is only one half of one of two mirrored vortices. A complete geometry for a similar initial condition appears in Bustamante & Kerr (2008).



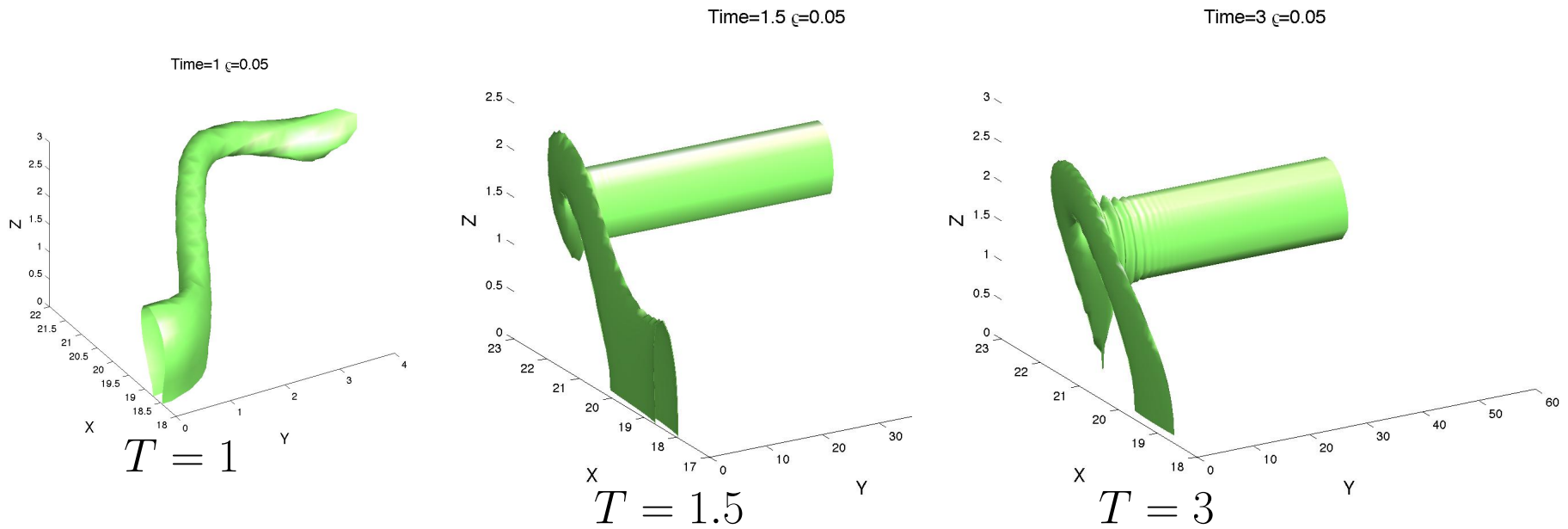
$t = 1$ . Left: 3D. Right:  $y = 0$ ,  $\rho$  contours. Vortex stretches as in a classical fluid, causing the isosurface to thin, most evident for the segment near  $y = z = 2$ . Near  $y = 0$  at this time, the stretching has pulled sufficient density away that an extended gap of  $\rho \approx 0$  is opening up. Reconnection will occur across this gap.



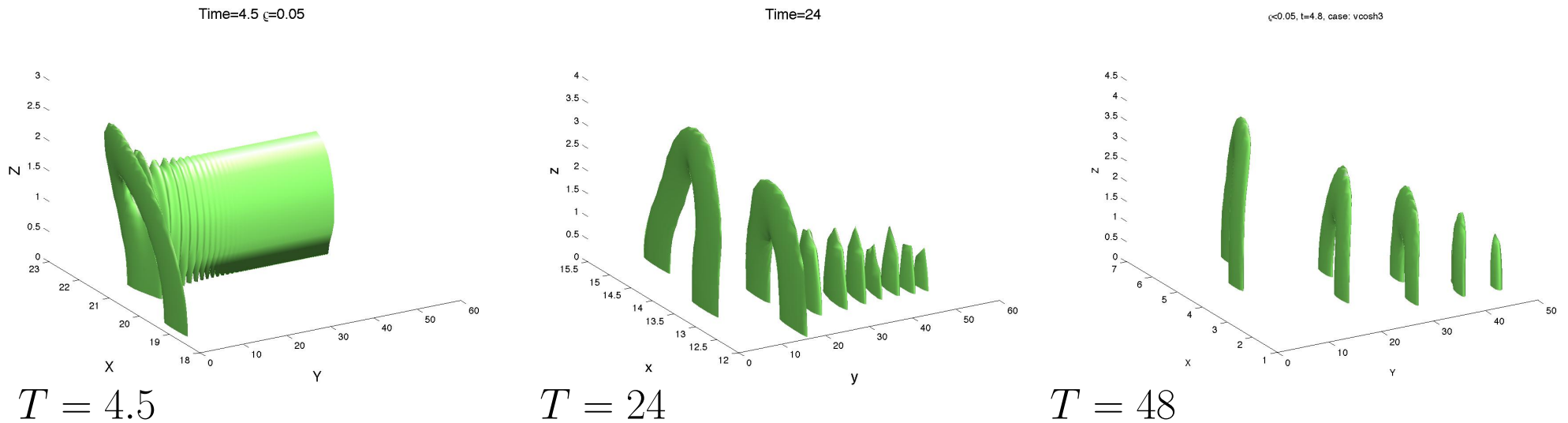
# 1.2 Intermediate time: Waves on vortices, which deepen



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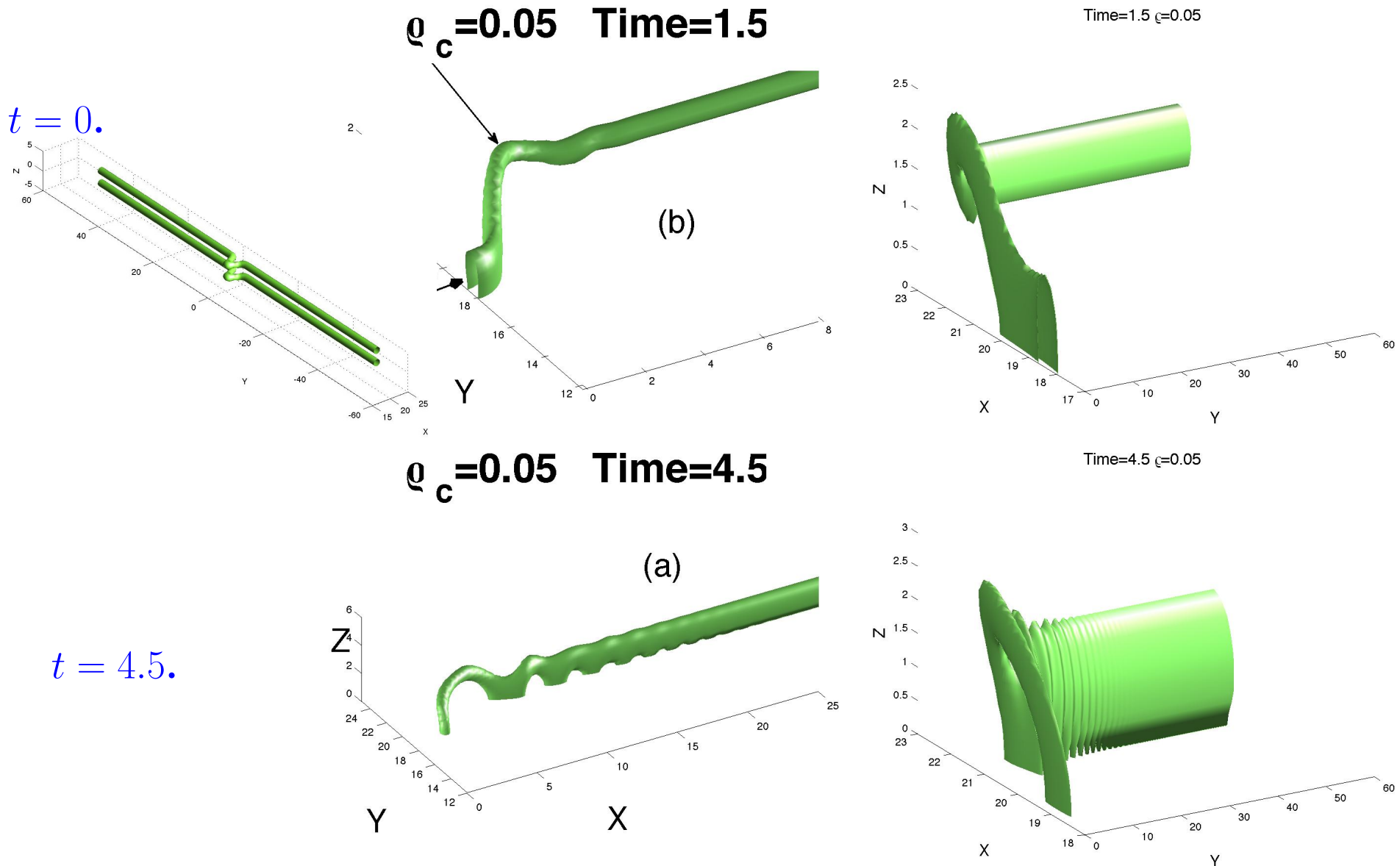


## 1.3 Late time: One ring separates, **then more**, then leave system



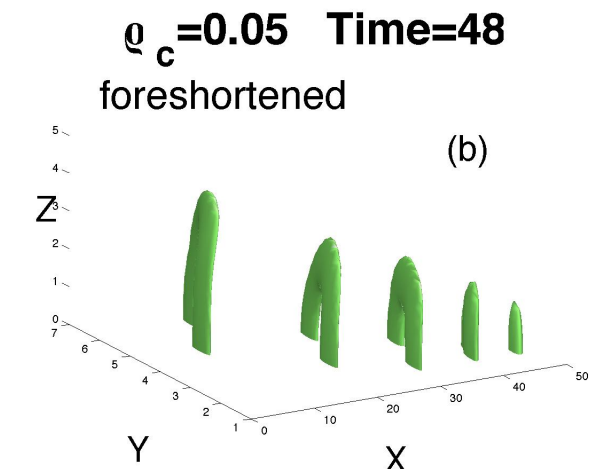
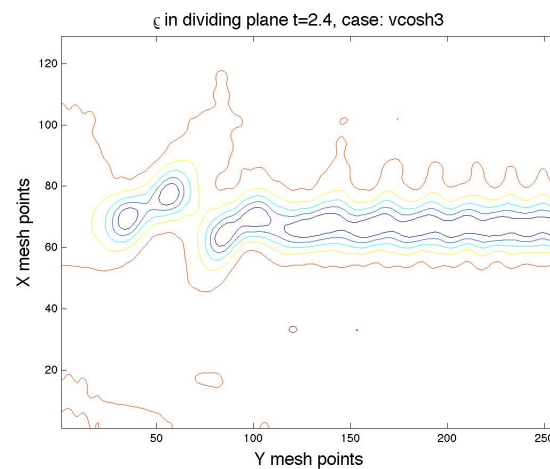
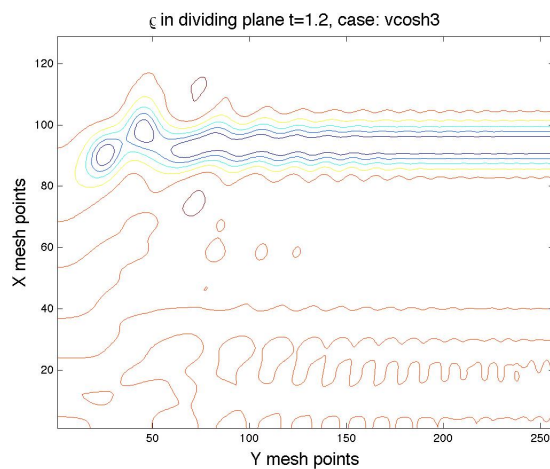
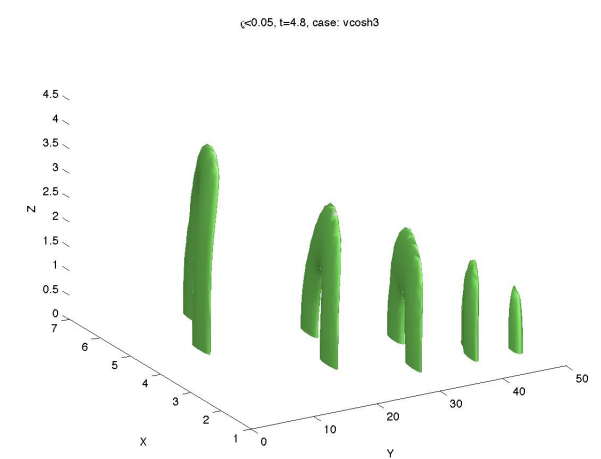
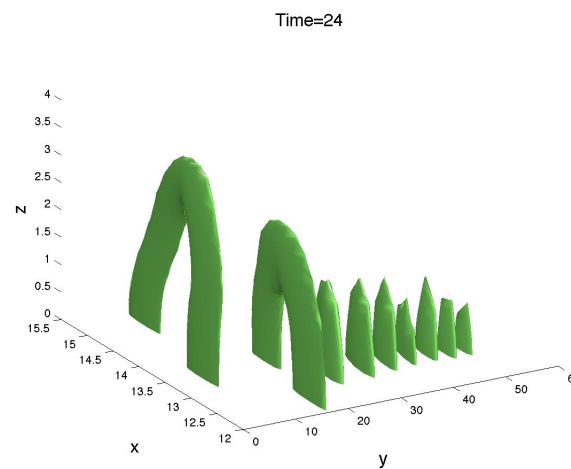
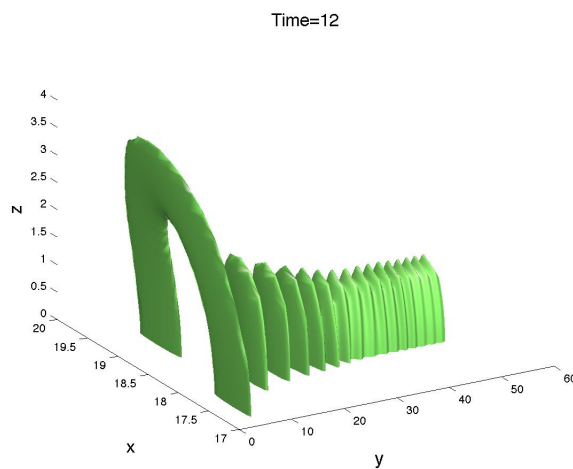
# Twisting and 'waves' $\rho = 0.05$ isosurfaces. Larger calculation

Left: Normal views. Right: Foreshortened to emphasize twisting. Leading up to reconnection, a kink appears at transition where the collapsing twisted vortex meets straight continuation. Out of this kink, waves propagate outward along the vortex. After reconnection, the waves don't simply propagate. They deepen until a second reconnection occurs and a vortex ring separates for the origin vortices.



- Rings identified by isosurfaces for  $\rho < 0.05$  on the top.
- Density contours in the  $x - y$  dividing plane between the two original vortices.
- **Left:** Only one ring. Rest are a zig-zag of original vortex.
- **Middle:** Rings disconnect. **Right:** Rings propagate to right.
- Radius decreases with  $y$ . Velocity - circulation/radius:  $\mathbf{V} = \Gamma/R$ , increases.

## Rings separate



But is this turbulence?

**What makes a flow turbulent?**

- An energy cascade? A  $k^{-5/3}$  spectrum? Energy decay?

**What is the energy?**

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- There are two parts to the Hamiltonian, which is conserved.
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- There is  $E_I = \int dV \frac{1}{4} (1 - \rho)^2 = \int dV \frac{1}{4} (1 - |\psi|^2)^2$ . This is the interaction energy.

$K_{\nabla\psi}$  and  $E_I$  can be expressed in Fourier space. Thus, their interactions and the direction of cascade in Fourier space can be calculated. **Work in progress**



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- All explanations for how energy can be removed in a quantum fluid assume that the energy sink is the non-ideal boundaries.

The question is how to get it there. Three mechanisms have been proposed:

- i) Quantum vortex lines could reconnect to form vortex rings, which then propagate out (Feynman, 1955).
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All two ring and two line calculations I have recently done, many reproducing existing results, **say no**.

Why did Klaus Schwarz suggest it? That is another talk.

- ii) Phonon generation probably requires ring generation first.

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- All explanations for how energy can be removed in a quantum fluid assume that the energy sink is the non-ideal boundaries.

The question is how to get it there. Three mechanisms have been proposed:

- i) Quantum vortex lines could reconnect to form vortex rings, which then propagate out (Feynman, 1955).
- ii) Linear waves, or phonons could be generated internally and propagate out.
- iii) Waves on vortices could cascade to small scales and their energy be radiated as phonons (Kozik/Svistunov, 2004; Laurie et al., 2010).

- **Do any work?**

- iv) I will propose vortex stretching and the conversion of  $K_{\nabla\psi}$  into  $E_I$ .

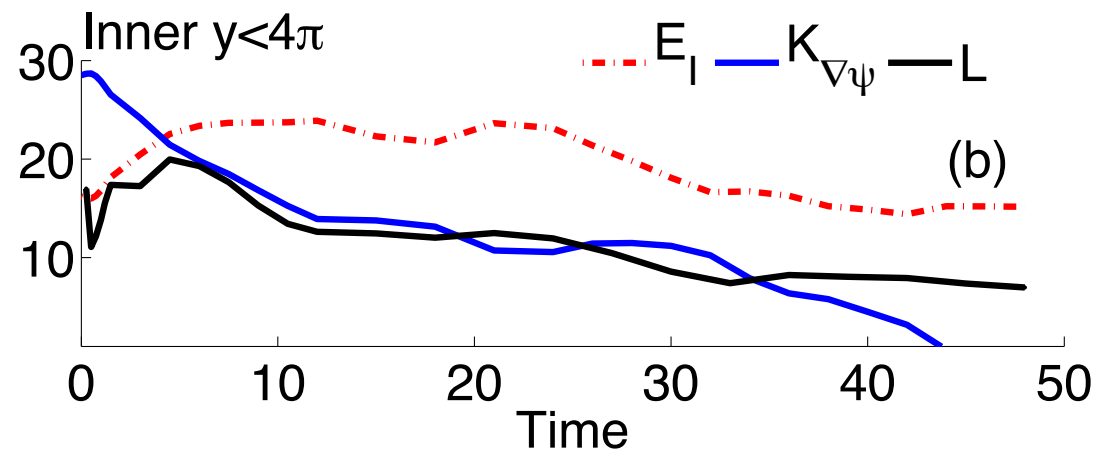
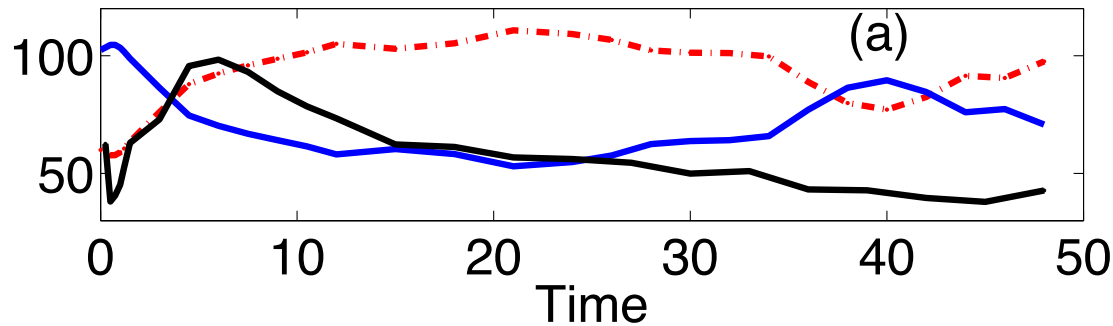
- iii) All vortex wave explanations assume that the local induction approximation is valid approximation for quantum vortex motion.

All two ring and two line calculations I have recently done, many reproducing existing results, **say no**.

Why did Klaus Schwarz suggest it? That is another talk.

- ii) Phonon generation probably requires ring generation first.

- **My first goal is careful analysis of energy components components and the vortex line length, then compare to i) and iv).**

Global  $E_I$ ,  $K_{\nabla\psi}$ ,  $L$ 

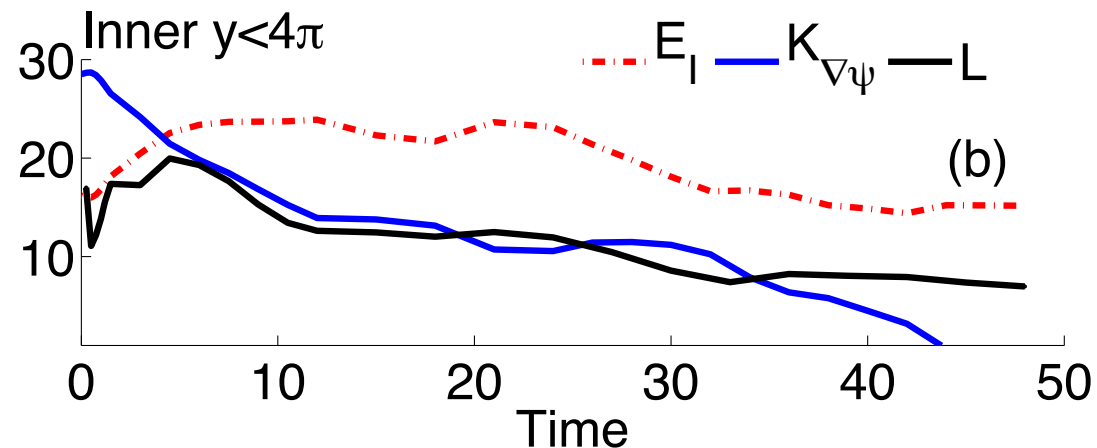
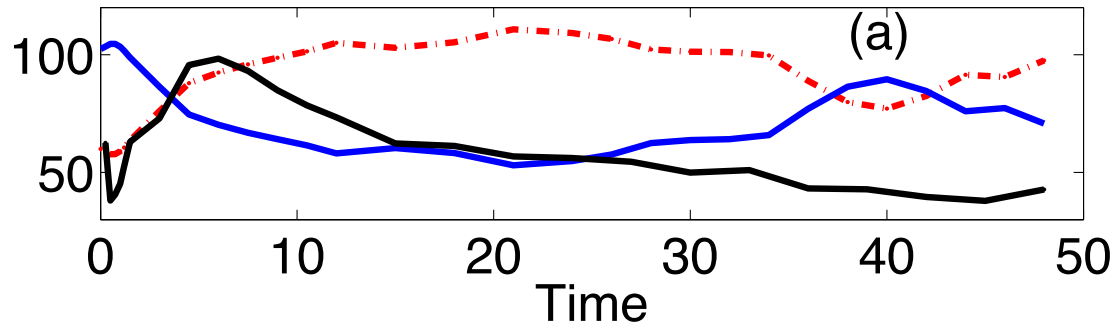
Estimates of the line length compared to changes in the interaction and kinetic energies.

a) Analysis over the full domain.

b) Only the first  $y$ -quadrant.

a) There is strong global  $E_I$  and vortex line  $L$  growth for  $0.5 < t < 6$ . For  $6 < t < 25$  both  $K_{\nabla\psi}$  and  $L$  decrease. For  $T > 30$  the global kinetic energy  $K_{\nabla\psi}$  grows again. This is associated with the accumulation of energy for  $y > 4\pi$ .

b) First  $y$ -quadrant. Shows that  $K_{\nabla\psi}$  and  $L$  continue to decrease in the original interaction region.

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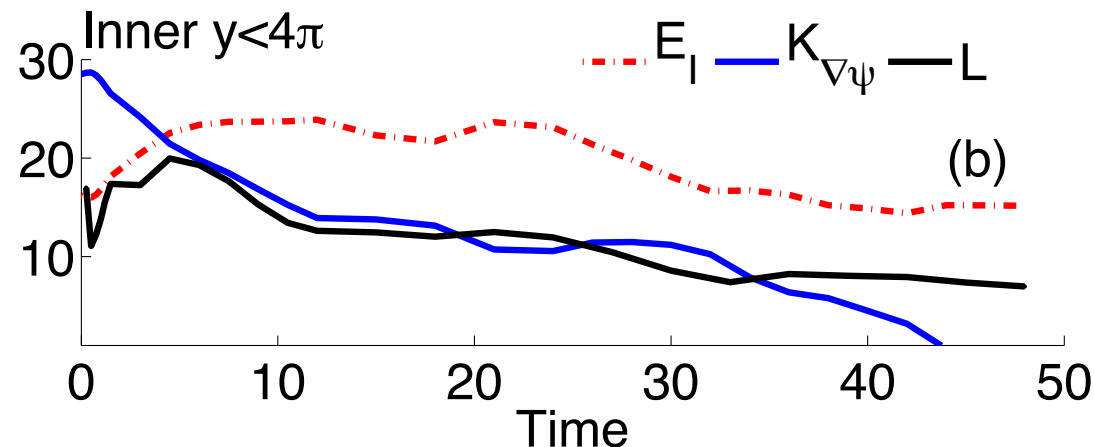
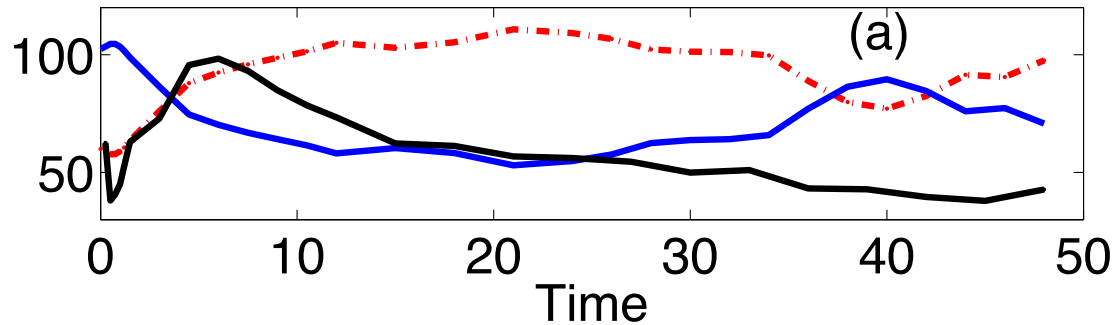
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In a physical cell, this energy would be absorbed by the outer wall.

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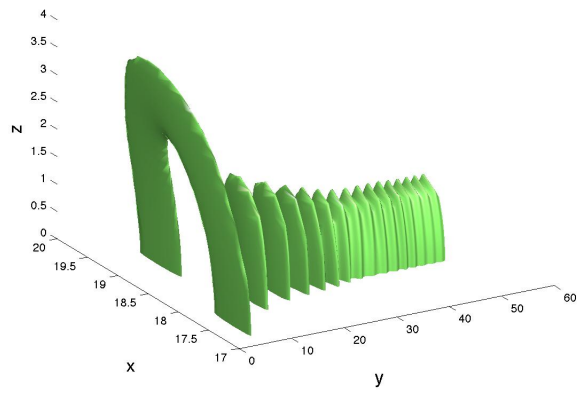
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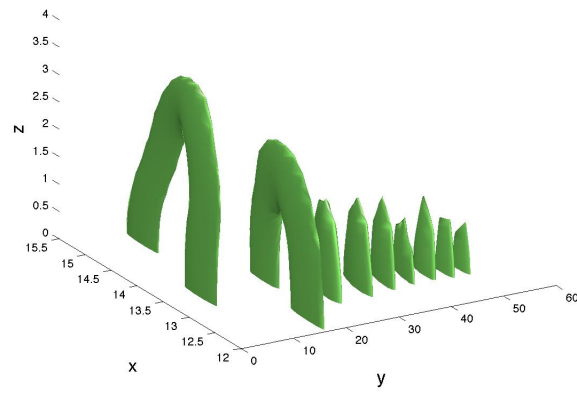
- **Does this energy become rings or phonons in the present case?**

# Rings propagate out

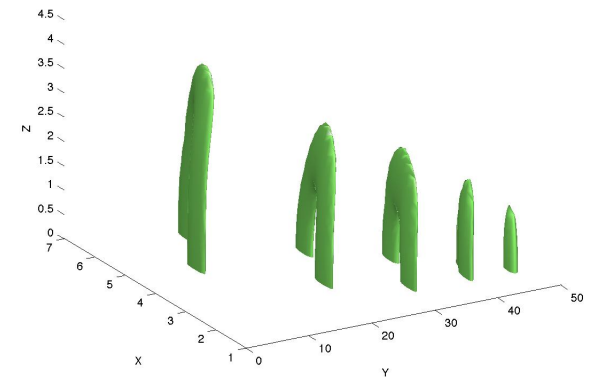
Time=12



Time=24

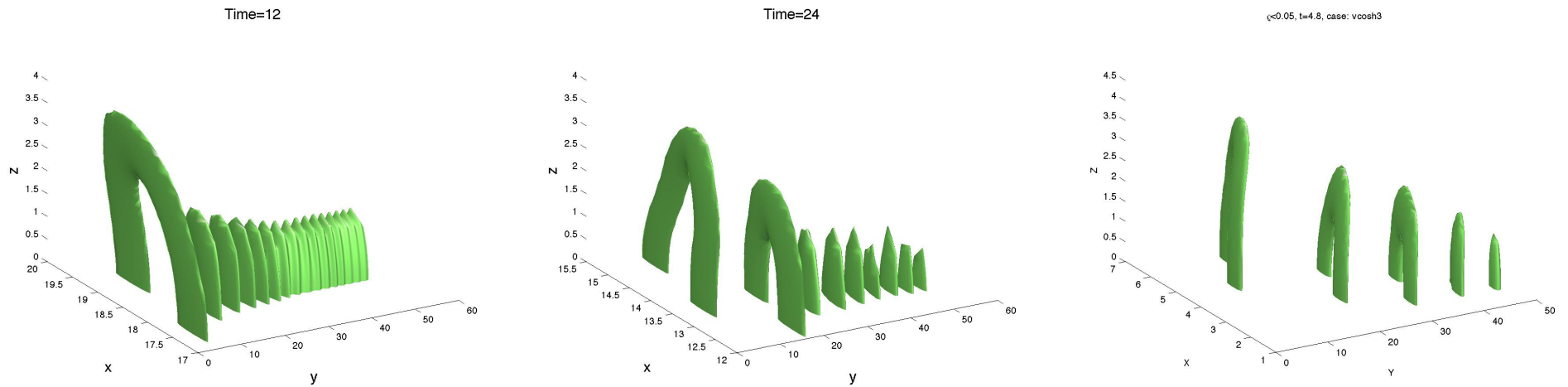


$\nu < 0.05$ ,  $t = 4.8$ , case: vcosh3

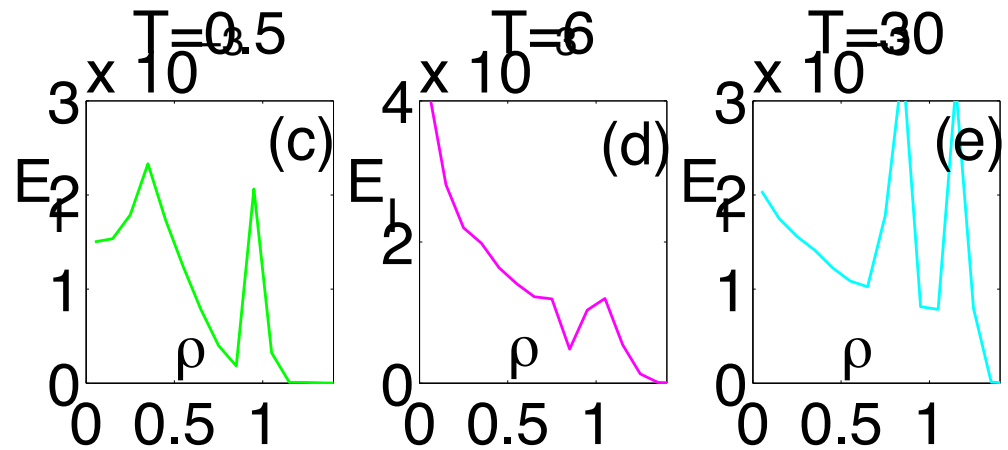
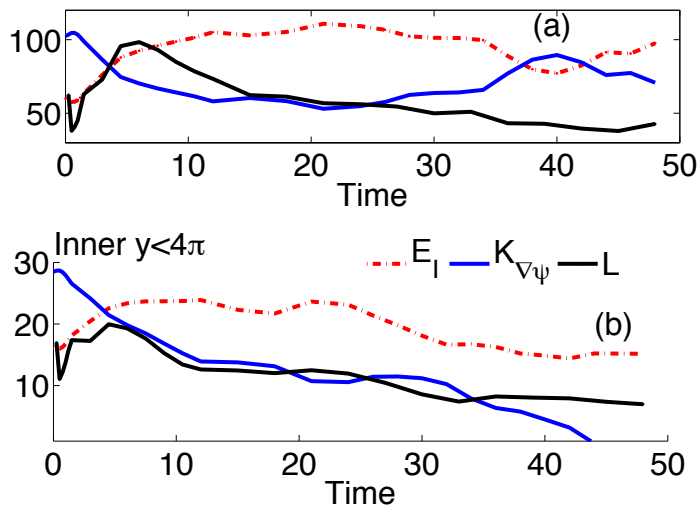




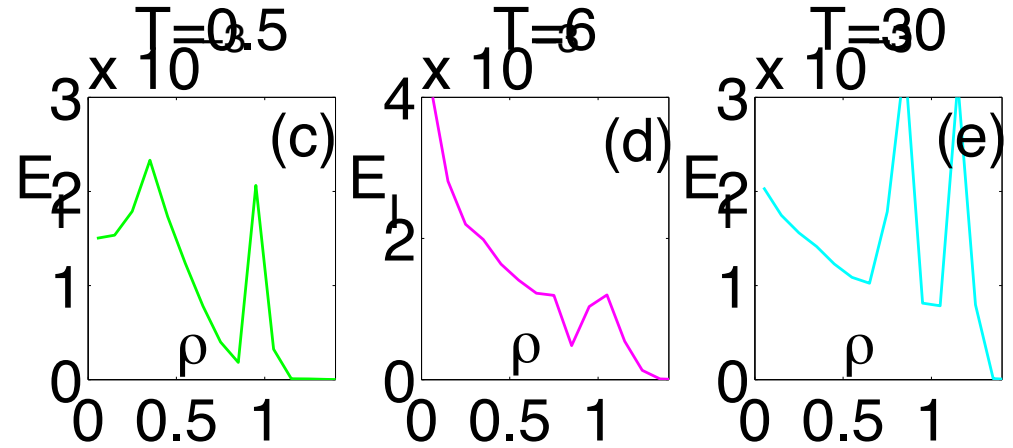
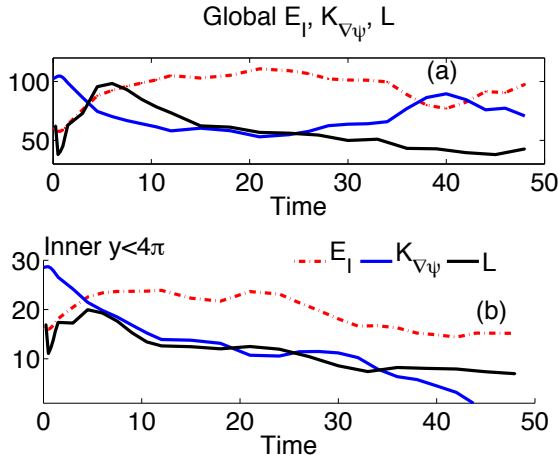
# Rings propagate out



Global  $E_I, K_{\nabla\psi}, L$



c-e) Distributions of the  $E_I$  with respect to density at  $t = 0.5, 6, 30$  to show how energy appears to flow from  $K_{\nabla\psi}$  to  $E_I$  to waves.



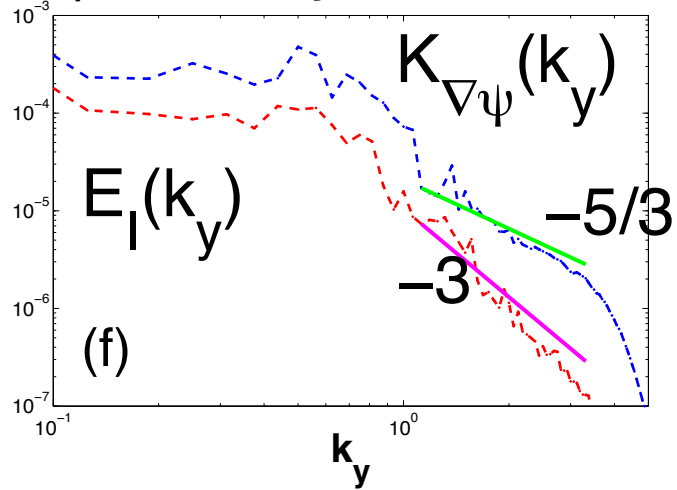
**Distributions and line length** To understand the different stages, subplots Fig. c-e show distributions of  $E_I$  with respect to density at three times. The  $t = 0.5$  distribution in Fig. c demonstrates that initially  $E_I$  has a maximum near  $\rho = 1$ .

Fig. d shows that at  $t = 6$ , when stretching is greatest, there has been a dramatic growth in  $E_I$ , with most of the growth for  $\rho \approx 0$ . This implies a large growth in the number of points with  $\rho \approx 0$ . Note that the increases in  $E_I$  for  $t \leq 20$  are compensated for by a strong decrease in the global kinetic energy in Fig. a.

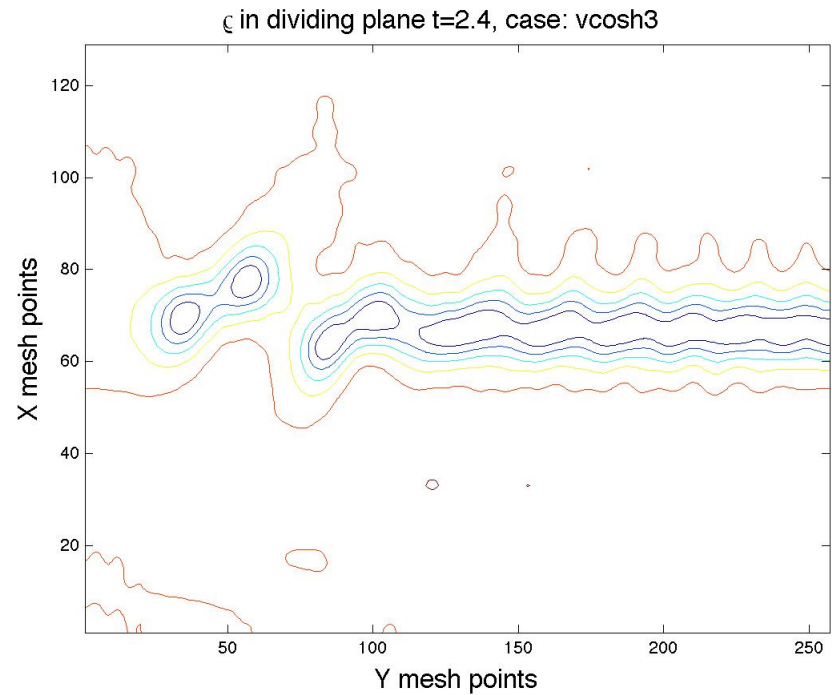
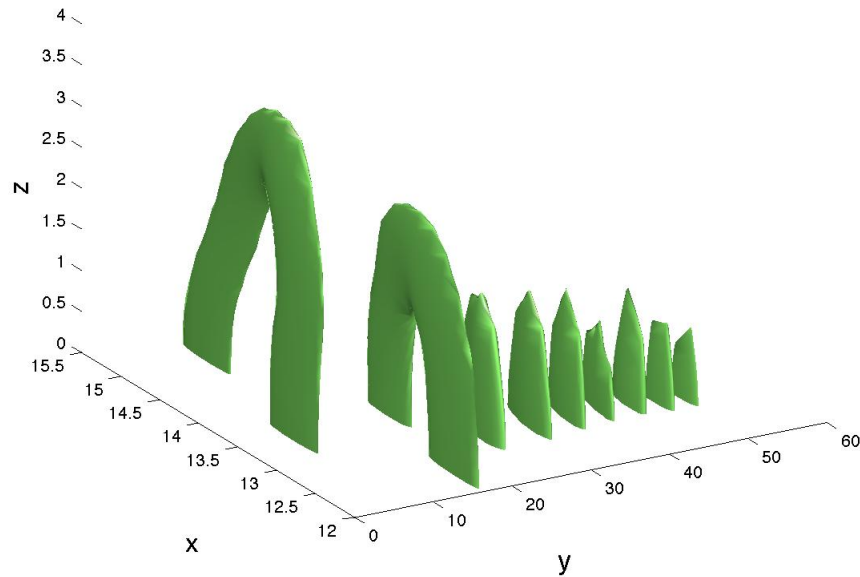
Immediately after  $t = 6$ ,  $L$  begins to decrease dramatically while the kinetic energy  $K_{\nabla\psi}$  continues to decay, which is compensated for by a continuing increase in the interaction energy  $E_I$ . At the end of this stage, there is a growth in large values of  $E_I$  on either side of  $\rho = 1$ , shown by the distribution at  $t = 30$ . Around, not at, because for  $\rho = 1$ ,  $E_I \equiv 0$ , This would be consistent the development of waves and visualizations of waves being emitted from colliding vortices.

The decrease in the global kinetic energy does not persist. Eventually interaction energy is converted back into kinetic energy, possibly due to oscillations between  $K_{\nabla\psi}$  and  $E_I$  in the released phonons. Similar oscillations were observed in GP calculations with a symmetric Taylor-Green initial condition (Nore et al., 1997). This would not persist in a real experimental device because the waves would be absorbed by the non-ideal boundaries.

# $K_{\nabla\psi}$ and $E_I(k_y)$ spectra. $T=48$

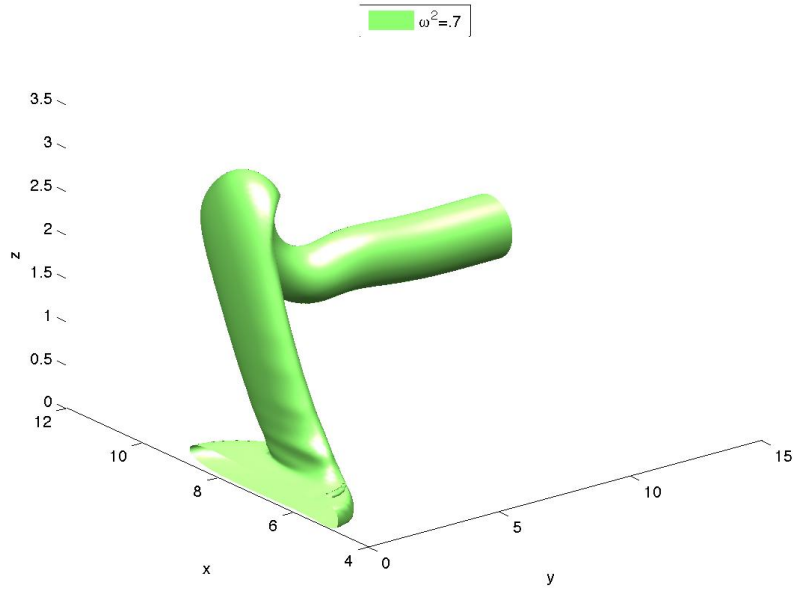


**Spectra:** f) By  $t = 48$ , there is a long  $K_{\nabla\psi}(k_y)$  the order of  $k_y^{-5/3}$ , while  $E_I(k_y)$  is still dominated by a  $k_y^{-3}$  slope. Spectra in the other directions have similar trends but are less distinct.

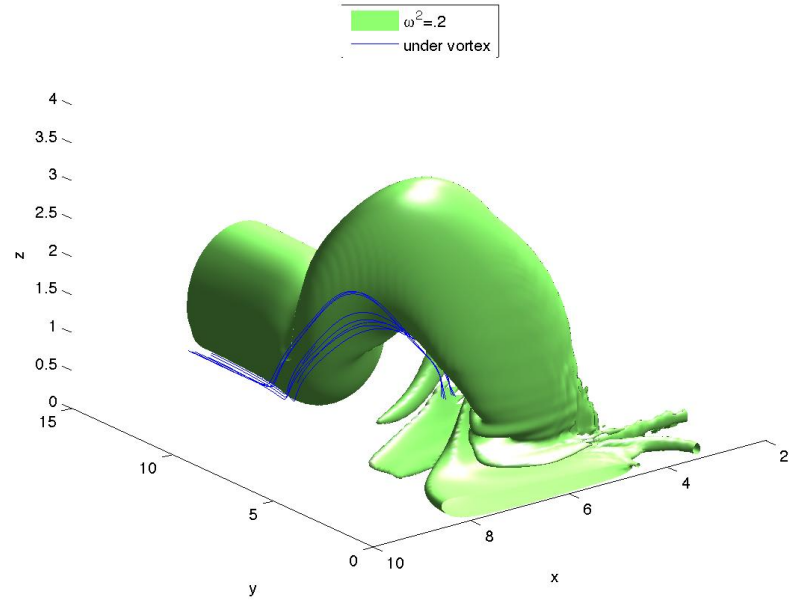


# 1.4 Classical reconnection with improved I.C. (less $\omega < 0$ ) **Ring forms**

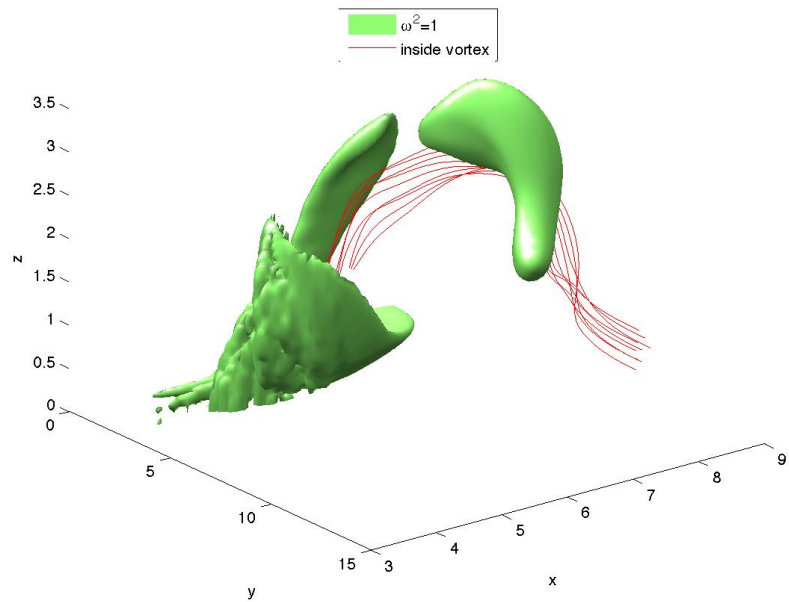
t=10,  $\nu=6e-5$ , SMOOTH=16e-21, SMXYZ=[.5, 5, 1],  $\max(\omega^2)=20$



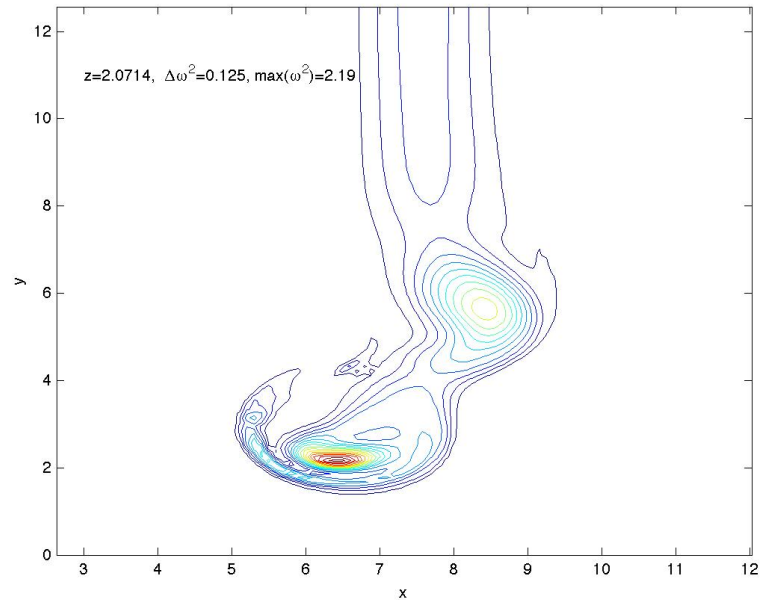
t=21.25,  $\nu=6e-5$ , SMOOTH=16e-21, SMXYZ=[.5, 5, 1],  $\max(\omega^2)=108$



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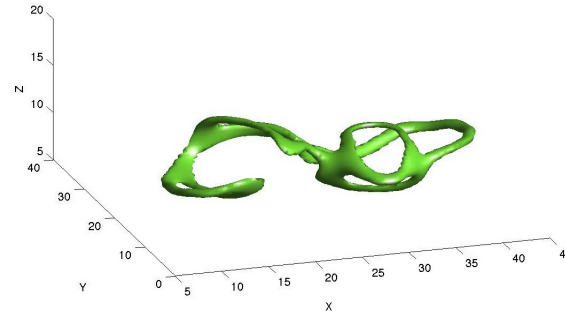
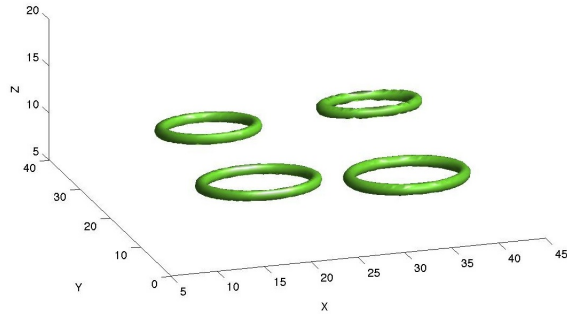
t=21.25,  $\nu=6e-5$ , SMOOTH=16e-21, SMXYZ=[.5, 5, 1],  $\max(\omega^2)=108$



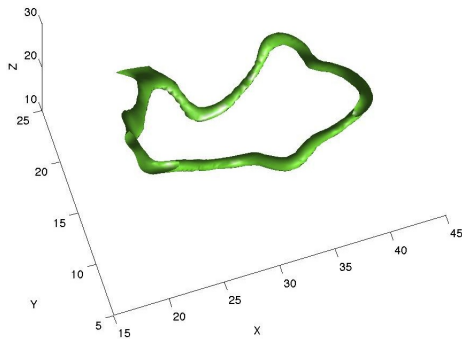
# Four colliding vortices

tb9\_4elb\_1286464  $c_c = .1 T = 0$  az-18 el18

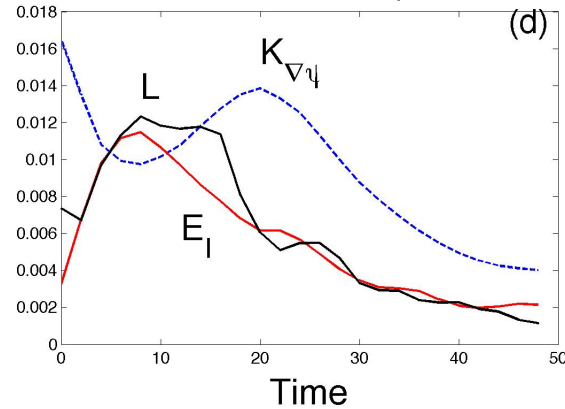
tb9\_4elb\_1286464  $c_c = .1 T = 18$  az-18 el18



tb9\_4elb\_1286464  $c_c = .1 T = 48$  az-18 el68



Compare inner  $K_{\nabla\psi}$ ,  $E_I$ ,  $L^*$



Four colliding rings, the entangled state generated, the final relaxed state, and the time dependence of the kinetic and interaction energies plus a measure of line length in the inner region that contained the original vortices. In this case the measure of line length, the volume where  $\rho < 0.1$ , tracks the interaction energy  $E_I$  more closely than the kinetic energy.

**Summary** A long-standing question in classical turbulence is whether the energy cascade is mostly statistical, or originates with the interaction of fluid structures. No matter how special or non-classical, even a single case that started with a simple vortical configuration and then generated a cascade could provide new insight. Such an initial condition could then be adapted to classical reconnection and turbulence calculations to determine whether similar dynamics and stages can form. The results here suggest how to start a search for similar classical events that would begin with vortex stretching, then form a tangle followed by multiple reconnections, and finally lead to the creation of small scale dissipative structures.

The other major point is the roles stretching and the creation of interaction energy play in decreasing the kinetic energy. This provides the first step in allowing waves to be created and serve as an energy sink far from boundaries. These properties seem to hold for a number of cases where rings and lines are allowed to interact. In the anti-parallel case, the release of one ring is followed by further reconnections and smaller rings, which is evidence for a physical space cascade.

How much of this can be transferred over to classical fluids? A preliminary calculation of reconnection in Navier-Stokes using the improved trajectory and initial profile suggested by these calculations does produce one ring after two reconnections. Further work is in progress.

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(Filament calculations, mine and de Waele/Aarts.) **No spirals.**

**Stretching increases line length which leads to the generation of interaction energy, and removal of kinetic energy.**

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These are NOT the Kelvin waves resulting from sharp vortex filament reconnections in LIA (Schwarz, mid-1980s).

- *Oscillations deepen further:*

Second reconnection releases a vortex ring. Cascade of rings forms as well as a cascade of kinetic energy to small scales and  $k^{-5/3}$  kinetic energy spectrum.

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- **Finally: Can classical reconnection do the same?**

Acknowledge: Support of the Leverhulme Foundation. Discussions with Miguel Bustamante, Carlo Barenghi, Sergey Nazarenko, ME Fisher, Dan Lathrop.